



The Abdus Salam  
International Centre for Theoretical Physics



SMR 1666 - 24

**SCHOOL ON QUANTUM PHASE TRANSITIONS  
AND  
NON-EQUILIBRIUM PHENOMENA IN COLD ATOMIC GASES**

11 - 22 July 2005

***Dipolar gases: Experiments***

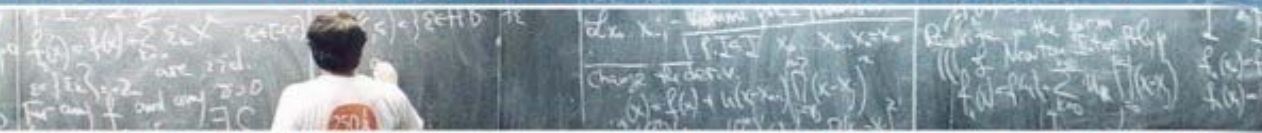
Presented by:

**Jürgen Stuhler**

University of Stuttgart, Germany

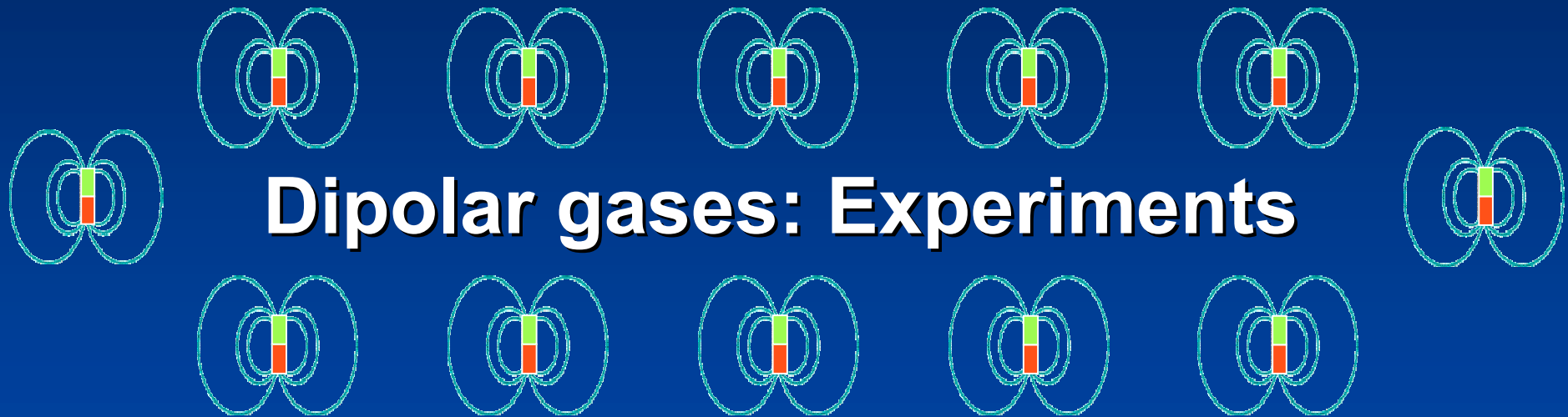


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"Scientific thought is the common heritage of mankind" – Abdus Salam

# School on Quantum Phase Transitions and Non-Equilibrium Phenomena in Cold Atomic Gases

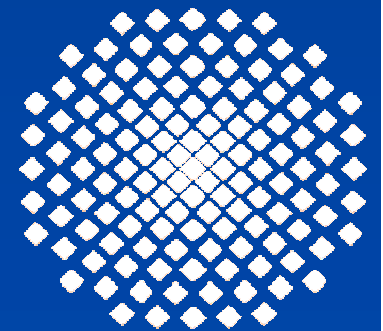


## Dipolar gases: Experiments



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5. Physikalisches Institut (Tilman Pfau)  
[www.physik.uni-stuttgart.de/institute/pi/5/](http://www.physik.uni-stuttgart.de/institute/pi/5/)



# outline

- motivation & dipolar systems “in the game”
- production of cold molecules
- BEC of atoms with high magnetic moments (Cr)
- first observation of dipole-dipole interaction in a degenerate quantum gas

# dipole-dipole vs. contact interaction

interactions make life interesting!

contact interaction

short range

$$U_{\text{eff}}(r) = g \delta(r)$$

isotropic

$$g = \frac{4\pi\hbar^2 a}{m}$$

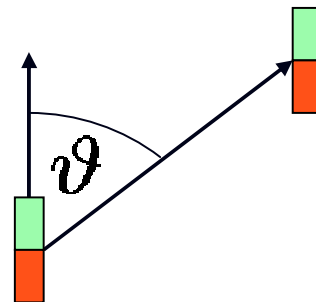
dipole-dipole interaction

anisotropic

$$U_{dd}(\vartheta, r) = -\frac{C_{dd} (3 \cos^2 \vartheta - 1)}{4\pi r^3}$$

long range

$$C_{dd} = \mu_0 \mu^2 = p^2 / \epsilon_0$$



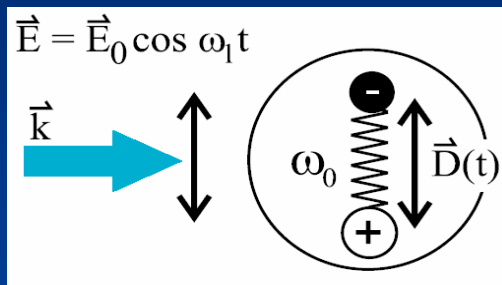
# dipolar systems “in the game”

## electric dipoles $p$

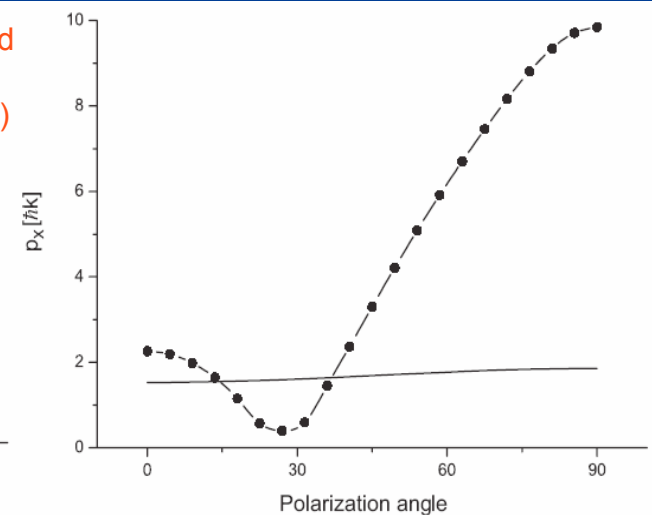
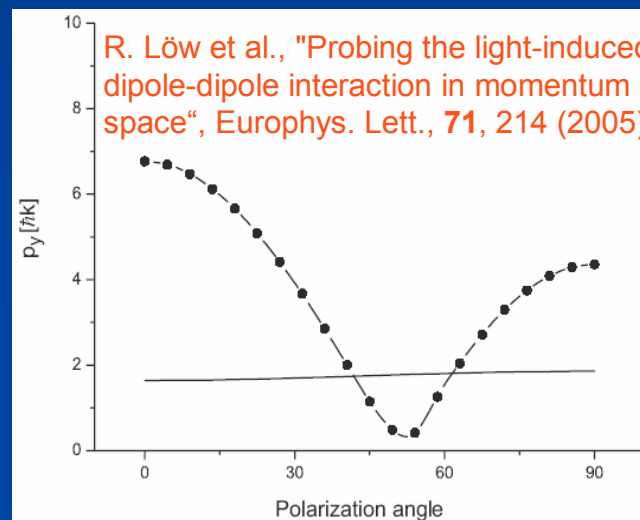
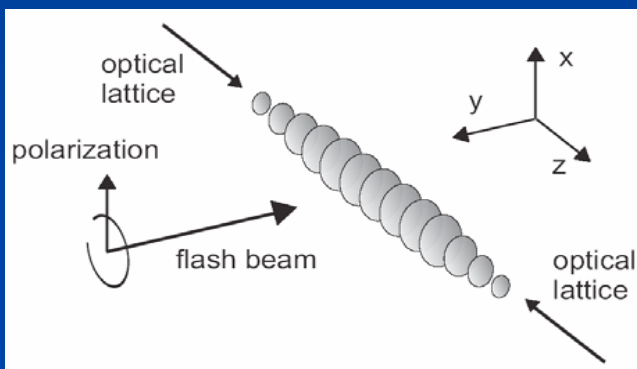
$[p] = 1 \text{ Debye} = 1 \text{ D} = 3.33564 \times 10^{-30} \text{ Cm}$

e.g.:  $p^+, e^- @ a_0 \sim 2.5 \text{ D}$

light-induced  
dipoles



- oscillating dipoles
- large amplitudes  $p \sim 5 \text{ D}$
- retardation effects



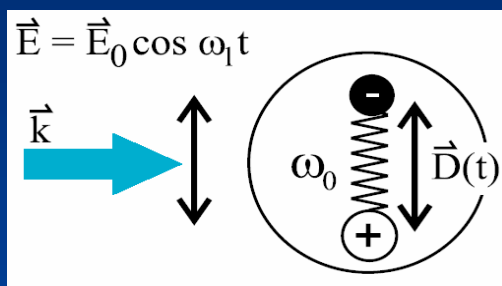
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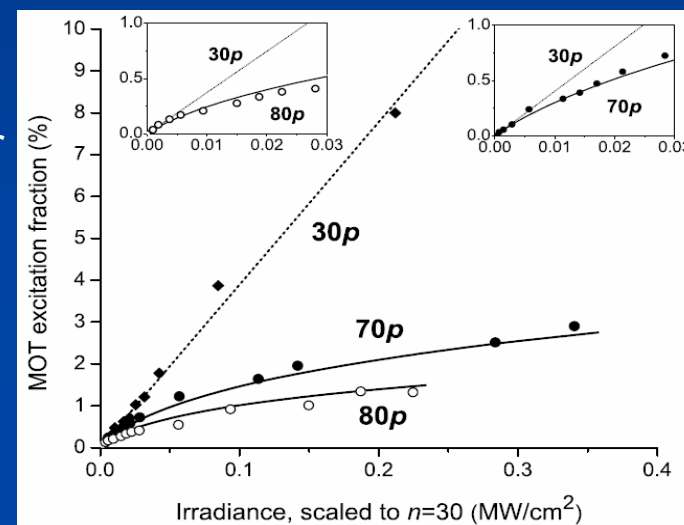
Rydberg  
atoms



- oscillating dipoles
- large amplitudes  $p \sim 5 \text{ D}$
- retardation effects

- static dipoles (E-field)
- $p \propto n^2$ ,  $p(n=40) \sim 2000 \text{ D}$  !
- fragile, difficult to prepare (1- or 2-photon excitation)
- dipole blockade, QC<sup>1)</sup>
- van der Waals blockade<sup>2)</sup>

1) Jaksch et al., PRL **85**, 2208 (2000)  
 2) Tong et al., PRL **93**, 063001 (2004)  
 groups: Gallagher, Gould, Pillet, Weidemüller, Raithel, Walker, Shaffer, Pfau



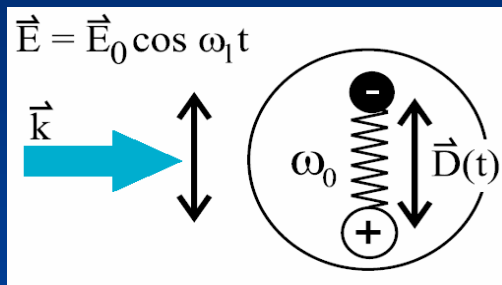
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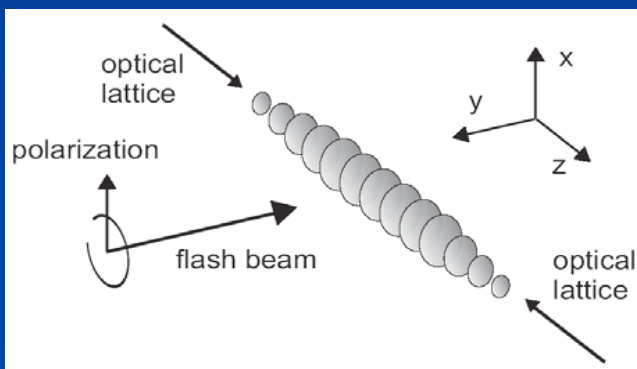
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### light-induced dipoles



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### Rydberg atoms



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### heteronuclear molecules



- large dipoles  $p \sim \text{several D}$
- starting from molecules: cooling difficult
- starting from atoms: formation, ground state, stability ?

# dipolar systems “in the game”

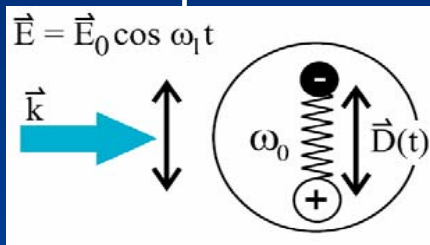
## electric dipoles $p$

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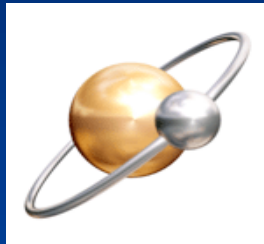
## magnetic dipoles $\mu$

$[\mu] = 1 \text{ Bohr magneton} = 1 \mu_B$   
 $= \hbar e / 2 m_e = 9.2742 \times 10^{-24} \text{ Jm}^2/\text{Vs}$

### light-induced dipoles



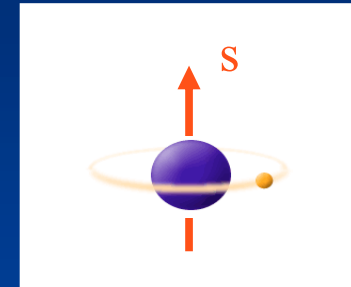
### Rydberg atoms



### heteronuclear molecules



### atoms with magn. moment



- large dipoles  $p \sim$  several D
- starting from molecules: cooling difficult
- starting from atoms: formation, ground state, stability ?

- BEC & deg. fermi gas
- typ. small dipoles  $\mu \sim 1 \mu_B$
- exceptions:
  - Er  $\mu \sim 7 \mu_B$  (MOT, McClelland, NIST)
  - Cr  $\mu \sim 6 \mu_B$  (BEC)



# strength of dipole-dipole interaction

$$C_{dd} = \mu_0 \mu^2 = p^2 / \epsilon_0$$

$$U_{dd}(r) \sim C_{dd} / 4\pi r^3$$

$$n \sim 10^{15} \text{ cm}^{-3} \rightarrow r \sim 100 \text{ nm}$$

$$p = 1 \text{ D} \rightarrow U_{dd} \sim 10 \text{ } \mu\text{K}$$

$$\mu = 1 \text{ } \mu\text{B} \rightarrow U_{dd} \sim 1 \text{ nK}$$

compare to  
contact interaction:

$$\epsilon_{dd} = \frac{C_{dd}}{3g} = \frac{\mu_0 \mu^2 M}{12\pi \hbar^2 a}$$

dipole interaction

contact interaction

atoms

molecules

Rb  $\epsilon_{dd} = 0.007$

Na  $\epsilon_{dd} = 0.003$

Cr  $\epsilon_{dd} = 0.15$

CaH, NH<sub>3</sub>, ...

di-alkalis

$\epsilon_{dd} \sim 100$

# strength of dipole-dipole interaction

$$C_{dd} = \mu_0 \mu^2 = p^2 / \epsilon_0$$

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compare to  
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$$\epsilon_{dd} = \frac{C_{dd}}{3g} = \frac{\mu_0 \mu^2 M}{12\pi \hbar^2 a}$$

dipole interaction  
**tunable!**  
contact interaction

atoms

Rb	$\epsilon_{dd} = 0.007$
Na	$\epsilon_{dd} = 0.003$
Cr	$\epsilon_{dd} = 0.15$

**tuning**

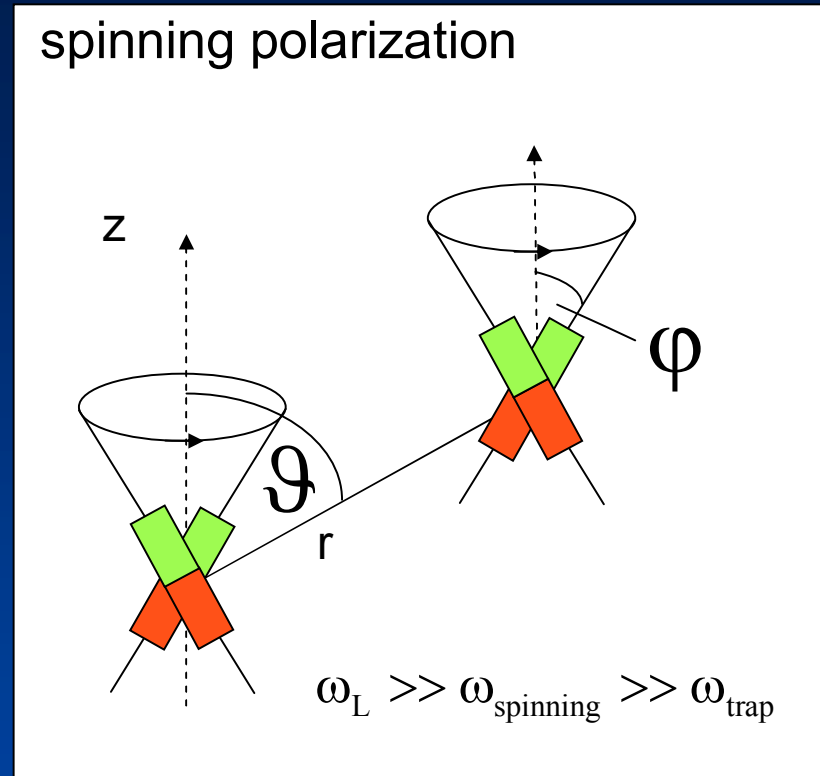
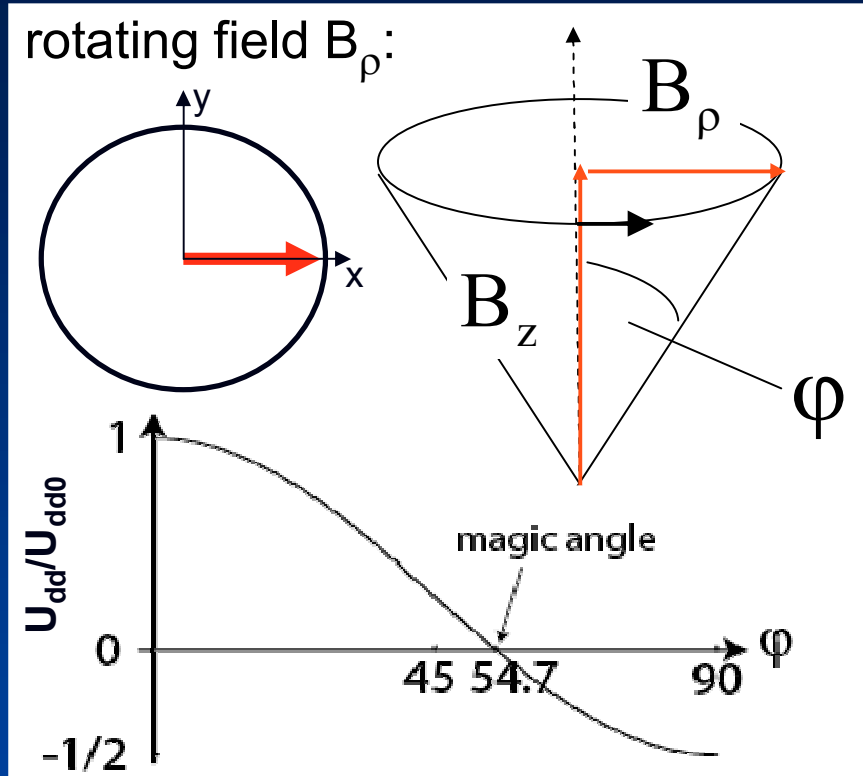
Feshbach  
resonance

