



the **abdus salam**  
international centre for theoretical physics

*ICTP 40th Anniversary*

SMR.1572 - 30

**Workshop on  
Novel States and Phase Transitions in Highly Correlated Matter**

**12 - 23 July 2004**

---

**MnSi**

**Christian PFLEIDERER  
Physikalisches Institut  
Universität Karlsruhe  
Wolfgang-Gaede-Str. 1  
76131 Karlsruhe  
GERMANY**

---

These are preliminary lecture notes, intended only for distribution to participants

MnSi

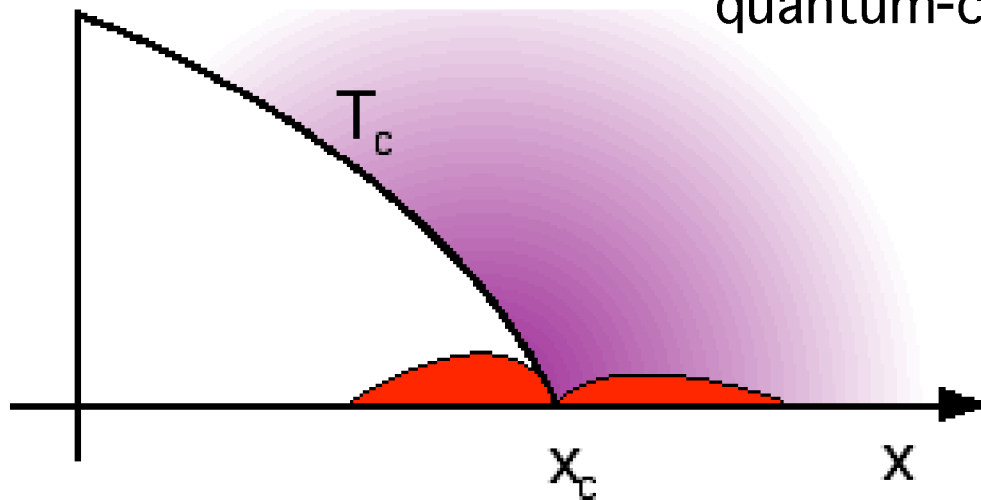
---

Christian Pfeiderer  
Universität Karlsruhe



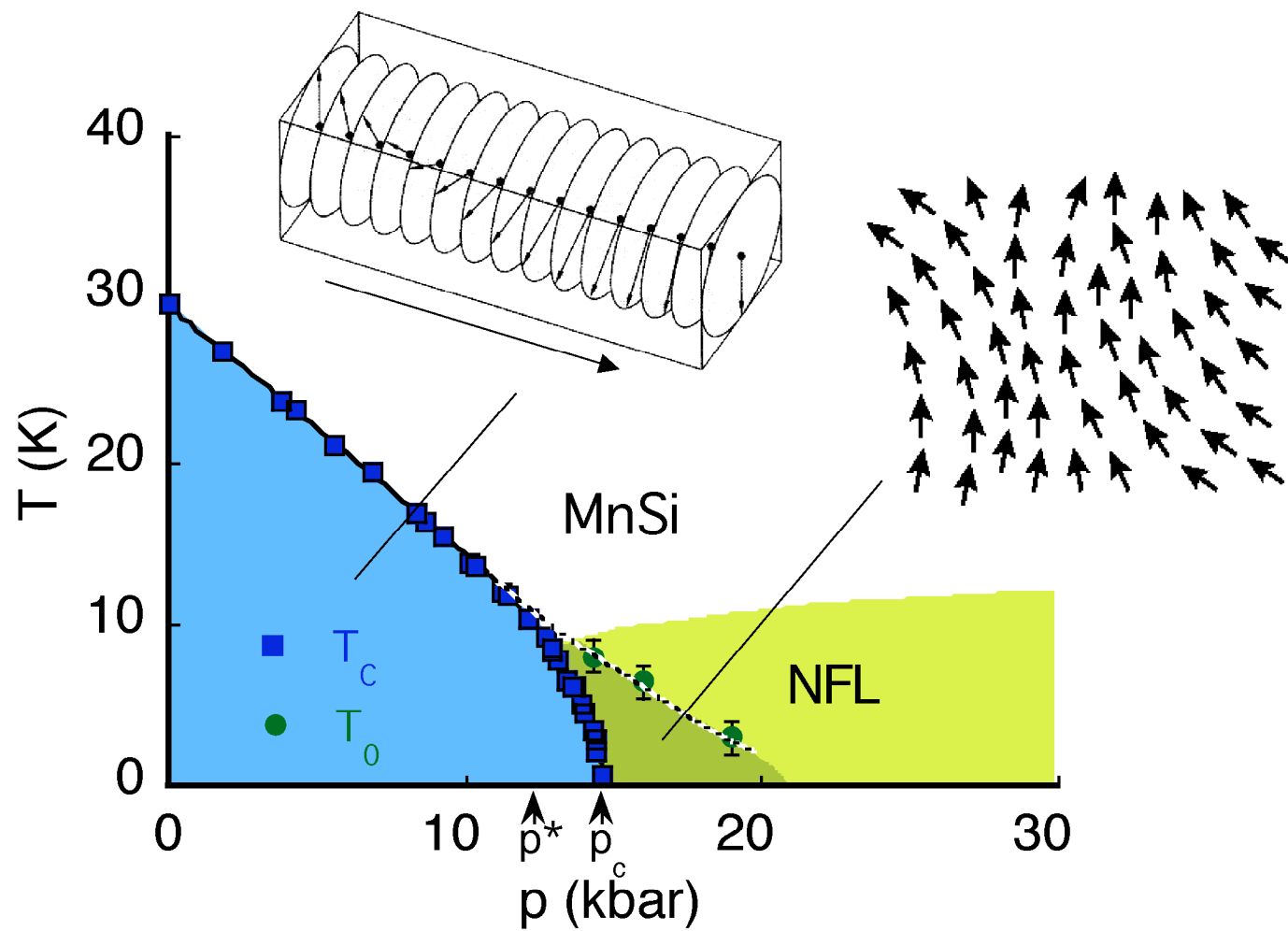
# Why study quantum phase transitions?

for  $T_c \rightarrow 0$ :  
quantum-critical continuum



at  $T=0$  exact QM wave function:  
quantum coherence  $\Rightarrow$  novel states

# Instead of an Overview ...



# Weak “Itinerant-Electron” Ferromagnets

pre-60ies: local moment ferrimagnets  
⇒ Dzyaloshinsky-Moriya interaction

1958 B. Matthias: ferromagnetism in  $\text{ZrZn}_2$  (C15 Laves phase)

„FM without magnetic elements“

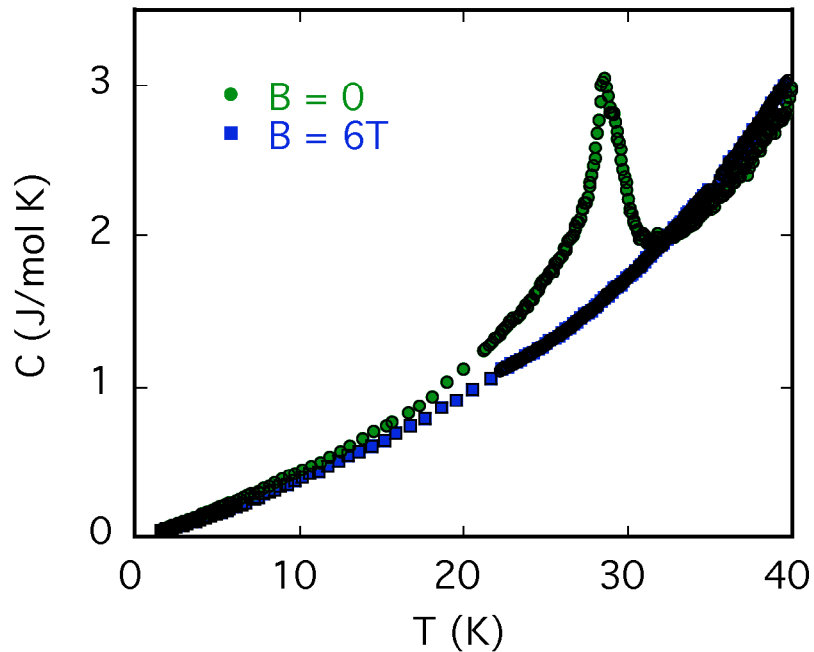
„new“ material class:  $\text{MnSi}$ ,  $\text{Sc}_3\text{In}$ ,  $\text{Ni}_3\text{Al}$ ,  $\text{YNi}_3$ ,  $\text{CoS}_2$ , ...

- low ordering temperature
- small ordered moments
- large Curie-Weiss moment
- unsaturated magnetisation  $M(B)$
- small entropy of order

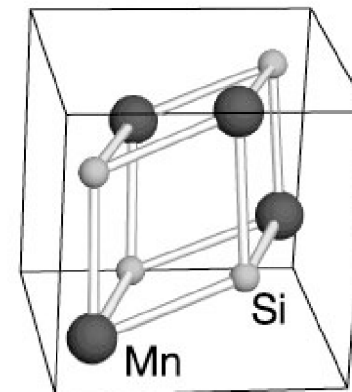
⇒ weakly exchange split band magnets

⇒ self-consistent linear response theory (Moriya, Lonzarich, ...)

# Some Basic Properties of MnSi



very nice metallurgy!!  
“perfect” single crystals!



Ferromag.:  $T_C \approx 30$  K  
 $\mu_s \approx 0.4$  mB/f.u.  
 $\gamma \approx 38$  mJ/mol K<sup>2</sup>

n-scattering & dHvA : spin-split FL  
QP dressing cloud: paramagnons

B20 structure:  
no inversion symmetry

# Search for quantum criticality

„break-through“ for paramagnons:

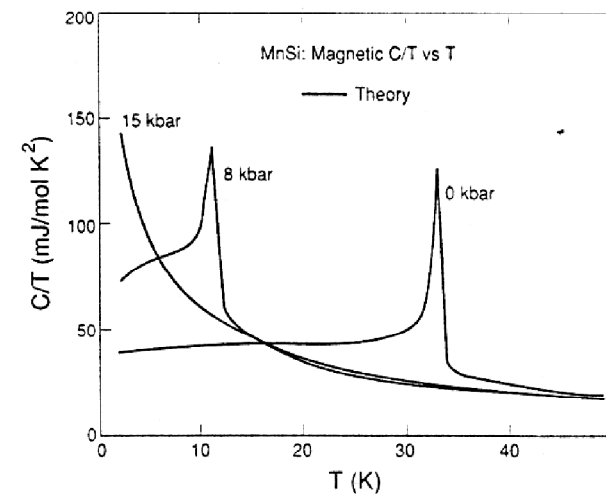
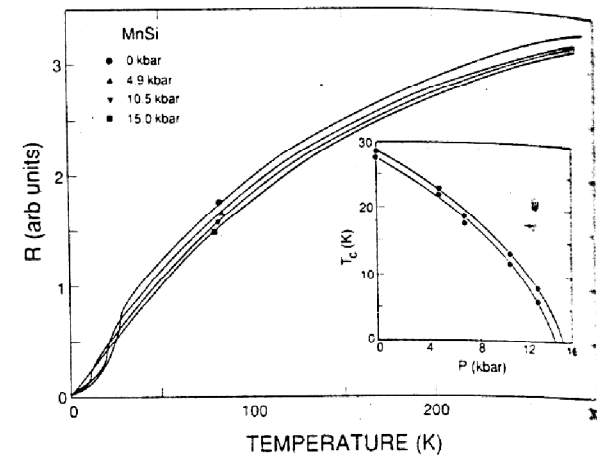
$$\langle m_\nu^2 \rangle = 4\hbar \int \frac{d^3\mathbf{q}}{(2\pi)^3} \int_0^\infty \frac{d\omega}{2\pi} n(\omega) \text{Im}\chi_\nu(\mathbf{q}, \omega)$$

origin of Curie-Weiss susceptibility:  
itinerant spin fluctuations

quantitative estimate of  $T_c$

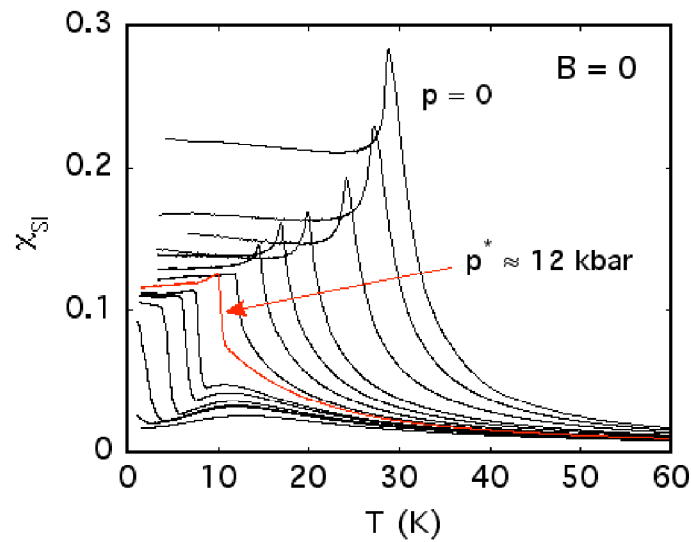
$$T_c = 2.387cM_0^{3/2} \frac{(\hbar\gamma)^{1/4}}{k_B}$$

