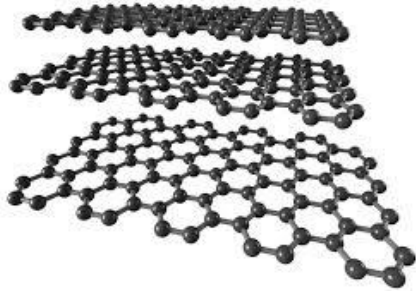


# Sliding Friction of Graphene/*h*-BN Heterojunctions: Towards Robust Solid Nano-Lubrication

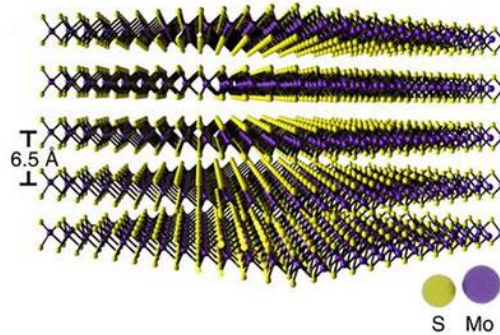
**Davide Mandelli, Itai Leven, Oded Hod, Michael Urbakh**



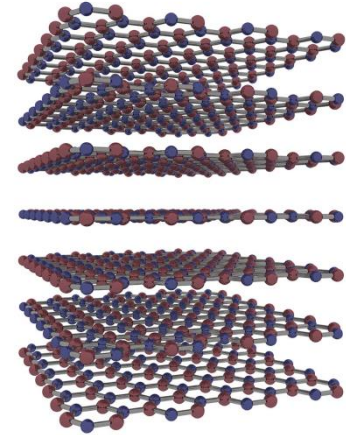
# Layered Materials as Solid Lubricants



Graphite



MoS<sub>2</sub>

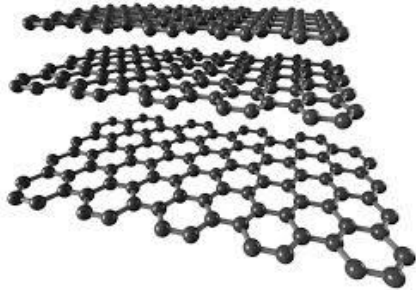


*h*-BN

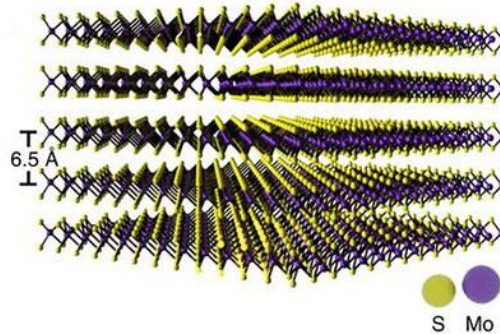
Strong covalent intra-layer bonds  
Weak Van-der-Waals interlayer interaction

**Easy, low-strength shearing between adjacent layers**

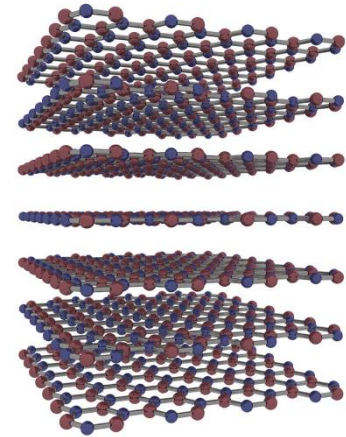
# Layered Materials as Solid Lubricants



**Graphite**



**MoS<sub>2</sub>**



**h-BN**

Strong covalent intra-layer bonds  
Weak Van-der-Waals interlayer interaction

**Easy, low-strength shearing between adjacent layers**

ALREADY IN USE AS LUBRICANT ADDITIVES

*Lubricants* **2014**, 2, 44-65; doi:10.3390/lubricants2020044

## **Graphite and Hybrid Nanomaterials as Lubricant Additives**

Zhenyu J. Zhang, Dorin Simionesie and Carl Schaschke \*

*Wear* **302** (2013) 981–986

Evaluation of hexagonal boron nitride nano-sheets as a lubricant additive in water

Dae-Hyun Cho <sup>a</sup>, Jin-Seon Kim <sup>a</sup>, Sang-Hyuk Kwon <sup>a</sup>, Changgu Lee <sup>\*,a,b</sup>, Young-Ze Lee <sup>\*,a</sup>

POTENTIAL APPLICATIONS IN NANO-  
AND MICRO-MECHANICAL DEVICES



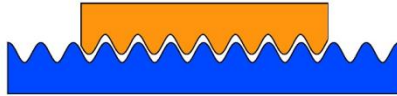
NEMS, data storage, ...

# Structural lubricity: graphitic junctions

## Commensurate

High barriers: large static friction

Stick-slip: large kinetic friction

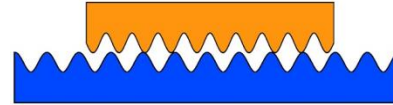


Identical lattices

## Incommensurate

Small barriers: small static friction

Smooth-sliding: small kinetic friction

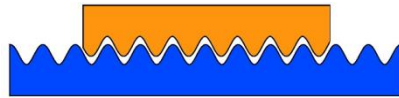


Mismatched lattices

# Structural lubricity: graphitic junctions

## Commensurate

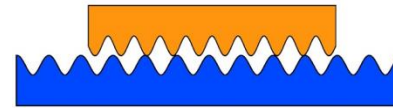
High barriers: large static friction  
Stick-slip: large kinetic friction



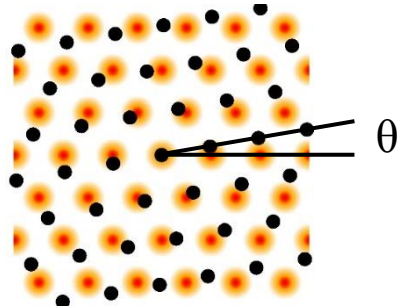
Identical lattices

## Incommensurate

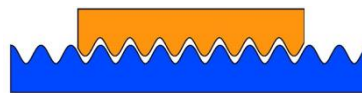
Small barriers: small static friction  
Smooth-sliding: small kinetic friction



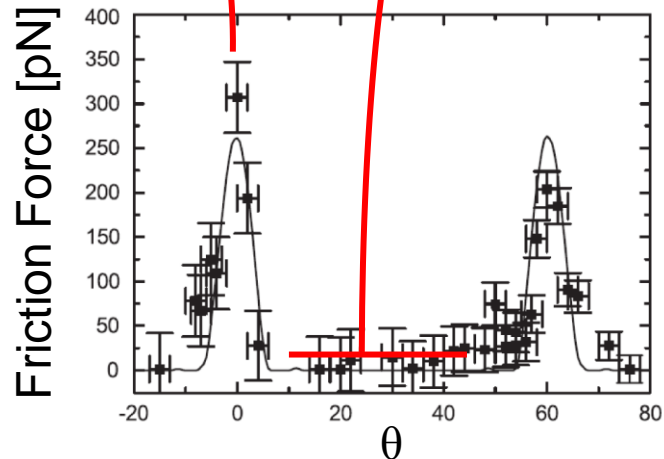
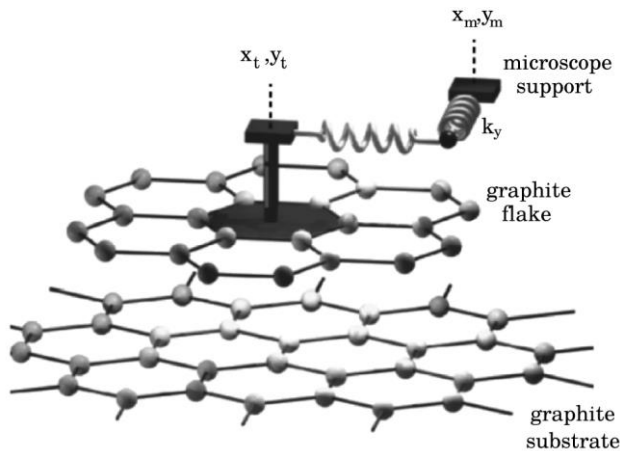
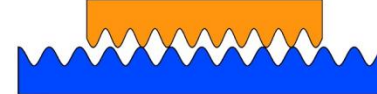
Mismatched lattices



Aligned  $\theta = k \cdot 60$



Misaligned:  $0 < \theta < 60$



# Structural lubricity: graphitic junctions

## Drawbacks of homogeneous junctions

PRL **100**, 046102 (2008)

PHYSICAL REVIEW LETTERS

week ending  
1 FEBRUARY 2008

### **Torque and Twist against Superlubricity**

Alexander E. Filippov,<sup>1</sup> Martin Dienwiebel,<sup>2,3</sup> Joost W. M. Frenken,<sup>2</sup> Joseph Klafter,<sup>4</sup> and Michael Urbakh<sup>4</sup>

Superlubricity in nano-sliders is only temporary as they tend to realign with the substrate.

# Structural lubricity: graphitic junctions

## Drawbacks of homogeneous junctions

PRL **100**, 046102 (2008)

PHYSICAL REVIEW LETTERS

week ending  
1 FEBRUARY 2008

### Torque and Twist against Superlubricity

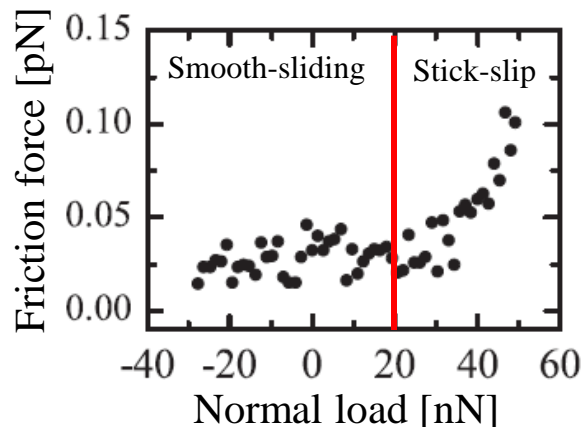
Alexander E. Filippov,<sup>1</sup> Martin Dienwiebel,<sup>2,3</sup> Joost W. M. Frenken,<sup>2</sup> Joseph Klafter,<sup>4</sup> and Michael Urbakh<sup>4</sup>

Superlubricity in nano-sliders is only temporary as they tend to realign with the substrate.

PHYSICAL REVIEW B **88**, 235423 (2013)

### Superlubric to stick-slip sliding of incommensurate graphene flakes on graphite

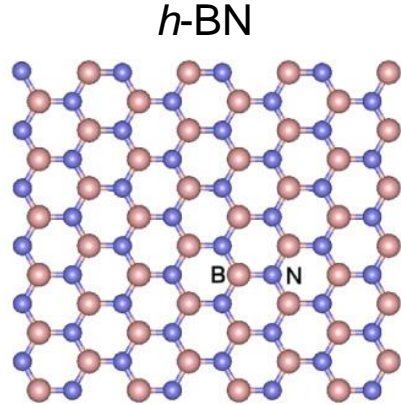
M. M. van Wijk,<sup>1</sup> M. Dienwiebel,<sup>2,3</sup> J. W. M. Frenken,<sup>4</sup> and A. Fasolino<sup>1</sup>



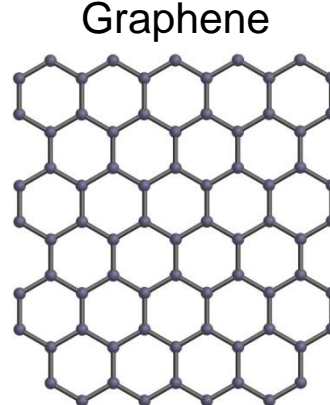
Even in misaligned, incommensurate conditions superlubricity may break at sufficiently high normal loads.