J. Werner et al.  
PRL **94**, 183201 (2005)

spinning  
polarization

S. Giovanazzi et al.  
PRL **89**, 130401 (2002)

# tuning the dipole-dipole interaction



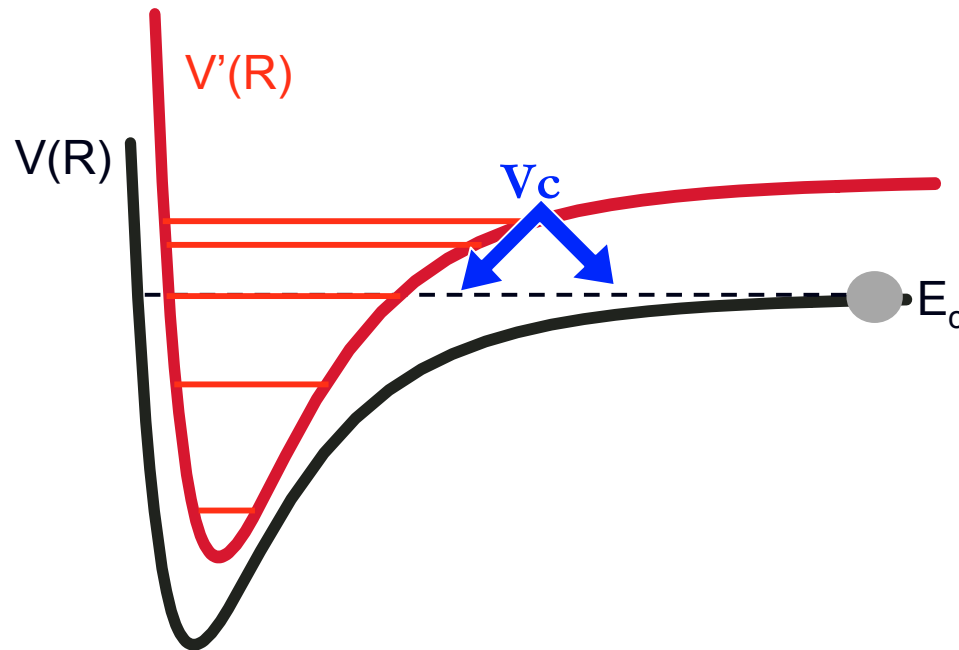
$$\langle U_{dd}(\vec{r}) \rangle = -\frac{\mu_0 \mu^2}{4\pi} \left( \frac{3 \cos^2 \vartheta - 1}{r^3} \right) \left( \frac{3 \cos^2 \varphi - 1}{2} \right)$$

$$[-1/2, 1]$$

# tuning a with Feshbach resonances

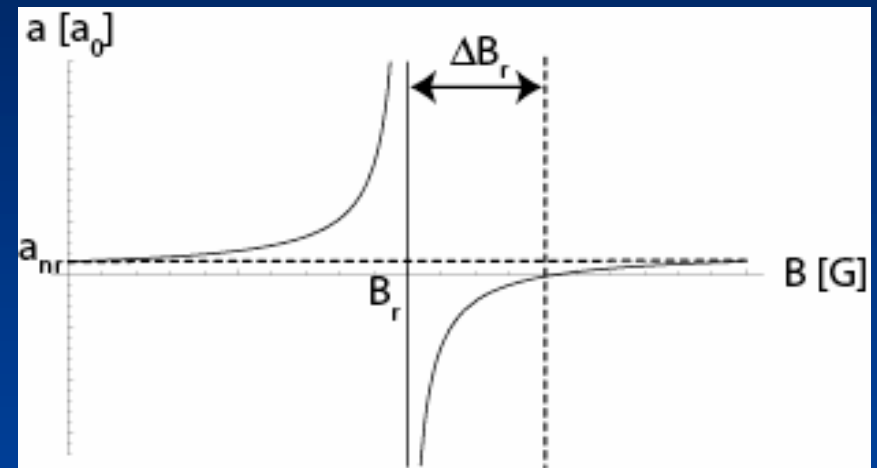
collision with molecular potential  $V(R)$ :

$V'(R)$  with  $M_s \neq M_s + B\text{-field} + \text{coupling}$ :



$\Rightarrow a$  describes scattering @ low T

$\Rightarrow a$  is modified !

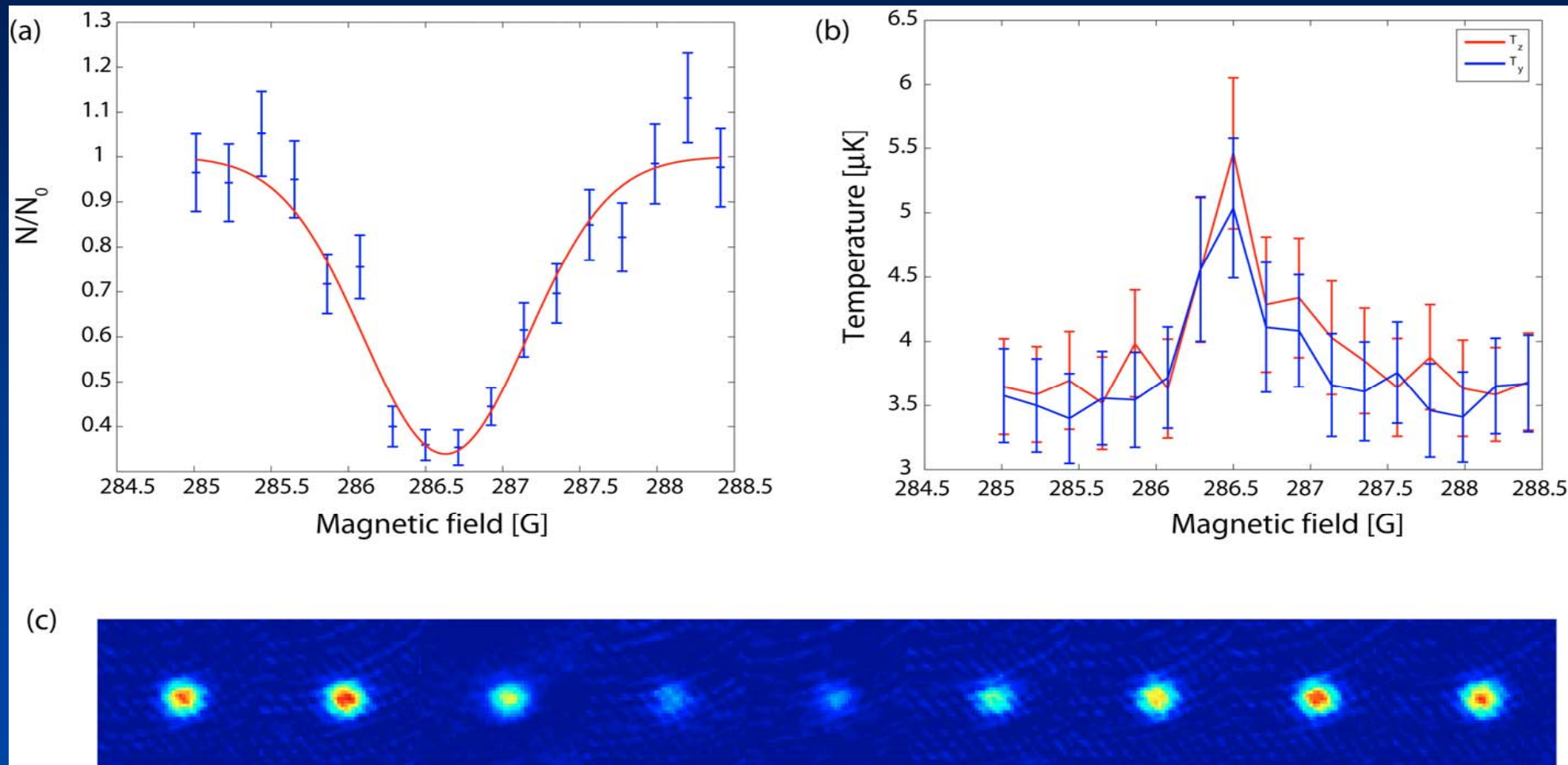


$$a_{FB}(B) = a_{nr} \left( 1 - \frac{\Delta B_r}{B - B_r} \right)$$

scattering length  $a$  can be tuned with B-field !

# detection of Feshbach resonances in $^{52}\text{Cr}$

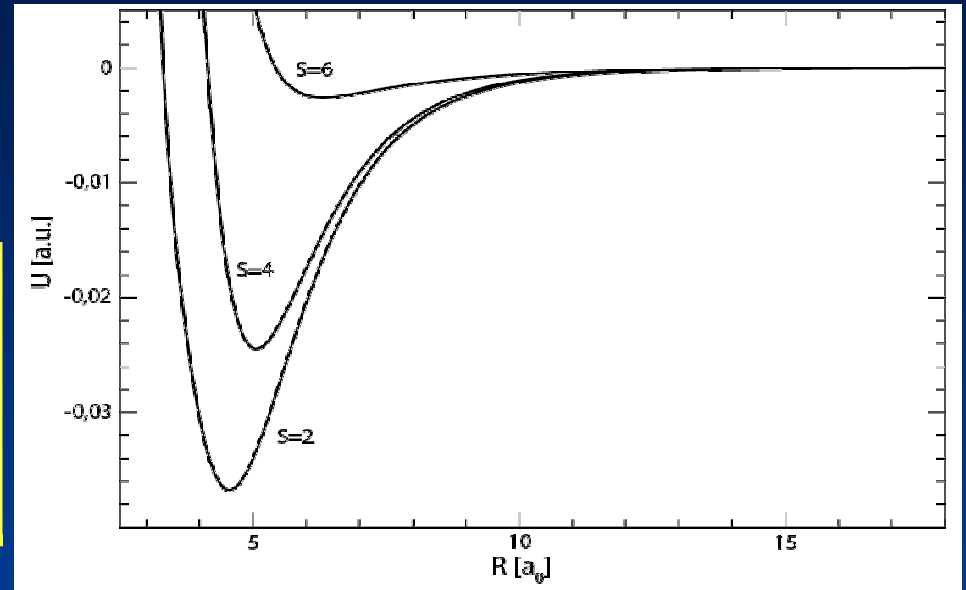
atom loss measurement in crossed ODT typical result:



observed all 11 expected FRs

# theory – multichannel calculations

- parametrize potential
- start with 5 adjustable parameters  
 $C_6$ ,  $C_8$ ,  $a_6$ ,  $a_4$ ,  $a_2$
- integrate Schrödinger eq. incl. spin-spin dipole interaction
- get theo. resonance positions
- compare to exp./compute  $\chi^2$
- vary parameters... **until  $\chi^2$  is minimal!**



A. Simoni, E. Tiesinga  
NIST Gaithersburg (USA)



$$a_6 = 112(14) a_0$$

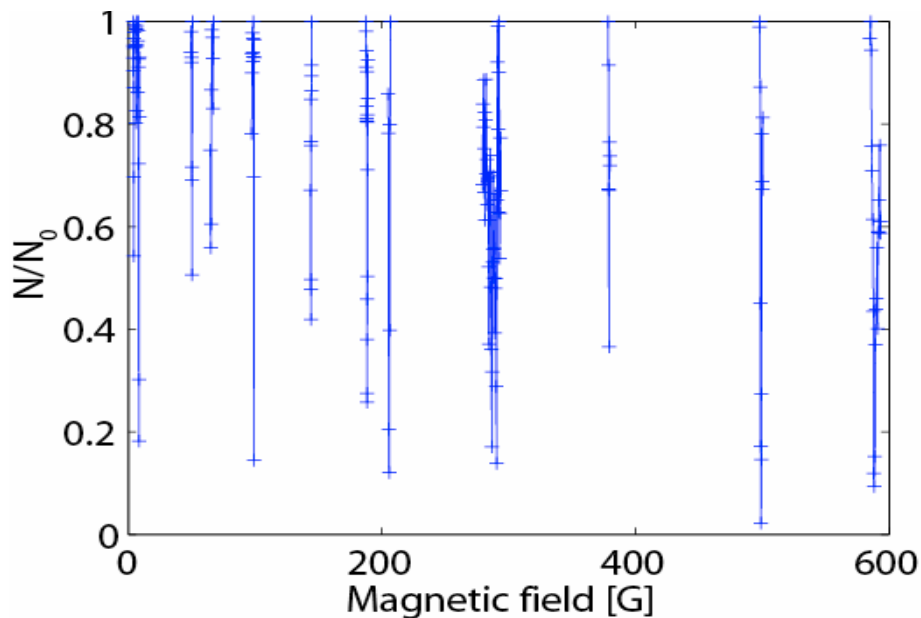
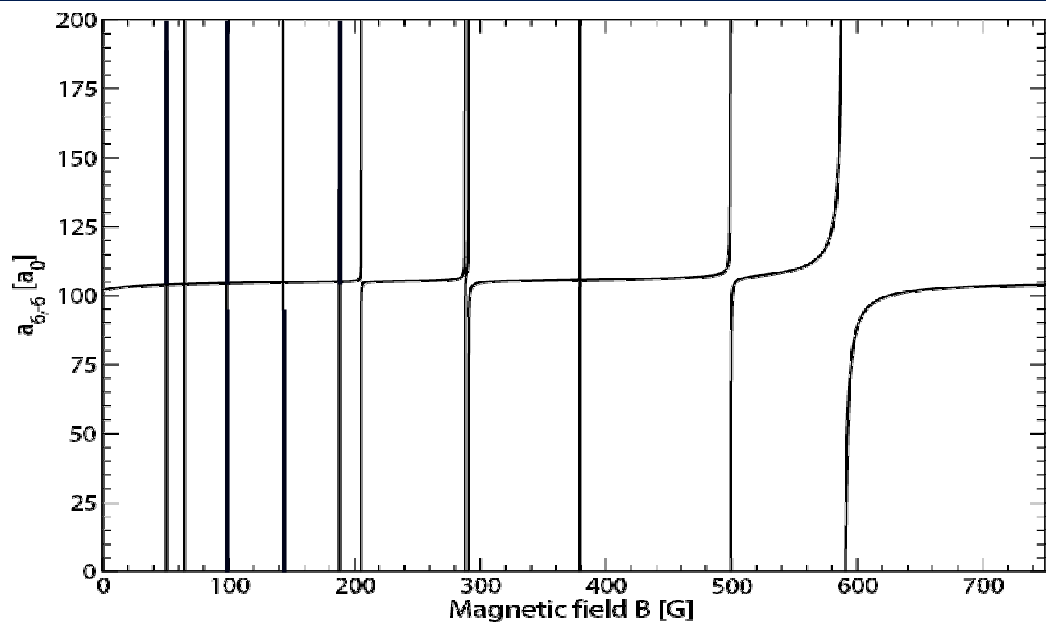
$$a_4 = 58(6) a_0$$

$$a_2 = -7(20) a_0$$

$$C_6 = 733(70) a.u.$$

$$C_8 = 75(+90/-75)10^3 a.u.$$

# FB-resonances: exp. vs. theory



Exp. Pos. [mT]	Theo. Pos. [mT]	Theo. $\Delta$ [ $\mu$ T]
0.41	0.40	-
0.61	-	-
0.82	0.81	-
5.01	5.01	$< 1 \cdot 10^{-4}$
6.51	6.49	$6 \cdot 10^{-4}$
9.89	9.85	0.030
14.39	14.32	0.012
18.83	18.79	0.022
20.58	20.56	1.2
28.66	28.60	1.2
29.03	29.07	5.1
37.92	37.92	0.042
49.09	49.32	8.1
58.91	58.92	170

$\Delta B_r \sim 2 \times 10^{-4}$

$\Delta B_r \sim 0.003$

**Cr is textbook element:**

- no hyperfine interaction ( $I=0$ )
- dipole-dipole interaction is dominant coupling mechanism
- **<0.6 G av. agreement !**

