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**Workshop on
Novel States and Phase Transitions in Highly Correlated Matter
12 - 23 July 2004**

**Thermoelectricity of correlated electrons:
insights and enigmas**

**Kamran BEHNIA
Ecole Supérieure de Physique et de Chimie Industrielles
ESPCI - CNRS - UPR5
10 rue Vauquelin
75005 Paris
FRANCE**

These are preliminary lecture notes, intended only for distribution to participants

Thermoelectricity of correlated electrons: insights and enigmas

Kamran Behnia
ESPCI-Paris

- Romain Bel & Hao Jin (ESPCI-Paris)

In collaboration with:

Heavy fermions:

- Didier Jaccard (Geneva),
- Jacques Flouquet (Grenoble),
- Koichi Izawa & Yuji Matsuda (Tokyo)

Overdoped LSCO:

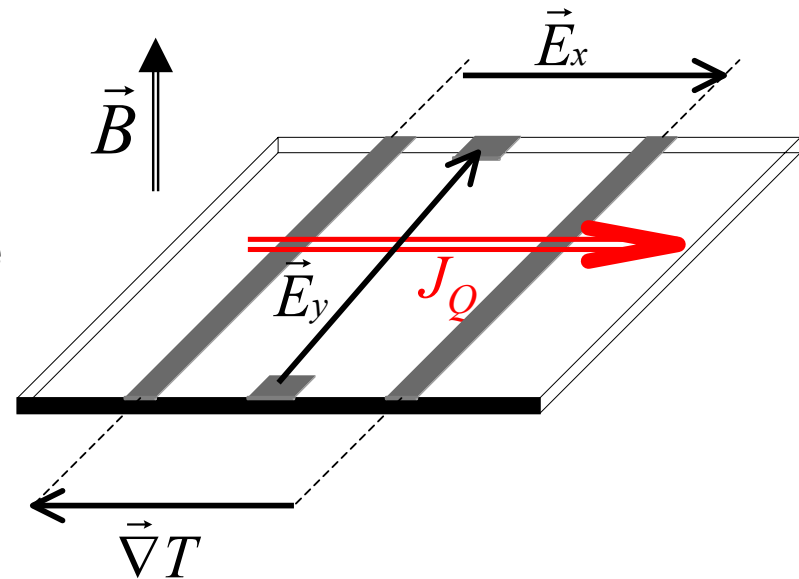
- Saco Nakame (Orsay),
- S. Yaters & Nigel Hussey (Bristol)
- M. Nohara & Hide Takagi (Tokyo)

Underdoped cuprates:

- Cigdem Capan (Los Alamos)
- Z.Z. Li & H el ene Raffy (Orsay)

The thermoelectric coefficients

- In presence of a thermal gradient, electrons produce an electric field.
- Seebeck and Nernst effect refer to the longitudinal and the transverse components of this field.



$$S = \frac{-E_x}{\nabla_x T} \quad N = \frac{-E_y}{\nabla_x T} \quad \left[v = \frac{-E_y}{B_z \nabla_x T} \right]$$

Seebeck coefficient of the free electron gas

In the Boltzmann picture thermopower is linked to electric conductivity:

$$S = -\frac{\pi^2 k_B^2 T}{3 e} \left(\frac{\partial \ln \sigma(\epsilon)}{\partial \epsilon} \right)_{\epsilon_F}$$

This yields:

$$S = -\frac{\pi^2 k_B^2 T}{3 e} \left[\underbrace{\left(\frac{\partial \ln \tau(\epsilon)}{\partial \epsilon} \right)_{\epsilon_F}}_{\text{transport}} + \underbrace{\frac{\int d\mathbf{k} \delta(\epsilon_F - \epsilon(\mathbf{k})) \mathbf{M}^{-1}(\mathbf{k})}{\int d\mathbf{k} \delta(\epsilon_F - \epsilon(\mathbf{k})) v(\mathbf{k}) v(\mathbf{k})}}_{\text{thermodynamic}} \right]$$

For a free electron gas, with $\tau = \tau_0 \epsilon^\zeta$:

$$S = -\frac{\pi^2 k_B^2 T}{3 e \epsilon_F} \left(\frac{3}{2} + \zeta \right)$$

For a proper treatment of the first term, see Miyake and Kohno '04

Thermopower and specific heat

In a free electron gas (with $\xi=0$):

$$S = -\frac{\pi^2}{3} \frac{k_B^2 T}{e} \frac{N(\epsilon_F)}{n} \qquad C_{el} = \frac{\pi^2}{3} k_B^2 T N(\epsilon_F)$$

Thermopower is a measure of specific heat per carrier

The dimensionless ratio: $q = N_{Av} e \frac{S}{T\gamma}$

is equal to -1 ($+1$) for free electrons (holes)

Thermoelectricity in real metals

- The free-electron-gas picture is inadequate at finite temperature
- Even in simple elemental metals, $S(T)$ is not linear in temperature and displays a complex structure

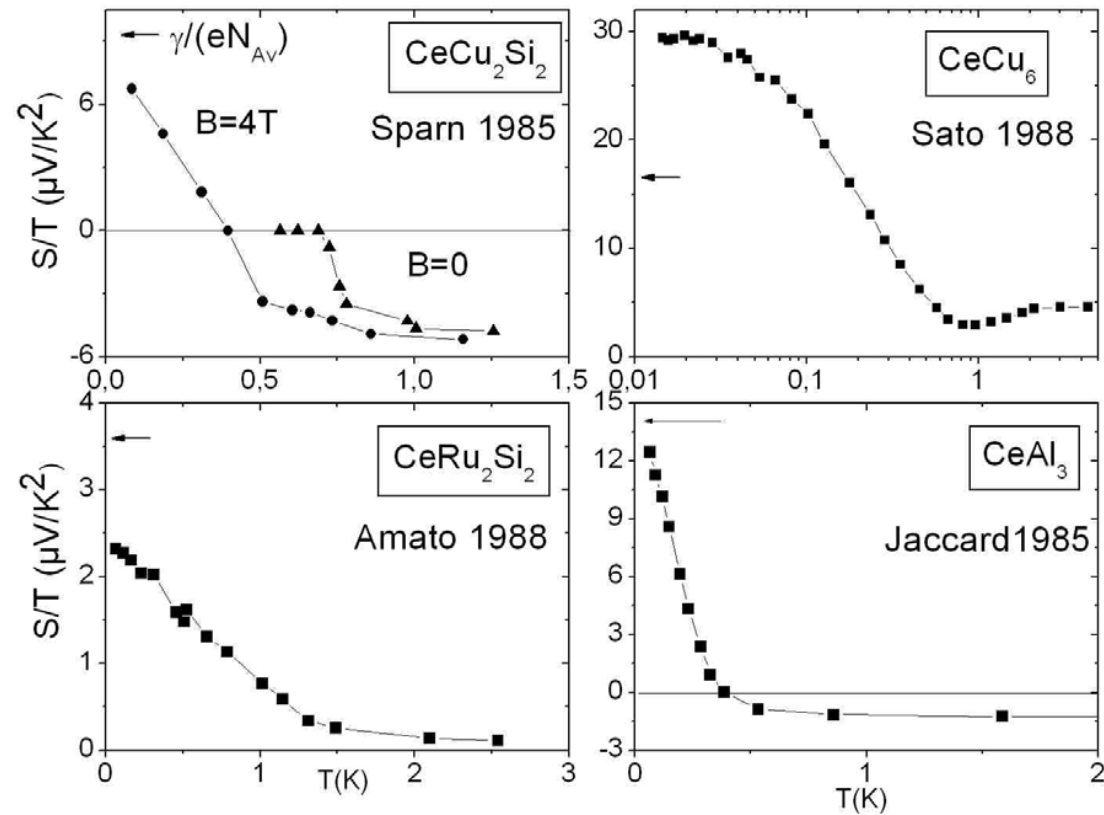
What about the zero-temperature limit?

- The issue of carrier density : Is there a single carrier per formula unit?(often yes)
- The sign problem: The contribution of hole-like bands and electron-like bands are expected to be opposite in sign!

The magnitude of S/T has never been put under scrutiny in the zero-temperature limit!

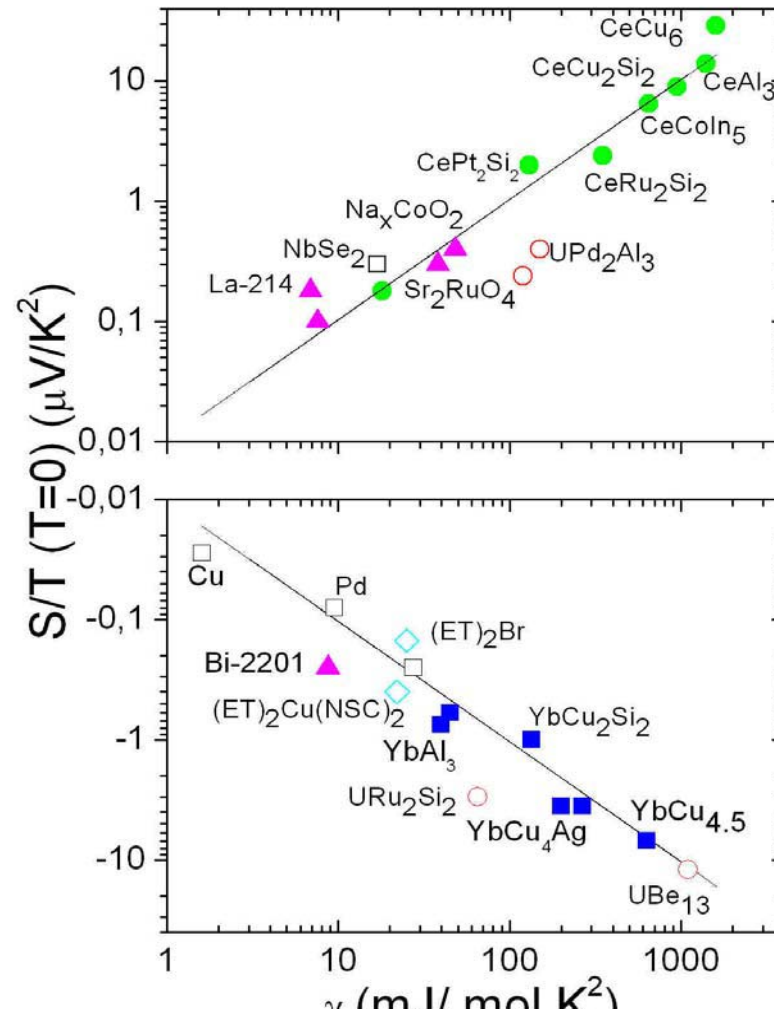
Heavy electrons in the T=0 limit

Two-decades-old data reconsidered!

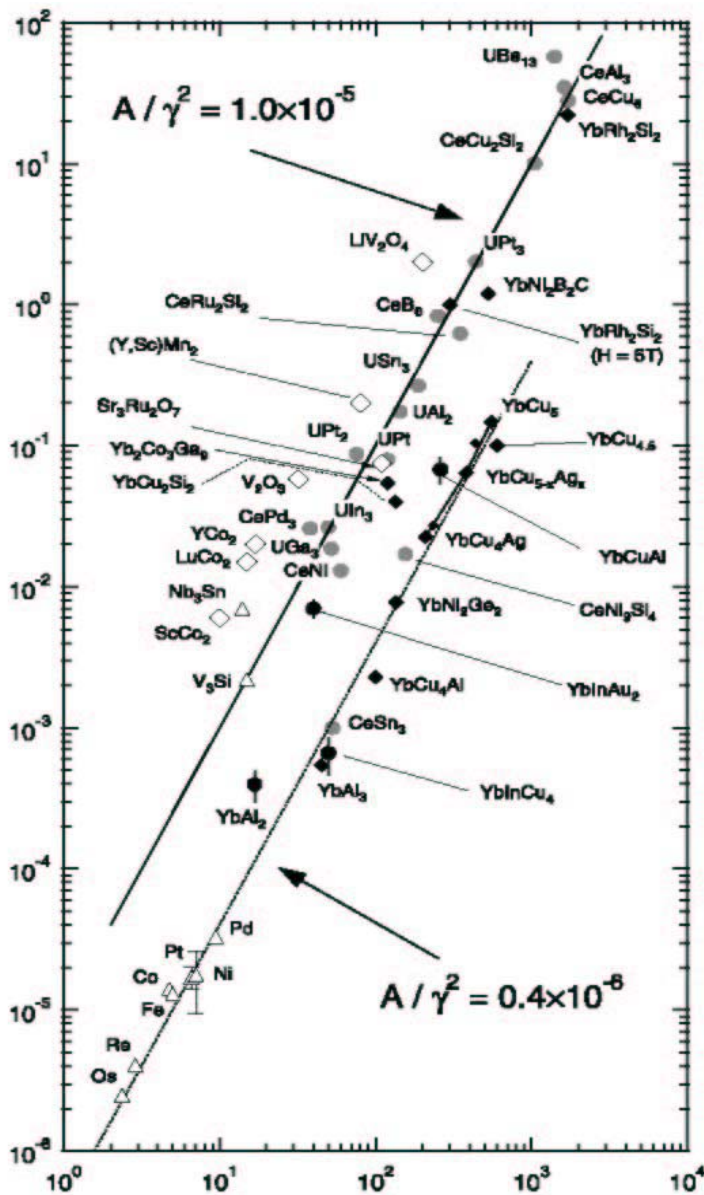


Extrapolated to $T=0$, data yields a q close to unity!

