

# Prompt Atmospheric Neutrino Fluxes

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# Atmospheric neutrino fluxes

*CR + Air* interactions:

- $AA'$  interaction approximated as  $A NA'$  interactions (superposition);
- $NA'$  approximated as  $A' NN$  interactions: up to which extent is this valid ?

\* conventional neutrino flux:



\* prompt neutrino flux:



$$c\tau_{0,\pi^\pm} = 780 \text{ cm}, c\tau_{0,K^\pm} = 371 \text{ cm}, c\tau_{0,D^\pm} = 0.031 \text{ cm}$$

Critical energy  $\epsilon_h = m_h c^2 h_0 / (c\tau_{0,h} \cos(\theta))$ , above which hadron decay probability is suppressed with respect to its interaction probability:

$\epsilon_\pi^\pm < \epsilon_K^\pm \ll \epsilon_D$   $\Rightarrow$  conventional flux is suppressed with respect to prompt one, for energies high enough.

## Conventional → prompt transition

Prompt fluxes expected to dominate above  $E_{lab,\nu} > 10^5 - 10^6 \text{ GeV}$ , depending of the flavour and zenith angle.

Investigating the transition requires accurate computation of both fluxes:

- predictions for conventional fluxes at high energies are more uncertain than at lower ones.
- same applies to prompt fluxes.
- characterizing the transition point is important for an explicit detection of prompt fluxes.
- Possible computation of both fluxes in a consistent framework.  
But the physics of the interactions at the core of the two fluxes differs.

# Prompt neutrino flux hadroproduction in the atmosphere: theoretical predictions in literature

\* Long non-exhaustive [list of papers](#), including, among the others:

- Lipari, Astropart. Phys. 1 (1993) 195
- Battistoni, Bloise, Forti et al., Astropart. Phys. 4 (1996) 351
- Gondolo, Ingelman, Thunman, Astropart. Phys. 5 (1996) 309
- Bugaev, Misaki, Naumov et al., Phys. Rev. D 58 (1998) 054001
- Pasquali, Reno, Sarcevic, Phys. Rev. D 59 (1999) 034020
- Enberg, Reno, Sarcevic, Phys. Rev. D 78 (2008) 043005

\* Updates and [recently renewed interest](#):

- Bhattacharya, Enberg, Reno, et al., JHEP 1506 (2015) 110,  
JHEP 1611 (2016) 167
- Fedynitch, Riehn, Engel, Gaisser et al., presented at many conferences
- Garzelli, Moch, Sigl, JHEP 1510 (2015) 115
- Gauld, Rojo, Rottoli, Sarkar, Talbert, JHEP 1602 (2016) 130
- Halzen, Wille, arXiv:1601.03044, PRD 94 (2016) 014014
- Laha, Brodsky, PRD 96 (2017) 123002
- PROSA Collaboration, JHEP 1712 (2017) 021 → [updates in this talk](#)
- Benzke, Garzelli, Kniehl, Kramer, Moch, Sigl, JHEP 1712 (2017) 021
- .....

[motivated by new results from VLV \$\nu\$ T's](#)  
[and updated theory and new results from LHC](#)

# How to get atmospheric fluxes ? From cascade equations to Z-moments [review in Gaisser, 1990; Lipari, 1993 ]

Solve a system of **coupled differential equations** regulating particle evolution in the atmosphere (interaction/decay/(re)generation):

$$\frac{d\phi_j(E_j, X)}{dX} = -\frac{\phi_j(E_j, X)}{\lambda_{j,int}(E_j)} - \frac{\phi_j(E_j, X)}{\lambda_{j,dec}(E_j)} + \sum_{k \neq j} S_{prod}^{k \rightarrow j}(E_j, X) + \sum_{k \neq j} S_{decay}^{k \rightarrow j}(E_j, X) + S_{reg}^{j \rightarrow j}(E_j, X)$$

Under assumption that  $X$  dependence of fluxes factorizes from  $E$  dependence, analytical approximated solutions in terms of  $Z$ -moments:

– Particle Production:

$$S_{prod}^{k \rightarrow j}(E_j, X) = \int_{E_j}^{\infty} dE_k \frac{\phi_k(E_k, X)}{\lambda_k(E_k)} \frac{1}{\sigma_k} \frac{d\sigma_{k \rightarrow j}(E_k, E_j)}{dE_j} \sim \frac{\phi_k(E_j, X)}{\lambda_k(E_j)} Z_{kj}(E_j)$$

– Particle Decay:

$$S_{decay}^{j \rightarrow l}(E_l, X) = \int_{E_l}^{\infty} dE_j \frac{\phi_j(E_j, X)}{\lambda_j(E_j)} \frac{1}{\Gamma_j} \frac{d\Gamma_{j \rightarrow l}(E_j, E_l)}{dE_l} \sim \frac{\phi_j(E_l, X)}{\lambda_j(E_l)} Z_{jl}(E_l)$$

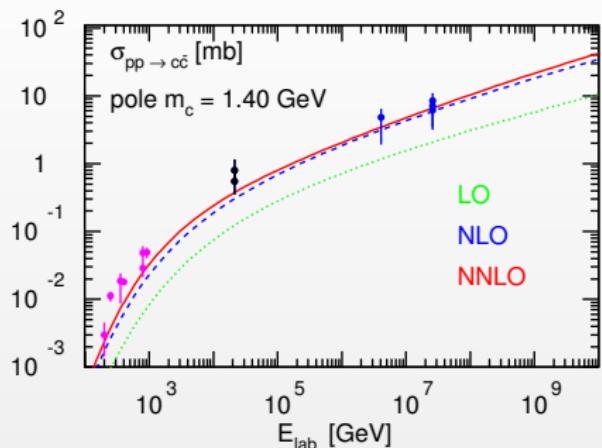
Solutions available for  $E_j \gg E_{crit,j}$  and for  $E_j \ll E_{crit,j}$ , respectively, are interpolated geometrically.