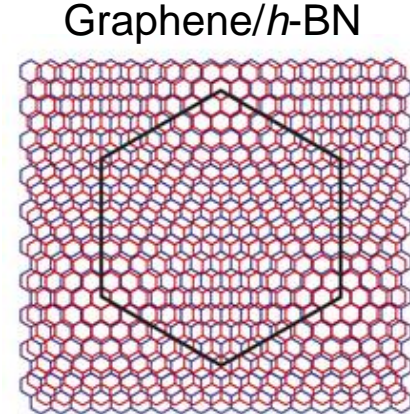
# Heterogeneous graphene/*h*-BN junctions



$$a_{h\text{-BN}} = 2.50 \text{ \AA}$$



$$a_g = 2.46 \text{ \AA}$$

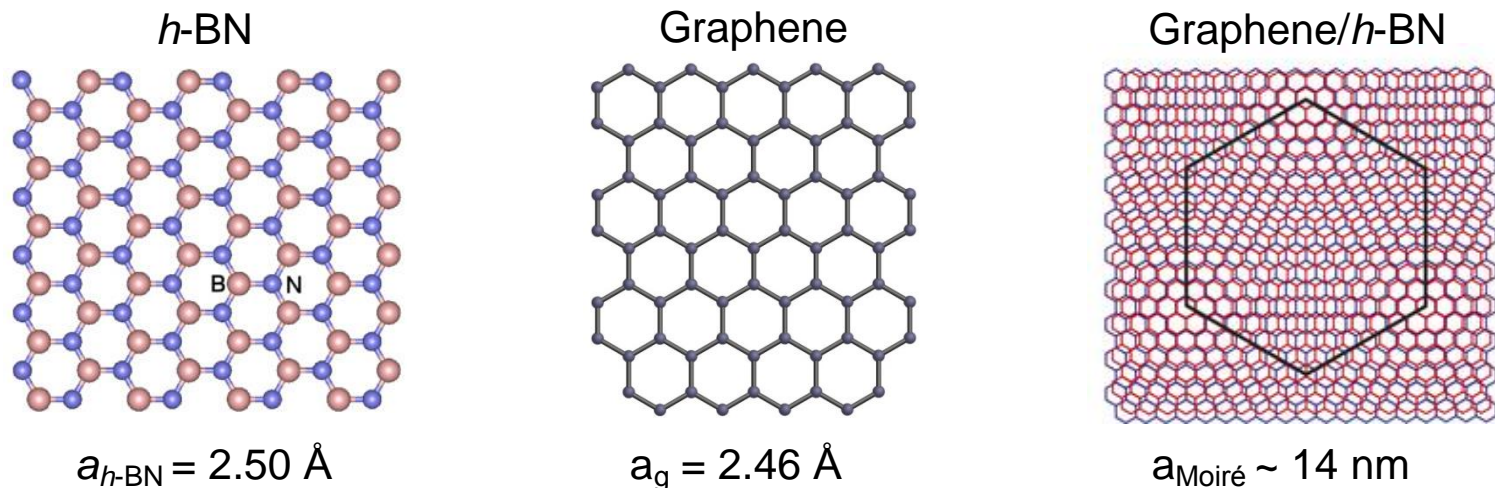


$$a_{\text{Moiré}} \sim 14 \text{ nm}$$

The natural intra-layer mismatch envisages the possibility to achieve superlubricity even in aligned configurations, when the size of the contact exceeds the Moiré periodicity.<sup>1</sup>



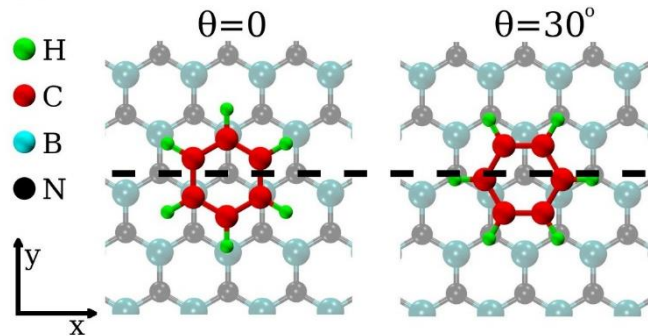
# Heterogeneous graphene/*h*-BN junctions



The natural intra-layer mismatch envisages the possibility to achieve superlubricity even in aligned configurations, when the size of the contact exceeds the Moiré periodicity.<sup>1</sup>

We performed fully atomistic molecular dynamics simulations of the sliding friction at **graphene/graphene** and **graphene/*h*-BN** interfaces

# Model and simulation protocol



Hexagonal graphene flakes of increasing size  $N_C$ .  
Edge carbons are saturated with Hydrogen atoms.  
Sliding along high symmetry 'x' direction.  
Substrate: rigid monolayer.

$$H = V_{inter} + V_{intra}^{flake} (+V_{intra}^{substrate})$$

$h$ -BN/graphene-ILP for the heterojunction.<sup>1</sup>  
Kolmogorov-Crespi + CH-ILP for the homojunction.<sup>2</sup>

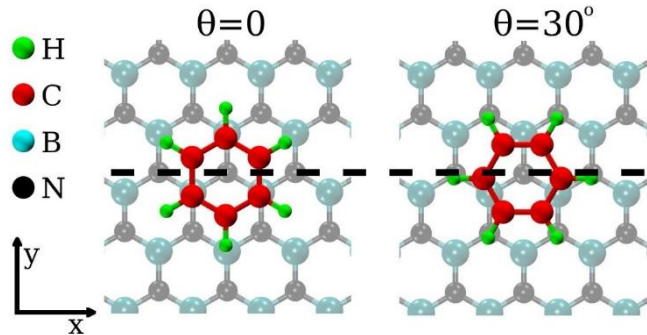
REBO-potential.<sup>3</sup>

1. Leven, I.; Maaravi, T.; Azuri, I.; Kronik, L.; Hod, O. *Journal of Chemical Theory and Computation* 2016, **12**, 2896-2905.

2. Kolmogorov, A. N.; Crespi, V. H. *Physical Review B* 2005, **71**, 235415.

3. Brenner, D. W.; Shenderova, O. A.; Harrison, J. A.; Stuart, S. J.; Ni, B.; Sinnott, S. B. *Journal of Physics: Condensed Matter* 2002, **14**, 783-802.

# Model and simulation protocol

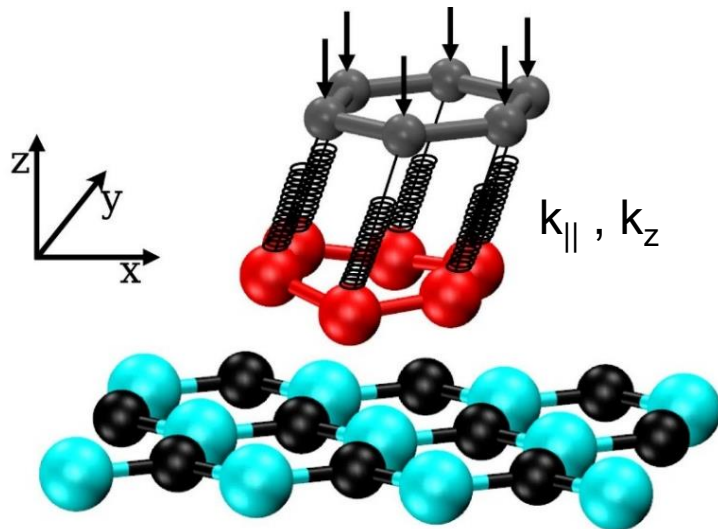


Hexagonal graphene flakes of increasing size  $N_C$ .  
 Edge carbons are saturated with Hydrogen atoms.  
 Sliding along high symmetry 'x' direction.  
 Substrate: rigid monolayer.

$$H = V_{inter} + V_{intra}^{flake} + \frac{1}{2} \sum_{i=1}^{N_{tot}} \{k_{\parallel} |\mathbf{r}_{i\parallel}^f - \mathbf{r}_{i\parallel}^{tip}|^2 + k_z^i (z_i^f - z^{tip})^2\}$$

DRIVING

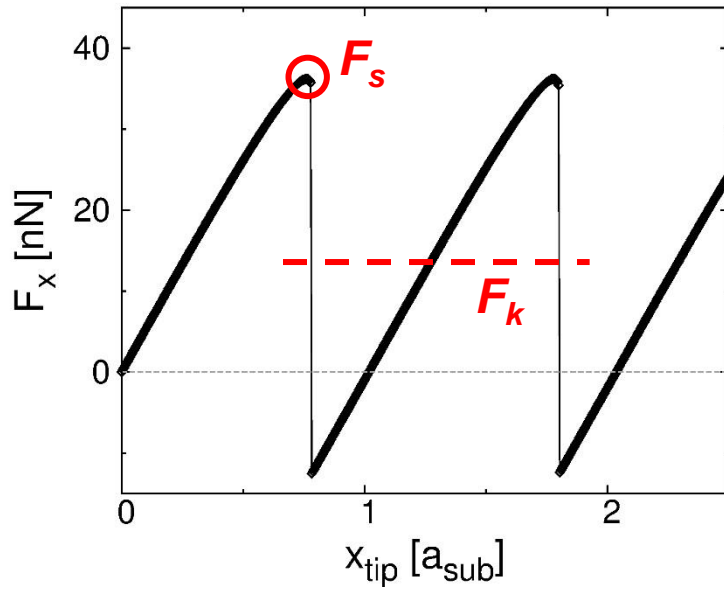
Normal load



## Quasi-static protocol

Rigid tip displaced in step  $\Delta x = 0.012 \text{ \AA}$ .  
 Load applied along 'z' to the tip center-of-mass.  
 Geometry optimized until  $\text{Max}_i(F_i) < 3.14 \times 10^{-4} \text{ eV/\AA}$ .  
 $k_{\parallel} = 16 \text{ meV/\AA}^2$   
 $k_{z,C} = 150 \text{ meV/\AA}^2$   
 $k_{z,H} = 43 \text{ meV/\AA}^2$   
 Load/atom =  $0.05 - 0.2 \text{ nN} = 2 - 8 \text{ GPa}$ .

