

# Characterization of photoelectrochemical processes for energy conversion through computer simulations

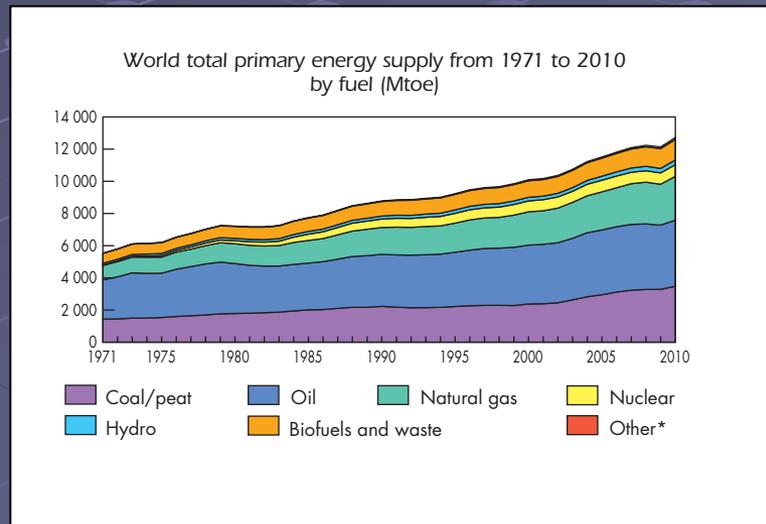
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Strada Costiera 11, 34151 Trieste, Italy

# The energy challenge

- Sustainably providing clean energy for the needs of tomorrow is one of the key challenges humankind has to face



- Shift towards renewable energy sources

# Solar energy

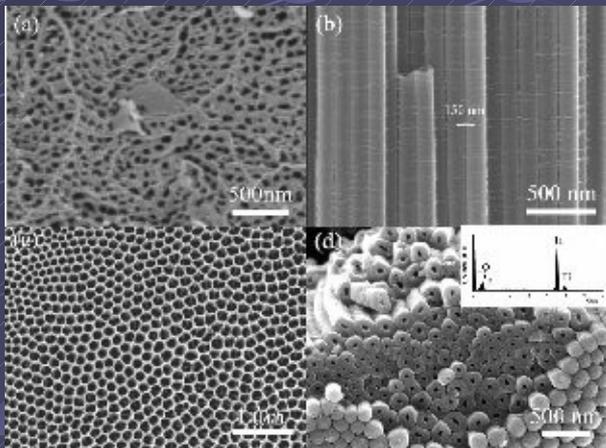
- Solar energy is abundant
- Source is irregular → importance of energy storage (batteries, solar-to-fuel, hydrogen storage,...)
- So far, mainly photovoltaics: but electricity is difficult and expensive to store
- Moreover, some applications need storage at high energy density: liquid fuels for airplanes
- Solar fuels: the goal is to use solar energy to produce fuels (hydrogen, hydrocarbons, methanol,...)

# Solar fuels

- Solar fuels: the goal is to use solar energy to produce fuels (hydrogen, hydrocarbons, methanol,...)
- Three main routes:
  1. Solar thermal
  2. Photovoltaics + electrocatalysis
  3. Photo(electro)catalysis

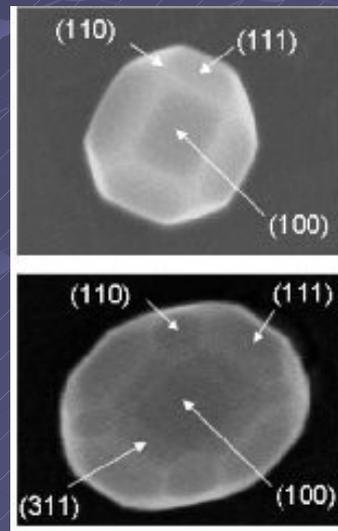
# Nanostructures for energy applications

- Ability to control, manipulate and understand materials at the nanoscale could lead to major advancement in the field of energy conversion and storage
- Properties at the nanoscale different from bulk



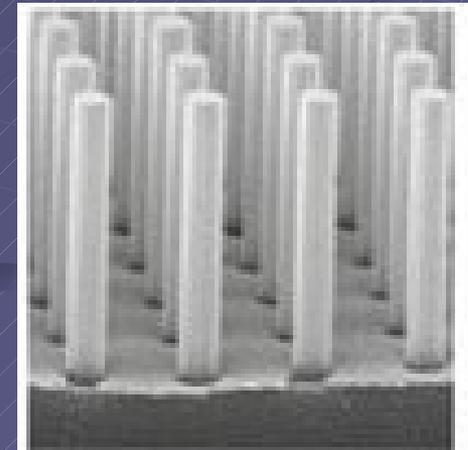
TiO<sub>2</sub> nanotubes as anode material for dye-sensitized solar cells

Li et al., Chem. Mater. 22, 5707 (2010)



Platinum nanoparticles for fuel cells

Komanicky et al., Electrochim. Acta 55, 7934 (2010)

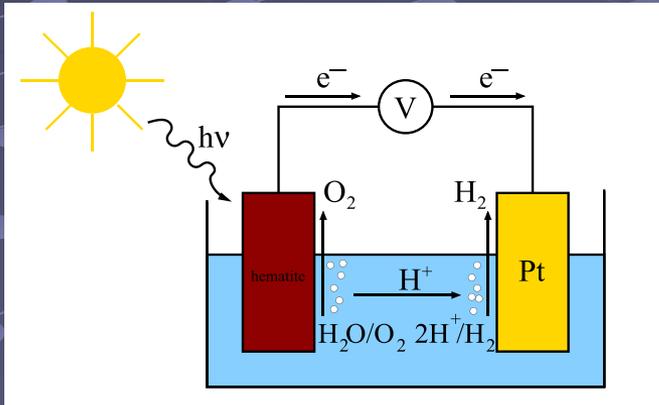


Silicon nanowires as anode for Li batteries

Chang et al., Adv. Funct. Mater. 20, 4364 (2010)

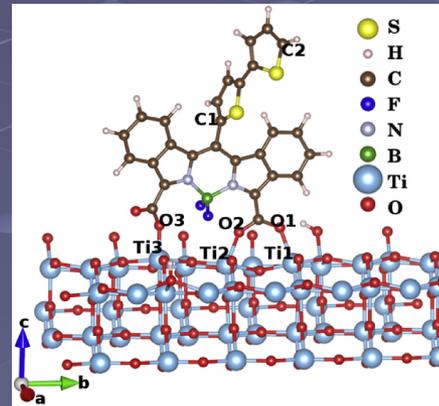
# Understanding functional materials at the atomic level

## Photocatalysis for solar fuels



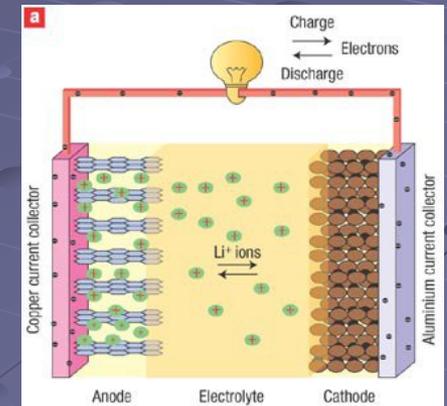
N. Seriani, *J. Phys.: Condens. Mat.* 29, 463002 (2017)

## Photovoltaics



Songkhao et al., *Dyes and Pigments* 142, 558 (2017)

## Batteries



B. Scrosati, *Nature Nanotechnology* 2, 598 (2007)

Complex composition: defects, dopants, ...  
Complex environment affecting composition and interfaces  
Complex processes: photoabsorption, charge dynamics,  
interface reactions

# Computational materials science for sustainable energy

Environment  
(pressure, temperature, applied voltage, pH,...)



Properties  
(atomic structure, stability, electronic properties,...)



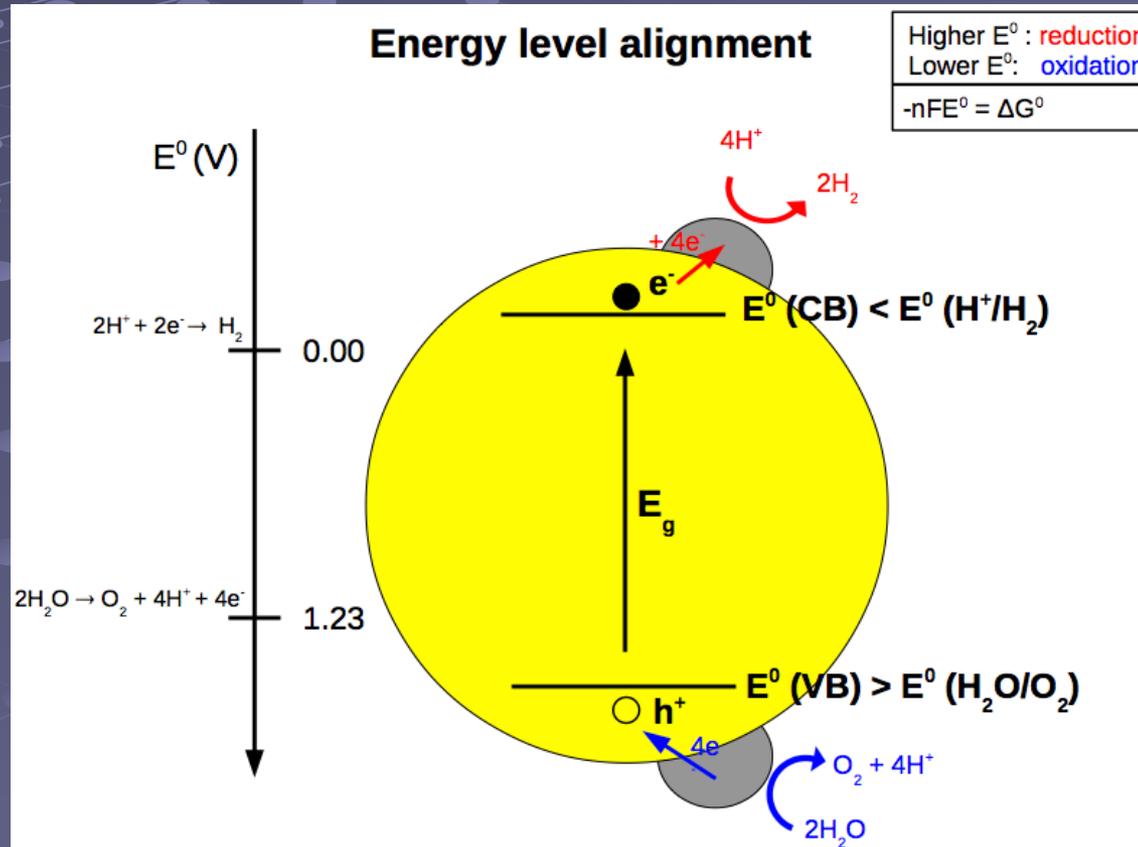
Function  
(photocatalytic activity, lithium storage capacity,...)



