Asymptotically free nonabelian Higgs models

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& Luca Zambelli, PRD 92, 025016 (2015) [arXiv:1502.05907], arXiv:16XX.YYYYY

Prologue: & M.M. Scherer, S. Rechenberger, L. Zambelli, EPJC 73, 2652 (2013)[arXiv:1306.6508], ...

ERG 2016, Trieste, September 2016

"If you got a problem, ...

... just put a scalar field"

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..., massive gauge bosons, symmetry breaking, CP problem...

... inflation, dark matter, dark energy, ...

Standard model Higgs sector

Extremely successful:



Price to be paid:

naturalness?

$$\delta m^2 \sim \Lambda^2$$

- # of parameters?
- UV completion? Triviality?

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• SUSY

• . . .

- technicolor
- extra-dim's



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FRG offers:

• . . .

+ gravity

[ERG'16: RAHMEDE,OHTA,EICHHORN]

asymptotic safety

[ERG'16:

Sannino,Bond,Litim,Buyukbese]

UV completion: triviality problem



▷ lattice evidence:

 \triangleright SU(*N*) action:

$$S = \int d^4x \Big[rac{1}{4} F^i_{\mu
u} F^{i\mu
u} + (D^\mu \phi)^\dagger (D_\mu \phi) + rac{1}{2} m^2 \phi^\dagger \phi + rac{\lambda}{8} (\phi^\dagger \phi)^2 \Big]$$
 $D^{ab}_
u = \partial_
u \delta^{ab} - i g W^i_
u (T^i)^{ab}$

▷ (too) naive argument:

- gauge coupling g is asymptotically free
- \implies UV theory may reduce to pure scalar sector
- \implies scalar triviality in λ

▷ closer look at perturbation theory:

(E.G., GROSS, WILCZEK'73)

$$\partial_t g^2 = \beta_{g^2} = -b_0 g^4$$

 $\partial_t \lambda = \beta_\lambda = A \lambda^2 - B' \lambda g^2 + C g^4$

(mass-independent reg'scheme, deep Euclidean region)

⊳ e.g., SU(2):

$$b_0 = \frac{43}{48\pi^2}, \quad A = \frac{3}{4\pi^2}, \quad B' = \frac{9}{16\pi^2}, \quad C = \frac{9}{64\pi^2}$$

▷ analytic solution:

$$\lambda(g^{2}) = -\frac{g^{2}}{2A} \left[B + \sqrt{\Delta} \tanh\left(\frac{\sqrt{\Delta}}{2b_{0}} \ln \frac{g_{\Lambda}^{2}}{g^{2}}\right) \right]$$
$$B = b_{0} - B' \quad , \quad \Delta = B^{2} - 4AC$$

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 $\lambda \sim g^2$, if $\Delta > 0$

BUT: $\Delta < 0$ for all SU($N \ge 2$):

 \implies Landau pole

▷ lattice studies:



(LANG ET AL'81; KUHNELT ET AL'83; JERSAK ET AL. 85; MAAS'13'15)

"Total" asymptotic freedom

$$B = b_0 - B'$$
 , $\Delta = B^2 - 4AC$

 $\triangleright \Delta$ can be made positive by adjusting *N* and adding fermions

(GROSS,WILCZEK'73; CHANG'74; FRADKIN,KALASHNIKOV'75; SALAM,STRATHDEE'78)

(CALLAWAY'88; GIUDICE ET AL.'14; HOLDOM, REN, ZHANG'14)

⊳ good news:

gauge-Higgs locking $\lambda \sim g^2$ implies $m_{\rm H}^2 \sim m_{W/Z}^2$... "reduction of couplings"

(ZIMMERMANN'84)

▷ bad news:

- residual symmetry generically too large: \geq SU(2)
- · many possibilities but no ordering principle

Asymptotically free Higgs sectors for $\Delta > 0$

 \triangleright gauge-Higgs locking: $\lambda \sim g^2$

▷ phase diagram in (λ, g^2) plane



Asymptotically free Higgs sectors for $\Delta > 0$

▷ flow of gauge-rescaled coupling:

$$\xi := \frac{\lambda}{g^2}, \qquad \partial_t \xi = \beta_\xi = g^2 \left[A \xi^2 + B \xi + C \right]$$

▷ phase diagram in (ξ, g^2) plane

> quasi fixed points:

$$eta_{\xi} = 0 \quad ext{at} \quad g^2 > 0$$
 $\implies \xi^*_+, \xi^*_-$



Things to ponder

· general relevance/meaning of quasi fixed points

 $\beta_{\xi} = 0$ at finite g^2

· different viewpoint: field rescalings, e.g.

$$\lambda \, \phi^4 = \xi \, \left(\sqrt{g} \, \phi \right)^4$$

 \implies for $\xi \to \xi^*$ and $g \to 0$: large amplitude fluctuations expected

... higher dimensional operators?

