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**Superconducting-induced spectral weight transfers  
in  $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ : BCS-like to unconventional  
superconductivity crossover**

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These are preliminary lecture notes, intended only for distribution to participants

# Superconducting-induced spectral weight transfers in $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$ : BCS-like to unconventional superconductivity crossover.

**Andrés Felipe Santander-Syro**

Laboratoire de Physique des Solides - Orsay

R. Lobo, N. Bontemps



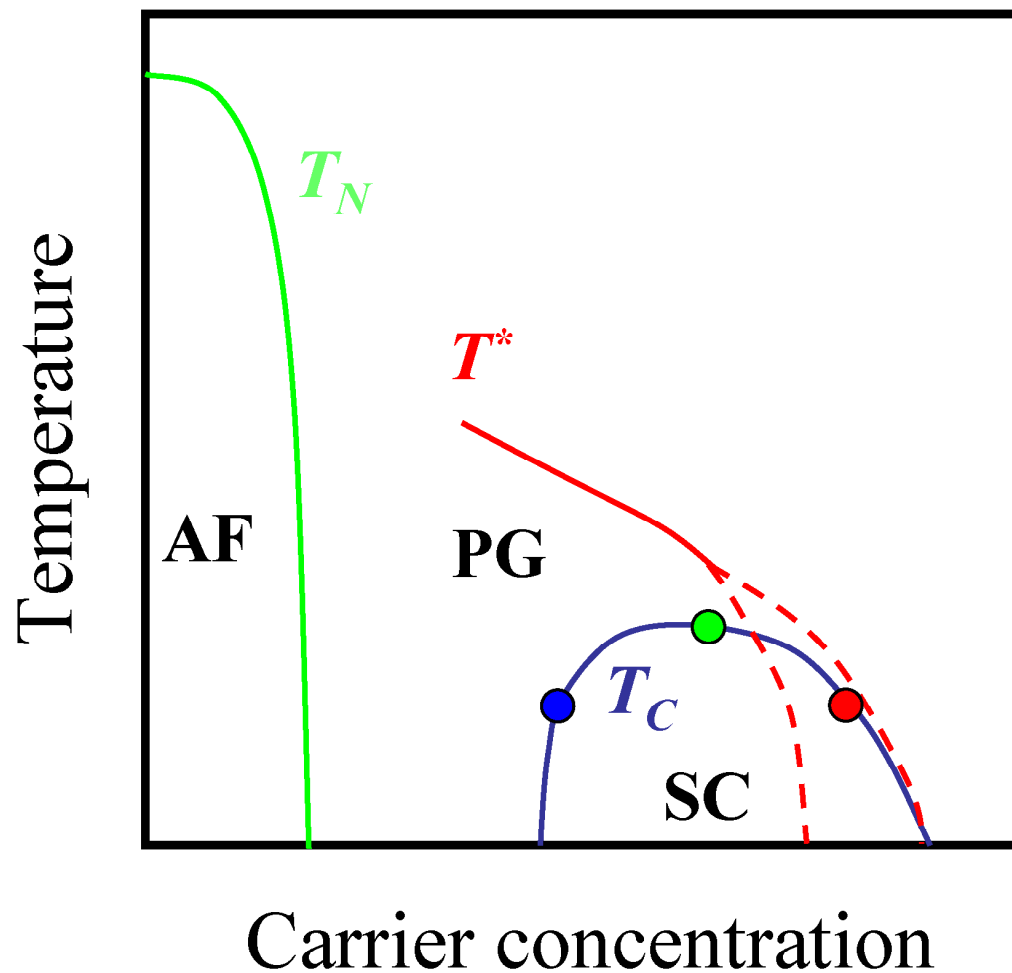
ESPCI - Paris  
IR spectroscopy

Z. Konstantinovic, Z. Li, H. Raffy

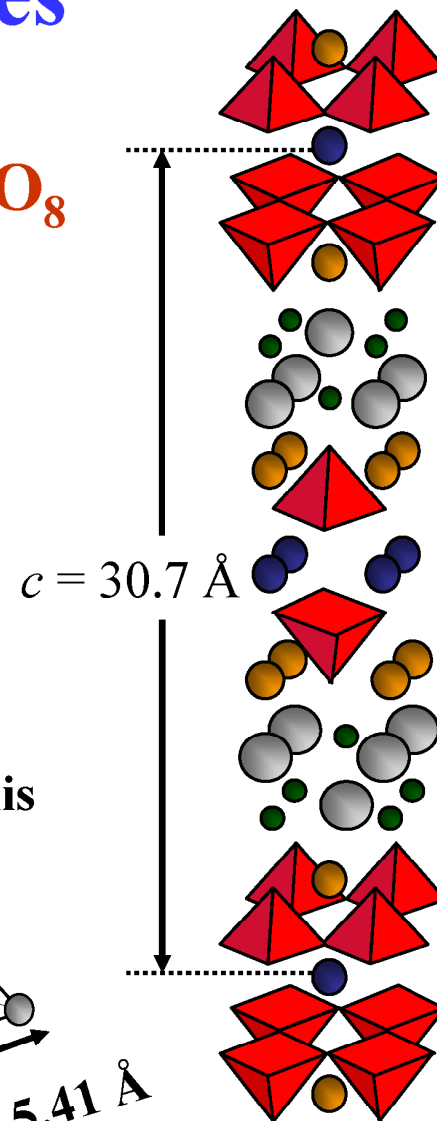
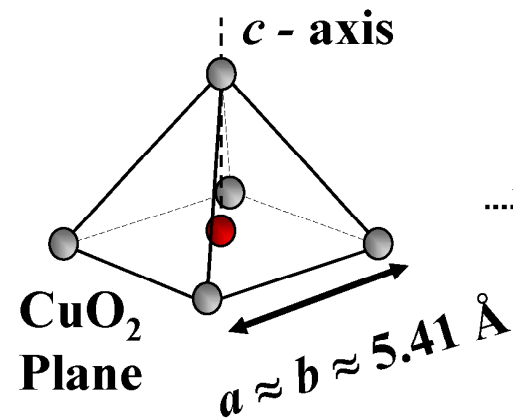


