

Ab-initio spin and time-resolved ARPES with QED-TDDFT: driving WSe₂ out of equilibrium



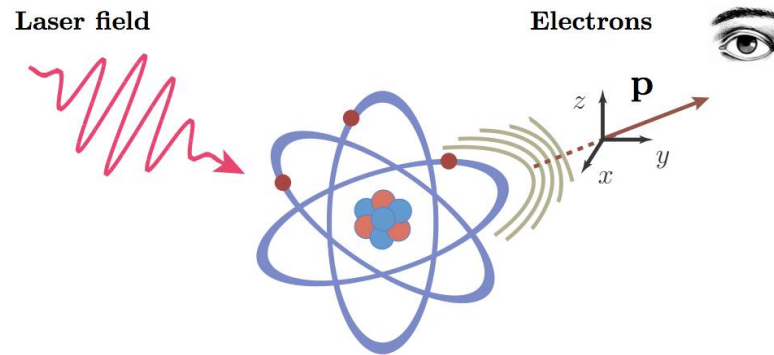
Angel Rubio

Max Planck Institute for the Structure and Dynamics of Matter, Hamburg, Germany

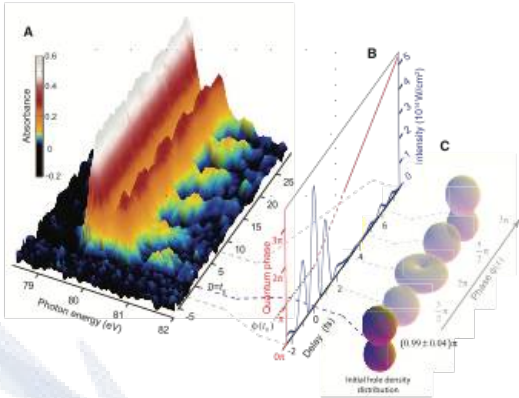
NanoBio Spectroscopy Group Universidad del País Vasco, San Sebastián, Spain



Transient Absorption and Photoelectron Spectroscopies



Hole states time evolution



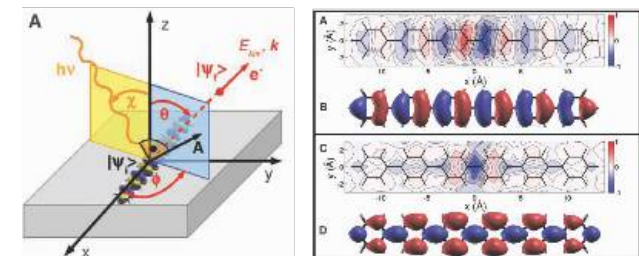
A. Wirth, et al. *Science* 334, 195 (2011).

Shearing interferograms



T. Remetter et al., *Nat Phys* 2, 323 (2006)

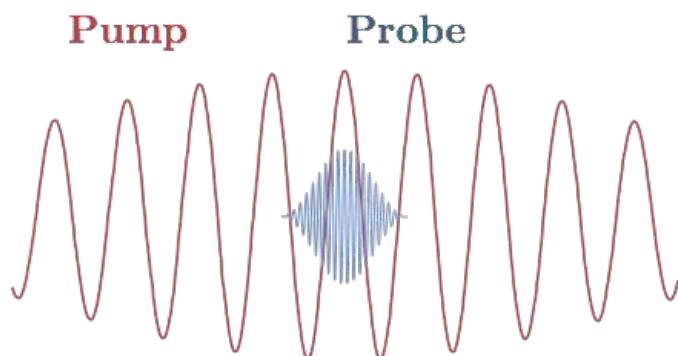
Orbital reconstruction



P. Puschnig et al. *Science* 326, 702 (2009).

Time resolved pump-probe spectroscopy
Image reconstruction, monitoring electron-ion dynamics,
time-dependent band-structure ("light induced topological states")

Transient Absorption and Photoelectron Spectroscopies



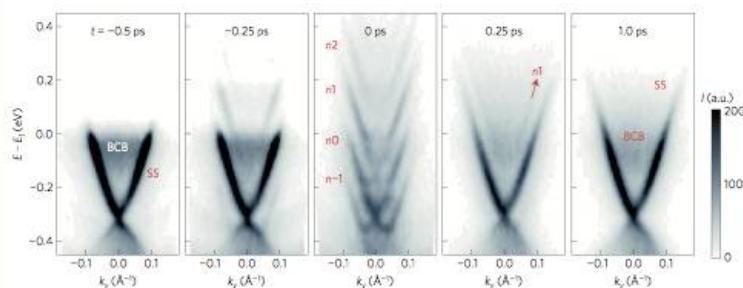
We are **probing** stationary states in a periodically **driven system**



Harvard Natural Sciences Lecture Demonstrations

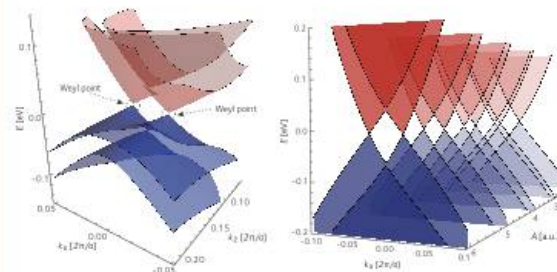
Examples:

Floquet sidebands



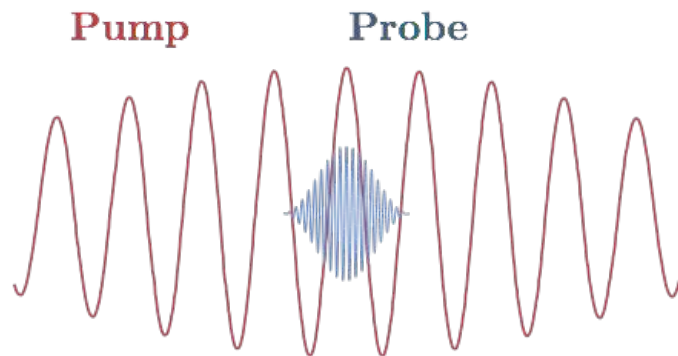
F. Mahmood, et al. Nat Phys **12**, 306 (2016)

Floquet Weyl semimetal

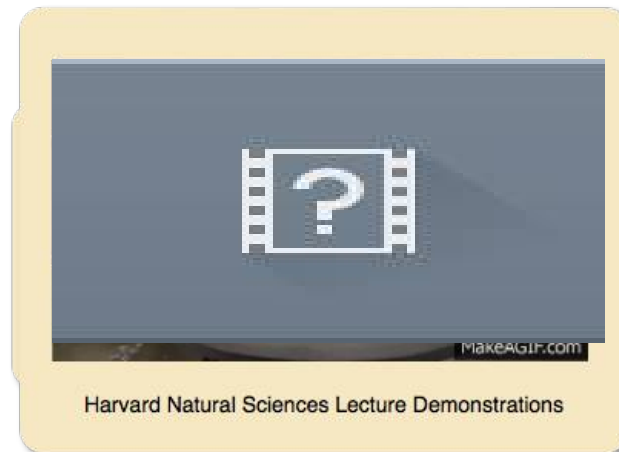


H. Hübener, et al. arXiv:1604.03399 (2016)

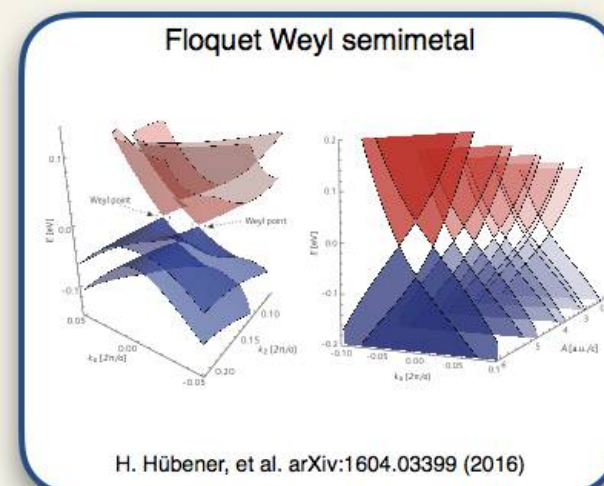
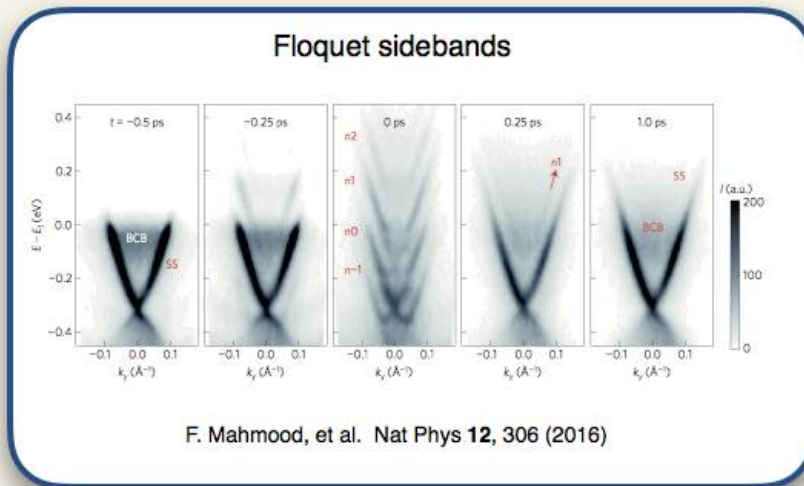
Transient Absorption and Photoelectron Spectroscopies



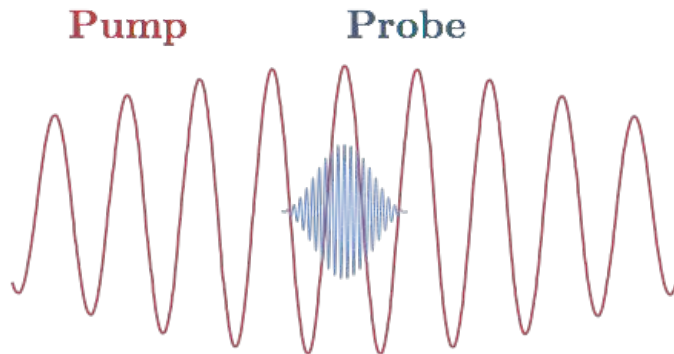
We are **probing** stationary states in a periodically **driven system**



Examples:



Transient Absorption and Photoelectron Spectroscopies



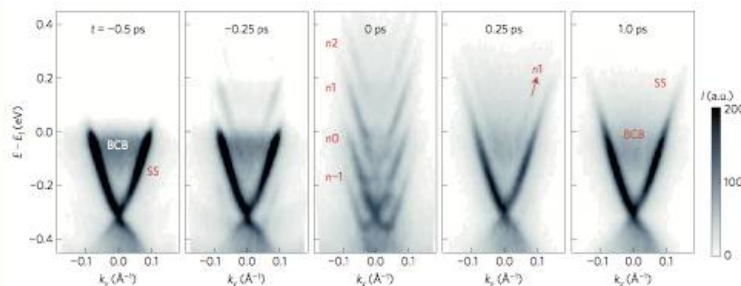
We are **probing** stationary states in a periodically **driven system**

New quasiparticle states:
photon-dressed electronic
states.

Can be described with
Floquet theory

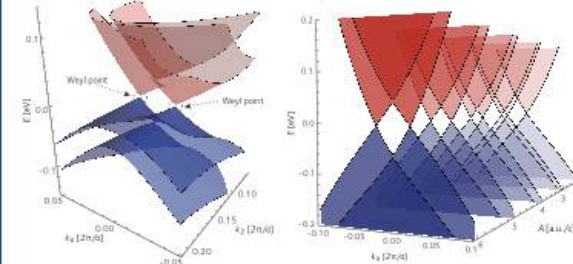
Examples:

Floquet sidebands



F. Mahmood, et al. Nat Phys **12**, 306 (2016)

Floquet Weyl semimetal



H. Hübener, et al. arXiv:1604.03399 (2016)

Many body problem out of equilibrium:

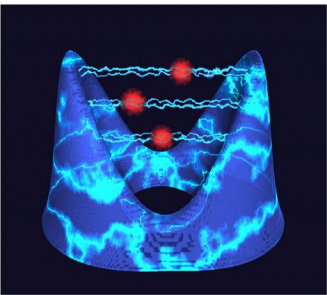
A Time Dependent DFT approach
Some example(s):

Simulating real-time photon-dressing
of quasiparticles with TD-ARPES in TMDs

Quantum Electrodynamics DFT: QED-TDDFT
bridging quantum optics and materials modeling

QED Materials: light induced topology

Theoretical Development: *QED-TDDFT* “New States of Matter”



“bridging quantum optics and materials modeling”

Correlated photon-electron wavefunctions in cavity QED

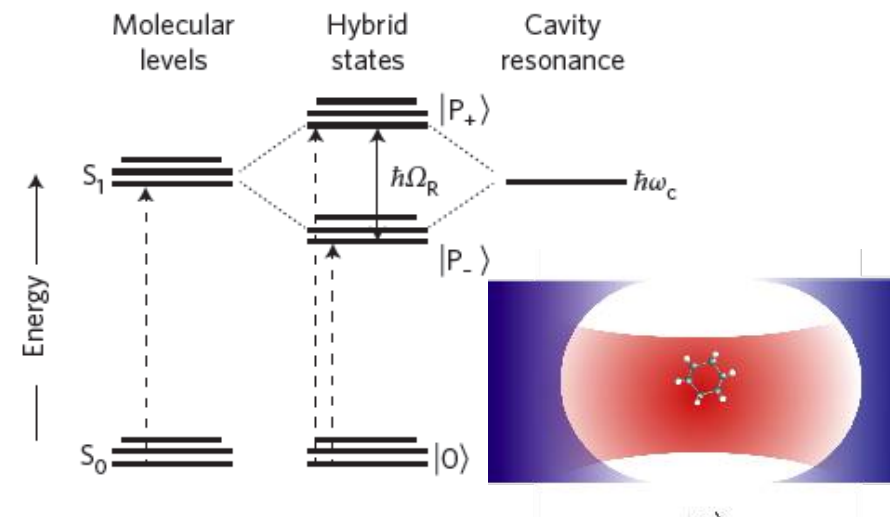
Why?