(MnSi expt.: 29.5K, calc.: 31K)

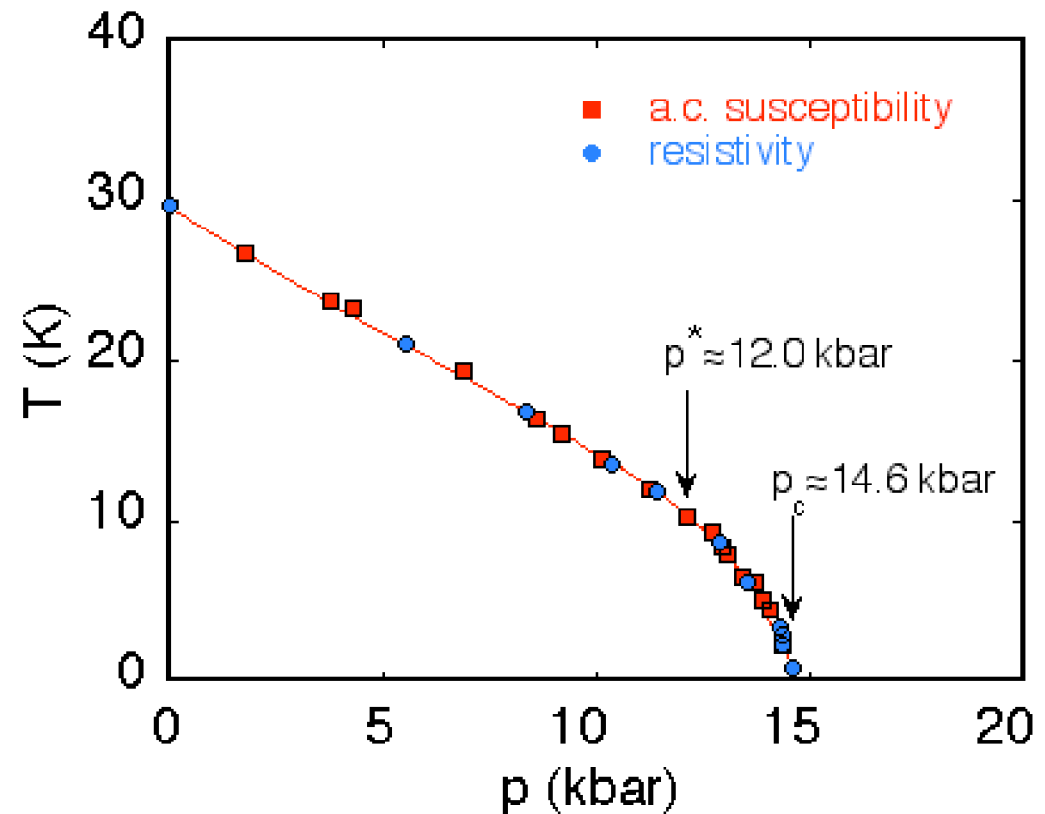




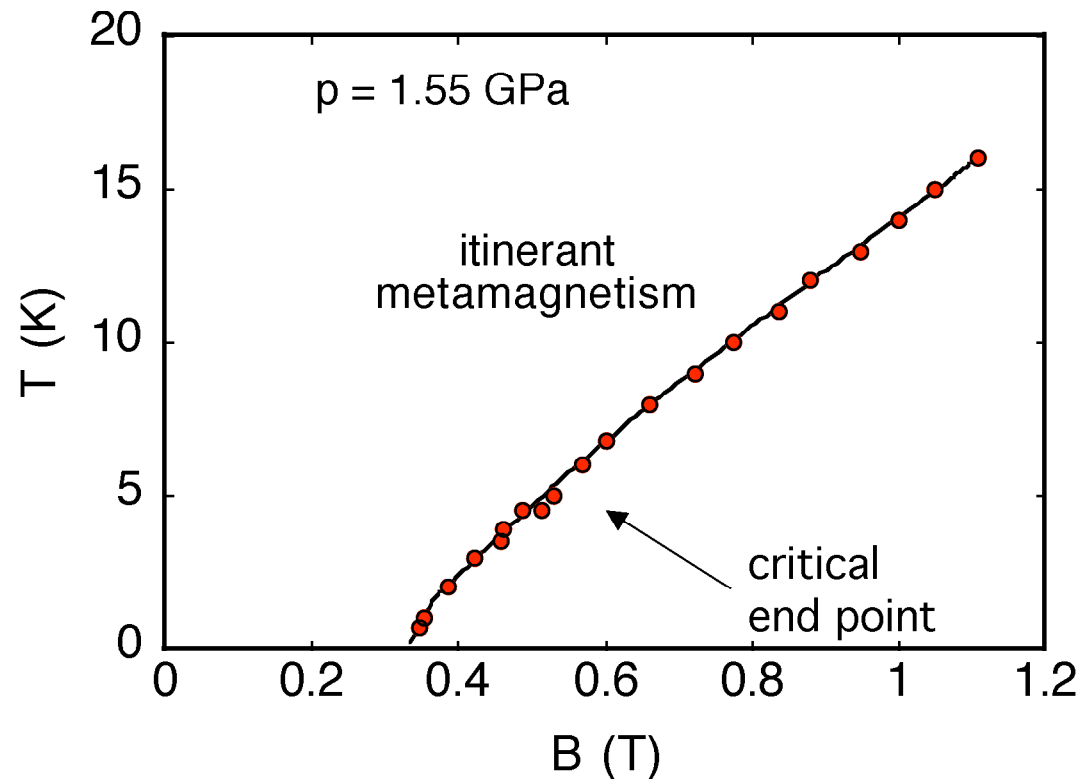
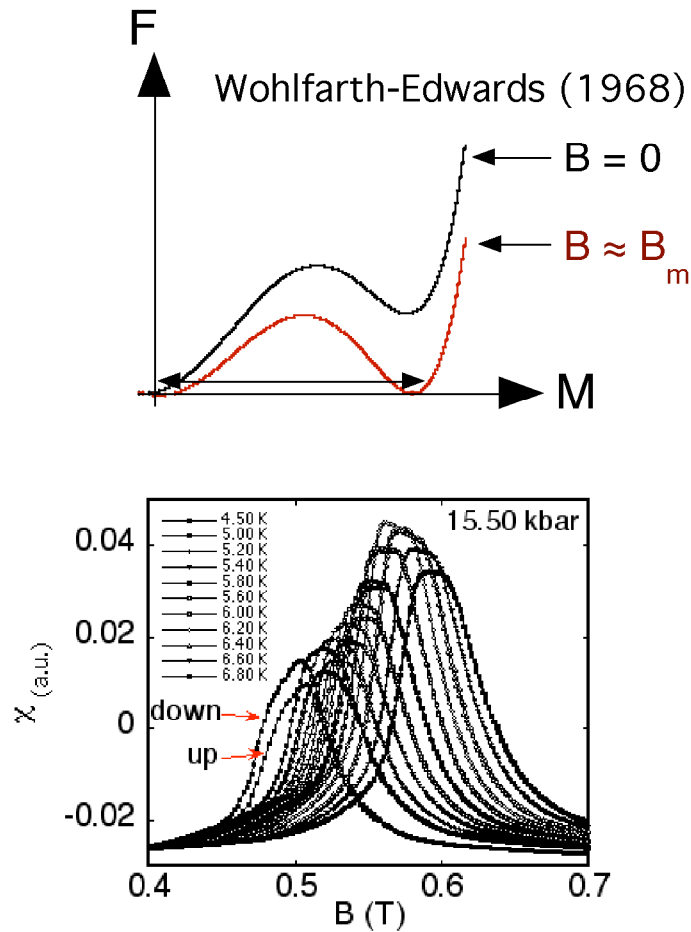
# Pressure-Temperature Phase Diagram of MnSi



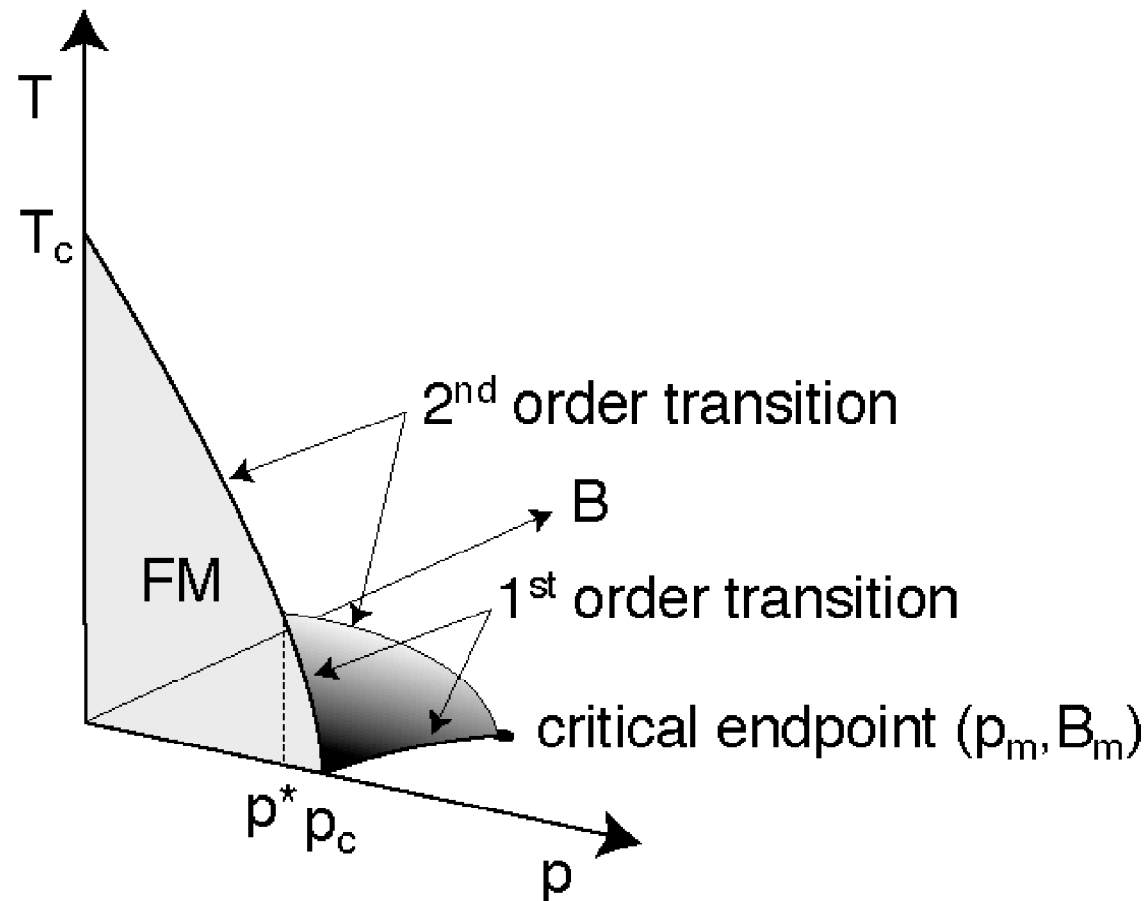
1<sup>st</sup> order transition  
for  $12 \text{ kbar} < p < p_c$