Materials design

Density functional theory and high-performance computing

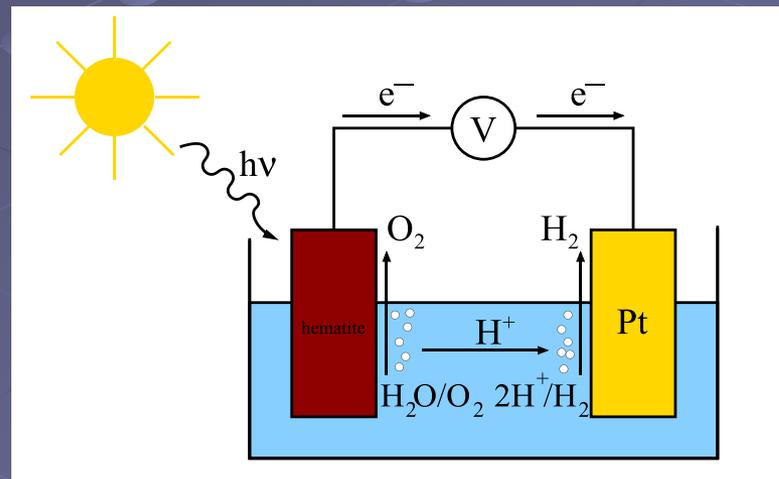
# Photocatalysis



# Photoelectrocatalysis

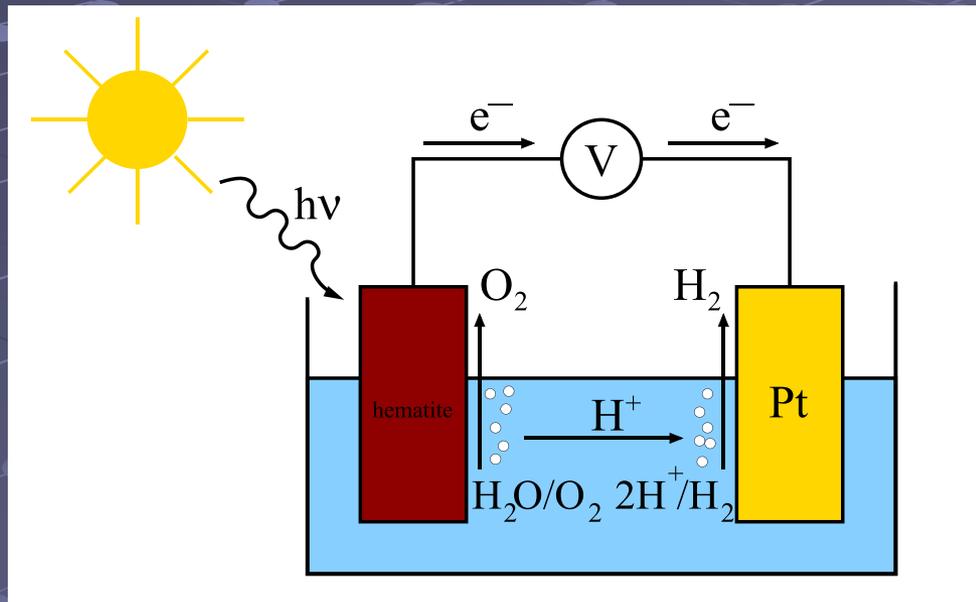


Acidic conditions...

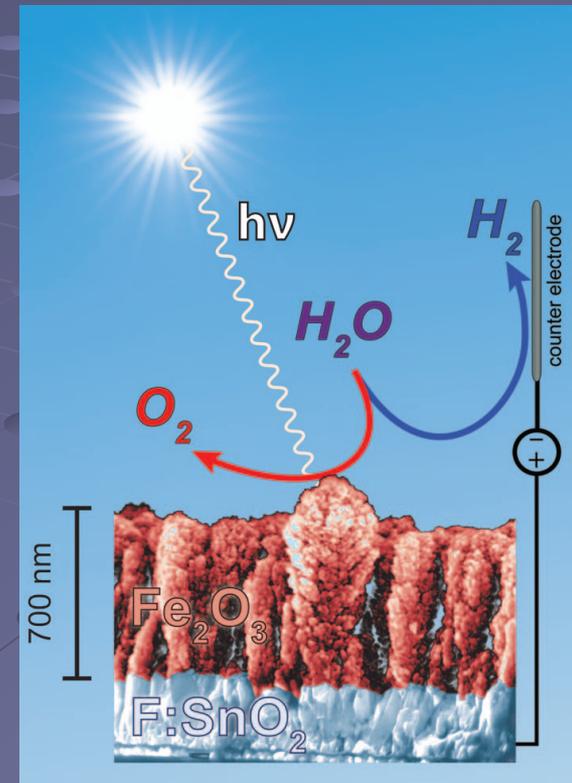


N. Seriani, J. Phys.: Condens. Mat. 29, 463002 (2017)

# Photoelectrochemical cells for solar-fuel production



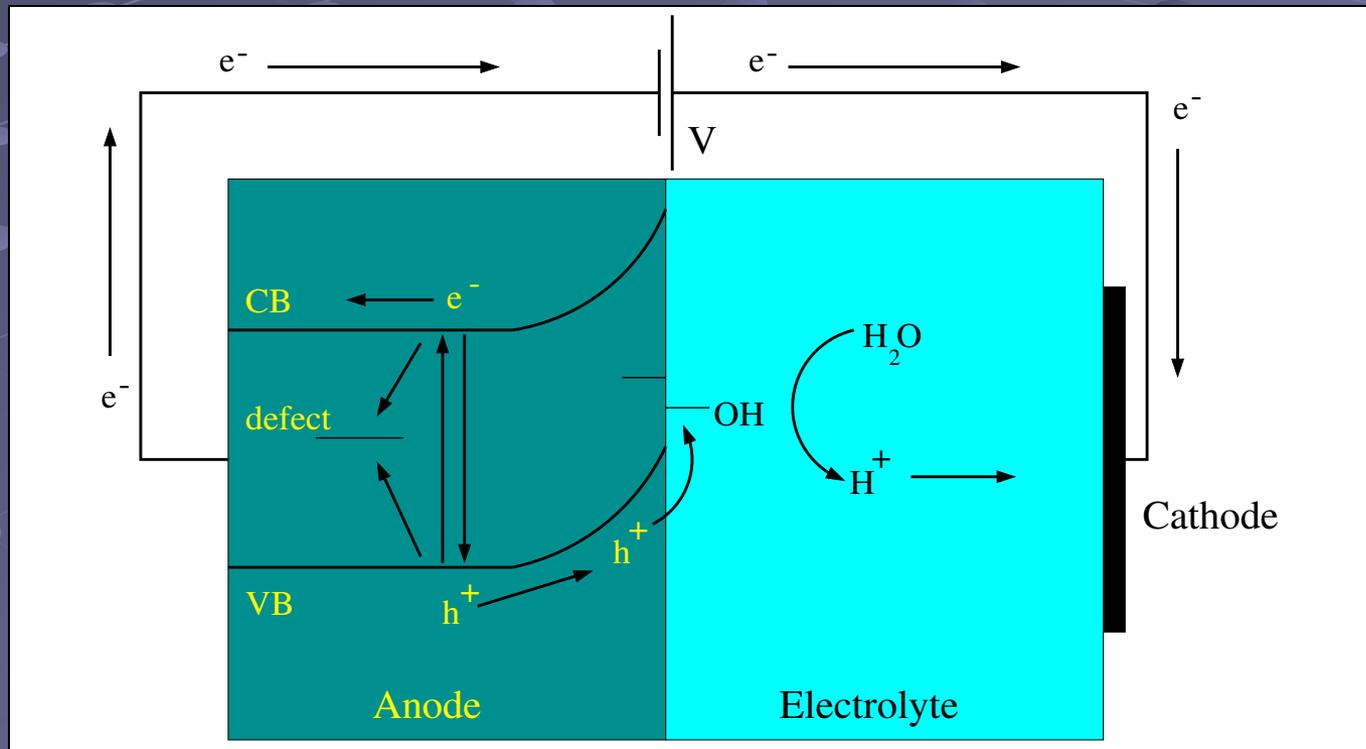
N. Seriani, *J. Phys.: Condens. Mat.* 29, 463002 (2017)



K. Sivula et al.,  
*ChemSusChem* 4, 432 (2011)

# Complex (photo-)physics and (photo-)chemistry

- Photoabsorption, recombination, charge separation, charge transfer, adsorption, proton-coupled electron transfer, ...

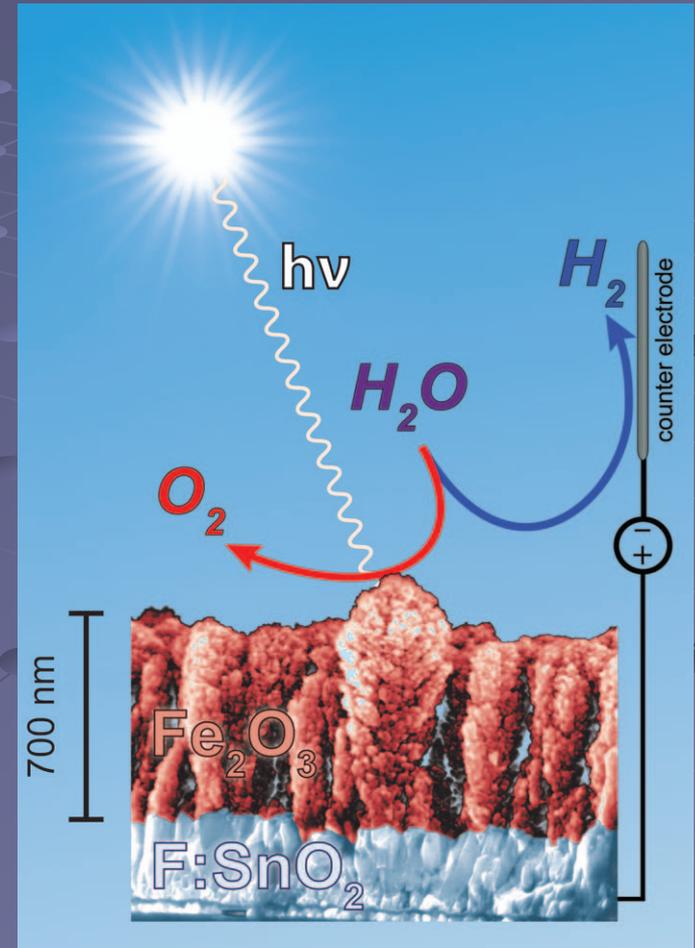


# Titania as a photocatalyst

- The material of choice is  $\text{TiO}_2$ , for its wide availability, safety, stability, and activity
- It has a gap of  $\sim 3$  eV, it absorbs in the UV range
- This accounts for less than 5% of the energy in the visible range
- Need to find other materials (hematite), to modify the titania photocatalyst and to understand the mechanisms of the photocatalytic process

