the
abdus salam
international centre for theoretical physics

Icrr 40th Anniversaxy

SMR.1555-3

Workshop on
Nuclear Reaction Data and Nuclear Reactors:
Physics, Design and Safety

16 February - 12 March 2004

WIMS Exercises

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These are preliminary lecture notes, intended only for distribution to participants


## HOMOGENEOUS CALCULATIONS

No spatial problems
Use full library groups
Solve neutron balance equations
In any energy group, for a critical system
Source of neutrons $=$ Removal rate.

| Source | $=\quad$ Fission neutrons + Inscatter |
| :--- | :--- |
| Removal $=$ | Absorption + Outscatter + Leakage |

For a 2-group calculation without upscatter or leakage
Group 1: $\quad \frac{\mathbf{1}}{\mathbf{k}_{\infty}}\left(v \Sigma_{\mathbf{f}_{1}} \phi_{1}+v \Sigma_{\mathbf{f}_{2}} \phi_{\mathbf{2}}\right)=\Sigma_{\mathbf{a}_{1}} \phi_{\mathbf{1}}+\Sigma_{\mathbf{1 2}} \phi_{1}$
Group 2: $\quad \Sigma_{12} \phi_{1}=\Sigma_{\mathbf{a}_{2}} \phi_{2}$

## INFINITE HOMOGENEOUS

Infinite medium of one material: k-infinity
Typical variable parameters are: fissile concentration (H:Pu) enrichment
degree of poisoning
Leakage can be introduced (buckling): k-effective.
Very quick and cheap.


Examples: $\mathrm{Pu}(\mathrm{NO} 3) 4$ storage; UO2(NO3)2 evaporator.
Warning: Parameters that give the maximum k-infinity may
not be those that give the maximum k-effective

## WORKSHOP 1

> k-effective for an Oak Ridge Sphere

Use DSN method
Solution composition:

| Hydrogen | 0.066394 |
| :--- | :--- |
| Oxygen | 0.033592 |
| Nitrogen | $1.11 \mathrm{e}-4$ |
| U234 | $4.090 \mathrm{e}-7$ |
| U235 | $3.6185 \mathrm{e}-5$ |
| U236 | $2.2 \mathrm{e}-7$ |
| U238 | $1.985 \mathrm{e}-6$ |

Calculate buckling for sphere of radius 61.01 cm with extrapolation of 7 cm

## READDATA

Input is in the form of:

- CODEWORD (upper or lower case) followed by numerical data items.

Only the first 4 letters of a codeword are relevant.
Data items may be real or integer or containing E for exponent, but must contain no blanks(eg. 1.0e-2).

Data items for one codeword may occupy several lines (without \$ signs) but must not extend beyond column 72.

Repeated items may be input as:
13@101* (instead of 11111111111110 1)
$3(123)$ * (instead of 123123123 )

An asterisk(*) indicates that all the following information on the current line is a comment

## WORKSHOP 1

$$
\begin{align*}
& \text { k-effective }=\frac{\text { k-infinity }}{1+\mathbf{M}^{2} \mathbf{B g}^{2}}  \tag{1}\\
& M^{2}=\frac{\text { k-infinity }-1}{\mathbf{B}_{\mathbf{C}}^{2}} \tag{2}
\end{align*}
$$

When k-effective $=1$

$$
\begin{equation*}
\mathbf{B}_{\mathbf{c}}{ }^{2}=\mathbf{B}_{\underline{g}}{ }^{2} \tag{3}
\end{equation*}
$$

## WORKSHOP 1

Taking the output from CHAIN 14 to obtain k-infinity from the case without Buckling and $\mathrm{Bc}^{2}$ from the case with Buckling and using equations 1,2 and 3 , find:
(a) The dimensions of a sphere whose contents are just critical at various Pu concentrations.
(b) The dimensions of a sphere whose contents have k-effective $=0.95$, at various Pu concentrations.

$$
\text { Assume }=7 \mathrm{~cm}
$$

## WORKSHOP 1 <br> CRITICAL CYLINDER RADII



## WORKSHOP 2

k-effective for a regular PWR benchmark lattice

1. U235 enrichment $3.0 \mathrm{w} / \mathrm{o}$
2. Square pin pitch 1.32 cm
3. Assume: fuel density $10.4 \mathrm{~g} / \mathrm{cc}$
fuel radius 0.5065 cm
aluminium wrapper radius 0.5199 cm
clad radius $\quad 0.54685 \mathrm{~cm}$
clad material $7.8 \mathrm{~g} / \mathrm{cc} \quad$ (Fe 58\% Ni 12\% Cr 18\%)
4. Bucklings: radial 0.00415 , axial 0.00215