# Definitions



## FRICION FORCE

$$F_x = \sum_{i=1}^{N_{tot}} k_{\parallel} (x_i^{tip} - x_i^f)$$

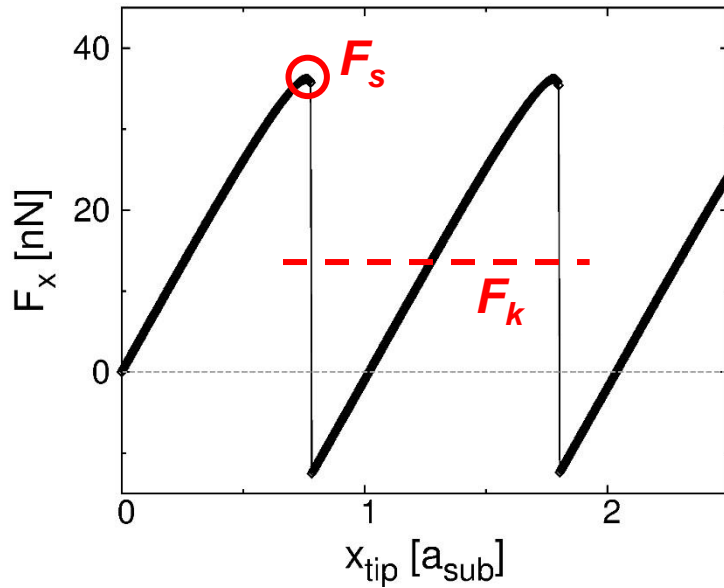
STATIC

$$F_s = \text{Max} (F_x)$$

KINETIC

$$F_k = \langle F_x \rangle$$

# Definitions

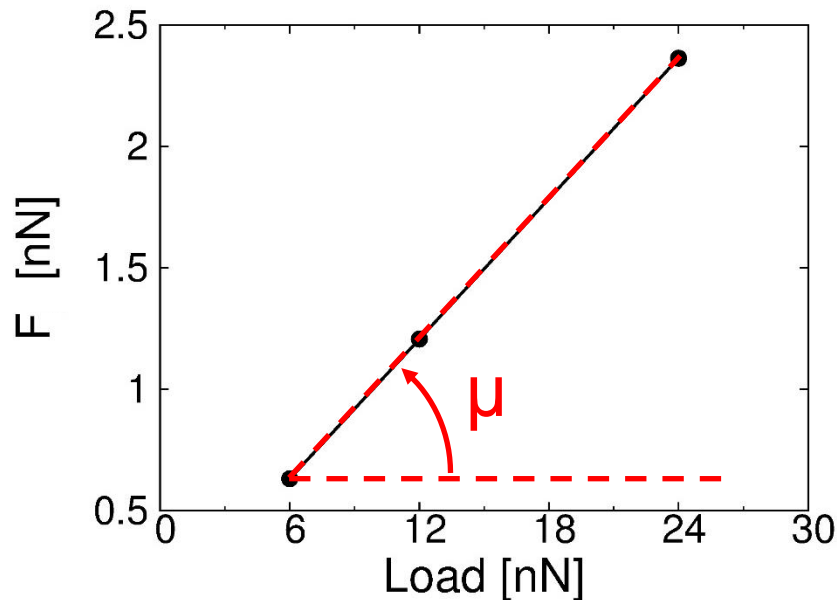


## FRICION FORCE

$$F_x = \sum_{i=1}^{N_{tot}} k_{\parallel} (x_i^{tip} - x_i^f)$$

STATIC  
 $F_s = \text{Max} (F_x)$

KINETIC  
 $F_k = \langle F_x \rangle$



## FRICION COEFFICIENTS

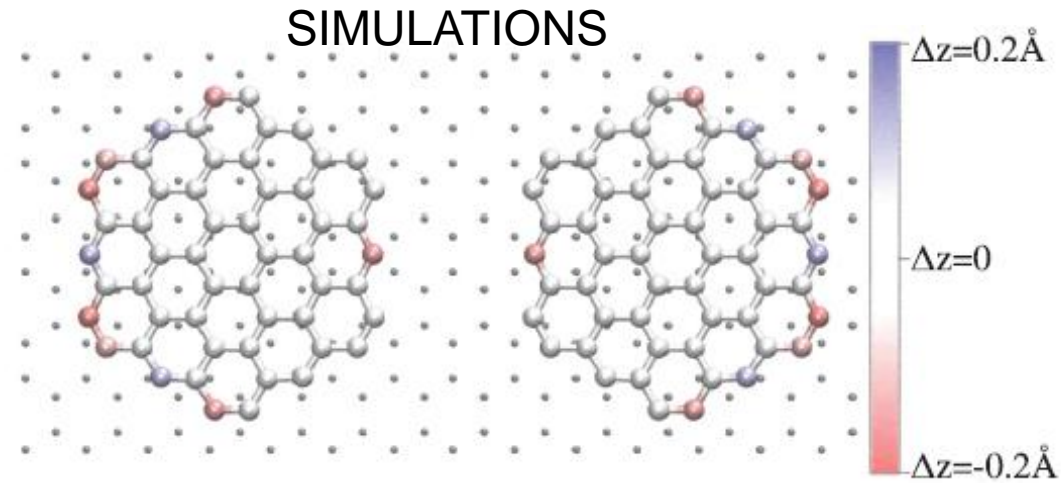
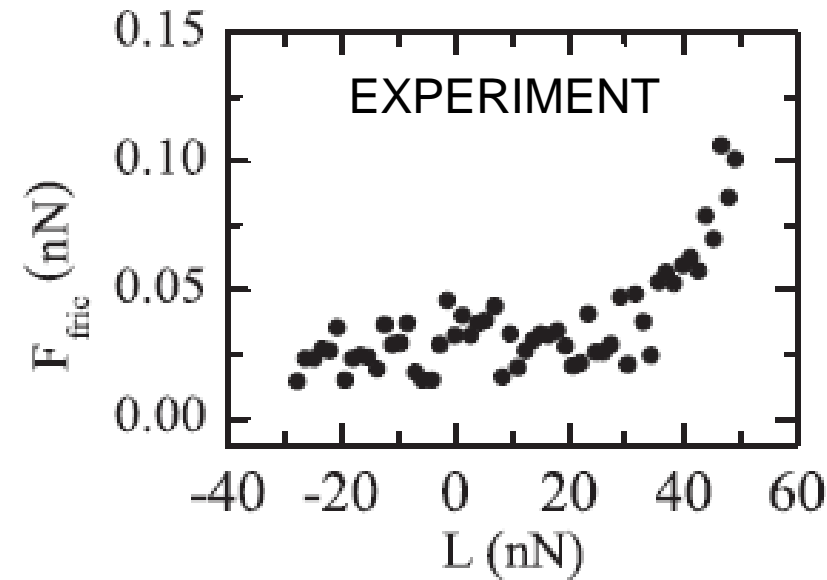
$$F \approx \alpha + \mu \cdot \text{Load}$$

STATIC  
 $\mu_s = \langle \frac{\Delta F_s}{\Delta L} \rangle$

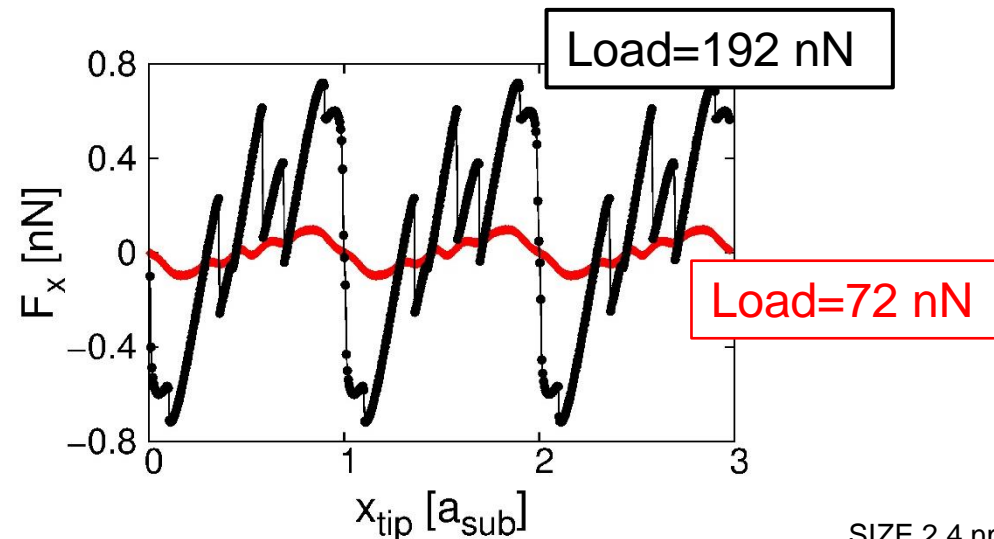
KINETIC  
 $\mu_k = \langle \frac{\Delta F_k}{\Delta L} \rangle$

# Superlubric to stick-slip sliding of incommensurate graphene flakes on graphite

M. M. van Wijk,<sup>1</sup> M. Dienwiebel,<sup>2,3</sup> J. W. M. Frenken,<sup>4</sup> and A. Fasolino<sup>1</sup>

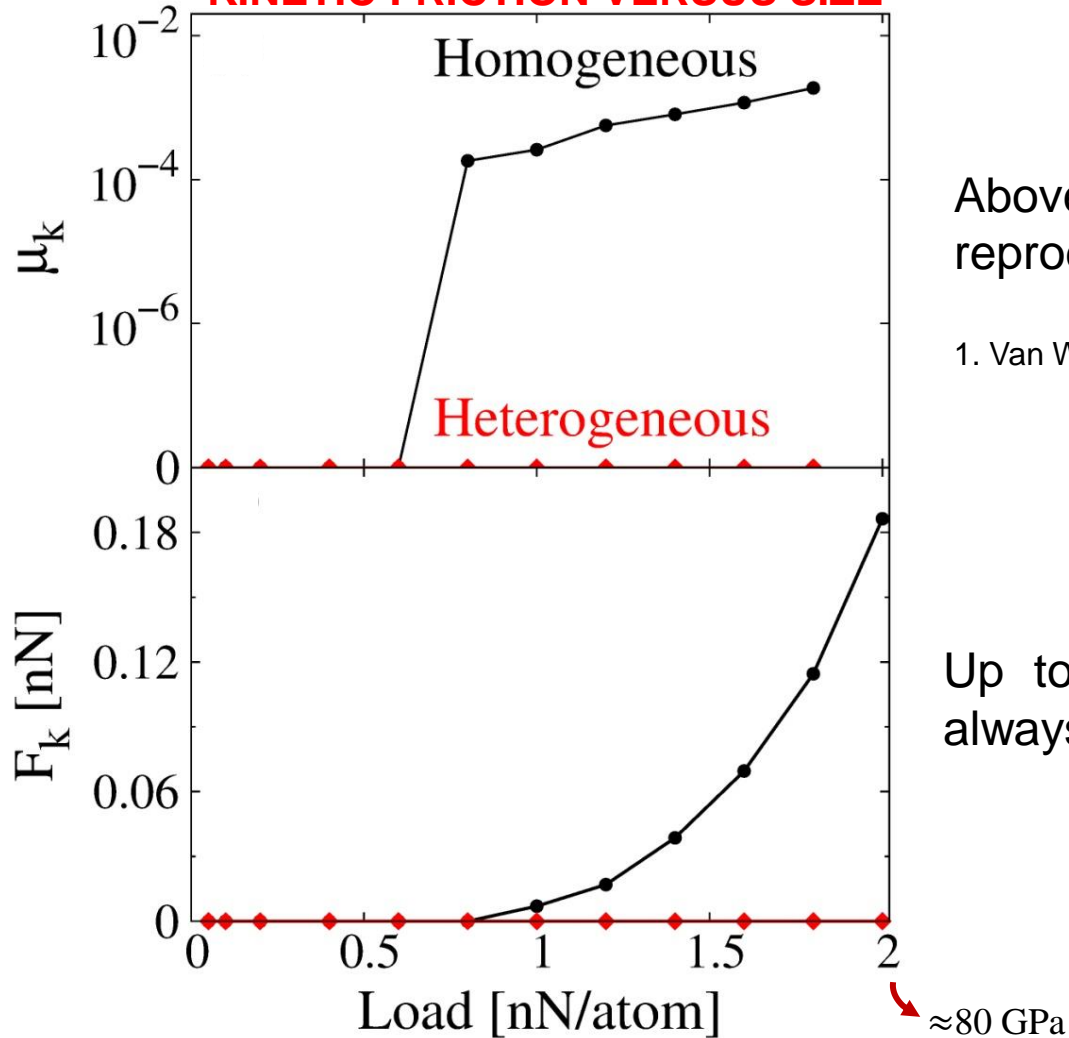


**EDGE ATOMS ARE MORE MOBILE**  
 At high loads they tend to lock the flake to the substrate.



# Results: misaligned interfaces $\theta=30^\circ$

## KINETIC FRICTION VERSUS SIZE



### Homogeneous junction

Above  $L=0.8$  nN/atom onset of stick-slip, reproducing the results of van Wijk *et al.*<sup>1</sup>

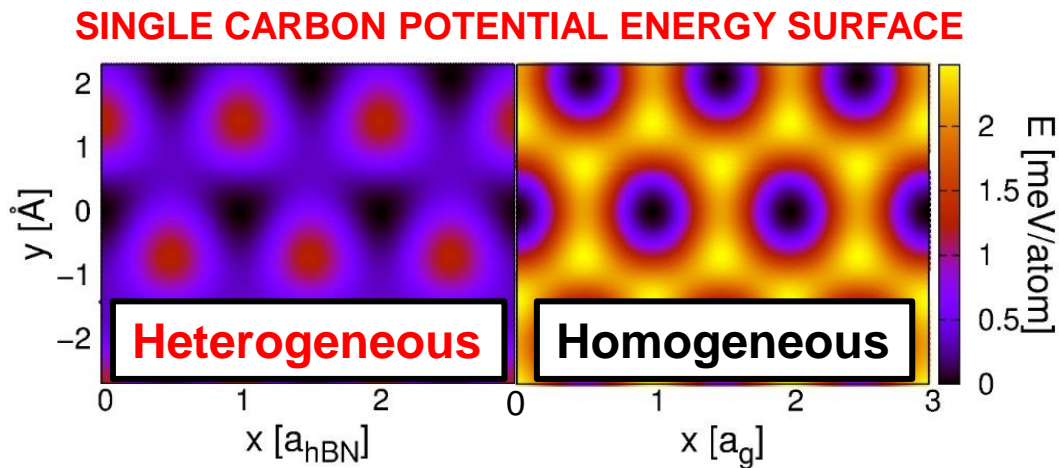
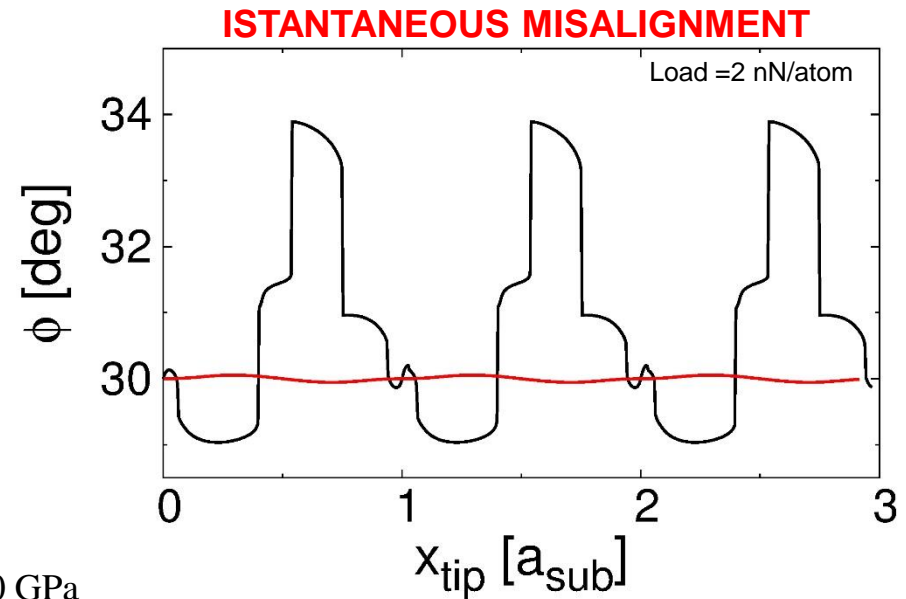
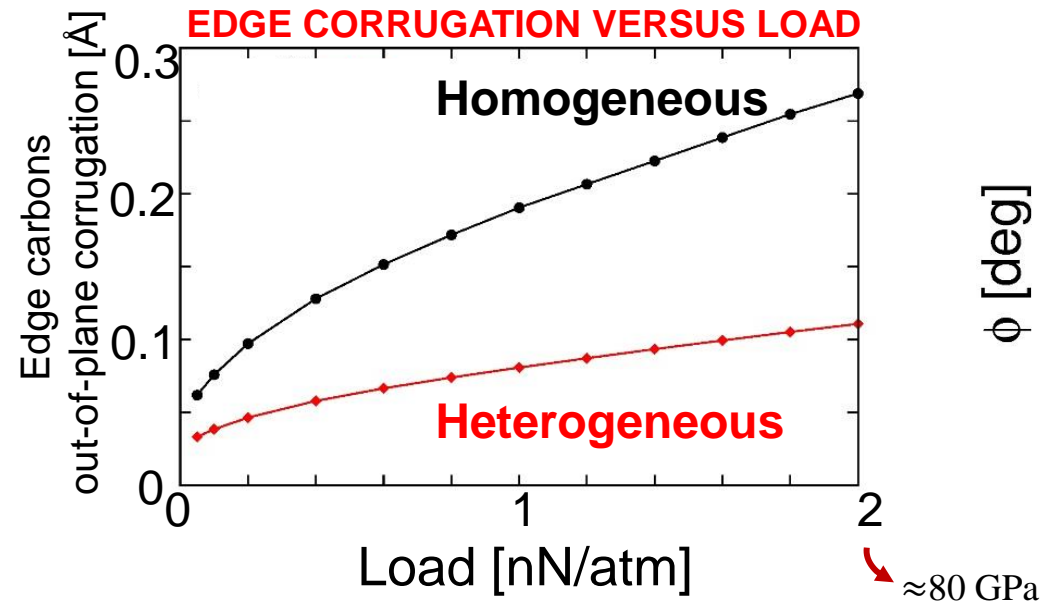
1. Van Wijk *et al.*, PRB **88**, 235423 (2013).