# outline & first summary

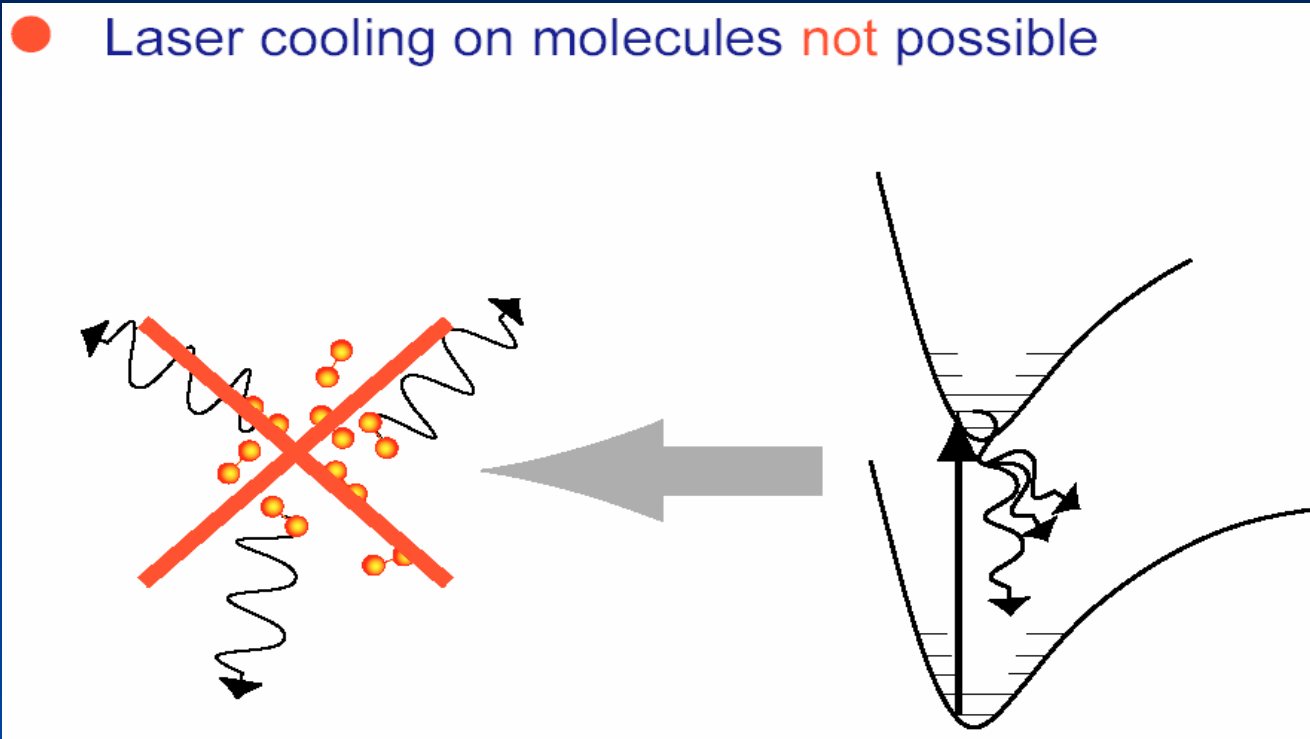
- motivation & dipolar systems “in the game”
  - atoms
    - light-induced electric dipoles (oscillating, retardation)
    - static electric dipoles (Rydberg atoms in E-field)
    - magnetic dipoles (weak, but stronger for Cr, tuning possible)
  - heteronuclear molecules
    - large static electric dipoles
- production of cold molecules [Eur. Phys. J. D 31 iss. 2 \(2004\)](#)
  - slowing & cooling of molecules (direct production)
  - making molecules out of cold atoms (indirect production)
  - trapping dipolar molecules
- BEC of atoms with high magnetic moments (Cr)
- first observation of dipole-dipole interaction in a degenerate quantum gas



# direct production of cold molecules

## How to get cold molecules ???

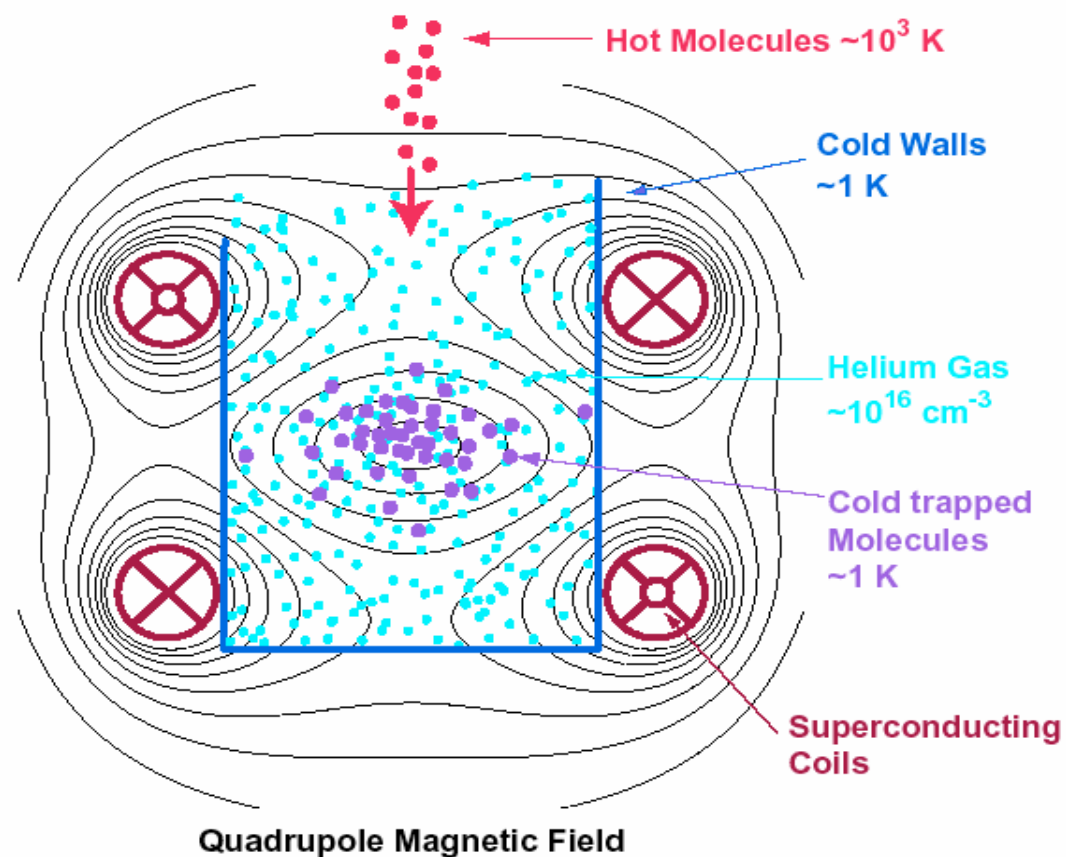
- Laser cooling on molecules **not** possible



- select cold molecules out of beam (Pinkse/Rempe)
- buffer gas cooling
- slow down molecules of a beam

# buffer gas cooling

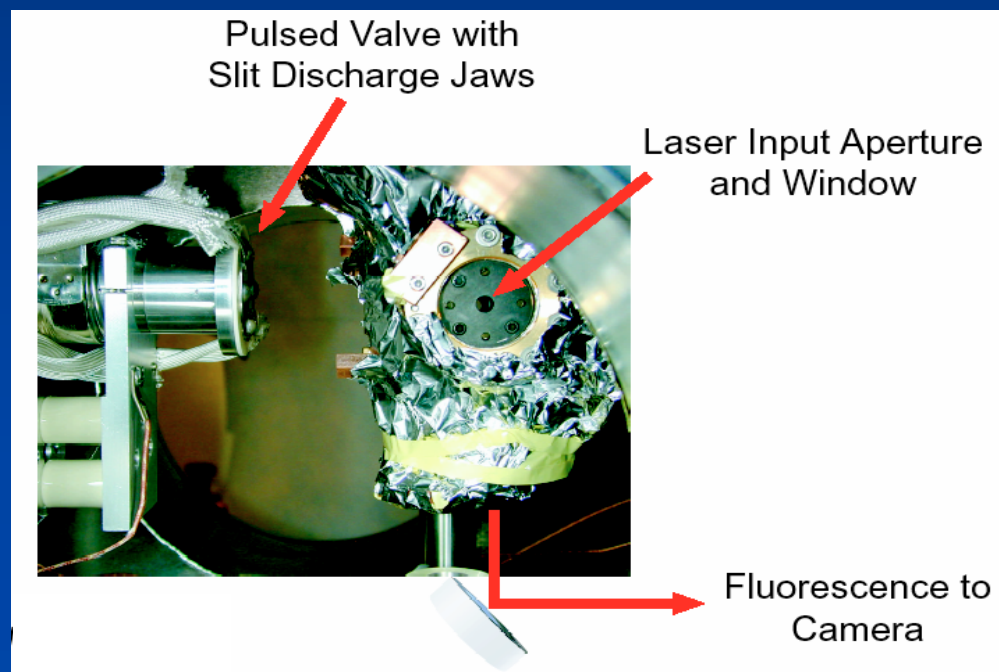
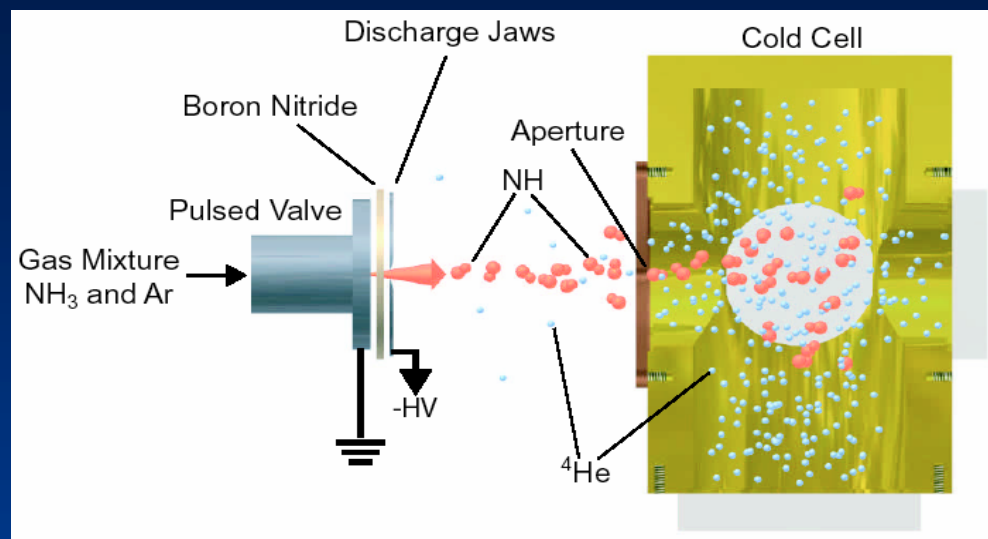
## Principle of Buffer-gas Cooling and Trapping



Cooling by collisions with cryogenically prepared helium atoms

J. M. Doyle et al. PRA 52, R2515 (1995)

# buffer gas cooling



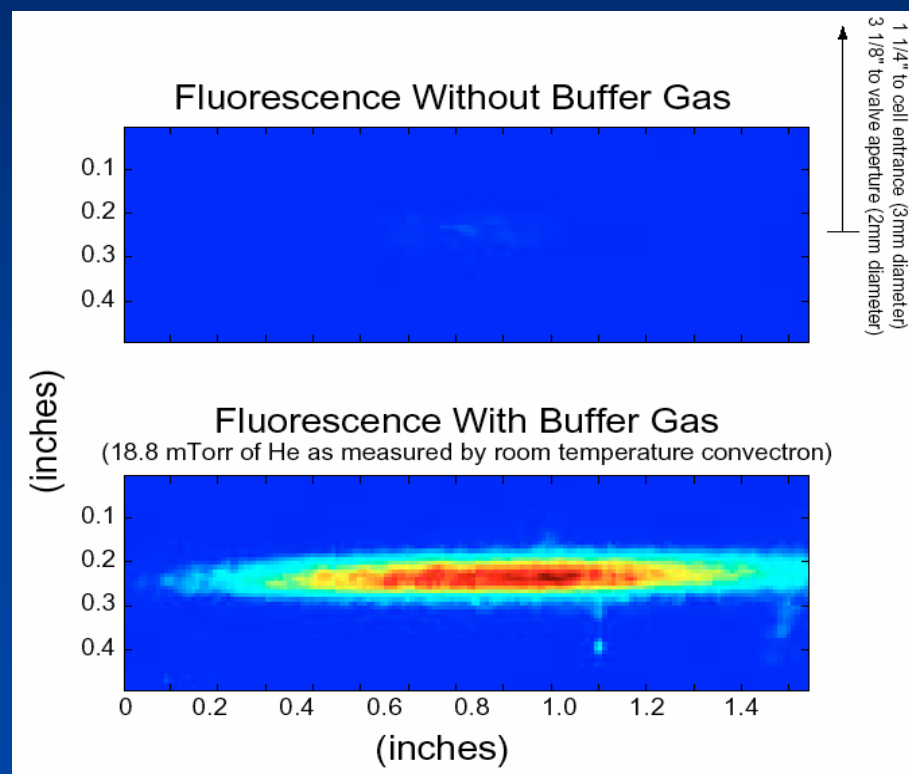
# buffer gas cooling

## Buffer-gas Cooling of an NH Molecular Beam for Magnetic Trapping

L. D. van Buuren<sup>1</sup>, W. C. Campbell<sup>1</sup>, D. Egorov<sup>1</sup>, B. Friedrich<sup>1,2</sup>, S. Maxwell<sup>1</sup>, E. Tsikata<sup>1</sup>, J. M. Doyle<sup>1</sup>

<sup>1</sup>Harvard University, Dept. of Physics and Center for Ultracold Atoms

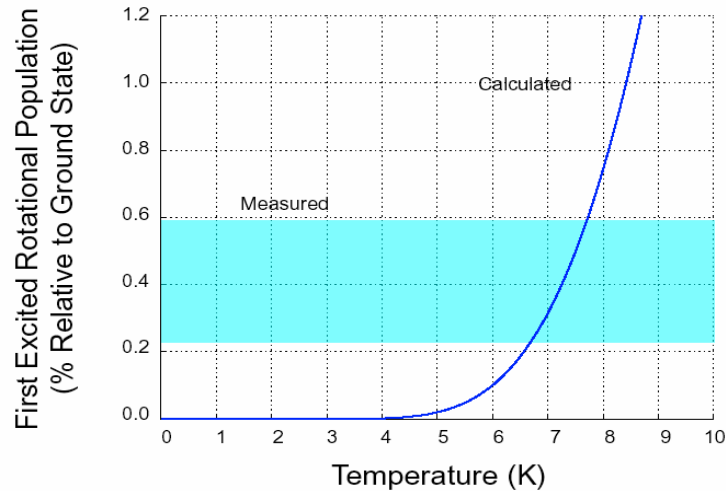
<sup>2</sup>Harvard University, Dept. of Chemistry and Chemical Biology



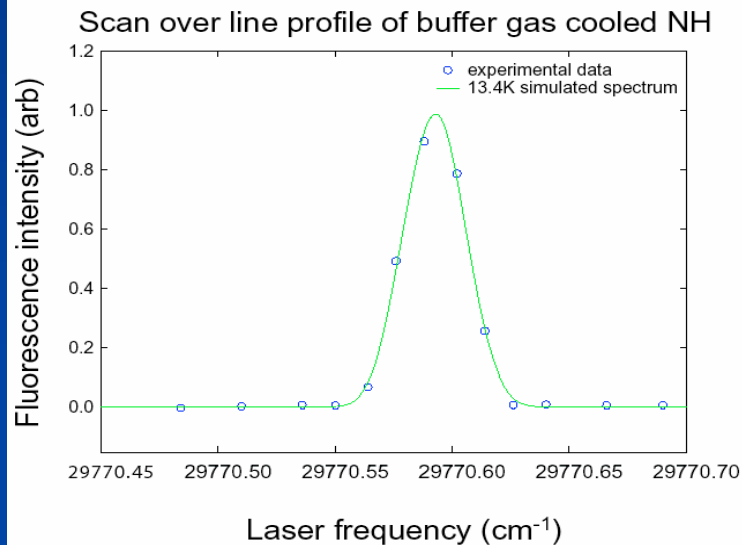
$N \sim 10^{11} - 10^{12}$ ,  $n \sim 3 \times 10^9 \text{ cm}^{-3}$ ,  $T \sim 10 \text{ K}$

# buffer gas cooling

## Rotational Temperature Determination



## Translational Temperature Determination



## Average Ground State NH Density in Cold Cell

$$n \approx 3 \times 10^9 \text{ cm}^{-3}$$

## Total Number of Ground State NH Radicals in Cold Cell

$$N = 10^{11} - 10^{12}$$

## Cell Temperature

$$8 \text{ K} < T_{\text{cell}} < 12 \text{ K}$$

## NH Rotational Temperature from State Distribution

$$T_{\text{rot}} = 7.2 \pm 0.5 \text{ K}$$

## NH Translational Temperature from Doppler Width

$$T_{\text{trans}} = 13 \pm 5 \text{ K}$$

## NH Mean-Free Path in Cold Cell

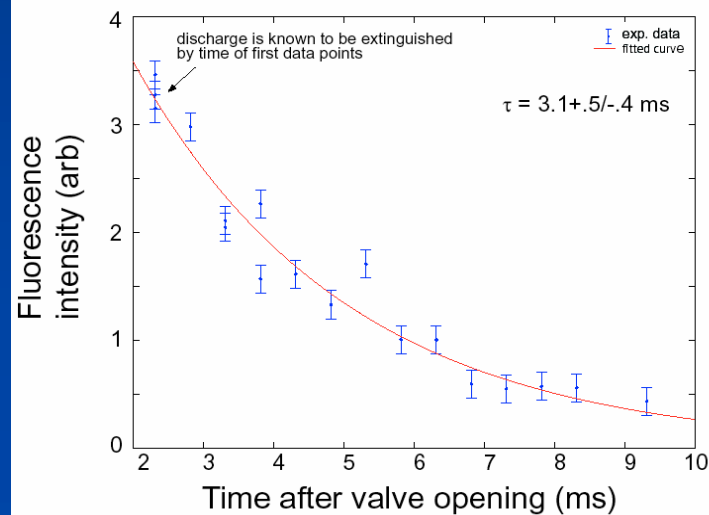
$$\lambda = 350^{+300}_{-200} \mu\text{m}$$

