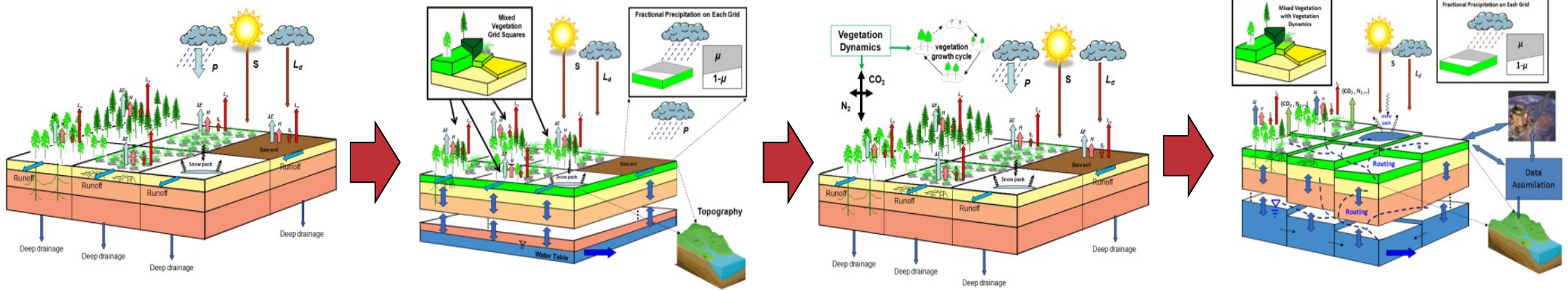


# The use of cosmic-ray neutron sensors in hydrometeorology



Rafael Rosolem

# At the end of this lecture, you should...

- Understand the broader context and motivation of environmental modeling and the links to soil moisture process
- Be familiar with land surface and hydrological models
- Identify potential uses of cosmic-ray neutron sensing observations in combination with models

# A quick recap

# Over the years, the community has learned more about the cosmic-ray neutron sensors

$$\theta_{VOL} = \left[ \frac{\frac{a_0}{N_{pihv}} - a_2 - LW - SOC}{\frac{N_0}{N_0} - a_1} \right] \cdot \rho_{bd}$$

where

$$N_{pihv} = N_{raw} \cdot f_p \cdot f_i \cdot f_h \cdot f_v$$

Based on Franz et al. (2012), Rosolem et al. (2013); and Baatz et al. (2015?)

$\theta_{VOL}$  = volumetric water content ( $\text{m}^3 \text{m}^{-3}$ )

$N_{pihv}$  = fully-corrected measured neutron counting rate (counts per hour)

$N_{raw}$  = raw measured neutron counting rate (counts per hour)

$N_0$  = site-specific calibration parameter

**LW** = lattice water content ( $\text{g g}^{-1}$ )

**SOC** = soil organic carbon ( $\text{g g}^{-1}$ )

$\rho_{bd}$  = dry soil bulk density ( $\text{g cm}^{-3}$ )

$f_p$  = atmospheric pressure correction factor (-)

$f_i$  = solar intensity correction factor (-)

$f_h$  = atmospheric water vapor correction factor (-)

$f_v$  = aboveground biomass correction factor (-)

$a_0, a_1, a_2$  = fixed coefficients (-)

# The cosmic-ray neutron sensor signal is affected by all sources of hydrogen within its support volume

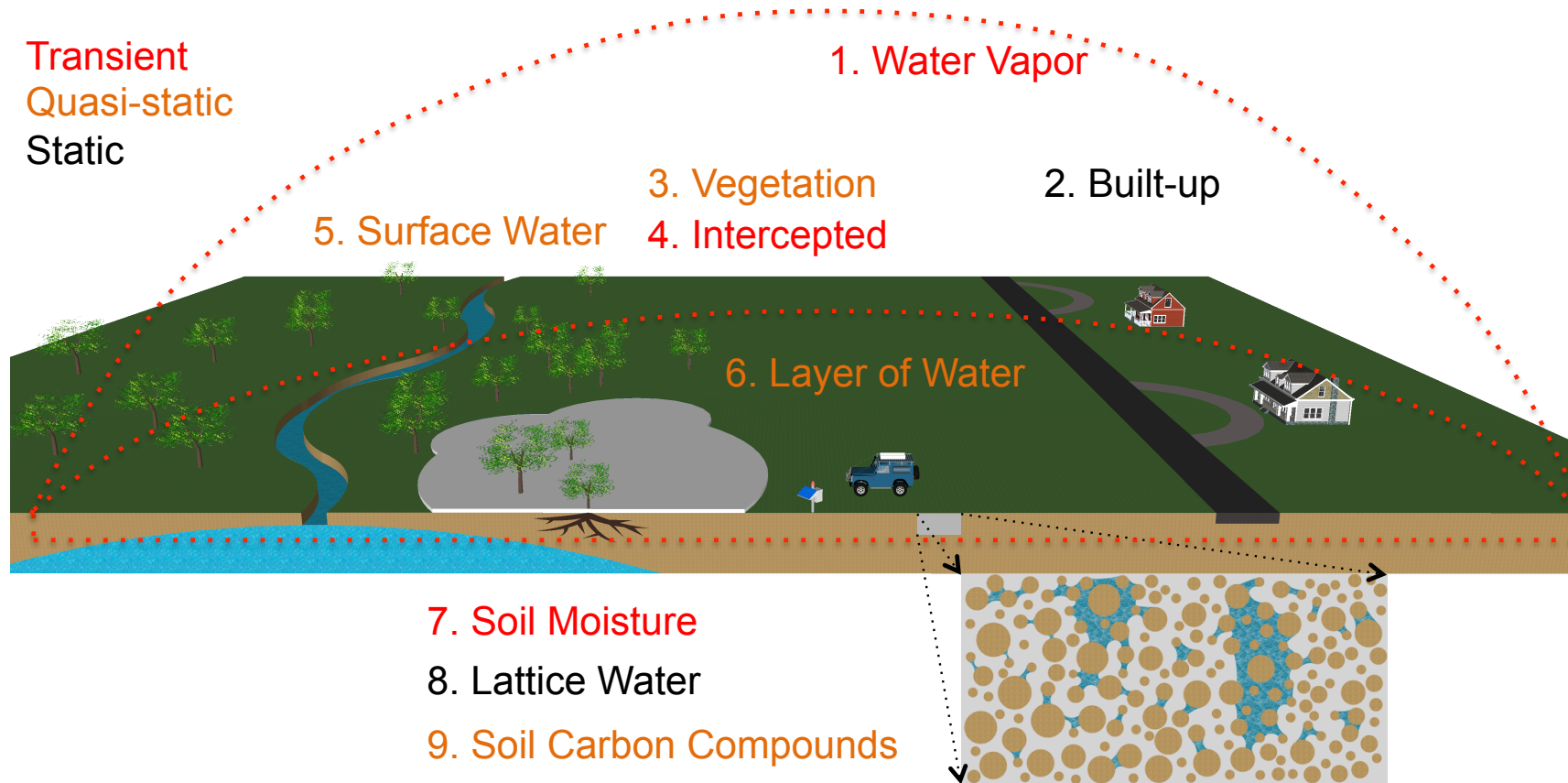
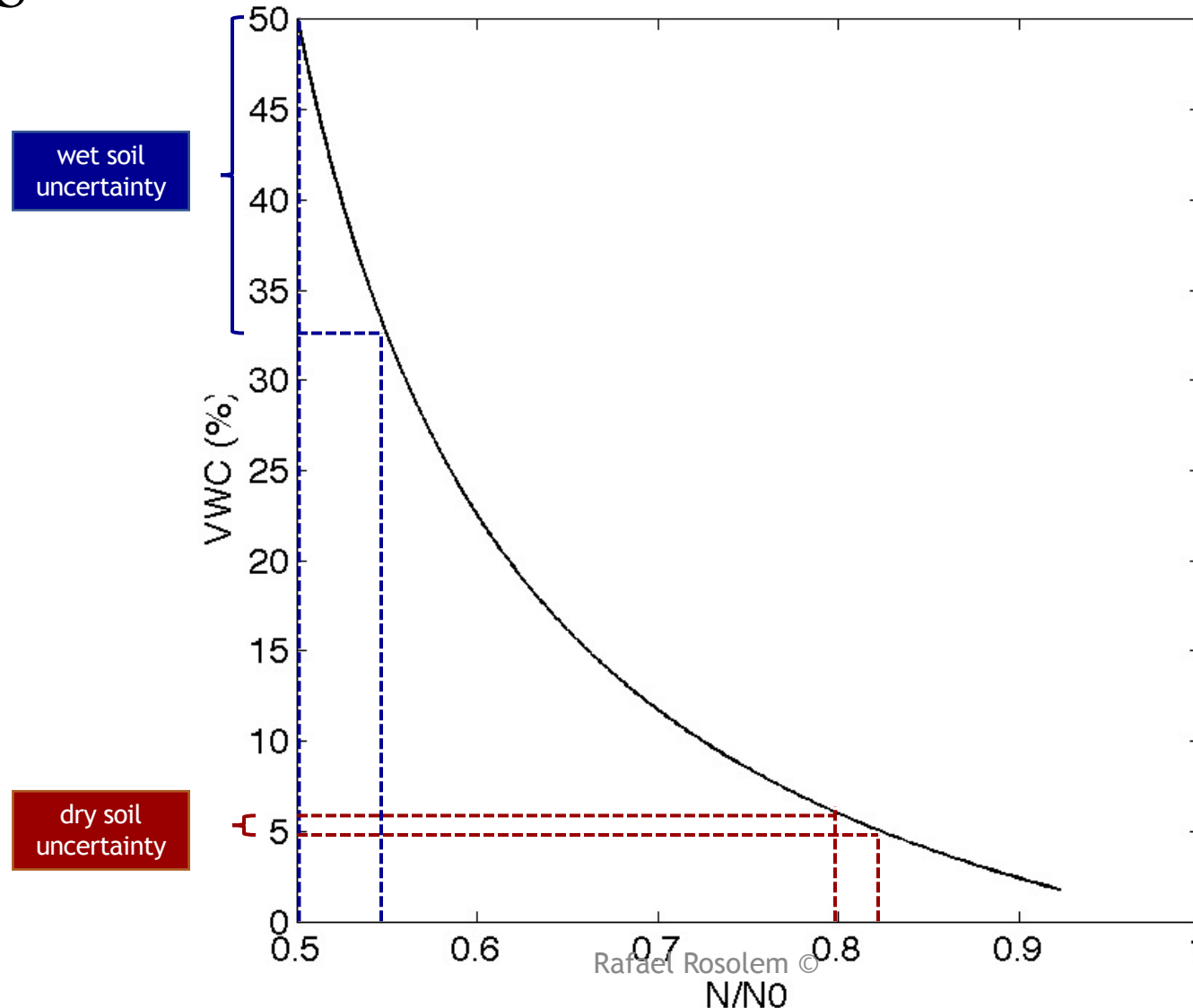


Image kindly provided by Trenton Franz (Nebraska-Lincoln)

# Propagation of uncertainty: dry versus humid regions



In a humid region:

Uncertainty of neutron counts on the order of 5%

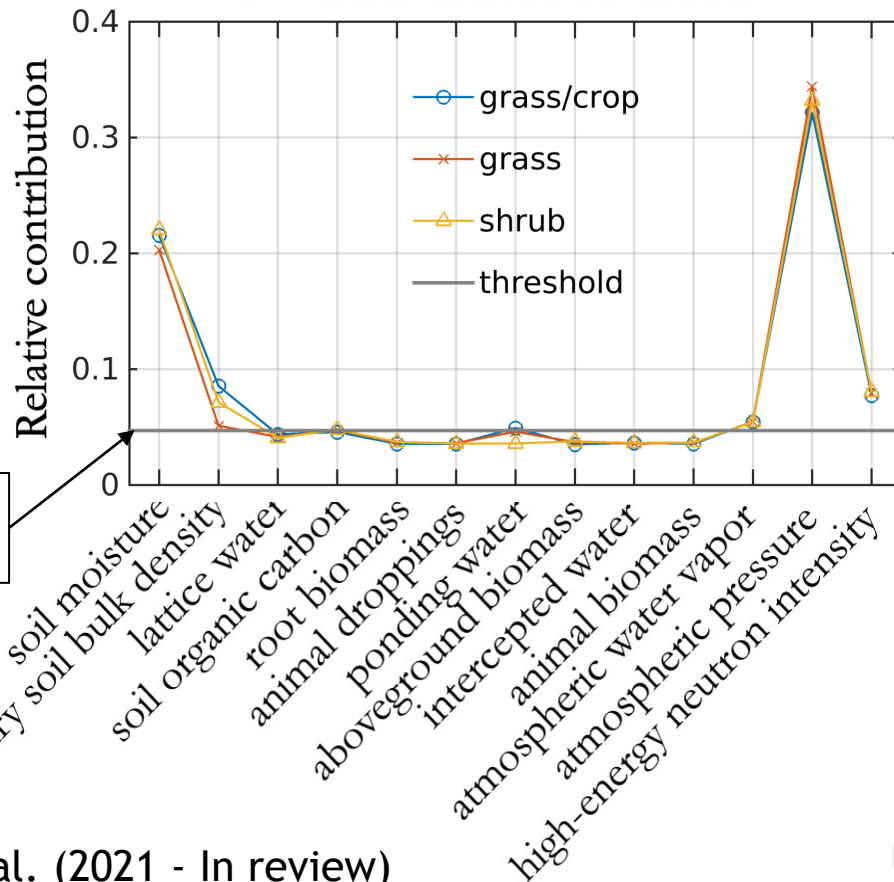
Do you know why?

Propagated uncertainty of soil moisture on the order of 17% vol.

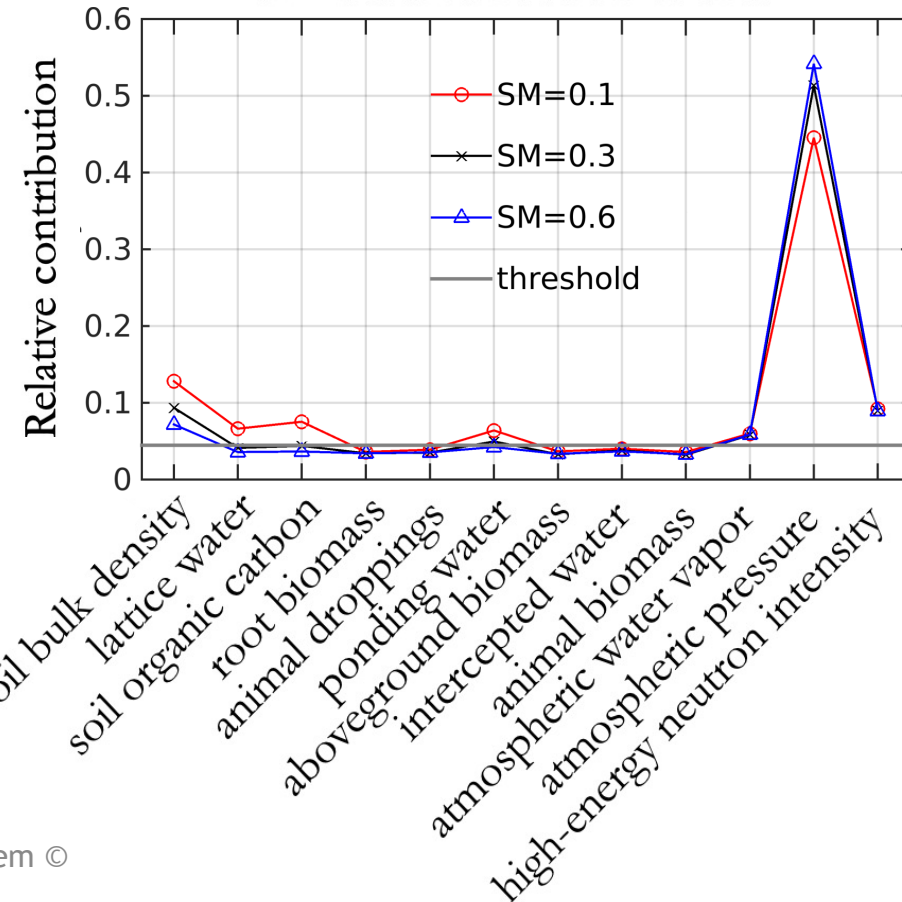
Can you understand why?

# How does each factor influence the neutron signal?

Relative contribution to sensitivity of measured neutron counts



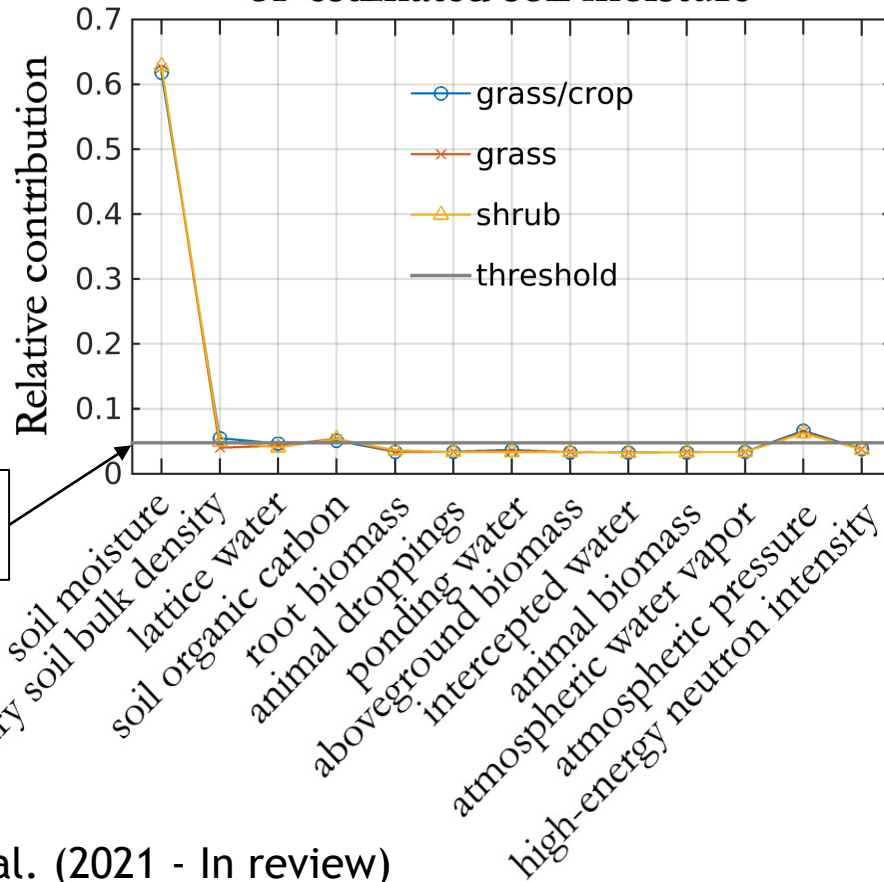
Relative contribution to sensitivity of measured neutron counts



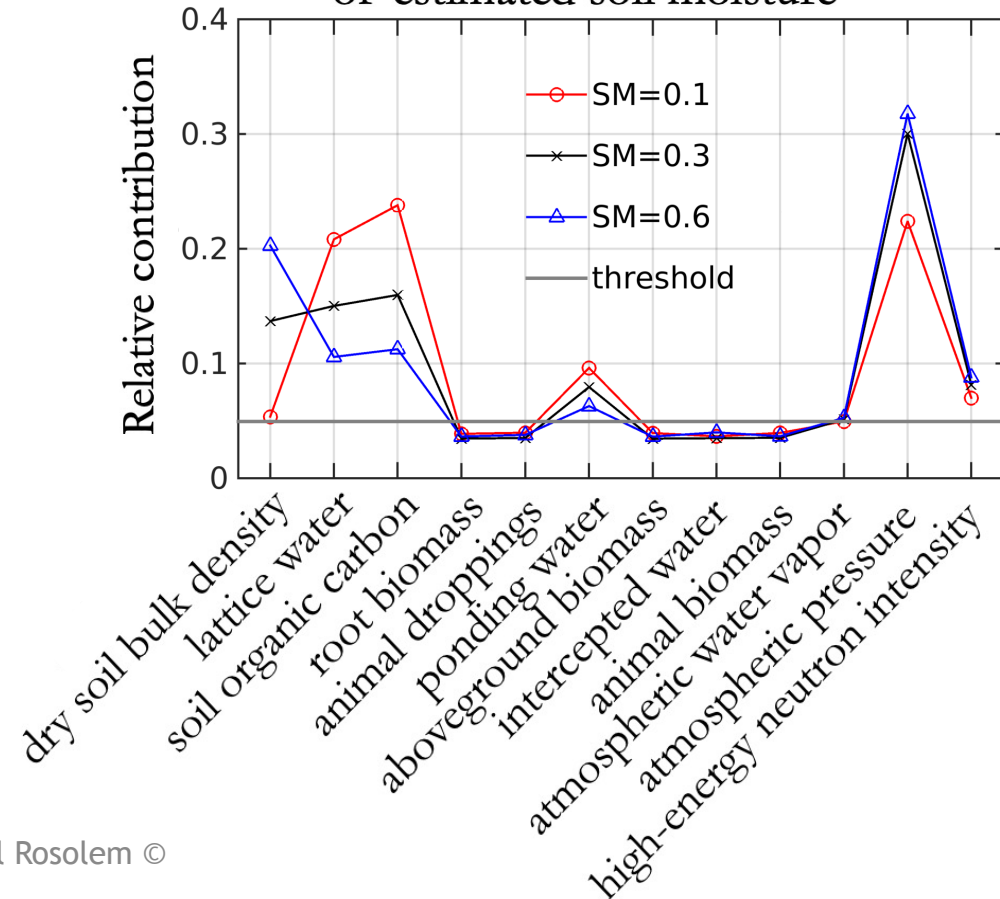
dummy factor threshold

# How is that propagated to the derived soil moisture estimation?

Relative contribution to sensitivity of estimated soil moisture



Relative contribution to sensitivity of estimated soil moisture





**COSMOS-UK**  
UK Soil Moisture Monitoring Network

**TERENO**  
TERRESTRIAL ENVIRONMENTAL OBSERVATORIES

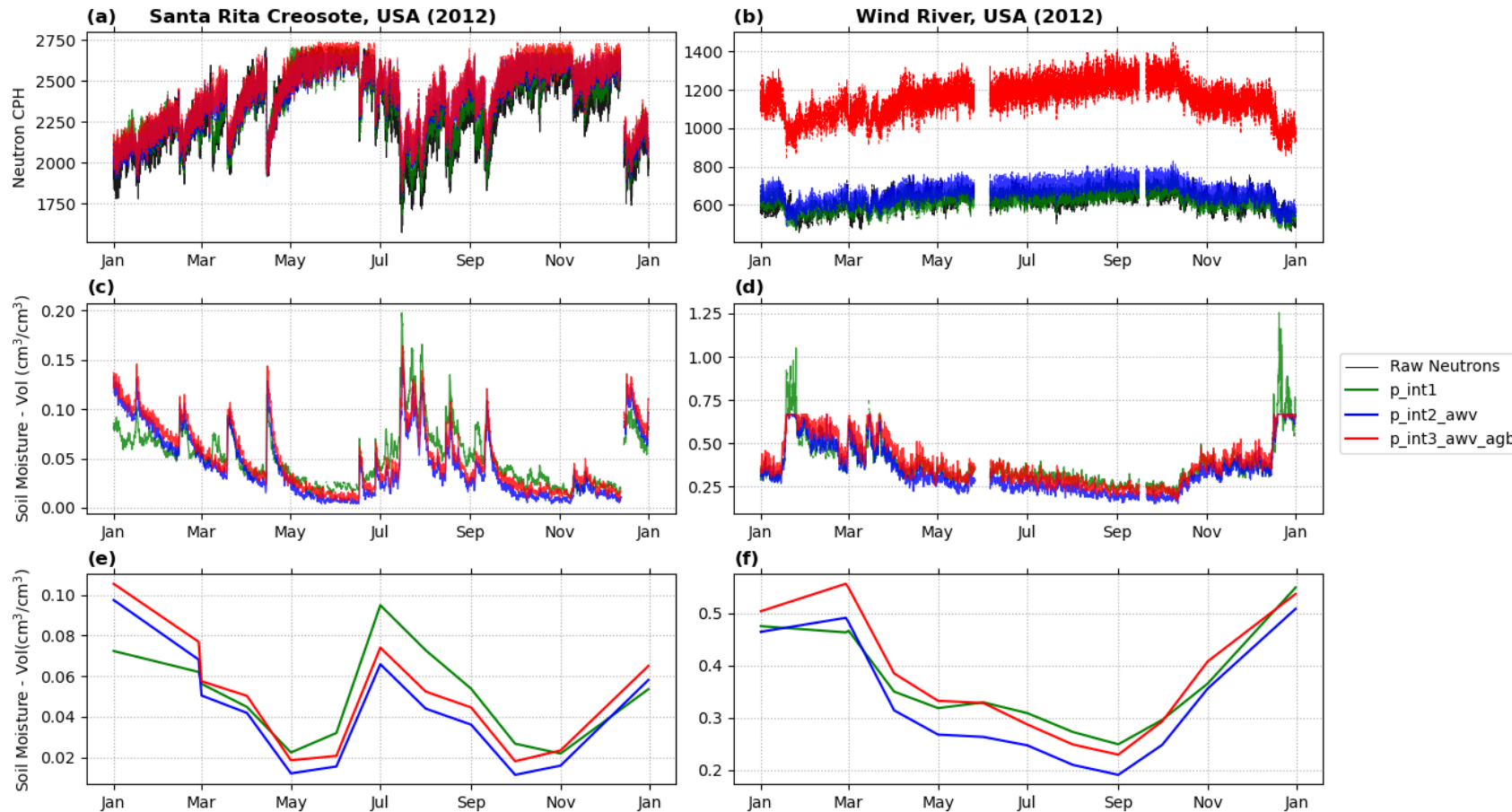


**COSMOS**  
Cosmic-ray Soil Moisture Observing System



**CosmOz**

# Different data processing procedures can lead to different estimates of soil moisture



# We have developed 'crspy': a comprehensive data processing tool for cosmic-ray sensor

<https://github.com/danpower101/crspy>

master 1 branch 1 tag [Go to file](#) [Add file](#) [Code](#)

danpower101 Added refs		
		a223362 2 days ago 87 commits
crspy	Added refs	2 days ago
data	Added alternative intensity correction.	5 months ago
example	delete duplicate file to avoid confusion	last month
.gitignore	adding gitignore	3 months ago
LICENSE	Create LICENSE	4 months ago
README.md	Update README.md	2 months ago
name_list.py	change to name_list default	last month
run_crspy_workthrough.ipynb	Added notebook workthrough (mk2)	2 months ago
setup.py	Changes to n0 calib	26 days ago

README.md

## Cosmic-Ray Sensor PYthon tool (crspy)

This tool can process Cosmic Ray Sensor data into soil moisture estimates. It is based on research conducted by many individuals and groups (see references).

Please note: this is a work in progress that is being updated regularly, so bugs or issues may be found. If you have any issues with crspy please do get in touch [daniel.power@bristol.ac.uk](mailto:daniel.power@bristol.ac.uk)

python v3.7+ contributions welcome license LGPL-3.0

<https://doi.org/10.5194/gmd-2021-77>  
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[Abstract](#) [Discussion](#) [Metrics](#)

Submitted as: model description paper

07 May 2021

Review status: this preprint is currently under review for the journal GMD.