### Heterogeneous junction

Up to the highest load investigated we always observe a smooth-sliding regime.



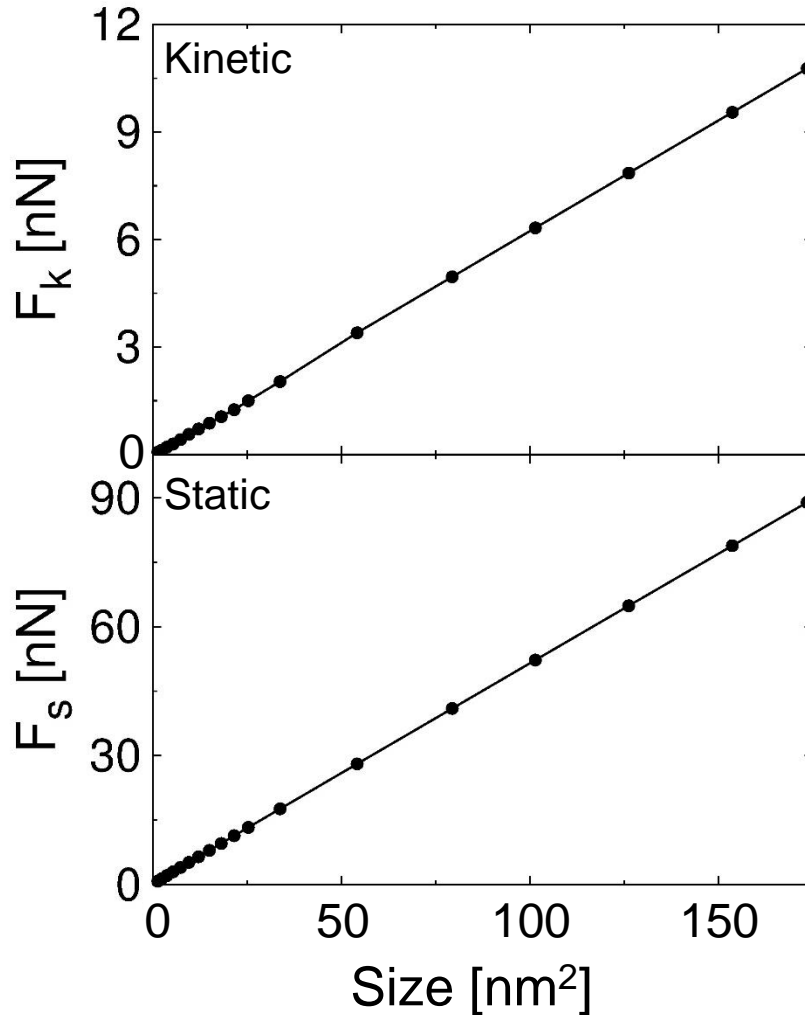
# Results: misaligned interfaces $\theta=30^\circ$



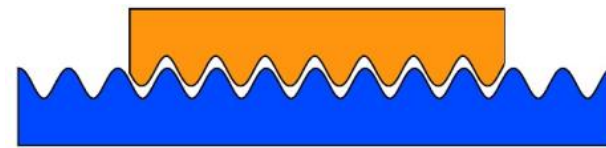
Over graphene edge carbons explore a more corrugated potential.

# Results: aligned interfaces $\theta=0$

## FRICTION FORCE VERSUS SIZE



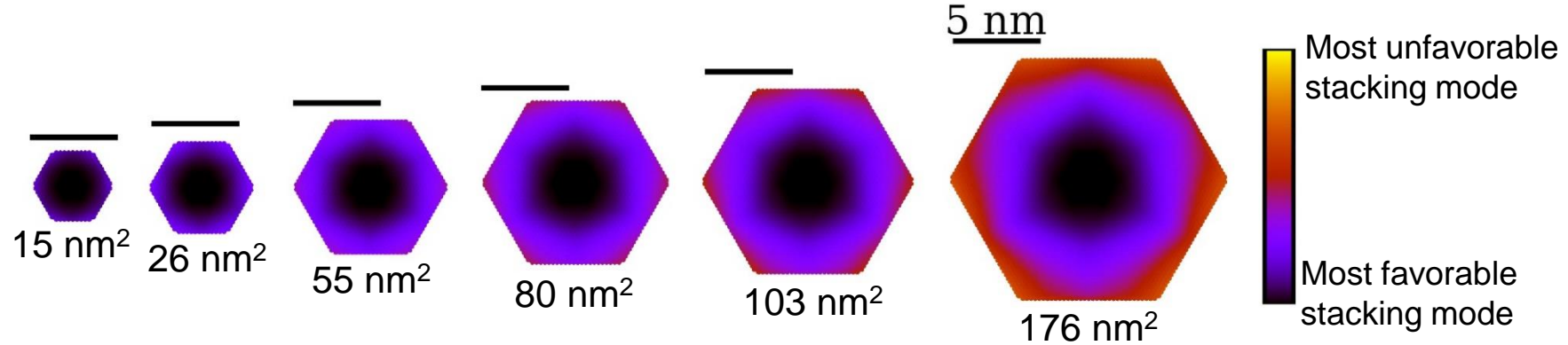
## Homogeneous junction

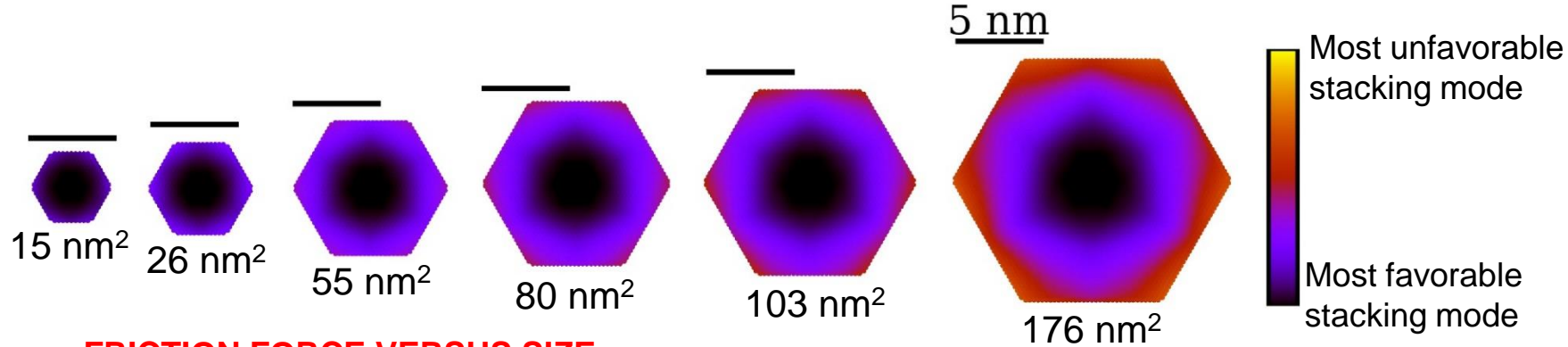


*Commensurate contact:*

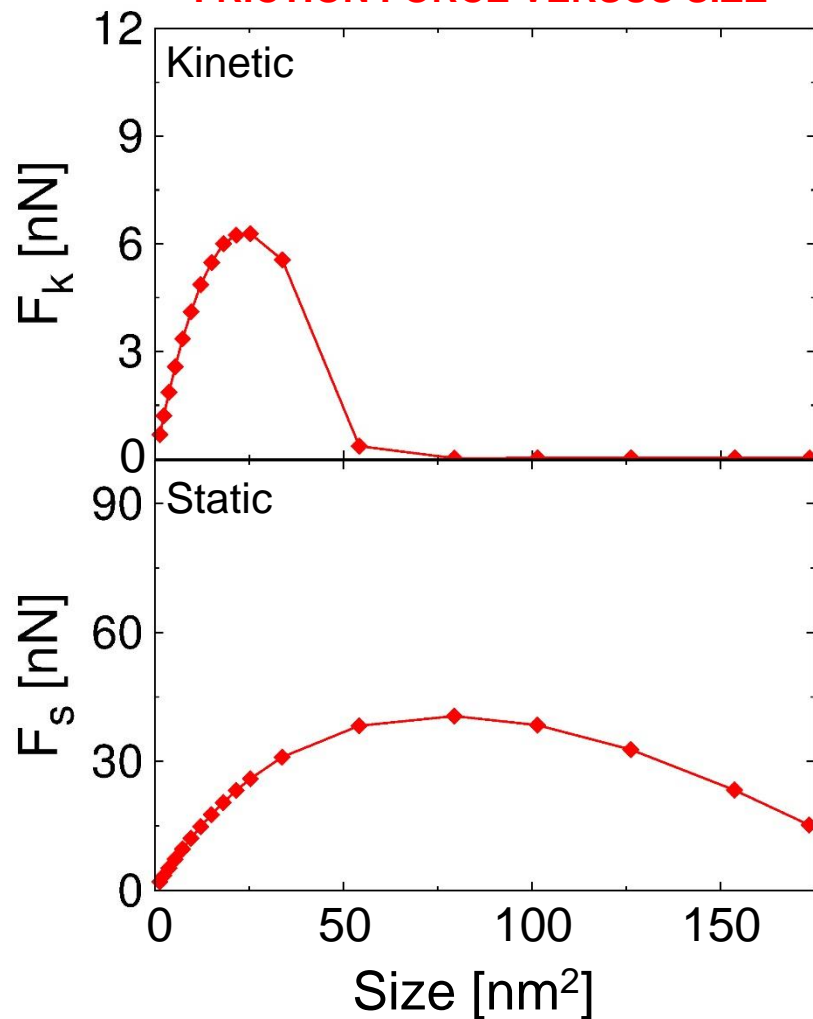
Highly dissipative stick-slip motion.

$F_k$ ,  $F_s$  grow linearly with size.





### FRICTION FORCE VERSUS SIZE



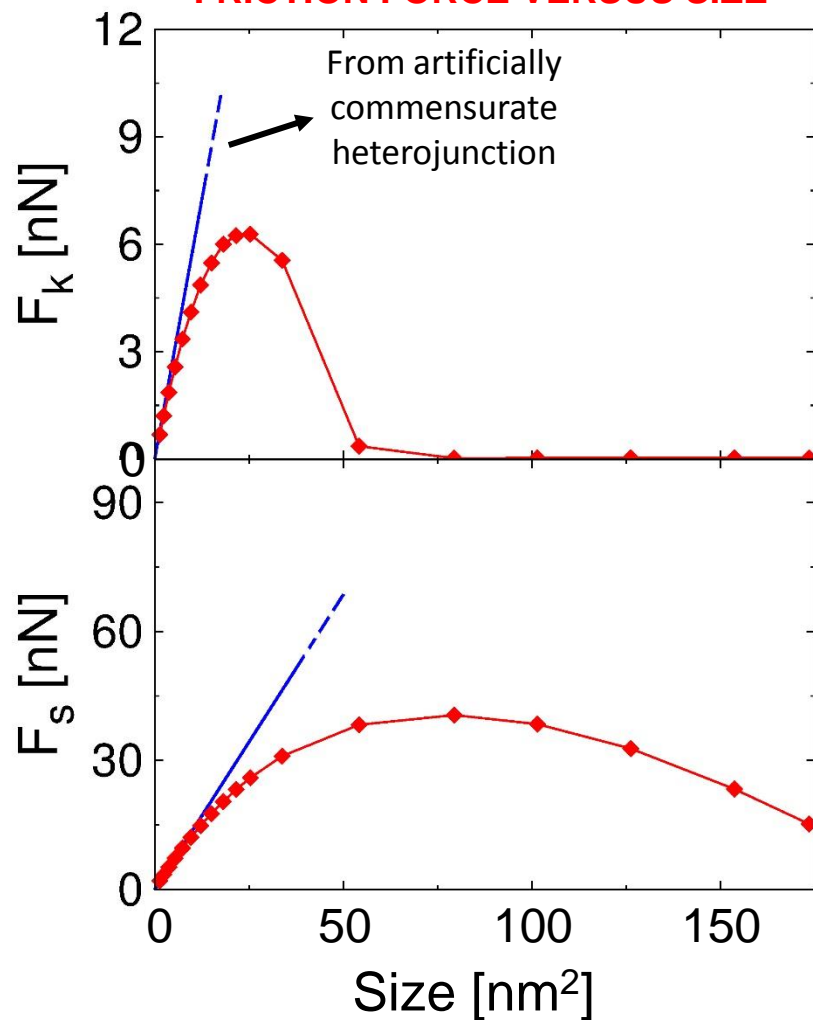
### Heterogeneous junction

Non-monotonic behavior of kinetic and static friction due to the progressive appearance of Moiré.