## Diffusion Lifetime in Cold Cell at He density $3 \times 10^{16} \text{ cm}^{-3}$

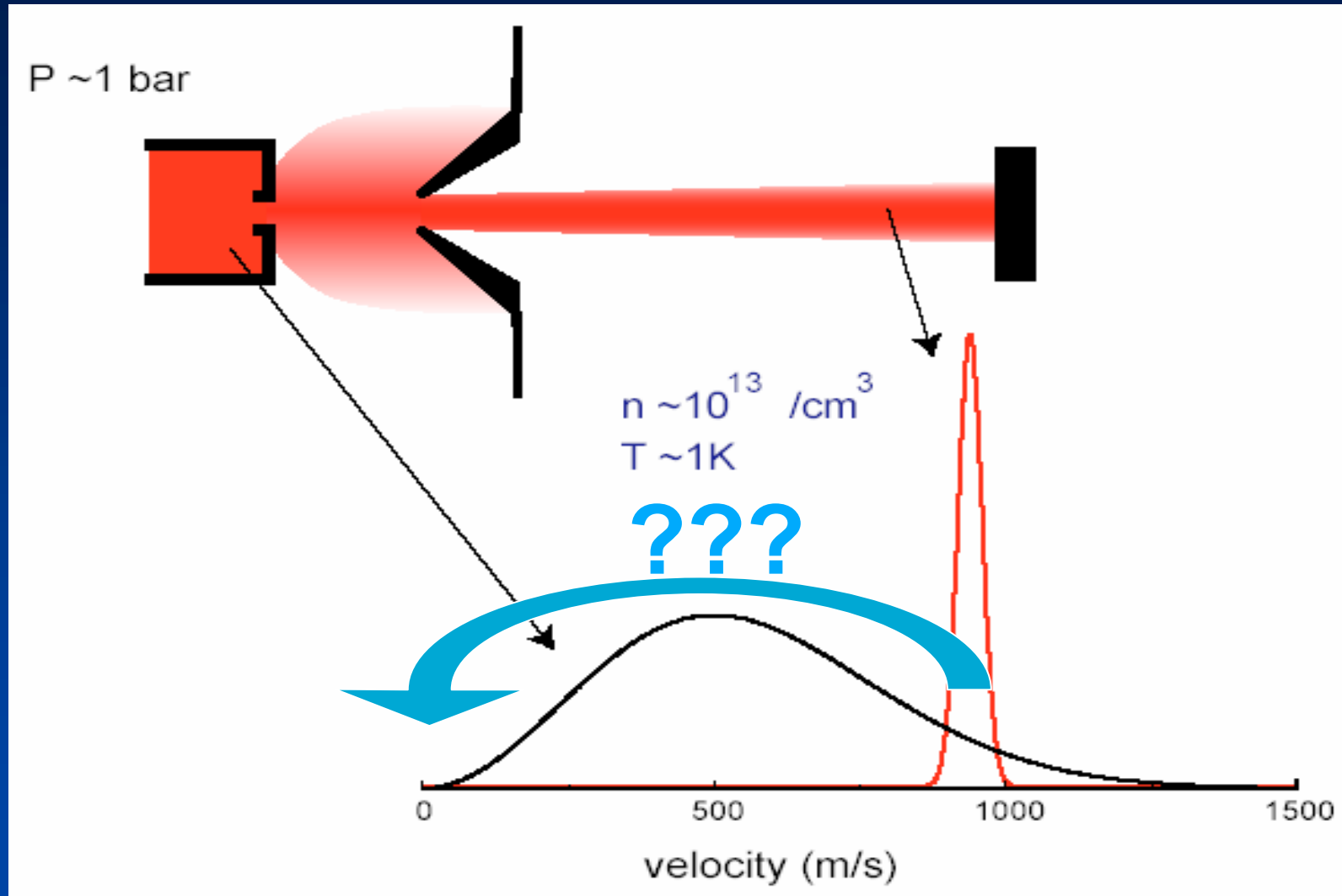
$$\tau_{\text{cell}} = 3.1^{+0.5}_{-0.4} \text{ ms}$$

## Measurement of lifetime of NH in buffer gas cell

with 9.4-9.6 mTorr of He as measured by room temperature convection

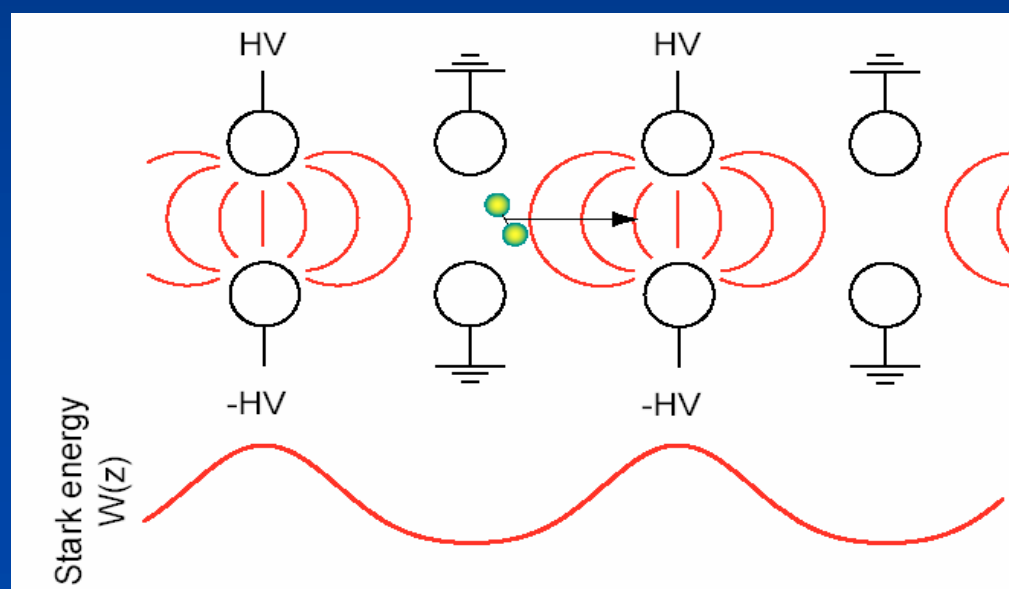
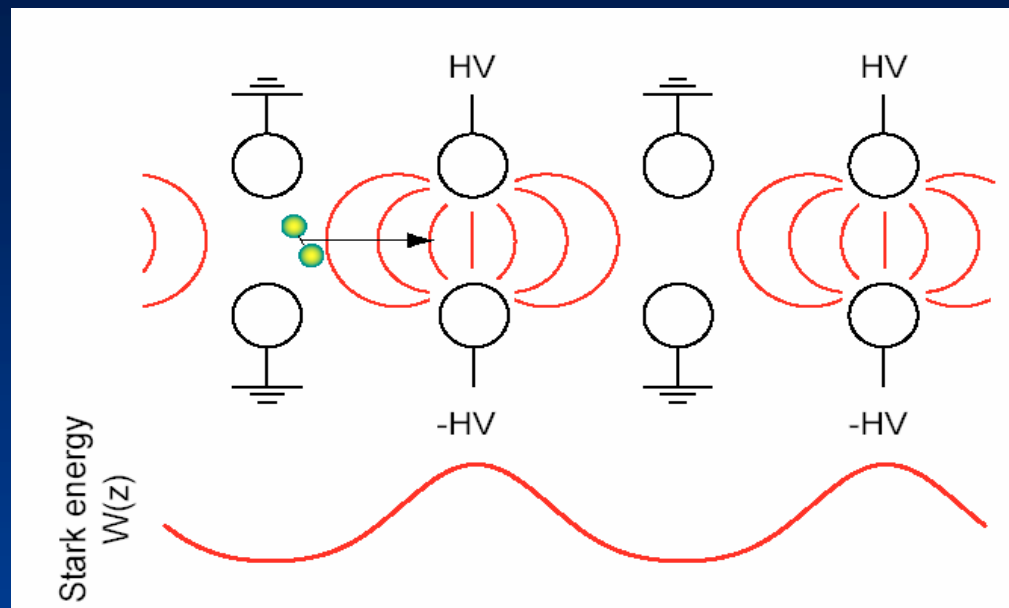
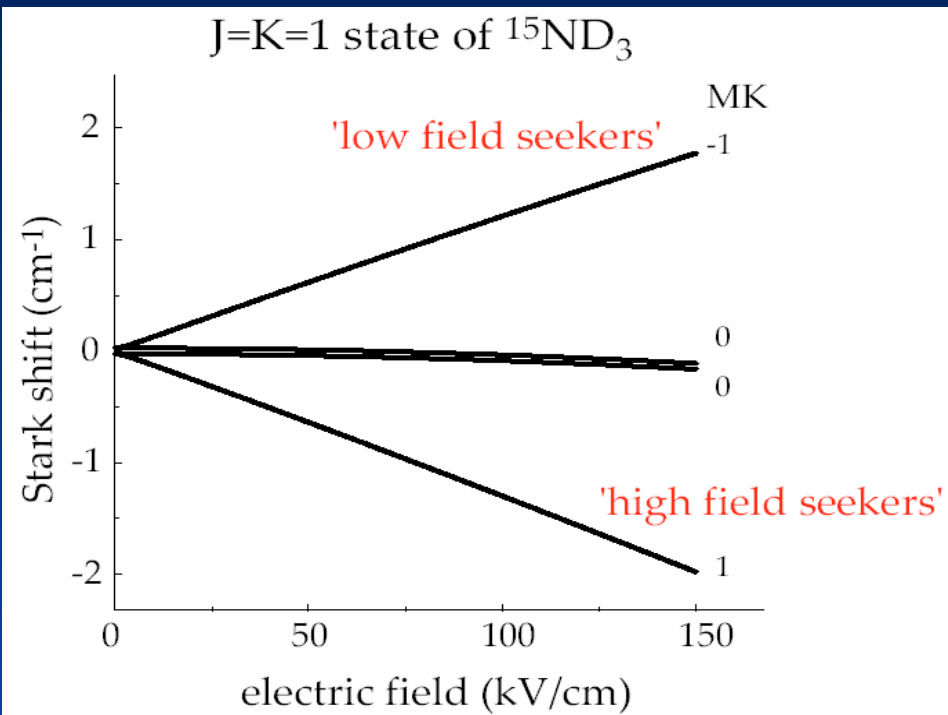


# stark slowing of polar molecules

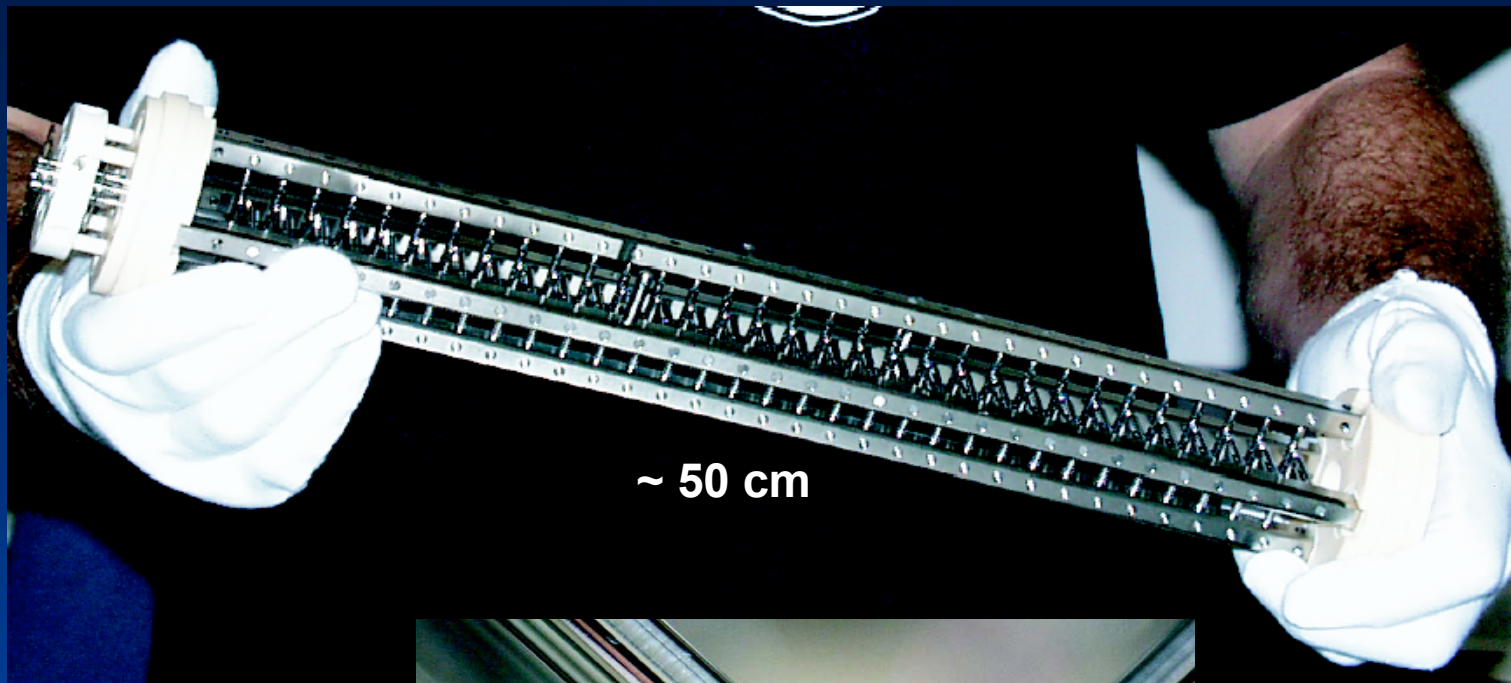


# stark slowing of polar molecules

use stark shift!!!



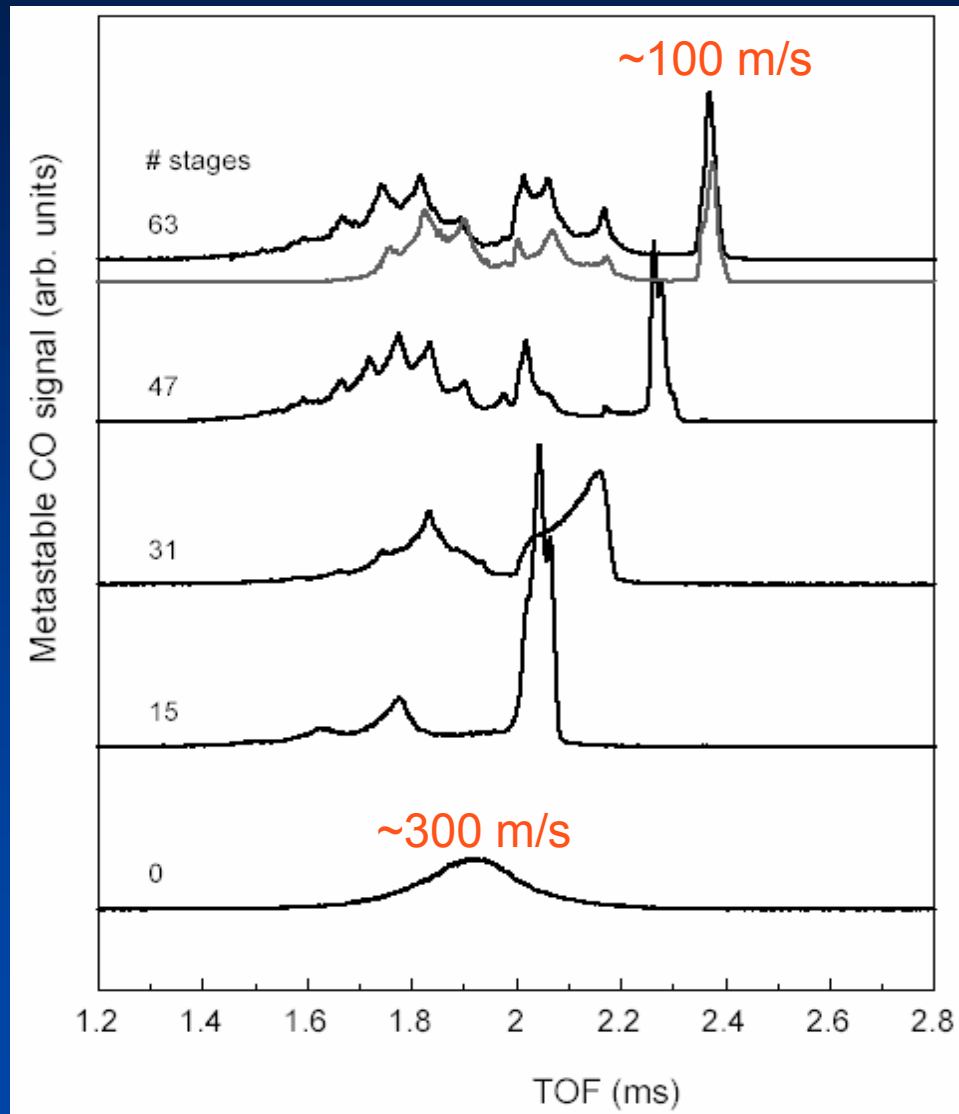
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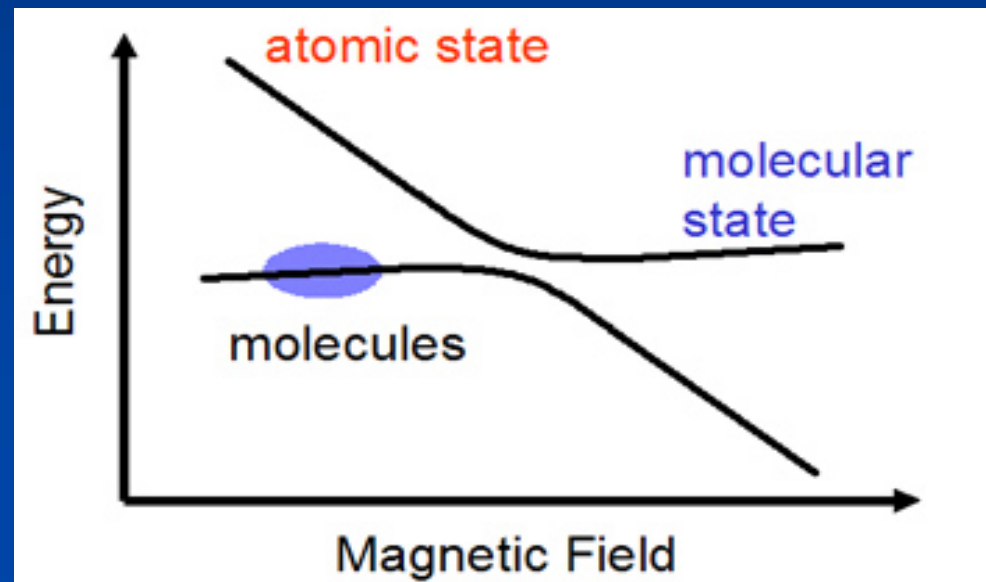
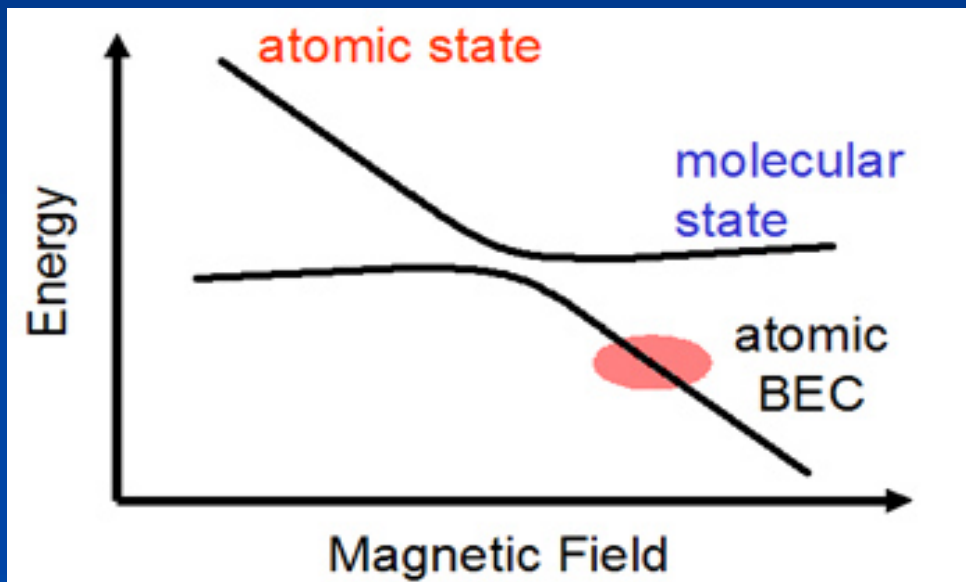
# stark slowing of polar molecules