## $Z$ -moments for prompt fluxes: $Z_{ph}$ definition

$$Z_{ph}(E_h) = \int_{E_h}^{+\infty} dE'_p \frac{\phi_p(E'_p, 0)}{\phi_p(E_h, 0)} \frac{\lambda_{p,int}(E_h)}{\lambda_{p,int}(E'_p)} \frac{1}{\sigma_{p-Air}^{tot,inel}(E'_p)} \frac{d\sigma_{p-Air \rightarrow c+X \rightarrow h+X'}(E'_p, E_h)}{dE_h}$$

- \*  $Z_{ph}$  (as well as the other  $Z$ -moments) are energy dependent.
- \*  $Z_{ph}$  at a fixed  $E_h$ , depends on charm production cross-section  $\sigma(pA \rightarrow c + X)$  over a range of proton energies  $E_h < E'_p < +\infty$ .
- \* Crucial inputs: all.  
Differences among predictions of different authors can come from:
  - differences in the calculation of  $\sigma_{p-Air}^{tot,inel}$ ,
  - nuclear treatment of  $pA$  interactions: relation between  $pA$  and  $pp$ ,
  - theory and input parameters in  $\sigma(pp \rightarrow c + X)$ .

# $\sigma(pp \rightarrow c\bar{c}(+X))$ at LO, NLO, NNLO QCD



$$\begin{aligned} (E_{lab} &= 10^6 \text{ GeV} \sim E_{cm} = 1.37 \text{ TeV}) \\ (E_{lab} &= 10^8 \text{ GeV} \sim E_{cm} = 13.7 \text{ TeV}) \\ (E_{lab} &= 10^{10} \text{ GeV} \sim E_{cm} = 137 \text{ TeV}) \end{aligned}$$

data from fixed target exp (E769, LEBC-EHS, LEBC-MPS, HERA-B)  
+ colliders (STAR, PHENIX, ALICE, ATLAS, LHCb).

- \* Assumption: collinear factorization valid on the whole energy range.
- \* Sizable QCD uncertainty bands not included in the figure.

## Different computations of $\sigma(pp \rightarrow c + X)$ used in prompt neutrino flux estimates

- \* Dipole model(s): ERS 2008, updated in BEJRSS 2016
- \* Computations with a pQCD core (collinear or  $k_T$  factorization):  
the post-LHC ones are BERSS 2015, GMS 2016, GRSST 2015,  
BERSS 2016, PROSA 2016, GM-VFNS 2017

Why is pQCD applicable on the whole kinematics space ?

The crucial reason is that the charm quark is massive.

No divergence of  $d\sigma/dp_T$  for  $p_T \rightarrow 0$ :

⇒ No strict need of a description in terms of soft physics for  $p_T \rightarrow 0$ .

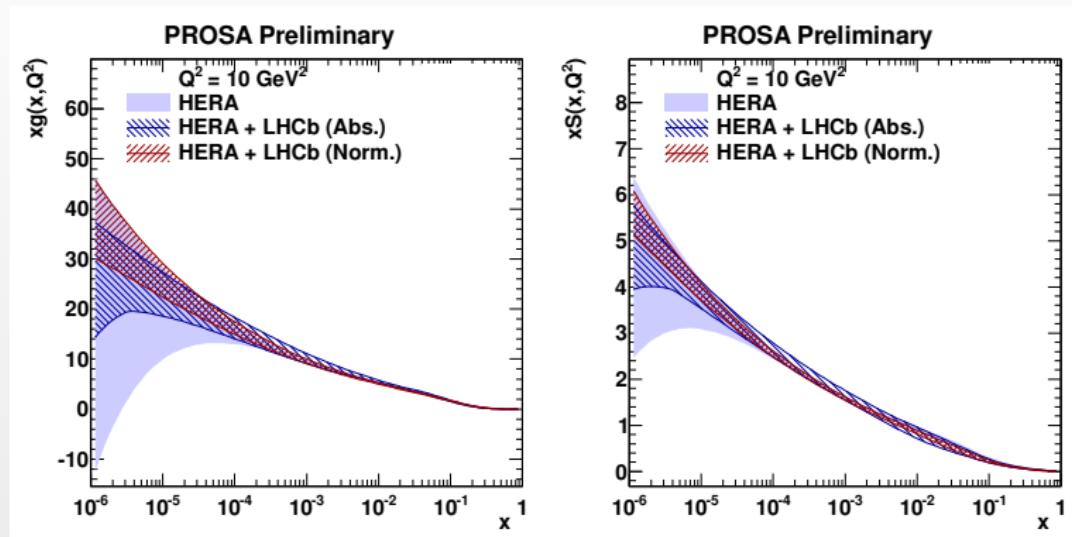
⇒ Situation radically different from  $\pi$  and  $K$  hadroproduction !!!

# Where do non-perturbative physics enter in the so-called pQCD computations ?

- \* it enters in Parton Distribution Functions  $\text{PDF}_{i/A}(x_i, Q^2)$  of partons in protons and nuclei
- \* it enters in Fragmentation Functions  $F_{c,q,g \rightarrow H}(z, Q^2)$  / hadronization
- \* it can enter in soft multiple parton interactions  
(in those calculations where these interactions are accounted for).

