

**Workshop on  
NUCLEAR STRUCTURE AND DECAY  
DATA EVALUATION**

**Trieste, April 4 – 15, 2005**

**Trieste, November 17 – 28, 2003**

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# Decay Data

1. Statistical treatment of data
2. Properties of the parent nucleus
3. Gamma rays
4. Decay scheme normalization
5. Beta particles
6. Electron capture
7. Alpha particles
8. Level structure and decay scheme

# 1. Statistical treatment of data

- Weighted and unweighted averages
- Limits
- Discrepant data
- Limitation of relative statistical weight method

## 2. **Properties of the parent nucleus**

- Energy, spin/parity, half-life, Q-value

### 3. Gamma rays

- Energy ( $E_\gamma$ )
- Relative intensity ( $I_\gamma$ )
- Multipolarity and mixing ratio ( $\delta$ )
- Internal conversion coefficient ( $\alpha_i$ )
- Total transition intensity [ $I_\gamma (1 + \alpha)$ ]
- Absolute intensity ( $\%I_\gamma$ )

## 4. Beta particles

- Relative intensity ( $I_{\beta}$ ), absolute intensity ( $\%I_{\beta}$ )
- Average energy ( $I_{\text{avg}}$ )
- Log  $ft$
- Energy ( $E_{\beta}$ )

## 5. Electron capture

- Relative probability ( $I_\varepsilon$ ), absolute probability ( $\%I_\varepsilon$ )
- Relative sub-shell probabilities ( $P_K, P_L, P_M, P_N$ )
- Log  $ft$

## 6. Alpha particles

- Energy ( $E_{\alpha}$ )
- Relative intensity ( $I_{\alpha}$ ), absolute intensity ( $\%I_{\alpha}$ )
- Hindrance factor (HF)



## 7. Level structure and decay scheme

- Level energy ( $E$ )
- Level spin/parity ( $J\pi$ ), particle configuration (CONF)
- Level half-life ( $T_{1/2}$ )
- Decay scheme normalization

# 1. Statistical treatment of data

- Average, Weighted Average (weight =  $1/\sigma_i^2$ )
- Limits (given by authors: <10; changed by evaluator: 5 5)
- Confidence level for limits deduced by evaluators from transition intensity balances (Tom Burrows will talk about this matter.)
- Discrepant data – Limitation of Relative Statistical Weight (LWEIGHT)

# Averages

## Unweighted

$$x(\text{avg}) = 1 / n \sum x_i$$

$$\sigma_{x(\text{avg})} = [ 1 / n (n - 1) \sum (x(\text{avg}) - x_i)^2 ]^{1/2} \text{ Std. dev.}$$

## Weighted

$$x(\text{avg}) = W \sum x_i / \sigma_{x_i}^2 ; \quad W = 1 / \sum \sigma_{x_i}^{-2}$$

$$\chi^2 = \sum (x(\text{avg}) - x_i)^2 / \sigma_{x_i}^2 \text{ Chi sqr.}$$

$$\chi_v^2 = 1 / (n - 1) \sum (x(\text{avg}) - x_i)^2 / \sigma_{x_i}^2 \text{ Red. Chi sqr}$$

$$\sigma_{x(\text{avg})} = \text{larger of } W^{1/2} \text{ and } W^{1/2} \chi_v. \text{ Std. dev.}$$

# Limits

$B_m$  = measured value

$\sigma$  = Standard deviation

$B_0$  = True value

Example:  $-2 \pm 3$

For a Gaussian distribution the formulas to convert measured values to limits are:

$B_0 < B_m + 1.28 \sigma$  (90% confidence limit); Example:  $< 1.84$

$B_0 < B_m + 1.64 \sigma$  (95% confidence limit); Example:  $< 2.92$

$B_0 < B_m + 2.33 \sigma$  (99% confidence limit); Example;  $< 4.99$

# Discrepant Data

**Simple definition:** A set of data for which  $\chi_v^2 > 1$ .

But,  $\chi_v^2$  has a Gaussian distribution, i.e. it varies with the degrees of freedom  $(n - 1)$ .

**Better definition:** A set of data is discrepant if  $\chi_v^2$  is greater than  $\chi_v^2$  (critical). Where  $\chi_v^2$  (critical) is such that there is a 99% probability that the set of data is discrepant.

## Limitation of Relative Statistical Weight Method

For discrepant data ( $\chi^2_{\nu} > \chi^2_{\nu}(\text{critical})$ ) with at least three sets of input values, we apply the *Limitation of Relative Statistical Weight* method. The program identifies any measurement that has a relative weight  $>50\%$  and increases its uncertainty to reduce the weight to  $50\%$ .

Then it recalculates  $\chi^2_{\nu}$  and produces a new average and a best value as follows:

If  $\chi^2_v \leq \chi^2_v(\text{critical})$ , the program chooses the weighted average and its uncertainty (the larger of the internal and external values).

If  $\chi^2_v > \chi^2_v(\text{critical})$ , the program chooses either the weighted or the unweighted average, depending on whether the uncertainties in the average values make them overlap with each other. If that is so, it chooses the weighted average and its (internal or external) uncertainty. Otherwise, the program chooses the unweighted average. In either case, it may expand the uncertainty to cover the most precise input value

## 2. Properties of the parent nucleus

- Level energy (keV): 0.0, 328.0 25, 942 4, 0.0 + X
- Spin/parity:  $1/2^+$ ,  $(3/2^+)$ ,  $5^-$ ,  $6(+)$ ,  $(5/2^-, 7/2^-)$
- Half-life: 3.8 d 2, 432.2 y 7, 2 m, 35 ms 10,  $\sim 3$  s,  $1.2 \times 10^{15}$  y
- Units: (sidereal) y (= 365.25636 d), d, h, m, s, ms,  $\mu$ s, ns, ps, fs, ...
- Q-value (keV): 2003Au03 (G. Audi et al., Nucl. Phys. A729, 337 (2003))
- Theoretical values: 1997Mo25 (P. Moller et al., At. Nucl. Data Tables 66, 131 (1997))



### 3. Gamma rays

#### 1. Energy (keV)

- Weighted average from radioactive decay
- Very precise measurements (e.g. bent crystal)
- Recommended standards for energy calibration:  
Helmer and Van der Leun (Nucl. Instr. and Meth. in Phys. Res. **A450**, 35 (2000))
- Not observed, but expected (From level energy difference)
- Deduced from conversion electron energies (Give atomic electron binding energy)
- Multiplets:
  - Broader peak in spectrum
  - Known levels involved



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2000 He 14

## Recommended standards for $\gamma$ -ray energy calibration (1999)

R.G. Helmer<sup>a,\*</sup>, C. van der Leun<sup>b,\*</sup>

<sup>a</sup>*Idaho Accelerator Center, Idaho State University, Pocatello, Idaho, USA*

<sup>b</sup>*R.J. Van de Graaff Laboratorium, Utrecht University, P.O. Box 80,000, 3508 TA Utrecht, The Netherlands*

Received 3 November 1999; received in revised form 10 January 2000; accepted 10 January 2000

- Uncertainties: Statistical

Give (in comments) estimate of systematic errors.

When uncertainties are known to include systematic errors, no result from weighted average should have an uncertainty smaller than the smallest on the input uncertainty.

No uncertainty should be smaller than the uncertainty in the calibration standard.

Uncertainties larger than 25 should be rounded off.

Author

ENSDF

351.53  $\pm$  0.25

351.53 25

351.53  $\pm$  0.30

351.5 3

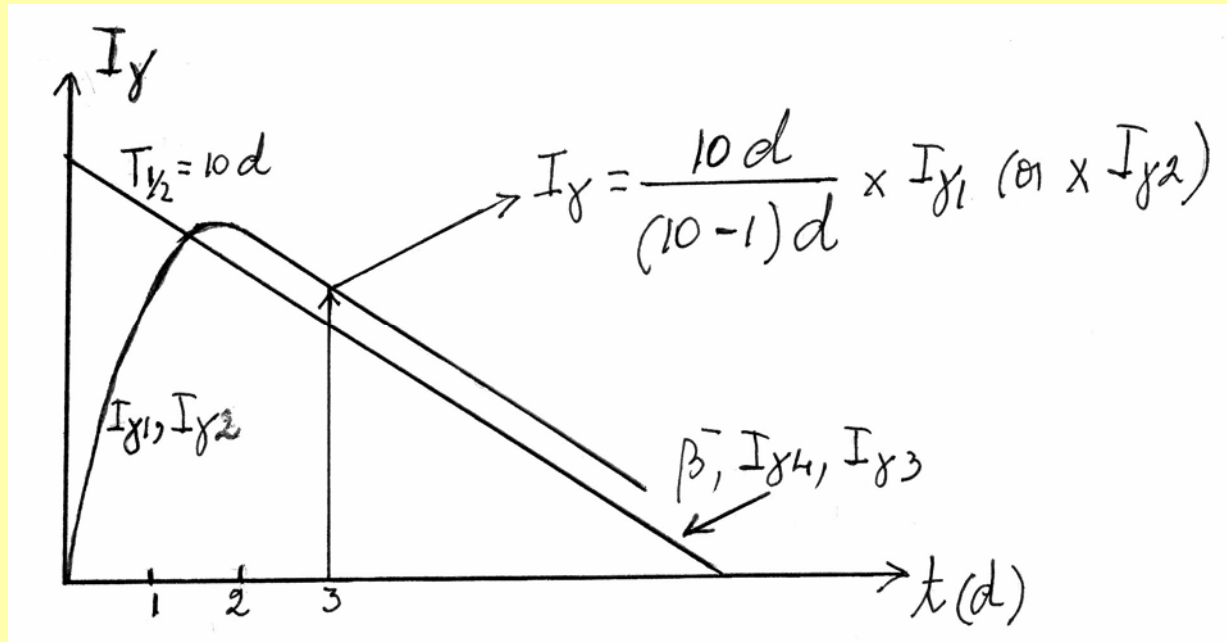
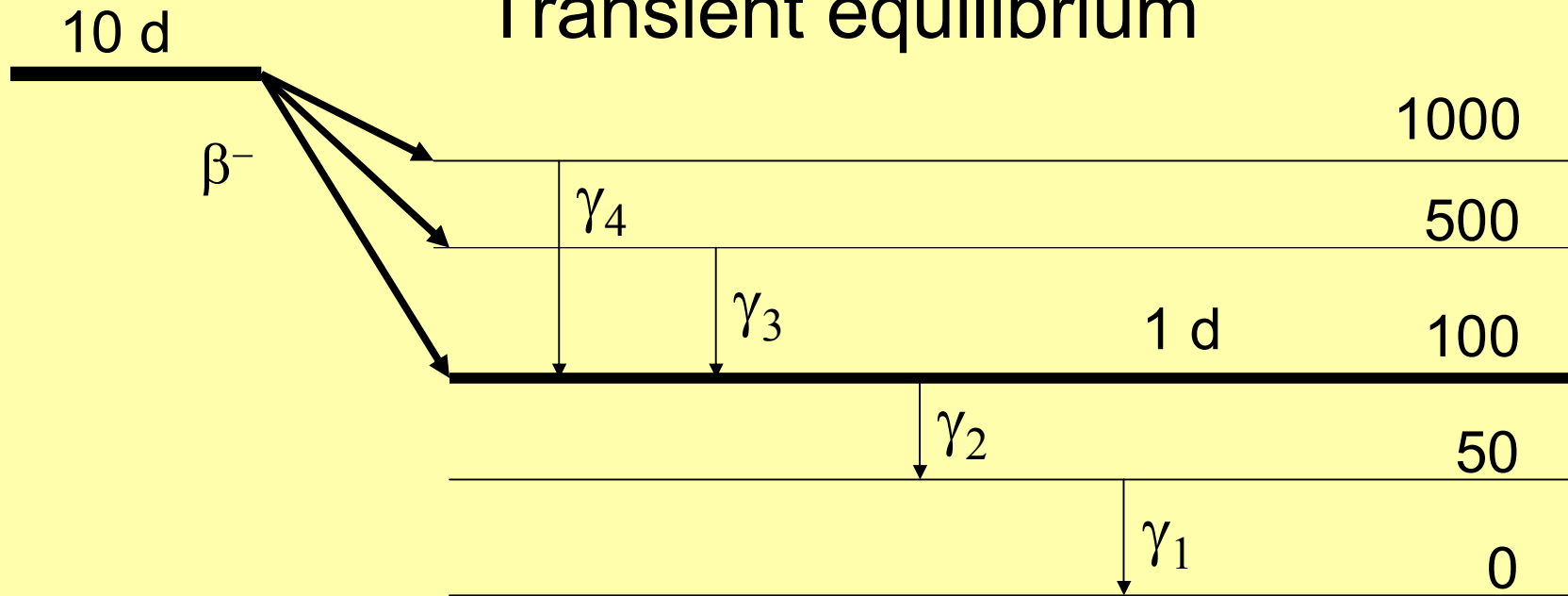
8346  $\pm$  29

83.5E2 3

## 2. Relative intensity

- Weighted average from radioactive decay
- Use 100 for the most intense gamma ray.
- Use a limit for an expected (but unobserved)  $\gamma$  ray.
- Use total transition intensity (TI) if this is the only quantity measured, or deduced from transition intensity balance. If  $\alpha_T$  is known, then deduce and give  $I_\gamma$ .
- Limits are acceptable (e.g.  $I_\gamma < A$ ), but  $I_\gamma = \frac{1}{2} A \pm \frac{1}{2} A$  is preferable (for calculating transition intensity balances).
- Intensity from an isomer in the daughter nucleus should not be given if such intensity is time dependant. Include a comment giving the percent feeding to the isomer, and explain the reason for not giving  $I_\gamma$ .

# Transient equilibrium



### 3. Multipolarity and mixing ratio ( $\delta$ )

- From conversion electron data. If  $I_K$  and  $I_\gamma$  were used to determine  $\alpha_K$ , explain normalization between electron and photon intensity scales. Conversion electron sub-shell ratios.
- From  $\gamma$ -ray angular correlations ( $\gamma(\theta)$ ). Notice that  $\gamma(\theta)$  determines *only* the L component of the  $\gamma$ -ray character, thus mult.= D, D+Q, etc.  $T_{1/2}(\text{exp.})$  may be used to rule out choices. For example, Q=M2 and D+Q=E1+M2.

## Multipolarity and mixing ratio ( $\delta$ ) from conversion electron data

- Using experimental conversion coefficients

$$\delta^2 = \text{E2 } \gamma\text{-ray intensity} / \text{M1 } \gamma\text{-ray intensity} = I_\gamma(\text{E2})/I_\gamma(\text{M1}) \dots (1)$$

$$I_\gamma(\text{M1}) + I_\gamma(\text{E2}) = I_\gamma \dots (2)$$

From equations (1) and (2) we obtain:

$$I_\gamma(\text{M1}) = I_\gamma / 1 + \delta^2, \text{ and } I_\gamma(\text{E2}) = I_\gamma \delta^2 / 1 + \delta^2$$

Conversion electron intensity:  $I_e = I_e(\text{M1}) + I_e(\text{E2})$

Experimental conversion coefficient

$$\alpha(\text{exp}) = I_e / I_\gamma = 1 / I_\gamma [I_\gamma(\text{M1}) \times \alpha(\text{M1})^{\text{th}} + I_\gamma(\text{E2}) \times \alpha(\text{E2})^{\text{th}}]$$

$$\text{or, } \alpha(\text{exp}) = 1 / I_\gamma [I_\gamma / 1 + \delta^2 \times \alpha(\text{M1})^{\text{th}} + I_\gamma \delta^2 / 1 + \delta^2 \times \alpha(\text{E2})^{\text{th}}]$$

$$\delta^2 = (\alpha(\text{M1})^{\text{th}} - \alpha(\text{exp})) / (\alpha(\text{exp}) - \alpha(\text{E2})^{\text{th}})$$

$$\% \text{M1} = 100 / 1 + \delta^2, \quad \% \text{E2} = 100 \delta^2 / 1 + \delta^2$$

- Using experimental electron sub-shell ratios

$$R(\text{exp}) = I_e(\text{L1}) / I_e(\text{L3})$$

Then

$$\delta^2 / 1 + \delta^2 = A / [\alpha(\text{E2,L1})^{\text{th}} - \alpha(\text{M1,L1})^{\text{th}} + R(\text{exp}) (\alpha(\text{M1,L3})^{\text{th}} - \alpha(\text{E2,L3})^{\text{th}})]$$

where

$$A = R(\text{exp}) \alpha(\text{M1,L3})^{\text{th}} - \alpha(\text{M1,L1})^{\text{th}}$$



- Consistency of entries for  $\alpha$  and  $\delta$ :

For a single multipolarity the  $\delta$  field should be blank.

For  $\delta < V$ :

Give *only* dominant multipolarity and corresponding  $\alpha$ .

Give  $\delta < V$  in a comment, or

give both multipolarities and  $\delta < V$  in the  $\delta$  field.

Calculate  $\alpha$  from  $\delta = \frac{1}{2} V \pm \frac{1}{2} V$ .

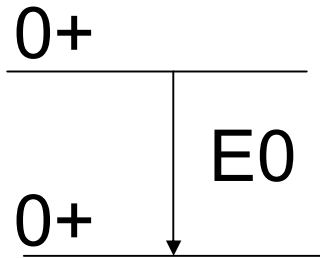
Examples: E2+M3 with  $\delta < 0.5$  should preferably be entered as E2, whereas M1+E2 with  $\delta < 0.5$ , as M1+E2 ( $\delta = 0.25 \pm 0.25$ ).

M1, E2 is not the same as M1+E2.

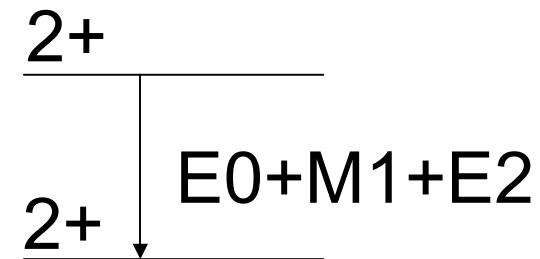
- Assumed multipolarity

[M1], [E2], [M1+E2], [M4], etc.

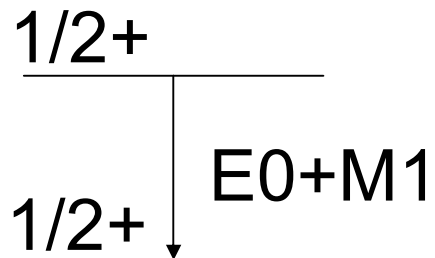
# More about multipolarities



$$0 \leq l \leq 0 ; l = 0$$

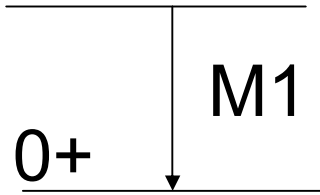


$$0 \leq l \leq 2 ; l = 0, 1, 2$$



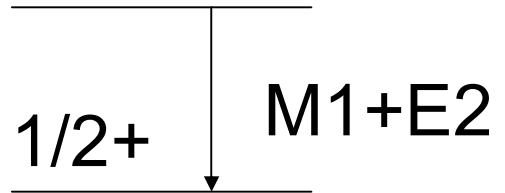
$$0 \leq l \leq 1 ; l = 0, 1$$

1+



$$1 \leq \ell \leq 1 ; \ell = 1$$

3/2+



$$1 \leq \ell \leq 2 ; \ell = 1, 2$$

#### 4. Internal conversion coefficients

- Theoretical values:

From Hager and Seltzer (1968Ha53) for K, L<sub>i</sub>, M<sub>i</sub> shells, and  $Z \geq 30$

From Dragoun et al. (1971Dr11) for N, O, ... shells.

From Dragoun et al. (1971Dr09) for N<sub>i</sub> shells.

From Band et al. (1976Ba63) for  $E_\gamma \leq 6000$  keV,  $Z=3, 6, 10$ , and  $14 \leq Z \leq 30$ .

From Trusov (1972Tr09) for  $E_\gamma > 2600$  keV.

From Hager and Seltzer (1969Ha61), K/L<sub>1</sub>, L<sub>1</sub>/L<sub>2</sub>, for E0 transitions.

