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**abdus salam**  
international centre for theoretical physics

**COURSE ON CLIMATE VARIABILITY  
STUDIES IN THE OCEAN  
"Tracing & Modelling the Ocean Variability"  
16 - 27 June 2003**

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**Tracing and Modelling the Ocean Variability -II**

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Cambridge MA, USA**

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***Please note: These are preliminary notes intended for internal distribution only.***



# Tracing and modeling ocean variability

ICTP – June 2003

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variability {  
Ocean's 'weather'  
Geostrophic eddies

**Discuss:**

1. Eddies: are they important for climate?
2. Eddies and their role in setting structure of thermocline, mixing....

# Eddies, mixing and large-scale ocean circulation

1 Role of geostrophic eddies in diabatic processes

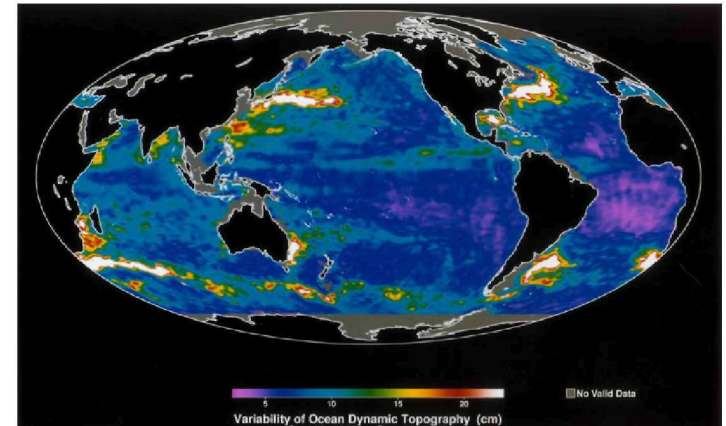
2 Maintenance of the thermocline in a turbulent ocean

# 1 Eddies and diabatic processes

Eulerian mean

$$\mathbf{v} \cdot \nabla \bar{b} = \frac{\partial}{\partial z} \left( k_v \frac{\partial \bar{b}}{\partial z} \right) - \nabla \cdot (\overline{\mathbf{v}' b'})$$

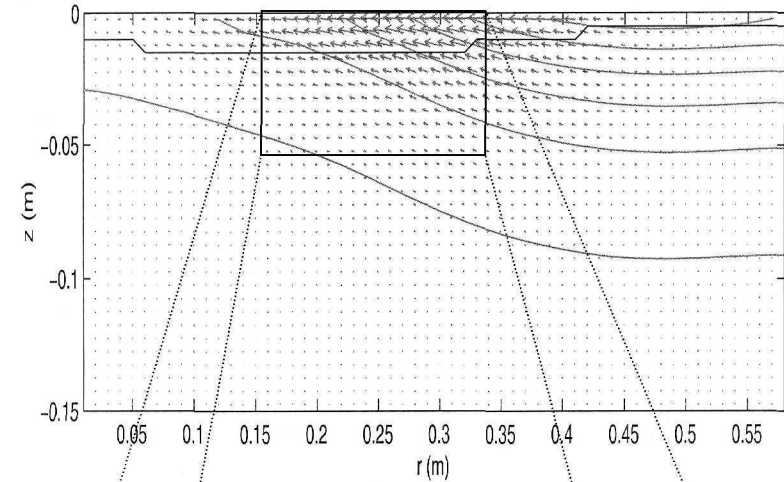
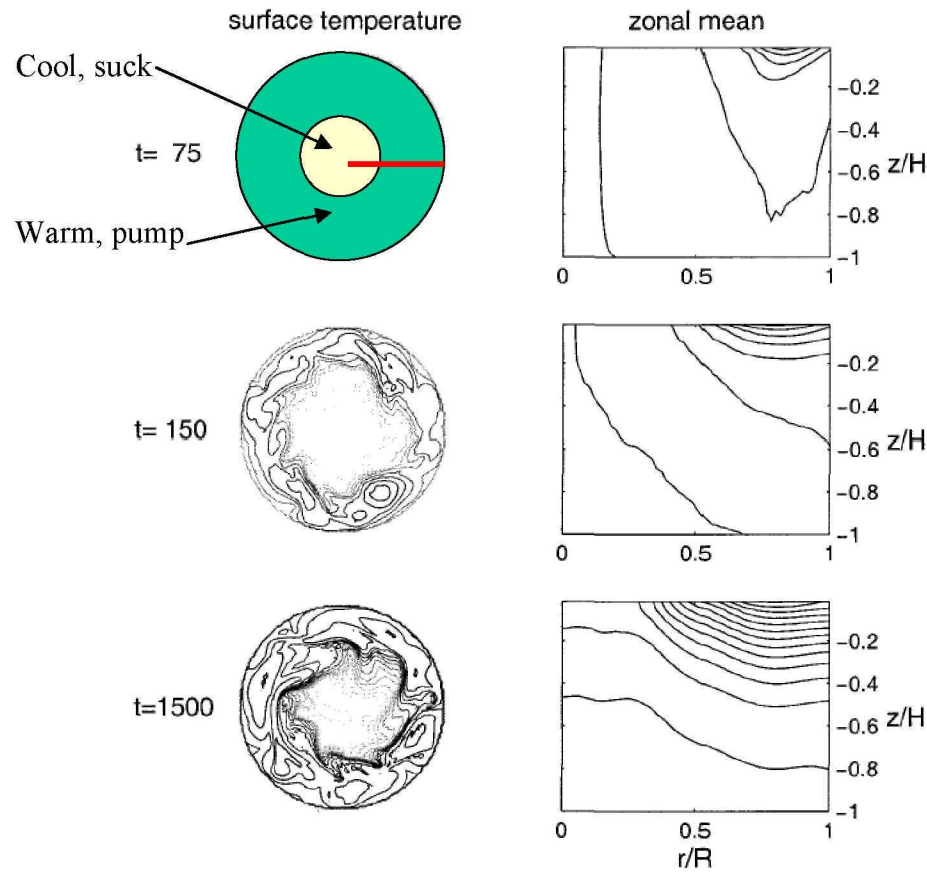
usually ignored because



- eddy fluxes are only large in boundary currents and jets.  $\nabla \cdot (\overline{\mathbf{v}' b'}) \rightarrow 0$  over most of ocean most of the time.
- eddy fluxes are adiabatic anyway, aren't they?  $\nabla \cdot (\overline{\mathbf{v}' b'})$  can then be written entirely as an *advective* flux.