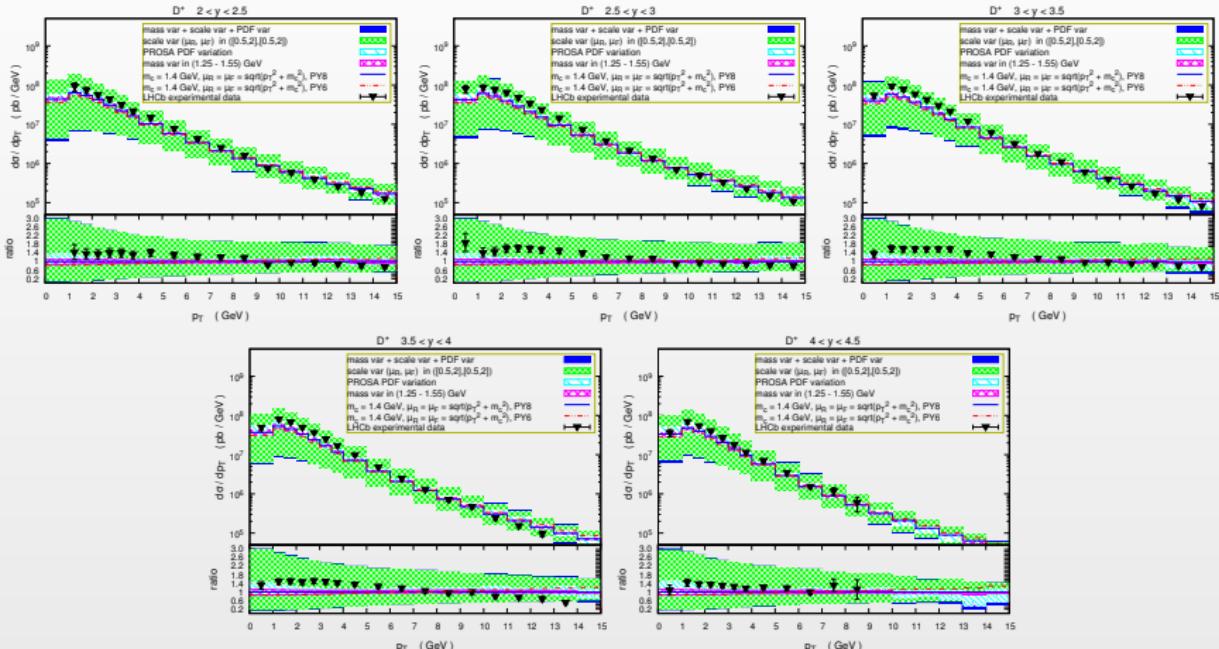
# PROSA PDF fit [arXiv:1503.04581]

Basic idea: use the data on  $D$ -meson and  $B$ -meson hadroproduction at LHCb to constrain PDFs (especially gluon PDFs) at low  $x = p_z, \text{parton} / p_z, \text{proton}$  values.



- \* The gluon and the sea quark distributions are correlated:  
a reduction on the uncertainty of the former propagates to the latter.
- \* good at “low”  $x$ ’s, but how low shall we go for high-energy astroparticle physics ?
- \* LHCb data constrains down to  $x \sim 10^{-6}$ . This is not enough for prompt fluxes at extremely high energies.....

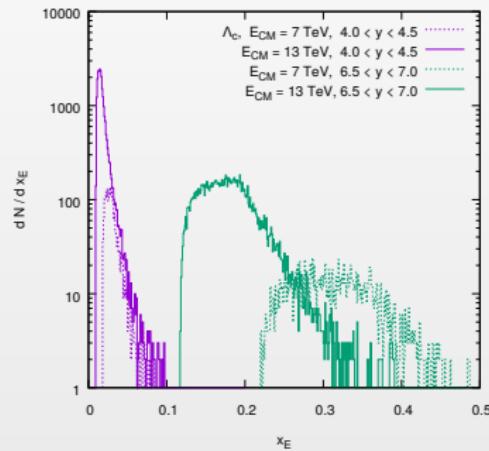
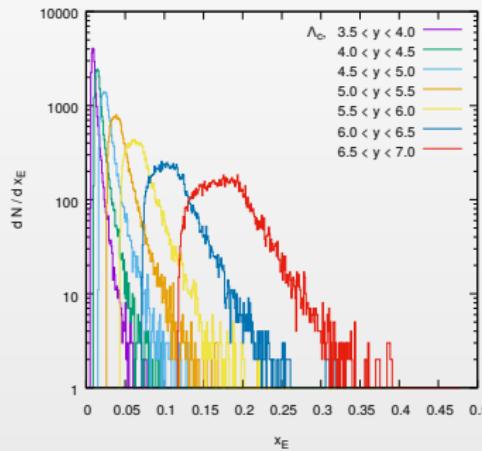
# Performances of PROSA PDF fit with respect to LHCb data non included in the fit



- \*  $d^2\sigma/(dp_T dy)$  measured for  $pp \rightarrow D^\pm + X$  at  $\sqrt{s} = 13$  TeV.
- \* Experimental data always within the theory uncertainty bands.

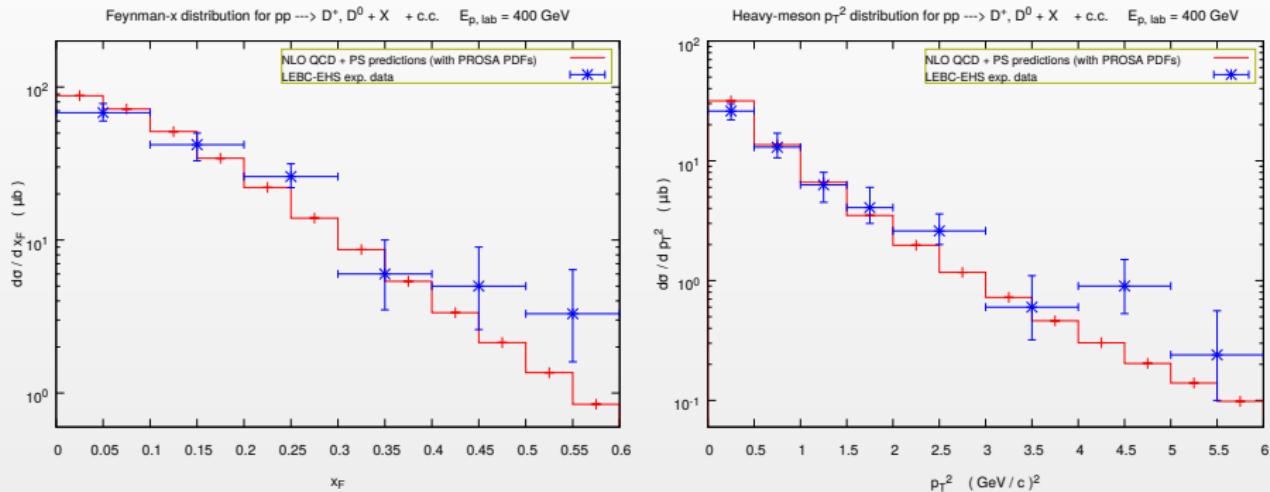
# LHCb experimental data coverage for charm hadroproduction in astrophysical applications:

