BED Applications in Practice

The main application of the BED model is to design and/or compare different fractionation or dose-rate schemes

Examples of the use of the BED model

- Simple fractionation changes
- Conversion to 2 Gy/fraction equivalent dose
- Effect of change in overall treatment time
- Correction for rest periods
- Change in dose rate
- Conversion from LDR to HDR
- Effect of half life on permanent implant doses

Example 1: simple change in fractionation

- Question: what dose/fraction delivered in 25 fractions will give the same probability of late normal tissue damage as 60 Gy delivered in 30 fractions at 2 Gy/fraction?
- The L-Q equation is:

$$BED = Nd \left(1 + \frac{d}{\alpha / \beta} \right)$$

Assuming α/β for late reacting normal tissues is 3 Gy, the BED for 60 Gy at 2 Gy/fraction is 60(1 + 2/3) = 100

Solution (cont'd) Then the dose/fraction, d, is given by: 100 = 25d(1 + d/3)Solving this quadratic equation for d gives: d = 2.27 Gy/fraction

Example 2

What total dose given at 2 Gy/fraction is equivalent to 50 Gy delivered at 3 Gy/fraction for (a) cancers with $\alpha/\beta = 10$ Gy? (b) normal tissues with $\alpha/\beta = 3$ Gy? Answers (a) $D_2 = 50(1 + 3/10)/(1 + 2/10) = 54.2$ Gy (b) $D_2 = 50(1 + 3/3)/(1 + 2/3) = 60.0 \text{ Gy}$

Example 3: change in fractionation accounting for repopulation

- Problem: it is required to change a fractionation scheme of 60 Gy delivered in 30 fractions at 2 Gy/fraction over 42 days to 10 fractions delivered over 14 days
- What dose/fraction should be used to keep the same effect on cancer cells and will the new scheme have increased or decreased effect on late-reacting normal tissues?

Solution I: assume no repopulation and no geometrical sparing

Assuming the tumor $\alpha/\beta = 10$ Gy, the tumor BED for 30 fractions of 2 Gy is: BED_t = 30 x 2(1 + 2/10) = 72 Then, for this same BED in 10 fractions of dose *d*/fraction:

 $72 = 10 \times d(1 + d/10)$ The solution to this quadratic equation is: d = 4.85 Gy

Solution I (cont'd.): effect on late-reacting normal tissues

Assuming the late-reacting normal tissue $\alpha/\beta = 3$ Gy, the normal tissue BED for 30 fractions of 2 Gy is:

 $\mathsf{BED}_I = 30 \times 2(1 + 2/3) = 100$

and the normal tissue BED for 10 fractions of 4.85 Gy is:

 $BED_{I} = 10 \times 4.85(1 + 4.85/3) = 127$ It appears that the 10 fraction scheme is far more damaging to normal tissues (127 vs. 100)

Solution II: assume a geometrical sparing factor of 0.6

The dose to normal tissues will now be $2 \times 0.6 = 1.2$ Gy for the 30 fraction treatments and $4.85 \times 0.6 =$ 2.91 Gy for the 10 fraction treatments Then the BEDs for normal tissues will be: $BED_1 = 30 \times 1.2(1 + 1.2/3) = 50$ $BED_1 = 10 \times 2.91(1 + 2.91/3) = 57$ It appears that the 10 fraction scheme is somewhat more damaging to normal tissues (57 vs. 50)

Solution III: assume geometrical sparing and repopulation (at k = 0.3/day) Now we need to recalculate the tumor BEDs The tumor BED for 30 fractions of 2 Gy is: $BED_t = 30 \times 2(1 + 2/10) - 0.3 \times 42 = 55.2$ Then, for this same BED in 10 fractions of dose *d*/fraction: $55.2 = 10 \times d(1 + d/10) - 0.3 \times 14$ The solution to this quadratic equation is:

d = 4.26 Gy

Solution III (cont'd.): effect on late reactions

The dose to normal tissues will still be $2 \times 0.6 = 1.2$ Gy for the 30 fraction treatments but will become 4.26 x 0.6 = 2.56 Gy for the 10 fraction treatments Then the BEDs for normal tissues will be: $BED_1 = 30 \times 1.2(1 + 1.2/3) = 50$ $BED_1 = 10 \times 2.56(1 + 2.56/3) = 47$ It appears that the 10 fraction scheme is now somewhat less damaging to normal tissues (47 vs. 50)

What does this mean?

 Decreasing the number of fractions, i.e. hypofractionation, does not necessarily mean increasing the risk of normal tissue damage when keeping the effect on tumor constant

 This is why we may be using far more hypofractionation in the future, especially since it will be more costeffective

Example 4: Rest period during treatment

 Problem: a patient planned to receive 60 Gy at 2 Gy/fraction over 6 weeks is rested for 2 weeks after the first 20 fractions

 How should the course be completed at 2 Gy/fraction if the biological effectiveness is to be as planned?