## Cosmic-Ray neutron Sensor PYthon tool (crspy): An open-source tool for the processing of cosmic-ray neutron and soil moisture data

Daniel Power<sup>1</sup>, Miguel Angel Rico-Ramirez<sup>1</sup>, Sharon Desilets<sup>2</sup>, Darin Desilets<sup>2</sup>, and Rafael Rosolem<sup>1,3</sup>

<sup>1</sup>Faculty of Engineering, University of Bristol, Bristol, UK

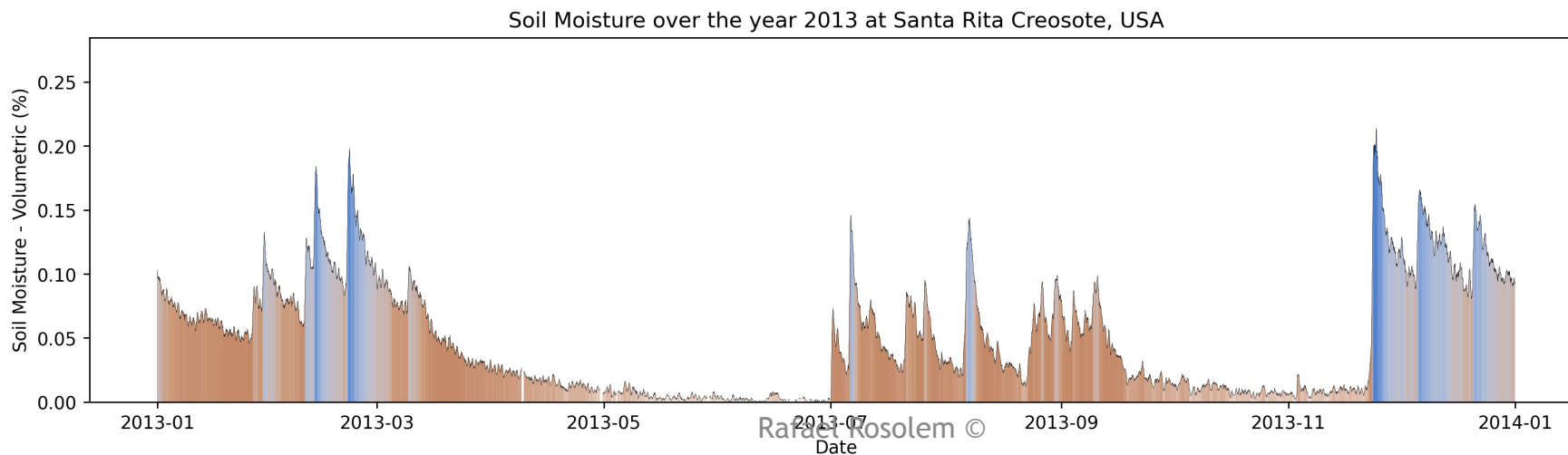
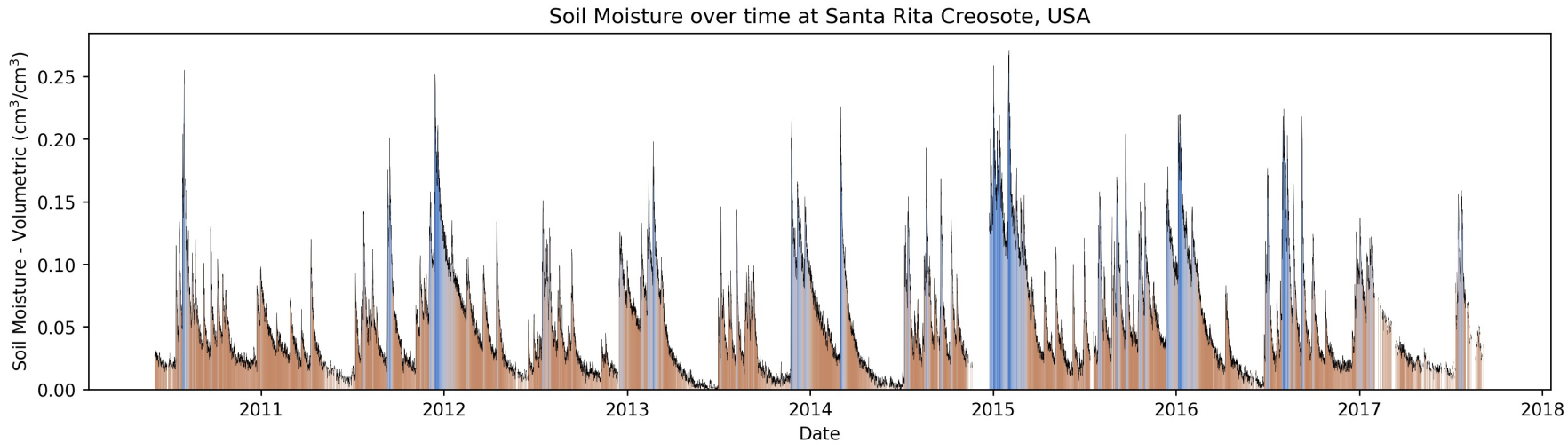
<sup>2</sup>Hydroinnova, Albuquerque, New Mexico, USA

<sup>3</sup>Cabot Institute for the Environment, University of Bristol, Bristol, UK

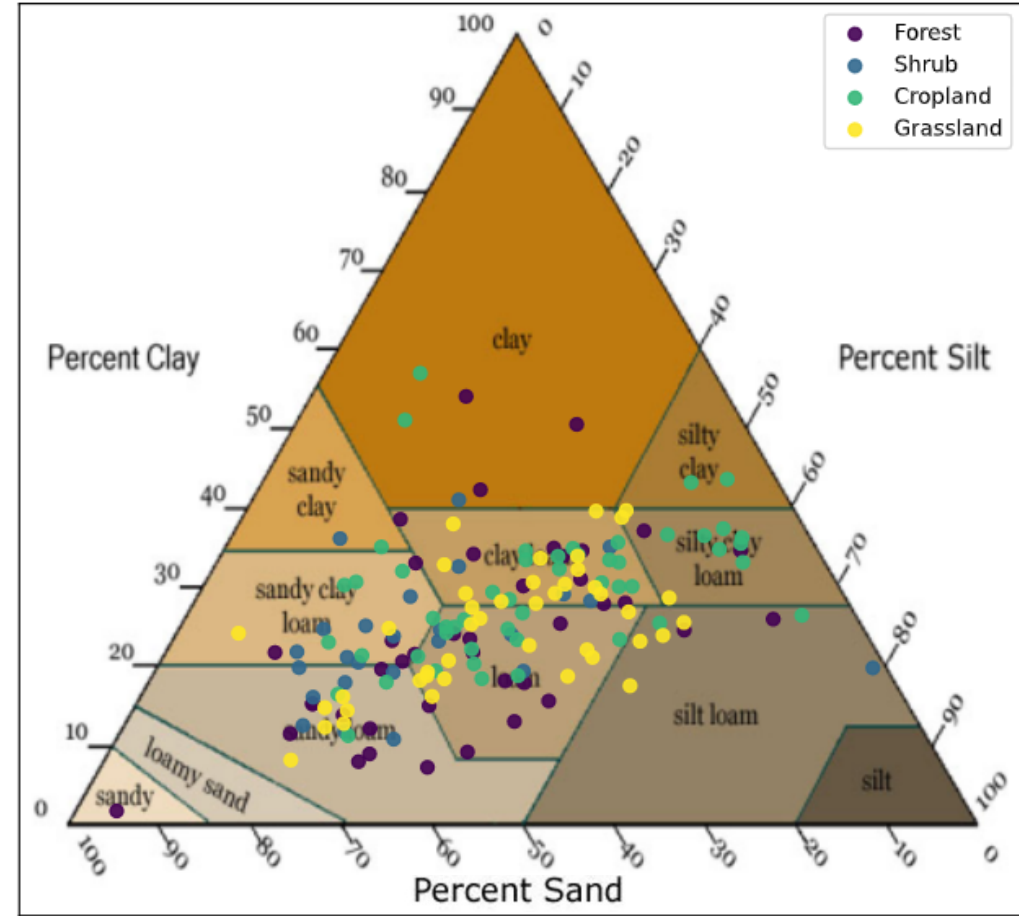
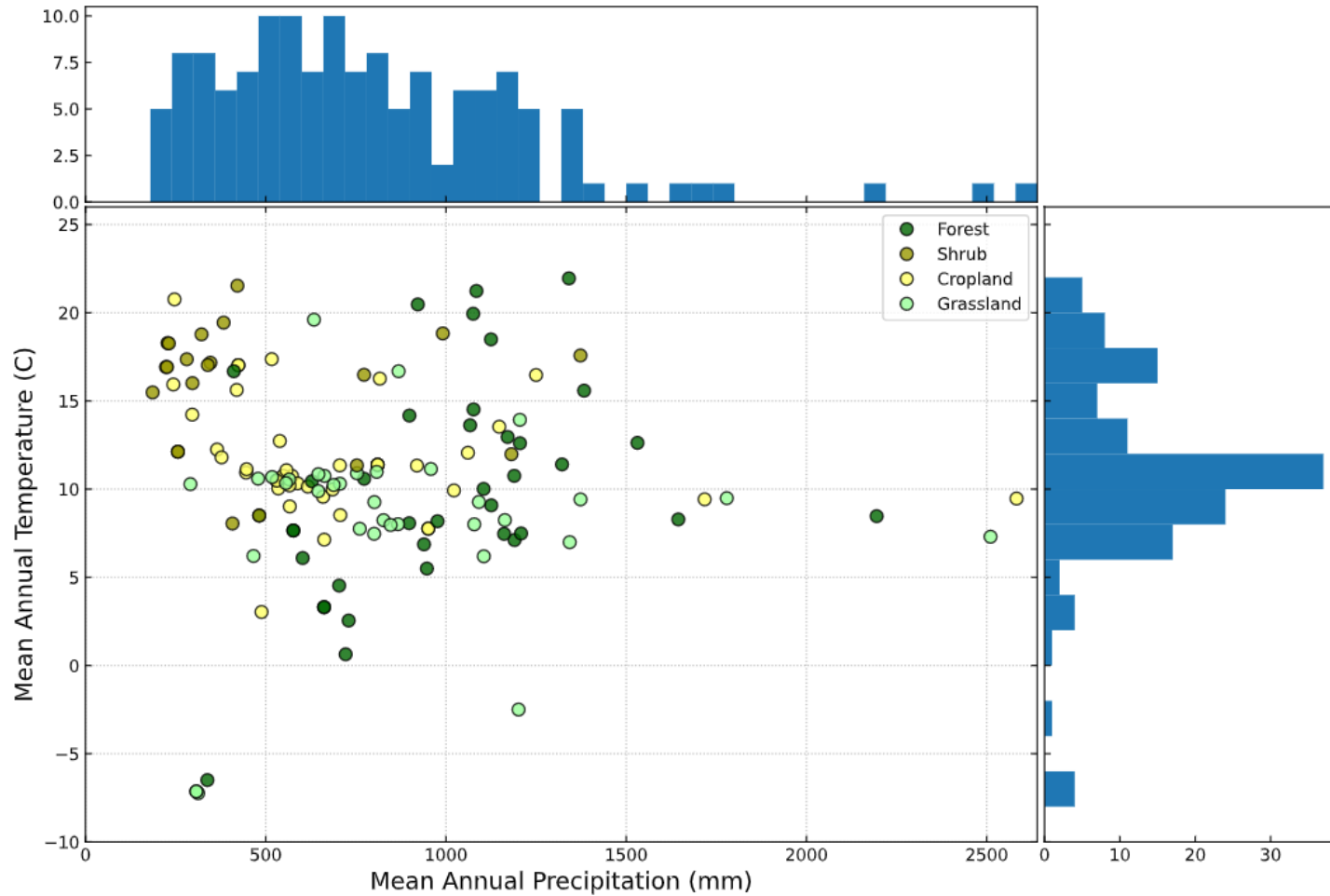
Received: 12 Mar 2021 – Accepted for review: 05 May 2021 – Discussion started: 07 May 2021

Power et al. 2020 (GMDD)

# crspy generates soil moisture analysis for easy checks

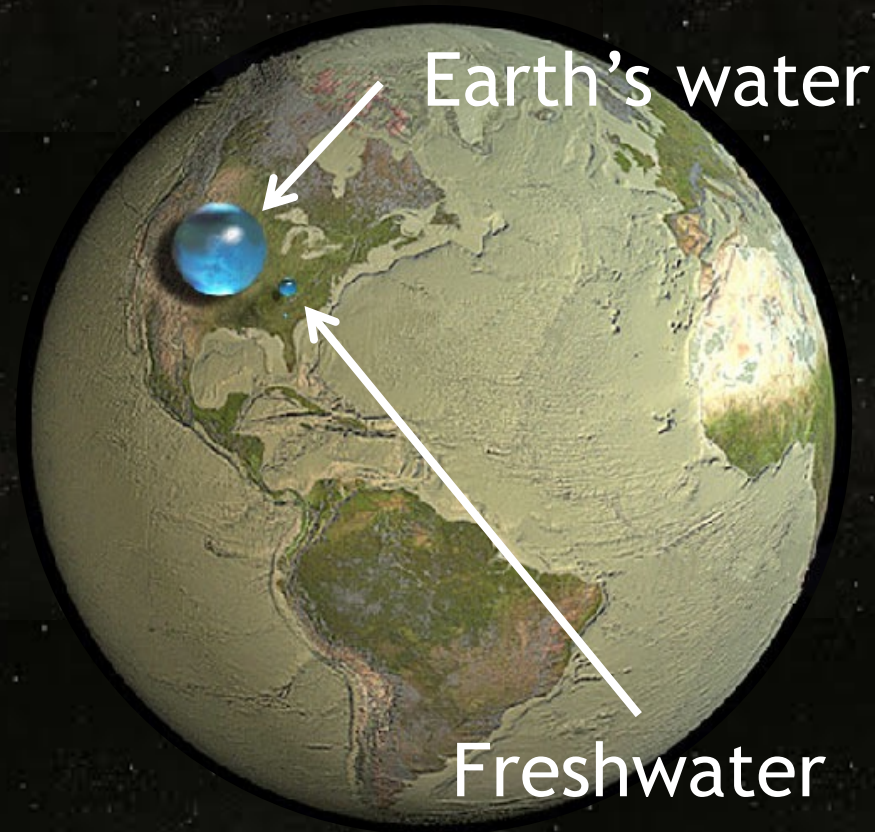


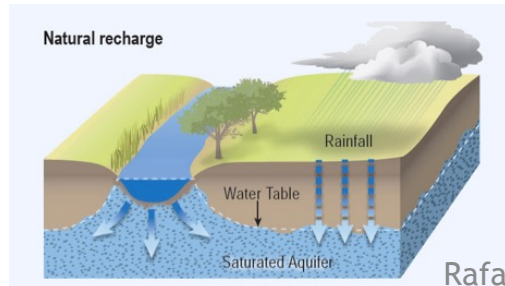
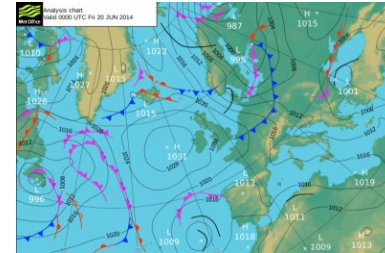
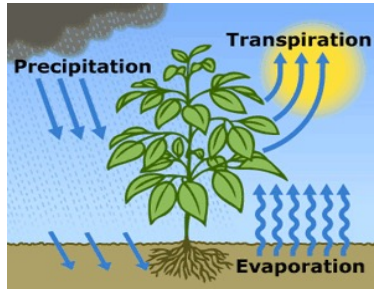
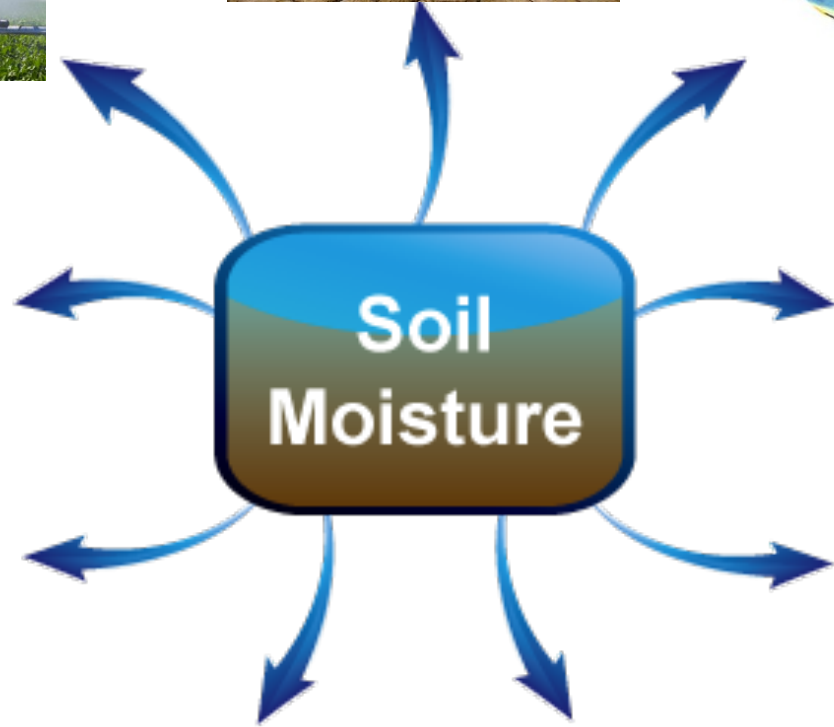
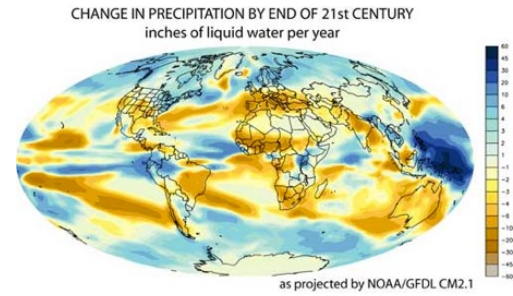
# New harmonization tool crspy



# Hydrology context for environmental models

Soil moisture represents only a tiny fraction of the available freshwater on Earth (about 3.5%)

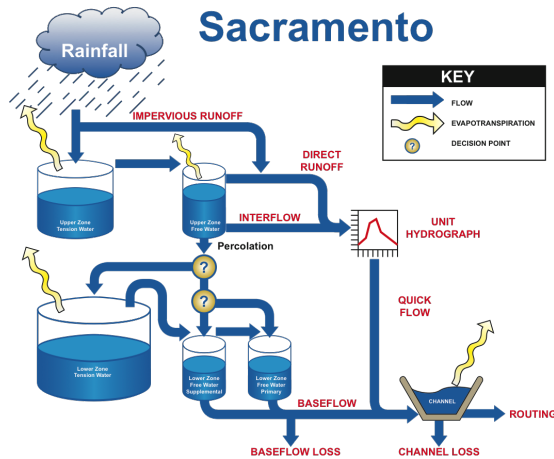
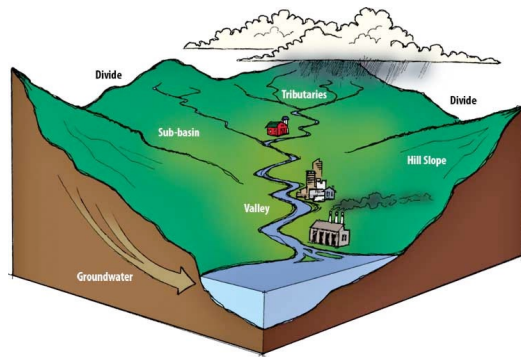






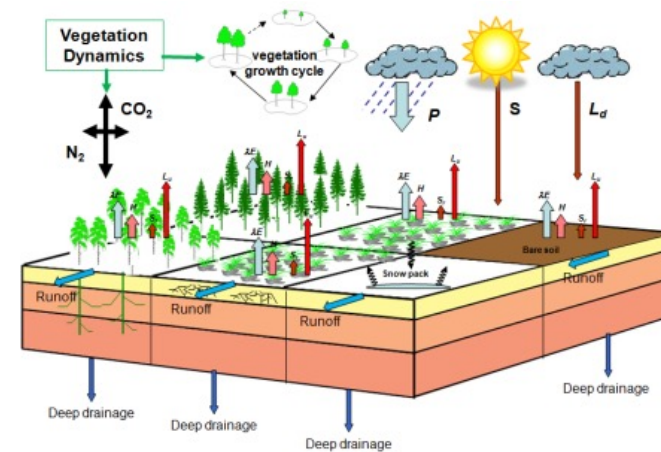
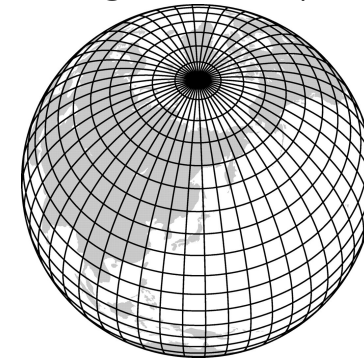
# In the past, hydrological and land surface models had focused on different spatial scales

## Hydrological Model



Conceptual lumped response  
 Dependent on calibration  
 Catchment scale

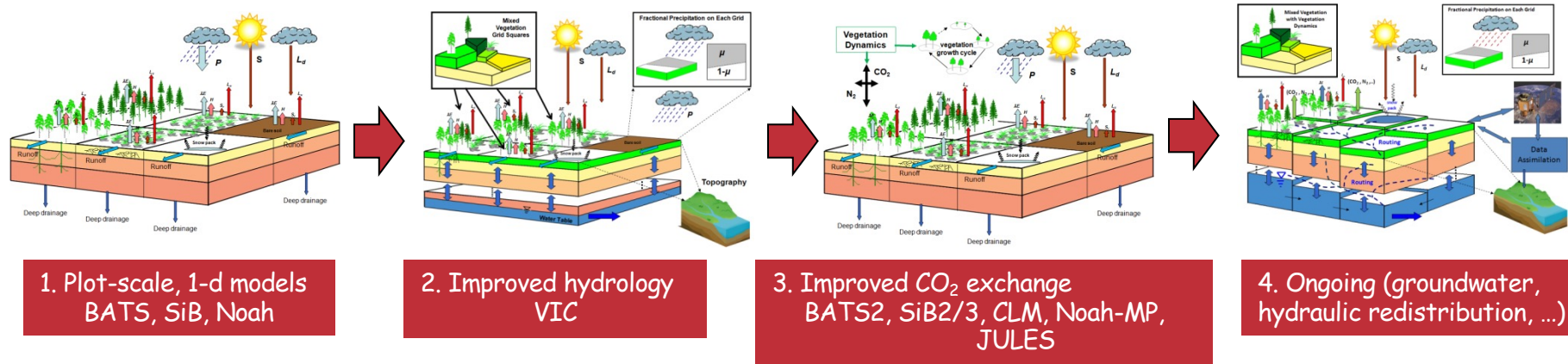
## Land Surface Model



Physics-based  
 Look up tables vs. calibration  
 Larger grid domain

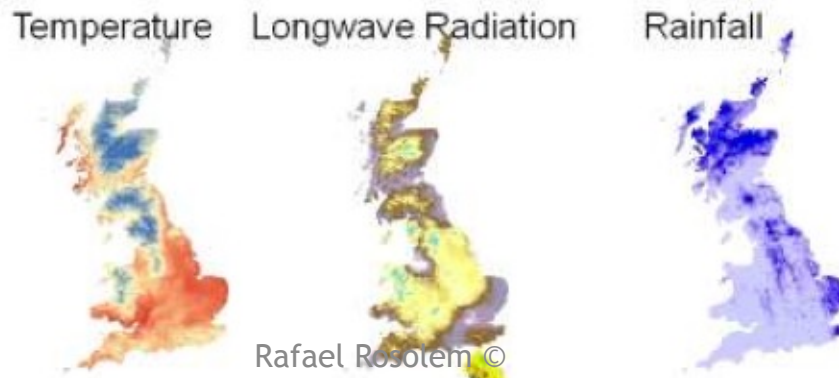
# Hydrological and land surface models have converged to “hyper-resolution” at sub-kilometer scales supported by new datasets

## Further improvement in the realism of hydrometeorological models



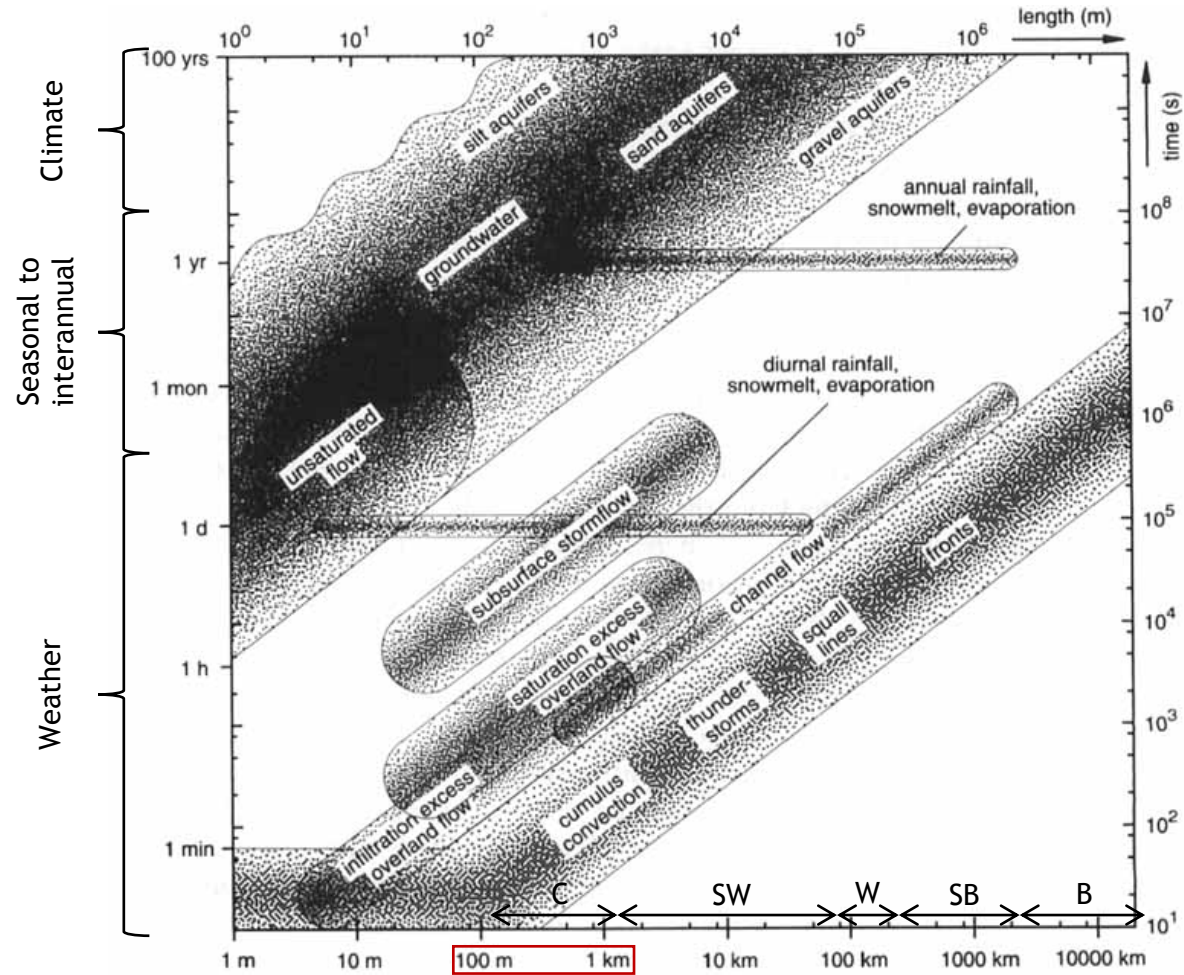
## Model grid resolution of regional and global models has increased hugely

