



The Abdus Salam  
International Centre for Theoretical Physics



SMR.1663- 18

## *SUMMER SCHOOL ON PARTICLE PHYSICS*

*13 - 24 June 2005*

### Physics at New Colliders

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# Physics at New Colliders

Lectures at the Summer School on Particle  
Physics

Abdus Salam ICTP, Trieste, June 2005

# Plan of the Lectures

- Status of the Standard Model
- Open issues beyond the Standard Model
- Origin of particle masses
- Search for the Higgs boson
- Supersymmetry
- Searches for supersymmetry
- Possible other new physics at colliders

# Summary of the Standard Model

- Particles and SU(3) X SU(2) X U(1) quantum numbers:

$L_L$	$\begin{pmatrix} \nu_e \\ e^- \end{pmatrix}_L, \begin{pmatrix} \nu_\mu \\ \mu^- \end{pmatrix}_L, \begin{pmatrix} \nu_\tau \\ \tau^- \end{pmatrix}_L$	(1,2,-1)
$E_R$	$e_R^-, \mu_R^-, \tau_R^-$	(1,1,-2)
$Q_L$	$\begin{pmatrix} u \\ d \end{pmatrix}_L, \begin{pmatrix} c \\ s \end{pmatrix}_L, \begin{pmatrix} t \\ b \end{pmatrix}_L$	(3,2,+1/3)
$U_R$	$u_R, c_R, t_R$	(3,1,+4/3)
$D_R$	$d_R, s_R, b_R$	(3,1,-2/3)

- Lagrangian:
 

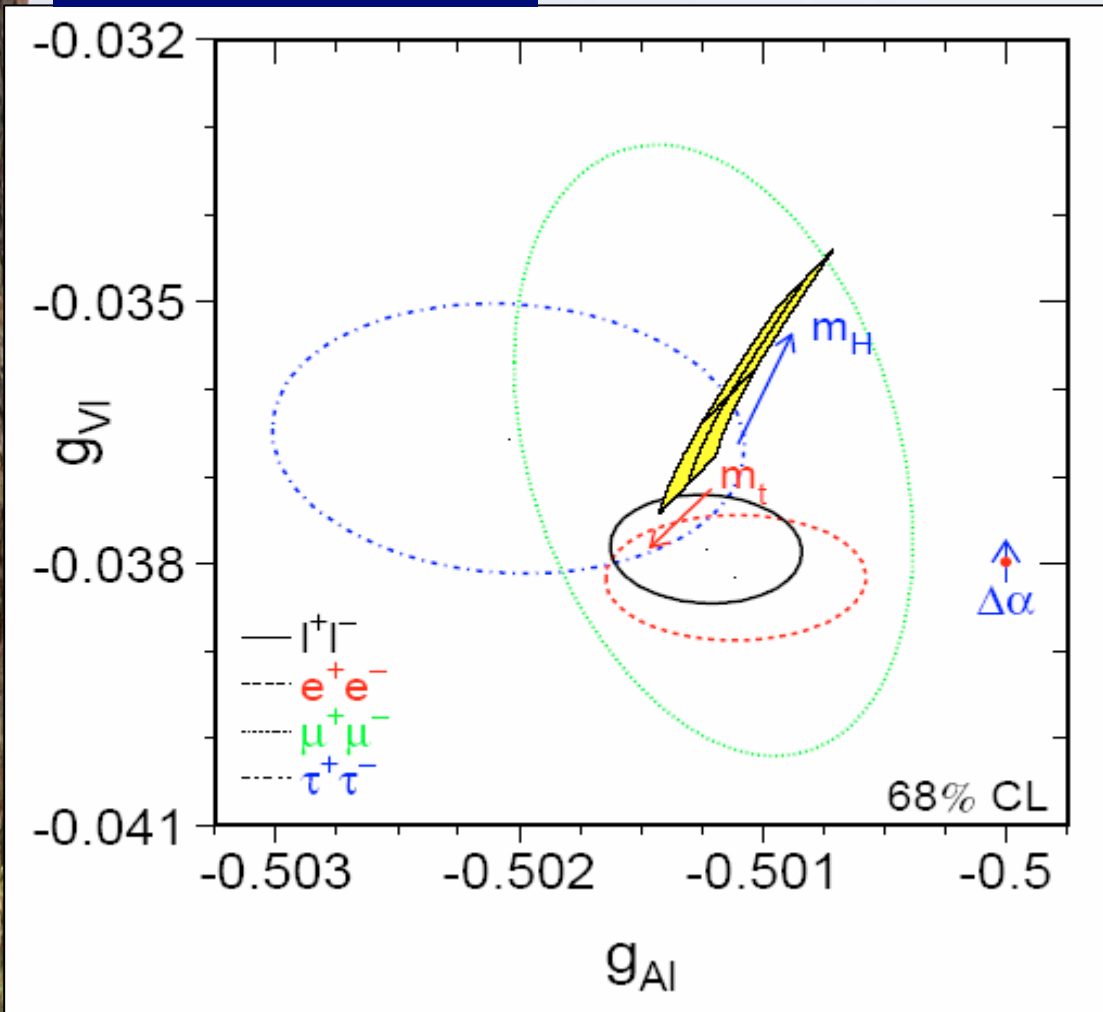
$\mathcal{L}$	$=$	$-\frac{1}{4} F_{\mu\nu}^a F^{a\ \mu\nu}$	gauge interactions
	$+$	$i\bar{\psi} \not{D}\psi + h.c.$	matter fermions
	$+$	$\psi_i y_{ij} \psi_j \phi + h.c.$	Yukawa interactions
	$+$	$ D_\mu \phi ^2 - V(\phi)$	Higgs potential

# Status of the Standard Model

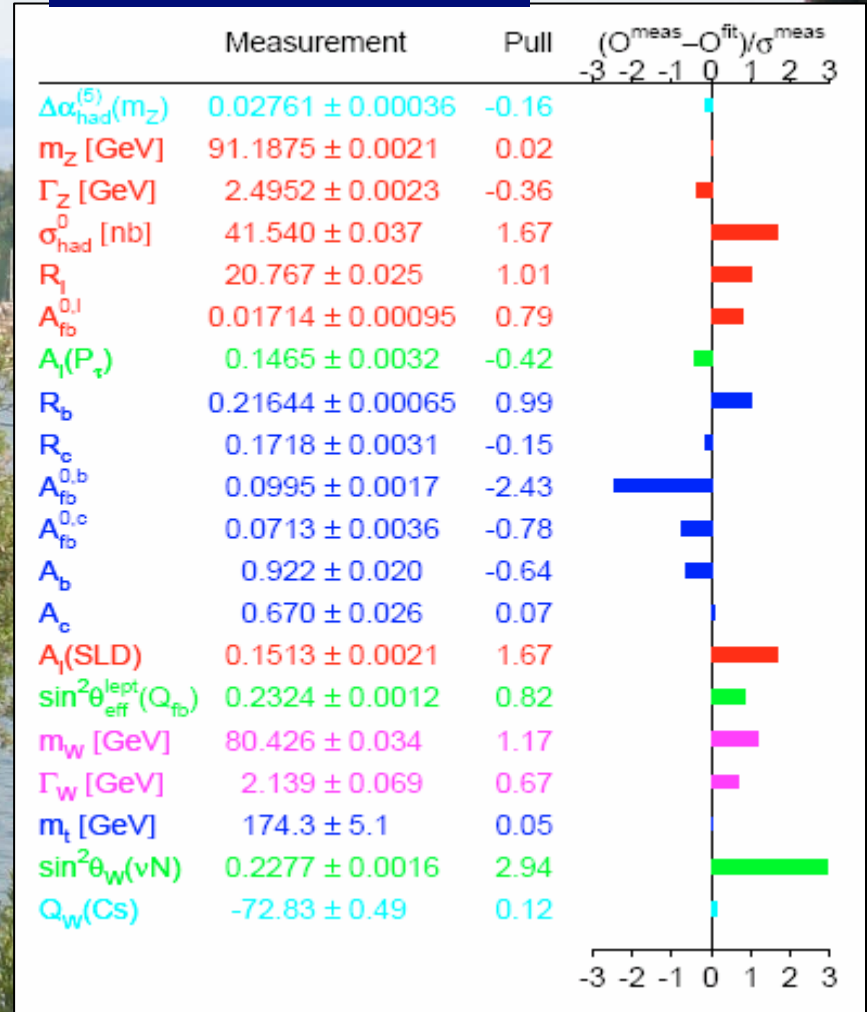
- Perfect agreement with all *confirmed* accelerator data
- Consistency with precision electroweak data (LEP et al) *only if there is a Higgs boson*
- Agreement seems to require *a relatively light Higgs boson* weighing  $< 300 \text{ GeV}$
- Raises many unanswered questions:  
*mass? flavour? unification?*

# Precision Tests of the Standard Model

## Lepton couplings



## Pulls in global fit



# Open Questions beyond the Standard Model

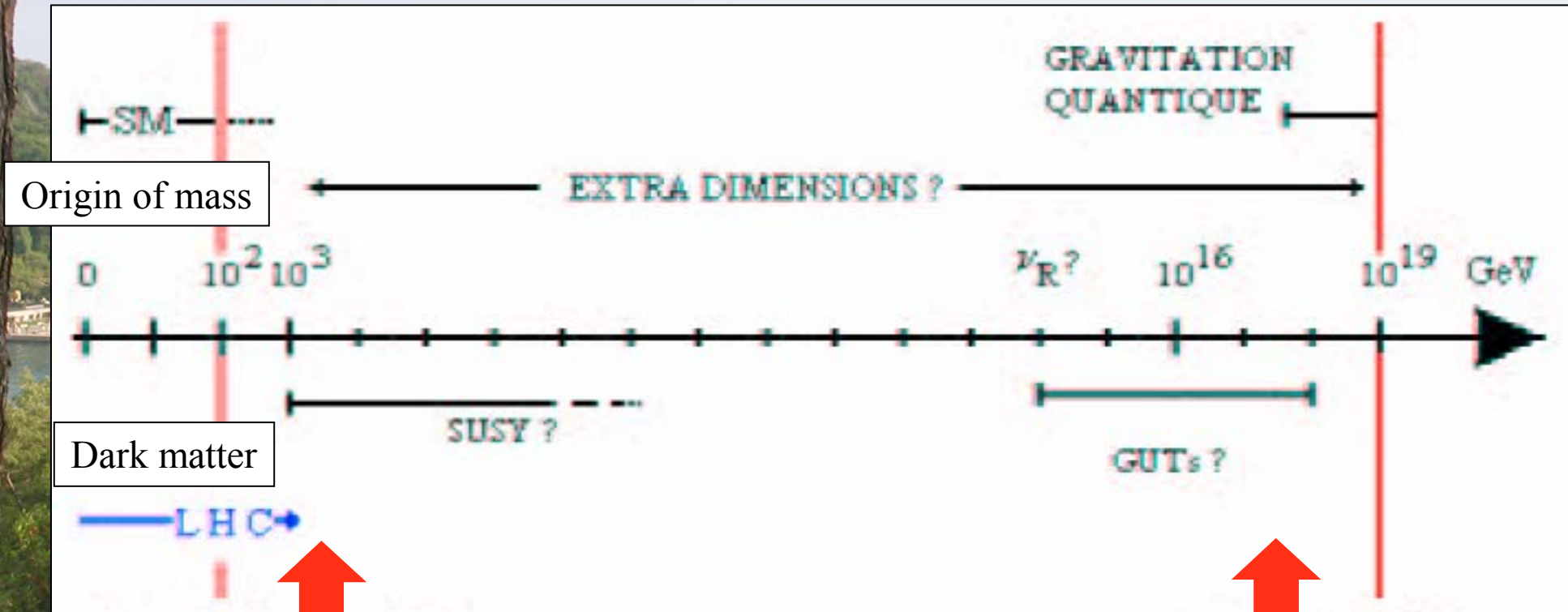
- What is the origin of particle masses?  
due to a Higgs boson? + other physics?  
solution at energy  $< 1 \text{ TeV}$  (1000 GeV)
- Why so many types of matter particles?  
matter-antimatter difference?
- Unification of the fundamental forces?  
at very high energy  $\sim 10^{16} \text{ GeV}$ ?  
probe directly via neutrino physics, indirectly via masses, couplings
- Quantum theory of gravity?  
(super)string theory: extra space-time dimensions?

Susy

Susy

Susy

# At what Energy is the New Physics?



A lot accessible  
To the LHC, ILC

Some accessible  
only indirectly



# Some particles have mass, some do not

Where do the masses  
come from ?

Newton:

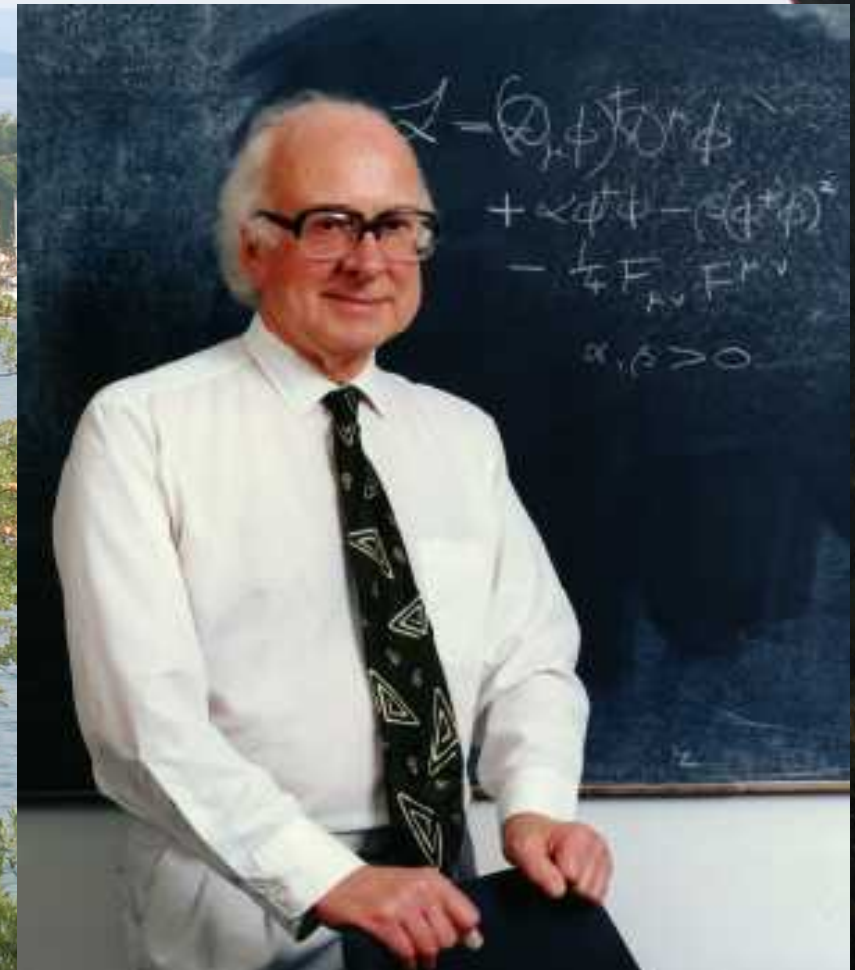
Weight **proportional to** Mass

Einstein:

Energy **related to** Mass

Neither explained origin of Mass

Are masses due to Higgs boson?  
(yet another particle)



# The Higgs Mechanism

- Postulated effective Higgs potential:

$$V[\phi] = -\mu^2 \phi^\dagger \phi + \lambda (\phi^\dagger \phi)^2$$

- Minimum energy at non-zero value:

$$\phi_0 = \langle 0 | \phi | 0 \rangle = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ +v \end{pmatrix} \quad v = \sqrt{\frac{\mu^2}{\lambda}}$$

- Non-zero masses:

$$M_f = y_f \frac{v}{\sqrt{2}} \quad M_W = \frac{g v}{2}$$

- Components of Higgs field:

$$\phi(x) = \frac{1}{\sqrt{2}} (v + \sigma(x)) e^{i\pi(x)}$$

- $\pi$  massless,  $\sigma$  massive:

$$m_H^2 = 2\mu^2 = 2\lambda v$$

# Constraints on Higgs Mass

- Electroweak observables sensitive via quantum loop corrections:

$$m_W^2 \sin^2 \theta_W = m_Z^2 \cos^2 \theta_W \sin^2 \theta_W = \frac{\pi\alpha}{\sqrt{2}G_F}(1 + \Delta r)$$

- Sensitivity to top, Higgs masses:

$$\frac{3G_F}{8\pi^2\sqrt{2}}m_t^2$$

$$\frac{\sqrt{2}G_F}{16\pi^2}m_W^2\left(\frac{11}{3}\ln\frac{M_H^2}{m_Z^2} + \dots\right), M_H \gg m_W$$

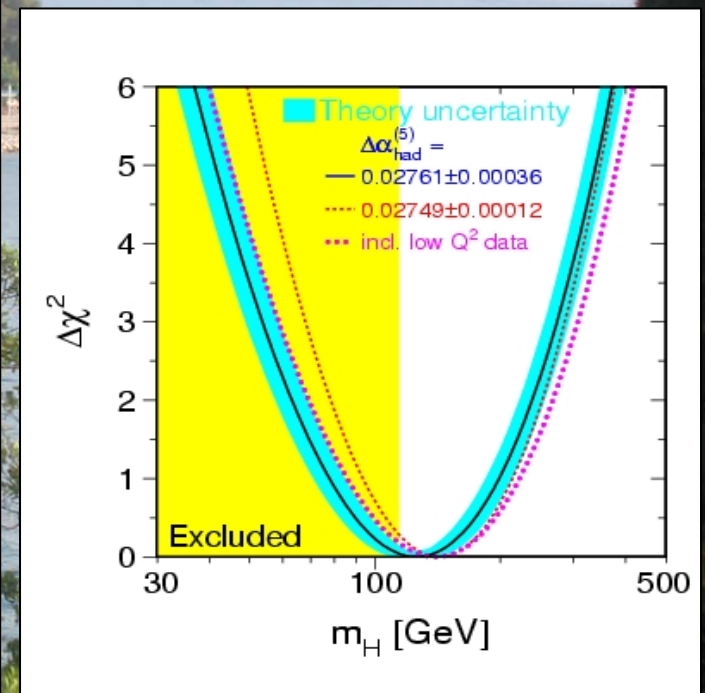
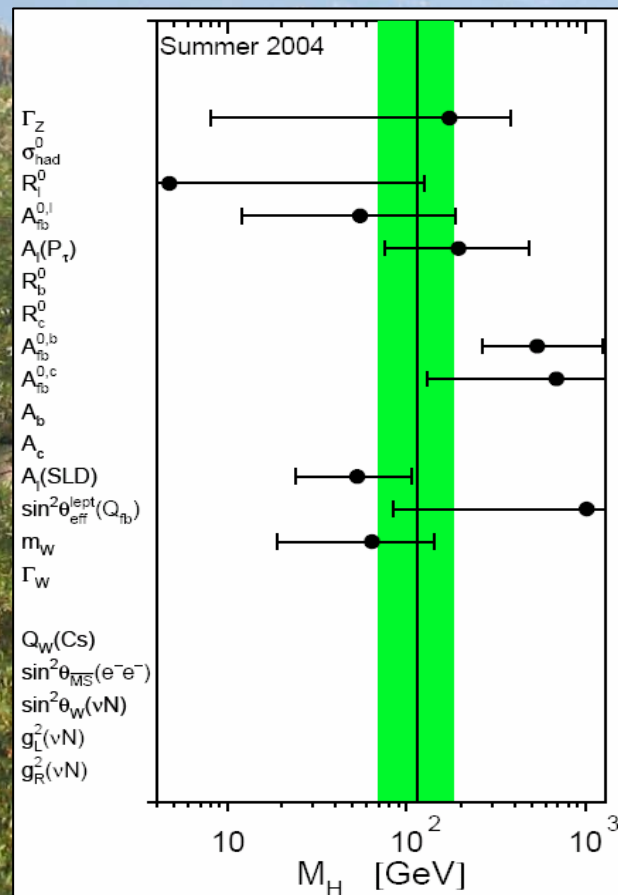
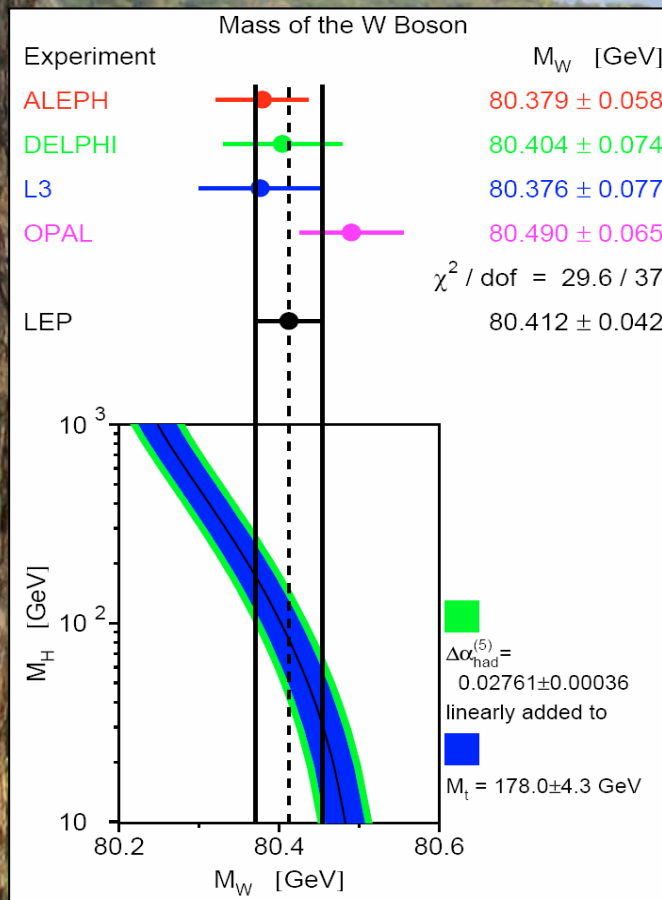
- Preferred Higgs mass:  **$m_H \sim 126 \text{ GeV}$**
- Compare with lower limit from direct searches:  
 **$m_H > 114 \text{ GeV}$**

# Indications on the Higgs Mass

Sample observable:  
W mass @ LEP

Sensitivities of  
many observables

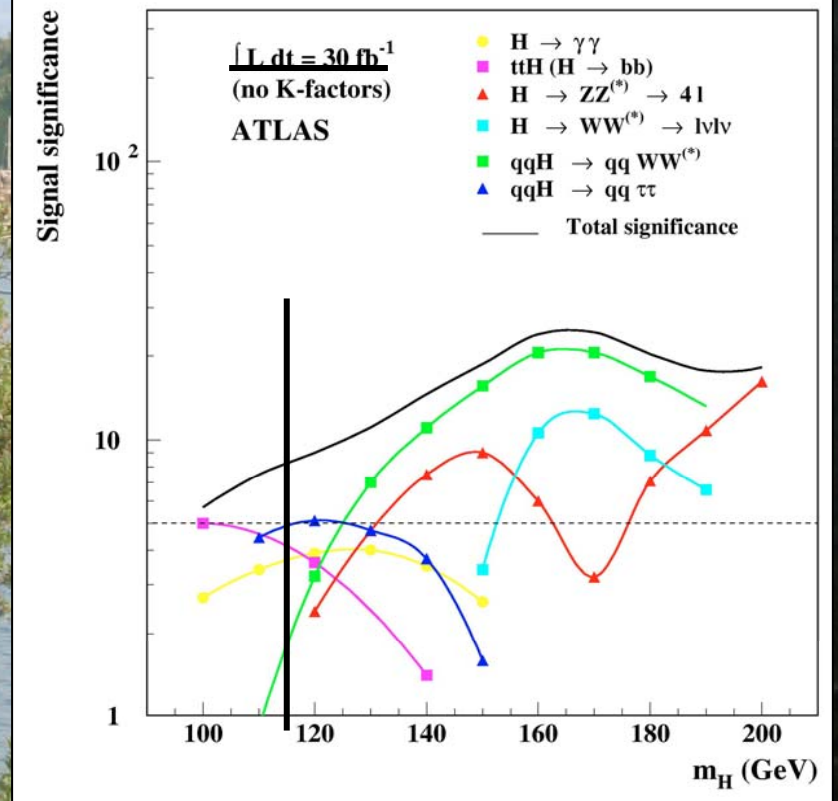
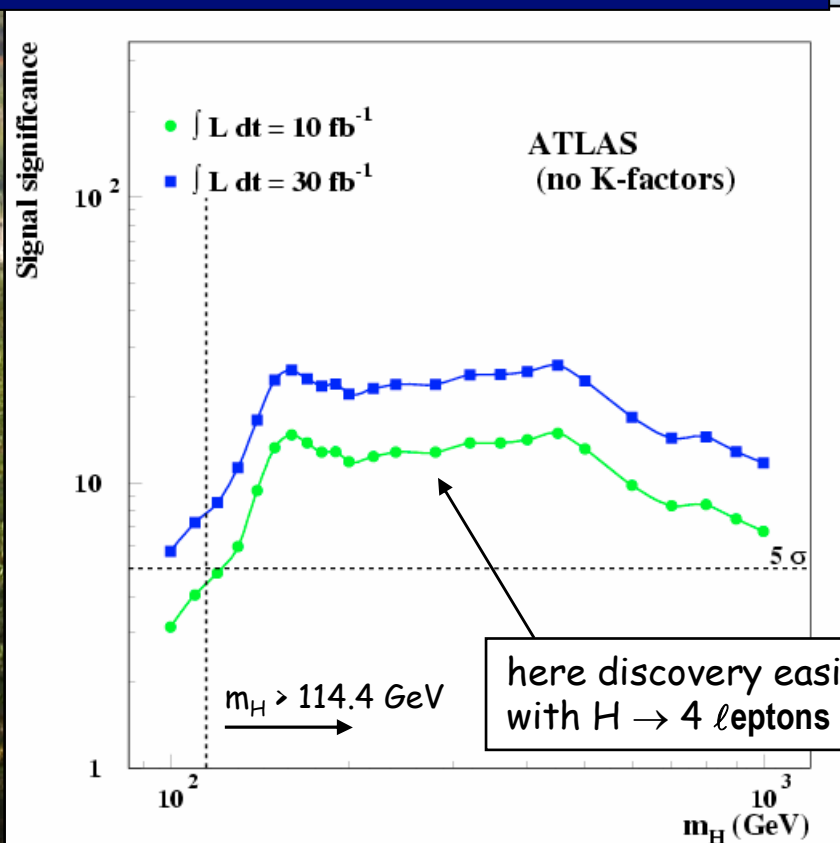
Combined information  
on Higgs mass



# Higgs Detection at the LHC

The Higgs may be found quite quickly ...

... in several different channels



# Theorists getting Cold Feet

- Composite Higgs model?  
conflicts with precision electroweak data
- Interpretation of EW data?  
consistency of measurements? Discard some?
- Higgs + higher-dimensional operators?  
corridors to higher Higgs masses?
- Little Higgs models?  
extra 'Top', gauge bosons, 'Higgses'
- Higgsless models?  
strong WW scattering, extra D?

# Loop Corrections to Higgs Mass<sup>2</sup>

- Consider generic fermion and boson loops:



- Each is quadratically divergent:  $\int^{\Lambda} d^4k/k^2$

$$\Delta m_H^2 = -\frac{y_f^2}{16\pi^2} [2\Lambda^2 + 6m_f^2 \ln(\Lambda/m_f) + \dots]$$

$$\Delta m_H^2 = \frac{\lambda_S}{16\pi^2} [\Lambda^2 - 2m_S^2 \ln(\Lambda/m_S) + \dots]$$

- Leading divergence cancelled if

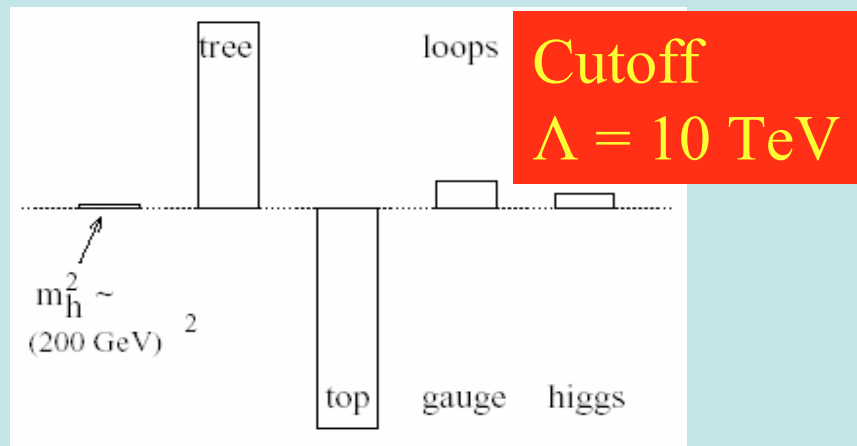
$$\lambda_S = y_f^2$$

# Elementary Higgs or Composite?

- Higgs field:

$$\langle 0|H|0\rangle \neq 0$$

- Quantum loop problems



- Cut-off  $\Lambda \sim 1 \text{ TeV}$  with  
Supersymmetry?

- Fermion-antifermion condensate
- Just like QCD, BCS superconductivity
- Top-antitop condensate? needed  $m_t > 200 \text{ GeV}$

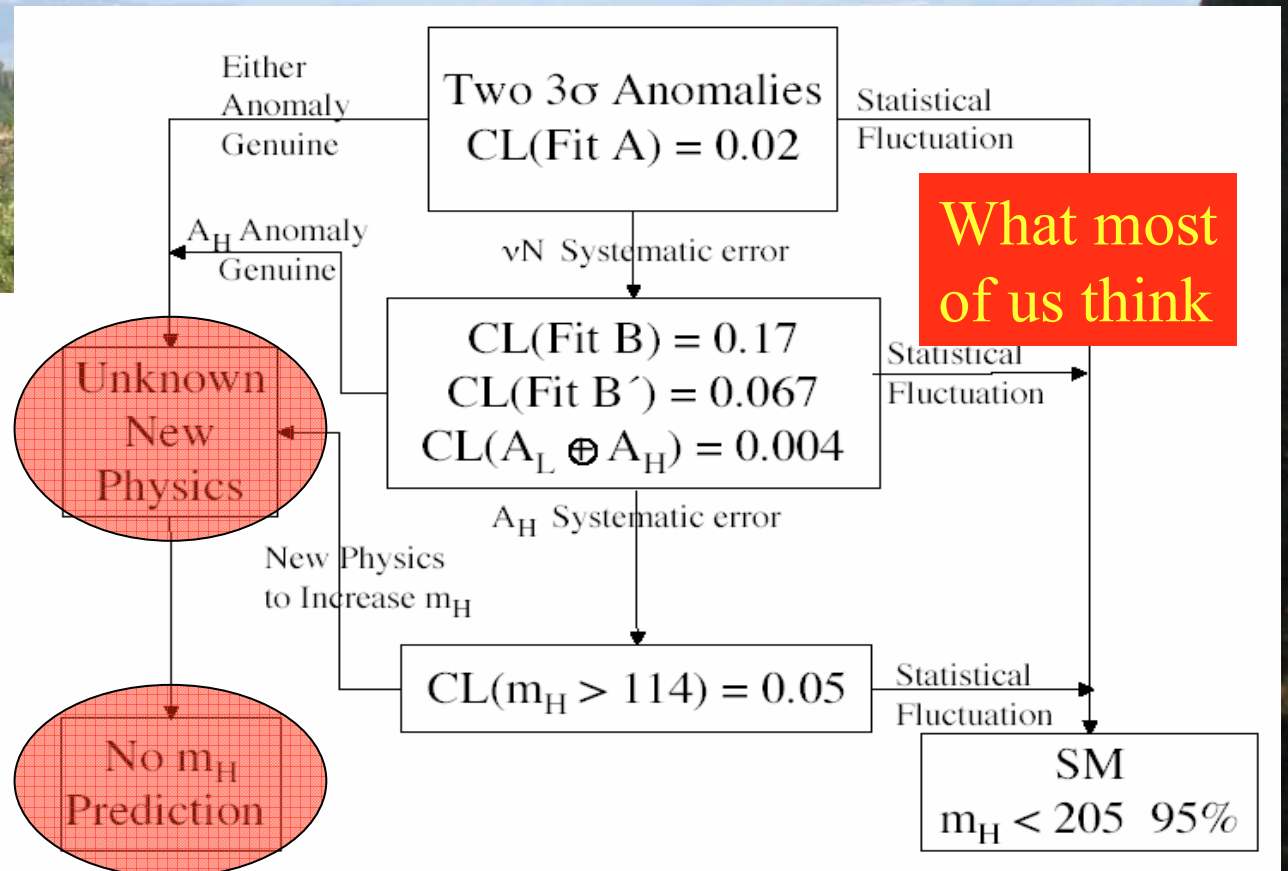
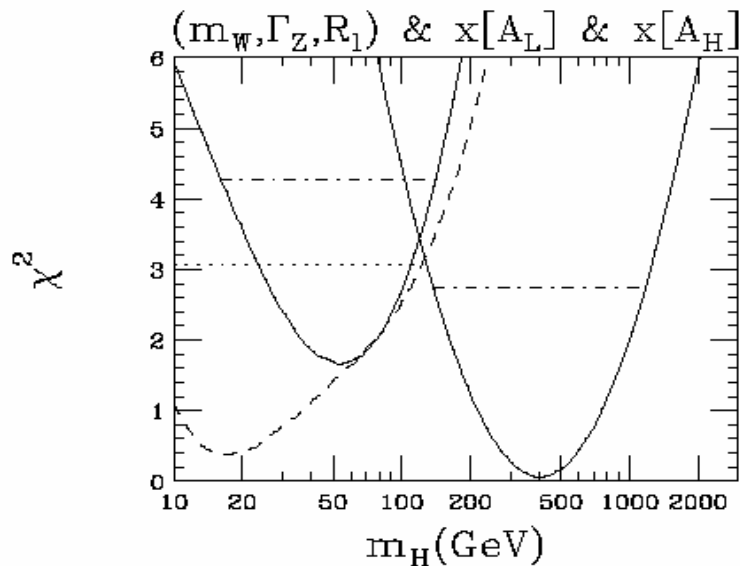
- New technicolour force?  
inconsistent with  
precision electroweak data?



# Heretical Interpretation of EW Data

Do all the data tell the same story?  
e.g.,  $A_L$  vs  $A_H$

What attitude towards LEP, NuTeV?



# Higgs + Higher-Order Operators

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{c_i}{\Lambda^p} \mathcal{O}_i^{(4+p)}$$

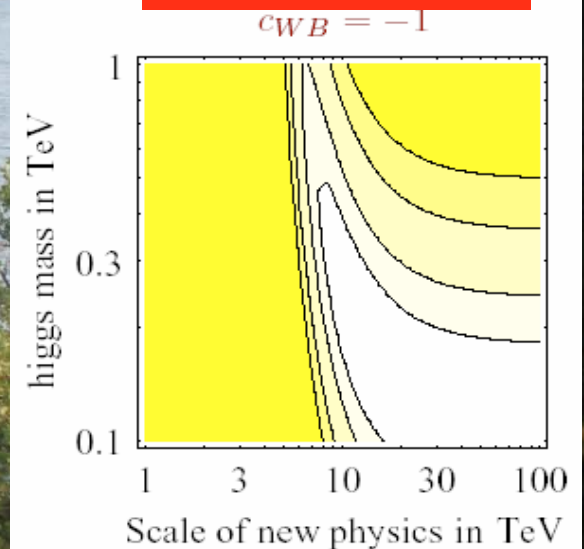
Precision EW data suggest they are small: **why?**

Dimension six operator	$c_i = -1$	$c_i = +1$
$\mathcal{O}_{WB} = (H^+ \sigma^a H) W_{\mu\nu}^a B_{\mu\nu}$	9.0	13
$\mathcal{O}_H =  H^+ D_\mu H ^2$	4.2	7.0
$\mathcal{O}_{LL} = \frac{1}{2} (\bar{L} \gamma_\mu \sigma^a L)^2$	8.2	8.8
$\mathcal{O}_{HL} = i (H^+ D_\mu H) (\bar{L} \gamma_\mu L)$	14	8.0

95% lower bounds on  $\Lambda/\text{TeV}$

But conspiracies are possible:  $m_H$  could be large, even if believe EW data ...?

Corridor to heavy Higgs?



Do not discard possibility of heavy Higgs

# Little Higgs Models

- Embed SM in larger gauge group
- Higgs as pseudo-Goldstone boson
- Cancel top loop

$$\delta m_{H,top}^2(SM) \sim (115 GeV)^2 \left( \frac{\Lambda}{400 GeV} \right)^2$$

with new heavy T quark

$$m_T > 2\lambda_t f \sim 2f \quad f > 1 \text{ TeV}$$

$$\delta m_{H,top}^2(LH) \sim \frac{6G_F m_t^2}{\sqrt{2}\pi^2} m_T^2 \log \frac{\Lambda}{m_T} \gtrsim 1.2 f^2$$

- New gauge bosons, Higgses
- Higgs light, other new physics heavy

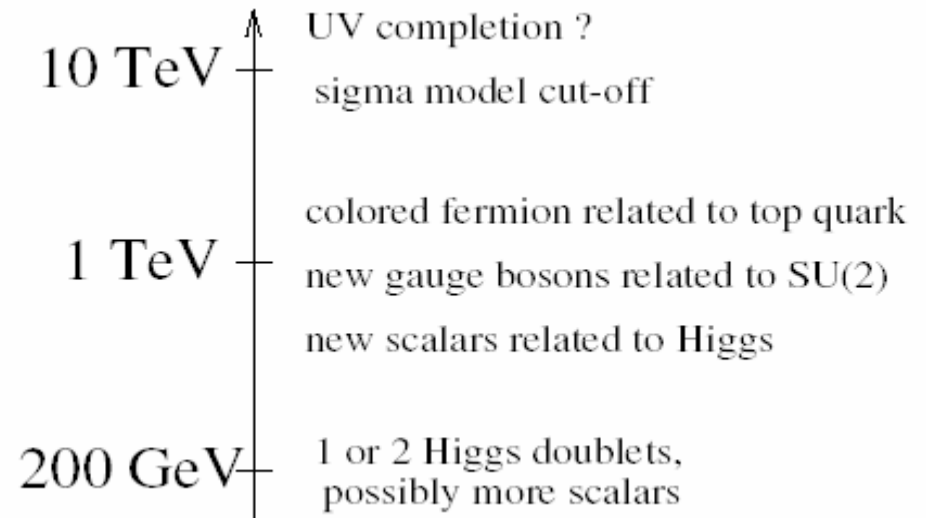
$$M_T < 2 \text{ TeV} (m_h / 200 \text{ GeV})^2$$

$$M_W' < 6 \text{ TeV} (m_h / 200 \text{ GeV})^2$$

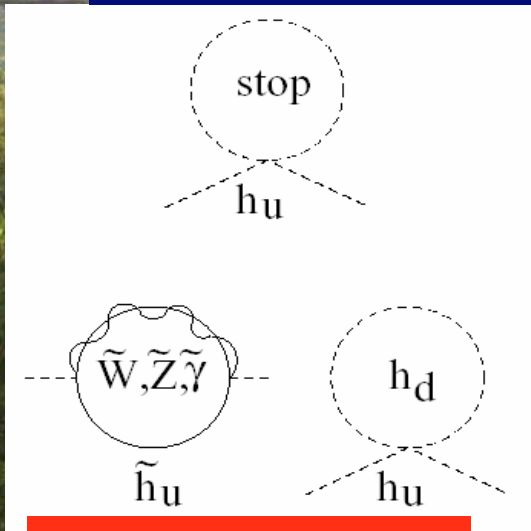
$$M_{H^{++}} < 10 \text{ TeV}$$

Not as complete as susy: more physics > 10 TeV

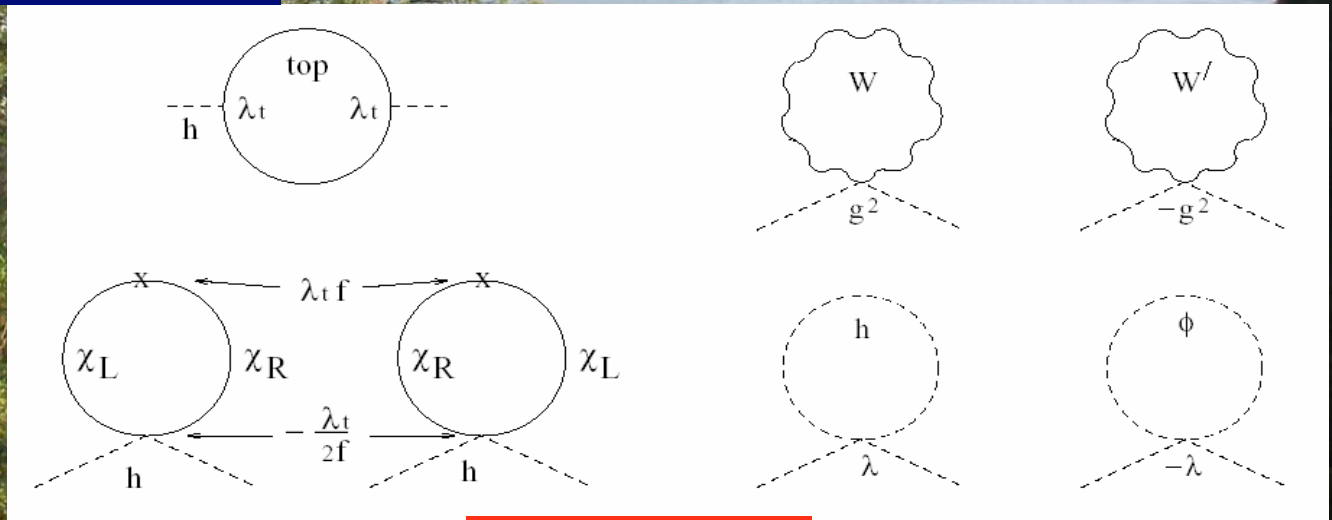
# Generic Little Higgs Spectrum



## Loop cancellation mechanisms



Supersymmetry



Little Higgs

# Higgsless Models?

- Four-dimensional versions:

Strong WW scattering @ TeV, incompatible with precision data?

- Break EW symmetry by boundary conditions in extra dimension:

delay strong WW scattering to  $\sim 10$  TeV?

Kaluza-Klein modes:  $m_{\text{KK}} > 300$  GeV?

compatibility with precision data?

- Warped extra dimension + brane kinetic terms?