Solution I: for latereacting normal tissues

 Since late-reacting normal tissues probably do not repopulate during the break, they do not benefit from the rest period so the dose should not be increased

 Complete the course in 10 more fractions of 2 Gy

Solution II: for cancer cells

- Assume that the cancer is repopulating at an average rate, so k = 0.3 BED units/day and α/β = 10 Gy
- For a rest period of 14 days, the BED needs to be increased by 14 x 0.3 = 4.2
- The BED for the additional *N* fractions of 2 Gy is then: $2N(1 + 2/10) - (7/5)N \times (0.3)$ which must equal 4.2 Solution is N = 2.12

i.e. instead of 10 fractions you need about 12 fractions of 2 Gy But remember, the effect on normal tissues will increase

Excellent reference work



The timely delivery of radical radiotherapy: standards and guidelines for the management of unscheduled treatment interruptions, Third edition, 2008

Board of Faculty of Clinical Oncology The Royal College of Radiologists

Example 5: change in dose rate

 A radiation oncologist wants to convert a 60 Gy implant at 0.5 Gy/h to a higher dose rate of 1 Gy/h, keeping the effect on the tumor the same

• What total dose is required?

The BED equation for LDR treatments

$$BED = Rt \left[1 + \frac{2R}{\mu(\alpha / \beta)} \left\{ 1 + \frac{1 - e^{-\mu t}}{\mu t} \right\} \right]$$

where

 $R = \text{dose rate (in Gy h}^{-1})$ t = time for each fraction (in h) $\mu = \text{repair-rate constant (in h}^{-1})$

Simplified forms of the LDR BED equation

 $For 10h \le t \le 100h$ $BED = Rt \left[1 + \frac{2R}{\mu(\alpha / \beta)} \left\{ 1 + \frac{1}{\mu t} \right\} \right]$ $For t \ge 100h$

 $BED = Rt \left[1 + \frac{2R}{\mu(\alpha / \beta)} \right]$

Solution

Assume that α/β (tumor) is 10 Gy, and μ (tumor) is 0.46 h⁻¹ (i.e. repair half time is 0.693/0.46 = 1.5 h) The approximate BED equation is: $BED = NRt \left(1 + \frac{2R}{u(\alpha/\beta)} \right)$

Hence the BED for 60 Gy at 0.5 Gy/h is: BED (tumor) = 60[1 + 2x0.5/(0.46x10)]= 73.0

To obtain this same BED of 73.0 at 1 Gy/h, the overall time *t* is given by: 73.0 = 1xt[1 + 2x1/(0.46x10)]Hence:

> t = 73.0/1.43= 51.0 h

The total dose is thus 51.0 times the dose rate of 1 Gy/h = 51.0 Gy

 Actually, this is only an approximate solution since only the approximate expression for BED was used

 Calculation of t using the full BED equation would have been far more mathematically challenging and would have yielded a required dose of 51.3 Gy, not much different from the approximate solution of 51.0 Gy obtained here

Example 6: conversion of LDR to HDR

Problem:

It is required to replace an LDR implant of 60 Gy at 0.6 Gy h⁻¹ by a 10-fraction HDR implant

What dose/fraction should be used to keep the effect on the tumor the same?

Solution

Since t = 100 h we can use the simplified version of the BED equation: $BED = Rt[1+2R/(\mu.\alpha/\beta)]$ Assume: $\mu = 1.4 \text{ h}^{-1}$ and $\alpha/\beta = 10 \text{ Gy}$ for tumor Then the BED for the LDR implant is: $BED = 60[1+1.2/(1.4 \times 10)]$ = 65.1

If *d* is the dose/fraction of HDR then:

65.1 = $Nd[1+d/(\alpha/\beta)] = 10d[1+0.1d]$ This is a quadratic equation in *d* the solution of which is

d = 4.49 Gy

Is this better or worse as far as normal tissues are concerned?

