



A self scale Z-pinch Scalability, Similarities and Differences in Plasma Focus Devices: Basic Research and Applications

Leopoldo Soto

Comisión Chilena de Energía Nuclear (CCHEN) Center for Research and Aplications in Plasma Physics and Pulsed Power, P4 Santiago, Chile

LEOPOLDO.SOTO@CCHEN.CL

Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy







- Part 1. Basic concepts. Z-pinch, pulsed power, plasma focus.
- Part 2. How to obtain information from a dense transient plasma? Plasma diagnostics

Basic Research and Applications

Part 3. How to design and to build a small plasma focus? Tricks and Recipes







- What is a pinch plasma: Z-pinch, θ-pinch, Screw pinch
- Why Z-pinches are interesting?
- Z-pinch in equilibrium
- Stability
- Pulsed power
- Plasma focus



Pinch plasmas





Thermal pressure vs Magnetic pressure

In quilibrium $\Box \to \nabla p = J \times \vec{B}$







Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



Why Z-pinches are interesting?



Physics- Possibility to study:

- Dense-hot plasmas
- High energy density and high mass density state of matter
- Fast plasma dynamics (instabilities, turbulence, magnetic field reconnection, filaments, anomalous transport phenomena)

Fusion:

- Basic studies
- The pinch is used as a very intense soft X-ray source which irradiates a D-T target.

Applications. Pinches produce:

- Ion and electron beams
- X-ray
- Neutrons (from fusion reactions in D₂)
- Plasma jets

X-ray and neutron nanoflashes (high resolution X-ray tomography, substance detection, non-destructive testing)



Momentum equation

$$\vec{\nabla}p = \vec{J} \times \vec{B} \Longrightarrow -\frac{dp}{dr} = J_z B_\theta \quad (1)$$

Ampère law

$$\vec{\nabla} \times \vec{B} = \mu_0 \vec{J} \Longrightarrow J_z = \frac{1}{\mu_0 r} \frac{d(rB_\theta)}{dr}$$
 (2)

(1) in (2)

$$\frac{dp}{dr} + \frac{B_{\theta}}{\mu_0 r} \frac{d(rB_{\theta})}{dr} = 0$$
 (3)

$$\frac{d}{dr}\left(p+\frac{B_{\theta}^2}{2\mu_0}\right)+\frac{B_{\theta}^2}{\mu_0 r}=0 \quad (4)$$



Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy





Considering a pinch of radius a, multiplying (4) by r^2 and integrating over the pinch cross section,

$$\int_{0}^{a} r^{2} \frac{dp}{dr} dr = -\frac{1}{\mu_{0}} \int_{0}^{a} (rB) d(rB)$$
 (5)

Integrating by parts the left hand side

$$\left[r^{2}p\right]_{0}^{a} - 2\int_{0}^{a} prdr = -\frac{1}{2\mu_{0}}\left[(rB)^{2}\right]_{a} \qquad (6)$$

p = 0 at r = a and $T(r) = T_i = T_e = T$, and for a cuasi neutral fully ionized gas, $n_i = n_e = n$, can be considered as an ideal gas,

$$p = (1+Z)n_i k_B T \tag{7}$$

$$(n_e = Zn_i; T_e = T_i = T)$$
 (8)

 n_i , n_e number of ions or electrons per unit volumen *Ti*, *Te* ions or electrons temperature





Obtaing the number of ions per unit lenght of the pinch

$$N_i = \int_0^a 2\pi r n_i(r) dr \qquad (9)$$

Integrating the Ampere law over the pinch

$$[(rB)^2]_a = \frac{(\mu_0 I)^2}{4\pi^2}$$
 (10)

Finally, (10), (9), (8) and (7) in (6)

 $\mu_0 I^2 = 8\pi (1+Z) N_i k_B T \qquad (10) \qquad \text{Bennett relation}$





$$\nabla p = J \times \vec{B} \longrightarrow \mu_0 I^2 = 8\pi (1+Z) N_i k_B T$$

$D_2 T = 1.56 \times 10^{11} I^2 / N (eV, A, m^{-1})$







MHD instabilities appears in nanoseconds









Stability parameters it is depends on I, a, N

Haines and Coppins, Phys. Rev. Lett. 66, 1462 (1991)

Larmor radius over pinch radius, $a_i/a \alpha N^{-1/2}$

Transient Alfvén time, $\iota_A = a/v_A \alpha a N^{1/2}I^{-1}$

Lundsquisdt number, S α I⁴aN⁻²

Ion cyclotron frecuency Ω_i by collision time for the ions ι_i . $\Omega_i\iota_i~~\alpha~~I^4~a~N^{-5/2}$



Universal Diagram for Z-pinch Stability





Haines and Coppins, Phys. Rev. Lett. 66, 1462 (1991)

Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



Figure 3. Various Z-pinch configurations. Reprinted from [52], copyright 1948, with kind permission from Springer Science + Business Media B.V..

will flow at first along the axis of the vessel. This is the gas-embedded Z-pinch [53]. This type of Z-pinch is the only one to be dominated by the m = 1 or kink instability, which we will discuss in section 3. A variant of this employing an additional hollow micro-discharge has been studied by Soto *et al* [54], figure 3.