LPS – Orsay  
Samples

# Some generalities of cuprates



- → Bi
- → Sr
- → Ca
- → O
- → Cu

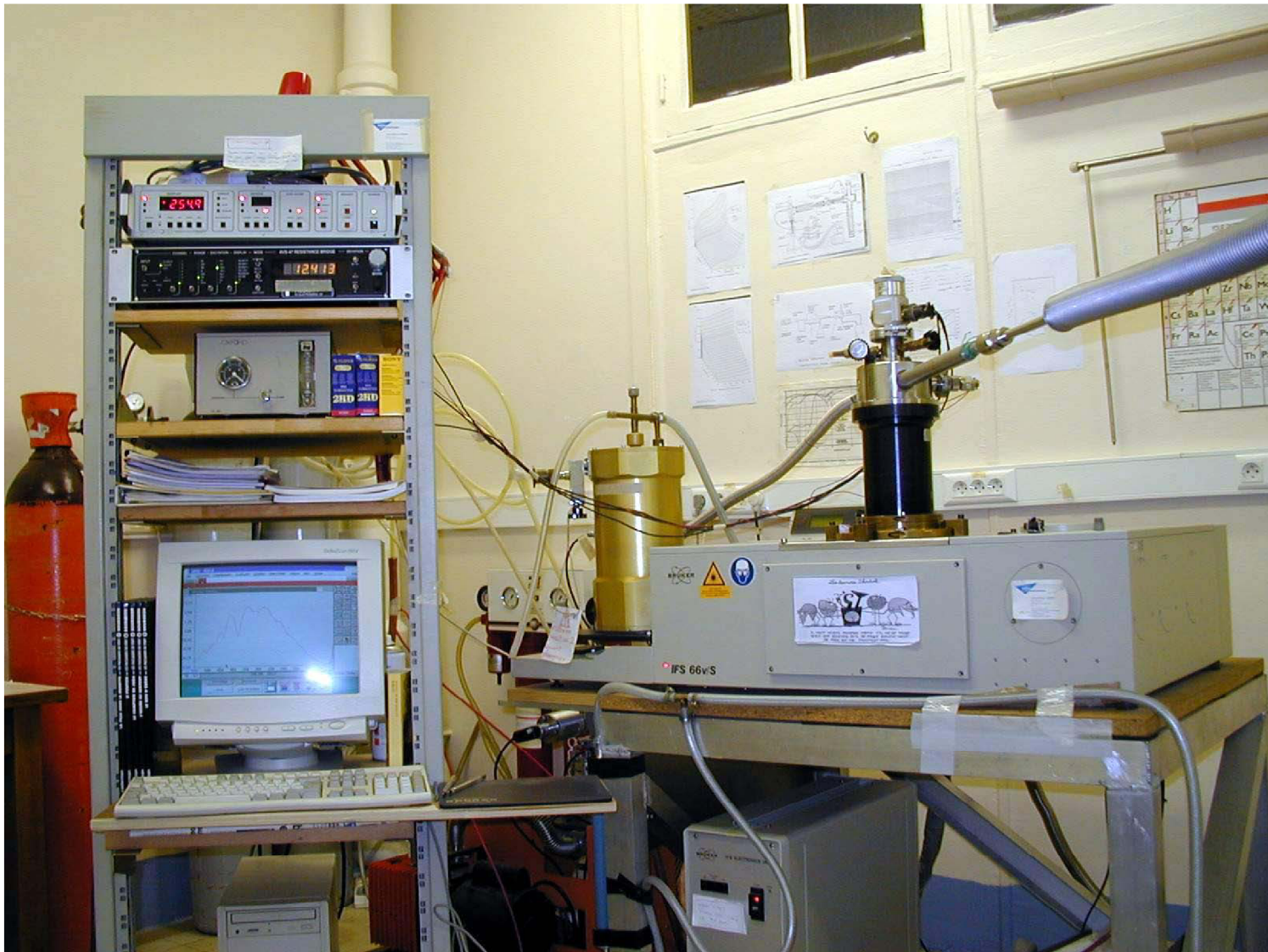


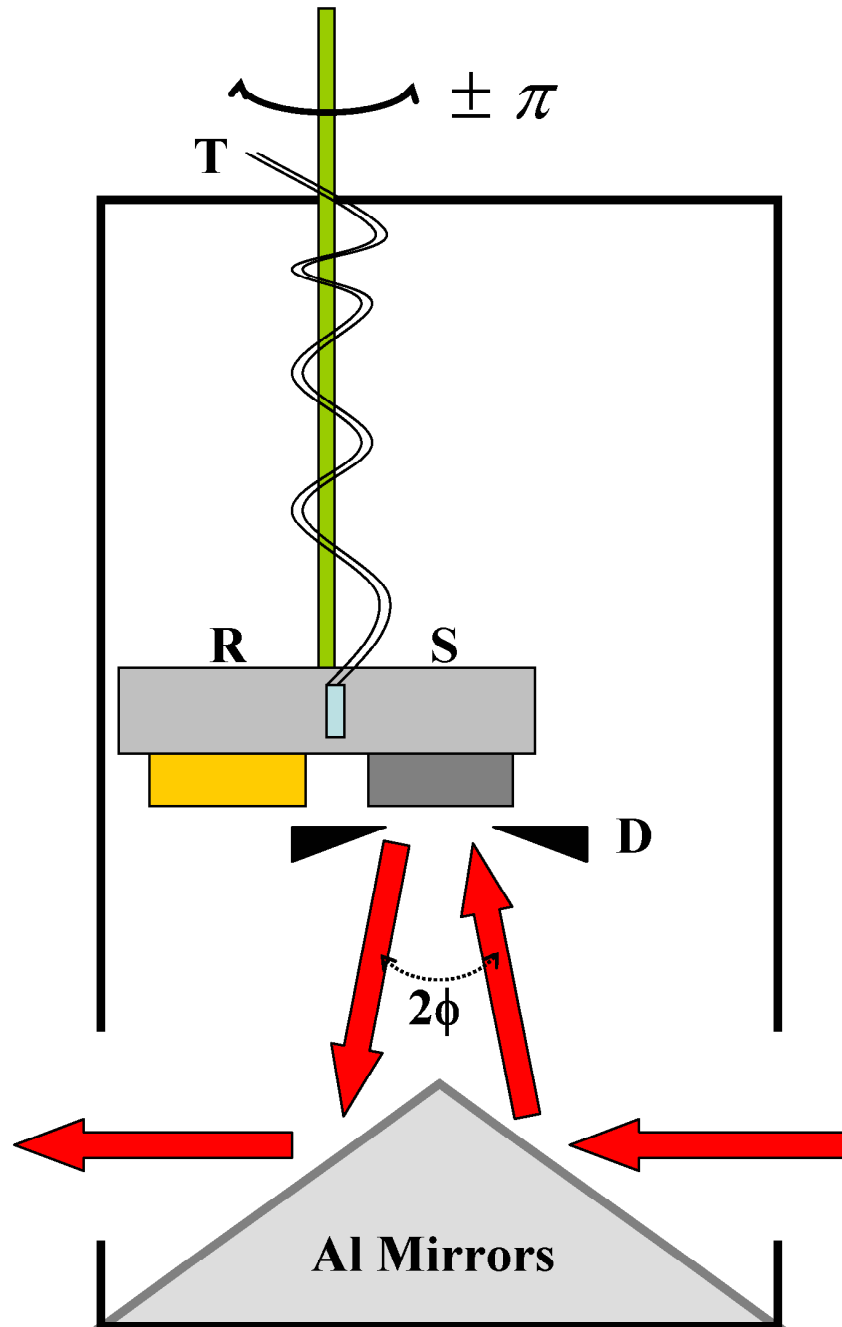
# Problems studied

## FROM UNDERDOPED TO OVERDOPED

- **Energy scale of the excitations that are modified by the superconducting transition.**
- **Superconducting-induced kinetic energy change of the in-plane charge carriers.**