A new plot linking two distinct signatures of electron correlation



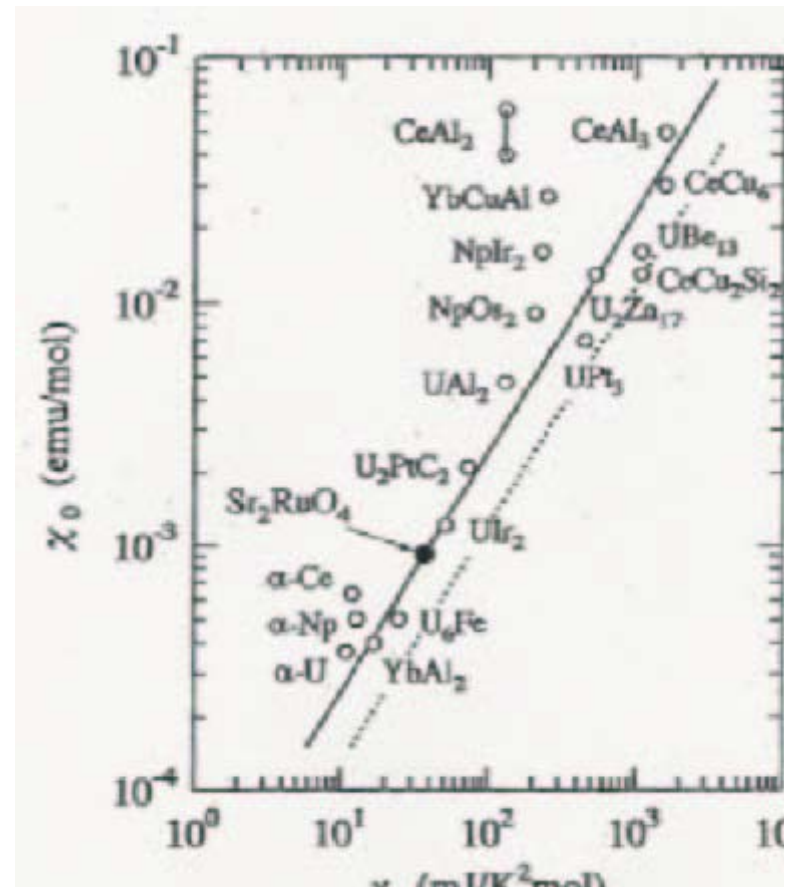
Ratios used to characterize a Fermi liquid



← *Kadowaki-Woods ratio (A/γ^2)*

$$[\rho = \rho_0 + AT^2] \quad \text{Tsujii, 2003}$$

Wilson Ratio (χ/γ)
Maeno 1997

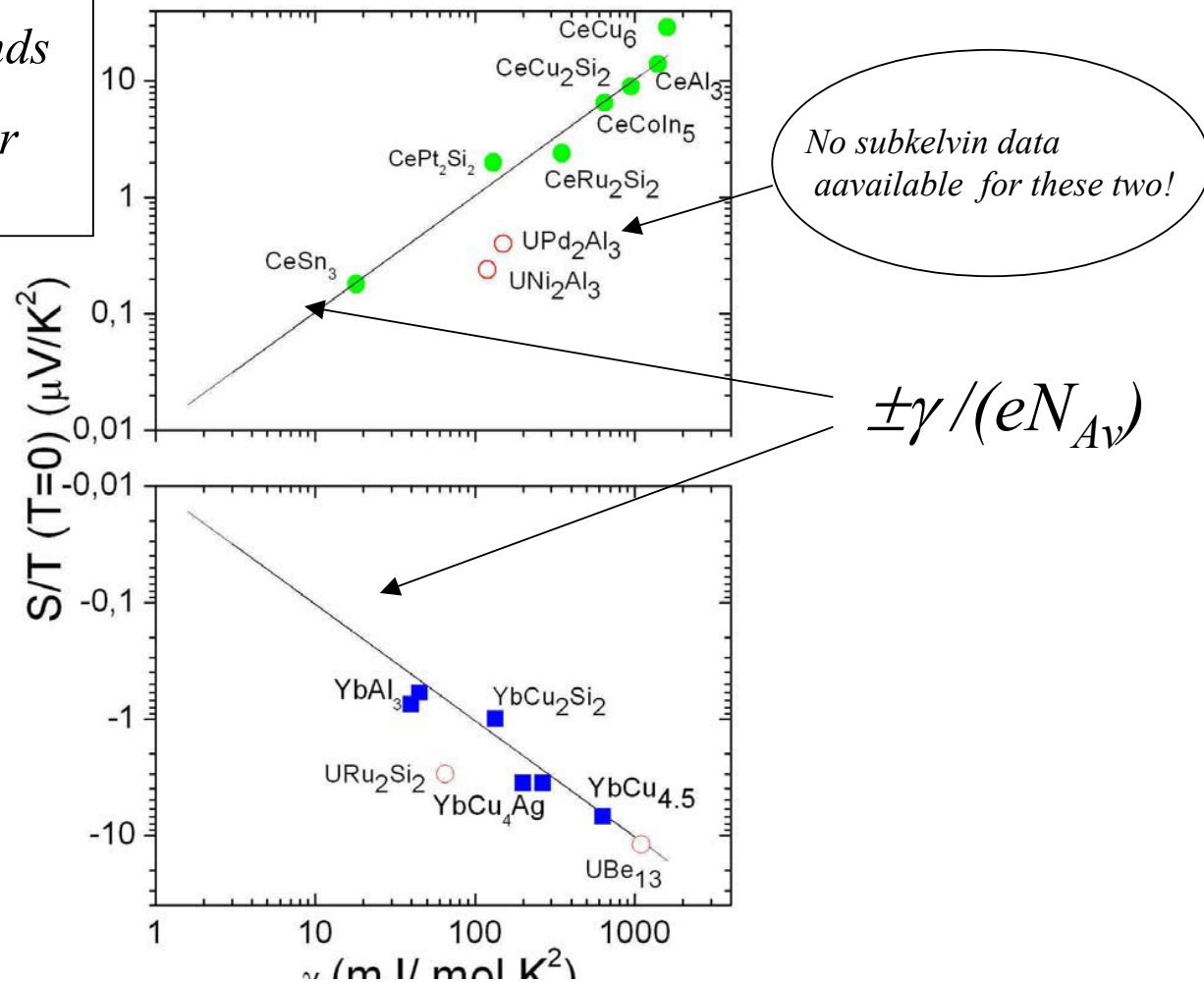


Heavy Fermions

$S > 0$ in Ce compounds

$S < 0$ in Yb Compounds

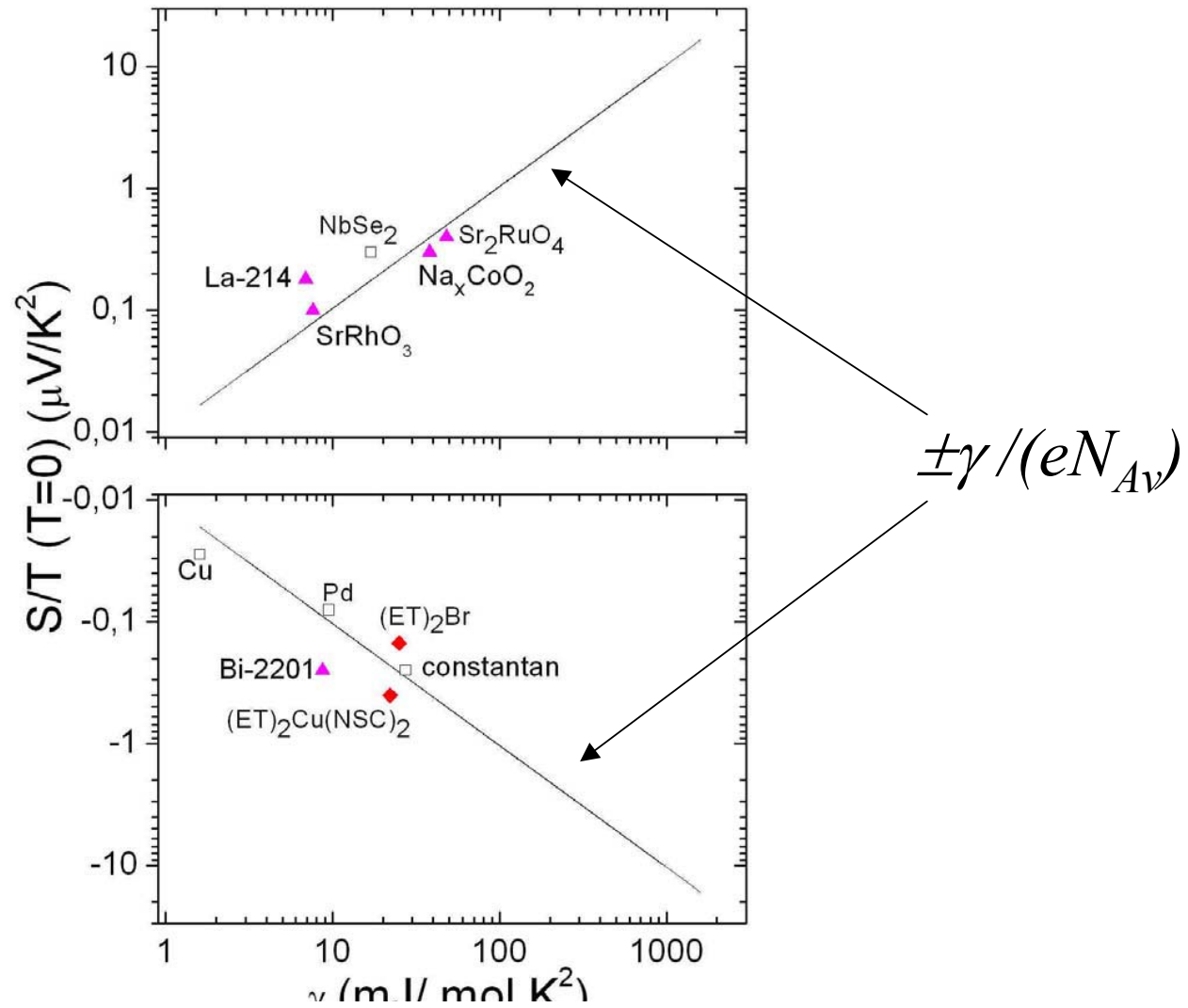
No subkelvin data for most U compounds



No subkelvin data available for these two!

$$\pm \gamma / (e N_A v)$$

Other metals



Compound	S/T ($\mu\text{V} / \text{K}^2$)	Remarks	γ (mJ/mol K^2)	q
CeCu ₂ Si ₂ ($B = 4T$)	9[30]	polycrystal	950[52]	0.9
CeCu ₈	29[33]	along [010]	1600[53]	1.7
CeAl ₃	14[32]	polycrystal	1400[32]	1.0
CeRu ₂ Si ₂	2.4[31]	in-plane	350[54]	0.7
CeCoIn ₅ ($B=6T$)	6[55]	in-plane	650[56]	0.9
CePt ₂ Si ₂	2[57]	along [110]	130[58]	1.5
CeSn ₃	0.18[59]	polycrystal	18[60]	1.0
CeNiSn	50[61]	polycrystal	45[62]	107
YbCu _{4.5}	-7[63]	polycrystal	635[64]	-1.1
YbCuAl	-3.6[65]	polycrystal	267[66]	-1.3
YbCu ₄ Ag	-3.6[67]	polycrystal	200[68]	-1.7
YbCu ₂ Si ₂	-1[20, 69]	polycrystal	135[70]	-0.7
YbAl ₃	-0.6[20]	polycrystal	45[71]	-1.3
YbInAu ₂	-0.75[69]	polycrystal	40[72]	-1.8
UPt ₃	unknown	none observed[35]	430[35]	-
UBe ₁₃ ($B=7.5T$)	-12[36]	polycrystal	1100[73]	-1.1
UNi ₂ Al ₃	0.24[37]	polycrystal	120[74]	0.2
UPd ₂ Al ₃	0.4[37]	S \perp c	150[75]	0.3
URu ₂ Si ₂	-3[38]	S \perp c	65[76]	-4.5
κ -(BEDT-TTF) ₂ Cu[N(CN) ₂] ₂ Br	-0.4[41]	in-plane	22[77]	-1.7
κ -(BEDT-TTF) ₂ Cu(NSC) ₂	-0.15[42]	in-plane	25[78]	-0.6
(TMTSF) ₂ ClO ₄	unknown	No report found	11[79]	-
Sr ₂ RuO ₄	0.3[44]	in-plane	38[4]	0.8
SrRuO ₃	unknown	No report found	30[80]	-
Sr ₃ Ru ₂ O ₇	unknown	No report found	38[81]	-
SrRhO ₃	0.03[82]	polycrystal	7.6[83]	1.3
Na _{∞} CoO ₂	0.4[45]	in-plane	48[46]	0.8
La _{1.7} Sr _{0.3} CuO ₄	0.18[47]	ceramic	6.9[6]	2.5
Bi ₂ Sr ₂ CuO _{6+δ}	-0.25[48]	ceramic	8.7[84]	-2.8
NbSe ₂	0.3[51]	in-plane	17[85]	1.7
Pd	-0.08[16]	polycrystal	9.5[86]	-0.8
Cu	-0.028[50]	along [231]	1.6[11]	-1.7
constantan (%43Ni-%57Cu)	-0.25[14]	wire	27.4[87]	-0.9

Table 1. Reported magnitudes of linear thermopower and specific heat for a number of metals. The significance of the coefficient $q = \frac{S}{T} \frac{NA_{22}}{\gamma}$ is discussed in the text.