$x_E = E_{h,LAB} / E_{p,LAB}$  spectra (of interest for prompt fluxes) at different rapidities  $y$  (of interest at colliders)



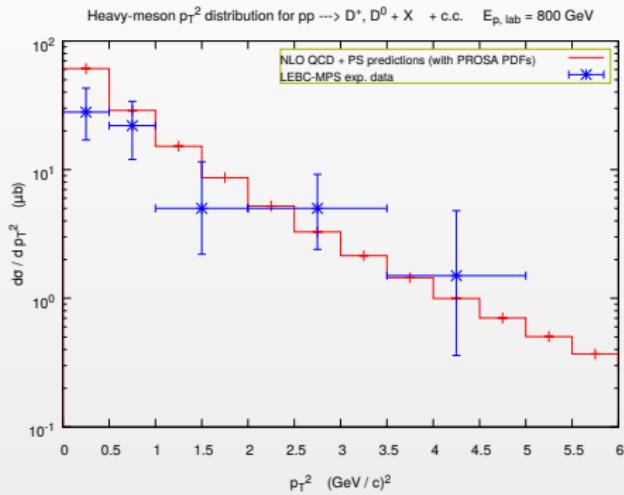
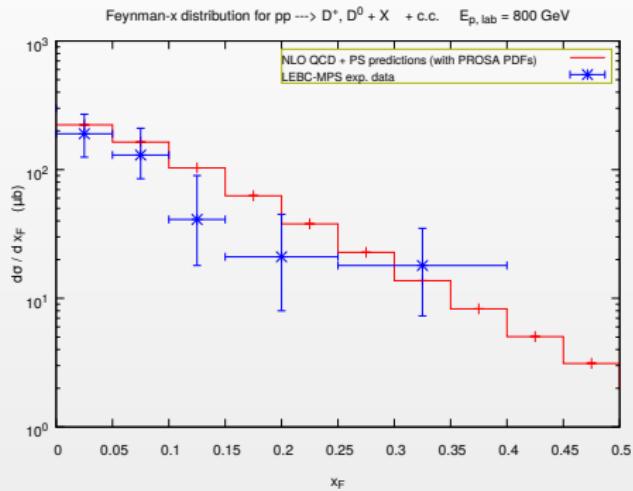
- \* case of  $\Lambda_c$  considered here,  
qualitatively similar behaviour for charmed mesons.
- \* high  $x_E$  corresponds to high  $y$  (forward particles)
- \* maximum rapidities  $y$  probed at LHCb corresponds to  $x_E < 0.15$ .

# Performances of the PROSA QCD computation of $D$ -meson production w.r.t. LEBC-EHS exp. data



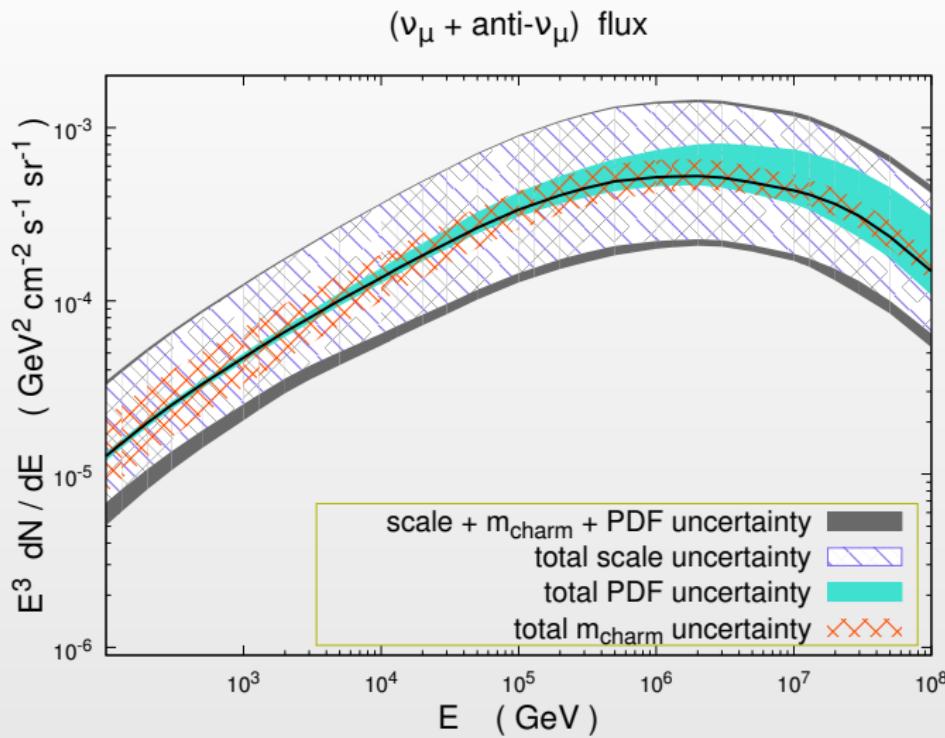
- \* Fixed target experiment with  $E_{p, \text{lab}} = 400 \text{ GeV}$ .
- \* Measure relatively large  $x_F = p_{z,D}/p_{z,D}^{\max}$  (up to  $x_F \sim 0.6$ ) and  $p_T^2$ .
- \* Sizable QCD uncertainty band not included in the plot.