# Diapycnal eddy fluxes

Karsten and Marshall, 2002

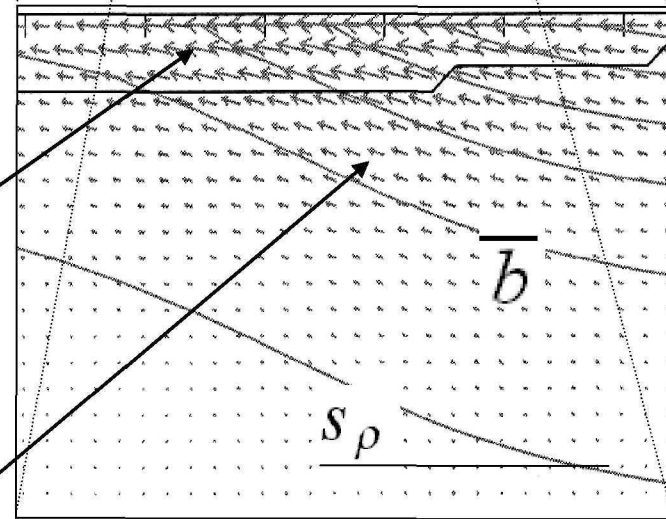


$$\overline{\mathbf{v}'b'} = (\overline{v'b'}, \overline{w'b'})$$

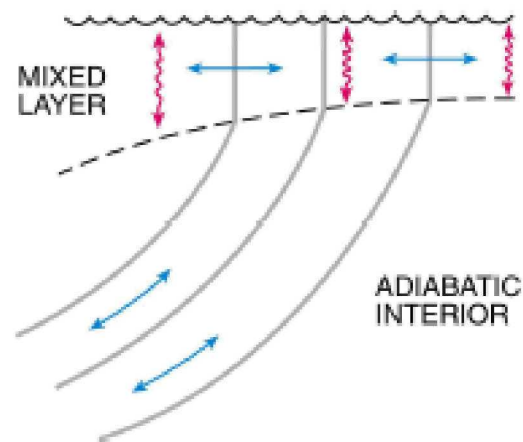
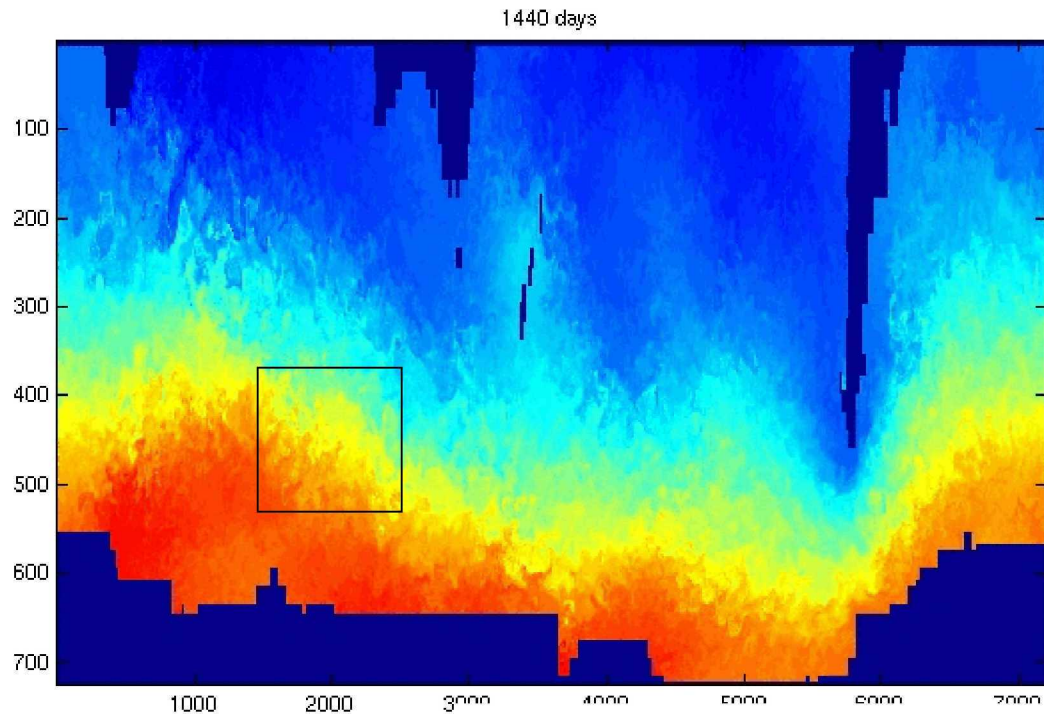
$$\mu = 0$$

$$\mu = \left( \frac{\overline{w'b'}}{\overline{v'b'}} \right) \left( \frac{1}{s_\rho} \right)$$

