

Coherent Diffraction Imaging (CDI) with X-Rays

School on Synchrotron and Free-Electron-Laser Based Methods: Multidisciplinary Applications and Perspectives

> ICTP Trieste, April 15 - 2016

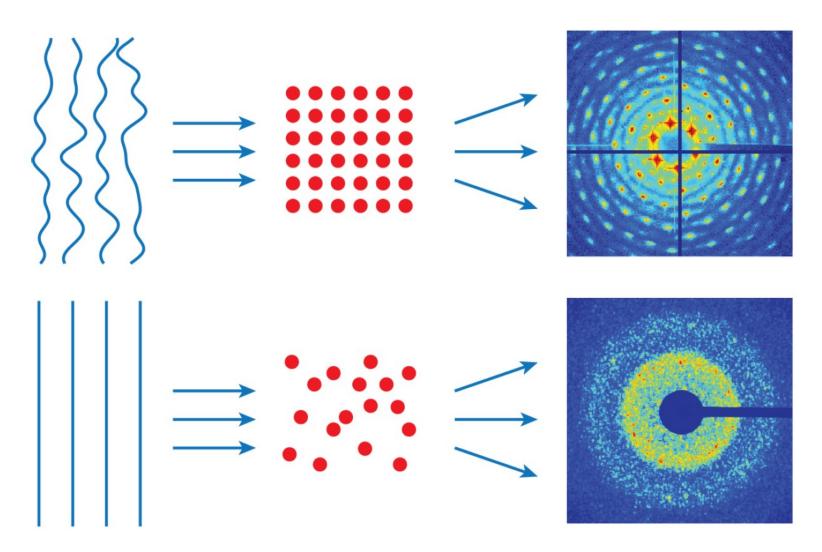
Anders Madsen European X-Ray Free-Electron Laser Facility Hamburg, Germany

anders.madsen@xfel.eu



- Motivation
- X-ray Imaging
- X-ray Coherence
- All the tricks of CDI
- Image reconstruction
- Related methods
- Applications
 - BREAK -
- Sources of Coherent X-rays
- The European XFEL project
- CDI science at XFELs
- Summary

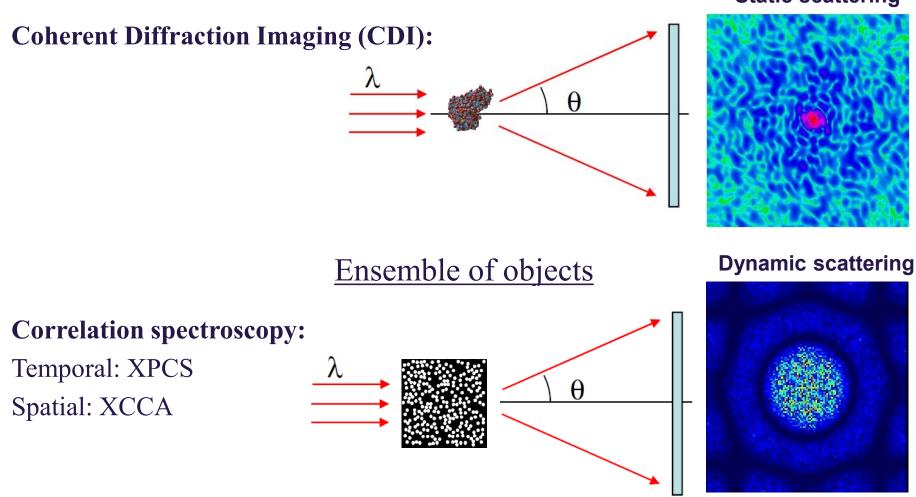
XFEL Coherent scattering. Motivation



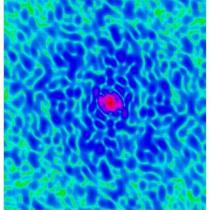
Slide courtesy of I. Vartaniants (DESY)

European **XFEL** Coherent scattering. Motivation

Isolated object



Static scattering

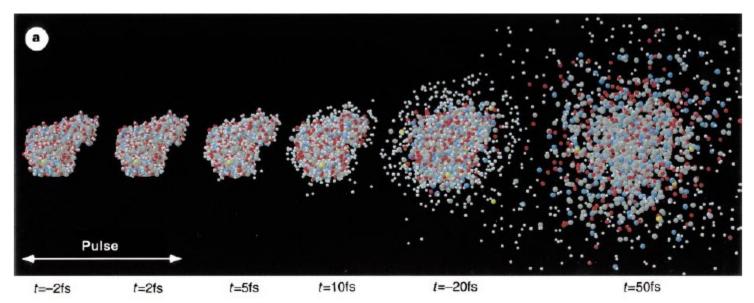




5

Diffraction imaging of biomolecules with coherent femtosecond X-FEL pulses

Very much excitement, now for >15 years:

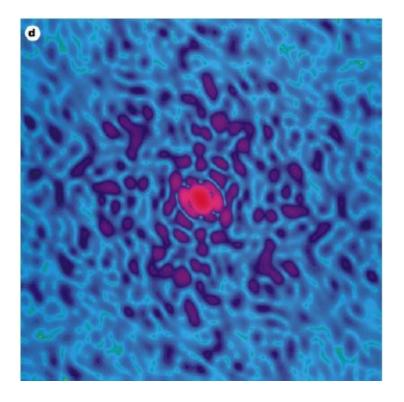


Coulomb explosion of T4 lysozyme

R. Neutze *et al.*, Nature **406**, 752 (2000)



Diffraction imaging of biomolecules with coherent femtosecond X-FEL pulses

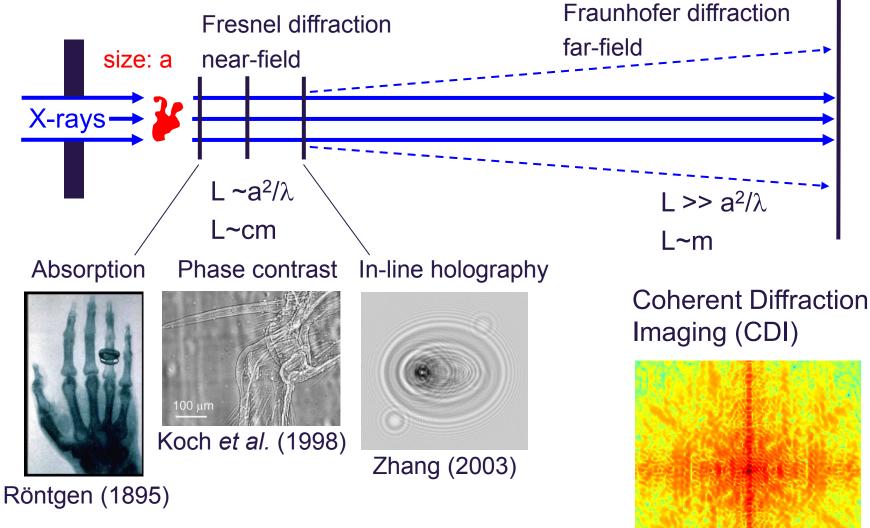


Simulated coherent scattering image (speckle) of a T4 lysozyme molecule

A. Madsen, European XFEL

R. Neutze *et al.*, Nature **406**, 752 (2000)







Absorption regime

- Easy reconstruction based on attenuation
- 3D tomographic reconstruction, inverse Radon transformation

Phase contrast regime

Edge enhanced contrast Transport-of-intensity (TIE) equation Holotomographic reconstruction (Talbot effect)

In-line holographic regime

Holographic reconstuction (detector dependent resolution) Twin image problem

Coherent diffraction imaging

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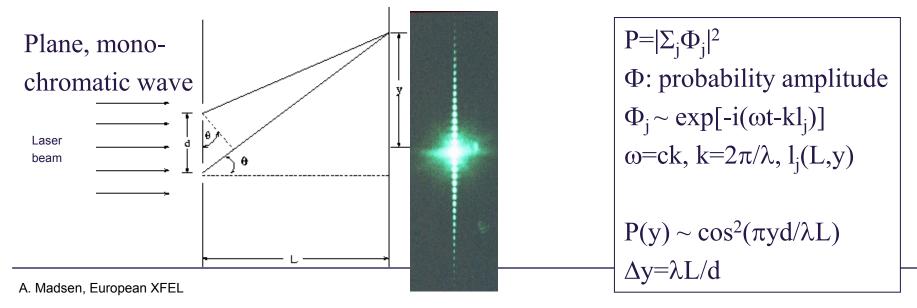
Tricky data treatment Resolution like in scattering, i.e. $\Delta_{min} = 2\pi/Q_{max}$

XFEL Coherence

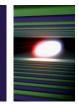


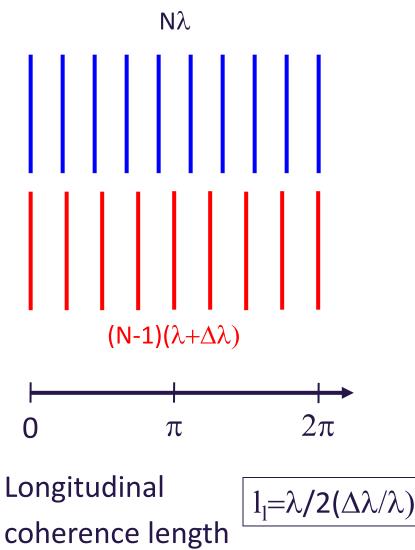
Quantum mechanics → probability amplitudes (waves) Optics → Young's double slit experiment, interference X-ray (and neutron) scattering It's all about probability amplitudes and interference !!!