QED-Chemistry:

Modifying Chemical Landscapes by Coupling to Vacuum Fields

QED-Materials

“New states of matter”



M. Ruggenthaler, J. Flick, C. Pellegrini, H. Appel, I.V. Tokatly, AR PRA (2014),
J. Flick, M. Ruggenthaler, H. Appel, AR PNAS (2015) and PNAS (in press 2017)

New Development: QED-DFT

Electronic system $\mapsto \{\mathbf{r}_i\}_{i=1}^N$, photons $\mapsto \{q_\alpha, p_\alpha, \omega_\alpha\}_{\alpha=1}^M$

Dipole length-form Hamiltonian

$$\hat{H} = \underbrace{\hat{T} + \hat{V}_{ee} + \hat{V}_{\text{ext}}(t)}_{\hat{H}_0} + \underbrace{\frac{1}{2} \sum_{\alpha} \left[\hat{p}_{\alpha}^2 + \omega_{\alpha}^2 \left(\hat{q}_{\alpha} - \frac{\lambda_{\alpha}}{\omega_{\alpha}} \hat{\mathbf{R}} \right)^2 \right]}_{\frac{1}{8\pi} \int (\hat{B}^2 + \hat{E}^2) d\mathbf{r}, \text{ where } \hat{E} = \hat{D} - \hat{P}}$$

$$\hat{V}_{\text{ext}} = \sum_i v_{\text{ext}}(\mathbf{r}_i t) \text{ classical, } \hat{\mathbf{R}} = \sum_i \mathbf{r}_i, \hat{q}_{\alpha} = -(\hat{a}_{\alpha} + \hat{a}_{\alpha}^{\dagger}) / \sqrt{2\omega_{\alpha}}$$

*M. Ruggenthaler, J. Flick, C. Pellegrini, H. Appel, I.V. Tokatly, AR PRA (2014),
J. Flick, M. Ruggenthaler, H. Appel, AR PNAS (2015) and PNAS (2017)*

TDDFT: All observables are functionals of $n(\mathbf{r}, t)$ (Runge&Gross 1984)

Linear and non linear phenomena accessible
Octopus Code <http://www.tddft.org>



Time-Dependent Density Functional Theory, Lecture Notes in Physics, Springer Vols. 837, 706 (2012, 2006)

QED-TDDFT Theorem

Basic variables: electron density and mean photon coordinates

$$\Psi(\{\mathbf{r}_j\}, \{q_\alpha\}, t) [\Psi_0, n, Q_\alpha]$$

where $n(\mathbf{r}t) = \langle \Psi | \hat{n}(\mathbf{r}) | \Psi \rangle$ and $Q_\alpha(t) = \langle \Psi | \hat{q}_\alpha | \Psi \rangle$

$$|\Psi(t)\rangle \xleftrightarrow{1:1} (n(\mathbf{r}t), q(t)) \xleftrightarrow{1:1} |\Phi(t)\rangle \otimes |\chi(t)\rangle$$

KS system: Schrödinger-Maxwell dynamics for N noninteracting e

$$i\partial_t \phi_j(\mathbf{r}t) = [-\nabla^2/2 + v_s(\mathbf{r}t)] \phi_j(\mathbf{r}t)$$

$$\underbrace{\ddot{Q}_\alpha + \omega_\alpha^2 Q_\alpha - \omega_\alpha \lambda_\alpha \mathbf{R}}_{\frac{\partial D}{\partial t} = \nabla \times B} = 0$$

$$n_s(\mathbf{r}t) = n(\mathbf{r}t) \text{ if } v_s = v_{\text{ext}} + v_{\text{Hxc}}^{\text{el}}[n] + v_{\text{eff}}^\alpha[n, Q_\alpha], \quad v_{\text{eff}}^\alpha = v_{\text{MF}}^\alpha + v_{\text{xc}}^\alpha$$

M. Ruggenthaler, J. Flick, C. Pellegrini, H. Appel, I.V. Tokatly, AR PRA (2014), I.V. Tokaly PRL -82104)
J. Flick, M. Ruggenthaler, H. Appel, AR PNAS (2015) and PNAS (accepted 2017)

- Quantum electrodynamics QED-TDDFT

Test **exact** Cases:

Spontaneous Emission: entangled photons

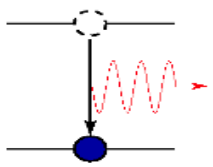
Strong light-matter coupling: Photon bound states

QED-Chemistry

Bond-length and vibrational control HD

Modifying and controlling conical intersections

bridging quantum optics and materials modeling



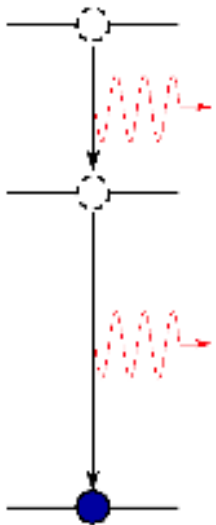
Spontaneous Emission



J. Flick, M. Ruggenthaler, H. Appel, AR PNAS (2015); PNAS(2017)

Spontaneous emission: correlated photon state

Weak
Coupling



Strong
Coupling



Towards large molecular systems and materials

Maxwell's equations in Schrödinger form

Riemann-Silberstein (R-S) vector in vacuum [1]:

$$\vec{F}(\vec{r}, t) = \sqrt{\epsilon_0/2} \vec{E}(\vec{r}, t) + i\sqrt{1/(2\mu_0)} \vec{B}(\vec{r}, t)$$

Maxwell's equations in vacuum:

$$\vec{\nabla} \cdot \vec{E} = \frac{1}{\epsilon_0} \rho$$

$$\vec{\nabla} \cdot \vec{B} = 0$$

$\Downarrow$

$$\vec{\nabla} \cdot \vec{F} = \frac{1}{\sqrt{2\epsilon_0}} \rho$$

$$\vec{\nabla} \times \vec{E} = -\partial_t \vec{B}$$

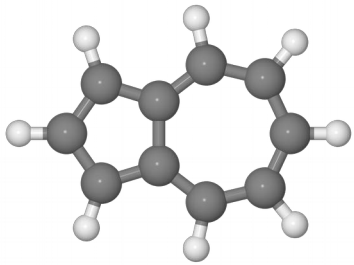
$$\vec{\nabla} \times \vec{B} = \mu_0 \epsilon_0 \partial_t \vec{E} + \mu_0 \vec{j}$$

$\Downarrow$

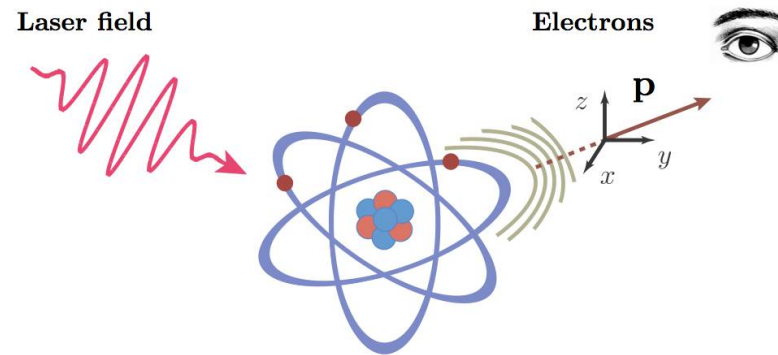
$$i\partial_t \vec{F}(\vec{r}, t) = \pm c_0 \vec{\nabla} \times \vec{F}(\vec{r}, t) - \frac{i}{\sqrt{2\epsilon_0}} \vec{j}$$

René Jestädt, Heiko Appel, Angel Rubio (to be published 2017)

Time-dependent Coupled Maxwell-Kohn-Sham *eg. Azulene molecule*



Transient Absorption and Photoelectron Spectroscopies



How to simulate trARPES with TDDFT

Application of trARPES on WSe₂:

- *ARPES and spin-ARPES*
- *Dichroic spin-valley resonant excitation*
- *Photon dressing and dressed-band hybridization*

Time resolved pump-probe spectroscopy
time-dependent band-structure (“light induced topological states”)

Absorb ejected electrons

Absorb ejected electrons

Flux of the photoelectron current thought surface

non-periodic dim

periodic dims

$\mathbf{p}_\perp$

$\mathbf{p}_\parallel = \mathbf{k}_\parallel$

Solve TDDFT equation for the periodic component

$$i \frac{\partial}{\partial t} u_{\mathbf{k}}(\mathbf{r}) = \hat{H}(t) u_{\mathbf{k}}(\mathbf{r})$$

$$\hat{H}(t) = -\frac{1}{2} \left(\nabla + i\mathbf{k} \right)^2$$

of time



It can describe any

$\mathbf{p}_\perp$

$\mathbf{p}_\parallel = \mathbf{k}_\parallel$

subspace:

$$i\frac{\partial}{\partial t}u_{\mathbf{k}}(\mathbf{r},t) = \hat{H}_{\mathbf{k}}(t)u_{\mathbf{k}}(\mathbf{r},t)$$

$$\hat{H}(t) = -\frac{1}{2} \left(\nabla + i\mathbf{k} - \frac{\mathbf{A}(t)}{c} \right)^2 + \hat{V}_{\text{ion}} + V_{\text{HXC}}$$

ARPES in real materials with QED-TDDFT: driving WSe₂ out of equilibrium
Workshop “Spectroscopy and Dynamics of Photoinduced Excitations”, ICTP, May 2017

Max Planck Institute for the Structure and Dynamics of Matter

Modeling ARPES with tSURFFP

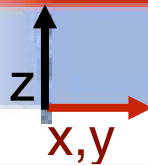
TDKS Hamiltonian

$$\hat{H}_{\mathbf{k}}(t)$$

$$\varphi_{\mathbf{k},j}(\mathbf{r},t) = e^{i\mathbf{k}\cdot\mathbf{r}} u_{\mathbf{k},j}(\mathbf{r},t)$$

$$B \quad \hat{H}_V(t), \chi_{\mathbf{p}} \quad S$$

$$A \quad \hat{H}_{\mathbf{k}}(t), \varphi_{\mathbf{k},j}$$



Working assumptions

$$\hat{H}(t) \approx \hat{H}_{\mathbf{k}}(t) + \hat{H}_V(t)$$

$$z < z_S \quad z \geq z_S$$

$$\varphi_{\mathbf{k},j} = \varphi_{\mathbf{k},j,A} + \varphi_{\mathbf{k},j,B}$$

Volkov Hamiltonian

$$\hat{H}_V(t) = \frac{1}{2} \left[-i\nabla - \frac{\mathbf{A}}{c} \right]^2$$

$$\chi_{\mathbf{p}}(\mathbf{r},t) = \sqrt{\frac{2\pi}{a_x a_y}} e^{i\mathbf{p}\cdot\mathbf{r}} e^{-i\phi(\mathbf{p},t)}$$

$$\phi(\mathbf{p},t) = \frac{1}{2} \int_0^t d\tau \left[\mathbf{p} - \frac{\mathbf{A}(\tau)}{c} \right]^2$$