□ I = 800kA

Currents of the order of ~ 1MA are required and must achieved in a short time < 100ns





Pulsed Power

Basic circuits for pulsed discharges

The simplest generator, a LC circuit



 I_{max} =Vo/Zo dI/dt~Vo/L Zo=(L/C)^{1/2}

T=2 π (LC)^{1/2} dI/dt~ I_{max}/(T/4)

Is it posible obtain MA in 100ns using this kind of generator?





Is it posible obtain MA in 100ns using a LC circuit as generator?



 $I_{max} = Vo/Zo$ $dI/dt \sim Vo/L$ $Zo = (L/C)^{1/2}$

T=2 π (LC)^{1/2} dI/dt~ I_{max}/(T/4)

Low inductance is required. 20nH is a real value but is not easy to obtain

 $L \sim 20$ nH and T/4~100ns \rightarrow C~200nF

Thus, Zo ~ 0.3 Ω , I_{max} ~ 1MA requires Vo ~ 300kV

Comisión Chilena de Energía Nuclea Ministerio de Energía



Marx generator

Capacitor bank charged in parallel and discharges in series

Vout=nVo, n=number of capacitors





. Schematic of IMP generator

Marx generator

Capacitor bank charged in parallel and discharges in series

Vout=nVo, n=number of capacitors

Pulse forming line, PFL

Pulse duration is 2 transist time





	GEPOPU (PUC, Chile)	Llampüdkeñ (PUC, Chile)	SPEED 2 (CCHEN, Chile)	MAGPIE (Imperial College, UK)	Z Acelerator (Sandia NL, USA)
Stored Energy	2kJ	28kJ	187kJ	86kJ	11.4MJ
Power	0.02 TW		0.5 TW	1 TW	50 TW
Max. load voltaje	300kV	450kV	300kV	2MV	2.5MV
Max. current	200kA	400kA	4MA	1.5MA	20MA
Rise time	100ns	260ns	400ns	150ns	100ns
dl/dt	1x10 ¹² A/s	2x10 ¹² A/s	1x10 ¹³ A/s	1x10 ¹³ A/s	2x10 ¹⁴ A/s
Impedance	1.5Ω	variable	0.070Ω	1.24Ω (5/4 Ω)	0.120Ω (4.32/36 Ω)
PFL's	Yes (1)	Yes(2)	No	Yes (4)	Yes (36)



Z-pinch experiments in Sandia





Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy







Is it posible to do relevant experimental plasma physics and fusion research in a small country?





OUR APPROACH

PLASMA ENERGY DENSITY

~10¹² J/m³

1J in a sub millimeter volume

0.1J in a sphere of $60\mu m$ of diameter

PLASMA PHYSICS IN SMALL DEVICES

Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



The plasma focus discharge



The Mather Plasma Focus (PF) is a transient electrical discharge produced in arranged coaxial electrodes, separated by an insulator, and driven typically by a capacitive pulsed power generator, which is controlled by a spark-gap switch.

(I) The discharge starts over the insulator.

(II) The Lorentz force pushes the plasma sheet to move axially.

(III) and then to move radially (sometimes plasma filaments appears).

(IV) The sheet collapses to form a dense column of plasma (pinch). During these stage, X-rays and neutron pulses (when operating with deuterium), are generated.