Behnia, Jaccard, Flouquet
J. Phys. Condens. Matter
16, 5187(2004)

Sr₂RuO₄: a well-established Fermi liquid

A. P. Mackenzie and Y. Maeno: Superconductivity of Sr₂RuO₄ and the physics of spin-triplet pairing

665

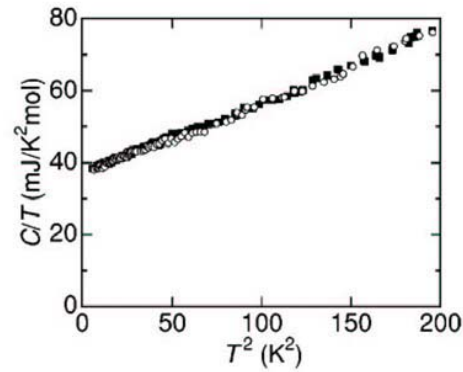


FIG. 7. The total specific heat of Sr₂RuO₄ divided by temperature between T_c and 14 K in zero field (filled squares) and an applied magnetic field of 14 T (open circles) applied parallel to c . From Mackenzie, Ikeda, *et al.* (1998).

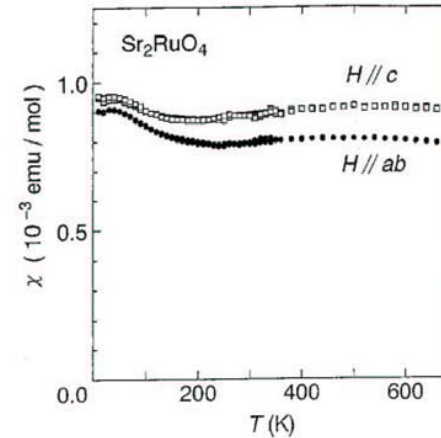
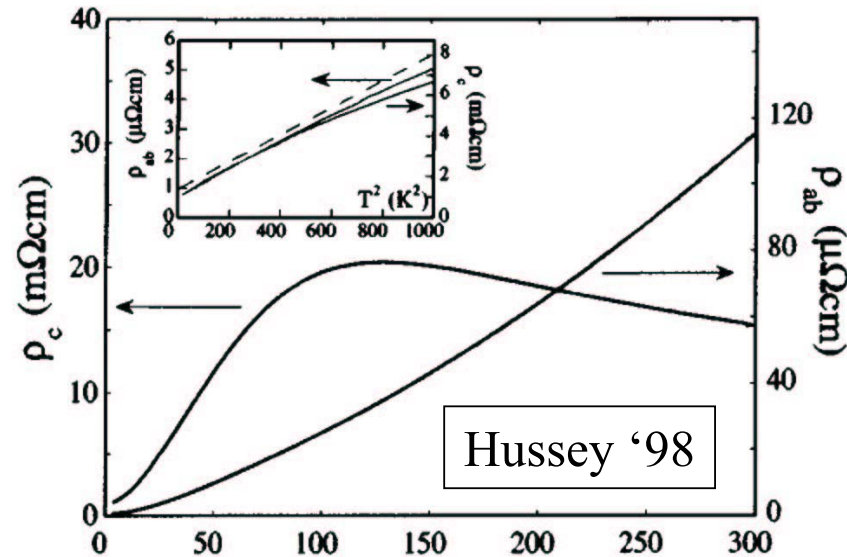
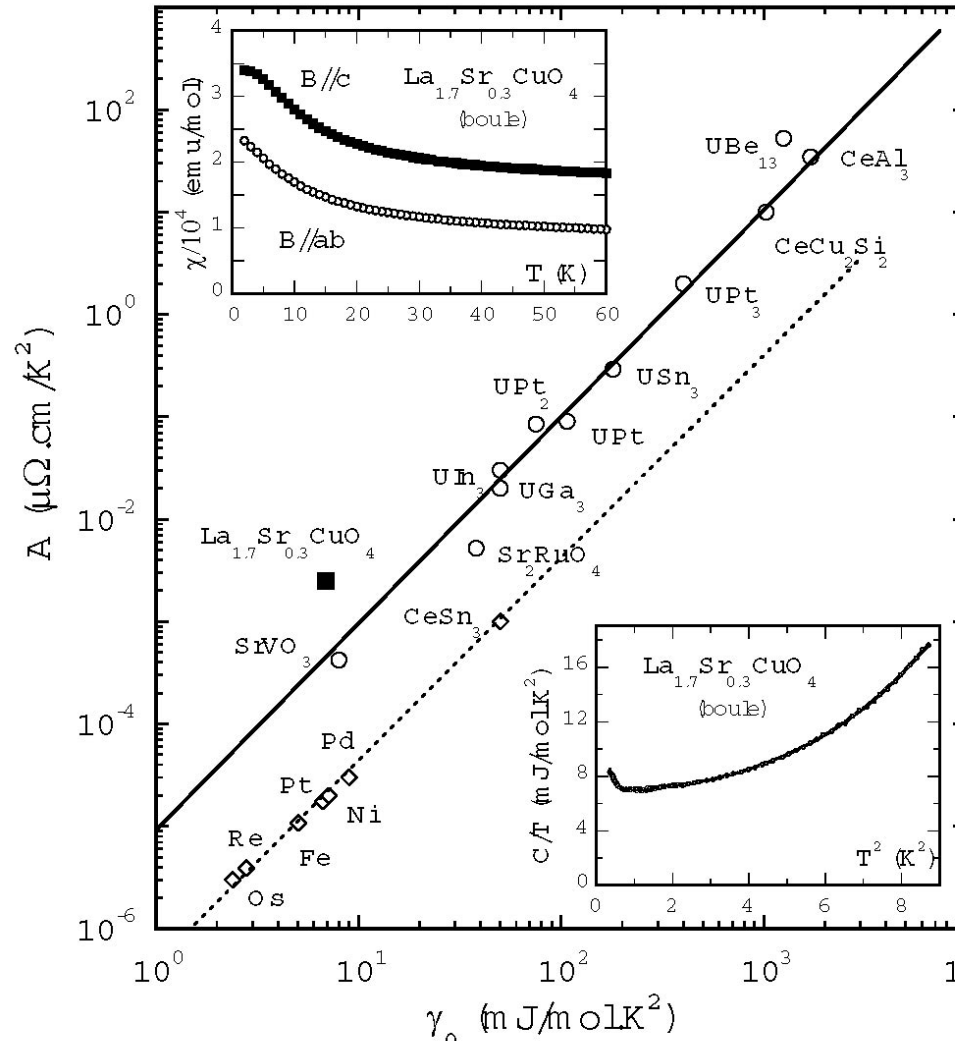
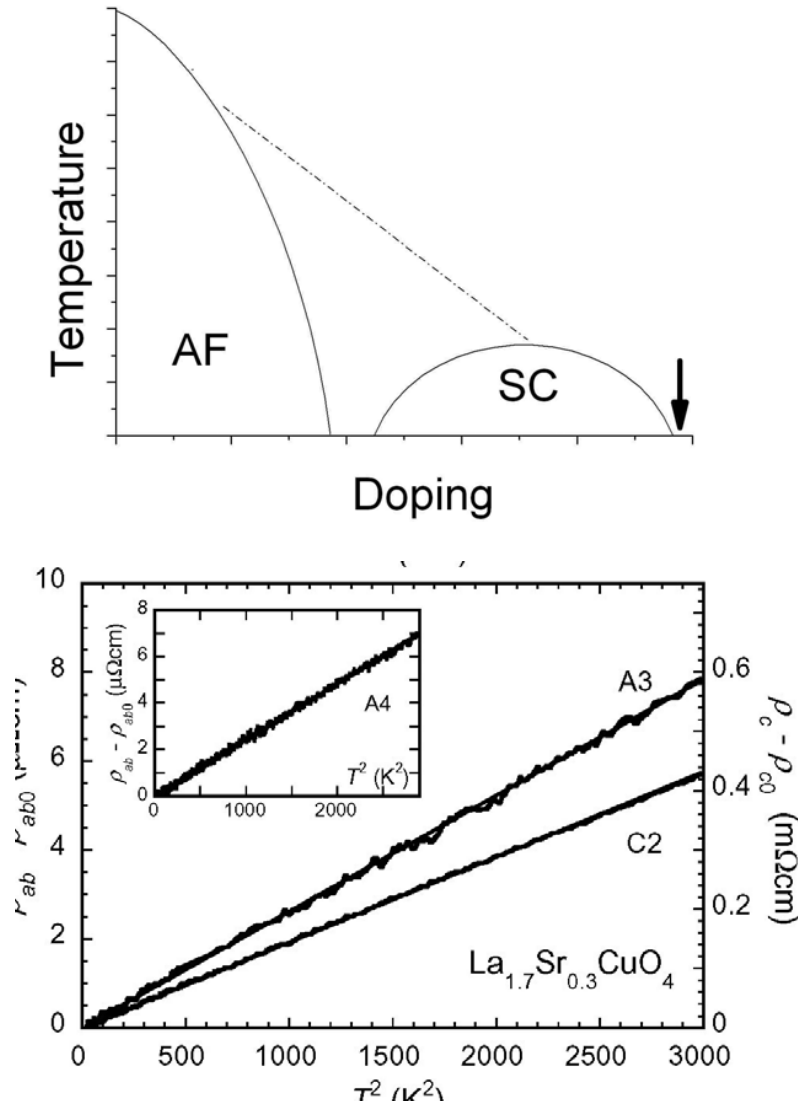


FIG. 8. The static susceptibility of Sr₂RuO₄ for fields of 1 T applied parallel to the ab plane and the c axis, from Maeno *et al.* (1997).

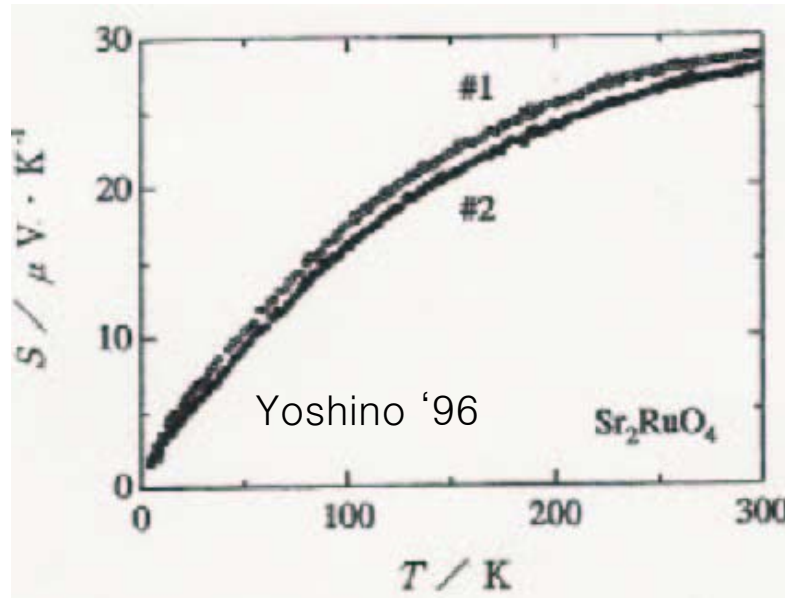


Hussey '98

Another remarkable Fermi liquid: $\text{La}_{1.7}\text{Sr}_{0.3}\text{CuO}_4$



The ratio q is a probe of carrier density!