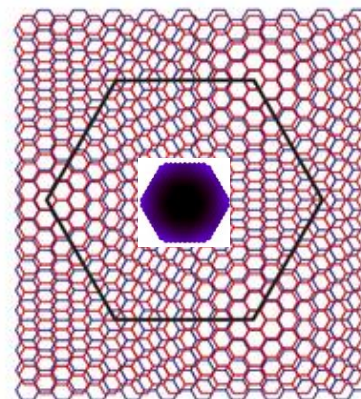
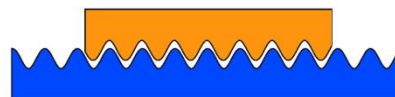
5 nm  
15 nm<sup>2</sup>

Most unfavorable  
stacking mode  
Most favorable  
stacking mode

### FRICTION FORCE VERSUS SIZE



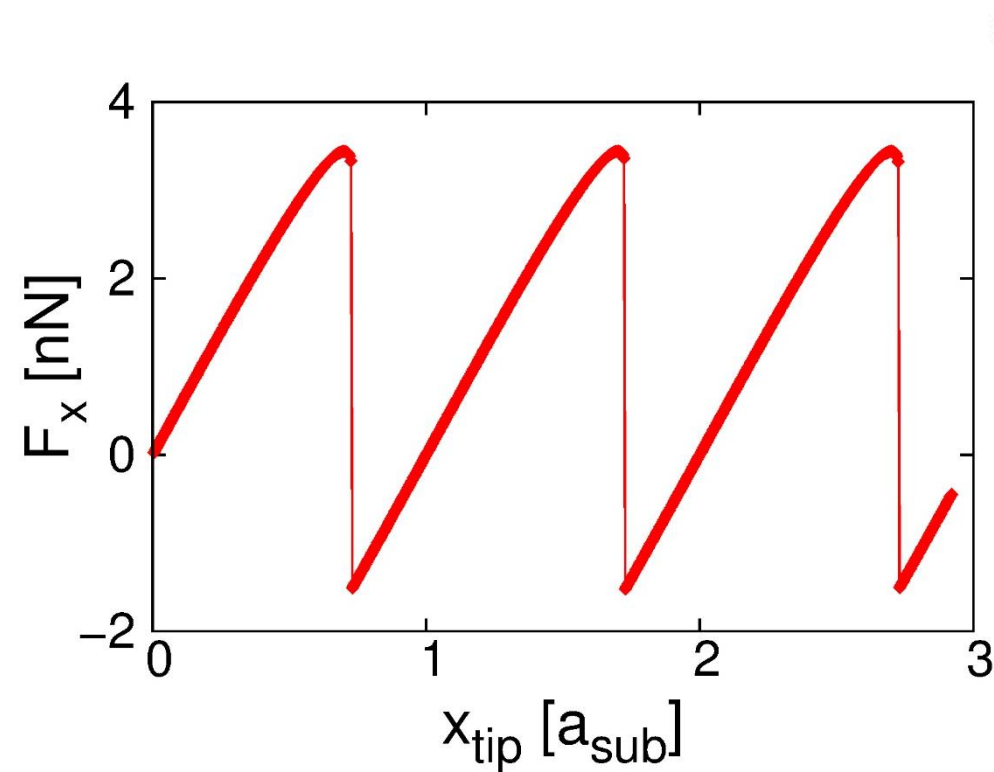
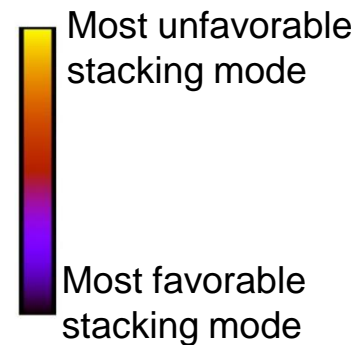
$0 < \text{size} < 20 \text{ nm}^2$  stick-slip, linear increase of  $F_k$ ,  $F_s$



Load = 0.1 nN/atom = 4 GPa

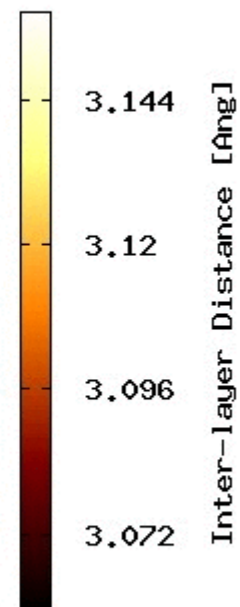
5 nm  
15 nm<sup>2</sup>

Diameter  $d < 5$  nm  
Nearly commensurate contact

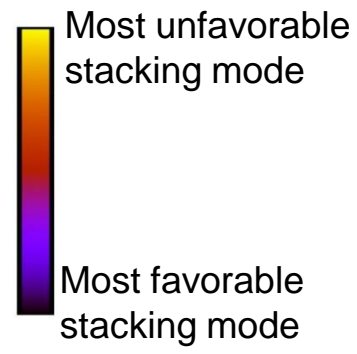
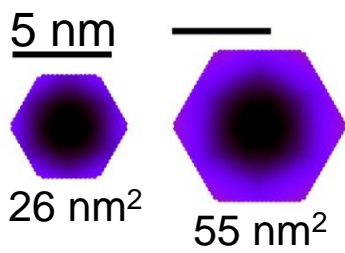


N=96 Load=0.1 nN/at X-tip=.012 Å

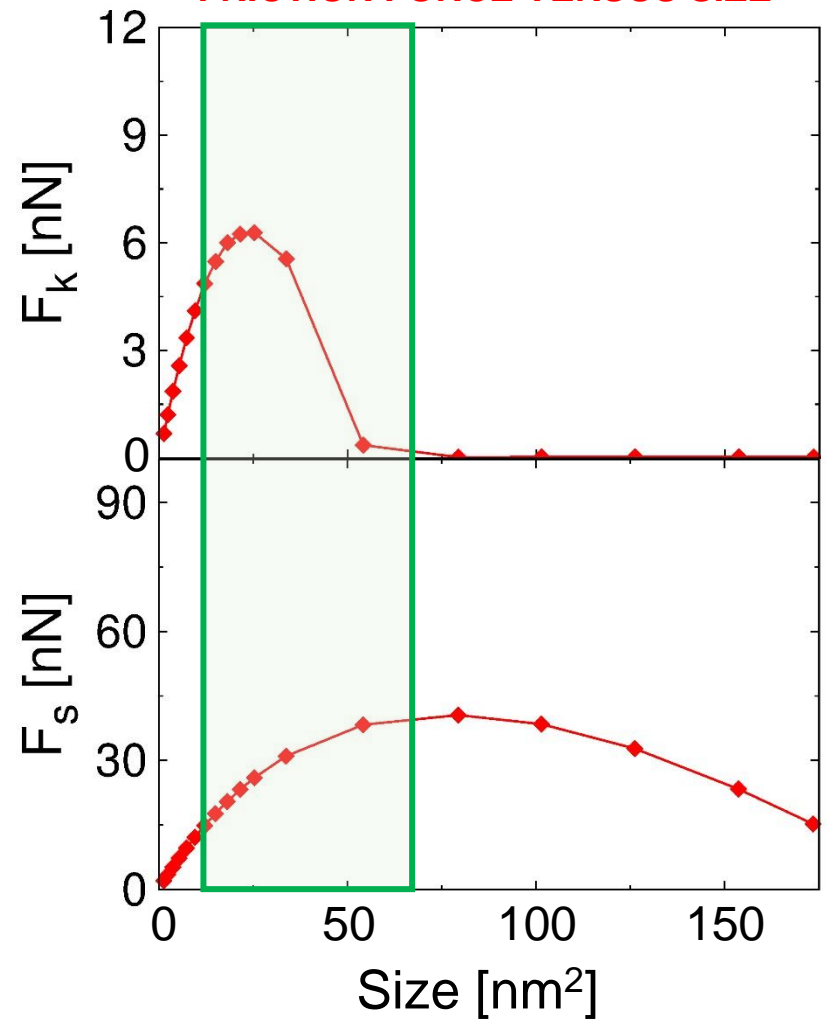
2.4 nm<sup>2</sup>



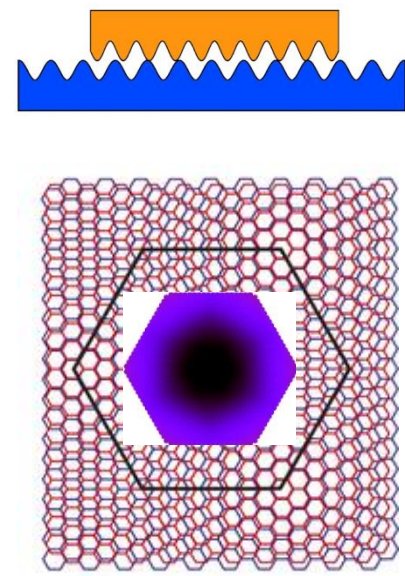
Load=0.1 nN/atom



# **FRICTION FORCE VERSUS SIZE**

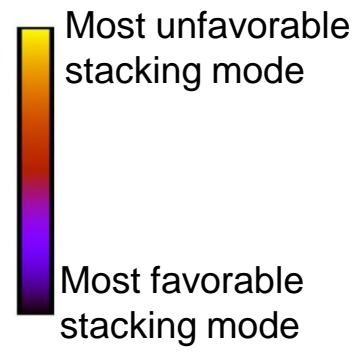
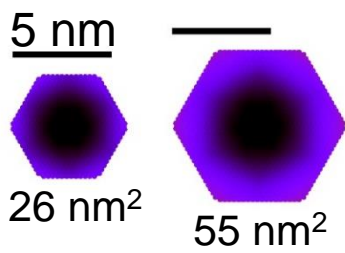


**20 < size < 70 nm<sup>2</sup> stick-slip, deviation from linearity.**



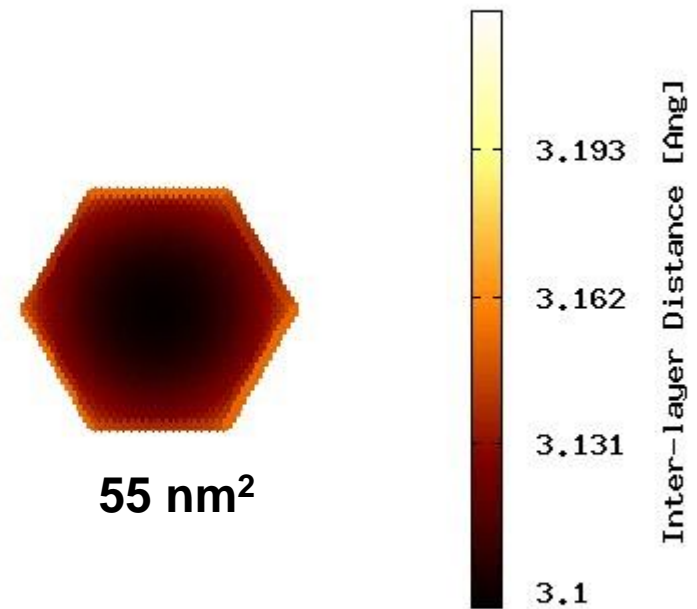
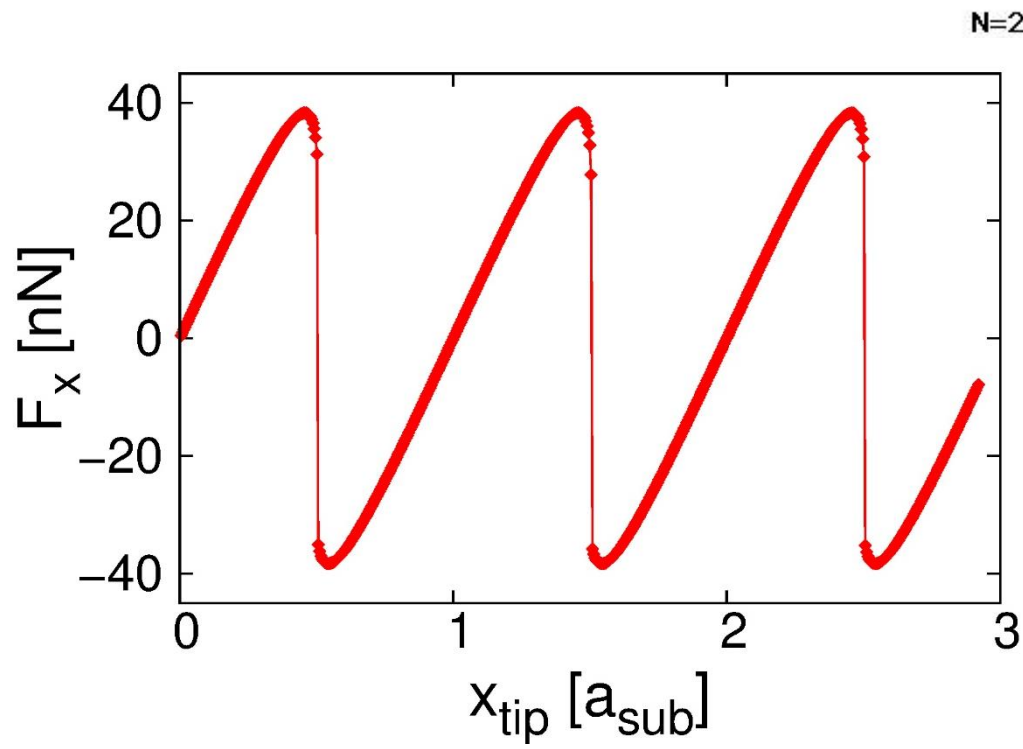
Load=0.1 nN/atom