Use continuity equation

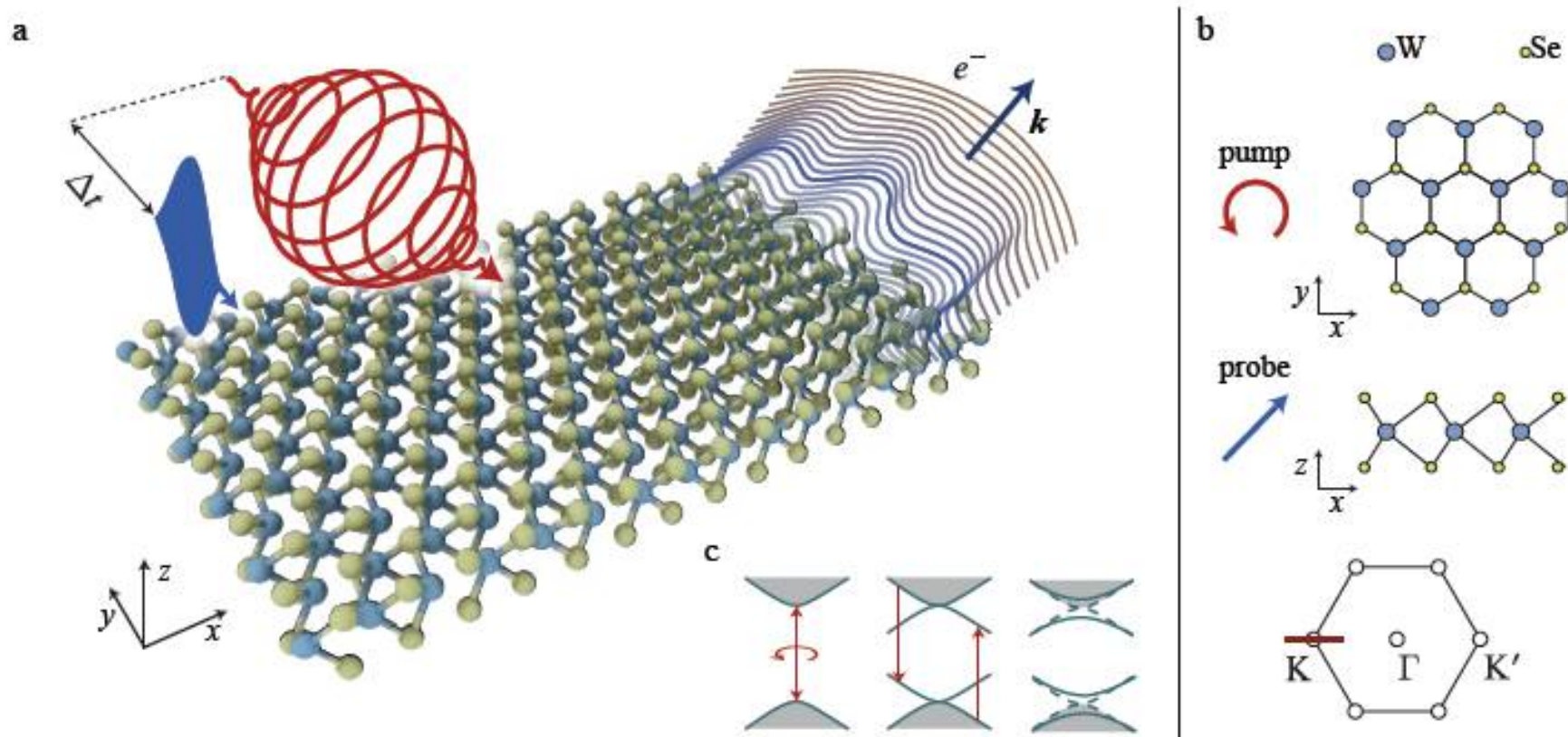
$$N_{\text{esc}}(t) = - \sum_{i=1}^N \int d\mathbf{p} \int_{BZ} d\mathbf{k} \left| \int_0^t d\tau \int_S d\mathbf{s} \cdot \langle \chi_{\mathbf{p}}(\tau) | \hat{\mathbf{j}} | \varphi_{i,\mathbf{k}}(\tau) \rangle \right|^2$$

Momentum-resolved emission probability

$$\mathcal{P}(\mathbf{p} = \mathbf{g} + \mathbf{k}) = \frac{\partial N_{\text{esc}}}{\partial \mathbf{p}} = \lim_{t \rightarrow \infty} \sum_{i=1}^N \int_{BZ} d\mathbf{k} \left| \int_0^t d\tau \int_S d\mathbf{s} \cdot \langle \mathbf{g} | \hat{\mathbf{j}} | u_{i,\mathbf{k}}(\tau) \rangle e^{i\phi(\mathbf{p},t)} \right|^2$$

U. de Giovanninni, H. Hübener, AR (2016)

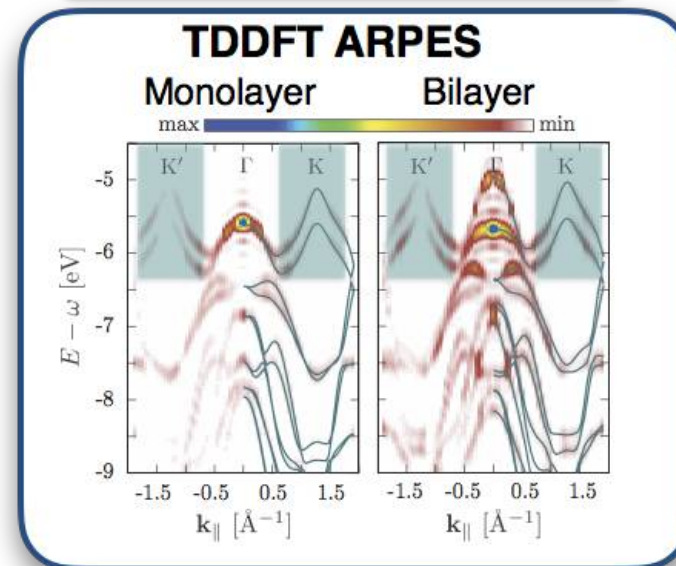
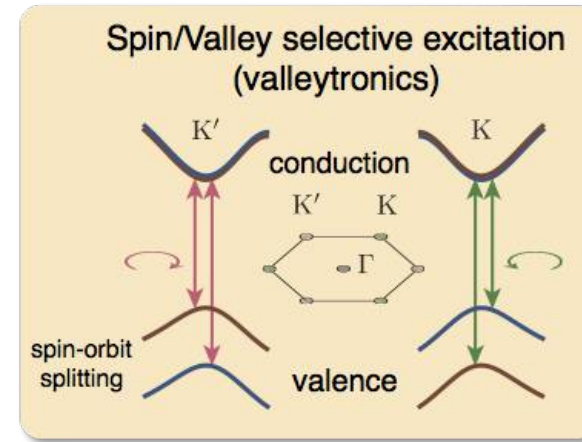
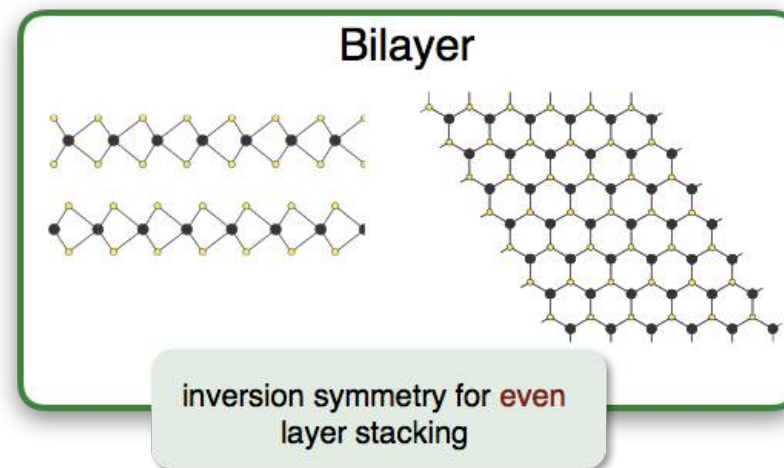
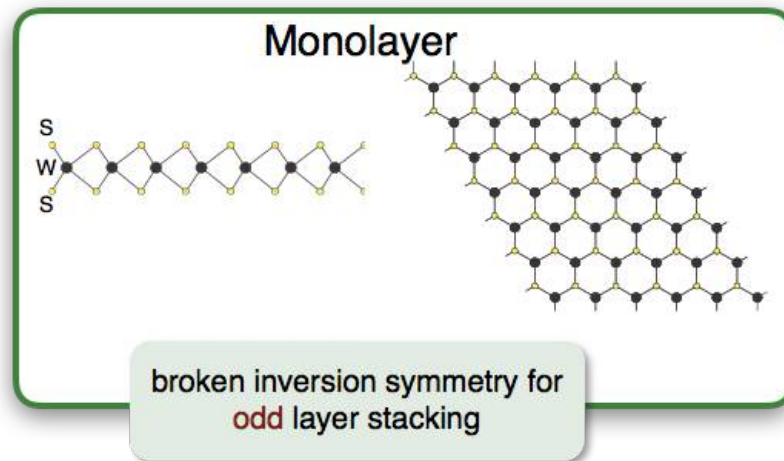
Simulating real-time photon-dressing of quasiparticles with TD-ARPES in TMDs



U. de Giovanninni, H. Hübener, AR, Nano Letters (2016)

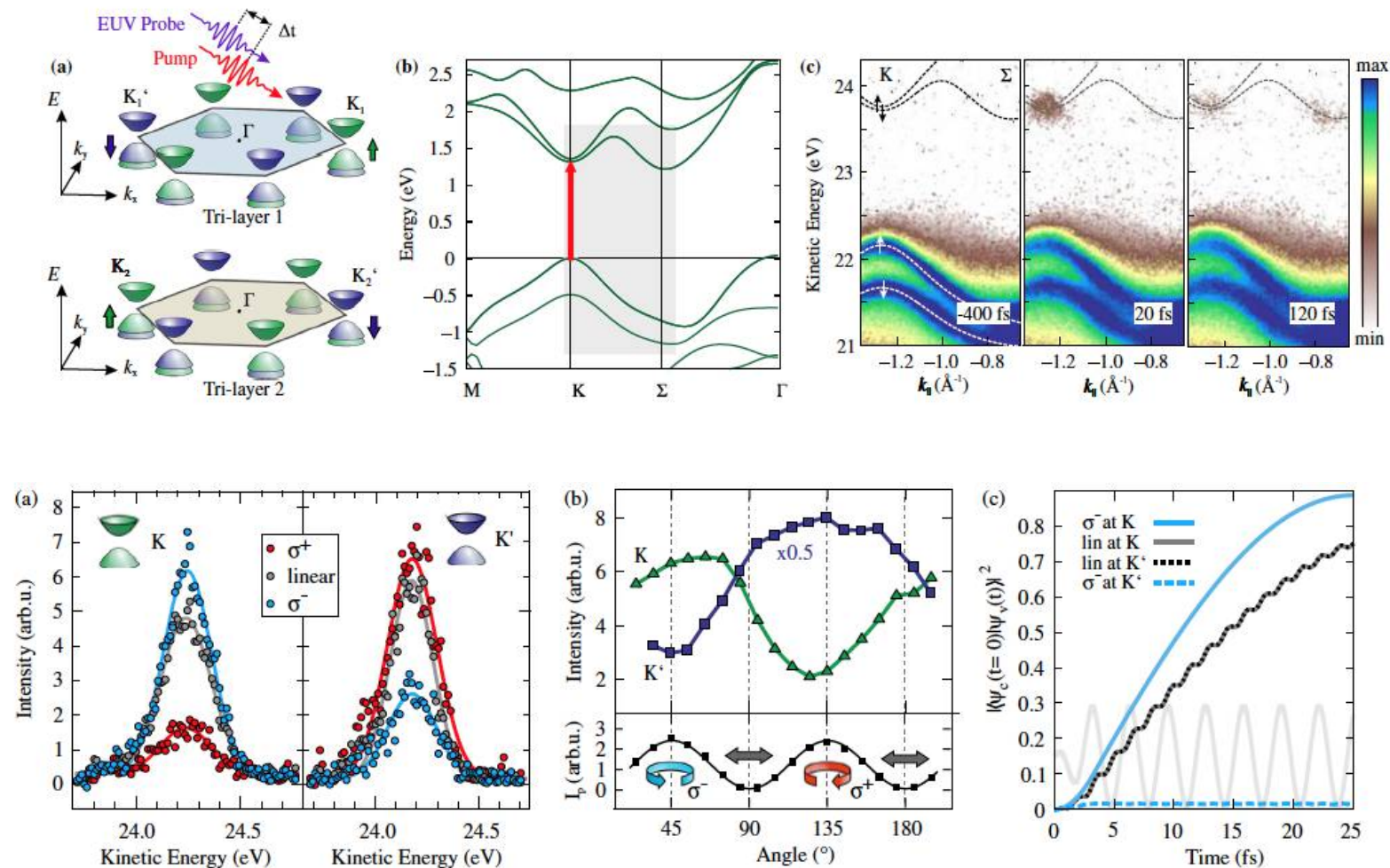
Simulating real-time photon-dressing of quasiparticles with TD-ARPES in TMDs