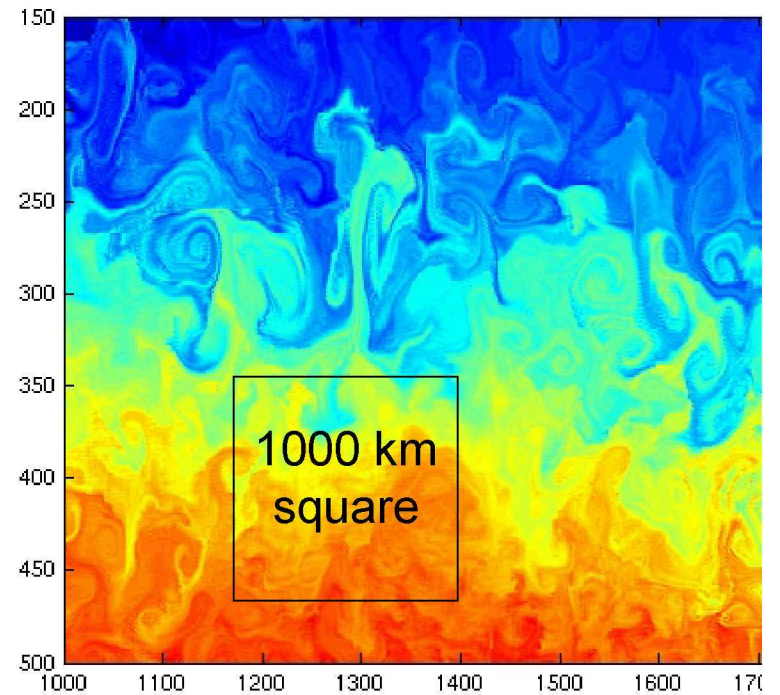
$$\mu = 1$$



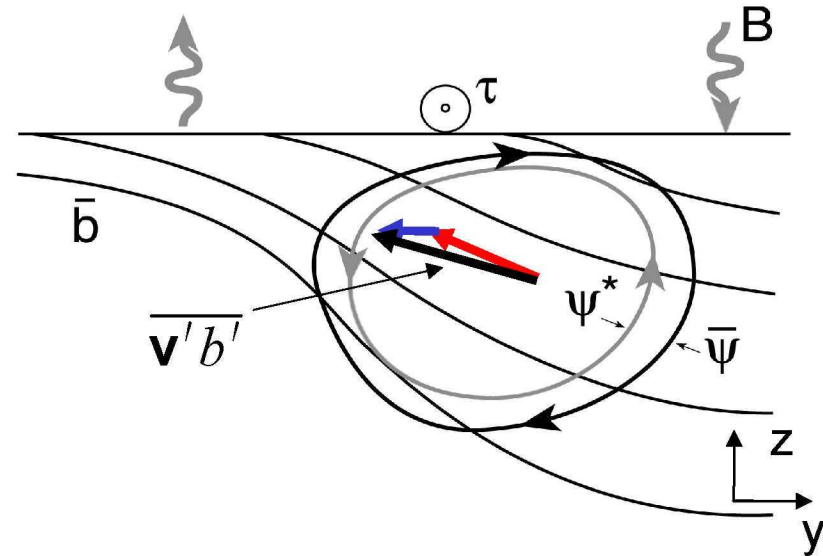
# Evolution of passive tracer



Idealized tracer driven by surface currents in ACC



# Residual mean



$$\mathbf{v}_R \cdot \nabla \bar{b} = \frac{\partial}{\partial z} \left( k_v \frac{\partial \bar{b}}{\partial z} \right) - (1 - \mu) \nabla \cdot (\overline{\mathbf{v}'_h b'})$$

where  $\mathbf{v}_R = \bar{\mathbf{v}} + \mathbf{v}^*$

Diapycnal  
eddy flux

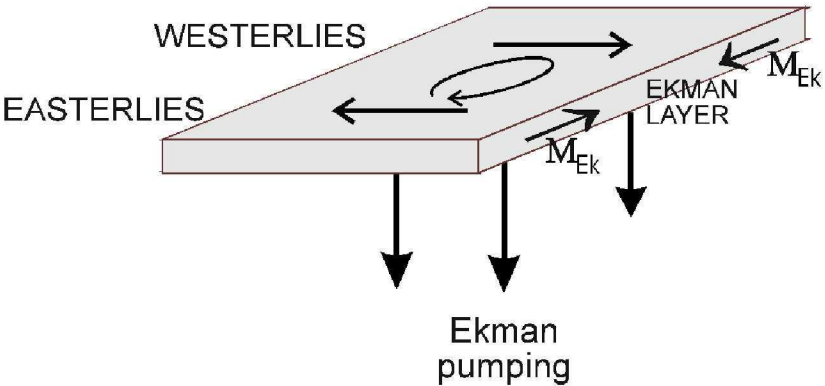
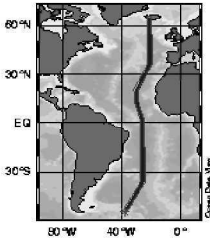
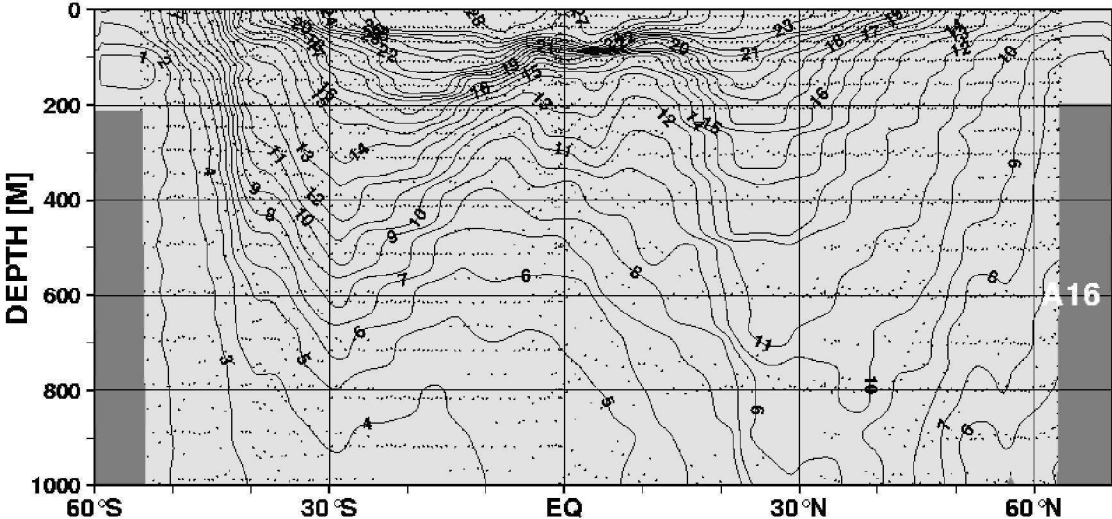
Diabatic parameter

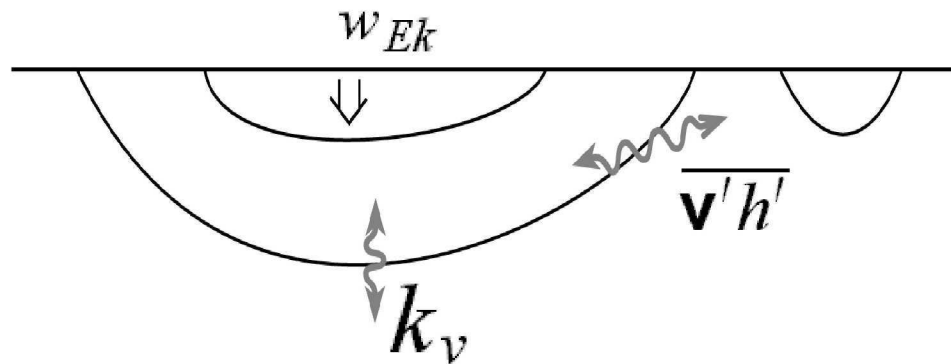
Held & Schneider



2

# Maintenance of the thermocline





Prevailing view:

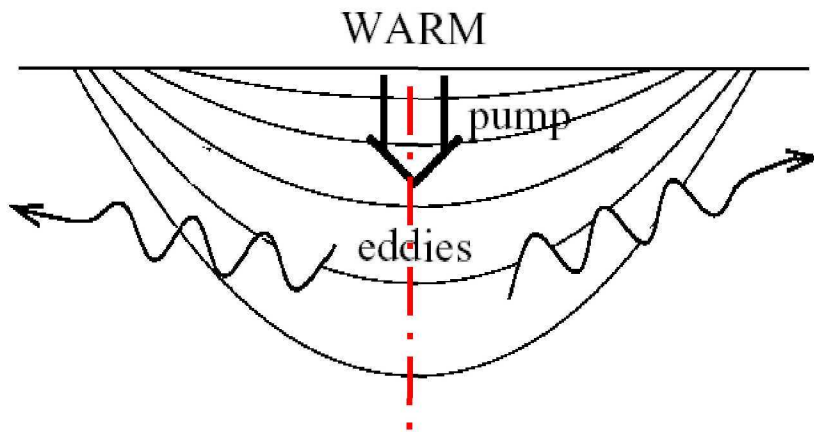
heat gets diffused away by ‘small-scale’ mixing

Alternative hypothesis:

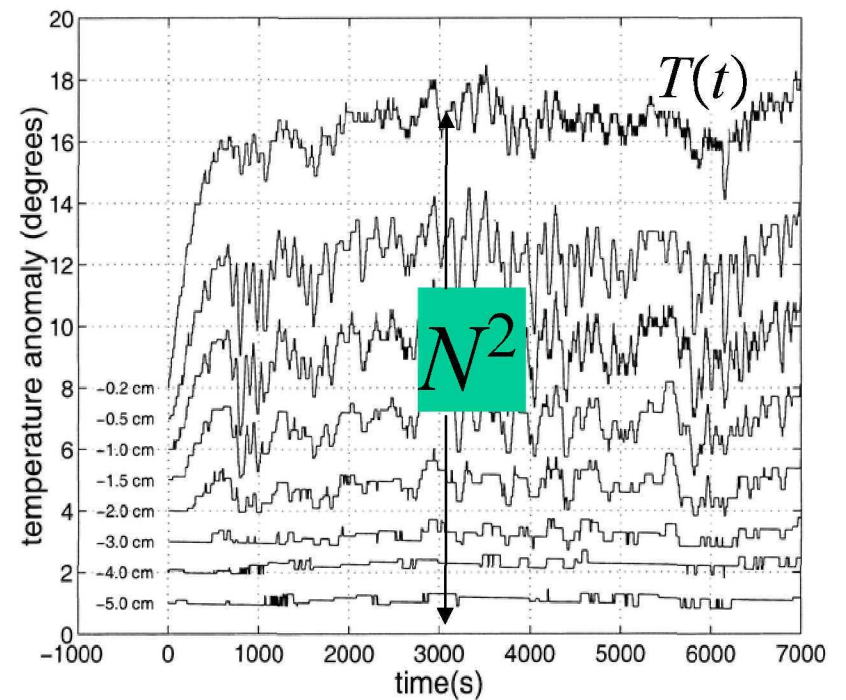
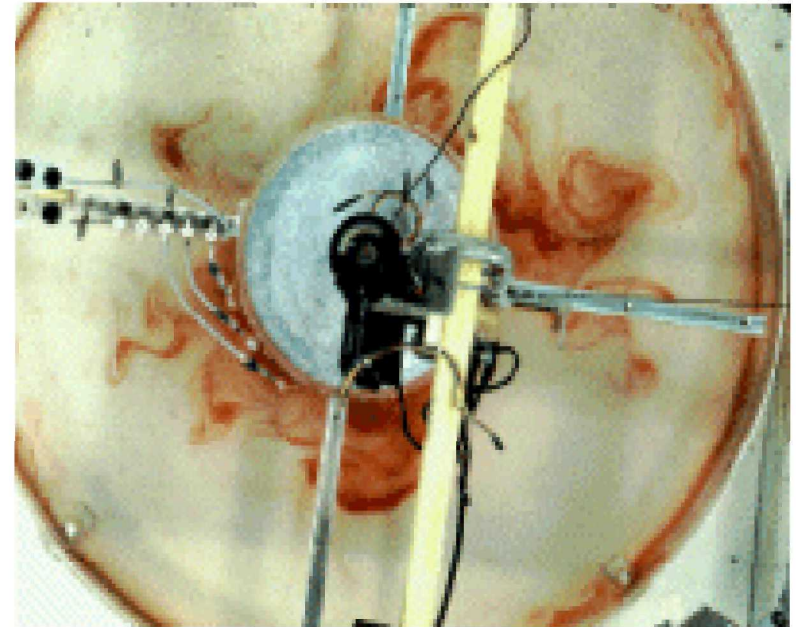
eddies play a central diabatic role, fluxing heat laterally

# Laboratory abstraction: warm pumped lenses

'f'-plane



Marshall et al. (2002)



# Theory

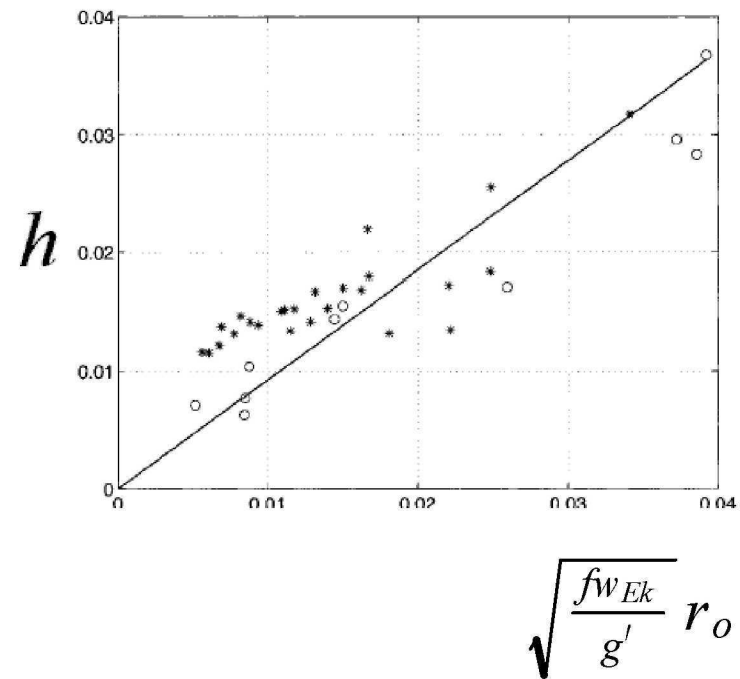
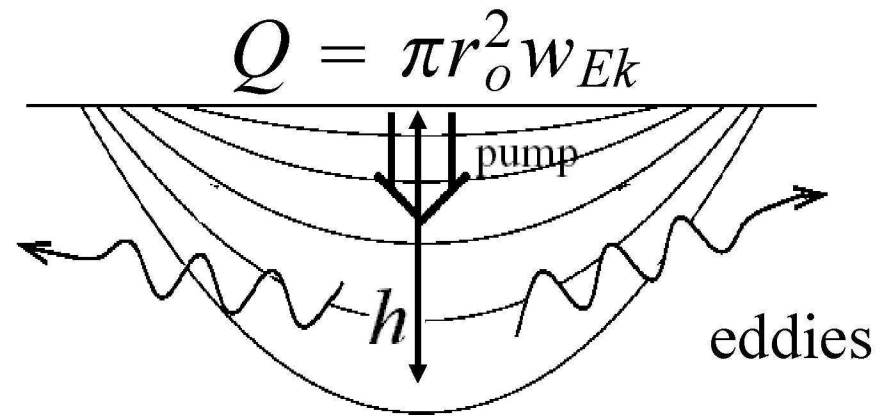
$$Q = 2\pi r_o \overline{v'h'}$$