## PIN CELL CALCULATION



## WORKSHOP 2

Required input data

| Prelude: | pincell <br> dsn <br> nmesh/nregion/nmaterial |
| :--- | :--- |
| Main: | material <br> annulus <br> mesh |
| Edit:: | buckling |

## WORKSHOP 2

$$
\begin{aligned}
& \mathbf{B}_{\mathrm{c}}^{2}=\frac{2.405^{2}}{(\mathbf{R}+\lambda)^{2}}+\frac{\pi^{2}}{(\mathbf{H}+2 \lambda)^{2}} \\
& \mathrm{~N}=\frac{\mathbf{R}^{2}}{\mathbf{R}_{\mathrm{p}}^{2}}
\end{aligned}
$$

where N is the number of pins
Rp is the pin cell radius

$$
\lambda=6.5 \mathrm{~cm} .
$$

1) For each of the pin cell radii considered, use Bc2 from the output to obtain the radial dimension of a cylindrical array of pins which is just critical.
2) How many pins will fit into the cylindrical array?

## WORKSHOP 2



## LEAKAGE OPTIONS in CHAIN 14

Homogeneous solutions based on:

Diagonal Transport Corrected Flux Solution B1 Flux Solution

Diffusion Coefficients based on:

Benoist 3-region model
Transport cross sections
Ariadne method

## WORKSHOP 3

## LEAKAGE and REACTION RATES

Repeat workshop 2 pincell: Using PERSEUS
adding all combinations of LEAKAGE CALCULATIONS adding 2-group reaction edits for U235 and U238

## WORKSHOP 3

## LEAKAGE EDITS

```
BEEONE to request diagonal transport and B1
    solutions
DIFFUSION to request all diffusion coefficient options
REACTION RATES
```

LEAKAGE to select spectrum
PARTITION to select structure
REACTION to select nuclides
Repeat workshop 2 pincell:

## WORKSHOP 4

Repeat Workshop 3 with CONDENSEDGROUP STRUCTURE


## WORKSHOP 4

Input Data

To Condense 'main transport' group structure to give energy bounds at 821 and 9 KeV , and at 4.00 .625 and 0.14 eV .

PRELUDE data: NGROUP
MAIN data:
EDIT data:
FEWGROUPS (define the 6 groups)
THERMAL

Output

Compare 69 group k-effective values from
WORKSHOP 3 and WORKSHOP 4

## RBMK FUEL ELEMENT



## WORKSHOP 5

k-infinity for an infinite array of RBMK assemblies

1. Model an RBMK assembly using ring-smearing and DSN
2. Fuel density $10.0 \mathrm{~g} / \mathrm{cc}$ and $2 \mathrm{w} / \mathrm{o}$ enrichment, temperature 1000k
3. Clad Zr , density $6.5 \mathrm{~g} / \mathrm{cc}$, temperature 600 k
4. Coolant H2O, density $0.5 \mathrm{~g} / \mathrm{cc}$, temperature 550 k
5. Moderator carbon, density $1.8 \mathrm{~g} / \mathrm{cc}$, temperature 500 k
6. Centre 'tie rod' and pressure tube also Zr
7. Condensed main transport group structure ( $\sim 6$ groups)

## WORKSHOP 5

Required Input
PRELUDE Data: CLUSTER geometry
NREGION to define annuli with rods

MAIN Data:
RODSUB data to define fuel rods
ARRAY data to position rods in cluster

## WORKSHOP 6

## DSN CLUSTER with BURNUP

Required Input

Prelude Data: NMATERIAL to define number of burnable materials
Main Data: POWER to define rating and steps
Edit Data: ALPHA Option

Exit one short step to get equilibrium Xe , and a few longer steps to get k at $4000 \mathrm{MWd} /$ te

## WORKSHOP 7

Required Input:

Prelude Data: NRODS
Main Data: $\quad$ Note the MESH data
Note the ANNULUS radii
PLOT to get a 'picture'
Edit Data: As for Workshop 5

Compare k values from Workshop 5 and 7
\{Optional extras: (a) try SQUARE boundary
(b) place 'empty tubes at corners\}

## SUMMARY OF WORKSHOPS

1. Homogeneous calculations
2. DSN Pincell in 69 groups
3. PERSEUS Pincell with leakage in 69 groups
4. As 3 with condensation to 6 groups
5. RBMK assembly - DSN ring-smearing

6 As 5 with depletion
7. As 5 with PIJ explicit geometry

