



# Role of thermal instabilities and anomalous transport in the density limit

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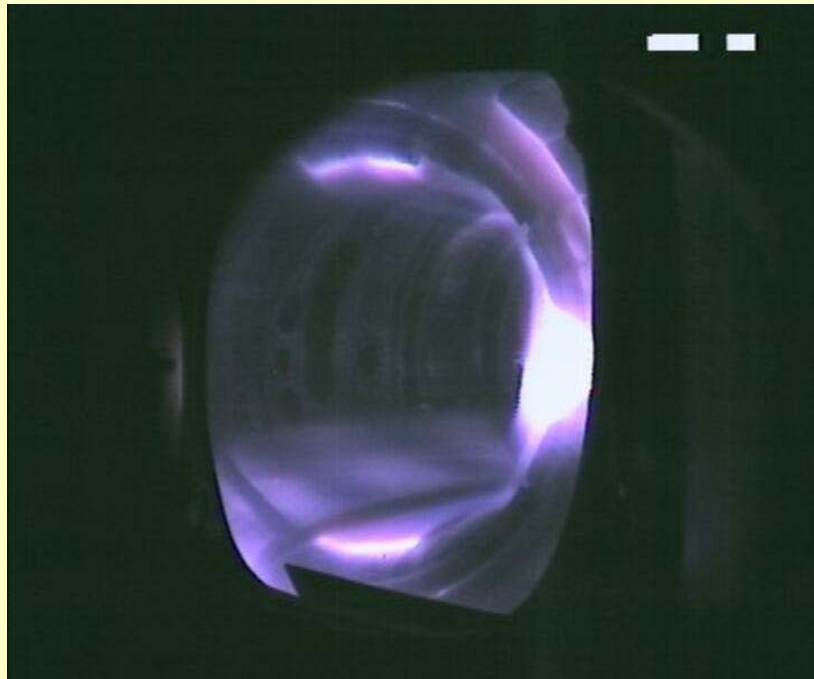
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- Motivation
- Standard explanation of Density Limit
- New experimental observations
- Interpretation and results of modelling
- Discussion and conclusion

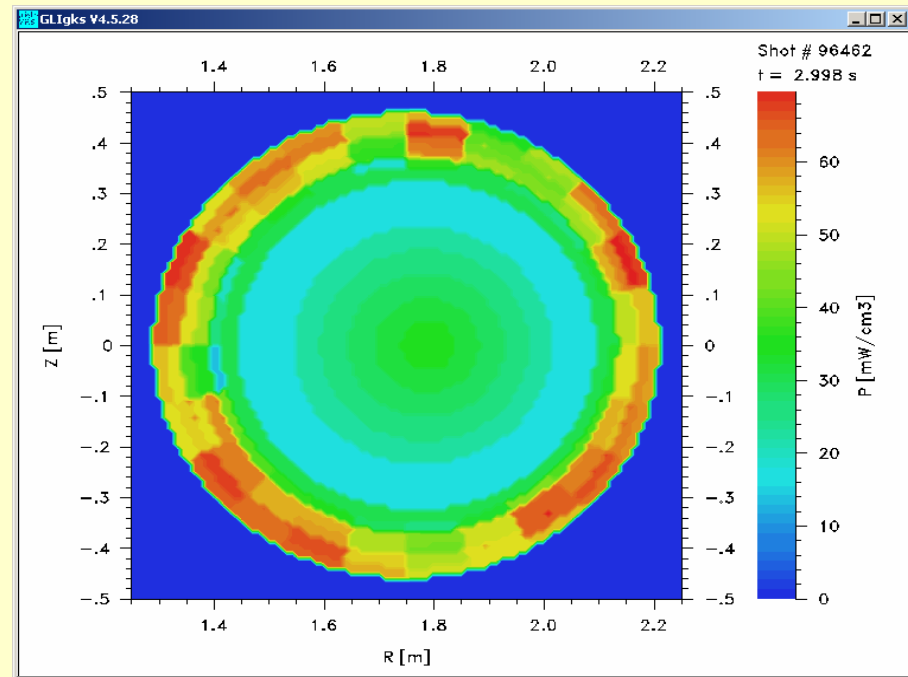


## Two scenarios for density limit (in TEXTOR)

Development of structures at the edge by critical density



MARFE in additionally heated plasmas



Detachment in ohmic plasmas

- What are the triggers and mechanisms of these events?
- What determines which kind of event will develop?