first  
results:



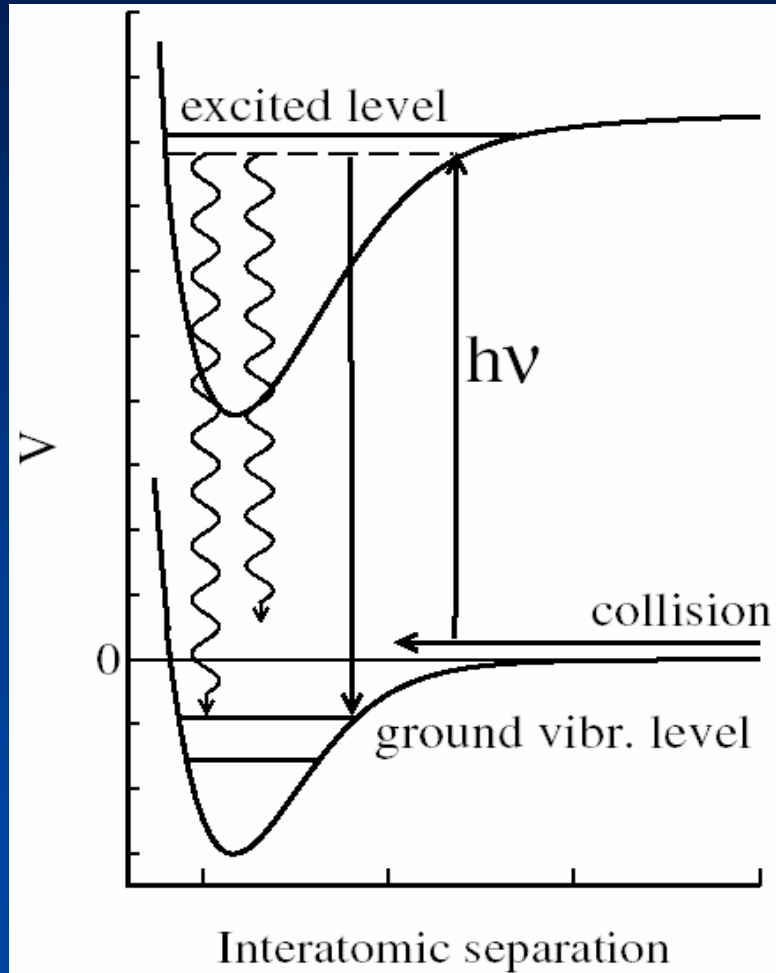
# indirect production of cold molecules

- use interspecies Feshbach resonance
  - Li-Na (Stan et al., PRL 93, 143001 (2004)), Rb-K (Simoni et al., PRL 60, 163202 (2003))
  - molecules have very short lifetime; exception: dimers of fermionic atoms (Petrov et al., J. Phys. B: At. Mol. Opt. Phys. 38, 645 (2005) )
  - high vibrational states  $\Rightarrow$  negligible dipole moment



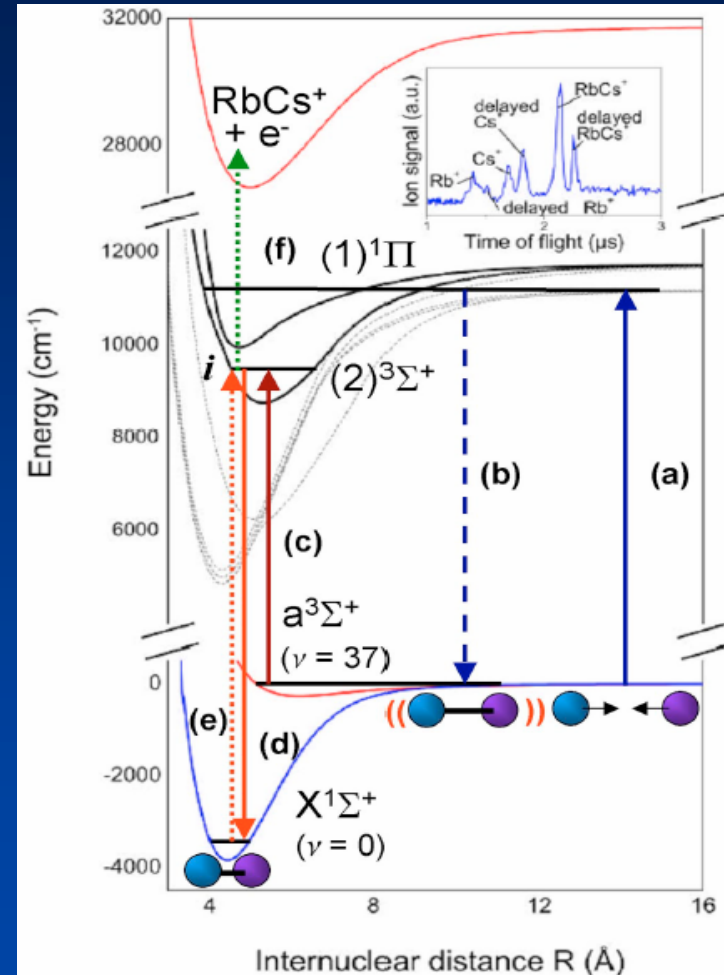
# indirect production of cold molecules

- photoassociation



eg. Rb-K, Wang et al.,  
arXiv:physics/0506232

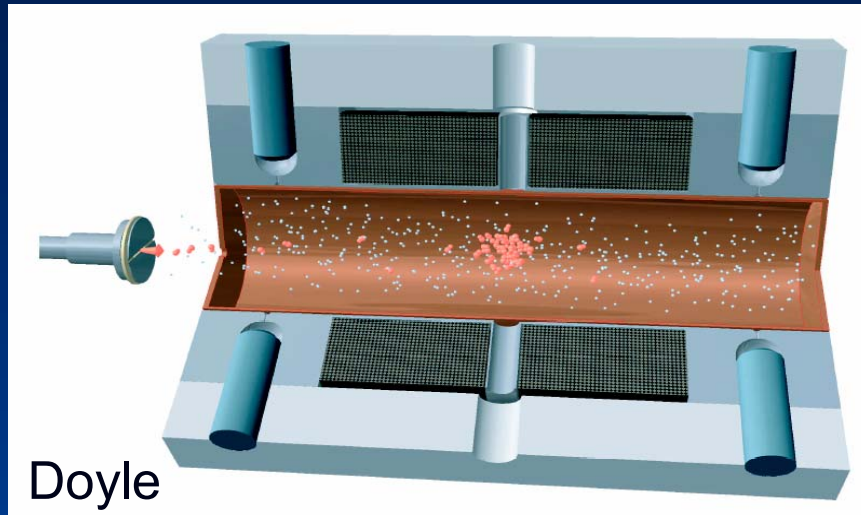
- multistep process



Rb-Cs ground state molecules (500/s)  
Sage et al., PRL 94, 203001 (2005)

# trapping of cold molecules I

## magnetic trapping:



### Trapping Magnet

Anti-Helmholtz quadrupole trapping field

Superconducting NbTi windings

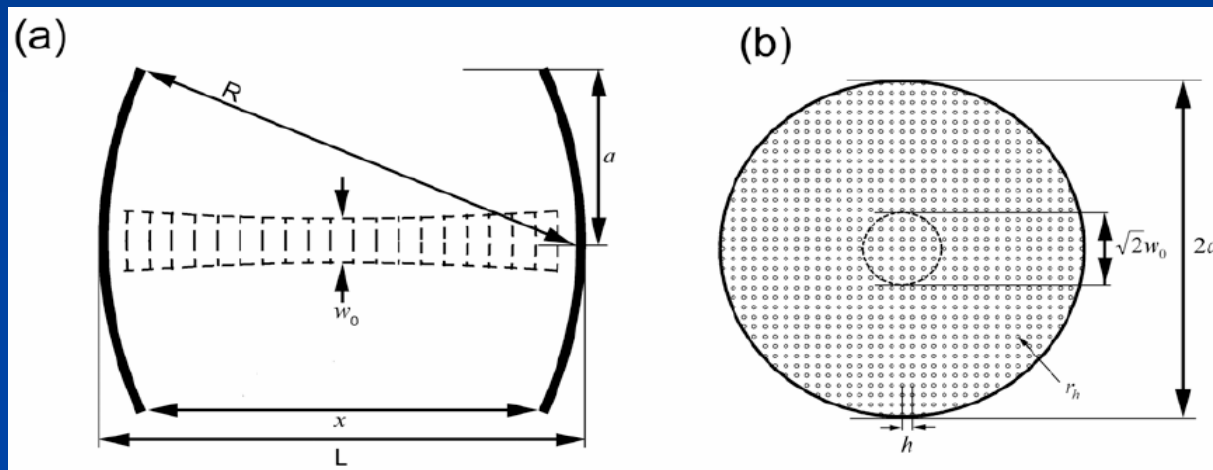
Large magnet bore (3") for loading and trapping

Current can be ramped for evaporative cooling

Magnet to operate in vacuum

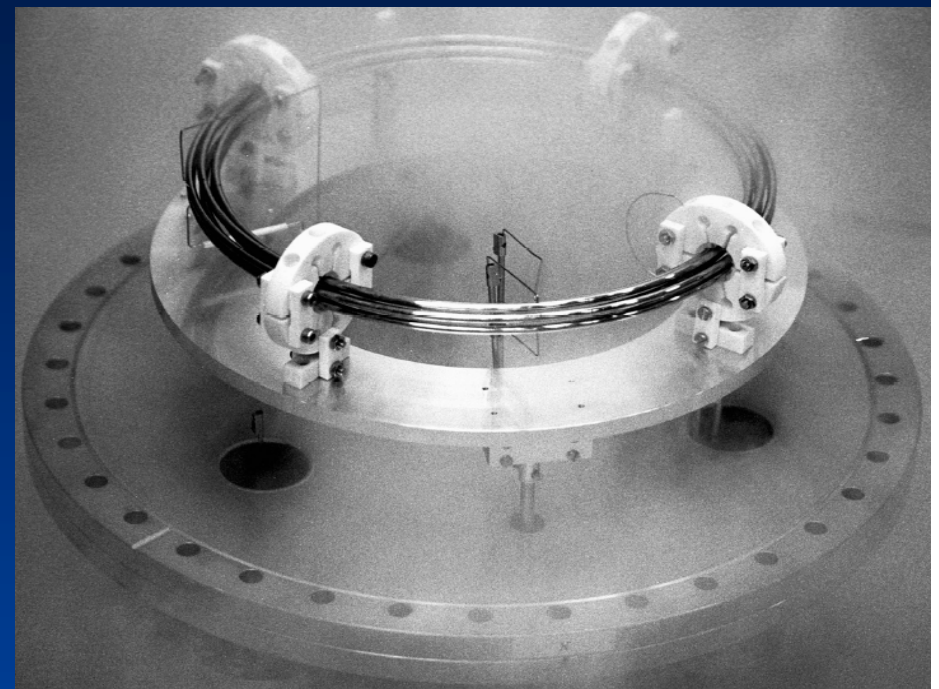
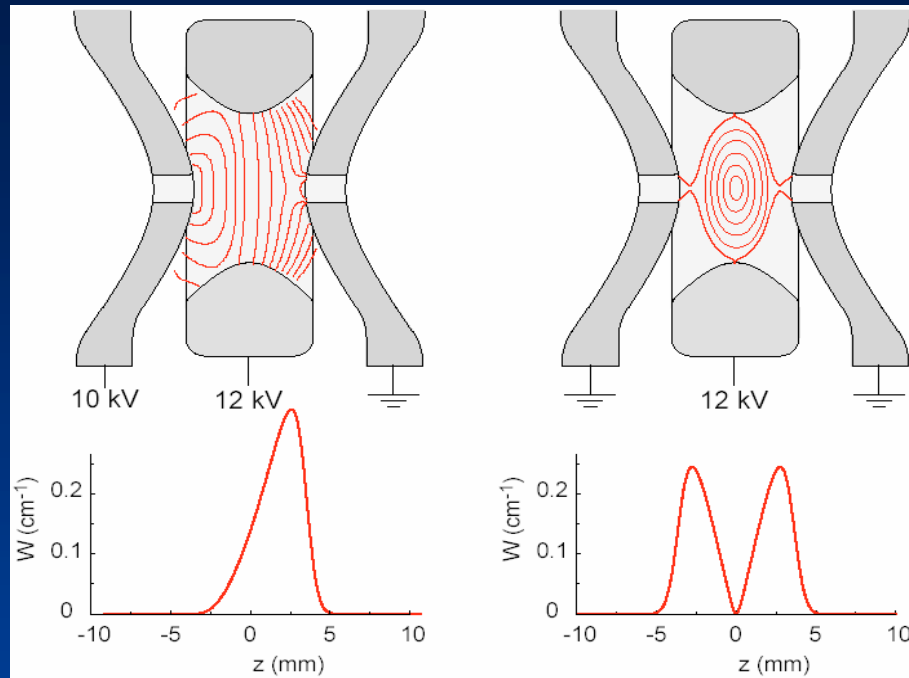
Trap Depth = 6 K for  $2\mu_B$  at 4.5 Tesla