(V) After the pinch is disrupted and an axial shock and plasma jets are produced



Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



The plasma focus discharge





Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



Some PF devices in operation in the world during the period 1990-2000



Device, location	Energy E (kJ)	Anode radius a (cm)	Peak current (kA)	Operation mode
PF-1000, Poland	1064	12.2	2300	Single shot
PF-360, Poland	130	6	1200	Single shot
SPEED2, Germany	70	5.4	2400	Single shot
7kJ PF, Japan	7	1.75	390	Single shot
GN1, Argentina	4.7	1.9	-	Single shot
Fuego Nuevo, Mexico	4.6	2.5	350	Single shot
UNU/ICTP-PF, AAAPT-Asia and Africa	2.9	0.95	172	Single shot
Fraunhofer Insitute ILT-Aachen, Germany	2-5			Repetitive, 2Hz
Research Lab. Alameda, USA	2			Repetitive, 2Hz
NX1, Singapore	3	3	250	Repetitive, 3Hz
NX2, Singapore	1.9	4	170	Repetitive, 16Hz





Our goal:

Miniature Plasma Focus Devices < 1kJ To find scaling laws



Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



Under kJ PF devices at CCHEN













PF-400J

PF-50J

PF-2J



Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy













- Plasma Focus characterization
- Before the pinch
- During the pinch
- After pinch



before the pinch

pinch

after the pinch

J. Moreno, P. Silva, and L. Soto, Plasma Sources Science and Technology 12, 39 (2003).





PF-400J Schlieren images





Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



- a) the plasma sheath is moving axially
- b) the pinch moment
- c) after the pinch disruptions.

 $r_p \sim 0.1 r_a$

 $z_p \sim 0.8 r_a$

This is the first time in which optical refractive diagnostics from a PF of only 2 joules is reported.





 $r_p \sim 0.1 r_a$

 $z_{\rm p} \sim 0.8 r_{\rm a}$

PF-400J

Interferograms



C. Pavez and L. Soto, Physica Scripta T131, 014030 (2008)

Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy



APPLIED PHYSICS LETTERS

VOLUME 83, NUMBER 16

Center for research and applications in plasma physics and pulsed ower

20 OCTOBER 2003

Neutron emission from a fast plasma focus of 400 Joules

Patricio Silva, José Moreno, Leopoldo Soto,^{a)} Lipo Birstein, Roberto E. Mayer,^{b)} and Walter Kies^{c)}

Comisión Chilena de Energía Nuclear, Casilla 188 D, Santiago, Chile

(Received 29 April 2003; accepted 2 September 2003)

IOP PUBLISHING J. Phys. D: Appl. Phys. 41 (2008) 205215 (7pp) JOURNAL OF PHYSICS D: APPLIED PHYSICS doi:10.1088/0022-3727/41/20/205215

Demonstration of neutron production in a table-top pinch plasma focus device operating at only tens of joules

Leopoldo Soto^{1,2,7} Patricio Silva¹, José Moreno^{1,2}, Marcelo Zambra¹, Walter Kies², Roberto E Mayer³, Alejandro Clausse⁴, Luis Altamirano^{2,5}, Cristian Pavez^{1,2} and Luis Huerta^{2,6}

 ¹ Comisión Chilena de Energía Nuclear, Casilla 188-D, Santiago, Chile
² Center for Research and Applications in Plasma Physics and Pulsed Power, P⁴, Chile
³ Centro Atómico Barlioche and Instituto Balseiro, 8400 Barlioche, Argentina
⁴ CNEA, CONICET and Universidad Nacional del Centro, 7000 Tandil, Argentina
⁵ Dicontek, Pasaje Galicia 1365, La Florida, Santiago, Chile
⁶ Universidad de Talca, Facultad de Ingeniería, Campus Curicó, Kilómetro 1 Camino a Los Niches, Curicó, Chile

E-mail: lsoto@cchen.cl

PHYSICS OF PLASMAS 24, 082703 (2017)



Evidence of nuclear fusion neutrons in an extremely small plasma focus device operating at 0.1 Joules

Leopoldo Soto, ^{1,2,3,a}) Cristián Pavéz, ^{1,2,3} José Moreno, ^{1,2,3} Luis Altamirano, ^{2,4} Luis Huerta, ^{2,5} Mario Barbaglia, ⁶ Alejandro Clausse, ⁶ and Roberto E. Mayer⁷ ¹Comisión Chilena de Energía Nuclear, Av. Nueva Bilbao 12,501, 7600713 Santiago, Chile ²P⁴-Center for Research and Applications in Plasma Physics and Pulsed Power Technology, 7600713 Santiago, Chile ³Departamento de Ciencias Físicas, Universidad Andres Bello, República 220, 8370134 Santiago, Chile ⁴Dicontek, Santiago, Chile ⁵Facultad de Ingeniería, Universidad de Talca, Camino Los Niches Km 1, 3340000 Curicó, Chile ⁶CREA-CONICET and Universidad Nacional del Centro, 7000 Tandil, Argentina ⁷Centro Atómico Bariloche and Instituto Balseiro, 8400 Bariloche, Argentina