# Itinerant Metamagnetism in MnSi for $p > p_c$

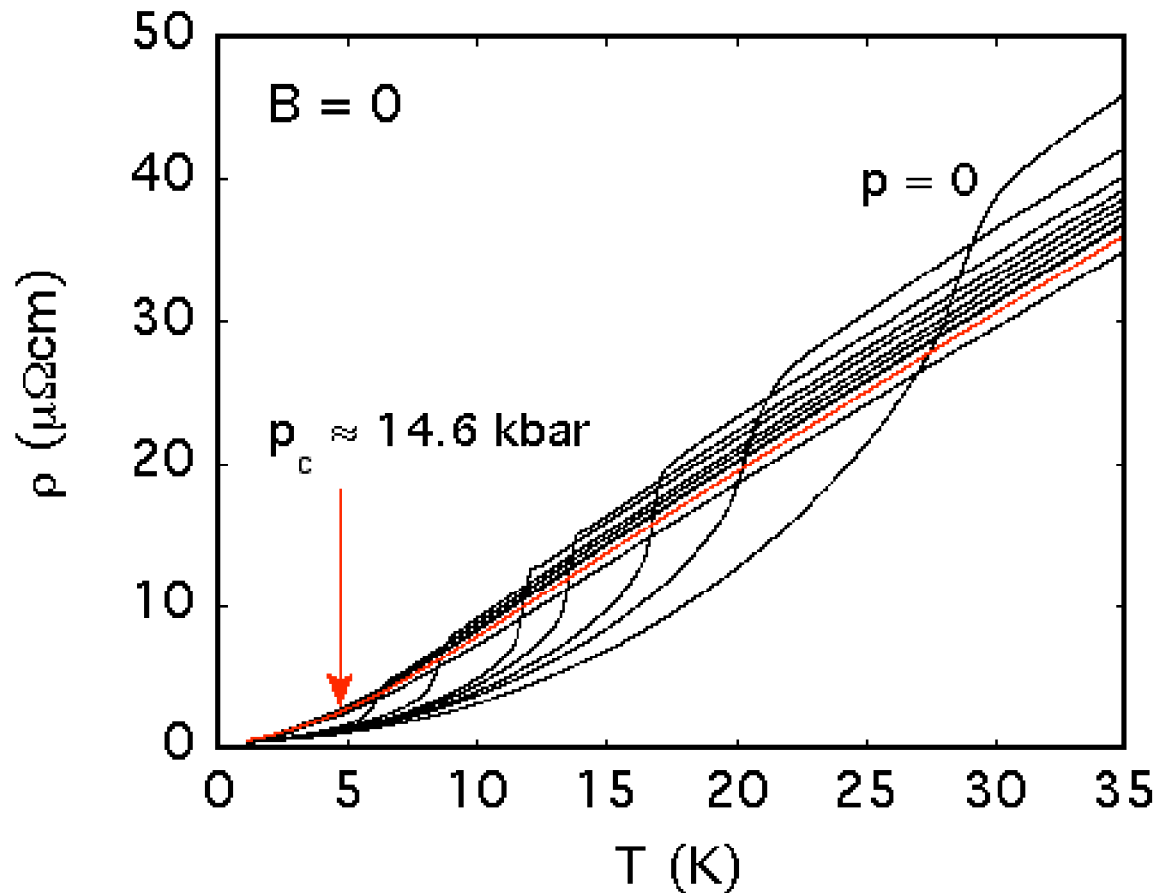


# Proposed Generic Phase Diagram of Itinerant Ferromagnets



also seen in:  
 $ZrZn_2$   
 $UGe_2$  (PRL 89 147504)

# Pressure Dependence of the Electrical Resistivity

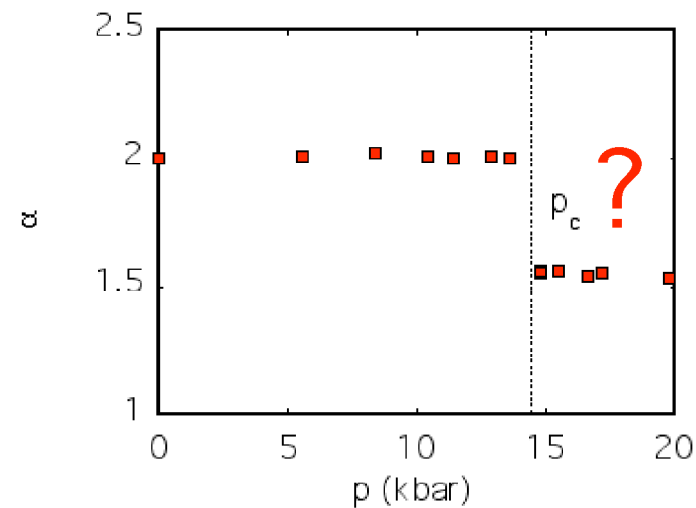
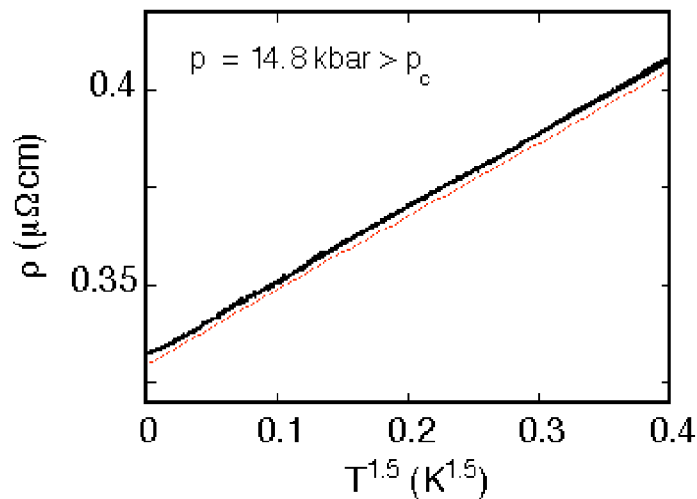
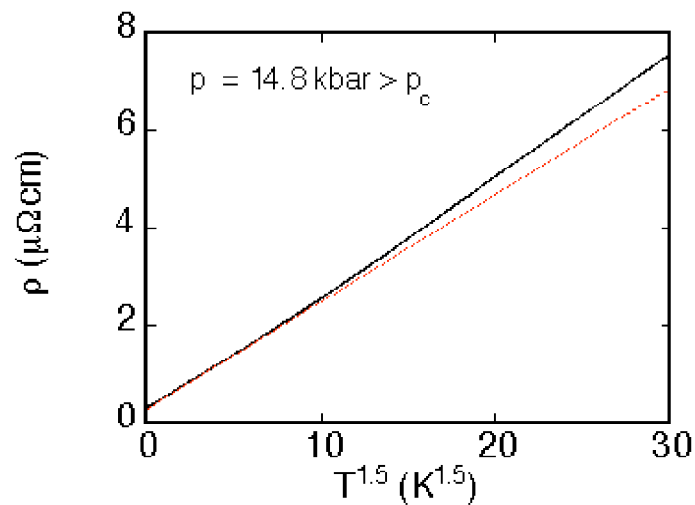


Fermi liquid:

$$\rho(T) = \rho_0 + AT^2$$

consequence of phase space constraint for QP-QP scattering by Pauli principle

# Non-Fermi Liquid Phase of MnSi for $p > p_c$



$$\rho(T) = \rho_0 + \Delta\rho(T)$$

$$\rho_0 \ll \Delta\rho(T) \propto T^{3/2} \ll \rho_0$$

$\Rightarrow$   $\text{mK} < T < \text{several K}$

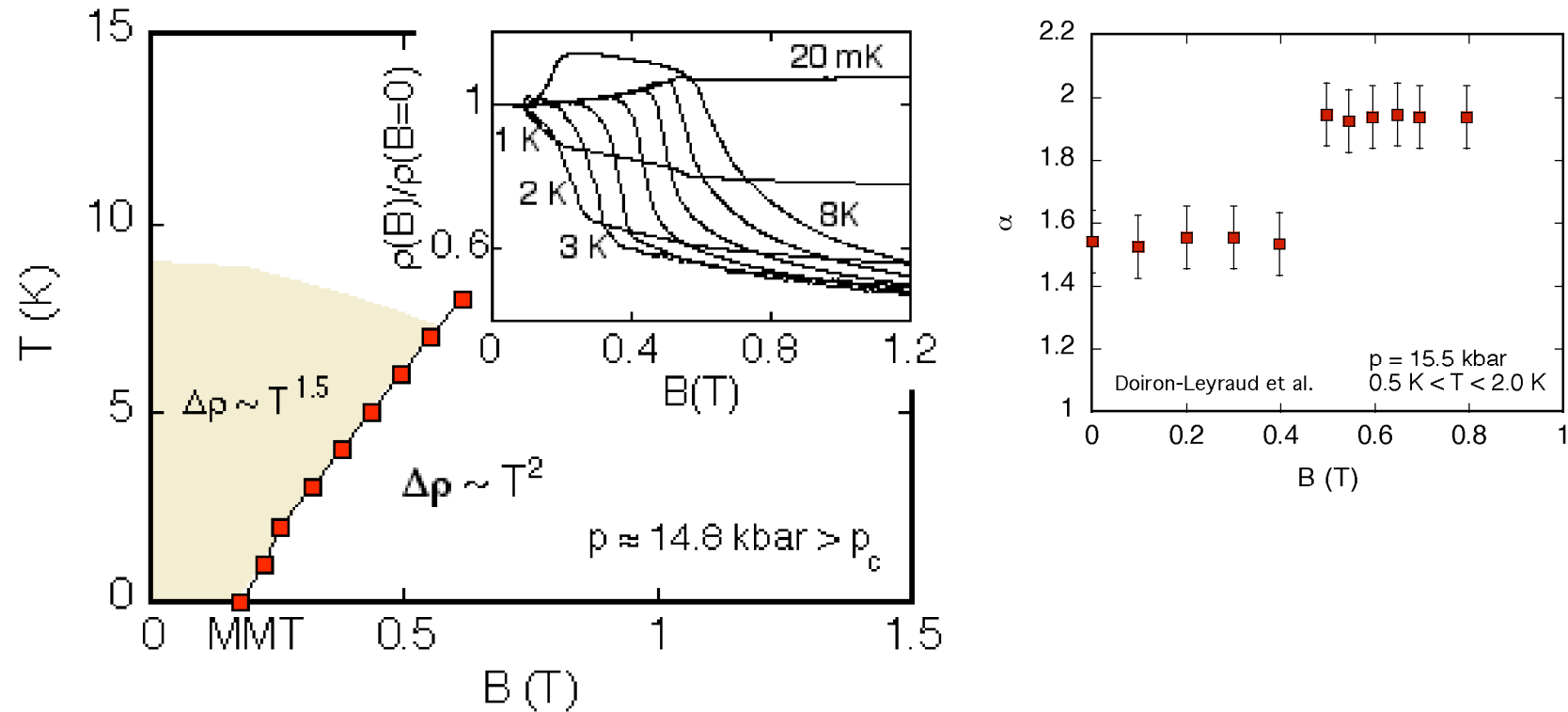
$\Rightarrow$   $\alpha$  insensitive to  $p$

CP et al., Nature 414 (2001) 427.

CP Physica B 328 (2003) 100.