# Performances of the PROSA QCD computation of $D$ -meson production w.r.t. LEBC-MPS exp. data



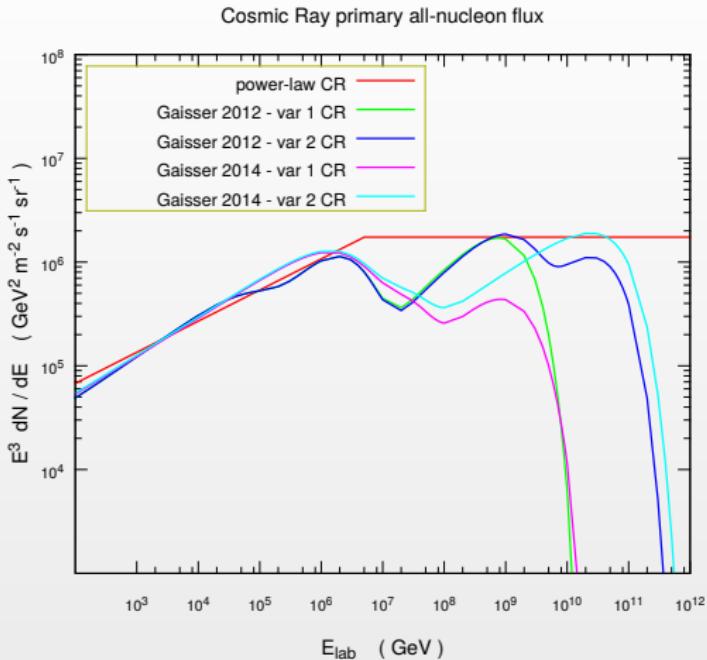
- \* Fixed target experiment with  $E_{lab} = 800$  GeV.
- \* Measure relatively large  $x_F$  (up to  $x_F \sim 0.4$ ).
- \* Sizable QCD uncertainty band not included in the plot.

# PROSA prompt ( $\nu_\mu + \bar{\nu}_\mu$ ) flux: QCD scale, mass and PDF uncertainties



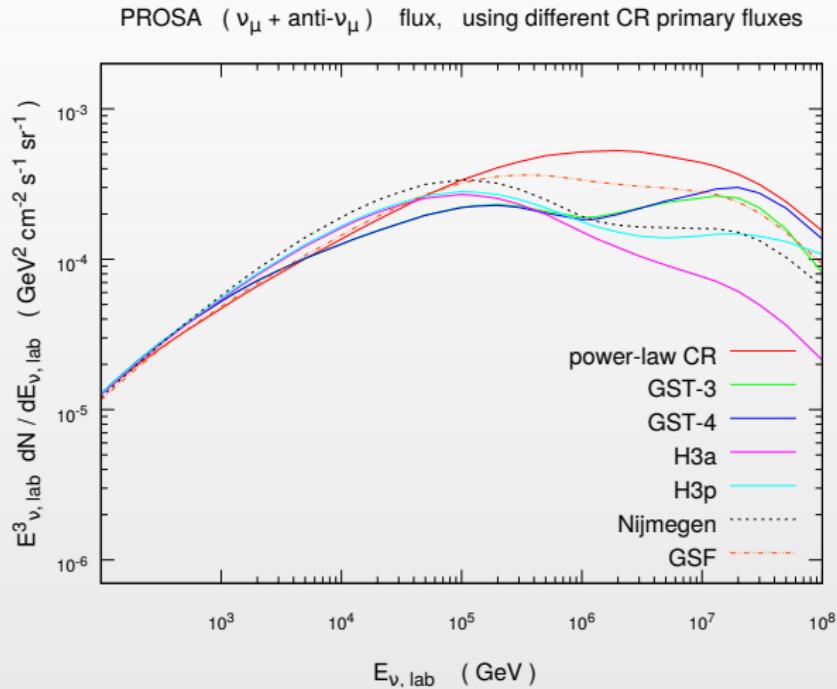
from [arXiv:1611.03815]

# The all-nucleon CR spectra: considered hypotheses



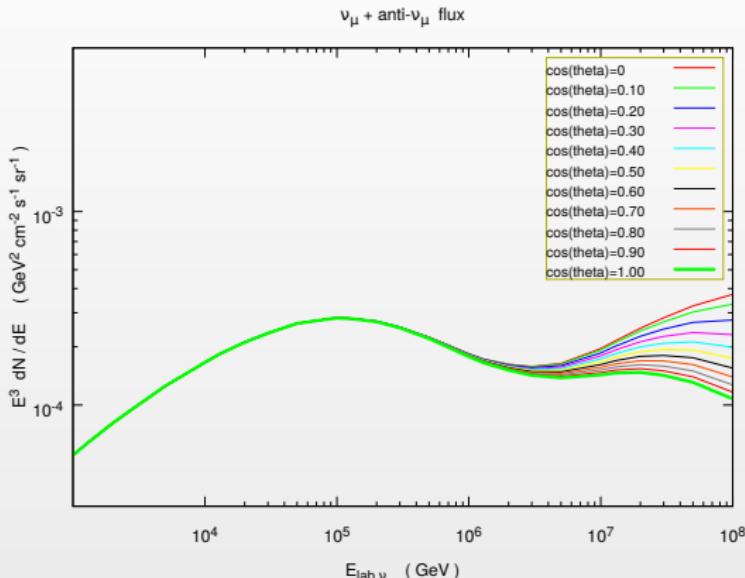
- \* All-nucleon spectra obtained from all-particles ones under different assumptions as for the CR **composition** at the highest energies.
- \* Models with 3 (2 gal + 1 extra-gal) or 4 (2 gal + 2 extra-gal) populations are available.

# PROSA prompt ( $\nu_\mu + \bar{\nu}_\mu$ ) fluxes with different CR primary fluxes



- \* GSF is the newest CR spectrum available by the Gaisser group (ICRC 2017), leading to results somehow similar to the broken power-law case.