# Hematite

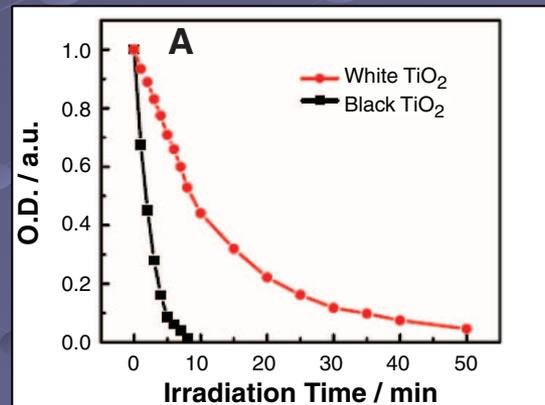
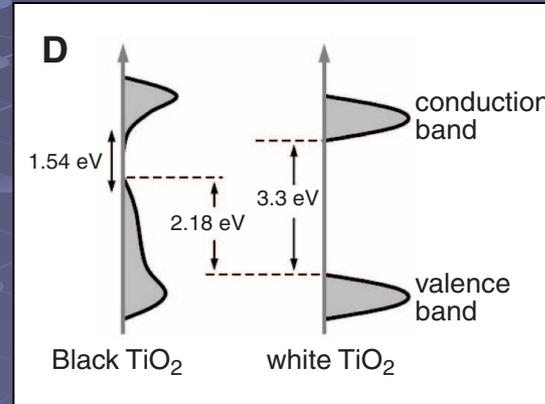
- $\alpha\text{-Fe}_2\text{O}_3$  (hematite) is a promising material as photoanode for photoelectrocatalytic water splitting.
- Gap  $\sim 2$  eV
- Problem of charge transport and recombination
- Charge transport problem is less important for nanostructured materials
- Some progress, but not definitive
- Need to characterize material and processes



K. Sivula et al., ChemSusChem 4, 432 (2011)

# Black hydrogenated titania

Hydrogenation improves  
photoabsorption and photocatalytic activity

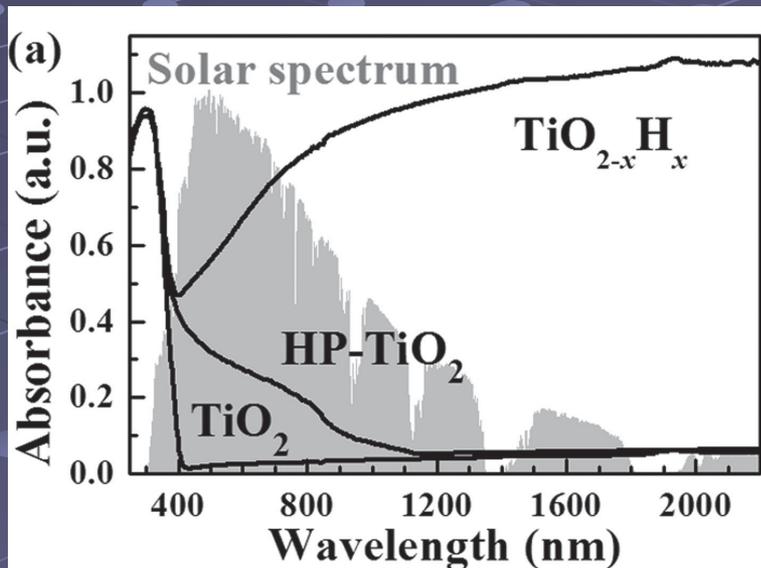


Optical density of methylene  
blue solution as function of time

X. Chen et al., Science 331, 746 (2011)

# Black hydrogenated titania

Optical absorption spectrum depends on hydrogenation method:



HP-TiO<sub>2</sub> by high-pressure thermal treatment

TiO<sub>2-x</sub>H<sub>x</sub> by plasma treatment

X. Chen et al., Science 331, 746 (2011)

Z. Wang et al., Adv. Funct. Mater. 23, 544 (2013)

# Computational details

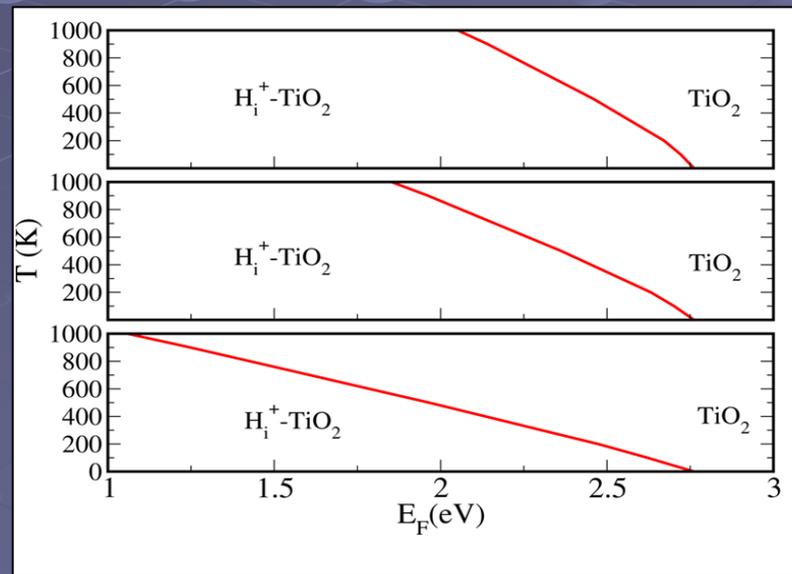
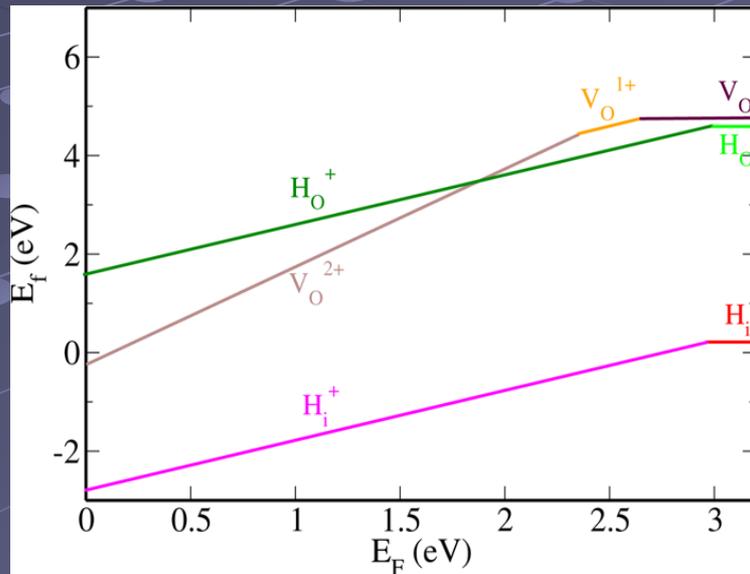
- Density functional theory: PBE + U
- Plane waves
- Norm-conserving pseudopotentials
  
- GW + Bethe-Salpeter Equation
- $G_0W_0$
- Plasmon pole approximation

<http://www.quantum-espresso.org>

<http://www.yambo-code.org>

# Hydrogenated titanium dioxide: thermodynamics

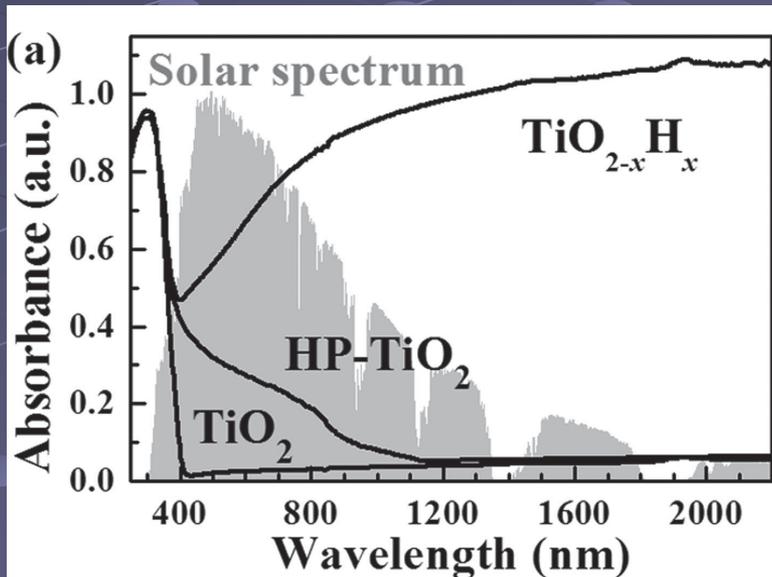
- )  $H_i$ : interstitial hydrogen
- )  $H_O$ : hydrogen in oxygen vacancy
- )  $V_O$ : oxygen vacancy



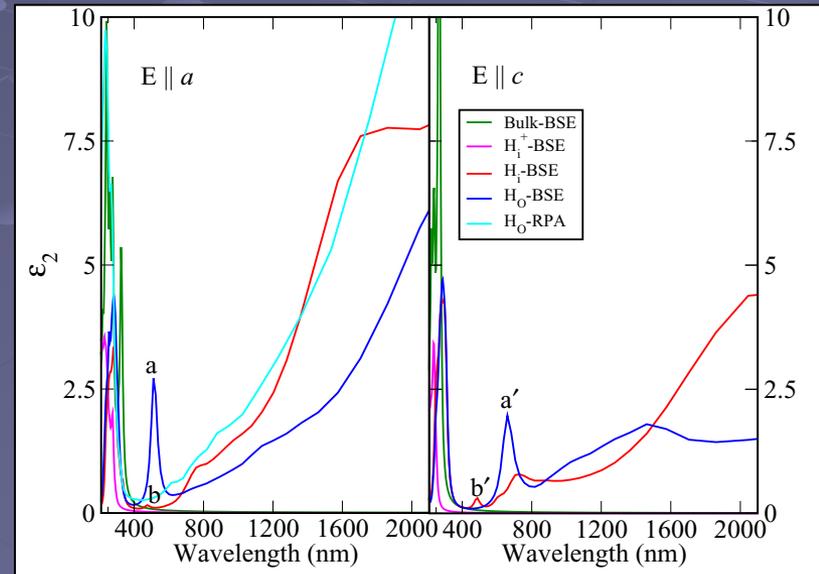
S. S. Ataei, M. R. Mohammadizadeh, N. Seriani, JPCC 120, 8421 (2016)