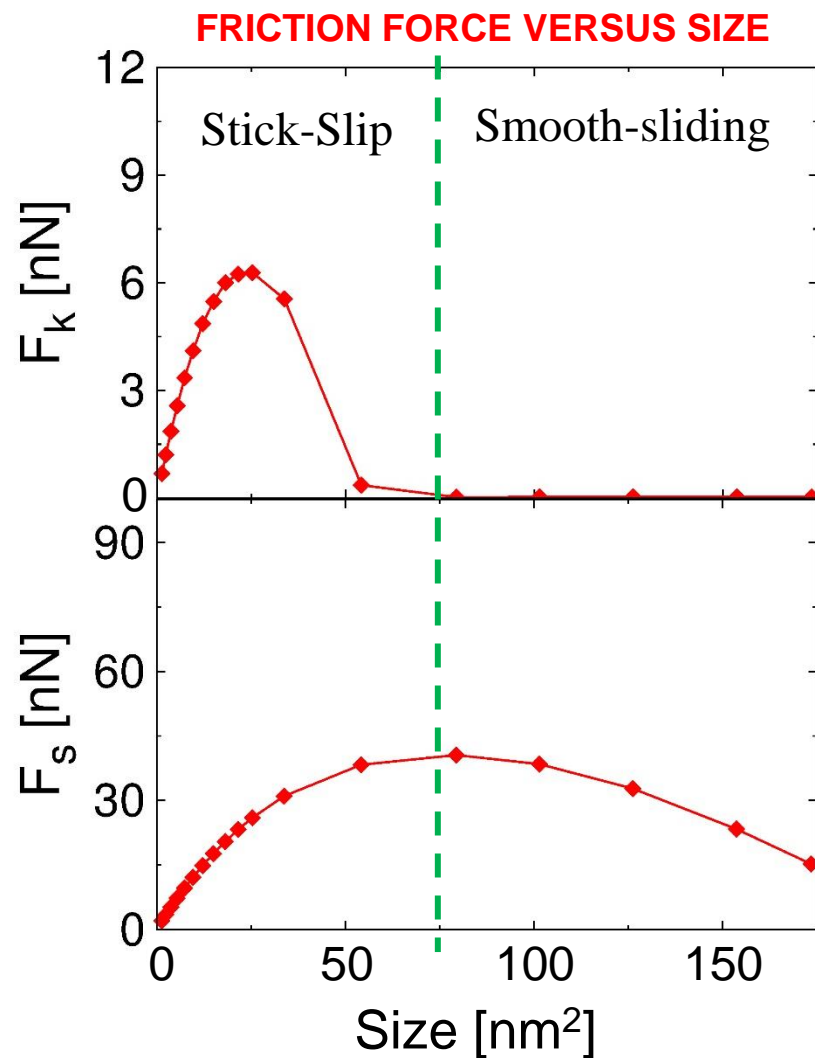
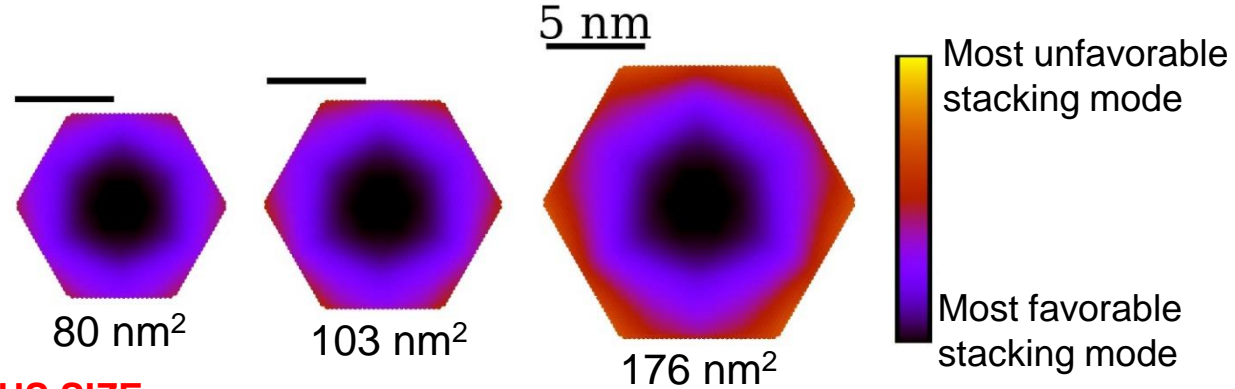




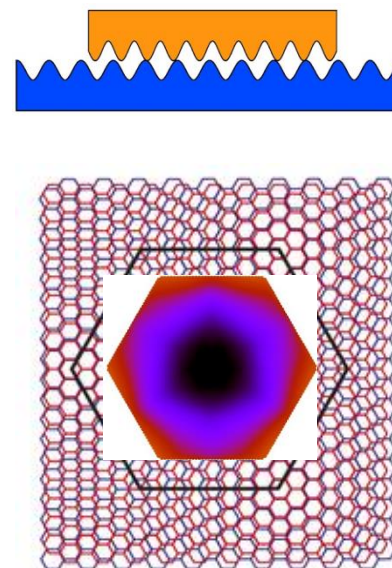
Diameter  $d \approx$  soliton-width  $\approx 5$  nm

Stick-slip instability  
triggered by the soliton

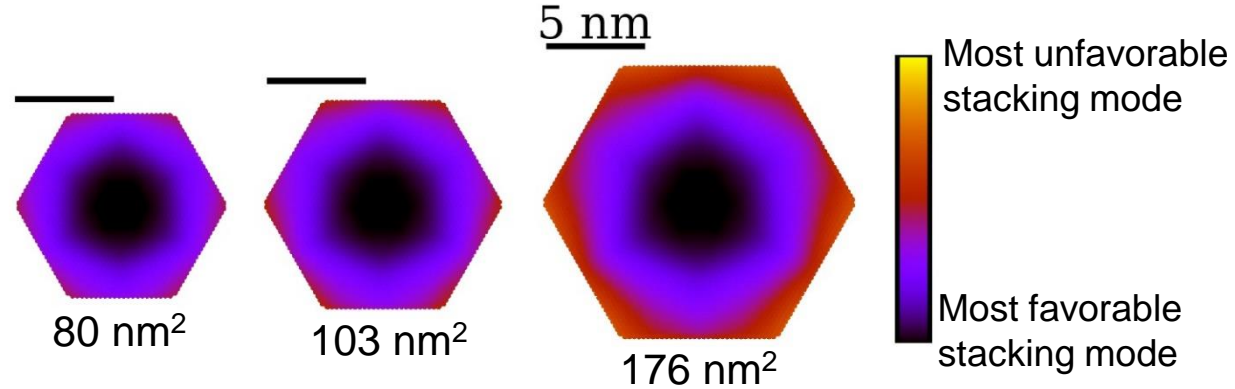




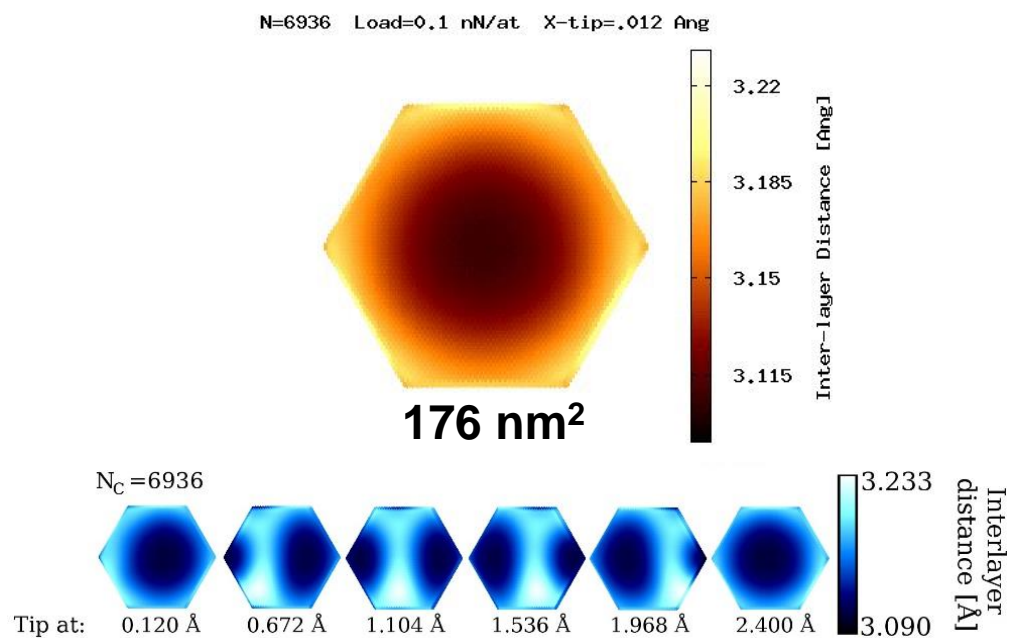
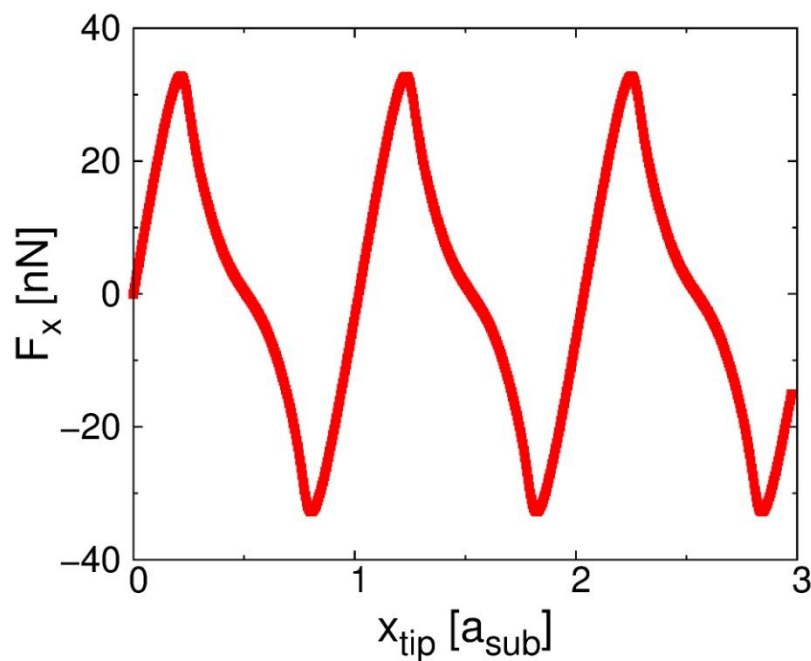
**Size > 70 nm<sup>2</sup> smooth sliding.**



Load=0.1 nN/atom



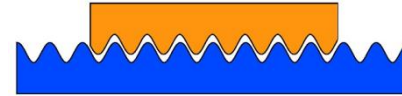
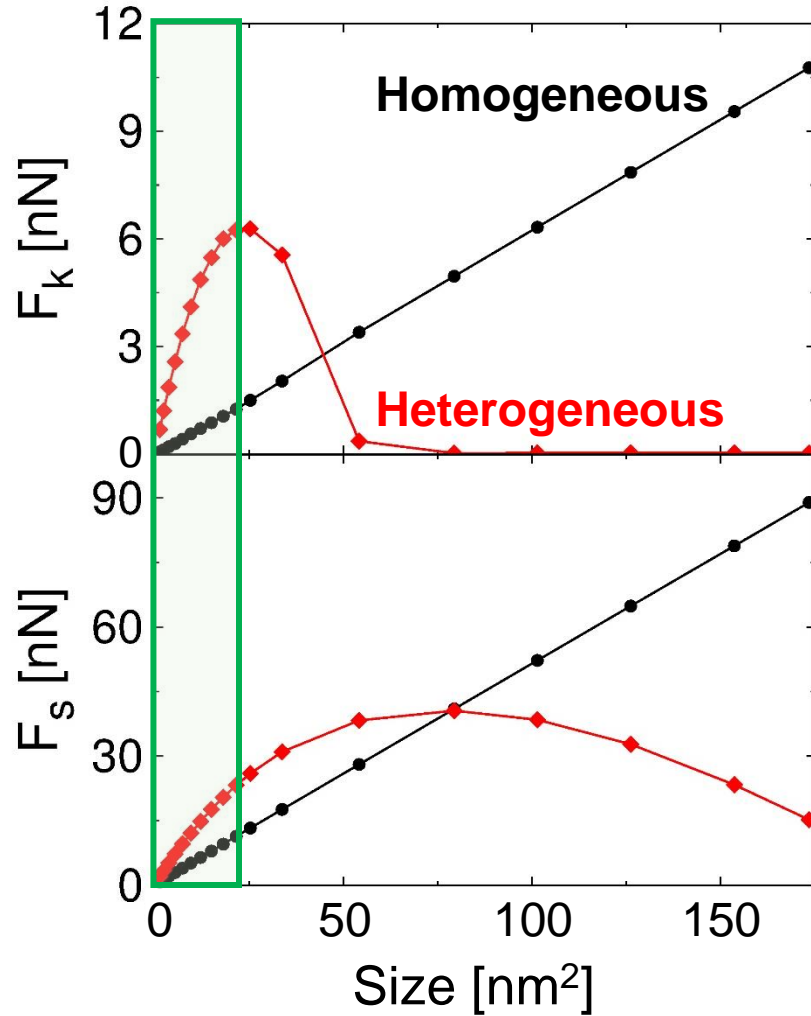
Diameter  $d >$  soliton-width  
**SMOOTH SLIDING**