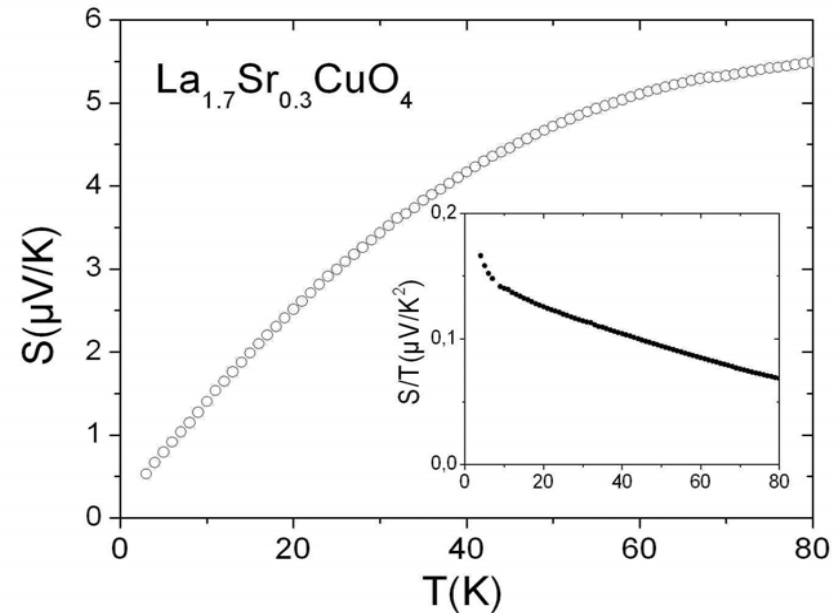
$$\gamma = 38 \text{ mJ / mol K}^2$$

$$S/T = 0.3 \text{ } \mu\text{V/K}^2$$

$$q = 0.8 \text{ (1.2 carrier per site)}$$

γ measures entropy per elementary cell!
 S/T measures entropy per carrier!

Jin *et al.*, to be published



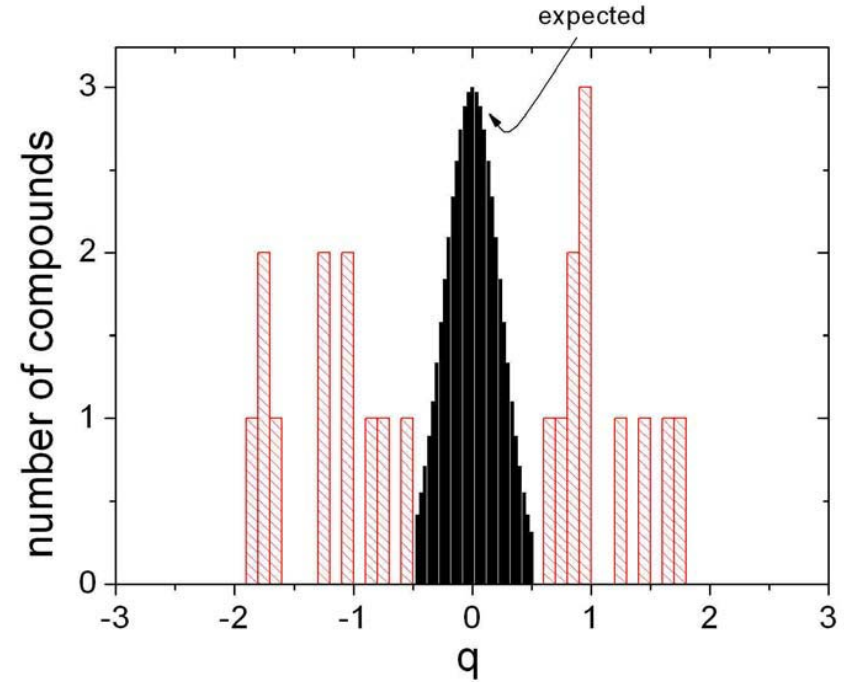
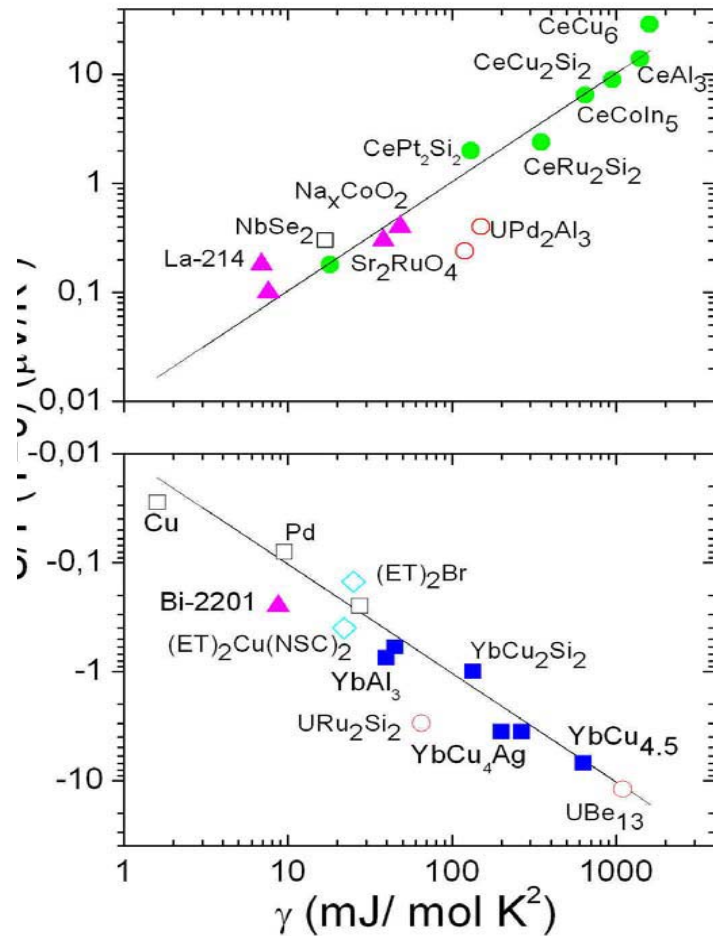
$$\gamma = 6.9 \text{ mJ / mol K}^2$$

$$S/T = 0.18 \text{ } \mu\text{V/K}^2$$

$$q = 2.5 \text{ (0.4 carrier per site)}$$

Is then the
 FS of LSCO at $x=0.3$
 still hole-like?
 What about ARPES?

An enigma!



Asymmetry of mass renormalisation for electrons and holes?

What governs the sign?

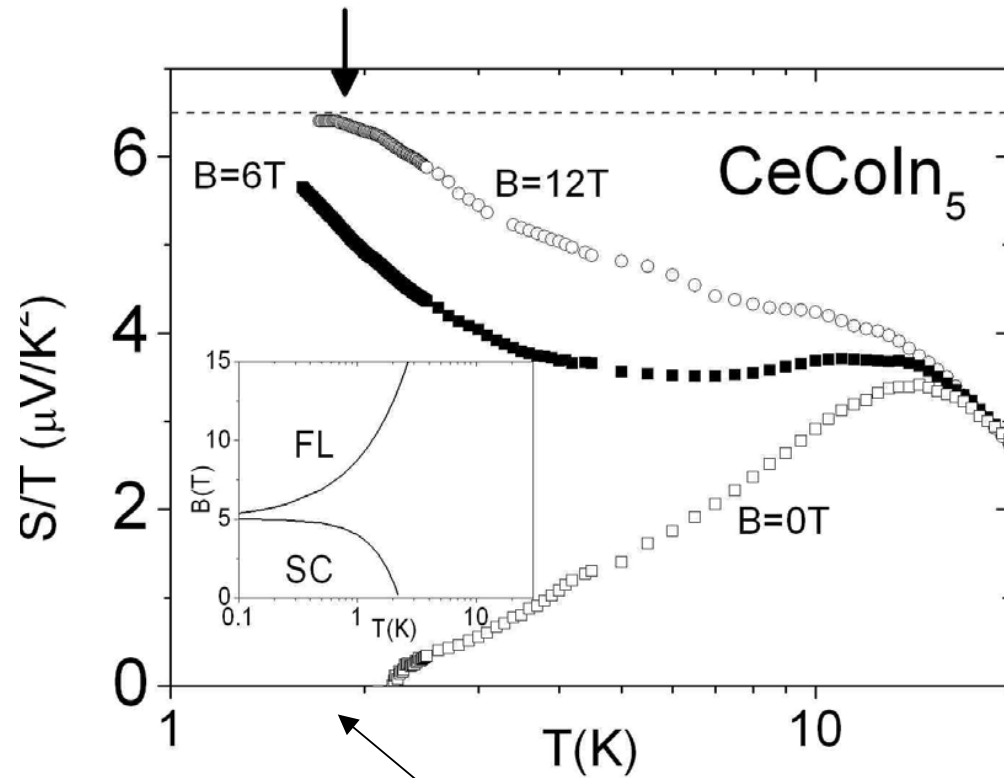
Why does this simple free-electron-gas picture work even in the case of multi-band Fermi surfaces?

An observation

- [Within the resolution of available data], the magnitude of q is the same for different families
- This contrasts with KW plot : A/γ^2 varies from $0.04a_0$ (in Yb compounds) to $50 a_0$ (Na_xCoO_2).
- Contrary to KW, q links two zero-energy properties. [Yet it should mirror anomalous $\tau(\varepsilon)$!]

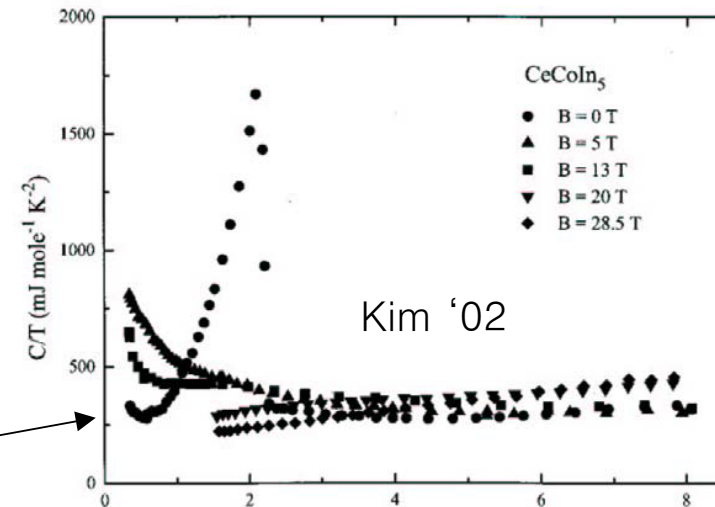
A tool for tracking non-trivial physics!

Example: $CeCoIn_5$ at the onset of superconductivity:

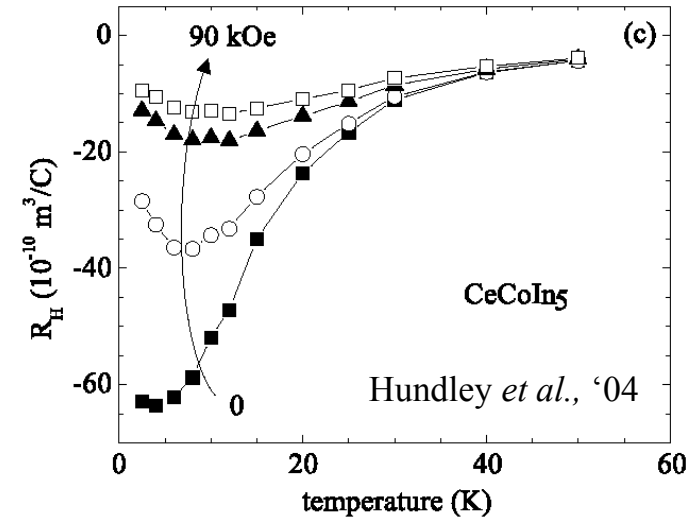
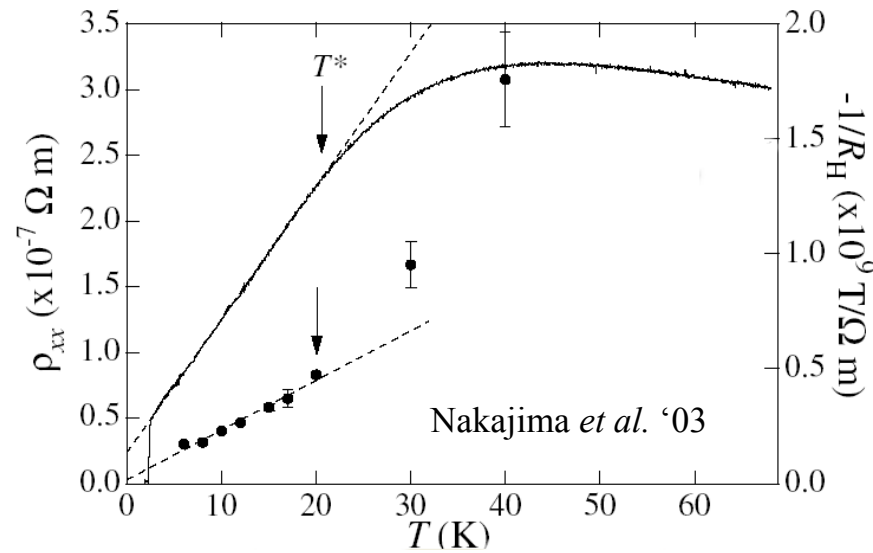


S/T strongly field-dependent!

And γ field-independent up to 13T!