Centro Atomico Bartiocne ana Instituto Baisetro, 8400 Bartiocne, Argentin

(Received 12 June 2017; accepted 4 July 2017; published online 24 July 2017)





Scaling parameters allow to reproduce similar phenomenology in devices operated in a wide range of bank energy (0.1 J – 1 MJ)

							Energy per
					Energy	Drive	mass
	_	Anode	Peak	_	density	parameter	parameter
Device -	Energy	radius	current	Pressure	parameter	$I/p^{1/2}a$	$E/a^{3}p$
location	<i>E</i> (kJ)	a (cm)	(kA)	(mbar)	$28 E/a^3 (J m^{-3})$	$(kA mbar^{-1/2} cm^{-1})$	$(\times 10^7 \mathrm{J}\mathrm{m}^{-3}\mathrm{mbar}^{-1})$
PF-1000-Poland	1064	12.2	2300	6.6	1.6×10^{10}	73.4	8.5
PF-360 -Poland	130	6	1200	1.6	1.7×10^{10}	61.4	38
SPEED2 -Chile	70	5.4	2400	2.7	1.2×10^{10}	_	15.9
7 kJ PF-Japan	7	1.75	390	6	3.7×10^{10}	91	22
GN1-Argentina	4.7	1.9	_	—	1.9×10^{10}	_	—
Fuego Nuevo II -Mexico	4.6	2.5	350	3.7	0.8×10^{10}	73	7.7
UNU/ICTP-PF - Asia and Africa	2.9	0.95	172	8.5	9.5×10^{10}	81	4.1
PACO ^a - Argentina	2	2.5	250	1.5	3.6×10^{9}	95	8.5
PF-400J-Chile	0.4	0.6	127	9	5.2×10^{10}	70	2
FMPF-1 Singapore	0.23	0.35	80	5.5	1.5×10^{11}	97	5.35
200J ^a Batt-PF India	0.2	0.5	83	10	4.5×10^{10}	52ª	1.6 ^a
125J PF Argentina	0.125	0.75	62	2	0.83×10^{10}	58ª	1.5 ^a
PF-50J -Chile	0.07	0.3	60	9	7.3×10^{10}	66.7	2.9
	0.05	0.3	50	6	5.2×10^{10}	68	
NF ^a -Chile	0.000 25	0.021	6	16	7.6×10^{11}	70	16.9
	0.0001	0.08	4.5	3	5.5×10^{9}	32ª	0.65ª

^a Some very small devices, recently developed, are probably not optimized yet. The energy density parameter has a value of the order of $(1-10) \times 10^{10}$ J m⁻³ for all the experimentally optimized machines listed. The drive parameter has practically the same value for all the experimentally optimized machines listed (68–95 kA cm⁻¹ mbar^{-1/2}). A new parameter related to the energy per mass was introduced now, 'energy per mass parameter' $E/a^3 p$. Note that the three parameters listed in the right-hand side columns are practically constant in comparison throughout the eight orders of magnitude in stored energy range.

L. Soto, C. Pavez, J. Moreno, A. Tarifeño and F. Veloso, Plasma Sources Sci. Technol. 19,055017 (2010)



Energy density parameter 28E/a³~5x10¹⁰J/m⁻³



Drive parameter I/ap^{1/2} ~ 77kA/cm mbar^{1/2}

 $v_a \alpha I / a p^{1/2}$ $v_r \alpha I / a p^{1/2}$

 $r_p \sim (0.1-0.2) \ a, \ z_p \sim (0.8-1) \ a$

a: anode radius

- S. Lee and A. Serban, IEEE Trans. Plasma Science 24, 1101 (1996)
- P. Silva, L. Soto, W. Kies and J. Moreno, Plasma Sources Science and Technology 13, 329 (2004)
- L. Soto, Plasma Phys. Control. Fusion **47**, A361 (2005)
- T. Zhang, R. S. Rawat, S. M. Hassan, J. J. Lin, S. Mahmood, T. L. Tan, S. V. Springham, V. A. Gribkov, P. Lee, and S. Lee, IEEE, Trans. Plasma Sci. 34, 2356 (2006)
- L. Soto, C. Pavez, J. Moreno, A. Tarifeño and F. Veloso, Plasma Sources Sci. Technol. 19,055017 (2010)



Similarities in PF devices operated in a wide range of bank energy (0.1 J – 1 MJ)