Standard explanation:

# Thermal Instabilities at the Edge due to Impurity Radiation

Impurity radiation density:

$$Q_{rad} = n n_I L_I \Rightarrow$$

Poloidally symmetric detachment:

densities  $n, n_I \approx const$ , temperature  $T$

$$\downarrow: T = T_0 + \tilde{T}, \tilde{T} < 0 \Rightarrow \tilde{Q}_{rad} = Q_{rad} \frac{d \ln L_I}{d \ln T} \frac{\tilde{T}}{T}$$

impurity radiation  $\uparrow$  if cooling rate  $\uparrow$  with  $\downarrow$  temperature

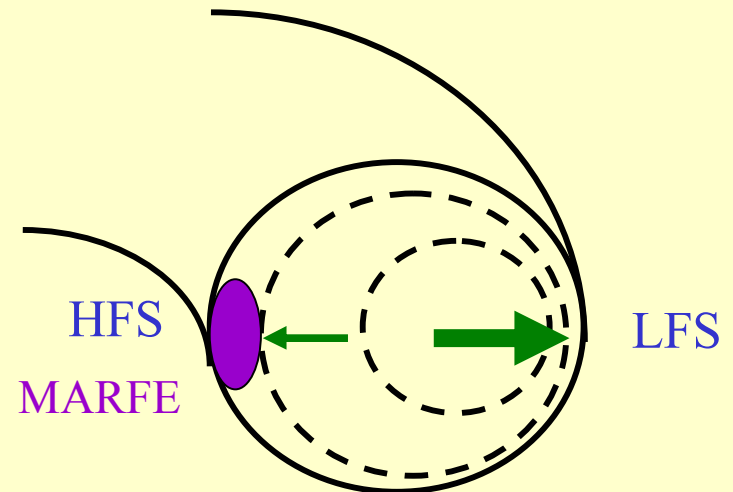
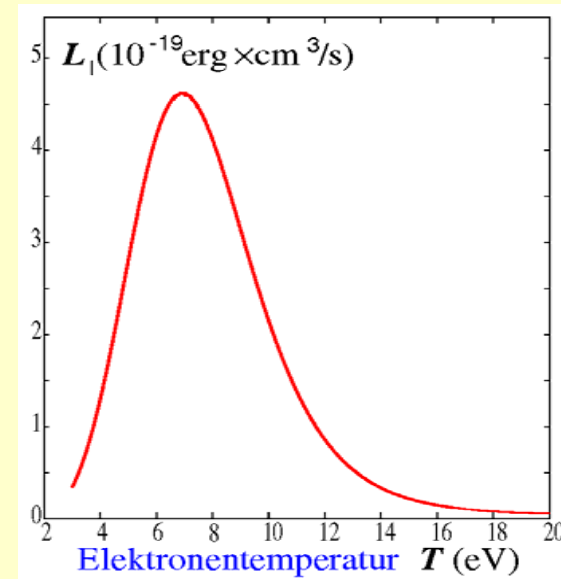
MARFE due to poloidally localized perturbations:

$nT, n_I T \approx const$ ,  $T \downarrow \Rightarrow n, n_I \uparrow$  pressures

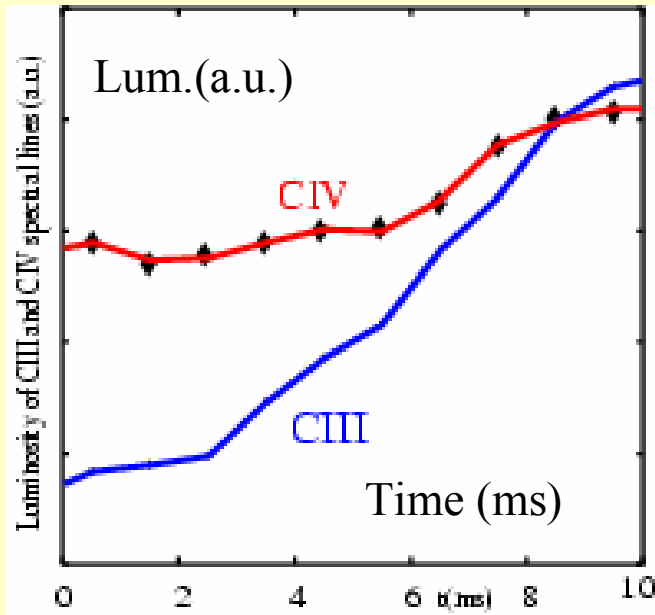
$$\tilde{Q}_{rad} = Q_{rad} \left( \frac{d \ln L_I}{d \ln T} - 2 \right) \frac{\tilde{T}}{T}$$

MARFE position : heat supply from core, counteracting radiation, is the **smallest** at HFS due to **shift** of magnetic surfaces