ARPES on WSe₂



U. de Giovanninni, H. Hübener, AR (2016)

Simulating real-time photon-dressing of quasiparticles with TD-ARPES in TMDs



Ralph Ernstorfer

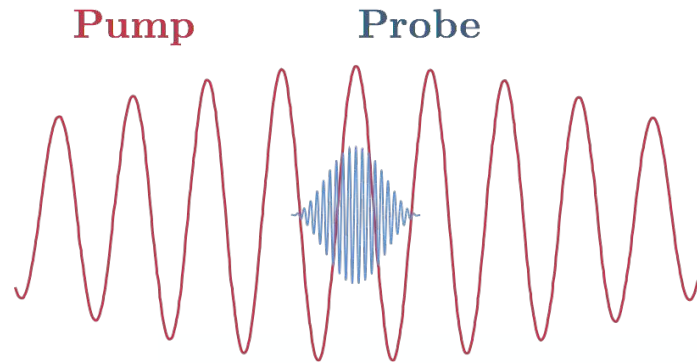
R. Bertoni, C. W. Nicholson, L. Waldecker, H. Hübener, C. Monney, U. De Giovannini, M. Puppini, M. Hoesch, E. Springate, R. T. Chapman, C. Cacho, M. Wolf, A. Rubio, R. Ernstorfer PRL (2016)

U. de Giovannini, H. Hübener, AR NanoLetters (2016);

[ARPES in real materials with QED-TDDFT: driving WSe₂ out of equilibrium](#)

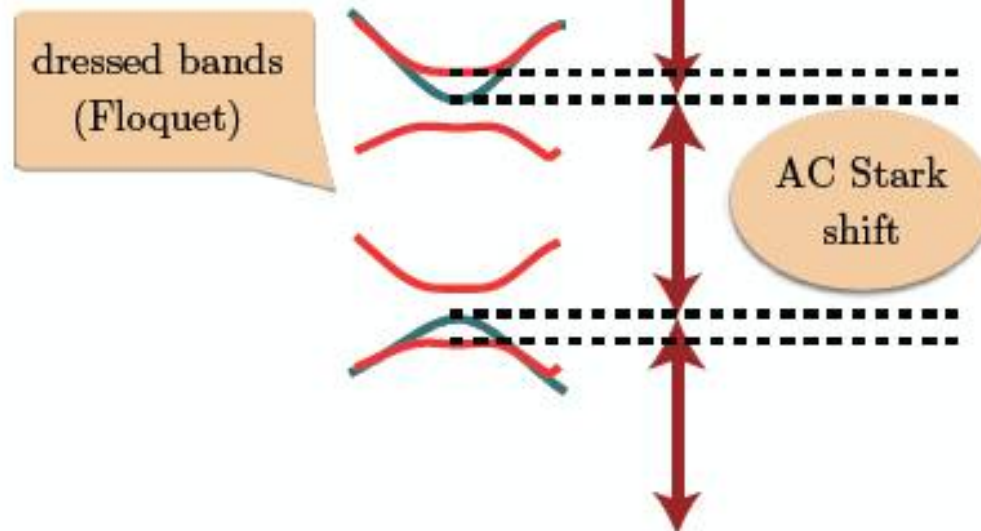
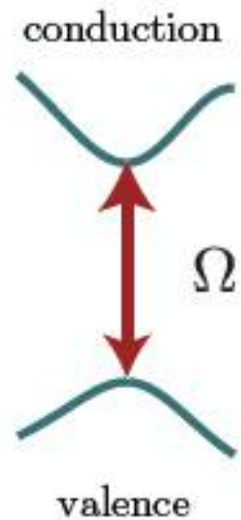
Workshop “Spectroscopy and Dynamics of Photoinduced Excitations”, ICTP, May 2017

Simulating real-time photon-dressing of quasiparticles with TD-ARPES in TMDs



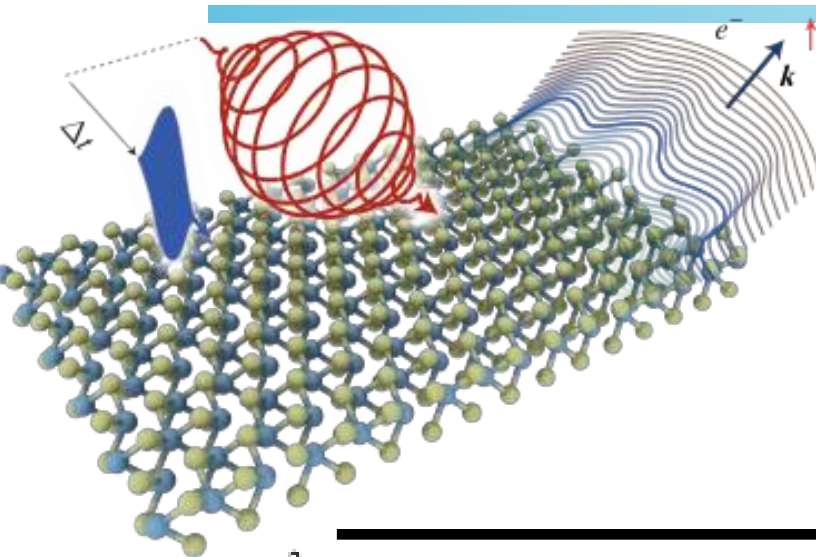
Probing while the pump is switched on?