Lightest KK mode @ 300 GeV, strong WW @ 6-7 TeV

# The Large Hadron Collider (LHC)

Proton-Proton Collider

7 TeV + 7 TeV



1,000,000,000 collisions/second

Total energy over 14,000 proton masses

Primary targets:

- Origin of mass
- Nature of Dark Matter
- Primordial Plasma
- Matter vs Antimatter



# LHC Progress Dashboard

## Main dipoles

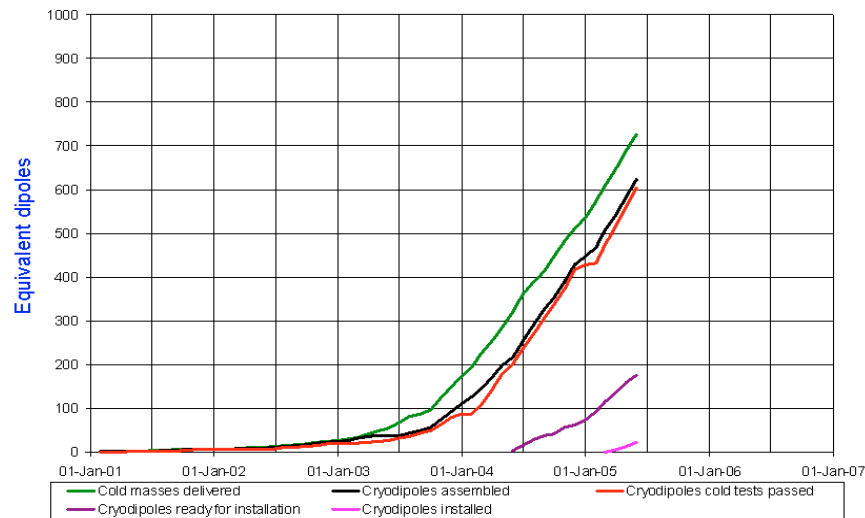
## Cryogenic line



LHC Progress Dashboard



Cryodipole overview



Updated 31 May 2005

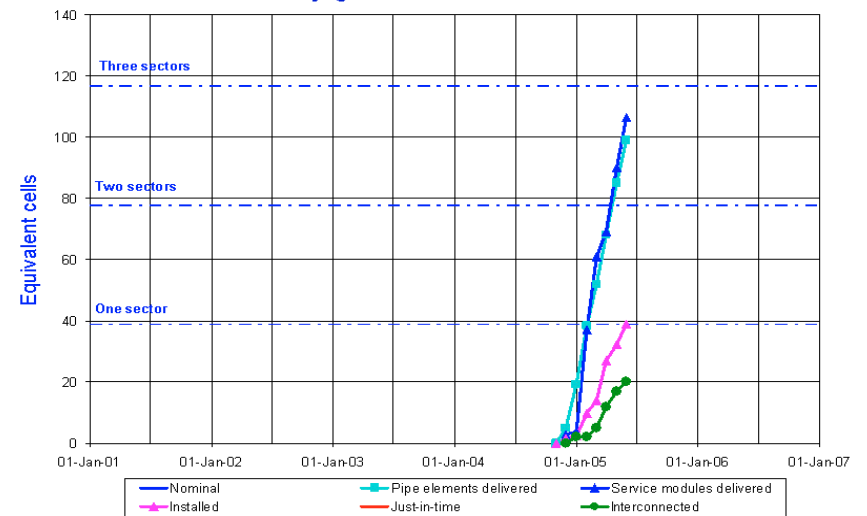
Data provided by D. Tommasini AT-MAS



LHC Progress Dashboard



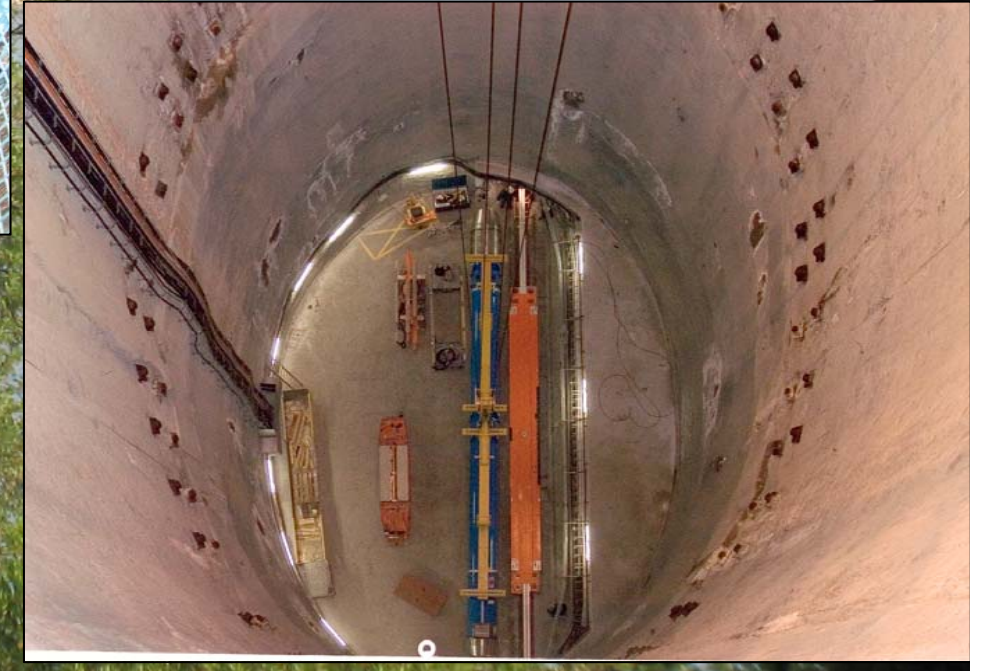
Cryogenic distribution line



Updated 31 May 2005

Data provided by G. Riddone AT-ACR

# The First Magnets are in the Tunnel

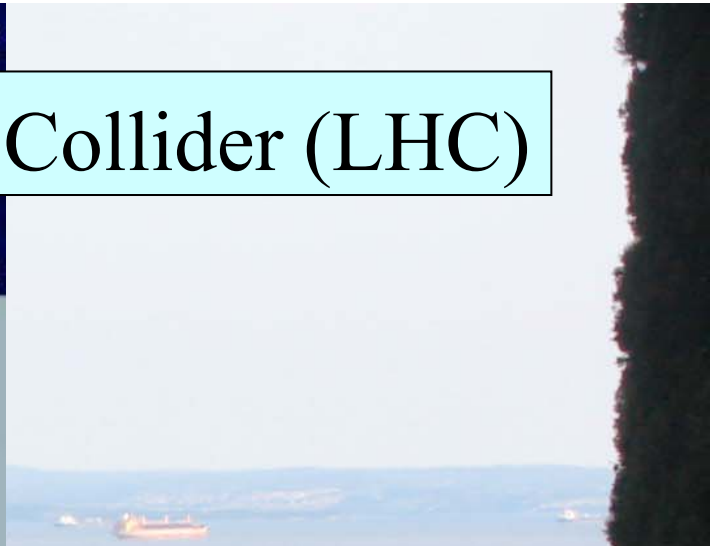
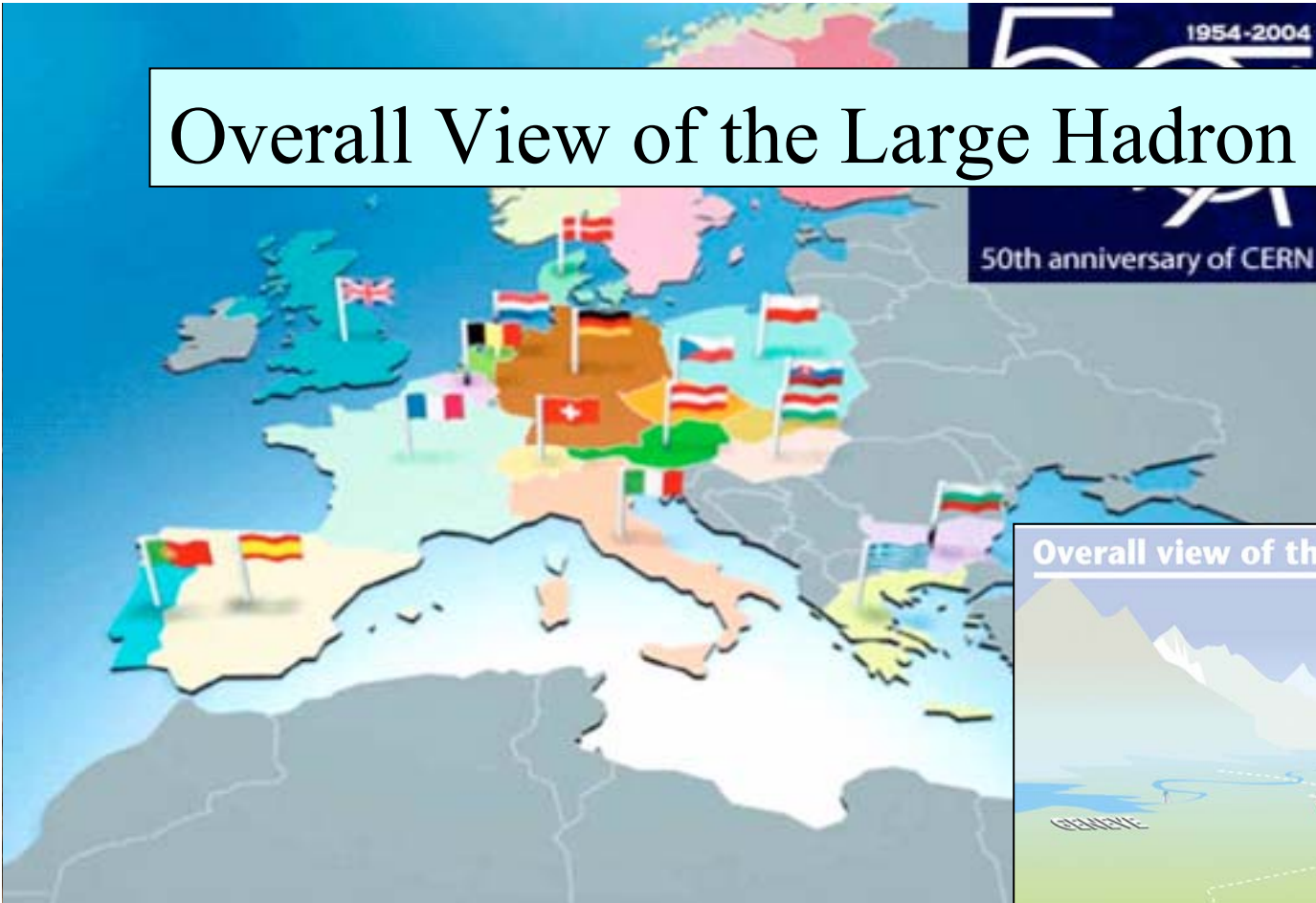




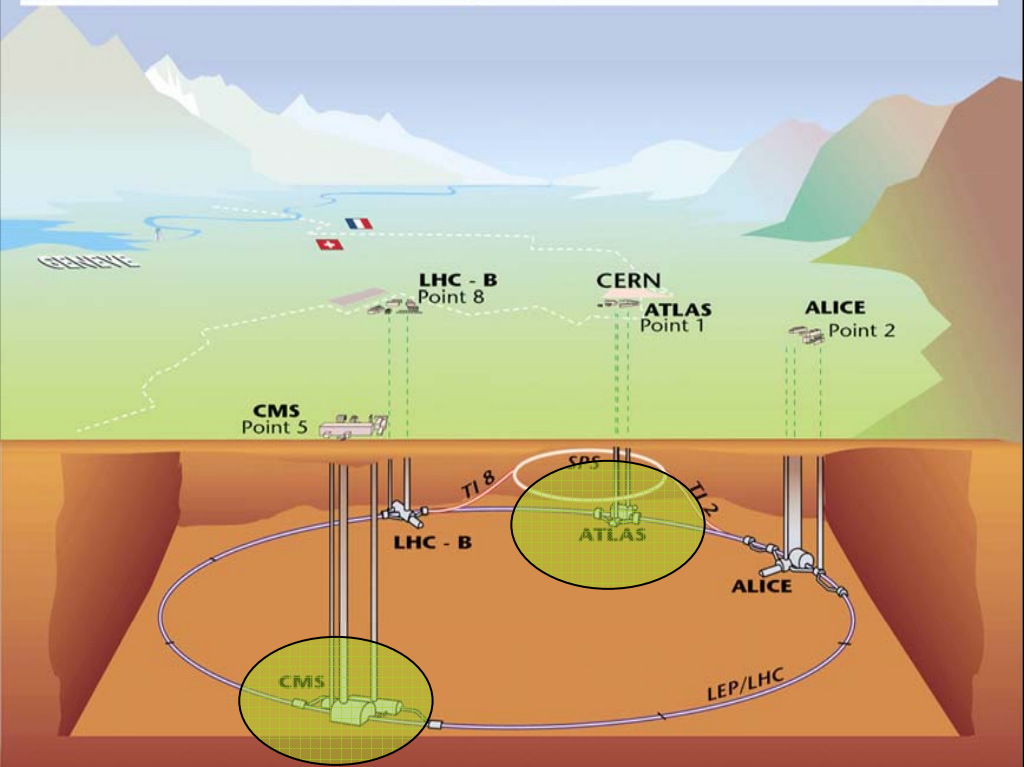
# Installation of the First LHC Magnets



# Overall View of the Large Hadron Collider (LHC)



Overall view of the LHC experiments.



# CMS Experiment

36 Nations, 160 Institutions, 2008 Scientists and Engineers (November 2003)

## TRIGGER & DATA ACQUISITION

Austria, CERN, Finland, France, Greece, Hungary, Italy, Korea, Poland, Portugal, Switzerland, UK, USA

## TRACKER

Austria, Belgium, CERN, Finland, France, New Zealand, Germany, Italy, Japan\*, Switzerland, UK, USA

## CRYSTAL ECAL

Belarus, CERN, China, Croatia, Cyprus, France, Ireland, Italy, Japan\*, Portugal, Russia, Serbia, Switzerland, UK, USA

## PRESHOWER

Armenia, Belarus, CERN, Greece, India, Russia, Taipei, Uzbekistan

## RETURN YOKE

Barrel: Czech Rep., Estonia, Germany, Greece, Russia  
Endcap: Japan\*, USA, Brazil

## SUPERCONDUCTING MAGNET

All countries in CMS contribute to Magnet financing in particular:  
Finland, France, Italy, Japan\*, Korea, Switzerland, USA

FEET  
Pakistan, China

## FORWARD CALORIMETER

Hungary, Iran, Russia, Turkey, USA

## HCAL

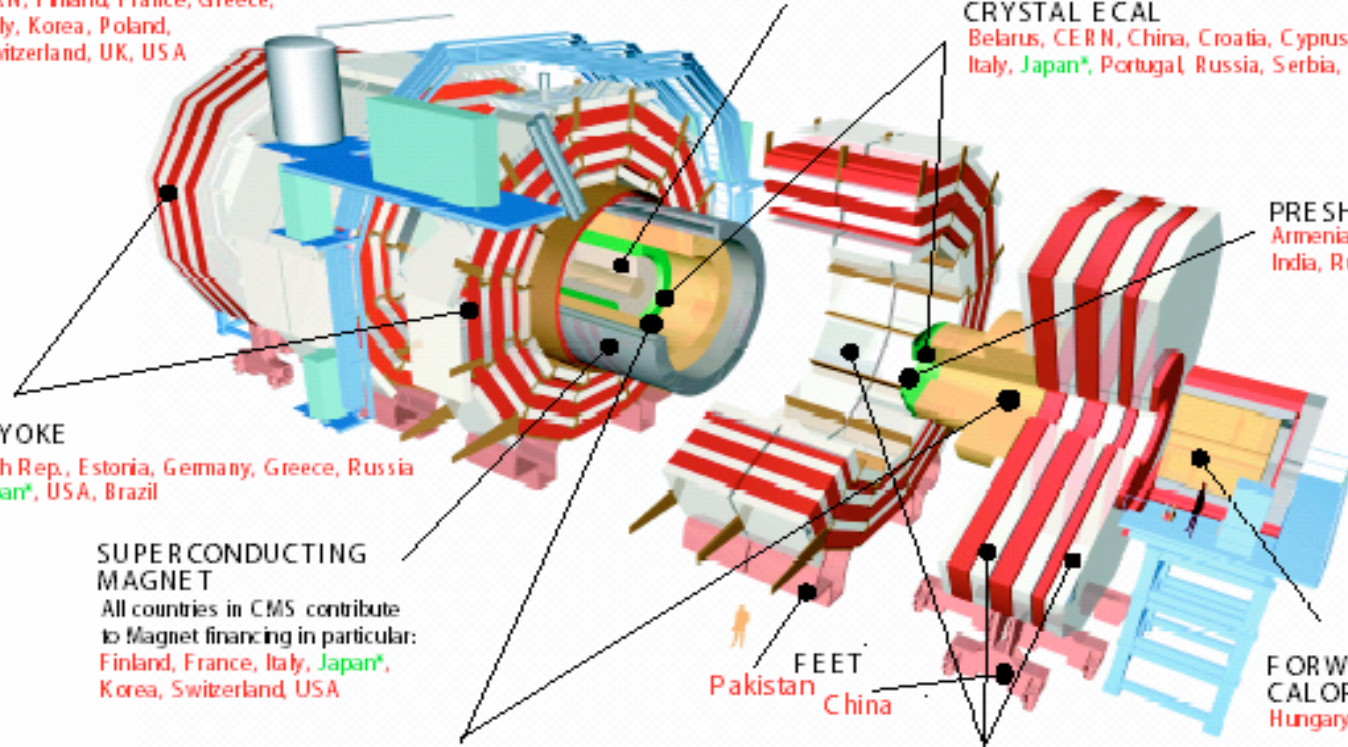
Barrel: Bulgaria, India, Spain\*, USA  
Endcap: Belarus, Bulgaria, Russia, Ukraine  
HO: India

## MUON CHAMBERS

Barrel: Austria, Bulgaria, CERN, China, Germany, Hungary, Italy, Spain  
Endcap: Belarus, Bulgaria, China, Korea, Pakistan, Russia, USA

\* Only through industrial contracts

Total weight : 12500 T  
Overall diameter : 15.0 m  
Overall length : 21.5 m  
Magnetic field : 4 Tesla



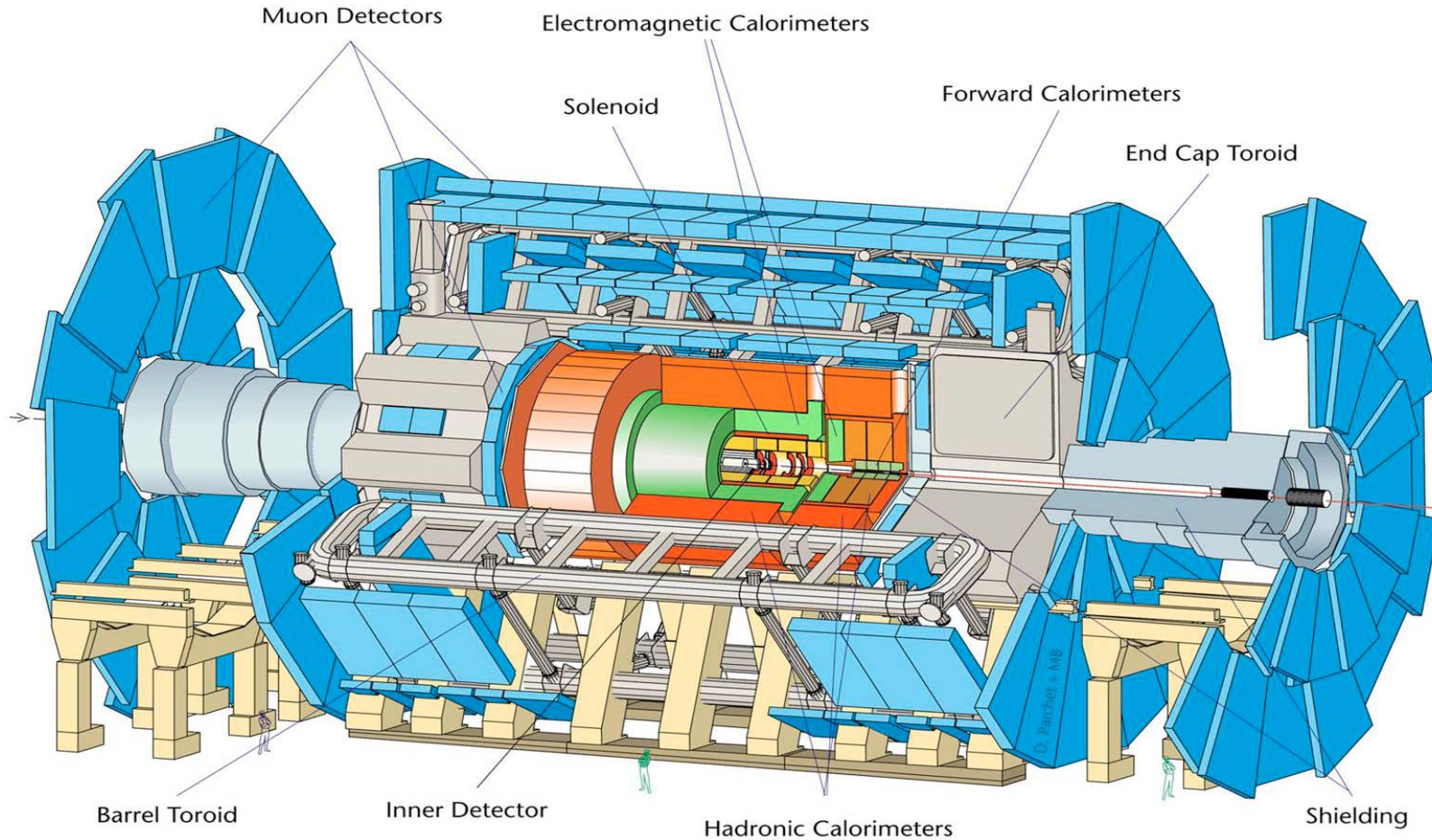
# CMS Under Construction

Recycling Russian naval shells



to be completed in  
2007

# ATLAS Experiment



<b><i>Diameter</i></b>	<b>25 m</b>
<b><i>Barrel toroid length</i></b>	<b>26 m</b>
<b><i>End-cap end-wall chamber span</i></b>	<b>46 m</b>
<b><i>Overall weight</i></b>	<b>7000 Tons</b>

# The ATLAS Cavern



# Huge Statistics thanks to High Energy and Luminosity

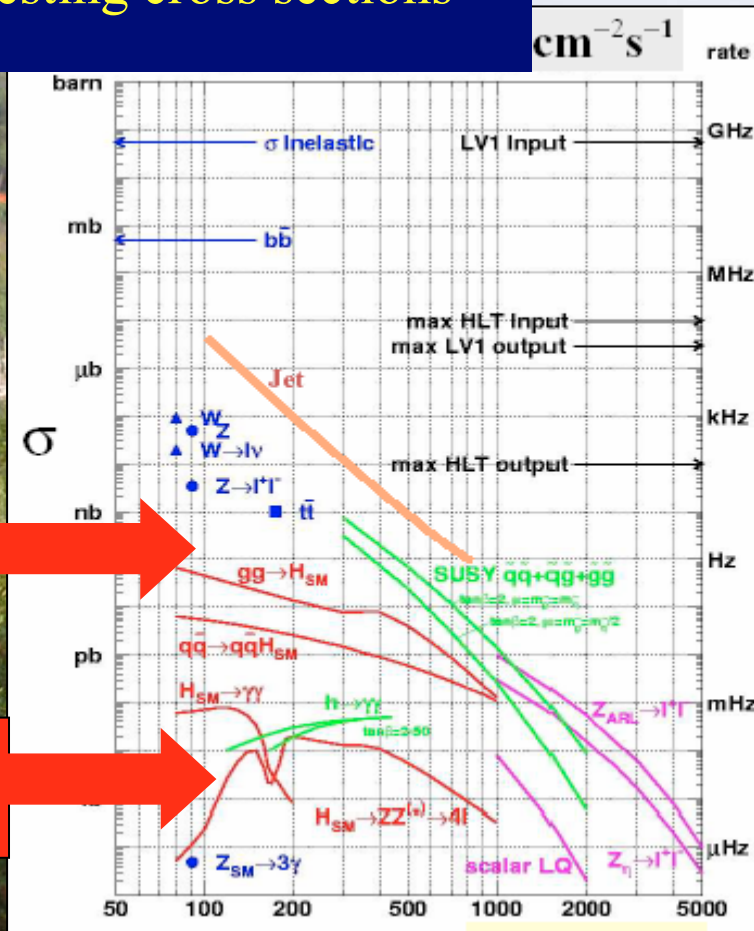
Event rates in ATLAS or CMS at  $L = 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

Process	Events/s	Events per year	Total statistics collected at previous machines by 2007
$W \rightarrow e\nu$	15	$10^8$	$10^4$ LEP / $10^7$ Tevatron
$Z \rightarrow ee$	1.5	$10^7$	$10^7$ LEP
$t\bar{t}$	1	$10^7$	$10^4$ Tevatron
$b\bar{b}$	$10^6$	$10^{12} - 10^{13}$	$10^9$ Belle/BaBar ?
$H$ $m=130 \text{ GeV}$	0.02	$10^5$	?
$\tilde{g}\tilde{g}$ $m=1 \text{ TeV}$	0.001	$10^4$	---
Black holes $m > 3 \text{ TeV}$ ( $M_D=3 \text{ TeV}, n=4$ )	0.0001	$10^3$	---

LHC is a factory for anything: top, W/Z, Higgs, SUSY, etc....  
mass reach for discovery of new particles up to  $m \sim 5 \text{ TeV}$

# The LHC Physics Haystack(s)

## Interesting cross sections



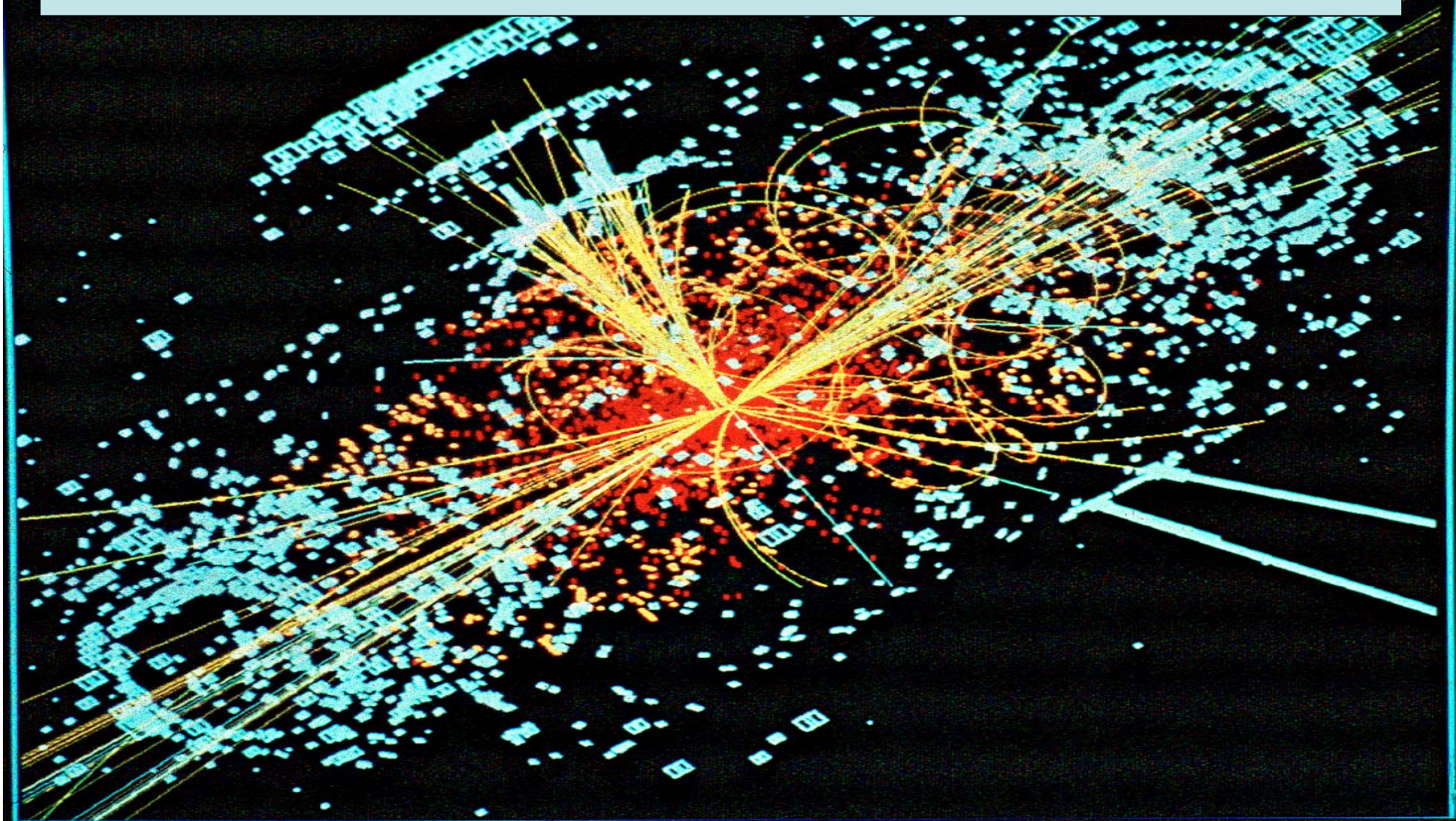
Susy

Higgs

- Cross sections for heavy particles  $\sim 1/(1 \text{ TeV})^2$
- Most have small couplings  $\sim \alpha^2$
- Compare with total cross section  $\sim 1/(100 \text{ MeV})^2$
- Fraction  $\sim 1/1,000,000,000,000$
- Need  $\sim 1,000$  events for signal
- Compare needle  $\sim 1/100,000,000 \text{ m}^3$
- Haystack  $\sim 100 \text{ m}^3$
- Must look in  $\sim 100,000$  haystacks

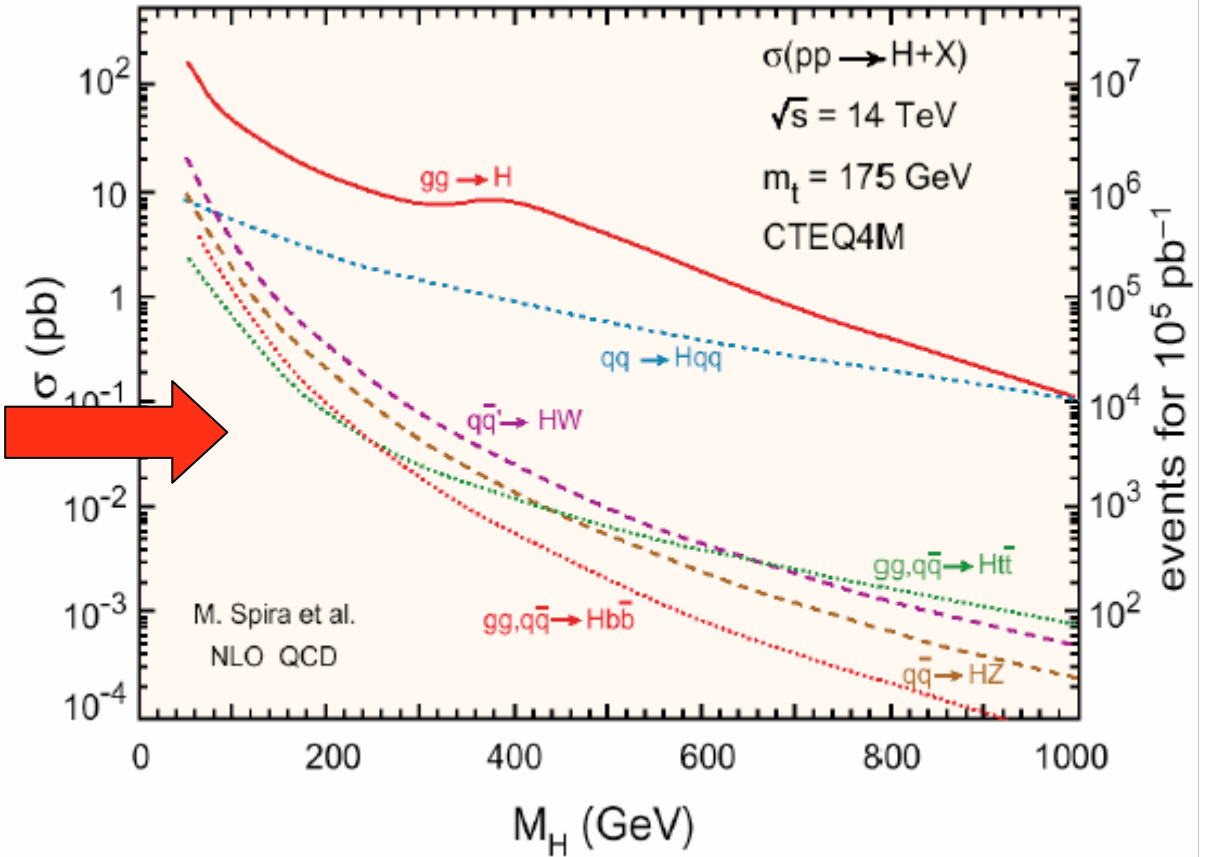
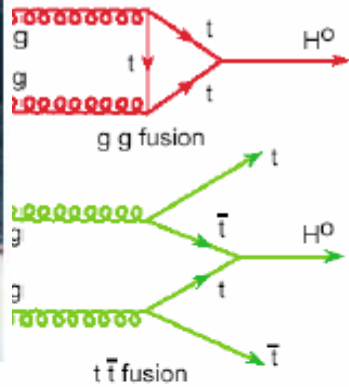
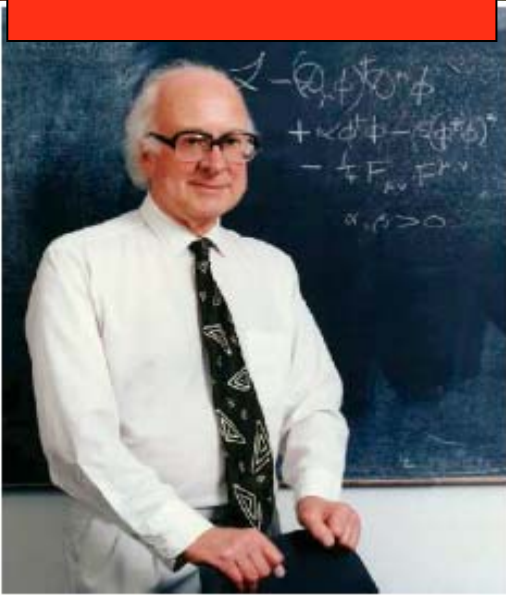


# A Simulated Higgs Event in CMS

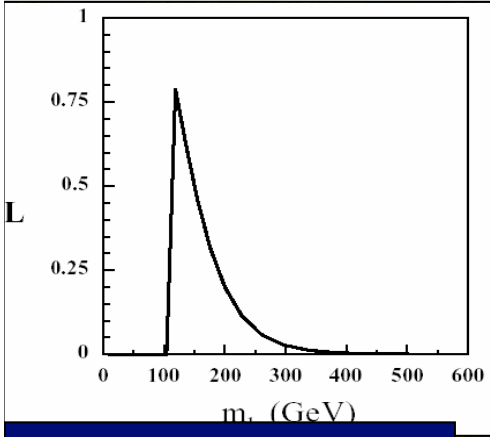
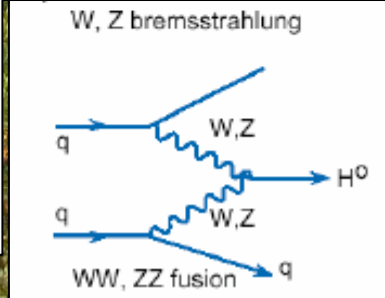


A la recherche du Higgs perdu ...

# Higgs Production at the LHC



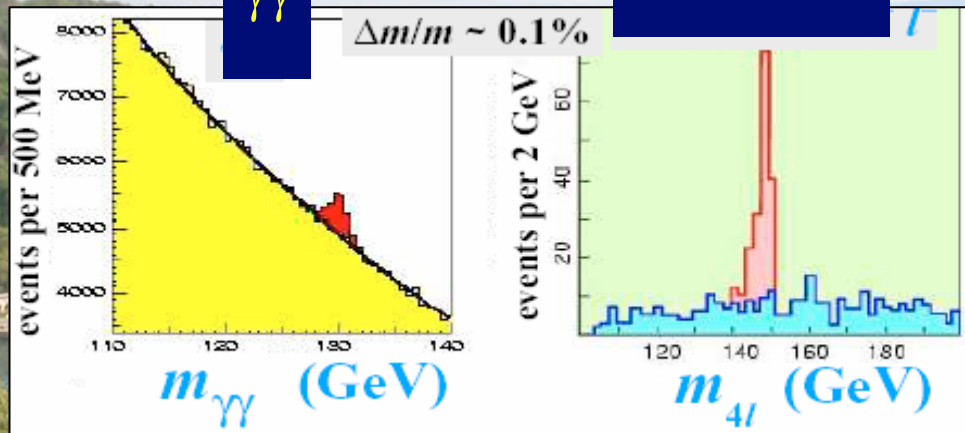
.. not far away?



Combining direct, Indirect information

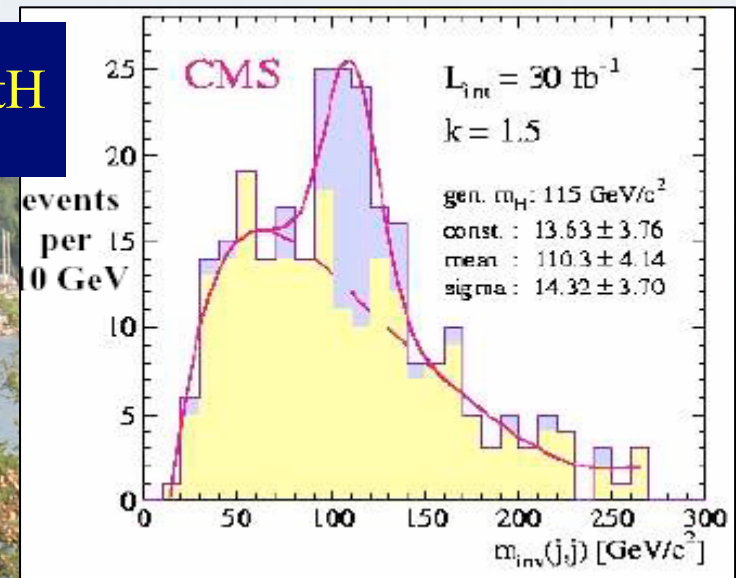
# Some Sample Higgs Signals

$\gamma\gamma$

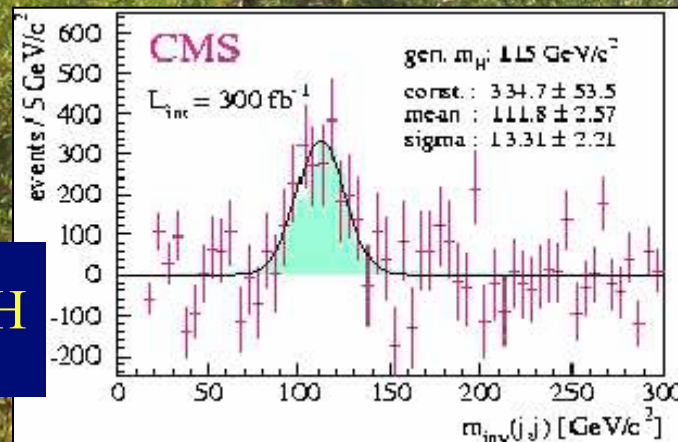


$ZZ^* \rightarrow 4l$

$ttH$



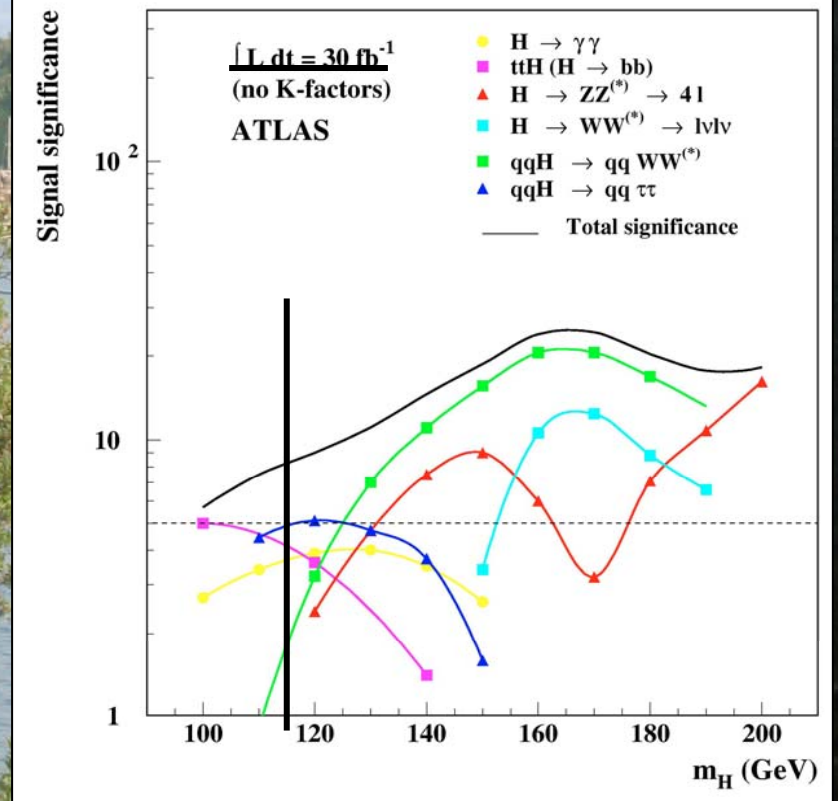
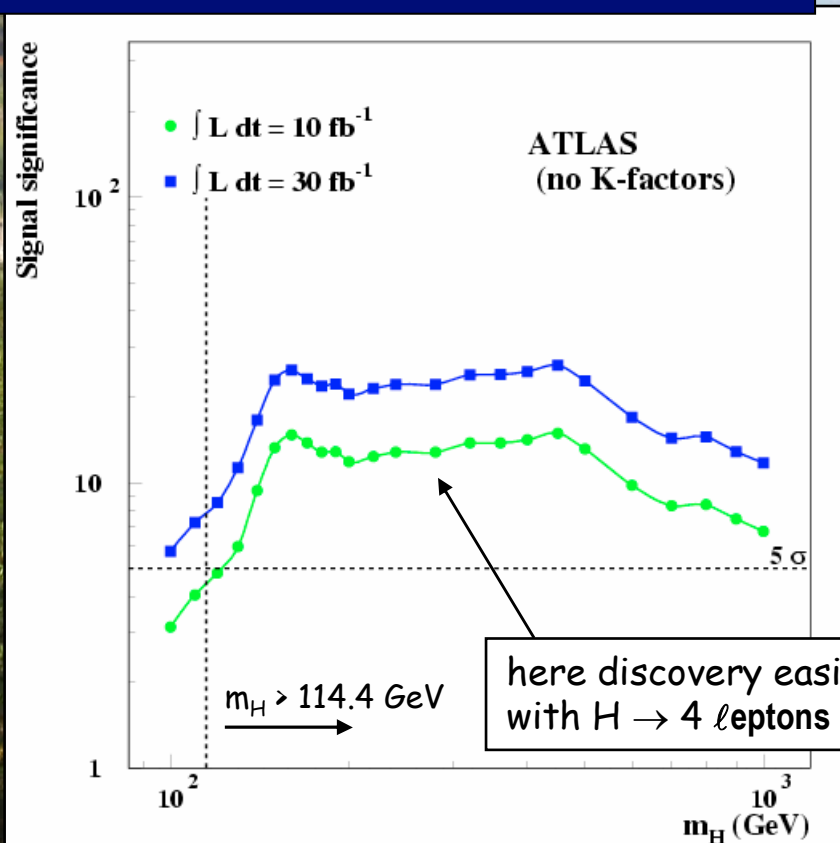
$bbH$



# Higgs Detection at the LHC

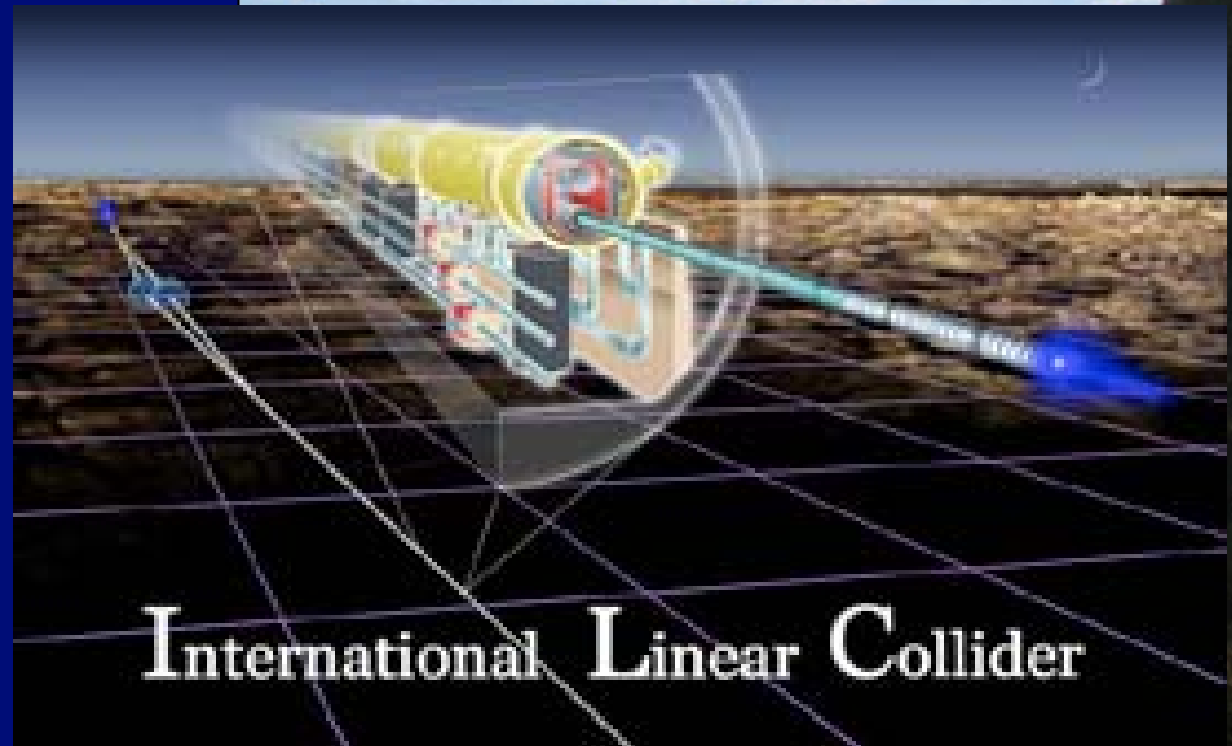
The Higgs may be found quite quickly ...

... in several different channels



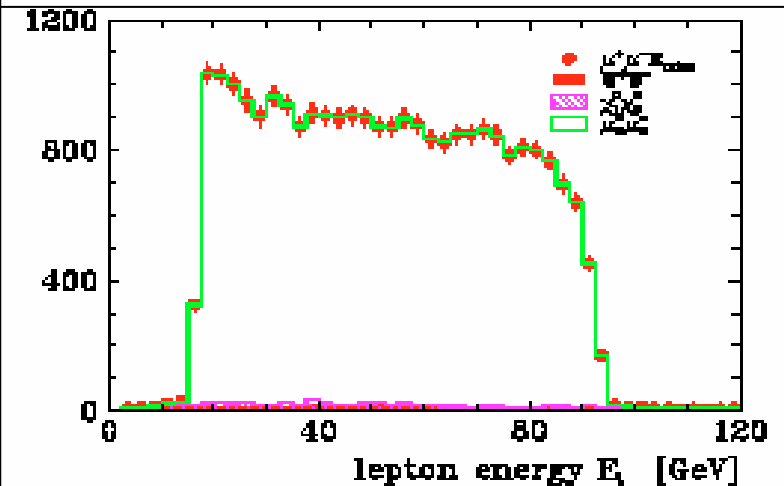
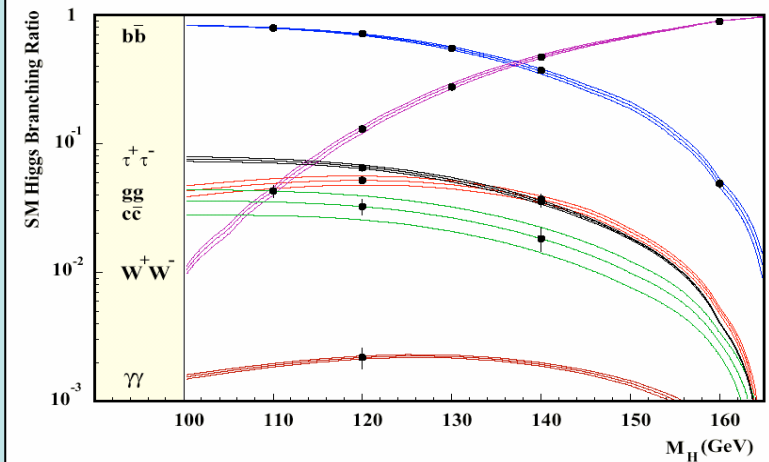
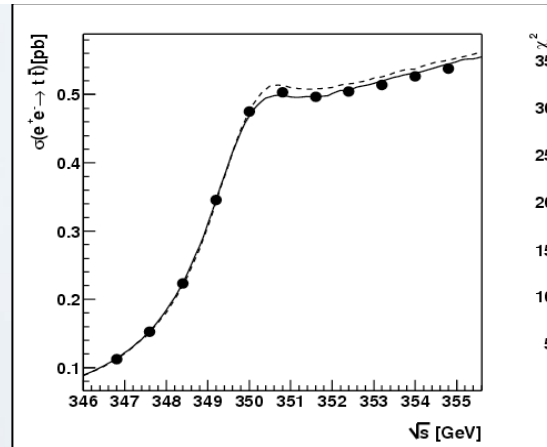
# International Linear Collider

- $e^+e^-$  collisions  
up to  $E_{\text{cm}} = 1 \text{ TeV}$
- Preferred choice  
for next collider
- Now subject of  
Global Design Effort
- Hope for decision  
2010 – 2012
- To be constructed by  
2015 – 2020?



# Tasks for the TeV ILC

- Measure  $m_t$  to  $< \pm 100$  MeV
- If there is a light Higgs of any kind, pin it down:
  - Does it have standard model couplings?
  - What is its precise mass?
- If there are extra light particles:
  - Measure mass and properties
- If LHC sees nothing new below  $\sim 500$  GeV:
  - Look for indirect signatures



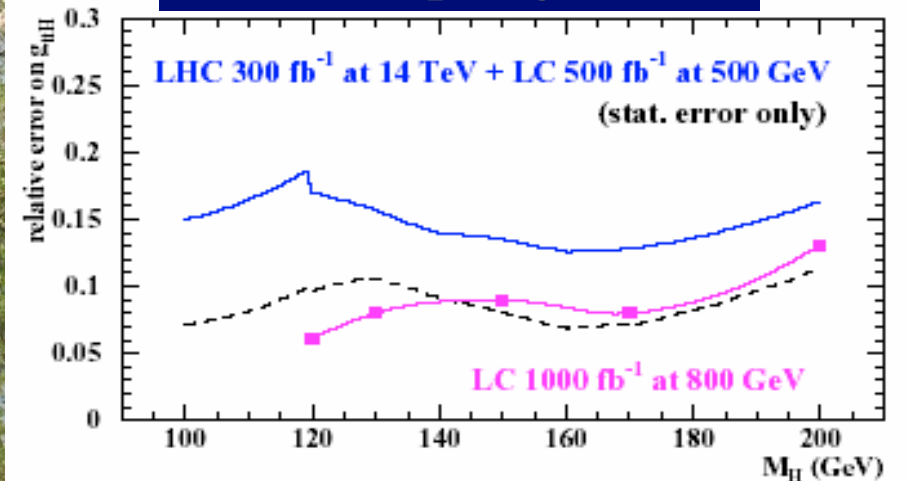
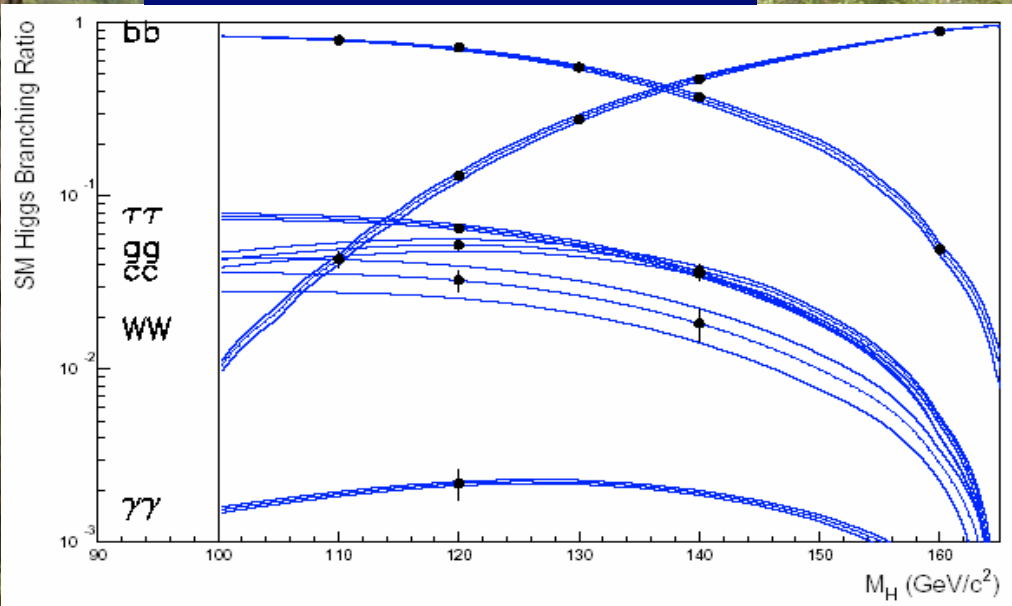
# Measuring Properties of Light Higgs

LC capabilities

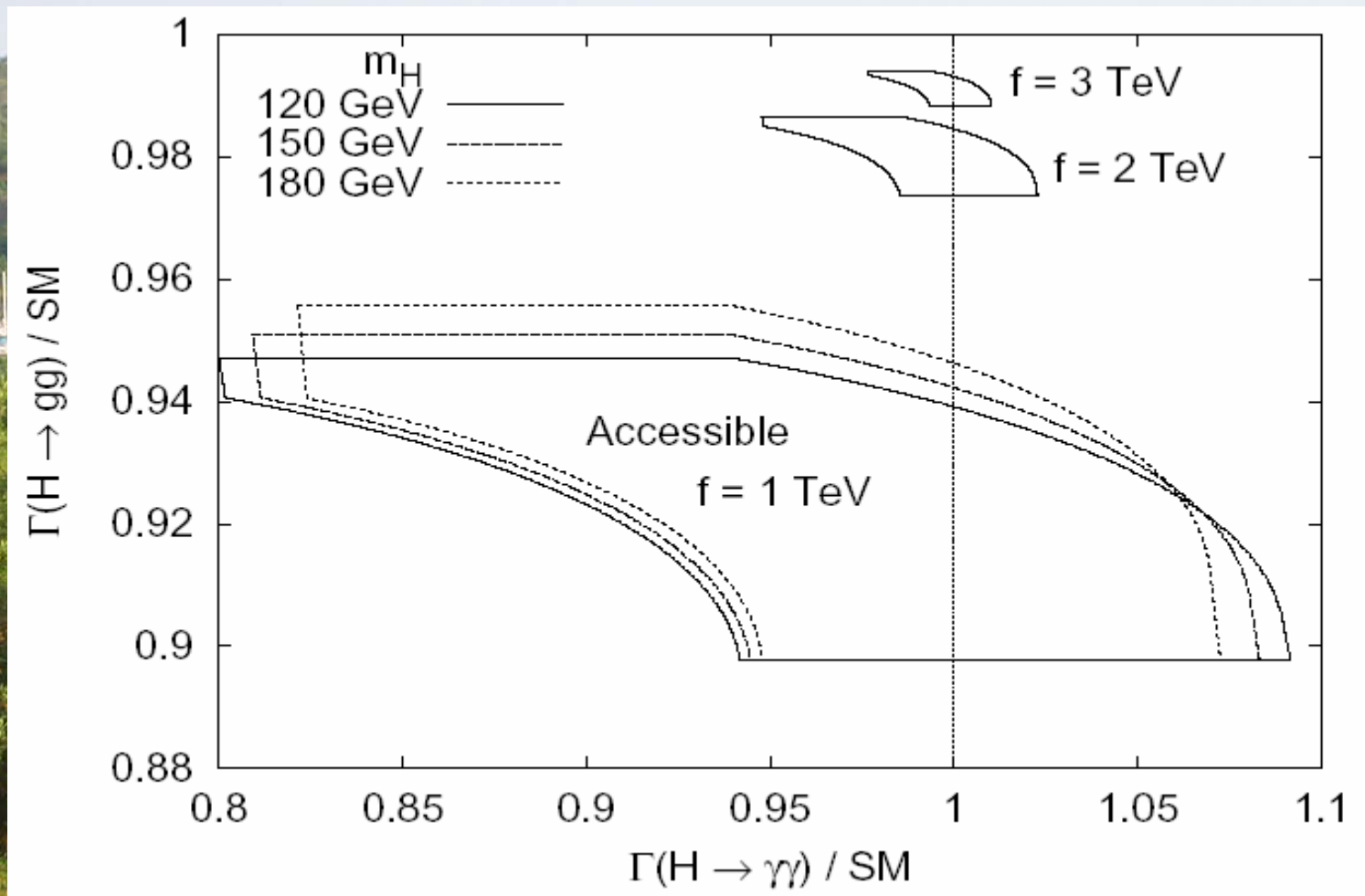
Some new studies ...

