

Parallelism Inherent in the Wavefront Algorithm

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The Benchmark code



- Particle transport code using wavefront algorithm
 - Primarily used for benchmarking
- Coded in Fortran 90 and MPI
 - Scales to thousands of cores for large problems
- Over 90% of time in one kernel at the heart of the computation



Serial Algorithm Outline

```
Outer iteration
    Loop over energy groups
        Inner iteration
            Loop over sweeps
                Loop over cells in z direction
                    Loop over cells in y direction
                        Loop over cells in x direction
                            Loop over angles (only independent loop!)
                               work (90% of time spent here)
                            End loop over angles
                         End loop over cells in x direction
                     End loop over cells in y direction
```



Close up of parallelised loops over cells

Loop over cells in z direction Possible MPI_Recv communications Loop over cells in y direction Loop over cells in x direction Loop over angles (number of angles too small for MPI) work End loop over angles End loop over cells in x direction End loop over cells in y direction Possible MPI_Ssend communications End loop over cells in z direction

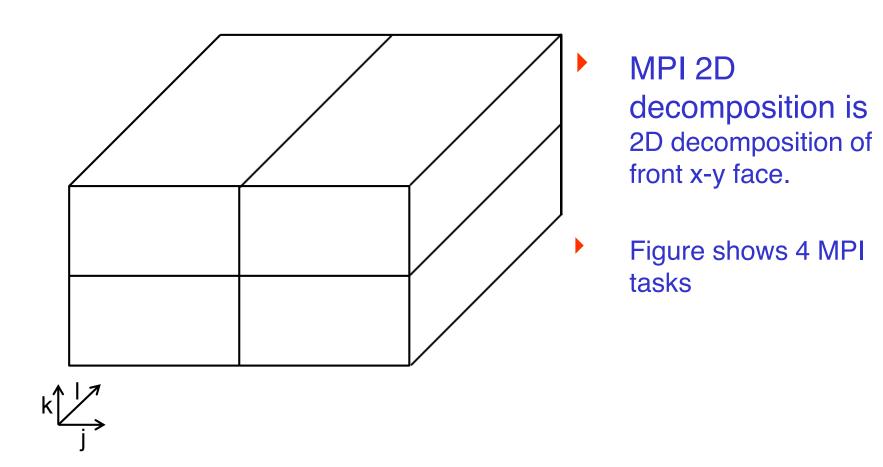
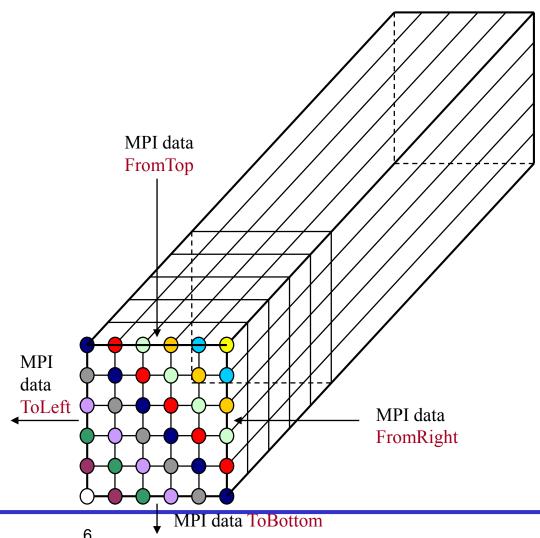


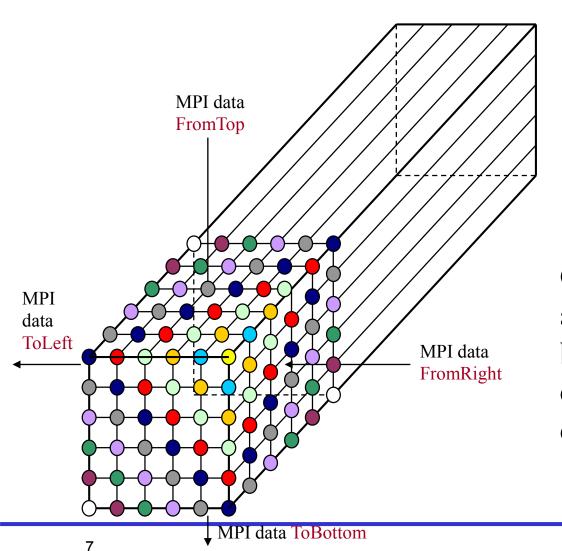
Diagram of dependicies



- This diagram shows the domain of one MPI task
- A cell cannot be processed until all cells "upstream" have been processed.