New Calculation of Conversion Coefficients

Dirac-Fock Internal Conversion Coefficients

*I.M. Band, M.B. Trzhaskovskaya, C.W. Nestor, Jr.,  
P.O. Tikkanen, and S. Raman*

Atomic Data and Nuclear Data Tables **81**, 1 (2002)

(To be discussed by Tom Burrows)

- Experimental values:

**For very precise values ( $\leq 3\%$  uncertainty).**

$$E_{\gamma} = 661 \text{ keV} ; {}^{137}\text{Cs} (\alpha_{\text{K}}=0.0902 \pm 0.0008, \text{M4})$$

## **Nuclear penetration effects.**

${}^{233}\text{Pa}$   $\beta^{-}$  decay to  ${}^{233}\text{U}$ .

$E_{\gamma} = 312 \text{ keV}$  almost pure M1 from electron sub-shell ratios.

However  $\alpha_{\text{K}}(\text{exp}) = 0.64 \pm 0.02$ .

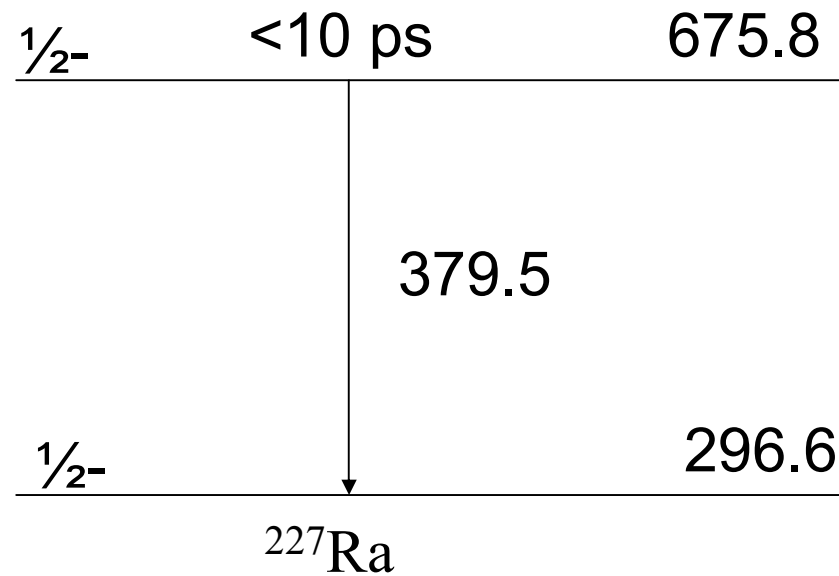
$(\alpha_{\text{K}}^{\text{th}}(\text{M1})=0.78, \alpha_{\text{K}}^{\text{th}}(\text{E2})=0.07)$

**For mixed E0 transitions (e.g., M1+E0).**

$^{227}\text{Fr} \beta^- ^{227}\text{Ra}$

$E_\gamma = 379.1 \text{ keV (M1+E0); } \alpha(\text{exp}) = 2.4 \pm 0.8$

$\alpha^{\text{th}}(\text{M1}) = 0.40; \alpha^{\text{th}}(\text{E2}) = 0.08$



- Total transition intensity

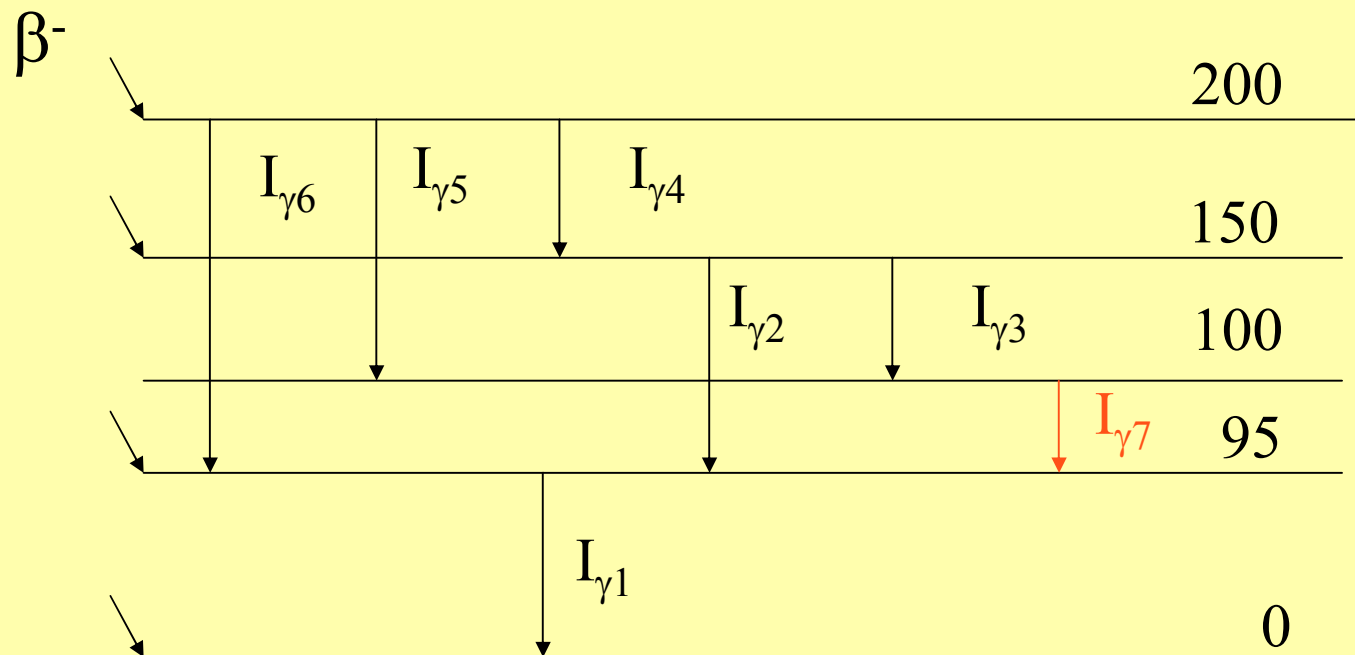
The TI field should be used *only* if TI (rather than  $I_\gamma$ ) is the measured or deduced quantity. Usual cases are:

TI deduced from transition intensity balance.

TI =  $\sum I_i(\text{ce})$ , if  $I_\gamma$  is known to be negligible. If not, but conversion coefficient is known, then deduced and give  $I_\gamma$ .



## Total intensity from transition-intensity balance



$$TI(\gamma_7) = TI(\gamma_5) + TI(\gamma_3)$$

If  $\alpha(\gamma_7)$  is known, then

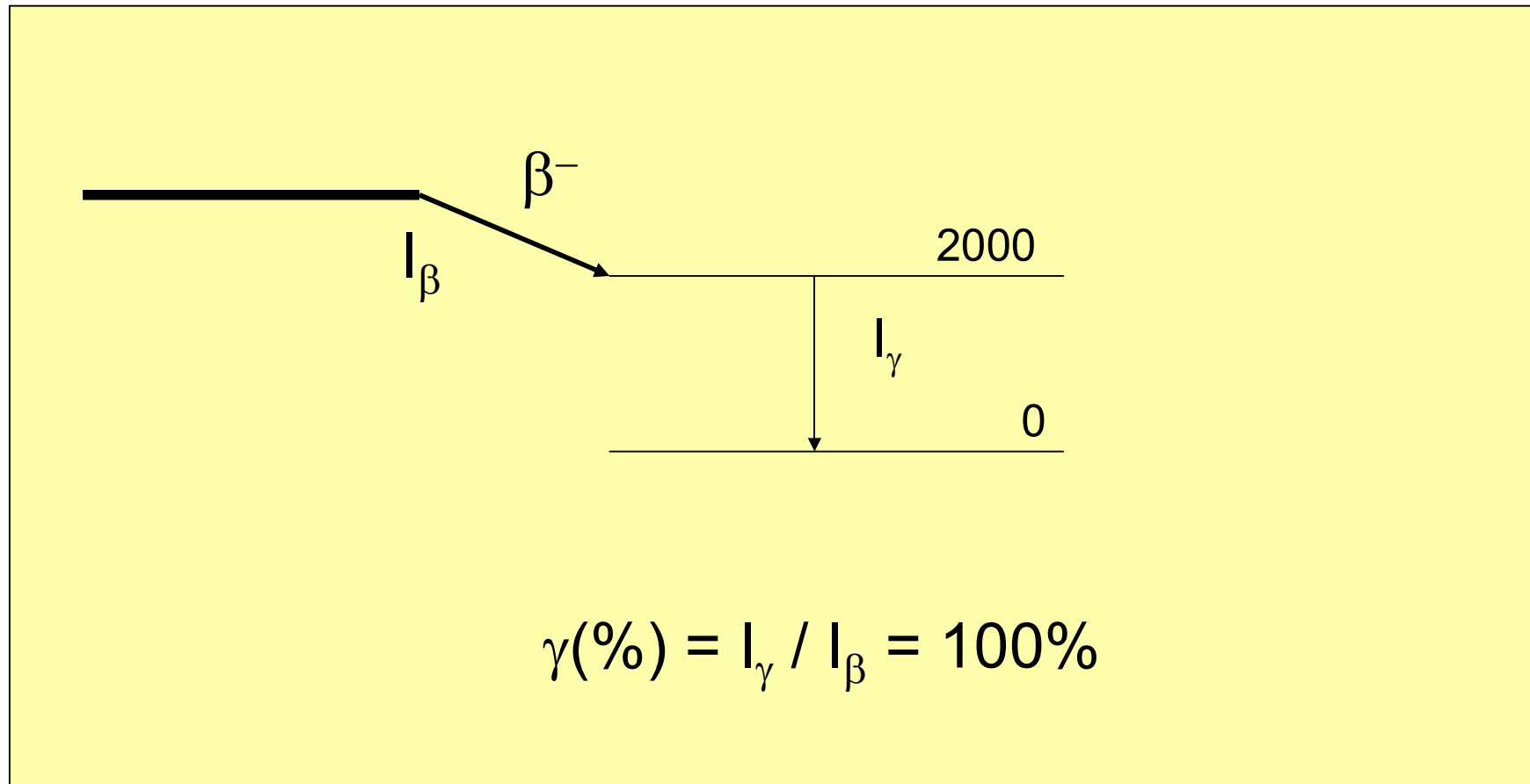
$$I_{\gamma_7} = TI(\gamma_7) / [1 + \alpha(\gamma_7)]$$

## 5. Absolute intensities

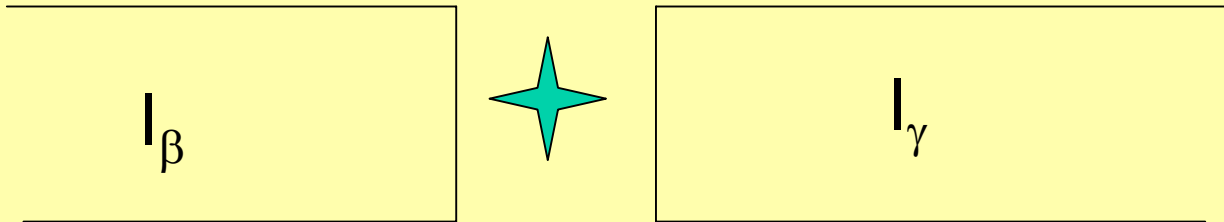
“Intensities per 100 disintegrations of the parent nucleus”

- Measured (Photons from  $\beta^-$ ,  $\epsilon+\beta^+$ , and  $\alpha$  decay)  
Simultaneous singles measurements  
Coincidence measurements

## Absolute $\gamma$ -ray intensity



## Simultaneous singles measurement



$I_{\beta}$ :  $\beta^{-}$  intensity corrected for detector efficiency

$I_{\gamma}$ :  $\gamma$ -ray intensity corrected for detector efficiency

$$I_{\gamma} / I_{\beta} = \text{absolute } \gamma\text{-ray intensity}$$

Units: photons per  $\beta^{-}$  (or per 100  $\beta^{-}$ ) disintegrations

## 4. Decay scheme normalization

Rel. int.	Norm. factor	Abs. Int.
$I_{\gamma}$	$NR \times BR$	$\%I_{\gamma}$
$I_T$	$NT \times BR$	$\%I_T$
$I_{\beta}$	$NB \times BR$	$\%I_{\beta}$
$I_{\varepsilon}$	$NB \times BR$	$\%I_{\varepsilon}$
$I_{\alpha}$	$NB \times BR$	$\%I_{\alpha}$

BR: Factor for converting intensity per 100 *decays through this decay branch*, to intensity per 100 *decays of the parent nucleus*

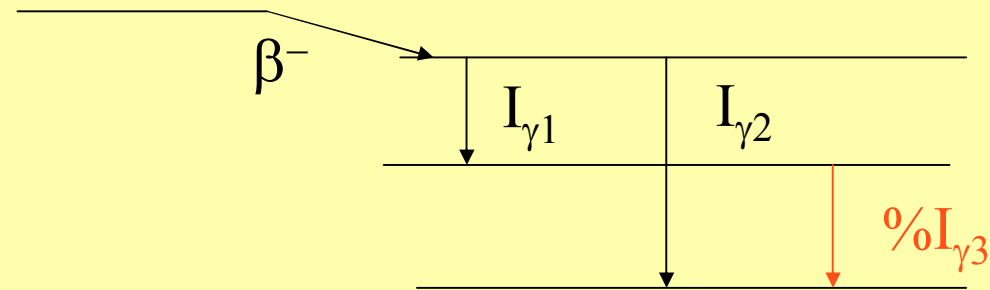
NR: Factor for converting relative  $I_{\gamma}$  to  $I_{\gamma}$  per 100 decays through this decay branch.

NT: Factor for converting relative TI to TI per 100 decays through this decay branch.

NB: Factor for converting relative  $\beta^{-}$  and  $\varepsilon$  intensities to intensities per 100 *decays of this decay branch*.

# Normalization Procedures

1. Absolute intensity of one gamma ray is known ( ${}^{\circ}\text{I}_{\gamma}$ )



Relative intensity  $I_{\gamma} \pm \Delta I_{\gamma}$

Absolute intensity  ${}^{\circ}\text{I}_{\gamma} \pm \Delta {}^{\circ}\text{I}_{\gamma}$

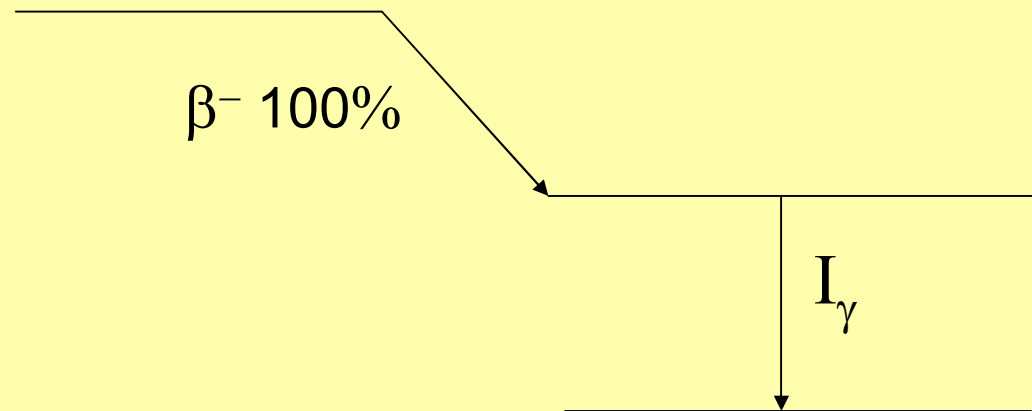
Normalization factor  $N = {}^{\circ}\text{I}_{\gamma} / I_{\gamma}$

Uncertainty  $\Delta N = [ (\Delta {}^{\circ}\text{I}_{\gamma} / {}^{\circ}\text{I}_{\gamma})^2 + (\Delta I_{\gamma} / I_{\gamma})^2 ]^{1/2} \times N$

Then  ${}^{\circ}\text{I}_{\gamma 1} = N \times I_{\gamma 1}$

$\Delta {}^{\circ}\text{I}_{\gamma 1} = [ (\Delta N / N)^2 + (\Delta I_{\gamma} / I_{\gamma})^2 ]^{1/2} \times I_{\gamma 1}$

## 2. From Decay Scheme



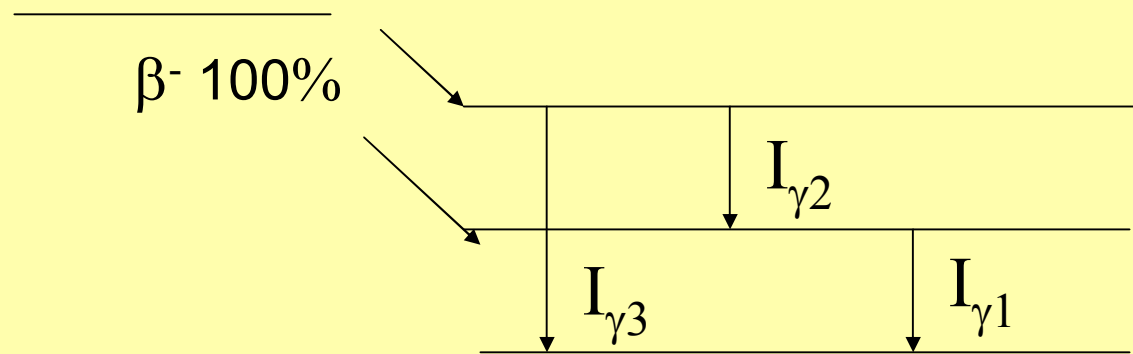
$I_\gamma$ : Relative  $\gamma$ -ray intensity;  $\alpha$ : total conversion coefficient

$$N \times I_\gamma \times (1 + \alpha) = 100\%$$

Normalization factor  $N = 100 / I_\gamma \times (1 + \alpha)$

Absolute  $\gamma$ -ray intensity  $\% I_\gamma = N \times I_\gamma = 100 / (1 + \alpha)$

Uncertainty  $\Delta\% I_\gamma = 100 \times \Delta\alpha / (1 + \alpha)^2$



Normalization factor  $N = 100 / I_{\gamma1}(1 + \alpha_1) + I_{\gamma3}(1 + \alpha_3)$

$$\% I_{\gamma1} = N \times I_{\gamma1} = 100 \times I_{\gamma1} / I_{\gamma1}(1 + \alpha_1) + I_{\gamma3}(1 + \alpha_3)$$

$$\% I_{\gamma3} = N \times I_{\gamma3} = 100 \times I_{\gamma3} / I_{\gamma1}(1 + \alpha_1) + I_{\gamma3}(1 + \alpha_3)$$

$$\% I_{\gamma2} = N \times I_{\gamma2} = 100 \times I_{\gamma2} / I_{\gamma1}(1 + \alpha_1) + I_{\gamma3}(1 + \alpha_3)$$

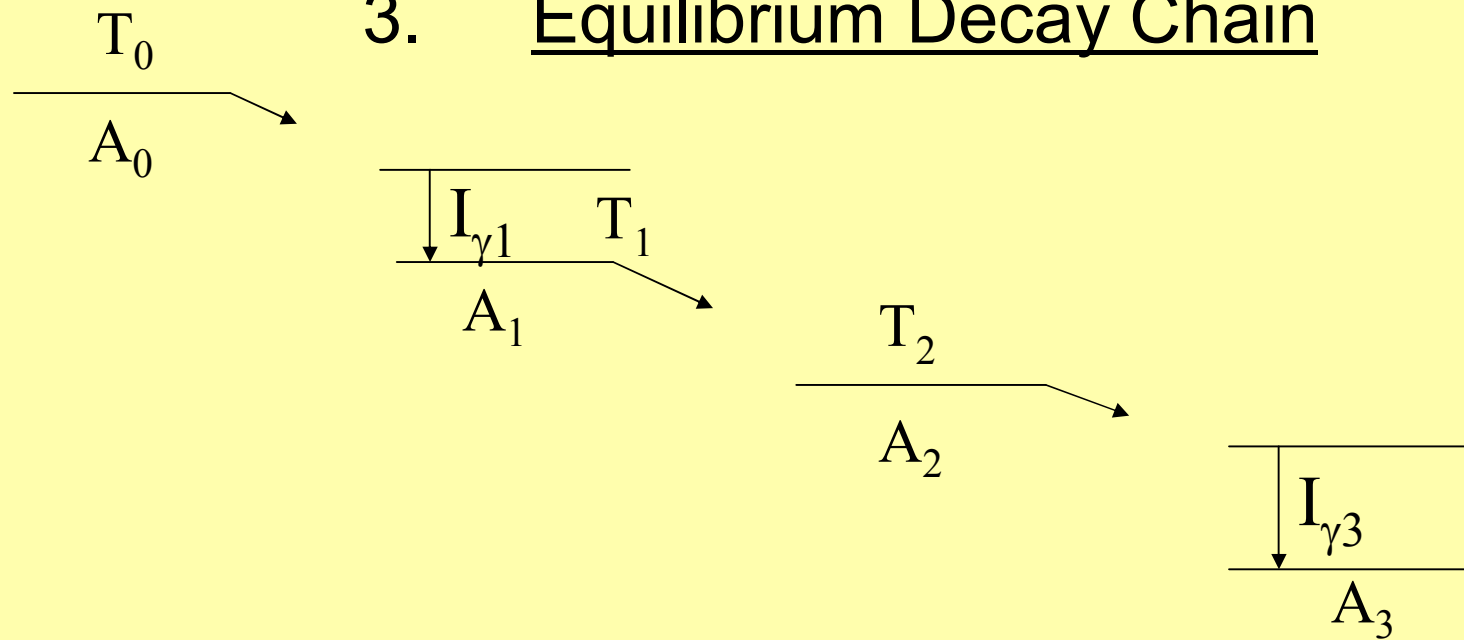
Calculate uncertainties in  $I_{\gamma1}$ ,  $I_{\gamma2}$ , and  $I_{\gamma3}$ . Use 3% fractional uncertainty in  $\alpha_1$  and  $\alpha_3$ .