$$\overline{v'h'} = cuh$$

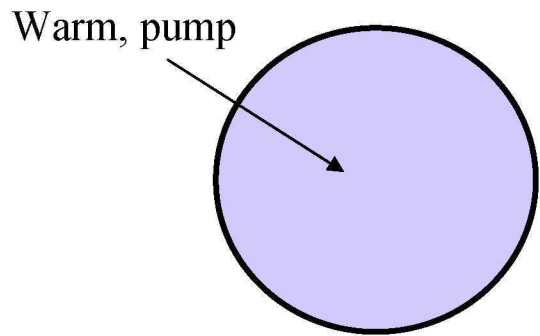
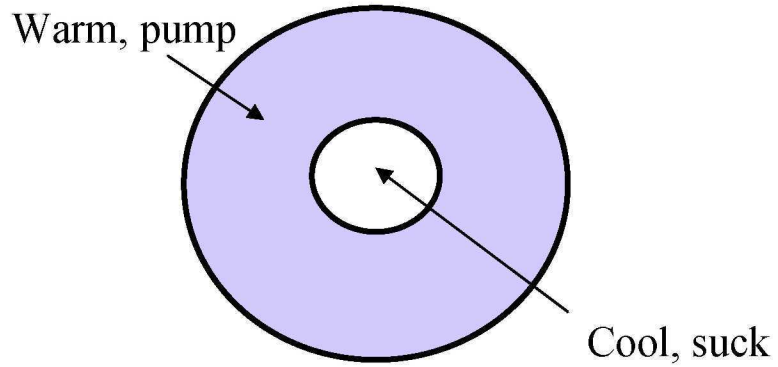
$$u = \frac{g'h}{fr_o}$$

$$h \sim \sqrt{\frac{f w_{Ek}}{g'}} r_o$$

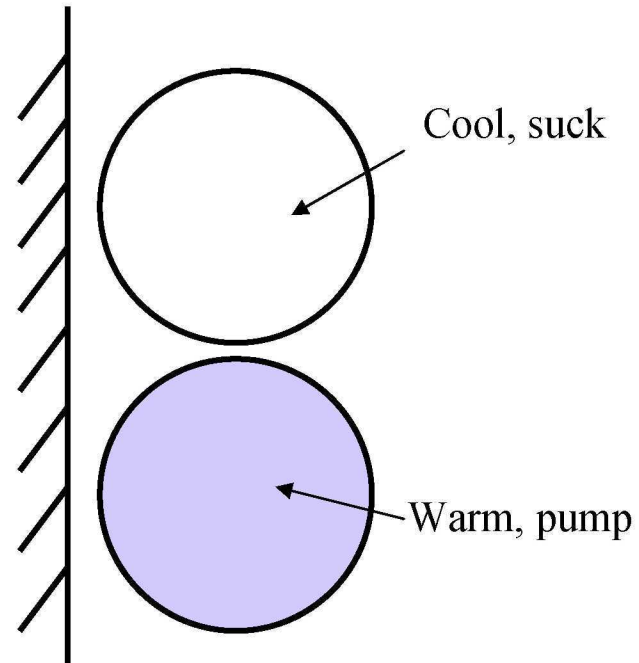
$$u \sim \sqrt{\frac{g' w_{Ek}}{f}}$$



# Variations on the theme



$f$ -plane

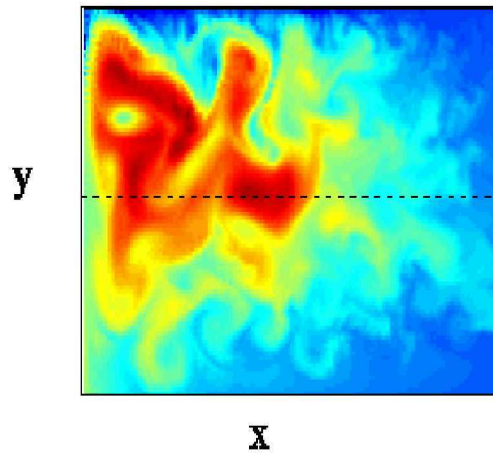


$\beta$ -plane gyres

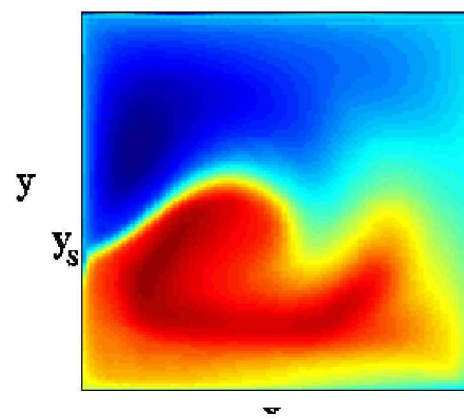
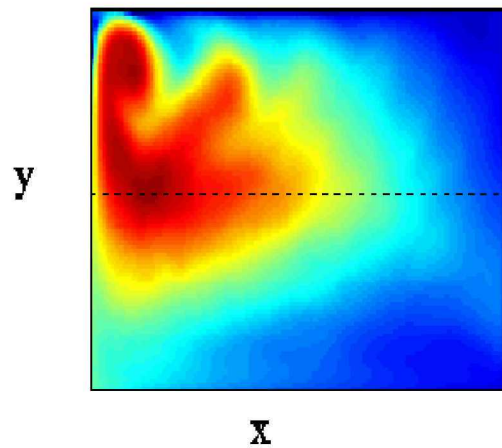
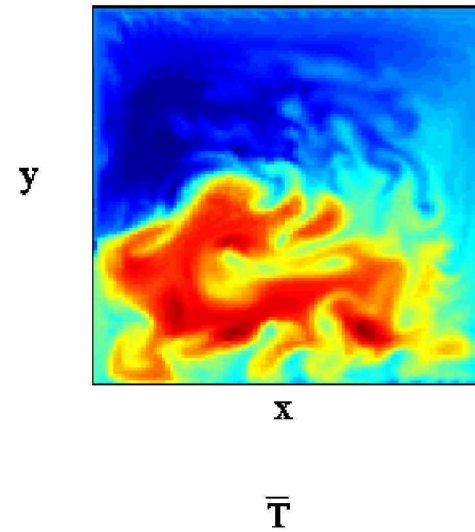
# $\beta$ -plane gyres