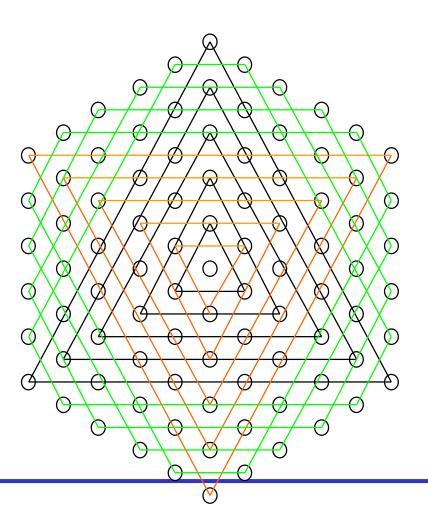
Sweep order: 3D diagonal slices



Cells of the same colour are independent and may be processed in parallel once preceding slices are complete.



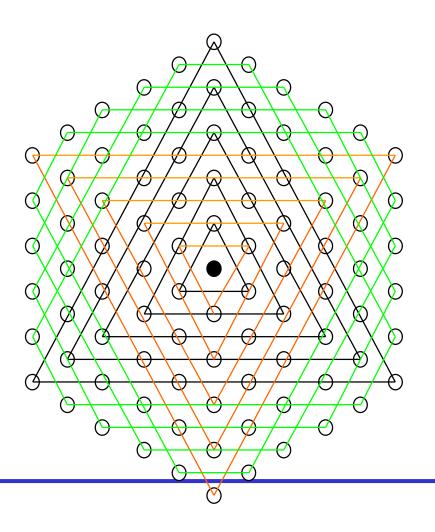
Slice shapes (6x6x6)