# **The art of infrared reflectivity measurements**

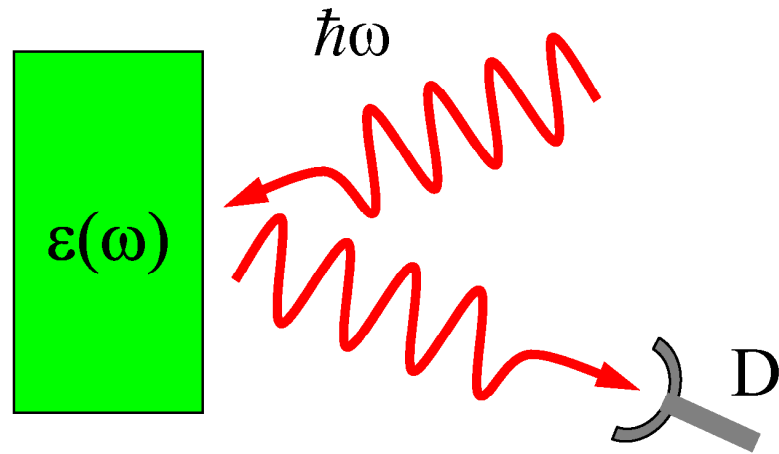




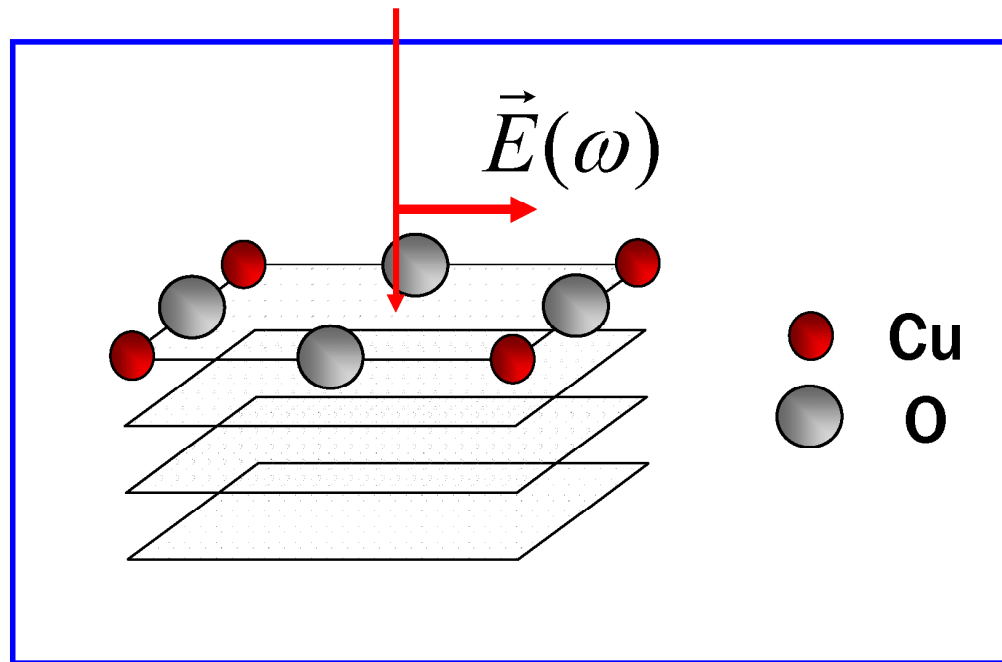
## The sample holder

- $\Phi < 8^\circ$
- Alignment S/R  
better than  $10^{-3}$  rad

# From reflectivity to conductivity



Normal incidence





# Optical response of the charge carriers

Reflectivity  $R(\omega)$   $\longrightarrow$   $\sigma(\omega)$  = Complex conductivity

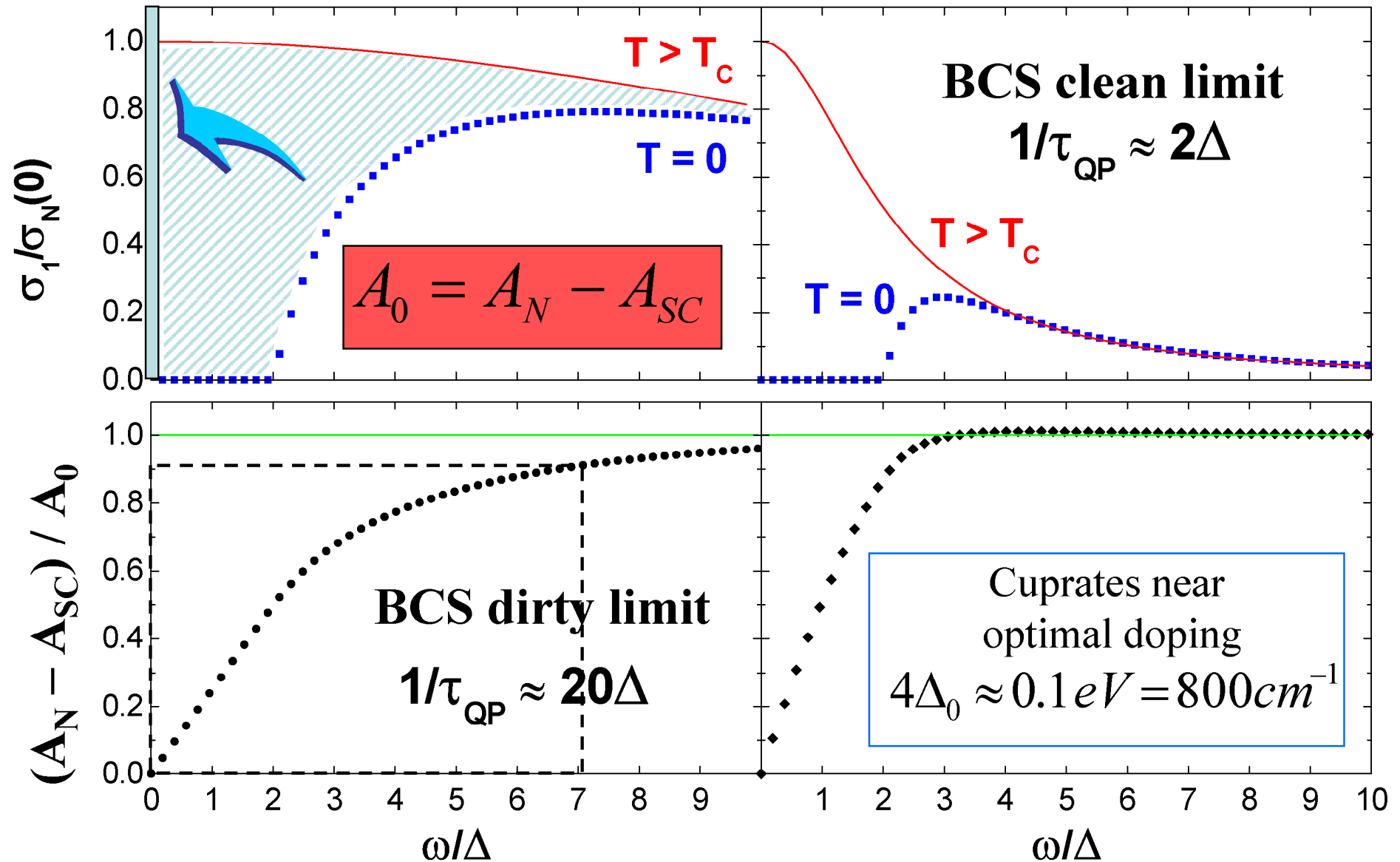
$\text{Re} [\sigma(\omega)] \sim$  Rate of electromagnetic energy absorption per unit volume

## « OSCILLATOR STRENGTH » SUM RULE

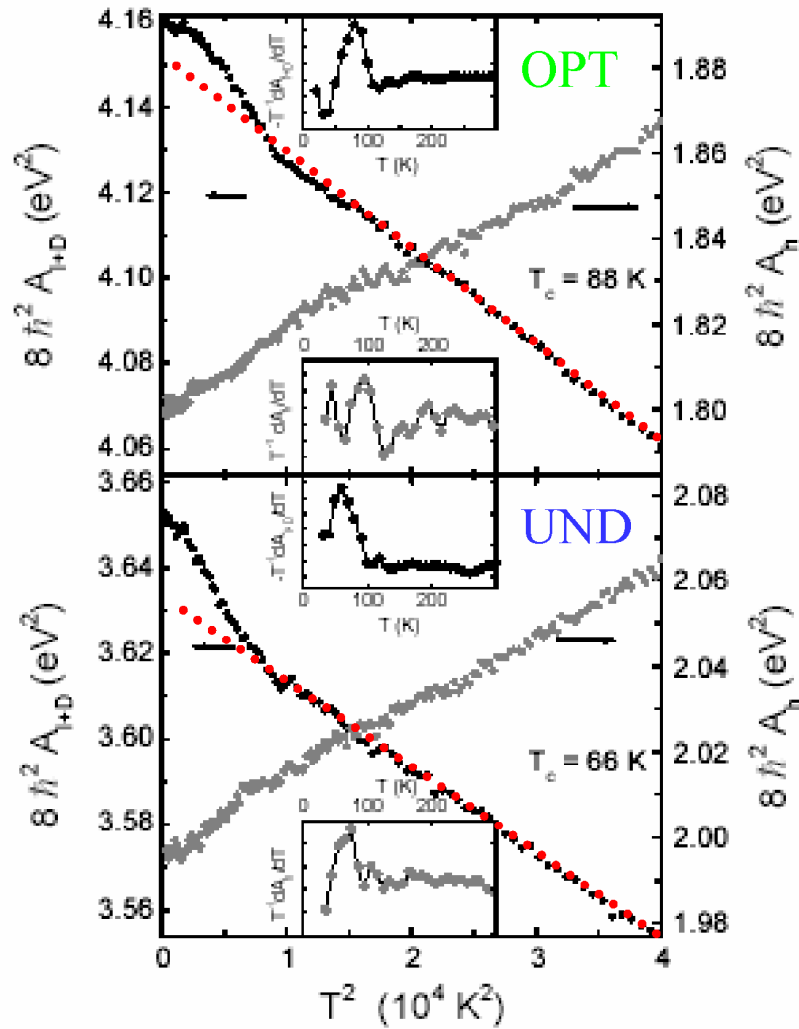
$$\int_0^{\infty} \text{Re}[\sigma(\omega)] d\omega = \frac{\pi n e^2}{2 m_e}$$