# Hydrogenated titanium dioxide: optics

- ) Neutral hydrogen defects lead to adsorption in visible and IR
- ) Proton defects barely influence photoabsorption
- ) HP-TiO<sub>2</sub> spectrum is reproduced in presence of disordered Ti-H and O-H (L. Liu et al., PRL 111, 065505 (2013))



Z. Wang et al.,  
Adv. Funct. Mater. 23, 544 (2013)  
X. Chen et al., Science 331, 746 (2011)



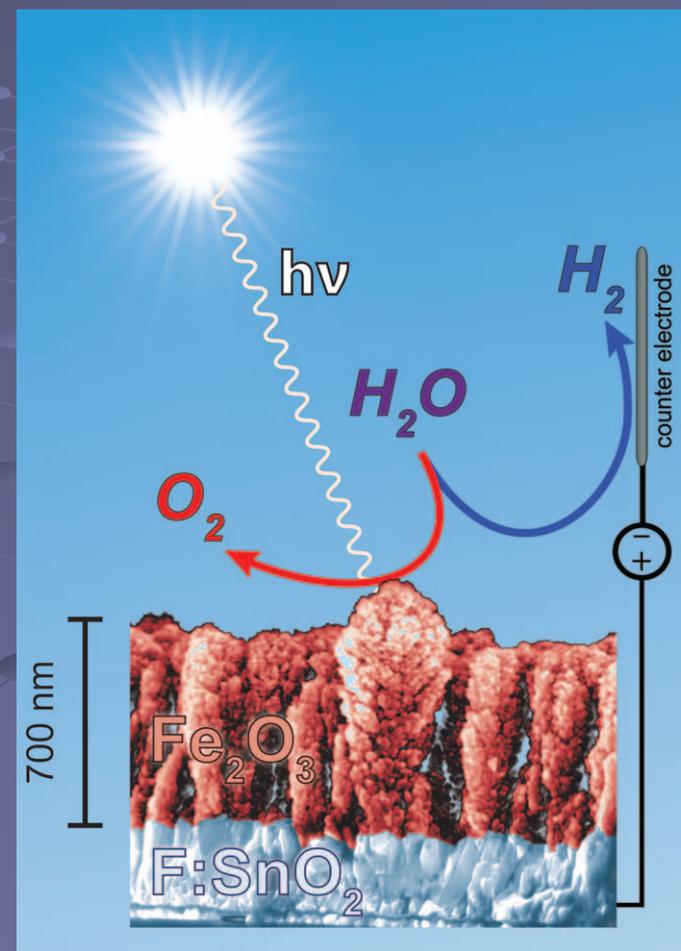
S. S. Ataei, M. R. Mohammadzadeh, N. Seriani,  
PRB 95, 155205 (2017)  
S. S. Ataei, M. R. Mohammadzadeh, N. Seriani,  
JPCC 120, 8421 (2016)

# Hydrogenated titania: conclusions

- Hydrogenated  $\text{TiO}_2$  has an improved photoabsorption and photocatalytic activity
- The photoabsorption spectrum depends heavily on the hydrogenation conditions (high pressure vs. plasma treatment)
- First-principles simulations show that neutral hydrogen defects lead a photoabsorption spectrum compatible to that of plasma treated H- $\text{TiO}_2$
- Charged H defects show only marginal differences with respect to defect-free titania

# Reactions at the surface of the photocatalyst

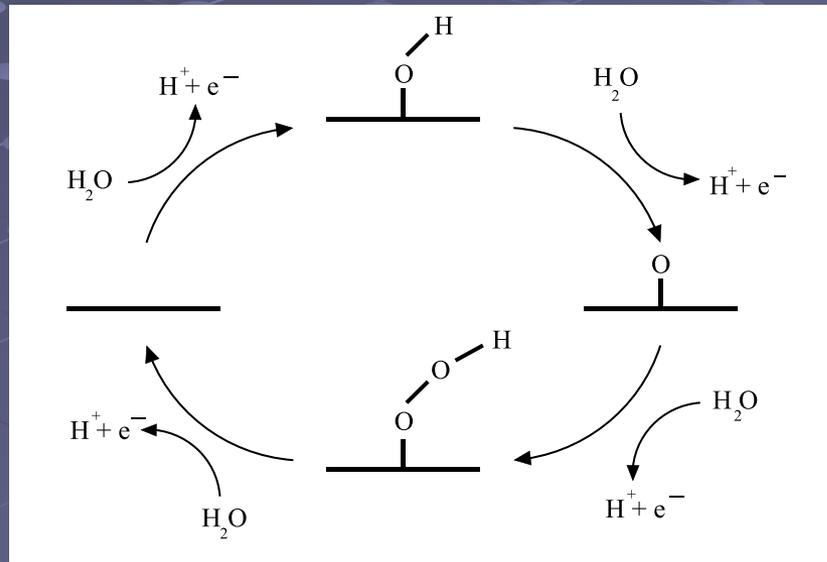
- Oxygen evolution takes place at the interface between the photocatalyst and the electrolyte
- Important to characterize thermodynamics and kinetics chemical reactions, and of charge transfer



K. Sivula et al., ChemSusChem 4, 432 (2011)

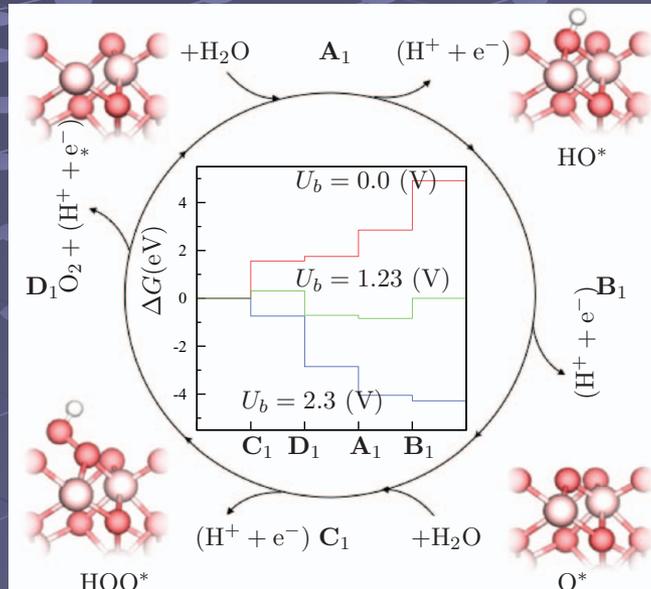
# Water oxidation at the photoanode

At the anode:  $2\text{H}_2\text{O} \rightarrow \text{O}_{2,\text{g}} + 4\text{H}^+_{\text{aq}} + 4\text{e}^-$



At the surface of the photoanode, the reaction proceeds through 4 elementary steps (proton coupled electron transfers)  
This takes place however in a complex environment

# Thermodynamics of water splitting at the (0001) surface of hematite



Nguyen et al., J. Chem. Phys.  
140, 064703 (2014)

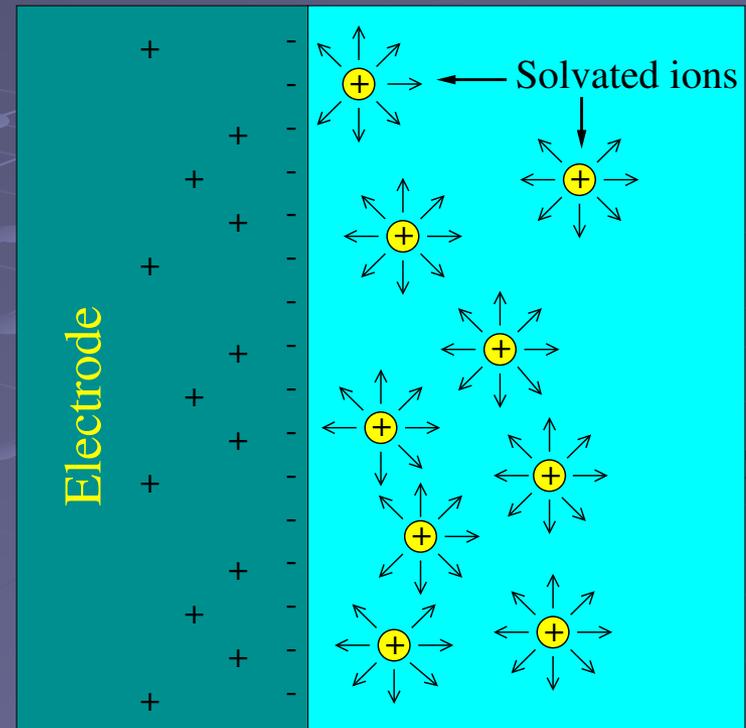
Seriani, J. Phys.: Condens.  
Mat. 29, 463002 (2017)

Crucial to take into account the photoelectrochemical conditions (in water, under illumination)  
We find an overpotential of 0.8 V for photo-driven water oxidation, in fair agreement with experiments

# The electrochemical interface

A crucial role is played by the electrochemical interface, specially for charge dynamics:

space charge layer,  
double layer,  
ions,  
electric field,  
illumination,  
hole transfer

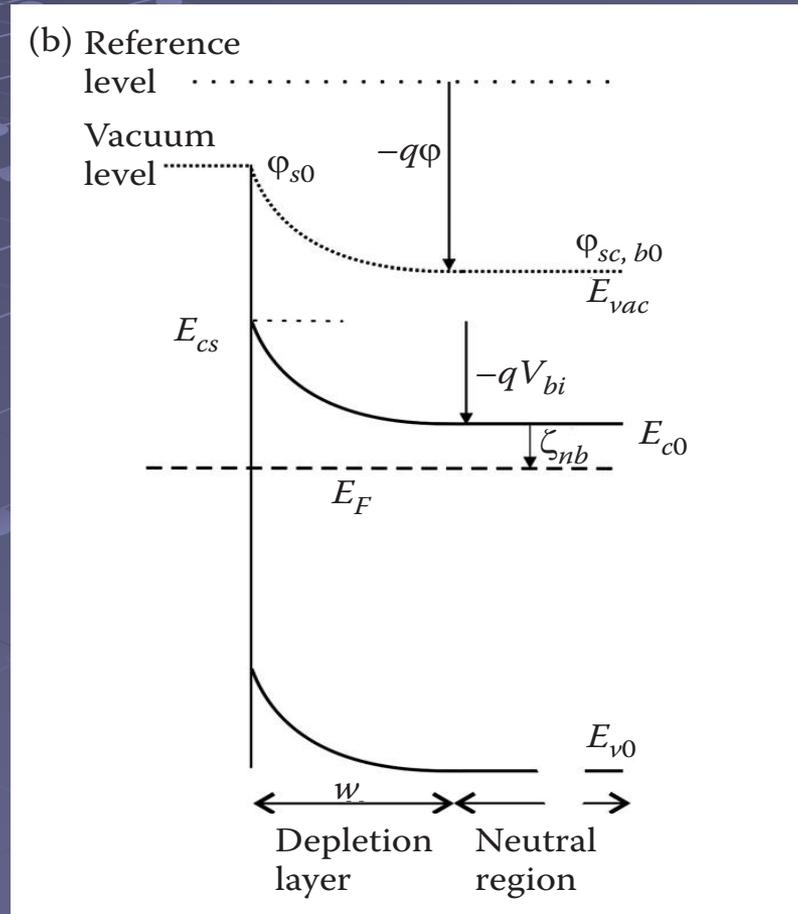


Goal is to take a second look (with new tools) at old models\*\* of the interface and of the double layer