Climate Hydrology Ecology  
Support System (CHESS)

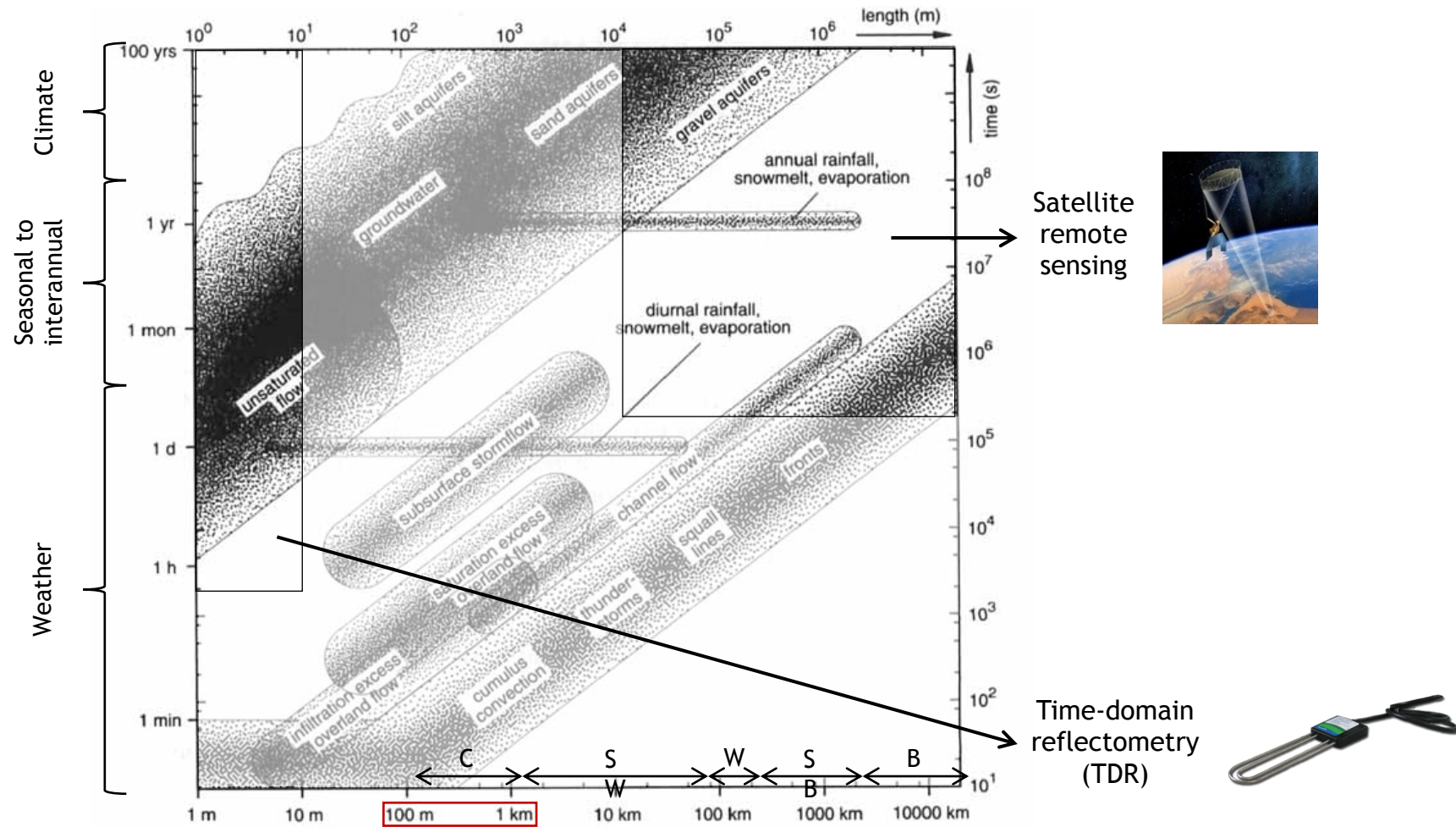


Rafael Rosolem ©

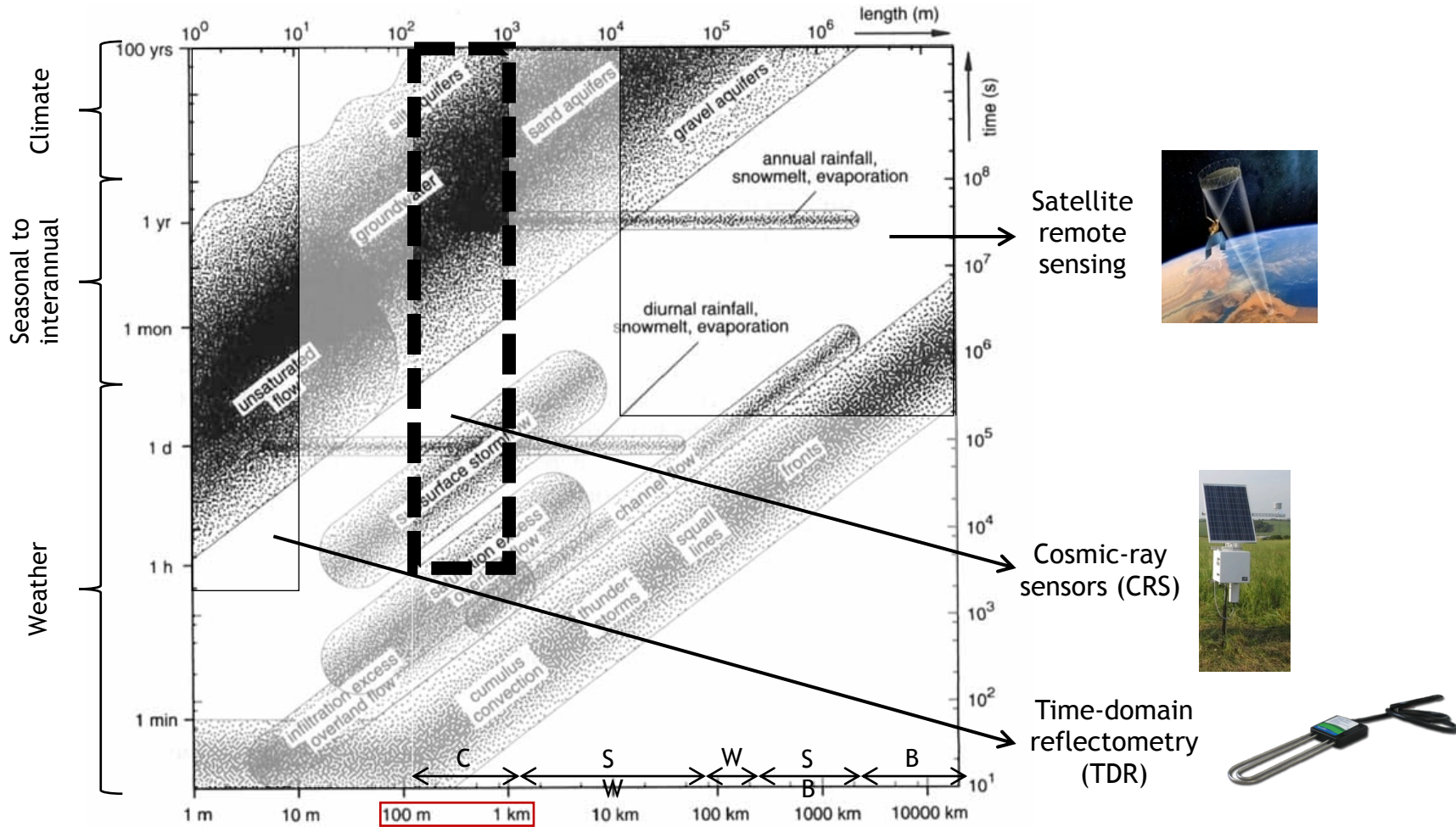
# Soil moisture across spatiotemporal scales



# Soil moisture across spatiotemporal scales



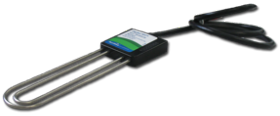
# Cosmic-ray sensors fills the gap between traditional methods



Satellite remote sensing



Cosmic-ray sensors (CRS)

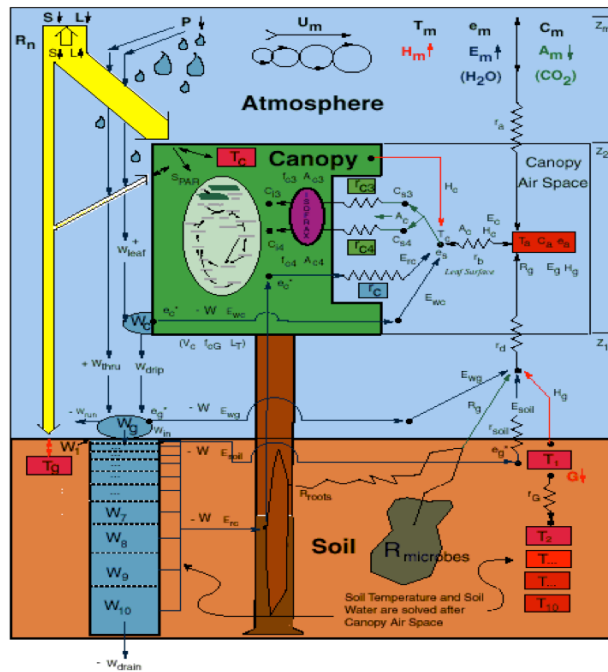


Time-domain reflectometry (TDR)

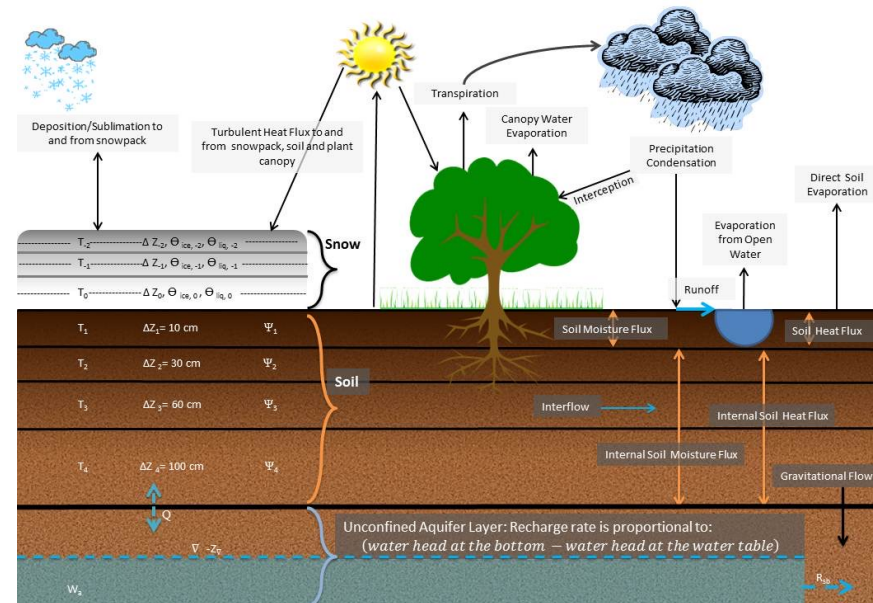
# Example of applications using land surface models

# Example applications with land surface models

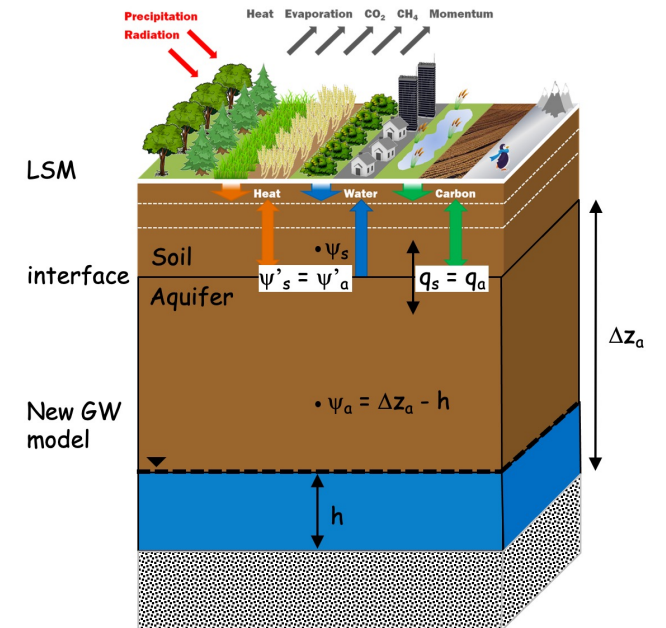
Simple Biosphere Model



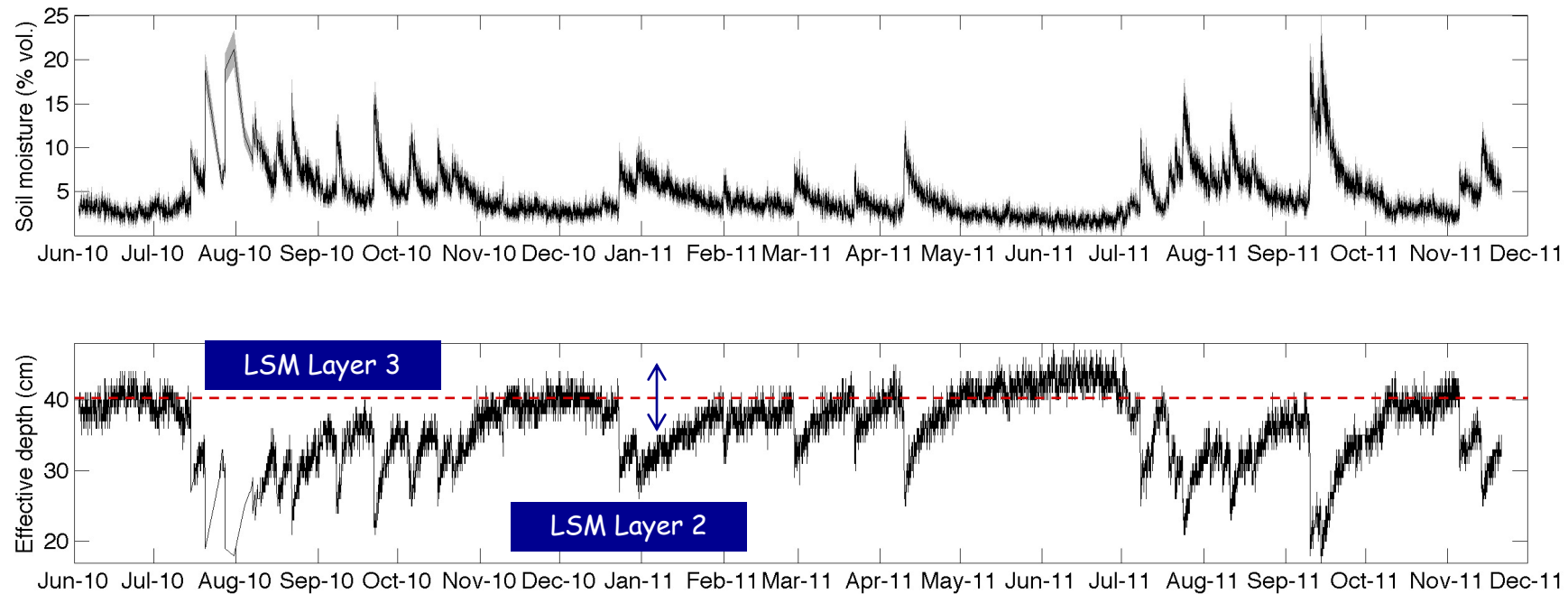
NOAH model



Joint UK Land Environment Model



# Soil layers in models poses challenges when combining with cosmic-ray neutron sensors



Integrated soil moisture from cosmic-ray sensors can reach multiple soil layers in land models!!!

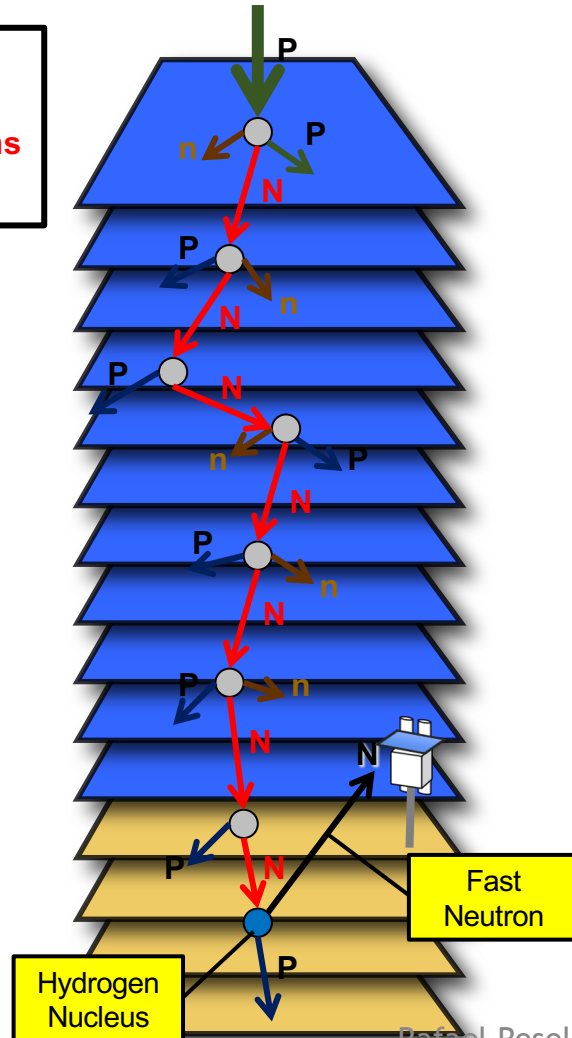


# Incoming Cosmic-rays

P - protons  
n - air or soil nuclei  
N - high energy neutrons  
N - fast neutrons

Air

Soil

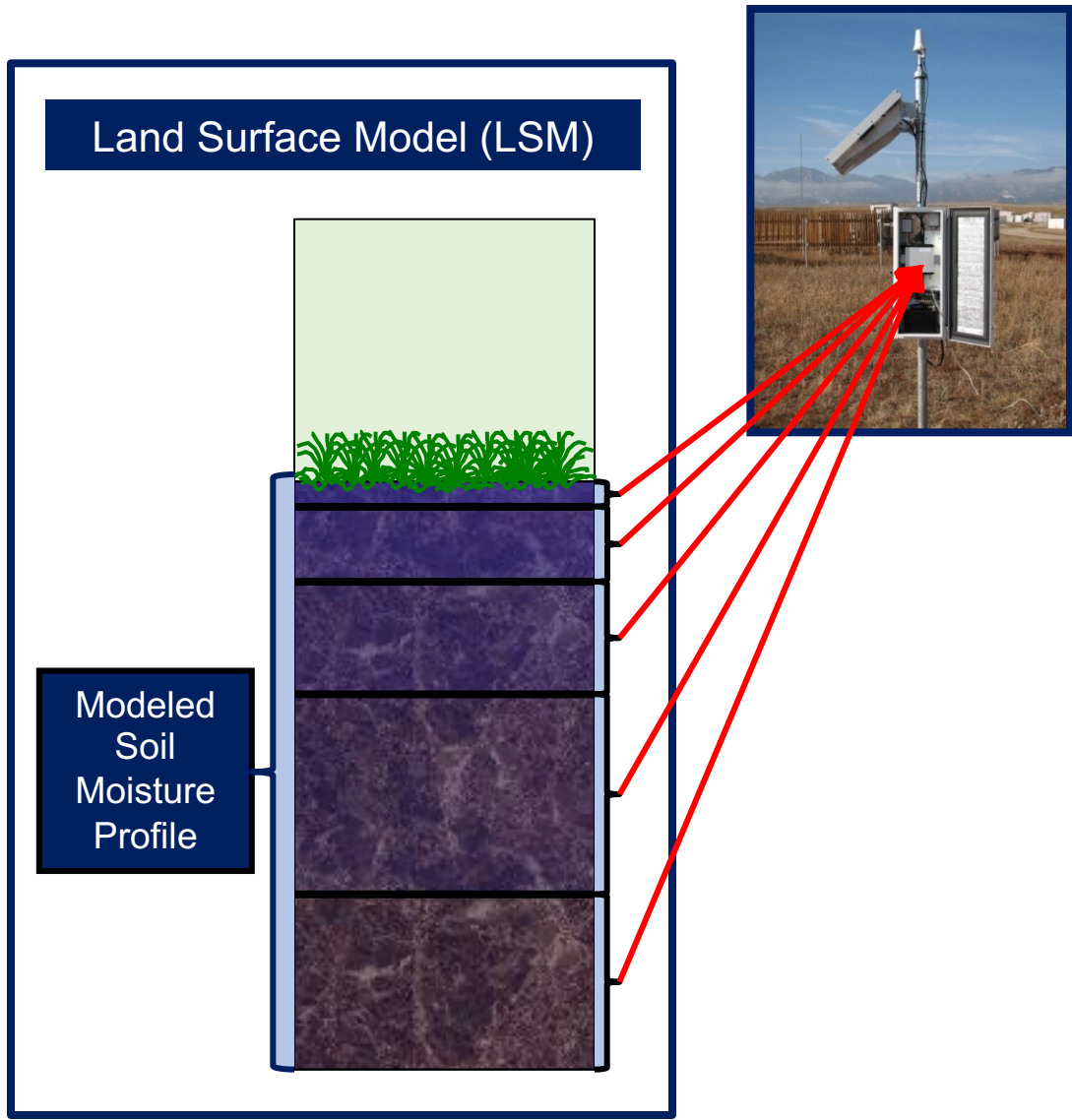


## The *Monte Carlo N-Particle eXtended* (MCNPX) model

(created to design nuclear bombs!)

- requires specified chemistry for the atmosphere and soil, including hydrogen.
- uses measured nuclear collision cross sections for all constituents
- tracks the life history of randomly selected, individual cosmic rays and their collision products
- counts the “fast neutrons” (~1 MeV) that pass through the detector volume of the COSMOS probe

But it is too computationally demanding

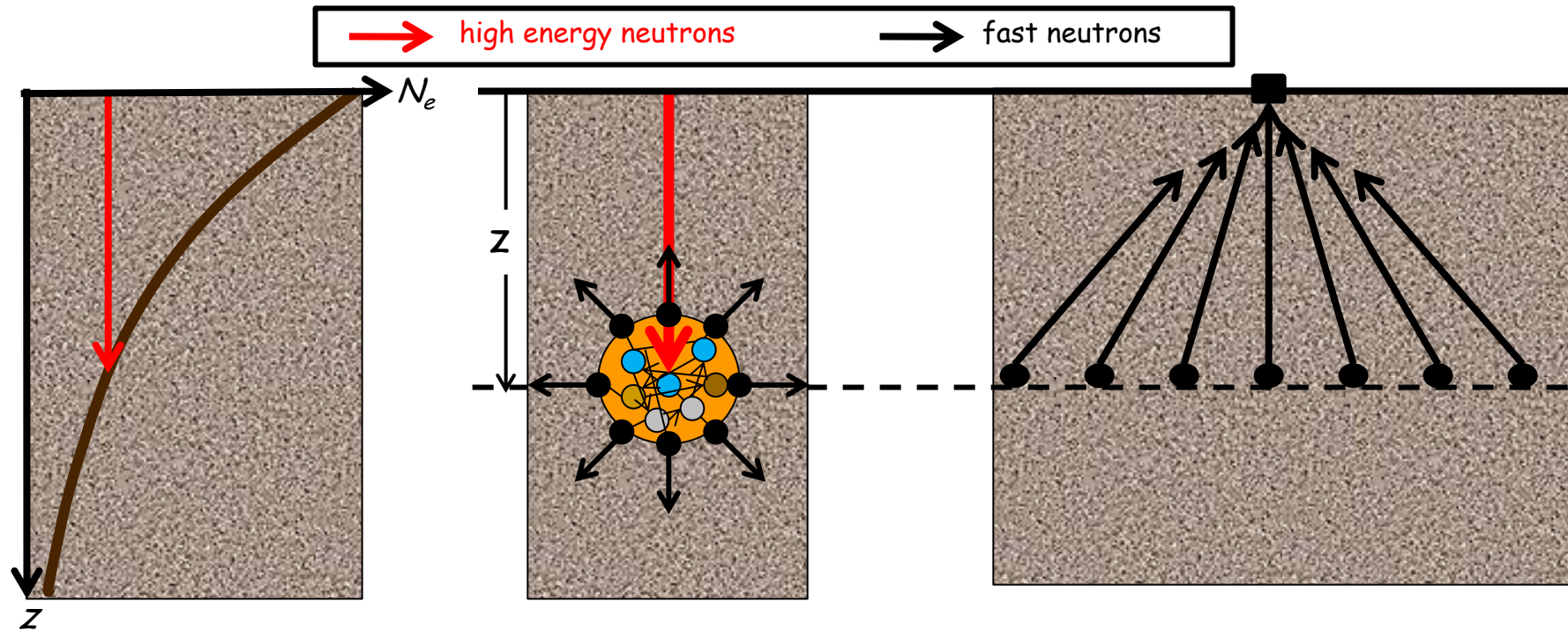


We developed the COsmic-ray Soil Moisture Interaction Code (COSMIC) to resolve the issues with multi-layers in land surface models

COSMIC translates model-derived soil moisture profiles into an equivalent neutron count which can be compared directly with the measurement from cosmic-ray sensors

This reduces the uncertainty in the process and eventual propagation of errors

# COSMIC captures essential below-ground physics in parametric form



Exponential reduction in the number of high energy neutrons with depth

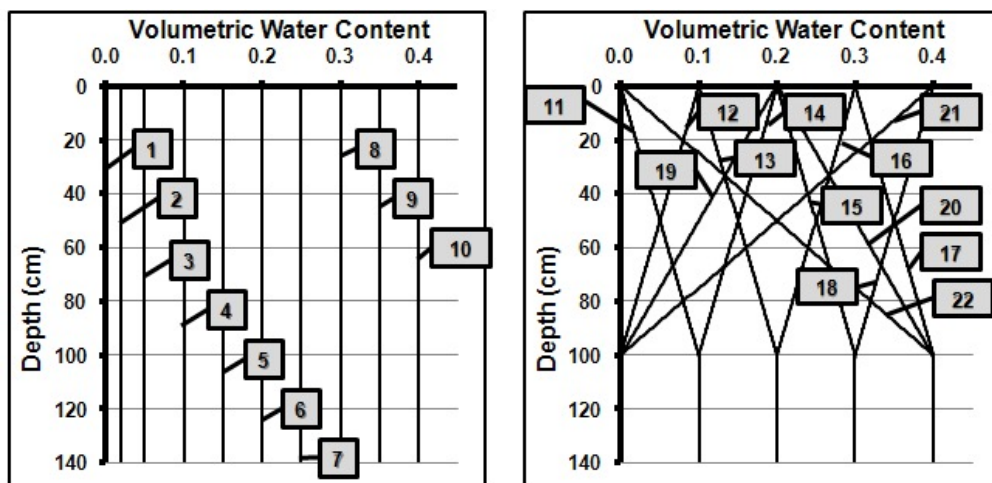
Isotropic creation of fast neutrons from high energy neutrons at level "z"