$n$  [ $\text{m}^{-3}$ ] = Total density of carriers  
 $m_e$  [Kg] = Carrier bare mass  
 $e$  [C] = Electron charge

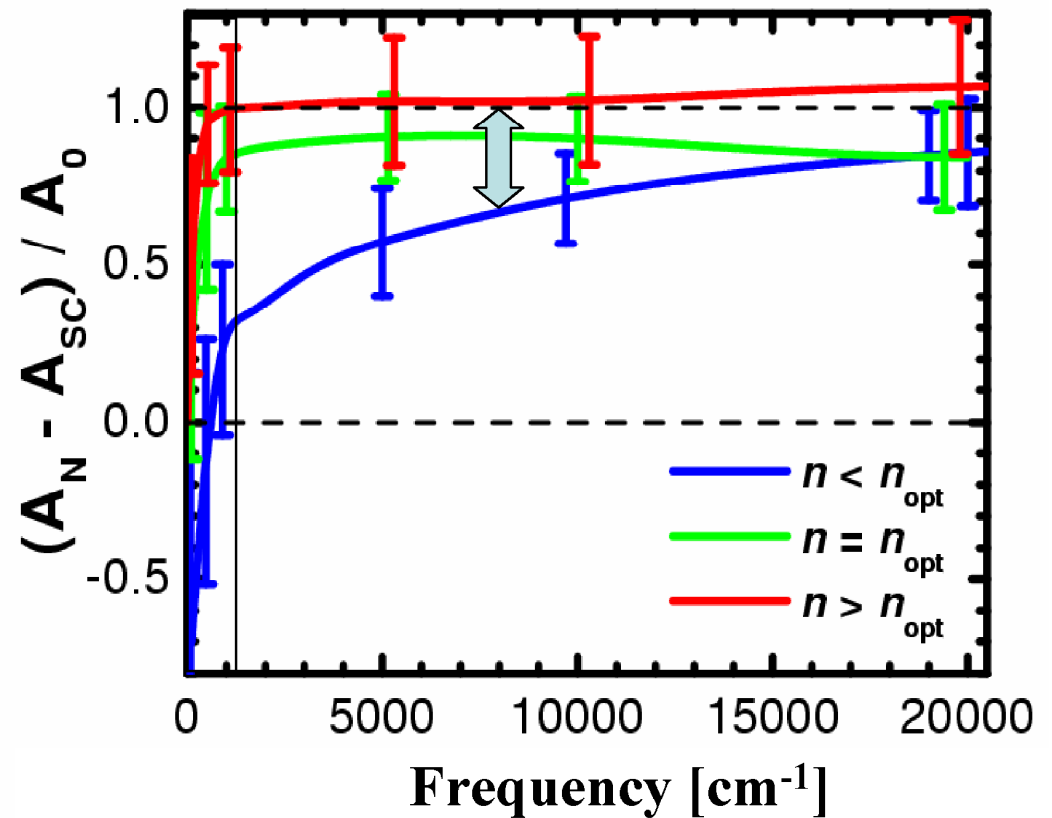
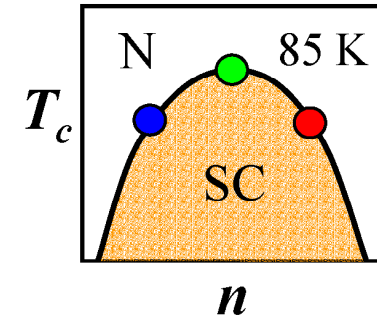
# BCS superconductors: the Ferrel-Glover-Tinkham sum rule



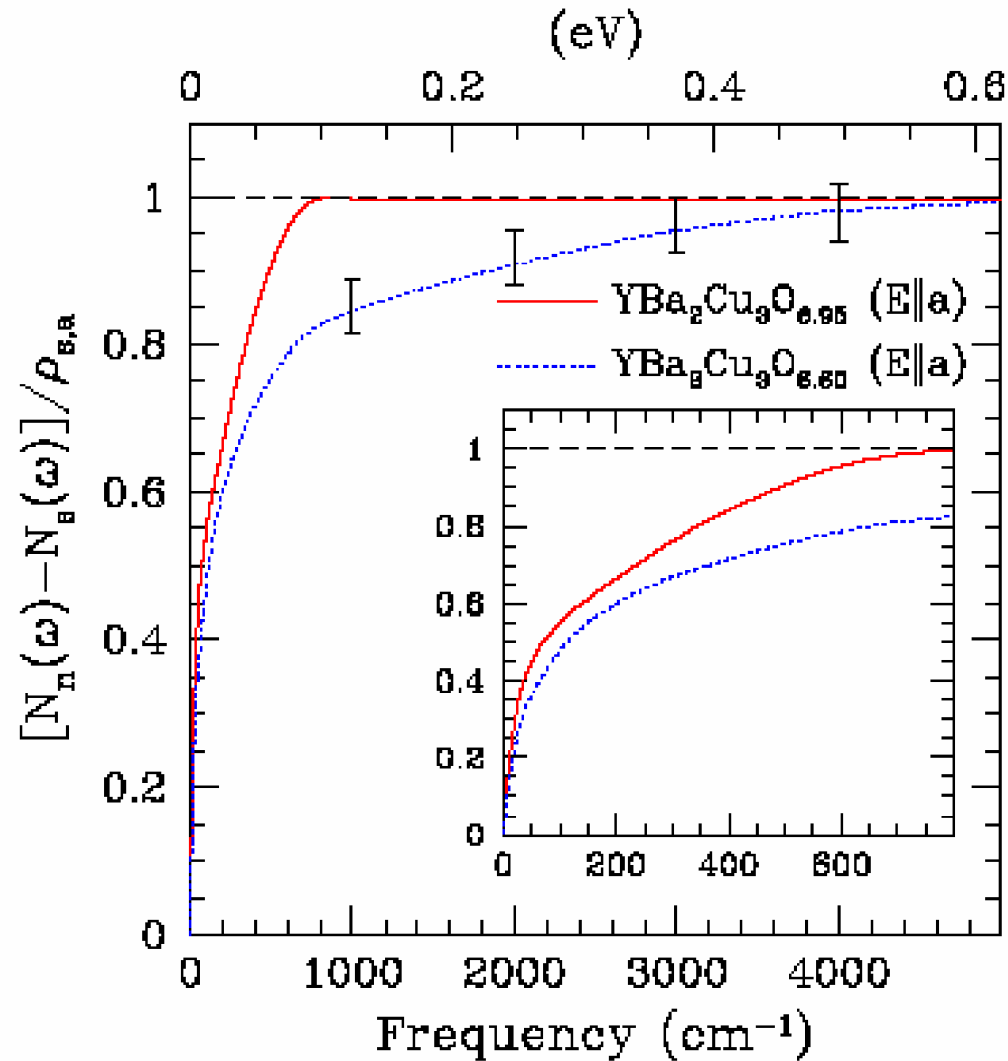
# Previous results on underdoped to optimally-doped Bi-2212...