$bb, \tau\tau, gg, cc, WW, \gamma\gamma$

Measuring top-Higgs couplings



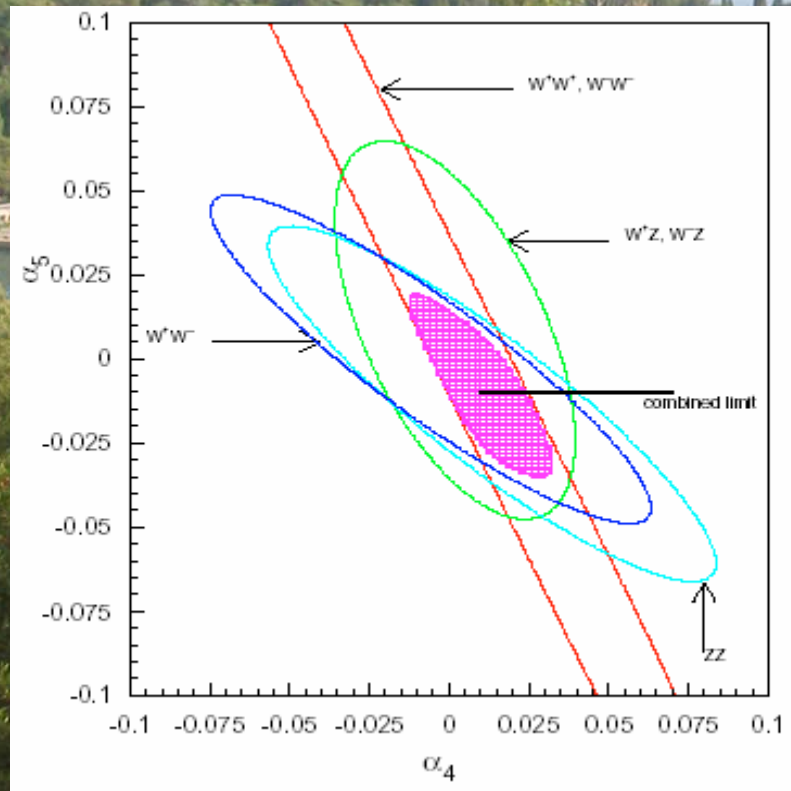
# Measure Little Higgs Decays @ LC



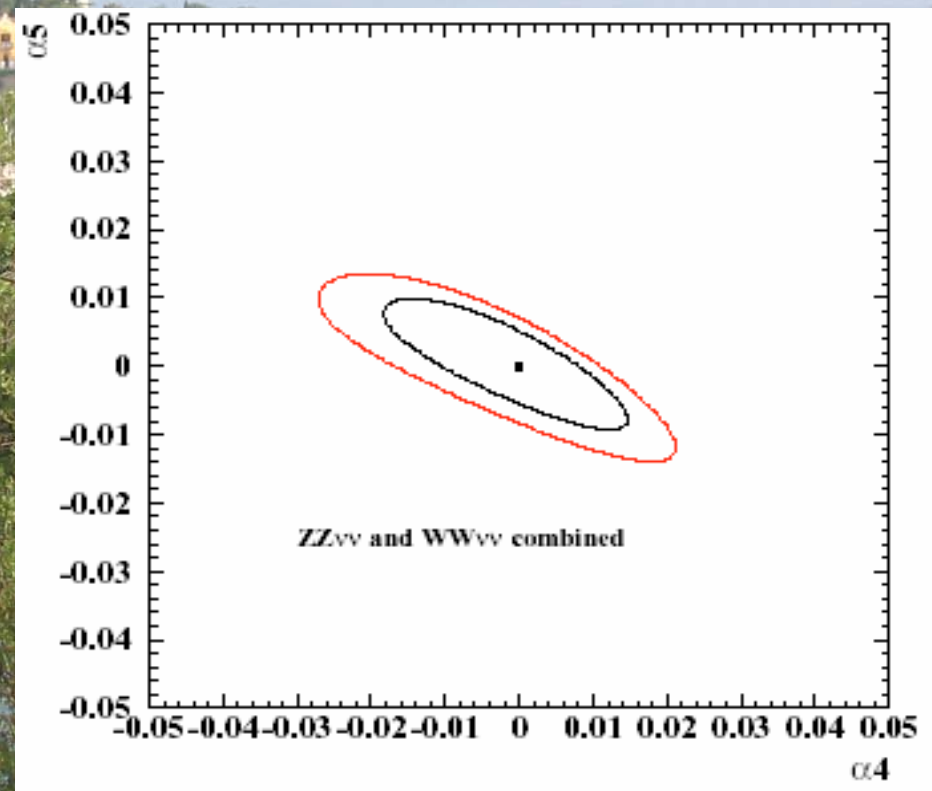


# Sensitivity to Strong WW scattering

@ LHC

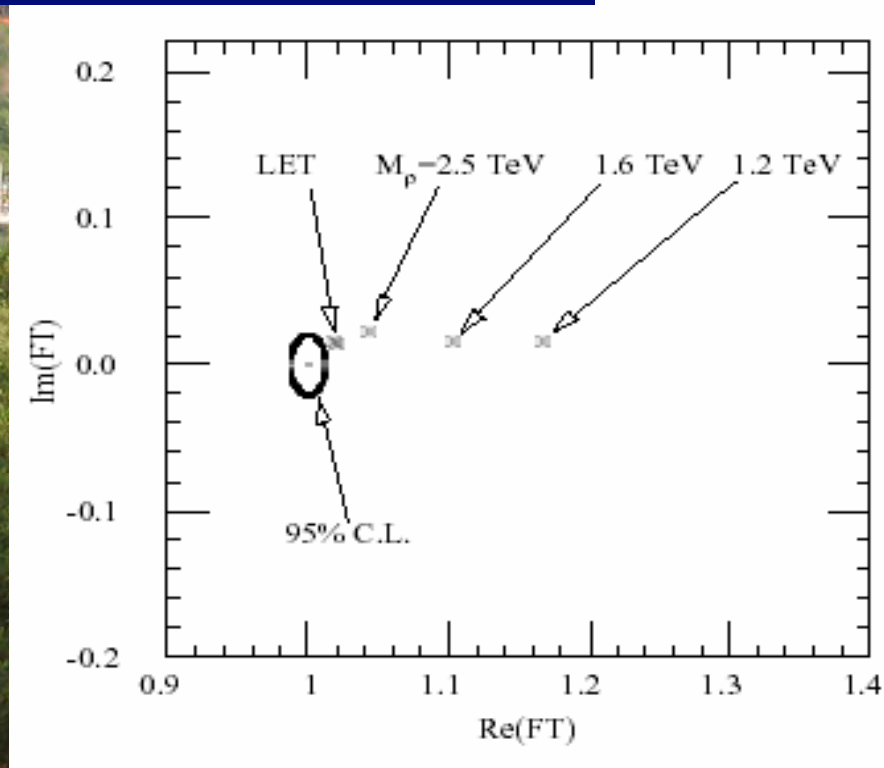


@ 800 GeV LC

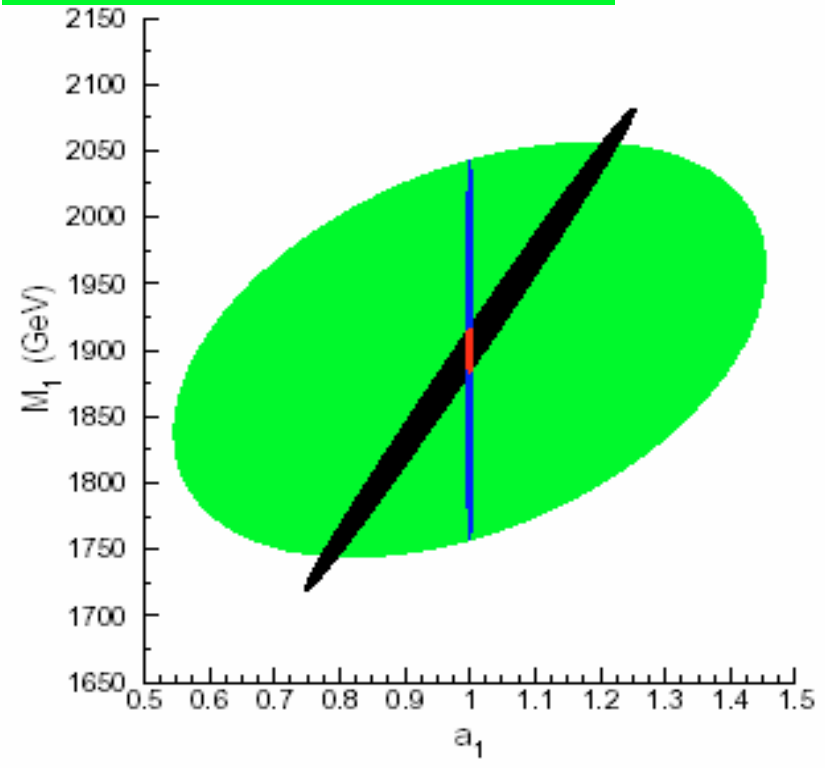


# Measuring a WW Resonance

Form factor measurements  
@ 500 GeV LC

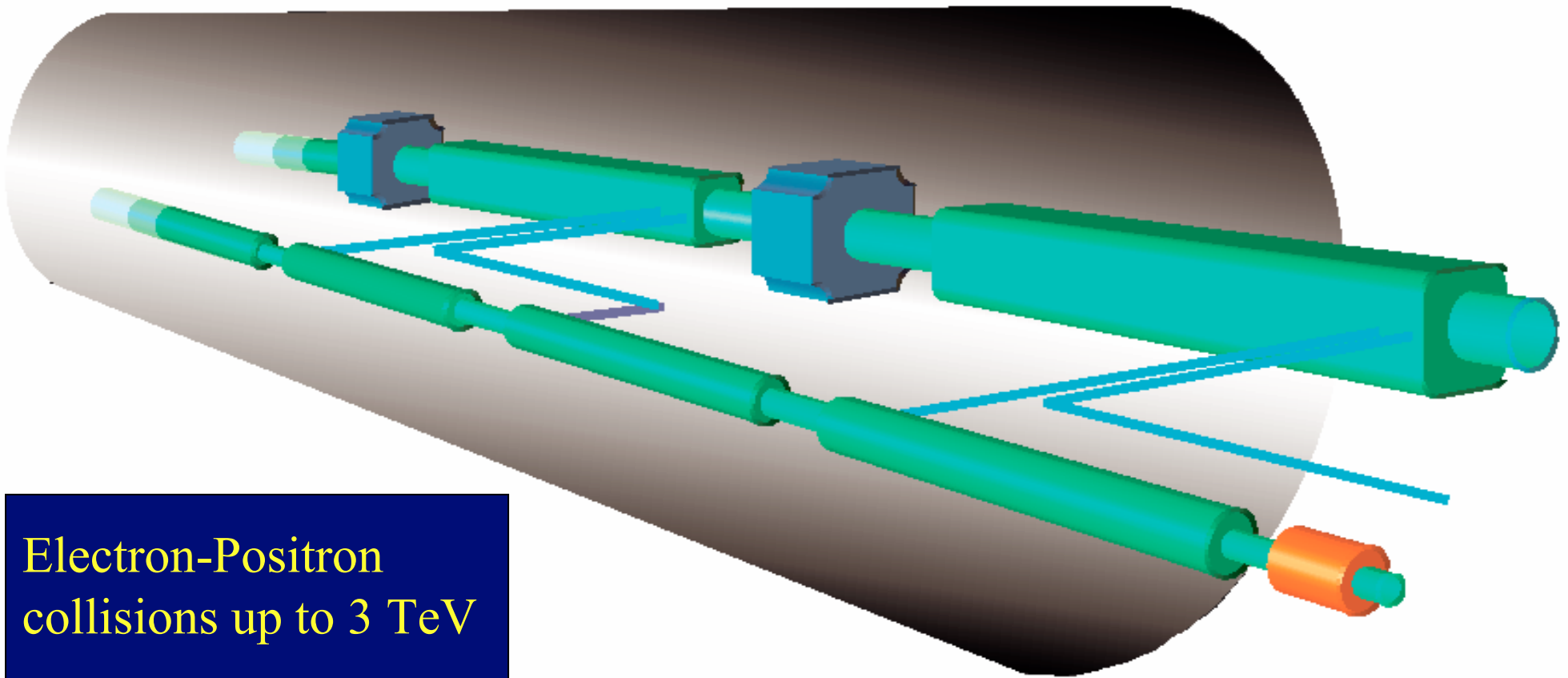


Resonance parameters  
@ LHC



Resonance parameters @ 500 GeV LC

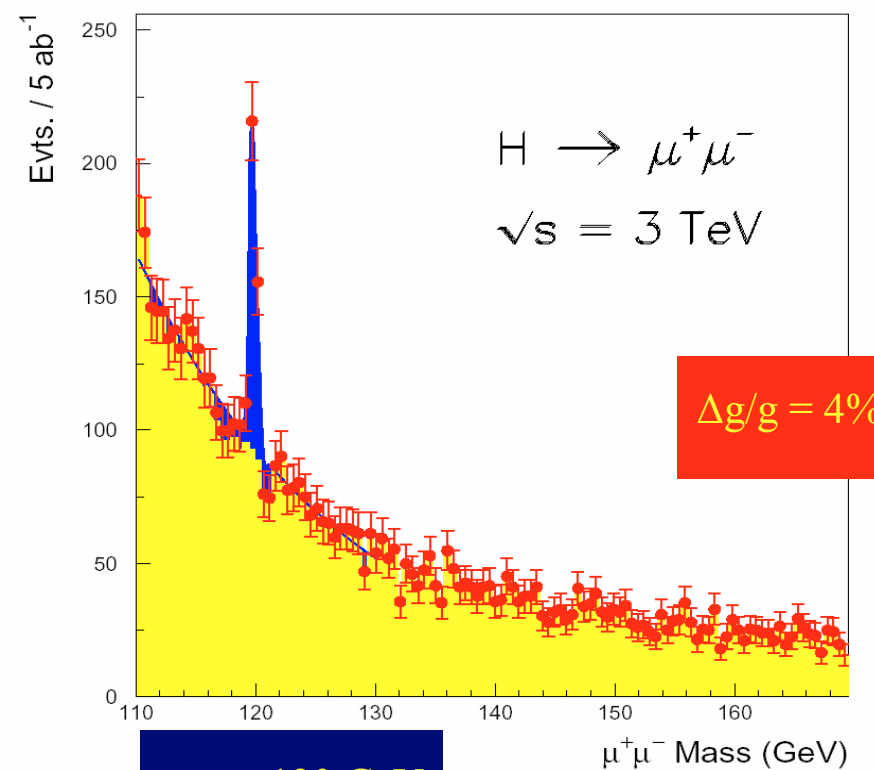
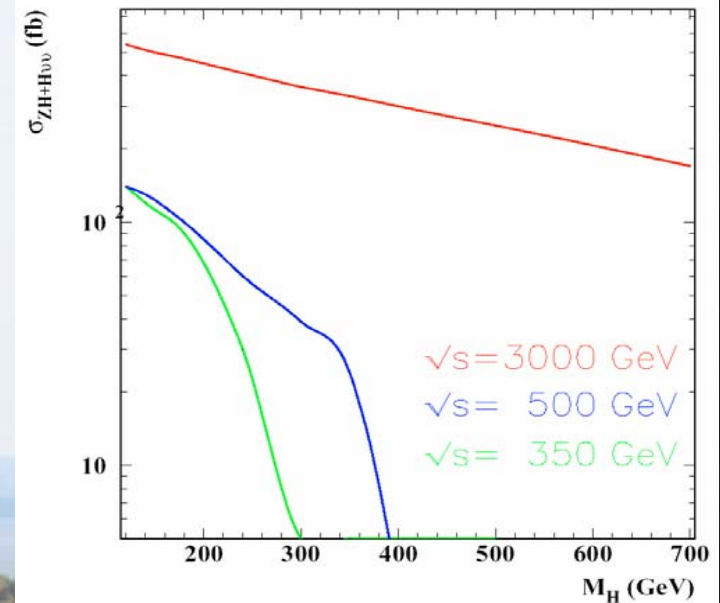
# After LHC @ CERN - CLIC?



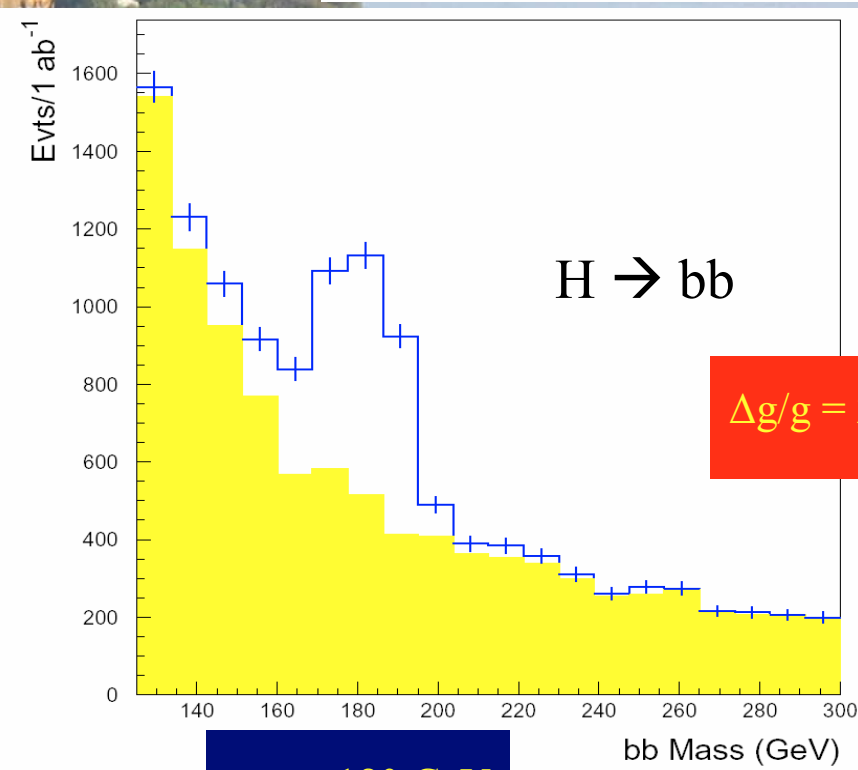
Electron-Positron  
collisions up to 3 TeV

# Advantages of Higher Energy LC

Larger cross section @ 3 TeV  
can measure rare decay modes



$m_H = 120 \text{ GeV}$



$m_H = 180 \text{ GeV}$



# Physics at New Colliders

Lectures at the Summer School on Particle  
Physics

Abdus Salam ICTP, Trieste, June 2005

# Plan of the Lectures

- Status of the Standard Model
- Open issues beyond the Standard Model
- Origin of particle masses
- Search for the Higgs boson
- **Supersymmetry**
- **Searches for supersymmetry**
- Possible other new physics at colliders

# What is Supersymmetry (Susy)?

- Unifies matter and force particles?

- Links fermions and bosons

Exclusion principle vs laser coherence

- Relates particles of different spins

0 -  $\frac{1}{2}$  - 1 -  $\frac{3}{2}$  - 2

Higgs - Electron - Photon - Gravitino - Graviton

- Helps fix masses, unify fundamental forces

# Why Supersymmetry (Susy)?

- **Hierarchy problem: why is  $m_W \ll m_P$  ?**

( $m_P \sim 10^{19}$  GeV is scale of gravity)

- **Alternatively, why is**

$$G_F = 1/m_W^2 \gg G_N = 1/m_P^2 ?$$

- **Or, why is**

$$V_{\text{Coulomb}} \gg V_{\text{Newton}} ? \quad e^2 \gg G m^2 = m^2 / m_P^2$$

- **Set by hand? What about loop corrections?**

$$\delta m_{H,W}^2 = O(\alpha/\pi) \Lambda^2$$

- **Cancel boson loops  $\leftrightarrow$  fermions**

- **Need  $|m_B^2 - m_F^2| < 1 \text{ TeV}^2$**



# Loop Corrections to Higgs Mass<sup>2</sup>

- Consider generic fermion and boson loops:



- Each is quadratically divergent:  $\int^{\Lambda} d^4k/k^2$

$$\Delta m_H^2 = -\frac{y_f^2}{16\pi^2} [2\Lambda^2 + 6m_f^2 \ln(\Lambda/m_f) + \dots]$$

$$\Delta m_H^2 = \frac{\lambda_S}{16\pi^2} [\Lambda^2 - 2m_S^2 \ln(\Lambda/m_S) + \dots]$$

- Leading divergence cancelled if

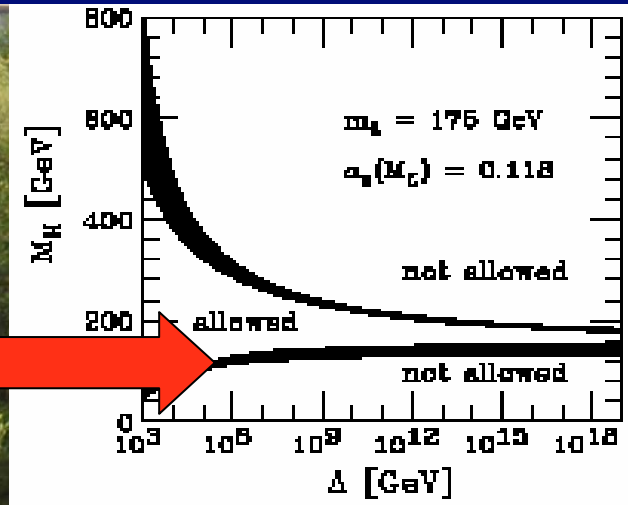
$$\lambda_S = y_f^2$$

# Other Reasons to like Susy

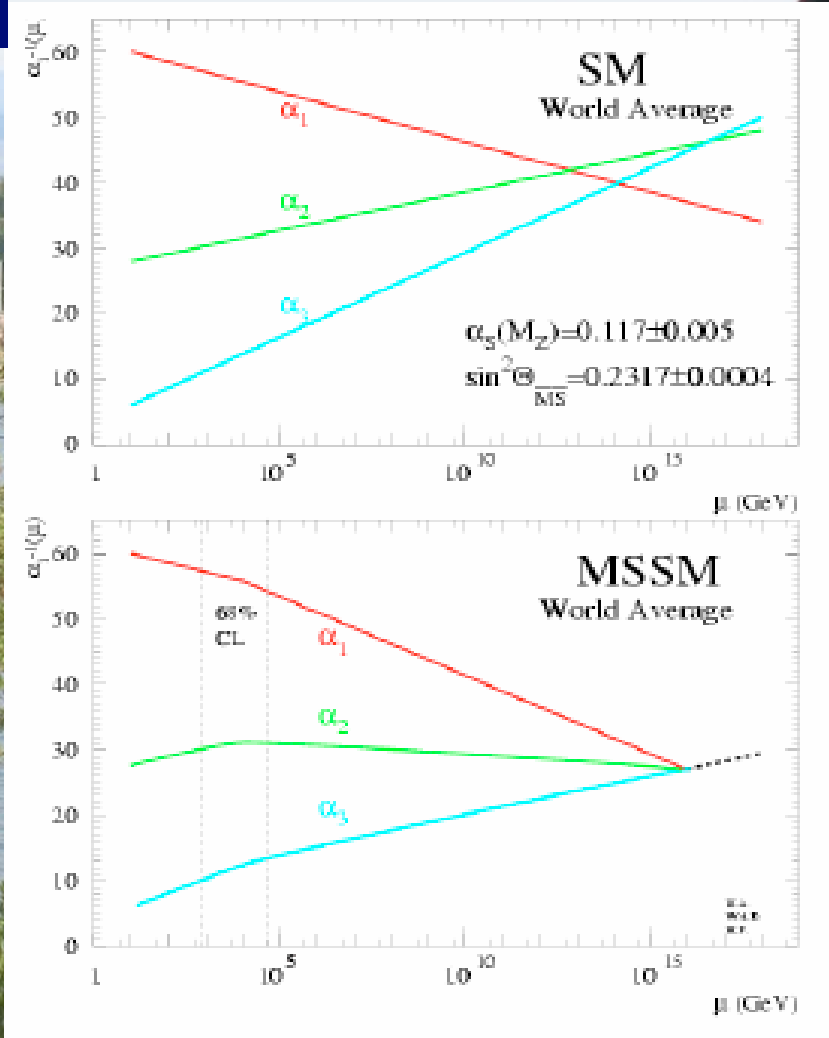
It enables the gauge couplings to unify

It predicts  $m_H < 150 \text{ GeV}$

It stabilizes the Higgs potential for low masses



Approved by Fabiola Gianotti



# Dark Matter in the Universe

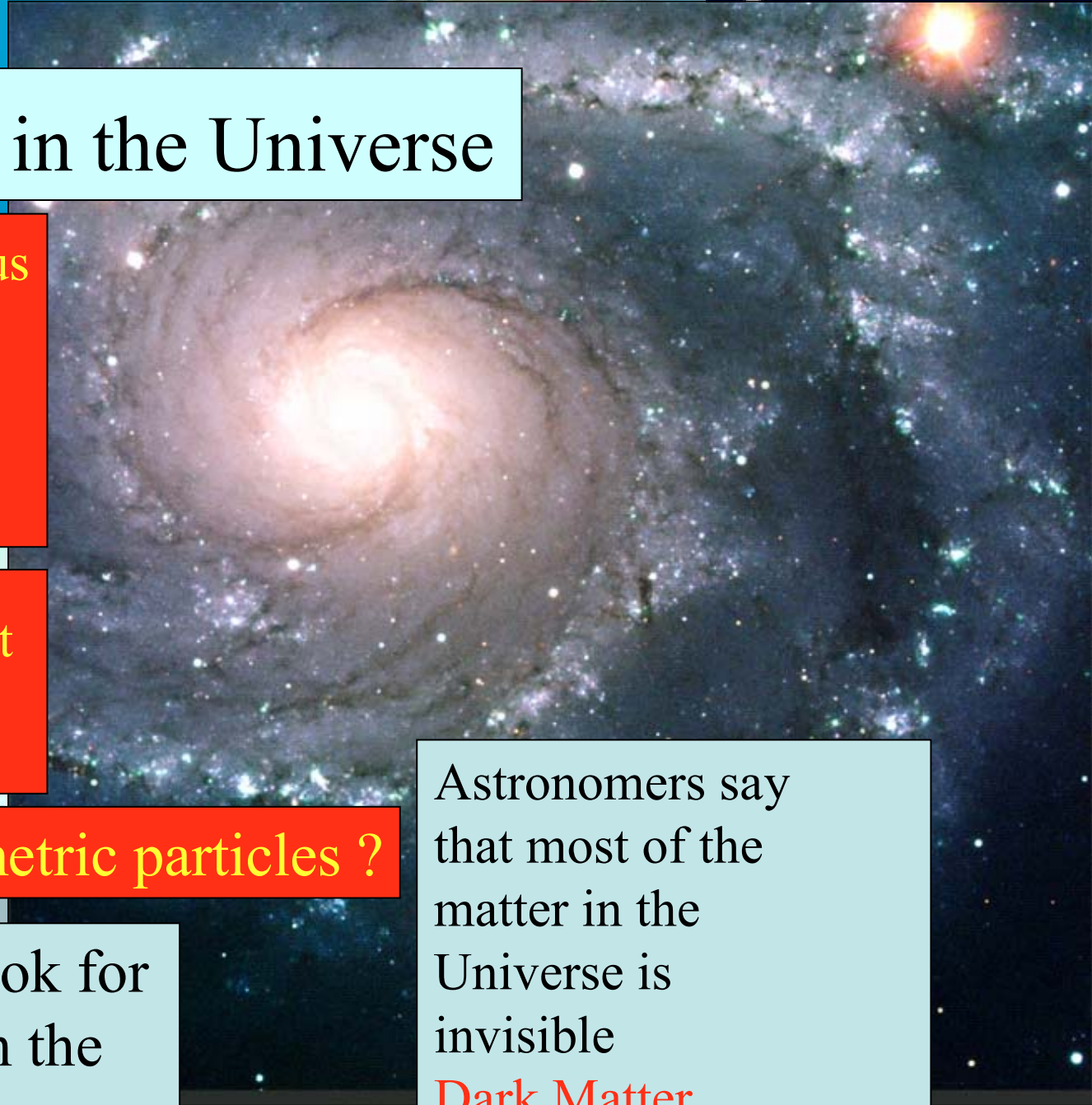
Astronomers tell us  
that most of the  
matter in the  
universe is  
invisible

We will look for it  
with the LHC

Lightest Supersymmetric particles ?

We shall look for  
them with the  
**LHC**

Astronomers say  
that most of the  
matter in the  
Universe is  
invisible  
**Dark Matter**



# Supersymmetry Algebra

- Simply stated:

$$\begin{aligned} Q|Boson\rangle &= |Fermion\rangle \\ Q|Fermion\rangle &= |Boson\rangle \end{aligned}$$

- Spinorial charges obey algebra:

$$\begin{aligned} [P^\mu, Q_\alpha] &= 0 = [P^\mu, \bar{Q}^{\dot{\alpha}}] \\ \{Q_\alpha, \bar{Q}_{\dot{\beta}}\} &= 2(\sigma_\mu)_{\alpha\dot{\beta}} P^\mu \\ \{Q_\alpha, Q_\beta\} &= \{\bar{Q}^{\dot{\alpha}}, \bar{Q}^{\dot{\beta}}\} = 0 \end{aligned}$$

- Only possible symmetry of S-matrix that combines particles of different spins
- Supermultiplets: chiral (0, 1/2), vector (1/2, 1)

# Simplest Supersymmetric Field Theory

- Free scalar boson and free spin-1/2 fermion:

$$S = \int d^4x \mathcal{L}_{\text{scalaire}} + \mathcal{L}_{\text{fermion}}$$
$$\mathcal{L}_{\text{scalaire}} = -\partial^\mu \phi \partial_\mu \phi^*$$
$$\mathcal{L}_{\text{fermion}} = -i\psi^\dagger \bar{\sigma}^\mu \partial_\mu \psi$$

- Transform boson to fermion:

$$\delta\phi = \epsilon^\alpha \psi_\alpha \quad \text{et} \quad \delta\phi^* = \bar{\epsilon}_{\dot{\alpha}} \bar{\psi}^{\dot{\alpha}}$$
$$\Rightarrow \delta\mathcal{L}_{\text{scalaire}} = -\epsilon^\alpha (\partial^\mu \psi_\alpha) \partial_\mu \phi^* - \partial^\mu \phi \bar{\epsilon}_{\dot{\alpha}} (\partial_\mu \bar{\psi}^{\dot{\alpha}})$$

- Fermion to boson:  $\delta\psi_\alpha = i(\sigma^\mu \epsilon^\dagger)_\alpha \partial_\mu \phi$  et  $\delta\bar{\psi}^{\dot{\alpha}} = -i(\epsilon \sigma^\mu)^{\dot{\alpha}} \partial_\mu \phi^*$

- Lagrangian changes by total derivative: action  $A = \int d^4x L(x)$  invariant

- Supersymmetry:  $QQ = P$   $\phi \rightarrow \psi \rightarrow \partial\phi, \quad \psi \rightarrow \partial\phi \rightarrow \partial\psi$

# Supersymmetry with Interactions

- General form:  $L = L_0 - V(\phi^i, \phi_j^*) - \frac{1}{2} M_{ij}(\phi, \phi^*) \bar{\psi}^{ci} \psi^j$

- Variation includes:  $\frac{\partial M}{\partial \phi^*} \psi^* \bar{\psi}^c \psi$   $\frac{\partial M_{ij}}{\partial \phi^k} \bar{E} \psi^k \bar{\psi}^{ci} \psi^j$

- Cannot cancel, so  $M = M(\phi)$  symmetric  $M_{ij} = \frac{\partial W}{\partial \phi^i \partial \phi^j}$

- Cancel variation in potential:

$$\frac{\partial V}{\partial \phi^i} \bar{E} \psi^I + (\text{Herm. Conj.}) \rightarrow V = \left| \frac{\partial W}{\partial \phi^i} \right|^2$$

- Final form:

$$L = i \bar{\psi}_i \gamma_\mu \partial^\mu \psi^i + |\partial_\mu \phi^i|^2 - \left| \frac{\partial W}{\partial \phi^i} \right|^2 - \frac{1}{2} \frac{\partial^2 W}{\partial \phi^i \partial \phi^j} \bar{\psi}^{ci} \partial \psi^j + (\text{Herm. Conj.})$$

- Simple case:

$$W = \frac{\lambda}{3} \phi^3 + \frac{m}{2} \phi^2$$

$$L = i \bar{\psi} \gamma_\mu \partial^\mu \psi + |\partial_\mu \phi|^2 - |m\phi + \lambda\phi^2|^2 - m \bar{\psi}^c \psi - \lambda \phi \bar{\psi}^c \psi$$

# More Supersymmetric Field Theories

- Gauge bosons + adjoint spin-1/2 fermions = supersymmetric gauge theory

- Effective potential fixed by Yukawa, gauge couplings:  $V = g^2 \phi^2 \phi^{*2} + y^2 \phi^2 \phi^{*2}$

→ prediction for Higgs mass

$m_h < m_Z$  at tree level, loops

$$\delta m_h^2 \propto \frac{m_t^4}{m_W^2} \ln \left( \frac{m_{\tilde{t}}^2}{m_t^2} \right) + \dots$$

- Graviton minimally coupled to spin-3/2 fermion = supergravity

# Minimal Supersymmetric Extension of Standard Model (MSSM)

- Particles + spartners

$$\begin{pmatrix} \frac{1}{2} \\ 0 \end{pmatrix} \text{ e.g., } \begin{pmatrix} \ell \text{ (lepton)} \\ \tilde{\ell} \text{ (slepton)} \end{pmatrix} \text{ or } \begin{pmatrix} q \text{ (quark)} \\ \tilde{q} \text{ (squark)} \end{pmatrix} \begin{pmatrix} 1 \\ \frac{1}{2} \end{pmatrix} \text{ e.g., } \begin{pmatrix} \gamma \text{ (photon)} \\ \tilde{\gamma} \text{ (photino)} \end{pmatrix} \text{ or } \begin{pmatrix} g \text{ (gluon)} \\ \tilde{g} \text{ (gluino)} \end{pmatrix}$$

- 2 Higgs doublets, coupling  $\mu$ , ratio of v.e.v.'s =  $\tan \beta$
- Unknown supersymmetry-breaking parameters:  
Scalar masses  $m_0$ , gaugino masses  $m_{1/2}$ ,  
trilinear soft couplings  $A_\lambda$ , bilinear soft coupling  $B_\mu$
- Often assume universality:  
Single  $m_0$ , single  $m_{1/2}$ , single  $A_\lambda, B_\mu$ : not string?
- Called constrained MSSM = **CMSSM**
- Gravitino mass? Minimal supergravity: not string?  
 $m_{3/2} = m_0, B_\mu = A_\lambda - m_0$



# Lightest Supersymmetric Particle

- Stable in many models because of conservation of R parity:

$$R = (-1)^{2S - L + 3B}$$

where S = spin, L = lepton #, B = baryon #

- Particles have R = +1, sparticles R = -1:
  - Sparticles produced in pairs
  - Heavier sparticles  $\rightarrow$  lighter sparticles
- Lightest supersymmetric particle (LSP) stable

# Possible Nature of LSP

- No strong or electromagnetic interactions  
Otherwise would bind to matter  
Detectable as anomalous heavy nucleus
- Possible weakly-interacting candidates  
Sneutrino  
(Excluded by LEP, direct searches)  
Lightest neutralino  $\chi$   
Gravitino  
(nightmare for detection)

# Constraints on Supersymmetry

- Absence of sparticles at LEP, Tevatron

selectron, chargino  $> 100$  GeV

squarks, gluino  $> 250$  GeV

- Indirect constraints

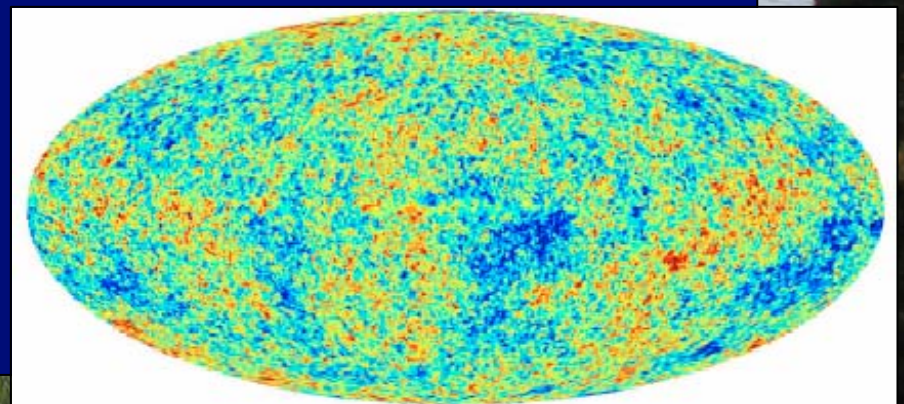
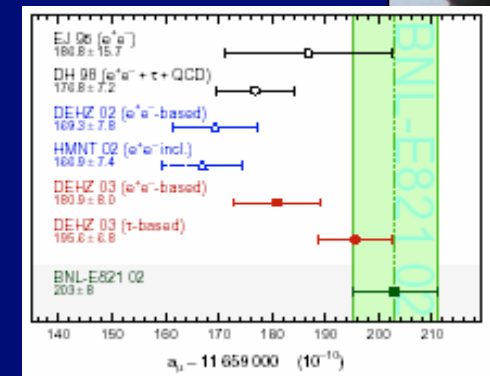
Higgs  $> 114$  GeV,  $b \rightarrow s \gamma$

$g_\mu - 2$

- Density of dark matter

lightest sparticle  $\chi$ :

WMAP:  $0.094 < \Omega_\chi h^2 < 0.124$



# Squark & Gluino Searches @ FNAL

General Squarks & gluinos

- Exclude:  $m(\tilde{q}/\tilde{g}) < 292/333 \text{ GeV}$

- Gluino and Squark mass limits:

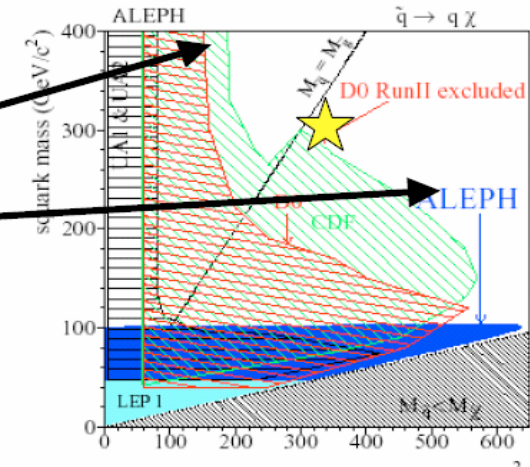
- $M(q) > M(g)$ :  $\tilde{u}, \tilde{d}, \tilde{s}, \tilde{c}, \tilde{b}$  mass equal

- $M(g) < M(q)$ :  $\tilde{u}, \tilde{d}, \tilde{s}, \tilde{c}$  mass equal

- Improves Run I limits:

- Include more data

- Scan parameter space



Specific search for light sbottom

- $BR(\tilde{g} \rightarrow \tilde{b}b) \sim 100\%$  assumed

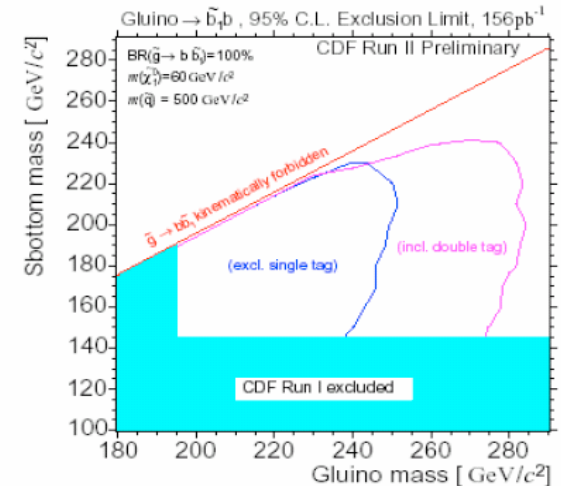
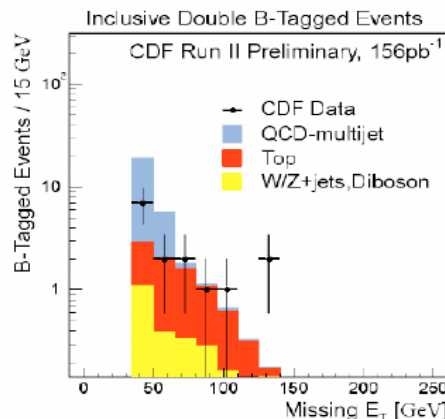
- Spectacular signature:

- 4 b-quarks +  $\cancel{E}_T$

- Require b-jets and  $\cancel{E}_T > 80 \text{ GeV}$

Expect:  $2.6 \pm 0.7$

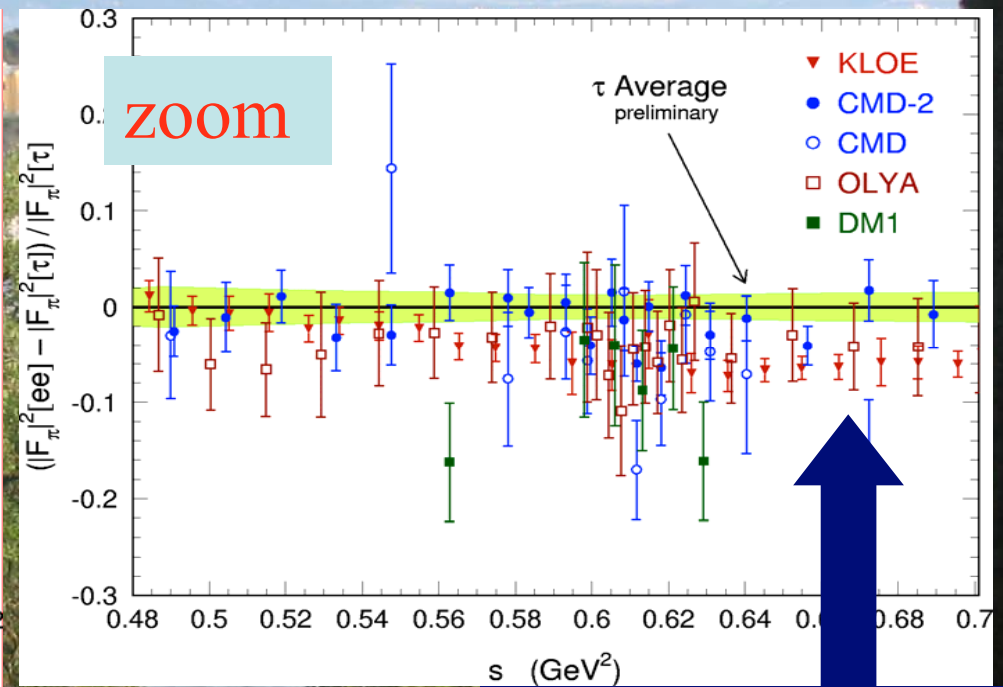
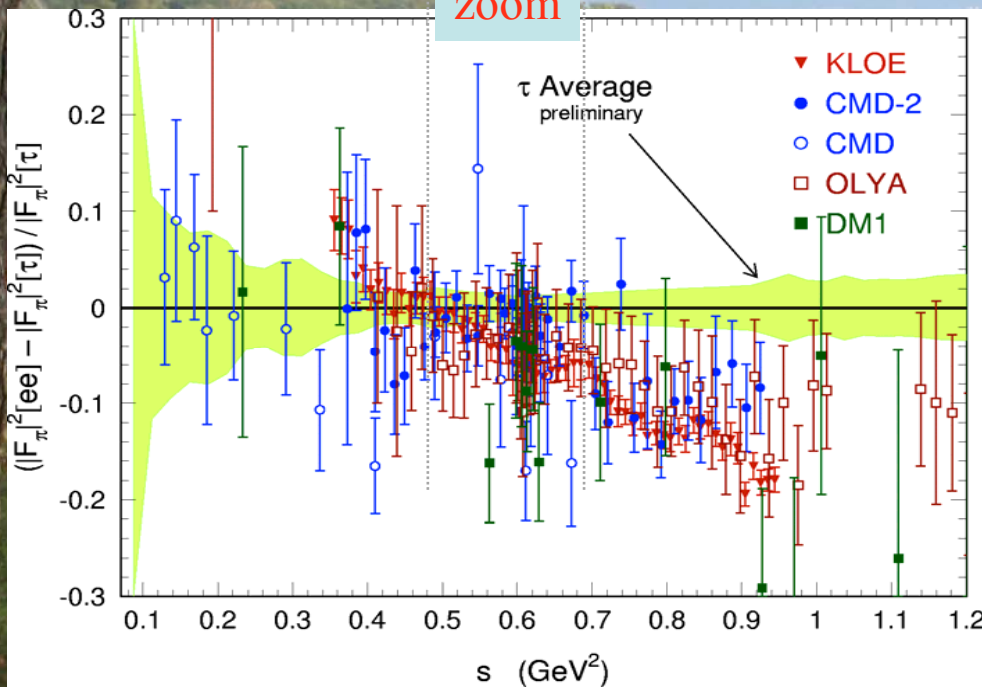
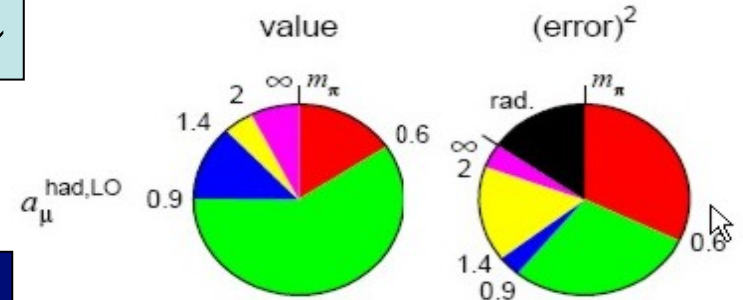
Observe: 4



Exclude new parameter space in gluino vs. sbottom mass plane

# $g_\mu - 2: e^+e^-$ Data vs $\tau$ Data

Largest contributions, errors from low energies



KLOE agrees with CMD-2: discard  $\tau$  data

Why the 10%  $\tau - e^+e^-$  discrepancy above  $\rho$  peak?