Exponential reduction in the number of the fast neutrons created at level "z" before their surface measurement

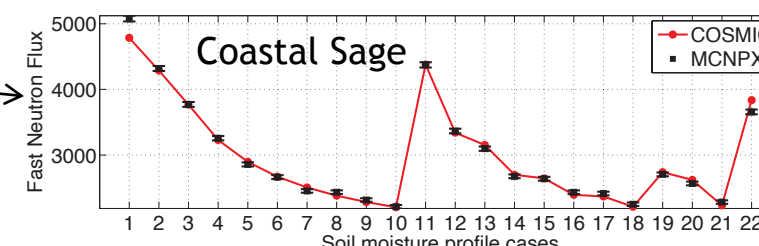
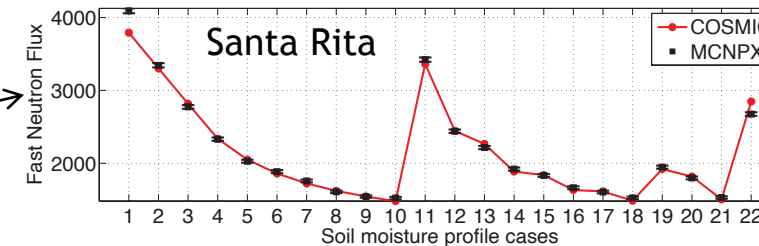
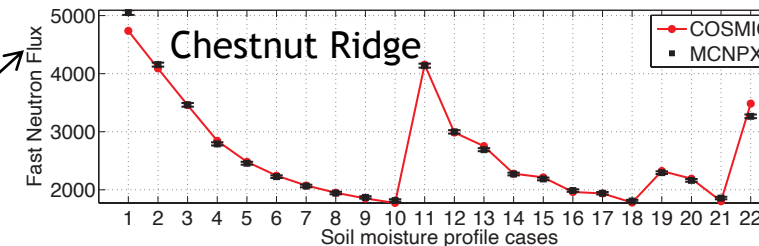
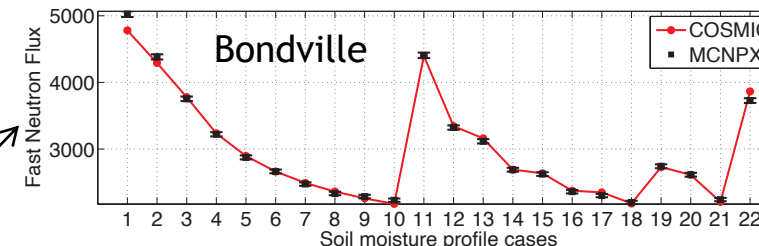
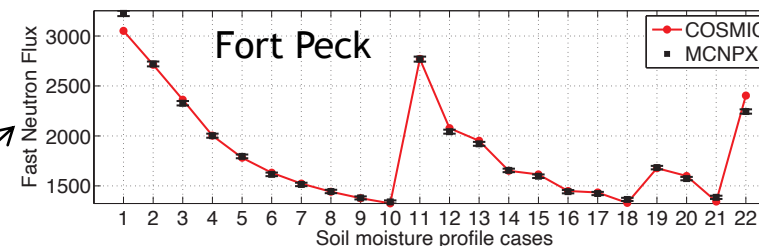
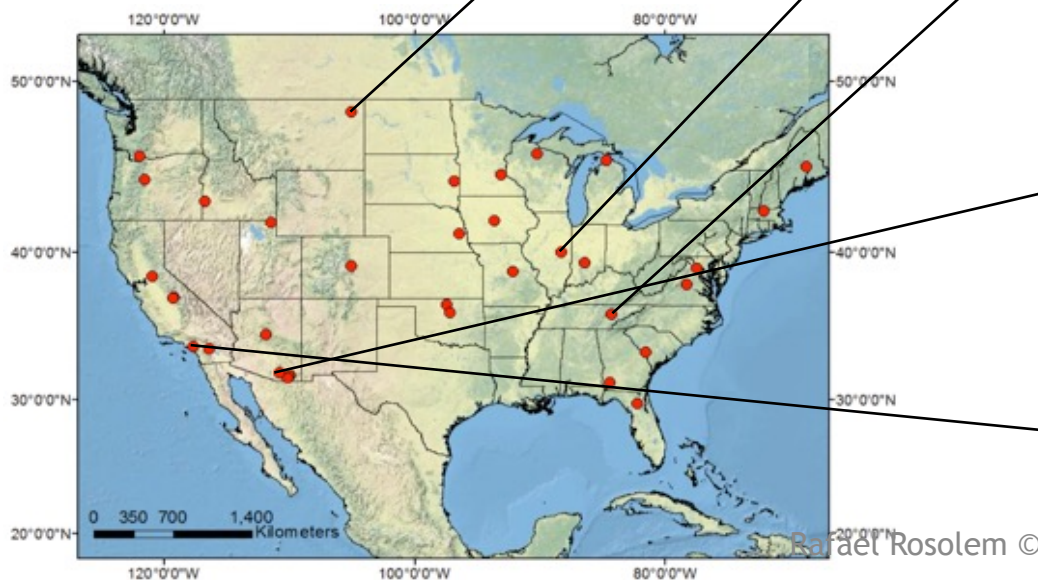
$$N_{\text{COSMOS}} = N \int_0^{\infty} \left[ \exp\left(-\left[\frac{m_s(z)}{L_1} + \frac{m_w(z)}{L_2}\right]\right) \cdot \left[\alpha \rho_s(z) + \rho_w(z)\right] \cdot \left(\frac{2}{\pi}\right)^{\pi/2} \int_0^{\pi/2} \exp\left(\frac{-1}{\cos(\theta)} \left[\frac{m_s(z)}{L_3} + \frac{m_w(z)}{L_4}\right]\right) \cdot d\theta \right] \cdot dz$$

# Initial COSMIC calibration against MCNPx at 42 sites using synthetic soil moisture profiles

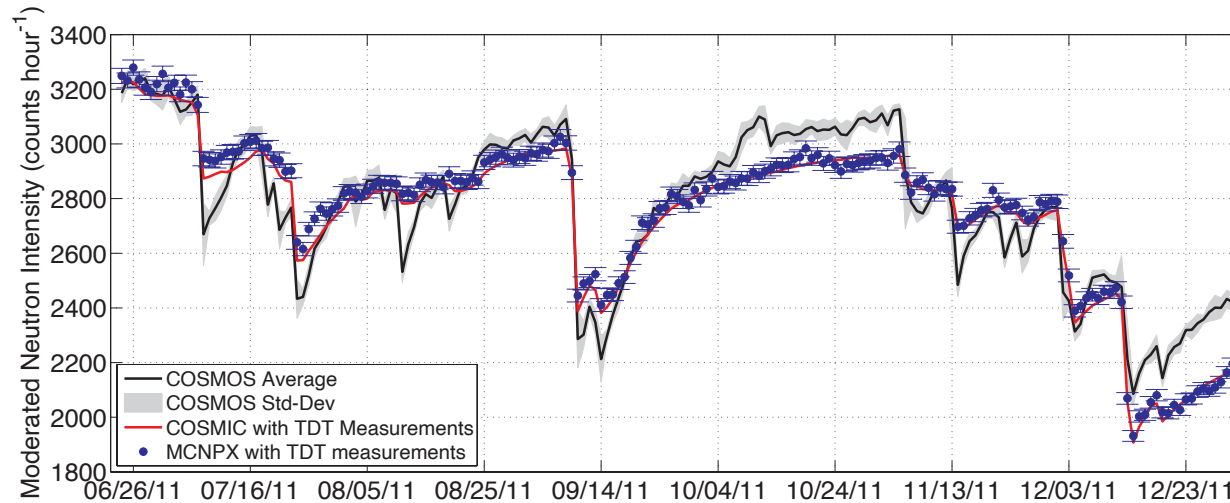
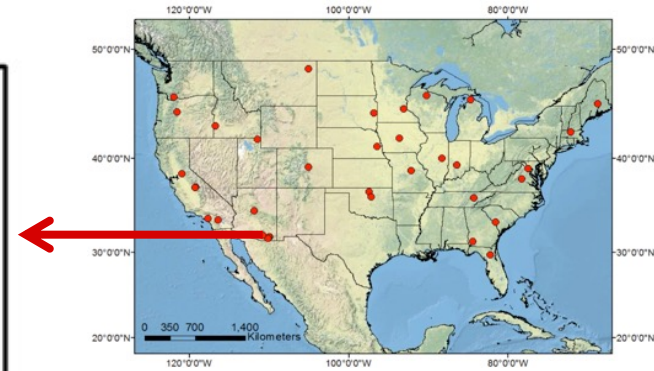
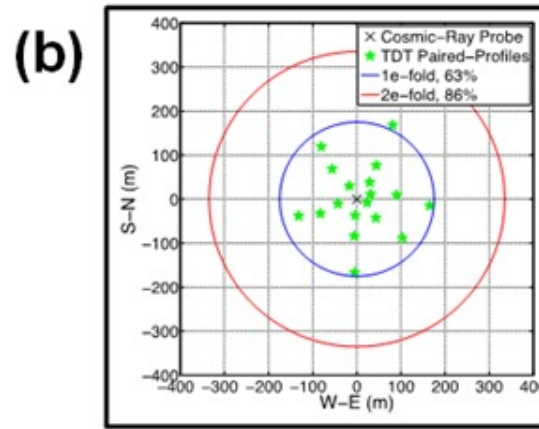
Hypothetical soil water profiles



Shuttleworth et al. 2013



# COSMIC comparison against independent network of soil moisture sensors



Running time for a single soil moisture profile  
MCNPx ~ 30-60 minutes  
COSMIC ~ 0.5 seconds

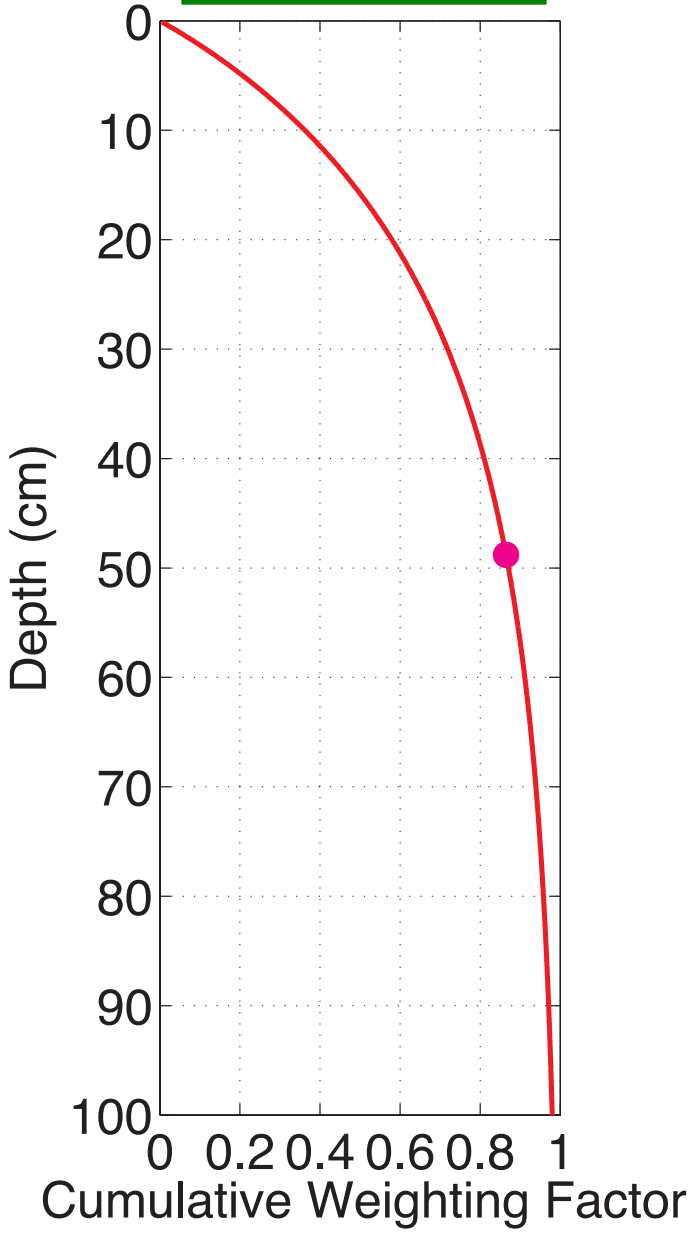
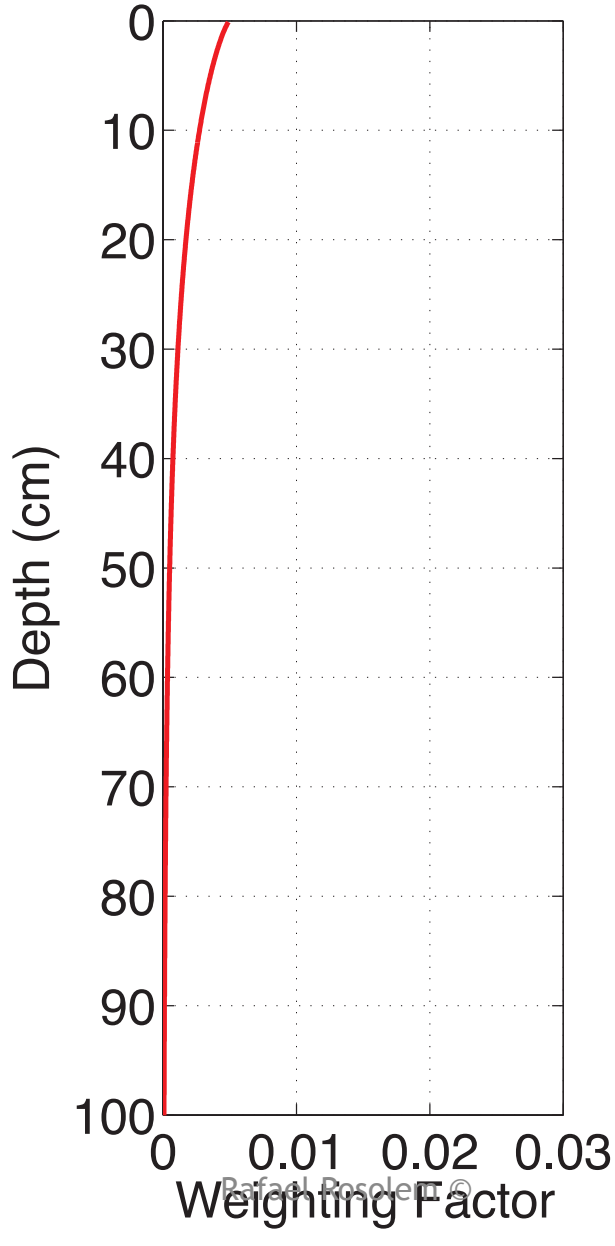
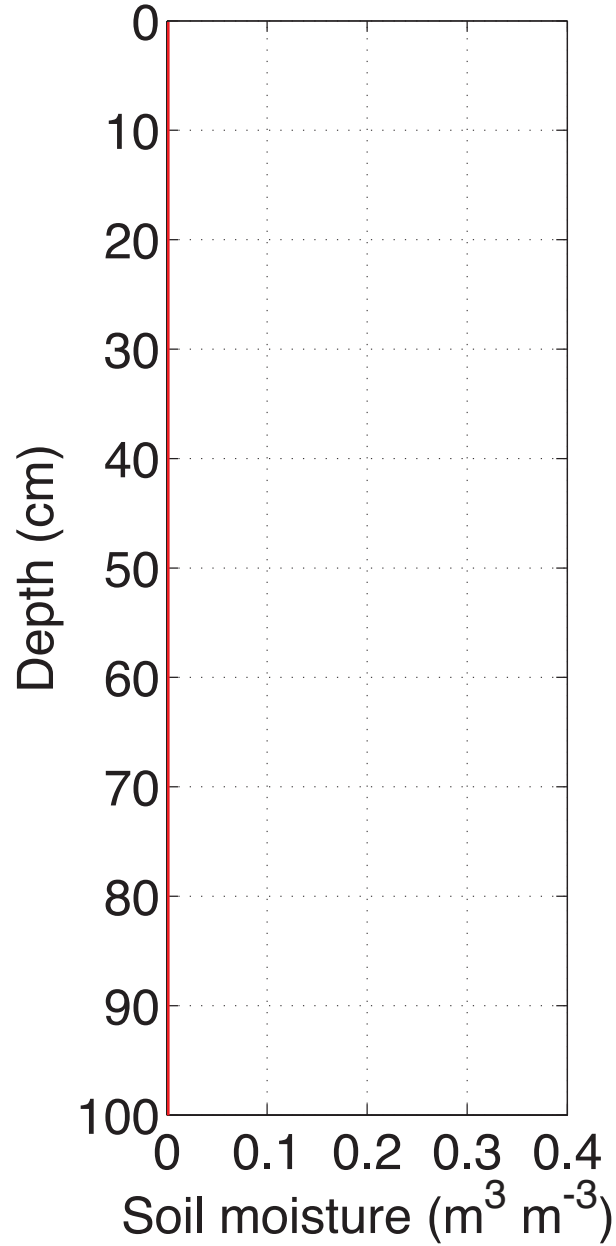
Output Data

Input Data

→  $\theta$  profile case #01

$\theta_{\text{INTEGRATED}} (\text{m}^3 \text{m}^{-3}) = 0.00$   
 $\theta_{\text{AVERAGE}} (\text{m}^3 \text{m}^{-3}) = 0.00$

$z^* = 48.8\text{cm}$   
 $N = 3793\text{cph}$



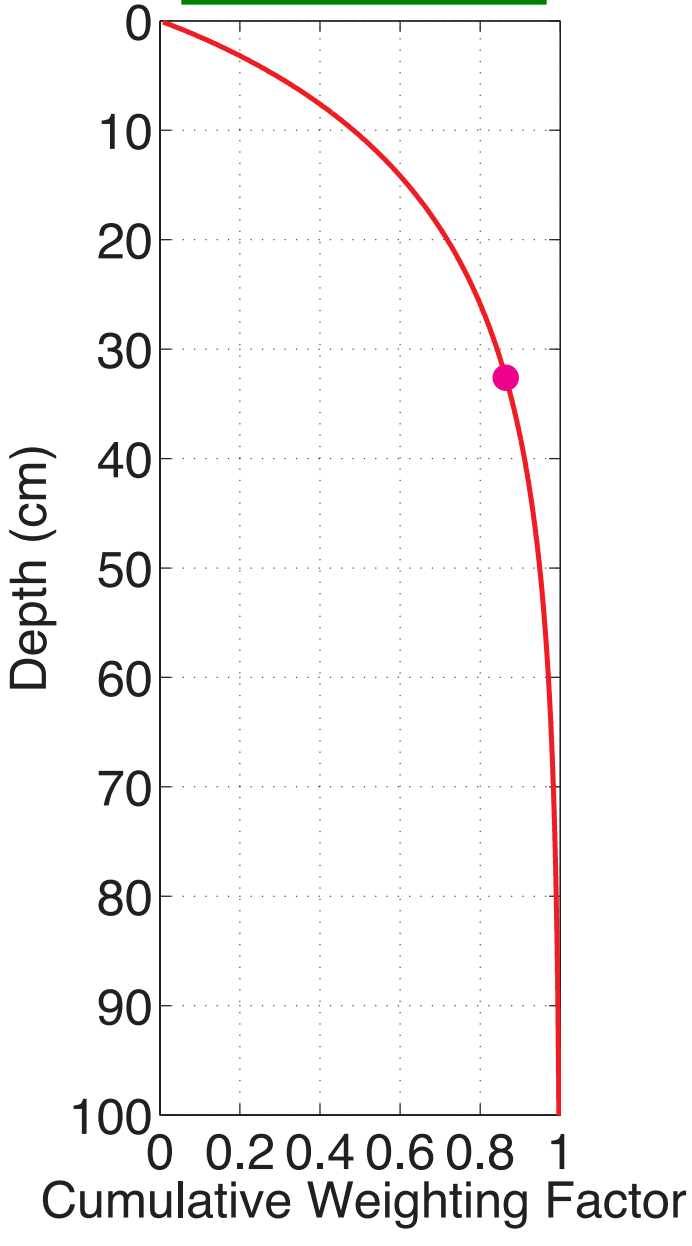
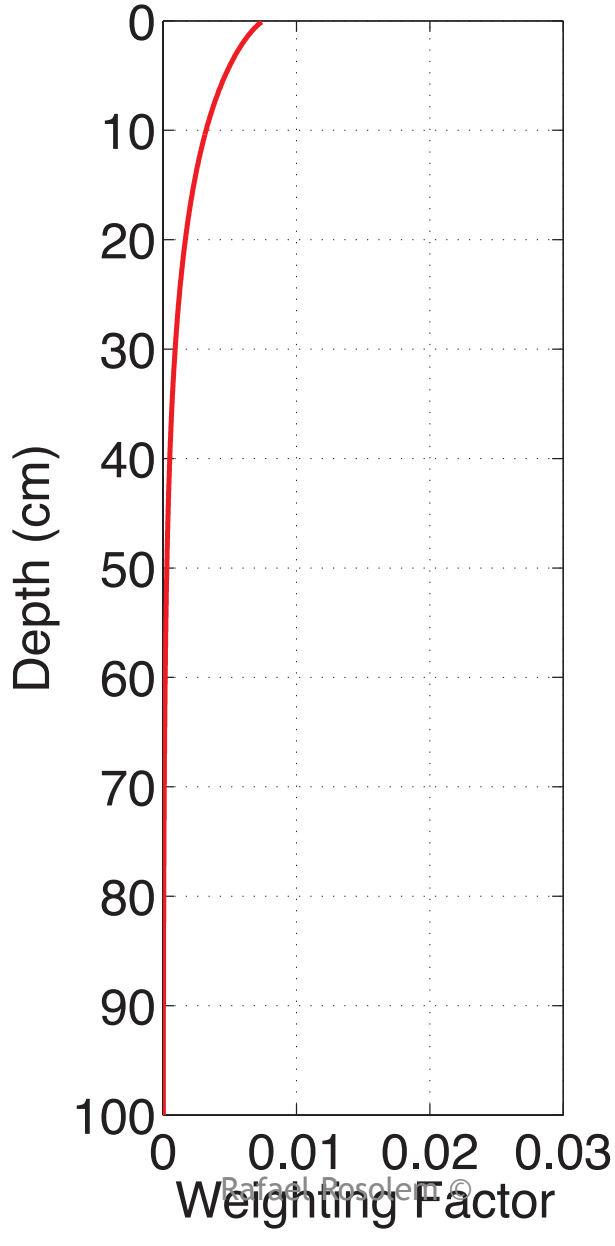
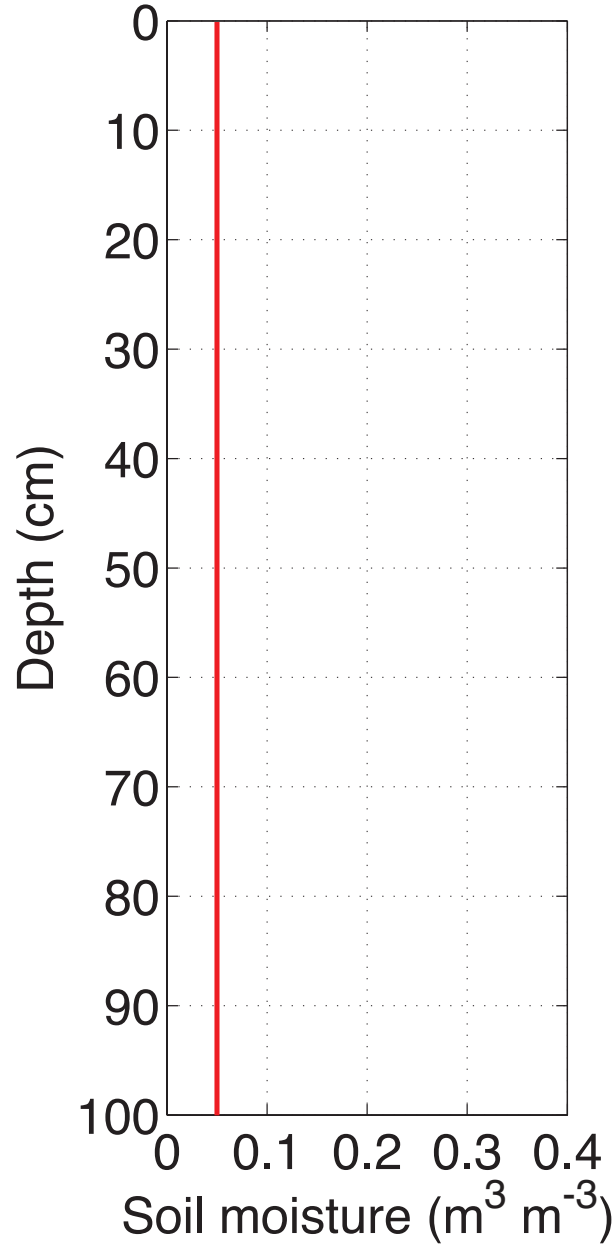
Output Data

Input Data

→  $\theta$  profile case #03

$\theta_{\text{INTEGRATED}} (\text{m}^3 \text{m}^{-3}) = 0.05$   
 $\theta_{\text{AVERAGE}} (\text{m}^3 \text{m}^{-3}) = 0.05$