$$\Delta E_{kin} \approx 1 \text{ meV}$$



# Consistent results in clean-limit underdoped YBCO-6.6

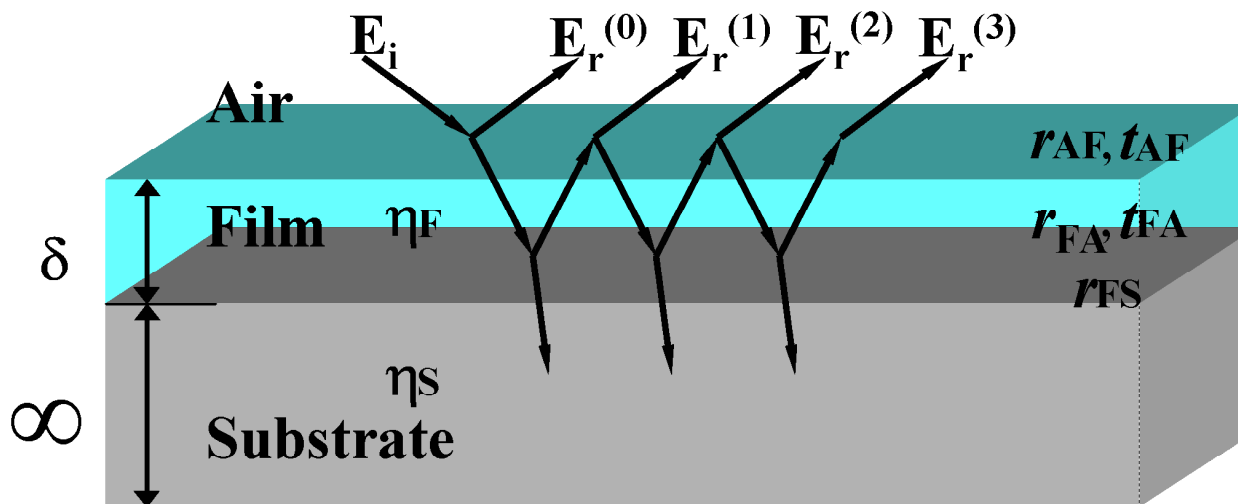
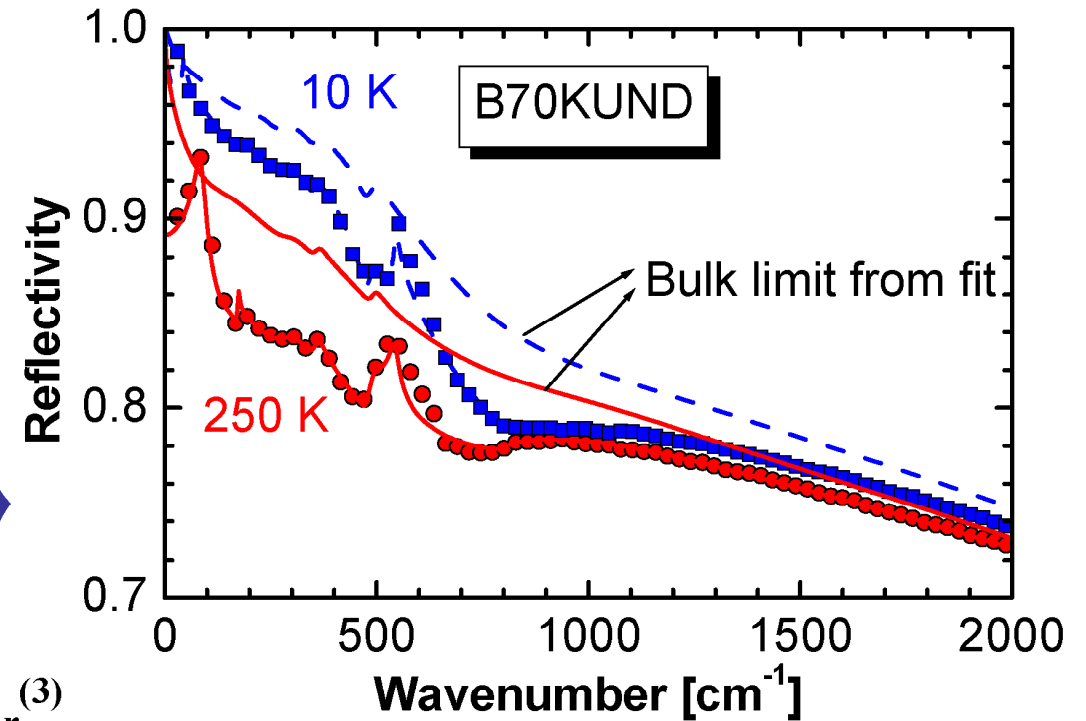


C. Homes *et al.*, PRB **69**, 0024514 (2004).

# Temperature dependencies require unprecedented accuracy

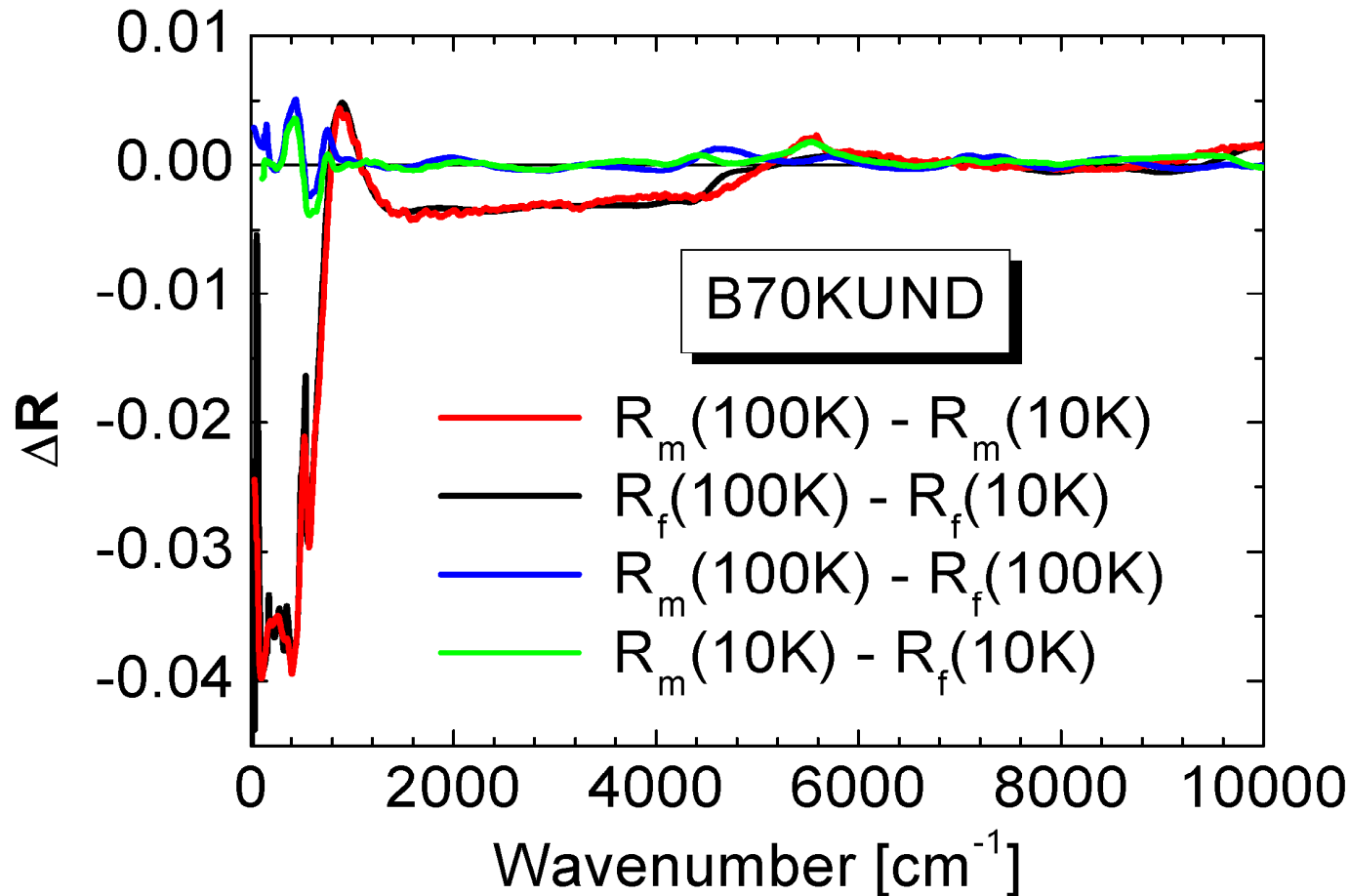
## → State of the art thin-films

Epitaxial  
Large surface (36 mm<sup>2</sup>)  
No intergrowth phases  
Stoichiometry 2212