See Nucl. Instr. and Meth. **A249**, 461 (1986).

To save time use computer program GABS



### 3. Equilibrium Decay Chain



$T_0 > T_1, T_2$  are the radionuclide half-lives,

For  $t = 0$  only radionuclide  $A_0$  exists,

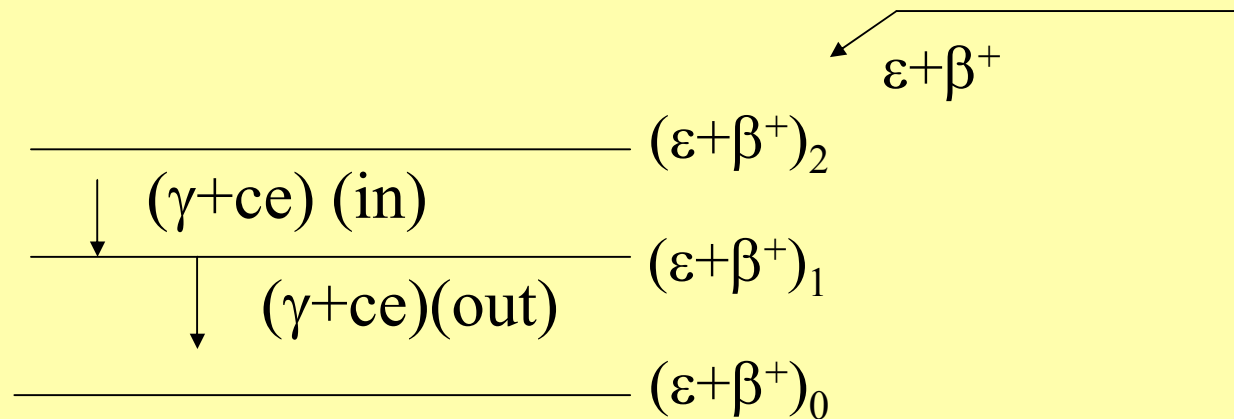
$\% I_{\gamma 3}, I_{\gamma 3}$ , and  $I_{\gamma 1}$  are known.

Then, at equilibrium

$$\% I_{\gamma 1} = (\% I_{\gamma 3} / I_{\gamma 3}) \times I_{\gamma 1} \times (T_0 / (T_0 - T_1)) \times (T_0 / (T_0 - T_2))$$

Normalization factor  $N = \% I_{\gamma 1} / I_{\gamma 1}$

4. Annihilation radiation intensity is known



$I(\gamma_{\pm})$  = Relative annihilation radiation intensity

$X_i$  = Intensity imbalance at the  $i$ th level =  $(\gamma + ce)$  (out) –  $(\gamma + ce)$  (in)

$r_i = \varepsilon_i / \beta_i^+$  theoretical ratio to  $i$ th level

$X_i = \varepsilon_i + \beta_i^+ = \beta_i^+ (1 + r_i)$ , therefore  $\beta_i^+ = X_i / (1 + r_i)$

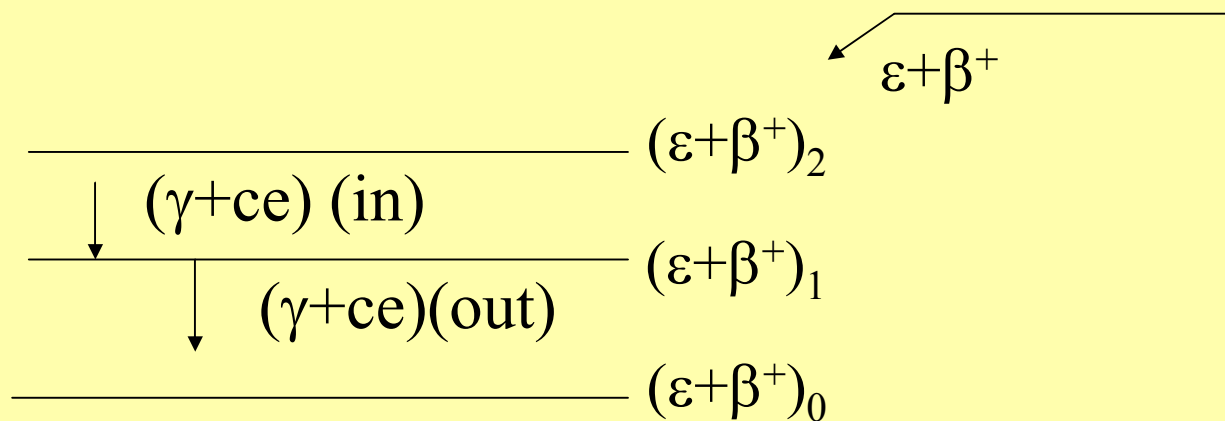
$$2 [X_0 / (1 + r_0) + \sum X_i / (1 + r_i)] = I(\gamma_{\pm}) \dots \dots \dots (1)$$

$$[X_0 + \sum I_{\gamma_i} (\gamma + ce) \text{ to gs } ] N = 100 \dots \dots \dots (2)$$

Solve equation (1) for  $X_0$  (rel. gs feeding).

Solve equation (2) for  $N$  (normalization factor).

## 5. X-ray intensity is known



$I_K$  = Relative Kx-ray intensity

$X_i$  = Intensity imbalance at the  $i$ th level =  $(\gamma + ce) \text{ (out)} - (\gamma + ce) \text{ (in)}$

$r_i = \epsilon_i / \beta_i^+$  theoretical ratio to  $i$ th level

$X_i = \epsilon_i + \beta_i^+$ , so  $\epsilon_i = X_i r_i / 1 + r_i$  (atomic vacancies);  $\omega_K$  = K-fluorosc.yield

$P_{Ki}$  = Fraction of the electron-capture decay from the K shell

$$I_K = \omega_K [\epsilon_0 \times P_{K0} + \sum \epsilon_i \times P_{Ki}]$$

$$I_K = \omega_K [P_{K0} \times X_0 r_0 / (1 + r_0) + \sum P_{Ki} \times X_i r_i / 1 + r_i] \dots (1)$$

$$[X_0 + \sum I_i (\gamma + ce) \text{ to gs}] N = 100 \dots (2)$$

Solve equation (1) for  $X_0$ , equation (2) for  $N$ .

## 5. Beta particles

1. Energy (keV)
  - Give  $E_{\beta}(\text{max})$  *only* if experimental value is so accurate that it could be used as input to mass adjustment.
  - Do not give  $E_{\beta}(\text{avg.})$ , program LOGFT calculates its value.
2. Absolute intensity ( $\%I_{\beta}$ , per 100 decays of the parent nucleus)
  - Give experimental value, if used for normalizing the decay scheme.
  - Give absolute value deduced from  $\gamma$ -ray transition intensity balance (Program GTOL).
3. Logft

Usually authors assign spins and parities. Nevertheless, verify that the relevant logft values are consistent with their assignments.

## 6. Electron capture

- Give  $(I_{\varepsilon} + I_{\beta^+})$  feedings deduced from  $\gamma$ -ray transition intensity balance. Program LOGFT calculates (from theory)  $\varepsilon$  and  $\beta^+$  probabilities.
- Program LOGFT calculates (from theory) sub-shell ( $P_K$ ,  $P_L$ ,  $P_M$ , ...) probabilities.
- Give (in comments) x-ray intensities. These are useful for normalizing or testing the decay scheme.

## 7. Alpha particles

- Energy (keV)

Most measurements are relative to a line from a standard radionuclide. Include this information in a comment.

Use Ritz's (At. Data and Nucl. Data Tables **47**, 205 (1991)) evaluated  $E_\alpha$  and  $I_\alpha$  when no new values are available.

- Intensity

Give intensities preferably "per 100  $\alpha$  decays" (NB=1), and a branching factor BR to convert them to "per 100 decays of the parent nucleus.

- Hindrance factor

HF= experimental  $T_{1/2}(\alpha)$ /theoretical  $T_{1/2}(\alpha)$ . The theoretical value is from 1947Pr17 (M.A. Preston). The assumption is that  $0^+$  to  $0^+$   $\alpha$  transitions from even-even nuclei are the fastest (HF=1). These transitions are used to determine the radius parameter  $r_0$  (See 1998Ak04, Y.A. Akovali). Use program ALPHAD.

# Favored alpha-particle transition

- $HF < 4$
- Takes place between levels with the same spin and parity

## The radius parameter $r_0$ (Y. Akovali, Oak Ridge)

- Odd-N nucleus (Z, A)

$$r_0(Z, N) = [r_0(Z, N-1) + r_0(Z, N+1)]/2$$

- Odd-Z nucleus (Z, A)

$$r_0(Z, N) = [r_0(Z-1, N) + r_0(Z+1, N)]/2$$

- Odd-Odd nucleus (Z, A)

$$r_0(Z, N) = [r_0(Z, N-1) + r_0(Z, N+1)]/2 = \\ [r_0(Z-1, N+1) + r_0(Z-1, N-1) + r_0(Z+1, N+1) + r_0(Z+1, N-1)]/4$$



## Example

$^{219}\text{Rn} \Rightarrow ^{215}\text{Po}$  (Odd-N)

$$r_0 (Z=84, N=131) = [r_0(84, 130) + r_0(84, 132)] / 2$$

From 1998Ak04:

$$r_0(84,214) = 1.5598$$

$$r_0(84,216) = 1.55552, \text{ therefore}$$

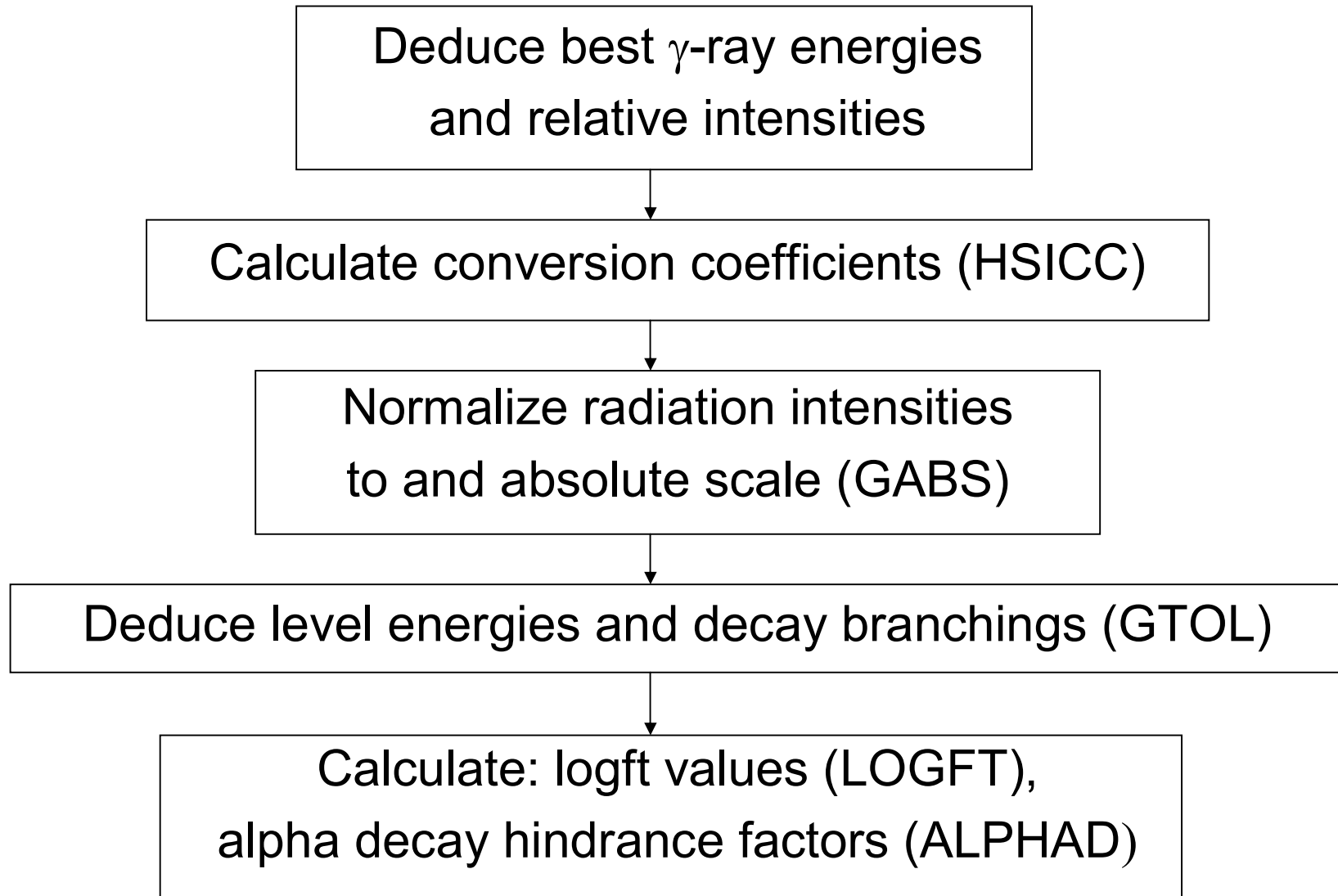
$r_0 (Z=84, N=131) = 1.557$
-----------------------------

Use Table 1 – “Calculated  $r_0$  for even-even nuclei” (1998Ak04). Insert R0= ... in *comment* record:

CA HF R0=...

Run program ALPHAD to calculate hindrance factors.

## 8. Level structure and decay scheme



**Workshop on  
NUCLEAR STRUCTURE AND DECAY  
DATA EVALUATION**

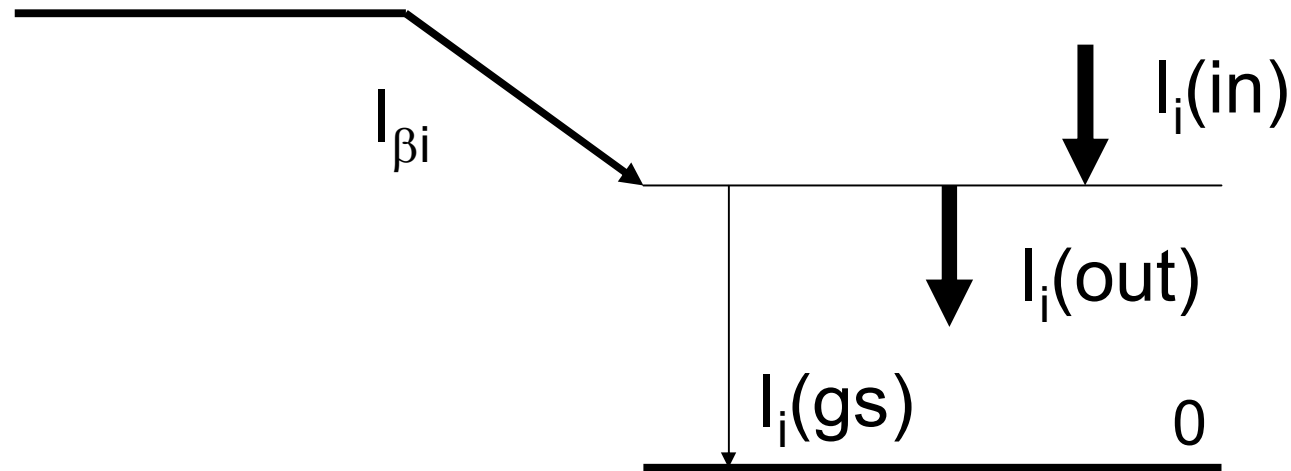
**Model exercise**

**Trieste, April 4 – 15, 2005**

**Trieste, November 17 – 28, 2003**

**Edgardo Browne**

## $\gamma$ -ray transition intensity balance



The corresponding normalization factor is

$$\begin{aligned} N &= 100 / \Sigma [ I_i(\text{out}) + I_i(\text{gs}) - I_i(\text{in}) ] = \\ &= 100 / \Sigma [ I_i(\text{out}) - I_i(\text{in}) ] + \Sigma I_i(\text{gs}), \text{ but} \\ &\Sigma [ I_i(\text{out}) - I_i(\text{in}) ] = 0, \text{ therefore} \\ N &= 100 / \Sigma I_i(\text{gs}) \end{aligned}$$

# $^{233}\text{Pa}$ $\beta^-$ decay

$I_\gamma(312) = 38.6 (5) \%$  (experimental value, Gehrke et al.)

$\Sigma I(\gamma+ce) (gs) = 102 (2) \%$

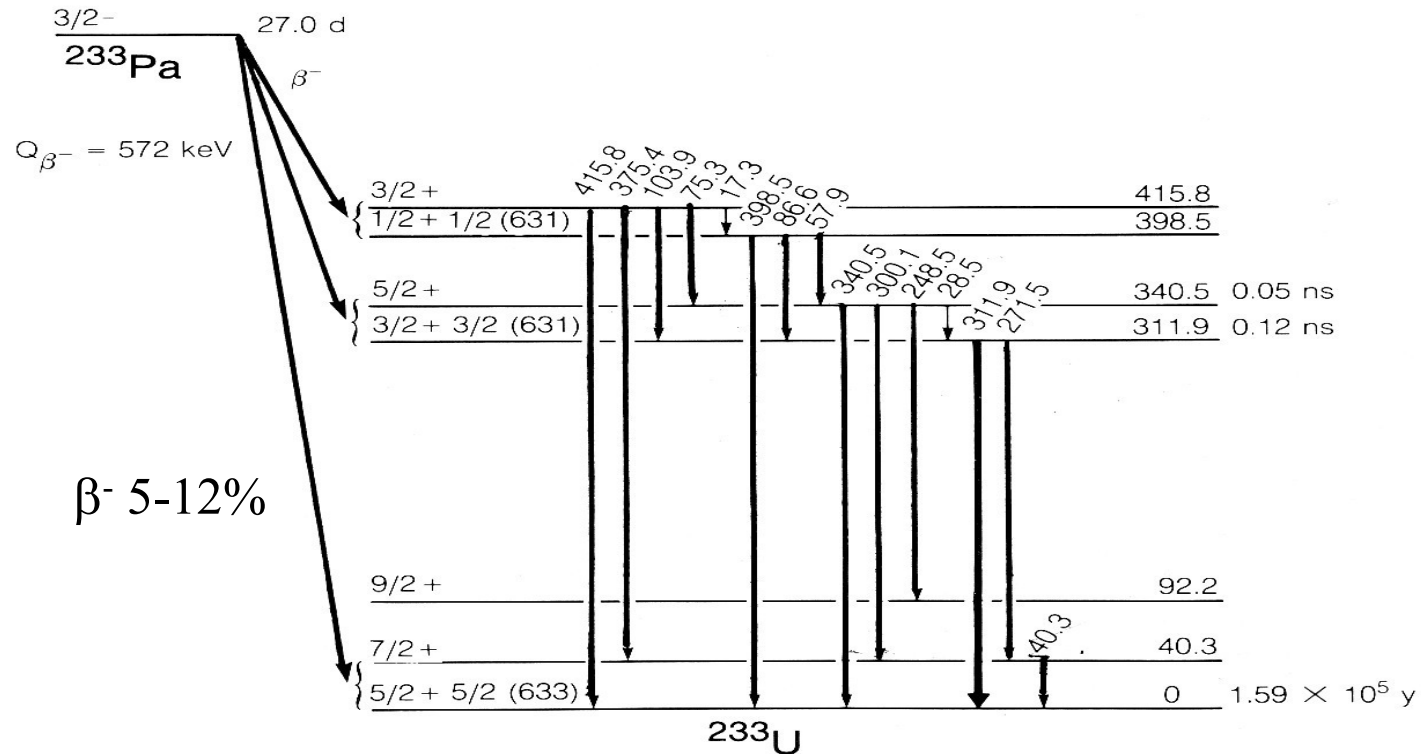


Fig. 1. Simplified  $^{233}\text{Pa}$  decay scheme from ref. <sup>1</sup>).