driven is different



U. de Giovanninni, H. Hübener, AR NanoLetters (2016)

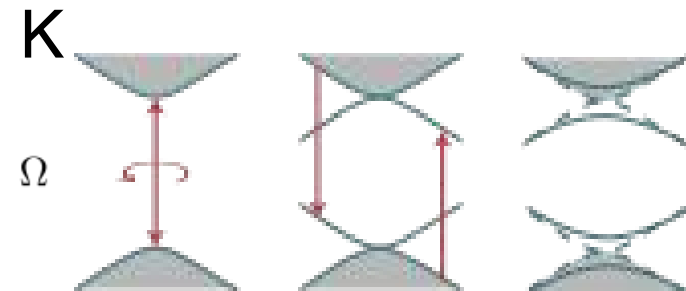
Photon dressing and undressing



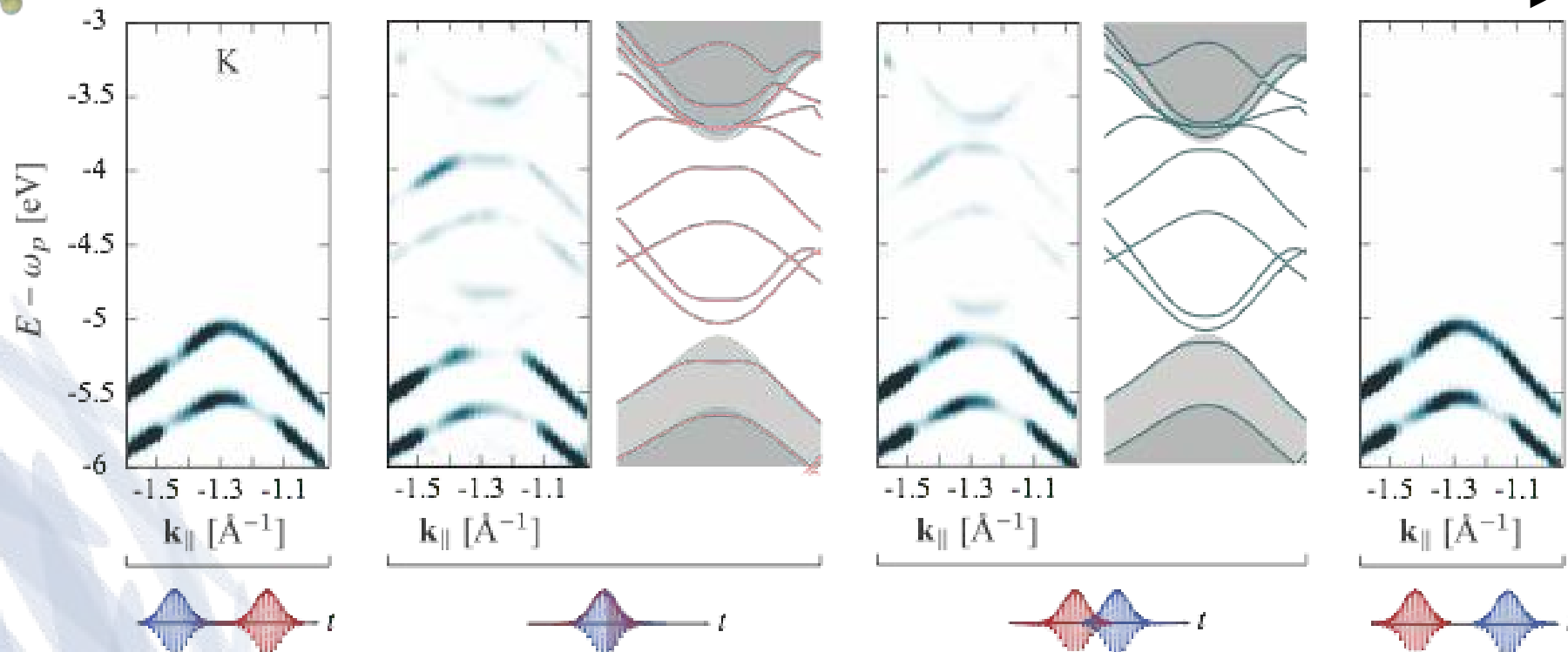
Two independent approaches

trARPES

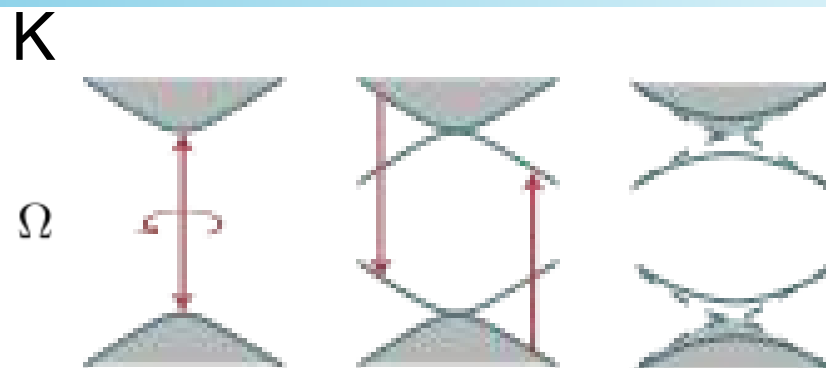
Floquet



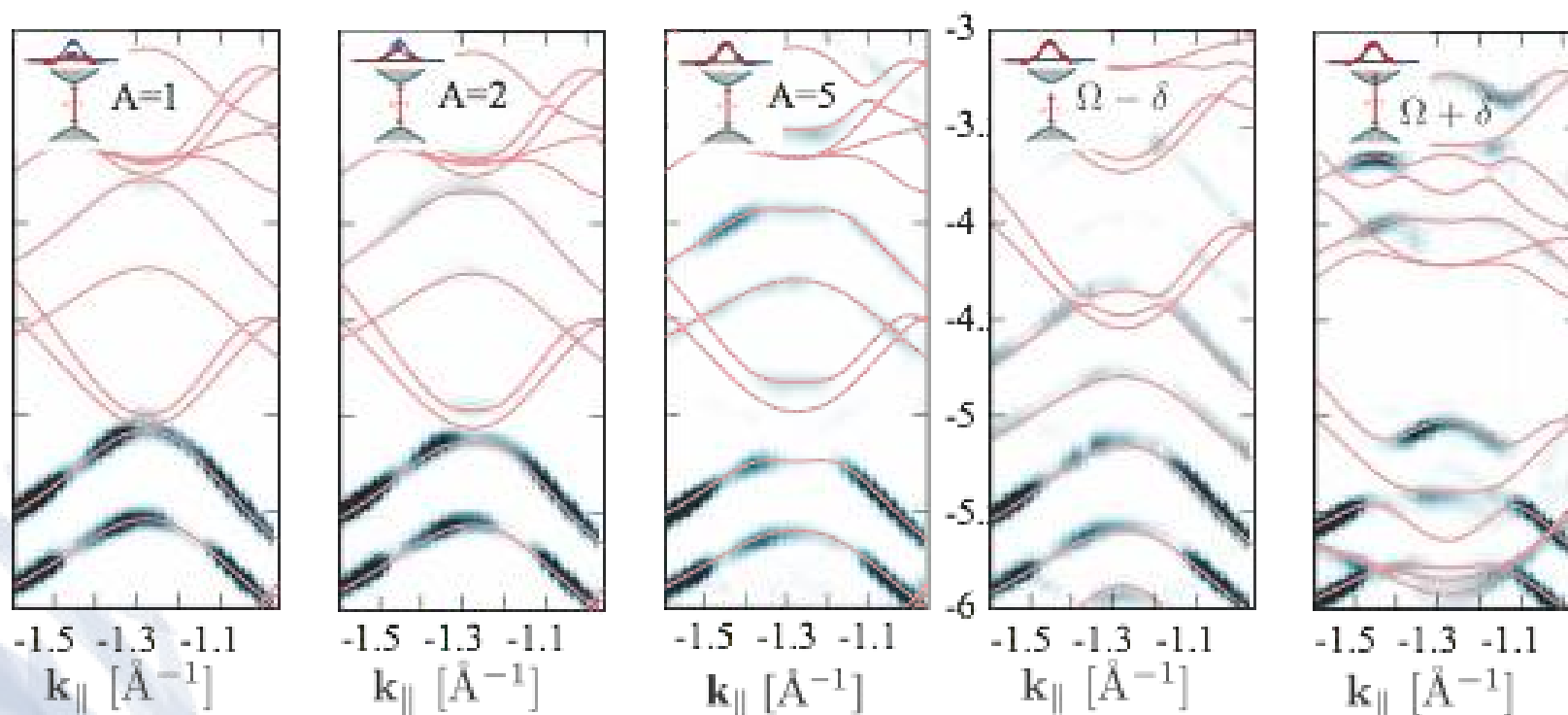
Time delay



Photon dressing and undressing



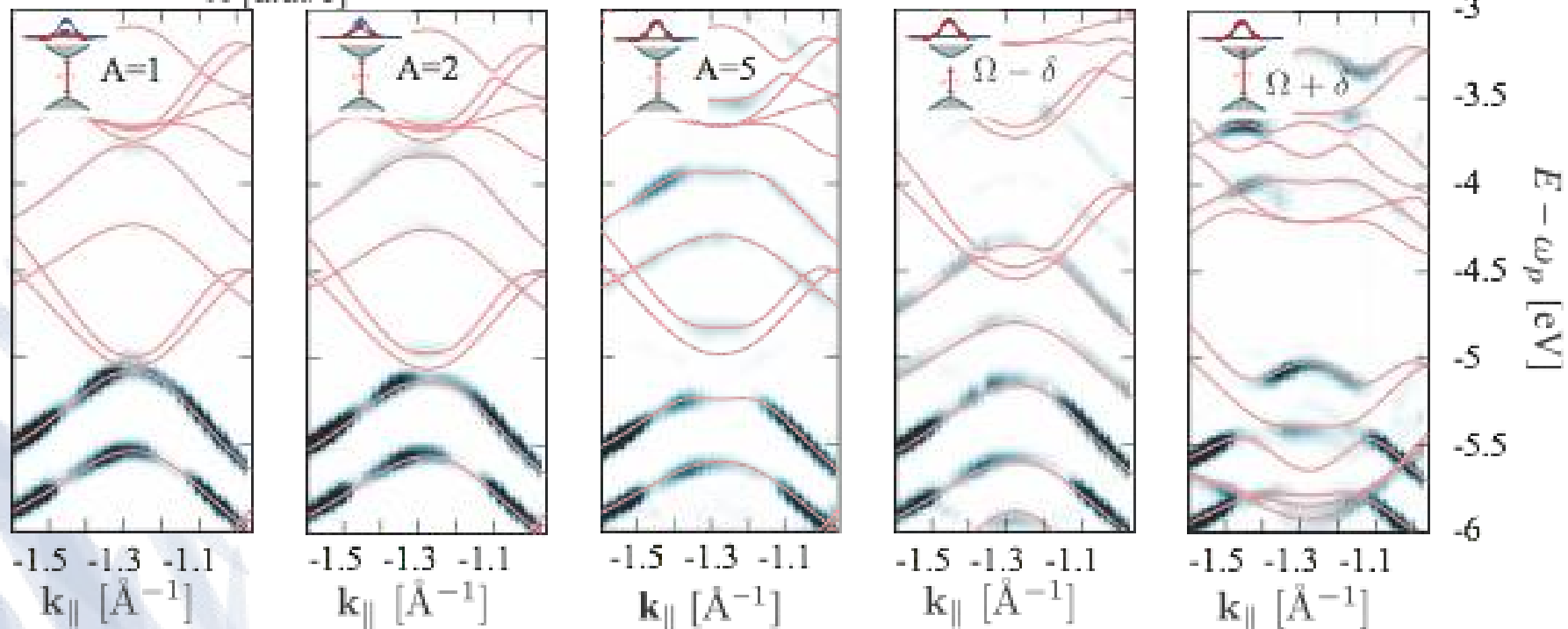
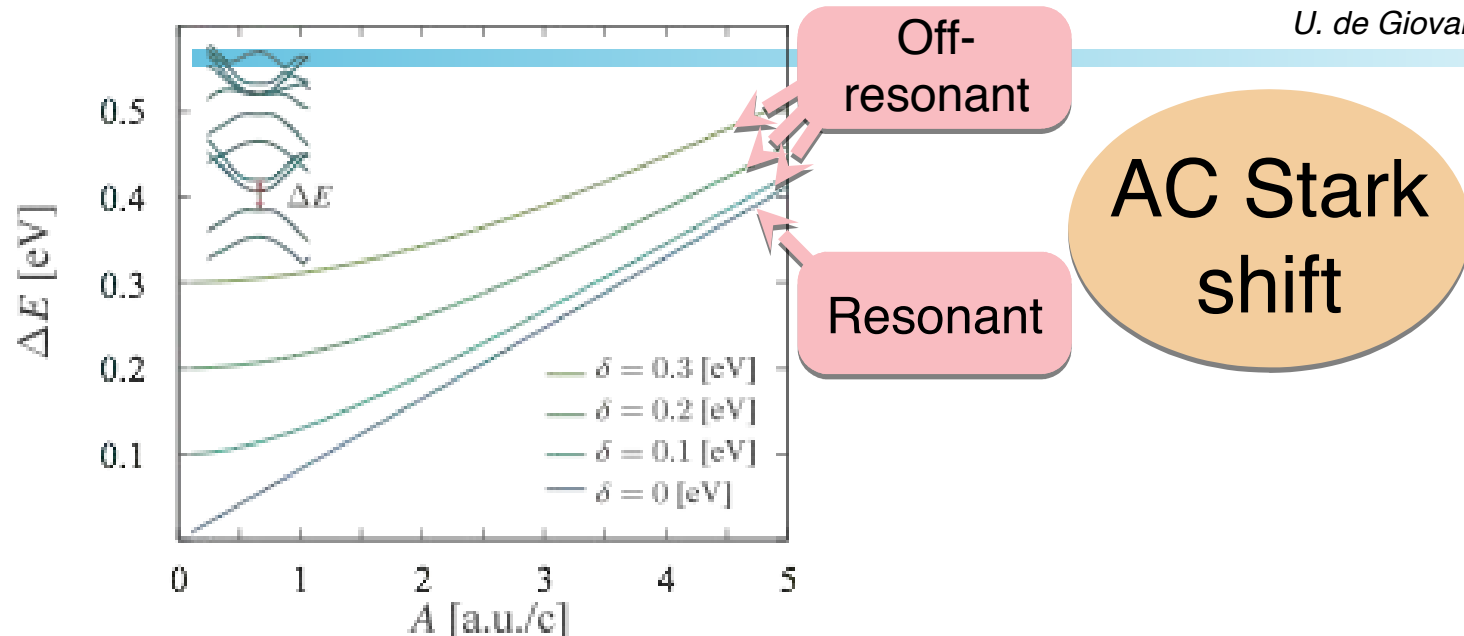
Field amplitude A
 $1 \text{ [a.u.] } = 0.02 \text{ V/\AA}$



Field amplitude

Detuning

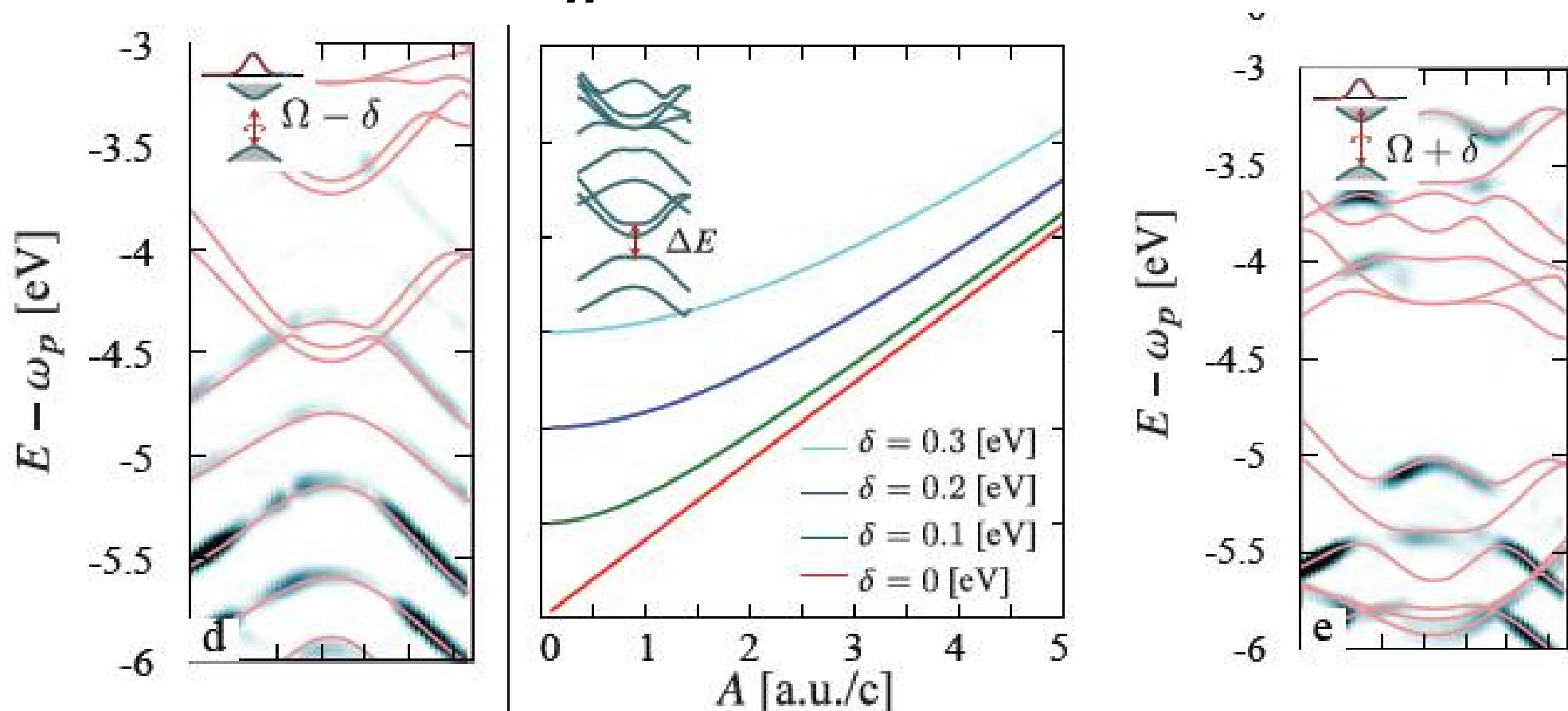
Photon dressing and undressing



Simulating real-time photon-dressing of quasiparticles with TD-ARPES in TMDs

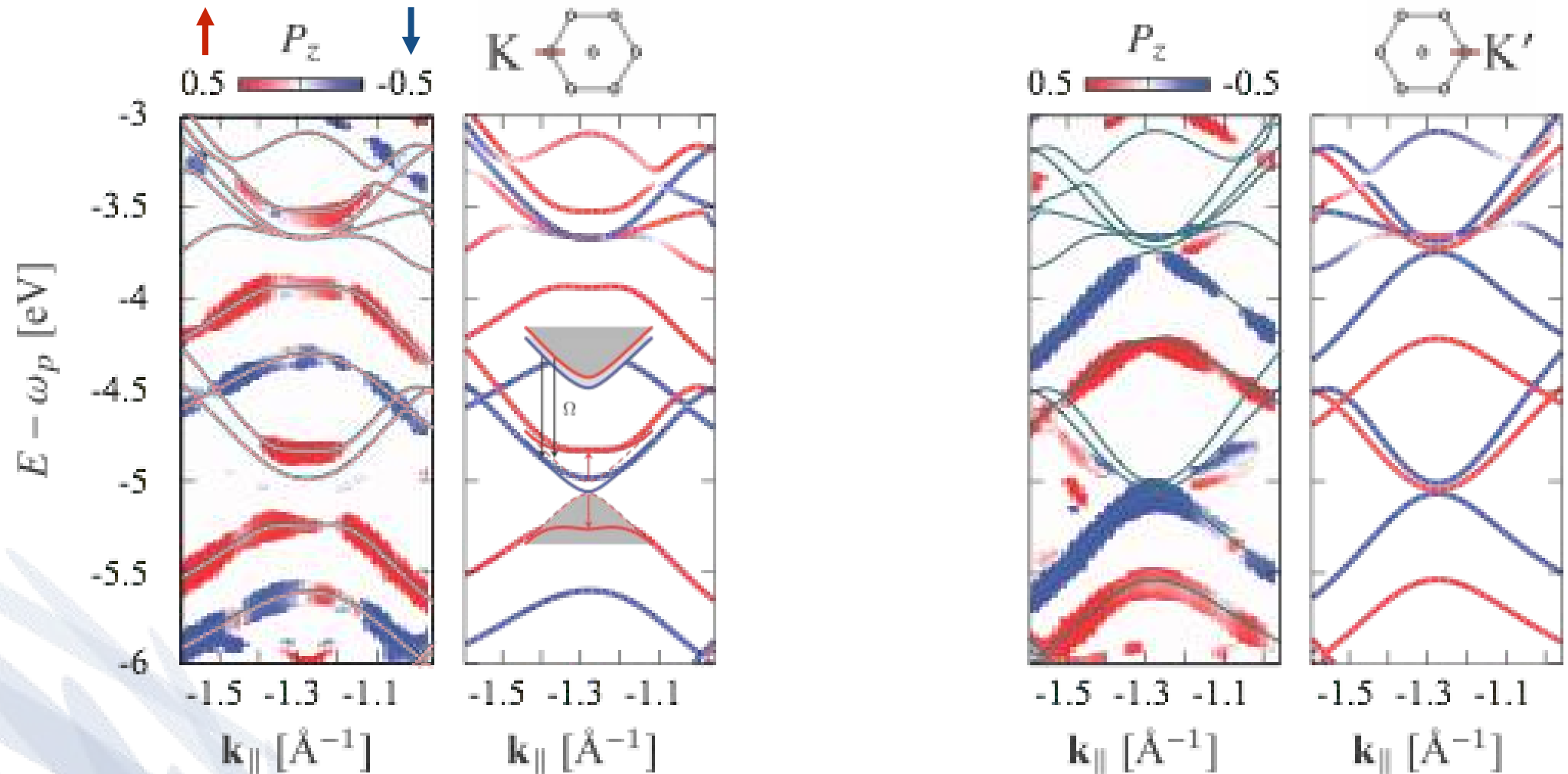
Dependence on the laser frequency and intensity