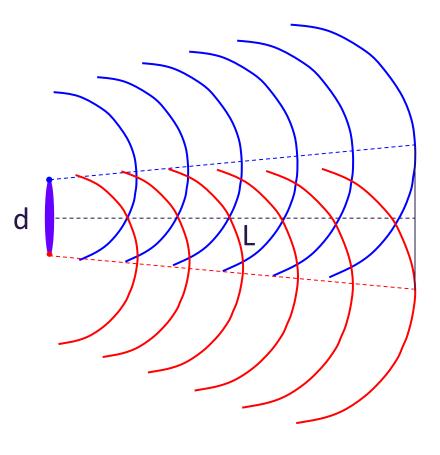
Example: Young's double slit experiment (Thomas Young, 1801) [wave-character of quantum mechanical particles (photons)]









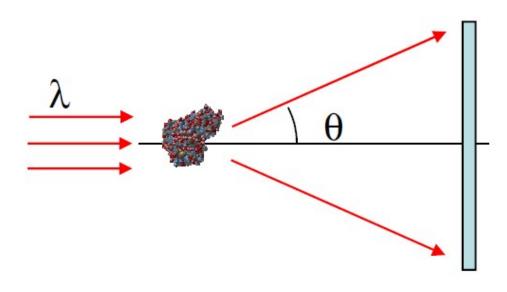


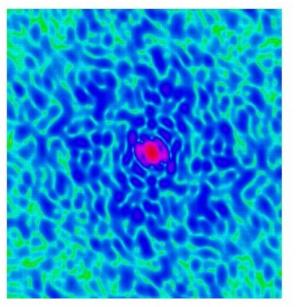
Transverse coherence length

 $l_t = \lambda L/2d$

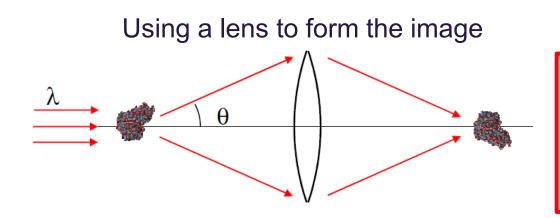
XFEL The CDI Challenge





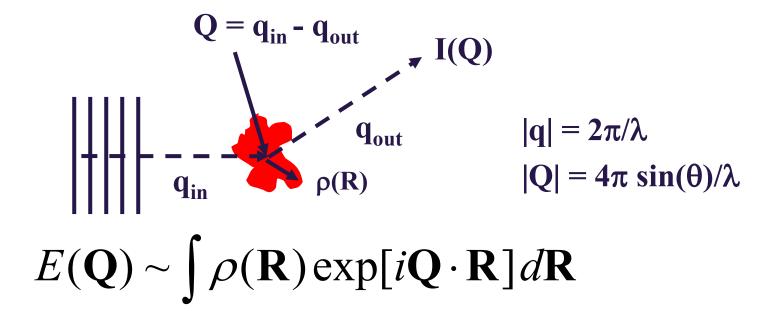


l(q)



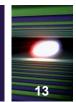
Question

Speckle pattern does not look like sample. How to determine the sample from I(q) ? **XFEL** The phase problem in scattering



Reciprocal space $E(\mathbf{Q}) \leftarrow \leftarrow \leftarrow FT \rightarrow \rightarrow \rightarrow \rho(\mathbf{R})$ Real space

But...
$$I(\mathbf{Q}) = E(\mathbf{Q})E^{*}(\mathbf{Q}) = |E(\mathbf{Q})|^{2}$$



Aim: To find E(Q) from measurements of $I(Q) = |E(Q)|^2$ But E(Q) is a complex number with both phase and amplitude

 $E(Q) = A \exp(i\phi)$

Measurement: $I(Q) = |E(Q)|^2 = A^2$

No direct access to phase....

Exercise

FT of XFEL logo \rightarrow E(Q)

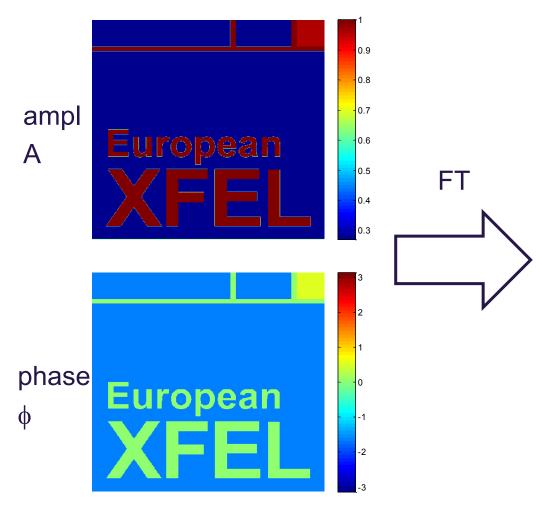
 $I(Q) = |E(Q)|^2$ (simulation of coherent scattering)