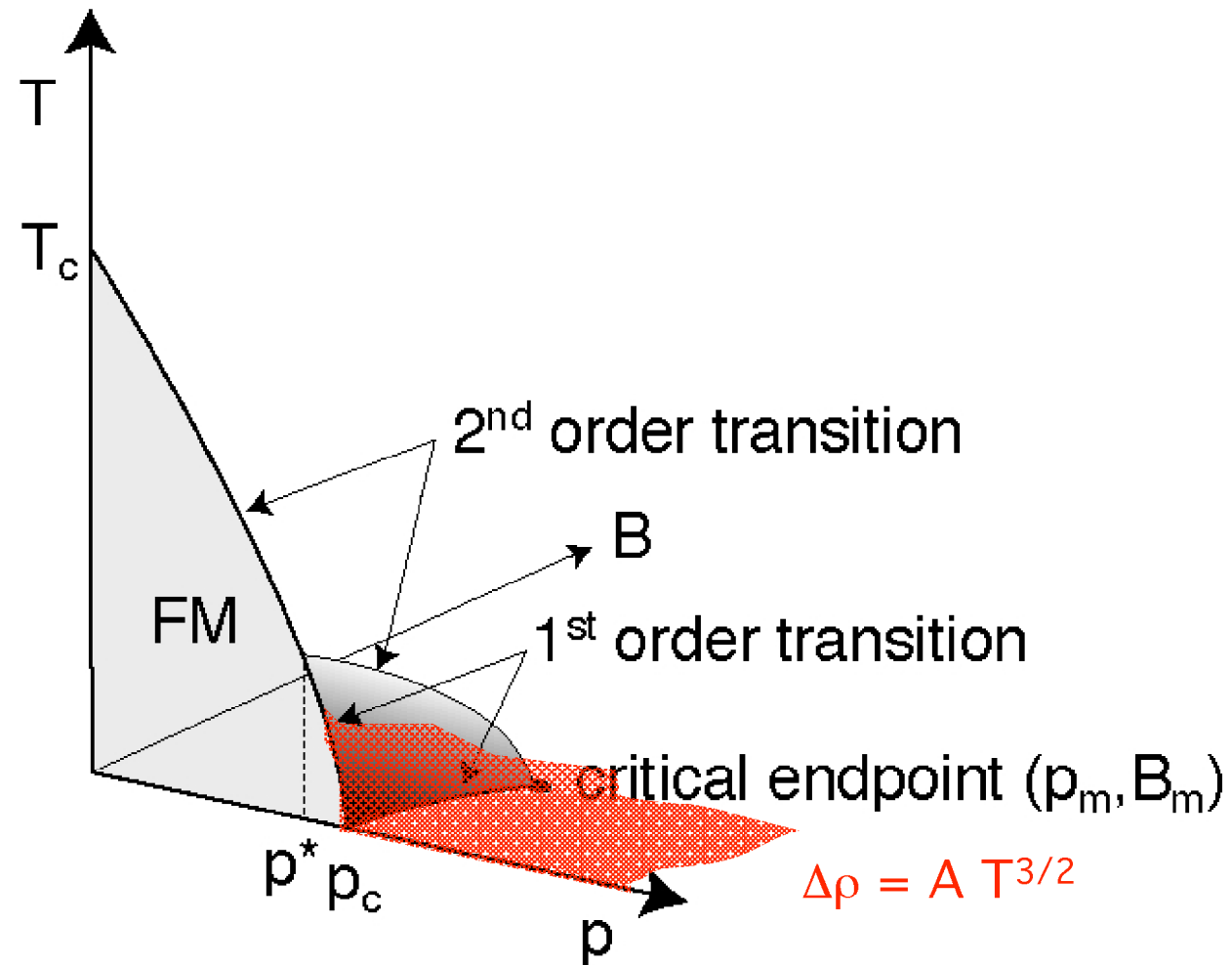
Doiron-Leyraud et al., Nature 425 (2003) 595.

# Variation of $T^{3/2}$ with Magnetic Field near $p_c$



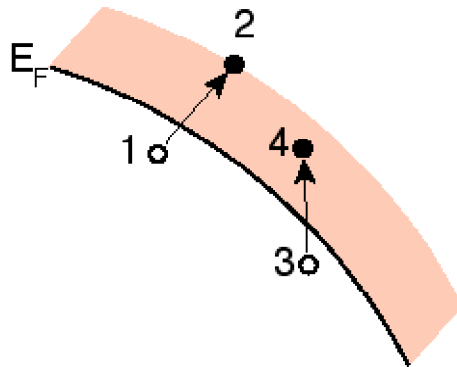
- NFL phase stable up to MMT
- drop of  $\rho$  at  $B_c$

# Phase diagram of MnSi revisited



# What is special about the $T^{3/2}$ resistivity?

Landau (1957)

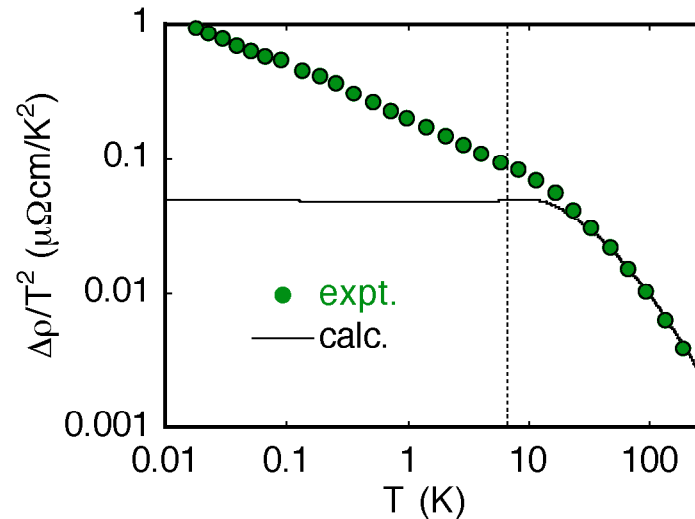


$$1/\tau = a (\varepsilon_1 - E_F)^2 + b (k_B T)^2$$

for  $T \rightarrow 0$  always long-lived!

electrical resistivity (Pauli)

$$\rho(T) = AT^2 + \rho_0$$



$\Delta\rho/T^2 = A$  singular für  $T \rightarrow 0$

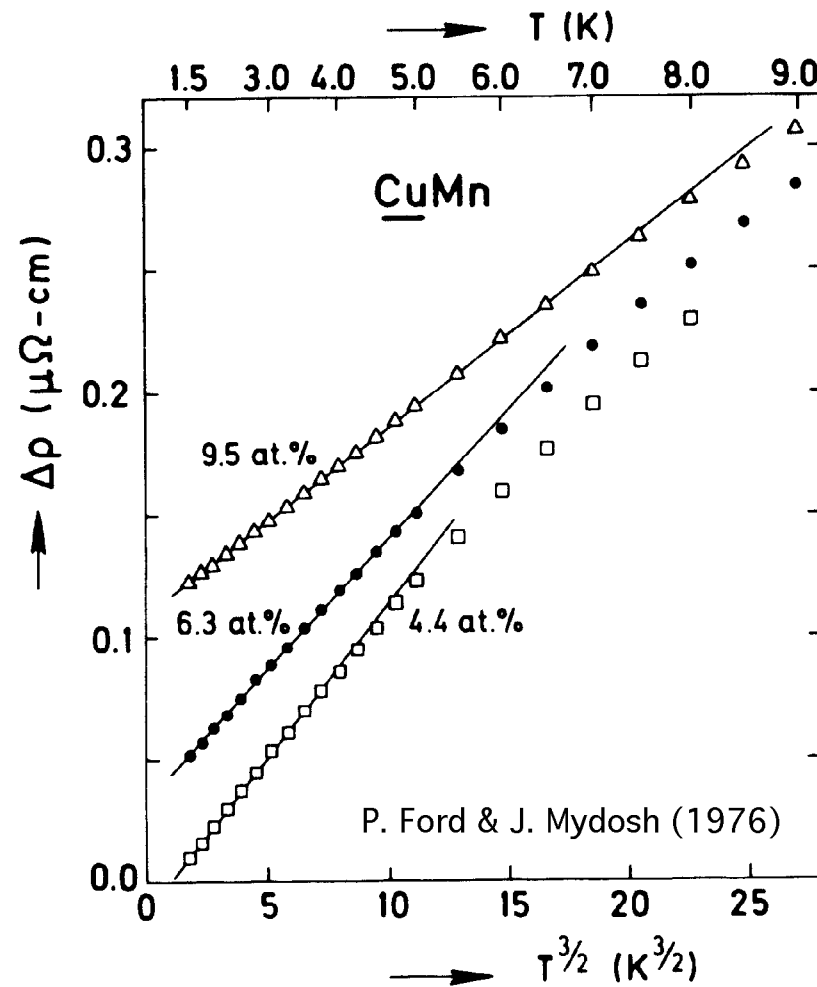
phenomenology inconsistent with Pauli principle

collective charge transport?  
fractional charge carriers?

....



# Origin of the $T^{3/2}$ Resistivity?



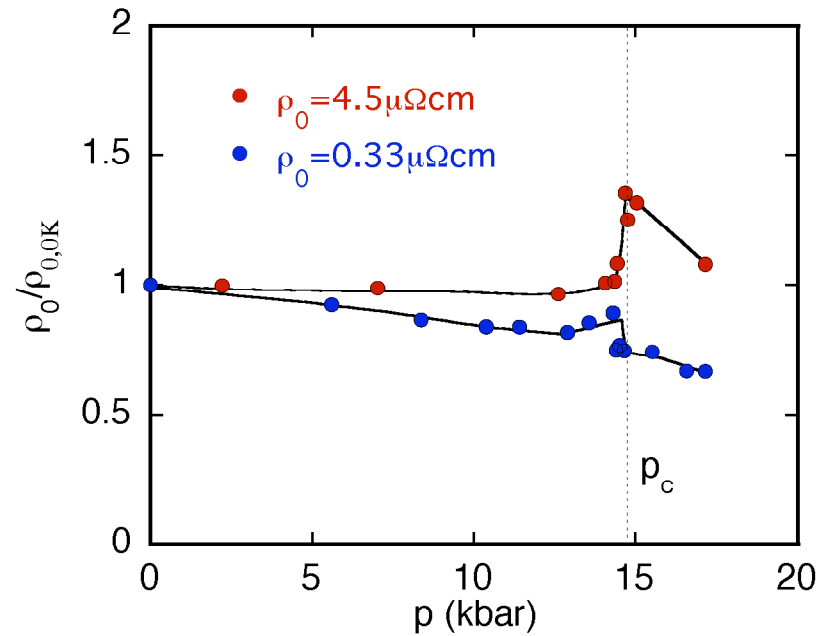
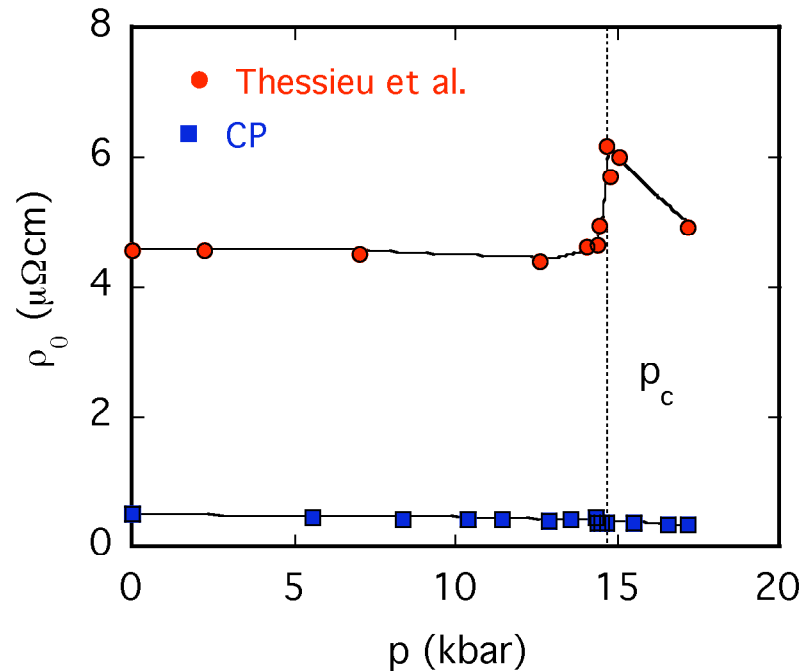
Metallic spin-glasses

Is the NFL phase of MnSi  
an intrinsic “glassy” state?