\*\* Stern, Z. Electrochem., 30, 508 (1924)

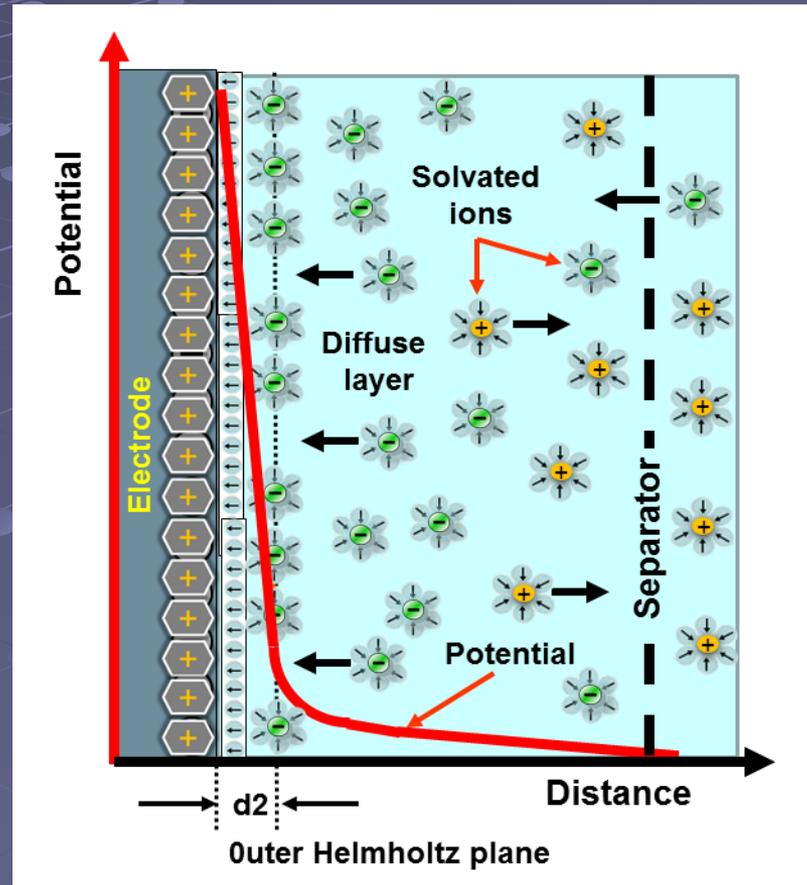
\*\* Gouy, J. Phys. 9, 457 (1910)

# On the semiconductor side: the space charge layer



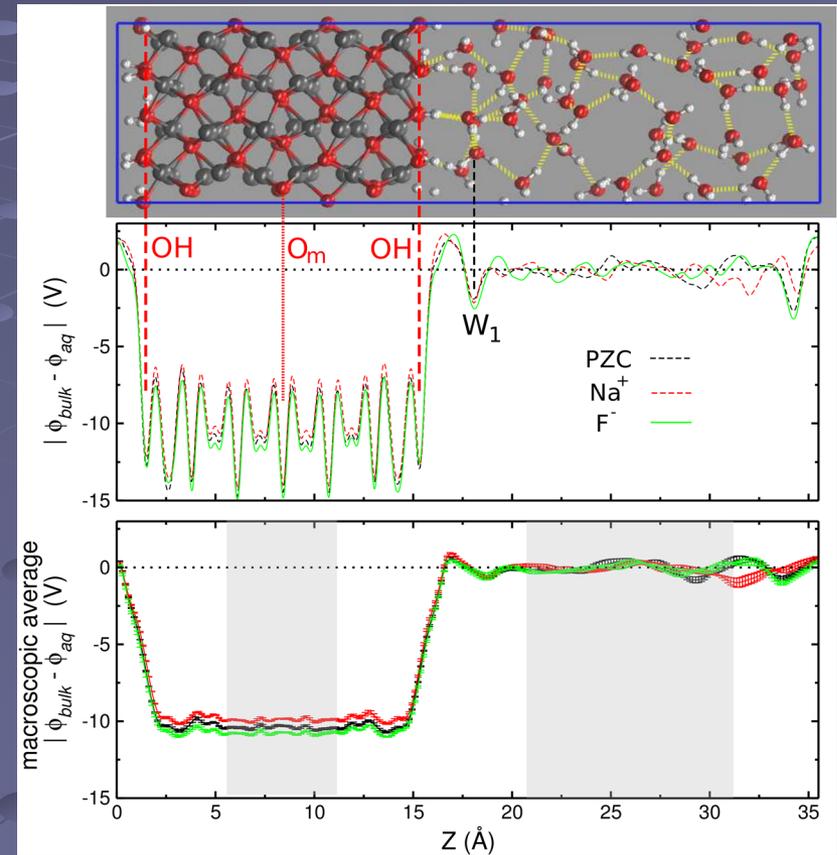
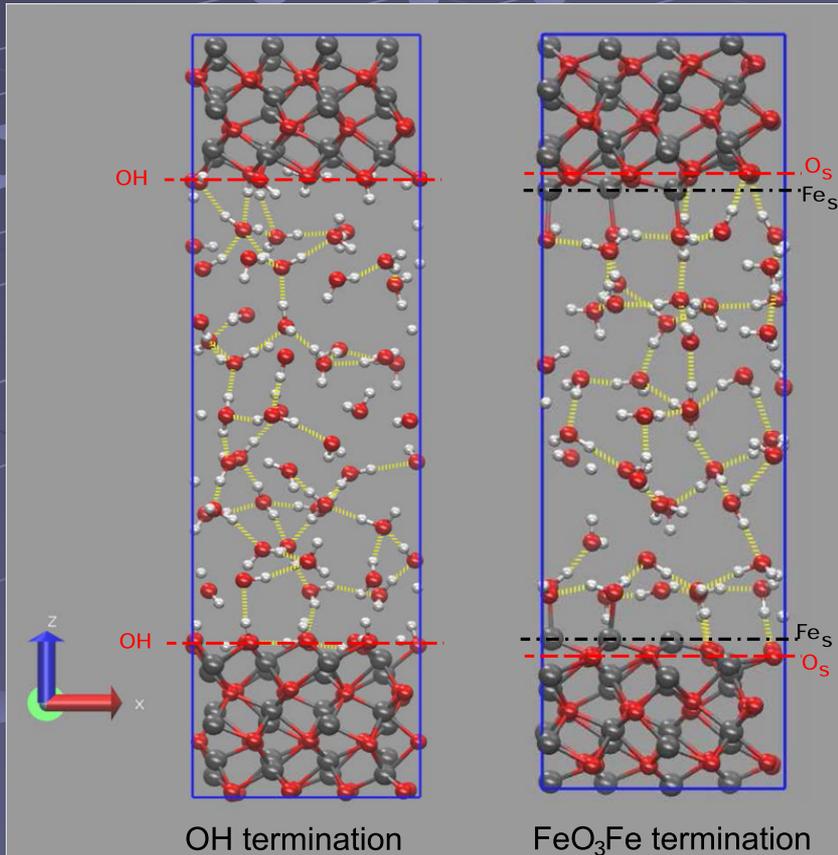
J. Bisquet, Nanostructured energy devices (CRC Press)

# On the electrolyte side: the double layer



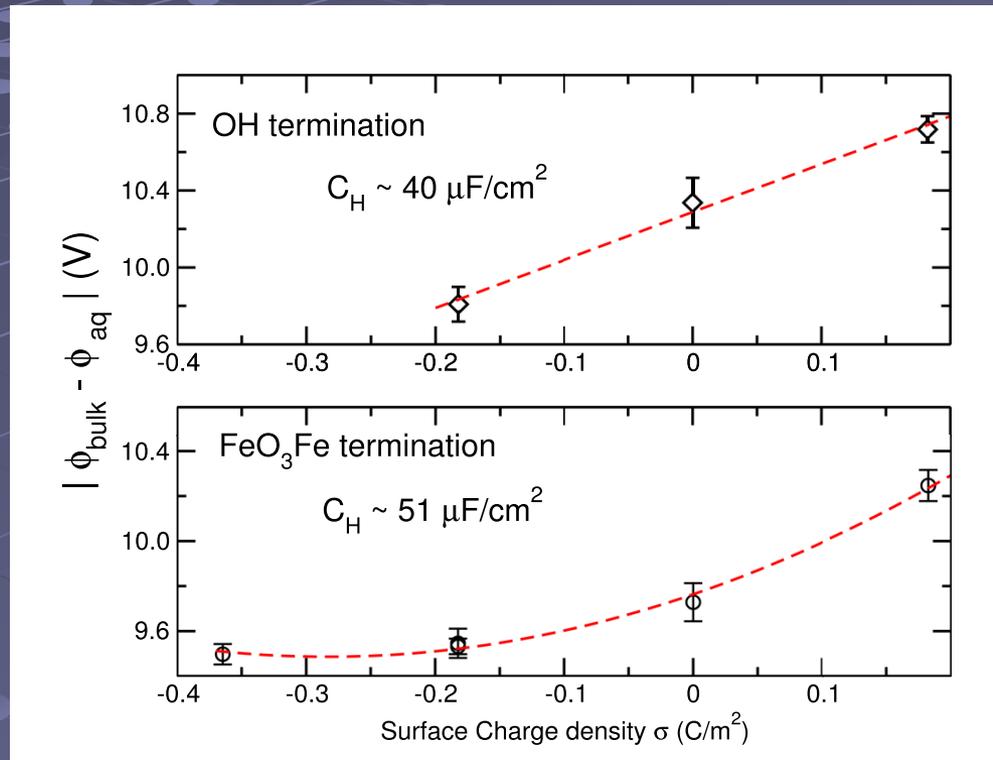
By Elcap - Own work, CC0,  
<https://commons.wikimedia.org/w/index.php?curid=25771148>

# The double layer at the (0001) hematite surface



Ulman, Poli, Seriani, Piccinin, Gebauer,  
J. Chem. Phys. 150, 041707 (2019)

# The capacitance of the double layer



Ulman, Poli, Seriani, Piccinin, Gebauer,  
J. Chem. Phys. 150, 041707 (2019)

# The capacitance of the double layer

**TABLE I.** The estimates of various capacitances for the hematite water interface under different pH conditions reported by various experiments. The values reported by Lucas and Boily<sup>42,43</sup> are converted to  $\mu\text{F}/\text{cm}^2$  by area normalization assuming a cross-sectional area of a micro-electrode  $\sim 491 \mu\text{m}^2$ . Capacitance  $\bar{C}_{\text{bulk}}$ <sup>57,59</sup> effectively amounts to capacitance of  $C_{\text{SC}}$  and  $C_{\text{H}}$  in series.