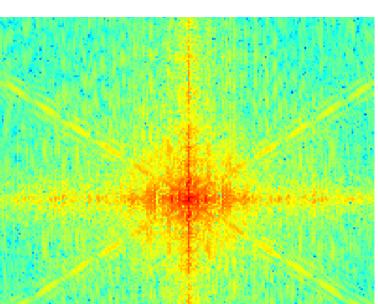
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Construct E(Q):
```

A = sqrt(I(Q))

Take random phases ϕ

Inverse FT transform of A exp(i\u00f3)





$$|FT{\rho(R)}|^2 = |E(Q)|^2 = I(Q)$$

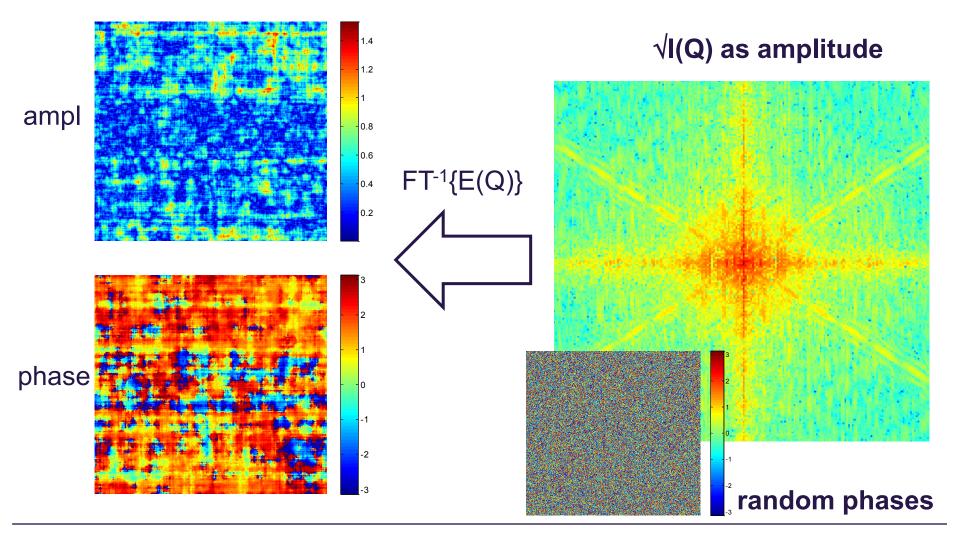
European XFEL Phase matters!

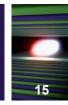
ρ(R)



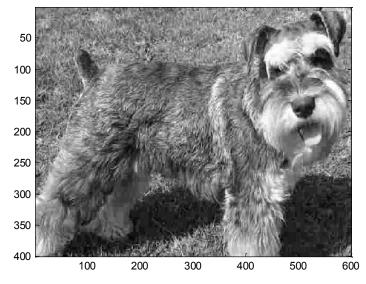


ρ(R)





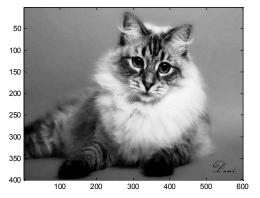
XFEL Phase is more important than amplitude

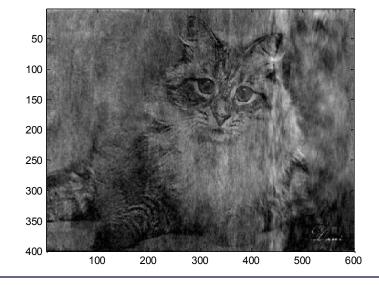


Fourier transform my dog $\rightarrow A e^{i\phi}$ Keep amplitudes *A* Substitute with another image's phases ϕ

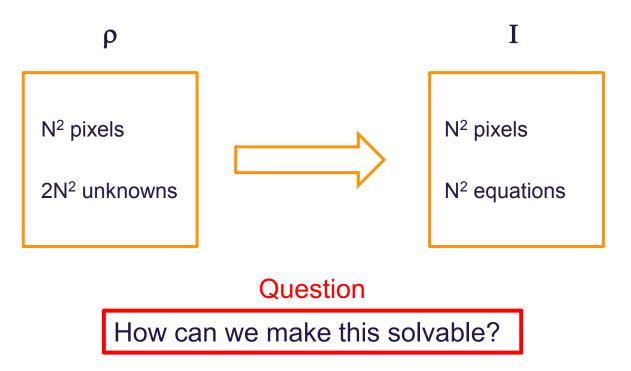
Inverse Fourier transform



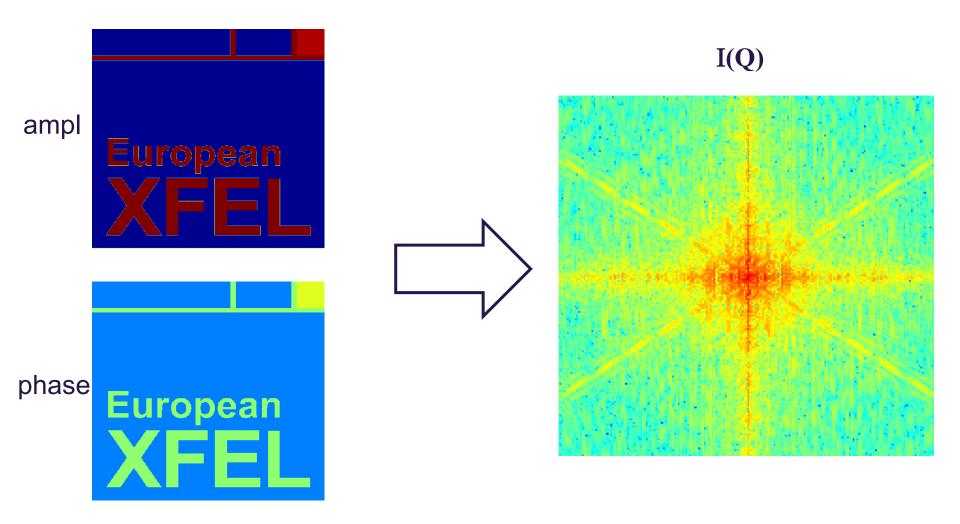






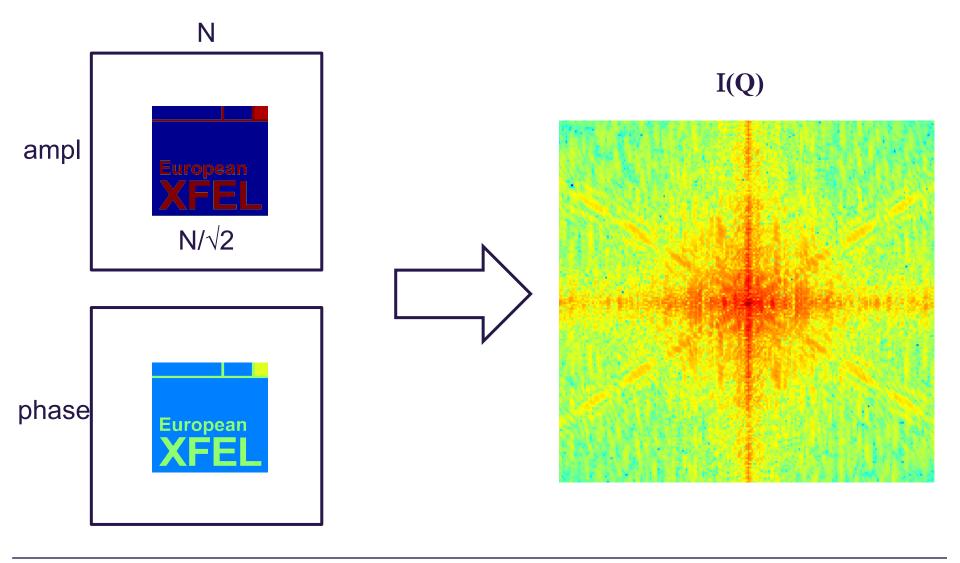






18

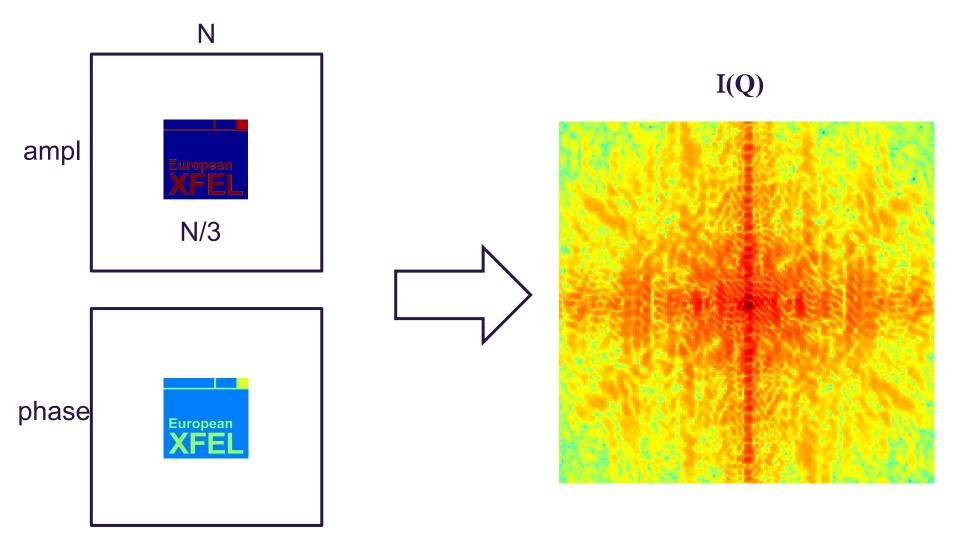




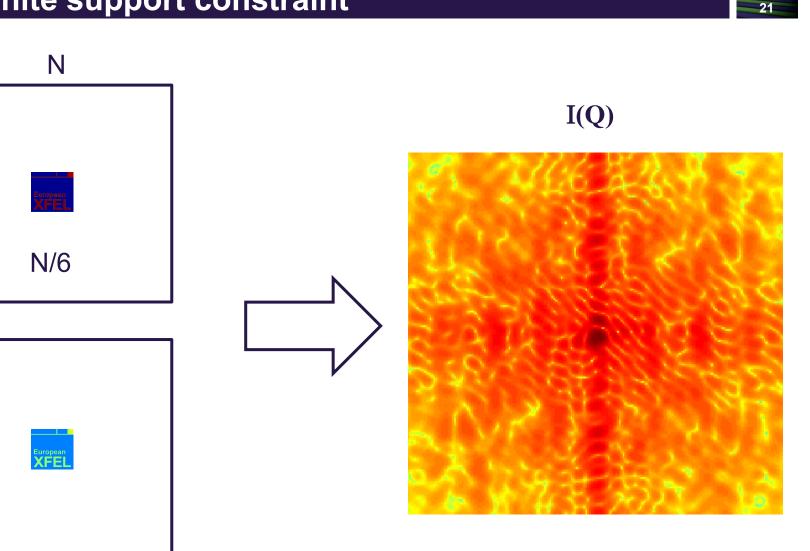
19











Angular speckle size ~ λ /sample size

A. Madsen, European XFEL

ampl

phase

XFEL Oversampling

David Sayre (1952)

Acta Cryst. (1952). 5, 843

Some implications of a theorem due to Shannon. By D. SAYRE, Johnson Foundation for Medical Physics, University of Pennsylvania, Philadelphia 4, Pennsylvania, U.S.A.

(Received 3 July 1952)

Shannon (1949), in the field of communication theory, has given the following theorem: If a function d(x) is known to vanish outside the points $x = \pm a/2$, then its Fourier transform F(X) is completely specified by the values which it assumes at the points $X = 0, \pm 1/a,$ $\pm 2/a, \ldots$ In fact, the continuous F(X) may be filled in merely by laying down the function $\sin \pi a X/\pi a X$ at each of the above points, with weight equal to the value of F(X) at that point, and adding.

Now the electron-density function d(x) describing a single unit cell of a crystal vanishes outside the points $x = \pm a/2$, where a is the length of the cell. The reciprocal-lattice points are at $X = 0, \pm 1/a, \pm 2/a, \ldots$, and hence the experimentally observable values of F(X)would suffice, by the theorem, to determine F(X) everywhere, if the phases were known. (In principle, the necessary points extend indefinitely in reciprocal space, but by using, say, Gaussian atoms both d(x) and F(X)can be effectively confined to the unit cell and the observable region, respectively.)

For centrosymmetrical structures, to be able to fill in the $|F|^2$ function would suffice to yield the structure, for sign changes could occur only at the points where $|F|^2$ vanishes. The structure corresponding to the $|F|^2$ function is the Patterson of a single unit cell. This has twice the width of the unit cell, and hence to fill in the $|F|^2$ function would require knowledge of $|F|^2$ at the half-integral, as well as the integral h's. This is equivalent to a statement made by Gay (1951).

I think the conclusions which may be stated at this point are:

1. Direct structure determination, for centrosymmetric structures, could be accomplished as well by finding the sizes of the $|F|^2$ at half-integral h as by the usual procedure of finding the signs of the F's at integral h.