# Updated Results for $g_\mu - 2$

$$a_\mu^{\text{had}} [e^+e^-] = (693.4 \pm 5.3 \pm 3.5) \times 10^{-10}$$

$$a_\mu^{\text{SM}} [e^+e^-] = (11\,659\,182.8 \pm 6.3_{\text{had}} \pm 3.5_{\text{LBL}} \pm 0.3_{\text{QED+EW}}) \times 10^{-10}$$

Weak contribution

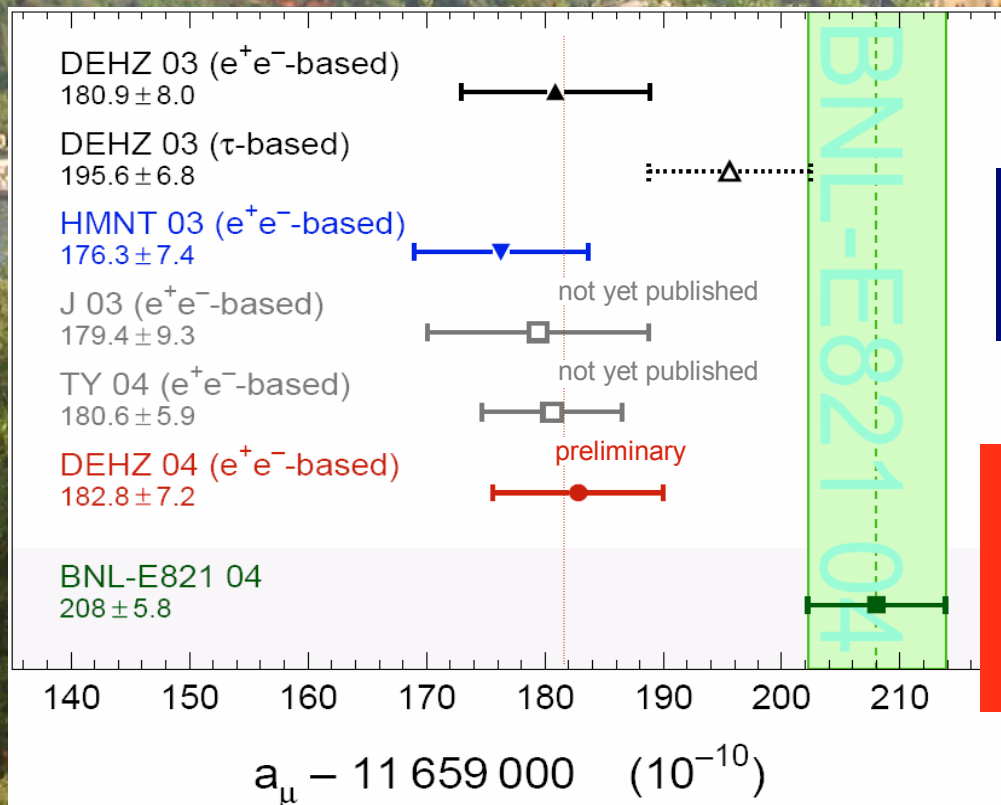
$$: a_\mu^{\text{weak}} = + (15.4 \pm 0.3) \times 10^{-10}$$

Hadronic contribution from higher order

$$: a_\mu^{\text{had}} [(\alpha/\pi)^3] = - (10.0 \pm 0.6) \times 10^{-10}$$

Hadronic contribution from LBL scattering:

$$: a_\mu^{\text{had}} [\text{LBL}] = + (12.0 \pm 3.5) \times 10^{-10}$$



BNL E821 (2004):

$$a_\mu^{\text{exp}} = (11\,659\,208.0 \pm 5.8) 10^{-10}$$

$$a_\mu^{\text{exp}} - a_\mu^{\text{SM}} = (25.2 \pm 9.2) \times 10^{-10}$$

➔ 2.7 standard deviations

# Current Constraints on CMSSM

Assuming the lightest sparticle is a neutralino

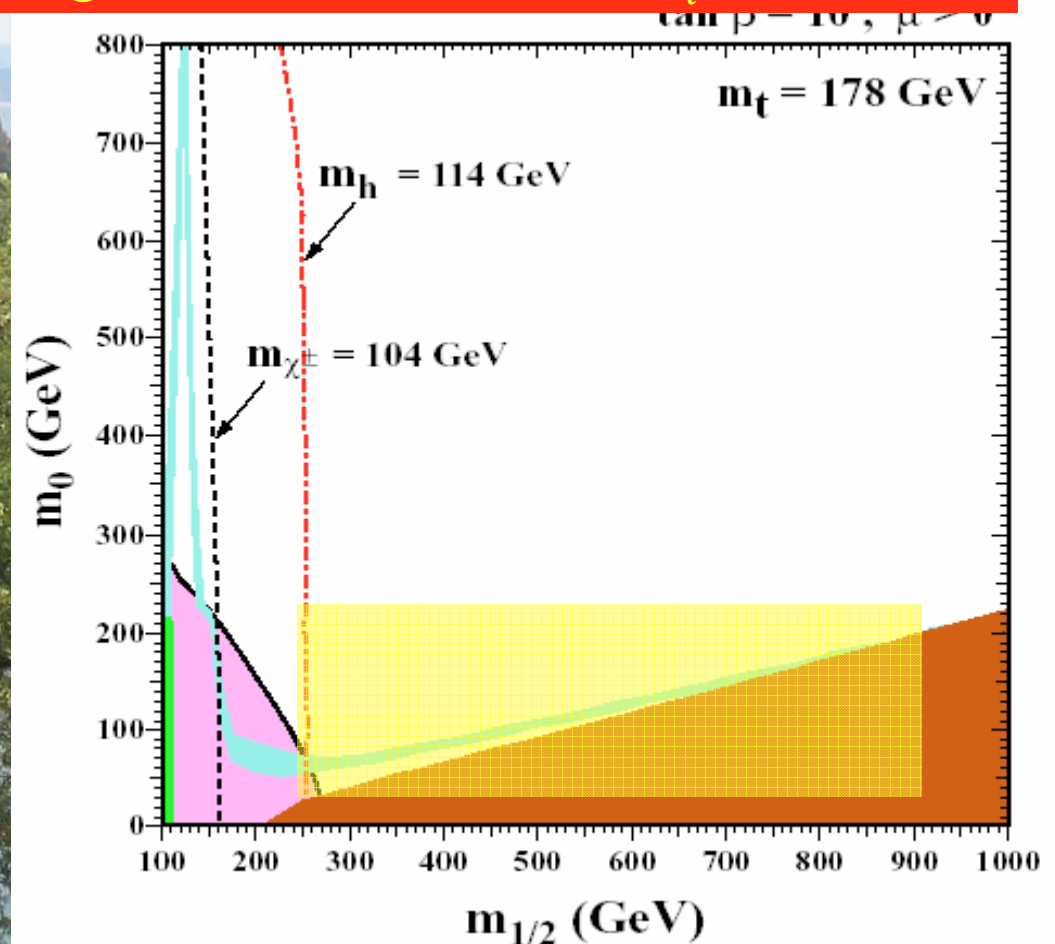
Focus-point region above 7 TeV for  $m_t = 178$  GeV

Excluded because stau LSP

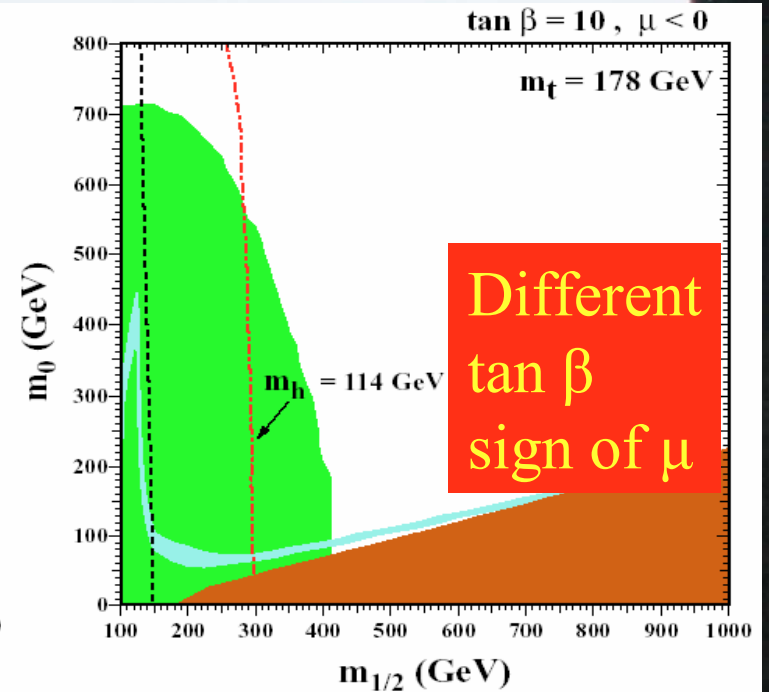
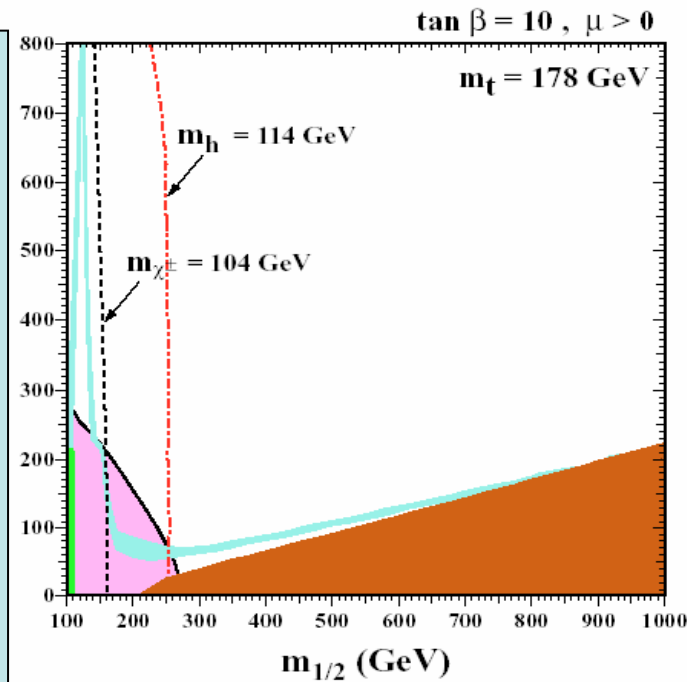
Excluded by  $b \rightarrow s$  gamma

WMAP constraint on relic density

Excluded (?) by latest  $g - 2$

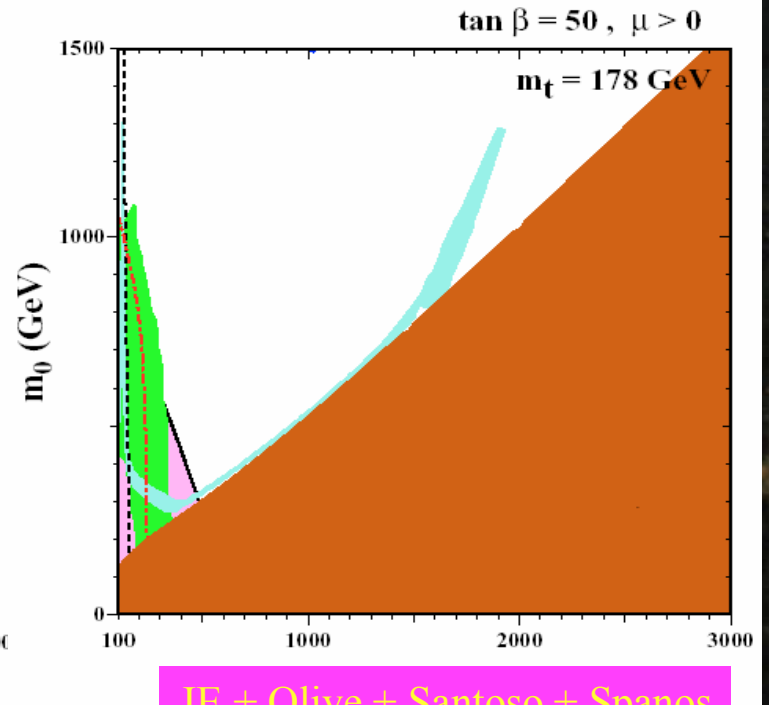
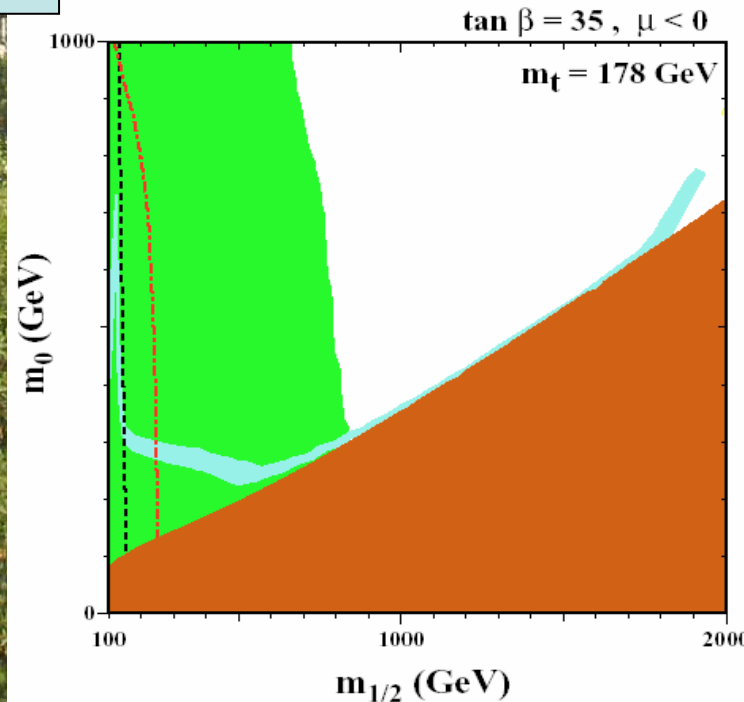


# Current Constraints on CMSSM



Different  $\tan \beta$  sign of  $\mu$

Impact of Higgs constraint reduced if larger  $m_t$   
Focus-point region far up



JE + Olive + Santoso + Spanos



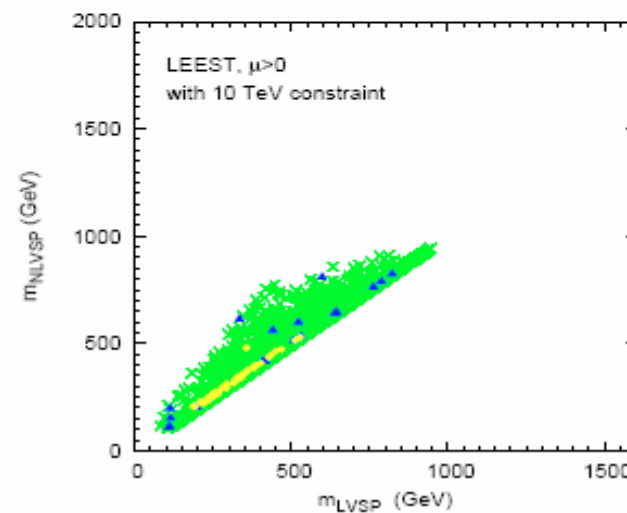
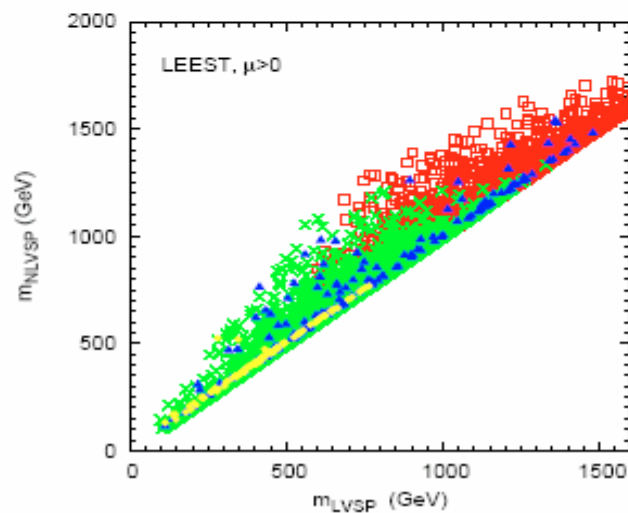
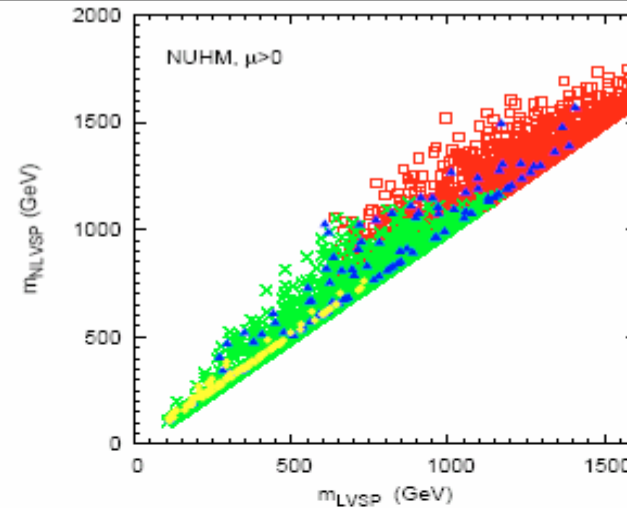
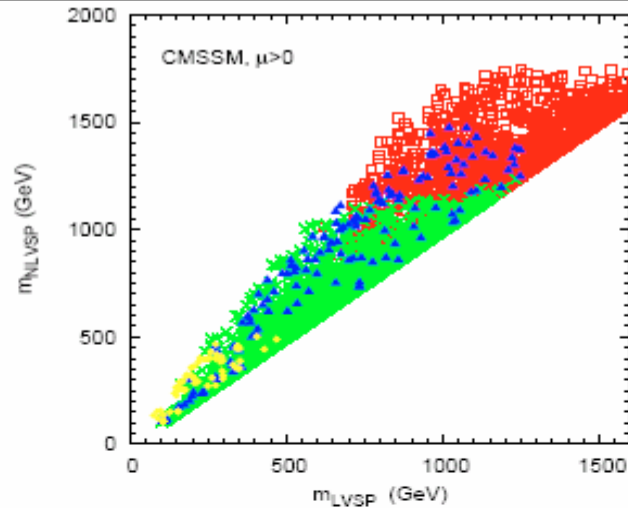
# Sparticles may not be very light

Full  
Model  
samples

Detectable  
@ LHC

Provide  
Dark Matter

Dark Matter  
Detectable  
Directly



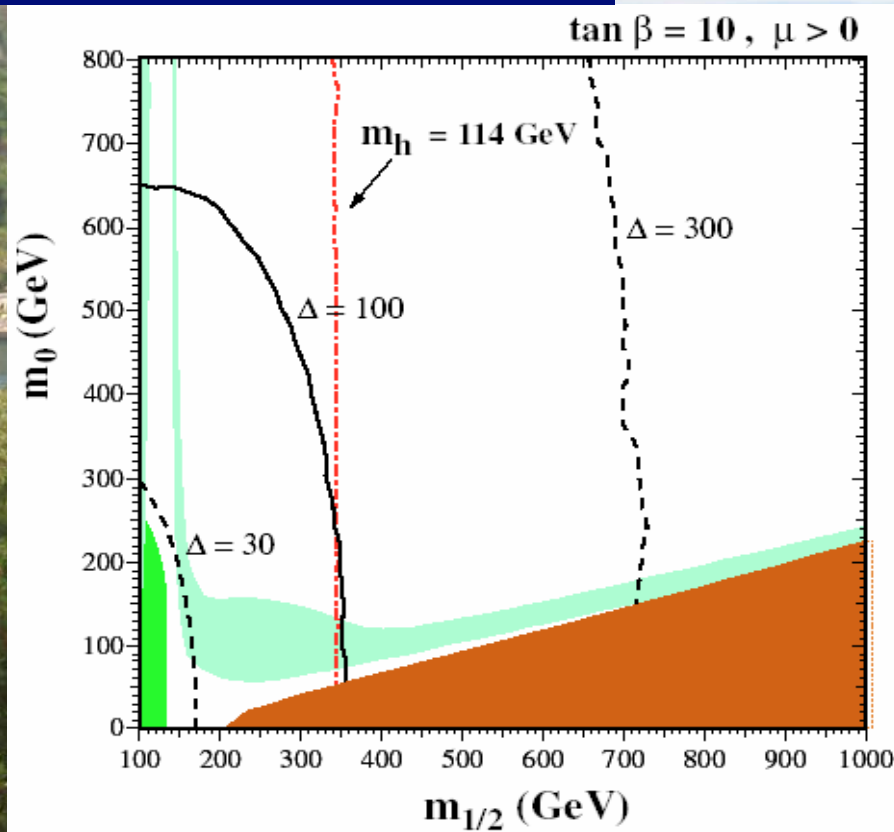
← Second lightest visible sparticle

Lightest visible sparticle →

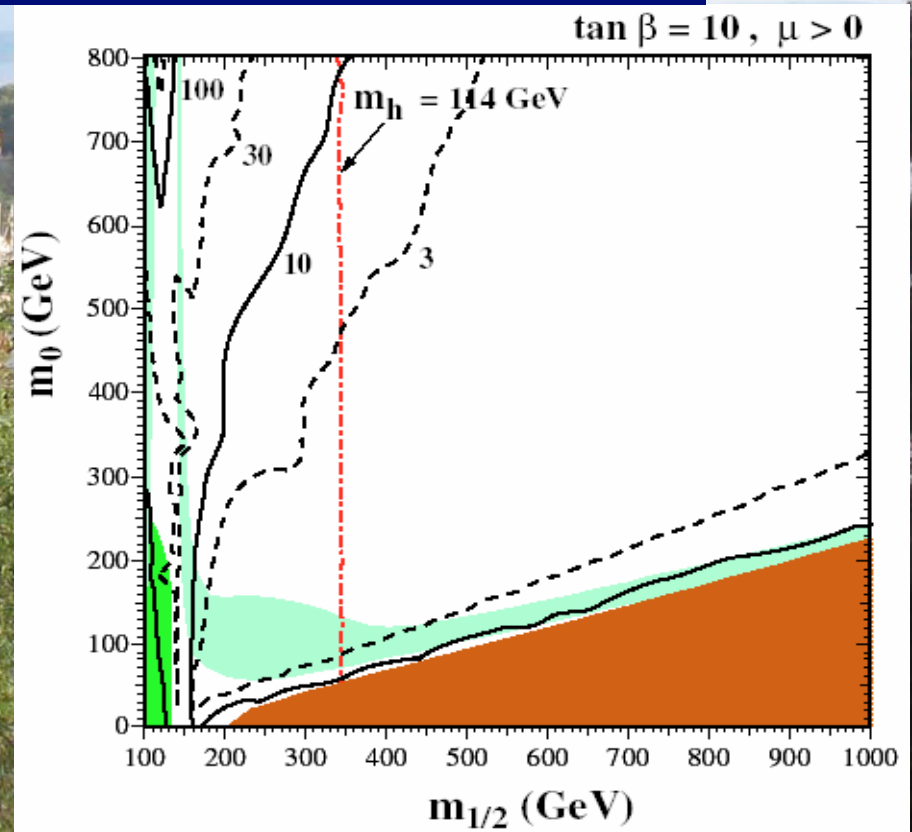
JE + Olive + Santoso + Spanos

# How 'Likely' are Heavy Sparticles?

## Fine-tuning of EW scale



## Fine-tuning of relic density

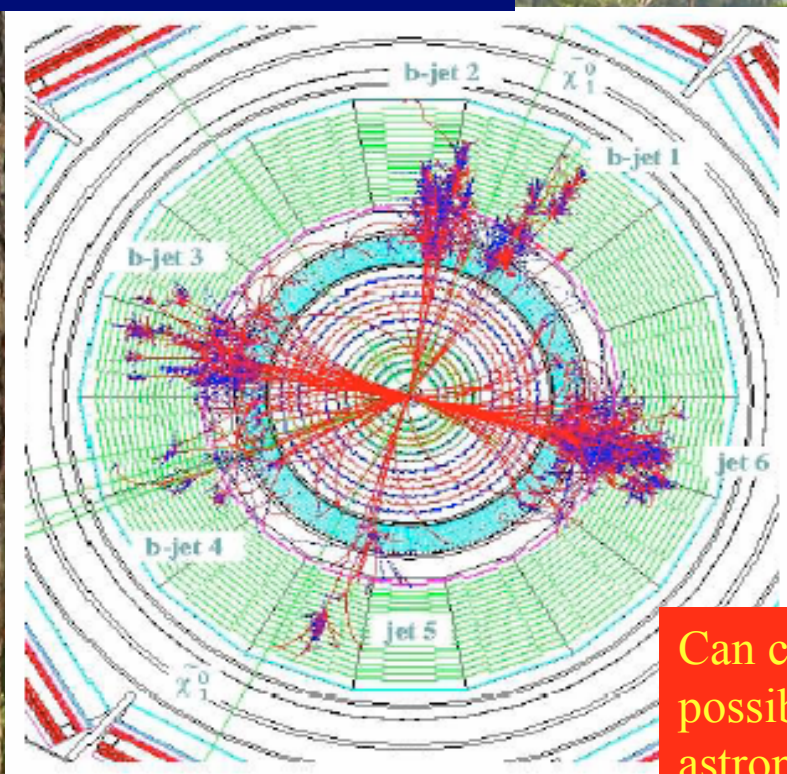


Larger masses require more fine-tuning: but how much is too much?

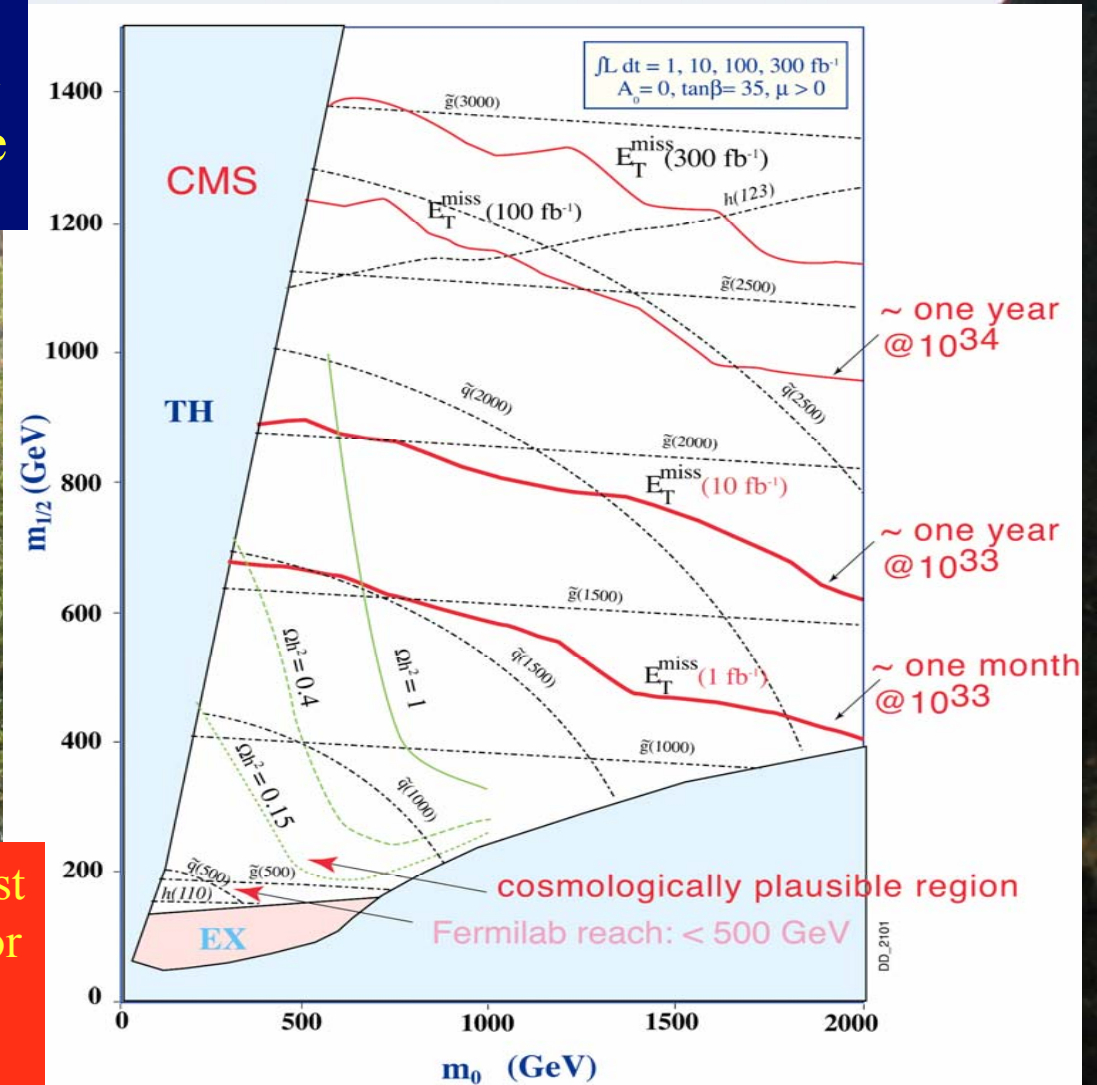
# Supersymmetry Searches at LHC

'Typical' supersymmetric Event at the LHC

LHC reach in supersymmetric parameter space

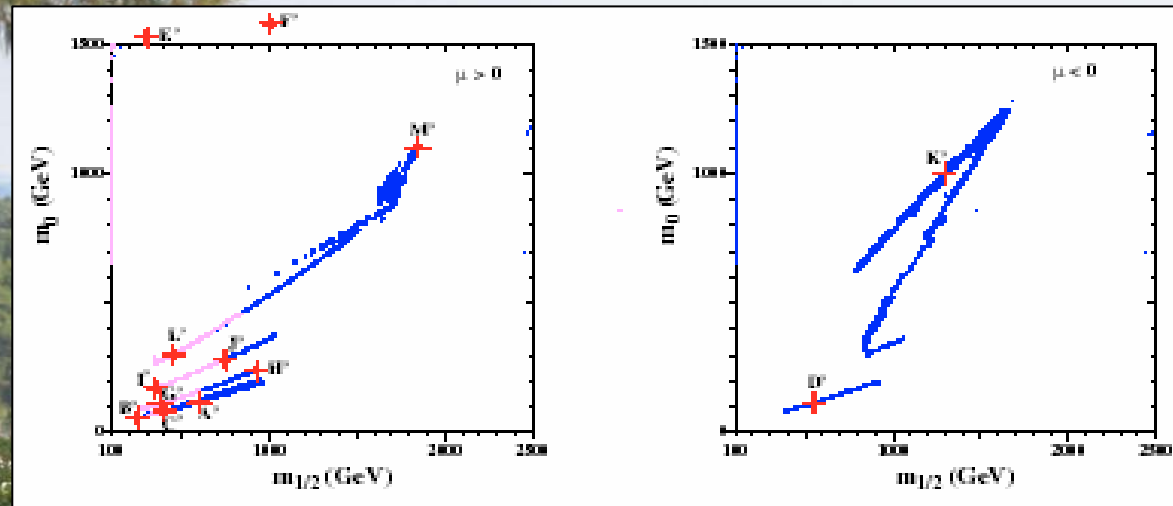


Can cover most possibilities for astrophysical dark matter



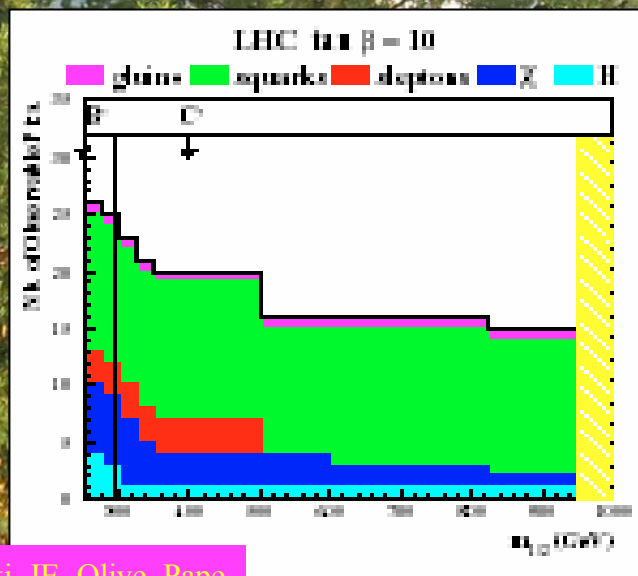
# Supersymmetric Benchmark Studies

Lines in susy space allowed by accelerators, WMAP data

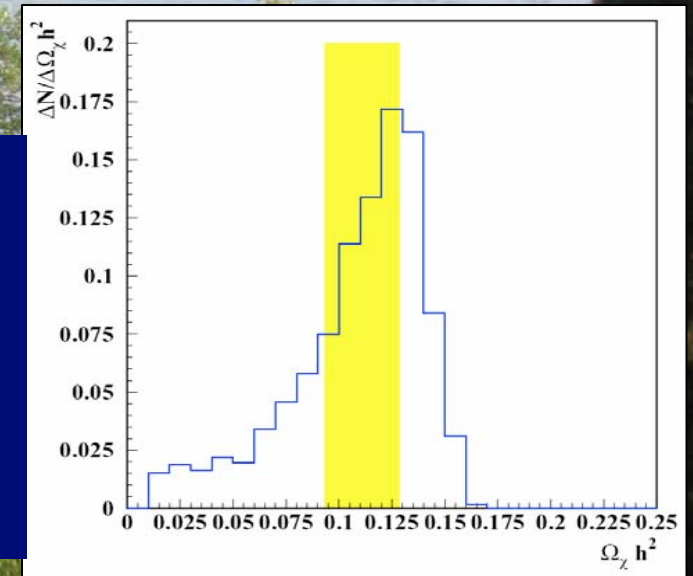


Specific benchmark Points along WMAP lines

Sparticle detectability Along one WMAP line

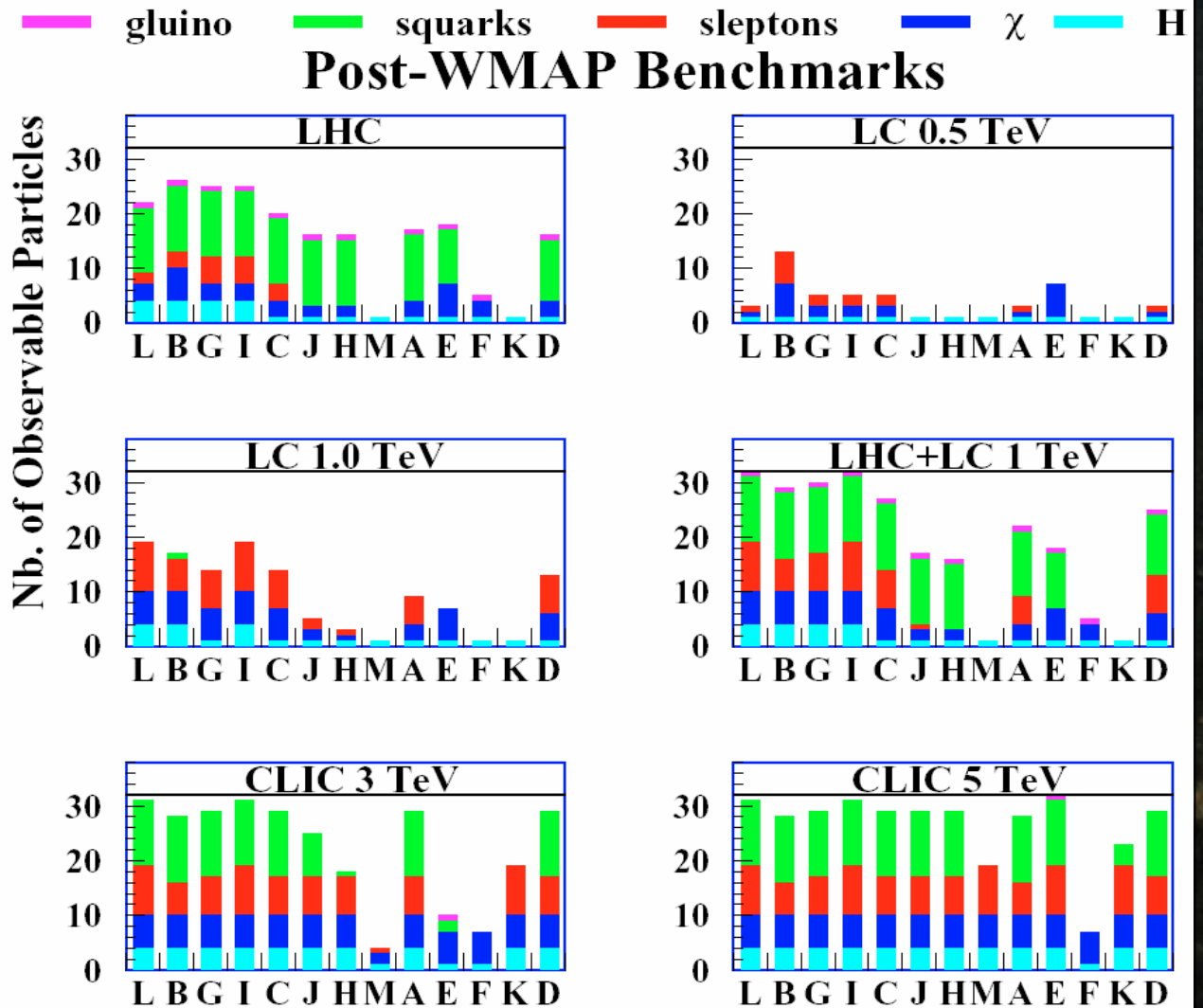


Calculation of relic density at a benchmark point



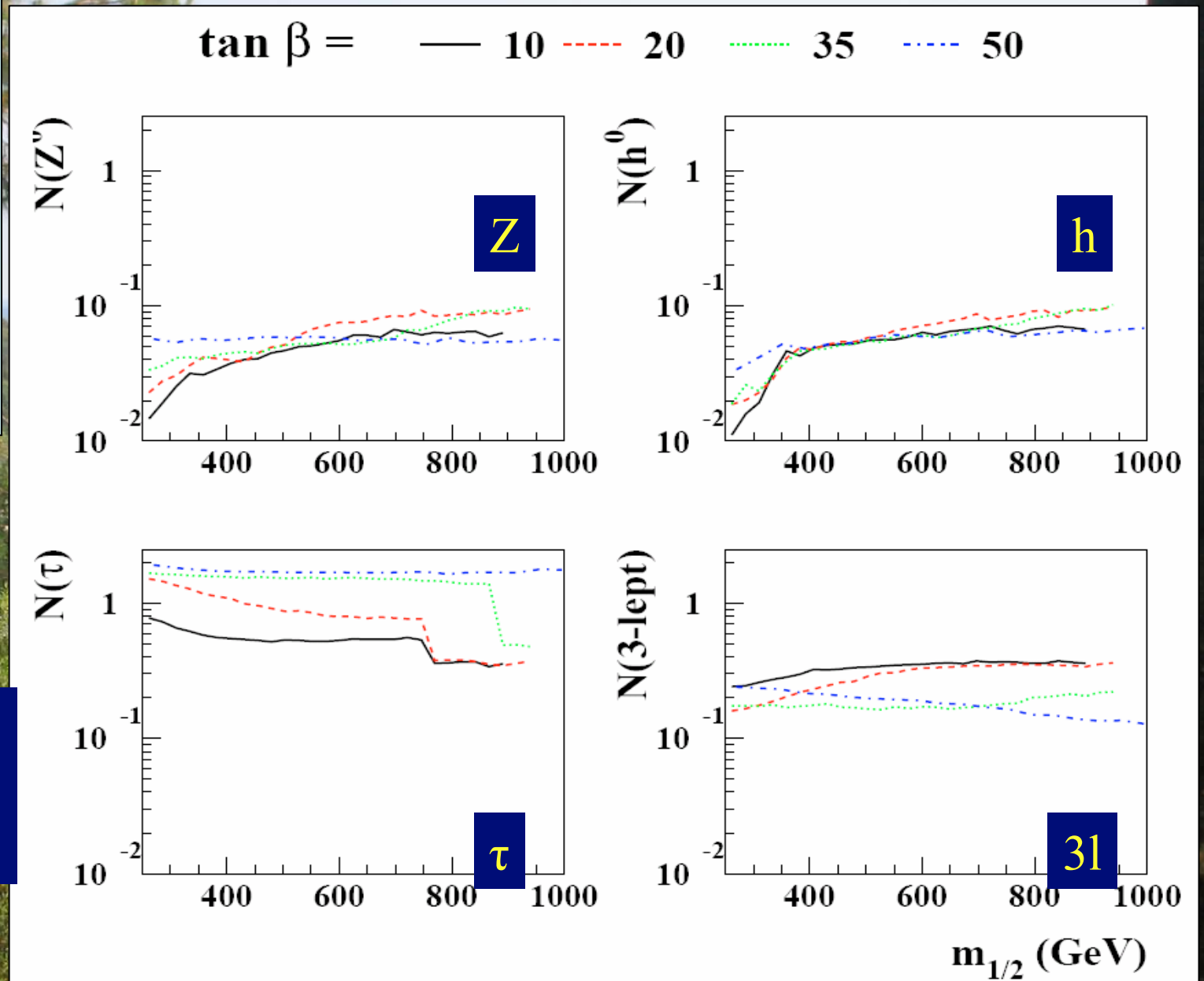
# Summary of LHC Scapabilities ... and Other Accelerators

LHC almost  
'guaranteed'  
to discover  
supersymmetry  
if it is relevant  
to the mass problem

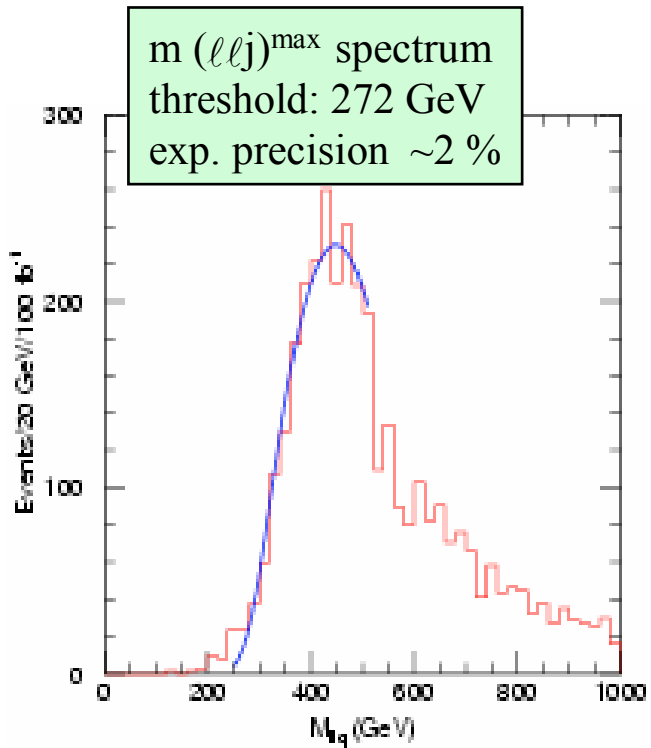
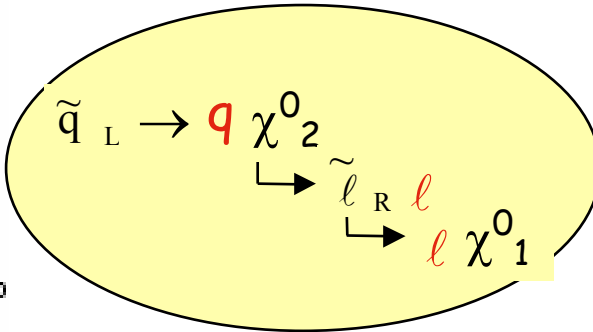
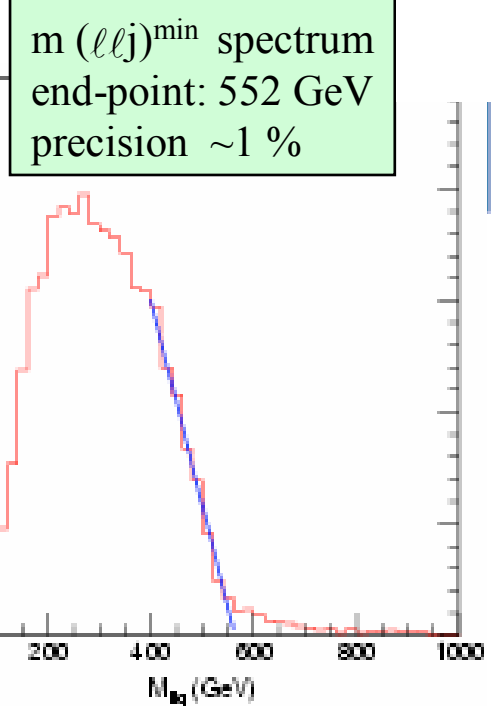
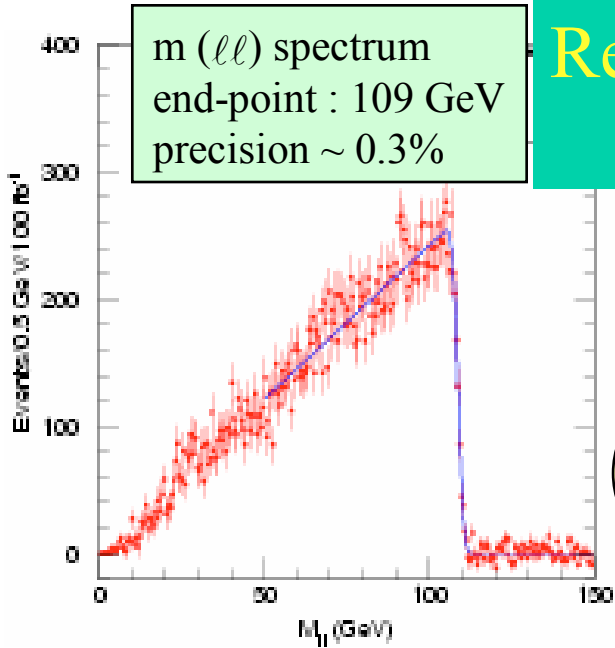


# Sparticle Signatures along WMAP lines

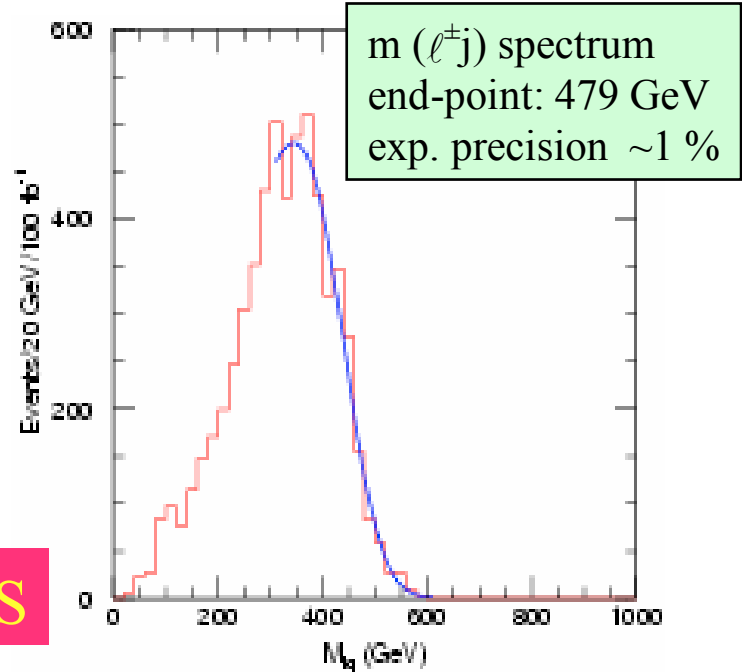
Average numbers of particles per sparticle event



# Reconstruction of 'Typical' Sparticle Decay Chain



$M_{\text{squark}} = 690$   
 $M_{\chi^+} = 232$   
 $M_{\text{slepton}} = 157$   
 $M_{\chi^0} = 121$   
 (GeV)

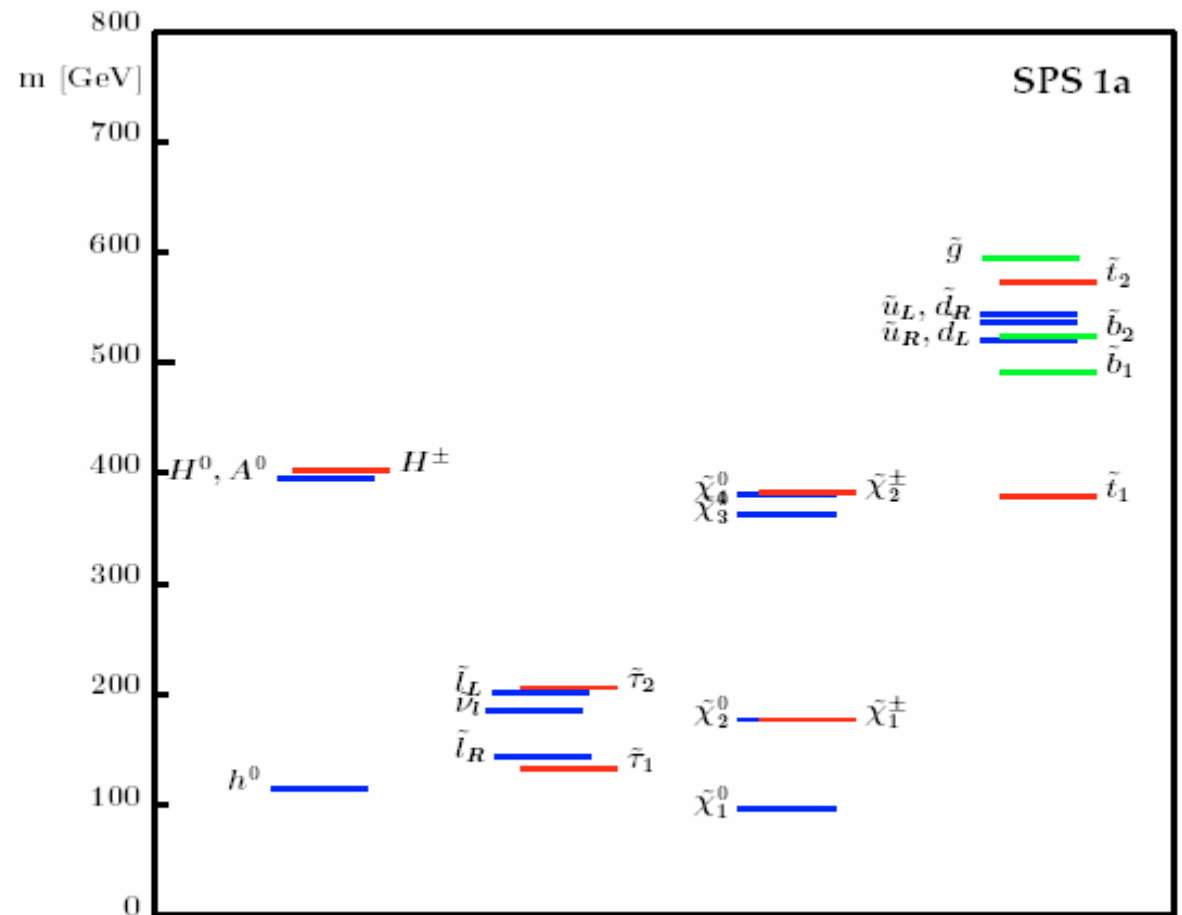


ATLAS

# Example of Benchmark Point

Spectrum of  
Benchmark SPS1a  
~ Point B of  
*Battaglia et al*

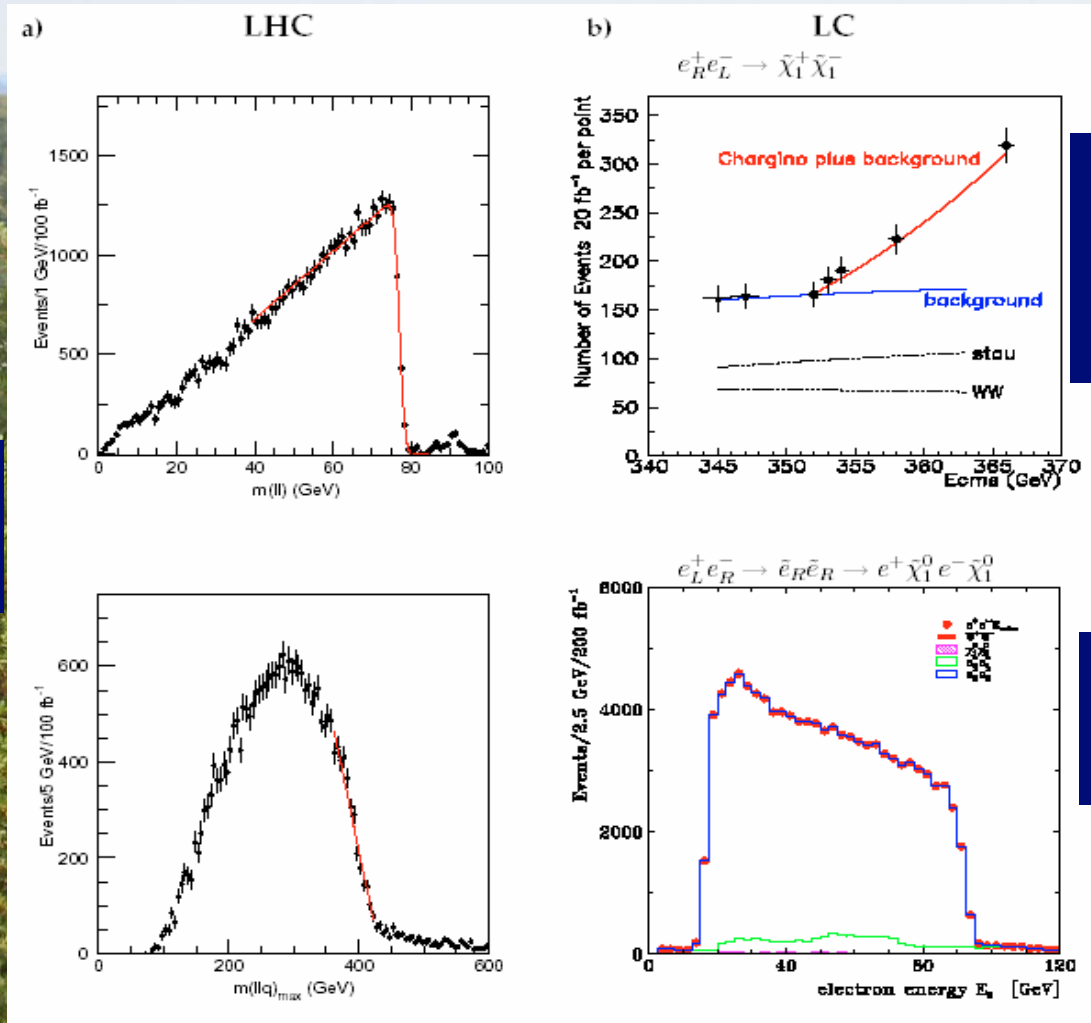
Several sparticles  
at 500 GeV LC,  
more at 1000 GeV,  
some need higher E





# Examples of Sparticle Measurements

Spectrum edges  
@ LHC



Threshold  
excitation  
@ LC

Spectra  
@ LC

Can one estimate the scale of supersymmetry?