BUT: high purity single crystals

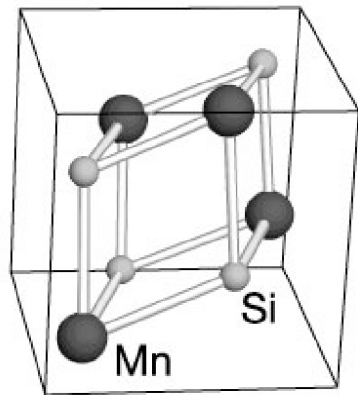
mean free path  $\approx 3000\text{\AA}$ !  
structural perfect (cf. Silicon)

# Pressure dependence of the residual resistivity



maximum near  $p_c$  vanishes for better samples

# Characteristic Energy Scales in MnSi



cubic (B20)  
no inversion

(1) ferromagnetism

(2) spin-orbit coupling:

Dzyaloshinsky-Moriya interaction

$\mathbf{s}^* (\nabla \times \mathbf{s})$ , rotation-invariant

$\lambda \approx 170 \text{ \AA}$  ( $a = 4.558 \text{ \AA}$ )

(3) crystal field potential ( $P2_13$ ):

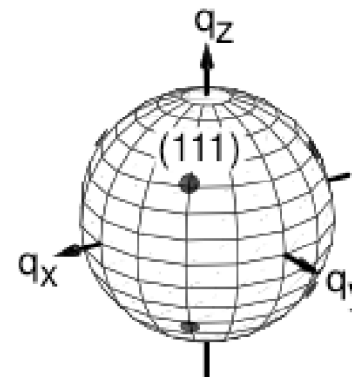
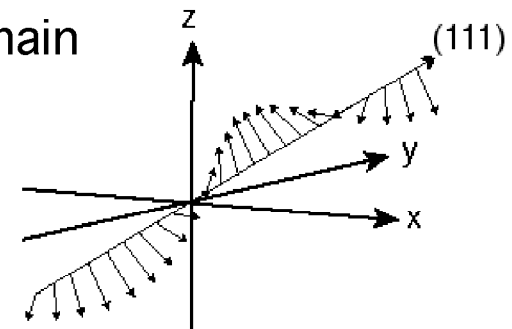
helix locked at  $\langle 111 \rangle$  or  $\langle 100 \rangle$

(not  $\langle 110 \rangle$ )

cool from high T:

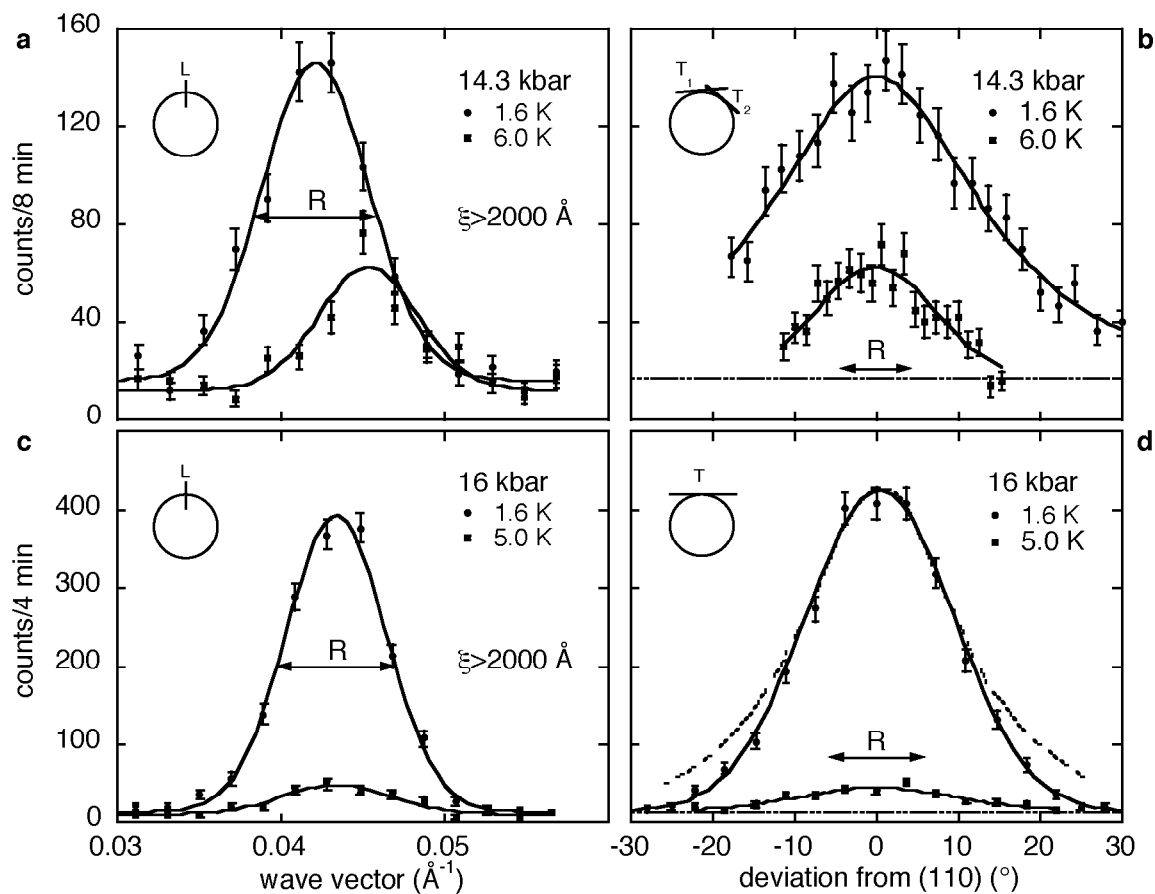
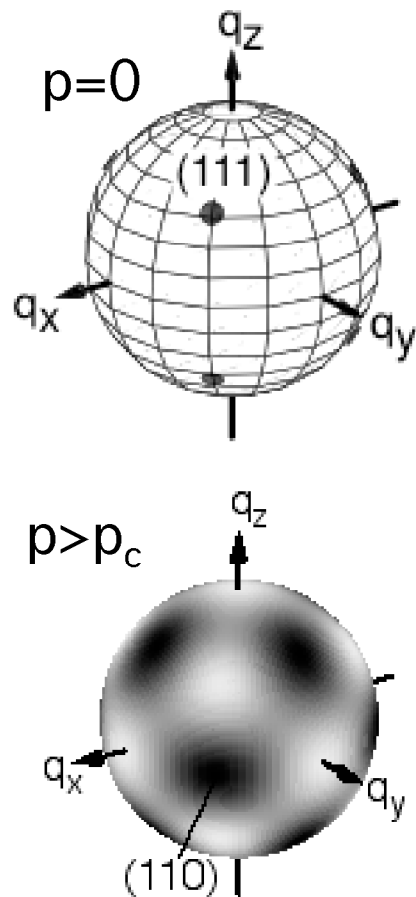
- ferromagnetic fluctuations
- chiral fluctuations (Q)
- 2<sup>nd</sup> order phase transition

single domain



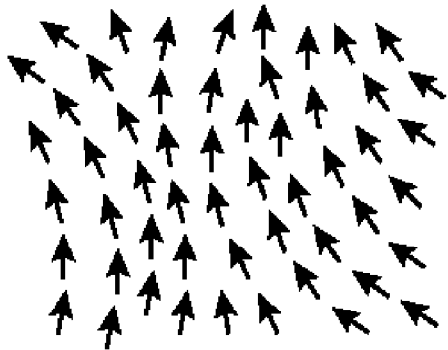
magn. domains  
in recip. space:  
sharp satellites

# Partial Magnetic Order in the NFL-Phase of MnSi



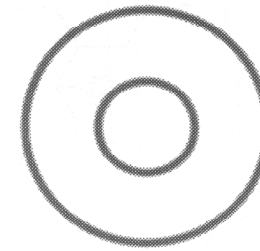
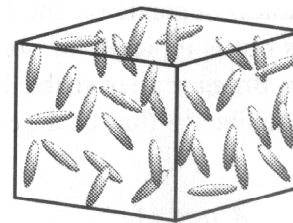
experiments at 4F1 (LLB Saclay)

# Analogy with Partial Order in Liquid Crystals

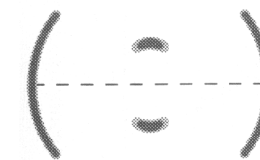
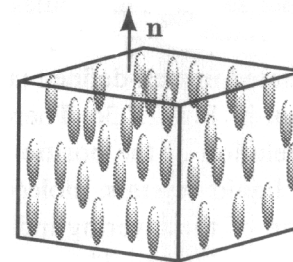


loss of pinning  
(weakest scale)  
flat crystal field potential

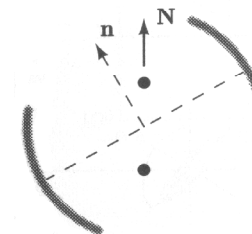
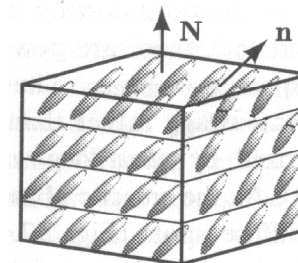
⇒ disordered chunks of helix



isotropic



nematic



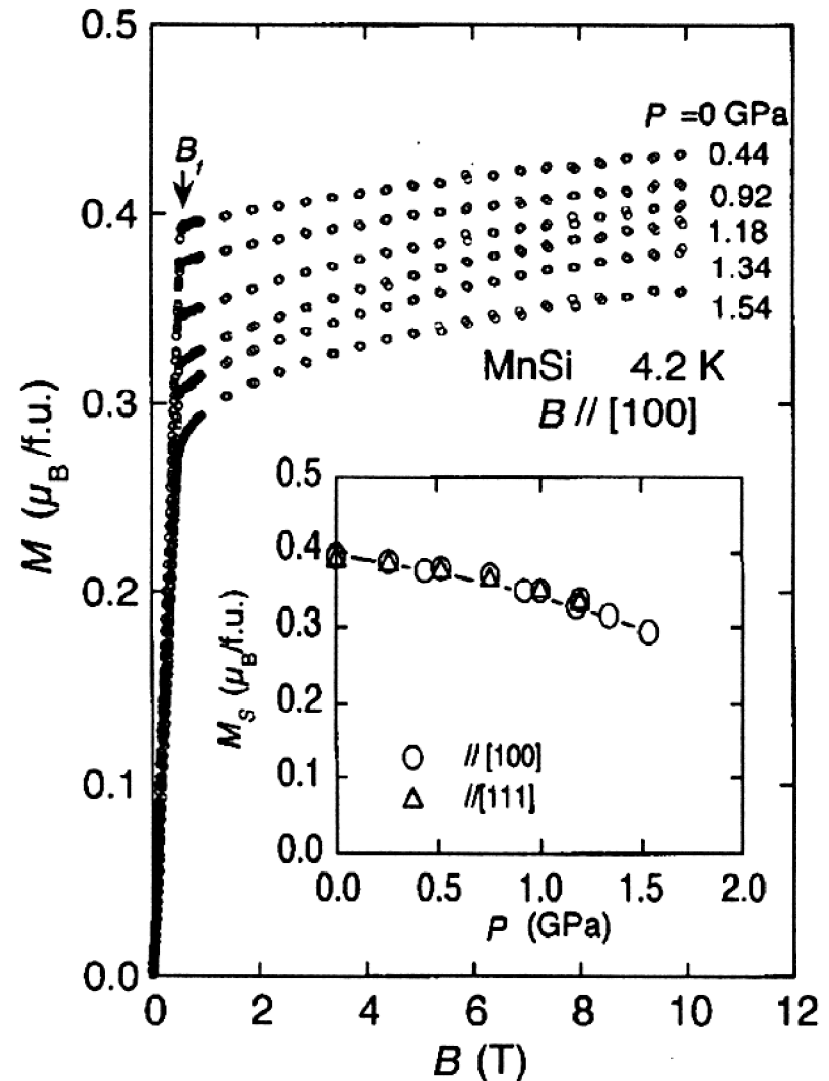
smectic

Analogy with cholesterics?