Reference	$C_{\text{SC}}$ ( $\mu\text{F}/\text{cm}^2$ )	$C_{\text{H}}$ ( $\mu\text{F}/\text{cm}^2$ )	$C_{\text{dl}}$ ( $\mu\text{F}/\text{cm}^2$ )	$C_{\text{SS}}$ ( $\mu\text{F}/\text{cm}^2$ )	Surface	pH	Experimental technique and model
Boily, Chatman, and Rosso <sup>35</sup>	...	31-73	...	...	(001)	0-14	OCPM and 1-pK/2-pK BSM
Chatman, Zarzycki, and Rosso <sup>36</sup>	...	30-88	18-35	...	(001)	3-11	OCPM and TLM
	...	20-88	18-60	...	(012)		
	...	59-80	12-68	...	(113)		
Hwang and Lenhart <sup>37</sup>	...	56-156	-	...	...	5-10	OCPM and TLM
Shimizu and Boily <sup>39</sup>	$C_{\text{int}} \sim 0.50$ and $0.55$		...	...	(001)	11 and 4.3	CV
	...	0.2-2.0	0.5-0.6	...	(001)	4-12	GEIS
Shimizu and Boily <sup>41</sup>	$10^{-8}$	0.2-0.6	0.2-0.6	...	(001)	3-13	GEIS
	$10^{-9}$	3-35	1-10	...	(012)		
Lucas and Boily <sup>42</sup>	...	12.6	1.46	...	(001)	5.9	GEIS
	...	75.1	9.06	...	(012)		
	...	44-124	2-63	...	(001)		
Lucas and Boily <sup>43</sup>	...	53-180	2-53	...	(012)	5.9	LEIS
	...	117	4.75	...	(001)	5 (NaCl)	LEIS
	...	212.8	10.84	...		5 (NaHCO <sub>3</sub> )	
	...	149.3	5.33	...		5 (NH <sub>4</sub> Cl)	
	...	144	1.06	...	(012)	5 (NaCl)	LEIS
	...	176.2	2.93	...		5 (NaHCO <sub>3</sub> )	
	...	243.4	1.42	...		5 (NH <sub>4</sub> Cl)	
	...	192	6.27	...	(001)	9 (NaCl)	LEIS
	...	368.4	7.33	...		9 (NaHCO <sub>3</sub> )	
	...	298.8	8.94	...		9 (NH <sub>4</sub> Cl)	
	...	227.5	2.01	...	(012)	9 (NaCl)	LEIS
	...	237.7	2.12	...		9 (NaHCO <sub>3</sub> )	
...	331	2.24	...	9 (NH <sub>4</sub> Cl)			
Iandolo et al. <sup>56</sup>	...	...	...	10-90	...	12.9	EIS under Illumination (ECM2)
Klahr et al. <sup>57</sup>	$\bar{C}_{\text{bulk}} \sim 1-4$		...	20-160	...	6.9	EIS under Illumination (ECM2)
			...	10-100	...	13.3	
Klotz et al. <sup>59</sup>	3.98	126	...	...	...	14	EIS under Illumination (ECM1)
	$\bar{C}_{\text{bulk}} \sim 3.86$		...	125	...	14	EIS under Illumination (ECM2)

Experimental data  
fall in a broad range

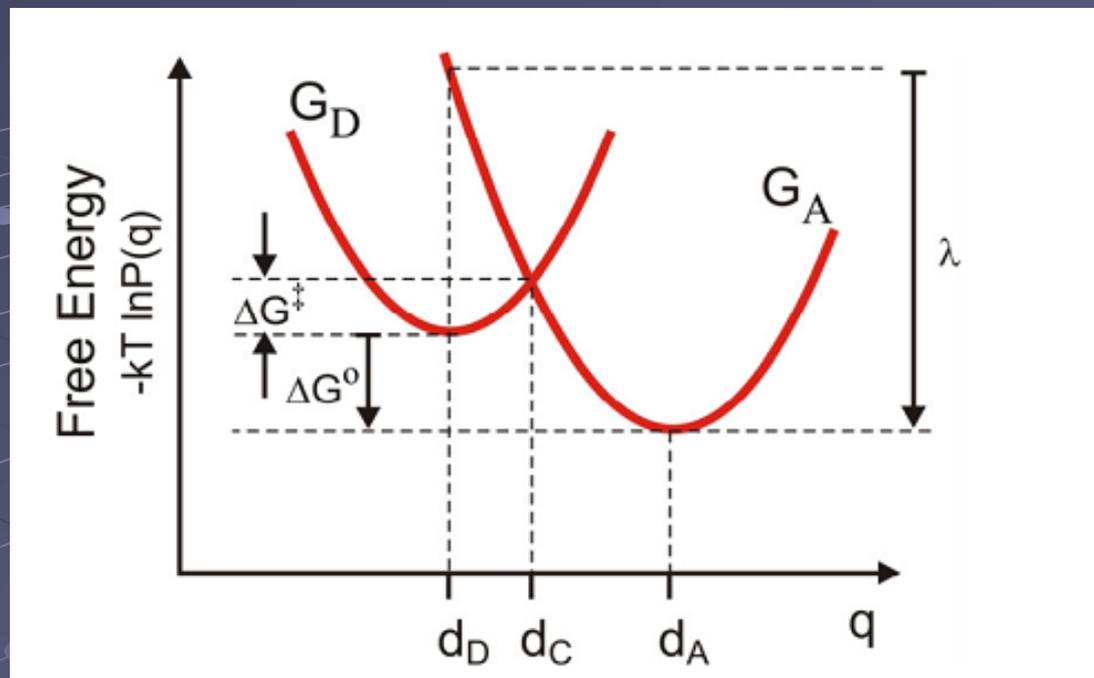
Ulman, Poli, Seriani, Piccinin, Gebauer,  
J. Chem. Phys. 150, 041707 (2019)

# Charge transfer kinetics at the interface

Transient absorption spectroscopy and intensity-modulated photocurrent spectroscopy indicate a very slow hole transfer at the interface, in the millisecond-to-second regime

Getting an insight into this process could be important

# Marcus theory of electron transfer



$\Delta G^0$ : reaction free energy  
 $\Delta G^\ddagger$ : reaction barrier  
 $\lambda$ : reorganization energy

Picture by Andrei Tokmakoff, CC BY-NC-SA 3.0 US licence

[https://chem.libretexts.org/Bookshelves/Physical\\_and\\_Theoretical\\_Chemistry\\_Textbook\\_Maps/Book%3A\\_Time\\_Dependent\\_Quantum\\_Mechanics\\_and\\_Spectroscopy\\_\(Tokmakoff\)/14%3A\\_Energy\\_and\\_Charge\\_Transfer/14.5%3A\\_Marcus\\_Theory\\_for\\_Electron\\_Transfer](https://chem.libretexts.org/Bookshelves/Physical_and_Theoretical_Chemistry_Textbook_Maps/Book%3A_Time_Dependent_Quantum_Mechanics_and_Spectroscopy_(Tokmakoff)/14%3A_Energy_and_Charge_Transfer/14.5%3A_Marcus_Theory_for_Electron_Transfer)

$$k_{\text{ET}} = \frac{2\pi}{\hbar} \frac{\langle |H_{ab}|^2 \rangle_T}{\sqrt{4\pi k_B T \lambda}} \exp \left[ -\frac{(\lambda + \Delta A)^2}{4k_B T \lambda} \right]$$

# Marcus rates from constrained density functional theory

$$k_{\text{ET}} = \frac{2\pi}{\hbar} \frac{\langle |H_{ab}|^2 \rangle_T}{\sqrt{4\pi k_B T \lambda}} \exp \left[ -\frac{(\lambda + \Delta A)^2}{4k_B T \lambda} \right]$$

$\Delta A$ : reaction free energy

$\lambda$ : reorganization energy

$H_{ab}$ : matrix element, electronic coupling

Constrained DFT allows to perform molecular dynamics while keeping the charge either in the initial or in the final state (CP2K code)

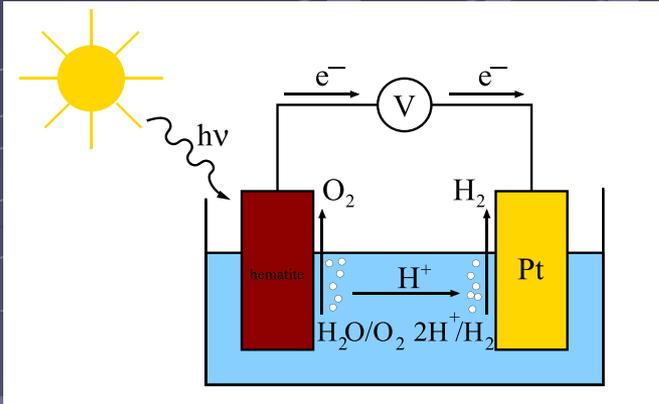
# Marcus theory of electron transfer: preliminary results

With one hole at the surface:  $k_{\text{et}} \approx 3 \cdot 10^{-7} \text{ s}^{-1}$

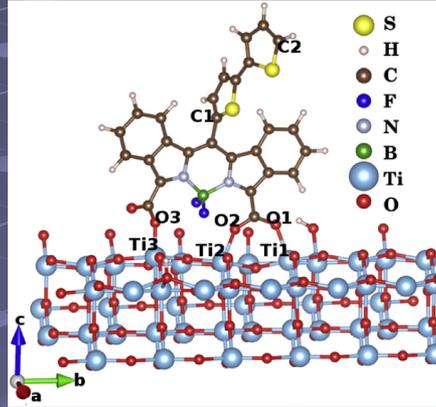
With two holes at the surface:  $k_{\text{et}} \approx 2 \cdot 10^3 \text{ s}^{-1}$

Experiments: timescale in the ms-to-s range

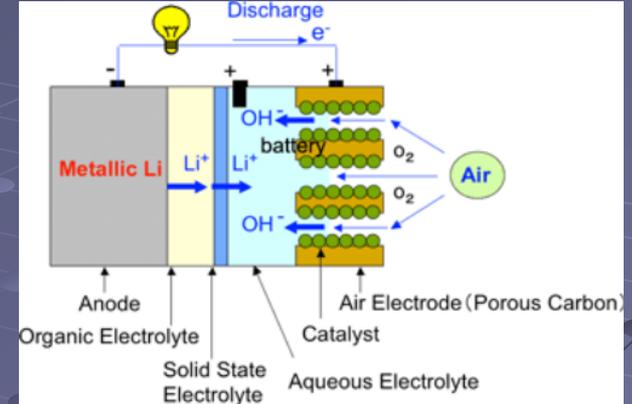
# The road travelled...