Zero-field anomalous transport properties of CeCoIn_5



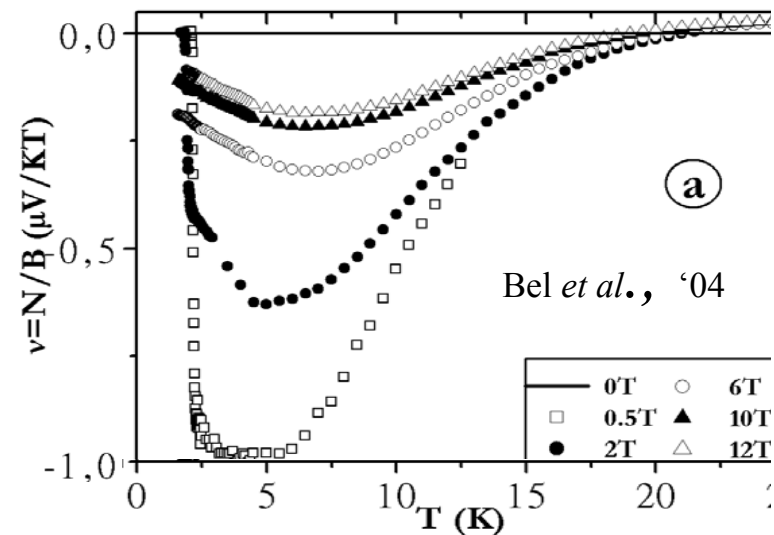
linear resistivity

temperature and field-dependent Hall effect

giant Nernst effect

low-magnitude thermopower

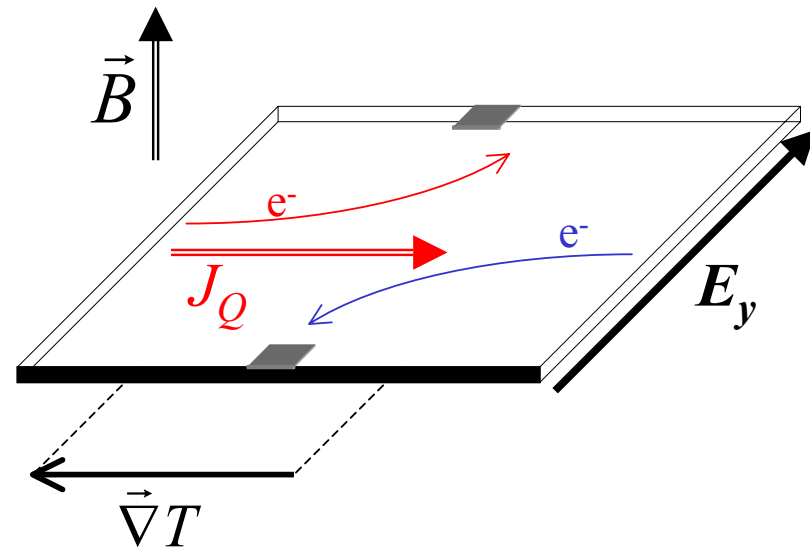
All zero-field anomalies!
 [Pointing to a non-trivial $\tau(\epsilon)$]



Sondheimer cancellation in single-band metals

- ✓ Counterflow of hot and cold electrons

$$J_Q \neq 0 ; J_e = 0 ; E_y = 0$$

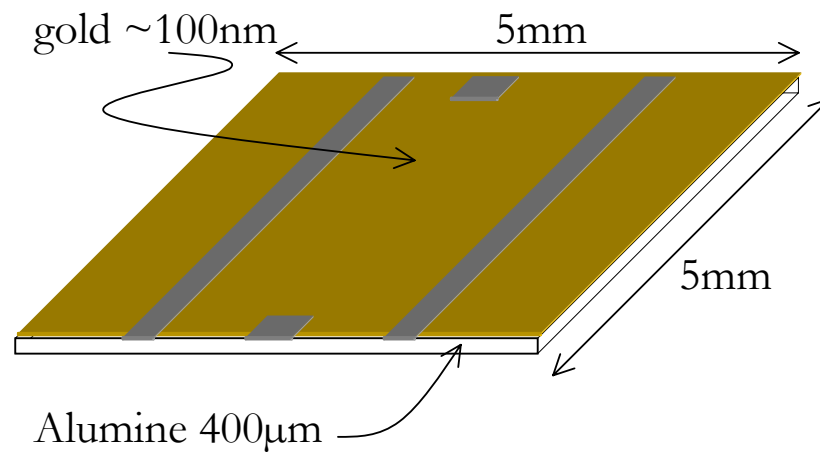
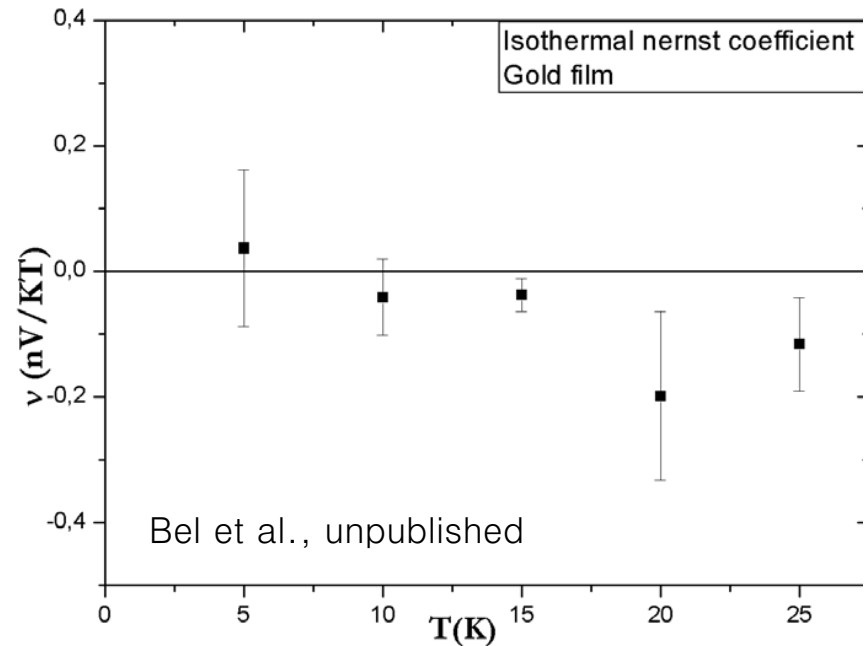


Dans un métal simple, l'effet Nernst est nul

Isothermal gold effect in gold

✓ Gold film evaporated on Alumine

✓ Very small Nernst coefficient ($\nu = N/B \sim 0.1 \text{ nV/KT}$)



Ambipolar Nernst effect in NbSe₂

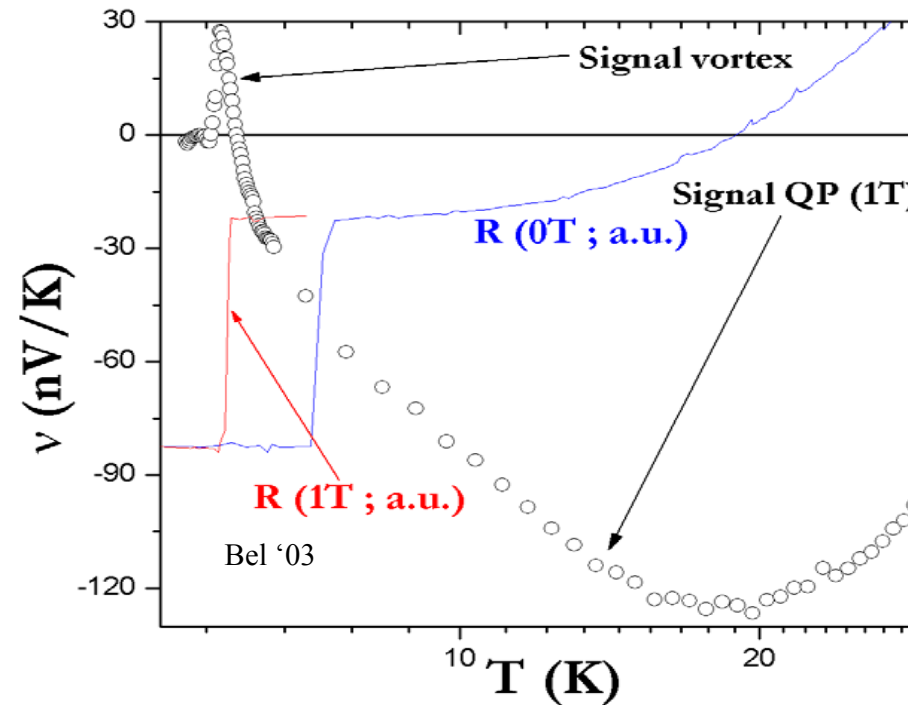
ˆ NbSe₂ : superconductor with T_c ~ 7,2 K.

ˆ Charge Density wave at ~32K.

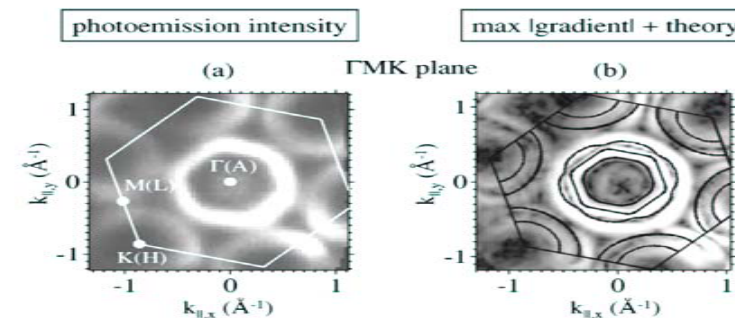
ˆ Multi-band metal

ˆ Positive vortex signal

ˆ A negative Nernst signal of comparable magnitude in the metallic state.



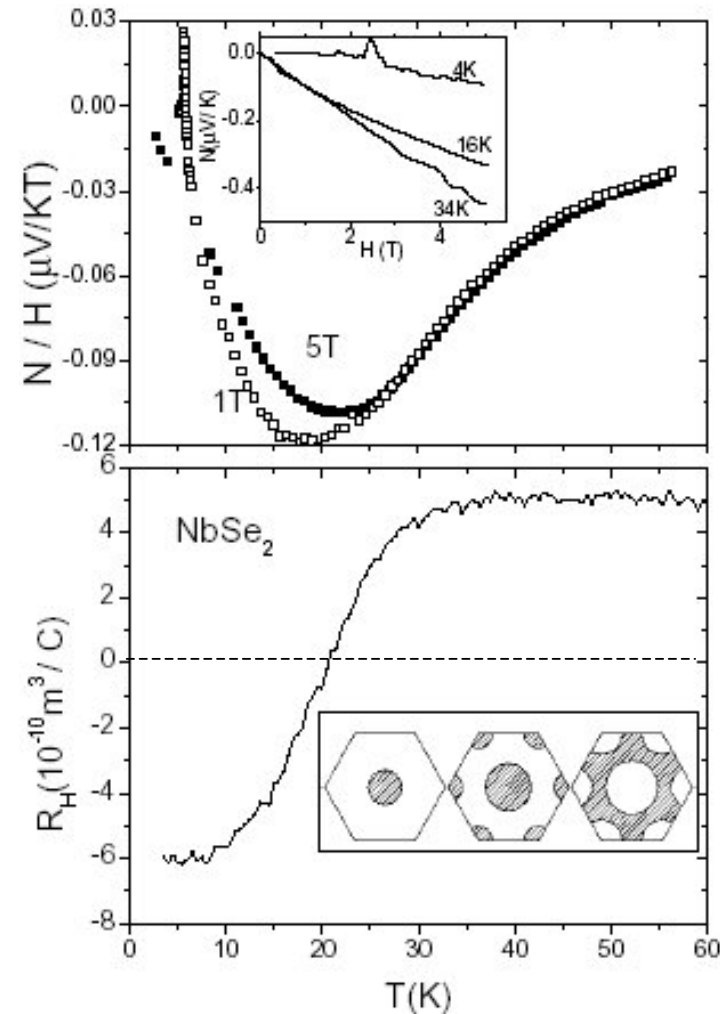
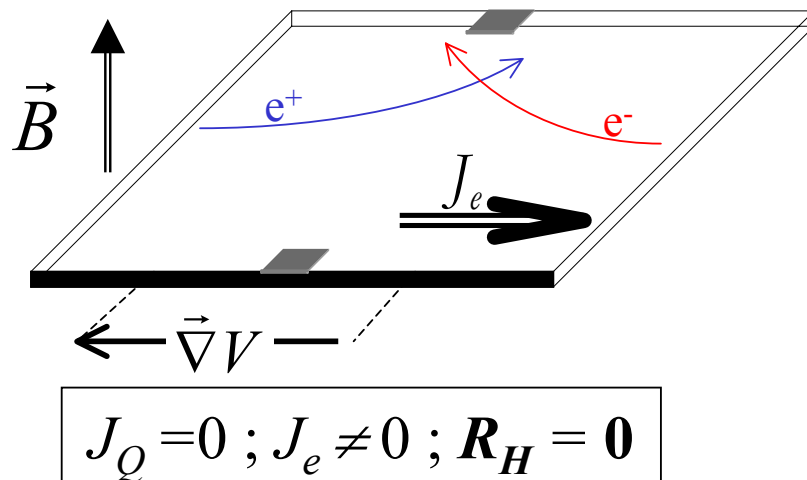
Surface de Fermi
 Rossnagel et al. *PRB* 64, 235119 (2001)