off-resonant case



U. de Giovanninni, H. Hübener, AR NanoLetters (2016)

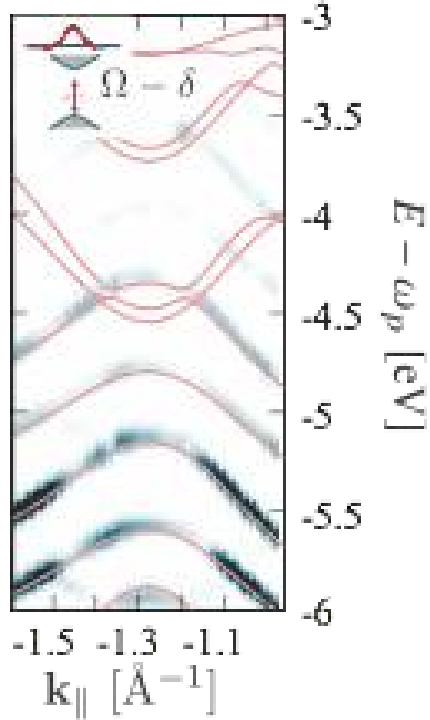
Photon dressing and undressing Spin texture



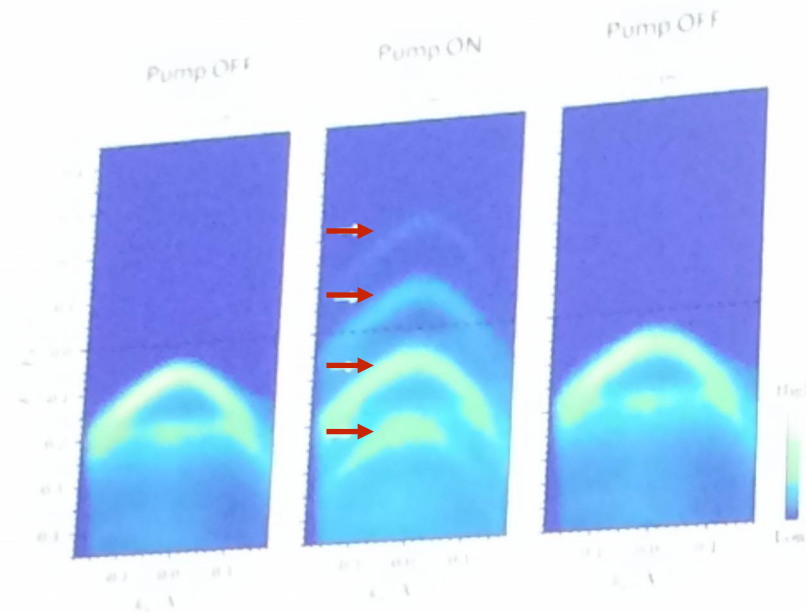
Dichroic optical Stark effect

U. de Giovanninni, H. Hübener, AR (2016)

How real is all this??



Floquet-Bloch states



EJ Sie et al (unpublished)

E. J. Sie, N. Gedik et al. (MIT, unpublished)

New Theoretical Developments: *QED-TDDFT*



“bridging quantum optics and materials modeling”

QED-Materials

“New states of matter”

QED-Chemistry:

Modifying Chemical Landscapes
by Coupling to Vacuum Fields

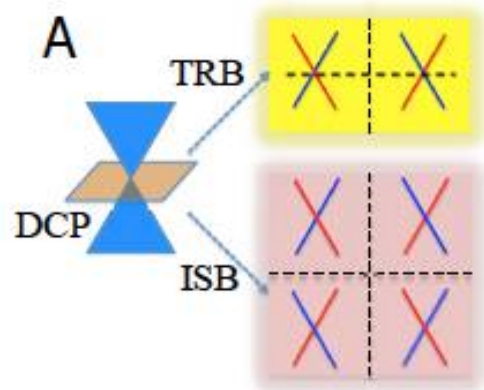
*M. Ruggenthaler, J. Flick, C. Pellegrini, H. Appel, I.V. Tokatly, AR PRA (2014),
J. Flick, M. Ruggenthaler, H. Appel, AR PNAS (2015) and PNAS (2017)*

Light-induced topological states

Discovery of a Weyl Fermion semimetal

Weyl semimetal in crystalline TaAs, TaP, SrSi₂
NbAs, NbP

B.Q. Lv et al, Phys. Rev. X (2015),
S-X, Xu et al, Science (2015)
Z.K. Liu, et al, Nat. Comm. (2015)



Dirac cones: two overlapping Weyl nodes with opposite chirality

Weyl fermions: exotic properties,

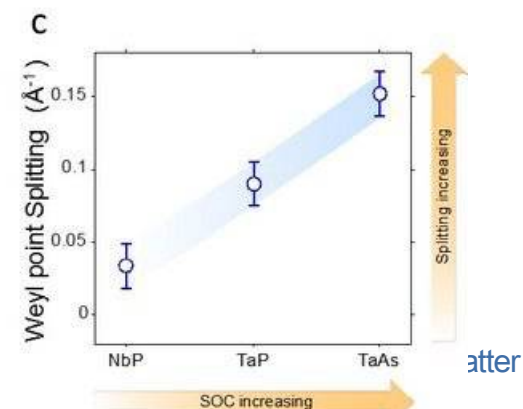
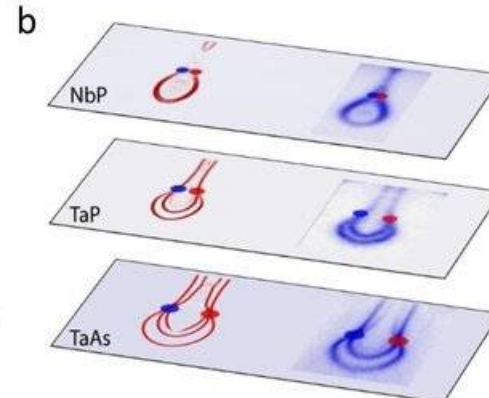
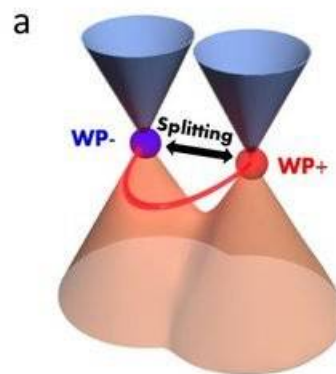
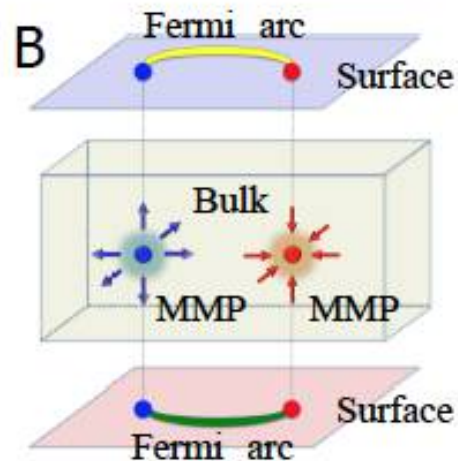
monopoles in crystal momentum space

chiral anomaly: negative magneto-resistance, chiral magnetic effects and anomalous Hall effect

Separated Weyl nodes are topologically stable:

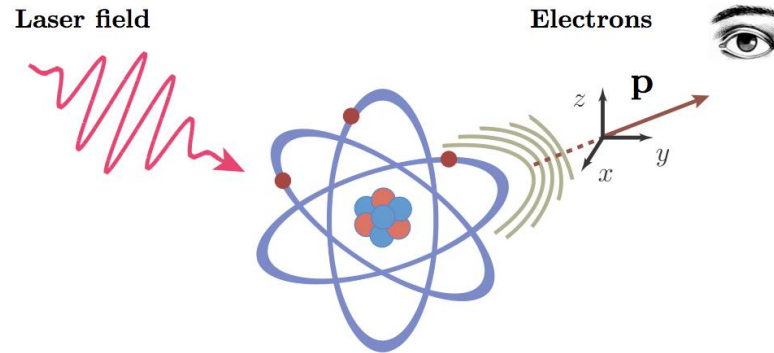
a perturbation respecting the translational symmetry can only shift but not annihilate them

Weyl semimetals show characteristic Fermi arcs on the surface

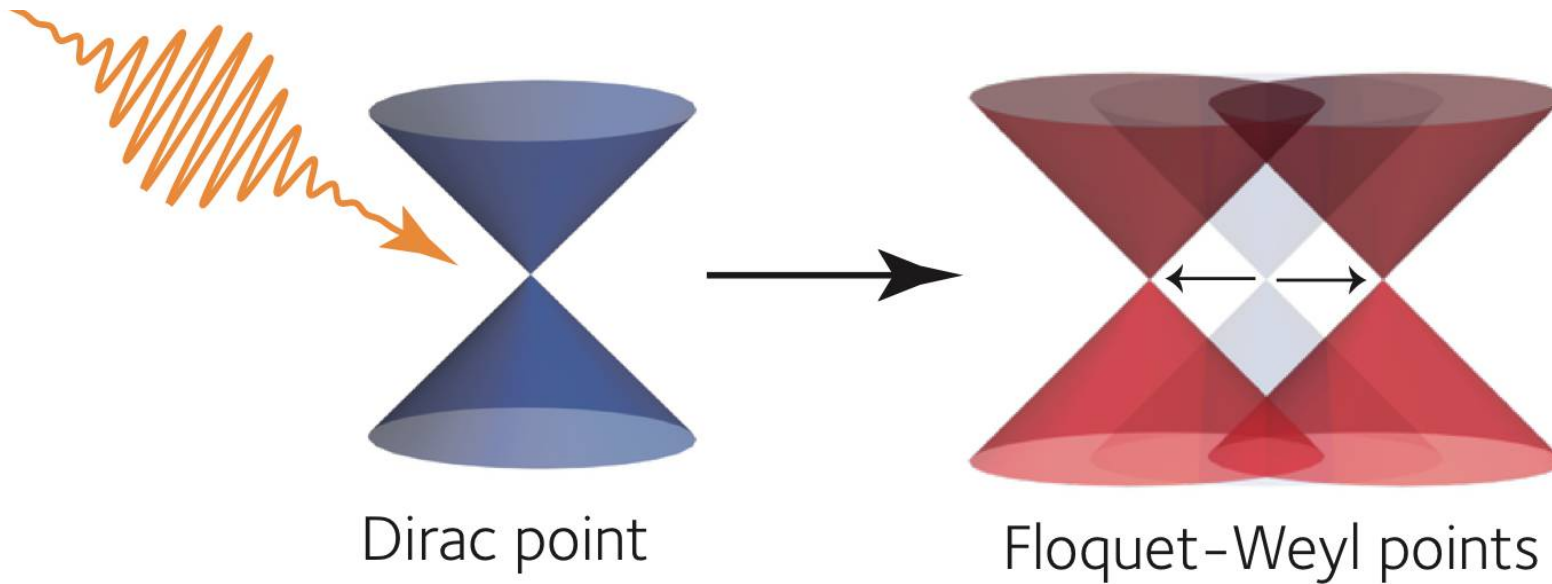


TD-ARPES and transient absorption spectroscopies

Light induced Floquet Topological states



$$\hat{H}_{\text{Dirac}}(\mathbf{k} - \mathbf{A}(t)) = \begin{pmatrix} \hat{H}_{\text{Weyl}}(\mathbf{k} - \mathbf{A}(t)) & 0 \\ 0 & \hat{H}_{\text{Weyl}}(\mathbf{k} - \mathbf{A}(t))^* \end{pmatrix} \quad \hat{H}_{\text{Weyl}}(\mathbf{k} - \mathbf{A}(t)) = \begin{pmatrix} k_z - A_0 \sin(\Omega t) & k_x - i(k_y - A_0 \cos(\Omega t)) \\ k_x + i(k_y - A_0 \cos(\Omega t)) & -k_z + A_0 \sin(\Omega t) \end{pmatrix}$$