Photocatalysis  
for solar fuels



Photovoltaics



Batteries

In some cases we are able to understand some effects of the environment on properties and functionality:

- ) simplified models of environment
- ) only some properties: photoabsorption, thermodynamics of reactions

# Open scientific issues

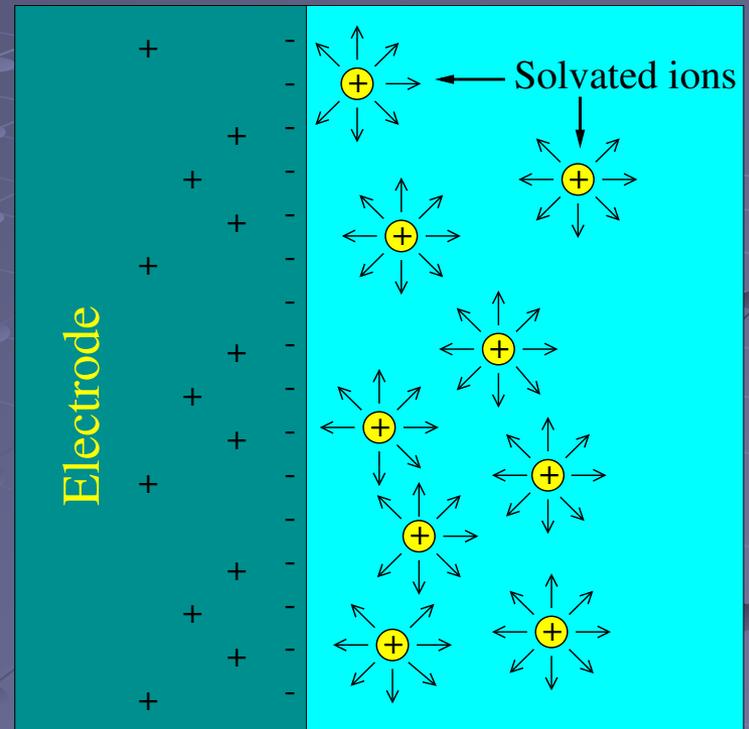
Which species are involved in the rate-limiting charge transfer?

How does their atomic configuration and dynamics depend on the structure of the interface?

Is it possible to engineer the interface to circumvent or change the nature of the rate-limiting step?

Interaction with experimentalists will be crucial

Use of advanced computational methods will be essential



# Conclusions

- Titania and hematite is an interesting photocatalyst for water oxidation
- DFT simulations can provide insight into important processes: photoabsorption, chemical reactions, charge transfer
- Black hydrogenated titania
- Processes at the hematite/water interface

# Acknowledgements

- M.-T. Nguyen (PNNL)
- K. Ulman (NUS)
- N. Ansari, E. Poli, N. Kumar, R. Gebauer (ICTP)
- S. Piccinin, M. Farnesi Camellone (CNR-IOM)
- S. S. Ataei, M. R. Mohammadzadeh (University of Tehran)

Financial support: ICTP

Computational resources: ICTP and CINECA

# Density functional theory

- Method to reduce the many-electron Schrödinger equation to equations for one-electron wavefunctions (Kohn-Sham equations)

Schrödinger equation

$$\left[ -\sum_i^N \frac{\hbar^2}{2m} \nabla_i^2 + \sum_i^N V(\vec{r}_i) + \sum_{i<j} U(\vec{r}_i, \vec{r}_j) \right] \Psi(\vec{r}_1, \dots, \vec{r}_N) = E \Psi(\vec{r}_1, \dots, \vec{r}_N)$$



$$\left[ -\frac{\hbar^2}{2m} \nabla_i^2 + V(\vec{r}_i) + \int \frac{n(\vec{r}')}{|\vec{r} - \vec{r}'|} + V_{xc}[n(\vec{r})] \right] \phi_i(\vec{r}) = \varepsilon_i \phi_i(\vec{r})$$

Kohn-Sham equation

Approximations necessary for  $V_{xc}$

# H in TiO<sub>2</sub>: Density functional theory (DFT)

- Density functional theory: PBE + U
- Hubbard  $U(\text{Ti}3d) = 3.5 \text{ eV}$ ;  $U(\text{O}2p) = 3.5 \text{ eV}$
- Plane waves
- Norm-conserving pseudopotentials
- $E_{\text{cut}} = 100 \text{ eV}$
- $6 \times 6 \times 2$  k-points
  
- $E_{\text{gap}} = 3.27 \text{ eV}$

# GW + Bethe-Salpeter Equation

- GW + Bethe-Salpeter Equation
- $G_0W_0$
- Plasmon pole approximation
- $E_{\text{cut}} = 7 \text{ Ry}$  for the correlation part of self-energy
- 6000 plane waves for the exchange self-energy
- $\hbar\omega_p = 3.94 \text{ eV}$  for the Drude term
- 4 occupied and 22 empty states for BSE

# Hematite: calculation details

- PBE+U
- $U = 4.2$  eV for Fe 3d states
- Plane waves
- Ultrasoft pseudopotentials
- Energy cutoff 40 Ry
- Quantum-ESPRESSO

# Nørskov's approach

**Finite V:**

$$V=0 \quad \mu(\text{H}^+) + \mu(\text{e}^-) = 1/2\mu(\text{H}_2)$$

$$V \neq 0 \quad \mu(\text{e}^-) \rightarrow \mu(\text{e}^-) - eV$$

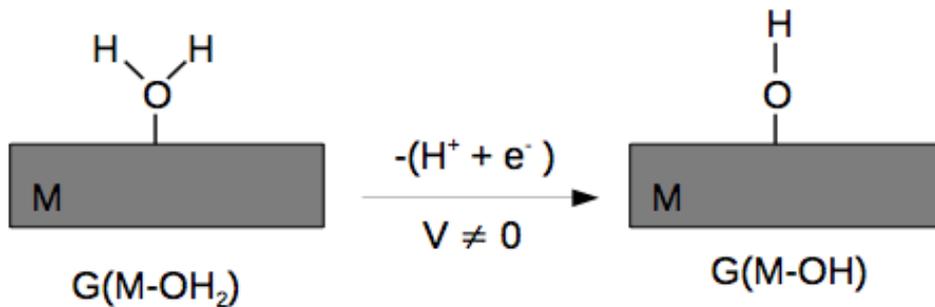
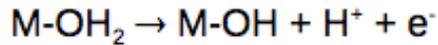
$$\mu(\text{H}^+) + \mu(\text{e}^-) = 1/2\mu(\text{H}_2) - eV$$

**All other effects of the bias V are neglected in this approach**

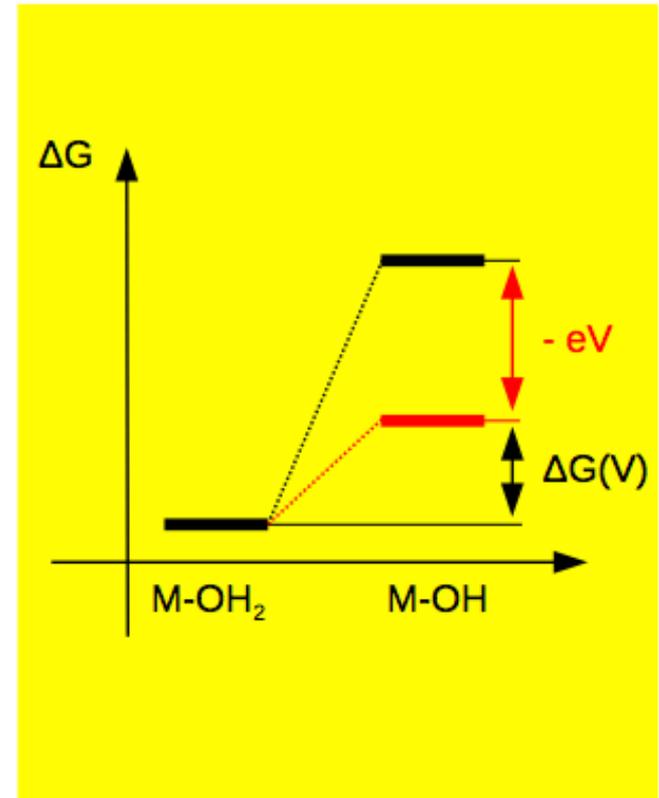
Proton coupled electron transfer

# Nørskov's approach

**Example:**  $V \neq 0$

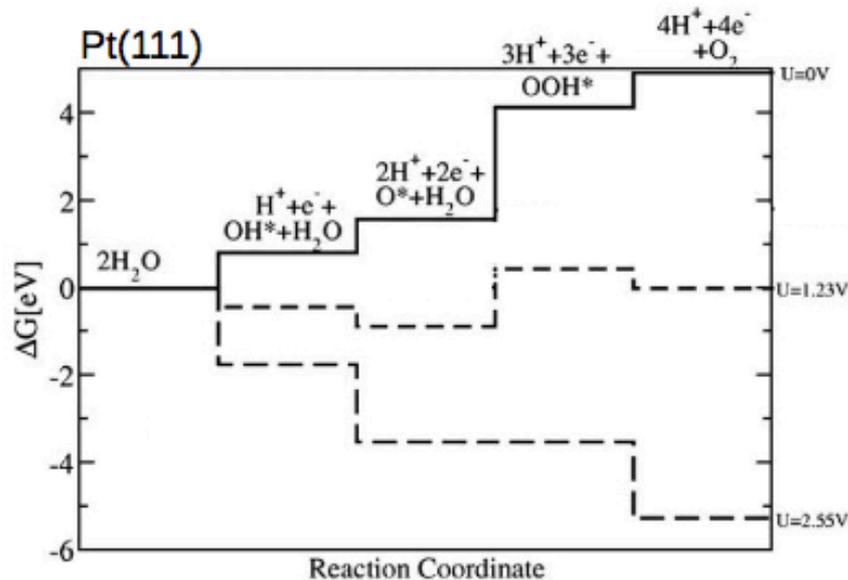
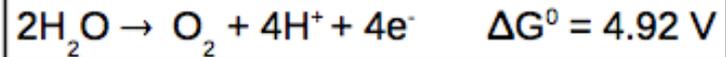


$$\begin{aligned} \Delta G(V) &= G(\text{M-OH}) + \underbrace{\mu(\text{H}^+) + \mu(\text{e}^-)} - G(\text{M-OH}_2) \\ &= G(\text{M-OH}_2) + 1/2\mu(\text{H}_2) - eV - G(\text{M-OH}) \\ &= \Delta G(V=0) - eV \end{aligned}$$