## quasi-electrostatic trapping:

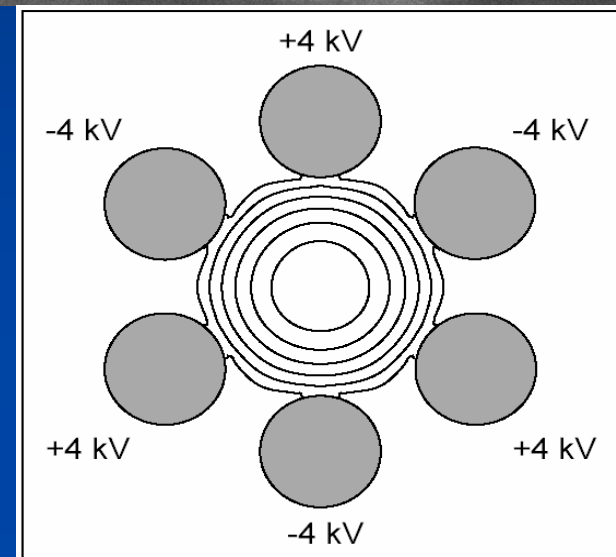
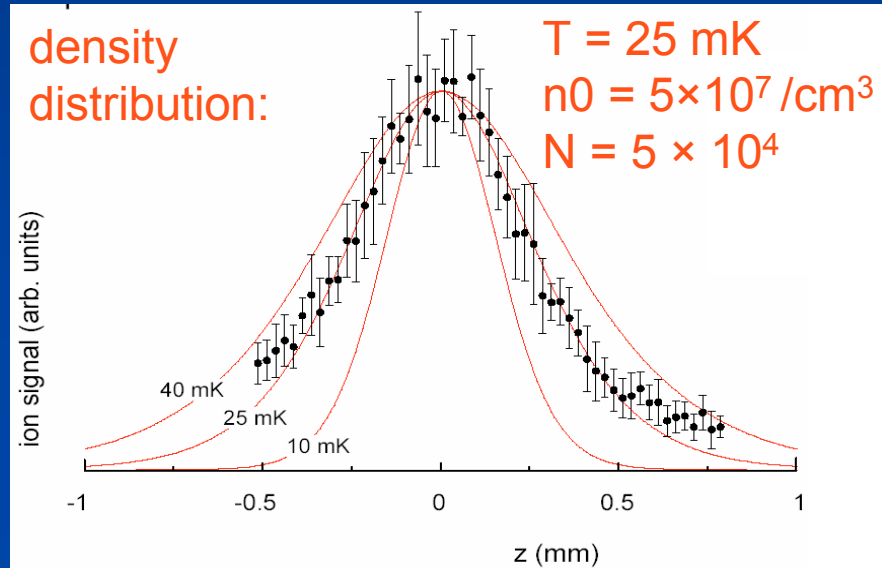


D. DeMille, D.R. Glenn, and J. Petrick, „Microwave traps for cold polar molecules”. Eur. Phys. J. D **31**, 375 (2004)

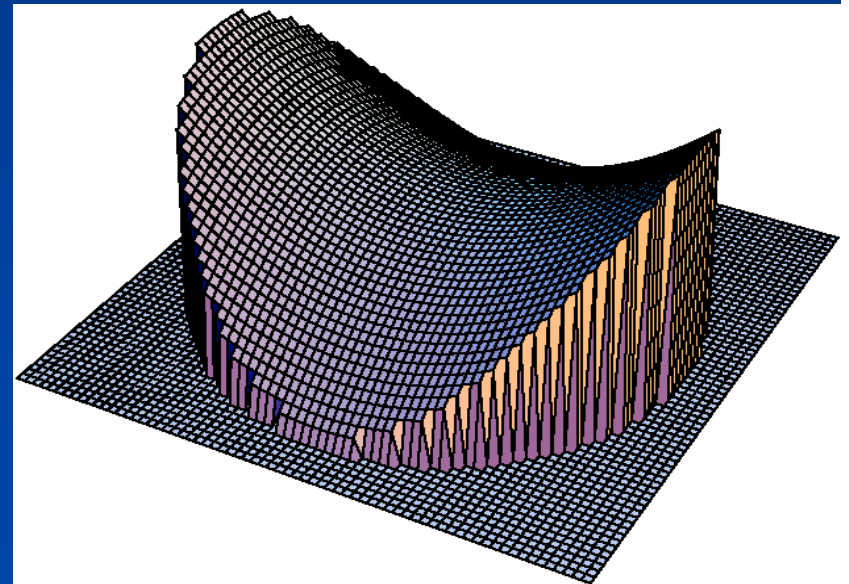
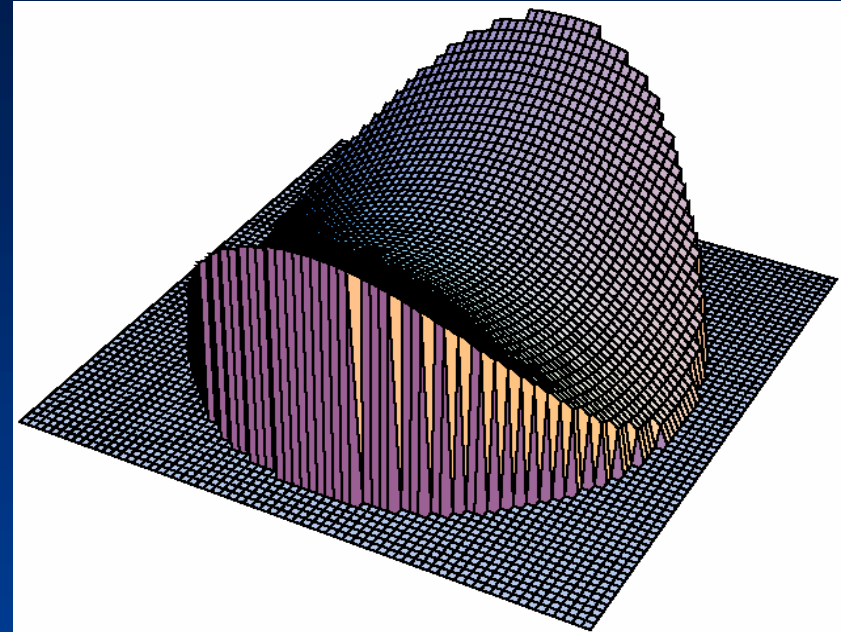
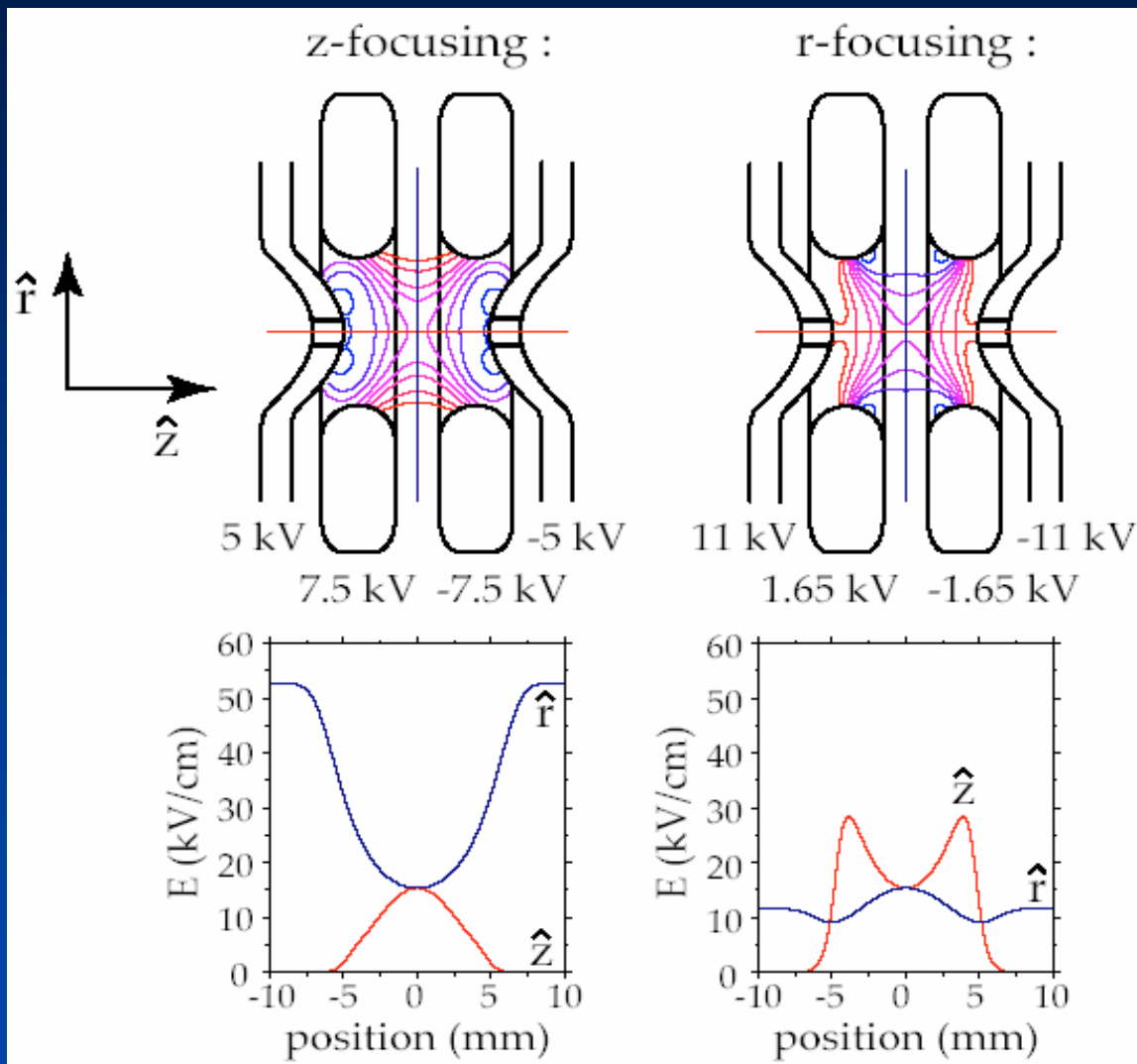
# electrostatic trapping of cold molecules



density  
distribution:



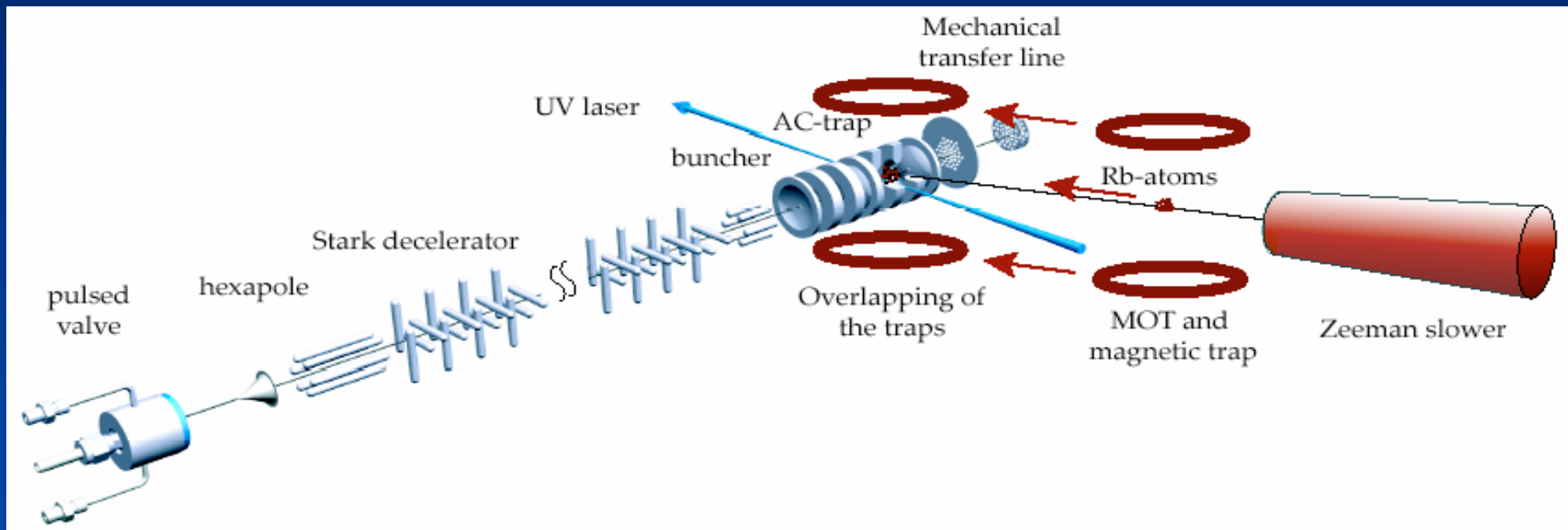
# electrodynamical trapping of cold molecules



J. v. Veldhoven et al., PRL **94**, 083001 (2005)  
 $T \sim 1 \text{ mK}$ ,  $N = 10^4$  in  $V = 0.02 \text{ cm}^3$ ,  $n = 5 \times 10^5 \text{ cm}^{-3}$

# from cold to ultracold molecules

further cooling plans: sympathetic cooling of molecules using MOT (Rb)



Gerard Meijer, Berlin

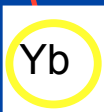
# outline & second summary

- motivation & dipolar systems “in the game”
  - atoms (magnetic dipoles, small, tuning possible)
  - heteronuclear molecules (large static electric dipoles)
- production of cold molecules
  - slowing & cooling of molecules (direct production)
  - making molecules out of cold atoms (indirect production)
  - trapping dipolar molecules
  - strong effort, many groups, promising results, not yet there
- BEC of atoms with high magnetic moments (Cr)
  - what is special about Cr?
  - how to get BEC... problems & solutions
- first observation of dipole-dipole interaction in a degenerate quantum gas



# Cr in periodic table of elements

<b>1</b> 1. Hg IA																<b>51,9961</b> [Ar]3d <sup>5</sup> 4s <sup>1</sup>																<b>18</b> 8. Hg VIIIA																																																																																																																																																																																																																																																															
1,00794 <b>1</b> H -1,1																<b>24</b> Cr 0,2,3,6																4,002602 <b>2</b> He -2,2																																																																																																																																																																																																																																																															
2. Hg IIA																1857 2482 Chrom																20,1797 Helium																																																																																																																																																																																																																																																															
3. Hg IIIA																13 5 B 3																14 6 C -4,2,4																15 7 N -3,2,3,4,5																16 8 O -2,-1																17 9 F -1																10 Ne																																																																																																																																																																																															
11 Na																12 Mg																3. Hg																4. Hg																5. Hg																6. Hg																7. Hg																8. Hg																																																																																																																																																																															
19 K																20 Ca																21 Sc																22 Ti																23 V																<b>24</b> Cr																25 Mn																26 Fe																27 Co																28 Ni																29 Cu																30 Zn																31 Ga																32 Ge																33 As																34 Se																35 Br																36 Kr															
37 Rb																38 Sr																39 Y																40 Zr																41 Nb																42 Mo																43 Tc																44 Ru																45 Rh																46 Pd																47 Ag																48 Cd																49 In																50 Sn																51 Sb																52 Te																53 I																54 Xe															
55 Cs																56 Ba																57 - 71 La-Lu Lanthanoide																72 Hf																73 Ta																74 W																75 Re																76 Os																77 Ir																78 Pt																79 Au																80 Hg																81 Tl																82 Pb																83 Bi																84 Po																85 At																86 Rn															
87 Fr																88 Ra																89 - 103 Ac-Lr Actinoide																104 Rf																105 Db																106 Sg																107 Bh																108 Hs																109 Mt																110 Uun																111 Uuu																112 Uub																113 Uut																114 Uuq																115 Uup																116 Uuh																117 Uus																118 Uuo															
Francium																Radium																Rutherfordium																Dubnium																Seaborgium																Bohrium																Hassium																Meitnerium																Ununilium																Unununium																Ununbium																Ununtrium																Ununquadium																Ununpentium																Ununhexium																Ununseptium																Unoctium																															



# motivation – Cr properties

51,9961	
[Ar]3d <sup>5</sup> 4s <sup>1</sup>	
24	Cr
0,2,3,6	
1857	1.6
2482	6.8
Chrom	

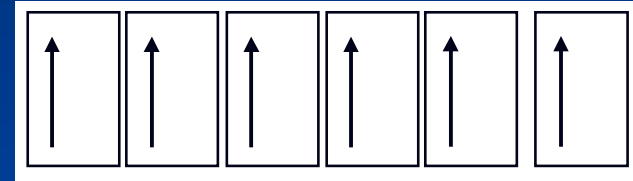
## ■ isotopic distribution

- Bosons ( $I=0$ ): <sup>52</sup>Cr (83.8%), <sup>50</sup>Cr (4.3%), <sup>54</sup>Cr (2.4%)
- Fermion ( $I=3/2$ ): <sup>53</sup>Cr (9.5%)

## ■ versatile level scheme

## ■ electronic configuration

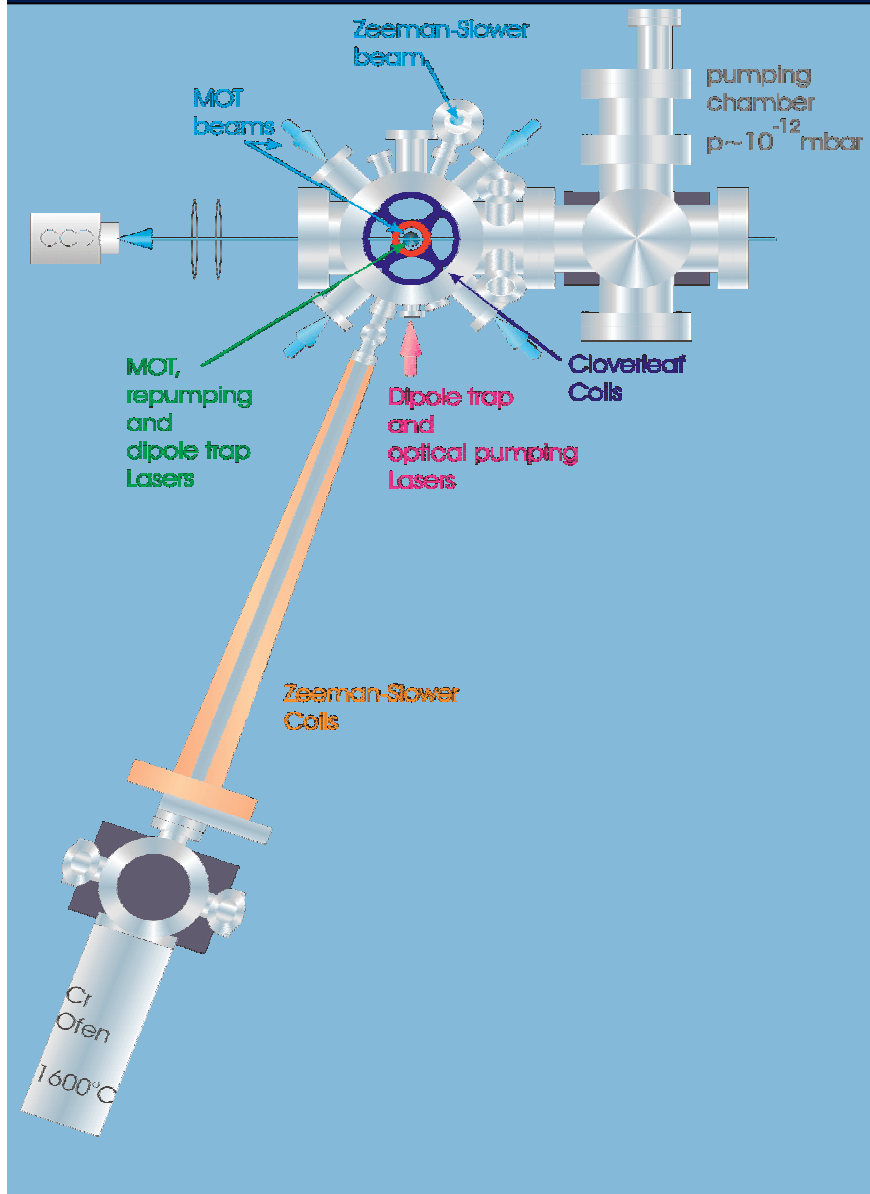
- [Ar]3d<sup>5</sup>4s<sup>1</sup> ⇒ **S=3**