Load=0.1 nN/atom

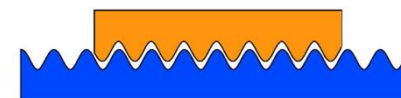
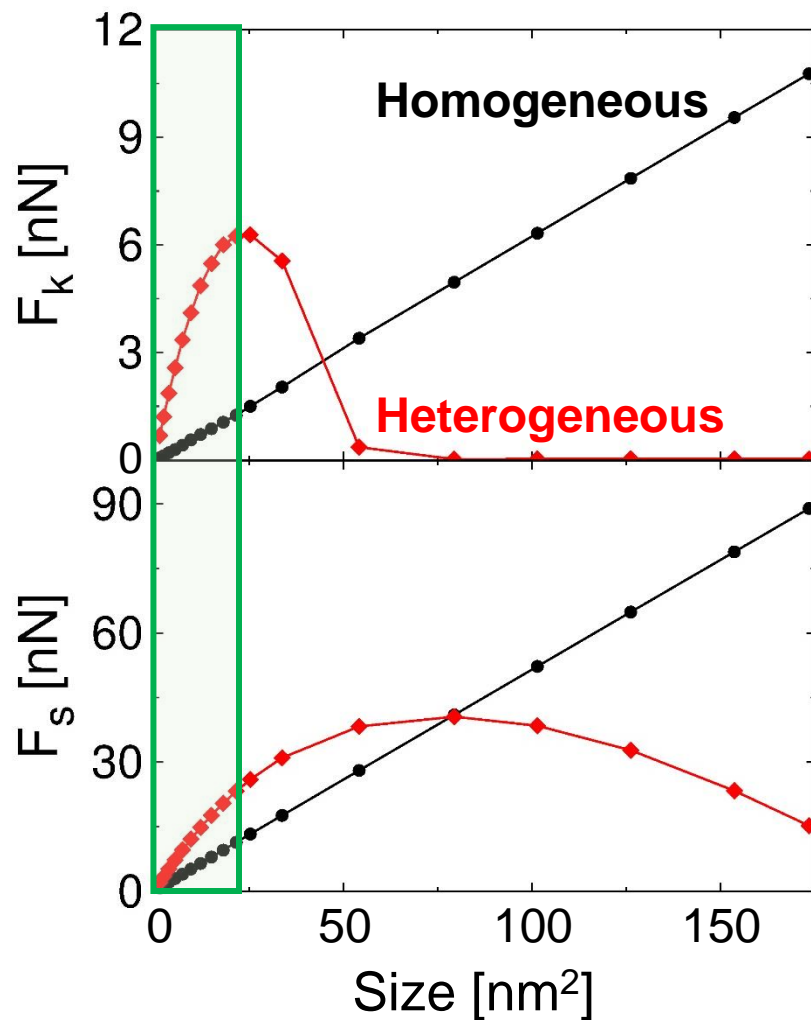
# Results: aligned interfaces $\theta=0$

## FRICTION FORCE VERSUS SIZE

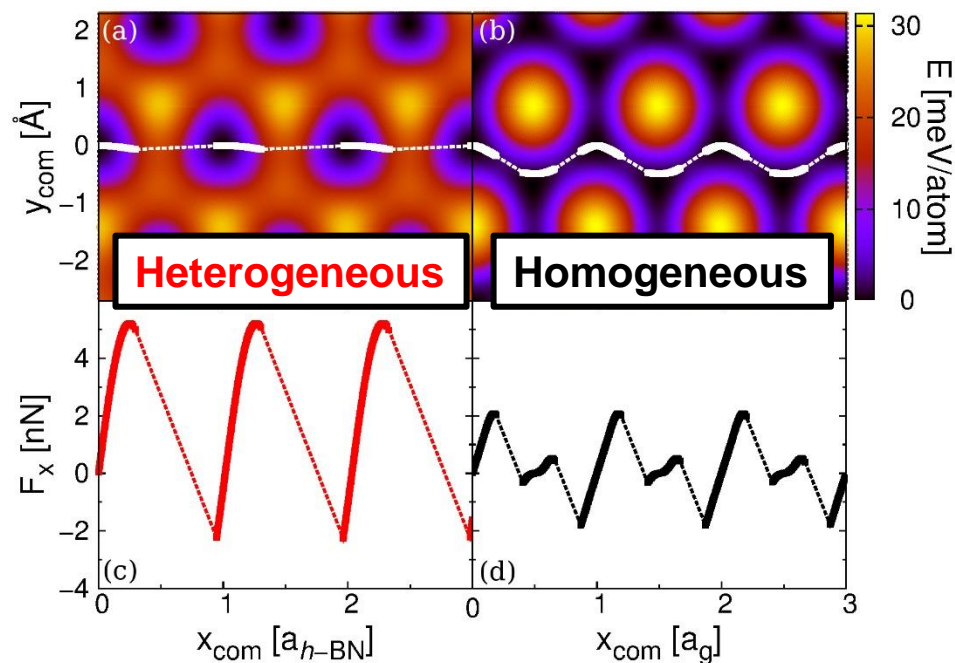


# Results: aligned interfaces $\theta=0$

FRICTION FORCE VERSUS SIZE

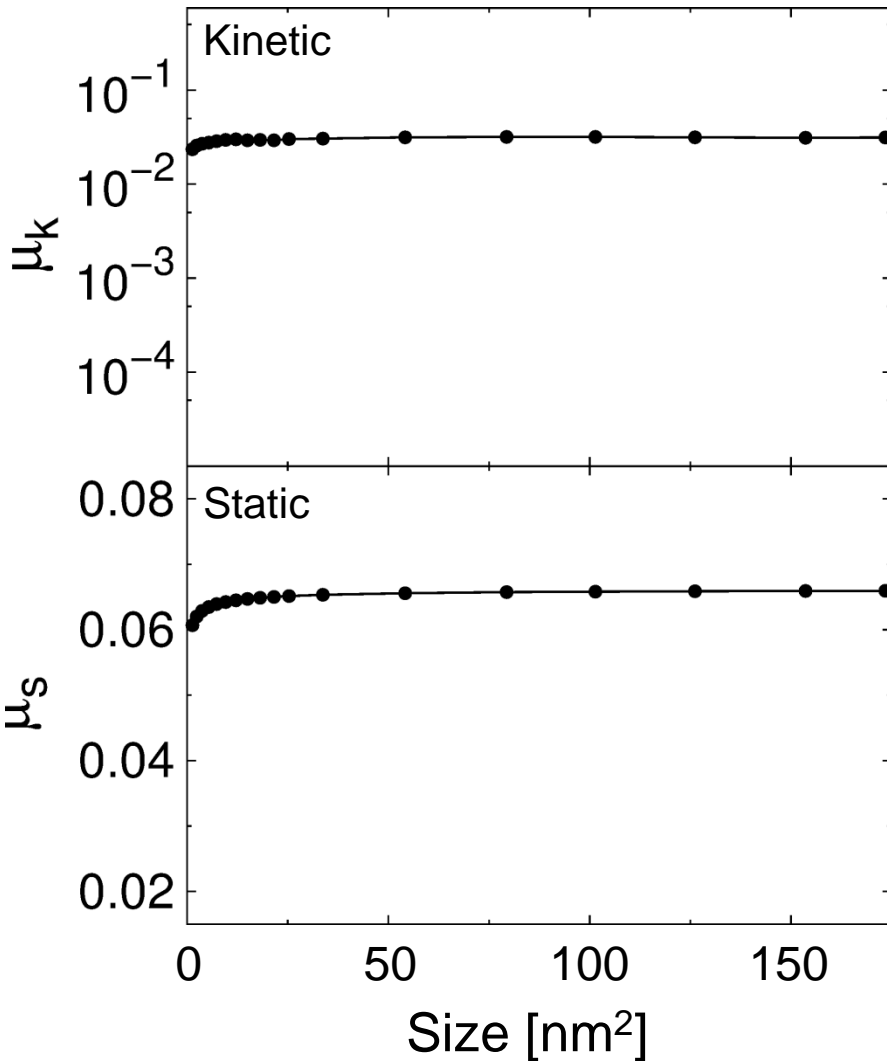


POTENTIAL ENERGY SURFACE



# Results: aligned junctions $\theta=0$

## FRICTION COEFFICIENT VERSUS SIZE



## Homogeneous

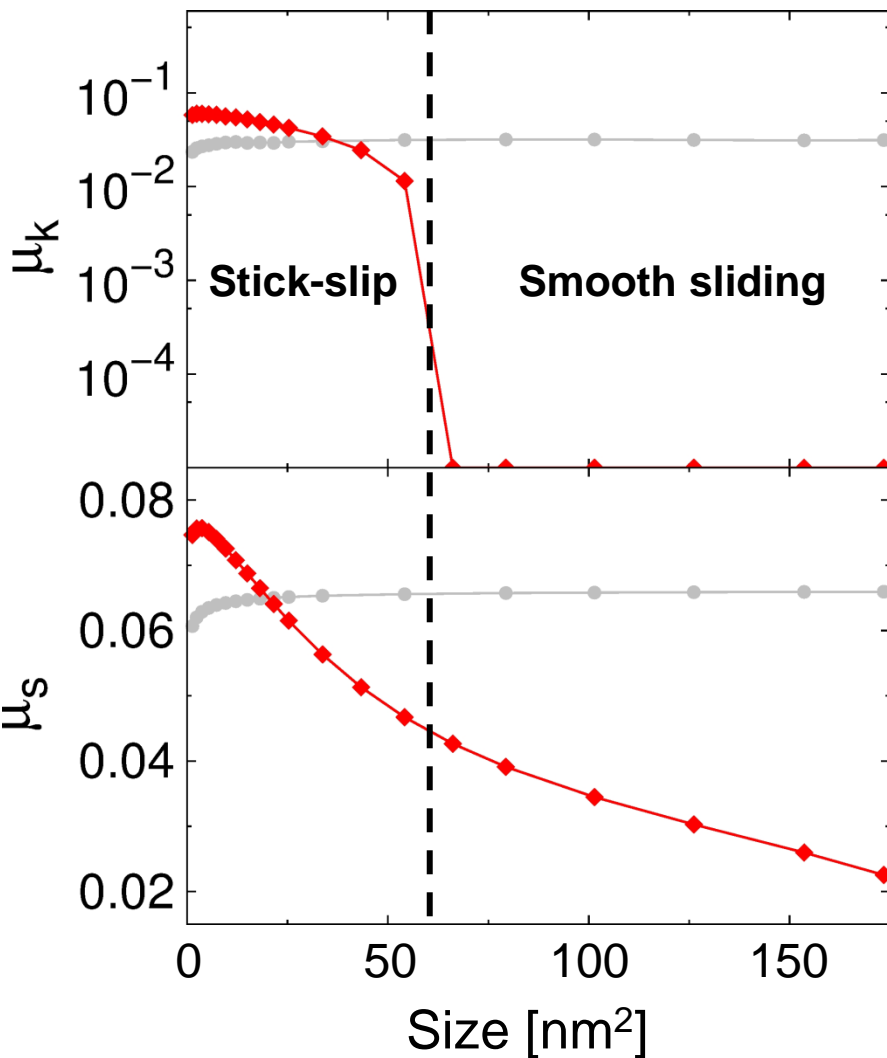
Friction coefficient saturates at large sizes.  
 $\mu_k \approx 0.03$  is in good agreement with typical exp. values for microscale graphitic contacts.

Edge effects account for the initial growth.

1. D. Marchetto *et al.*, Tribol. Lett. **48**, 77 (2012).

# Results: aligned junctions $\theta=0$

## FRICTION COEFFICIENT VERSUS SIZE



## Heterogeneous

Crossover between stick-slip to superlubric smooth sliding.

Onset of superlubricity at contact size  $\approx 60 \text{ nm}^2$ . Well below the size of the Moiré  $\approx 200 \text{ nm}^2$ .

## Dependence on $k_{||}$ :

The crossover occurs at sizes  $<$  Moiré in the whole estimated experimental range of  $k_{||} \approx 11\text{-}30 \text{ meV/\AA}^2$ .