- $r_{\rm p} \sim$ (0.1-0.2) a, $z_{\rm p} \sim$ (0.8-1) a
- $<v_a> ~ 5 \times 10^4 \text{ m/s}, v_{af} ~ 1 \times 10^5 \text{ m/s}$
- $\langle v_r \rangle \sim 1 \times 10^5 \text{ m/s}, v_{rf} \sim 2 \times 10^5 \text{ m/s}$
- <n>~18n₀~ 5x10²⁴ m⁻³ n~1x10²⁵ m⁻³
- Energy density parameter 28E/a³~5x10¹⁰J/m⁻³
- Drive parameter I/ap^{1/2} ~ 77kA/cm mbar^{1/2}
- The magnetic field at the pinch radius ~30 to 40 T
- Similar Alfvén speed in the pinch
- Similar drive parameter, energy density parameter and ion density \rightarrow similar temperature
 - L. Soto, C. Pavez, A. Tarifeño, J. Moreno and F. Veloso, Plasma Sources Sci. and Technol. 19, 055017 (2010).
 - D. Klir and L. Soto, IEEE Trans. Plasma Science 40, 3273 (2012)

Temperature does not depend on the energy of the device



$$E/a^3$$

On the one hand,

 $E/V_p \sim E/a^3 \sim \text{const}$

and $n \sim \text{const}$

 $E / ions \sim E / nV_p$ const

Therefore, temperature is constant.

 $I/a p^{1/2}$

On the other hand, the contribution to heating by the current can be estimated by the Bennett relation:

$$kT_{\rm B}=(\mu_0/16\pi)I^2/N,$$

with N the number of ions per unit length (ion line density),

$$\begin{split} N &= 2\pi \int nr \, \mathrm{d}r, \\ \langle n \rangle &= N/\pi r_\mathrm{p}^2, \\ N &= \langle n \rangle \pi r_\mathrm{p}^2 \propto n_0 a^2, \\ kT_\mathrm{B} \propto I^2/n_0 a^2 \propto I^2/a^2 p. \end{split}$$

Therefore, the Bennett temperature is proportional to the square value of the drive parameter.

Therefore, most nuclear and atomic reactions occurring in large plasma foci should also be expected in a miniaturized pinch, given the proper scaled design.

L. Soto, C. Pavez, J. Moreno, A. Tarifeño and F. Veloso, Plasma Sources Sci. Technol. 19,055017 (2010)

Differences in PF devices operated in a wide range of bank energy (0.1 J – 1 MJ)

The stability regime in which a particular PF device lives, depends on the energy of the device and of the size of the anode radius



L. Soto, C. Pavez, J. Moreno, A. Tarifeño and F. Veloso, Plasma Sources Sci. Technol. 19,055017 (2010)



At present other groups are working in sub kJ PF devices



As example:

1kJ to Hundred joules

Japan:

S. R. Mohanty, T. Sakamoto, Y. Kobayashi, I. Song, M. Watanabe, T. Kawamura, A. Okino, K. Horioka and E. Hotta, Rev. Sci. Instrum. 77, 043506 (2006)

India:

R. K. Rout, P. Mishra, A. M. Rawool, L. V. Kulkarani and S. C. Gupta, J. Phys. D: Appl. Phys. 41, 205211 (2008)

USA-Singapore:

R. Verma, R. S. Rawat, P. Lee, M. Krishnan, S. V. Sprinham and T. L. Tan, Plasma Phys. Control. Fusion 51, 075008 (2009)

LLNL, USA:

Ellsworth, J. L.; Falabella, S.; Rusnak, B.; Schmidt, A.; Tang, V., 54th Annual Meeting of the APS, DPP Division (2012)

J. L. Ellsworth, S. Falabella, V. Tang, A. Schmidt, G. Guethlein, S. Hawkins and B. Rusnak, Rev. Sci. Instrum. 85, 013504 (2014)

Tens of joules

India:

R. Shukla, S. K. Sharma, P. Banerjee, R. Das, P. Deb, T. Prabahar, B. K. Das, B. Adhikary, and A. Shyam, Rev. Sci. Instrum. 81, 083501 (2010)

Few Joules

Iran:

Hossein Jafari, Morteza Habibi, Gholam Reza Eta'ati, Physics Letters A, 381, 2813 (2017)



Joint ICTP-IAEA College on Plasma Physics 29 October to 9 November, 2018 Trieste, Italy





How to obtain information from a dense transient plasma

Diagnostics

- Electrical signals
- Visible plasma images
- X-ray detections (temporal and spatial resolution)
- Neutron detection (in particular low yield pulses)
- Charged particles
- Optical refractive diagnostics
- Spectroscopy











For this school the portable PF-2J was brought into a suitcase from Chile to Italy and it is operative at the Multidisciplinary Laboratory, ICTP