2. In work like that of Boyes-Watson, Davidson & Perutz (1947) on haemoglobin, where $|F|^2$ was observed at non-integral h, it would suffice to have only the values at half-integral h.

The extension to three dimensions is obvious.

References

BOYES-WATSON, J., DAVIDSON, E. & PERUTZ, M. F. (1947). Proc. Roy. Soc. A, 191, 83.

- GAY, R. (1951). Paper presented at the Second International Congress of Crystallography, Stockholm.
- SHANNON, C. E. (1949). Proc. Inst. Radio Engrs., N.Y. 37, 10.

XFEL Basic experimental requirements for CDI

In 2D:

- Need that sample size a is $\sqrt{2}$ smaller than beam size D:
- a < D/ $\sqrt{2}$ (reduce number of unknowns)

- Need to measure the speckle pattern with a resolution that is at least $\sqrt{2}$ finer that speckle size in both dimensions. Therefore, the pixel size Δp must fulfil: $\Delta p < L\lambda/(a\sqrt{2})$, where L is the sample-detector distance (increase number of equations)

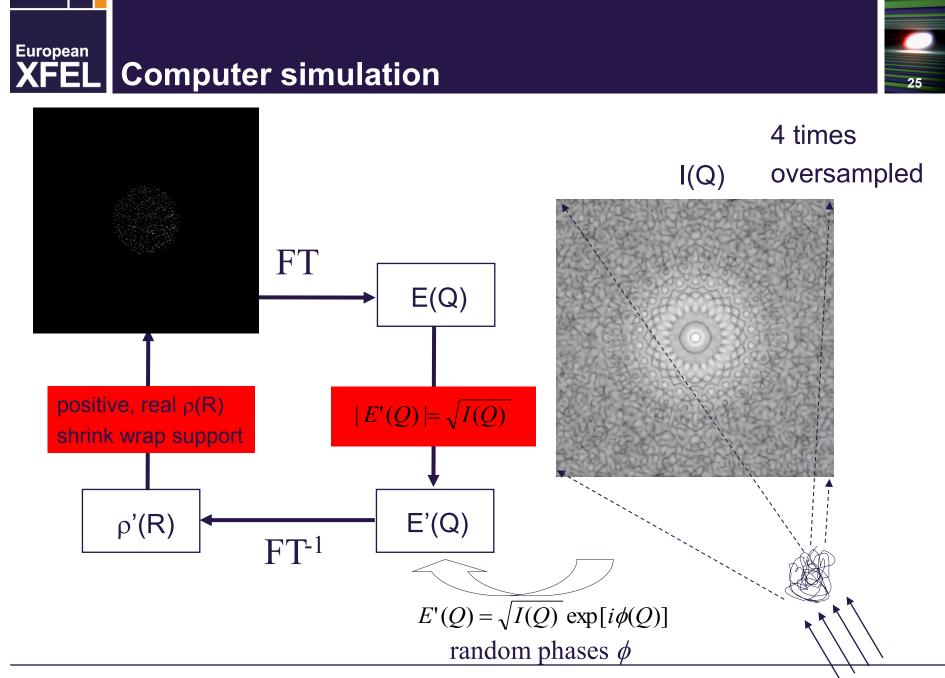
- Beam must be coherent over the sample size a, **otherwise the FT** relationship does not hold

Question

How to solve the non-linear system of N² equations and M unknowns (M < N²) to find $\rho(R)$? European **Iterative Phase Retrieval Algorithm** EEI FT Is this the real $\rho(\mathbf{x})$ solution? real space constraints reciprocal space constraints random phases E'(O $|\mathrm{E}(\mathrm{Q})| = \sqrt{\mathrm{I}(\mathrm{Q})}$ FT^{-1}

Real space constraints: finite support ($\rho=0$ outside sample) real ρ ? positive ρ ? other? **Reciprocal space constraints**

$$|\mathrm{E}(Q)| \rightarrow \sqrt{\mathrm{I}(Q)}$$





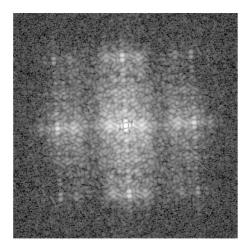
R. W. Gerchberg and W. O. Saxton, Optik 35, 237 (1972)J.R. Fienup, Appl. Opt. 21, 2758 (1982)

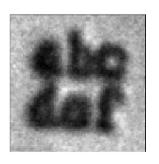
Review: R. Millane *et al.*, J. Opt. Soc. Am. **A14**, 568 (1997) Difference map: V. Elser, J. Opt. Soc. Am. **A20**, 40 (2003)



Data collected at NSLS beamline X1B

λ=1.8 nm soft x-ray diffraction pattern





Low angle data From optical micrograph

Scanning electron micrograph of object

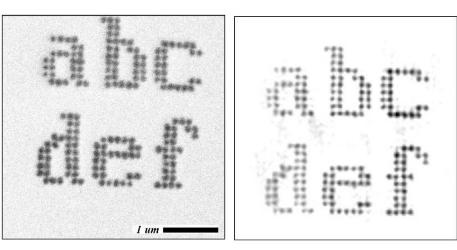
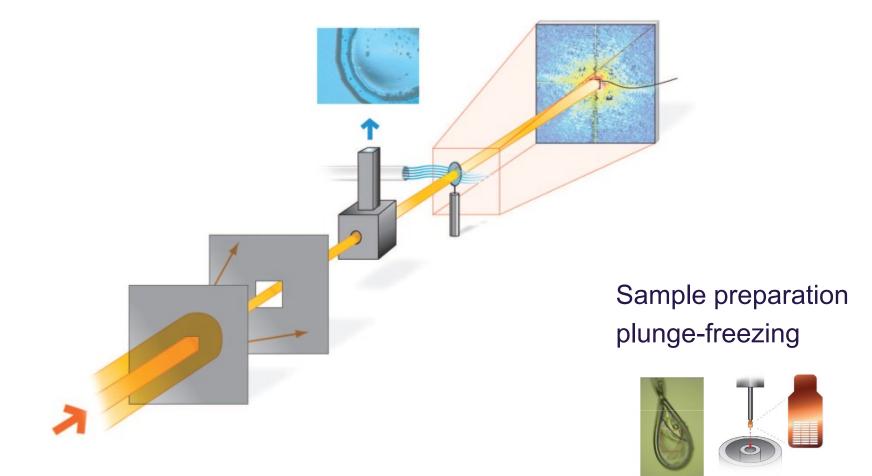


Image reconstructed from diffraction pattern $(\theta_{max} \text{ corresponds to}$ 80 nm). Assumed positivity

J. Miao et al, Nature 400, 342 (1999)



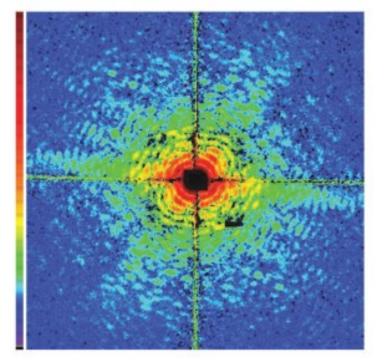


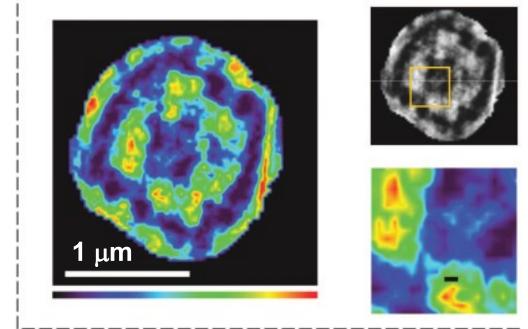






D. Radiodurans cell





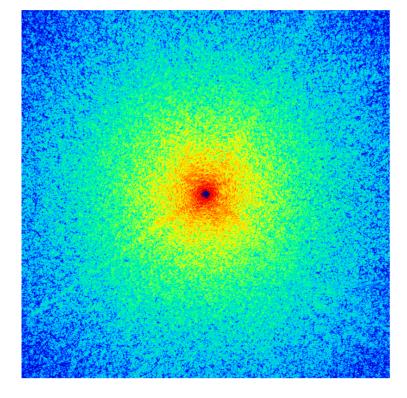
Resolution about 30 nm Goal: ~10 nm

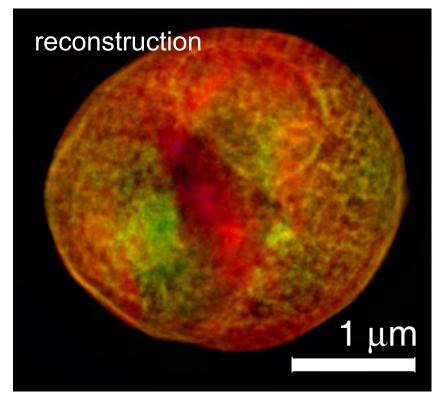
A. Madsen, European XFEL

E. Lima *et al*, PRL **103**, 198102 (2009)

EuropeanBio-CDI with soft X-rays

CDI from a yeast cell. Speckle pattern, λ =16.5 Å (ALS)





No shrink warp, "hand drawn" support Difference map algorithm Averaging iterates (Elser & Thibault) Resolution ~ 30 nm

D. Shapiro et al, PNAS 102, 15343 (2005)

EuropeanXFELPtychography

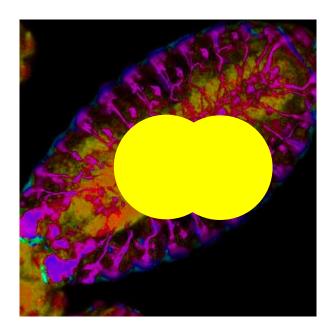


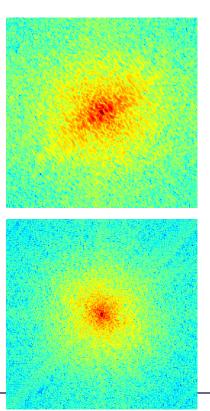
The requirement that sample < beam is a limitation for many practical purposes

Can we find another constraint so the 2N² unknowns can be determined?

The answer is : Ptychography!

