# Foundation of Modern Computer Architectures for HPC 

Ivan Girotto - igirotto@ictp.it
Information \& Communication Technology Section (ICTS)
International Centre for Theoretical Physics (ICTP)

## TO DO

## \$cd /scratch/

## \$mkdir \$USER

\$cd \$USER
\$scp hp83-inf-21:/scratch/ca_lab.tar.gz

## Exercises

## 1. Matrix Multiplication

2. Matrix Transpose

## MATRIX MUITIPIICATION



$$
C[i][j]=\operatorname{sum}(A[i][k] * B[k][j]) \text { for } k=0 \ldots n
$$

In our case:
C[1][1] $\Rightarrow$
$\mathrm{A}[1][0] * \mathrm{~B}[0][1]+\mathrm{A}[1][1] * \mathrm{~B}[1][1]+\mathrm{A}[1][2] * \mathrm{~B}[2][1]+\mathrm{A}[1][3] * \mathrm{~B}[3][1]+\mathrm{A}[1][4] * \mathrm{~B}[4][1]$

## Transpose

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 1 | 5 | 9 | 13 |
| :---: | :---: | :---: | :---: |
| 2 | 6 | 10 | 14 |
| 3 | 7 | 11 | 15 |
| 4 | 8 | 12 | 16 |

## Fast Transpose - Step 1

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 1 | 2 |
| :--- | :--- |
| 5 | 6 |


| 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

- Copy the data on the buffer block


## Fast Transpose - Step 2

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 1 | 5 |
| :--- | :--- |
| 2 | 6 |


| 0 | 0 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

- Transpose the block


## Fast Transpose - Step 3

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 1 | 5 |
| :--- | :--- |
| 2 | 6 |


| 1 | 5 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

- Copy the transposed block from the buffer block to the destination matrix


## Fast Transpose - Step 4

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 3 | 4 |
| :--- | :--- |
| 7 | 8 |


| 1 | 5 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

- Iterates over blocks


## Fast Transpose - Step 5

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 3 | 7 |
| :--- | :--- |
| 4 | 8 |


| 1 | 5 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | 0 |
| 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 |

- Iterates over blocks


## Fast Transpose - Step 6

| 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: |
| 5 | 6 | 7 | 8 |
| 9 | 10 | 11 | 12 |
| 13 | 14 | 15 | 16 |


| 3 | 7 |
| :--- | :--- |
| 4 | 8 |


| 1 | 5 | 0 | 0 |
| :--- | :--- | :--- | :--- |
| 2 | 6 | 0 | 0 |
| 3 | 7 | 0 | 0 |
| 4 | 8 | 0 | 0 |

- Iterates over blocks