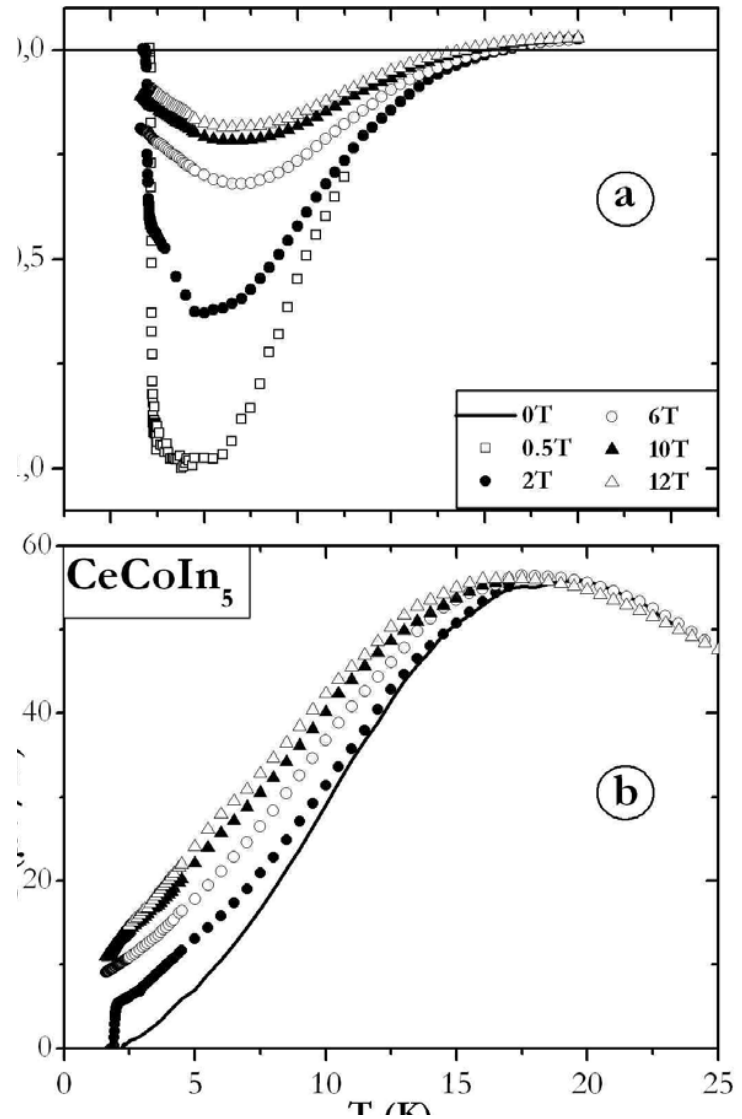
No Sondheimer cancellation in a multi-band metal!

✓ The Nernst signal is maximum when the hall coefficient is zero!

✓ Known as the ambipolar Nernst effect!



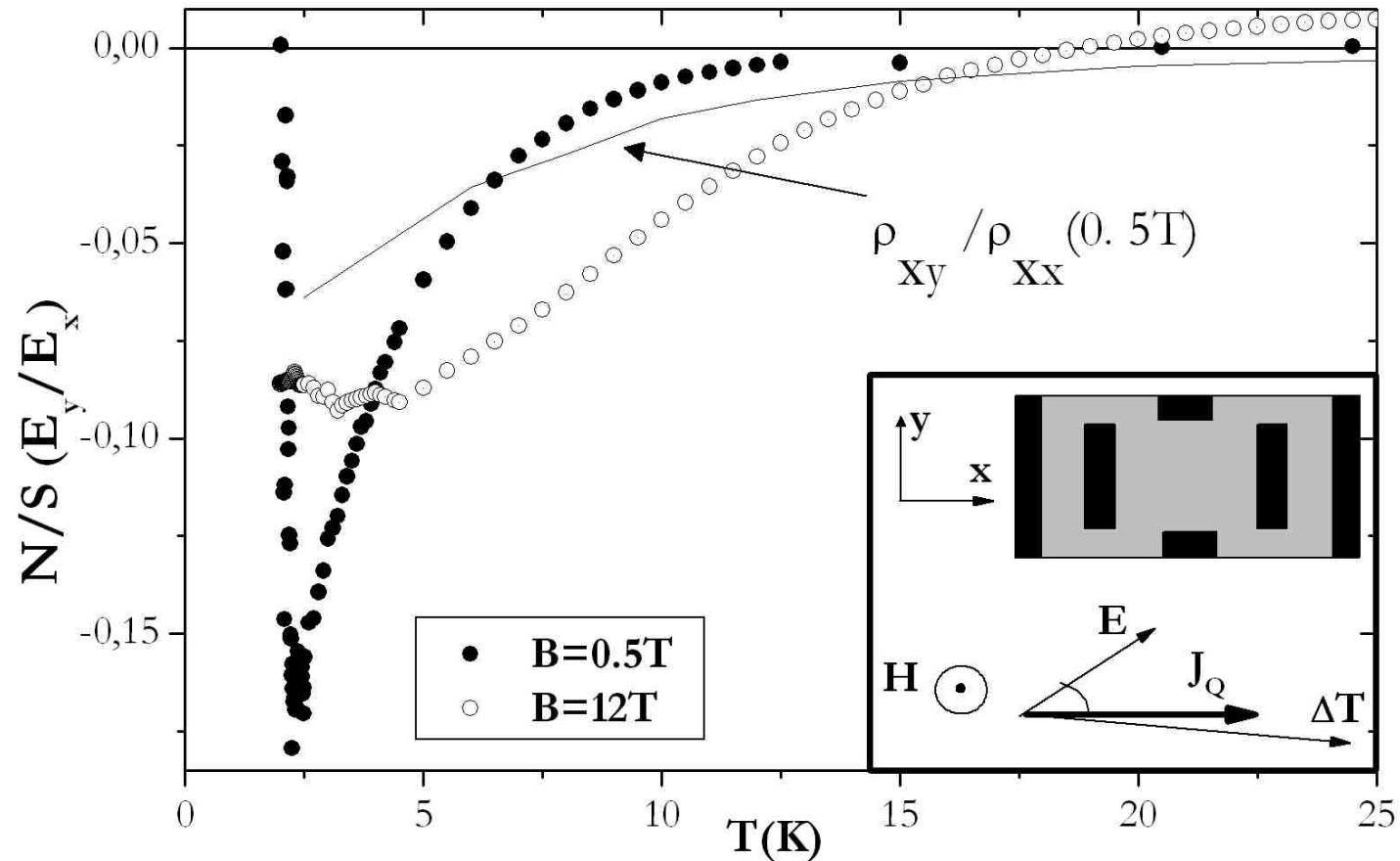
Giant Nernst effect in CeCoIn₅



- ✓ One order of magnitude larger
- ✓ Emerges in presence of a large Hall effect
- ✓ Restricted to a limited region in the H,T plane

$$V \propto \left(\frac{\partial \tau}{\partial \epsilon} \right)$$

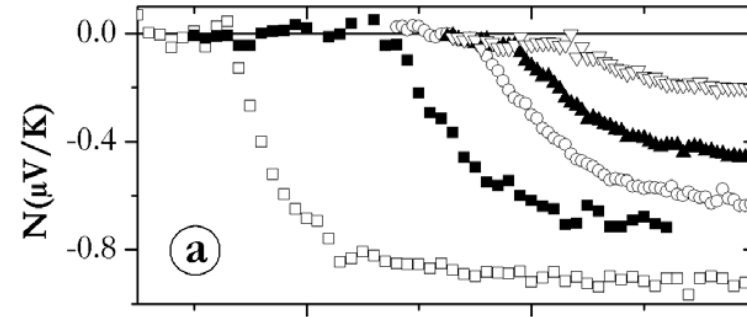
In the $T=0$ limit, the N/S ratio diverges!



A longitudinal thermal gradient produces a purely transverse electric field!

The vortex Nernst signal in CeCoIn_5

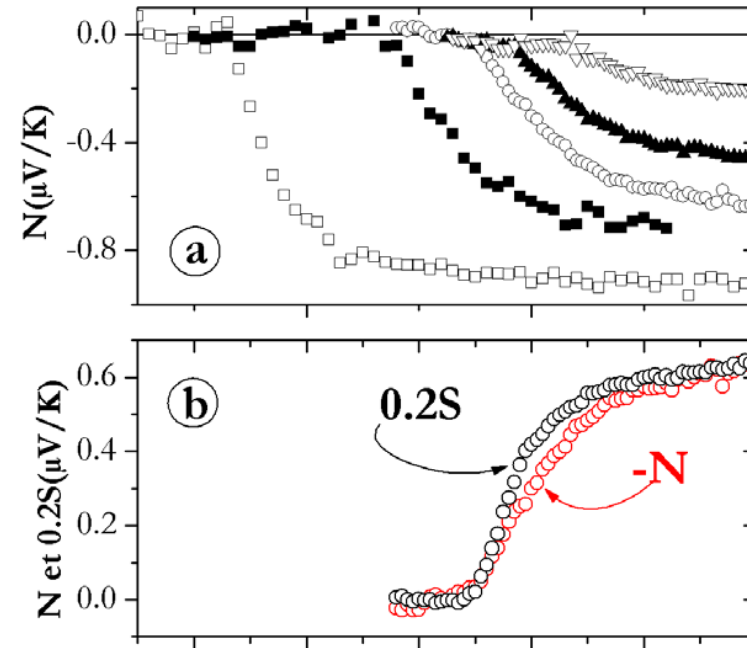
✓ No trace of a positive signal in the vicinity of the superconducting transition



The vortex Nernst signal in CeCoIn₅

✓ No trace of a positive signal in the vicinity of the superconducting transition!

✓ But Nernst signal collapses faster than the Seebeck signal.