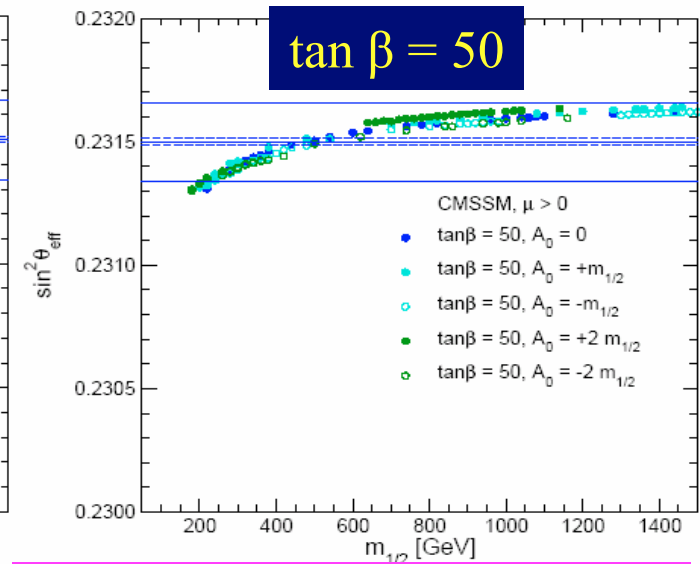
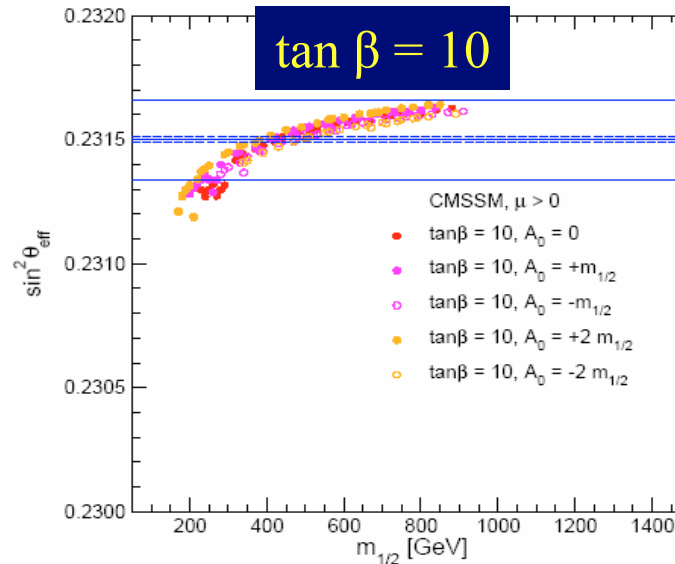
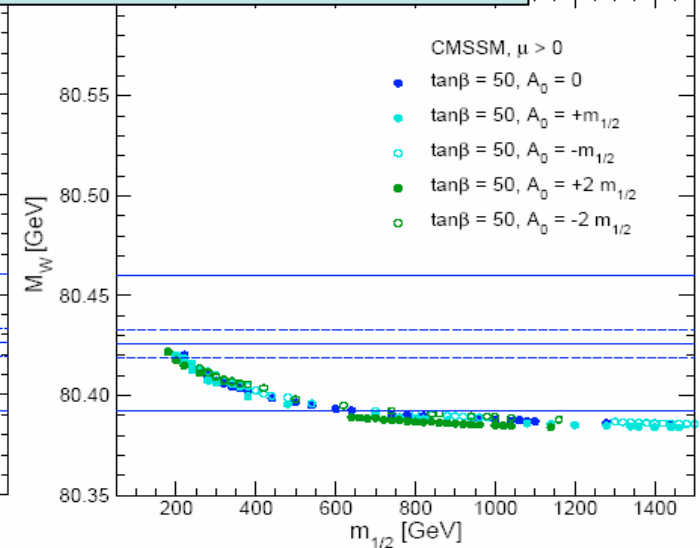
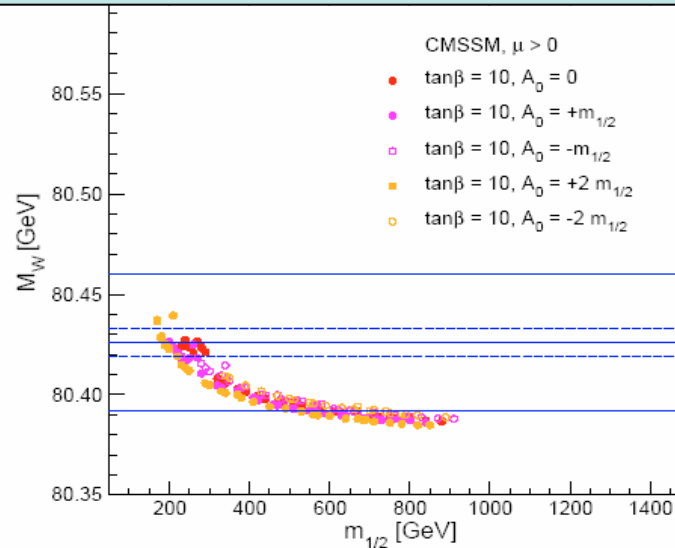
# Precision Observables in Susy

Sensitivity to  $m_{1/2}$   
in CMSSM  
along WMAP lines  
for different  $A$

$m_W$

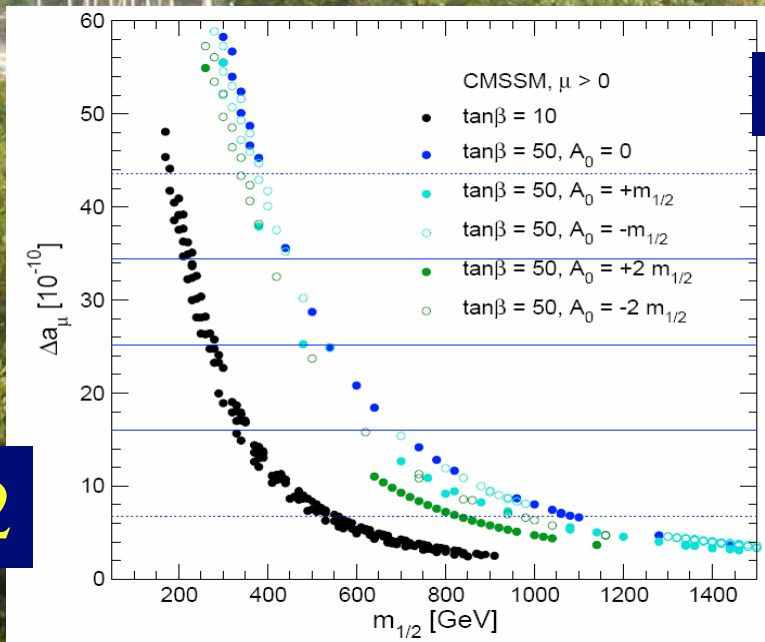
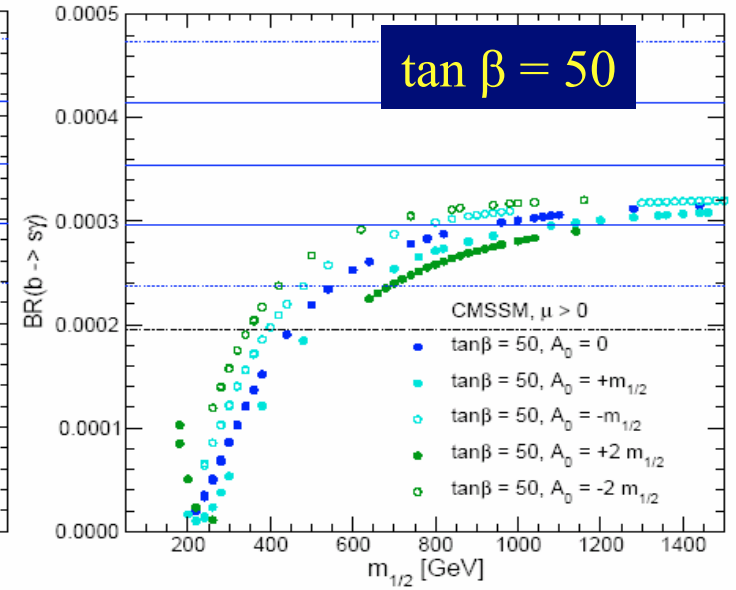
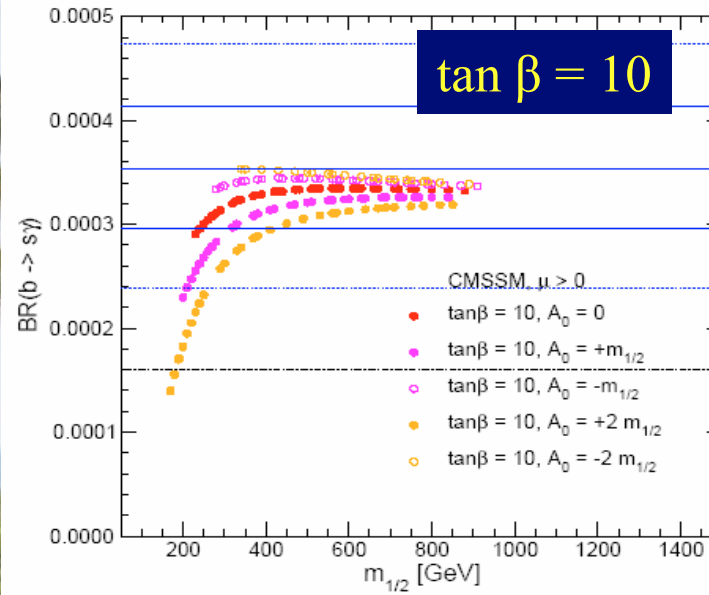
$\sin^2\theta_W$

Present & possible  
future errors



# More Observables

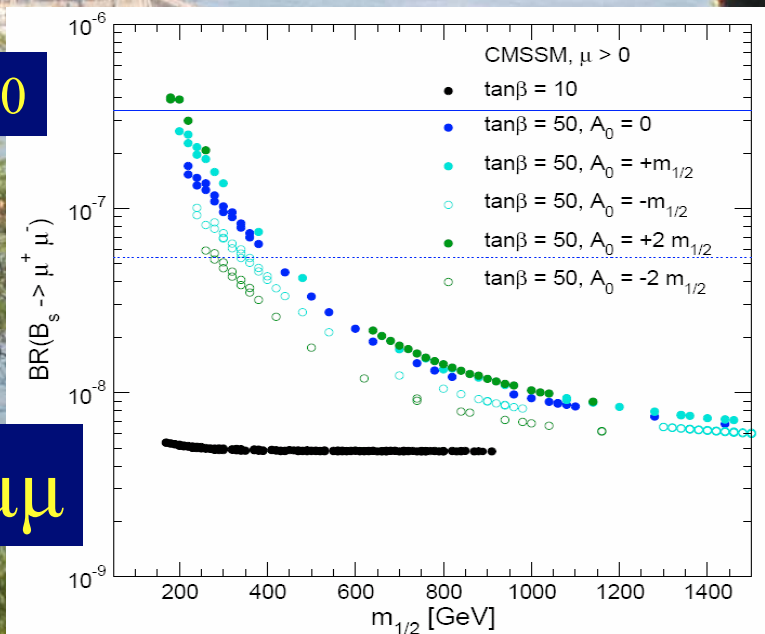
$$b \rightarrow sy$$



$$g_\mu - 2$$

$$\tan \beta = 10, 50$$

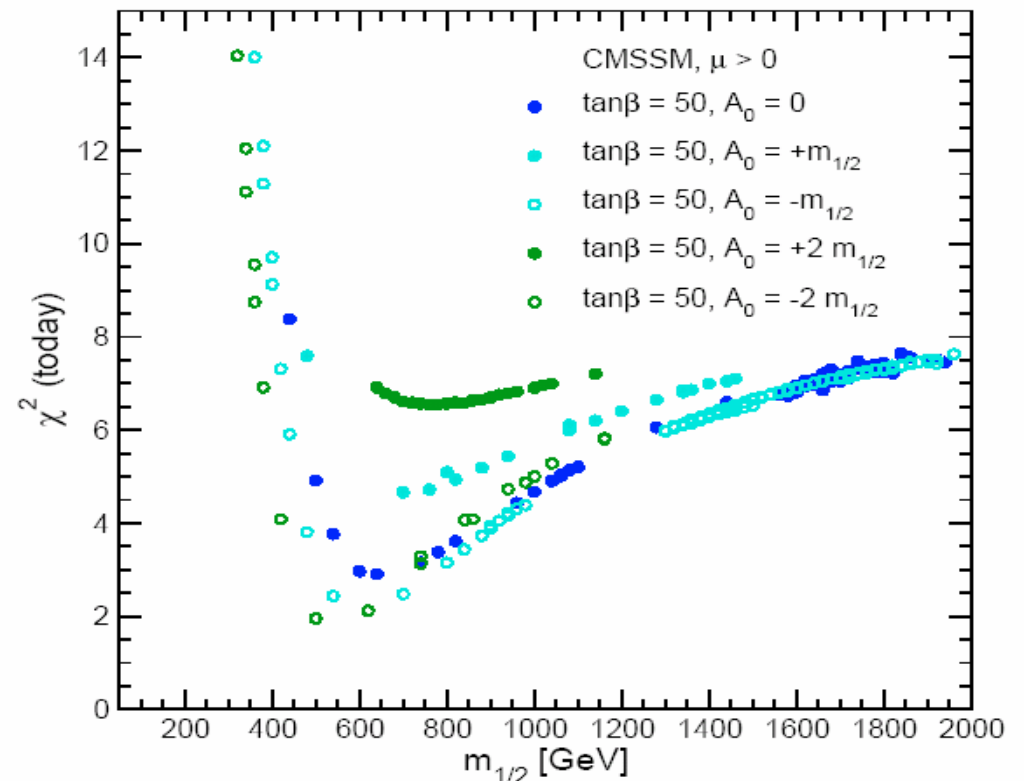
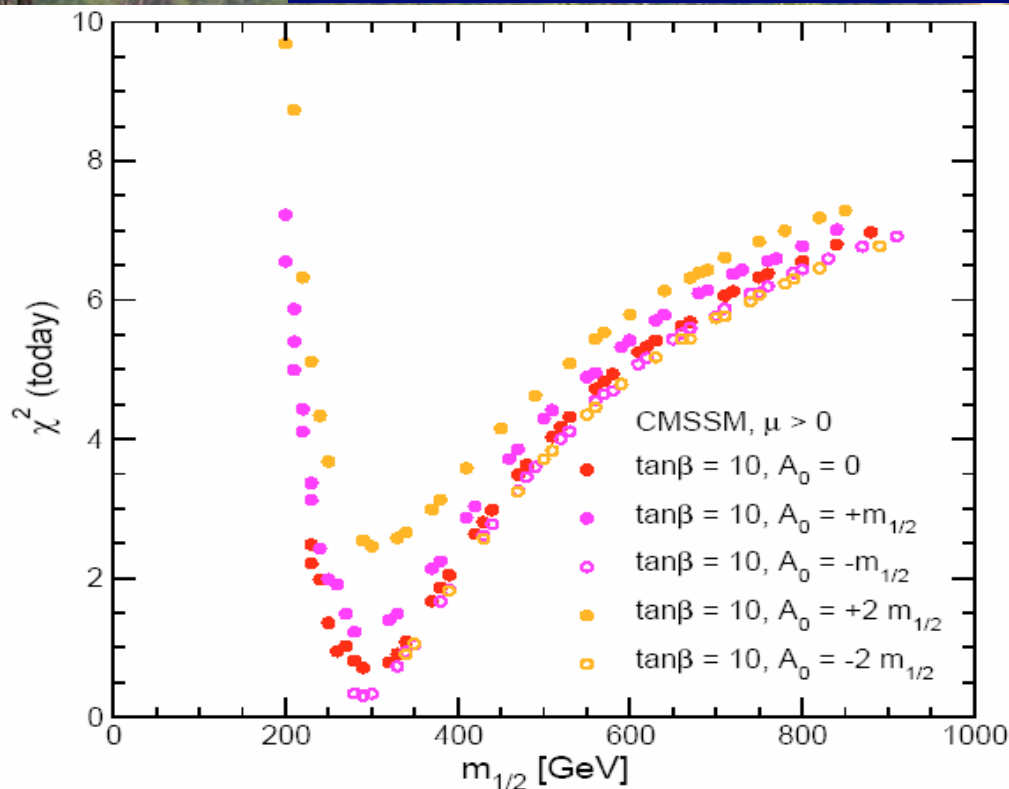
$$B_s \rightarrow \mu\mu$$



JE + Heinemeyer + Olive + Weiglein

# Global Fits to Present Data

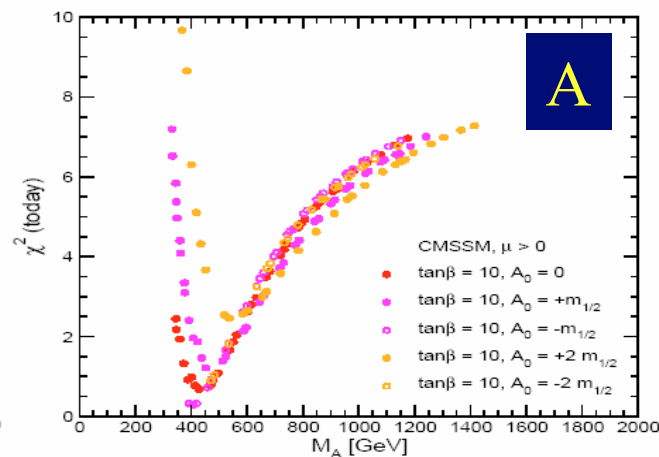
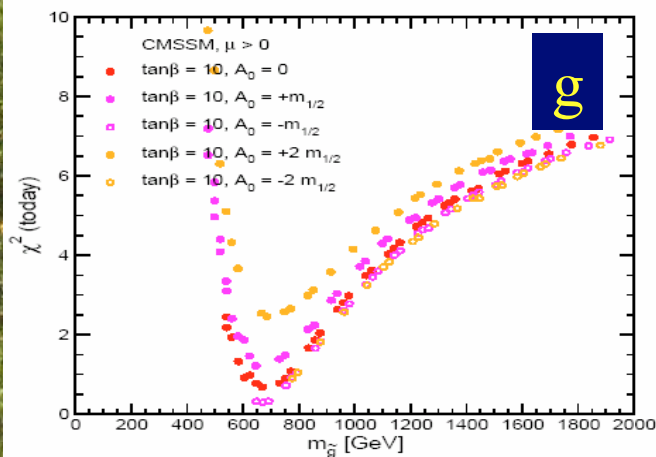
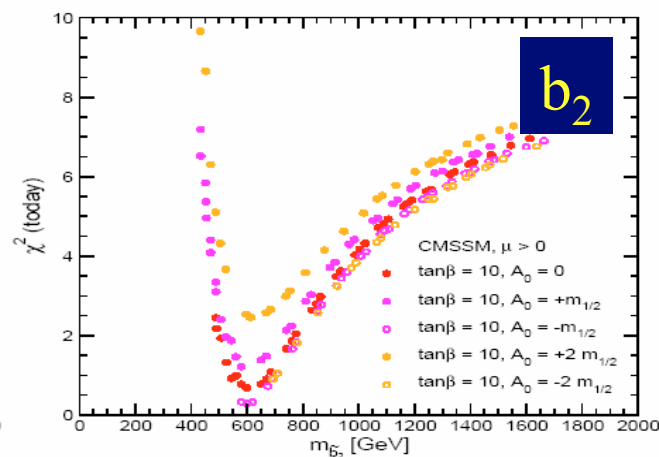
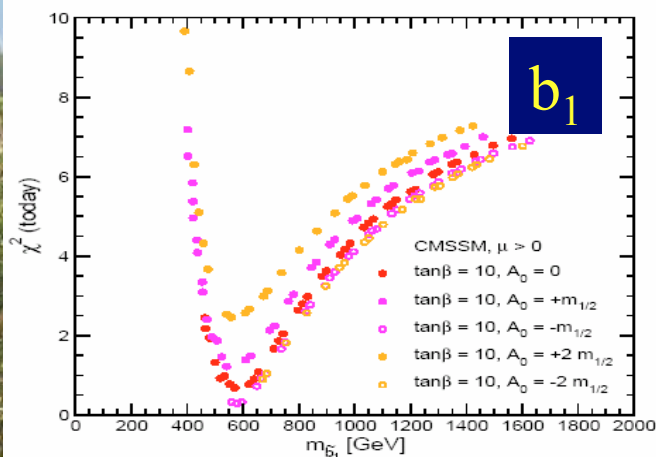
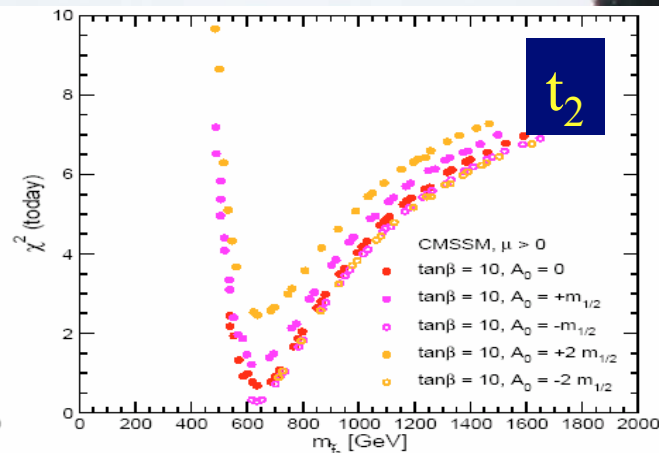
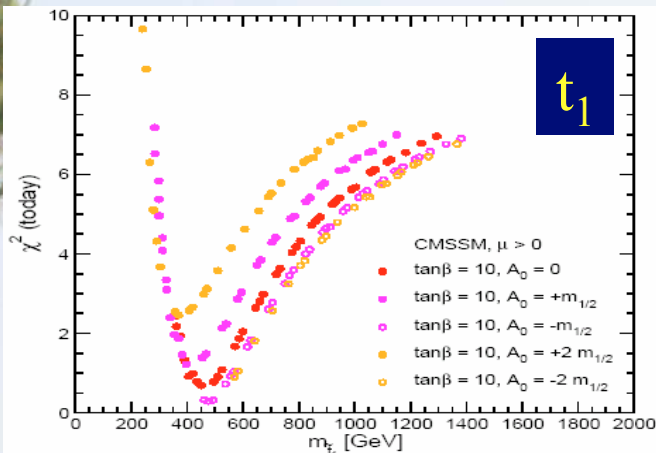
As functions of  $m_{1/2}$  in CMSSM for  $\tan \beta = 10, 50$



# Global Fits to Present Data

Preferred sparticle masses for  $\tan \beta = 10$

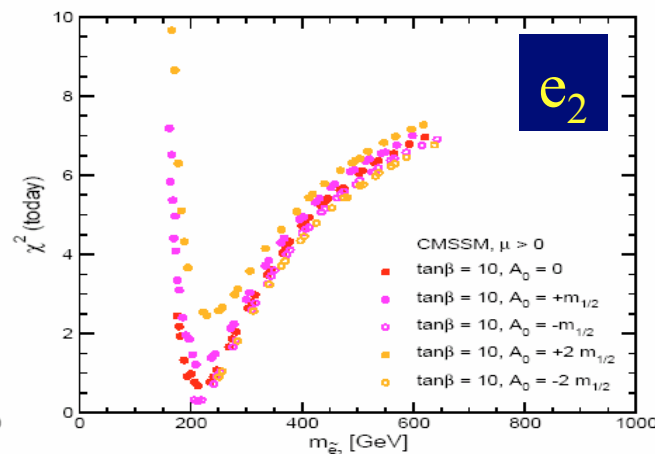
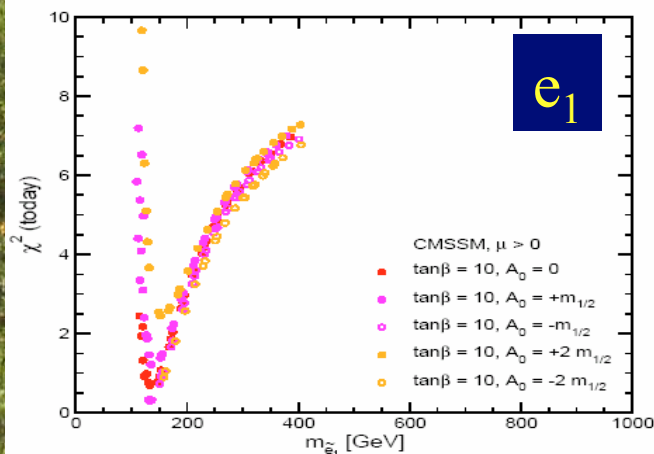
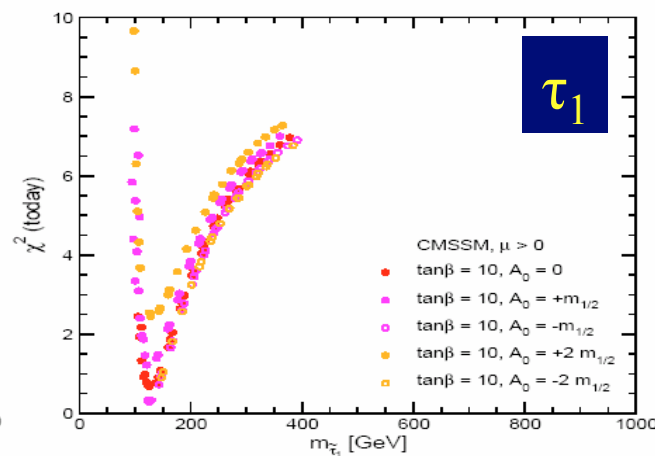
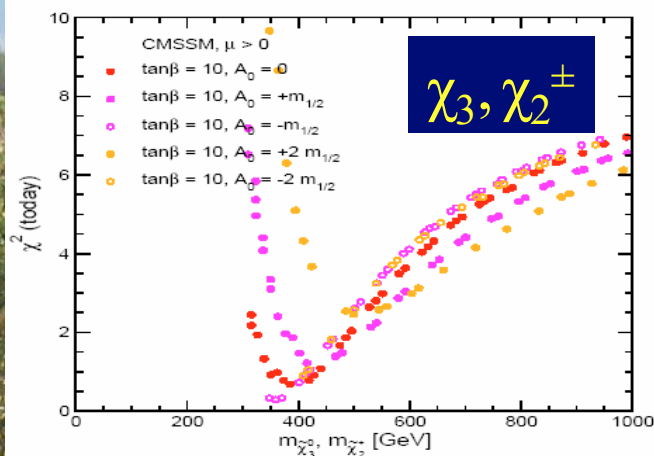
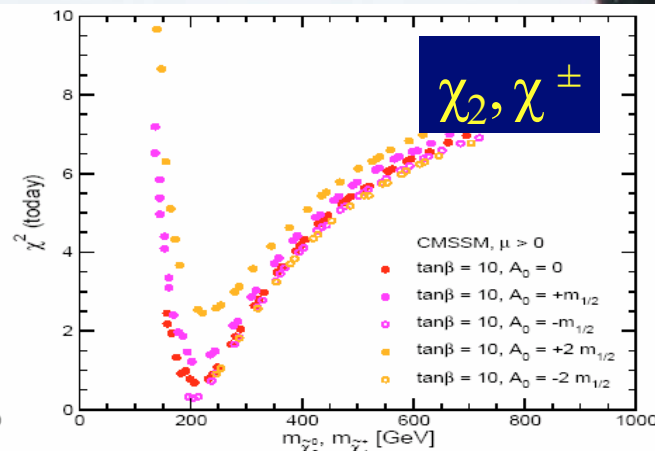
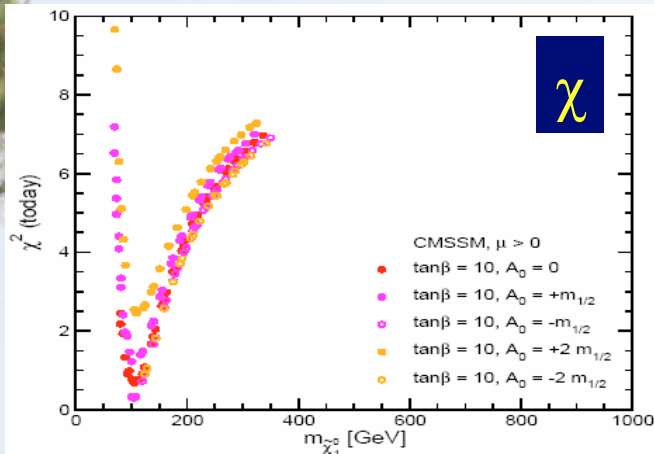
JE + Heinemeyer + Olive + Weiglein



# Global Fits to Present Data

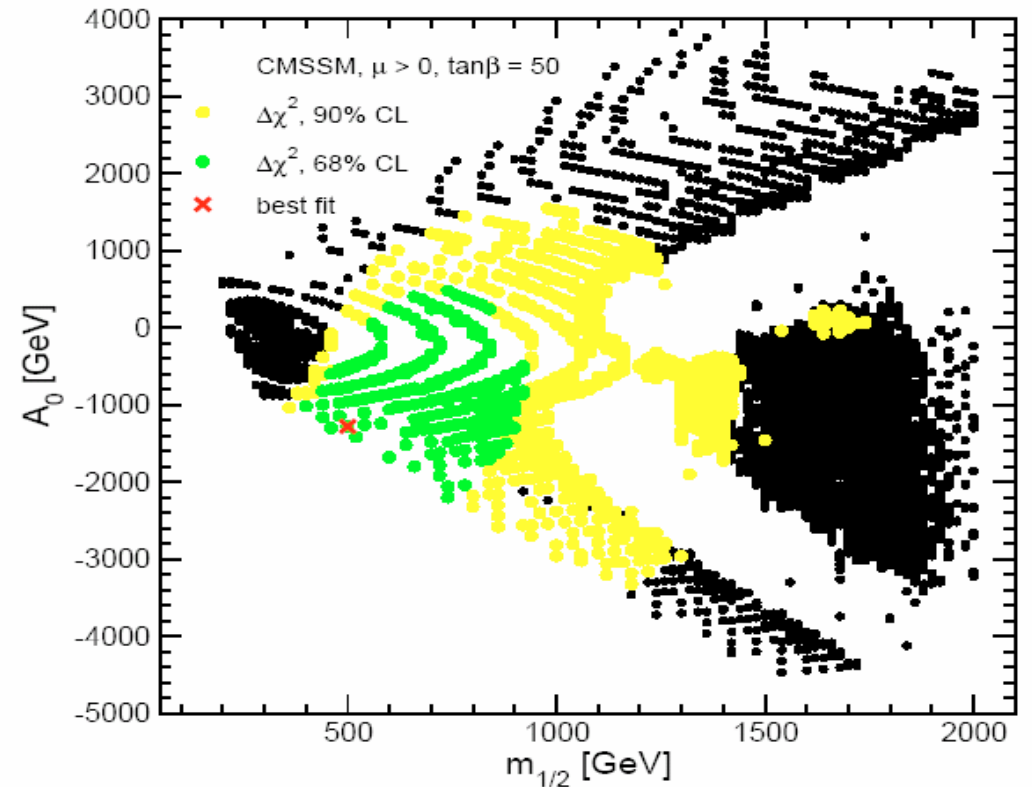
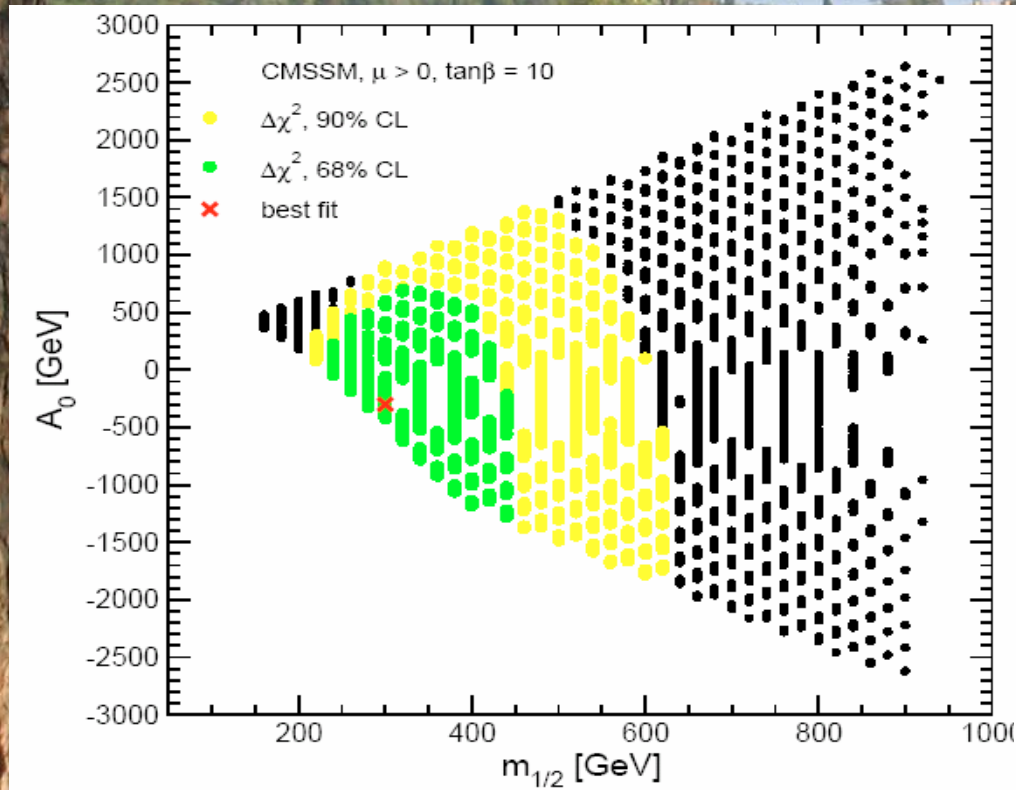
Preferred sparticle masses for  $\tan \beta = 10$

JE + Heinemeyer + Olive + Weiglein



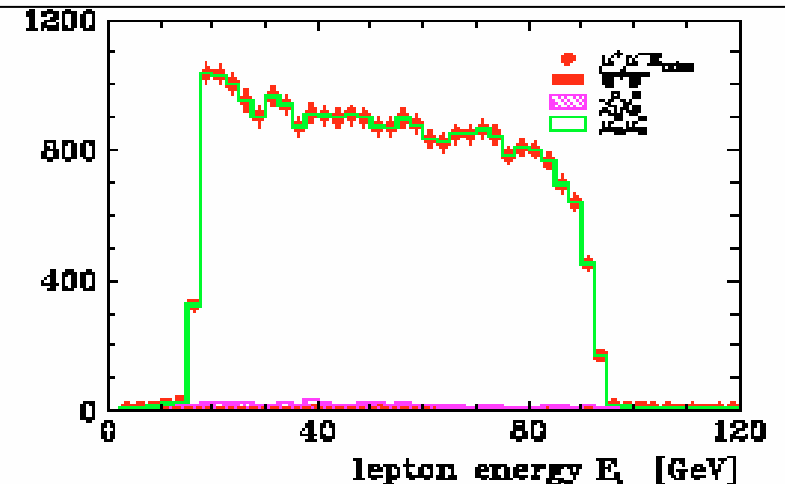
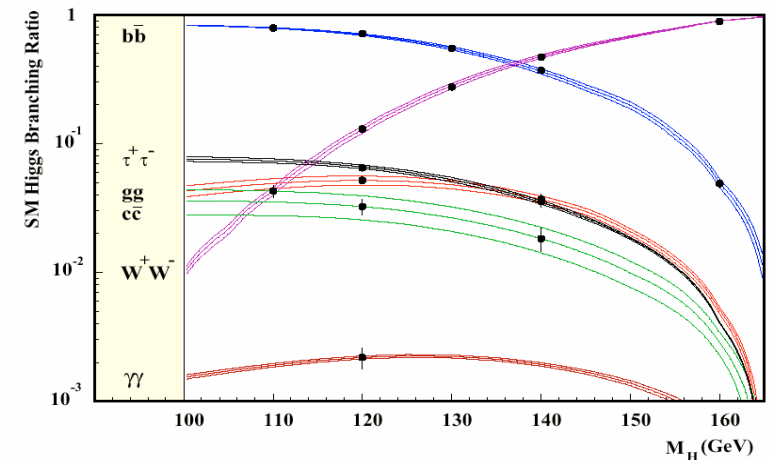
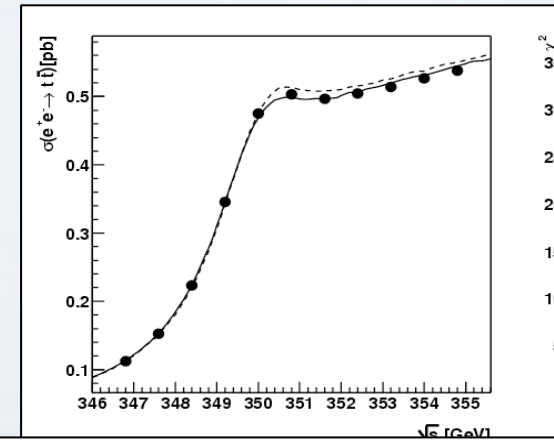
# Global Fits to Present Data

$(m_{1/2}, A_0)$  planes in CMSSM for  $\tan\beta = 10, 50$



# Tasks for the TeV ILC

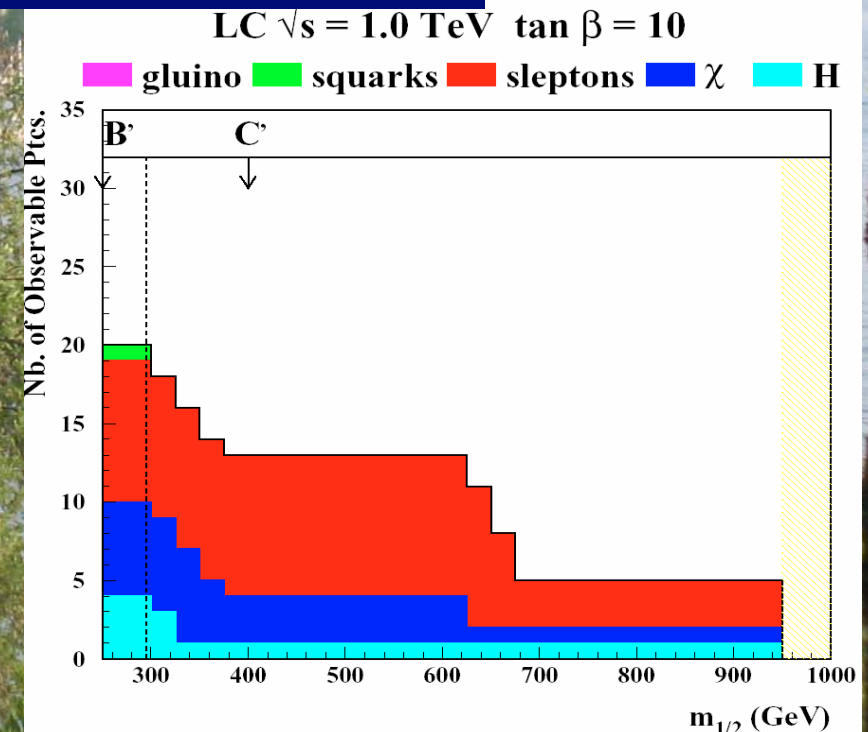
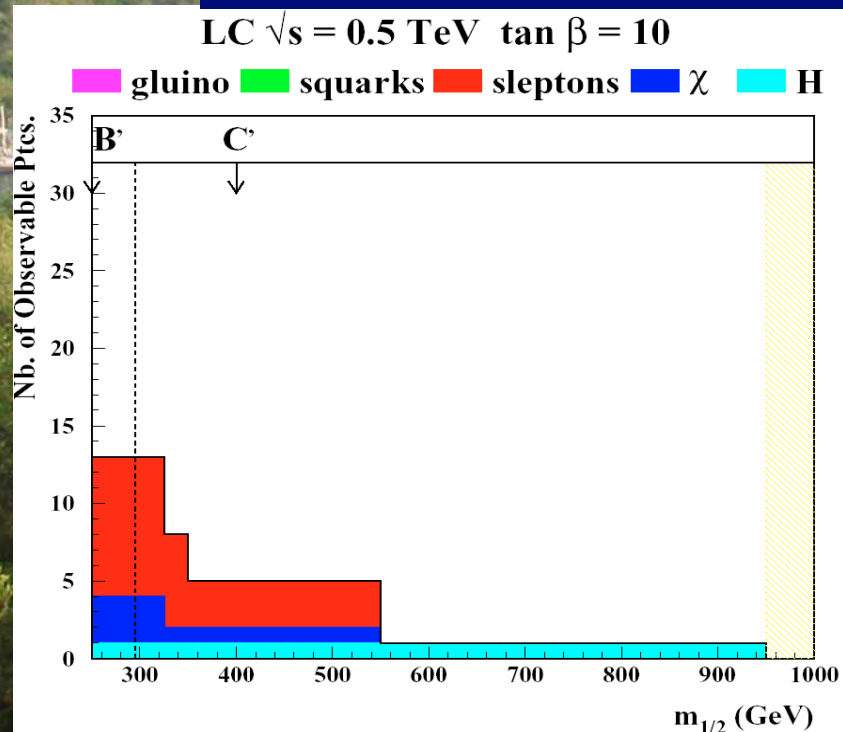
- Measure  $m_t$  to  $< \pm 100$  MeV
- If there is a light Higgs of any kind, pin it down:
  - Does it have standard model couplings?
  - What is its precise mass?
- If there are extra light particles:
  - Measure mass and properties
- If LHC sees nothing new below  $\sim 500$  GeV:
  - Look for indirect signatures