## ■ large magnetic

moment  **$\mu = 6 \mu_B!$**

# preparation of cold & dense Cr cloud

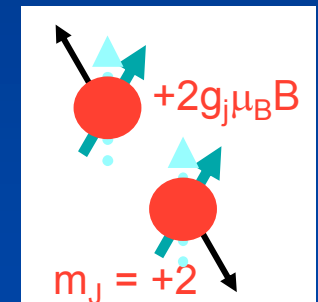
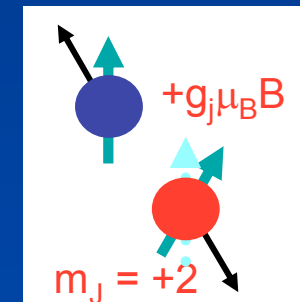
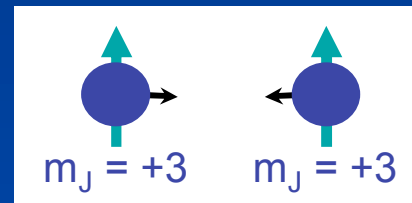


- continuously loaded Ioffe Pritchard trap (CLIP-trap)  
J. Stuhler et al. PRA **64**, 031405 (2001); P. O. Schmidt et al. J. Opt. B **5**, S170 (2003)

- Doppler cooling in compressed IP-trap  
P. O. Schmidt, et al., J. Opt. Soc. Am. B **20**, 5 (2003)

$2 \times 10^8$  atoms in the ground state  
phase space density  $\rho \sim 10^{-7}$

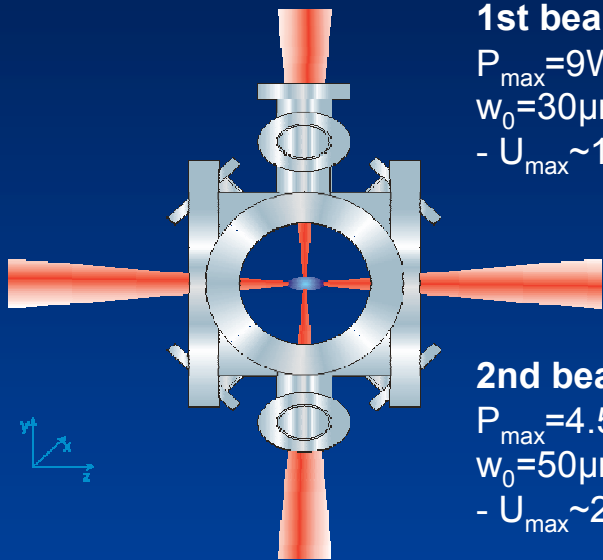
- rf-evaporation → stop by dipolar relaxation



- no BEC in MT! ( $\beta > 10^{12} \text{ cm}^3/\text{s}$ )  
S. Hensler et al., Appl. Phys. B **77**, 765 (2003)

# the way out

- optical dipole trap:  
20W fibre Laser @  $\lambda=1064$  nm

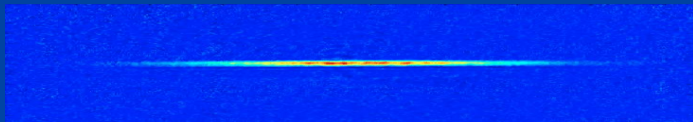


**1st beam:**  
 $P_{\max}=9W$   
 $w_0=30\mu m$   
 $-U_{\max}\sim 130\mu K$

**2nd beam:**  
 $P_{\max}=4.5W$   
 $w_0=50\mu m$   
 $-U_{\max}\sim 22\mu K$

## advantages:

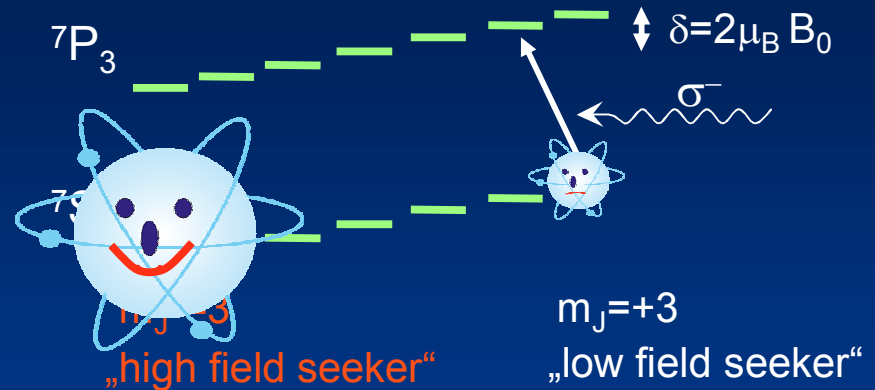
- operation at any offset field
- all magnetic substates trapable



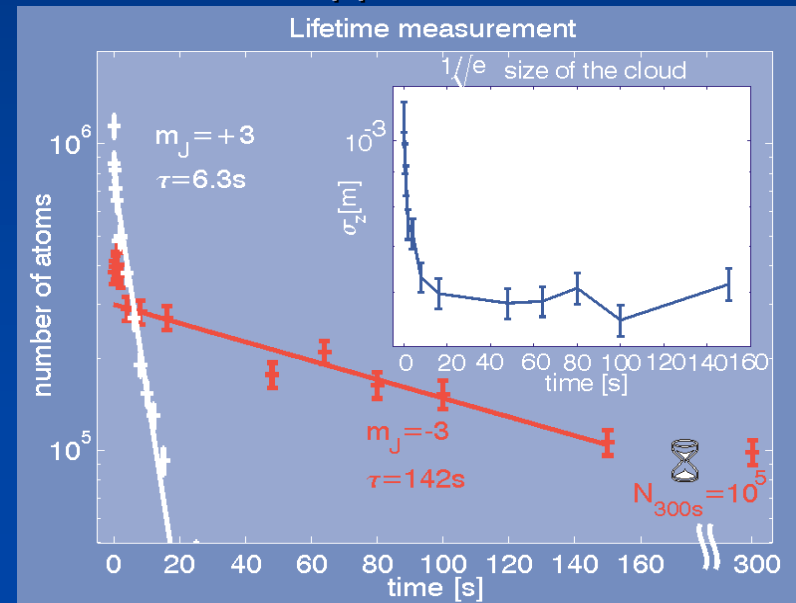
## problem:

- sample still mainly polarized in  $m_j=+3$

- pumping the atoms to magnetic ground state:

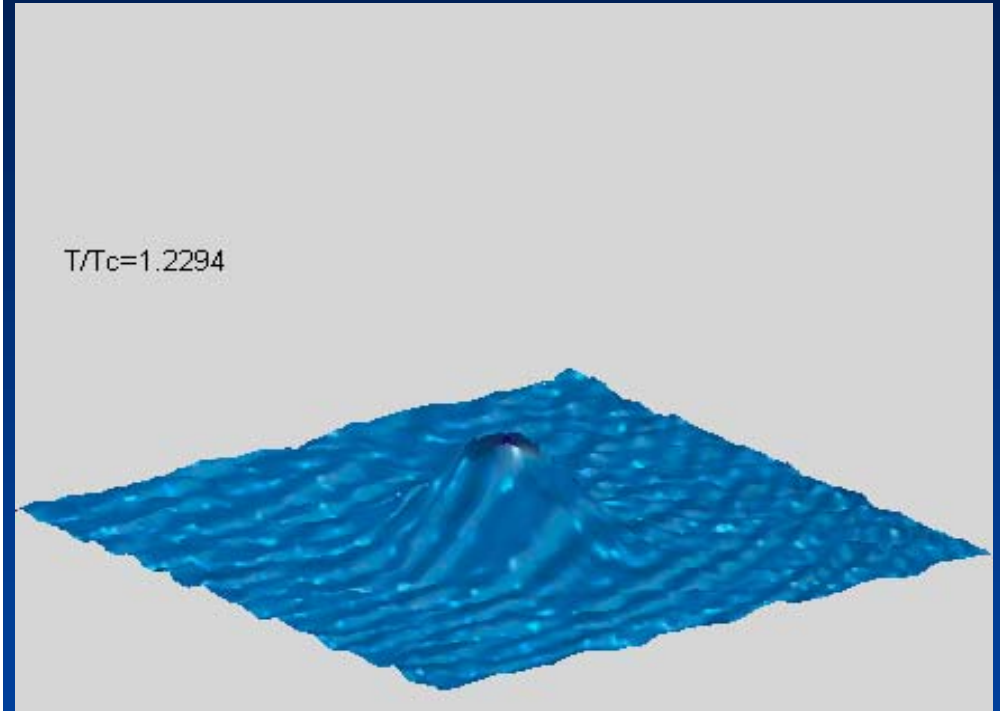
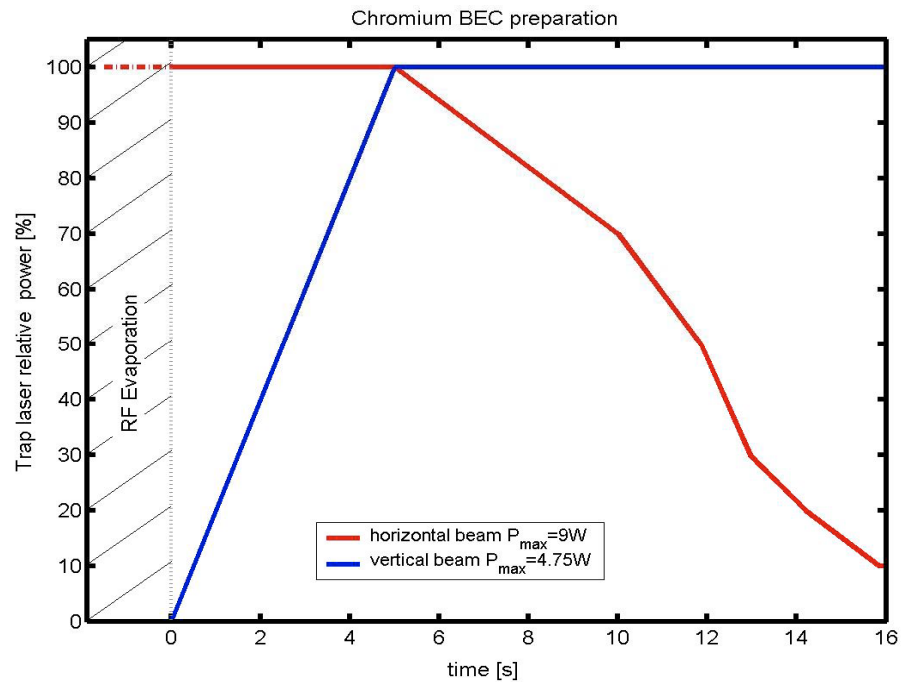