For late-reacting normal tissues assume $\alpha/\beta = 3$ Gy and $\mu = 0.46$ h⁻¹ Then the BED for 60 Gy at 0.6 Gy h⁻¹ is: BED_{LDR} = 60[1+1.2/(0.46 x 3)] = 112.2 and the BED for 10 HDR fractions of 4.49 Gy is:

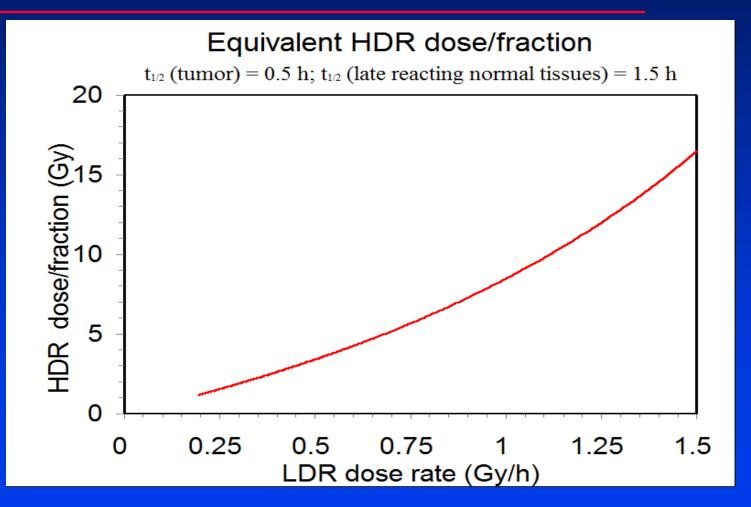
 $BED_{HDR} = 10 \times 4.49[1+4.49/3] = 112.2$

Is this better or worse as far as normal tissues are concerned?

- Amazing! By pure luck I selected a problem where the LDR and HDR implants are identical in terms of both tumor and normal tissue effects
- We will now demonstrate some general conditions for equivalence using the L-Q model

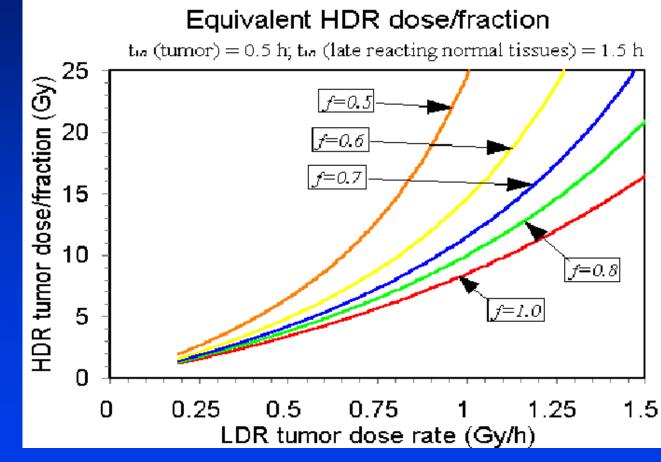
HDR equivalent to LDR for the same tumor and normal tissue effects

For equivalence to LDR at 0.6 Gy h⁻¹ need to use about 4.5 Gy/fraction with HDR (this was the example just shown)



Does geometrical sparing make any difference?

Yes, a big difference Now HDR at about 6 Gy/fraction is equivalent to LDR at $0.6 \text{ Gy } \text{h}^{-1} \text{ if the}$ geometrical sparing factor is 0.6 (yellow line)



Example 7: permanent implants

What total dose for a ¹⁰³Pd permanent prostate implant will produce the same tumor control as a 145 Gy ¹²⁵I implant, assuming α/β for prostate cancer is 1.5 Gy and assuming that repopulation can be ignored?

BED equation for permanent implants

Ignoring repopulation, the BED equation for a permanent implant of a radionuclide with decay constant λ at initial dose rate R_0 is:

$$BED = \frac{R_0}{\lambda} \left[1 + \frac{R_0}{(\mu + \lambda)(\alpha / \beta)} \right]$$

Solution

- R_0/λ is the total dose and λ for I-125, half life 60 days, is 0.693/(60 x 24) h⁻¹ = 0.00048 h⁻¹
 - Hence, for a total dose of 145 Gy, the initial dose rate R₀ is 145 x 0.00048 = 0.0696 Gy/h

Substituting this in the equation and assuming α/β for prostate cancer is 1.5 Gy and $\mu = 0.46 \text{ h}^{-1}$ gives:

 $BED = \frac{0.0696}{0.00048} \left[1 + \frac{0.0696}{(0.46)(1.5)} \right] = 159.6$

Now we need to substitute this in the BED equation in order to calculate the initial dose rate R_0 using the (17 day half life) Pd-103 λ of 0.693/(17 x 24) = 0.0017 h⁻¹

$$159.6 = \frac{R_0}{0.0017} \left[1 + \frac{R_0}{(0.462)(1.5)} \right]$$

The solution to this quadratic equation is
 $R_0 = 0.209 \text{ Gy/h}$
Hence the total dose of Pd-103 is 0.209/0.0017
 $= 122.9 \text{ Gy}$

Summary

- The BED model is useful for the solution of radiotherapy problems with changes in fractionation and/or dose rate
- But remember, this equation must be just an approximation for the highly complex biological changes that occur during radiotherapy
 - the model is approximate
 - the parameters are approximate

But the model is useful!