In collaboration with  
Timour Radko

## Single



## Double



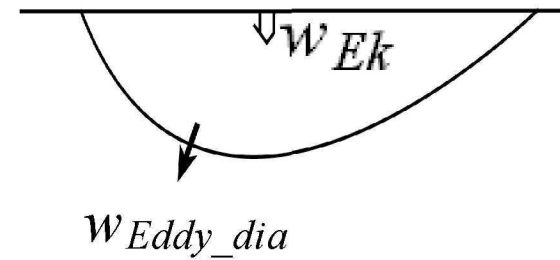
# Diagnostic framework

Buoyancy

$$\nabla \cdot (\mathbf{v} \bar{b}) = D_{Eddy} + D_{smallscale}$$

where

$$D_{Eddy} = -\nabla \cdot (\overline{\mathbf{v}' b'})$$



Define

$$w_{Eddy\_dia} = \frac{D_{Eddy}}{\bar{b}_z}$$

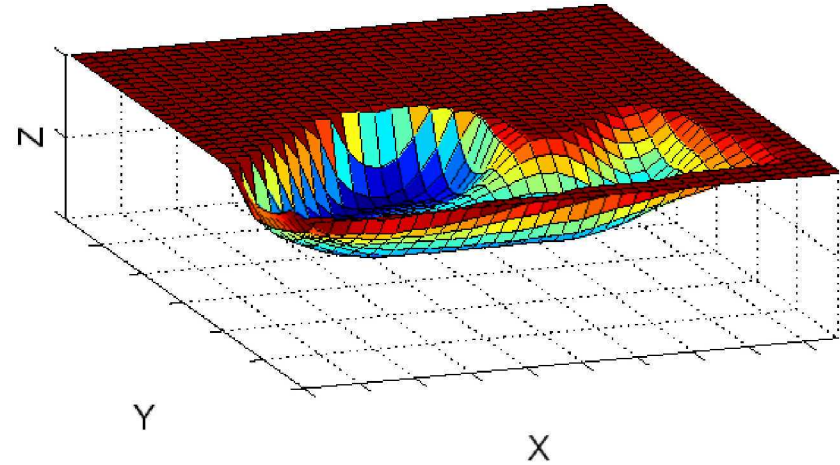
Evaluate

$$\alpha = \frac{w_{Eddy\_dia}}{w_{Ek}}$$

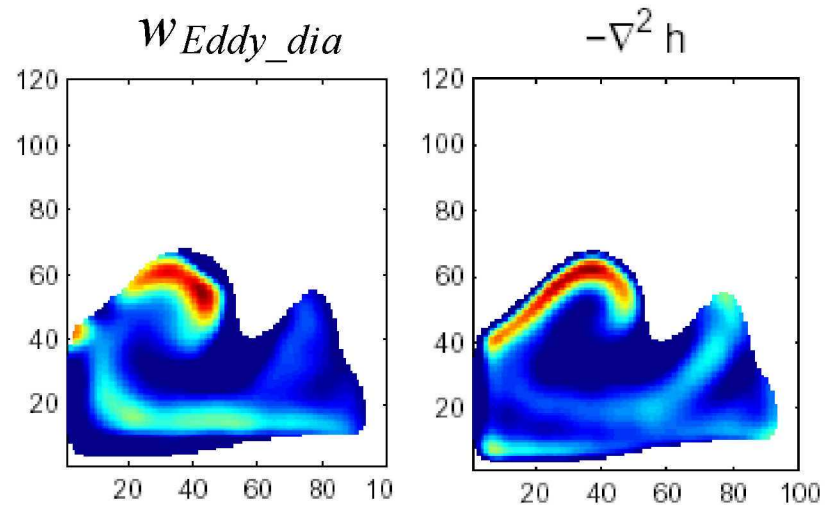
How is the volume balanced?

$$\alpha = \frac{w_{Eddy\_dia}}{w_{Ek}}$$

$$\alpha = 0.87$$



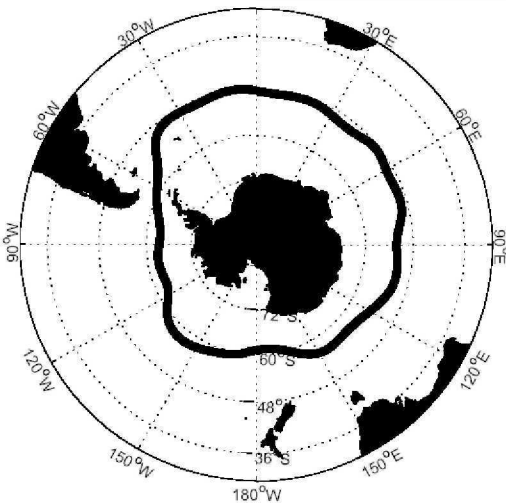
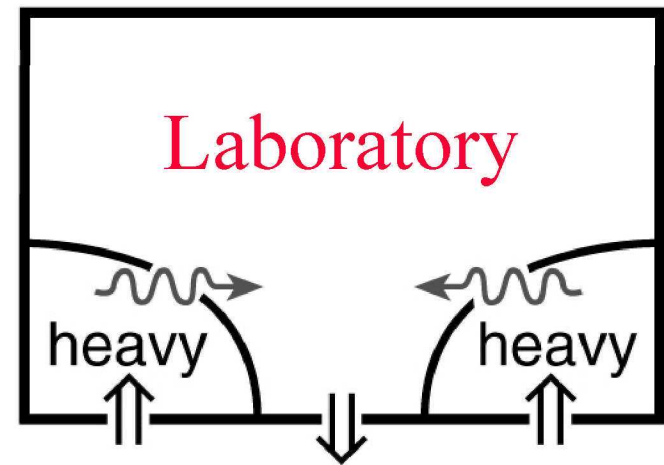
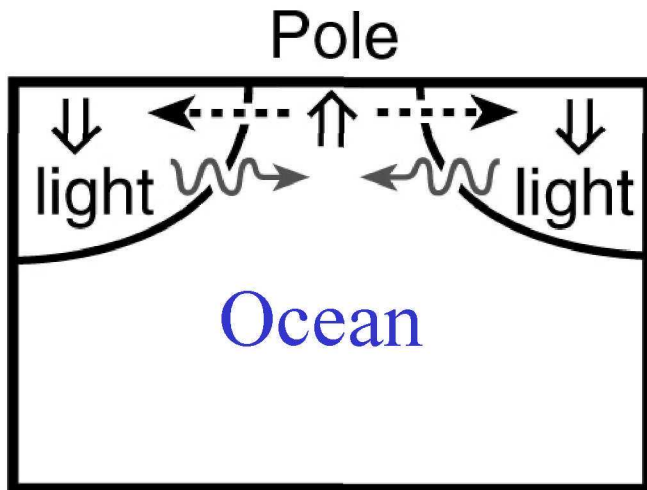
T	$\alpha$
21	0.88
19	0.86
18	0.85
17	0.78
15	0.73
13	0.61