# Zenith angle dependence of the PROSA prompt $(\nu_\mu + \bar{\nu}_\mu)$ flux

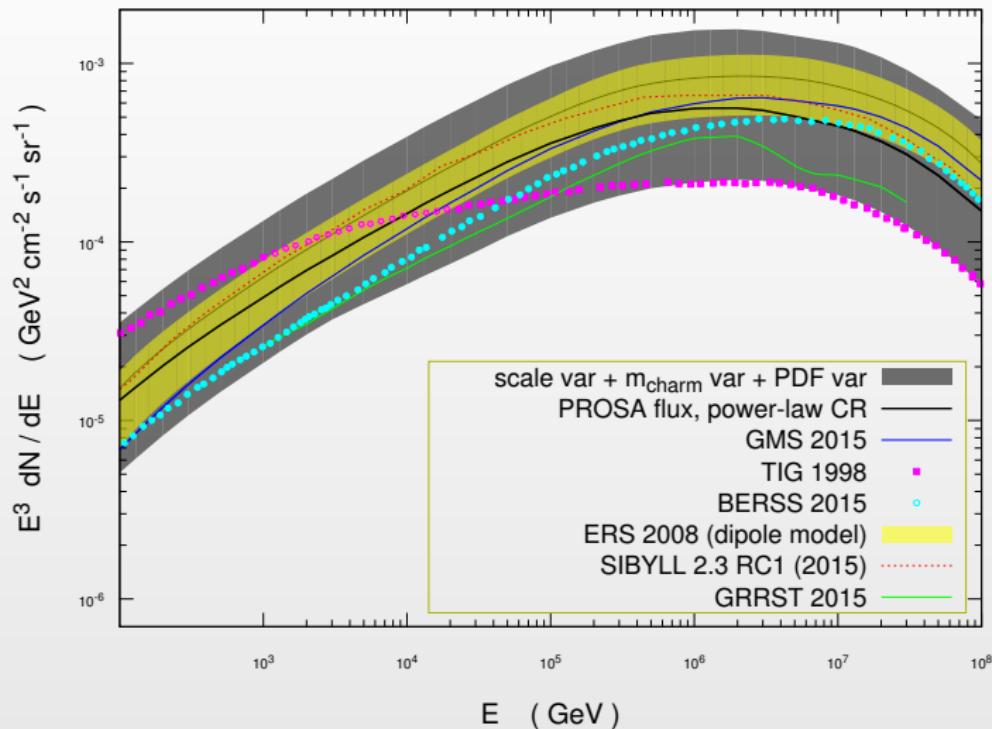


Flux computed with  
H3p primary CR  
spectrum

- \* prompt fluxes are not isotropic  
(although this approximation is good at low energies).
- \* At high energies, they increase towards the horizon.

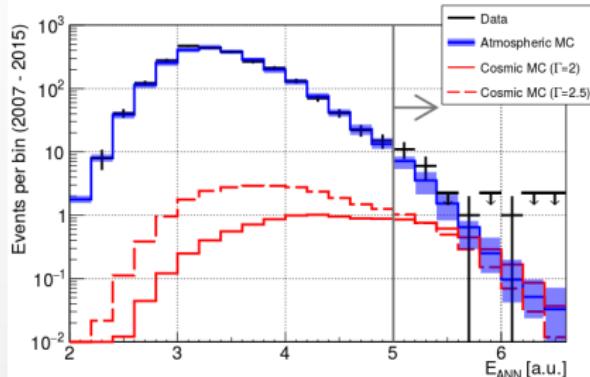
# Comparison of predictions by different groups

$\nu_\mu + \text{anti-}\nu_\mu$  flux

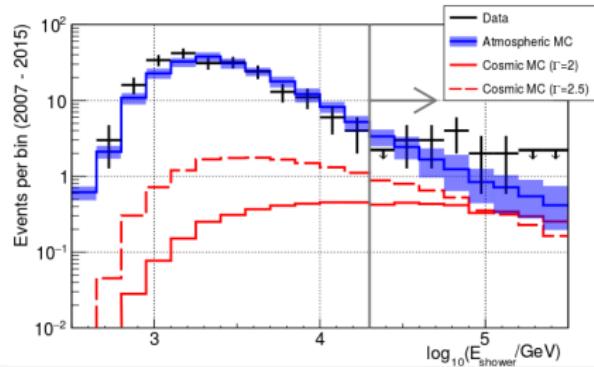


Different predictions compatible within the uncertainty band: accidentally ?

# Recent results from ANTARES on tracks and showers [arXiv:1711.07212]



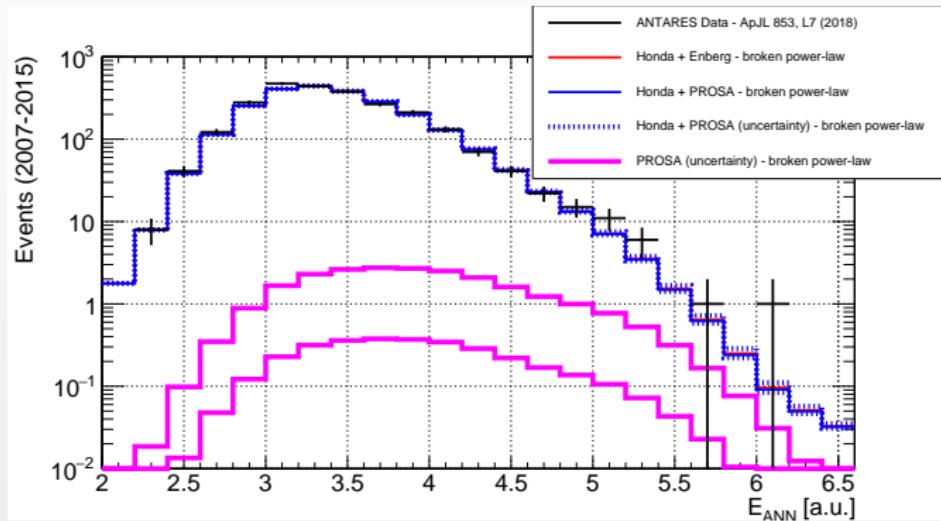
tracks



showers

- \* theory predictions for atmospheric flux = Honda + ERS
- \* interesting to extend to more recent predictions
- \* interesting to compare ANTARES data with IceCube data:  
warning  $E_{\text{ANN}}$  is an energy estimator, it is linearly related to the  
✓ reconstructed energy, but it does not coincide with it!