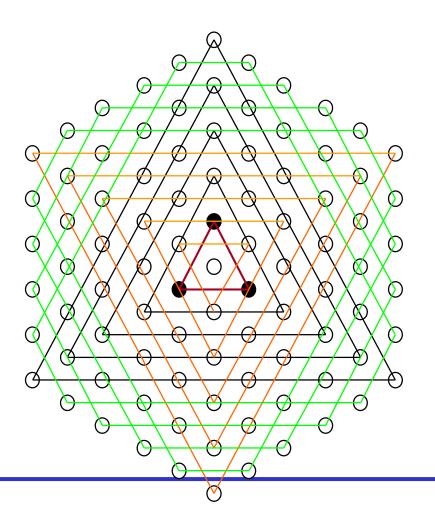
Increasing triangles

Then transforming Hexagons

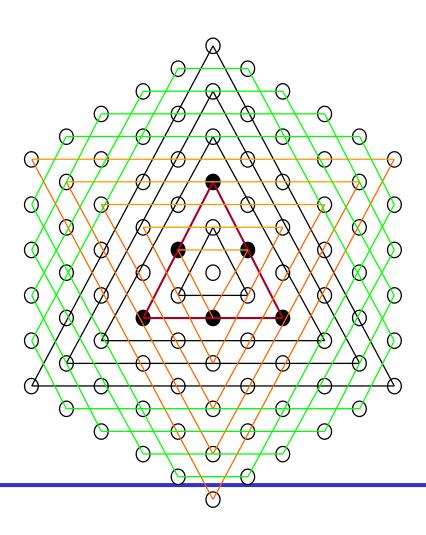
Then decreasing (flipped) triangles

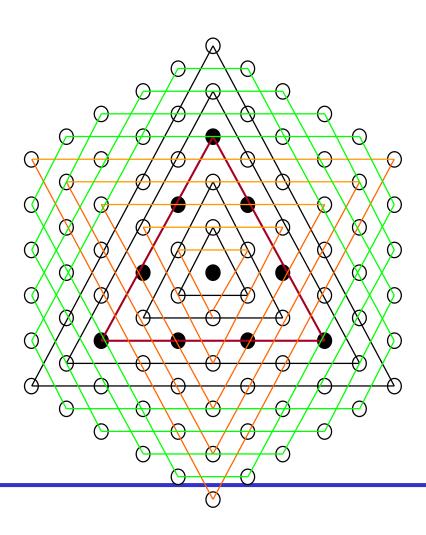


Cell nearest the viewer

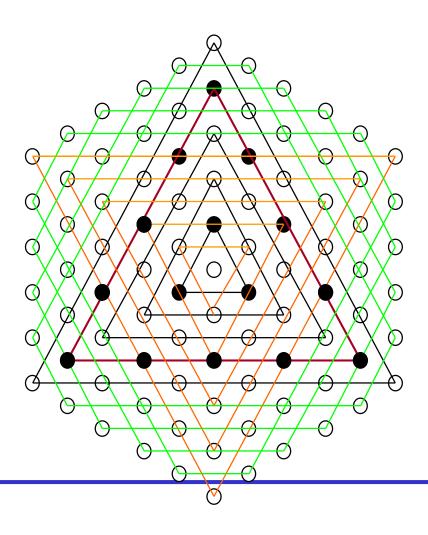


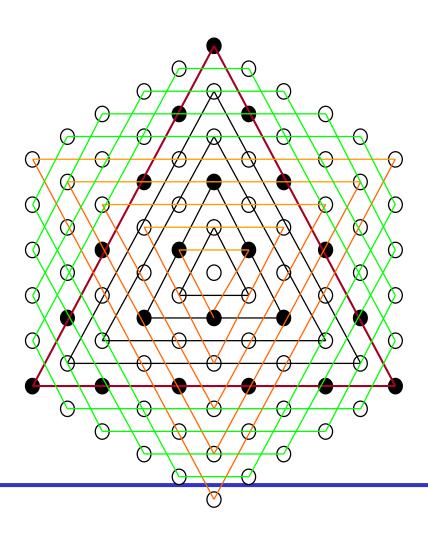
Moving down away from viewer



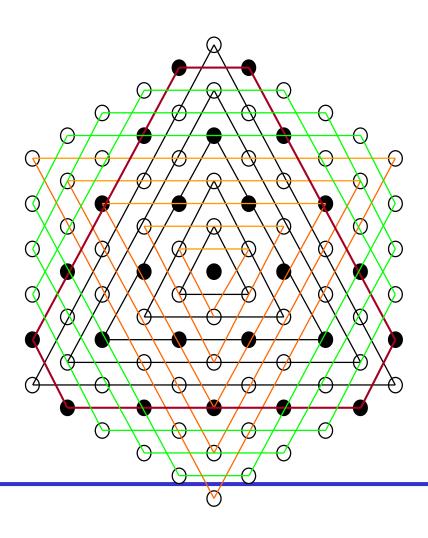




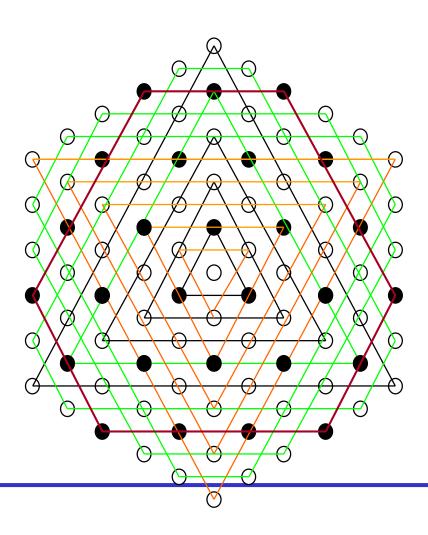




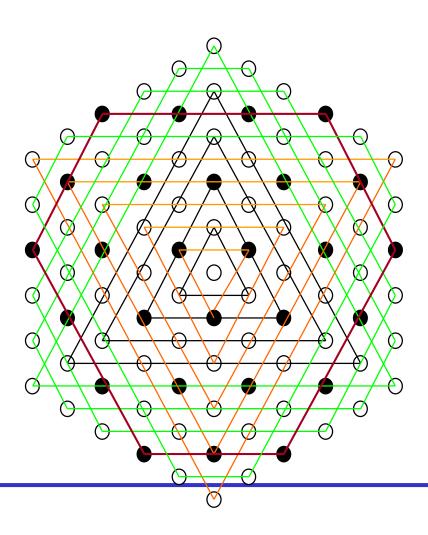




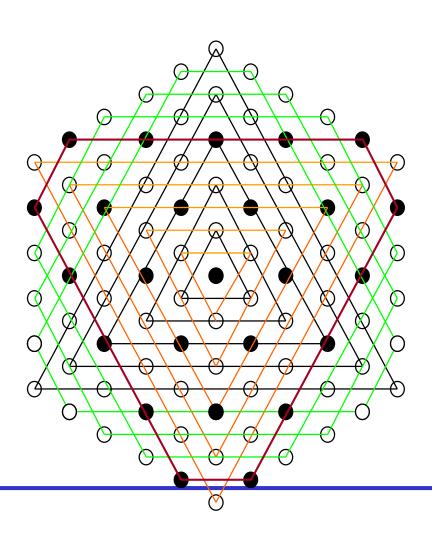




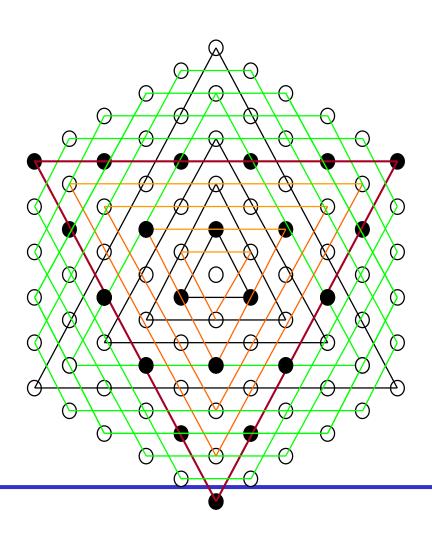




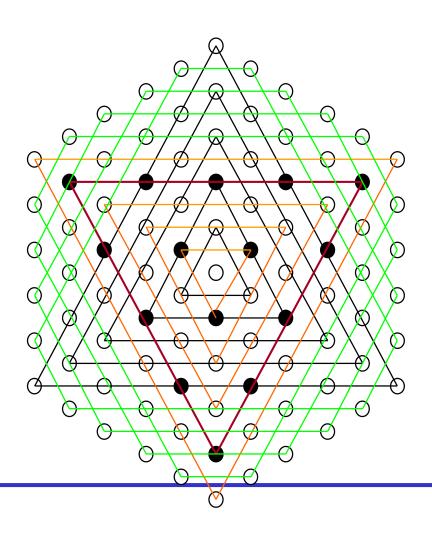




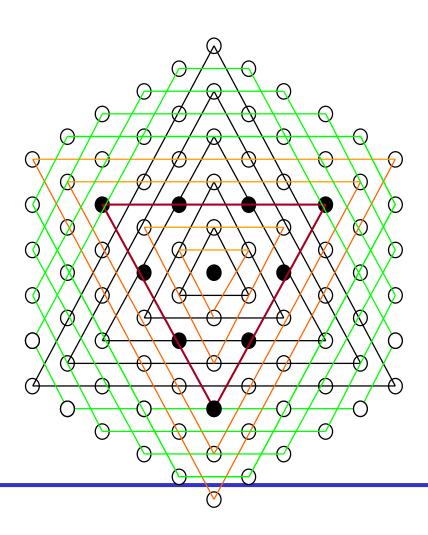




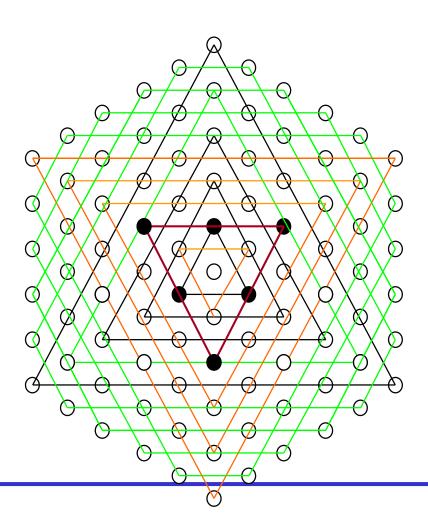




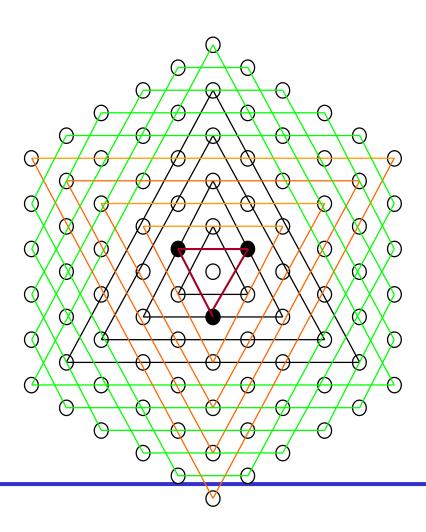


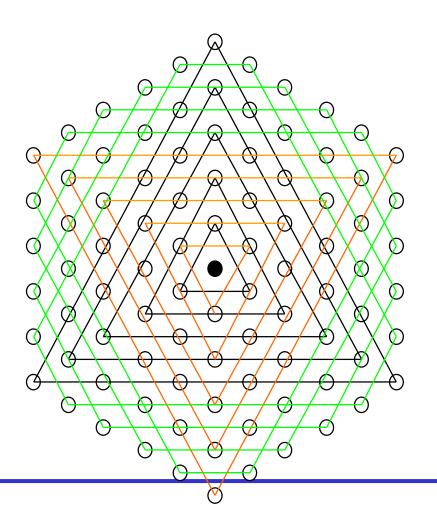












Point furthest from viewer



Close up of parallelised loops over cells using MPI

```
Loop over cells in z direction
   Possible MPI_Recv communications
   Loop over cells in y direction
       Loop over cells in x direction
           Loop over angles (number of angles too small for MPI)
              work
           End loop over angles
        End loop over cells in x direction
    End loop over cells in y direction