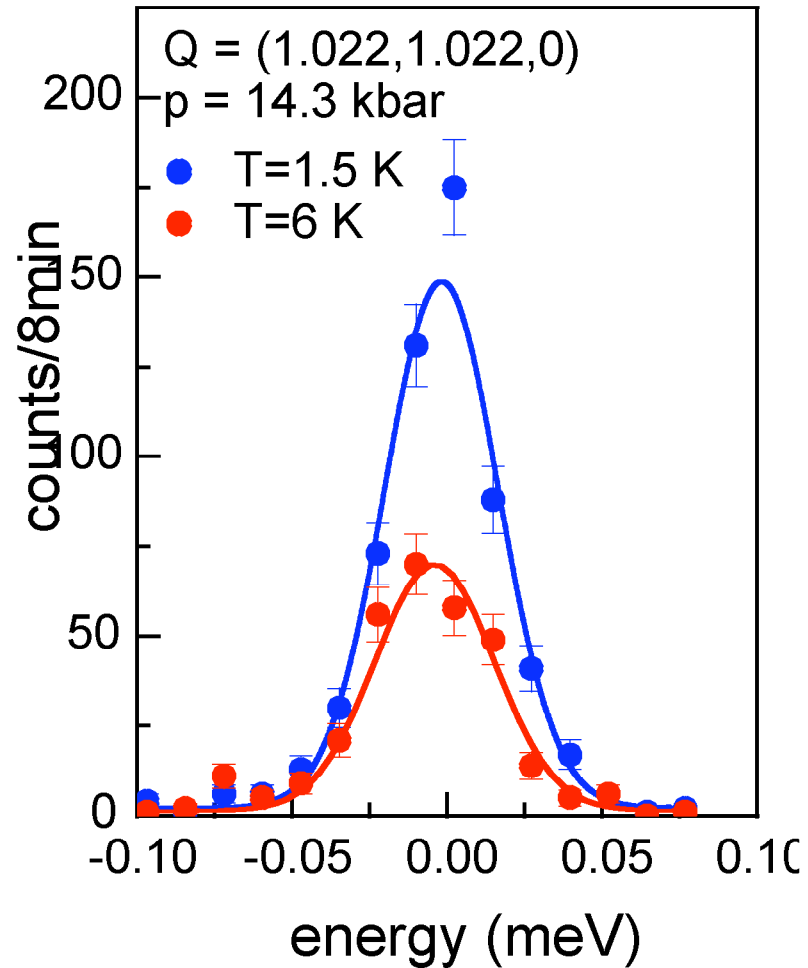
# Size of partially ordered moment

integrated scattering intensity  
of partial order unchanged:  
large moment survives  $p_c$   
(„no“ amplitude reduction at  $p_c$ )

consistent with magnetisation:  
ordered moment in 0.6T  
weakly pressure dependent



# Energy dependence near $p \approx p_c$

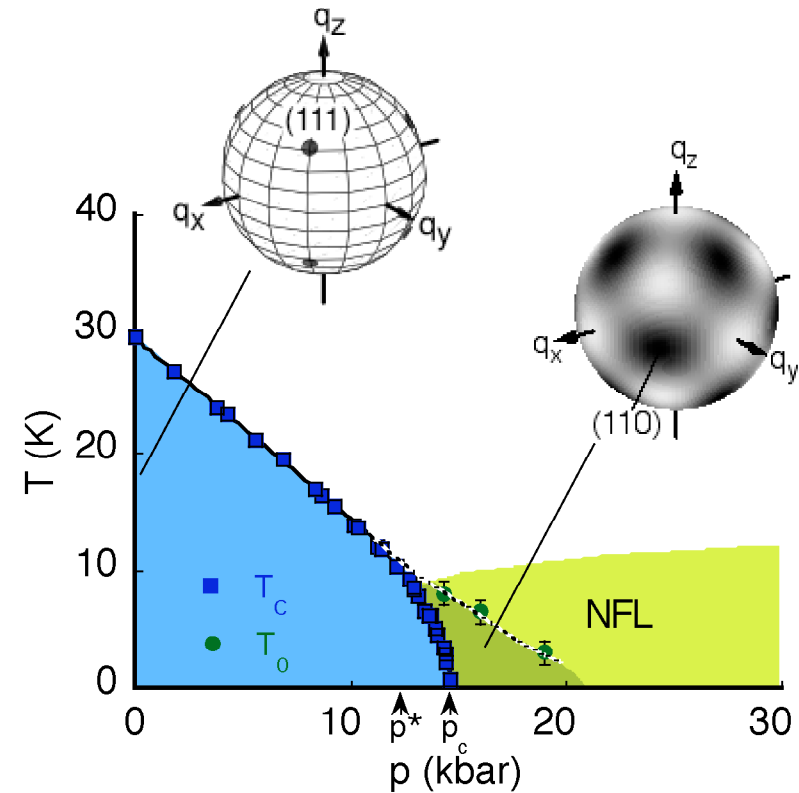
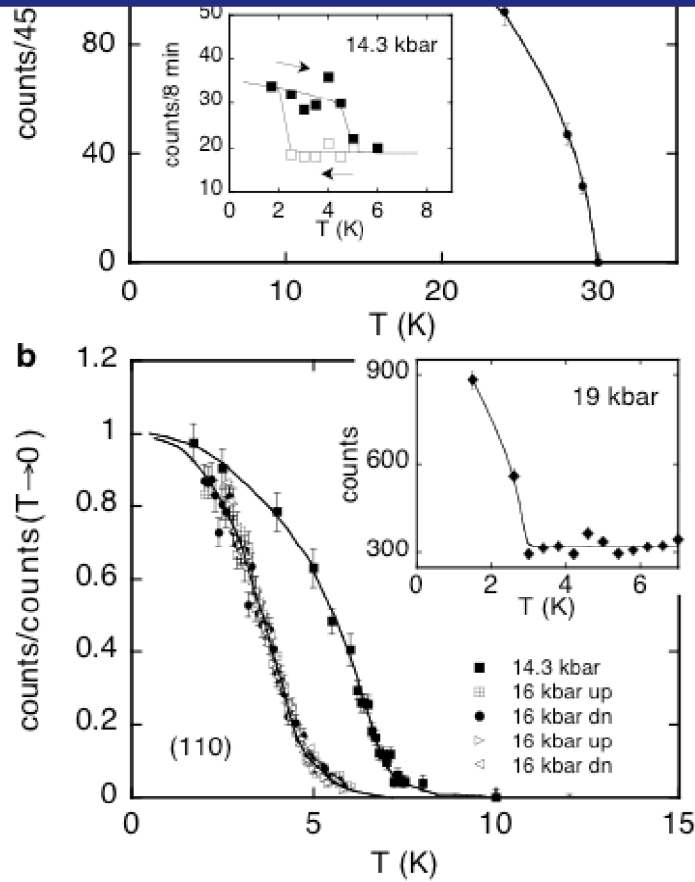


resolution limited:  
 $\Delta\omega \approx 50\mu\text{eV}$  (0.5K)

no broadening with T

quasi-static (very slow)

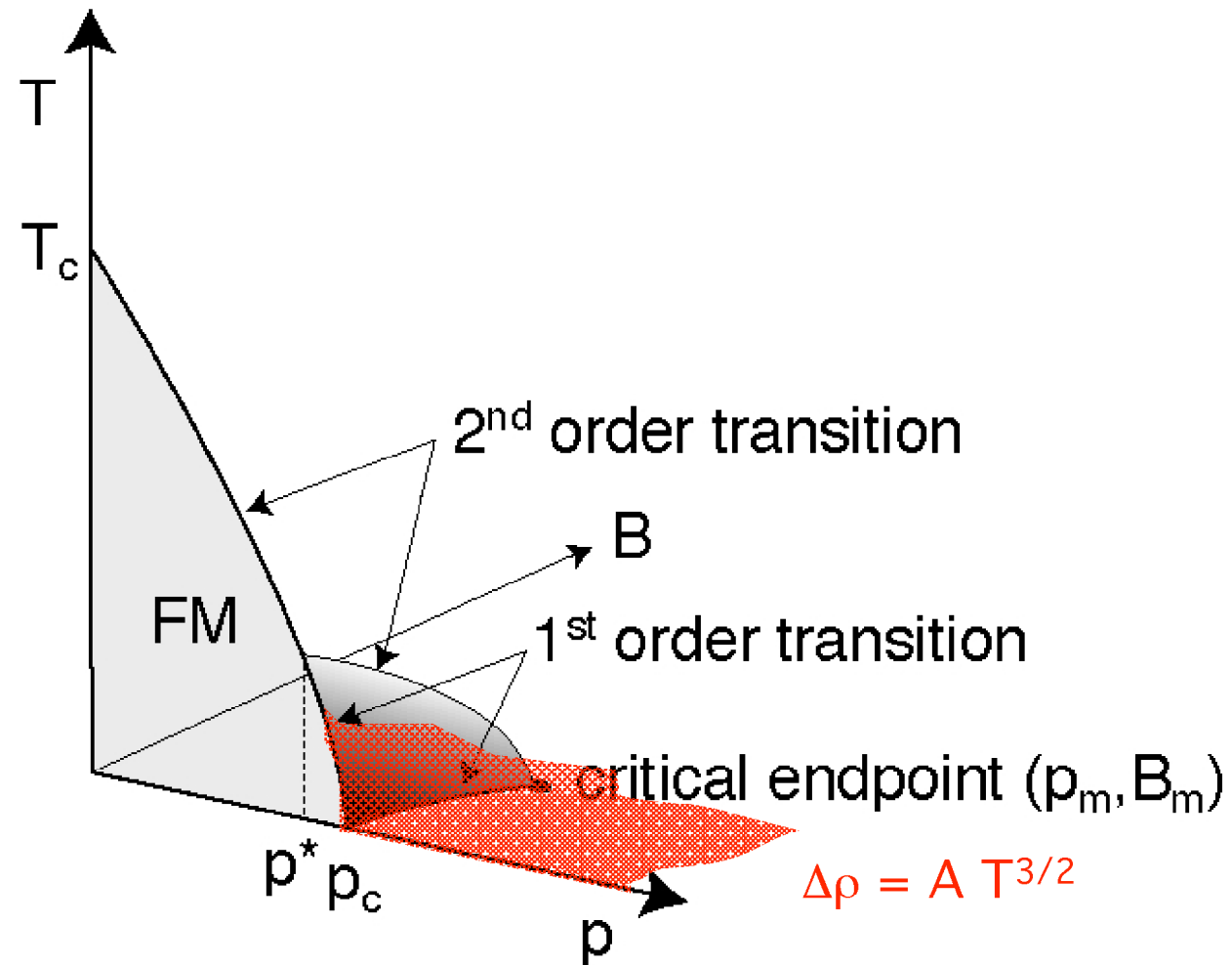
# Temperature Dependence of the Partial Order