· life beyond the deep Euclidean region?

...quasi-fixed point potentials with a minimum? ...quasi-conformal vev?



▷ inclusion of higher-dimensional operators, e.g. potential:

$$U(\phi) = \frac{1}{2}m^2(\phi^{\dagger}\phi) + \frac{1}{8}\lambda(\phi^{\dagger}\phi)^2 + \frac{1}{48}\frac{\lambda_3}{\Lambda_{\text{eff}}^2}(\phi^{\dagger}\phi)^3 + \dots$$

 $ightarrow \Lambda_{eff}$: "UV" scale of effective field theory

▷ inclusion of higher-dimensional operators, e.g. potential:

$$U(\phi) = \frac{1}{2}m^2(\phi^{\dagger}\phi) + \frac{1}{8}\lambda(\phi^{\dagger}\phi)^2 + \frac{1}{48}\frac{\lambda_3}{k^2}(\phi^{\dagger}\phi)^3 + \dots$$

▷ k: sliding scale

in the ERG spirit (WETTERICH'93)

ightarrow UV behavior visible for $k
ightarrow\infty$

▷ inclusion of higher-dimensional operators, e.g. potential:

$$U(\phi) = \sum_{n=1}^{N_{\mathrm{p}}} rac{\lambda_{2n}}{n! k^{2(n-2)}} \left(rac{\phi^{\dagger} \phi}{2}
ight)^n$$

 \triangleright with $N_{\rm p} \rightarrow \infty$

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 \triangleright with $N_p \rightarrow \infty$

 \triangleright conventional studies: λ_1 and v can be ignored in deep Euclidean region "asymptotic symmetry"

(LEE,WEISBERGER'74)

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▷ structure of the RG flow:

$$\partial_t \lambda_n = \beta_{\lambda_n}(g^2, \lambda_1, \lambda_2, \dots, \lambda_{n+1})$$

 \implies infinite tower of coupled ODE's

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$$\begin{aligned} \partial_t \lambda_2 &= \beta_{\lambda_2}(g^2, \lambda_1, \lambda_2, \lambda_3) \\ \partial_t \lambda_3 &= \beta_{\lambda_2}(g^2, \lambda_1, \lambda_2, \lambda_3, \lambda_4) \\ \vdots & \vdots \end{aligned}$$

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 \triangleright e.g., truncating at $N_p = 2$ (in deep Euclidean region):

$$\partial_t \lambda_2 = \beta_{\lambda_2}(g^2, \lambda_1, \lambda_2, \lambda_3) \partial_t \lambda_3 = \beta_{\lambda_2}(g^2, \lambda_1, \lambda_2, \lambda_3, \lambda_4) \vdots \vdots \vdots$$

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BUT: since $\partial_t \lambda_3 \neq 0$, setting $\lambda_3 = 0$ is as good/bad as any other choice:

e.g.,
$$\lambda_3 = \text{const.}$$
 or $\lambda_3 = f(g^2)$

 \triangleright simplest "agnostic" approximation $N_p = 2$ (deep E):

$$\partial_t \lambda_2 = A \lambda_2^2 - B' \lambda_2 g^2 + C g^4 - D \lambda_3, \qquad D_{SU(2)} = \frac{1}{4\pi^2}$$

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 \implies asymptotically free trajectory, if

$$\lambda_3 = \zeta g^4, \qquad \zeta = const.$$

▷ integrated flow:

$$\lambda_2(g^2) = -\frac{g^2}{2A} \left[B + \sqrt{\Delta'} \tanh\left(\frac{\sqrt{\Delta'}}{2b_0} \ln \frac{g_A^2}{g^2}\right) \right]$$

 $\Delta' = B^2 - 4AC', \qquad C' = C - D\zeta$

 \implies one-parameter family of asymptotically free trajectories

Asymptotically free trajectory: simple approximation

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Asymptotically free trajectory: simple approximation

▷ gauge-rescaled coupling:

$$\xi_2 := \frac{\lambda_2}{g^2}, \qquad \partial_t \xi_2 = \beta_{\xi_2} = g^2 \left[A \xi_2^2 + B \xi_2 + C - D \zeta \right]$$

▷ phase diagram in (ξ_2, g^2) plane

quasi fixed points:

$$\beta_{\xi} = 0$$
 at $g^2 > 0$

 \implies perturbation about ξ^*_+ is RG irrelevant



Asymptotically free trajectory: higher-orders?