# Sparticles at LC along WMAP Line

Complementary to LHC: weakly-interacting sparticles

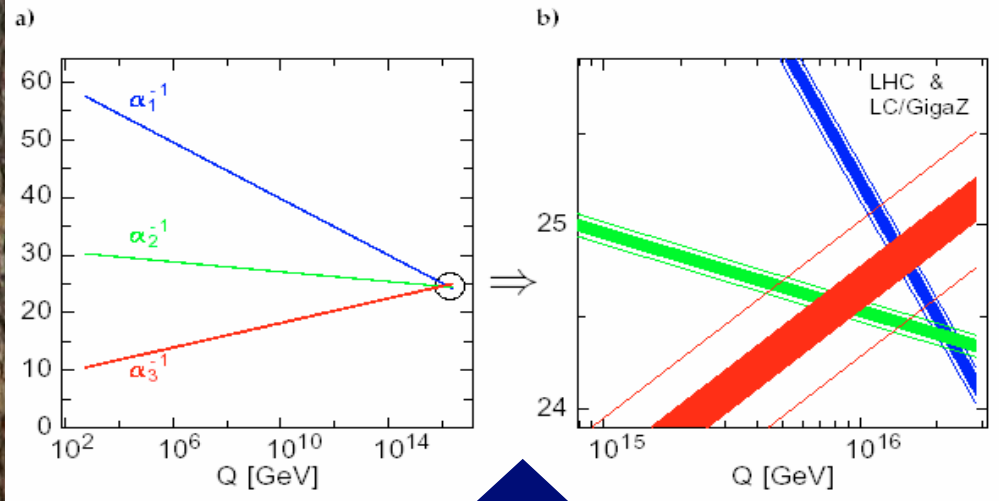


# Added Value of LC Measurements

	$m_{\text{SPS1a}}$	LHC	LC	LHC+LC		$m_{\text{SPS1a}}$	LHC	LC	LHC+LC
$h$	111.6	0.25	0.05	0.05	$H$	399.6		1.5	1.5
$A$	399.1		1.5	1.5	$H_+$	407.1		1.5	1.5
$\chi_1^0$	97.03	4.8	0.05	0.05	$\chi_2^0$	182.9	4.7	1.2	0.08
$\chi_3^0$	349.2		4.0	4.0	$\chi_4^0$	370.3	5.1	4.0	2.3
$\chi_1^\pm$	182.3		0.55	0.55	$\chi_2^\pm$	370.6		3.0	3.0
$\tilde{g}$	615.7	8.0		6.5					
$\tilde{t}_1$	411.8		2.0	2.0					
$\tilde{b}_1$	520.8	7.5		5.7	$\tilde{b}_2$	550.4	7.9		6.2
$\tilde{u}_1$	551.0	19.0		16.0	$\tilde{u}_2$	570.8	17.4		9.8
$\tilde{d}_1$	549.9	19.0		16.0	$\tilde{d}_2$	576.4	17.4		9.8
$\tilde{s}_1$							17.4		9.8
$\tilde{c}_1$							17.4		9.8
$\tilde{e}_1$							17.4		9.8
		SPS1a	StartFit	LHC	$\Delta_{\text{LHC}}$	LC	$\Delta_{\text{LC}}$	LHC+LC	$\Delta_{\text{LHC+LC}}$
$M_0$		100	500	100.03	4.0	100.03	0.09	100.04	0.08
$M_{1/2}$		250	500	249.95	1.8	250.02	0.13	250.01	0.11
$\tan\beta$		10	50	9.87	1.3	9.98	0.14	9.98	0.14
$A_0$		-100	0	-99.29	31.8	-98.26	4.43	-98.25	4.13

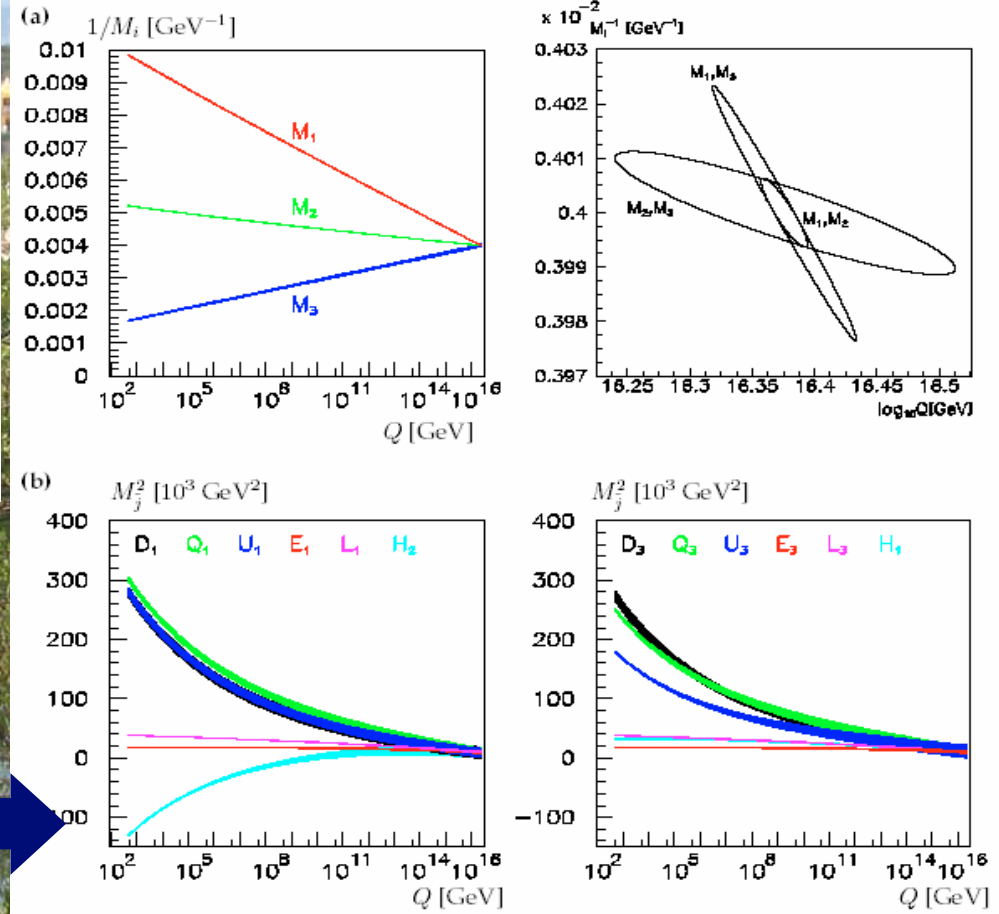
Determination of CMSSM parameters

# Tests of Unification Ideas



For gauge couplings

For sparticle masses



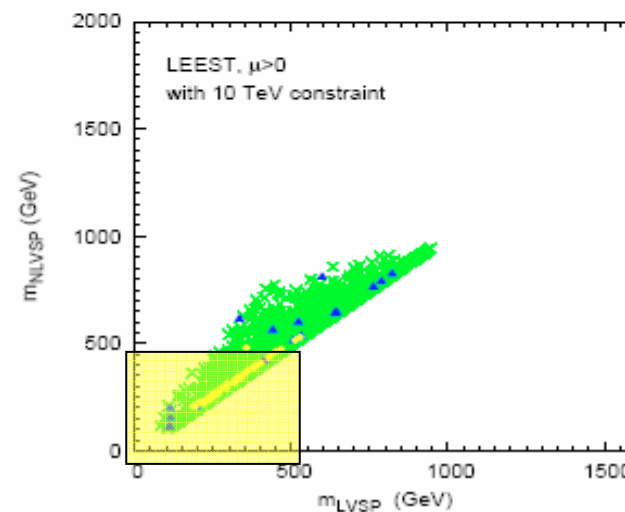
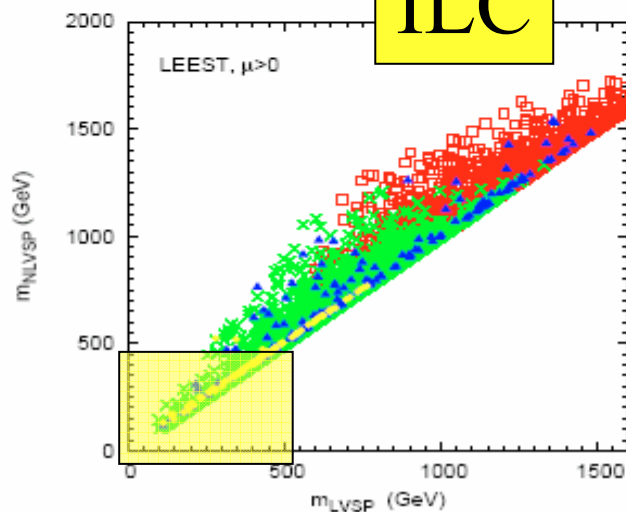
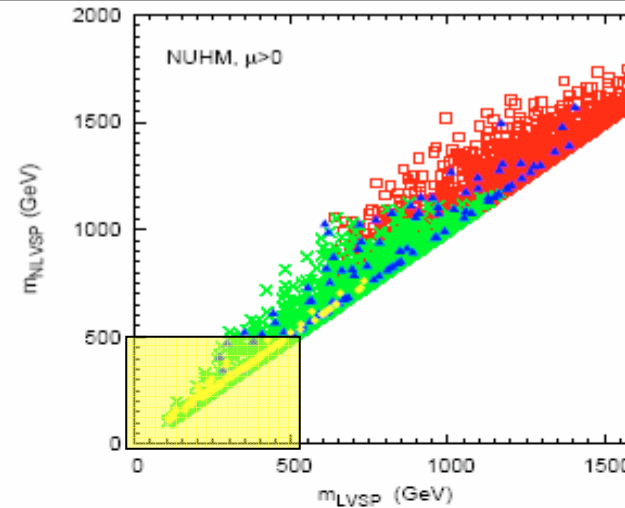
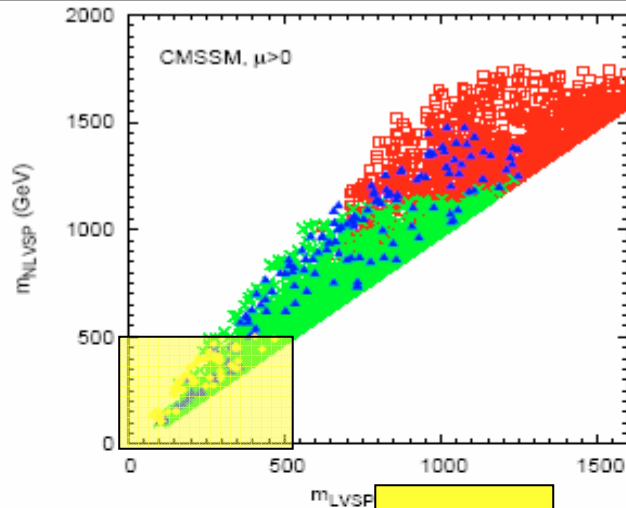
# Sparticles may not be very light

Full  
Model  
samples

Detectable  
@ LHC

Provide  
Dark Matter

Dark Matter  
Detectable  
Directly



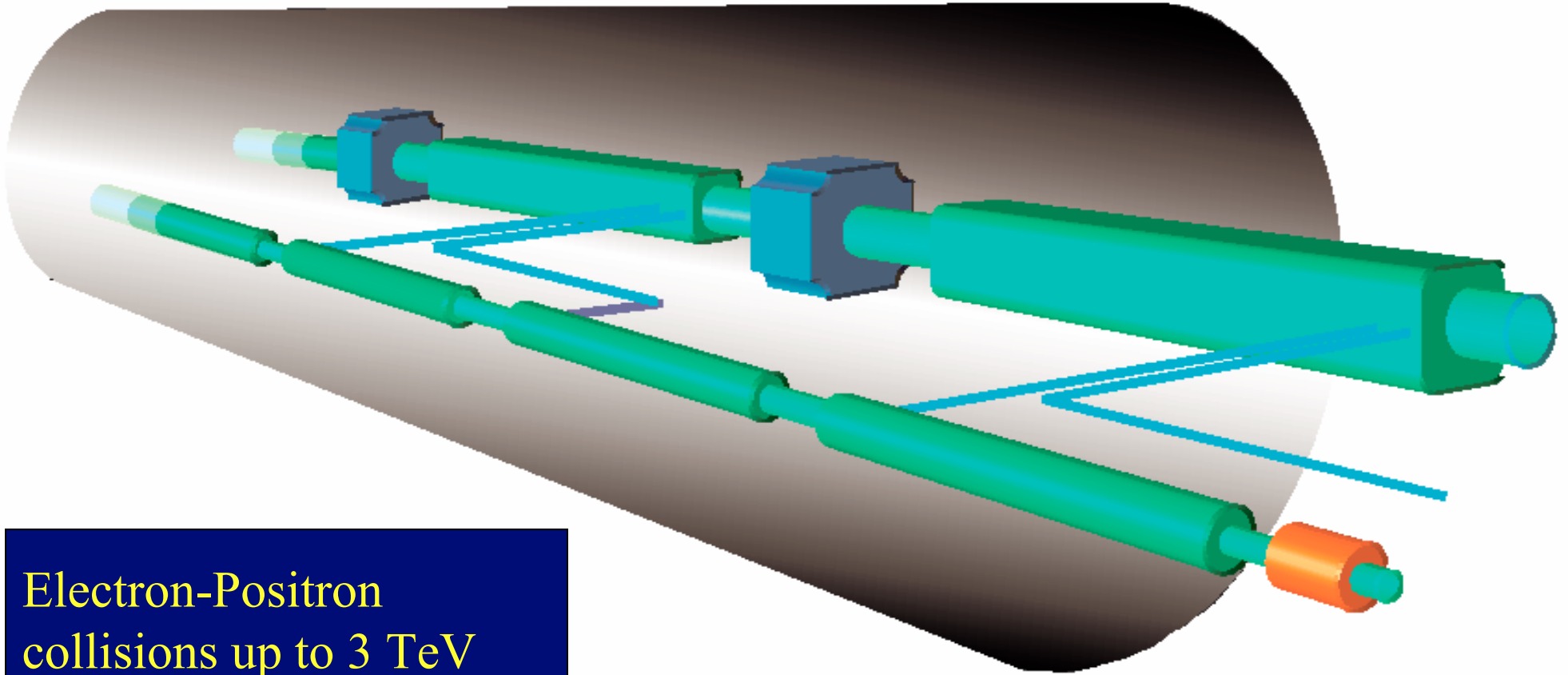
ILC

← Second lightest visible sparticle

Lightest visible sparticle →

JE + Olive + Santoso + Spanos

# After LHC @ CERN - CLIC?



Electron-Positron  
collisions up to 3 TeV

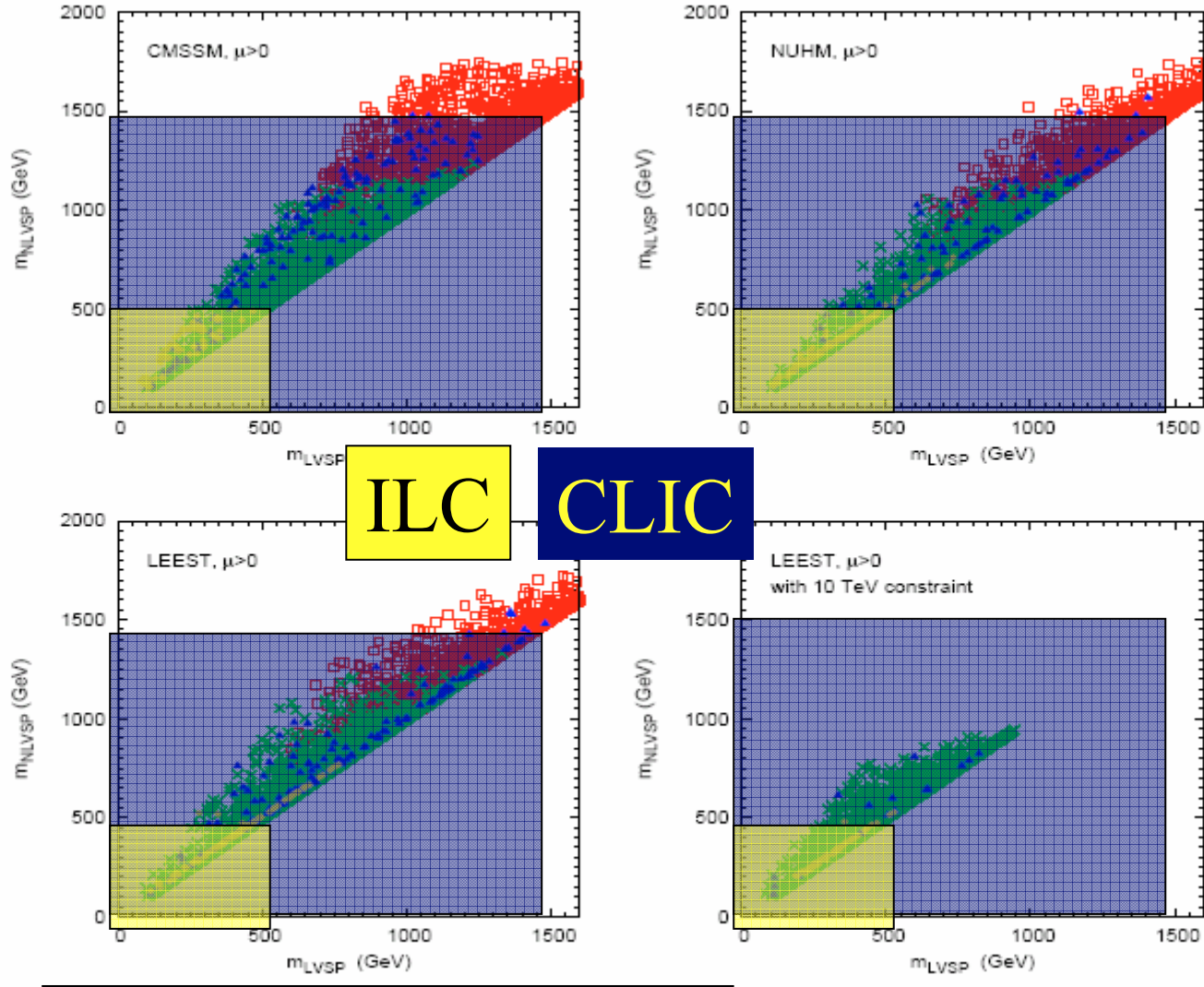
# Sparticles may not be very light

Full  
Model  
samples

Detectable  
@ LHC

Provide  
Dark Matter

Dark Matter  
Detectable  
Directly



← Second lightest visible sparticle

Lightest visible sparticle →

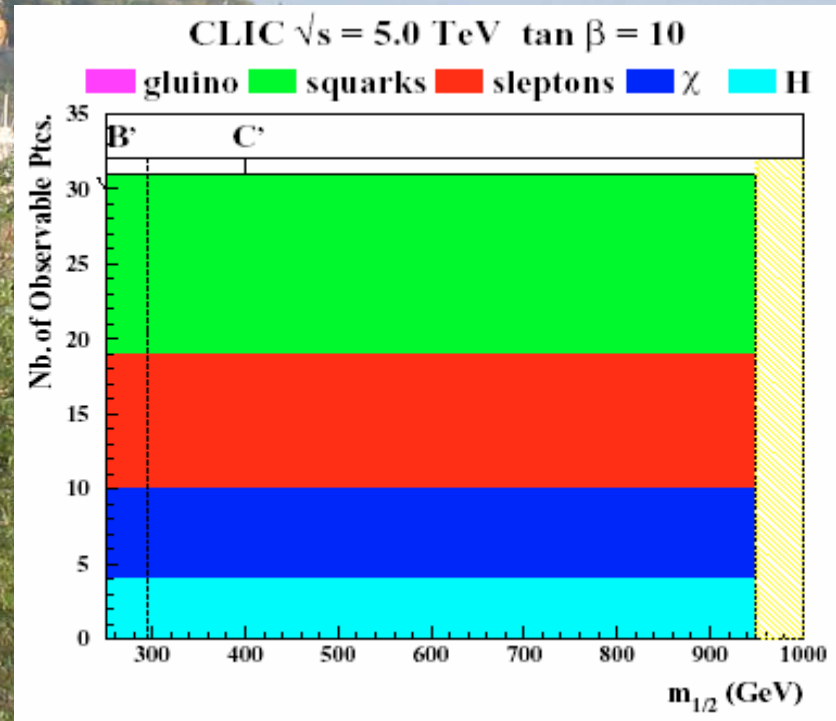
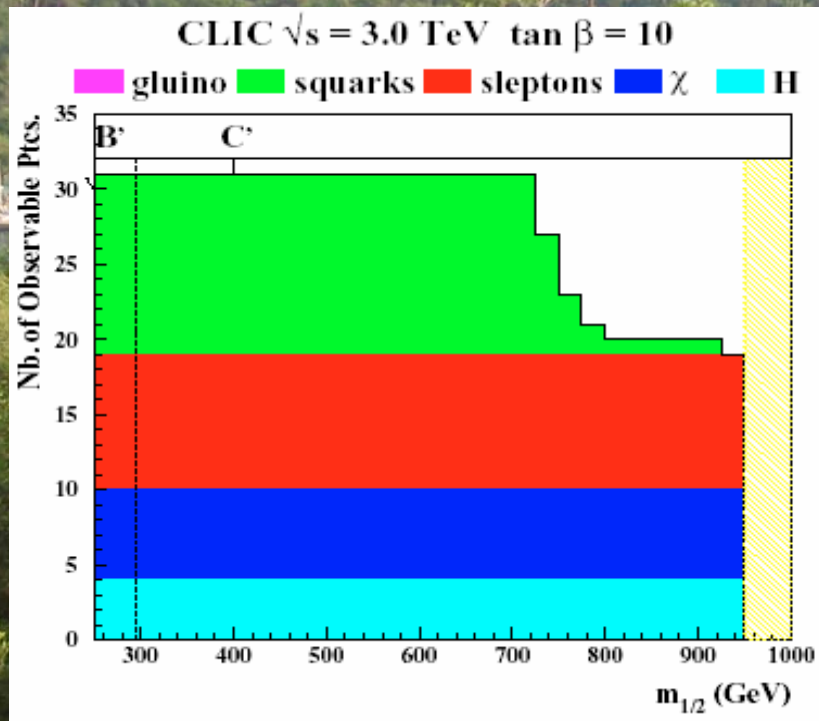
JE + Olive + Santoso + Spanos

# Sparticle Visibility at Higher E

CMSSM

3 TeV

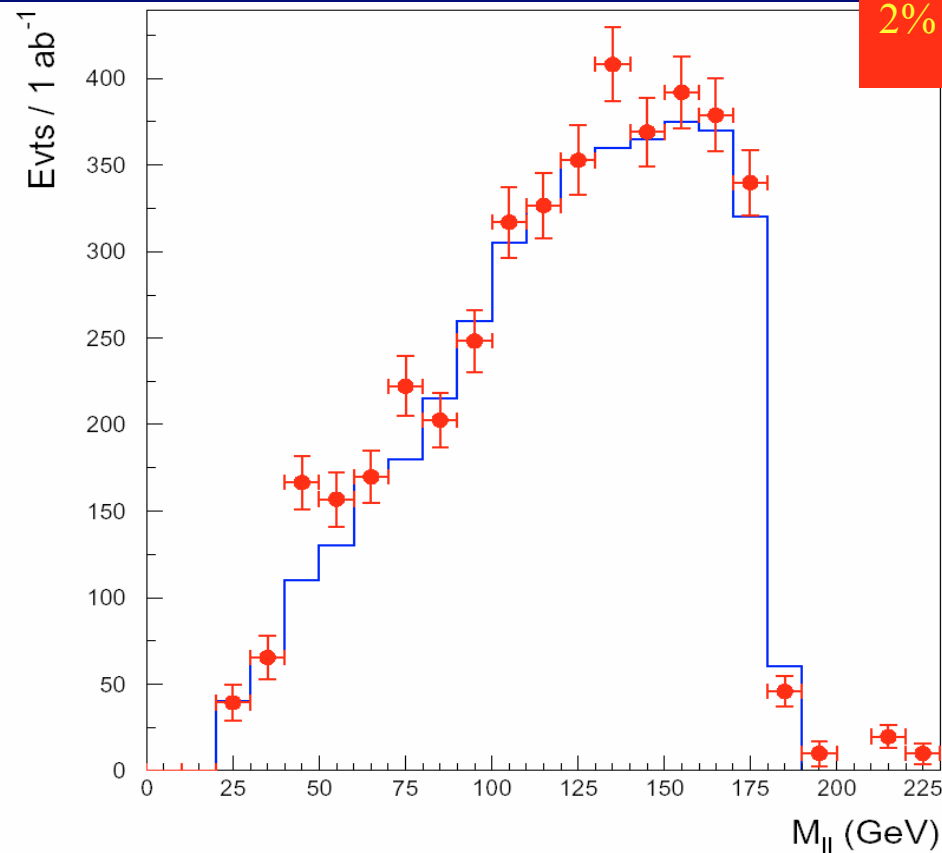
5 TeV



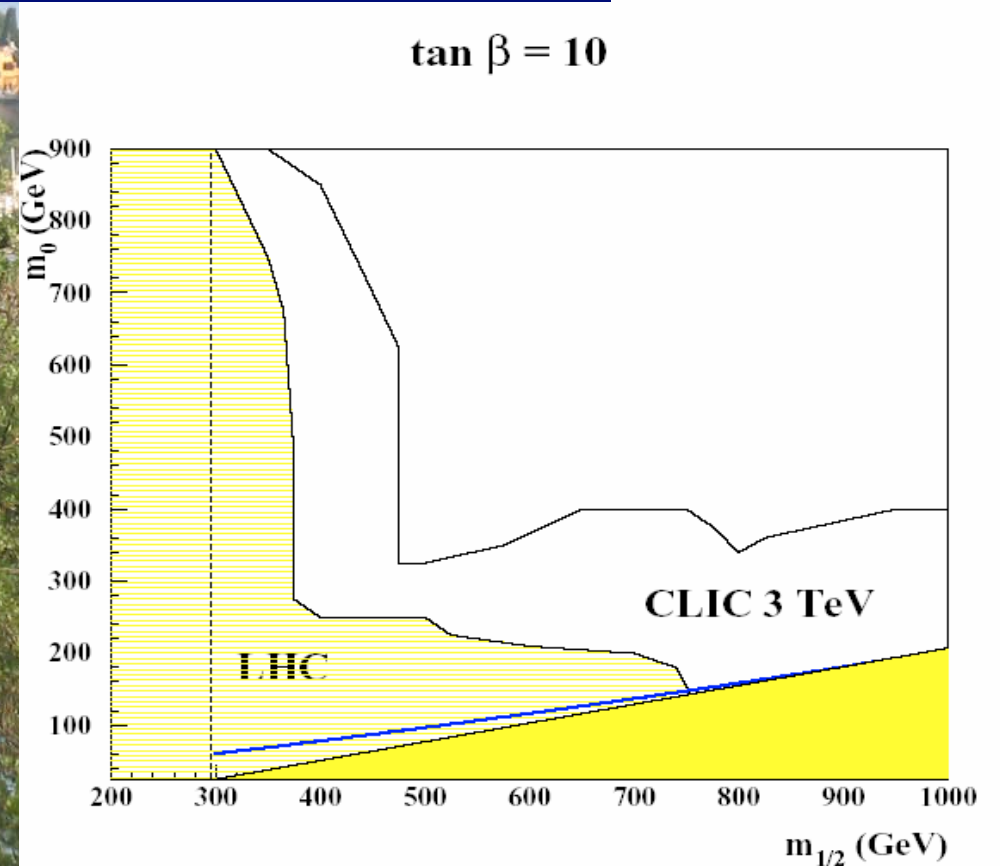
See 'all' sparticles: measure heavier ones better than LHC

# Example of CLIC Sparticle Search

## Dilepton spectrum in neutralino decay



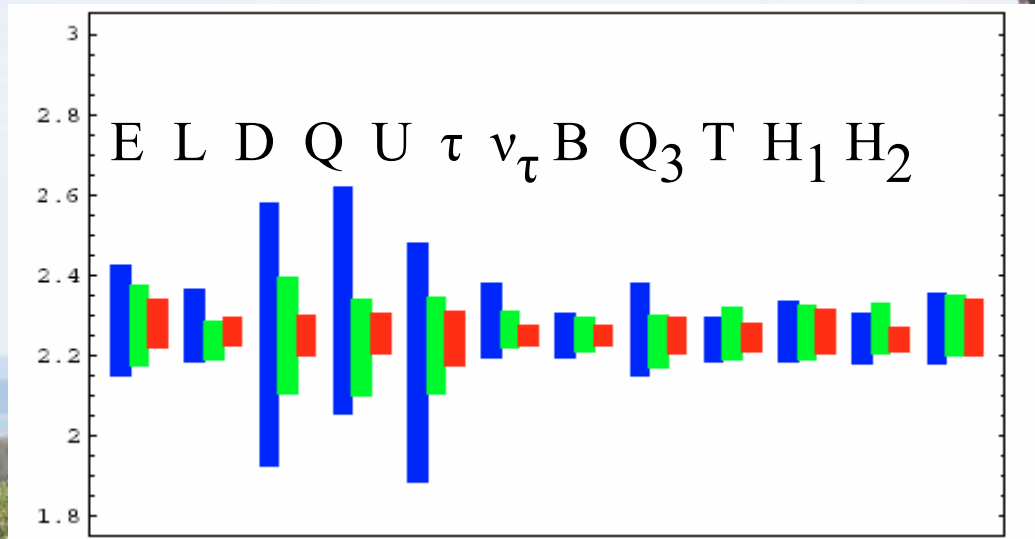
## Reach in parameter space



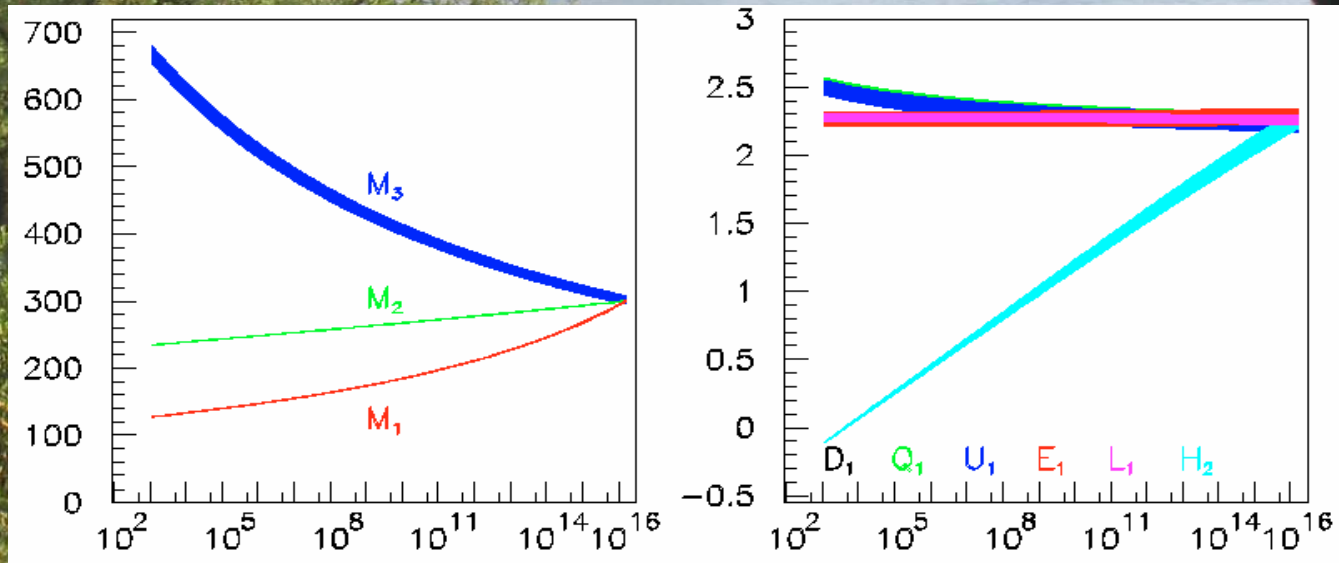


# Sparticle Mass Unification ?

Accuracy in measuring sparticle masses squared



Can test unification of sparticle masses – probe of string models?





# Physics at New Colliders

Lectures at the Summer School on Particle  
Physics

Abdus Salam ICTP, Trieste, June 2005

# Plan of the Lectures

- Status of the Standard Model
- Open issues beyond the Standard Model
- Origin of particle masses
- Search for the Higgs boson
- Supersymmetry
- Searches for supersymmetry
- Possible other new physics at colliders

A scenic view of a lake, likely Lake Michigan, framed by trees. In the foreground, there are green trees and a large, dark tree trunk on the right. In the middle ground, a yellow building with a tower sits on a hill overlooking a marina filled with sailboats. A large cargo ship is visible in the distance on the water. The sky is clear and blue.

# The Big Collider in the Sky

# Strategies for Detecting Supersymmetric Dark Matter

- Annihilation in galactic halo

$$\chi - \chi \rightarrow \text{antiprotons, positrons, ...?}$$

- Annihilation in galactic centre

$$\chi - \chi \rightarrow \gamma + \dots?$$

- Annihilation in core of Sun or Earth

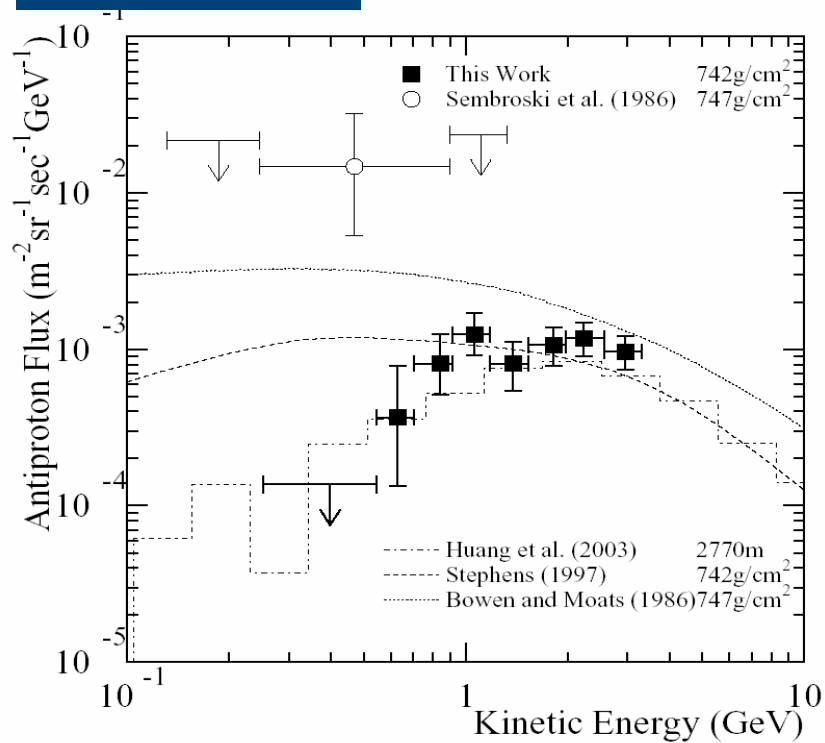
$$\chi - \chi \rightarrow \nu + \dots \rightarrow \mu + \dots$$

- Scattering on nucleus in laboratory

$$\chi + A \rightarrow \chi + A$$

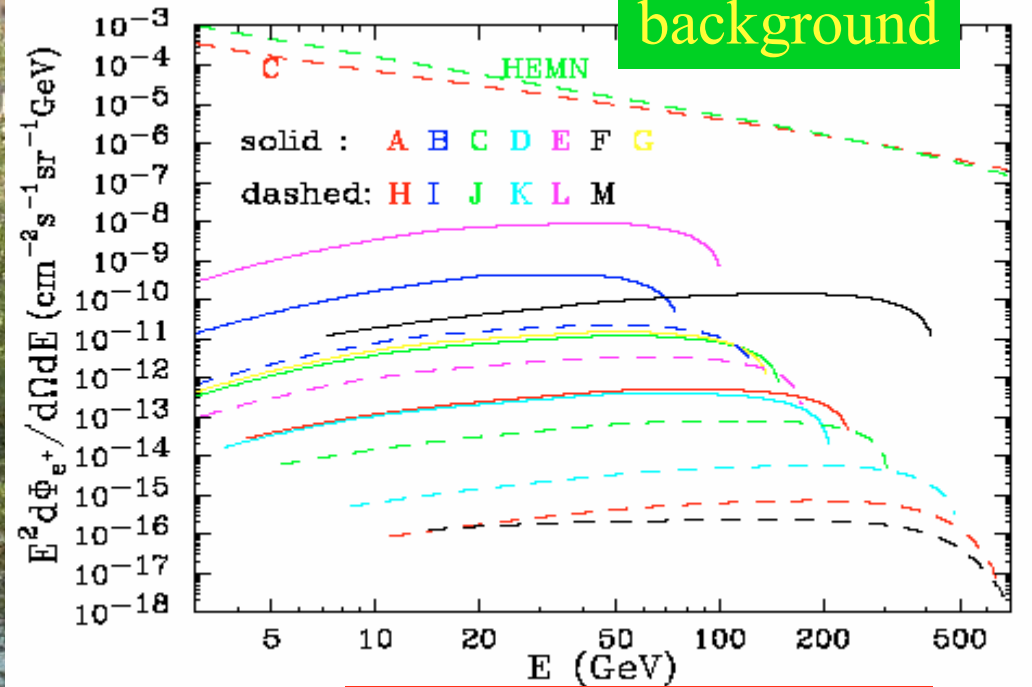
# Annihilation in Galactic Halo

## Antiprotons



Consistent with production by primary matter cosmic rays

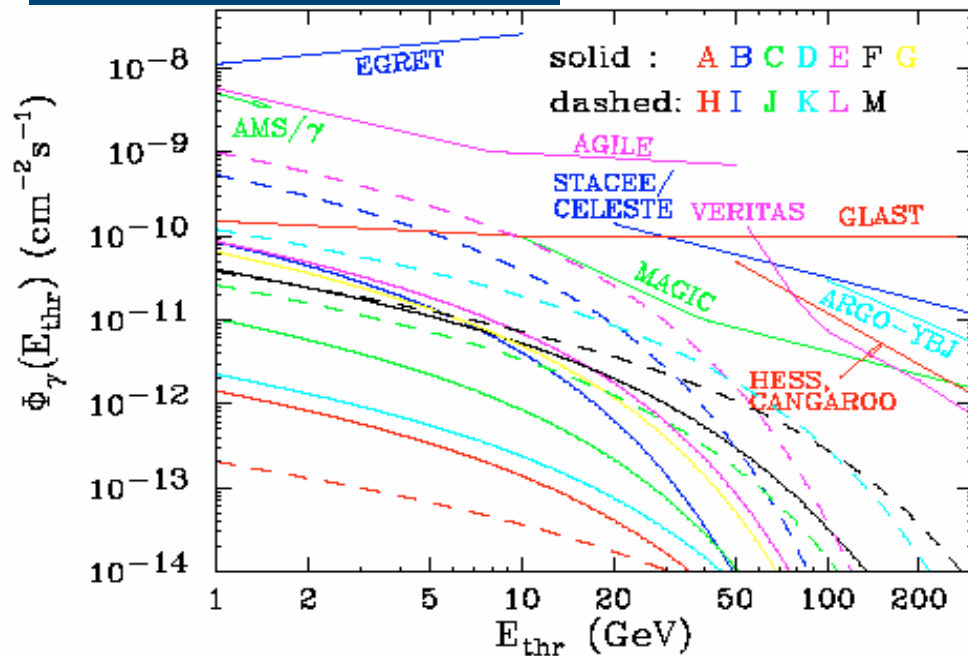
## Positrons



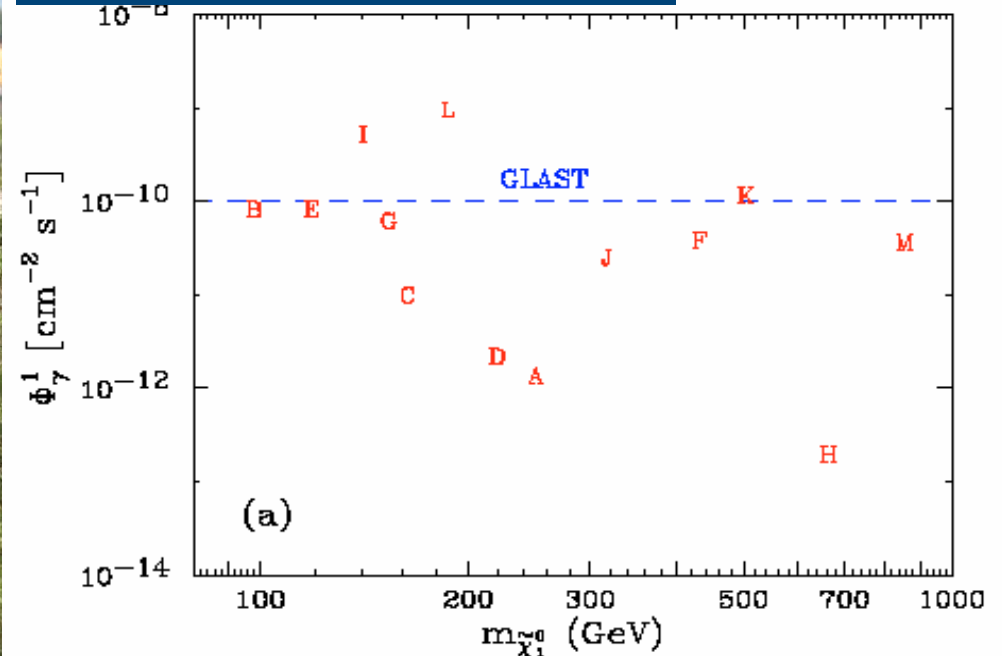
Benchmark scenarios

# Annihilations in Galactic Centre

## Benchmark spectra



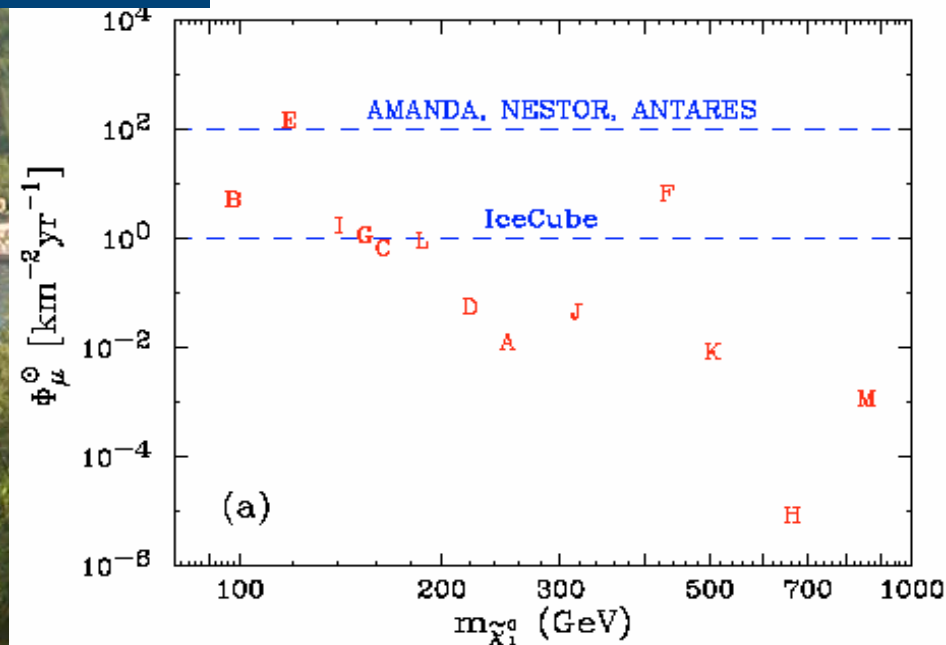
## Benchmarks $\rightarrow$ GLAST



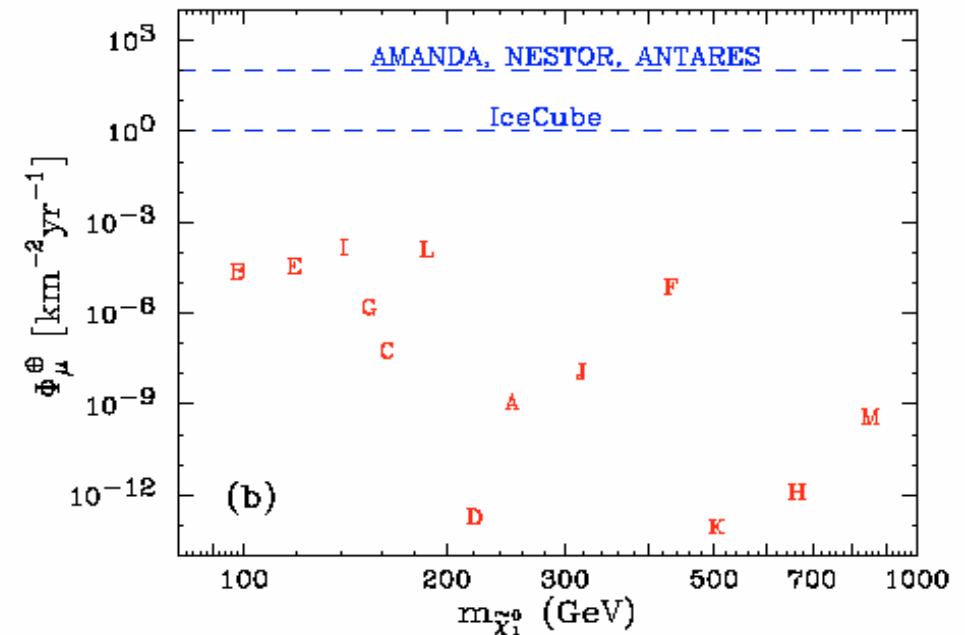
Enhancement of rate uncertain by factor  $> 100!$

# Annihilations in Solar System ...

... Sun



... Earth



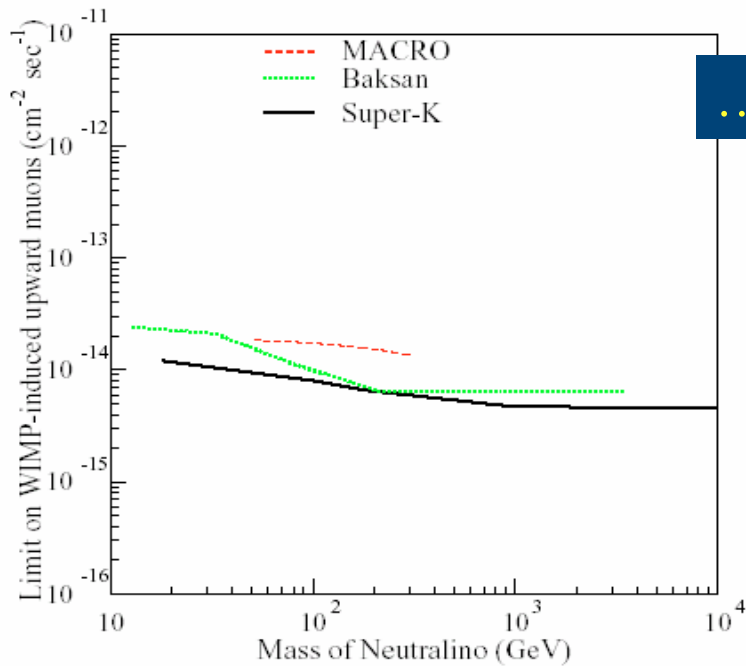
Prospective experimental sensitivities

Benchmark scenarios



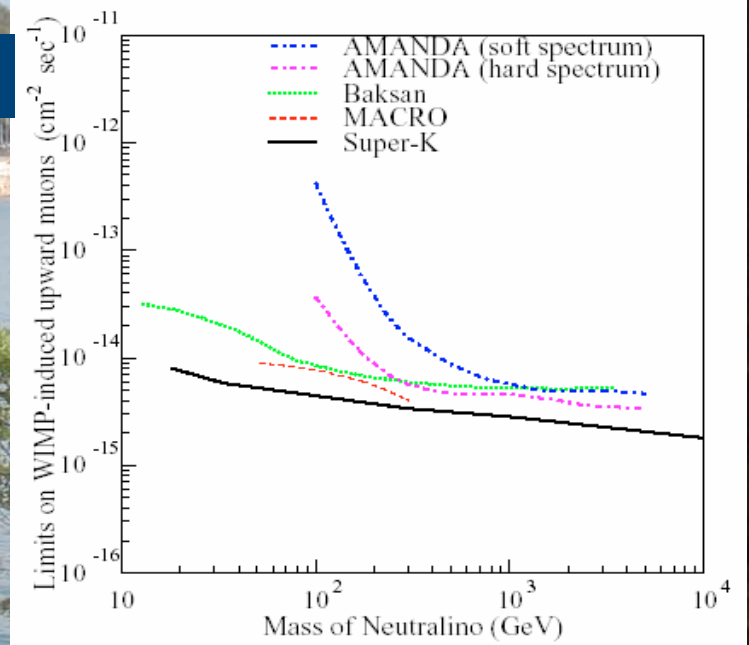
# Annihilations in Solar System ...

Present upper limits  $> 100/\text{km}^2/\text{year}$



... after capture inside ...