Ptych- : (to) fold (from Greek)









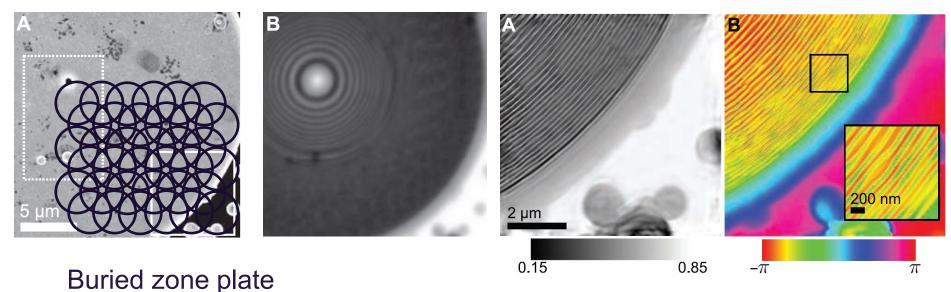
High-Resolution Scanning X-ray Diffraction Microscopy

Pierre Thibault,¹* Martin Dierolf,¹ Andreas Menzel,¹ Oliver Bunk,¹ Christian David,¹ Franz Pfeiffer^{1,2}

Science, **321,** 379-382 (2008)

SEM

absorption



XFEL Ptychography

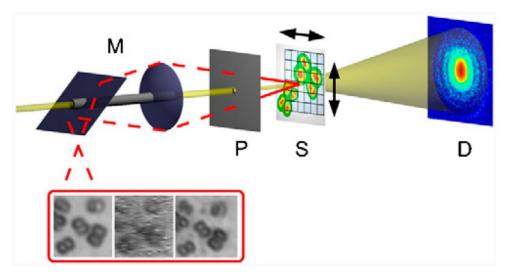


Quantitative biological imaging by ptychographic x-ray diffraction microscopy

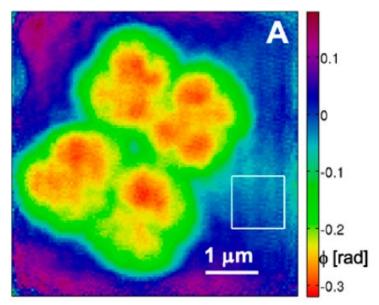
Klaus Giewekemeyer^{a,1}, Pierre Thibault^b, Sebastian Kalbfleisch^a, André Beerlink^a, Cameron M. Kewish^c, Martin Dierolf^b, Franz Pfeiffer^b, and Tim Salditt^{a,1}

Proc. Natl. Acad. Sci. USA 107, p. 529-534 (2010)

Setup at cSAXS beamline, SLS



D. Radiodurans







Question

Do you know another method where the phases

are encoded, i.e. easy reconstruction?

XFEL Holography



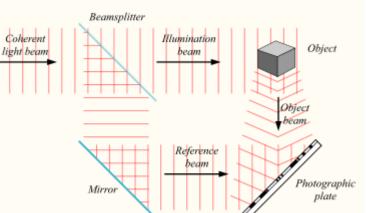
Famous method to encode the phases in the intensity pattern



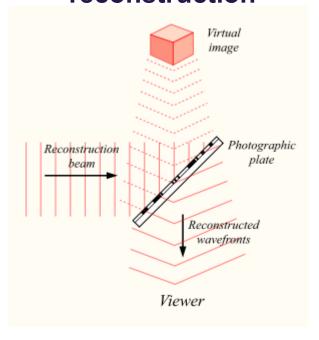
Dennis Gabor Nobel prize 1971

In-line holography (electrons, Gabor 1947); Laser (1960), 1st optical hologram ~1962

Recording



Holographic reconstruction



First SR hologram:

Aoki et al. Jap. J. Appl. Phy 11, 1857 (1972)

XFEL Fourier Transform Holography

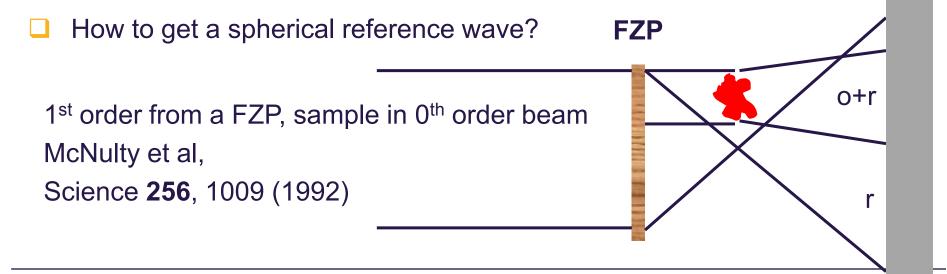
Fourier transform holography

- Spherical reference wave (r) spreads speckles and encodes phases of object wave (o)
- Simple reconstruction by FT:

 $I_{holo} = |FT{o+r}|^2 = |FT{o} + FT{r}|^2 = |O + R|^2 = |O|^2 + |R|^2 + OR^* + RO^*$

CCD

$$\mathsf{FT}\{\mathsf{I}_{\mathsf{holo}}\} = \mathsf{o} \otimes \mathsf{o} + \mathsf{r} \otimes \mathsf{r} + \mathsf{o} \otimes \mathsf{r} + \mathsf{r} \otimes \mathsf{o}$$



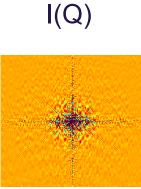
XFEL Fourier Transform Holography



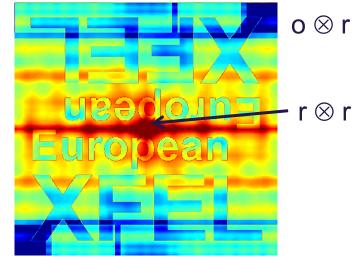
Strong reference

scatterer

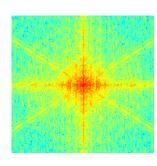






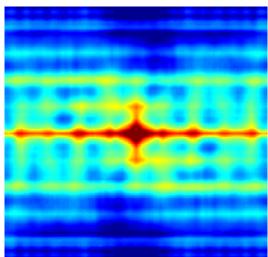






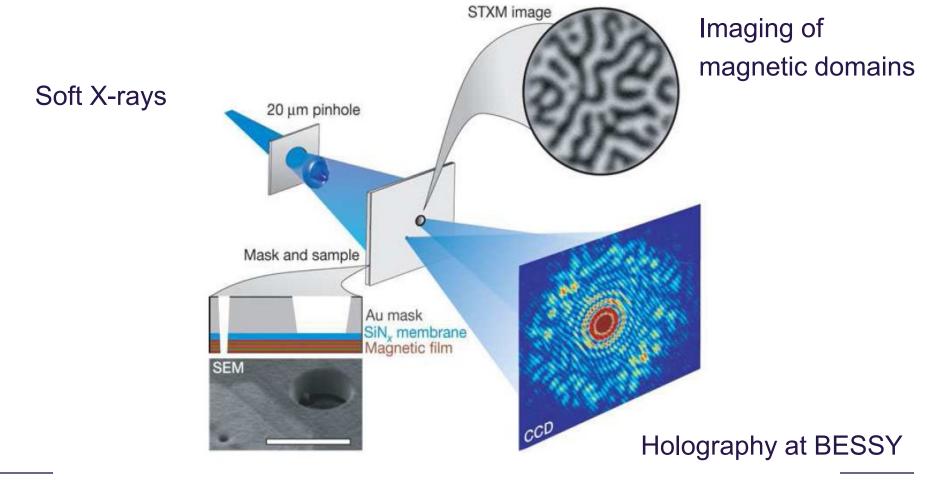


 $r \otimes o$



XFEL FT Holography with soft X-rays

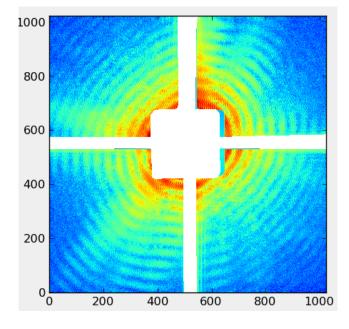
- 38
- S. Eisebitt, J. Lüning, W. F. Schlotter, M. Lörgen, O. Hellwig, W. Eberhardt and J. Stöhr Nature 432, 885-888(2004)

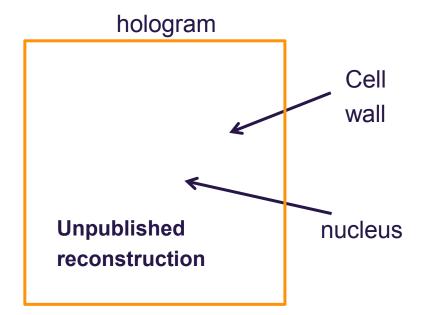


European **XFEL** Biological FT Holography

> Holography of Pichia Pastoris (yeast) cell + 250 nm Au particle







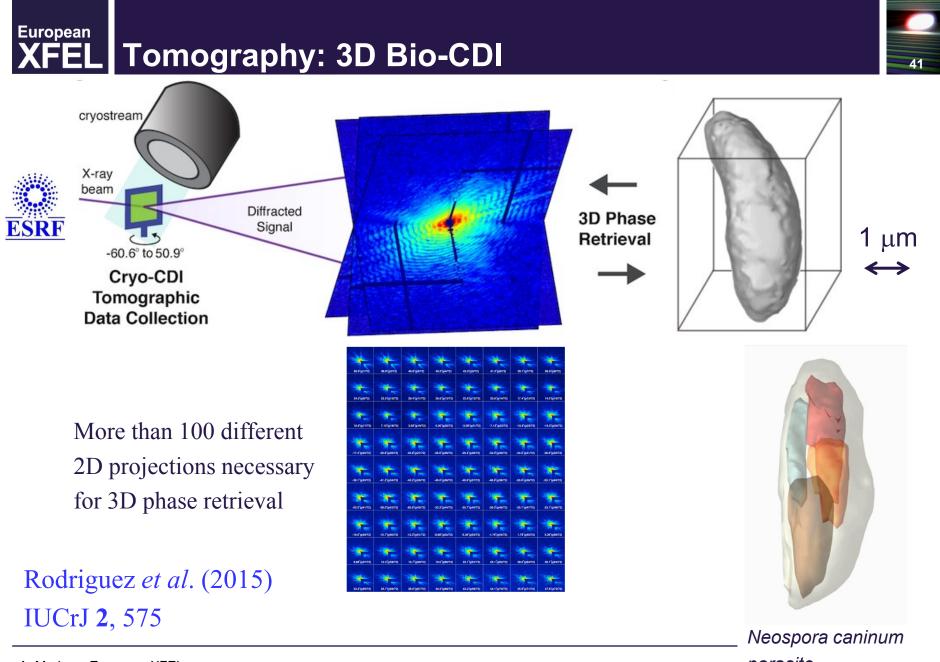
Stadler, Büldt, Madsen et al. (unpublished)





Shadow sculptures, Tim Noble and Sue Webster

http://www.thisismarvelous.com/amazing-shadow-sculptures-by-tim-noble-and-sue-webster/

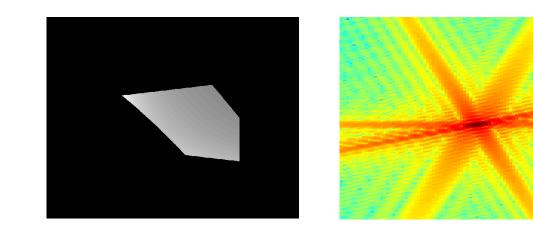


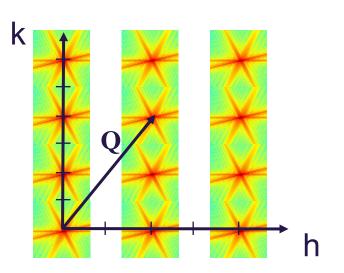
A. Madsen, European XFEL

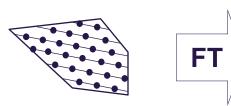
parasite

XFEL Tomography: 3D Bragg CDI



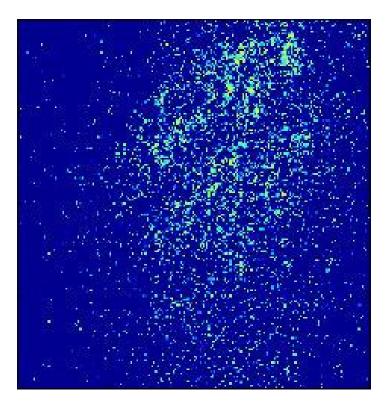


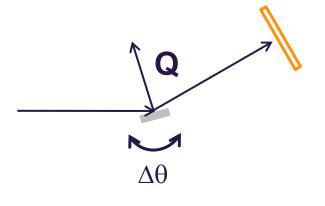




XFEL Tomography: 3D Bragg CDI

Rocking scan ($\Delta \theta$) sweeps the detectorplane through reciprocal space

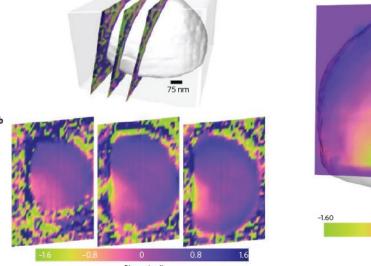




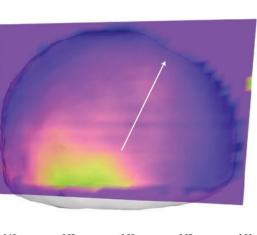
XFEL Tomography: 3D Bragg CDI