- dipolar relaxation suppressed



# the final step to BEC of Cr

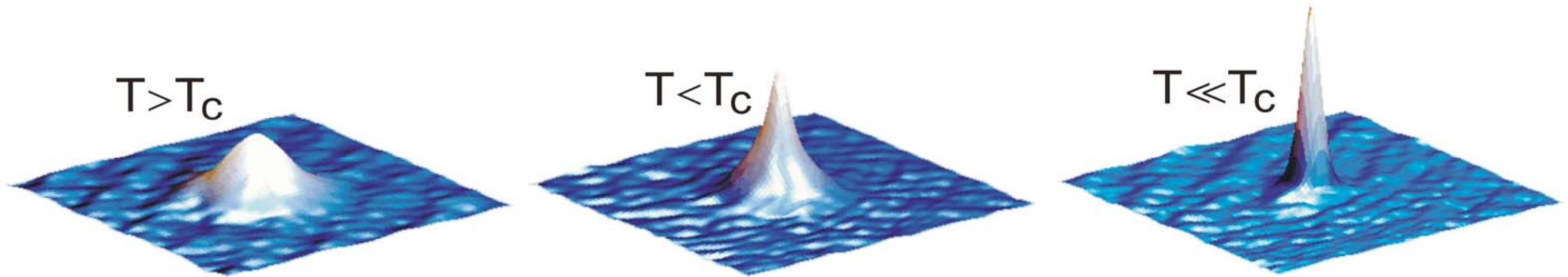
## evaporation in crossed ODT



⇒ BEC

A. Griesmaier et al., PRL 94, 160401 (2005)

# Cr-BEC

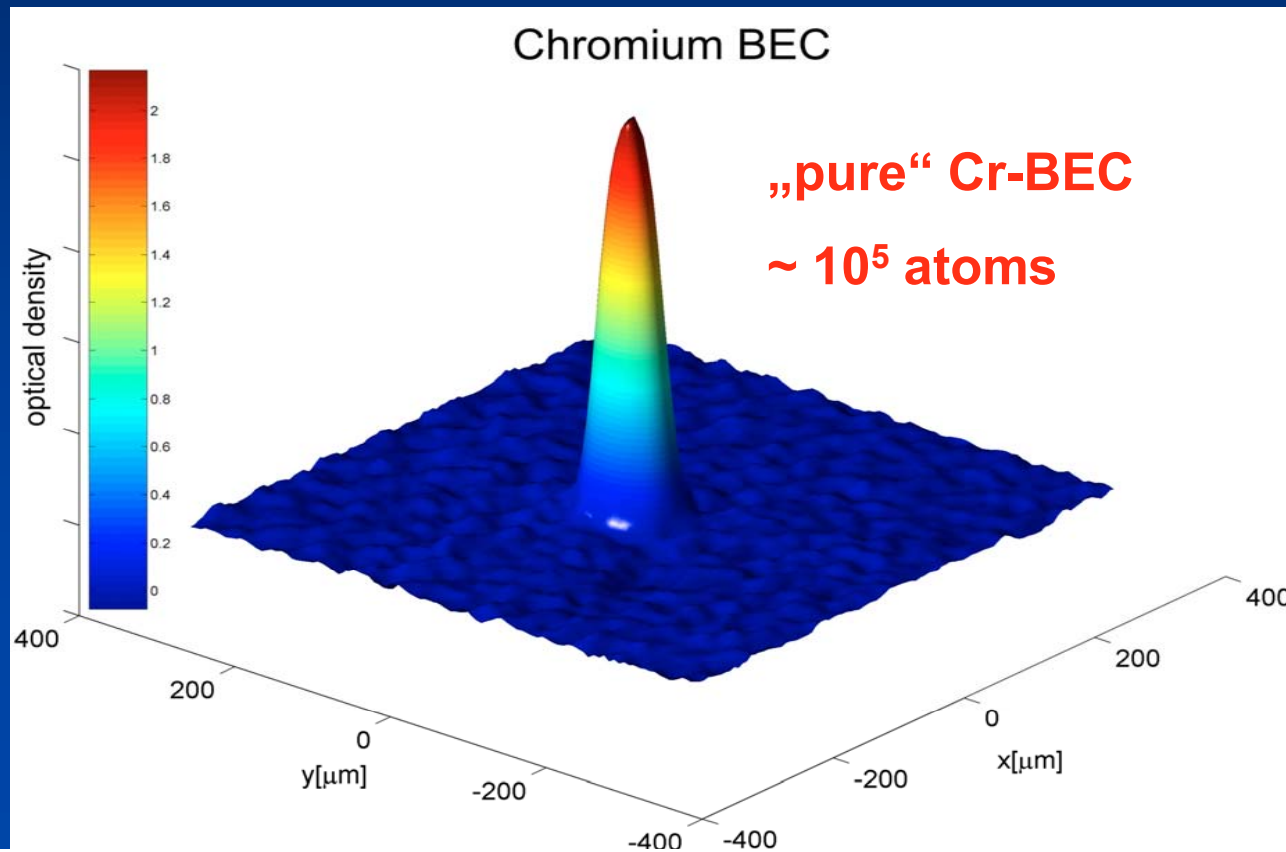


$T_c \sim 700$  nK

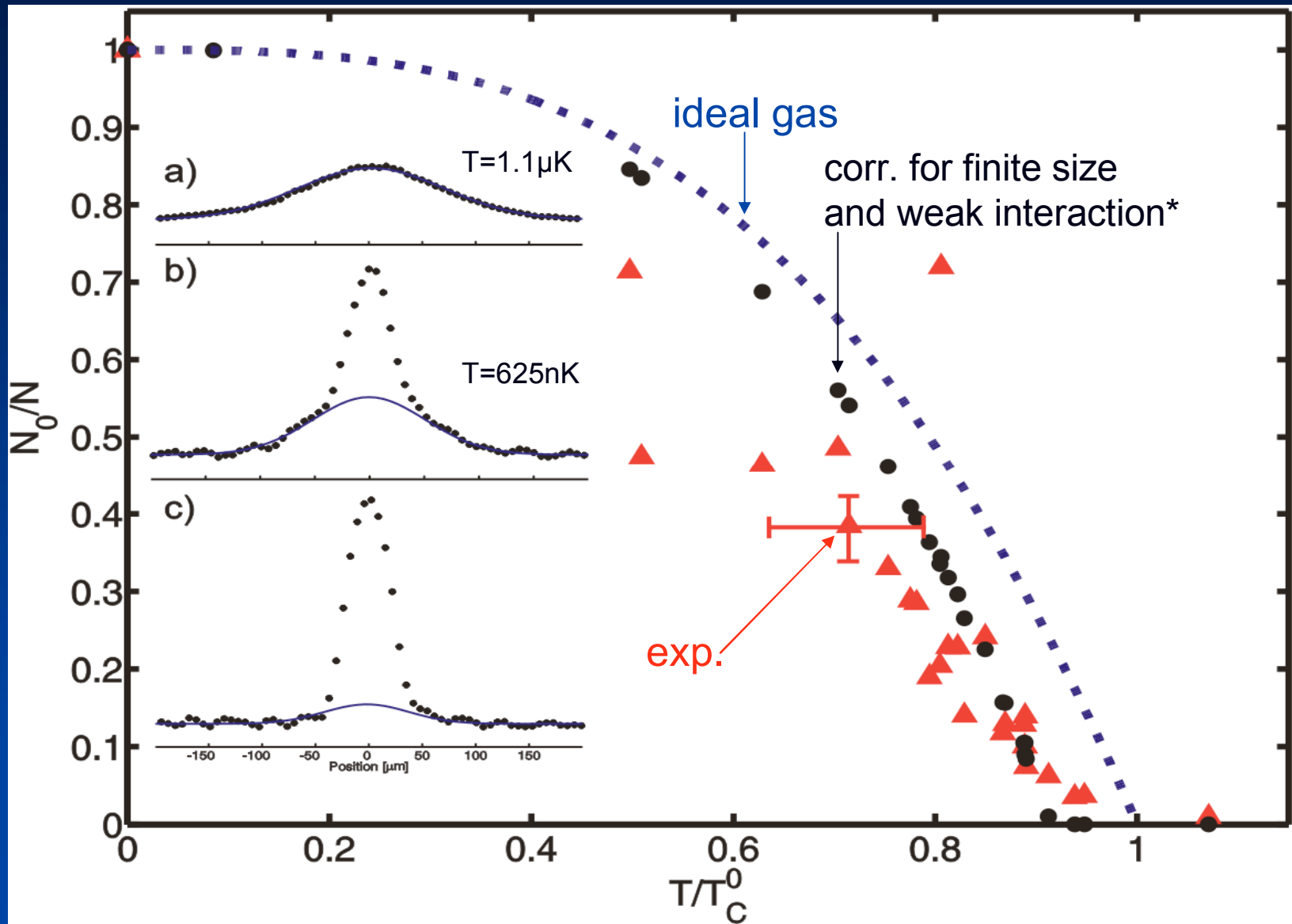
$\nu_x = 581$  Hz

$\nu_y = 406$  Hz

$\nu_z = 138$  Hz



# Cr-BEC & phase transition



$v_x=581\text{ Hz}$   
 $v_y=406\text{ Hz}$   
 $v_z=138\text{ Hz}$

$T_c \sim 700\text{ nK}$

\* S. Giorgini, L. P. Pitaevskii, and S. Stringari, Phys. Rev. A 54, R4633 (1996)

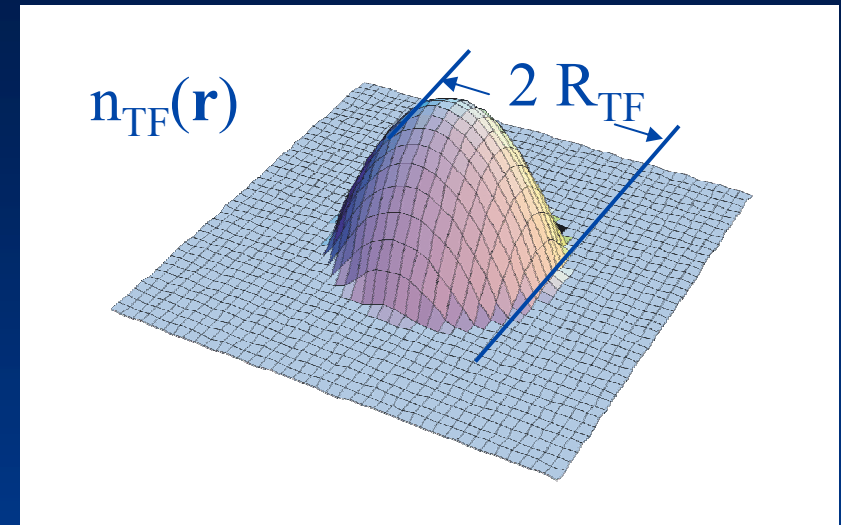
# outline & third summary

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  - making molecules out of cold atoms (indirect production)
  - trapping dipolar molecules
  - strong effort, many groups, promising results, not yet there
- BEC of atoms with high magnetic moments (Cr)
  - not easy but achieved, ready to go!
- first observation of dipole-dipole interaction in a degenerate quantum gas
  - dipole-dipole interaction modifies BEC expansion



# dipole-dipole interaction as perturbation

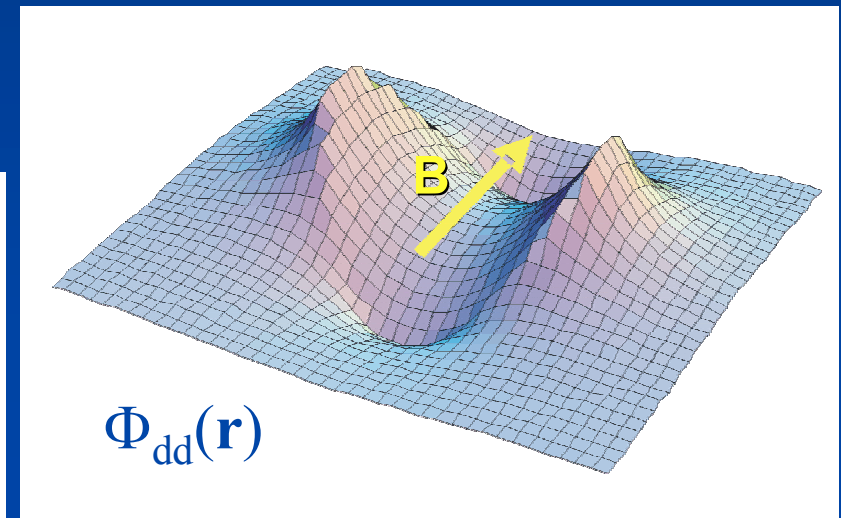
- BEC without dipoles in an
- isotropic harmonic trap
- in Thomas-Fermi limit



perturbation by dipole interaction:

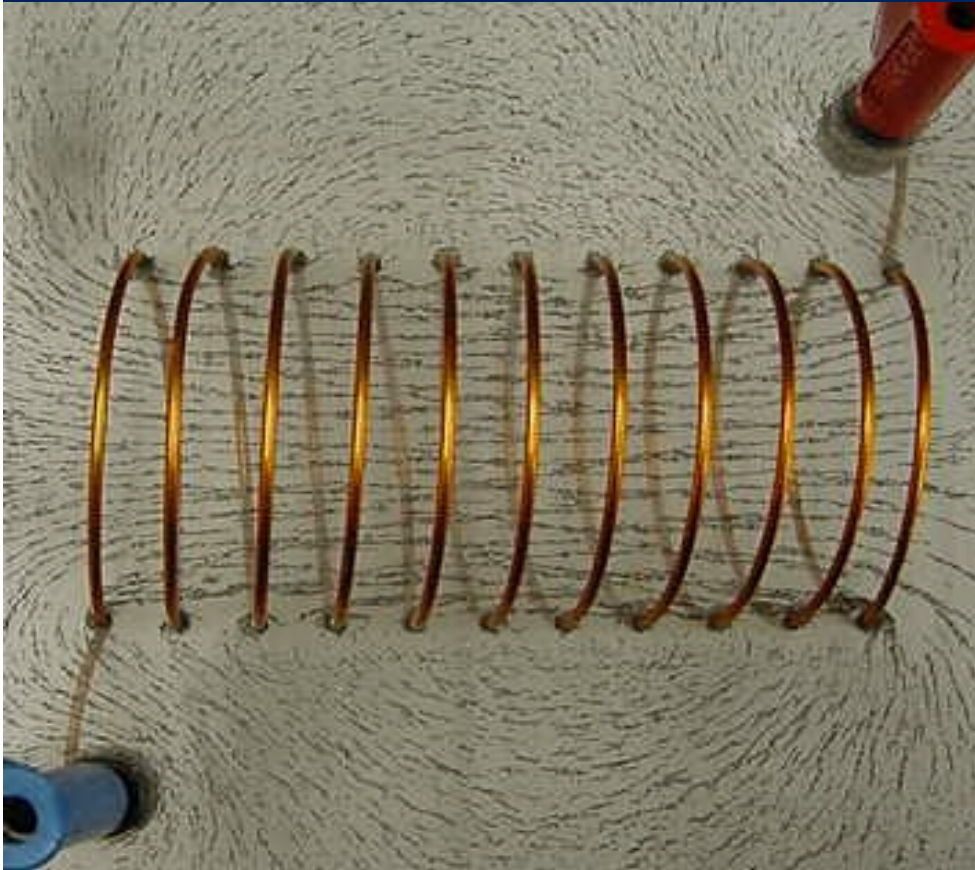
⇒ parabolic density profile

$$\begin{aligned}\Phi_{\text{dd}}(\mathbf{r}) &= \int n_{\text{TF}}(\mathbf{r}') U_{\text{dd}}(\mathbf{r} - \mathbf{r}') d\mathbf{r}' \\ &= -\frac{\varepsilon_{\text{dd}} m \omega_0^2}{5} [3 \cos^2 \vartheta - 1] r^2; \quad r < R_{\text{TF}}\end{aligned}$$



# similar behaviour with solids and liquids

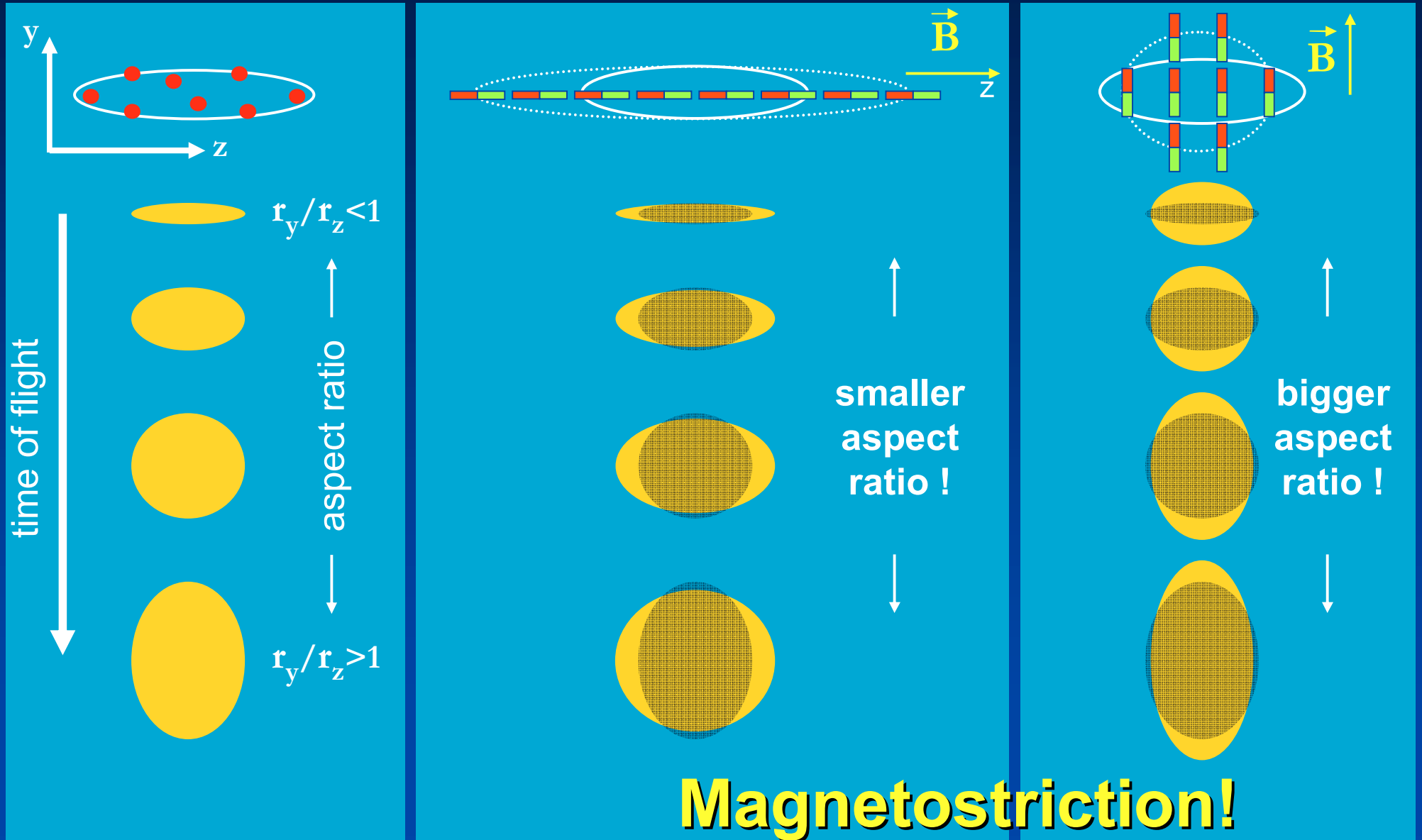
iron particles:



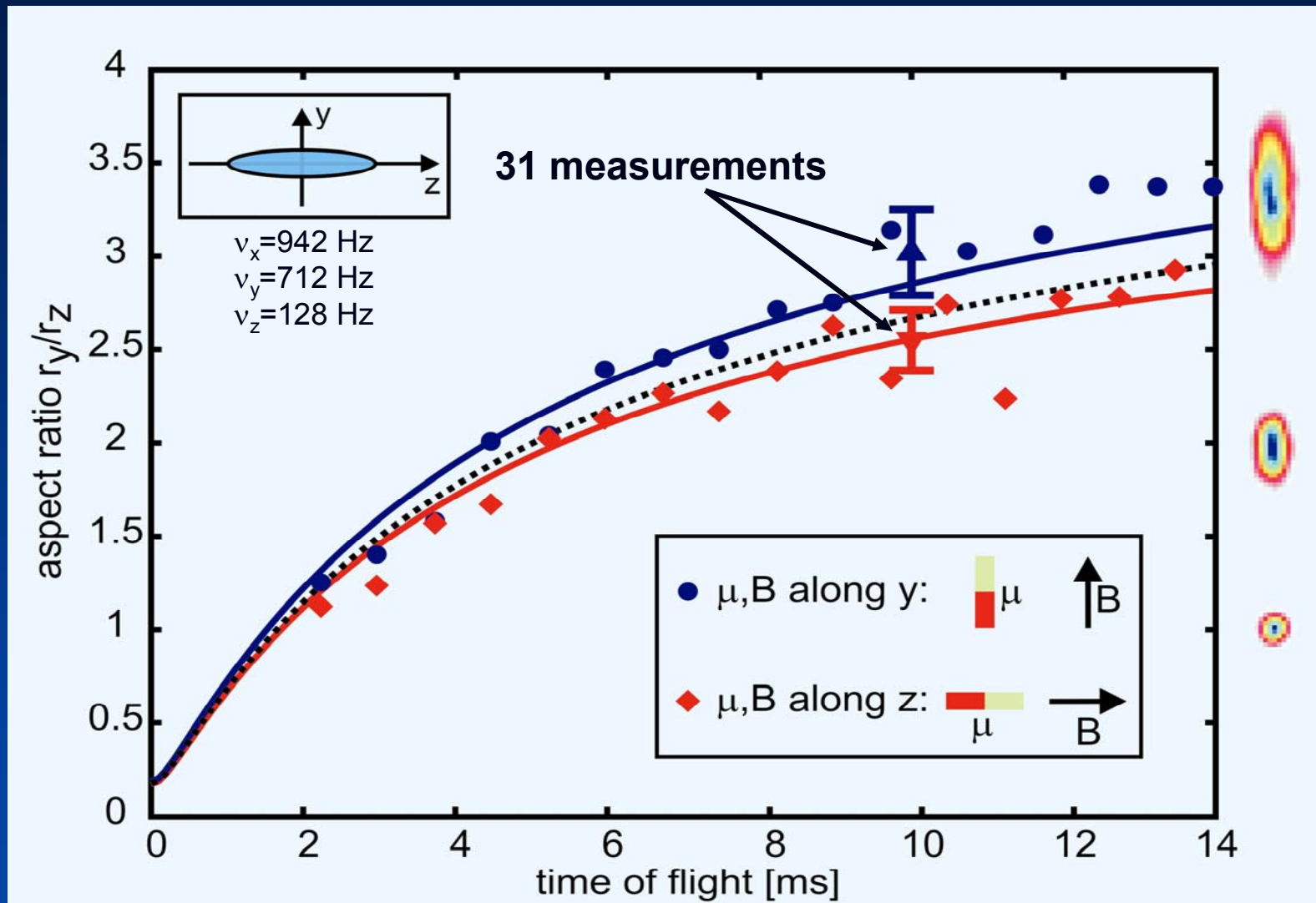
ferrofluids:



# dipole-dipole interaction & aspect ratio



# magnetostriction/dipolar expansion



**theory – no free parameters!**

S. Giovanazzi, P. Pedri, L. Santos

# final summary

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  - trapping dipolar molecules
  - strong effort, many groups, promising results, not yet there
- BEC of atoms with high magnetic moments (Cr)
- first manifestation of dipole-dipole interaction in a degenerate quantum gas
  - dipole-dipole interaction modifies BEC expansion (magnetostriction)