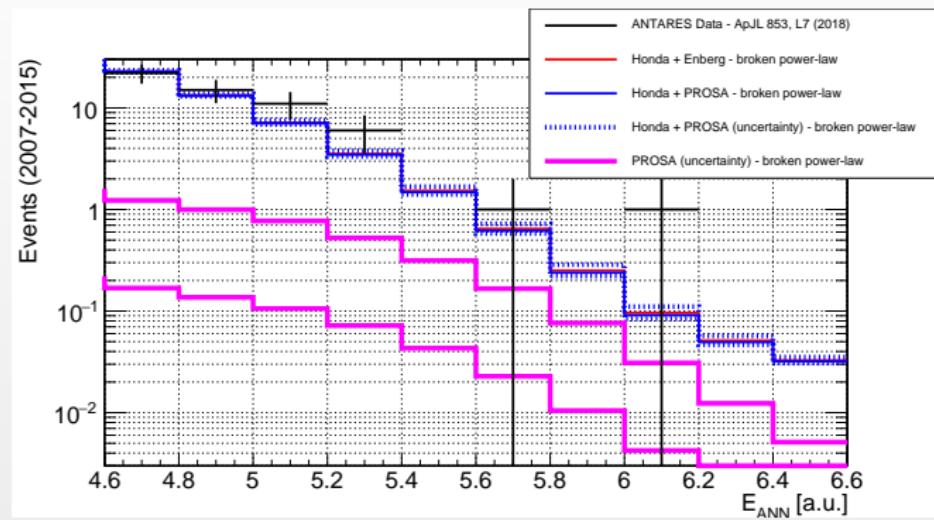
# Effects of PROSA prompt flux in the analysis of ANTARES High-Energy Track Events



*courtesy of L. Fusco, ANTARES collaboration*

- \* Broken power-law CR primary spectrum assumption.
- \* Only  $\sim 1 \sigma$  excess above the atmospheric only hypothesis:  
no striking need of astrophysical neutrinos to explain these data

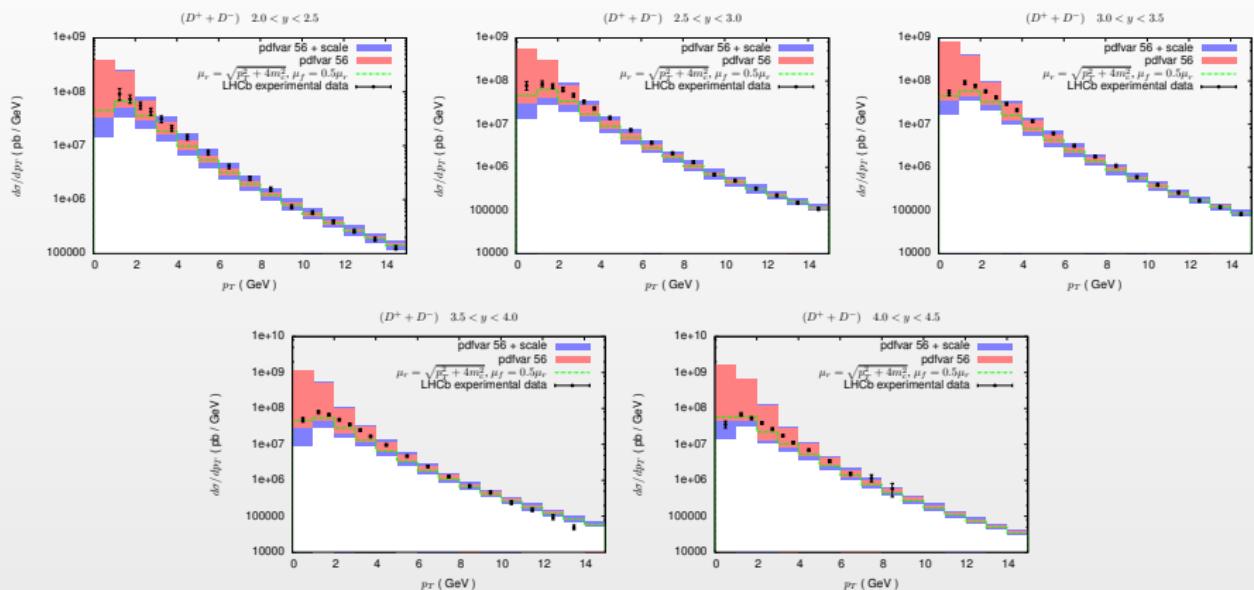
# Effects of PROSA prompt flux in the analysis of ANTARES High-Energy Track Events



*courtesy of L. Fusco, ANTARES collaboration*

- \* Effects of different prompt predictions hardly distinguishable.
- \* Accurate estimate of the uncertainties on conventional flux needed before reaching any firm conclusion on astrophysical neutrinos.
- \* Waiting for more statistics (KM3NeT).

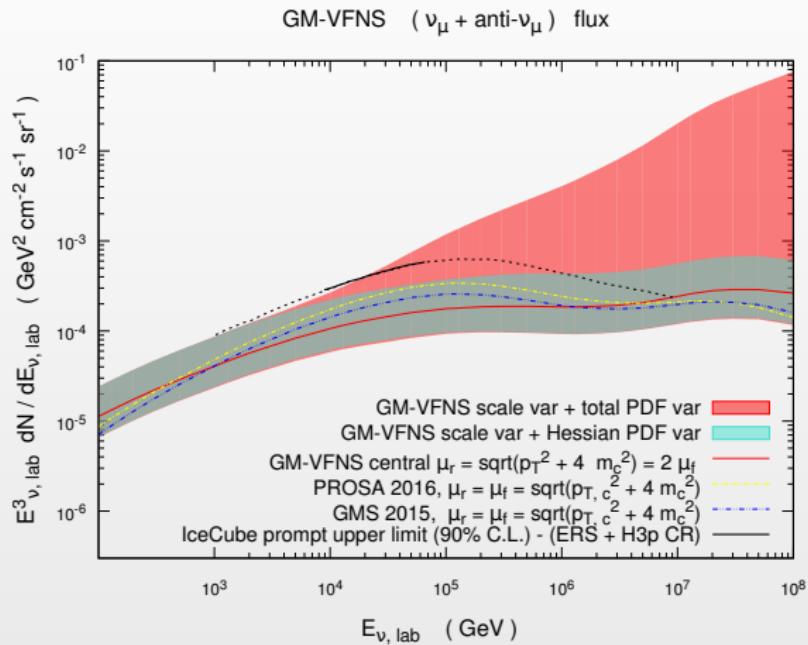
# How do other PDF fits (CT14nlo), not including LHCb data, behave ? $pp \rightarrow D^\pm + X$ at LHCb at 13 TeV