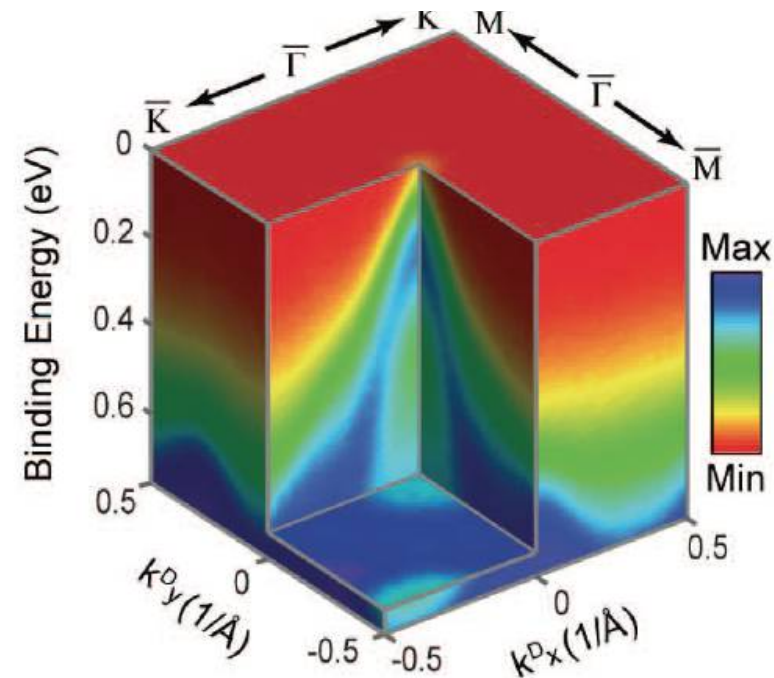
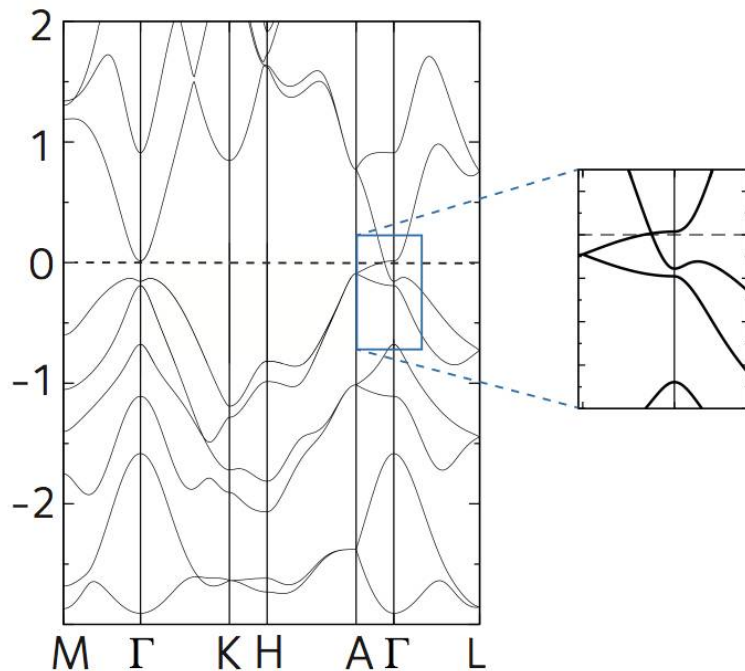
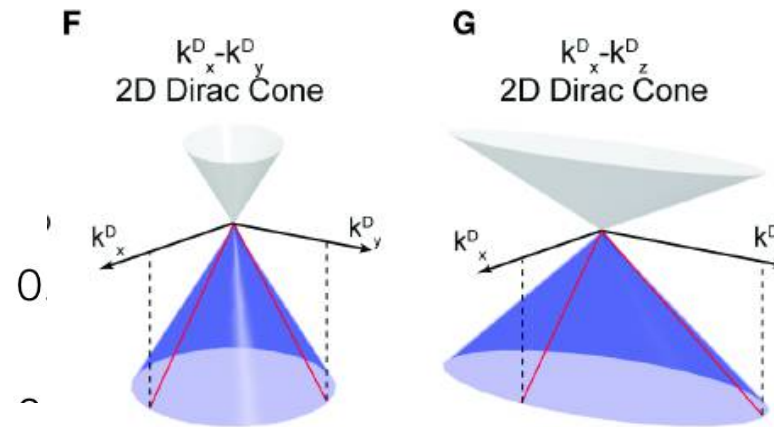
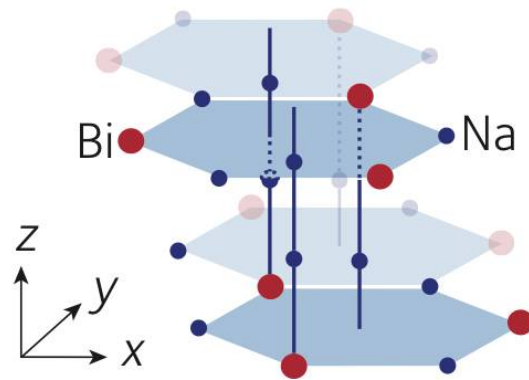


H. Hübener, M. Sentef, A. F. Kemper, U. de Giovannini, *AR Nature Comm.* (2017)

U. de Giovannini, H. Hübener, *AR NanoLetters* (2016)

Light-induced Floquet topological states

3D real Dirac material Na_3Bi

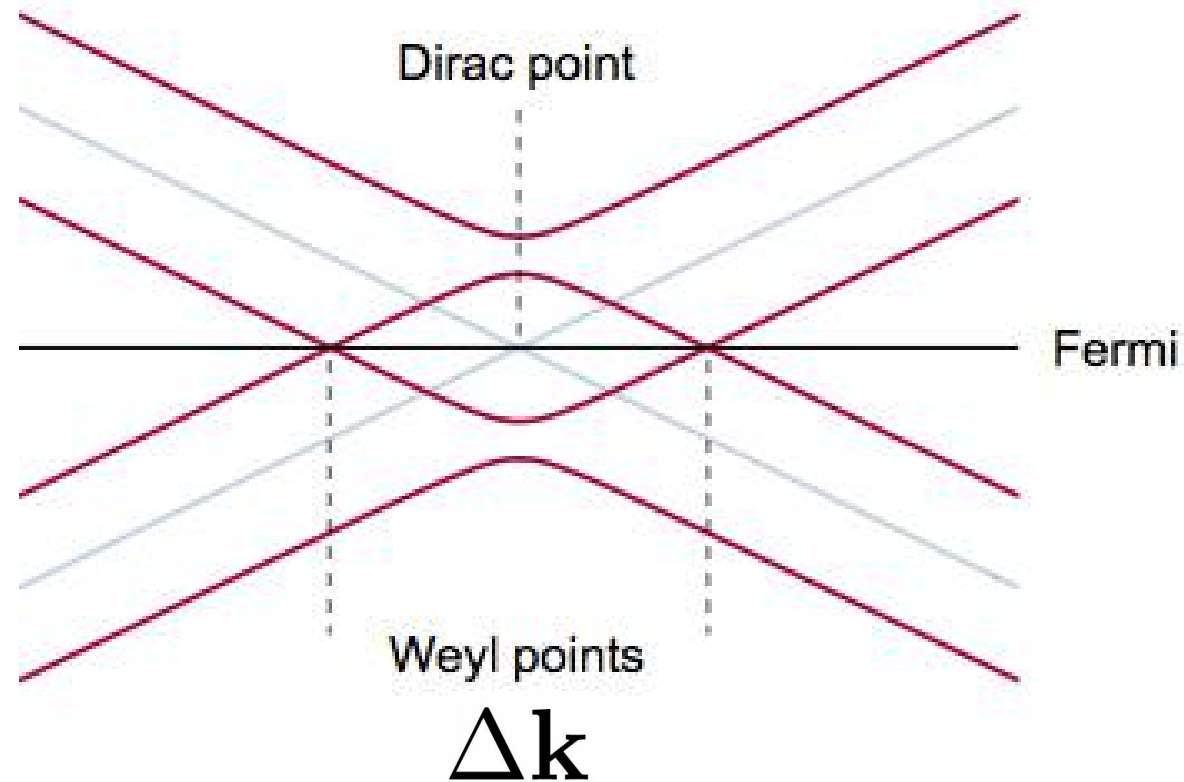


Z. K. Liu et al., Science 343, 864 (2014)

Light-induced Floquet topological states

3D Dirac material Na_3Bi

$$\Delta \mathbf{k} = 2v_F \frac{(\frac{e}{c} A)^2}{\Omega}$$

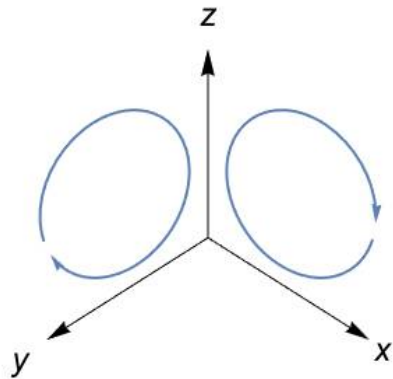


*Engineering of fictitious gauge fields with real laser fields laser
control of topological states of matter*

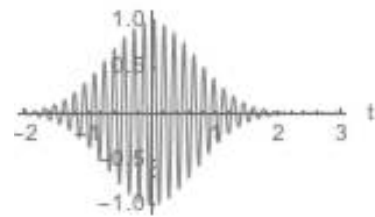
H. Hübener, M. Sentef, A. F. Kemper, U. de Giovannini, AR Nature Communications (2017)

Light-induced Floquet topological states

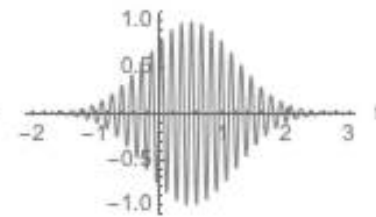
3D Weyl semimetal Na_3Bi



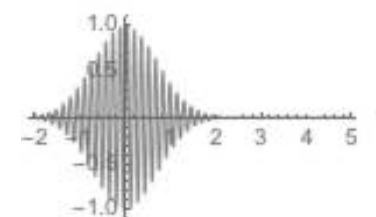
y-z Polarized light



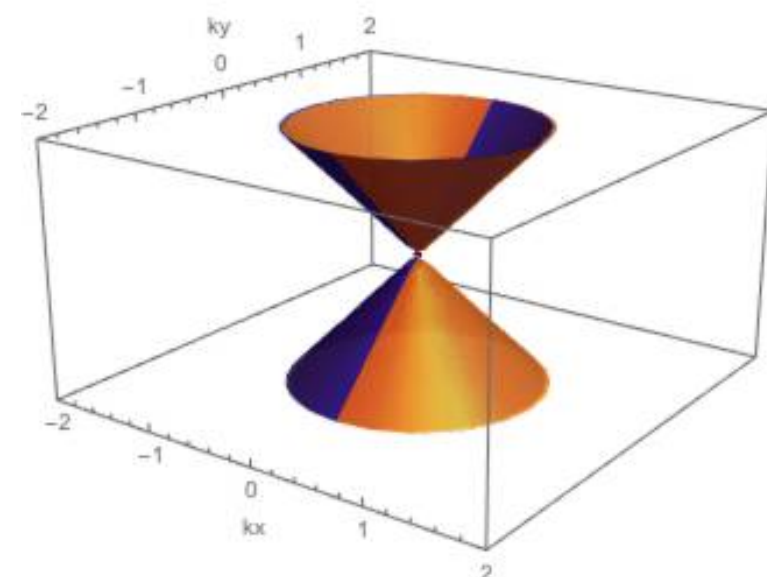
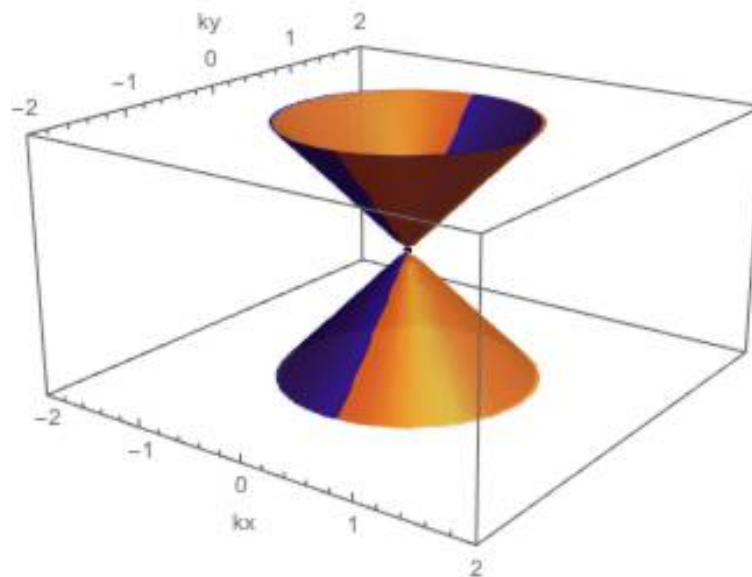
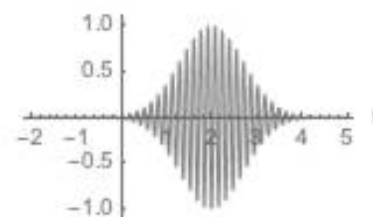
x-z Polarized light