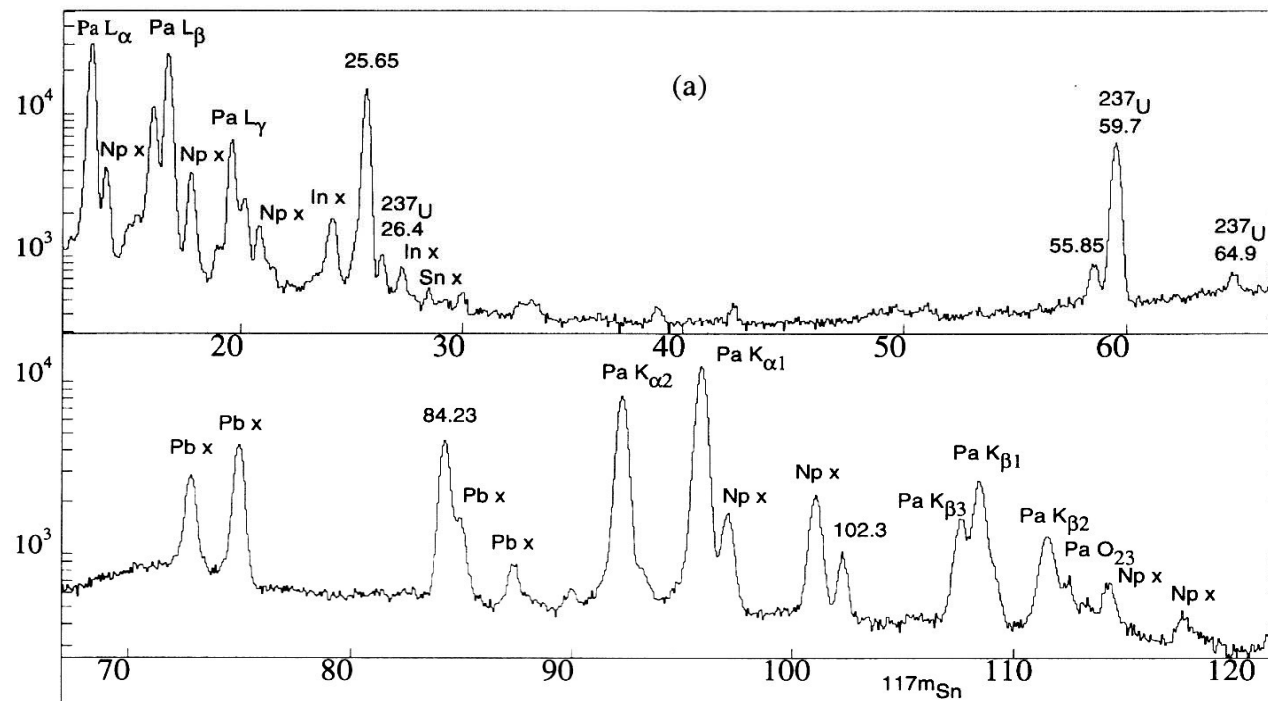
What went wrong?

$E_\gamma$ (keV)	$\alpha_T$ (exp.)	$\alpha_T$ (theo. M1)
300	0.83 (2)	1.04
312	0.79 (2)	0.96
340	0.61 (2)	0.75

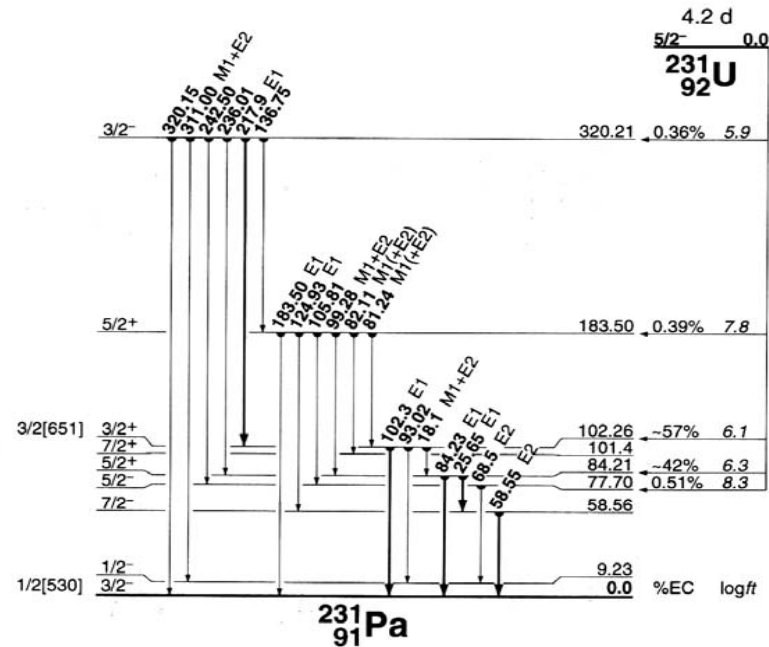
Answer: Nuclear penetration effects

# Using X rays to normalize a decay scheme

## $^{231}\text{U}$ $\gamma$ -ray spectrum



$I_{\gamma}(25)=100$  (6)  
 $I_{\gamma}(84)=50$  (3)  
 $I_{KX}=390$  (14)



$EC(K)/EC(\text{Total}) = 0.59$   
 $\omega_K = 0.972$

Fig. 4.  $^{231}\text{U}$  electron-capture decay scheme. Gamma rays measured in this work are shown with thicker arrows; other data are from refs. [3,11]. Electron-capture branches per 100 decays of  $^{231}\text{U}$  and  $\log ft$  values are from gamma-ray transition probability balances (see Table 3).

$B_K=115.6$  keV, thus most K-x rays originate from vacancies produced by the electron-capture process.

$$\text{Total vacancies} = I_{KX} EC(\text{Total}) / \omega_K EC(K) = 680 \text{ (33)}$$

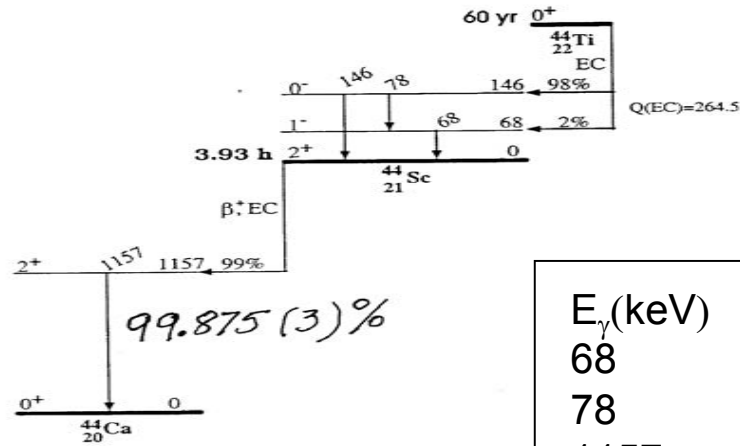
$$\text{Normalization factor } N = 100 / 680 \text{ (33)} = 0.147 \text{ (7)}$$

$$I_{\gamma}(25)=100 \text{ (6)} \times 0.147 \text{ (7)} = 15 \text{ (1)\%}$$

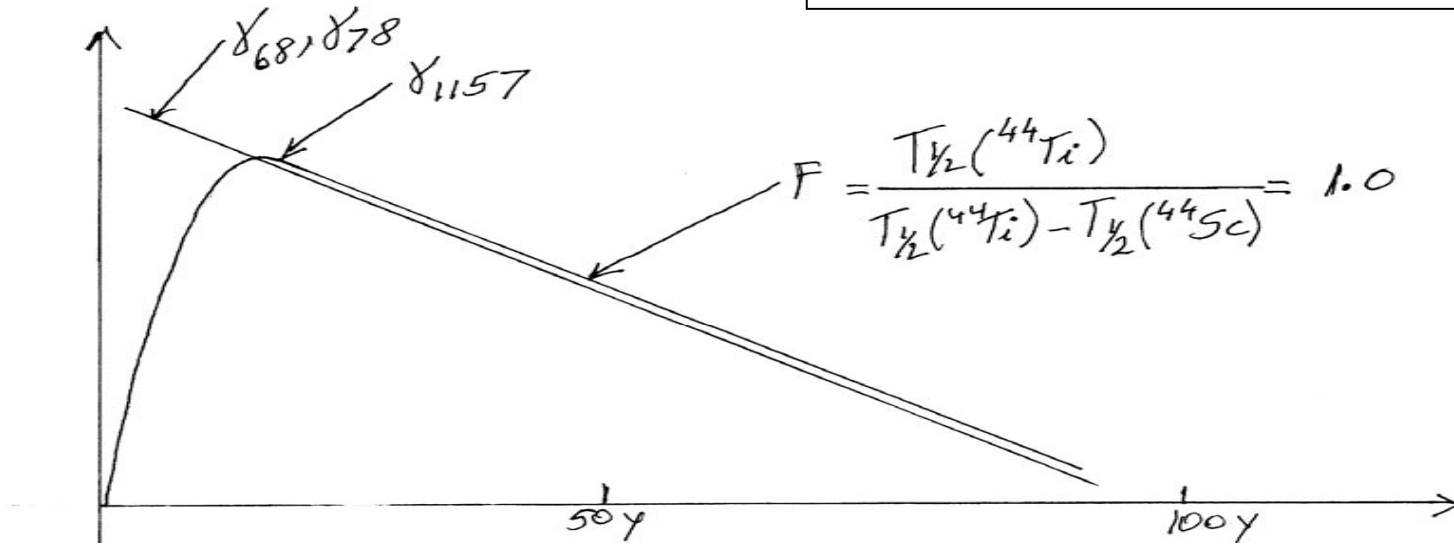
$$I_{\gamma}(84)=50 \text{ (3)} \times 0.147 \text{ (7)} = 7.5 \text{ (6)\%}$$

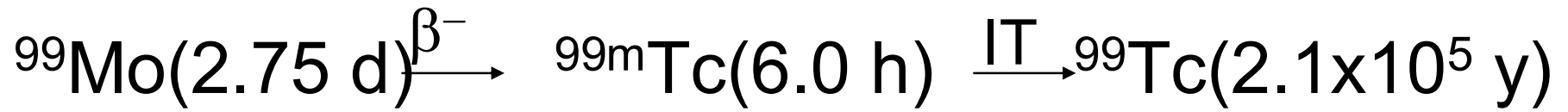


# $^{44}\text{Ti}$ electron capture decay

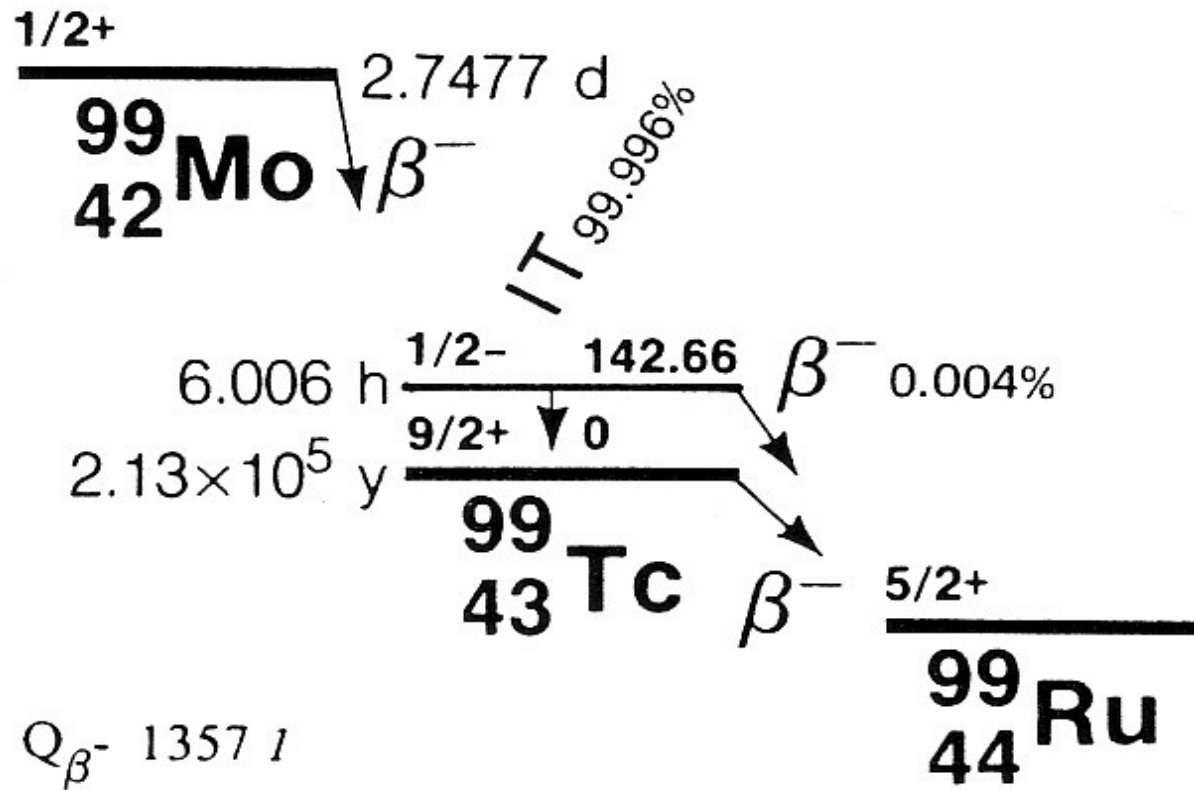


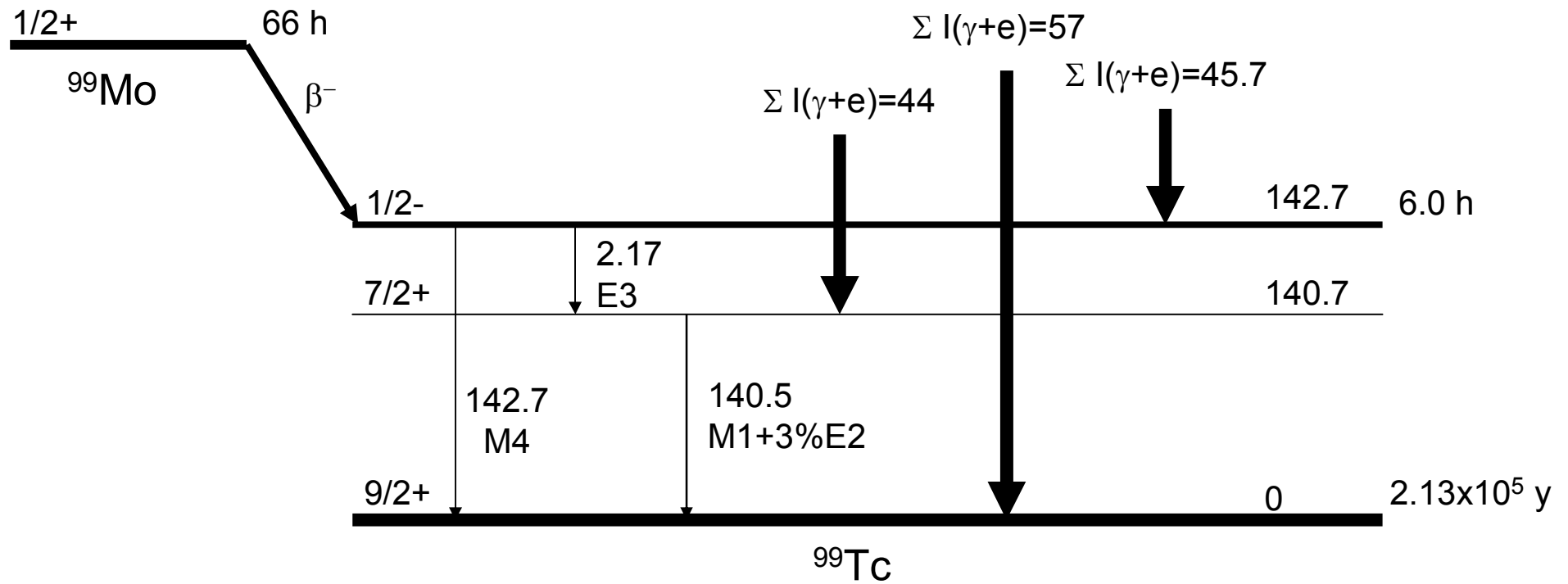
$E_\gamma$ (keV)	$I_\gamma$ (rel)	$I_\gamma$ (%)
68	100 (1)	96.6 (10)
78	94.2 (8)	91.0 (8)
1157	103.4 (10)	99.875 (3)