$$\sigma_{bulk}(\omega)$$

# Resolving 0.1% in reflectivity



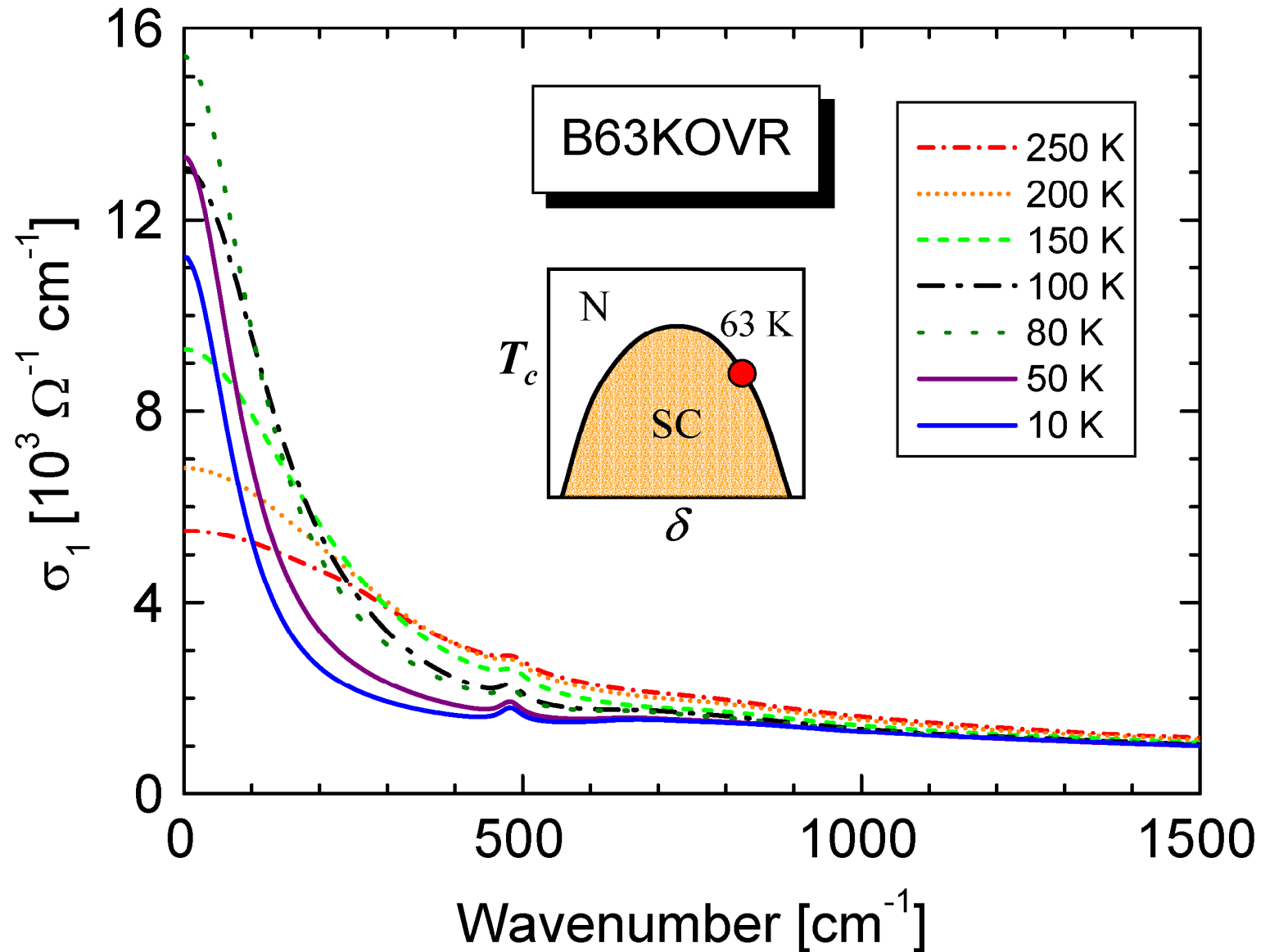
## Underdoped material:

$R_N - R_{SC} \sim 0.4\%$  in the mid-infrared

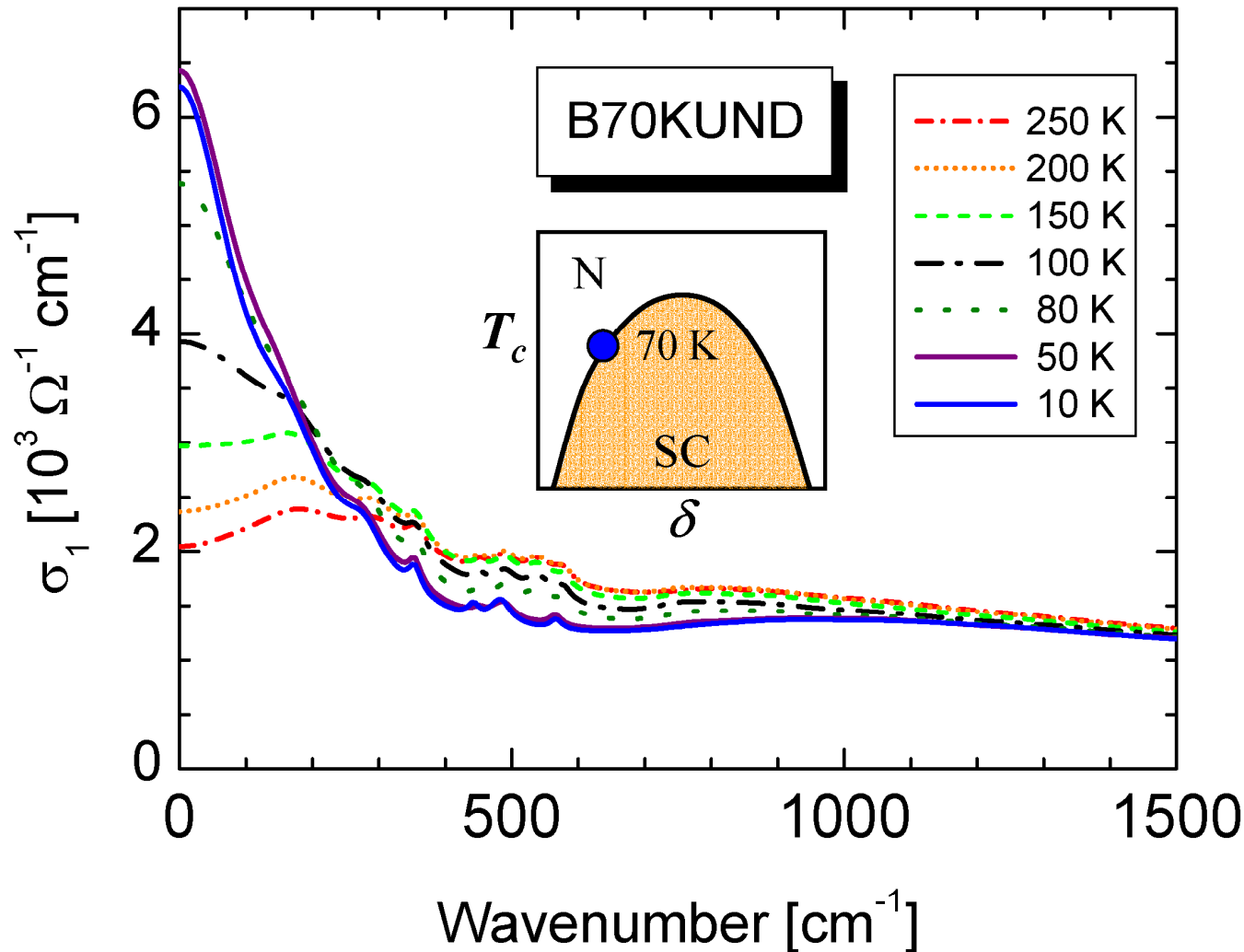
→ Spectral weight redistribution up to  $\sim 1.5$  eV

**Overdoped material:**  $\Delta R < 0.1\%$  (not shown)

# Conductivity of $\text{CuO}_2$ planes in overdoped Bi-2212



# Conductivity of $\text{CuO}_2$ planes in underdoped Bi-2212



Significant residual «free carrier» contribution in the SC state: a rather general characteristic of underdoped samples?