y-z Polarized light



x-z Polarized light



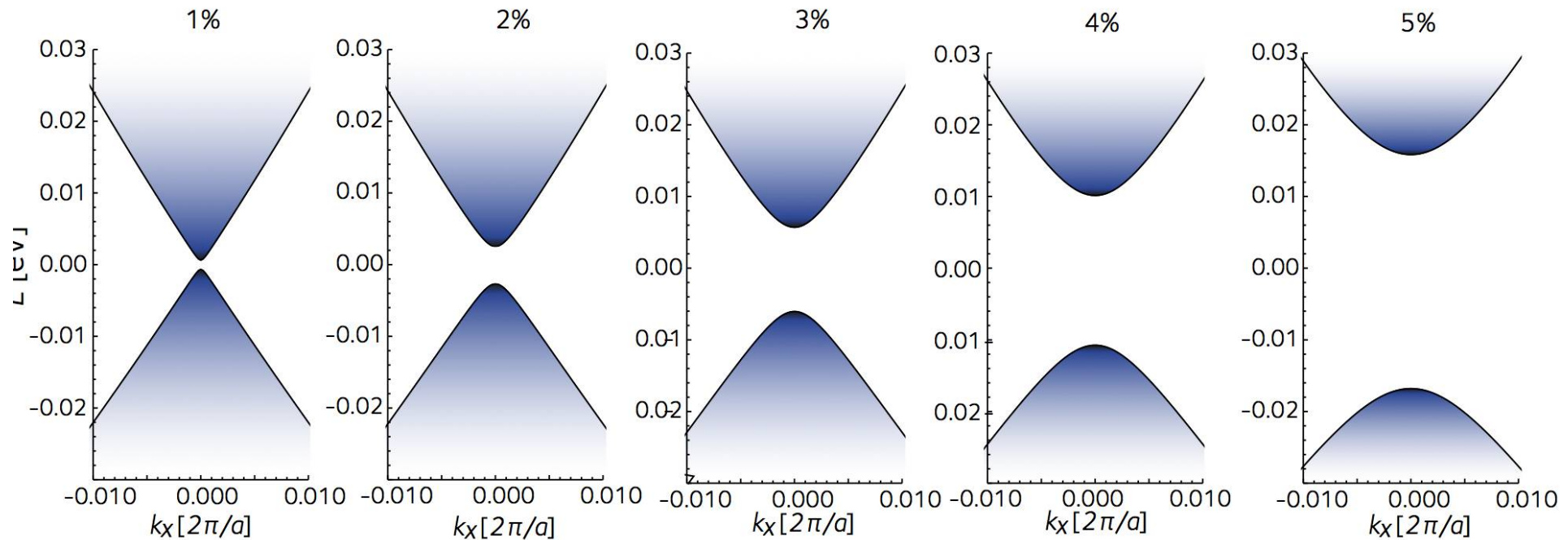
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Light-induced Floquet topological states

3D Dirac material Na_3Bi

Topological protection

- apply strain



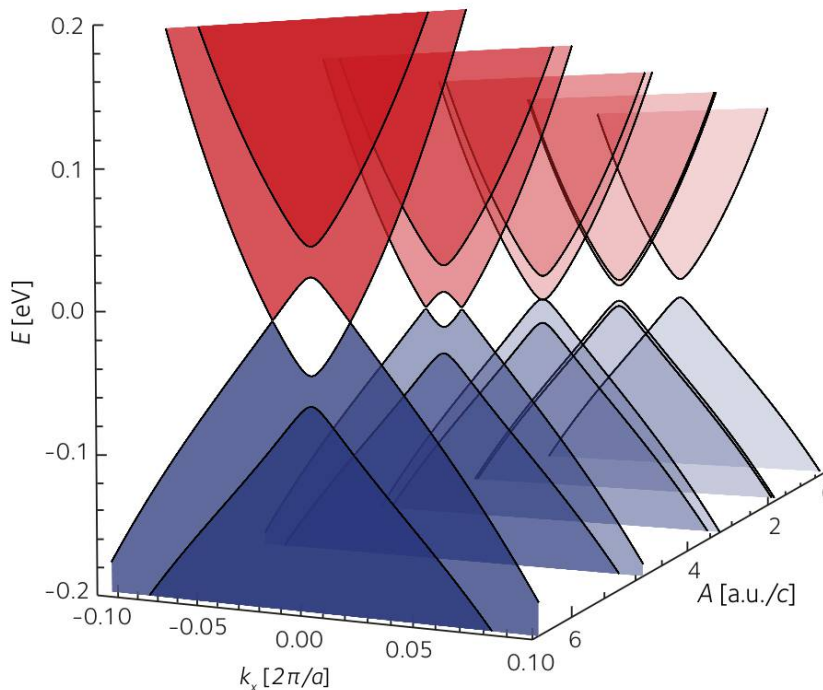
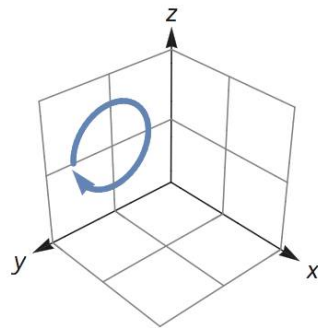
- topological insulator

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Light-induced Floquet topological states

3D Dirac material Na_3Bi

Topological protection



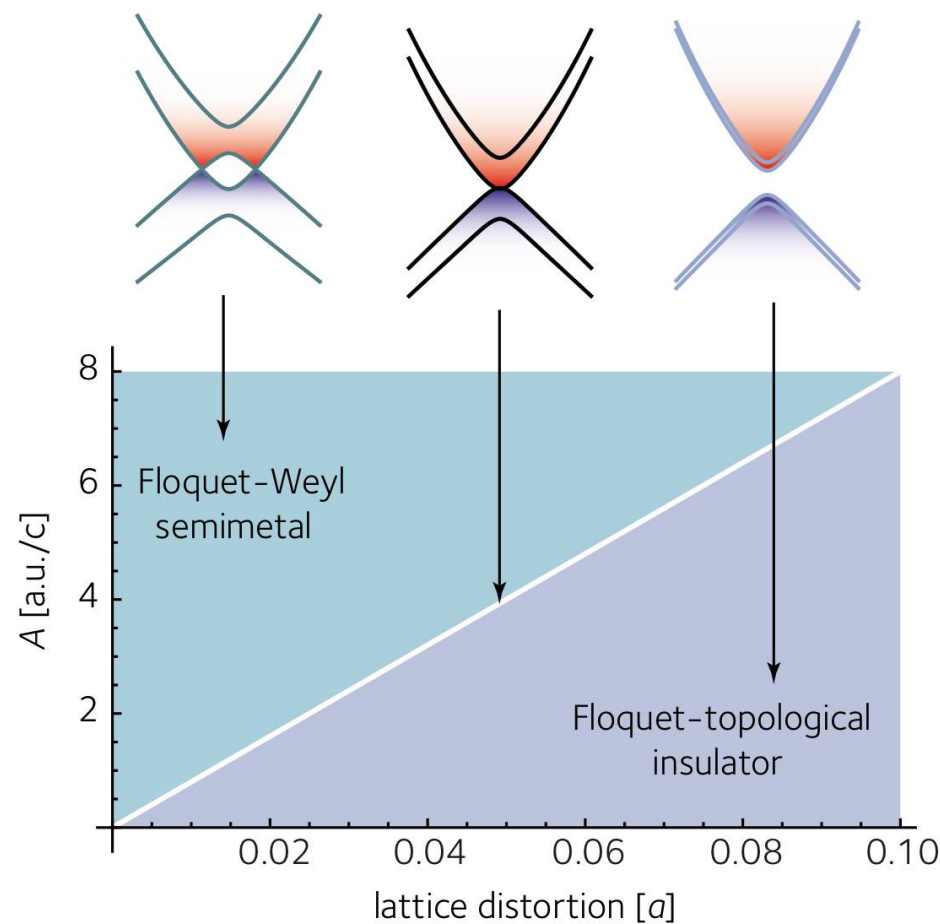
- Weyl semimetal restored

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Light-induced Floquet topological states

3D Dirac material Na_3Bi

Floquet phase diagram



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Acknowledgements

U.de Giovannini, H.Hübener, M. Sentef



Experiments

FHI-group



Ralph Ernstorfer



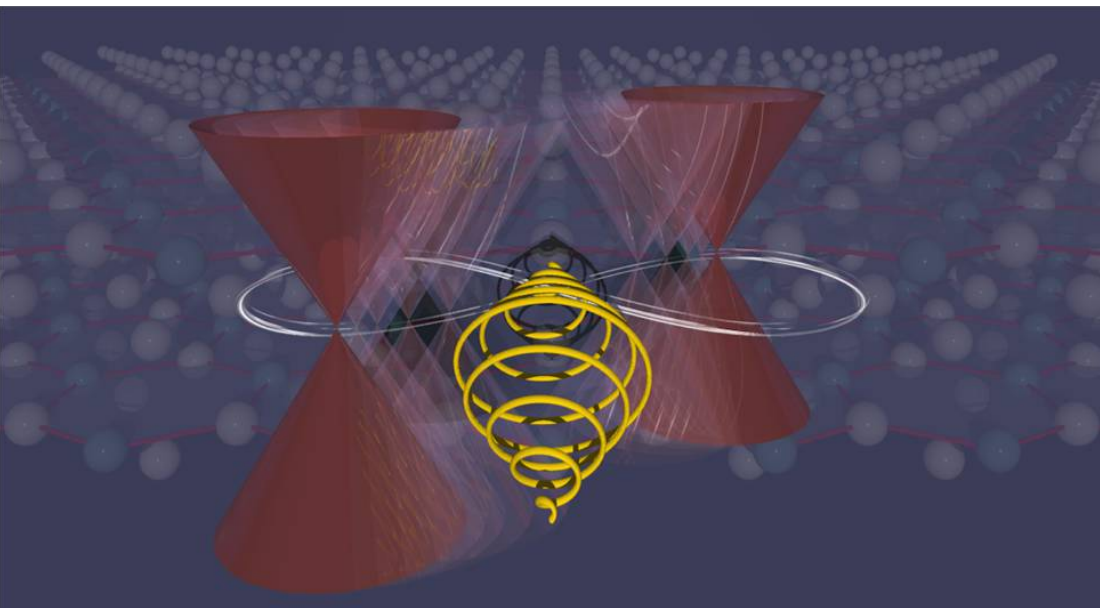
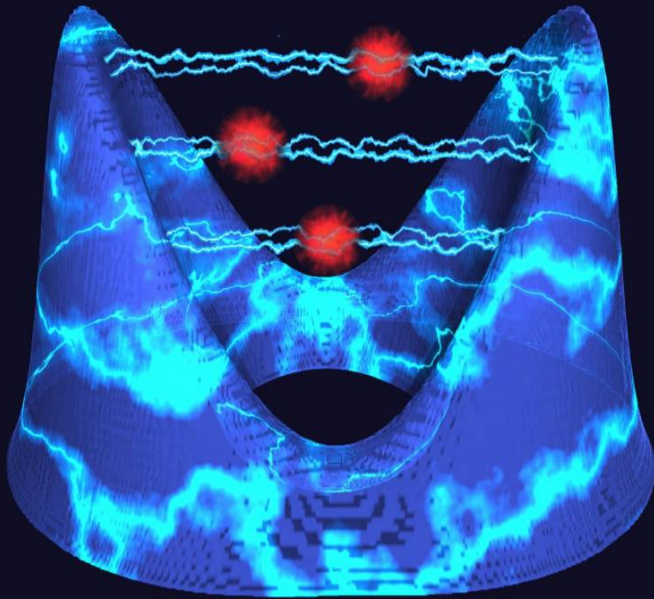
H. Appel, M. Ruggenthaler, J. Flick, R. Jestädt, C. Schäfer, T. Reinhard, U. Mordovina

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E.K.U. Gross, A. Castro



Thank You



Publications: (see group webpage)

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