▷ same conclusion for any finite truncation

⊳ if

$$\lambda_{n+1} = \text{const.} \times g^{n-1}$$

 \implies one free parameter ζ .

Existence of asymptotically free trajectories?

Crucial questions:

- Does the series expansion $\sim \sum \lambda_n (\phi^\dagger \phi)^n$ sum up to a

global fixed point potential : $U^*(\phi)$?

 $\implies \zeta$ parameter \rightarrow boundary condition for $U^*(\phi)$

• Is $U^*(\phi)$ polynomially bounded (uniform convergence)?

(Bridle, Morris'16; Morris'98)

... "singularity count", "quantization" of fixed-point potentials

- Are perturbations about $U^*(\phi)$ self-similar? (Morris'98)

... quantization of RG directions, predictivity

Classification of perturbations?

...# of physical parameters, ...





P-scaling solutions

▷ ... yet another parameter:

general field rescalings $\phi \to g^{P} \phi \to \xi_{n} = g^{-2Pn} \lambda_{n}$



 $\implies \zeta$ and *P* parametrize boundary conditions for correlation functions



Functional RG analysis

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▷ RG flow equation:

(WETTERICH'93)

$$\partial_t \Gamma_k \equiv k \partial_k \Gamma_k = \frac{1}{2} \operatorname{Tr} \partial_t R_k (\Gamma_k^{(2)} + R_k)^{-1}$$
$$= \checkmark$$

▷ functional differential equation

- initial value problem in "RG time" t
- fixed point condition for effective potential:

2nd order ODE: 2 initial/boundary conditions

Functional RG analysis

 \triangleright RG flow of the dimensionless scalar potential, $u = k^{-d} U(\phi)$

$$\begin{aligned} \partial_{t}\boldsymbol{u} &= -d\boldsymbol{u} + (d-2+\eta_{\phi})\tilde{\rho}\boldsymbol{u}' + 2\boldsymbol{v}_{d} \left\{ (d-1)\sum_{i=1}^{N^{2}-1} l_{0}^{(G)d} \left(\boldsymbol{\mu}_{W,i}^{2}(\tilde{\rho})\right) + (2N-1)l_{0}^{(B)d} \left(\boldsymbol{u}'\right) + l_{0}^{(B)d} \left(\boldsymbol{u}' + 2\tilde{\rho}\boldsymbol{u}''\right) \right\} \\ \eta_{\phi} &= \frac{8\boldsymbol{v}_{d}}{d} \left\{ \tilde{\rho}(3\boldsymbol{u}'' + 2\tilde{\rho}\boldsymbol{u}''')^{2} m_{2,2}^{(B)d} \left(\boldsymbol{u}' + 2\tilde{\rho}\boldsymbol{u}'', \boldsymbol{u}' + 2\tilde{\rho}\boldsymbol{u}''\right) + (2N-1)\tilde{\rho}\boldsymbol{u}''^{2} m_{2,2}^{(B)d} \left(\boldsymbol{u}', \boldsymbol{u}'\right) \\ -2g^{2}(d-1)\sum_{a=1}^{N}\sum_{i=1}^{N^{2}-1} T_{\hat{p}a}^{i} T_{a\hat{p}}^{i} l_{1,1}^{(BG)d} \left(\boldsymbol{u}', \boldsymbol{\mu}_{W,i}^{2}\right) + (d-1)\sum_{i=1}^{N^{2}-1} \frac{\boldsymbol{\mu}_{W,i}^{4}}{\tilde{\rho}} \left[2a_{1}^{d} \left(\boldsymbol{\mu}_{W,i}^{2}\right) + m_{2}^{(G)d} \left(\boldsymbol{\mu}_{W,i}^{2}\right) \right] \right\} \Big|_{\tilde{\rho} = \tilde{\rho}_{min}} \end{aligned}$$

 \triangleright 2nd order PDE in *k* and ϕ

(HG,Scherer,Rechenberger,Zambelli'13)

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▷ gauge-rescaled variables:

(HG,ZAMBELLI'15)

$$x = g^{2P} \frac{Z_{\phi} |\phi|^2}{k^2}, \quad f(x) = u$$

$$\partial_t f = \beta_f \equiv -4f + (2 + \eta_\phi - P\eta_W) x f' \\ + \frac{1}{16\pi^2} \left\{ 3 \sum_{i=1}^{N^2 - 1} l_{0T}^{(G)4} (g^{2(1-P)} \omega_{W,i}^2(x)) + (2N-1) l_0^{(B)4} (g^{2P} f') + l_0^{(B)4} (g^{2P} (f' + 2xf'')) \right\}$$