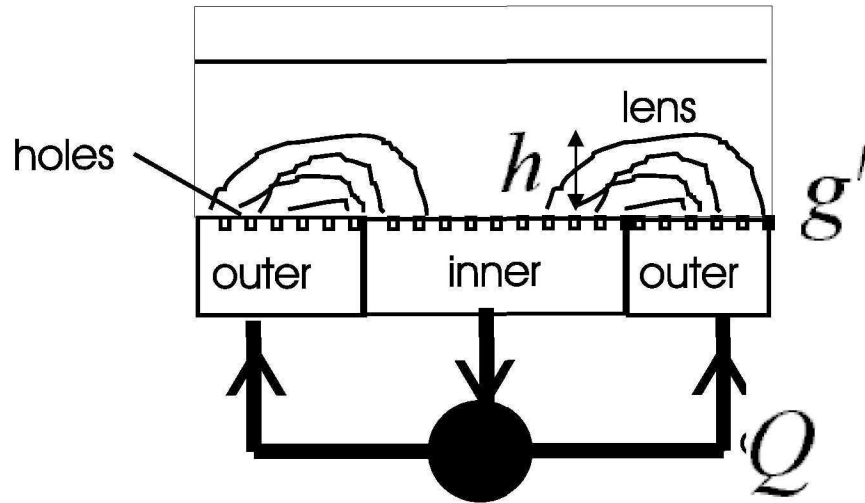
another example

## Laboratory Model of Circumpolar Current

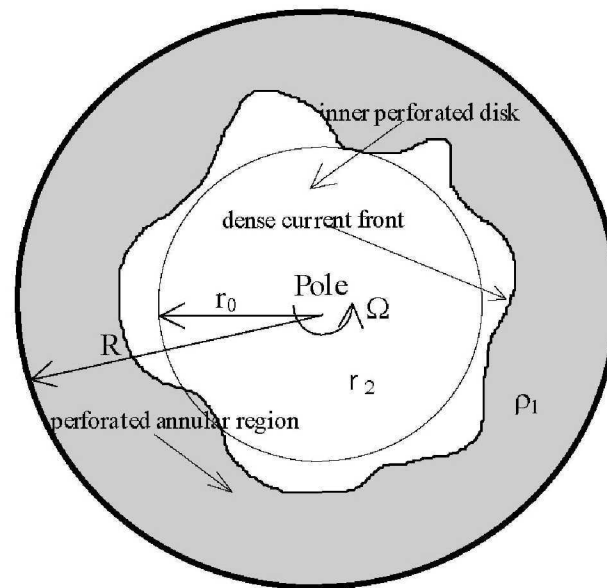


# Apparatus

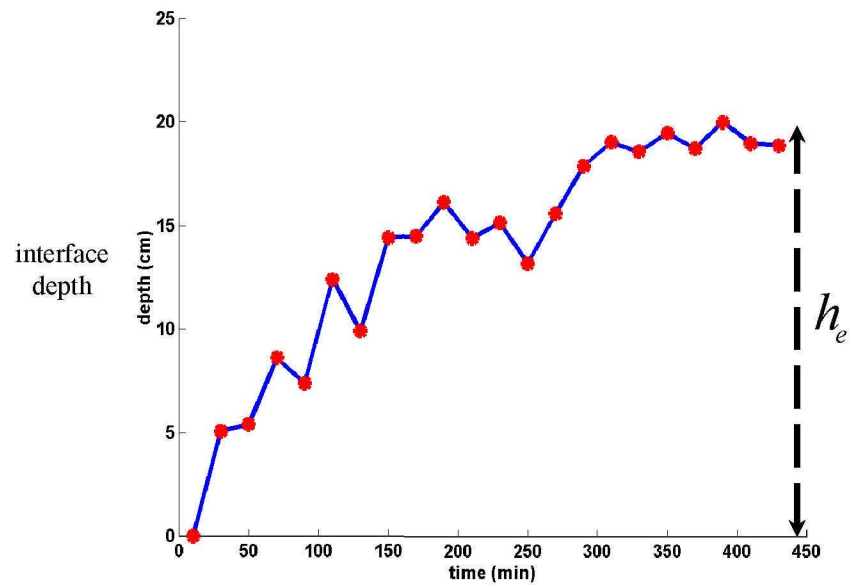
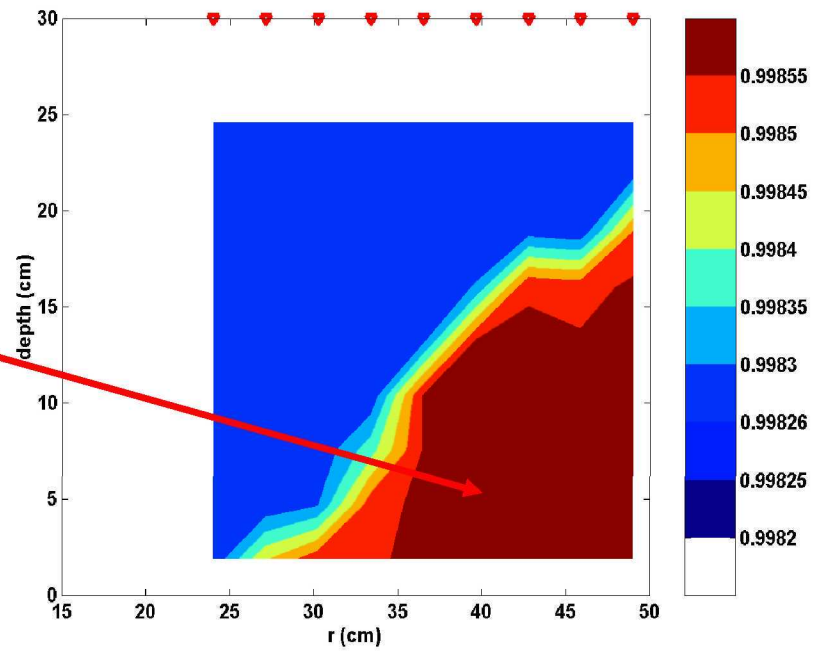
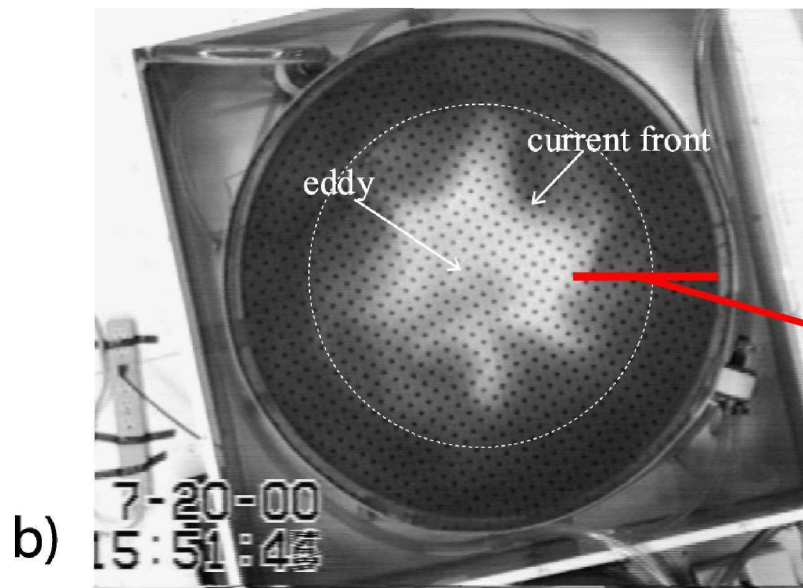
$$f = 2\Omega$$