$z^* = 32.6\text{cm}$   
 $N = 2817\text{cph}$



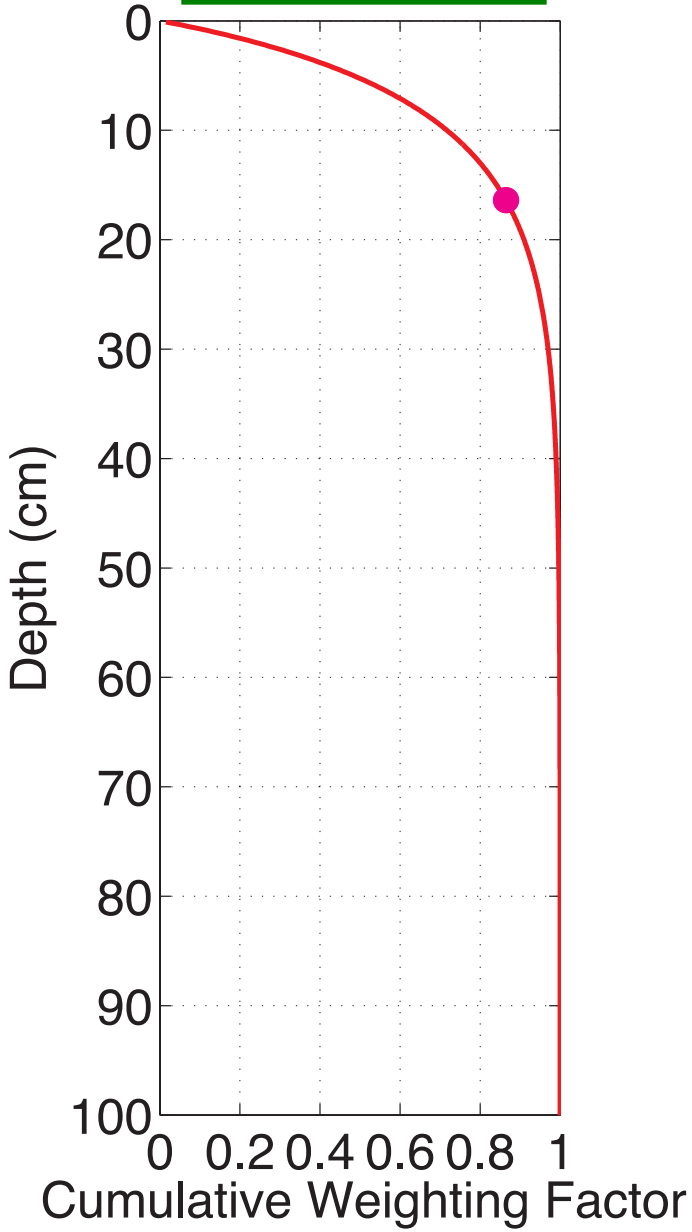
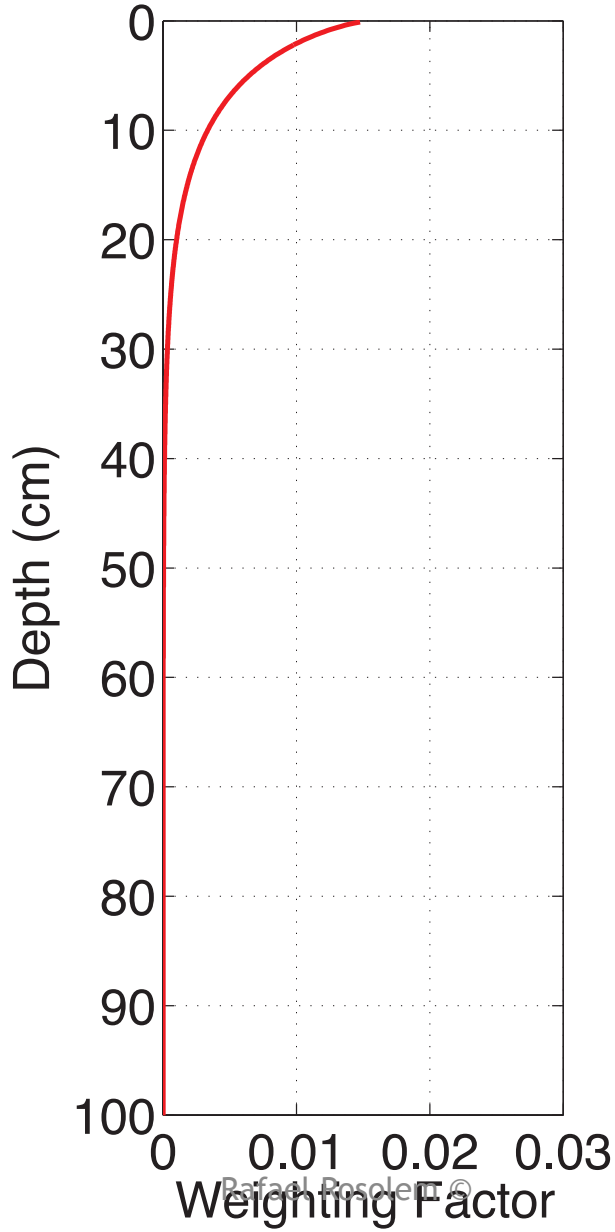
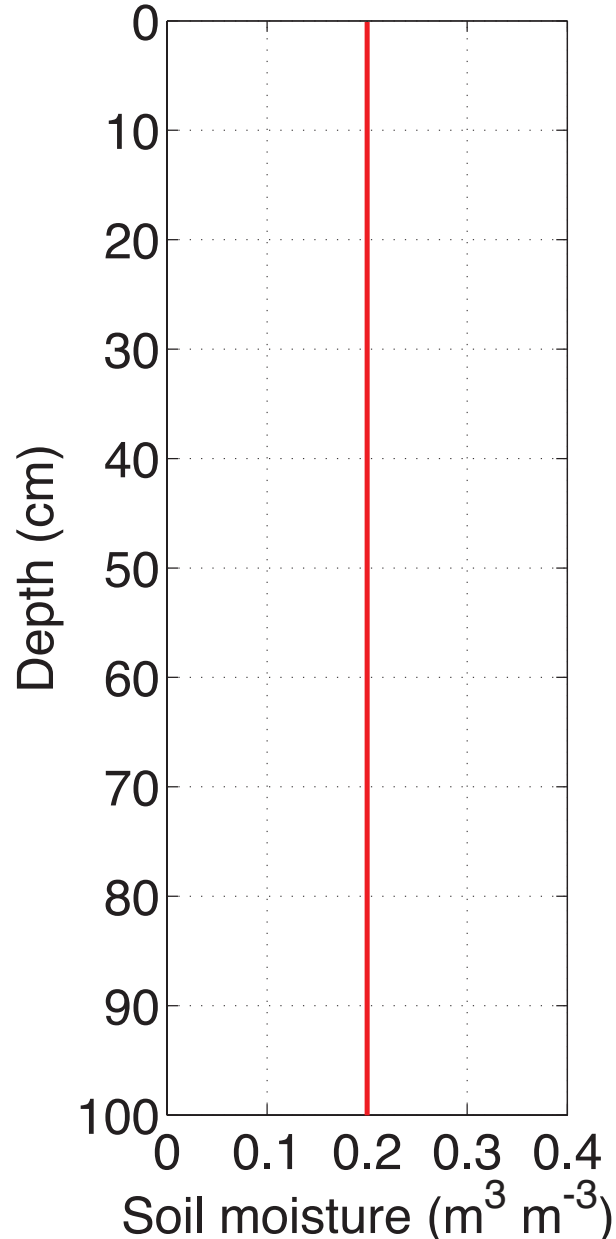
Output Data

Input Data

→  $\theta$  profile case #06

$\theta_{\text{INTEGRATED}} (\text{m}^3 \text{m}^{-3}) = 0.20$   
 $\theta_{\text{AVERAGE}} (\text{m}^3 \text{m}^{-3}) = 0.20$

$z^* = 16.4\text{cm}$   
 $N = 1861\text{cph}$





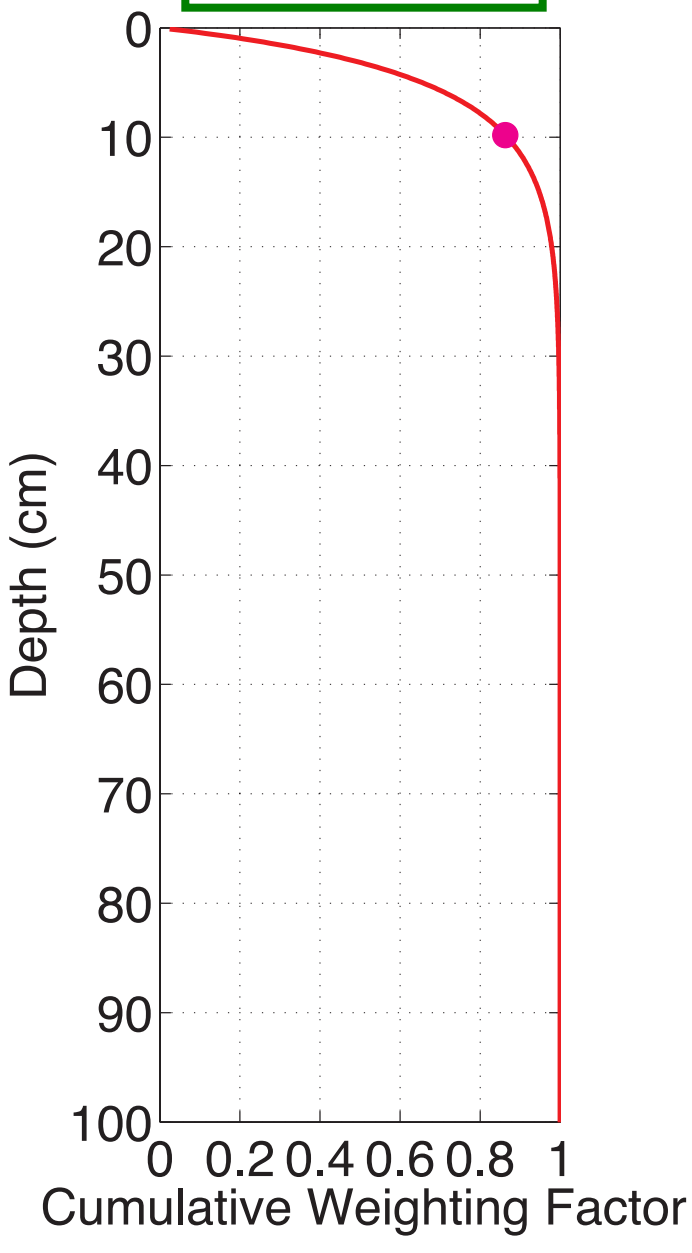
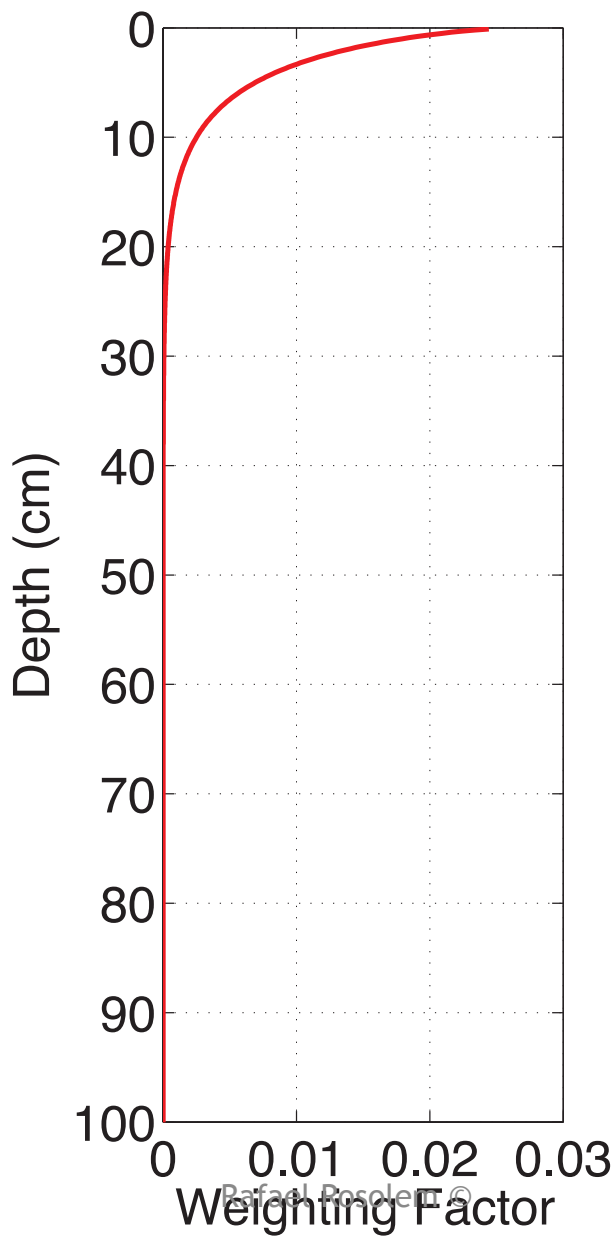
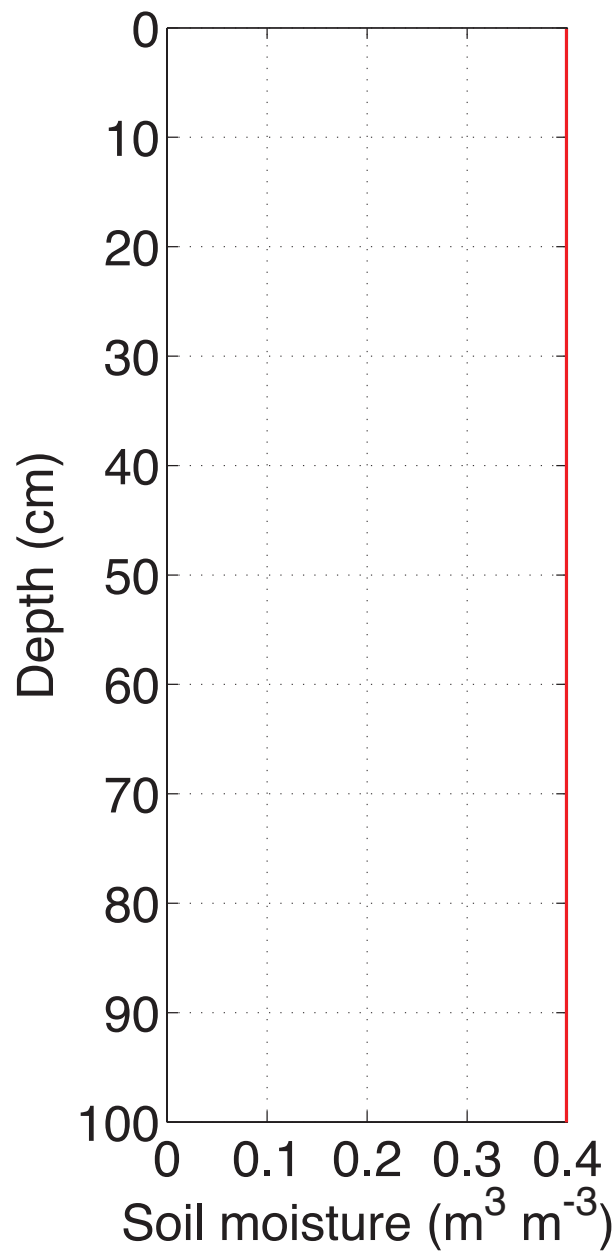
Output Data

Input Data

→  $\theta$  profile case #10

$\theta_{\text{INTEGRATED}} (\text{m}^3 \text{m}^{-3}) = 0.40$   
 $\theta_{\text{AVERAGE}} (\text{m}^3 \text{m}^{-3}) = 0.40$

$z^* = 9.8\text{cm}$   
 $N = 1482\text{cph}$



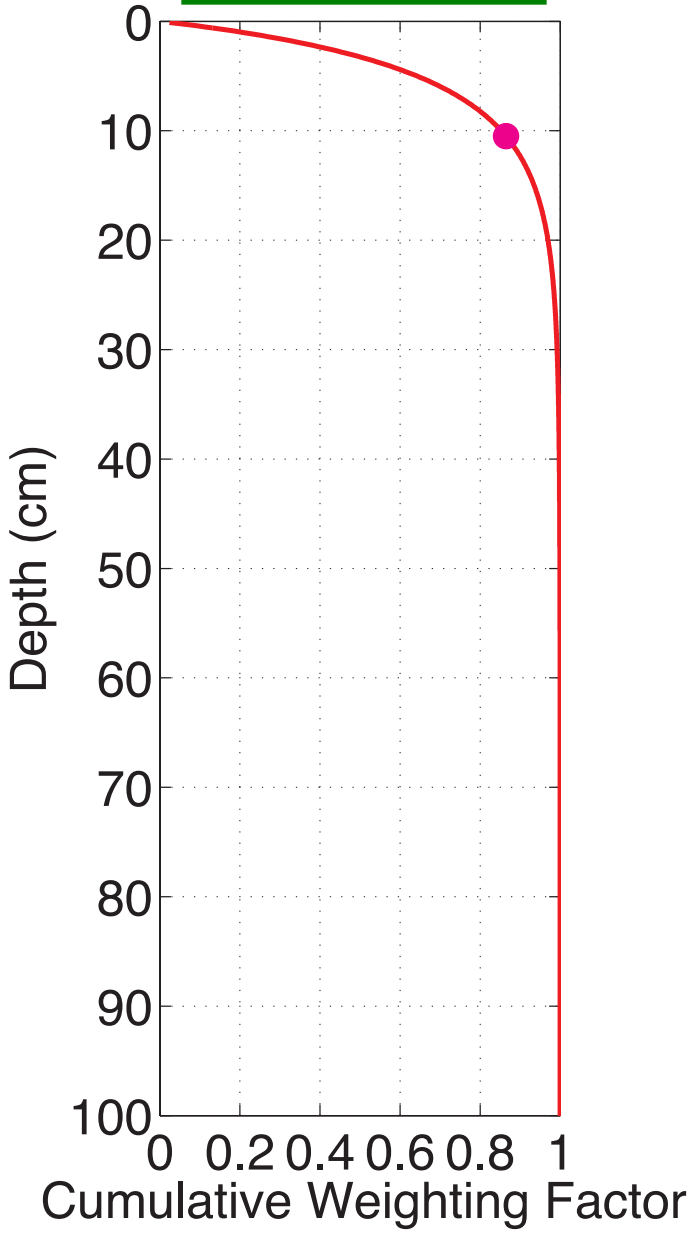
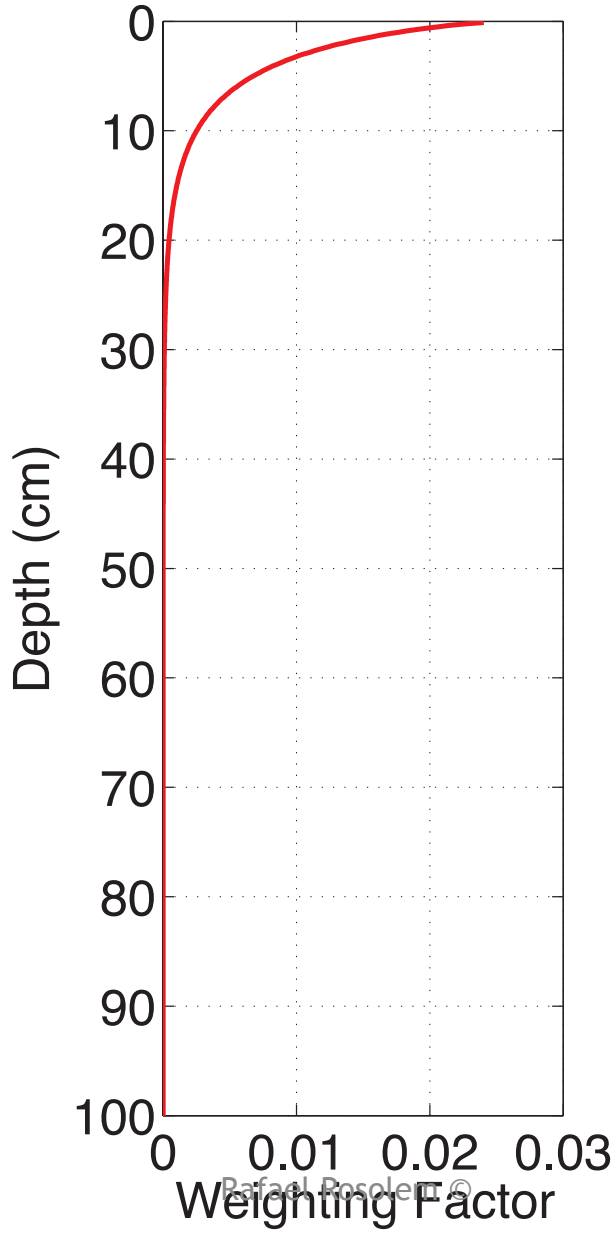
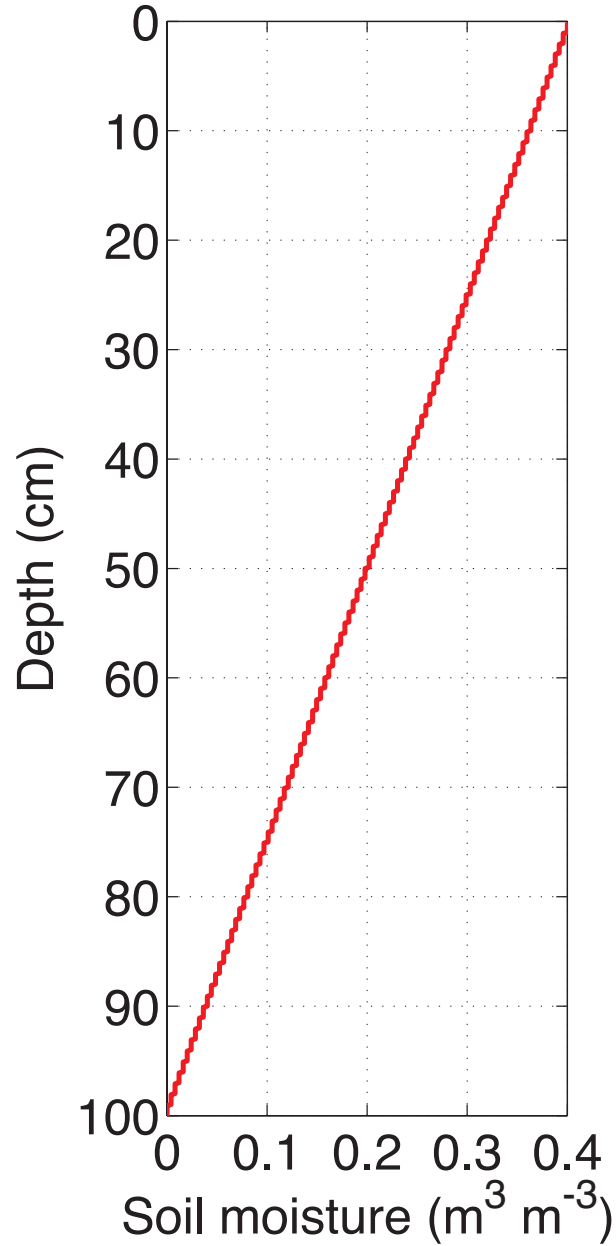
Output Data

Input Data

→  $\theta$  profile case #21

$\theta_{\text{INTEGRATED}} (\text{m}^3 \text{m}^{-3}) = 0.38$   
 $\theta_{\text{AVERAGE}} (\text{m}^3 \text{m}^{-3}) = 0.20$

$z^* = 10.5\text{cm}$   
 $N = 1506\text{cph}$



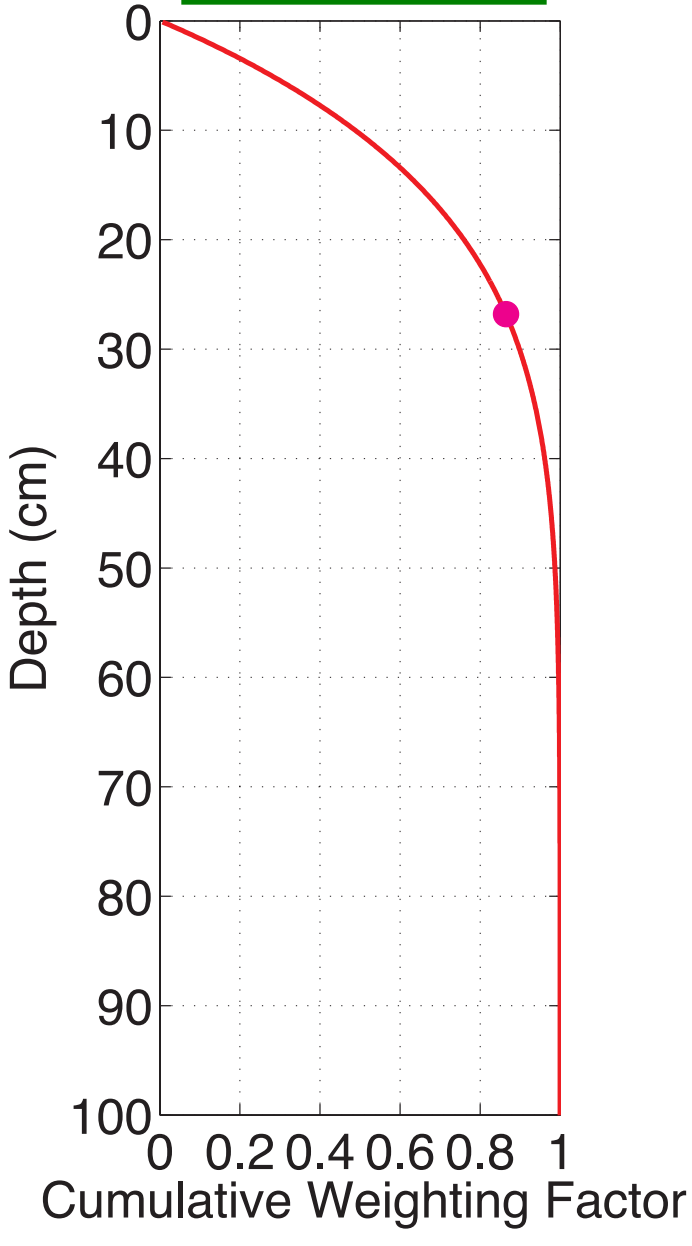
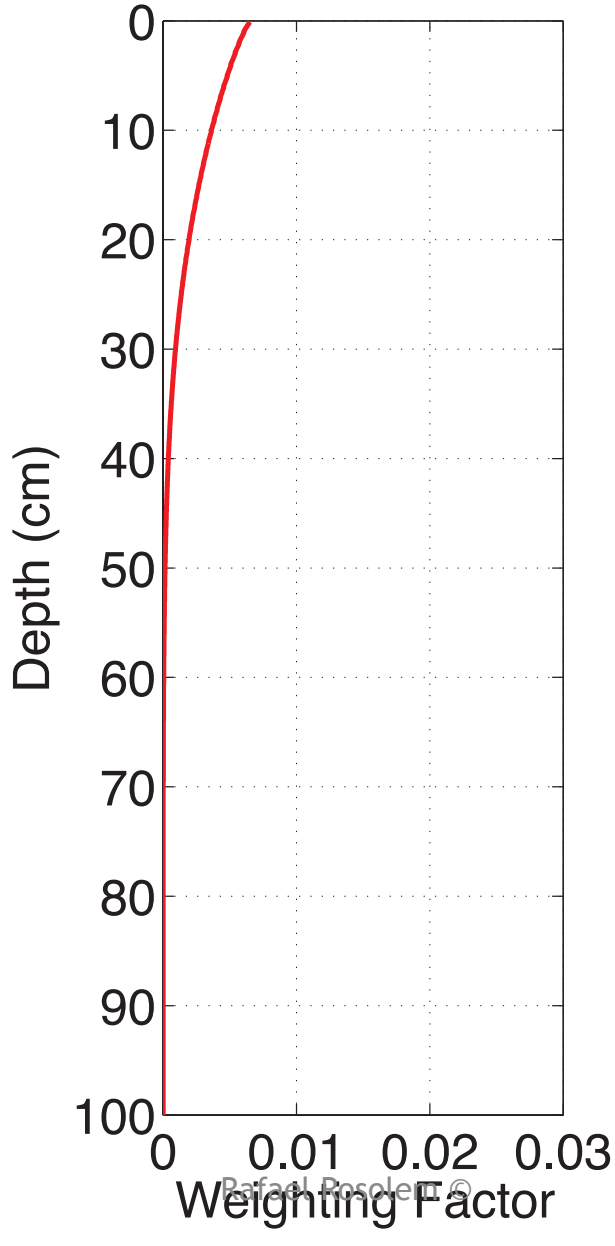
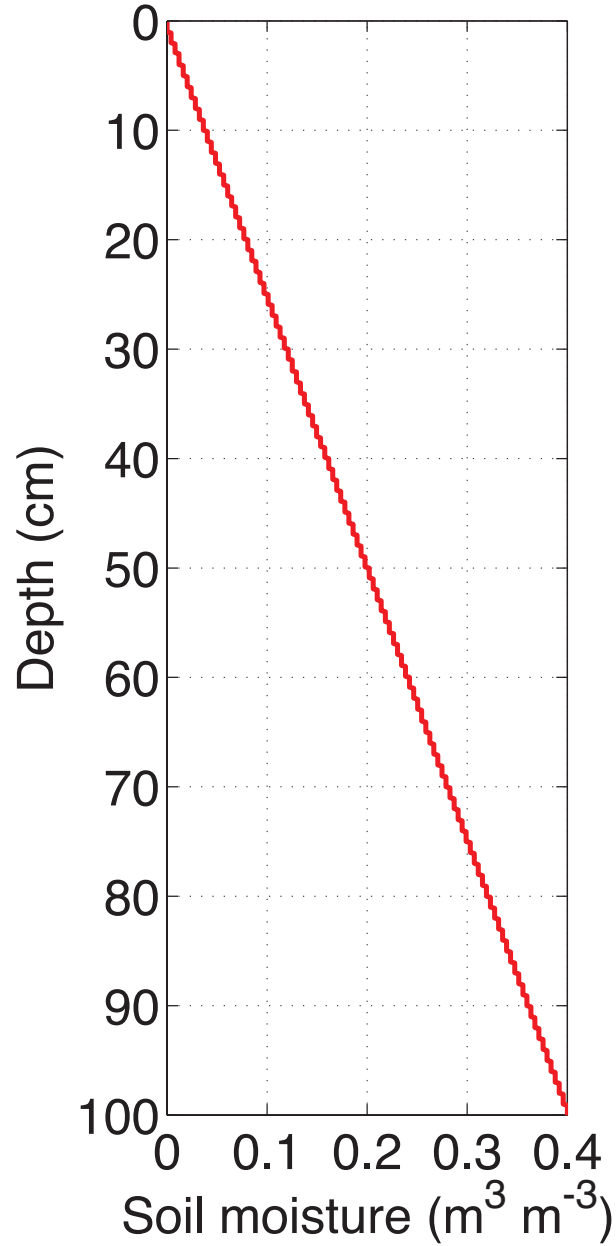
Output Data