**The relative energies of the intermediates depend linearly on the bias  $V$**

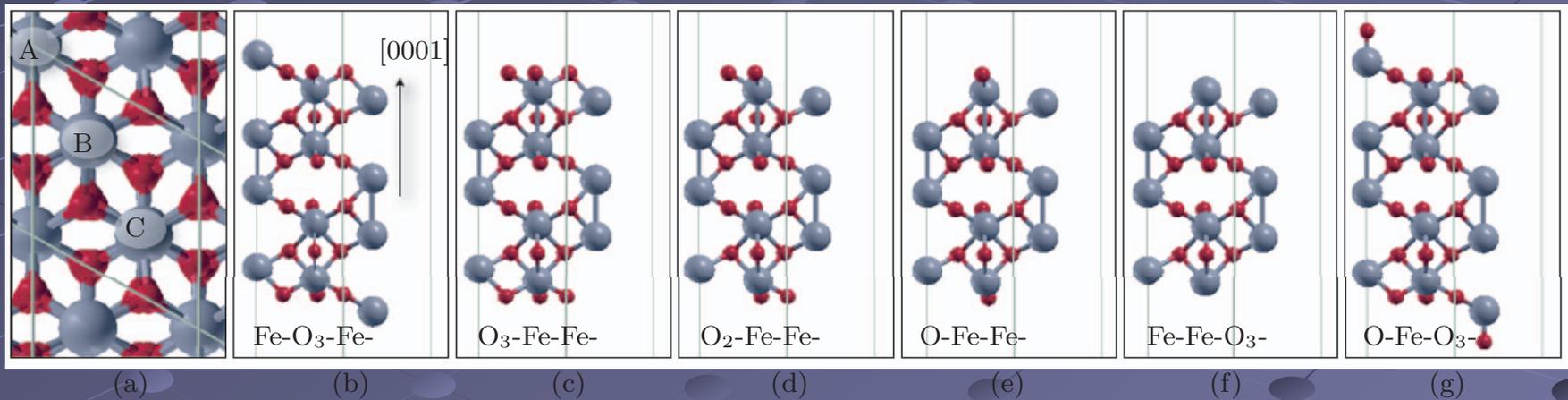
# Nørskov's approach



- $U = 1.23 \text{ V}$  is not sufficient to oxidize water on Pt(111):  $\text{OOH}^*$  is too weakly bound compared to  $\text{O}^*$
- At  $U = 2.55 \text{ V}$  all steps are downhill in energy
- The **overpotential** of Pt(111) is  $2.55 - 1.23 = 1.32 \text{ V}$

Rossmeisl *et al.* Phys. Chem **319**, 178-184 (2005)

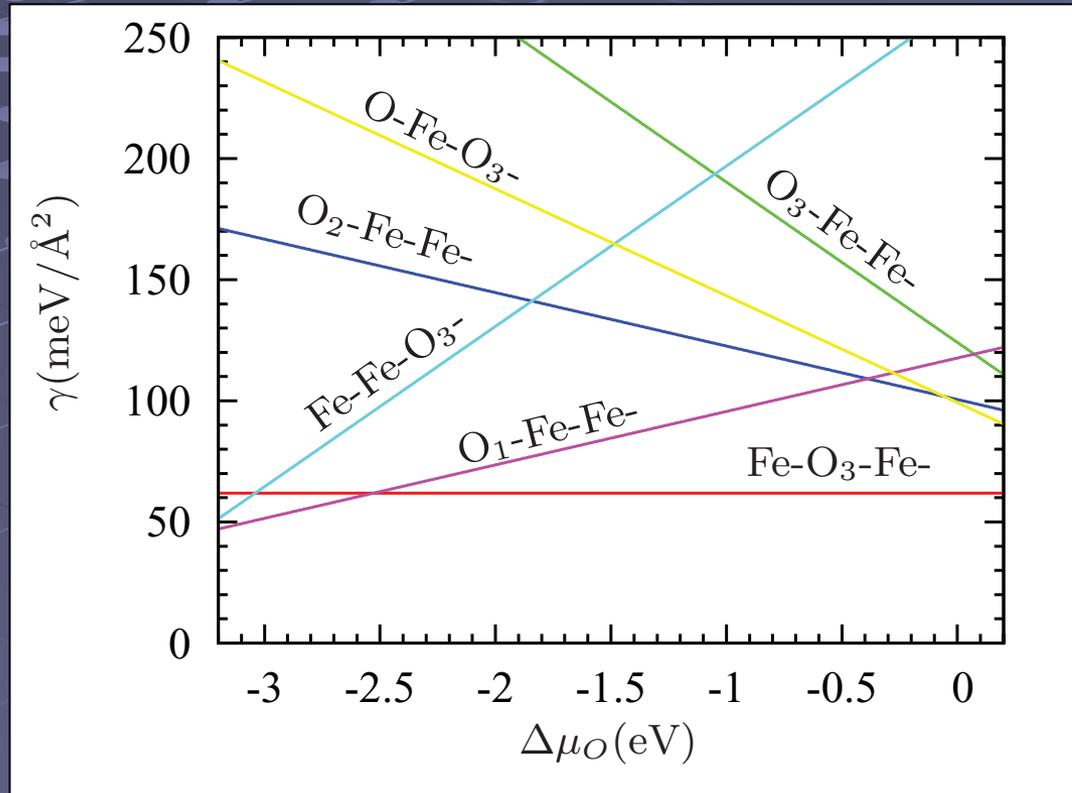
# Thermodynamics of the surface process: 1. Surface termination of hematite $\alpha\text{-Fe}_2\text{O}_3$ (0001)



Many surface terminations are possible

Nguyen, Seriani, Gebauer, J. Chem. Phys. 138, 194709 (2013)

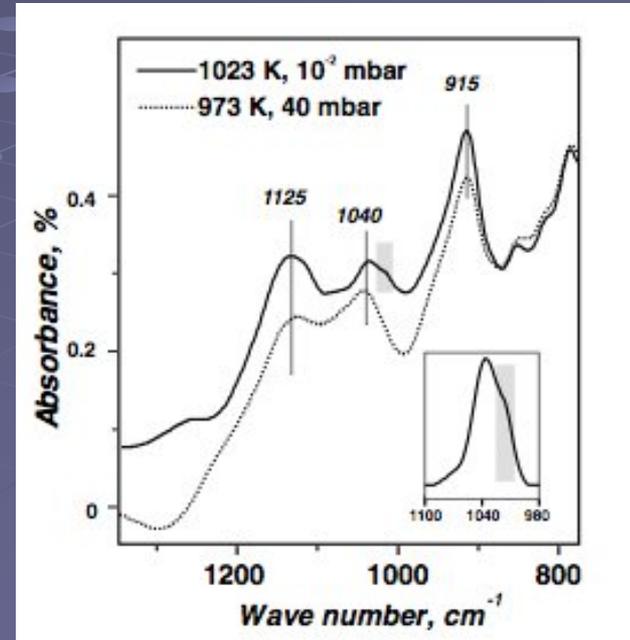
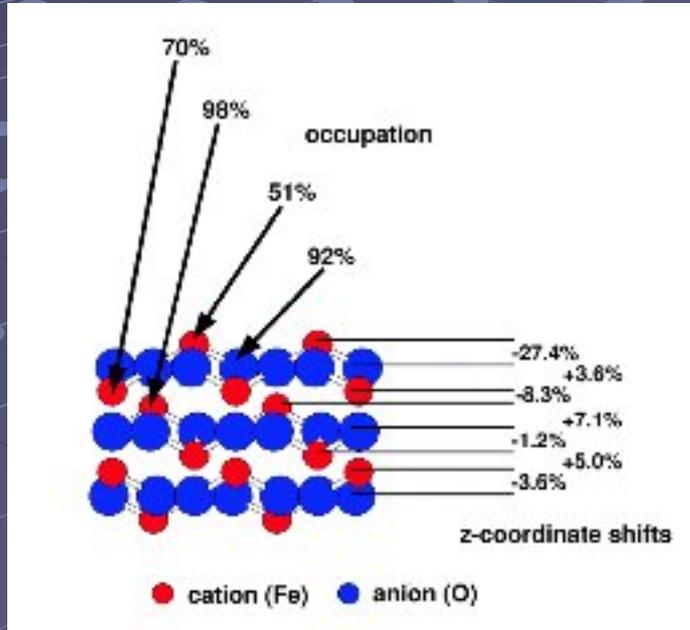
# Terminations of hematite $\alpha\text{-Fe}_2\text{O}_3$ (0001)



Surface free energies as function of the chemical potential of oxygen

Nguyen, Seriani, Gebauer, J. Chem. Phys. 138, 194709 (2013)

# Fe-O<sub>3</sub>-Fe-Fe termination



LEED after annealing in  
 $3 \cdot 10^{-8}$  mbar O<sub>2</sub> at 500° C

Lübbe and Moritz, J. Phys.:  
Condens. Matter 21, 134010 (2009)

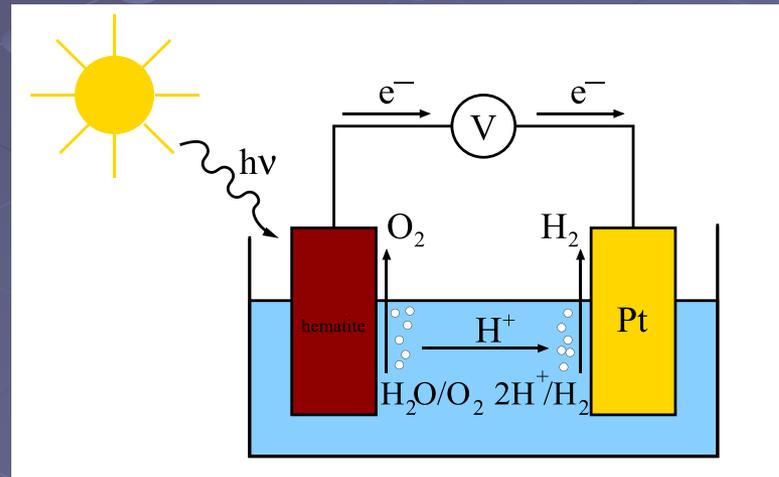
Coexistence with the ferryl  
termination; 10<sup>-3</sup> – 1 mbar O<sub>2</sub> at  
1050 K

Lemire et al., Phys. Rev. Lett. 94,  
166101 (2005)

# Water oxidation at the photoanode



Acidic conditions...



N. Seriani, J. Phys.: Condens. Mat. 29, 463002 (2017)