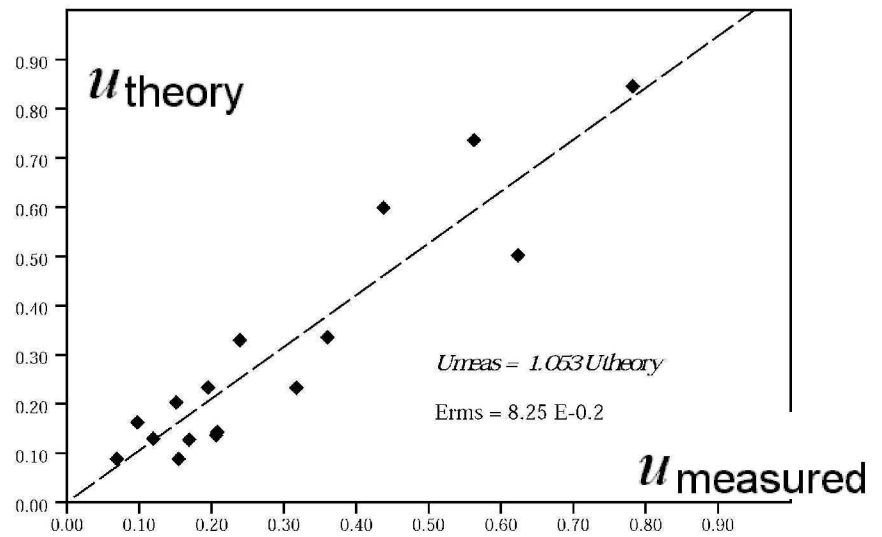
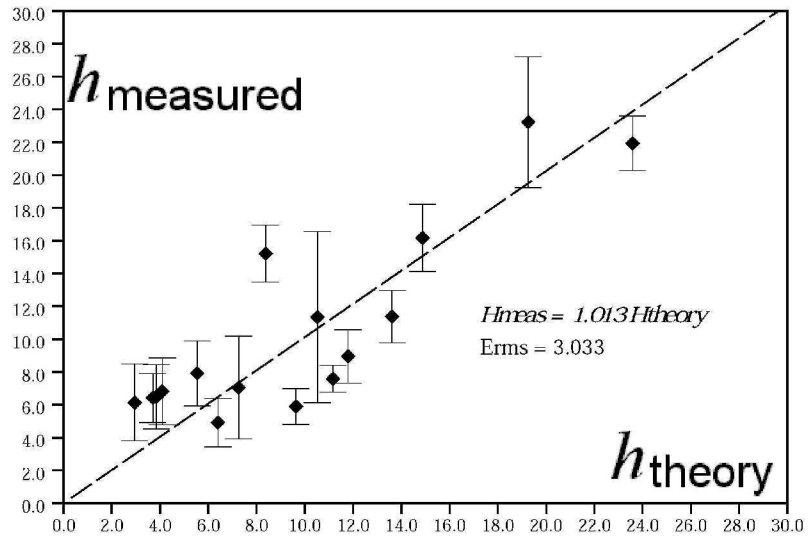
Claudia Cenedese  
Jack Whitehead



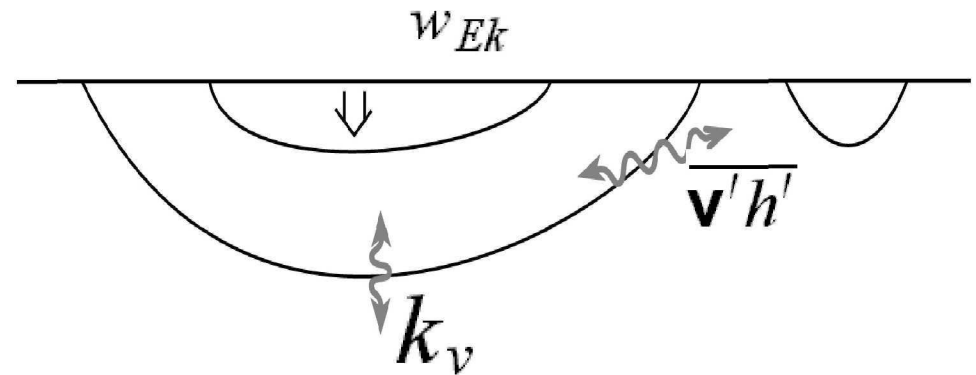




$$h \sim \sqrt{\frac{f w_{EK}}{g'}} r_0$$



## Conclusions



Geostrophic eddy transfer is often erroneously neglected in favor of small scale mixing in discussions of large scale buoyancy balances.

Numerical and laboratory experiments suggest that eddy transfer, rather than small-scale mixing, may play a central role in maintaining the structure of the thermocline, particularly in the southern ocean, but also in subtropical ocean gyres.

Geostrophic eddies are likely to play a key role in diabatic processes, particularly near the upper surface, where eddy fluxes inevitably have a diapycnal component.