- \* GM-VFNS predictions using CT14nlo PDFs, constrained only down to  $x \sim 10^{-4}$
- \* Large PDF uncertainties, increasing at low  $p_T$  / large  $y$ .

# Prompt neutrino fluxes:

theoretical predictions from [arXiv:1705.10386] vs. IceCube upper limits

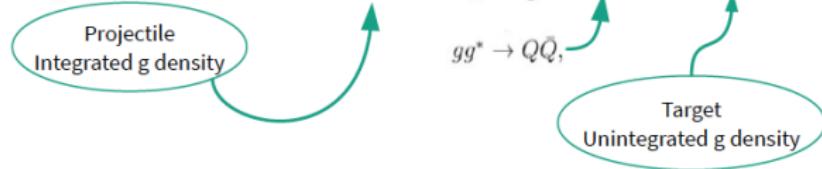


The extrapolation to high energy of IceCube results suggest that the CT14nlo gluon PDF uncertainty band at low  $x$ 's (see PDF error sets 53-56) is too large!

# Prompt neutrinos using QCD $k_T$ factorization

## $k_T$ Factorization approach

$$\frac{d\sigma}{dx_F}(s, m_Q^2) = \int \frac{dx_1}{x_1} \frac{dx_2}{x_2} dz \delta(zx_1 - x_F) x_1 g(x_1, M_F) \int \frac{dk_T^2}{k_T^2} \hat{\sigma}^{\text{off}}(z, \hat{s}, k_T) f(x_2, k_T^2).$$



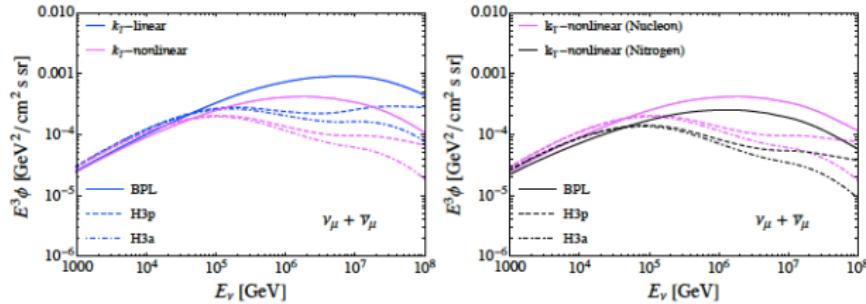
hybrid formalism:

low- $x$  parton from the target and large- $x$  parton from the projectile

*slide and calculation by Ina Sarcevic, M. H. Reno, et al.*

# KT factorization

Bhattacharya et al., JHEP 1611 (2016) 167

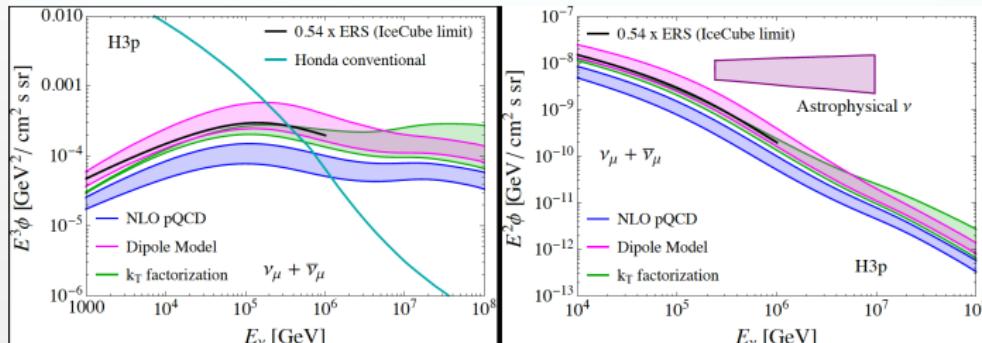


25

- \* saturation vs. no-saturation in the uPDF: saturation suppress fluxes
- \* cold nuclear matter effects likely suppress fluxes
- \* Large QCD and nuclear uncertainties (not included in these plots)

# Prompt Neutrino Flux

A. Bhattacharya, R. Enberg, Y.S. Jeong, M.H. Reno, I. Sarcevic and A. Stasto,  
JHEP 1611 (2016) 167



comparison between computations in different QCD frameworks:  
dipole model /  $k_T$  factorization / collinear factorization

*slide and calculation by I. Sarcevic, M. H. Reno, et al.*

# Conclusions

- \* Many theory computations of prompt atmospheric  $\nu$  fluxes.
- \* VLV $\nu$ T results published so far are not enough to rule out, confirm or prefer any of the most recent predictions  
(but they can rule out very extreme cases).
- \* **Open questions** which deserve further investigation in the future:
  - reduction of QCD uncertainties  
(in both collinear and  $k_T$ -factorization)
  - nuclear matter effects
  - transition region: conventional → prompt
  - explicit more dedicated searches of prompt fluxes at VLV $\nu$ Ts
  - intrinsic charm ?
  - BSM enhancement of charm production
  - Systematic inclusion of prompt flux contribution when looking for and fitting the “astrophysical” neutrino component.