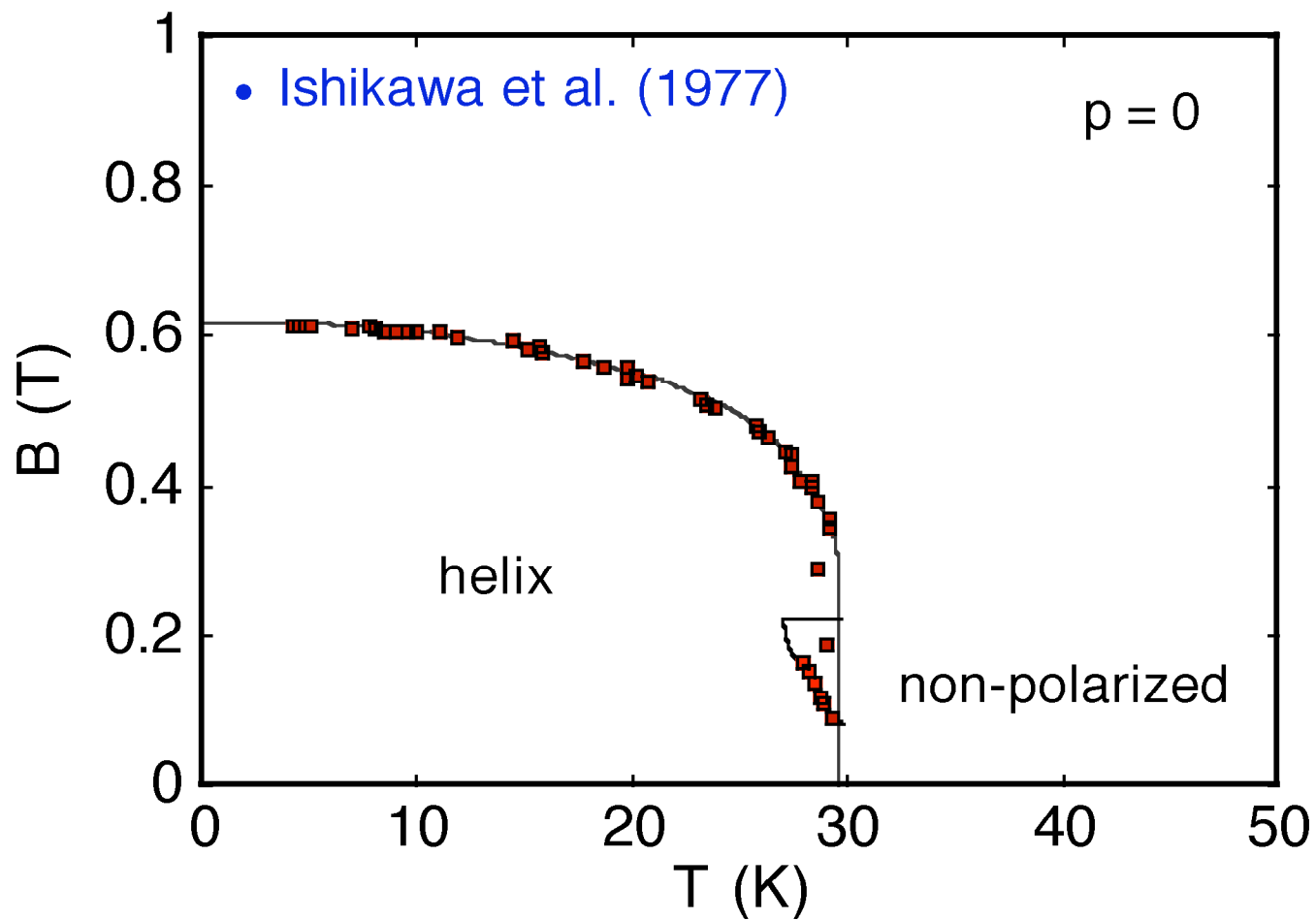
crossover  
(not sharp phase transition)



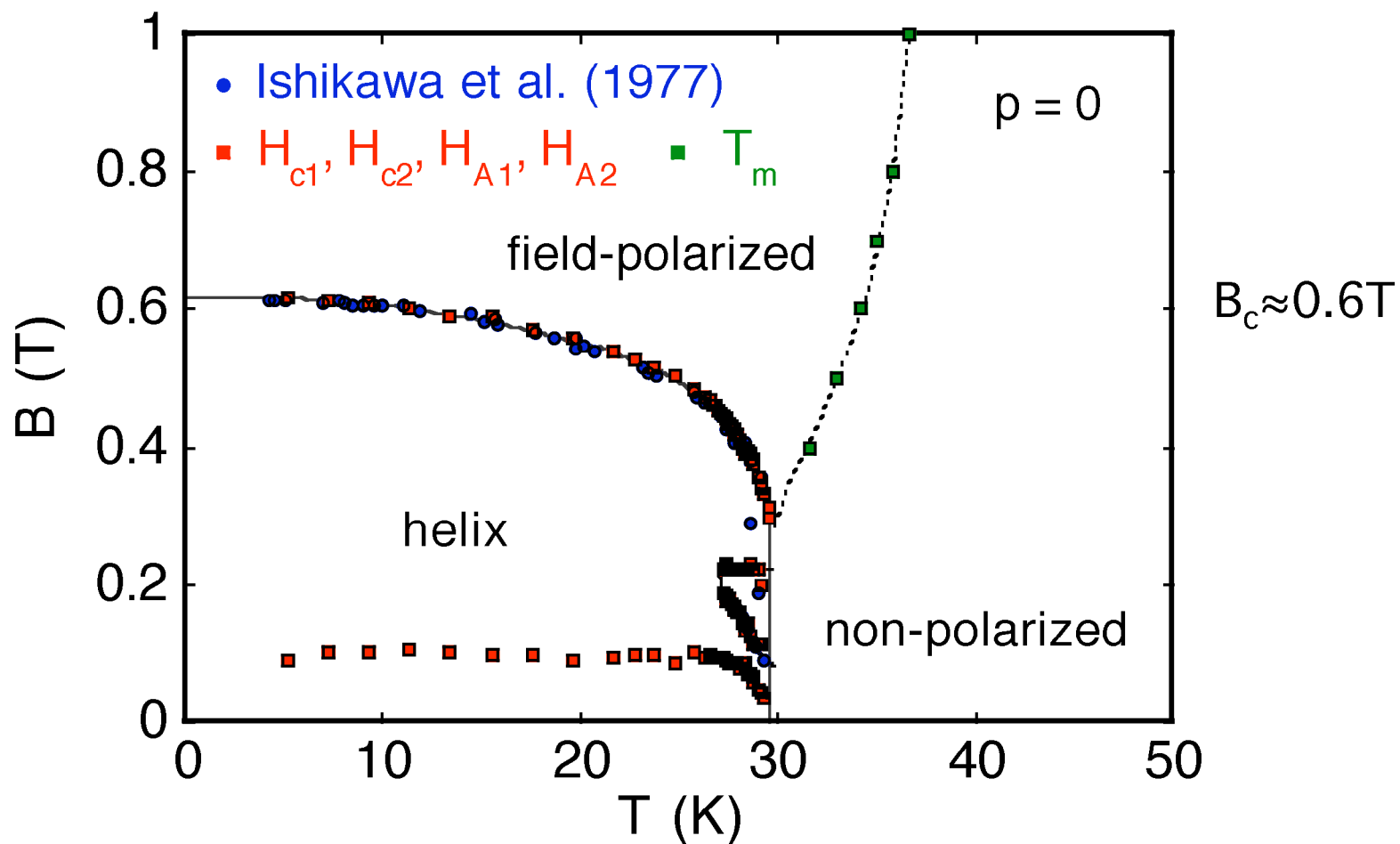
# What about the magnetic field dependence?



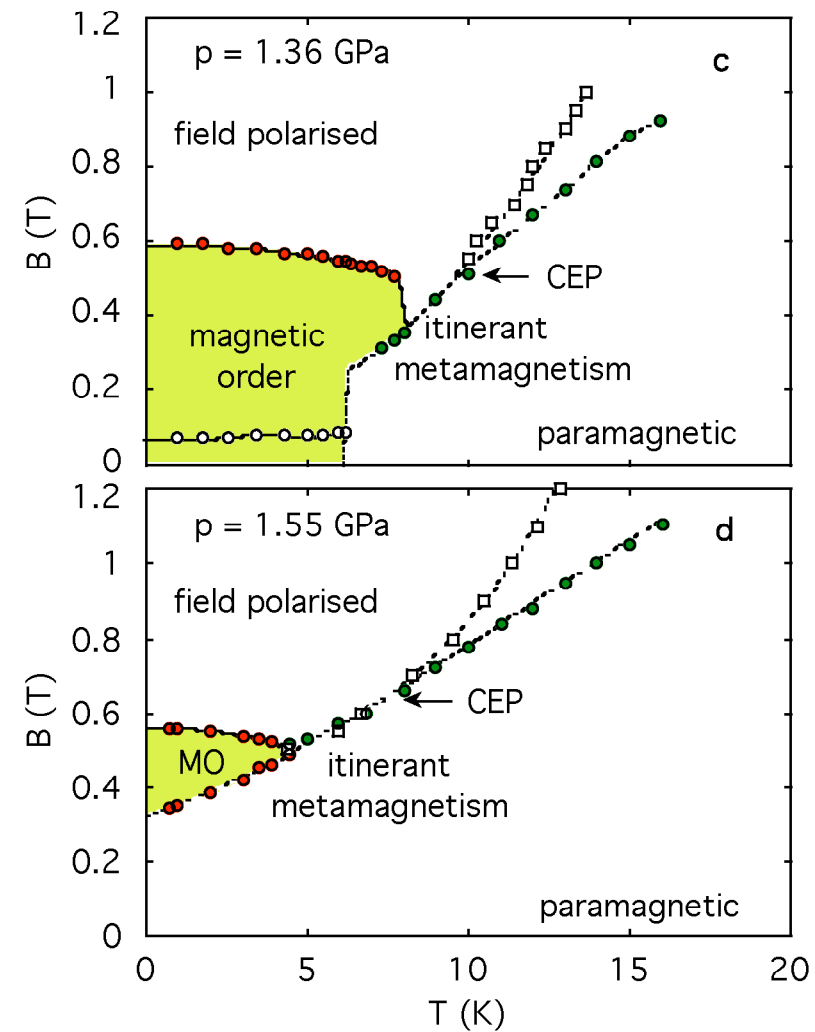
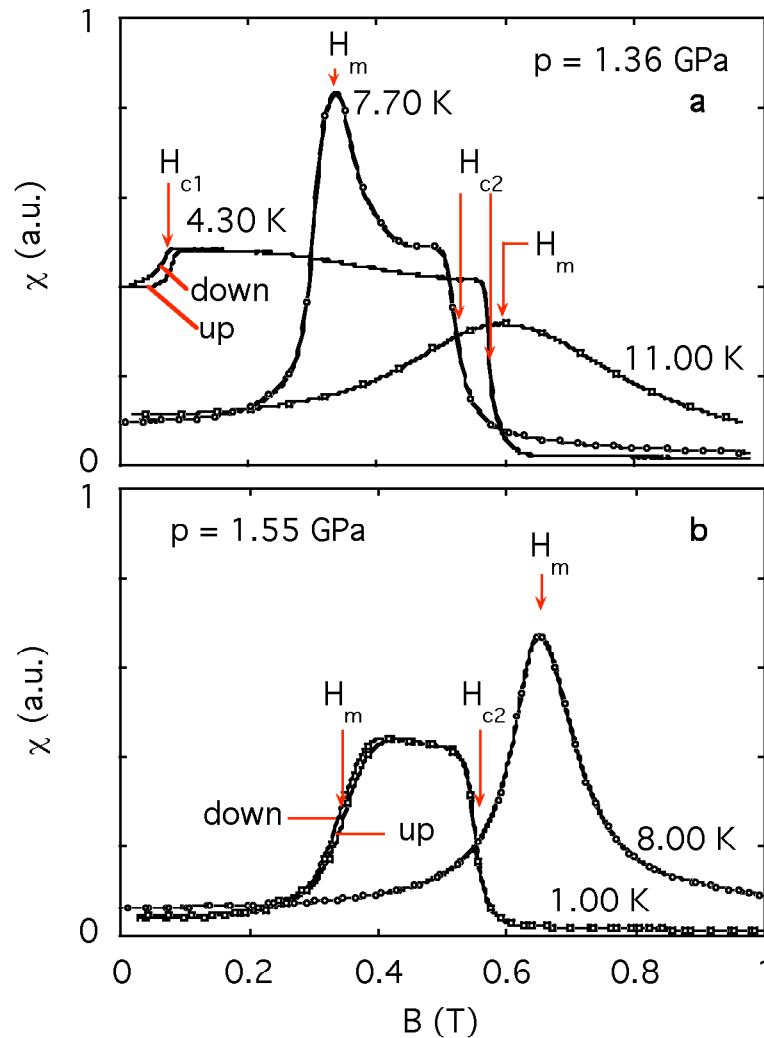
# Magnetic phase diagram at $p=0$