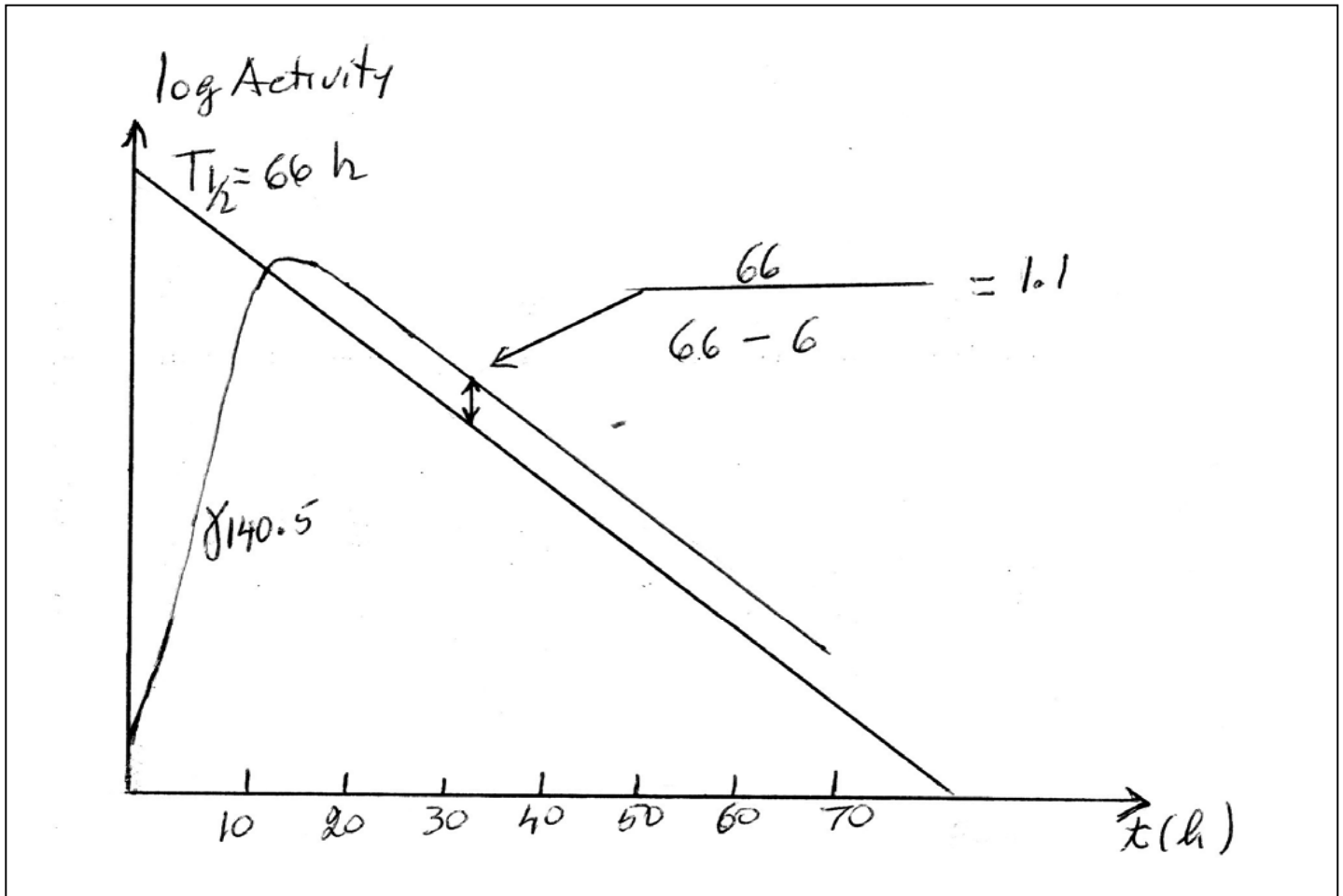
IT

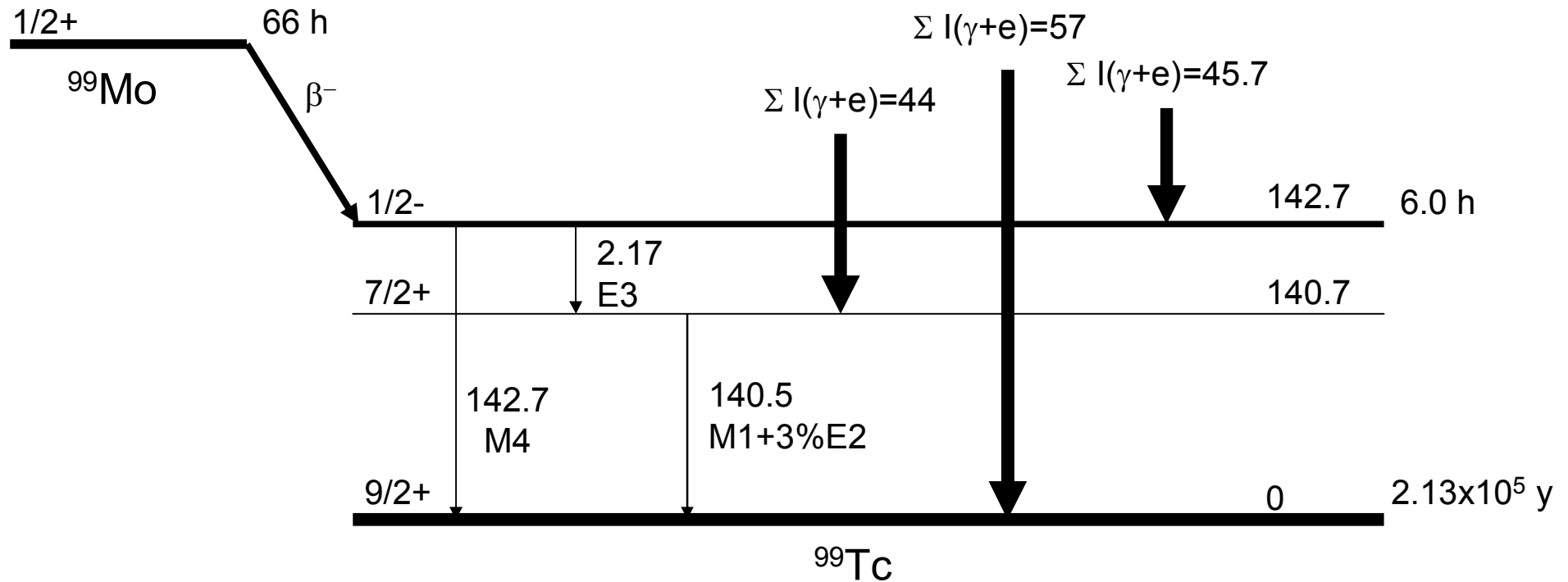




## Equilibrium Intensities

$E_\gamma$ (keV)	$I_\gamma$	$\alpha$	$I_{\gamma+ce}$
140.5	742 (11)	0.114 (3)	827 (12)
142.7	0.17 (2)	40.9 (12)	7.3 (7)





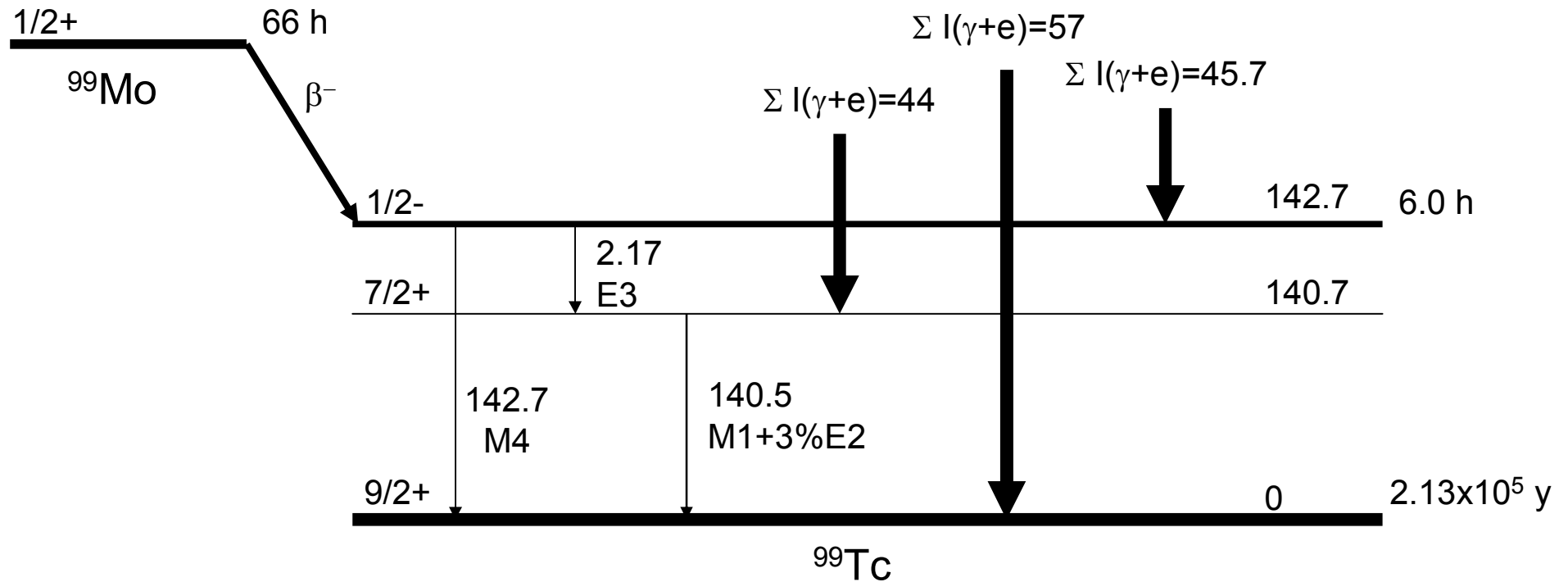
## Decay Scheme Normalization

$$[I(\gamma+ce)(142.7)/1.1 + I(\gamma+ce)(140.5)/1.1 + \Sigma I(\gamma+ce)_{gs}] \times N = 100$$

$$[7.3 (7)/1.1 + 827 (12)/1.1 + 57.0 (8)] \times N = 100$$

$$N = 100/816 (11) = 0.1226 (17)$$

$$\text{So, } I_{\gamma}(\%)(140.5) = 742 (11) \times 0.1226 (7) = 91.0 (3)\%$$



## $\beta^-$ feeding to 142.7-keV level

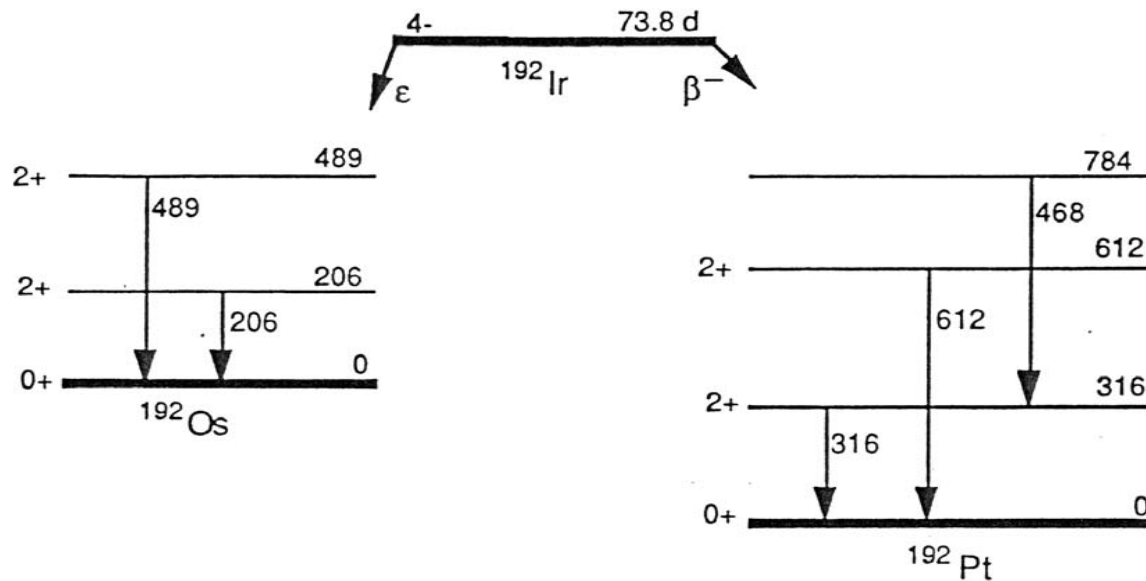
$$I_{\beta^-} = I(\gamma+ce)(142.7)/1.1 + I(\gamma+ce)(2.17)/1.1 - \Sigma I(\gamma+ce)_{142.7}$$

$$I(\gamma+ce)(140.5)/1.1 - I(\gamma+ce)(2.17)/1.1 - \Sigma I(\gamma+ce)_{140.5} = 0$$

$$I_{\beta^-} = 668$$

$$\text{So, } I_{\beta^-}(\%) = 668 \times 0.1226 = 82.0\%$$

# $^{192}\text{Ir}$ $\beta^-$ and electron capture decay



$E_\gamma$ (keV)	$I_\gamma$	$\alpha$	$I_\gamma (1+\alpha)$	
206	4.01 (6)	0.305 (9)	5.23 (8)	
489	0.527 (9)	0.0242 (7)	0.540 (9)	$\Sigma = 5.77 (8)$
316	100.0 (5)	0.085 (3)	108.5 (6)	
468	57.76 (20)	0.0294 (9)	58.43 (20)	
612	6.365 (25)	0.0155 (5)	6.464 (25)	$\Sigma = 114.9 (6)$

The normalization factor is:

$$N = 100 / [I_{\gamma}(489) (1+\alpha_{489}) + I_{\gamma}(206) (1+\alpha_{206}) + I_{\gamma}(316) (1+\alpha_{316}) + I_{\gamma}(612) (1+\alpha_{612})]$$
$$= 100 / 120.7 (7) = 0.828 (5)$$

$$N = 0.828 (5)$$

The electron capture ( $\varepsilon$ ) and  $\beta^-$  decay branchings are:

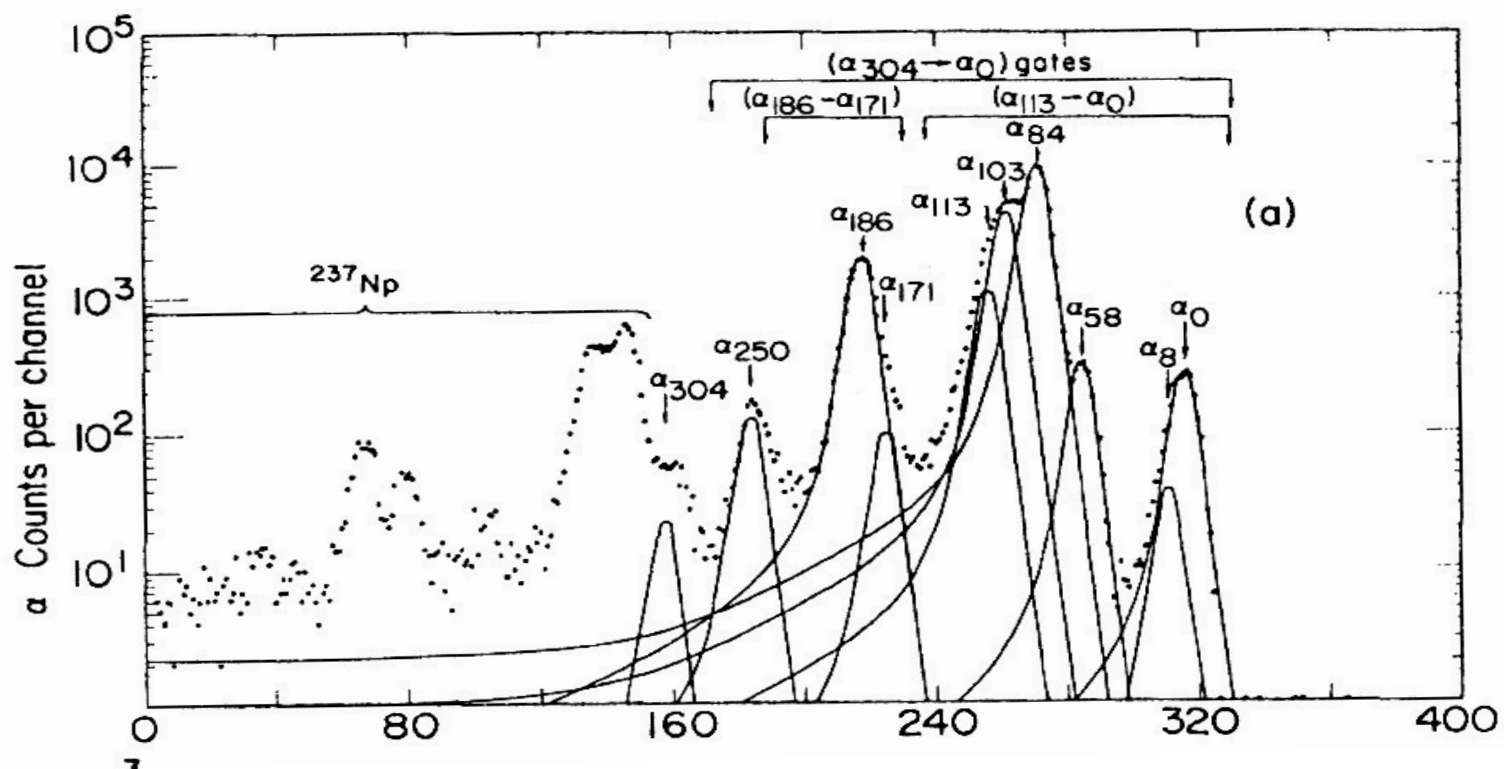
$$\varepsilon = 100 [I_{\gamma}(489) (1+\alpha_{489}) + I_{\gamma}(206) (1+\alpha_{206})] / 120.7 (7) =$$
$$100 / [1 + (I_{\gamma}(316) (1+\alpha_{316}) + I_{\gamma}(612) (1+\alpha_{612})) / (I_{\gamma}(489) (1+\alpha_{489}) + I_{\gamma}(206) (1+\alpha_{206}))] =$$
$$100 / [1 + 114.9 (6) / 5.77 (8)] = 100 / 20.9 (3) = 4.78 (7)\%$$
$$\beta^- = 100 - \text{EC} = 100 - 4.78 (7) = 95.22 (7)\%$$

$$\beta^- = 95.22 (7)\%$$

$$\varepsilon = 4.78 (7)\%$$



# $^{235}\text{Np}$ Alpha-Particle Spectrum



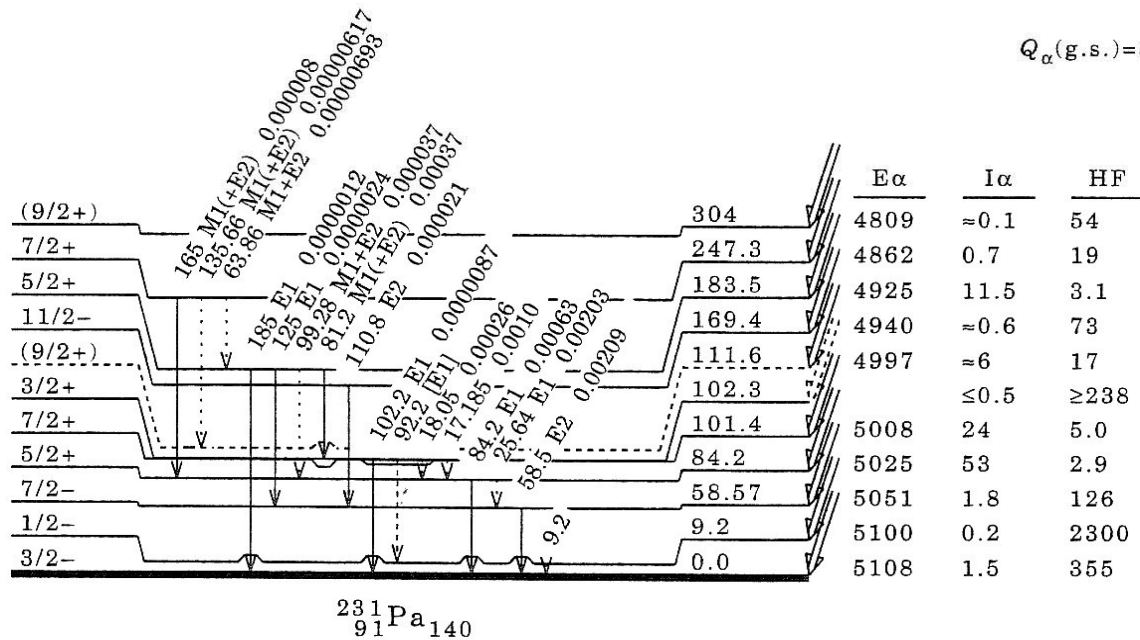
# $^{235}\text{Np}$ Alpha Decay Scheme

$^{235}\text{Np}$   $\alpha$  Decay 1973Br12 (continued)

Decay Scheme

Intensities: I( $\gamma$ +ce) per 100 parent decays

$^{235}_{93}\text{Np}_{142}$   $5/2+$   $0.0$   $396.2$  d  
 $\downarrow$   $\% \alpha = 2.60 \times 10^{-3}$  13  
 $Q_{\alpha}(\text{g.s.}) = 5191.6^{19}$



## $^{235}\text{Np}$ Alpha-particle intensities

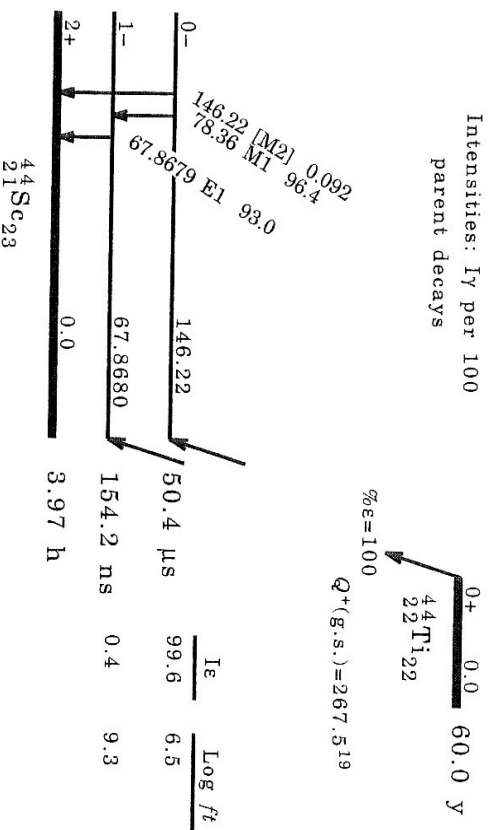
$E_{\alpha}$ (keV)	$E_{\text{lev}}$ (keV)	$I_{\alpha}$ (spec.)	$I_{\alpha}$ (bal.)
4809	304	~0.1	
4862	247	0.7 (1)	0.8 (2)
4925	183	11.5 (5)	16 (3)
4940	169	~0.6	0.8 (3)
4997	112	~6	
5008	101	24 (8)	33 (10)
5025	84	53 (8)	51 (12)
5051	58	1.8 (3)	~2
5100	9	0.2	
5108	0	1.5 (2)	