Rocking scan ($\Delta \theta$) sweeps the detectorplane through reciprocal space

Study of Pb nanocrystals



Phase (rad)



60 -0.95 -0.30 0.35 1.00

Phase (rad)

I. K. Robinson & R. Harder Nature Materials **8**, 291 (2009)

Q

 $\Delta \theta$

Work from APS, sector 34

XFEL Tomography: 3D ptychography



Ptychographic X-ray computed tomography at the nanoscale

Martin Dierolf¹, Andreas Menzel², Pierre Thibault¹, Philipp Schneider³, Cameron M. Kewish²[†], Roger Wepf⁴, Oliver Bunk² & Franz Pfeiffer¹

Nature 467, p. 436 (2010)

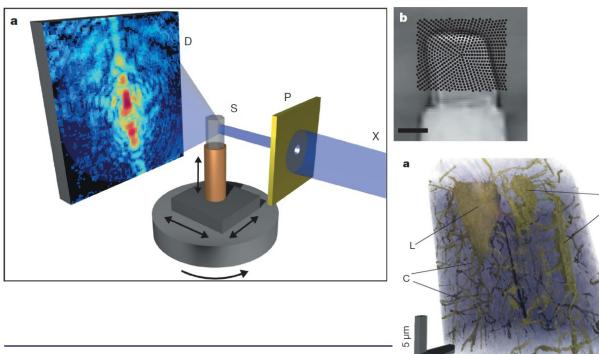
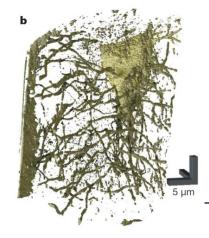
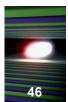


Figure 3 3D rendering of the tomographic reconstruction. a, Volume rendering with the bone matrix in translucent colours to show osteocyte lacunae (L) and the connecting canaliculi (C). b, Isosurface rendering of the lacunocanalicular network obtained by segmenting the corresponding peak in the density on histogram shown in Fig. 4c. Morphological analysis of tomographic reconstructions is most often based on this type of segmentation, which is independent of the absolute scale of the density. Long edges of 3D scale bars, 5 μm.

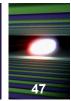






- Why is phase important
- How does phase retrieval work in coherent diffraction imaging
- How does phase retrieval work in ptychography
- How does phase retrieval work in holography
- Examples of published work
- 3D resolution is needed!

Next: X-ray sources, new opportunities with Free-electron lasers The European X-ray Free-Electron Laser in Hamburg **XFEL** Coherent Intensity



$$I_C = \lambda^2 B / 4^{(*)}$$

B: Brilliance (spectral brightness) of source $B: \frac{ph/s}{mm^2 mrad^2 \ 0.1\%BW}$

(*) only strictly valid for chaotic sources

European XFEL Development of X-ray sources

10³⁴

10³²

10³⁰

10²⁸

10²⁶

10²⁴

10²²

10²⁰

10¹⁸

10¹⁶

10¹⁴

10¹²

10¹⁰

10⁸

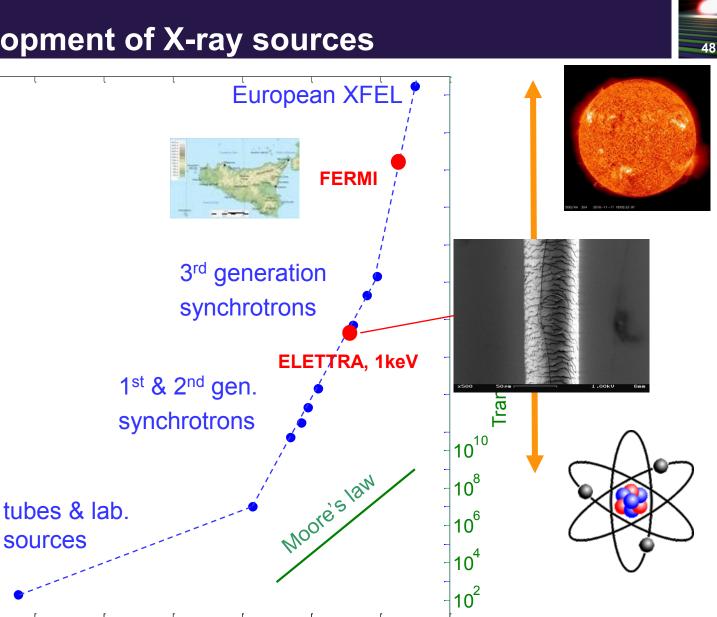
10⁶ '

1880

1900

1920

Peak Brilliance



2000

2020

1980

year

1940

1960



Soft X-Rays:

FLASH (Hamburg, Germany) FERMI (Trieste, Italy) [first x-ray laser] [first seeded x-ray laser]

Hard X-Rays:

. . .

LCLS (Stanford, USA) SACLA (Sayo, Japan) [first hard x-ray laser]

PAL-XFEL (Pohang, Korea), first beam ~2016 SwissFEL (Villingen, Switzerland), first beam ~2016 European XFEL (Hamburg, Germany), first beam ~2017

. . .





Undulator: Magnetic device installed in the straight sections of the synchrotron

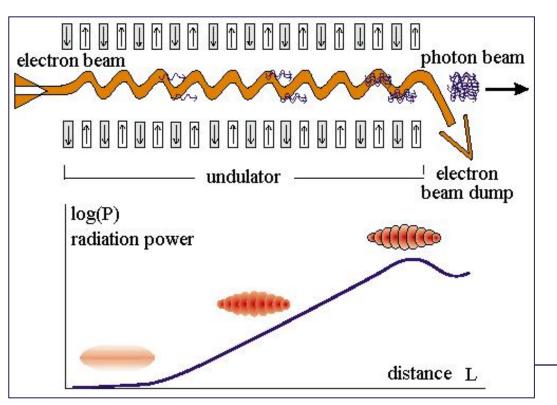
N~100 $\mathbf{F} = \mathbf{e}(\mathbf{v} \times \mathbf{B})$ magnetic poles 1st, 2nd and 3rd generation $I \propto N_e$ (Bending magnet) **Electron beam** Synchrotron light $I \propto N_e \cdot N$ (Wiggler) $I \propto N_e \cdot N^2$ (Undulator) Permanent magnet undulator

XFEL X-Ray Free-Electron Lasers



SASE: Self-Amplified Spontaneous Emission SR undulator: **2 - 5 m** SASE undulator at European XFEL: **175 m**

Operates with a linac feeding short (<100 fs) electron bunches into a long undulator



Interaction between intense EM-field and electrons leads to e-beam instability and micro-bunching of the electrons.