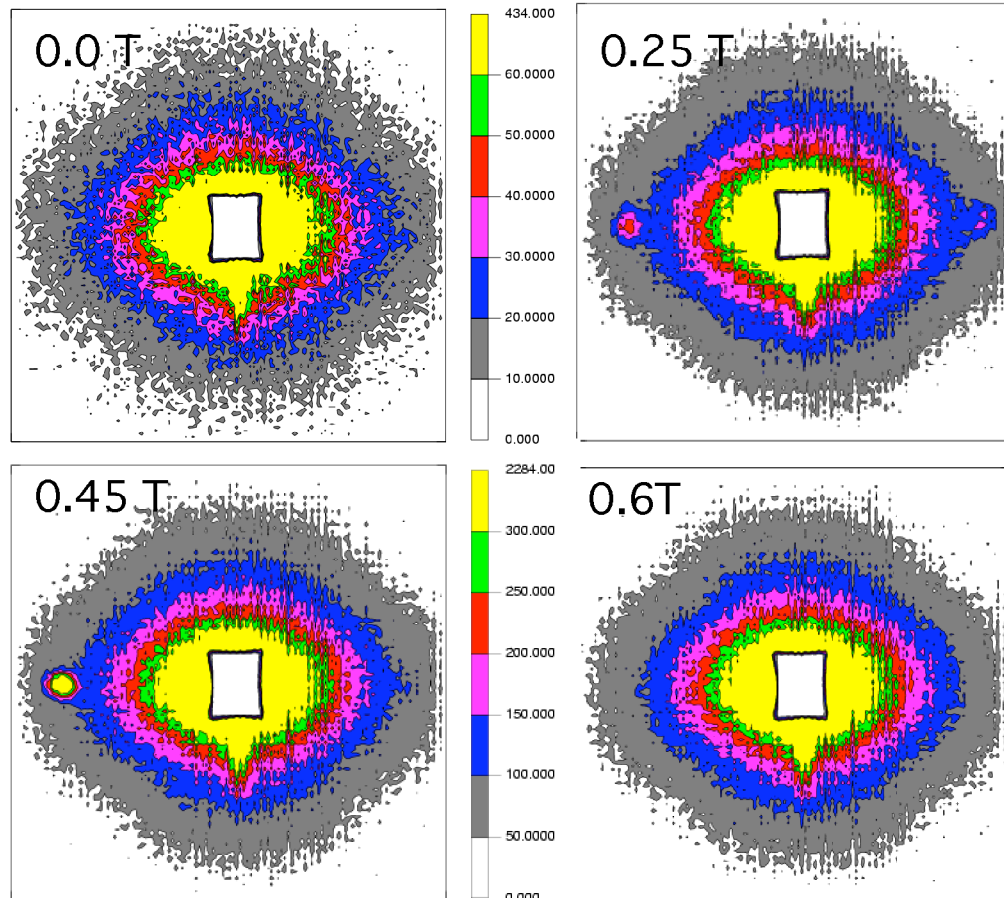
# Magnetic phase diagram at $p=0$



# Magnetic phase diagram near $p_c$

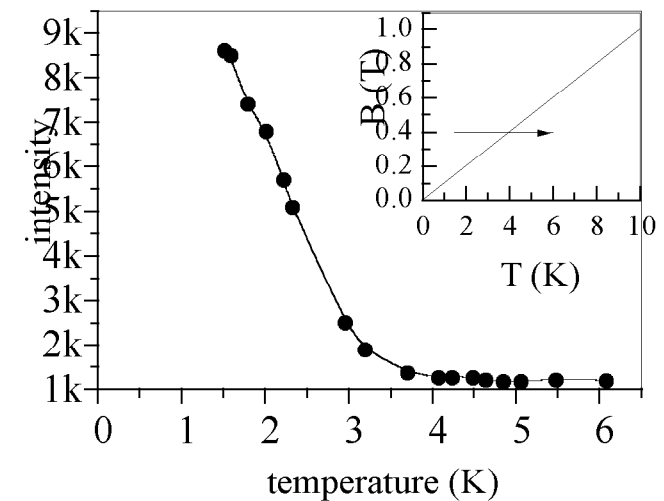
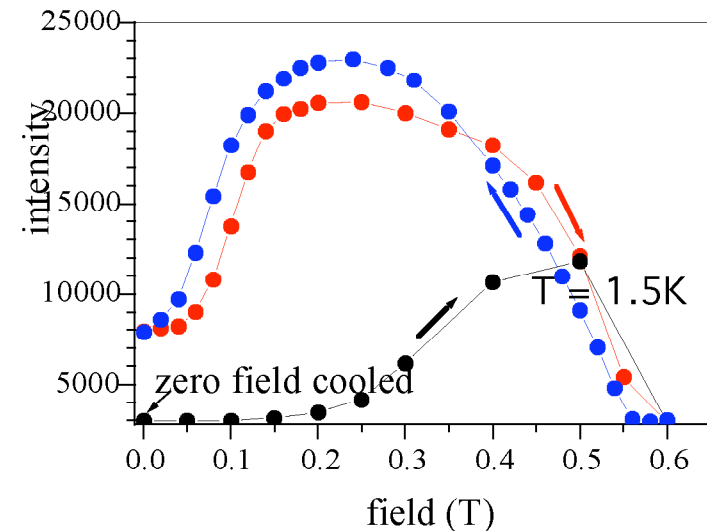


# Magnetic Field Dependence above $p_c$



$p \approx 18 \text{ kbar} > p_c$

SANS at V4 HMI Berlin

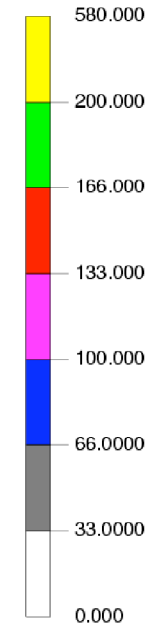
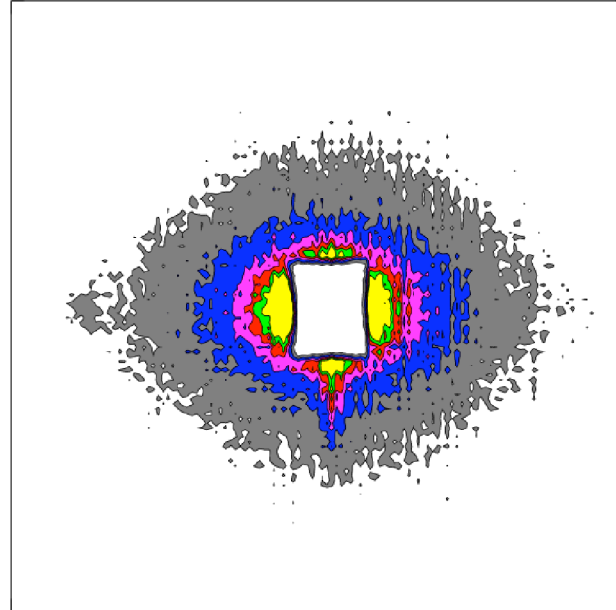
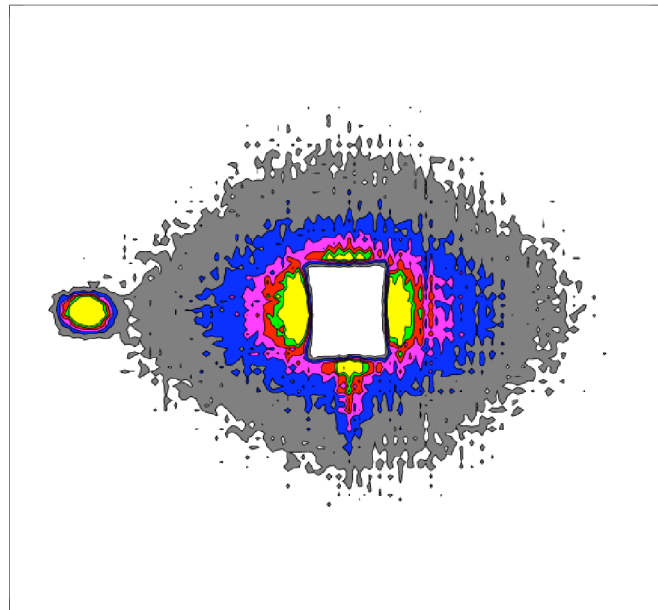


Magnetic field induced long-range order.

# Chirality above $p_c$

spin antiparallel to H

spin parallel to H



$p \approx 18$  kbar

H = 0.3 T   T = 1.5 K

Chirality of longitudinal order unchanged.

# Towards a theory of the phase diagram of MnSi

Rosch, et al.:

- anomalous Goldstone modes
- role of spin-orbit coupling

Turlakov, Schmalian:

- magnetic rotons

Vojta, Belitz, Kirkpatrick, et al.:

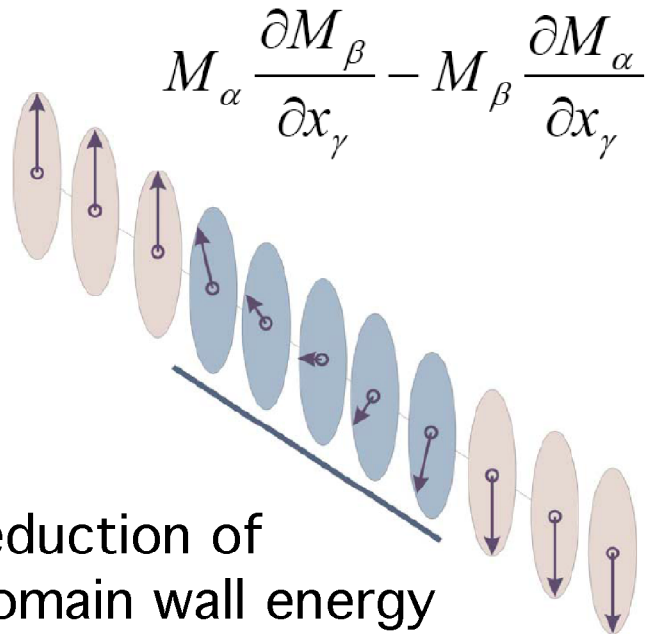
- breakdown of Ginzburg-Landau-Wilson

# “Change” role of spin-orbit coupling?

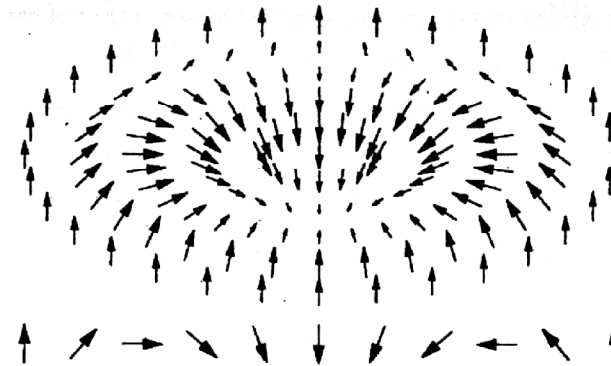
spin-orbit coupling:  
(Dzyaloshinsky-Moriya)

$$W_{DM} = D_{ij} \mathbf{S}_i \times \mathbf{S}_j$$

Lifshitz invariants



Prediction of magnetic vortex  
like superconducting vortex  
(doubly modulated state)  
A. Bogdanov, JETP (1989)





# Instead of a Summary ...