# Preparing ENSDF Data Sets

# 44Sc ENSDF Data Set

## Decay Scheme

Intensities: I<sub>γ</sub> per 100  
parent decays



44SC	44TI	EC	DECAY						
44TI	P	0		0+		60.0 Y	11		267.5
44SC	N	0.964		13		1.0			
44SC	L	0		2+		3.97 H	4		
44SC	L	67		1-		154.2 NS	8		
44SC	G	67.8679		14		96.5 16	E1		0.0845
44SCS	G	KC=		0.0766		\$LIC=	0.00664		
44SC	L	146		0-		50.4 US	7		
44SC	G	78.36		3		100.0 11	M1		0.0302
44SCS	G	KC=		0.0273		\$LIC=	0.00243		
44SC	G	146.22		3		0.095 3	[M2]		0.0460
44SCS	G	KC=		0.0414		\$LIC=	0.00385		

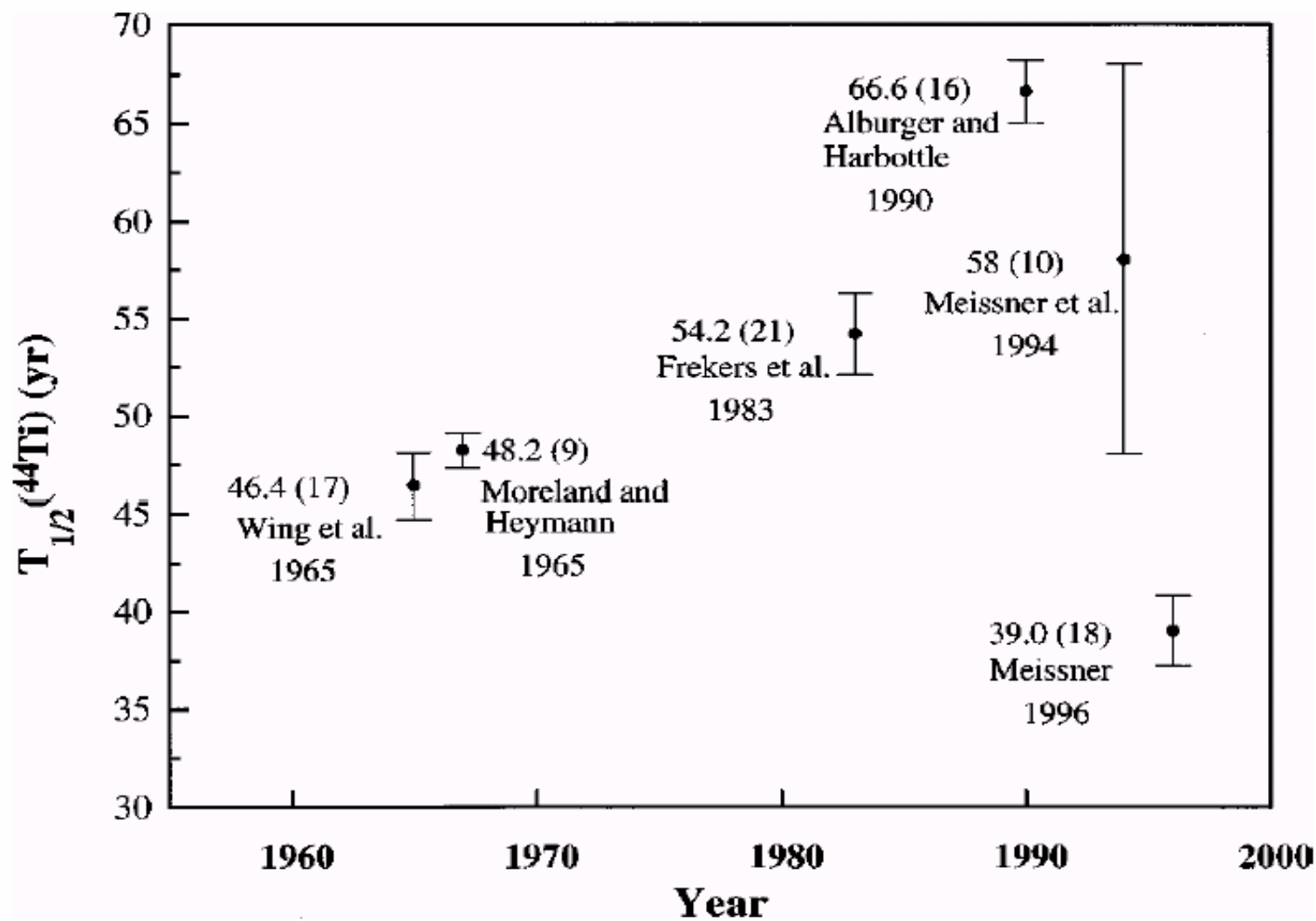


FIG. 2. Summary of previously reported values for the half-life of  $^{44}\text{Ti}$ . Numbers in parentheses represent the  $1\sigma$  uncertainties in the least significant digit(s).

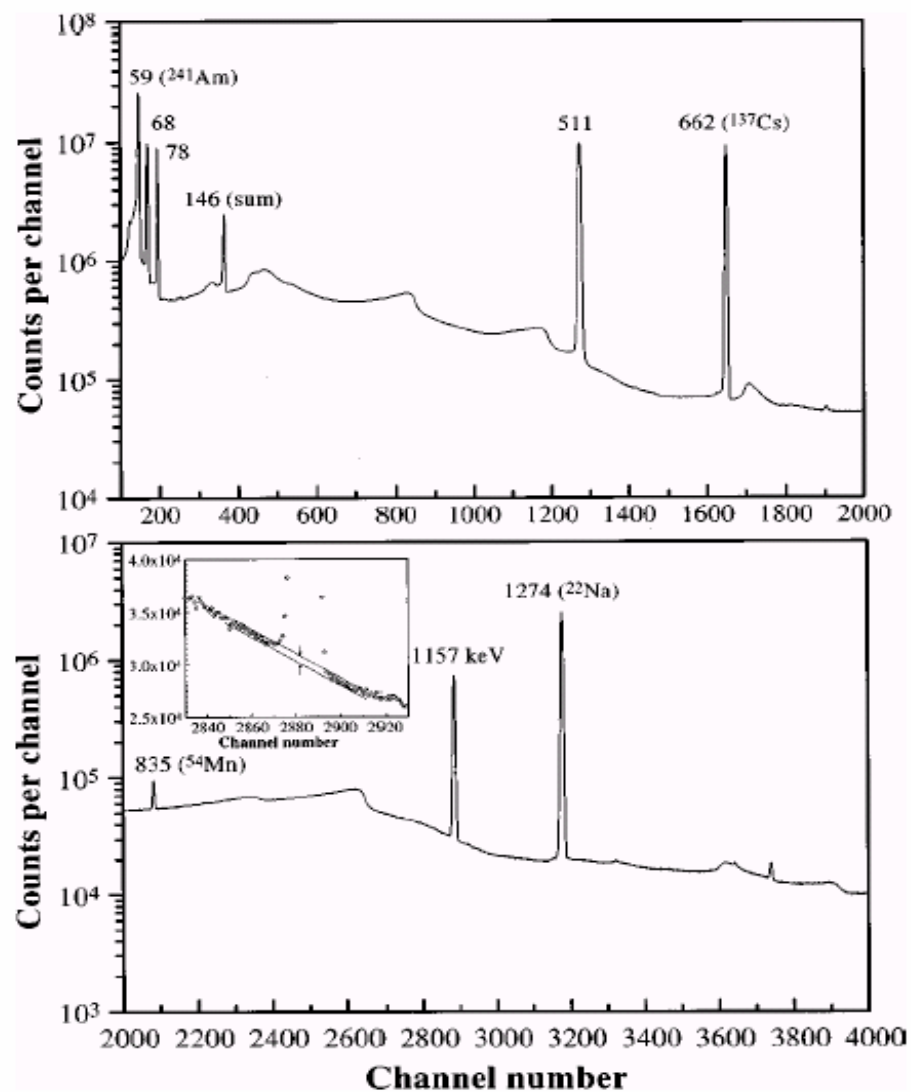


FIG. 4.  $\gamma$ -ray spectrum accumulated in 10 days of counting the mixed source of  $^{44}\text{Ti}$ ,  $^{241}\text{Am}$ ,  $^{137}\text{Cs}$ , and  $^{22}\text{Na}$ . All energies are in keV. Peaks labeled only by energy are from the decay of  $^{44}\text{Ti}$ . The inset illustrates the background under the 1157-keV peak. The arrows indicate a  $\pm 1\%$  systematic background uncertainty.

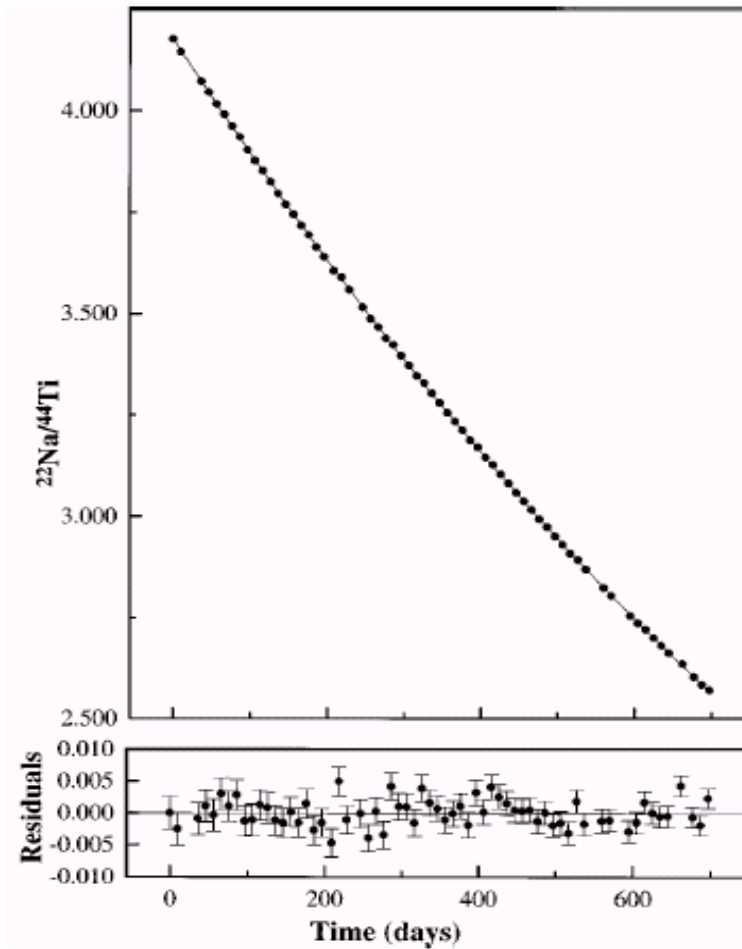


FIG. 5. The upper part of this figure shows the decrease in the ratio between the peak areas of the 1274-keV ( $^{22}\text{Na}$ ) and 1157-keV ( $^{44}\text{Ti}$ )  $\gamma$  rays as a function of time. The curve going through the data is the result of a least-squares fit of an exponentially decreasing function of time. The  $^{44}\text{Ti}$  half-life determined from this fit is 61.5(9) yr and  $\chi^2/\nu=1.1$ . The lower panel shows the residuals to this fit.



# <sup>44</sup>Ti Half-life (LWEIGHT)

## 44Ti Half-life Measurements

INP. VALUE	INP. UNC.	R. WGHT	chi**2/N-1	REFERENCE
.607000E+02	.120E+01	.141E+00	.826E-01	99Wi01
.590000E+02	.600E+00	MIN *.563E+00*	.479E+00	98Ah03
.603000E+02	.130E+01	.120E+00	.163E-01	98Go05
.620000E+02	.200E+01	.507E-01	.214E+00	98No06
.666000E+02	.160E+01	.792E-01	.348E+01	90Al11
.542000E+02	.210E+01	.460E-01	.149E+01	83Fr27

No. of Input Values N= 6 CHI\*\*2/N-1= 5.76 CHI\*\*2/N-1(critical)= 3.00

UWM :.604667E+02 .164796E+01  
WM :.599288E+02 .450317E+00 (INT.) .108057E+01 (EXT.)

INP. VALUE	INP. UNC.	R. WGHT	chi**2/N-1	REFERENCE
.607000E+02	.120E+01	.161E+00	.563E-01	99Wi01
.590000E+02	.681E+00	*.500E+00*	.487E+00	98Ah03
* Input uncertainty increased .114E+01 times *				
.603000E+02	.130E+01	.137E+00	.663E-02	98Go05
.620000E+02	.200E+01	.580E-01	.188E+00	98No06
.666000E+02	.160E+01	.907E-01	.334E+01	90Al11
.542000E+02	.210E+01	.526E-01	.156E+01	83Fr27

No. of Input Values N= 6 CHI\*\*2/N-1= 5.63 CHI\*\*2/N-1(critical)= 3.00

UWM :.604667E+02 .164796E+01  
WM :.600634E+02 .481846E+00 (INT.) .114378E+01 (EXT.)  
LWM :.600634E+02 .114378E+01 Min. Inp. Unc.=.600000E+00  
LWM has used weighted average and external uncertainty

Recommended value: 60.0 (11) y

# <sup>44</sup>Sc ENSDF Data Set (GTOL)

LEVEL	TI (OUT)	TI (IN)	TI (NET)	NET FEEDING	
				(CALC)	(USE)
0.0	0.000	104.8 18	-104.8 18	-1.0 17	0.0
67.8679 14	104.7 18	103.0 12	1.6 21	1.6 21	0.6 11
146.224 22	103.1 12	0.000	103.1 12	99.4 11	99.4 11

```

44SC    44TI EC DECAP
44TI P 0          0+          60.0 Y    11          267.5    19
44SC N 0.964      13          1.0
44SC L 0          2+          3.97 H    4
44SC L 67.8679   141-        154.2 NS  8
44SC E          0.6         11
44SC G 67.8679   14   96.5 16   E1          0.0845
44SCS G KC=    0.0766  $LC=    0.00664
44SC L 146.224   220-        50.4 US  7
44SC E          99.4         11
44SC G 78.36     3   100.0 11   M1          0.0302
44SCS G KC=    0.0273  $LC=    0.00243
44SC G 146.22    3   0.095 3    [M2]          0.0460
44SCS G KC=    0.0414  $LC=    0.00385
    
```

# $^{44}\text{Sc}$ ENSDF Data Set (LOGFT)

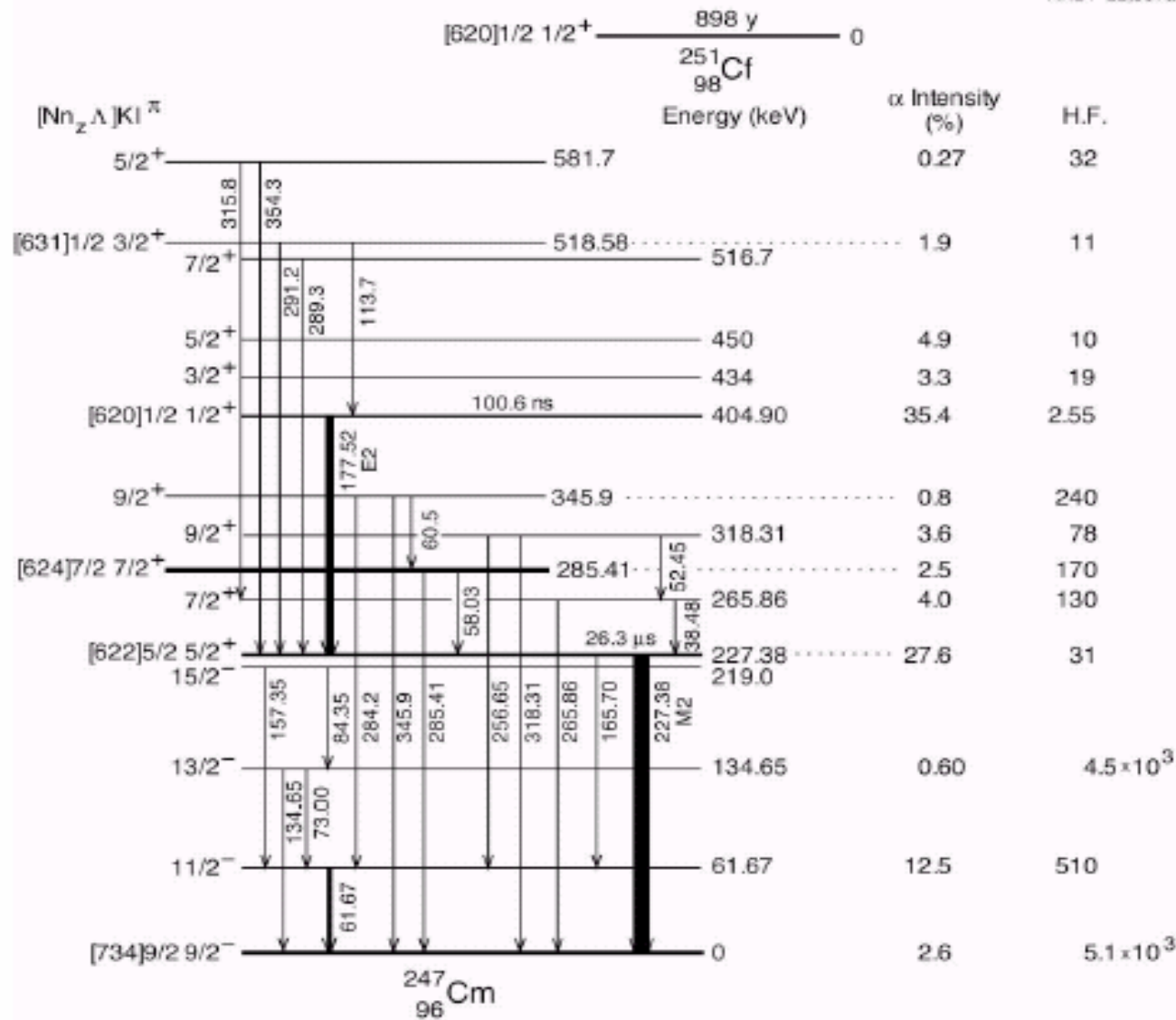
```
44SC    44TI EC DECAY
44TI    P 0                0+                60.0 Y    11                267.5    19
44SC    N 0.964           13                1.0
44SC    L 0                2+                3.97 H    4
44SC    L 67.8679        141-                154.2 NS  8
44SC    E                0.6 11    9.2    8
44SCS   E  CK=0.8910 $CL=0.09309 $CM+=0.01592
44SC    G 67.8679        14    96.5 16    E1                0.0845
44SCS   G KC=    0.0766 $LC=    0.00664
44SC    L 146.224        220-                50.4 US   7
44SC    E                99.4 11    6.509 17
44SCS   E  CK=0.8883 $CL=0.09533 $CM+=0.016352 18
44SC    G 78.36           3    100.0 11    M1                0.0302
44SCS   G KC=    0.0273 $LC=    0.00243
44SC    G 146.22         3    0.095 3    [M2]                0.0460
44SCS   G KC=    0.0414 $LC=    0.00385
```

# **New Exercise**

## **Trieste, April 4 – 15, 2005**

PHYSICAL REVIEW C **68**, 044306 (2003)