Micro-bunching gives lasing & saturation:

Coherent sum of emitted fields from all electrons

 $I \propto N_o^2$ for SASE

XFEL Self-Amplified Spontaneous Emission (SASE)



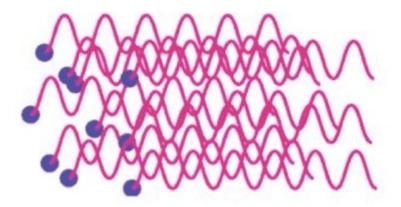
The "trick" of Free-Electron Lasers:

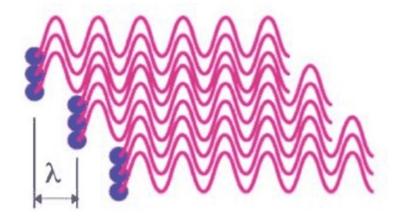
Spontaneous emission (SR)

Spontaneous emission (SASE)

Uncorrelated X-ray emission

Correlated X-ray emission



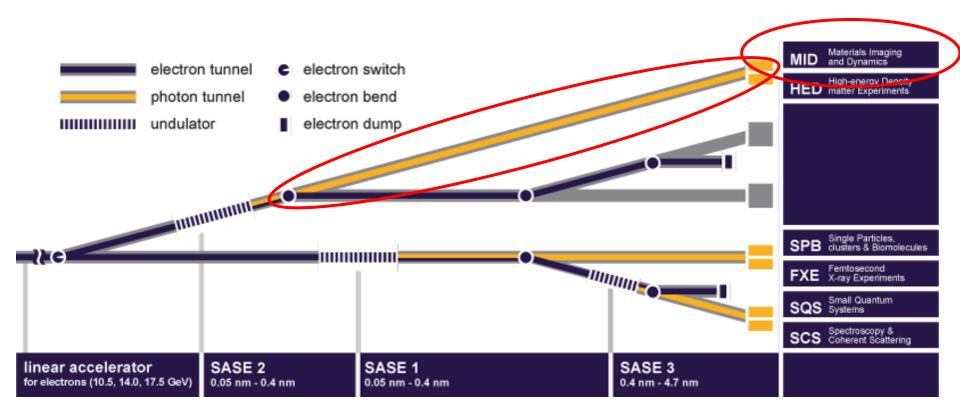


SASE: Self-Amplified Spontaneous Emission. First demonstrated at DESY (FLASH) in the soft X-ray range



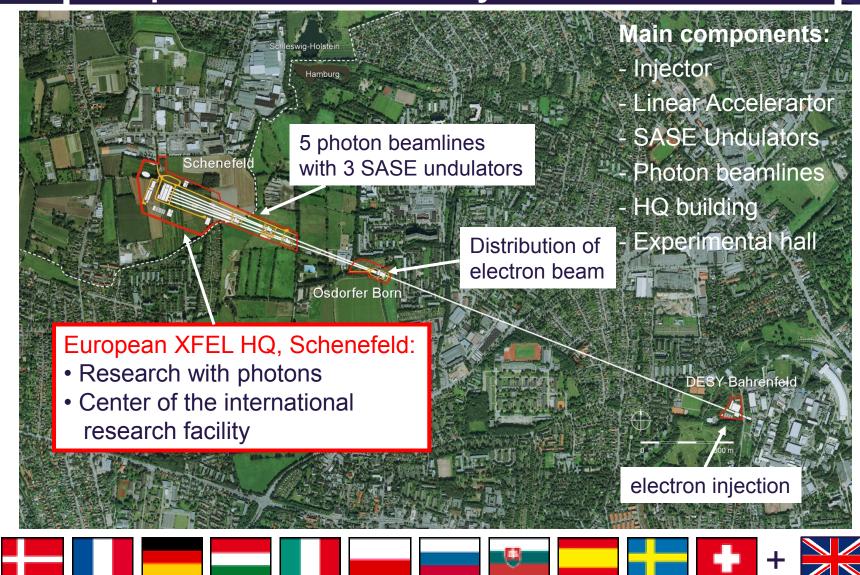


Materials Imaging and Dynamics Instrument @ SASE-2



XFEL European XFEL. Overall layout





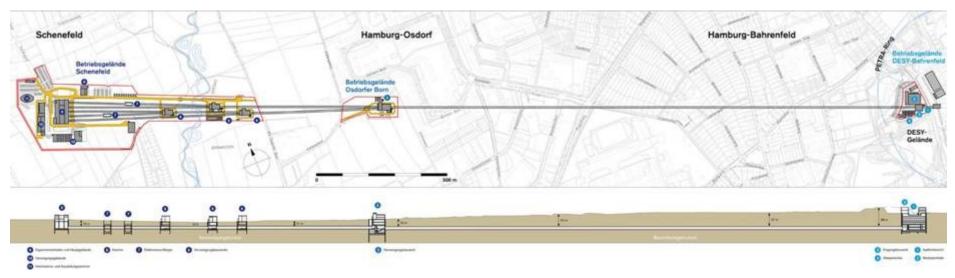
XFEL XFEL essentially an underground facility



Schenefeld

Osdorfer Born

Bahrenfeld



8 shafts and ca. 5.7 km tunnels, superconduction 2.1 km linac, 17.5 GeV Total straight length of facility: 3.4 km Underground experimental hall with 6 instruments, space for 6 more

XFEL Injector Installation and Commissioning



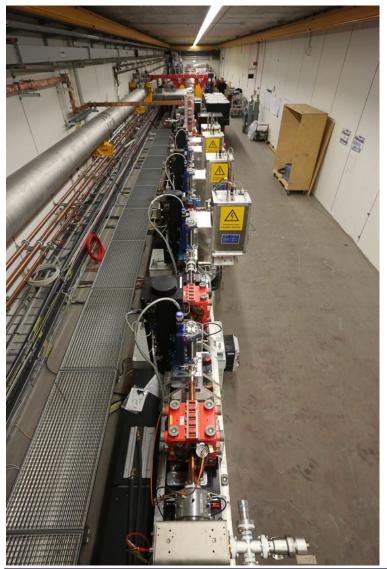






UNER Ithes Radiovale d Field Radiovale 56

XFEL Injector Installation and First Electron Beam



3.9 GHz module installed in 9/2015 Welding connections finished 10/2015 Isolation vacuum created

TÜV inspection on November 16th Injector cool-down started end of November

Christmas wish: first accelerated beam before end of the year



YES, WE DID IT! Dec 21, 2015: First electrons accelerated by injector (first 45 m of linac)

More info: www.xfel.eu

XFEL Linear Accelerator Modules





XFEL >65 modules (out of 100) installed in tunnel

Closing of tunnel: Sept 2016 Cool down to 4K starts...

59

XFEL SASE-1 Undulator (175 m magnetic length)



First 5 m segment installed in July 2015

Installation of all segments finished by end of:

SASE-1: **02.2016** SASE-3: **04.2016** SASE-2: **10.2016**





Status September 2015

and the

C

1200

XHQ – moving-in date: 4. June 2016

1000 111

10 000

0

34

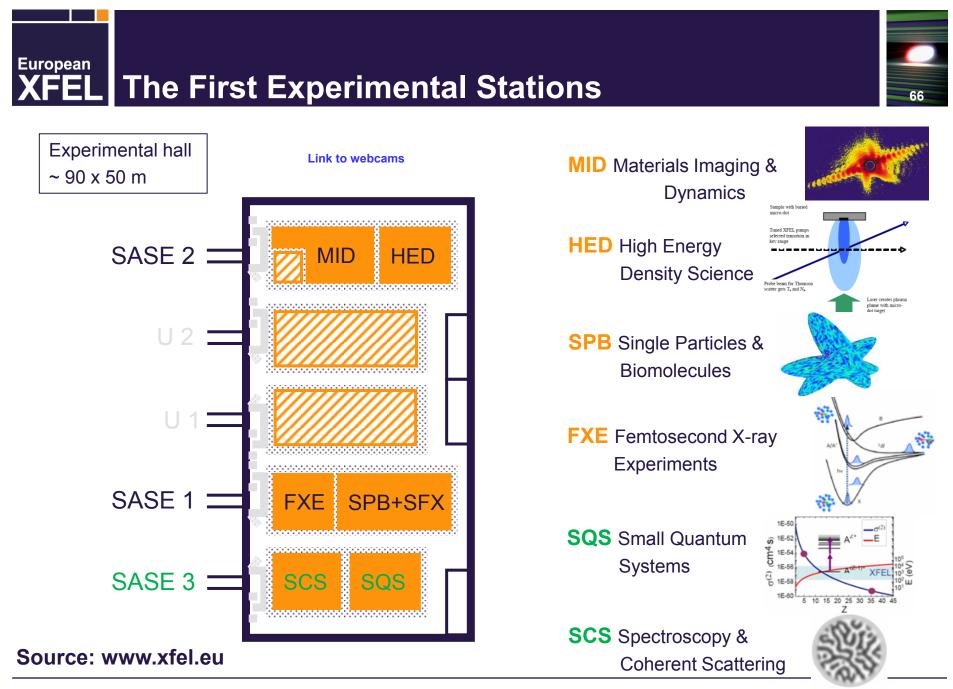
Batter

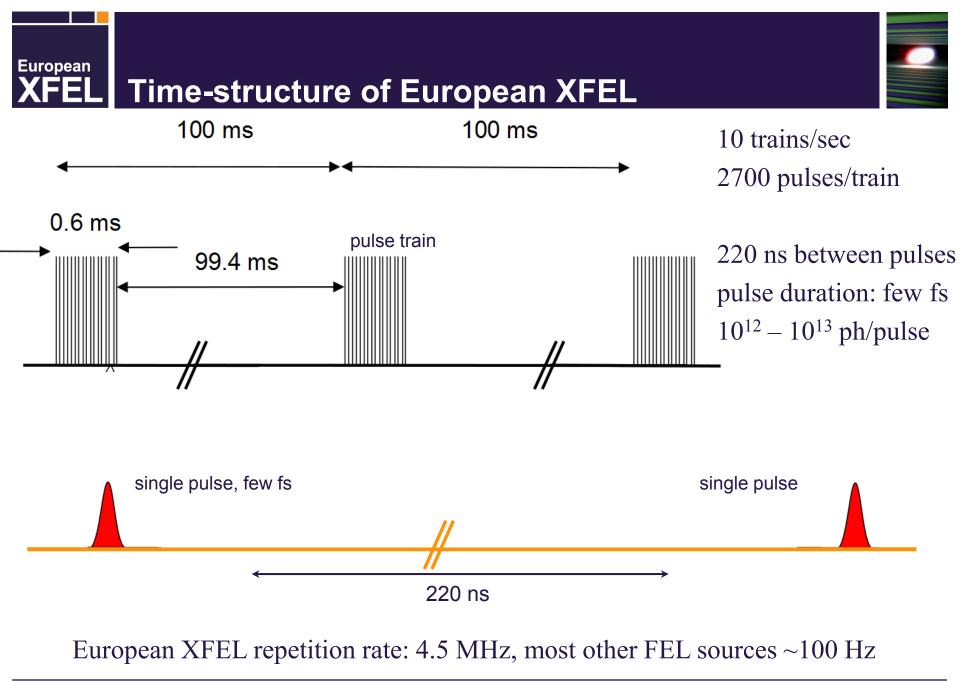
1

XFEL Underground Experimental Hall









The unique properties:

- Ultrafast time resolution
- Ultrahigh peak Brilliance at 4.5 MHz rep rate
- Ultrahigh average Brilliance (27000 pulses/s)
- Coherence of the XFEL beam

will enable completely new experiments to study structure and dynamics of materials

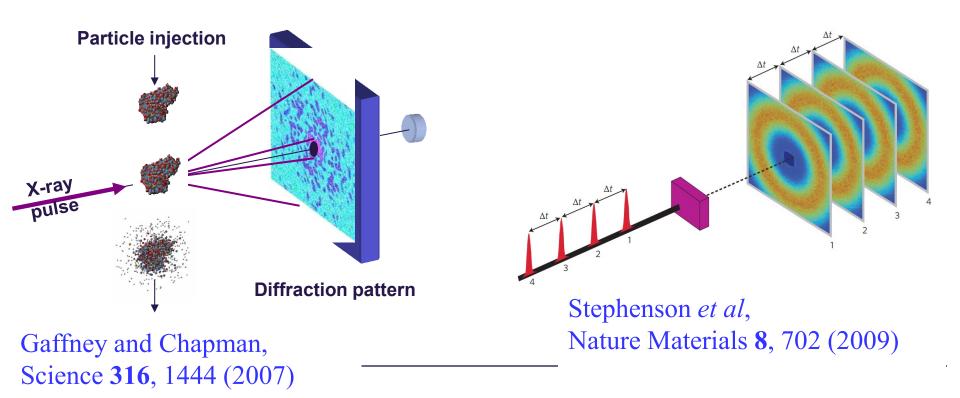


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Imaging of single molecules

Ultra-fast dynamics of molecules and materials

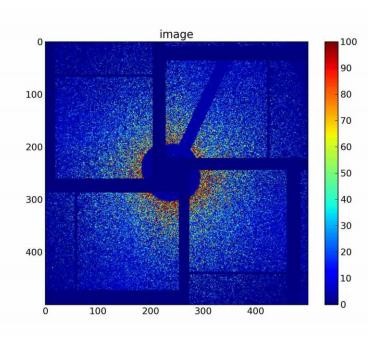




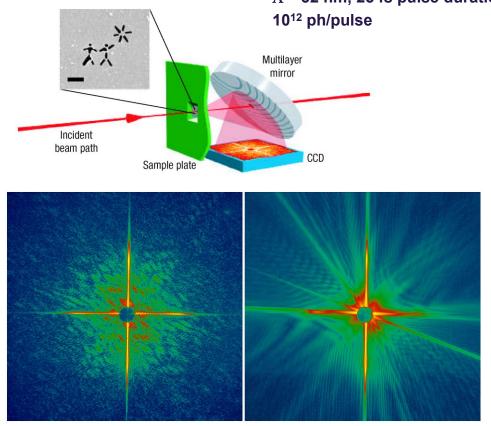


XFEL experiments can be destructive...

FLASH (DESY) Λ = 32 nm, 25 fs pulse duration, 10¹² ph/pulse



but not necessarily

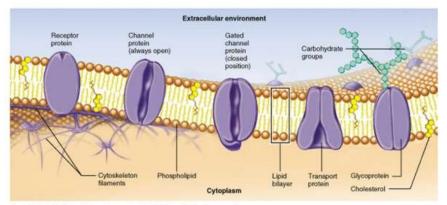


H. Chapman et al, Nature Physics 2, 839 (2006)

European **XFEL** Diffraction before destruction: Femto-second crystallography (destructive)



- Serial crystallography (sample injector)
- Femtosecond pulses (diffraction before destruction)
- Nanocrystals formed by most proteins

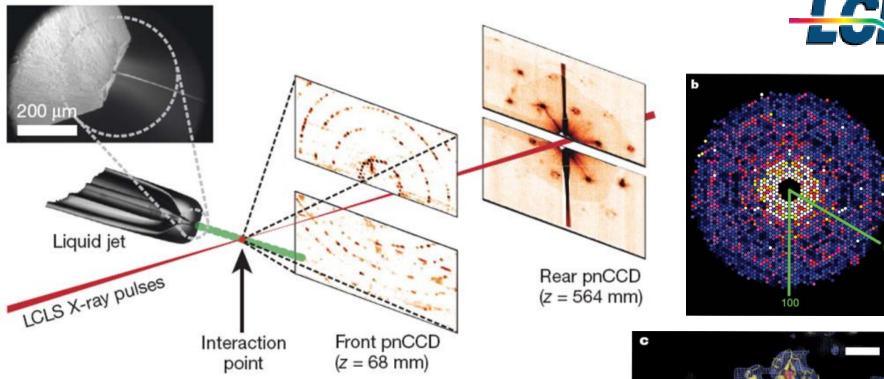