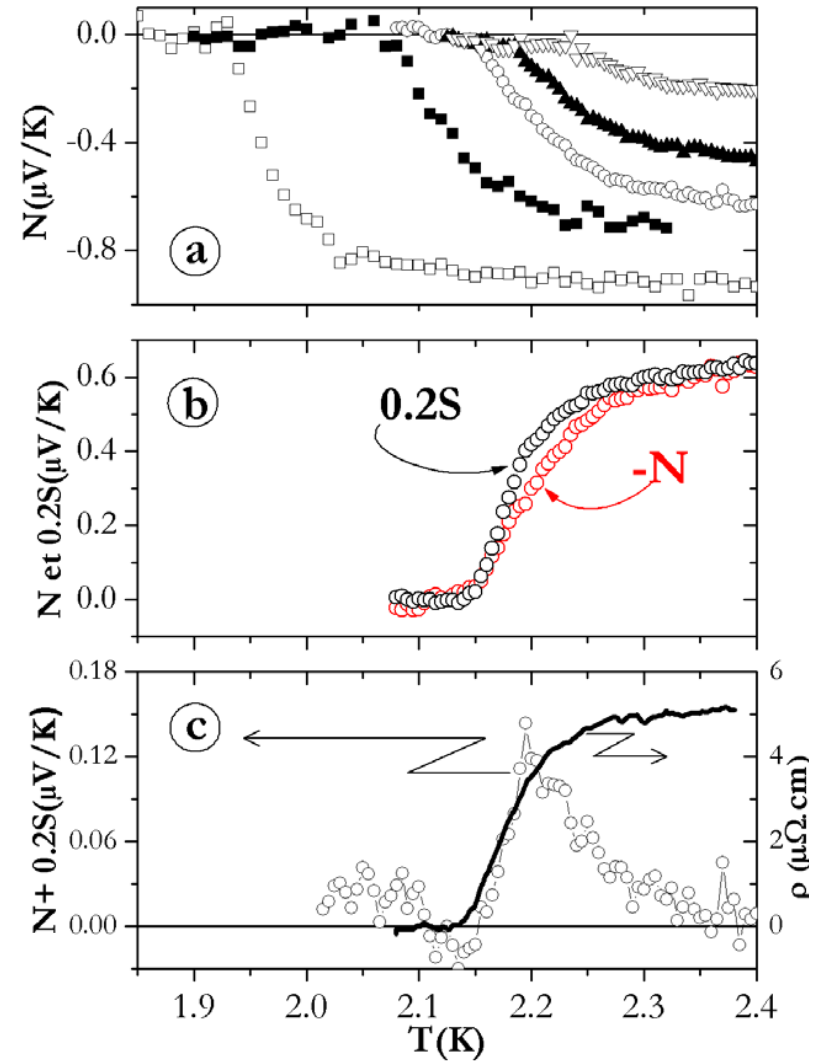


The vortex Nernst signal in CeCoIn₅

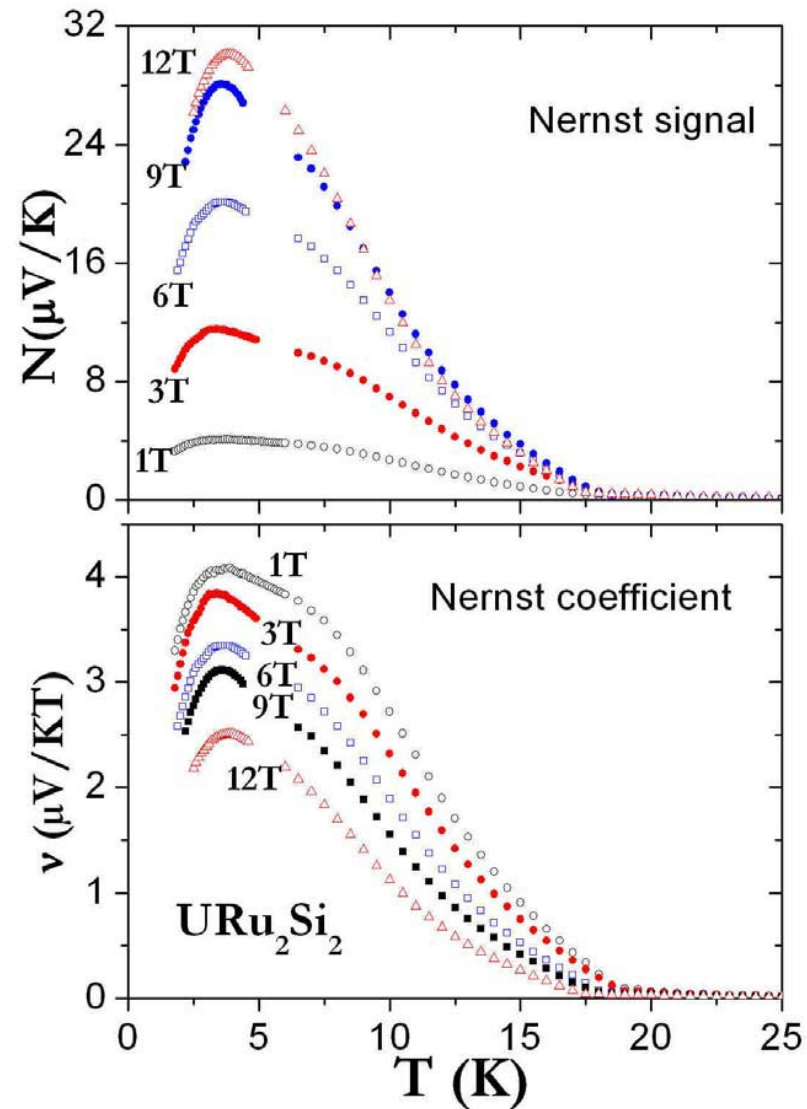
✓ No trace of a positive signal in the vicinity of the superconducting transition

✓ But Nernst signal collapses faster than the Seebeck signal.

✓ Plotting $aS - N$, the vortex Nernst signal, overwhelmed by the normal-state signal, can be extracted.



Giant Nernst effect in the hidden order phase of URu_2Si_2



Hidden order in URu₂Si₂

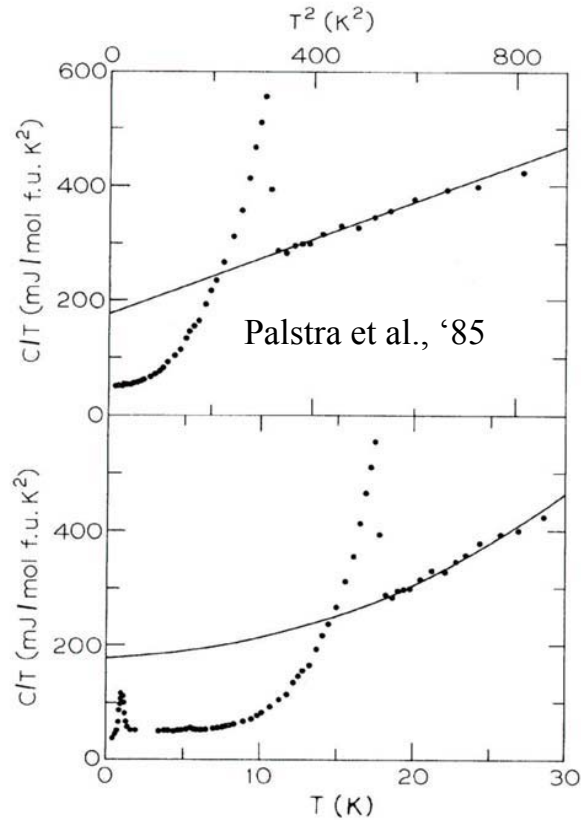


FIG. 1. Specific heat of URu₂Si₂ plotted as C/T vs T^2 (above) yielding γ and Θ_D , and as C/T vs T (below) showing the entropy balance.

- ✓ Large macroscopic anomalies occur at $T_0 \sim 18\text{K}$
- ✓ But only a tiny magnetic moment ($0.02\mu_B$) appears!
- ✓ The order parameter is yet to be identified!

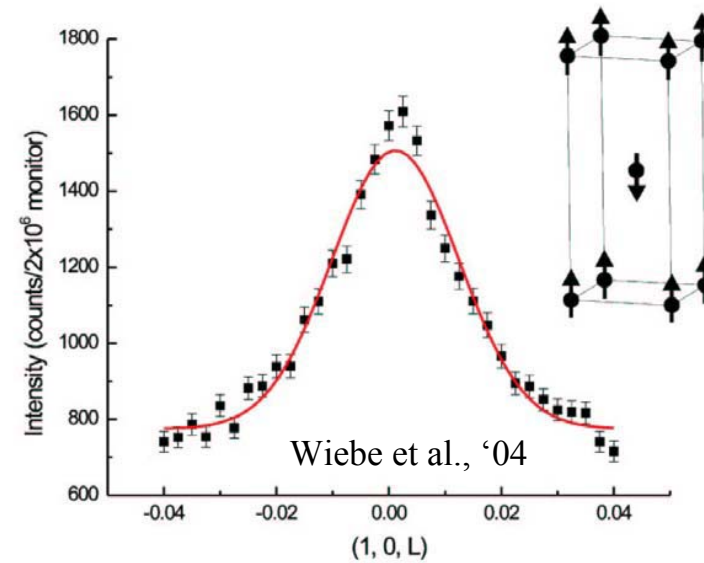
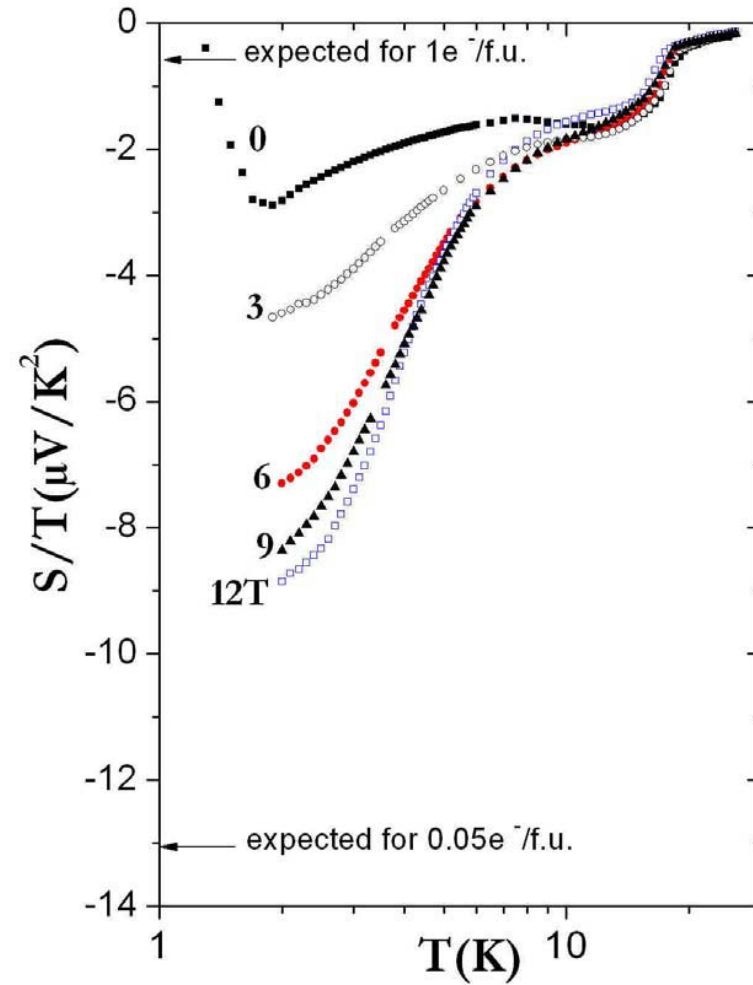
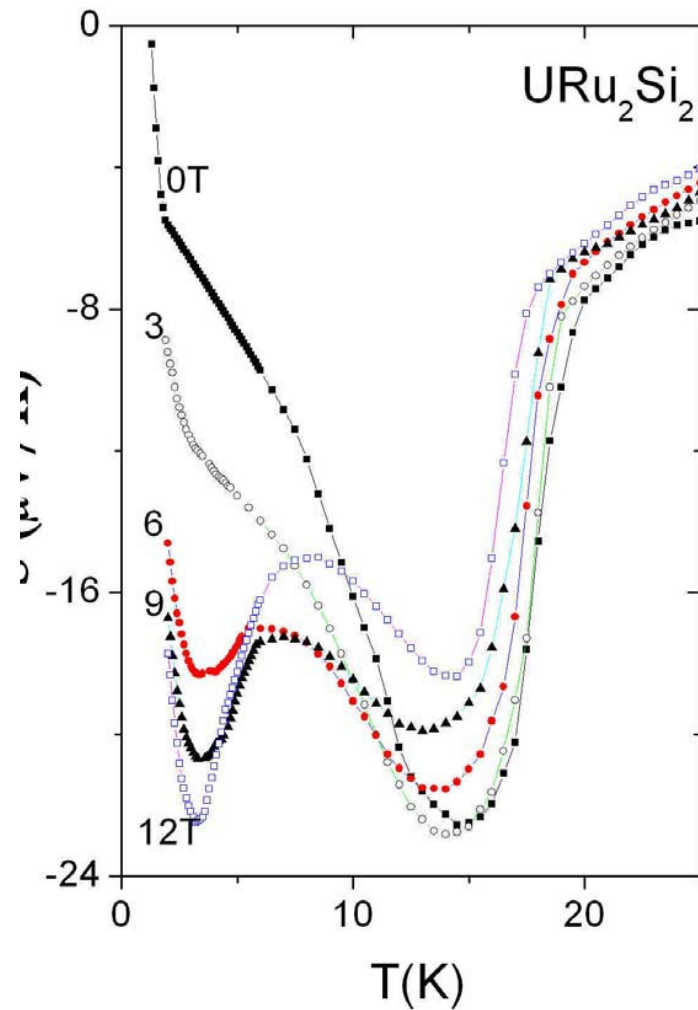


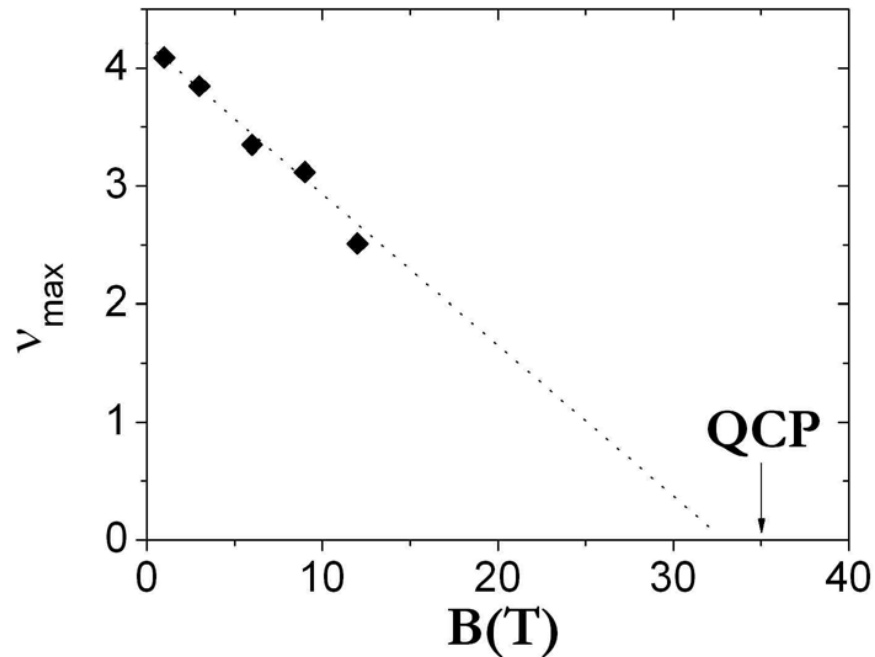
FIG. 1. The antiferromagnetic Bragg peak at $(1, 0, 0)$ and $T = 8\text{K}$ (fit is to a Gaussian). The inset shows the corresponding magnetic structure for the U^{4+} moments.