**Energy levels of  $^{247}\text{Cm}$  populated in the  $\alpha$  decay of  $^{251}_{98}\text{Cf}$**



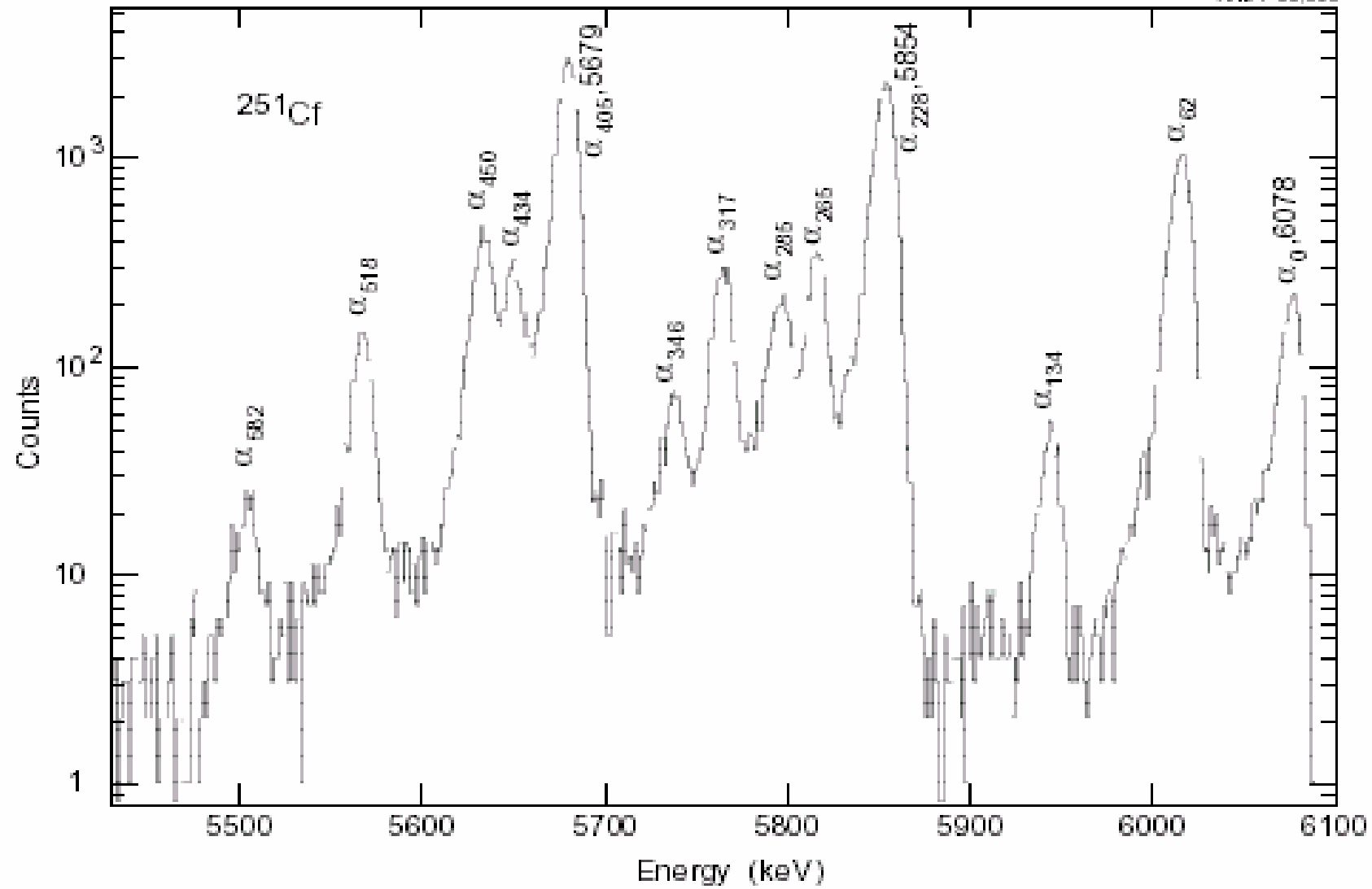


TABLE 1.  $^{251}\text{Cf}$   $\alpha$  groups.

Energy (MeV)	Excited state energy (keV)	Intensity (%)	Hindrance factor <sup>a</sup>
$6.078 \pm 0.002$	0	$2.6 \pm 0.1$	$5.1 \times 10^3$
$6.017 \pm 0.002$	62	$12.5 \pm 0.3$	$5.1 \times 10^2$
$5.946 \pm 0.002$	134	$0.60 \pm 0.06$	$4.5 \times 10^3$
$5.854 \pm 0.002$	228	$27.6 \pm 0.5$	31
$5.817 \pm 0.002$	265	$4.0 \pm 0.2$	$1.3 \times 10^2$
$5.798 \pm 0.002$	285	$2.5 \pm 0.2$	$1.7 \times 10^2$
$5.766 \pm 0.002$	317	$3.6 \pm 0.2$	78
$5.738 \pm 0.002$	346	$0.8 \pm 0.1$	$2.4 \times 10^2$
$5.679 \pm 0.002$	405	$35.4 \pm 0.5$	2.55
$5.651 \pm 0.002$	434	$3.3 \pm 0.2$	19
$5.635 \pm 0.002$	450	$4.9 \pm 0.2$	10
$5.568 \pm 0.002$	518	$1.9 \pm 0.1$	11
$5.505 \pm 0.002$	582	$0.27 \pm 0.05$	32

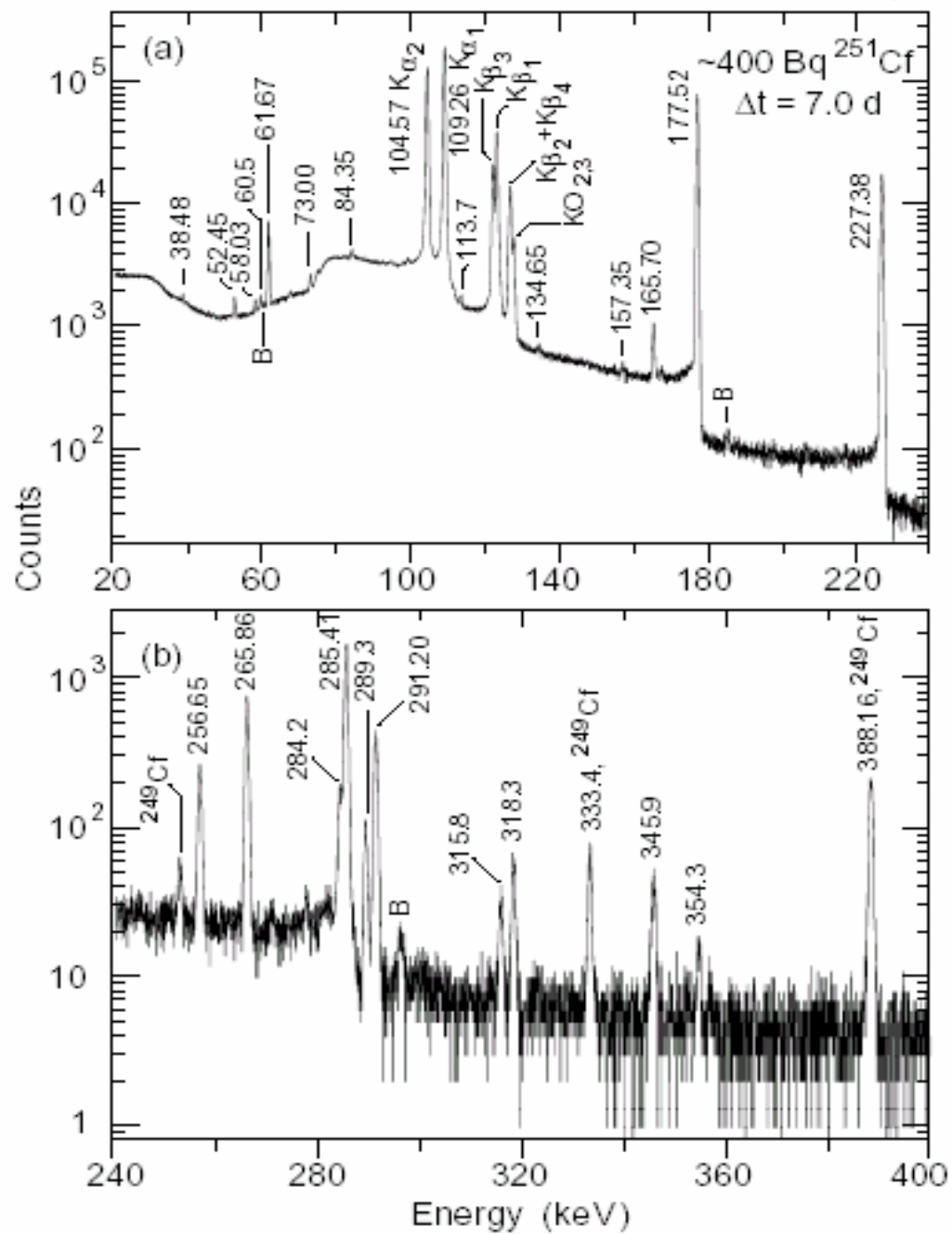




TABLE III.  $^{251}\text{Cf}$   $\gamma$  rays.

Energy (keV)	Intensity (%)	Transitions
		Initial $\rightarrow$ Final
38.48 $\pm$ 0.05	0.038 $\pm$ 0.006	265.86 $\rightarrow$ 227.38
52.45 $\pm$ 0.05	0.048 $\pm$ 0.005	318.31 $\rightarrow$ 265.86
58.03 $\pm$ 0.05	0.024 $\pm$ 0.005	285.41 $\rightarrow$ 227.38
60.5 $\pm$ 0.1	0.010 $\pm$ 0.003	345.9 $\rightarrow$ 285.41
61.67 $\pm$ 0.05	0.40 $\pm$ 0.03	61.67 $\rightarrow$ 0
73.00 $\pm$ 0.08	0.040 $\pm$ 0.005	134.65 $\rightarrow$ 61.67
84.35 $\pm$ 0.08	0.040 $\pm$ 0.005	219.0 $\rightarrow$ 134.65
104.57 $\pm$ 0.02	12.6 $\pm$ 0.7	Cm $K\alpha_2$
109.26 $\pm$ 0.02	19.8 $\pm$ 1.0	Cm $K\alpha_1$
113.7 $\pm$ 0.1	0.024 $\pm$ 0.005	518.58 $\rightarrow$ 404.90
122.31 $\pm$ 0.02+		Cm $K\beta_3$
123.40 $\pm$ 0.02	7.7 $\pm$ 0.5	Cm $K\beta_1$
127.01 $\pm$ 0.04+		Cm $K\beta_2+K\beta_4$
128.00 $\pm$ 0.05	2.6 $\pm$ 0.2	Cm $KO_{2,3}$
134.65 $\pm$ 0.08	0.014 $\pm$ 0.003	134.65 $\rightarrow$ 0
157.35 $\pm$ 0.08	0.020 $\pm$ 0.004	219.0 $\rightarrow$ 61.67
165.70 $\pm$ 0.05	0.12 $\pm$ 0.01	227.38 $\rightarrow$ 61.67
177.52 $\pm$ 0.02	17.3 $\pm$ 0.9	404.90 $\rightarrow$ 227.38
227.38 $\pm$ 0.02	6.8 $\pm$ 0.3	227.38 $\rightarrow$ 0
256.65 $\pm$ 0.08	0.13 $\pm$ 0.01	318.31 $\rightarrow$ 61.67
265.86 $\pm$ 0.08	0.43 $\pm$ 0.03	265.86 $\rightarrow$ 0
284.2 $\pm$ 0.1	0.12 $\pm$ 0.01	345.9 $\rightarrow$ 61.67
285.41 $\pm$ 0.08	1.13 $\pm$ 0.09	285.41 $\rightarrow$ 0
289.3 $\pm$ 0.1	0.070 $\pm$ 0.007	516.7 $\rightarrow$ 227.38
291.20 $\pm$ 0.08	0.30 $\pm$ 0.03	518.58 $\rightarrow$ 227.38
315.8 $\pm$ 0.1	0.024 $\pm$ 0.003	581.7 $\rightarrow$ 265.86
318.3 $\pm$ 0.1	0.050 $\pm$ 0.005	318.31 $\rightarrow$ 0
345.9 $\pm$ 0.1	0.043 $\pm$ 0.004	345.9 $\rightarrow$ 0
354.3 $\pm$ 0.1	0.013 $\pm$ 0.002	581.7 $\rightarrow$ 227.38

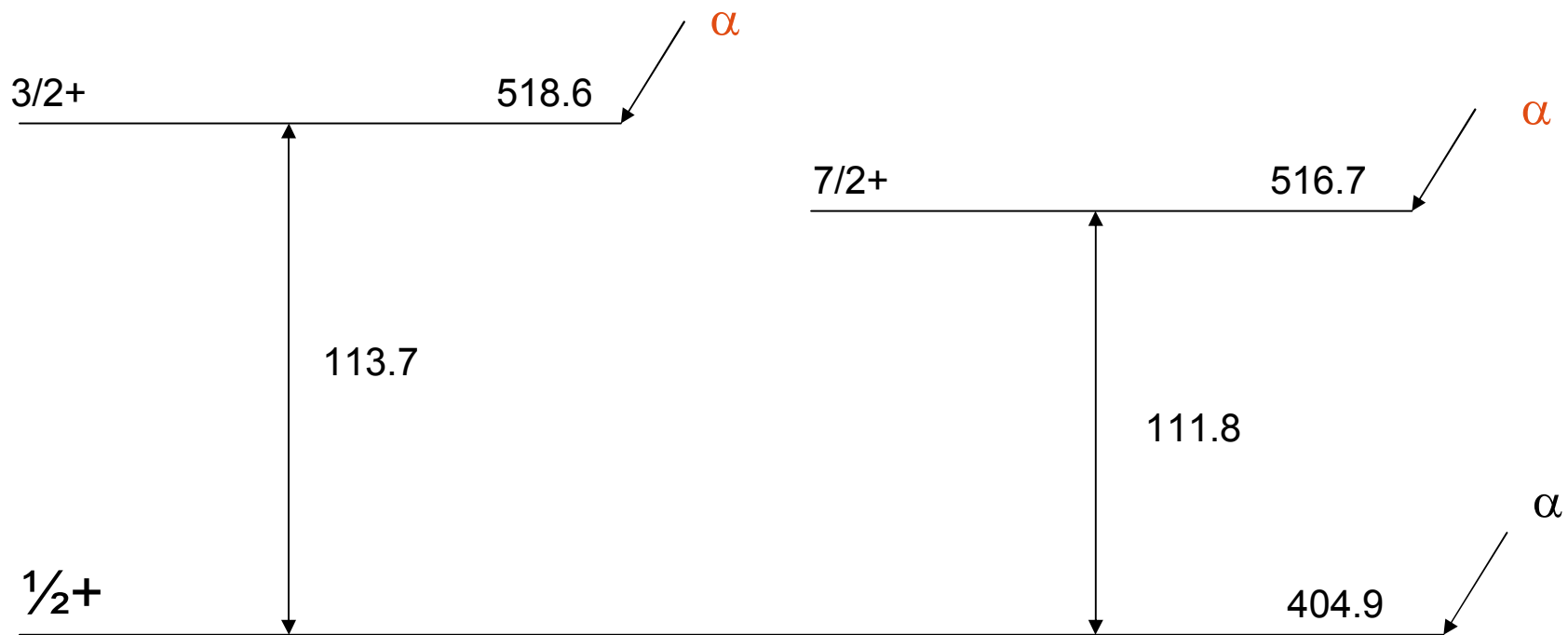
TABLE II.  $^{251}\text{Cf}$  conversion electron data.

Transition energy (keV)	Shell	Energy (keV)	Intensity (%)	Conversion coefficient	Theory	Mixing ratio $\delta$	Multipolarity
38.48	$L+M+\dots$			$183\pm 31^a$	122(M1), 1833(E2)	$0.19\pm 0.05$	$M1+3.6\%E2$
52.45	$L+M+\dots$			$70\pm 10^a$	49.3(M1), 410(E2)	$0.25\pm 0.06$	$M1+5.7\%E2$
58.03	$L+M+\dots$			$80\pm 19^a$	36.7(M1), 256(E2)	$0.50\pm 0.08$	$M1+20\%E2$
60.5	$L+M+\dots$			$62\pm 21^a$	32.6(M1), 208(E2)	$0.45\pm 0.12$	$M1+17\%E2$
61.67	$L_1+L_2$	37.4	$9.4\pm 1.0$	$23.5\pm 3.1$	22.8(M1), 78.7(E2)	$0.11\pm 0.025$	
	$L_3$	43.0	$1.3\pm 0.3$	$3.3\pm 0.8$	0.096(M1), 56.7(E2)	$0.24\pm 0.03$	
	$M+N$	55.5	$4.5\pm 0.6$	$11.0\pm 1.7$	7.7(M1), 53(E2)	$0.28\pm 0.07$	$M1+7\%E2$
73.00	$L+M+\dots$			$40\pm 16^a$	18.7(M1), 84.3(E2)	$0.69\pm 0.14$	$M1+32\%E2$
165.7	$L_1+L_2$	141.7	$1.8\pm 0.3$	$15\pm 3$	15.6(E3)		$E3$
	$L_3$	146.6	$0.8\pm 0.3$	$6.7\pm 2.6$	5.6(E3)		
177.52	$K$	49.3	$3.3\pm 0.5$	$0.19\pm 0.03$	0.17(E2)		
	$L_1+L_2$	153.7	$12.3\pm 1.2$	$0.71\pm 0.08$	0.73(E2)		$E2$
	$L_3$	158.6	$5.3\pm 0.5$	$0.31\pm 0.03$	0.31(E2)		
	$M+N$	171.8	$7.1\pm 0.7$	$0.41\pm 0.05$	0.40(E2)		
227.38	$K$	99.1	$41\pm 3$	$6.0\pm 0.5$	7.9(M2), 0.27(E3)	$0.58\pm 0.05$	$M2+25\%E3$
	$L_1+L_2$	202.9	$18.4\pm 1.9$	$2.7\pm 0.3$	2.76(M2), 3.26(E3)		
	$L_3$	208.2	$2.8\pm 0.3$	$0.41\pm 0.05$	0.28(M2), 0.91(E3)		
	$M+N$	221.1	$10.4\pm 1.1$	$1.53\pm 0.17$	1.13(M2), 1.73(E3)		

<sup>a</sup>Deduced from decay scheme  $\gamma$ -ray and  $\alpha$ -particle intensity balance.