# Conclusions

## **MISALIGNED INTERFACE, $\theta=30^\circ$**

### Small loads:

Superlubric smooth sliding;

Static and kinetic friction force independent of size;

No significant difference between homogeneous and heterogeneous contacts;

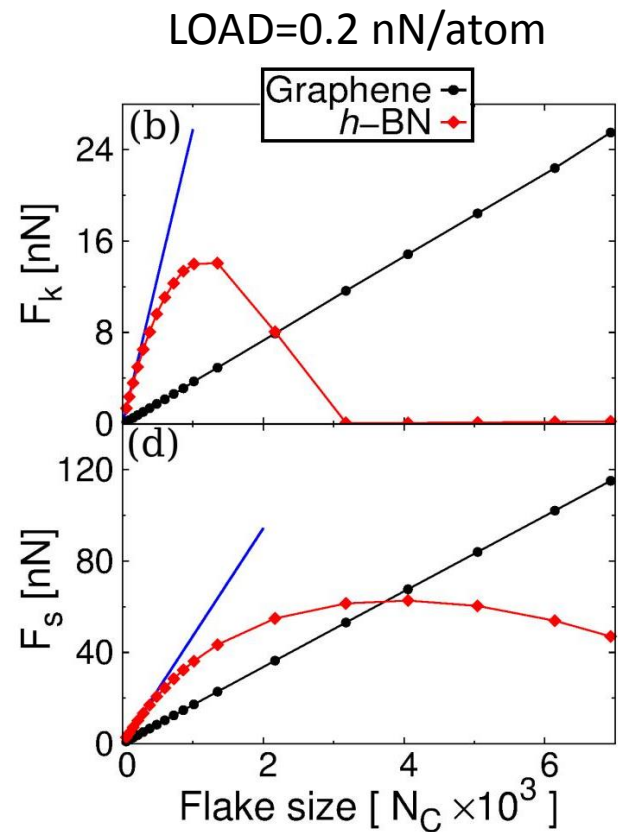
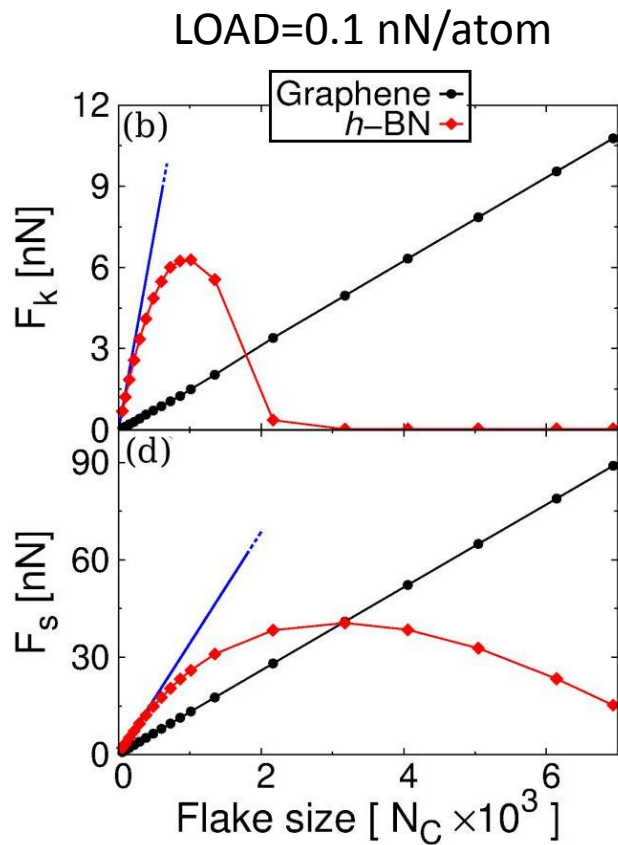
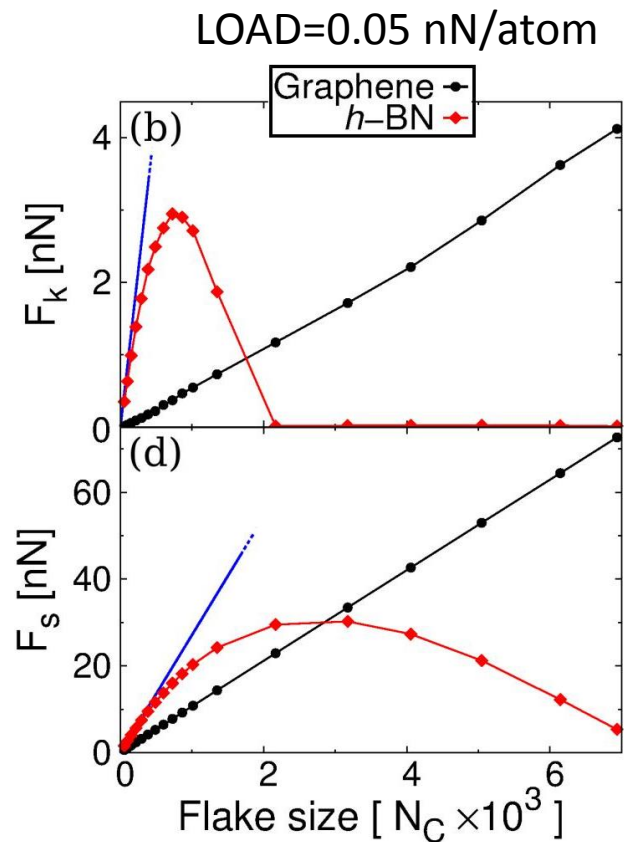
### High loads:

The smoother potential energy surface at small interlayer distances makes superlubricity more robust against load in heterogeneous nano-contacts when compared with their homogeneous counterparts.

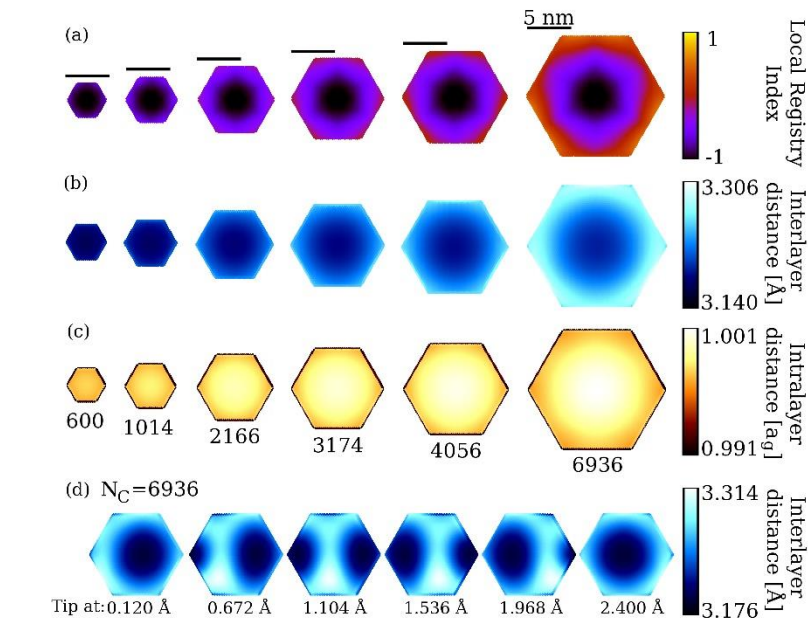
## **ALIGNED INTERFACE, $\theta=0^\circ$**

Crossover from stick-slip to superlubricity at contact size  $\approx 80 \text{ nm}^2$ , significantly smaller than the size  $\approx 200 \text{ nm}^2$  of one full Moiré “primitive cell”.

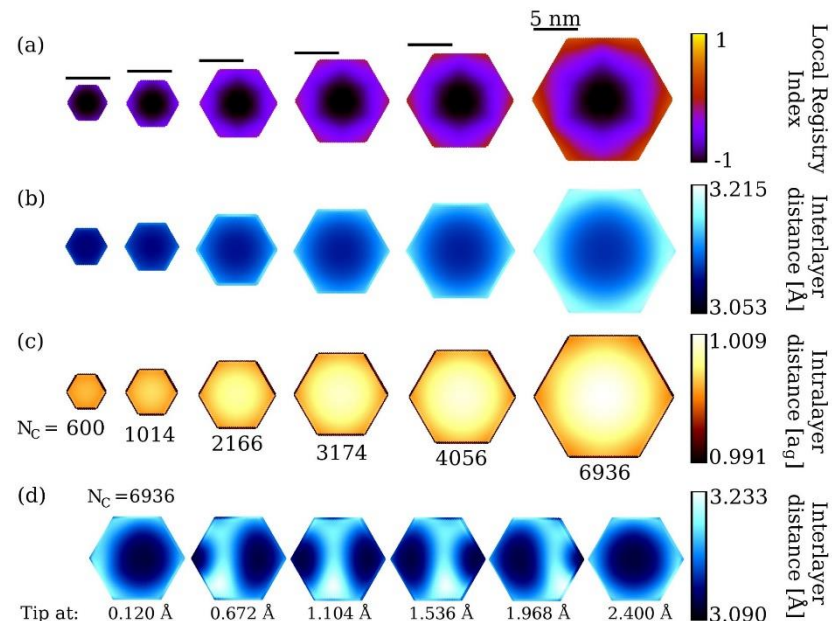
# Results: aligned interface $\theta=0$



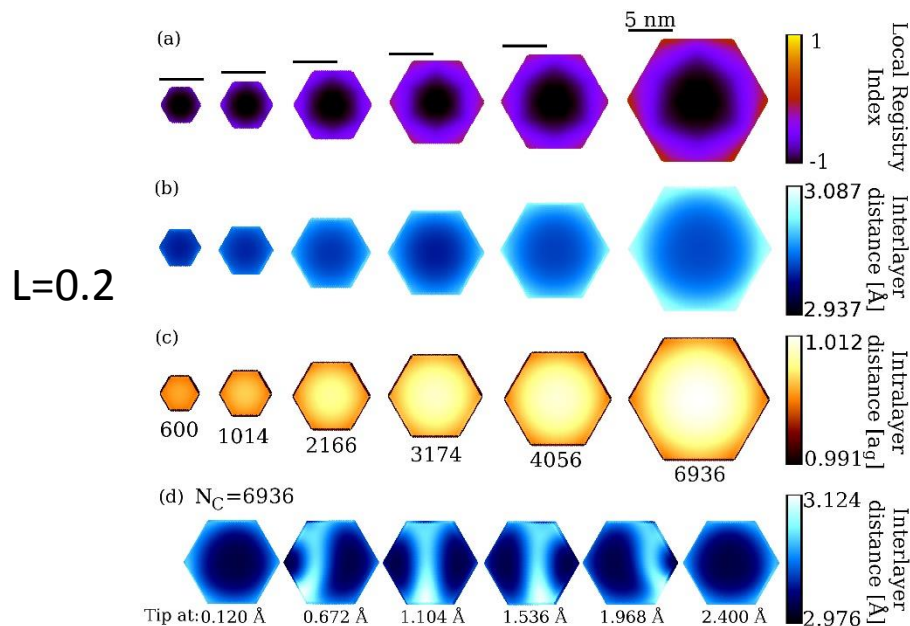
# Results: aligned interface $\theta=0$



L=0.05

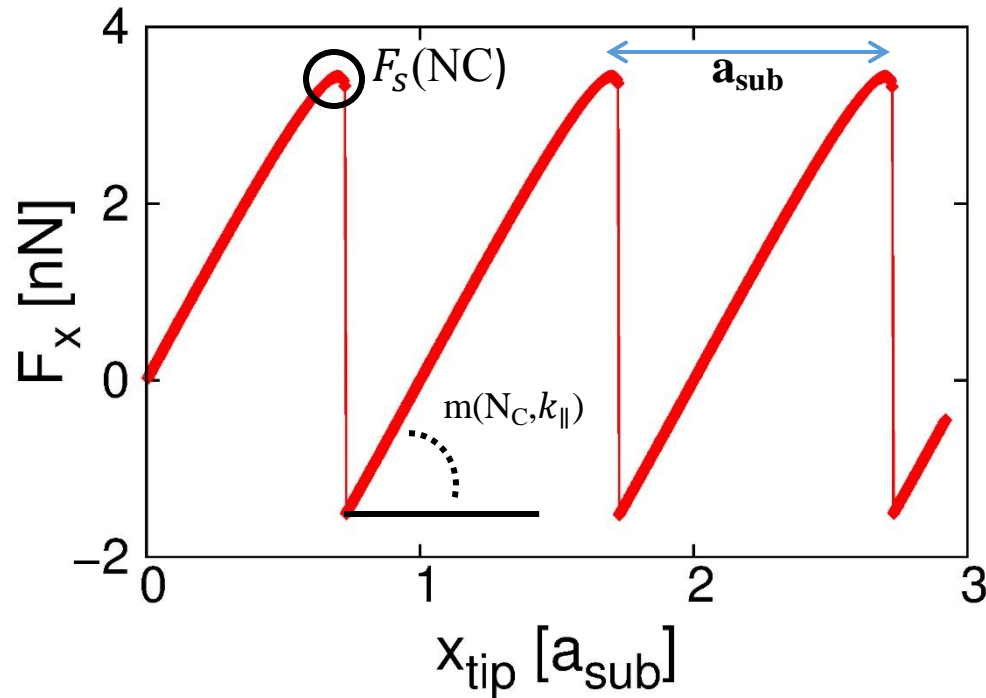


L=0.1



L=0.2

# Results: aligned interface $\theta=0$



$$F_k = F_s(N_C) - a_{\text{sub}} m(N_C, k_{\parallel}) \quad [1]$$

$$m(N_C, k_{\parallel}) \propto N_C, k_{\parallel}$$

Using estimates of ' $m$ ' eq.[1] reproduces the position of the maximum of  $F_k$ .