Input Data

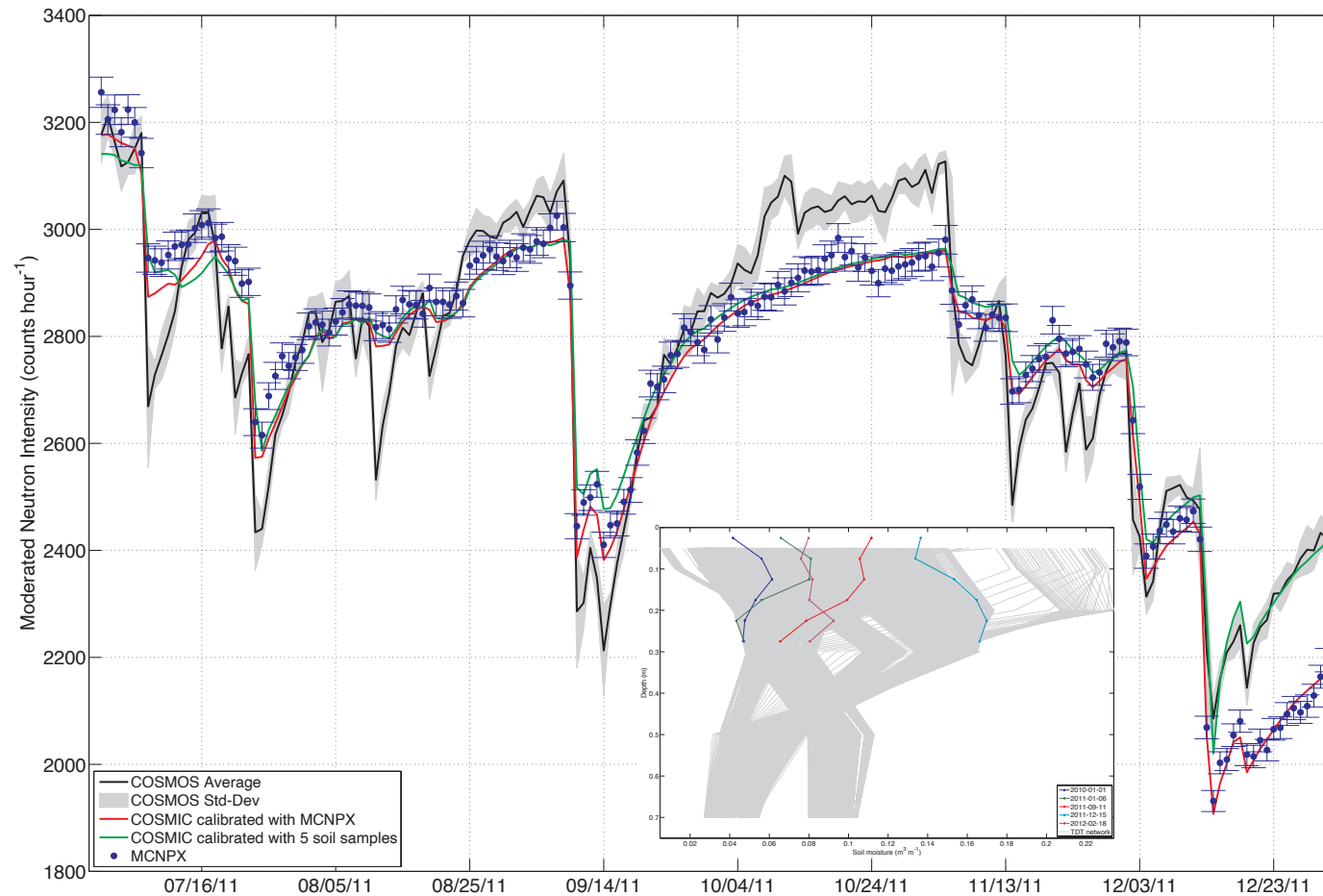
→  $\theta$  profile case #22

$\theta_{\text{INTEGRATED}} (\text{m}^3 \text{m}^{-3}) = 0.05$   
 $\theta_{\text{AVERAGE}} (\text{m}^3 \text{m}^{-3}) = 0.20$

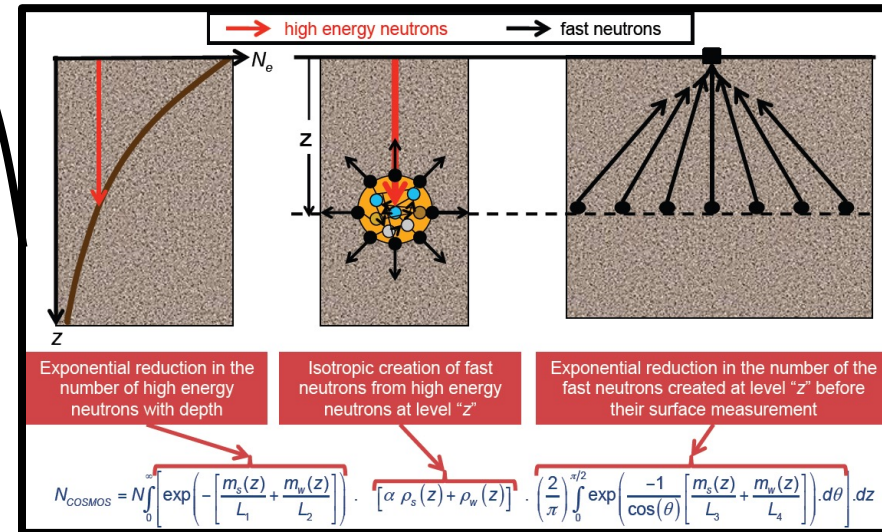
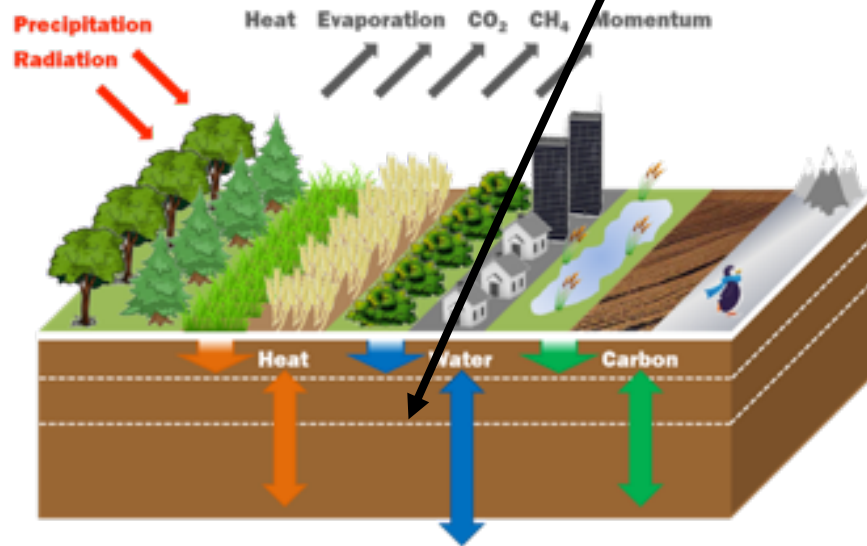
$z^* = 26.8\text{cm}$   
 $N = 2848\text{cph}$



# COSMIC can also be calibrated with in-situ soil samples - the more campaigns, the better!

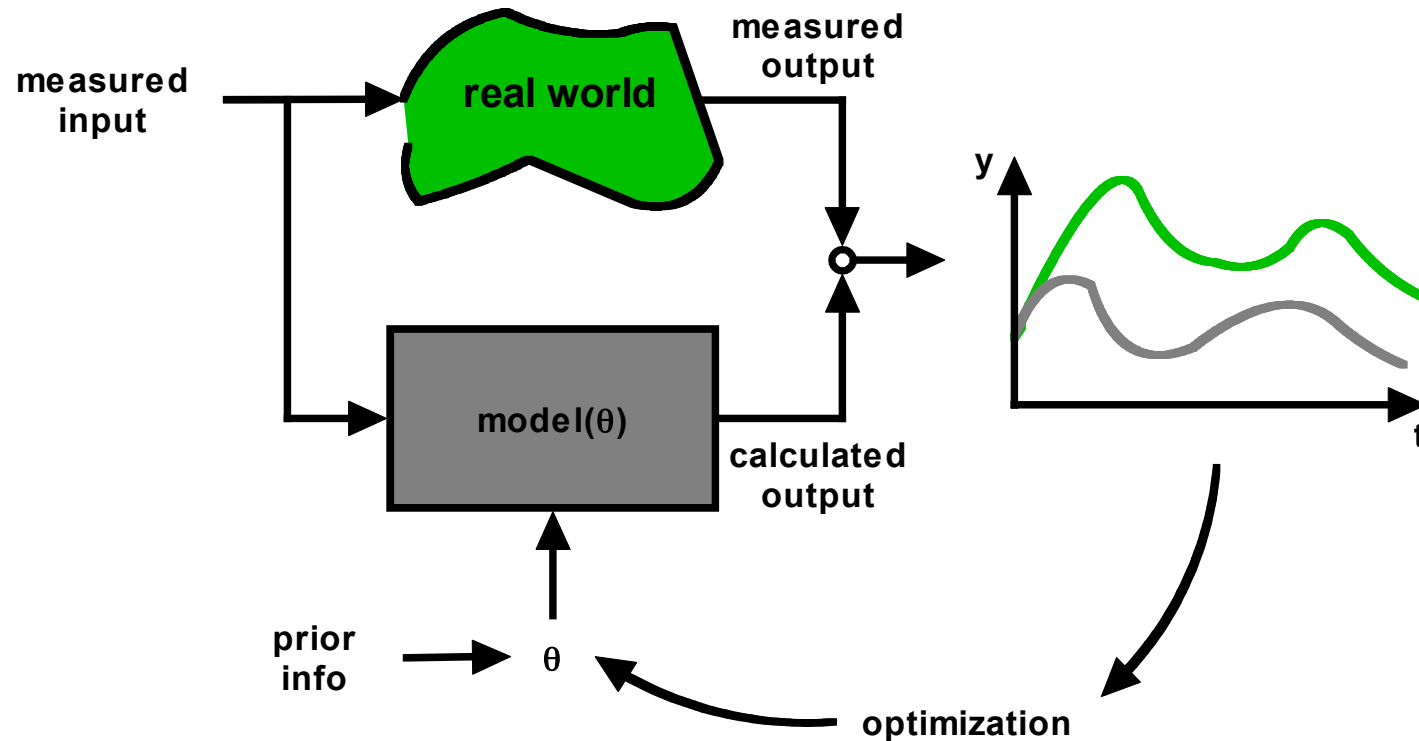


# We have incorporated COSMIC into land surface models



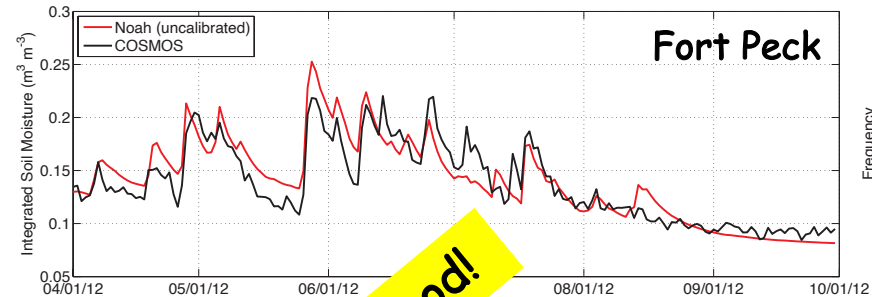
Shuttleworth et al. 2013 (HESS)  
Rosolem et al. 2014 (HESS)

Model optimization (or calibration) refers to tuning model parameters to reduce as much as possible the error against a reference measured quantity

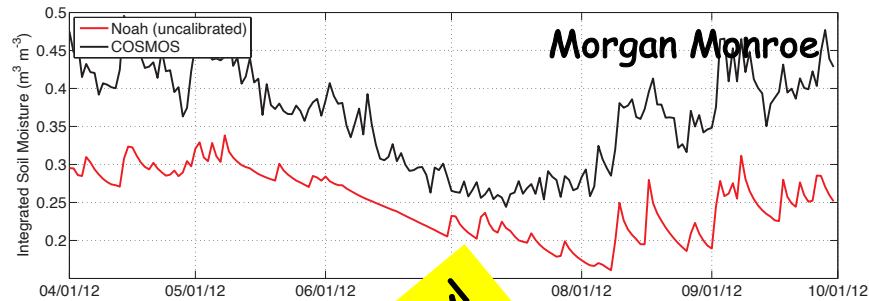
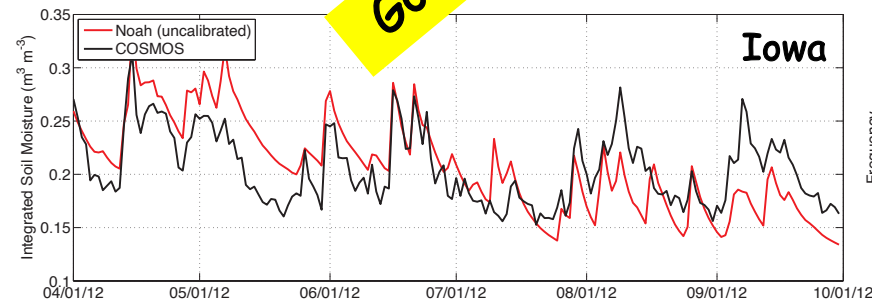


Adapted from Hoshin Gupta slides (Univ. of Arizona)

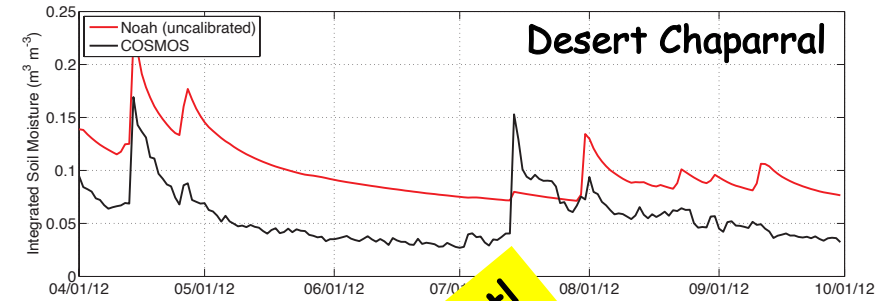
# Land surface models don't always represent soil moisture accurately



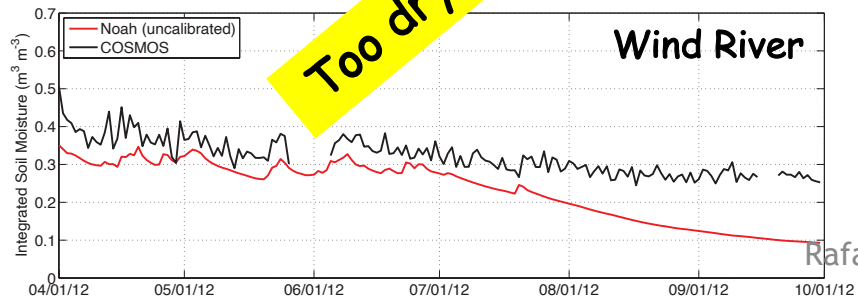
**Good!**



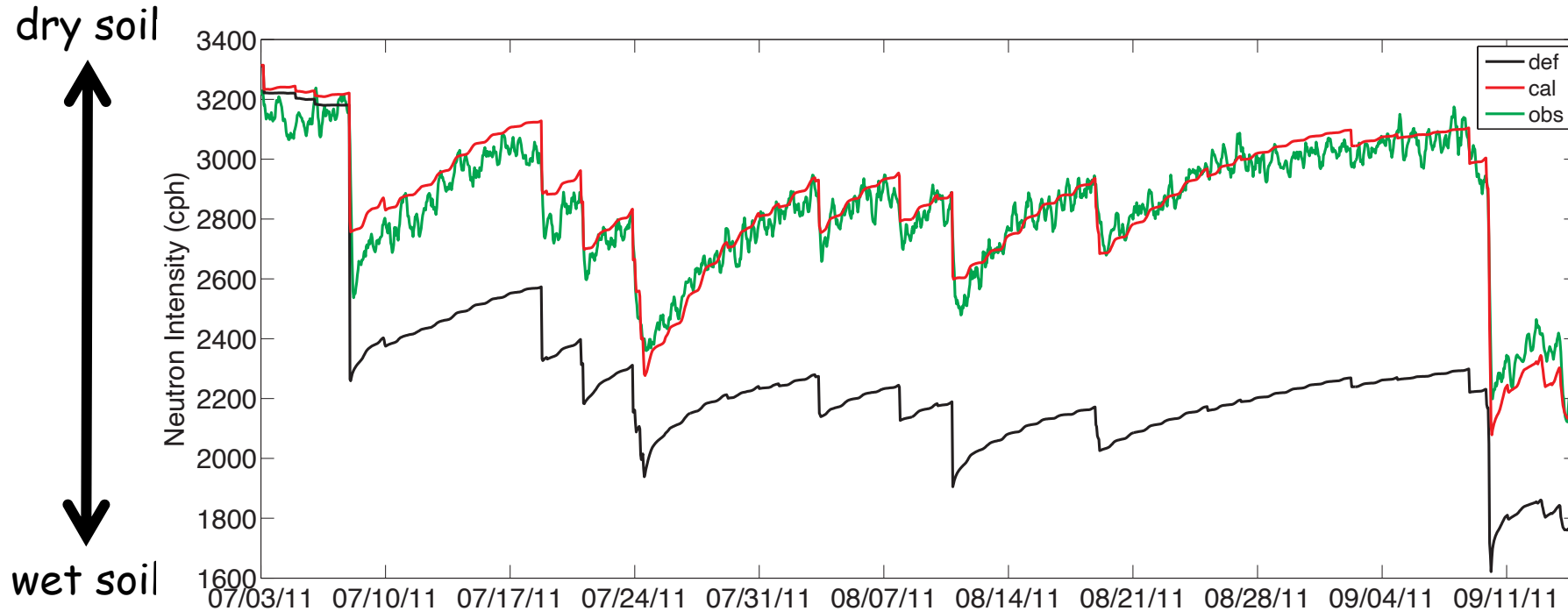
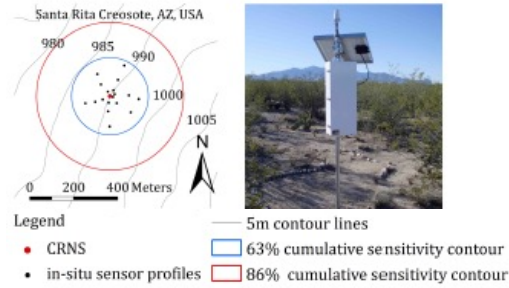
**Too dry!**



**Too wet!**

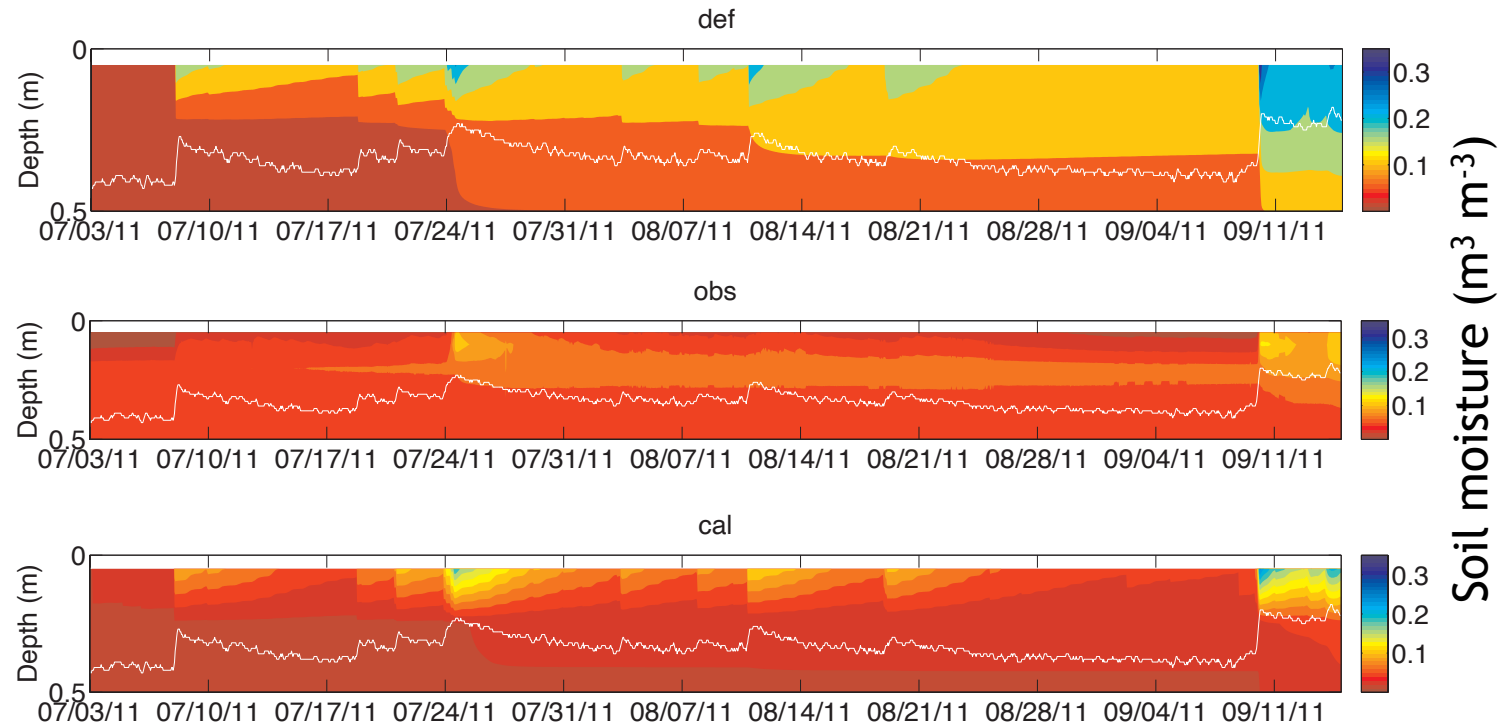
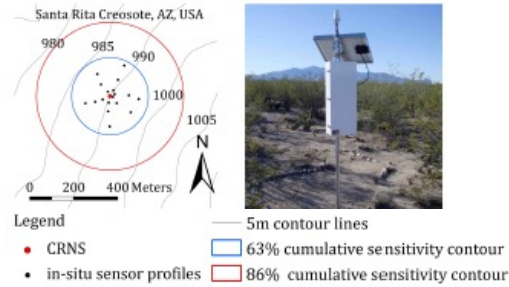


# We calibrated the soil properties in the model using only measured neutron counts



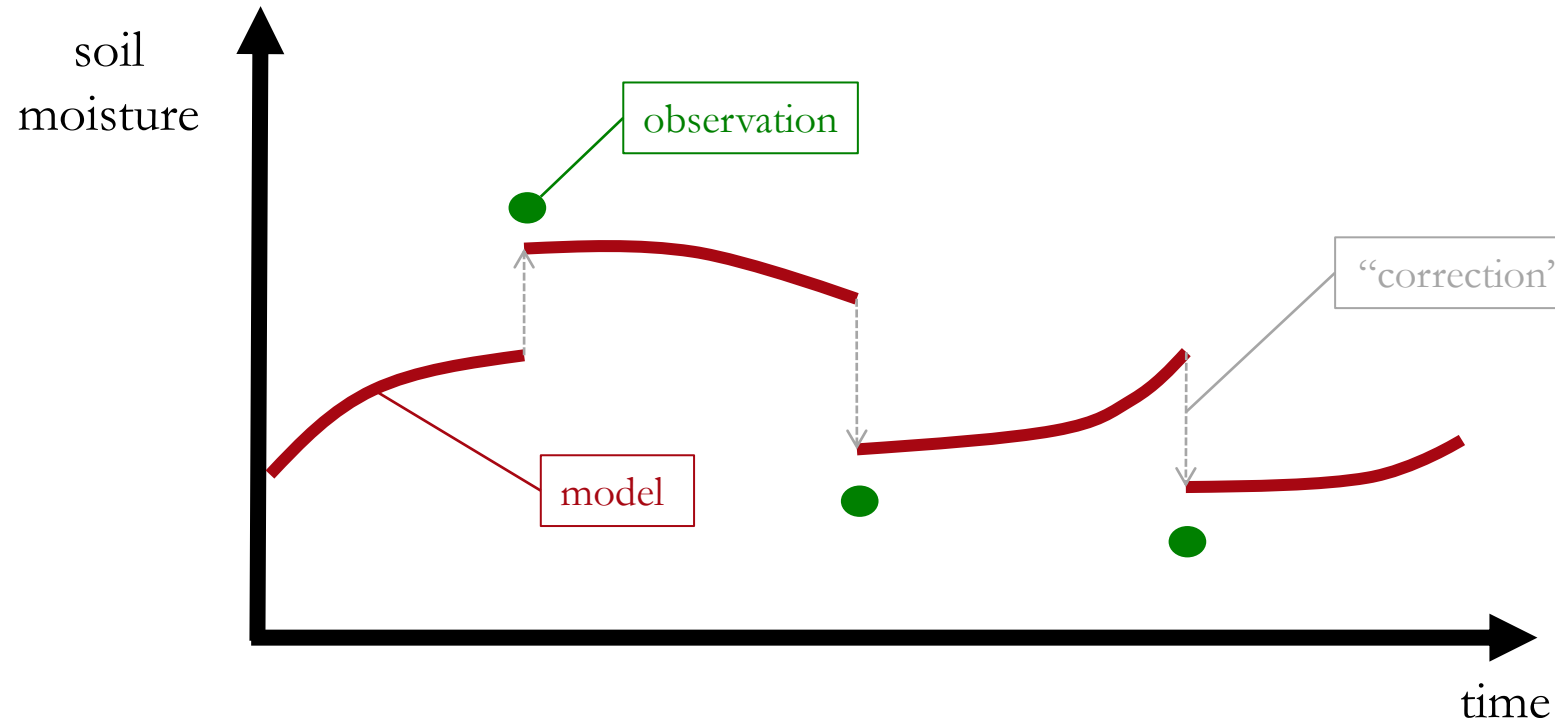


# Calibrated model reproduces well the soil moisture profile from independent measurements



Data assimilation attempts to correct model states (and sometimes parameters) continuously as independent observations become available

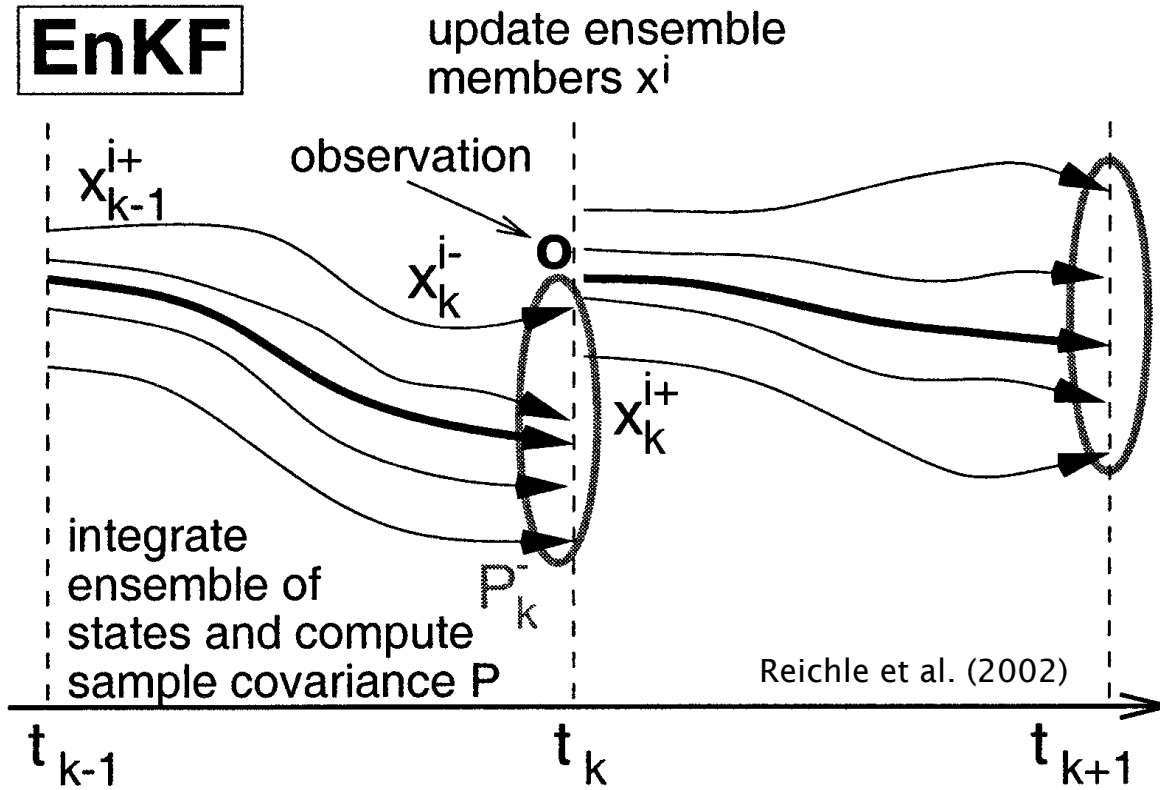
### Data assimilation techniques



All done with the use of probability distributions!