Copyright @ 2001 Benjamin Cummings, an imprint of Addison Wesley Longman, Inc.

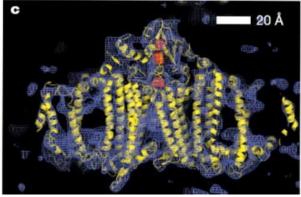


European **XFEL** Diffraction before destruction: Femto-second crystallography (destructive)





More than 3 million images collected Structure of Photosystem I determined (already known) Verification of diffraction before destruction in crystallography

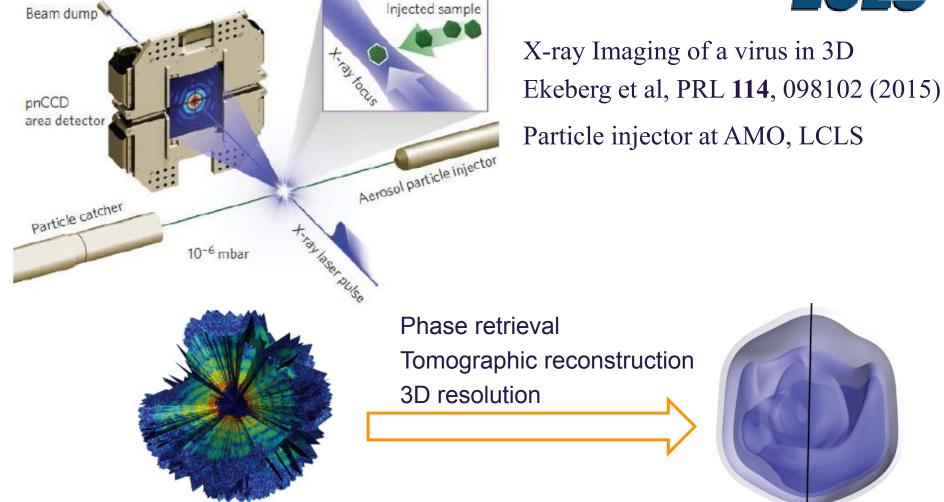


Chapman *et al*, Nature **470**, 73 (2011)

European **XFEL** Diffraction before destruction: CDI using single shot exposures

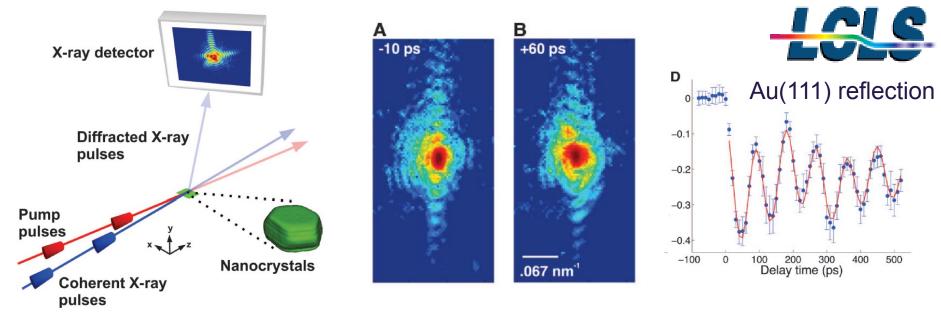






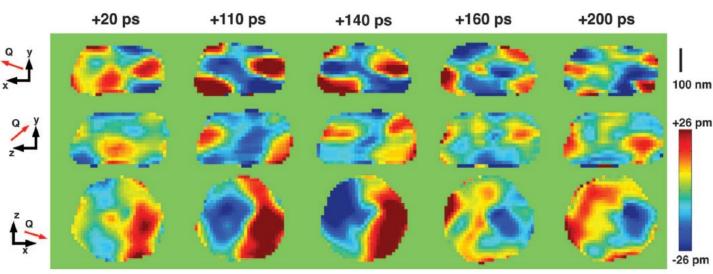
European Non-destructive XFEL Imaging: Combining CDI AFEL and pump-probe





Measuring phonons in Au nanocrystals by PP CDI at LCLS

J. Clark,...& I. Robinson, Science **341**, 56 (2013)

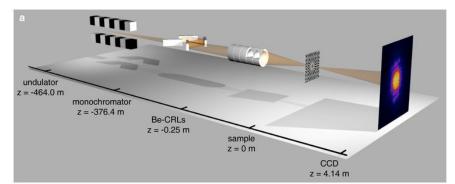


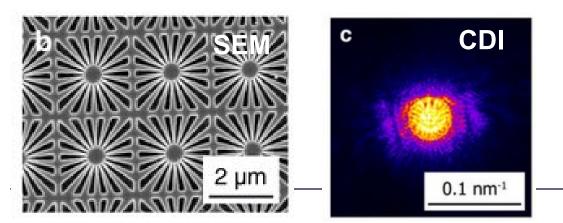
European Non-destructive XFEL Imaging: Ptychography **XFEL** using a Free-electron Laser



Full spatial characterization of a nanofocused x-ray free-electron laser beam by ptychographic imaging

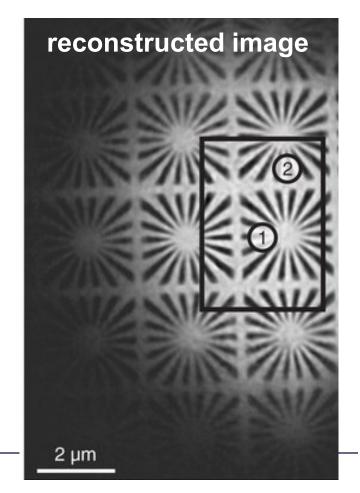
Andreas Schropp^{1,2}, Robert Hoppe¹, Vivienne Meier¹, Jens Patommel¹, Frank Seiboth¹, Hae Ja Lee², Bob Nagler², Eric C. Galtier², Brice Arnold², Ulf Zastrau², Jerome B. Hastings², Daniel Nilsson³, Fredrik Uhlén³, Ulrich Vogt³, Hans M. Hertz³ & Christian G. Schroer¹





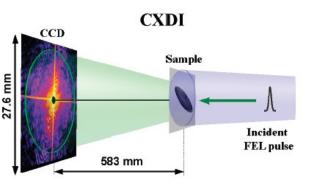


Sci. Rep. 3, 1633 (2013)

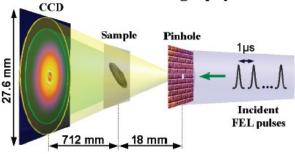


EuropeanNon-destructive XFEL Imaging: comparison ofXFELBio CXDI and Holography at FLASH

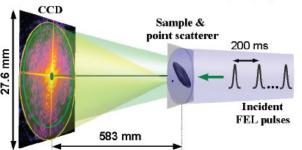




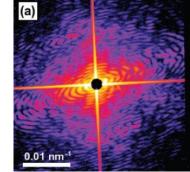
In-line Holography

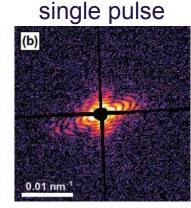


Fourier Transform Holography



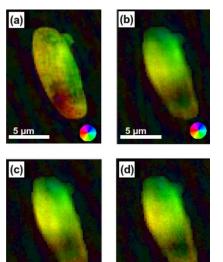
integrated





Unicellular algae (*Navicula perminuta*) 10 fs pulses, λ=8 nm ~1e10 ph/pulse

Integrated vs. single-shot reconstructions



Mancuso et al., New J. Phys. 12, 035003 (2010)

XFEL Summary



Coherent Diffraction Imaging is a method developed at synchrotron sources to overcome limitations of optics

- The phase retrieval is difficult but necessary to reconstruct the image from the measured Intensities
- Related methods exist that sometimes can make the phase retrieval easier
- 3D resolution is of course desired in many cases
- Novel X-ray laser sources promise a bright future for coherent imaging techniques but new experimental strategies are needed
- Femtosecond nano-crystallography is, until now, the biggest success of XFELs overall
- The combination of CDI and ultrafast science (fs-ns) is promising but only few experiments so far...

?? QUESTIONS ??



www.xfel.eu

lcls.slac.stanford.edu/

PAPER • OPEN ACCESS

Materials science in the time domain using Bragg coherent diffraction imaging

Ian Robinson^{1,2}, Jesse Clark³ and Ross Harder⁴ Published 14 March 2016 • © 2016 IOP Publishing Ltd Journal of Optics, Volume 18, Number 5

K. A. Nugent, Coherent methods in the X-ray sciences <u>https://arxiv.org/ftp/arxiv/papers/0908/0908.3064.pdf</u>





The End