    Possible MPI_Ssend communications
End loop over cells in z direction
```



Close up of parallelised loops over cells using MPI and OpenMP

. . .

```
Loop over slices
   Possible MPI_Recv communications
   OMP DO PARALLEL
    Loop over cells in each slice
       OMP DO PARALLEL
       Loop over angles
          work
       End loop over angles
       OMP END DO PARALLEL
   End Loop over cells in each slice
   OMP END DO PARALLEL
    Possible MPI Ssend communications
End loop over slices
```

. . .



Parallel Algorithm Outline

```
Outer iteration
   Loop over energy groups
       Inner iteration
           Loop over sweeps
               Loop over slices
                  Possible MPI_Recv communications
                  OMP DO PARALLEL
                    Loop over cells in each slice
                      OMP DO PARALLEL
                       Loop over angles
                         work
                       End loop over angles
                       Etc
```



Decoupling inter-dependant energy group calculations

- Initially, each energy group calculation used a previous energy groups results as input
- Decoupling the energy groups has two outcomes
 - Execution time is greatly increased
 - Energy Groups are now independent and can be parallelised
- Often seen in HPC
 - Modern algorithms can be inherently serial
 - An older version may be parallelisable



- If all the tasks take the same time to compute
 - Block distribution of tasks
 - Cyclic distribution of tasks
 - "dealing cards"
- else if all tasks have different execution times
 - If length of tasks are unknown in advance
 - Cyclic distribution of tasks
 - else
 - Order tasks: longest first, shortest last
 - Cyclic distribution of tasks
 - endif
- Endif



Final Parallel Algorithm Outline

```
Outer iteration
   MPI Task Farm of energy groups
       Inner iteration
           Loop over sweeps
               Loop over slices
                  Possible MPI_Recv communications
                  OMP DO PARALLEL
                    Loop over cells in each slice
                      OMP DO PARALLEL
                       Loop over angles
                         work
                      End loop over angles
                      Etc
```

Other wavefront codes have the loops in a different order

- Loop over energy groups can occur within loops over cells and might be parallelised with OpenMP
 - Must be decoupled

- Any questions?
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