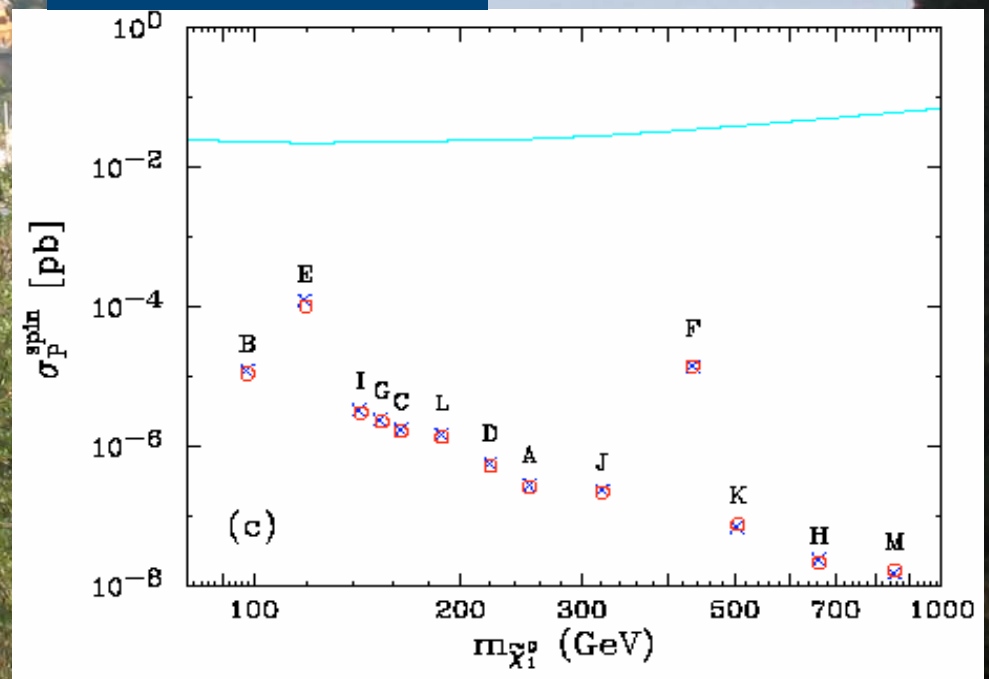
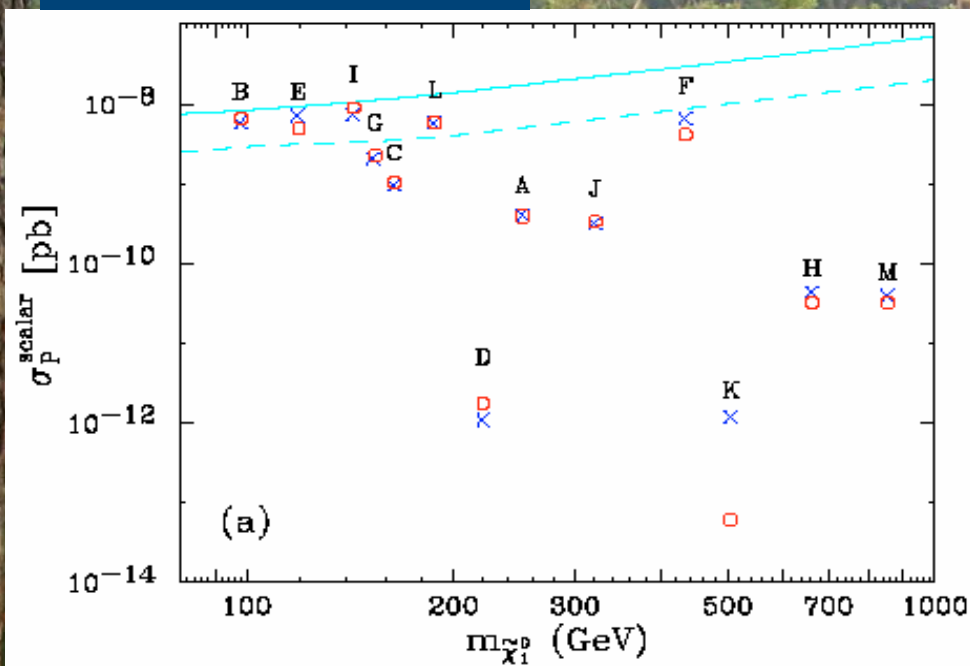
... Earth



# Scattering Cross Sections in Benchmark Scenarios

Spin-independent

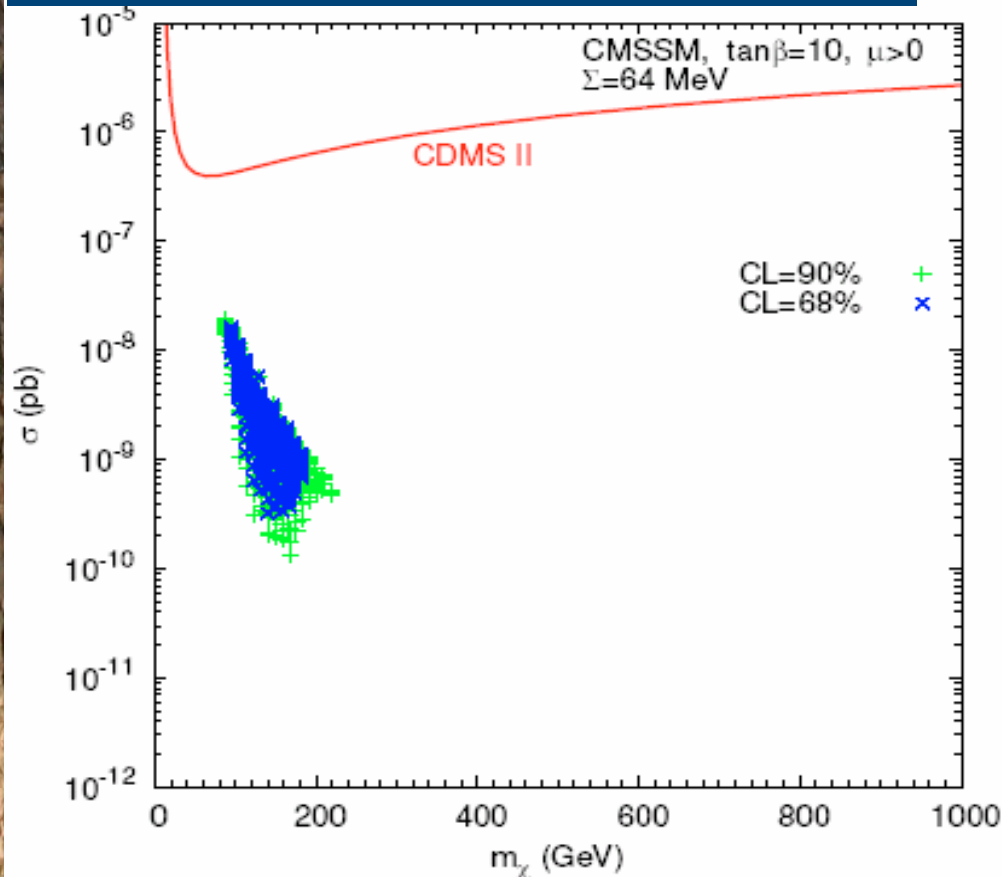
Spin-dependent



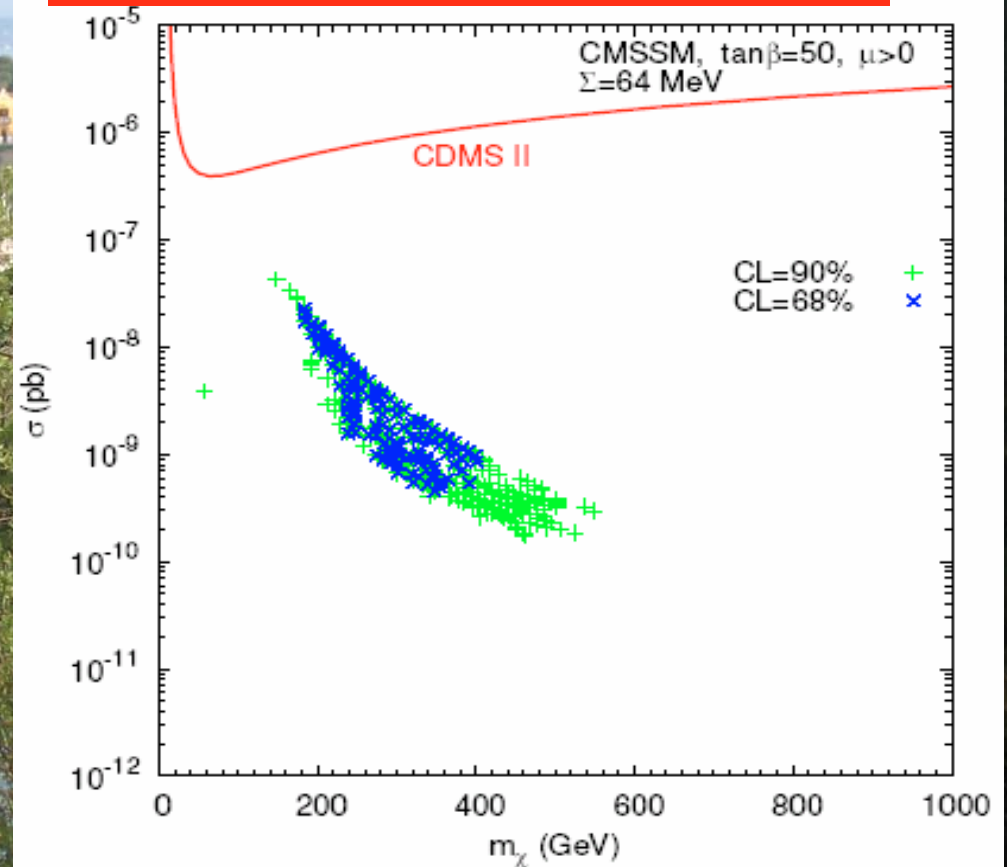
Compared with possible future experimental sensitivities

# Elastic Scattering Cross Sections

From global fit to accelerator data



Latest experimental upper limit



A scenic view of a coastal town, likely in the Adriatic region, featuring a prominent yellow building with a tower on a hillside overlooking a marina filled with sailboats. The view is framed by trees in the foreground and a clear blue sky above. In the distance, a large cargo ship is visible on the water.

# Beyond the CMSSM

# More General Supersymmetric Models

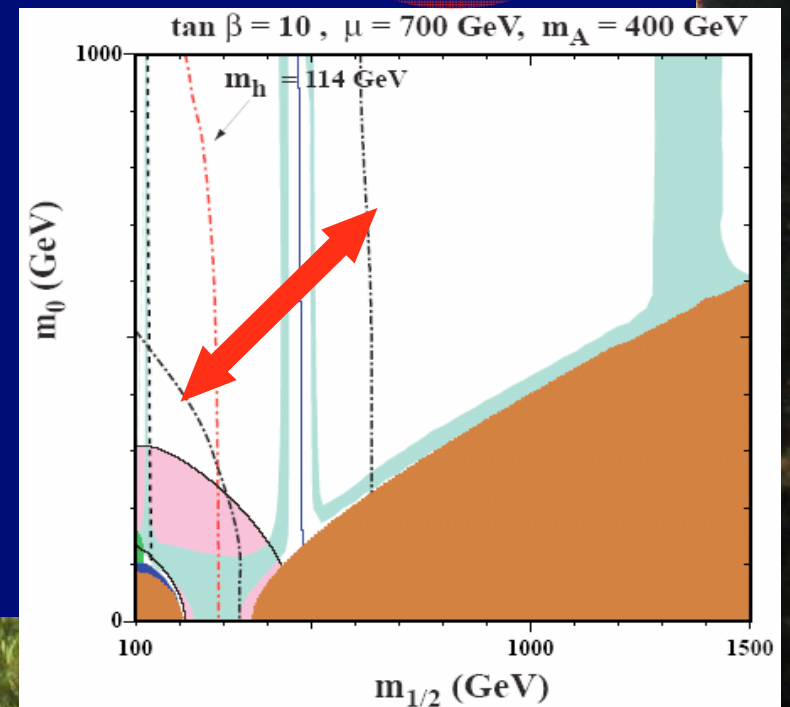
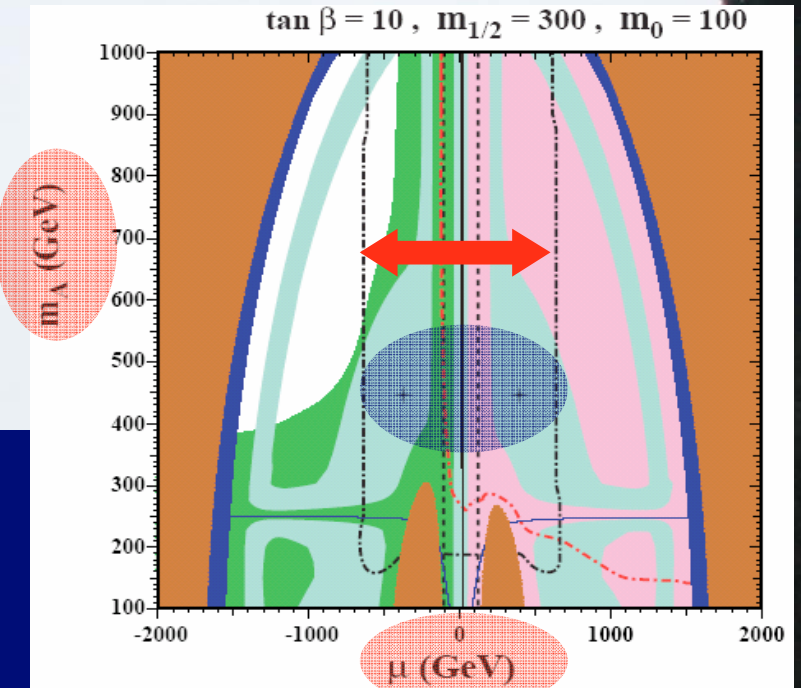
- MSSM with more general pattern of supersymmetry breaking:
  - non-universal scalar masses  $m_0$
  - and/or gaugino masses  $m_{1/2}$
  - and/or trilinear couplings  $A_0$
- Nature of the lightest supersymmetric particle (LSP)
- Extended particle content:
  - non-minimal supersymmetric model (NMSSM)

# Non-Universal Scalar Masses

- Different sfermions with same quantum #s?  
e.g., d, s squarks?  
disfavoured by upper limits on flavour-changing neutral interactions
- Squarks with different #s, squarks and sleptons?  
disfavoured in various GUT models  
e.g.,  $d_R = e_L$ ,  $d_L = u_L = u_R = e_R$  in SU(5), all in SO(10)
- Non-universal susy-breaking masses for Higgses?  
No reason why not!

# Non-Universal Higgs Masses

- Generalize CMSSM (+)  
$$m_{H_i}^2 = m_0^2(1 + \delta_i)$$
- Free Higgs mixing  $\mu$ ,  
pseudoscalar mass  $m_A$
- Larger parameter space
- Constrained by vacuum  
stability



# Possible Nature of LSP

- No strong or electromagnetic interactions  
Otherwise would bind to matter  
Detectable as anomalous heavy nucleus
- Possible weakly-interacting candidates  
Sneutrino  
(Excluded by LEP, direct searches)  
Lightest neutralino  $\chi$   
Gravitino  
(nightmare for detection)



# Possible Nature of NLSP

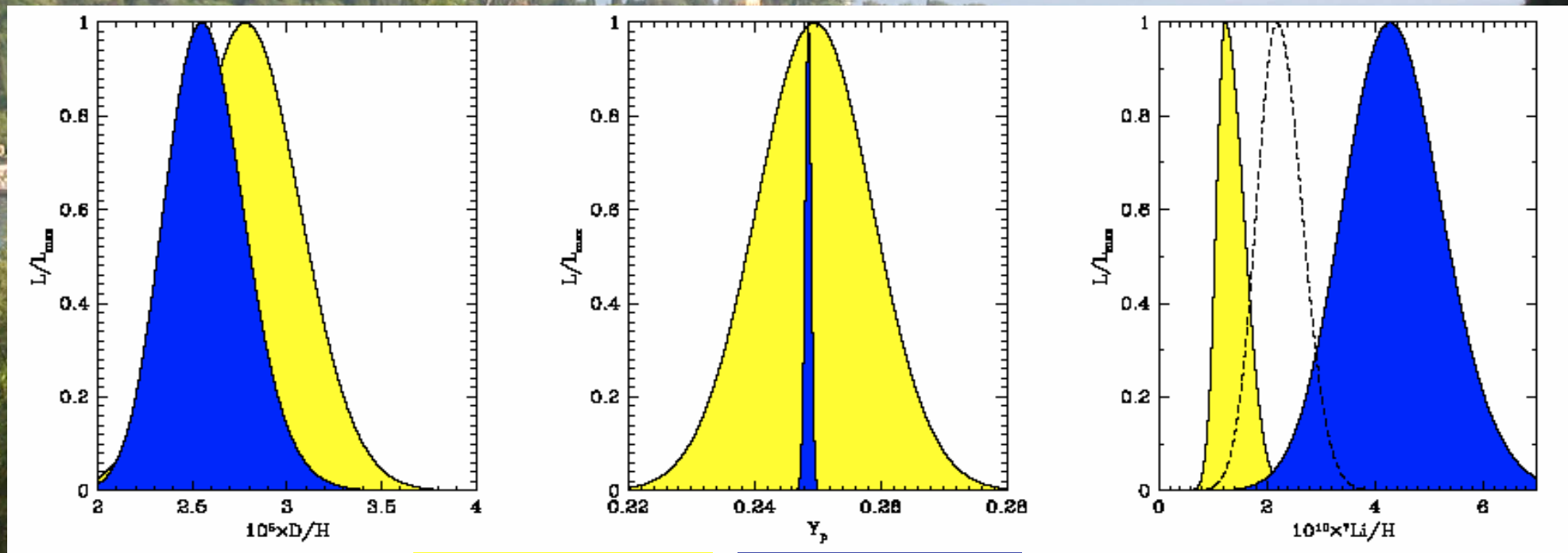
- NLSP = next-to-lightest sparticle
- Very long lifetime due to gravitational decay, e.g.:

$$\Gamma_{\tilde{\tau} \rightarrow \tilde{G} \tau} = \frac{1}{48\pi} \frac{1}{M_P^2} \frac{m_{\tilde{\tau}}^5}{m_{3/2}^2} \left(1 - \frac{m_{3/2}^2}{m_{\tilde{\tau}}^2}\right)^4$$

- **Could be hours, days, weeks, months or years!**
- Generic possibilities:
  - lightest neutralino  $\chi$
  - lightest slepton, probably lighter stau
- Constrained by astrophysics/cosmology

# Light Nuclei: BBN vs CMB

Good agreement for D/H,  $^4\text{He}$ : discrepancy for  $^7\text{Li}$ ?



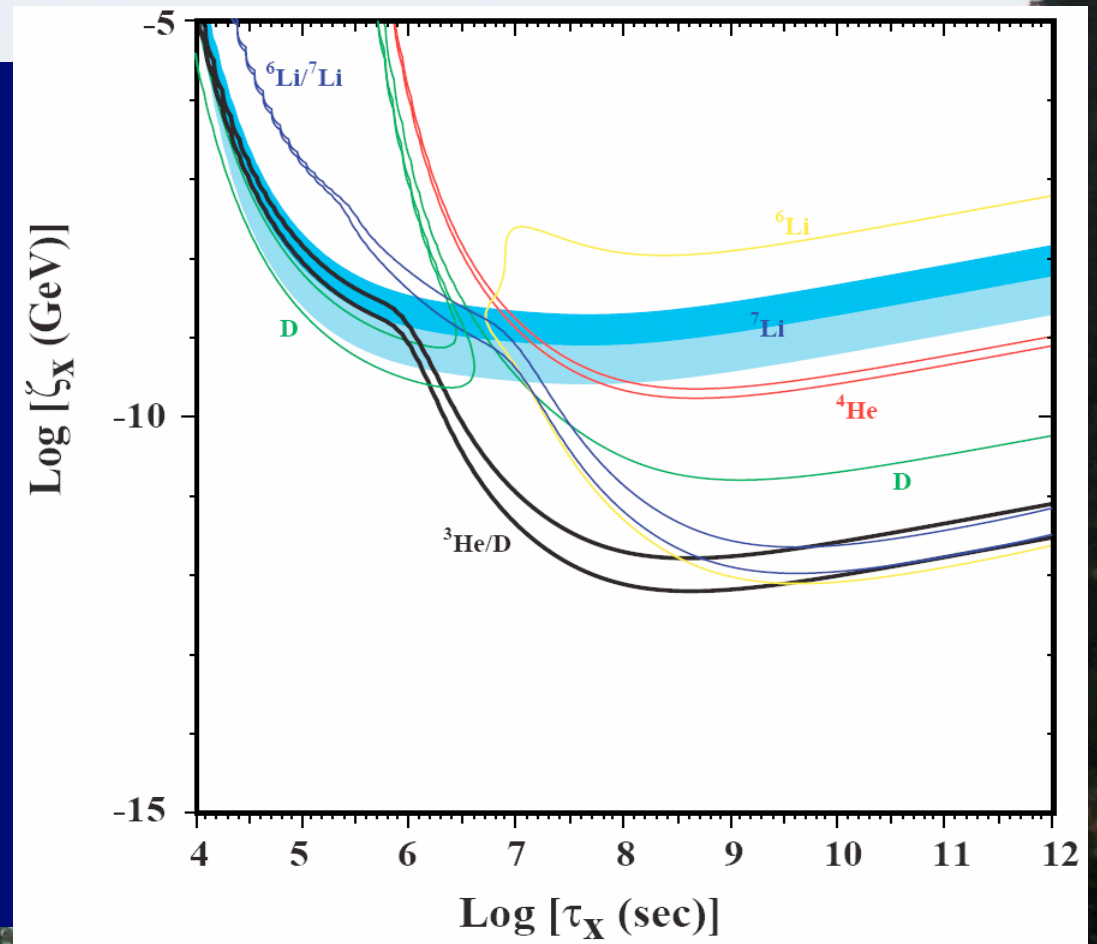
Observations

Calculations

Cyburt + Fields + Olive + Skillman

# Constraints on Unstable Relics

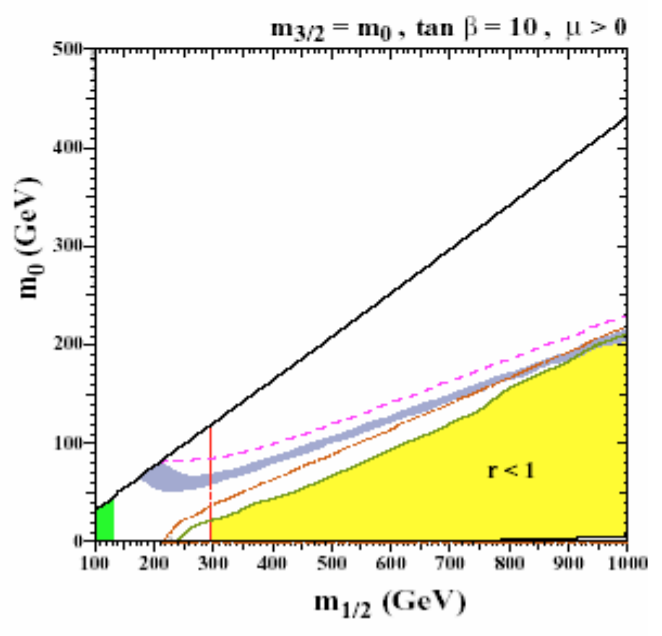
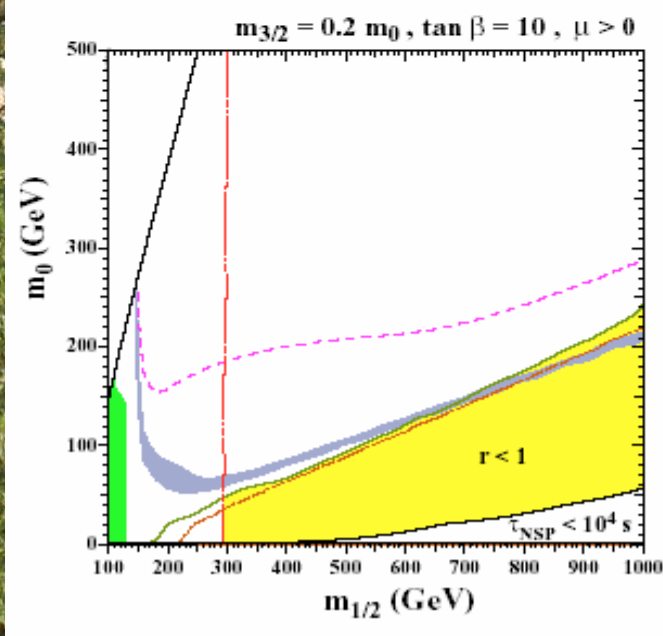
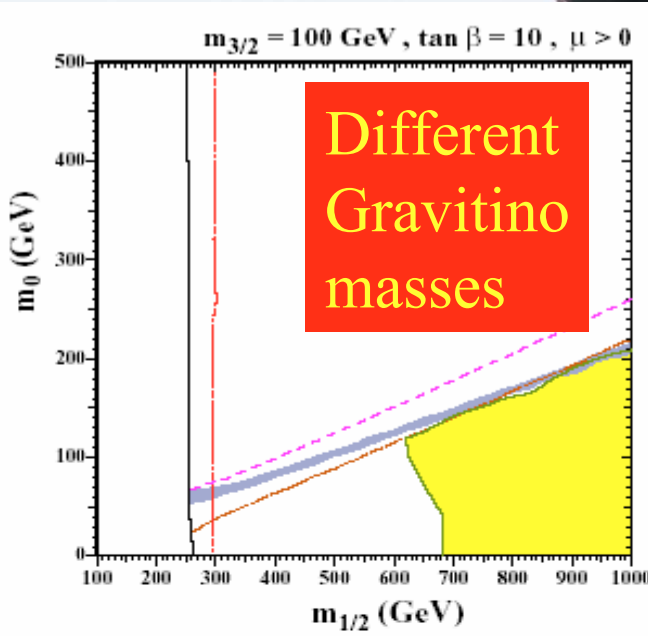
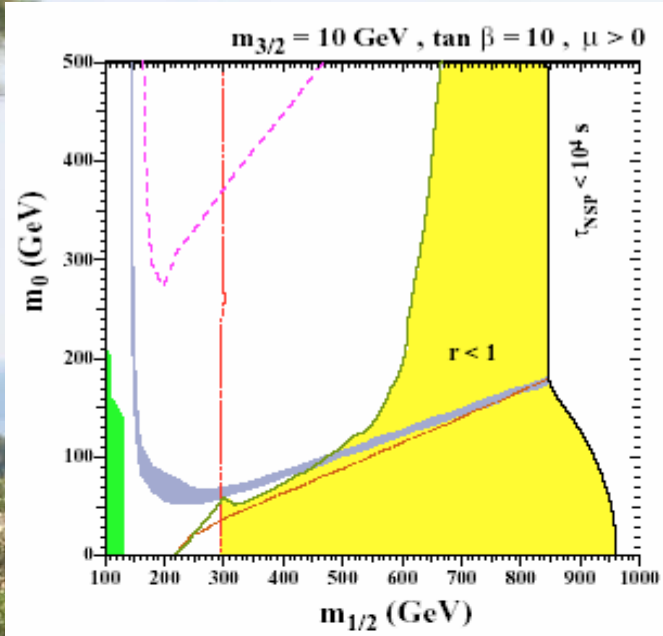
- ${}^7\text{Li} < \text{BBN?}$
- Effect of relic decays?
- Problems with D/H
- ${}^3\text{He}/\text{D}$  too high!
- Interpret as upper limits on abundance of metastable heavy relics



# Different Regions of Sparticle Parameter Space if Gravitino LSP

Density below WMAP limit

Decays do not affect BBN/CMB agreement



# Minimal Supergravity Model

More constrained than CMSSM:  $m_{3/2} = m_0$ ,  $B_\lambda = A_\lambda - 1$

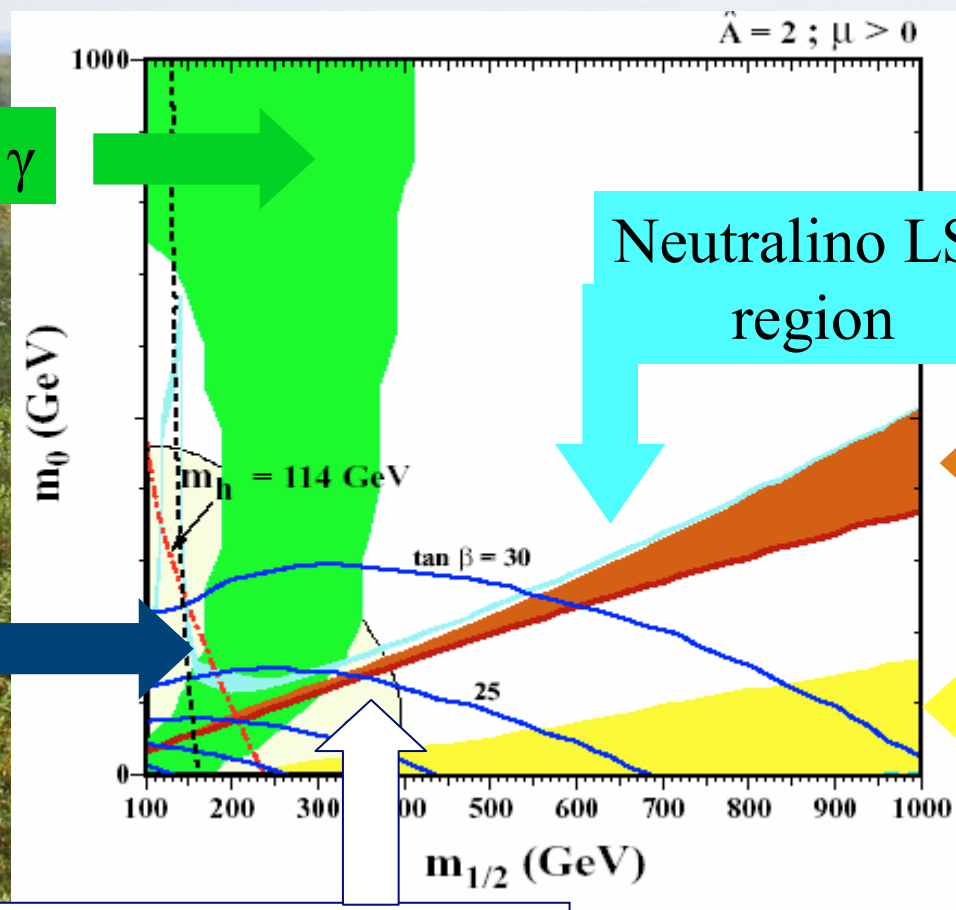
Excluded by  $b \rightarrow s \gamma$

Neutralino LSP region

stau LSP (excluded)

LEP constraints  
On  $m_h$ , chargino

Gravitino LSP region



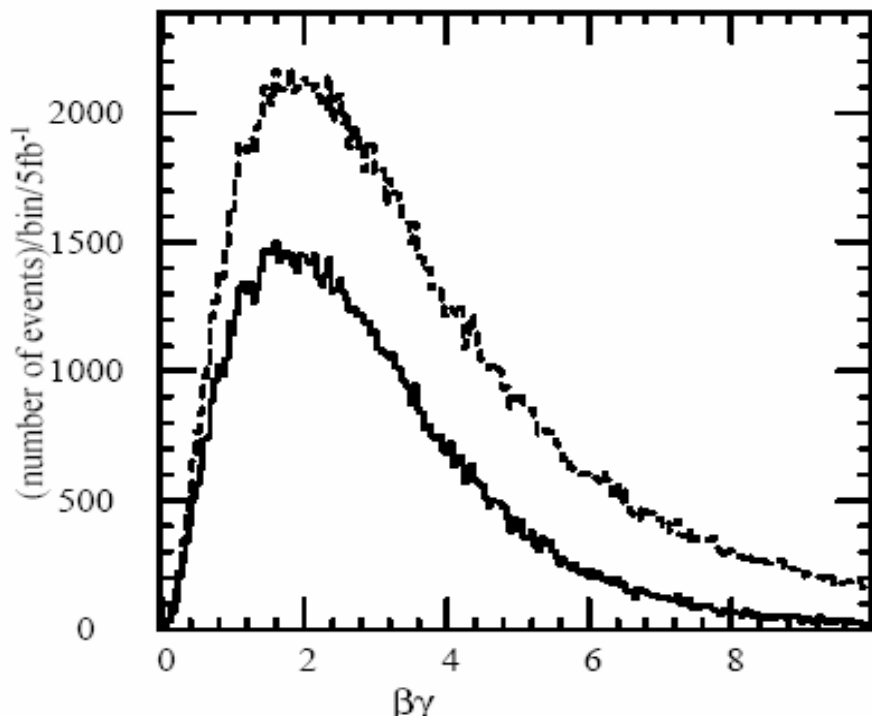
$\tan \beta$  fixed by vacuum conditions

JE + Olive + Santoso + Spanos

# Slepton Trapping at the LHC?

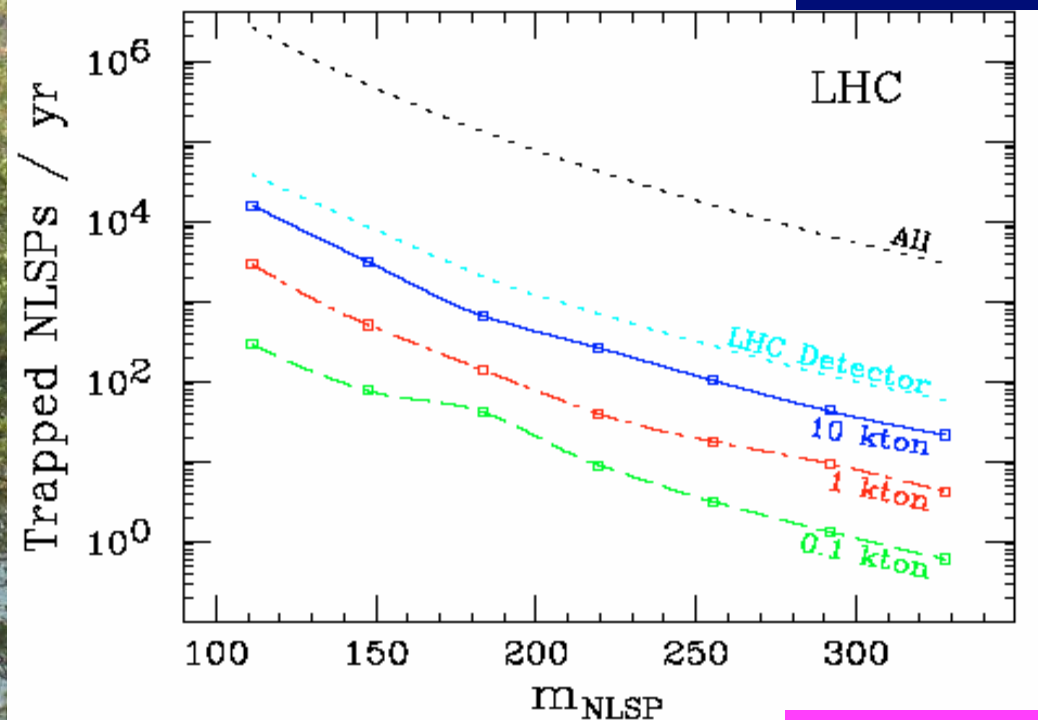
If stau next-to-lightest sparticle (NLSP)  
may be metastable  
may be stopped in detector/water tank

Kinematics



Hamaguchi + Kuno + Nakaya + Nojiri

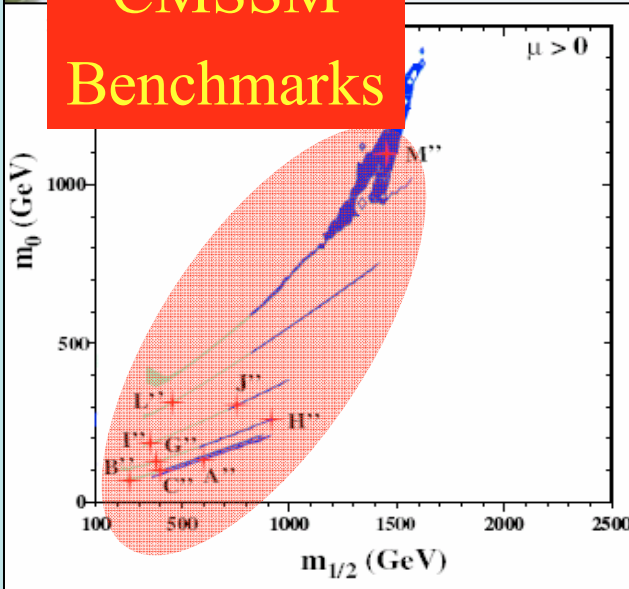
Trapping  
rate



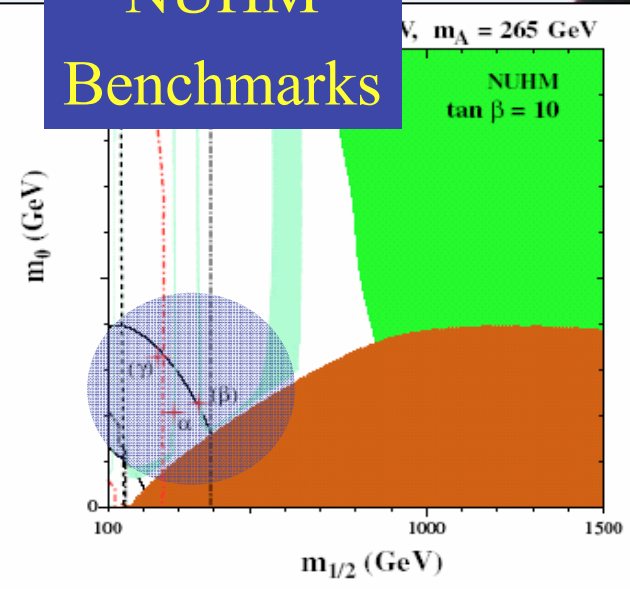
Feng + Smith

# Regions Allowed in Different Scenarios for Supersymmetry Breaking

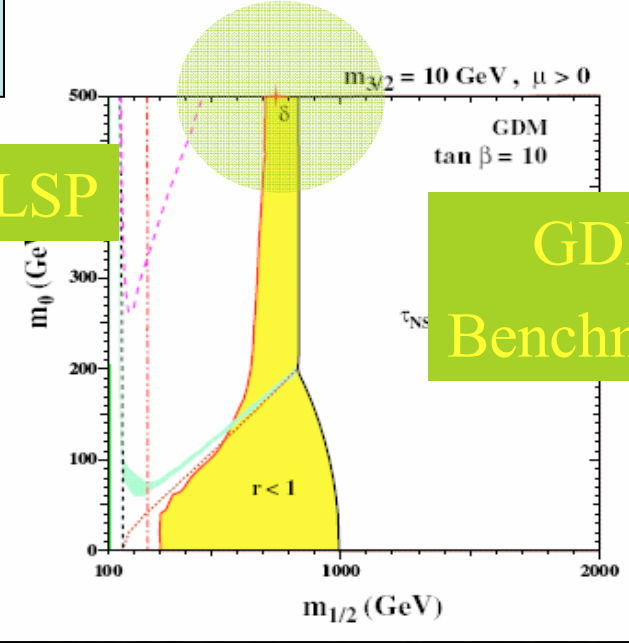
**CMSSM Benchmarks**



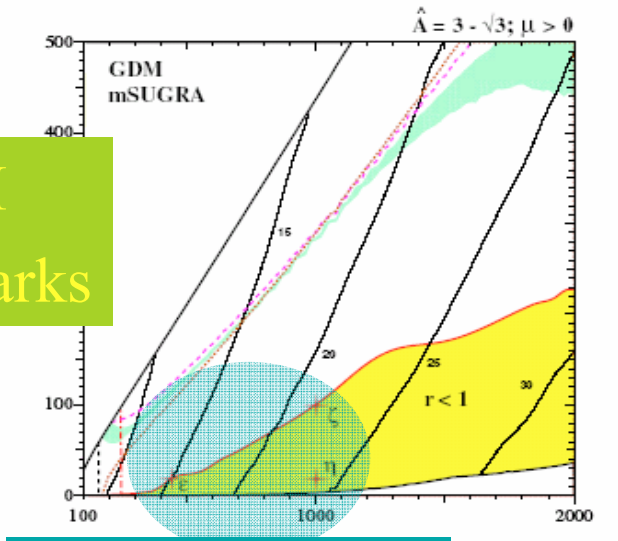
**NUHM Benchmarks**



**with neutralino NLSP**



**GDM Benchmarks**



**with stau NLSP**

# Spectra in NUHM and GDM Benchmark Scenarios

Typical example of  
non-universal Higgs masses:

$$m_{H_1}^2 = -(333\text{GeV})^2, \quad m_{H_2}^2 = +(294\text{GeV})^2$$

Models with gravitino LSP

Models with stau NLSP

Model	$\alpha$	$\beta$	$\gamma$	$\delta$	$\epsilon$	$\zeta$	$\eta$
$m_{1/2}$	285	360	240	750	440	1000	1000
$m_0$	210	230	330	500	20	100	20
$\tan\beta$	10	10	20	10	15	21.5	23.7
$\text{sign}(\mu)$	+	+	+	+	+	+	+
$A_0$	0	0	0	0	25	127	25
$m_t$	178	178	178	178	178	178	178
Masses							
$ \mu $	375	500	325	978	610	1176	1161
$h^0$	115	117	114	122	119	124	124
$H^0$	266	325	240	1177	641	1307	1277
$A^0$	265	325	240	1177	641	1307	1277
$H^\pm$	277	335	253	1179	646	1310	1279
$\chi_1^0$	113	146	95	323	183	436	436
$\chi_2^0$	212	279	178	625	349	840	840
$\chi_3^0$	388	515	341	954	578	1176	1165
$\chi_4^0$	406	528	358	964	593	1186	1175
$\chi_{1\pm}^{\pm}$	212	279	177	625	349	840	840
$\chi_{2\pm}^{\pm}$	408	529	360	965	594	1186	1176
$g$	674	835	575	1610	986	2097	2097
$e_L, \mu_L$	296	346	376	702	298	664	657
$e_R, \mu_R$	216	241	328	571	169	383	370
$\nu_e, \nu_\mu$	285	337	367	697	287	660	652
$\tau_1$	212	239	315	564	150	340	322
$\tau_2$	298	348	377	700	302	661	655
$\nu_\tau$	285	337	364	695	285	651	644
$u_L, c_L$	648	793	612	1532	897	1892	1889
$u_R, c_R$	637	778	607	1480	867	1817	1814
$d_L, s_L$	653	797	617	1534	901	1893	1891
$d_R, s_R$	630	768	599	1474	864	1807	1805
$t_1$	471	596	433	1159	682	1465	1472
$t_2$	652	784	600	1429	879	1758	1756
$b_1$	590	727	540	1395	824	1726	1723
$b_2$	629	767	594	1468	862	1781	1775



# Properties of NUHM and GDM Models

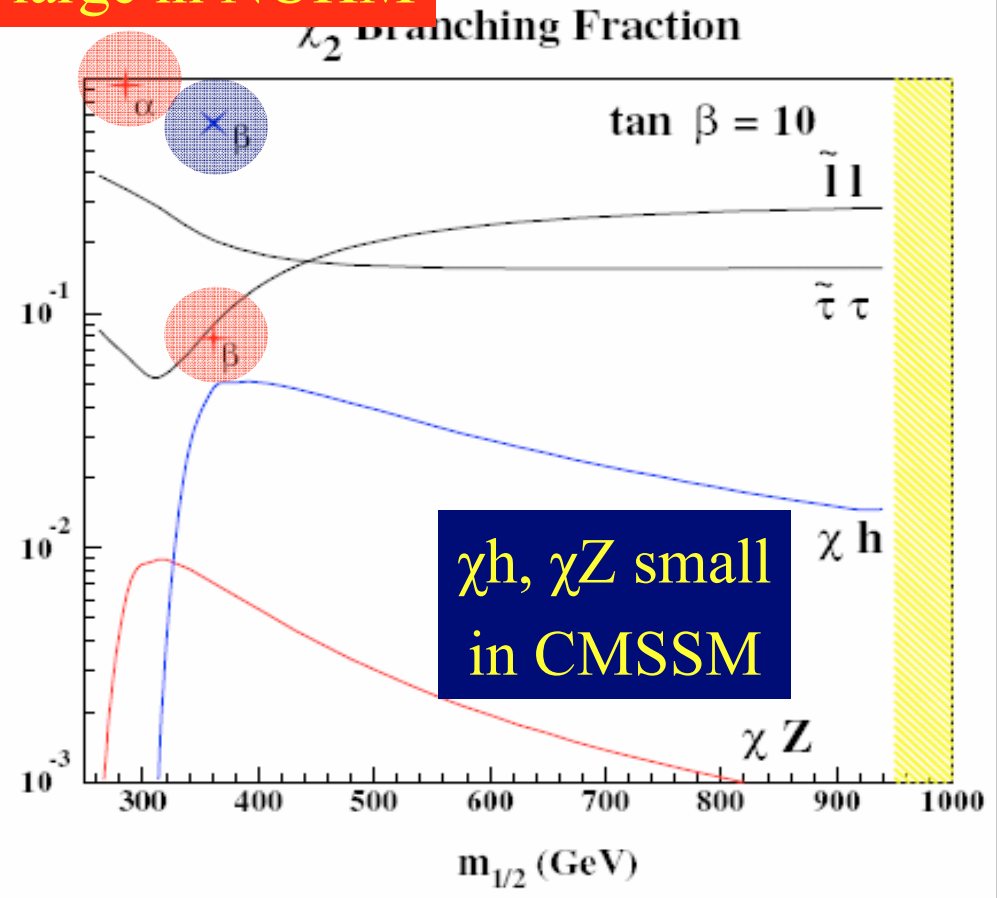
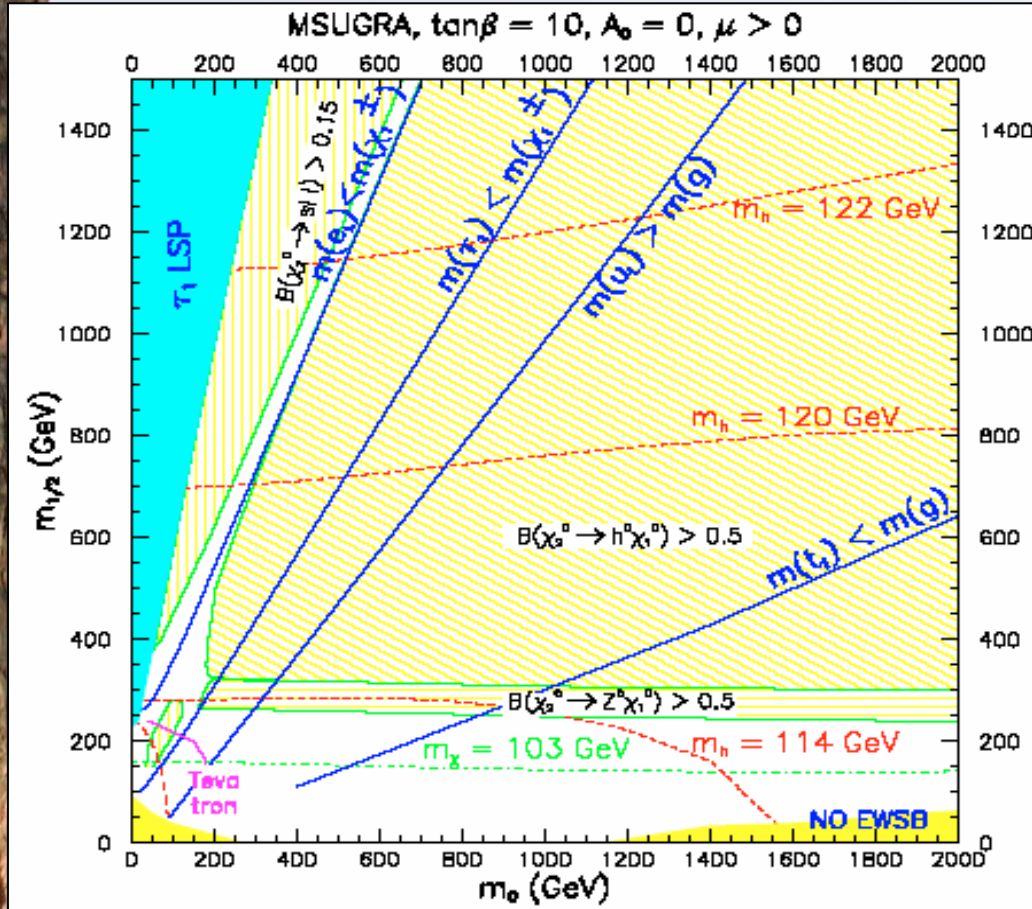
Relic density  $\Omega_\chi h^2$ ,  $b \rightarrow s\gamma$  and  $g_\mu - 2$  in post-WMAP benchmark scenarios, also  $\tau_{NLSP}$  in the GDM models