See:

- **Bi-2212:** A. V. Puchkov *et al.*, PRL **77**, 3212 (1996).
- **YBCO 6.6:** C. Homes *et al.*, PRB **69**, 0024514 (2004).
- **YBCO 6.9:** A. V. Boris *et al.*, Science **304**, 708 (2004) (supplementary material)



# Partial spectral weight

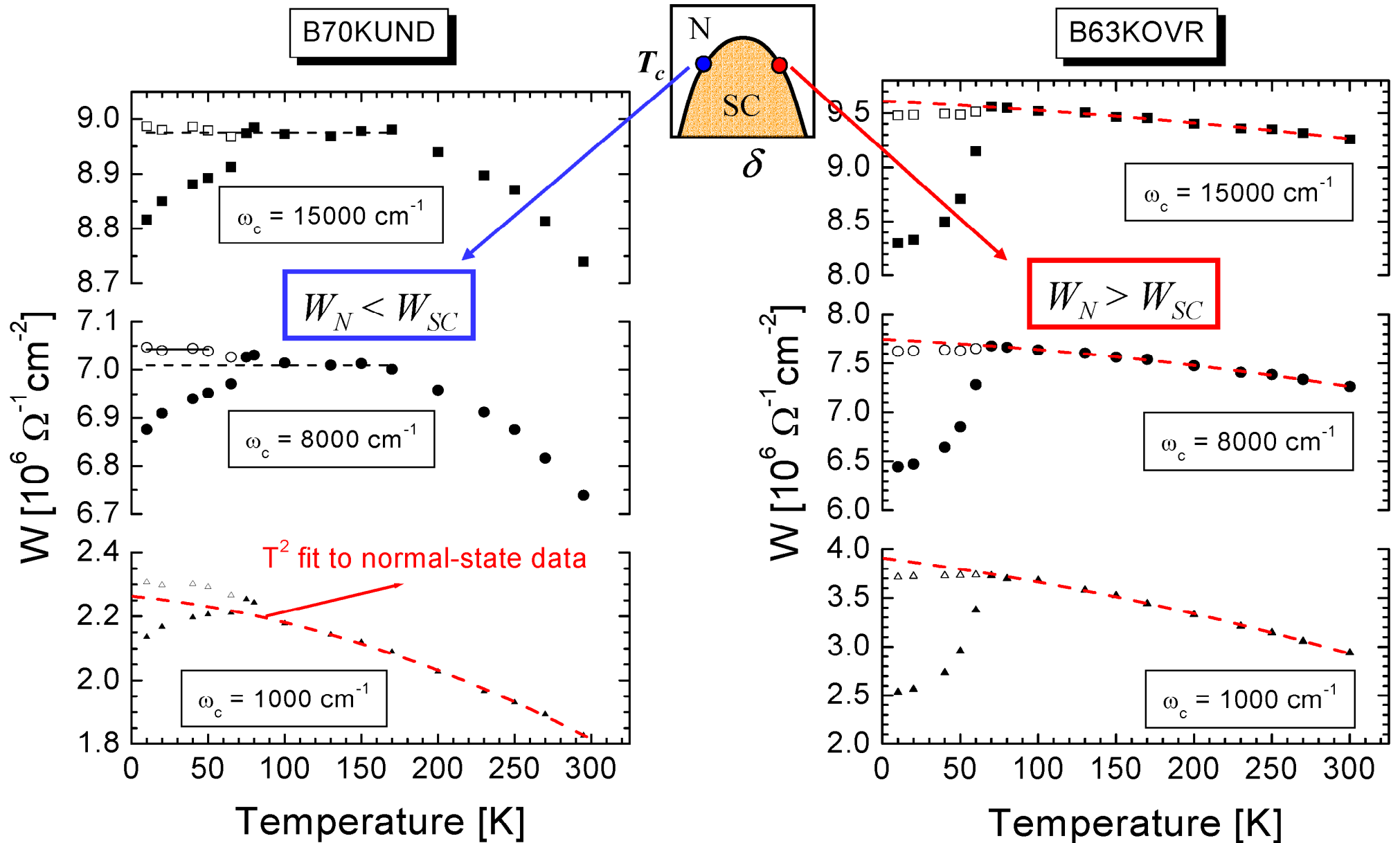
$$W(\omega_c, T) = \int_0^{\omega_c} \sigma_1(\omega, T) d\omega$$

- In the normal state, integration starts at  $0^+$
- In the **SC** state, **W includes the superfluid** at  $\omega = 0$

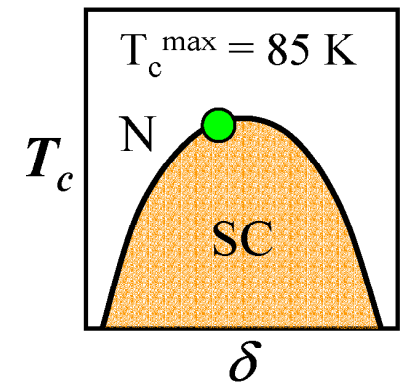
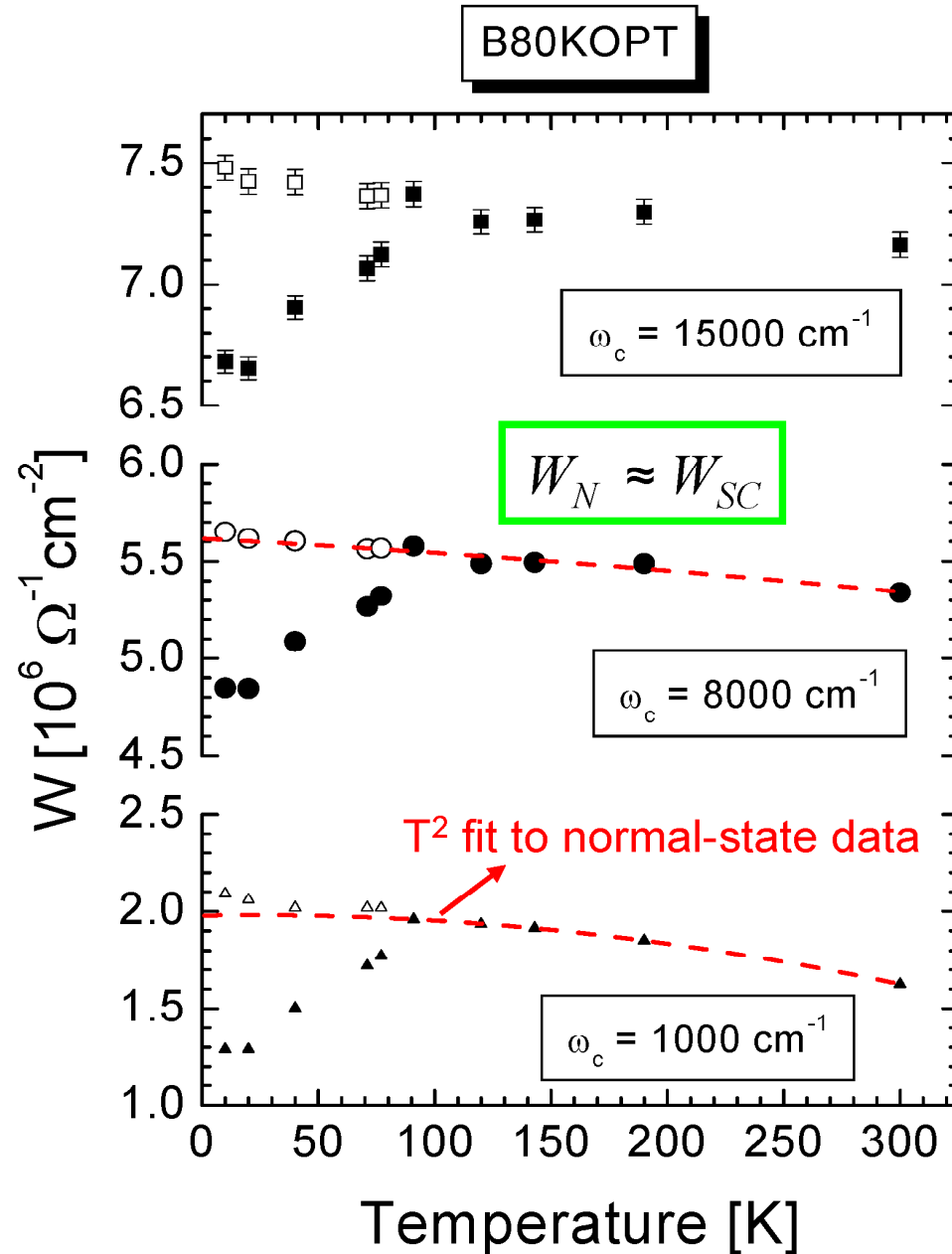
## The evaluation of $W$ requires:

- A good **extrapolation** of  $\sigma_1$  from the first measured frequency to  $\omega = 0^+$  } → Cross-check with DC resistivity
- The knowledge of the **superfluid density**  $\rho_s$  in the SC state } → Directly from  $\sigma_2$  at low frequencies (London model)

# SC-induced changes of intraband spectral weight: BCS-like to unconventional SC crossover



# At the crossover vicinity: spectral weight changes at near-optimal doping



# Single-band Hubbard model and kinetic energy change (in the $\text{CuO}_2$ plane)

$$W_{band} = \int_0^{\Omega_P} \sigma_1(\omega) d\omega = \frac{\pi \epsilon_V}{2} \frac{e^2}{\hbar^2} \frac{a^2}{V} (-E_{kin})$$

$$E_{kin}^N - E_{kin}^{SC} = \frac{2 \hbar^2}{\pi e^2} \frac{V}{a^2} [W_{band}^{SC} - W_{band}^N]$$

- J. Hirsch, Physica C **199**, 305-310 (1992).
- D. van der Marel. Trieste miniworkshop “*Strong correlation in the high- $T_C$  era*”. Trieste, 17-28 July 2000.

# BCS superconductors: kinetic energy change

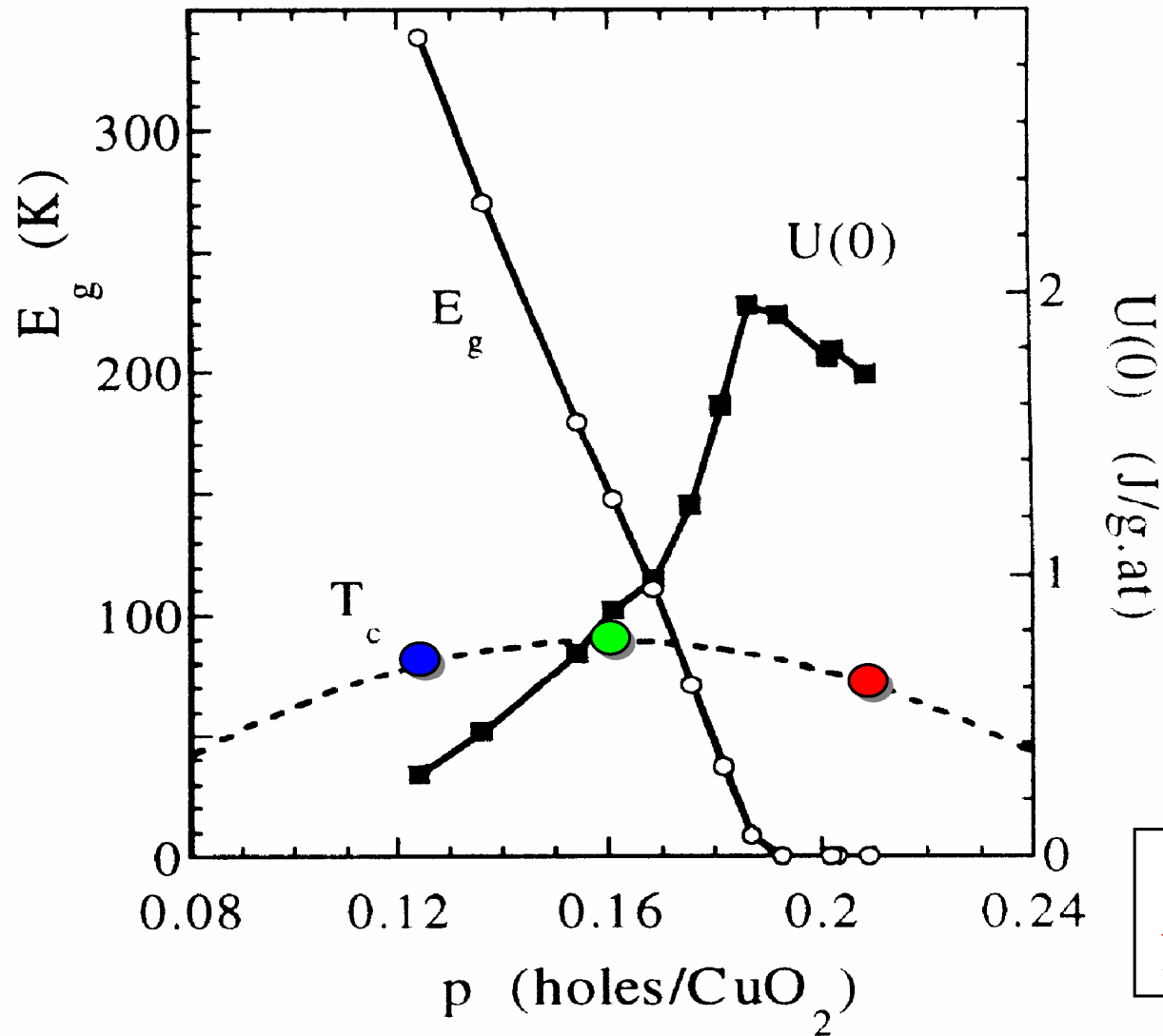
$$E_{total}^N - E_{total}^{SC} = \underbrace{\left[ \frac{1}{2} N(0) \Delta^2 - \frac{\Delta^2}{V_{int}} \right]}_{\Delta E_{kin}} + \underbrace{\frac{\Delta^2}{V_{int}}}_{\Delta E_{pot}}$$

$U_{cond}$

$$N(0)V_{int} < 1 \Rightarrow E_{kin}^N < E_{kin}^{SC} \text{ in BCS}$$

- **P. G. de Gennes**, Superconductivity of Metals and Alloys, Addison-Wesley, 1989

# Bi-2212: Condensation energy



Bi-2212  
1 J/g-at = 0.08 meV per Cu

• J. W. Loram *et al.*, Physica C 341-348, 831-834 (2000).

# Bi-2212: kinetic energy changes

## Underdoped Bi-2212

$$E_{kin}^N - E_{kin}^{SC} \approx 0.8 \pm 0.2 \text{ meV per Cu}$$

Compare to condensation energy:

$$U_0 < 0.08 \text{ meV/Cu}$$

## Overdoped Bi-2212

$$E_{kin}^N - E_{kin}^{SC} \approx -(1.2 \pm 0.3) \text{ meV per Cu}$$

$$\Rightarrow N(0)V_{\text{int}} \approx 0.2$$

# CONCLUSIONS

## UNDERDOPED Bi-2212

- **The formation of the superfluid condensate modifies the electronic excitations up to energies beyond 1 eV.**
- **This phenomenon can be assigned to a *decrease* of the carriers kinetic energy.**
- **The decrease in kinetic energy is large enough to account for the condensation energy.**

## OVERDOPED Bi-2212

**The electronic kinetic energy *increases* at the superconducting transition, displaying a BCS-like behavior.**