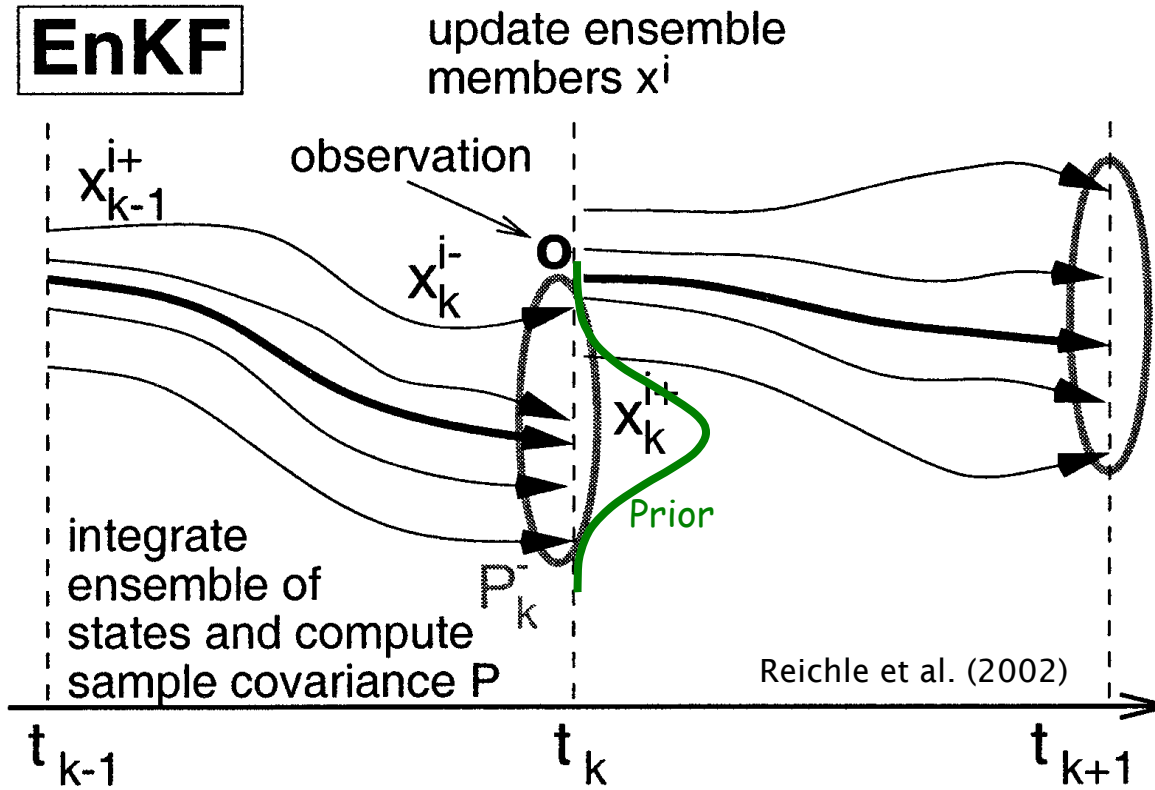
Bayes  
Theorem:

$$P(x_k | y_k) = \frac{P(y_k | x) P(x_k | y_{k-1})}{\text{normalization factor}}$$



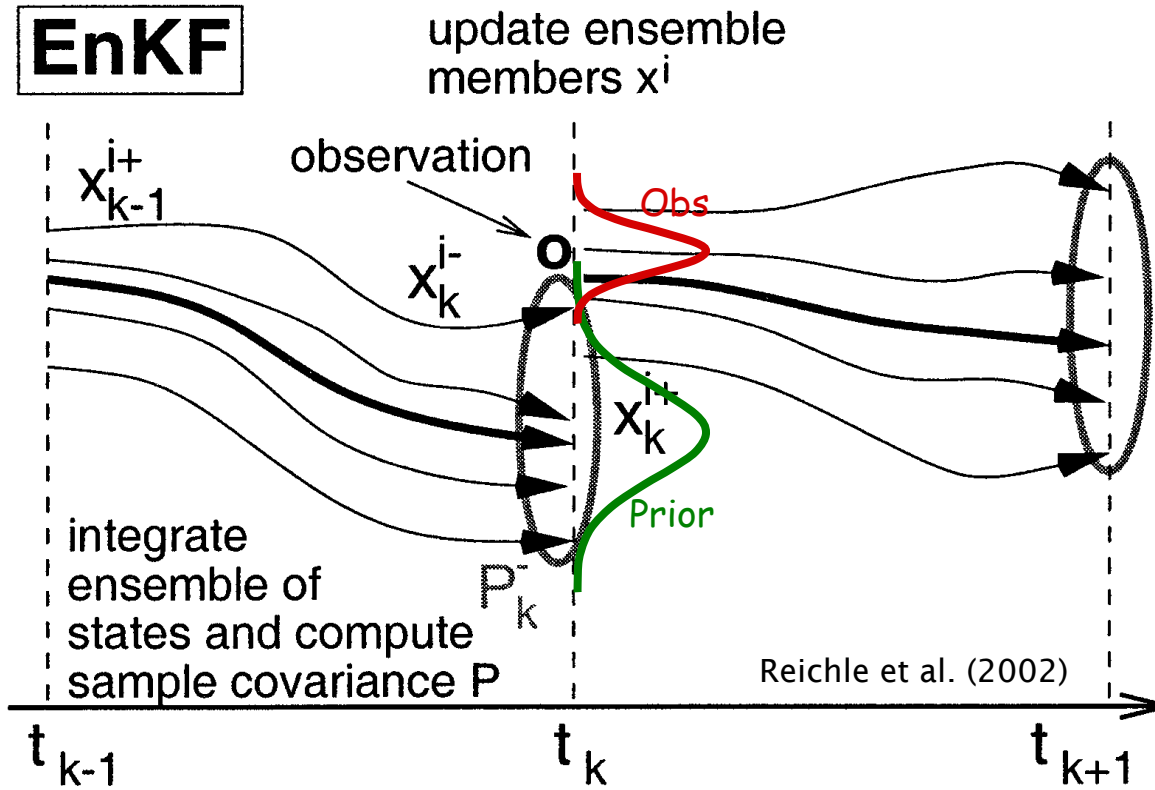
Bayes  
Theorem:

$$P(x_k | y_k) = \frac{P(y_k | x) P(x_k | y_{k-1})}{\text{normalization factor}}$$



Bayes  
Theorem:

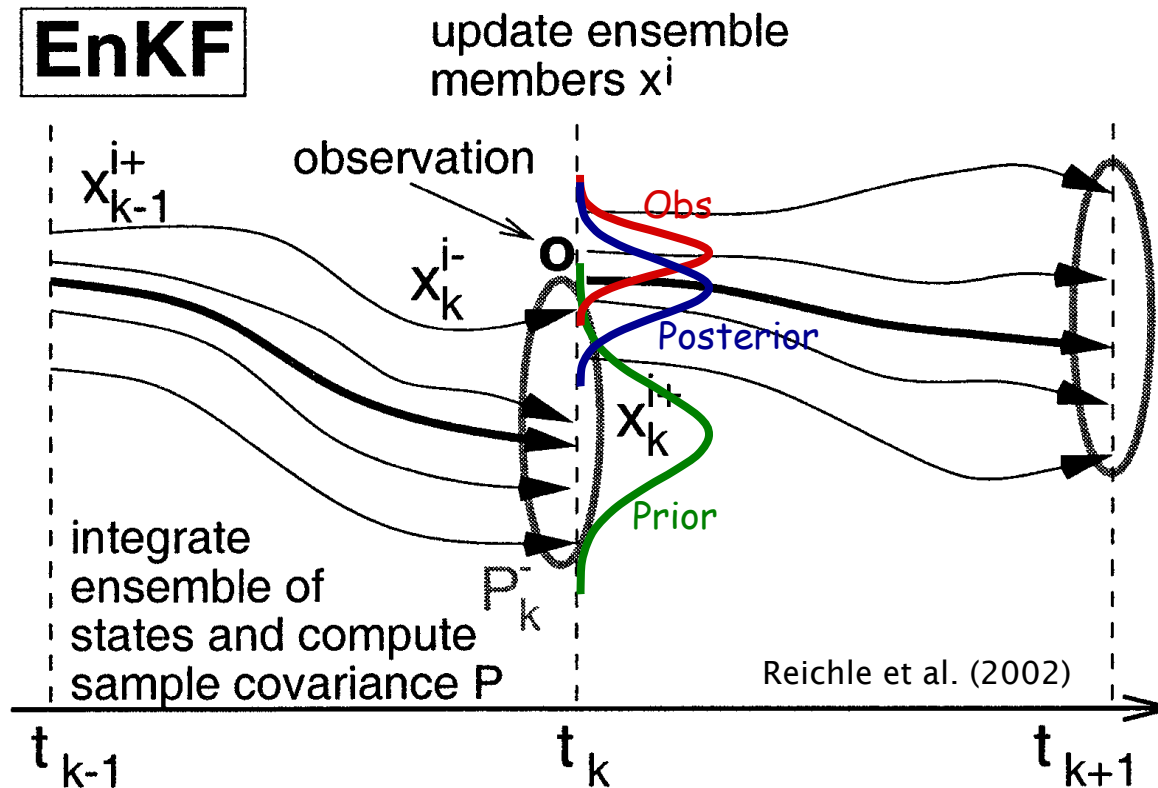
$$P(x_k | y_k) = \frac{P(y_k | x) P(x_k | y_{k-1})}{\text{normalization factor}}$$



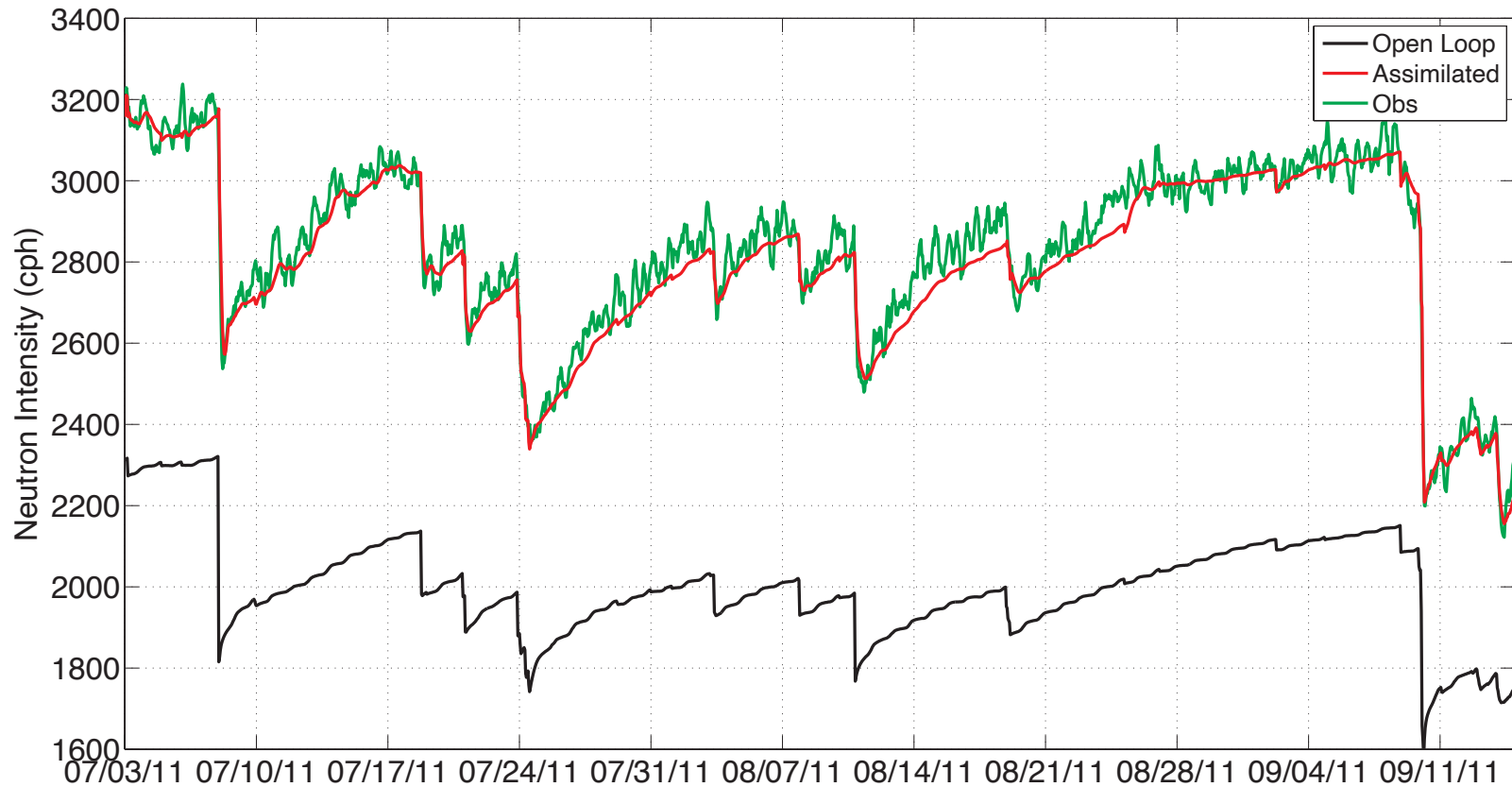
The ensemble data assimilation method is an approximation to a general filtering algorithm developed using Bayes Theorem

Bayes Theorem:

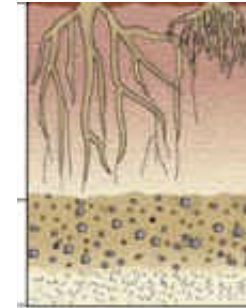
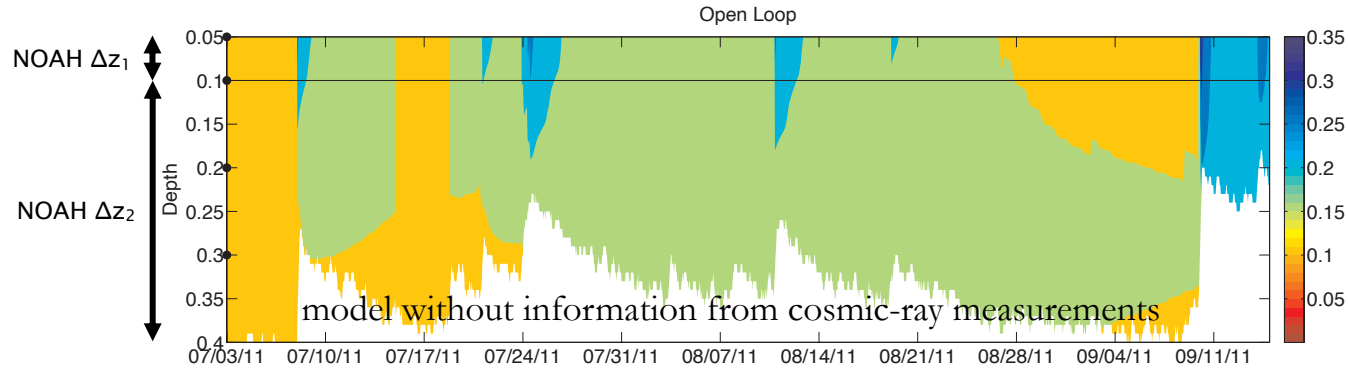
$$P(x_k | y_k) = \frac{P(y_k | x) P(x_k | y_{k-1})}{\text{normalization factor}}$$



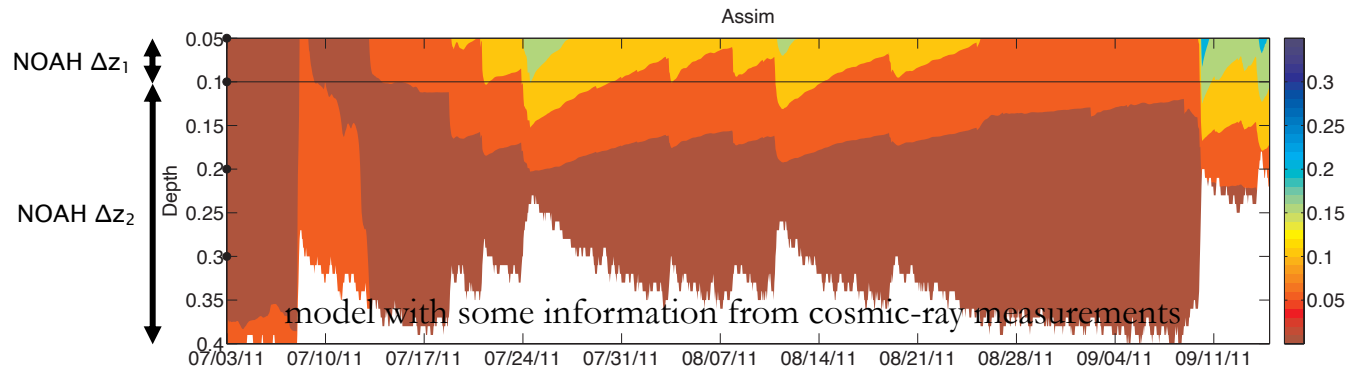
# Data assimilation of neutron counts



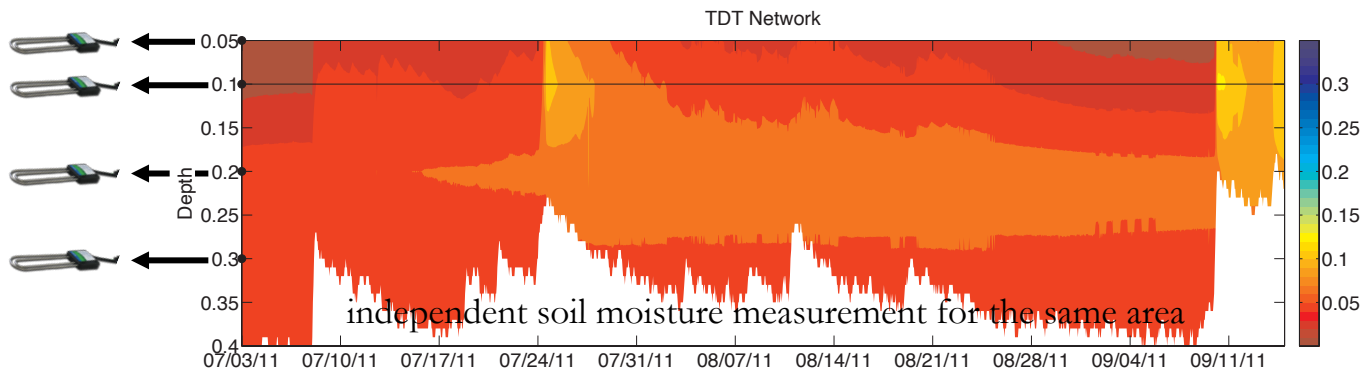
# Soil moisture estimates are improved!



model  
thinks is  
wet...



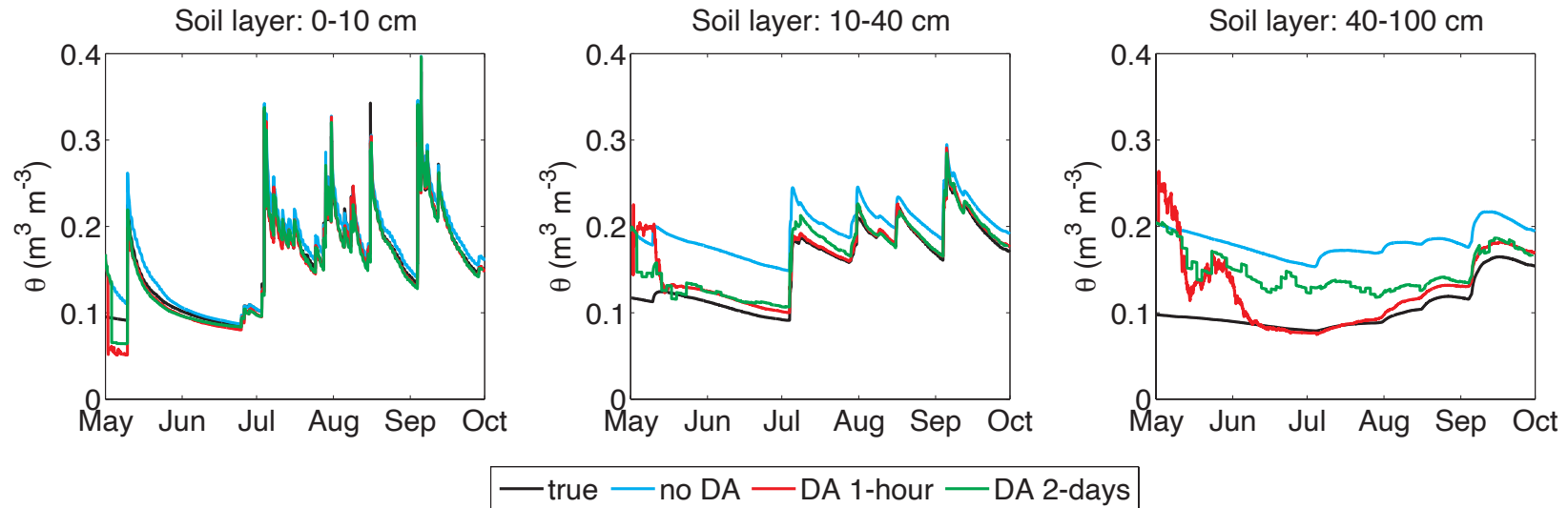
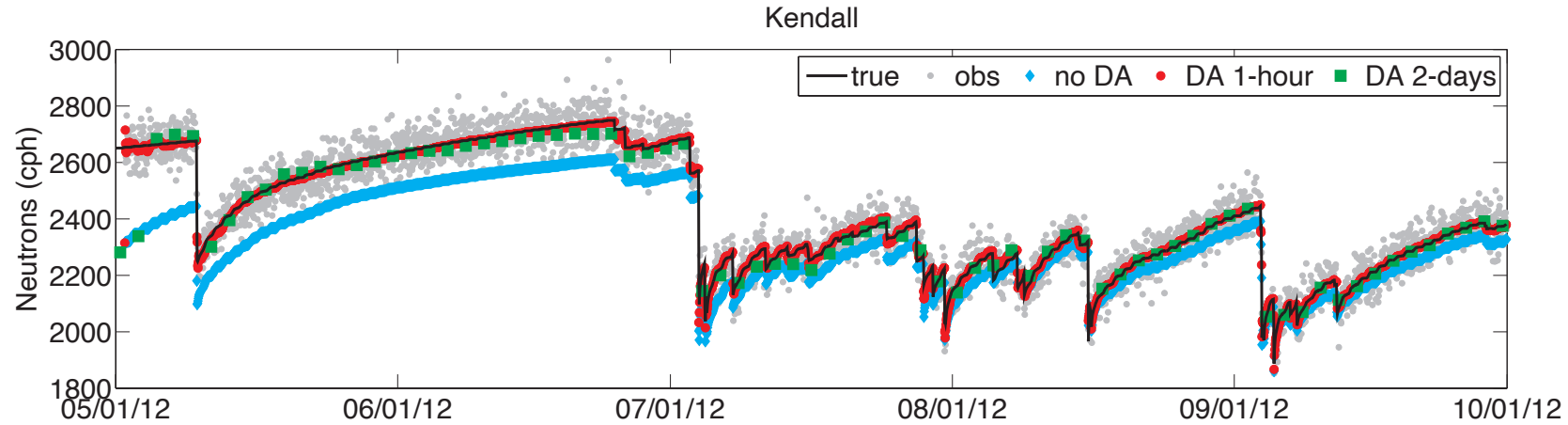
but information from  
measurements tells  
otherwise



model simulation in  
combination with  
measurements agree  
with independent  
observations