	$\alpha$	$\beta$	$\gamma$	$\delta$	$\epsilon$	$\zeta$	$\eta$
$\Omega_{LSP} h^2$	0.12	0.10	0.09	0.07	$1.0 \times 10^{-3}$	$0.9 \times 10^{-2}$	$1.6 \times 10^{-3}$
$\delta a_\mu (10^{-9})$	1.5	1.0	2.6	0.2	1.8	0.5	0.5
$B_{s\gamma} (10^{-4})$	4.1	4.4	2.8	3.7	3.6	3.6	3.6
$\tau_{NLSP} (s)$	$\infty$	$\infty$	$\infty$	$1.8 \times 10^4$	$3.3 \times 10^6$	$2.0 \times 10^6$	$6.8 \times 10^4$

- Relic density  $\sim$  WMAP in NUHM models
- Generally  $<$  WMAP in GDM models
  - Need extra source of gravitinos at high temperatures, after inflation?
- NLSP lifetime:  $10^4 s < \tau < \text{few } \times 10^6 s$

# Neutralino Masses and Decay Modes

$\chi h, \chi Z$  may be large in NUHM



# Final States in GDM Models with Stau NLSP

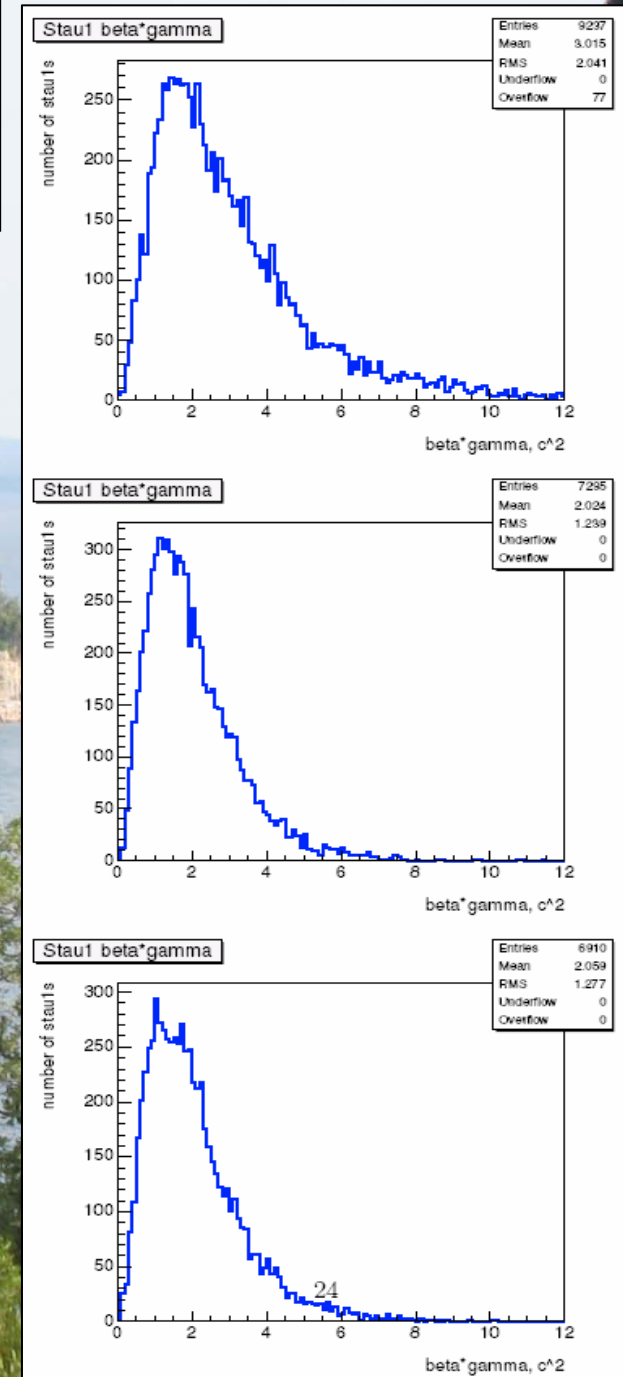
- All decay chains end with lighter stau
- Generally via  $\chi$
- Often via heavier sleptons
- Final states contain 2 staus, 2  $\tau$ , often other leptons

Final state	$\epsilon$	$\zeta$	$\eta$
via $\chi_2^0$			
$\tilde{q}_L \rightarrow qll\tilde{\tau}_1\tau$	6%	7%	6%
$\tilde{q}_L \rightarrow qlll'\tilde{\tau}_1\tau$	0.5%	2.3%	2.9%
$\tilde{q}_L \rightarrow q(Z^0, h^0)\tilde{\tau}_1\tau$	1.3%	4%	4%
$\tilde{q}_L \rightarrow q\tau\tau\tilde{\tau}_1\tau$	1.2%	0.8%	0.6%
$\tilde{q}_L \rightarrow q\tau\tau ll\tilde{\tau}_1\tau$	0.1%	0.3%	0.3%
$\tilde{q}_L \rightarrow q\tilde{\tau}_1\tau$	4%	1.3%	1.5%
decays with $\nu_s$	18%	17%	17%
via $\chi_1^\pm$			
$\tilde{q}_L \rightarrow q'W\tilde{\tau}_1\tau$	6%	10%	10%
decays with $\nu_s$	57%	56%	54%
via $\chi_1^0$			
$\tilde{q}_R \rightarrow q\tilde{\tau}_1\tau$	92%	75%	69%
$\tilde{q}_R \rightarrow qll\tilde{\tau}_1\tau$	8%	25%	31%

# Stau Momentum Spectra

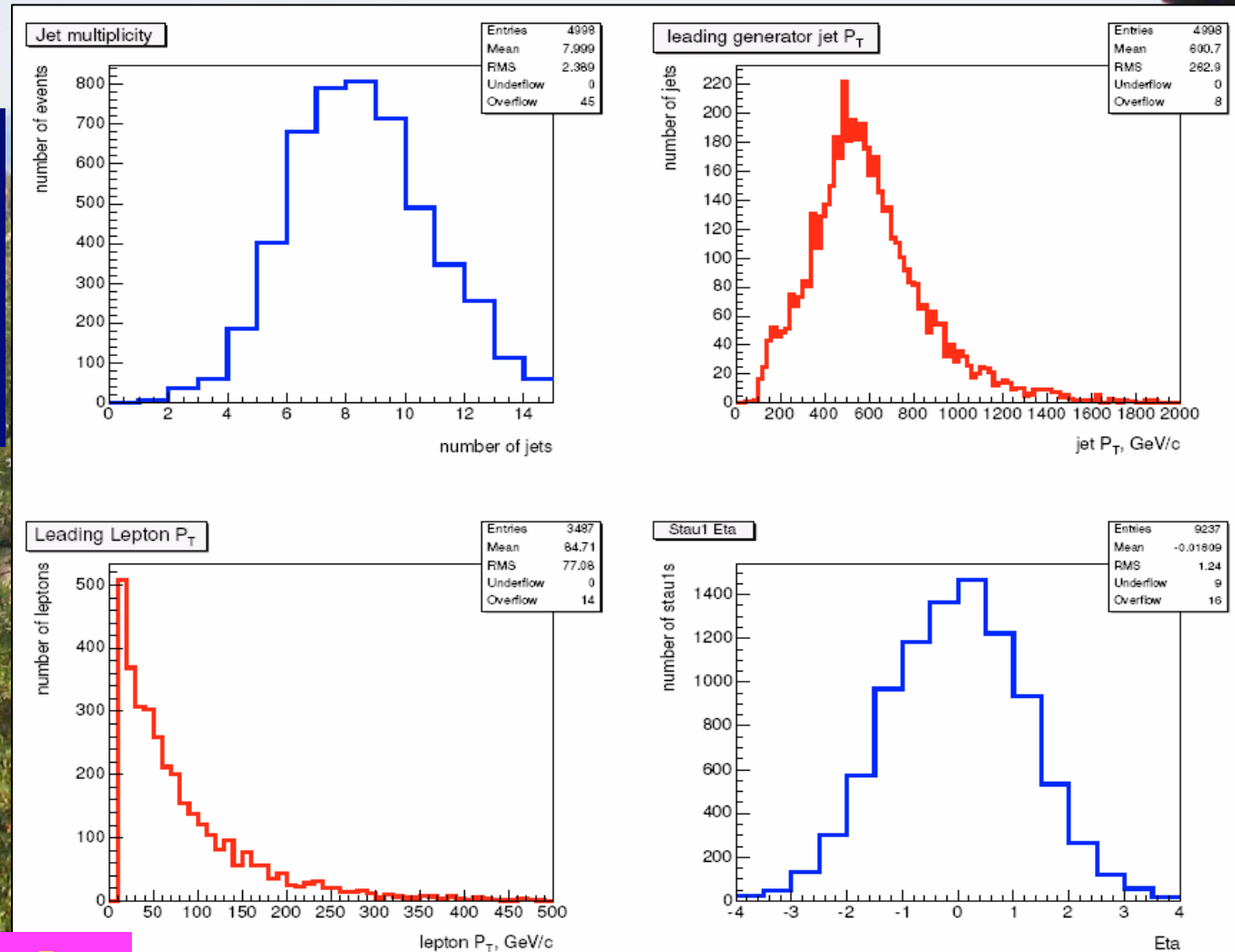
- $\beta\gamma$  typically peaked  $\sim 2$
- Staus with  $\beta\gamma < 1$  leave central tracker after next beam crossing
- Staus with  $\beta\gamma < 1/4$  trapped inside calorimeter
- Staus with  $\beta\gamma < 1/2$  stopped within 10m
- Can they be dug out?

Model	$\epsilon$	$\zeta$	$\eta$
Number of particles with $\beta\gamma < 0.25$	850	7	7
Range in C (cm)	60	136	129
Range in Fe (cm)	29	65	61
Number of particles with $\beta\gamma < 0.5$	7700	100	90
Range in C (cm)	600	1360	1290
Range in Fe (cm)	290	650	610



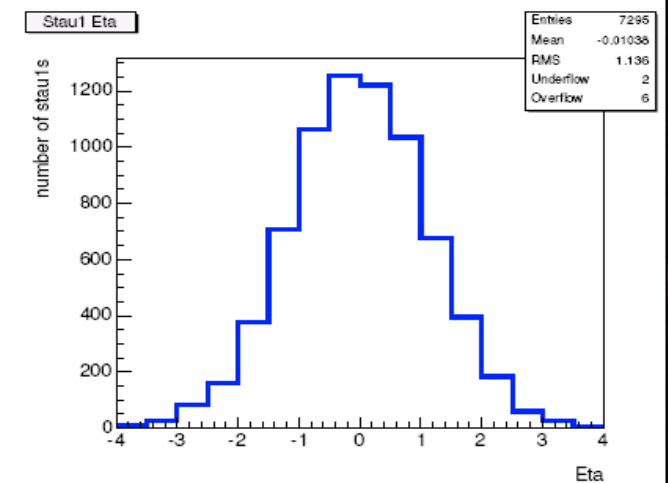
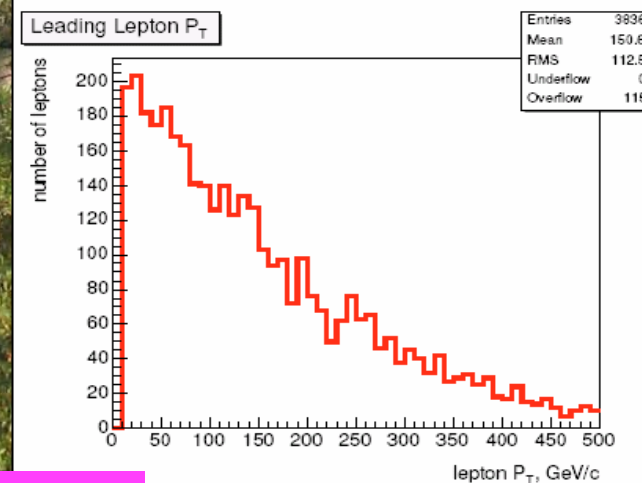
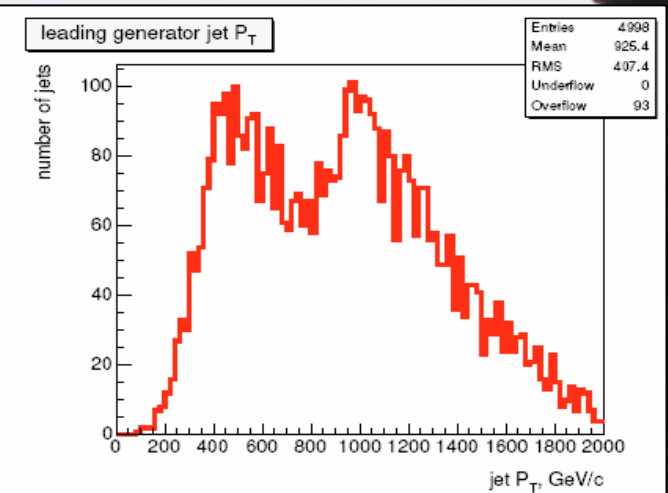
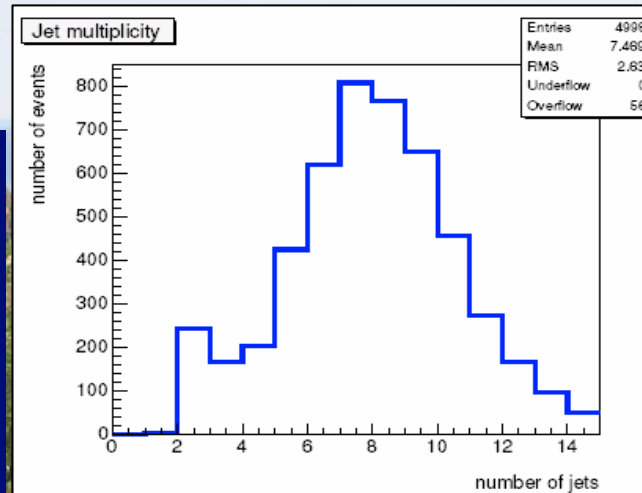
# Kinematic Distributions: Point $\varepsilon$

- Staus come with many jets & leptons with  $p_T$  hundreds of GeV, produced centrally



# Kinematic Distributions: Point $\zeta$

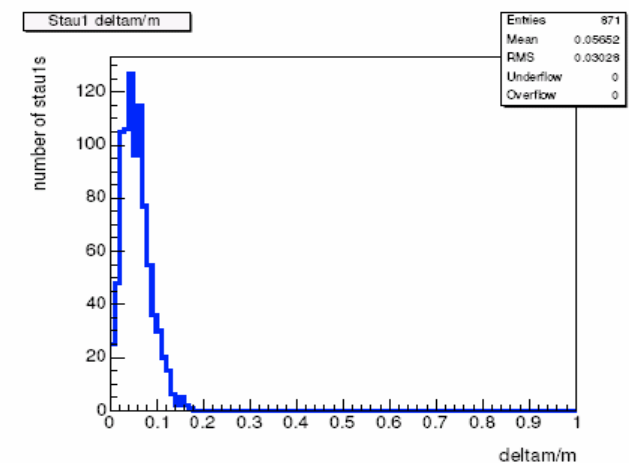
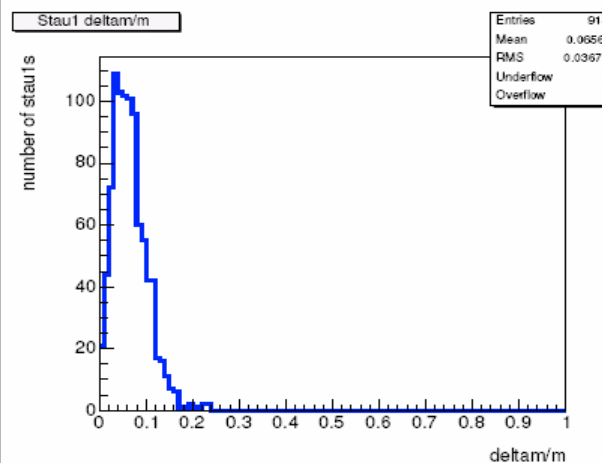
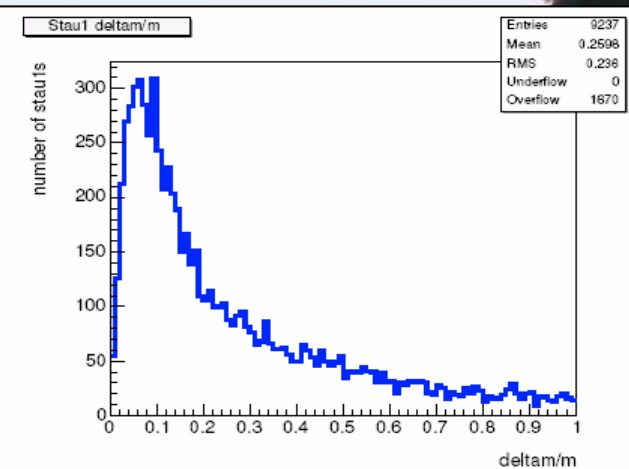
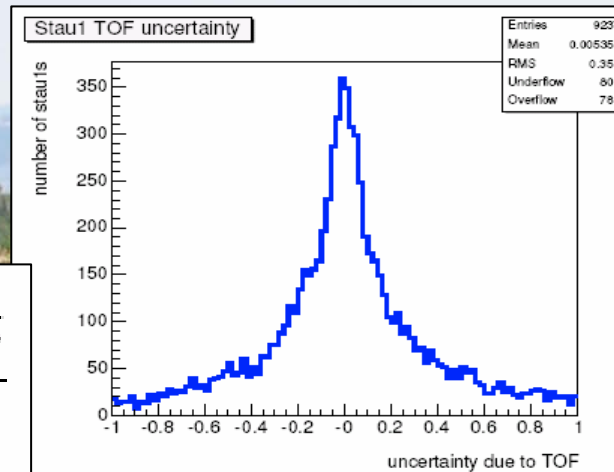
- Staus come with many jets & leptons with  $p_T$  hundreds of GeV, produced centrally



# Stau Mass Measurements by Time-of-Flight

$$\frac{\Delta M}{M} = \frac{\Delta p}{p} \oplus \beta \gamma^2 \frac{c \Delta t}{L}$$

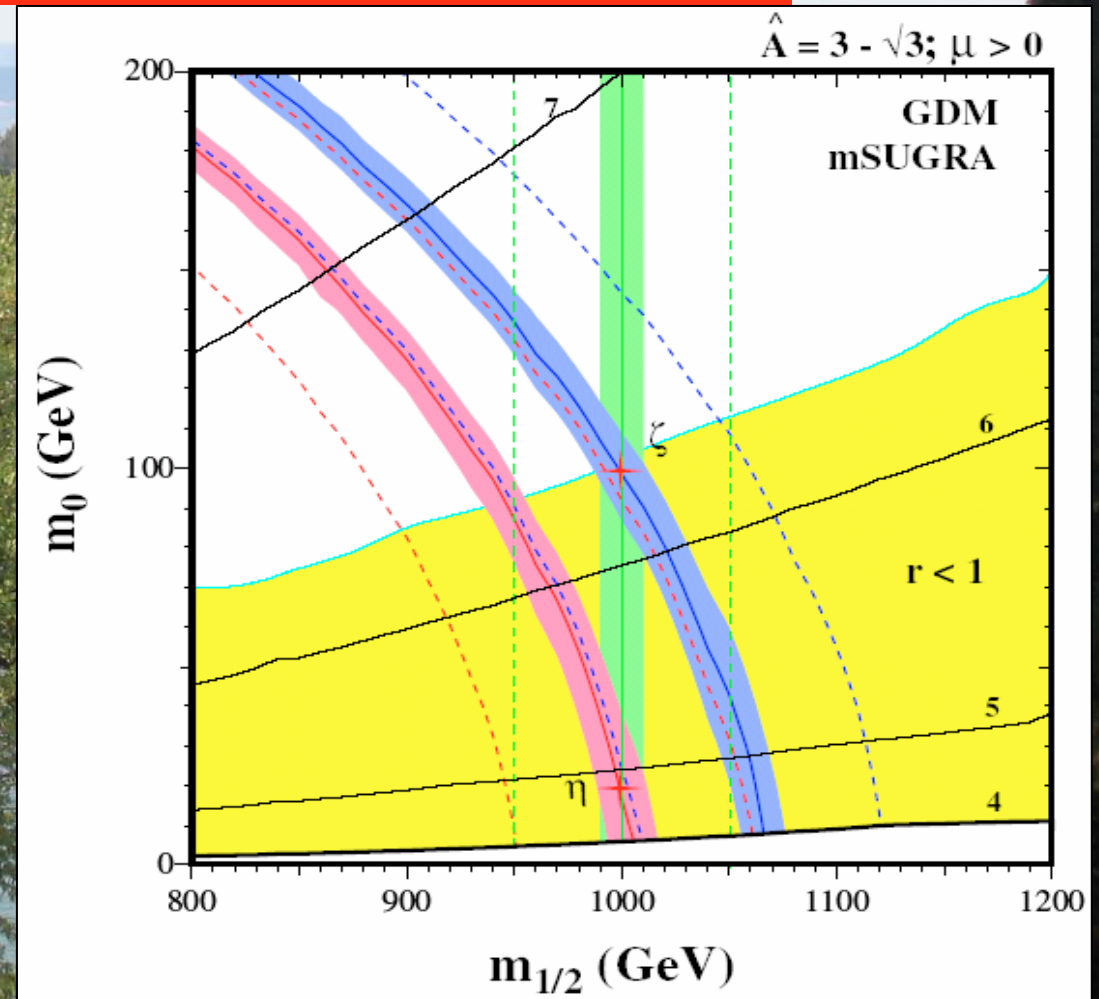
- Event-by-event accuracy < 10%
- < 1% with full sample



# Potential Measurement Accuracies

Gravitino Dark Matter even more interesting  
than Neutralino Dark Matter!

Measure stau mass to 1%  
Measure  $m_{1/2}$  to 1%  
via cross section, other masses?  
Distinguish points  $\zeta, \eta$





A scenic view of a lake, likely Lake Michigan, framed by trees. In the foreground, there are green trees and a large, dark tree trunk on the right. In the middle ground, a yellow building with a tower sits on a hill overlooking a marina filled with sailboats. A large orange and white ship is visible in the distance on the water. The sky is clear and blue.

Extra Dimensions at Colliders?

# Problems of Quantum Gravity

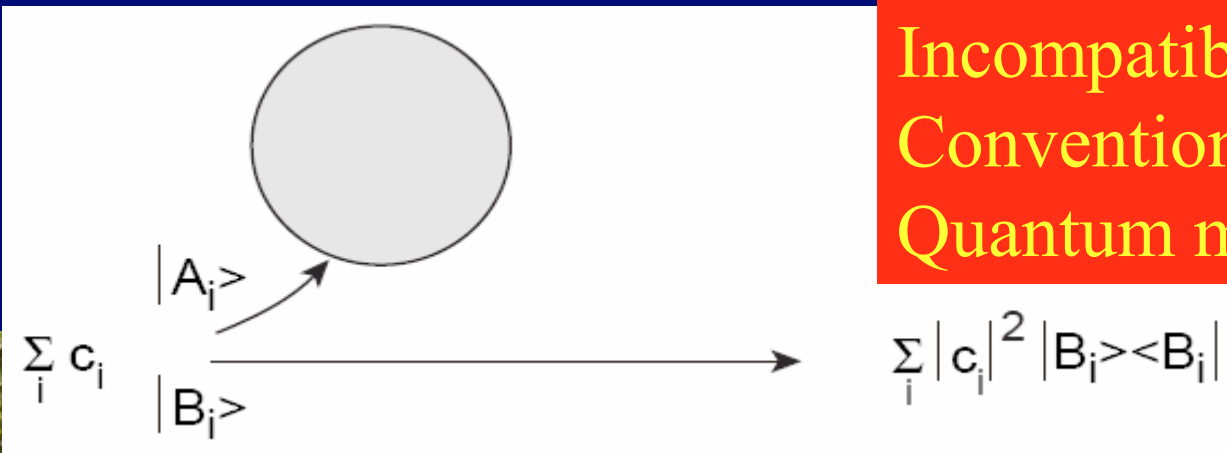
- Gravity grows with energy:

$$\sigma_G \sim E^2 / m_P^4$$

- Two-graviton exchange is infinite:

$$\int^{\Lambda \rightarrow \infty} d^4k \left( \frac{1}{k^2} \right) \leftrightarrow \int_{1/\Lambda \rightarrow 0} d^4x \left( \frac{1}{x^6} \right) \sim \Lambda^2 \rightarrow \infty$$

- **Gravity is a non-renormalizable theory**
- Pure states evolve to mixed states?



Incompatible with  
Conventional  
Quantum mechanics

# String Theory

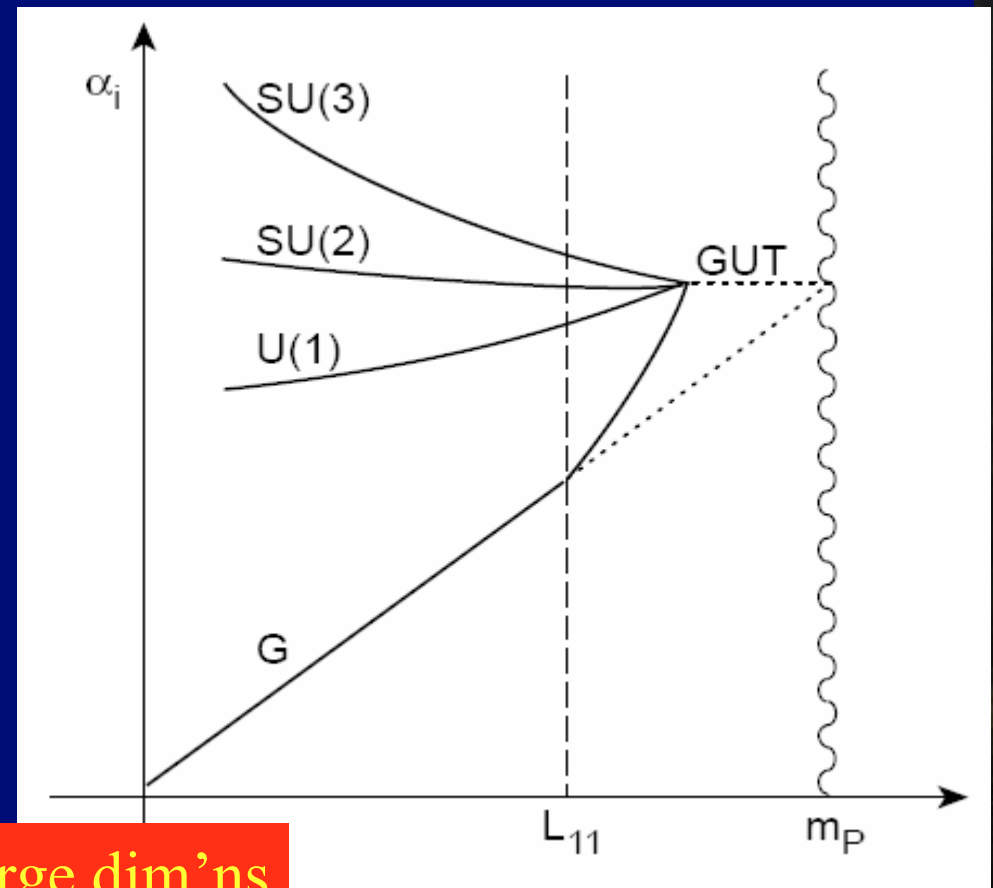
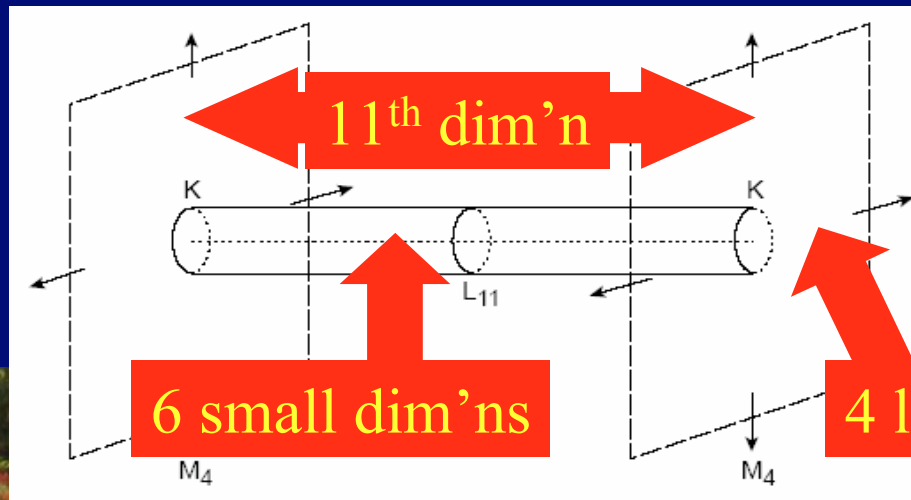
- Point-like particles  $\rightarrow$  extended objects
- Simplest possibility: lengths of string
- Open and/or closed
- Quantum consistency fixes # dimensions:
- Bosonic string: 26, superstring: 10
- Must compactify extra dimensions, scale  $\sim 1/m_p$ ?
- Perturbative string unification scale:

$$M_{GUT} = O(g) \times \frac{m_P}{\sqrt{8\pi}} \simeq \text{few} \times 10^{17} \text{ GeV}$$

Close to GUT scale, but larger?

# Scenario for String Unification

- Extra dimension below GUT scale: gravity grows faster with energy, unify at  $10^{16}$  GeV?
- E.g., in M theory with large 11<sup>th</sup> dimension

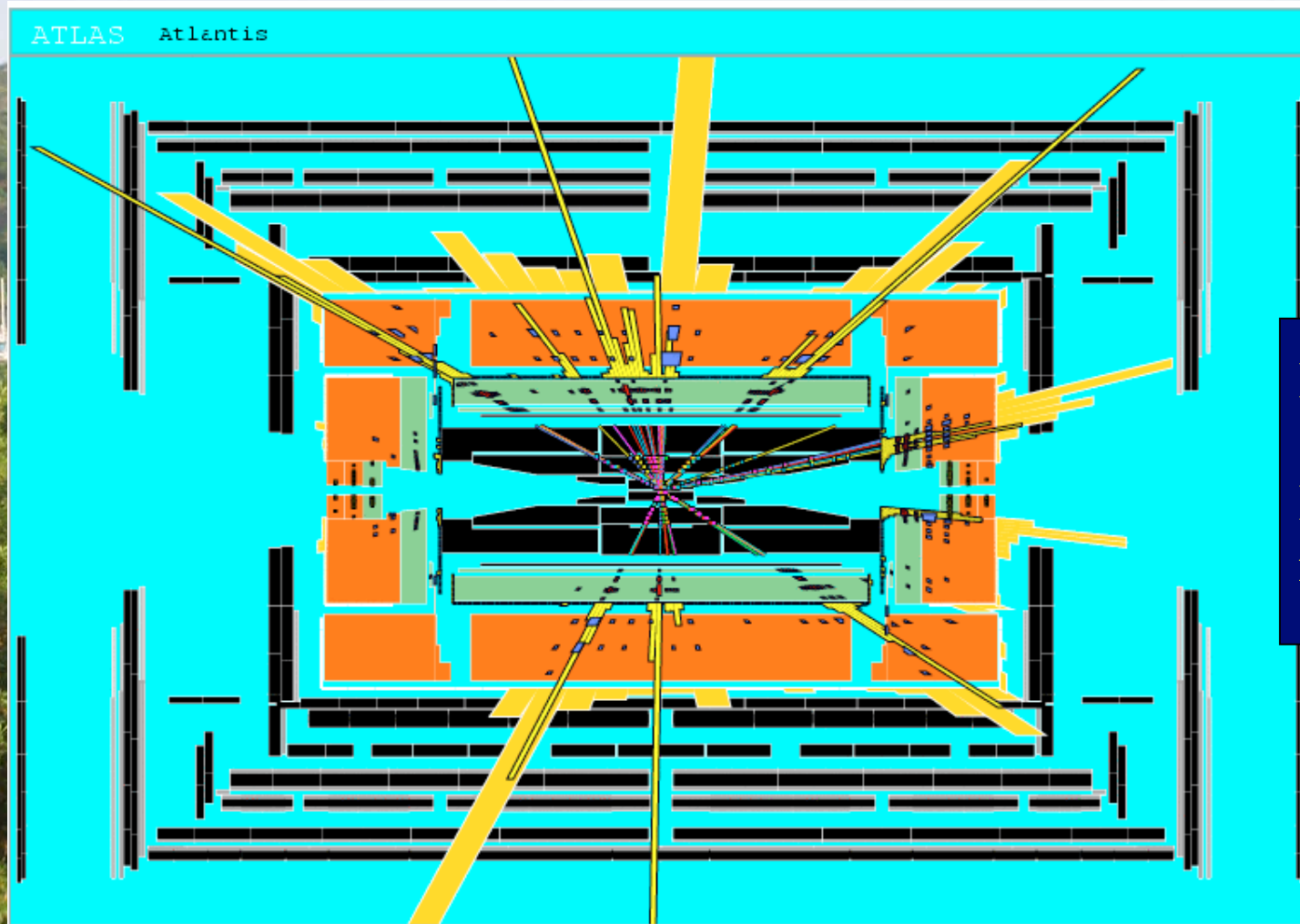


# How large could extra Dimensions be?

- 1/TeV?  
could break supersymmetry, electroweak
- micron?  
can rewrite hierarchy problem
- Infinite?  
warped compactifications
- **Look for black holes, Kaluza-Klein excitations @ colliders?**

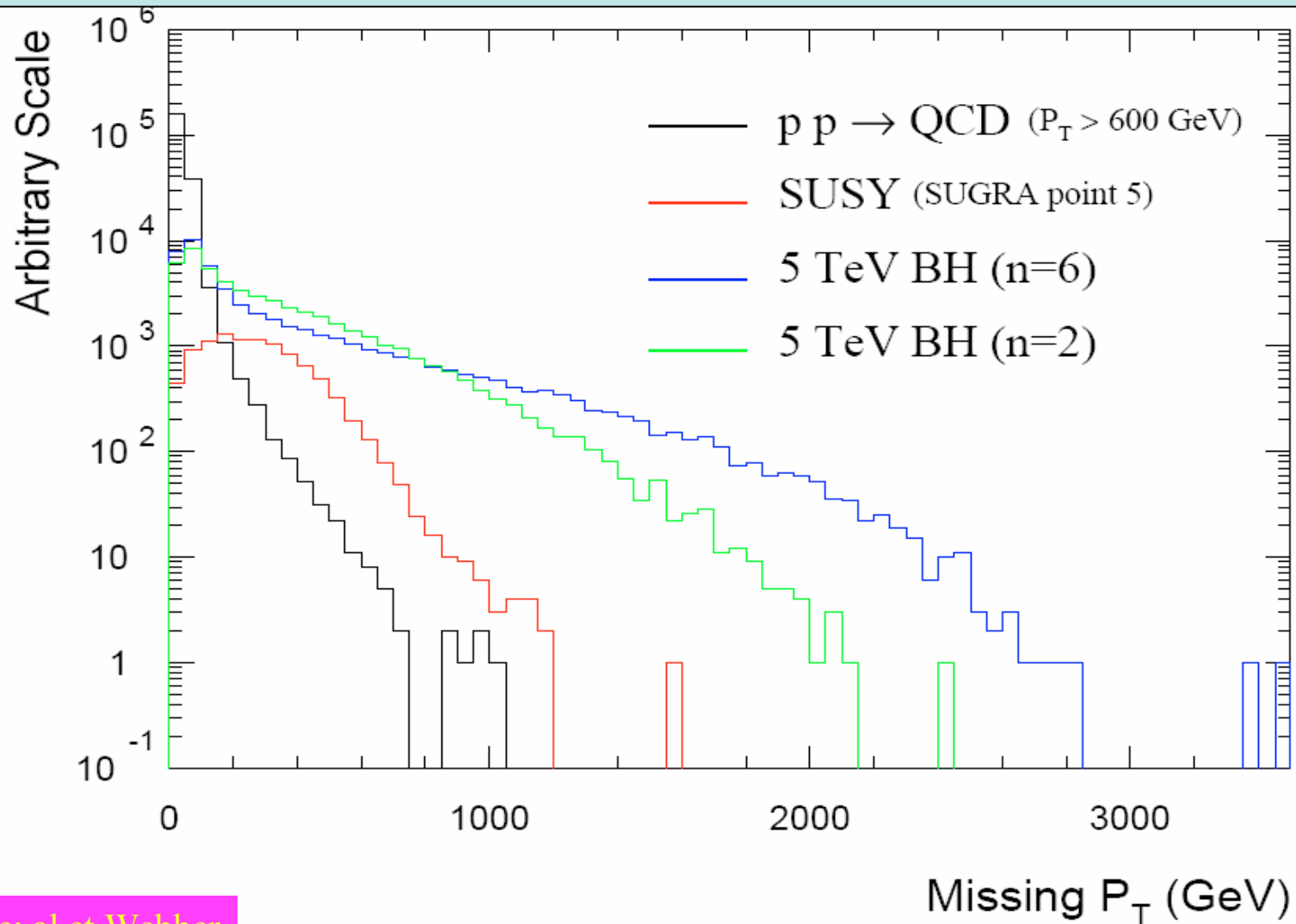
And if gravity becomes strong at the TeV scale ...

# Black Hole Production at LHC?

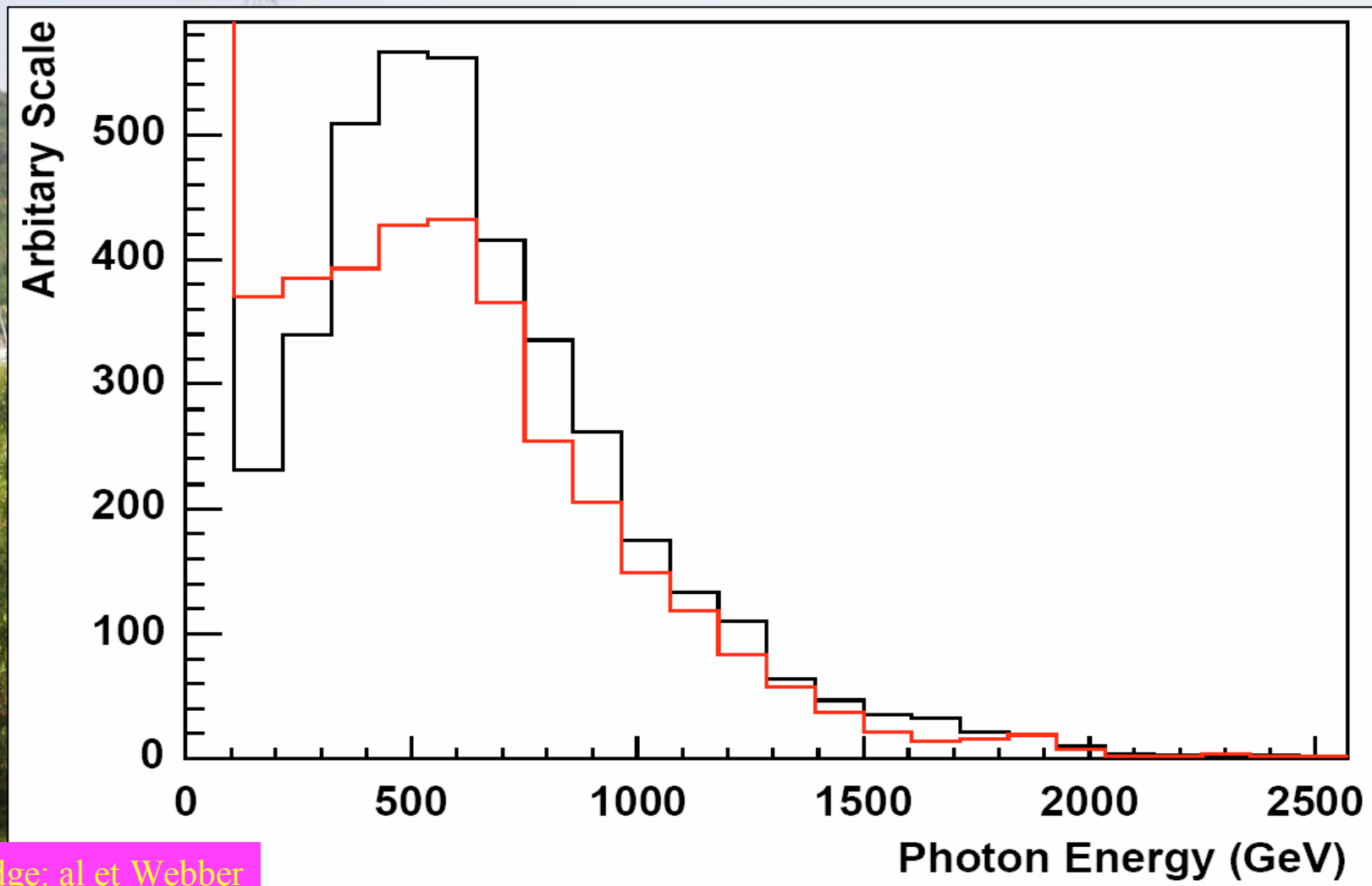


Multiple jets,  
leptons from  
Hawking  
radiation

# Black Hole Production



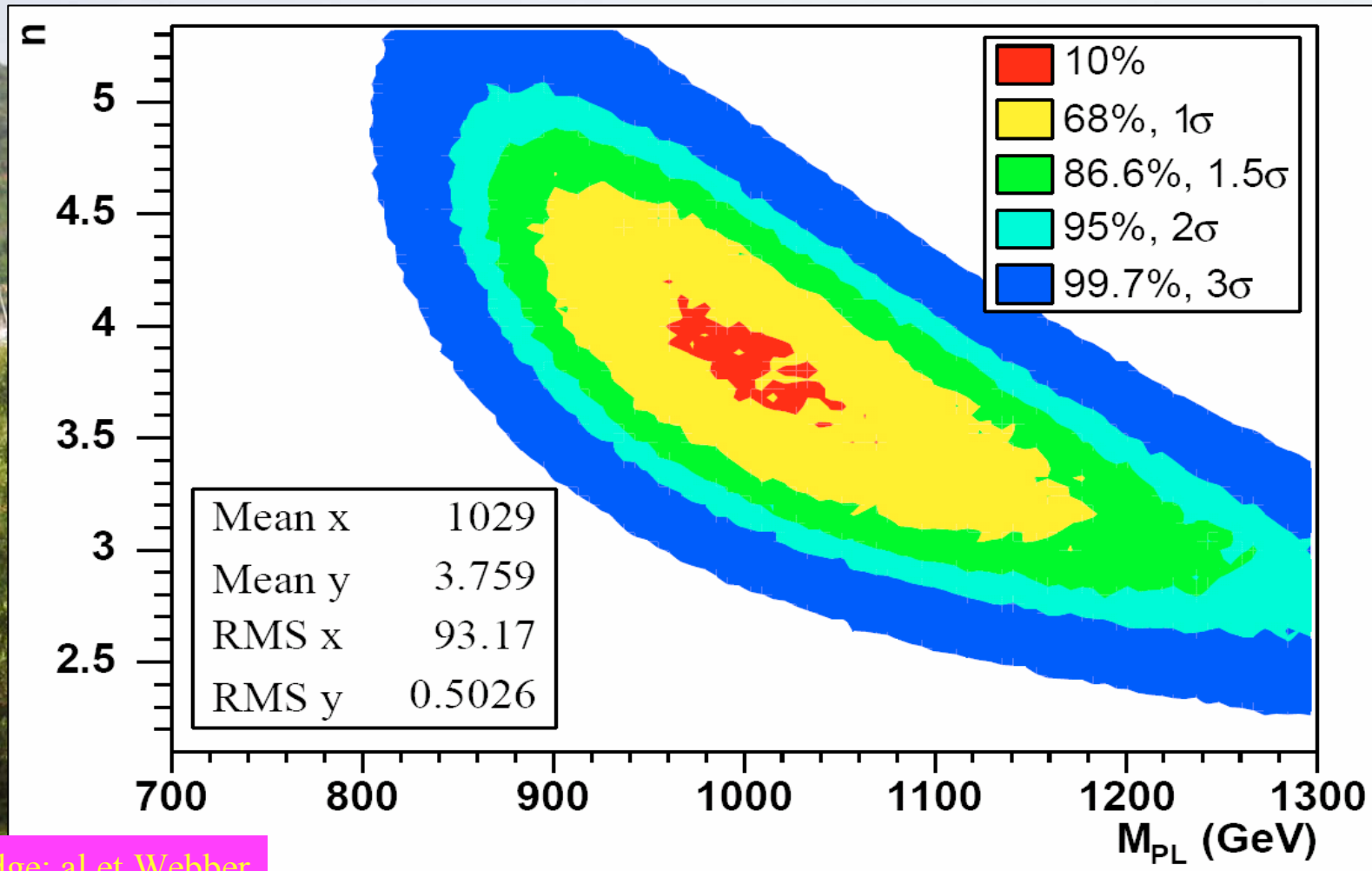
# Black Hole Decay Spectrum



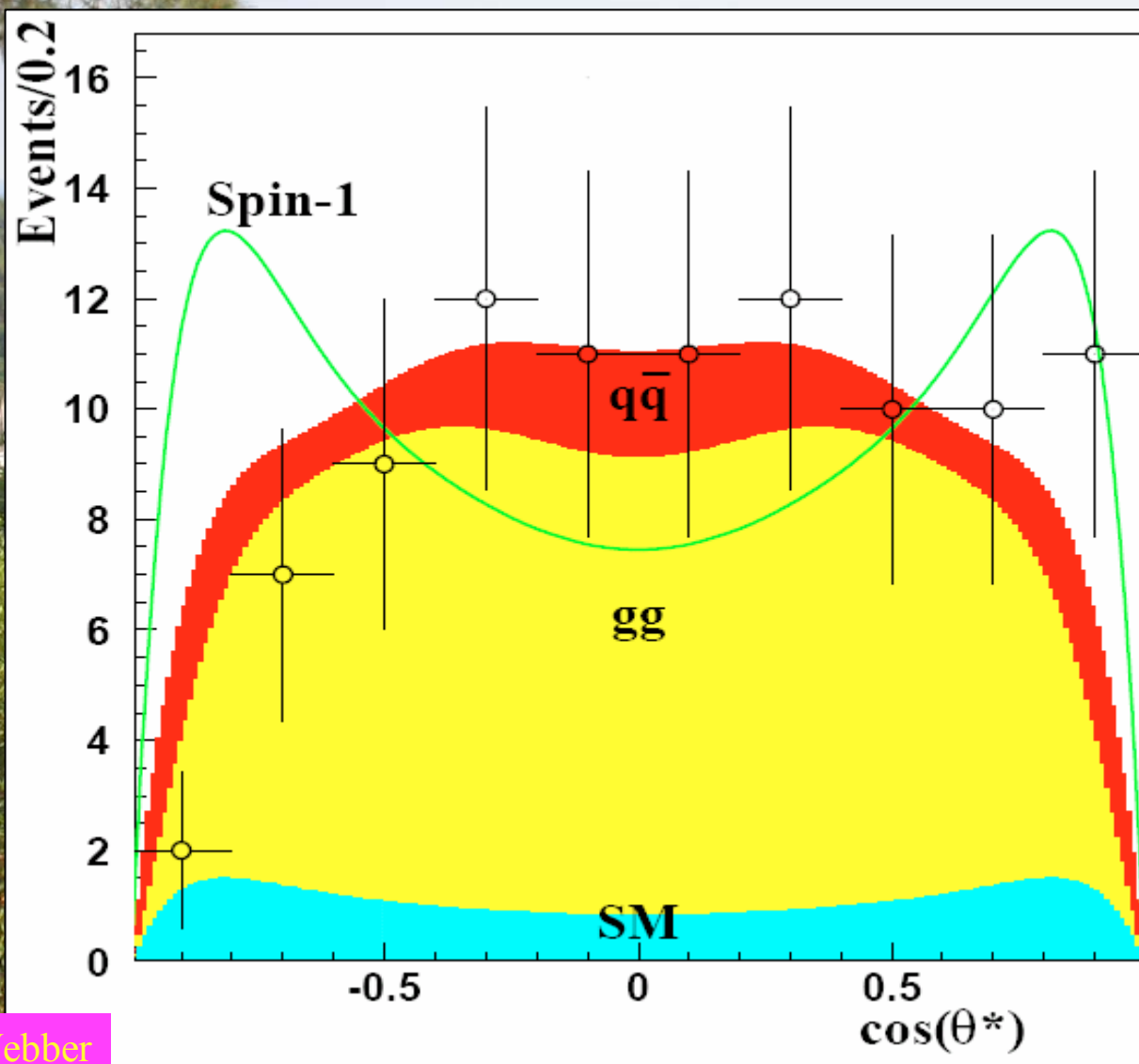
Cambridge: al et Webber



# Measuring Extra Dimensions



# Identifying a Graviton Resonance



# Summary

- There are good prospects for new physics discoveries with upcoming colliders
- Reasons to expect new physics @ TeV
  - Higgs, supersymmetry, extra dimensions (?)
- Distinctive experimental signatures
- The LHC @ CERN will open new energy range
- Linear  $e^+e^-$  colliders could explore in more detail
  - LHC will tell us the optimal energy