Global fixed point solution I

weak-coupling expansion

e.g., for P = 1 and SU(2):

$$f^*(x) = \zeta x^2 - \left(\frac{3}{16\pi}\right)^2 \left[2x + x^2 \ln\left(\frac{x}{2+x}\right)\right]$$

fixed-point solution \sim Coleman-Weinberg type, one-parameter family ζ

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▷ leading-order scaling solution for different *P*:

$$f(x) = \begin{cases} \zeta x^2 - \xi \frac{3}{16\pi^2} g^{2P} x & \text{for } P \in (0, 1/2) \\ \zeta x^2 - \frac{3(3+8\zeta)}{128\pi^2} g x & \text{for } P = 1/2 \\ \zeta x^2 - \frac{9}{128\pi^2} g^{2(1-P)} x & \text{for } P \in (1/2, 1) \end{cases}$$

(HG,ZAMBELLI'15)

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Asymptotically free UV gauge scaling solutions

 \triangleright gauge scaling towards flatness, P = 1

(RECHENBERGER,SCHERER,HG,ZAMBELLI'13; HG,ZAMBELLI'15)



 \triangleright approach to UV $k \rightarrow \infty$:

$$g^2
ightarrow 0, \quad |\phi_{\min}|^2 \sim rac{1}{g^2}
ightarrow \infty, \quad \underline{\lambda \sim g^4
ightarrow 0}, \quad rac{m_W^2}{k^2}
ightarrow {
m const.}$$

 \implies deep Euclidean region is sidestepped

... no "asymptotic symmetry"

Asymptotically free perturbations

 \triangleright classification of (ir-)relevant perturbations for given ζ and *P*:



Global fixed point solution II

 \triangleright origin of the free parameter ζ :

▷ "singularity count"

(Dietz, Morris'12; Demmel, Saueressig, Zanusso'15)

e.g. scalar models:
$$u^{\prime\prime}=-rac{1}{
ho}\,rac{e(u,\,u^\prime;\,
ho)}{s(u,\,u^\prime;\,
ho)}, \quad
ho=rac{1}{2}|\phi|^2$$

$$2^{nd}$$
 order PDE
1 fixed singularity at $\rho = 0$
1 movable singularity at $s(u, u'; \rho) = 0$
 $\Rightarrow 2 - 1 - 1 = 0$

 \implies 0 parameter family of solutions: only discrete "quantized" solutions ...e.g., Wilson-Fisher FP in d = 3

Global fixed point solution II

 \triangleright origin of the free parameter ζ :

▷ "singularity count"

nonabelian Higgs model: $f'' = -\frac{1}{x} \frac{e(f, f'; x)}{s(f, f'; x)}$

$$2^{nd} \text{ order PDE} \\ 1 \text{ fixed singularity at } \rho = 0 \\ 1 \text{ movable singularity at } s(f, f'; x) = 0 \end{cases} \Longrightarrow 2 - 1 - 1 = 0 ?$$

Global fixed point solution II

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nonabelian Higgs model:
$$f'' = -\frac{e(f, f'; x)}{x s(f, f'; x)}$$

$$2^{nd} \text{ order PDE} \\ \frac{1 \text{ fixed singularity at } \rho = 0}{1 \text{ movable singularity at } s(f, f'; x) = 0} \end{cases} \Longrightarrow 2^{-1} - 1 = 1$$

BUT: gauge loop induces log-like singularity at x = 0

with f and f' regular at x = 0

/ - - · ·

 \implies **1** parameter family of solutions: ζ



Estimates of IR Observables

Higgs to W boson mass ratio:

$$rac{m_{
m H}^2}{m_W^2} \sim c_P \zeta$$

UV-IR mapping of physical parameters:



$$\left. \begin{array}{c} v \\ m_{\rm H} \\ m_W \end{array} \right\} \quad \Longleftrightarrow \quad \left\{ \begin{array}{c} \delta m^2 & {\rm relevant} \\ \delta g^2 \oplus \delta f & {\rm marginal-relevant} \\ \zeta, P & {\rm ``exactly marginal''} \end{array} \right.$$

 \implies pheno-relevant parameter regime is accessible

Conclusions

- Interplay: asymptotic freedom \longleftrightarrow boundary conditions

b.c.'s for correlation functions

Non-abelian Higgs models can be asymptotically free and UV complete

if our choice of b.c.'s is legitimate

· scaling solutions satisfy necessary criteria

self-similarity, boundedness, predictivity

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