Seebeck coefficient in the hidden-order state

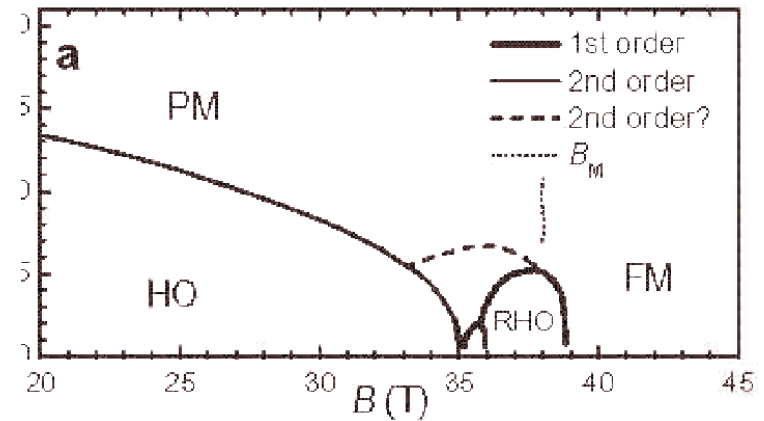


A small number of carriers survive in the hidden-order state!

The giant Nernst effect would not survive the destruction of the hidden order at a high magnetic field!



Decrease of maximum Nernst coefficient with magnetic field



Quantum Critical Point at 35 T
(Harisson, Kim, Jaime, Mydosh '03)

Correlation between the Nernst signal and the Hall angle

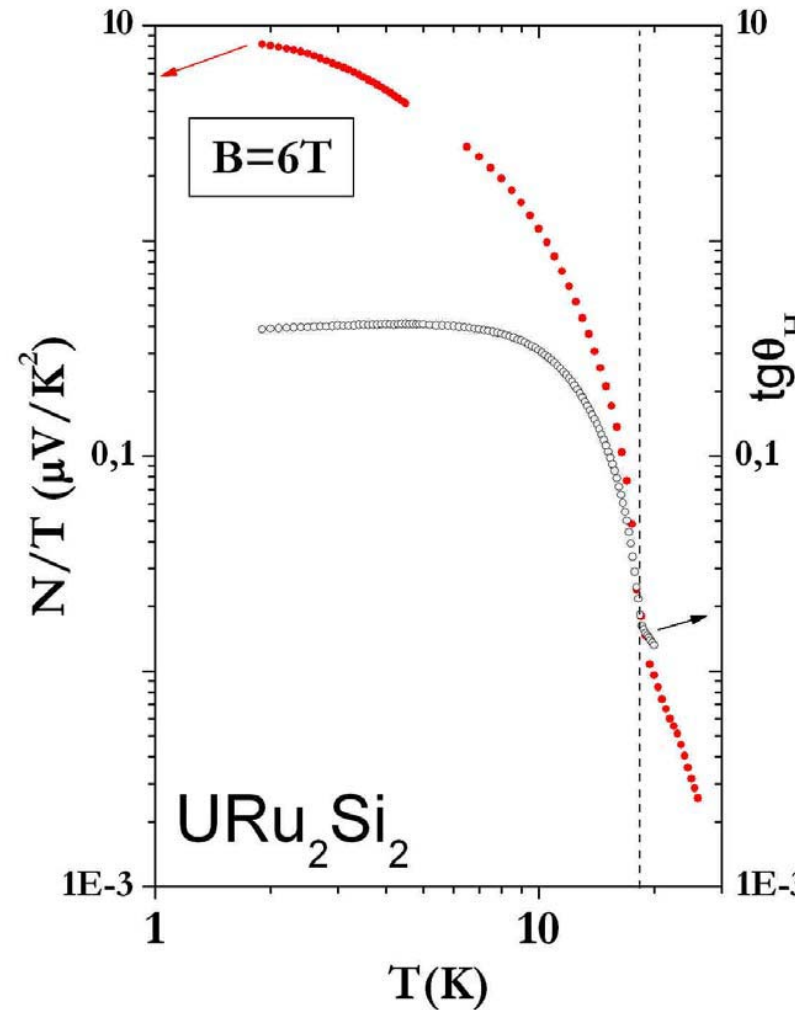
In a Boltzmann picture:

$$N = -\frac{\pi^2}{3} \frac{k_B^2 T}{e} \left. \frac{\partial \Theta_H}{\partial \epsilon} \right|_{\epsilon_F}$$

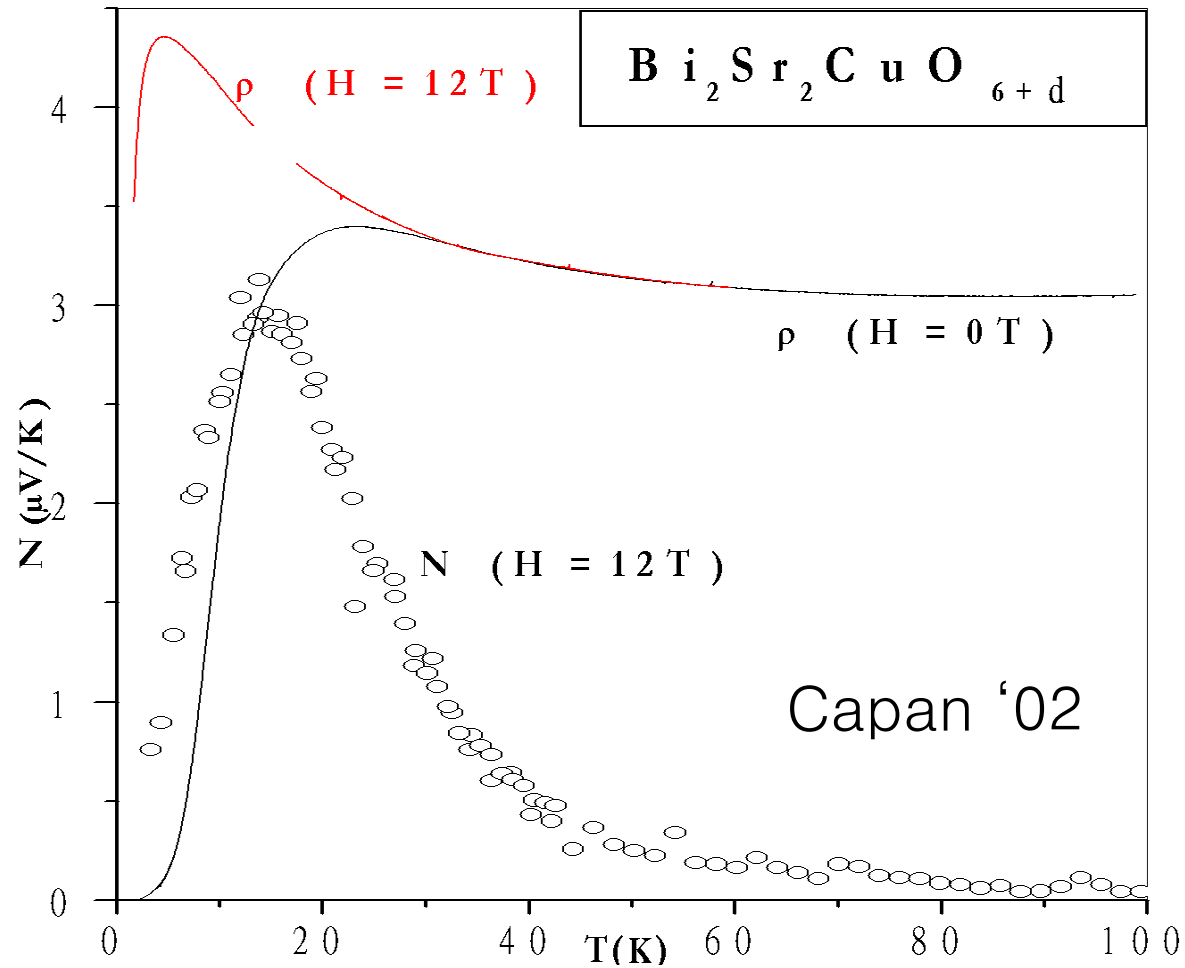
- Small ϵ_F in Heavy Fermions!
- Large θ_H in the hidden-order state!
- Could this combination explain the large N?

Only qualitatively:

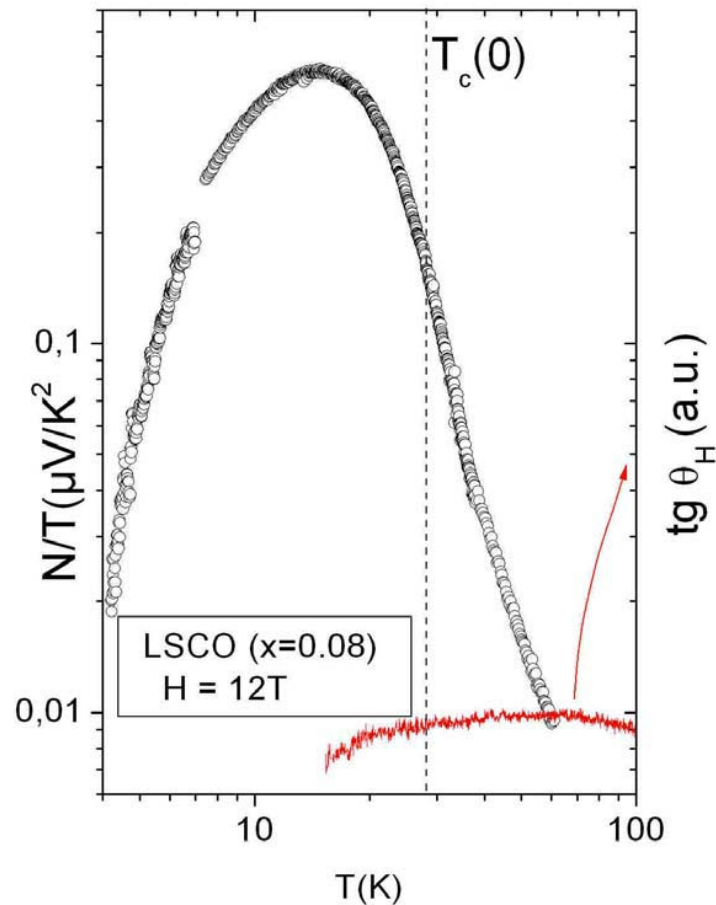
- Implies $\epsilon_F \sim 17\text{K}$!
- Even when θ_H constant, N/T increases!
- N/S diverges!



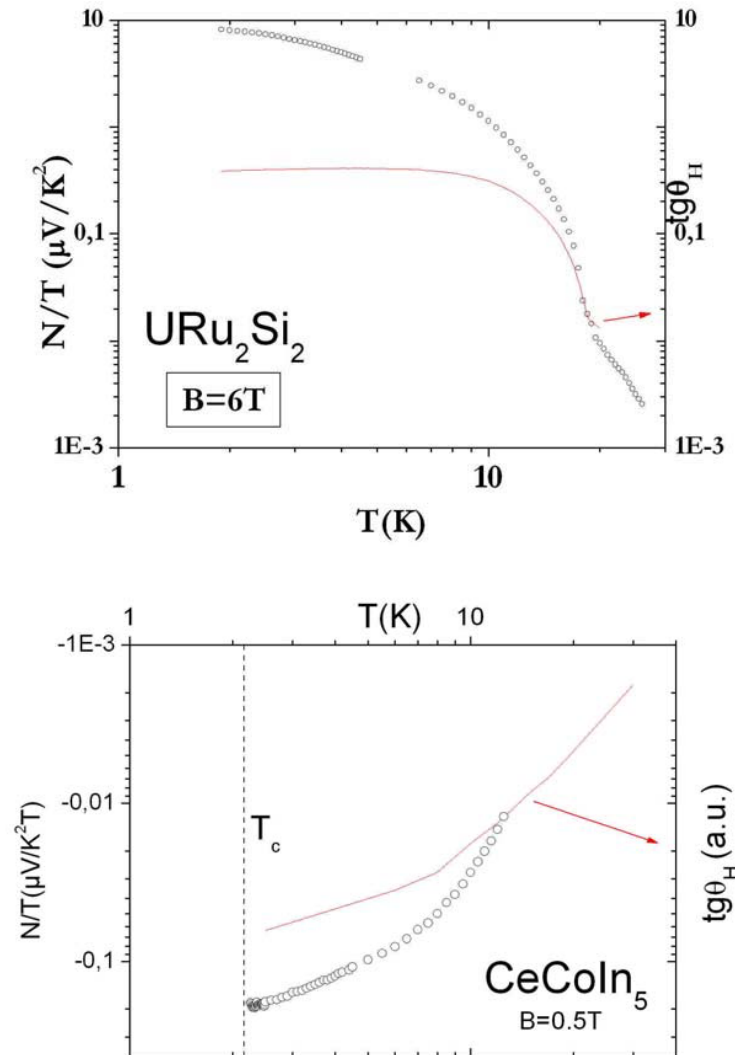
An order of magnitude larger than the vortex Nernst signal in cuprates



But, the anomalous Nernst signal in cuprates does NOT correlate with the Hall angle!



Superconducting fluctuations remain the most plausible source!



Summary

- It is instructive to look at the thermopower-to-specific heat ratio!
- In appropriate units, this ratio is close to unity for a wide range of compounds!
- Anomalously large Nernst signals CeCoIn_5 and URu_2Si_2 arise when this is not the case and point to a an unidentified source of transverse thermoelectricity!