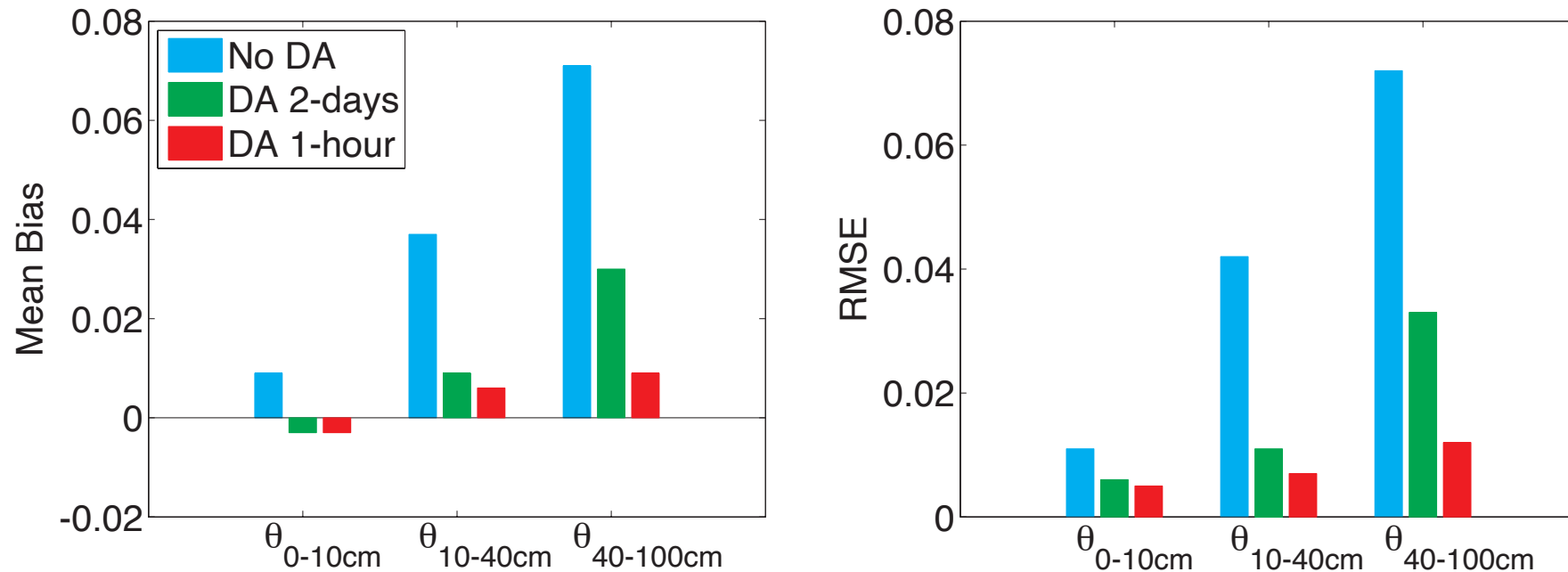


# Another example of data assimilation of neutron counts using a synthetic experiment



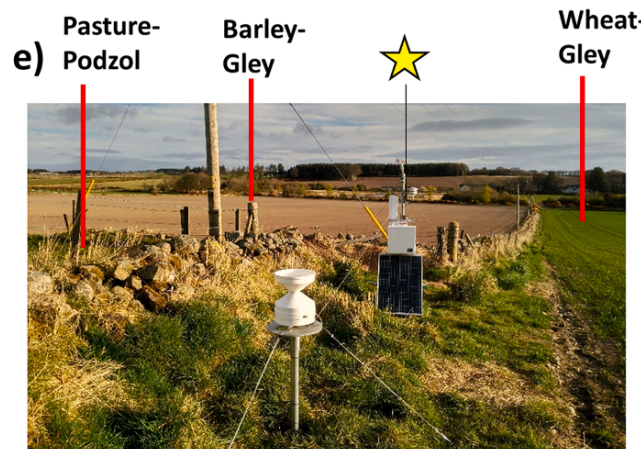
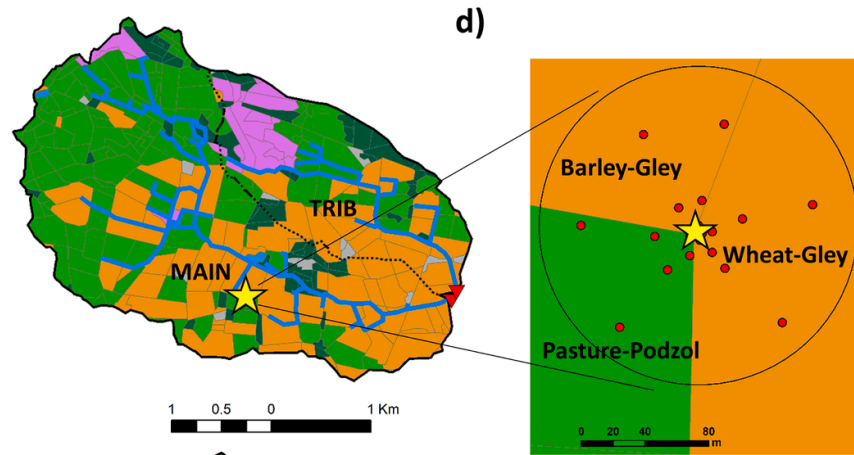
# High frequency of cosmic-ray neutron sensing data positively impacts the assimilation

## Kendall

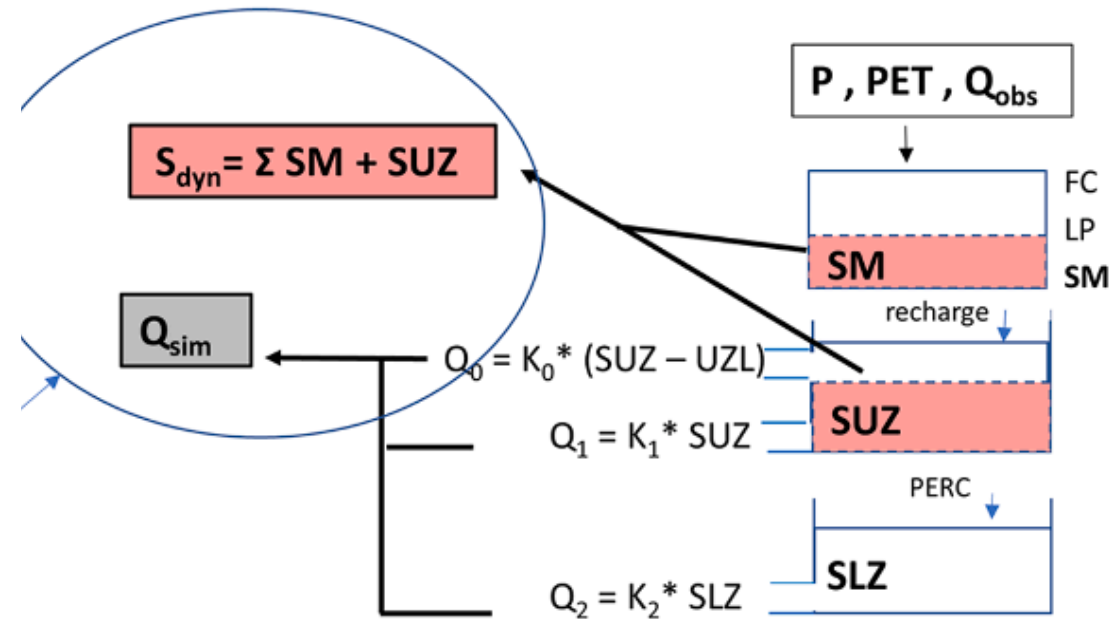


# Example of applications using hydrological models

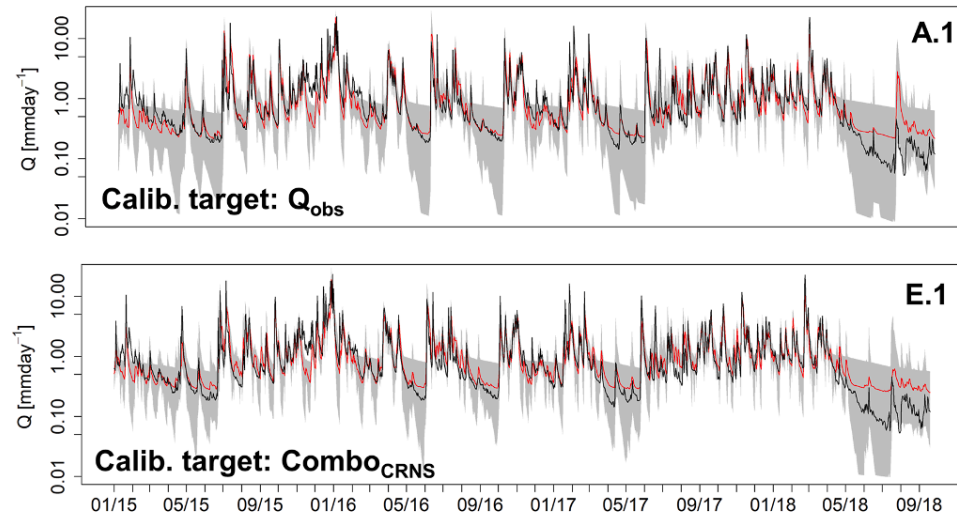
# Example of calibration of conceptual lumped hydrological model



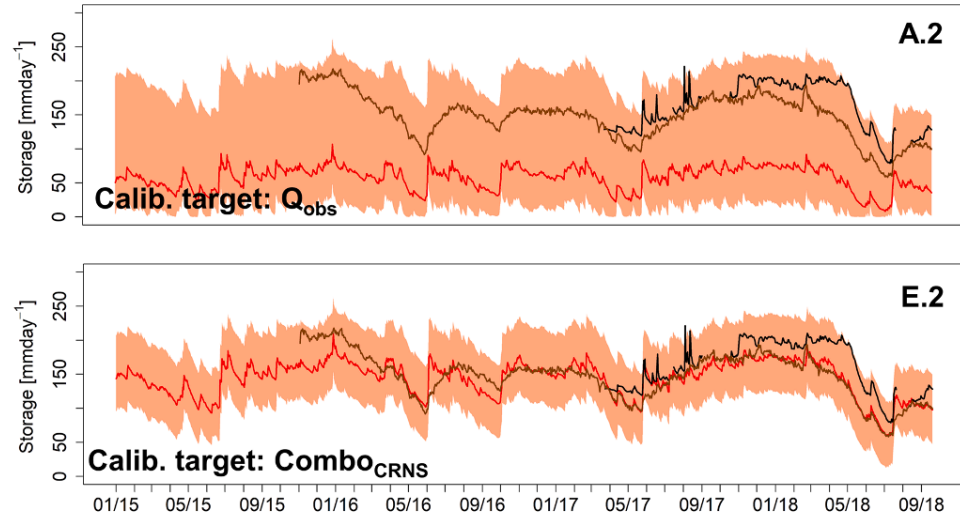
## V. Rainfall-runoff model structure



# More realistic representation of hydrological processes achieved when streamflow and storage information are available



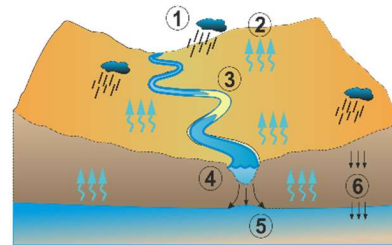
—  $Q_{obs}$   
— Median simulated  $Q_{sim}$   
— Simulation envelops  $Q_{sim}$



—  $S_{NS\_point}$   
—  $S_{NS\_CRNS}$   
— Median simulated  $S_{dyn}$   
— Simulation envelops  $S_{dyn}$

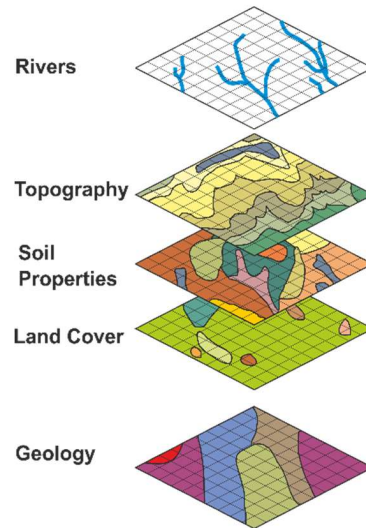
# Checking consistency of internal structure in newly-developed hydrological model for drylands using cosmic-ray neutron sensors

a) Main hydrological processes in drylands

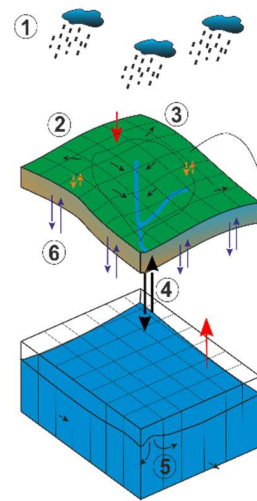


- Spatially restricted, short-lived rainstorms (1)
- High losses of precipitation by evapotranspiration (2)
- Brief and spatially variable runoff events in ephemeral drainage networks (3)
- Groundwater recharge via leaky ephemeral streams through transmission losses (4) as focussed recharge (5).
- Limited diffuse recharge (6)

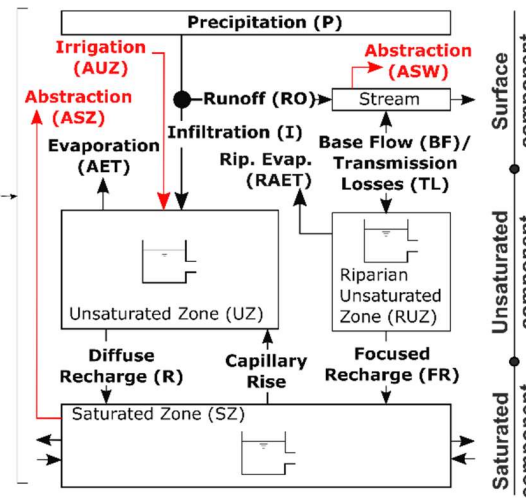
b) Data



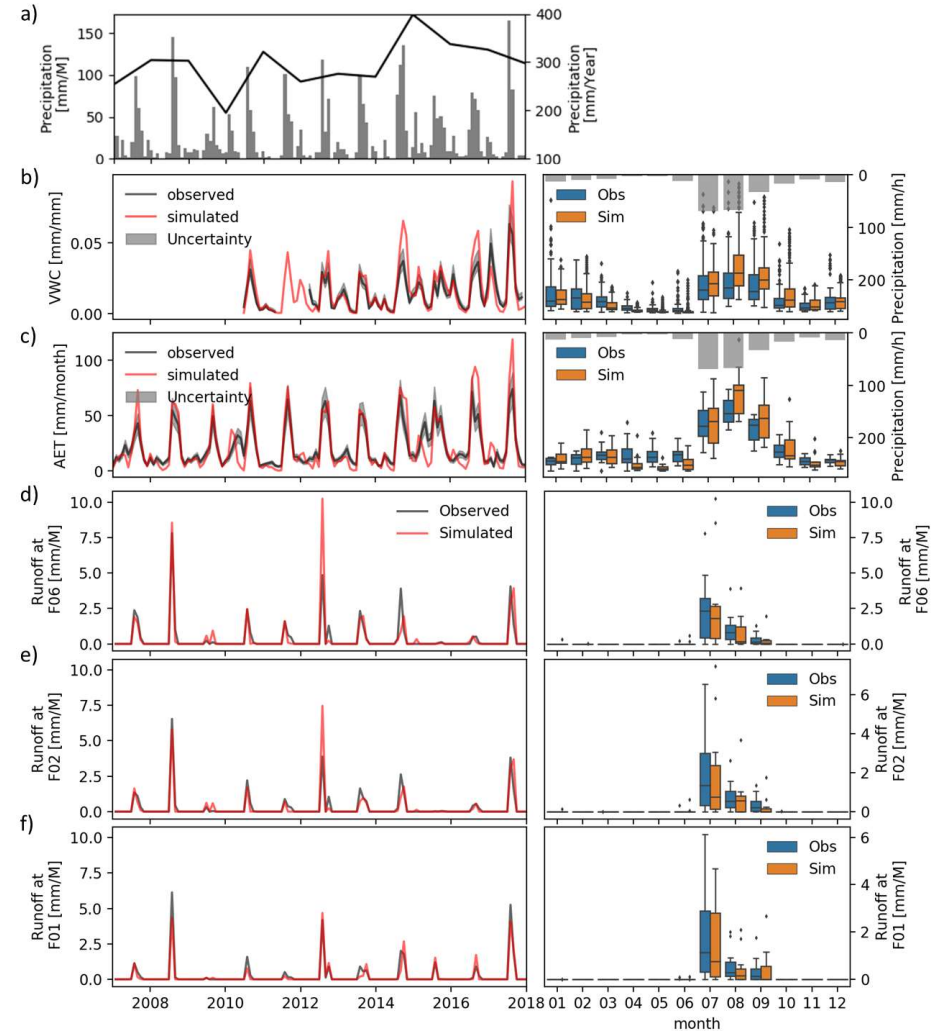
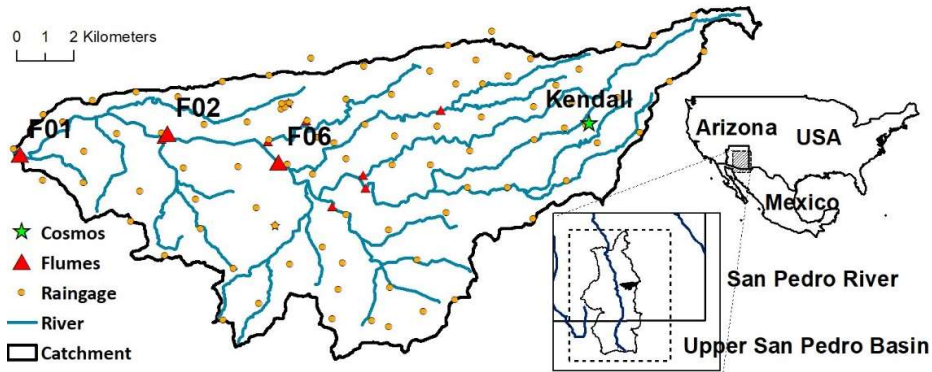
c) Spatial discretization



d) Model Cell Processes



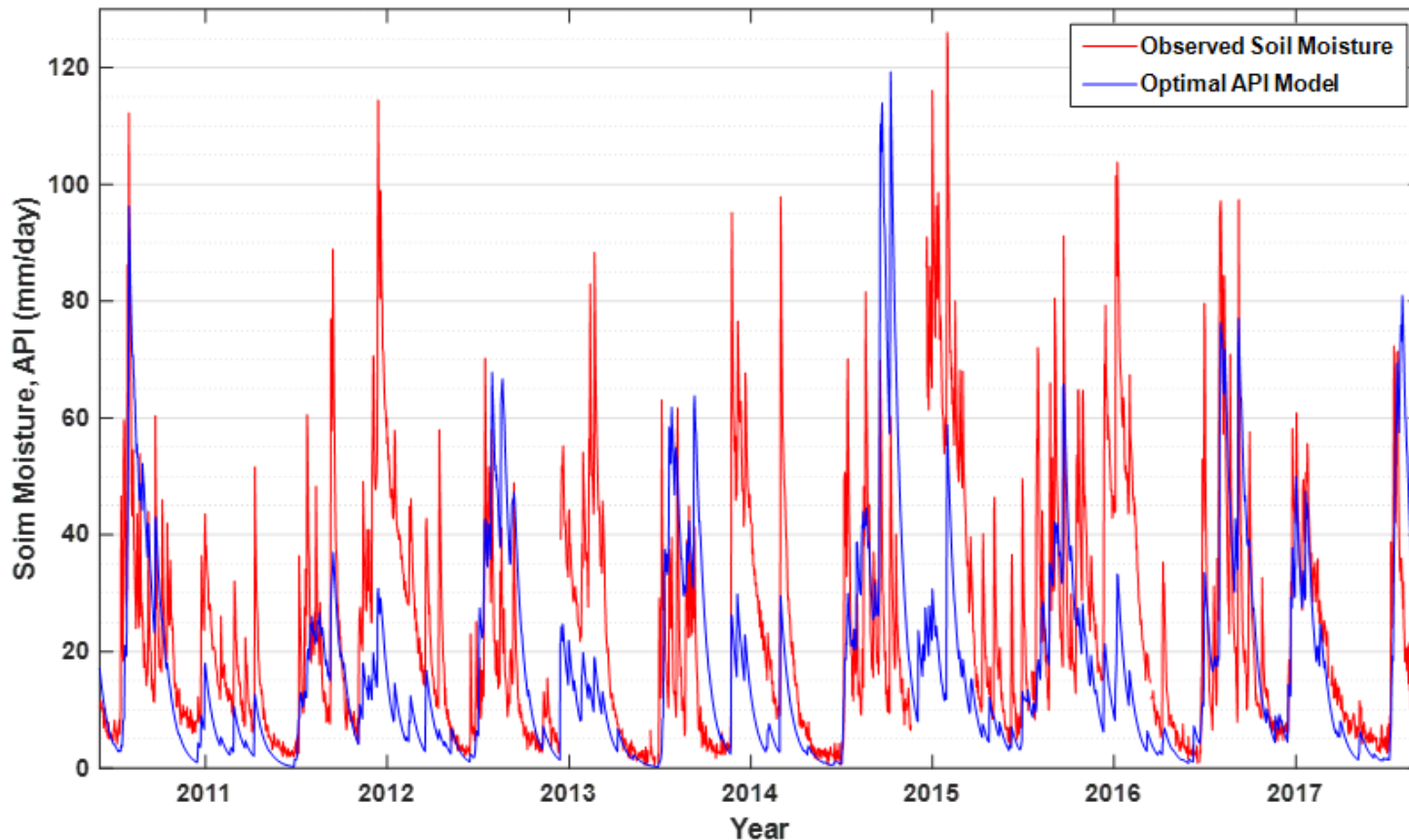
# Model results for the Walnut Gulch Experimental Watershed



# Example of applications using simple hydrologic engineering methods



# Cosmic-ray neutron sensors can also be used for simpler hydrologic and agricultural engineering applications



$$API(t) = P(t) + k.P(t-1) + k^2.P(t-2) + \dots$$

or

$$API(t) = k.API(t-1) + P(t)$$

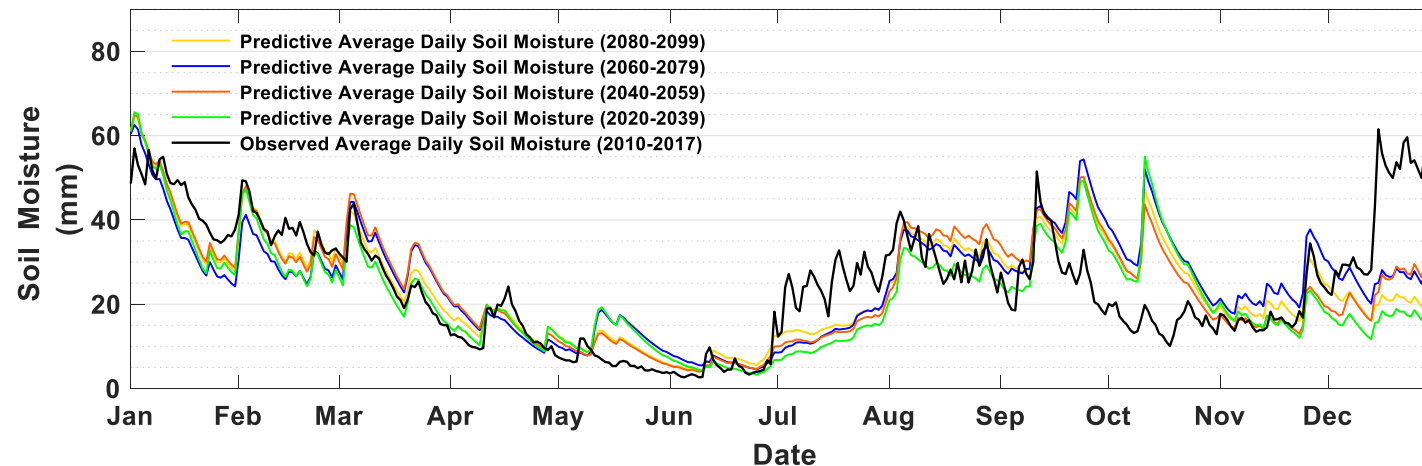
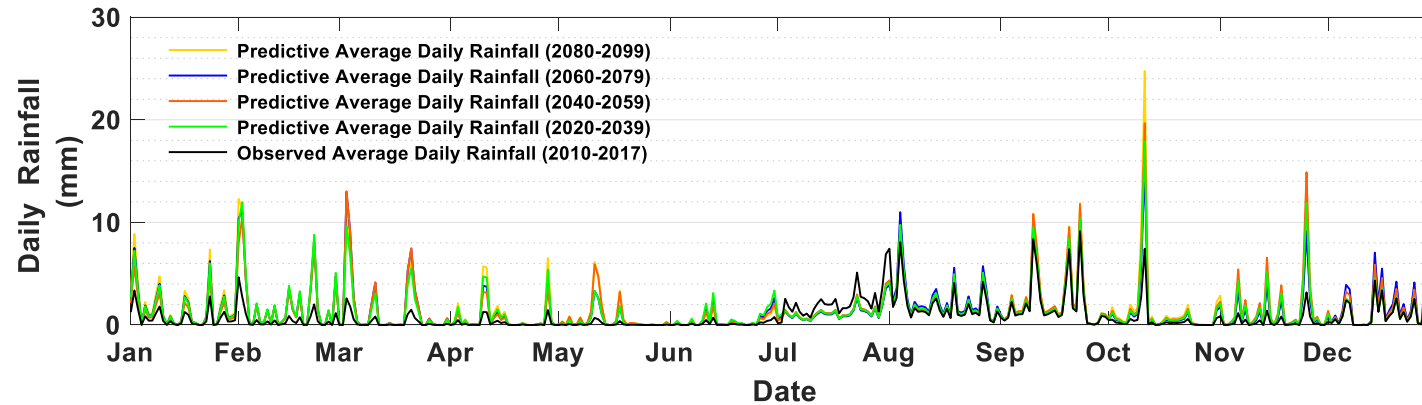
where

API(t) = is the Antecedent  
Precipitation Index for day  $t$

$k$  is an empirical decay factor ( $k < 1$ )

$P(t)$  is precipitation for day  $t$

# Simple API model allows for easy scenario analysis for wetness conditions of the region



# Final remarks

- Environmental modeling applications are interested in predicting many hydrological processes
- The spatial and temporal scales of cosmic-ray neutron sensors fills the gap between point-scale and satellite remote sensing methods, and are strongly related to establishment of hyper-resolution hydrological models
- Cosmic-ray neutron sensing observations can be used with models for calibration, data assimilation, or independent structural checks

# Structure for the day

## **Lecture 1:** *Factors affecting the accuracy of cosmic-ray neutron counts and estimated soil moisture*

- You learned how individual factors may impact the measured cosmic-ray neutron signals and ultimately can be propagated to the derived soil moisture estimation

## **Lecture 2:** *Efforts to a harmonized data processing approach for cosmic-ray neutron sensors*

- You learned that because individual networks apply different quality control and data processing protocols, adoption of global use of cosmic-ray neutron sensing technology has been limited, but recent efforts to provide harmonized datasets can mitigate some of the issues

## **Lecture 3:** *The use of cosmic-ray neutron sensors in hydrometeorology*

- You learned a few examples of applications using cosmic-ray neutron sensing technology in combination with land surface and hydrological models as well as from simple hydrologic and agricultural engineering approaches

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