# ENSDF Dataset (1)

247CM	251CF A	DECAY			2003AH07			
251CF	P 0.0		1/2+		898 Y	44	6175.8	10
247CM	N 1.0		1.0	1.0				
247CM	L 0.0		9/2-		1.56E+7 Y	5		
247CM	A 6078	2	2.6	1				
247CM	L 62		11/2-					
247CM	A 6017	2	12.5	3				
247CM	G 61.67	5	0.40	3	M1+E2	0.24	3	
247CM	L 135		13/2-					
247CM	A 5946	2	0.60	6				
247CM	G 73.00	8	0.040	5	M1+E2	0.69	14	
247CM	G 134.65	8	0.014	3	[E2]			
247CM	L 219		15/2-					
247CM	G 84.35	8	0.040	5	[M1+E2]			
247CM	G 157.35	8	0.020	4	[E2]			
247CM	L 227		5/2+		26.3 US	3		
247CM	A 5854	2	27.6	5				
247CM	G 165.70	5	0.12	1	E3			
247CM	G 227.38	2	6.8	3	M2+E3	0.58	5	
247CM	L 266		(7/2+)					
247CM	A 5817	2	4.0	2				
247CM	G 38.48	5	0.038	6	(M1+E2)	0.19	5	
247CM	G 265.86	8	0.43	3	[E1]			
247CM	L 285		(7/2+)					
247CM	A 5798	2	2.5	2				
247CM	G 58.03	5	0.024	5	(M1+E2)	0.50	8	
247CM	G 285.41	8	1.13	9	[E1]			
247CM	L 318		9/2+					
247CM	A 5766	2	3.6	2				
247CM	G 52.45	5	0.048	5	(M1+E2)	0.25	6	
247CM	G 256.65	8	0.13	1	[E1]			
247CM	G 318.3	1	0.050	5	[E1]			
247CM	L 346		(9/2+)					
247CM	A 5738	2	0.8	1				
247CM	G 60.5	1	0.010	3	(M1+E2)	0.45	12	
247CM	G 284.2	1	0.12	1	[E1]			
247CM	G 345.9	1	0.043	4	[E1]			



$$516.7 - 404.9 = 111.8 \text{ keV}$$

$$518.6 - 404.9 = 113.7 \text{ keV}$$

$$E_{\alpha}(516.7 + 518.6) = 5568 \text{ keV}$$

$$E_{\alpha}(404.9) = 5679.3 \text{ keV}$$

$$Q(516.7) = 5679.3 \times 251/247 - 111.8 = 5659.5 \text{ keV}$$

$$E_{\alpha}(516.7) = 5659.5 \times 247/251 = 5569 \text{ keV}$$

$$Q(518.6) = 5679.3 \times 251/247 - 113.7 = 5657.6 \text{ keV}$$

$$E_{\alpha}(518.6) = 5657.6 \times 247/251 = 5567 \text{ keV}$$

# ENSDF Dataset (2)

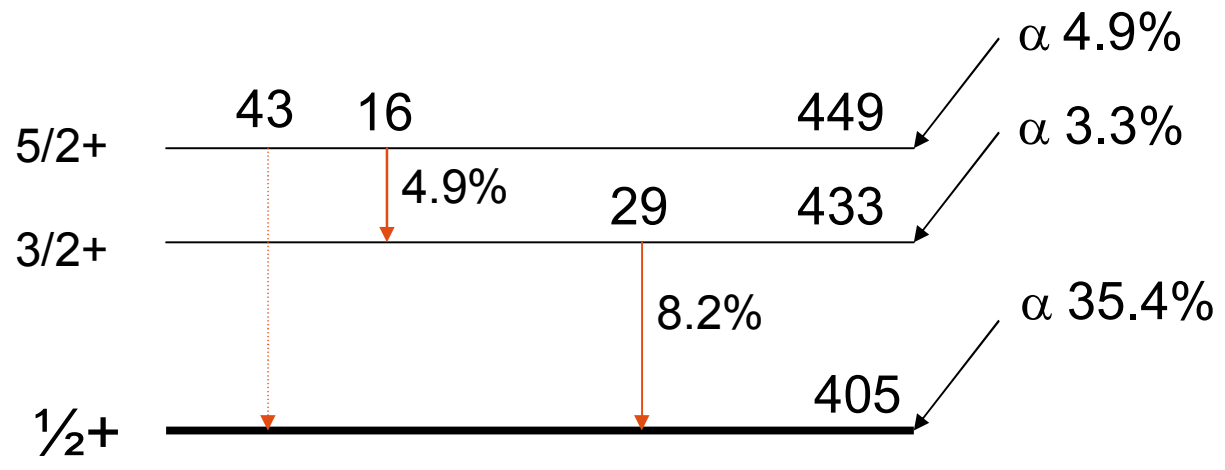
247CM	L	405	1/2+		100.6	NS	6		
247CM	A	5679.3	1635.4	5					
247CM	G	177.52	2 17.3	9	E2				
247CM	L	434	(3/2+)						
247CM	A	5651	2 3.3	2					
247CM	G	28	5		[M1+E2]	8.2		3	
247CM	L	450	2 (5/2+)						
247CM	A	5635	2 4.9	2					
247CM	G	16	5		[M1+E2]	4.9		2	
247CM	G	44							S
247CM	L	517	(7/2+)						
247CM	A	5569	2 1.9	LE					
247CM	cA	E	from E a(404.9 level)=5679.3 {I16} and the energy difference						
247CM2cA			between 516.7 and 404.9 levels (recoil energy is taken into account).						
247CM3cA			E a=5568 {I2}, measured by 2003Ah07, is assumed by the evaluator to be						
247CM4cA			a doublet, feeding the 516.7- and 518.58-keV levels.						
247CM	cA	IA	1.9 {I1} was measured by 2003Ah07 for the doublet.						
247CM	G	289.3	1 0.070	7	[M1+E2]				
247CM	L	519	(3/2+)						
247CM	A	5567	2 1.9	LE					
247CM	cA	E	from E a(404.9 level)=5679.3 {I16} and the energy difference						
247CM2cA			between 518.6 and 404.9 levels (recoil energy is taken into account).						
247CM	G	113.7	1 0.024	5	[M1+E2]				
247CM	G	291.20	8 0.30	3	[M1+E2]				
247CM	L	582	(5/2+)						
247CM	A	5505	2 0.27	5					
247CM	G	63	5		[M1+E2]	0.21		5	
247CM	G	315.8	1 0.024	3	[M1+E2]				
247CM	G	354.3	1 0.013	2	[M1+E2]				

# Program HSICC (1)

247CM	251CF A	DECAY			2003AH07				
251CF	P	0.0	1/2+		898 Y	44		6175.8	10
247CM	N	1.0	1.0	1.0					
247CM	L	0.0	9/2-		1.56E+7 Y	5			
247CM	A	6078	2	2.6	1				
247CM	L	62	11/2-						
247CM	A	6017	2	12.5	3				
247CM	G	61.67	5	0.40	3	M1+E2	0.24	3	39.2 22
247CMS	G	LC=29.0	16	MC=7.4	5	NC+=2.82	18		
247CM	L	135	13/2-						
247CM	A	5946	2	0.60	6				
247CM	G	73.00	8	0.040	5	M1+E2	0.69	14	40 6
247CMS	G	LC=29	5	MC=7.8	13	NC+=3.0	5		
247CM	G	134.65	8	0.014	3	[E2]			5.06
247CMS	G	KC=0.156	LC=3.52	MC=0.99	NC+=0.389				
247CM	L	219	15/2-						
247CM	G	84.35	8	0.040	5	[M1+E2]			27
247CMS	G	LC=20	11	MC=5	4	NC+=2.1	13		
247CM	G	157.35	8	0.020	4	[E2]			2.62
247CMS	G	KC=0.178	LC=1.76	MC=0.495	NC+=0.193				
247CM	L	227	5/2+		26.3 US	3			
247CM	A	5854	2	27.6	5				
247CM	G	165.70	5	0.12	1	E3			31.2
247CMS	G	KC=0.243	LC=21.7	MC=6.60	NC+=2.65				
247CM	G	227.38	2	6.8	3	M2+E3	0.58	5	10.6 2
247CMS	G	KC=6.0	3	LC=3.35	4	MC=0.93	2	NC+=0.364	6
247CM	L	266	(7/2+)						
247CM	A	5817	2	4.0	2				
247CM	G	38.48	5	0.038	6	(M1+E2)	0.19	5	1.8E2 4
247CMS	G	LC=135	25	MC=35	7				
247CM	G	265.86	8	0.43	3	[E1]			0.0571
247CMS	G	KC=0.0446	LC=0.0094	MC=0.00229	NC+=0.00084				
247CM	L	285	(7/2+)						
247CM	A	5798	2	2.5	2				
247CM	G	58.03	5	0.024	5	(M1+E2)	0.50	8	80 12
247CMS	G	LC=58	8	MC=15.6	23	NC+=6.0	9		
247CM	G	285.41	8	1.13	9	[E1]			0.0489
247CMS	G	KC=0.0383	LC=0.00795	MC=0.00194	NC+=0.00071				
247CM	L	318	9/2+						
247CM	A	5766	2	3.6	2				
247CM	G	52.45	5	0.048	5	(M1+E2)	0.25	6	71 11
247CMS	G	LC=52	8	MC=13.4	22	NC+=5.1	9		
247CM	G	256.65	8	0.13	1	[E1]			0.0617
247CMS	G	KC=0.0481	LC=0.0102	MC=0.00249	NC+=0.00091				
247CM	G	318.3	1	0.050	5	[E1]			0.0387
247CMS	G	KC=0.0304	LC=0.00620	MC=0.00151	NC+=0.00055				

# Program HSICC (2)

247CM L 346 (9/2+)  
 247CM A 5738 2 0.8 1  
 247CM G 60.5 1 0.010 3 (M1+E2) 0.45 12 62 14  
 247CMS G LC=45 10\$MC=12 3\$NC+=4.6 11  
 247CM G 284.2 1 0.12 1 [E1] 0.0494  
 247CMS G KC=0.0386\$LC=0.00803\$MC=0.00196\$NC+=0.00072  
 247CM G 345.9 1 0.043 4 [E1] 0.0324  
 247CMS G KC=0.0256\$LC=0.00515\$MC=0.00125\$NC+=0.00046  
 247CM L 405 1/2+ 100.6 NS 6  
 247CM A 5679.3 1635.4 5  
 247CM G 177.52 2 17.3 9 E2 1.61  
 247CMS G KC=0.168\$LC=1.04\$MC=0.291\$NC+=0.113  
 247CM L 434 (3/2+)  
 247CM A 5651 2 3.3 2  
 247CM G 28 5 [M1+E2] 4.E3 58.2 3  
 247CMS G L/T=0.73 23\$M/T=0.20 21  
 247CM L 450 2 (5/2+)  
 247CM A 5635 2 4.9 2  
 247CM G 16 5 [M1+E2] 1.9E4 194.9 2  
 247CMS G M/T=0.75 19  
 247CM G 44 S  
 247CM L 517 (7/2+)  
 247CM A 5569 2 1.9 LE  
 247CM cA E from E|a(404.9 level)=5679.3 {I16} and the energy difference  
 247CM2cA between 516.7 and 404.9 levels (recoil energy is taken into account).  
 247CM3cA E|a=5568 {I2}, measured by 2003Ah07, is assumed by the evaluator to be  
 247CM4cA a doublet, feeding the 516.7- and 518.58-keV levels.  
 247CM cA IA 1.9 {I1} was measured by 2003Ah07 for the doublet.  
 247CM G 289.3 1 0.070 7 [M1+E2] 1.0 8  
 247CMS G KC=0.7 7\$LC=0.21 7\$MC=0.052 15\$NC+=0.020 6  
 247CM L 519 (3/2+)  
 247CM A 5567 2 1.9 LE  
 247CM cA E from E|a(404.9 level)=5679.3 {I16} and the energy difference  
 247CM2cA between 518.6 and 404.9 levels (recoil energy is taken into account).  
 247CM G 113.7 1 0.024 5 [M1+E2] 8 3  
 247CMS G LC=5.7 19\$MC=1.5 6\$NC+=0.60 25  
 247CM G 291.20 8 0.30 3 [M1+E2] 1.0 7  
 247CMS G KC=0.7 7\$LC=0.20 7\$MC=0.051 15\$NC+=0.020 6  
 247CM L 582 (5/2+)  
 247CM A 5505 2 0.27 5  
 247CM G 63 5 [M1+E2] 1.0E2 70.21 5  
 247CMS G L/T=0.72 19\$M/T=0.20 16\$N/T=0.08 7  
 247CM G 315.8 1 0.024 3 [M1+E2] 0.8 6  
 247CMS G KC=0.6 5\$LC=0.16 6\$MC=0.040 13\$NC+=0.015 5  
 247CM G 354.3 1 0.013 2 [M1+E2] 0.6 5  
 247CMS G KC=0.4 4\$LC=0.11 5\$MC=0.028 11\$NC+=0.011 4





# Report from GTOL

LEVEL	RI (OUT)	RI (IN)	RI (NET)	TI (OUT)	TI (IN)	TI (NET)	NET FEEDING			
							(CALC)	(INPUT)		
0.0	0.000	8.9 4	-8.9 4	0.000	97 5	-97 5	3 5	2.6	1	
	Upper limit (90% C.L.) estimates:									
	Method 1: 9.80									
	Method 2: 9.10									
61.67 4	0.40 3	0.430 19	-0.03 4	16.1 16	5.8 5	10.2 17	10.2 17	12.5	3	
134.66 6	0.054 6	0.040 5	0.014 8	1.7 4	1.1 7	0.6 8	0.6 8	0.60	6	
	Upper limit (90% C.L.) estimates:									
	Method 1: 1.63									
	Method 2: 1.54									
219.02 7	0.060 7	0.000	0.060 7	1.2 7	0.000	1.2 7	1.2 7			
	Upper limit (90% C.L.) estimates:									
	Method 1: 2.05									
	Method 2: 2.03									
227.379 19	6.9 3	17.7 9	-10.8 10	83 5	55 4	28 6	28 6	27.6	5	
265.86 4	0.47 3	0.072 6	0.40 4	7.3 19	3.5 7	3.8 20	3.8 20	4.0	2	
	Upper limit (90% C.L.) estimates:									
	Method 1: 6.40									
	Method 2: 6.38									
285.41 5	1.15 9	0.010 3	1.14 9	3.1 5	0.63 24	2.5 6	2.5 6	2.5	2	
318.31 5	0.228 13	0.000	0.228 13	3.6 7	0.000	3.6 7	3.6 7	3.6	2	
345.89 6	0.173 12	0.000	0.173 12	0.80 24	0.000	0.80 24	0.80 24	0.8	1	
404.90 3	17.3 9	0.024 5	17.3 9	45.2 25	8.4 4	37 3	37 3	35.4	5	
433 4	0.000	0.000	0.000	8.2 3	4.90 20	3.3 4	3.3 4	3.3	2	
448.9 10	0.000	0.000	0.000	4.90 20	0.000	4.90 20	4.90 20	4.9	2	
516.68 11	0.070 7	0.000	0.070 7	0.14 6	0.000	0.14 6	0.14 6	1.9	LE	
518.59 7	0.32 3	0.000	0.32 3	0.82 24	0.21 5	0.61 24	0.61 24	1.9	LE	
581.67 8	0.037 4	0.000	0.037 4	0.27 6	0.000	0.27 6	0.27 6	0.27	5	

# Program GTOL (1)

```

247CM      251CF A DECAY                      2003AH07
251CF P 0.0          1/2+                      898 Y      44          6175.8    10
247CM N 1.0          1.0          1.0
247CM L 0.0          9/2-                      1.56E+7 Y 5
247CM A 6078        2 2.6          1 5080
247CM L          61.67 4 11/2-
247CM A 6017        2 12.5         3 512
247CM G 61.67        5 0.40         3 M1+E2      0.24      3          39.2 22
247CMS G LC=29.0 16$MC=7.4 5$NC+=2.82 18
247CM L          134.66 6 13/2-
247CM A 5946        2 0.60         6 4460
247CM G 73.00        8 0.040        5 M1+E2      0.69      14          40   6
247CMS G LC=29 5$MC=7.8 13$NC+=3.0 5
247CM G 134.65       8 0.014         3 [E2]          5.06
247CMS G KC=0.156$LC=3.52$MC=0.99$NC+=0.389
247CM L          219.02 7 15/2-
247CM G 84.35        8 0.040         5 [M1+E2]      27 16
247CMS G LC=20 11$MC=5 4$NC+=2.1 13
247CM G 157.35       8 0.020         4 [E2]          2.62
247CMS G KC=0.178$LC=1.76$MC=0.495$NC+=0.193
247CM L          227.37919 5/2+          26.3 US    3
247CM A 5854        2 27.6         5 31.3
247CM G 165.70       5 0.12          1 E3          31.2
247CMS G KC=0.243$LC=21.7$MC=6.60$NC+=2.65
247CM G 227.38       2 6.8          3 M2+E3      0.58      5          10.6 2
247CMS G KC=6.0 3$LC=3.35 4$MC=0.93 2$NC+=0.364 6
247CM L          265.86 4 (7/2+)
247CM A 5817        2 4.0          2 134
247CM G 38.48        5 0.038         6 (M1+E2)     0.19      5          1.8E2 4
247CMS G LC=135 25$MC=35 7
247CM G 265.86       8 0.43          3 [E1]          0.0571
247CMS G KC=0.0446$LC=0.0094$MC=0.00229$NC+=0.00084
247CM L          285.41 5 (7/2+)
247CM A 5798        2 2.5          2 168
247CM G 58.03        5 0.024         5 (M1+E2)     0.50      8          80 12
247CMS G LC=58 8$MC=15.6 23$NC+=6.0 9
247CM G 285.41       8 1.13          9 [E1]          0.0489
247CMS G KC=0.0383$LC=0.00795$MC=0.00194$NC+=0.00071
247CM L          318.31 5 9/2+
247CM A 5766        2 3.6          2 77
247CM G 52.45        5 0.048         5 (M1+E2)     0.25      6          71 11
247CMS G LC=52 8$MC=13.4 22$NC+=5.1 9
247CM G 256.65       8 0.13          1 [E1]          0.0617
247CMS G KC=0.0481$LC=0.0102$MC=0.00249$NC+=0.00091
247CM G 318.3        1 0.050         5 [E1]          0.0387
247CMS G KC=0.0304$LC=0.00620$MC=0.00151$NC+=0.00055

```

## Program GTOL (2)

```

247CM L 345.89 6 (9/2+)
247CM A 5738 2 0.8 1 244
247CM G 60.5 1 0.010 3 (M1+E2) 0.45 12 62 14
247CMS G LC=45 10$MC=12 3$NC+=4.6 11
247CM G 284.2 1 0.12 1 [E1] 0.0494
247CMS G KC=0.0386$LC=0.00803$MC=0.00196$NC+=0.00072
247CM G 345.9 1 0.043 4 [E1] 0.0324
247CMS G KC=0.0256$LC=0.00515$MC=0.00125$NC+=0.00046
247CM L 404.90 3 1/2+ 100.6 NS 6
247CM A 5679.3 1635.4 5 2.6
247CM G 177.52 2 17.3 9 E2 1.61
247CMS G KC=0.168$LC=1.04$MC=0.291$NC+=0.113
247CM L 433 4 (3/2+)
247CM A 5651 2 3.3 2 19.2
247CM G 28 5 [M1+E2] 4.E3 58.2 3
247CMS G L/T=0.73 23$M/T=0.20 21
247CM L 448.910 (5/2+)
247CM A 5635 2 4.9 2 10.5
247CM G 16 5 [M1+E2] 1.9E4 194.9 2
247CMS G M/T=0.75 19
247CM G 44 S
247CM L 516.6811 (7/2+)
247CM A 5569 2 1.9 LE11 GE
247CM cA E from E|a(404.9 level)=5679.3 {I16} and the energy difference
247CM2cA between 516.7 and 404.9 levels (recoil energy is taken into account).
247CM3cA E|a=5568 {I2}, measured by 2003Ah07, is assumed by the evaluator to be
247CM4cA a doublet, feeding the 516.7- and 518.58-keV levels.
247CM cA IA 1.9 {I1} was measured by 2003Ah07 for the doublet.
247CM G 289.3 1 0.070 7 [M1+E2] 1.0 8
247CMS G KC=0.7 7$LC=0.21 7$MC=0.052 15$NC+=0.020 6
247CM L 518.59 7 (3/2+)
247CM A 5567 2 1.9 LE11 GE
247CM cA E from E|a(404.9 level)=5679.3 {I16} and the energy difference
247CM2cA between 518.6 and 404.9 levels (recoil energy is taken into account).
247CM G 113.7 1 0.024 5 [M1+E2] 8 3
247CMS G LC=5.7 19$MC=1.5 6$NC+=0.60 25
247CM G 291.20 8 0.30 3 [M1+E2] 1.0 7
247CMS G KC=0.7 7$LC=0.20 7$MC=0.051 15$NC+=0.020 6
247CM L 581.67 8 (5/2+)
247CM A 5505 2 0.27 5 32
247CM G 63 5 [M1+E2] 1.0E2 70.21 5
247CMS G L/T=0.72 19$M/T=0.20 16$N/T=0.08 7
247CM G 315.8 1 0.024 3 [M1+E2] 0.8 6
247CMS G KC=0.6 5$LC=0.16 6$MC=0.040 13$NC+=0.015 5
247CM G 354.3 1 0.013 2 [M1+E2] 0.6 5
247CMS G KC=0.4 4$LC=0.11 5$MC=0.028 11$NC+=0.011 4

```

# Program AlphaD (Alpha Hindrance factors)

98 251. DATE RUN 23-FEB- 5  
Q ALPHA E TOTAL ALPHA HALF LIFE RADIUS RZERO TOTAL HALF LIFE ALPHA BRANCH  
6.1758 6.2154 3.280E+05 D 9.3638E-13 1.4924 8.980E+02 Y 1.000E+00

ENERGY LEVEL	ABUNDANCE	CALC. HALF LIFE	HINDRANCE FACTOR
0.00	2.60E-02	2.48E+03	5.08E+03
61.67	1.25E-01	5.13E+03	5.12E+02
134.66	6.00E-03	1.23E+04	4.46E+03
227.38	2.76E-01	3.80E+04	3.13E+01
265.86	4.00E-02	6.13E+04	1.34E+02
285.41	2.50E-02	7.83E+04	1.68E+02
318.31	3.60E-02	1.18E+05	7.69E+01
345.89	8.00E-03	1.68E+05	2.44E+02
404.90	3.54E-01	3.59E+05	2.58E+00
433.00	3.30E-02	5.17E+05	1.92E+01
448.90	4.90E-02	6.36E+05	1.05E+01
516.68	1.90E-02	1.56E+06	1.11E+01
518.59	1.90E-02	1.60E+06	1.08E+01
581.67	2.70E-03	3.74E+06	3.25E+01