Carbon cooling rate in corona model



# Spectroscopic measurements on TEXTOR during MARFE formation

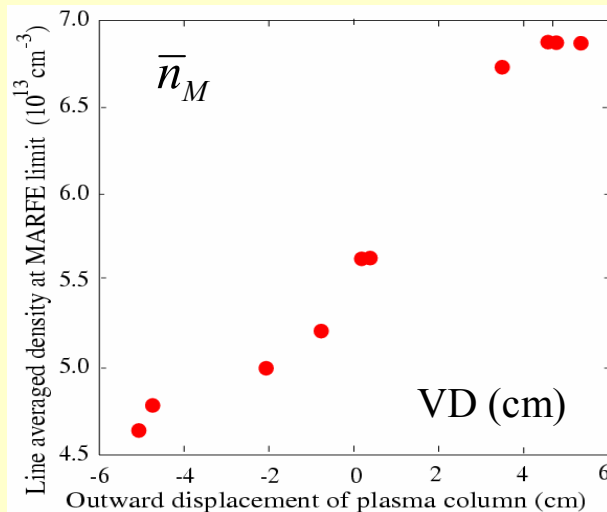


Contradicts to “ $dL_I/dT < 0$ ” concept: CIV radiation should grow first due to CV recombination

Why “ $dL_I/dT < 0$ ” does not work: effect of impurity transport

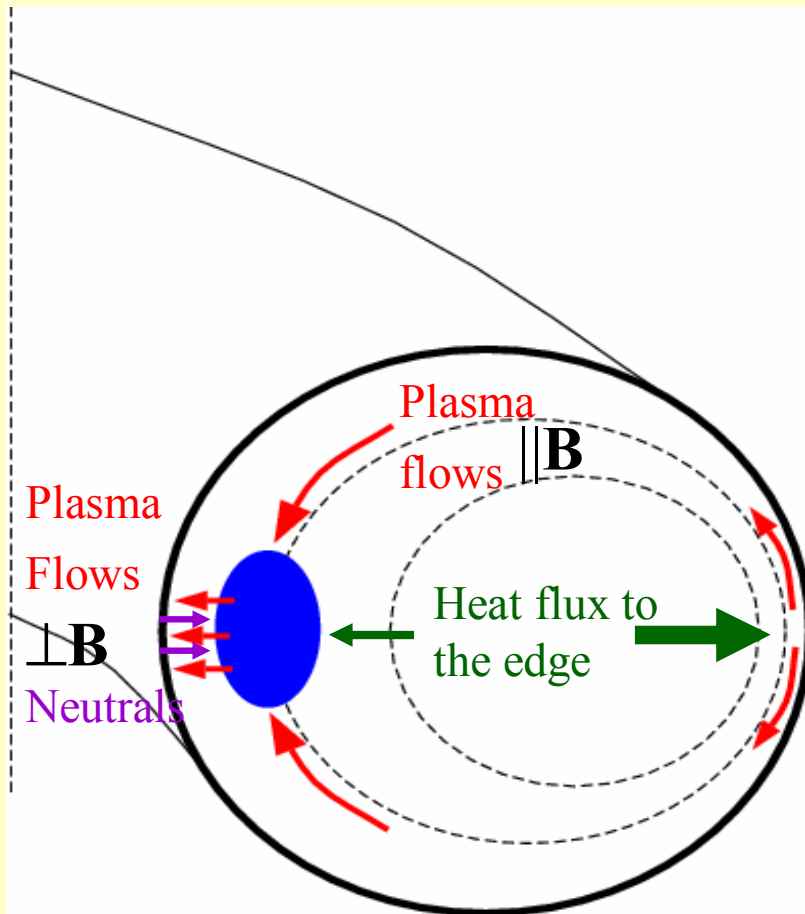
$$\frac{d \ln L_I}{d \ln T} = \left( \frac{d \ln L_I}{d \ln T} \right)_{cor} \frac{1}{1 + D_{\perp} k_{\perp}^2 / \nu_{rec}}$$

Observed time development: local release of impurity by a sudden increase of plasma-wall interaction at HFS



Important role of plasma-wall interaction: MARFE threshold  $\uparrow$  with plasma-wall clearance  $\uparrow$  at HFS

## Alternative Mechanism for MARFE Formation: instability of plasma recycling on inner wall



Charged particle losses to wall:

$$\Gamma_{\perp} = -D_{\perp} \nabla_{\perp} n \approx D_{\perp} \frac{n}{l_a} \propto D_{\perp} n^2$$

Energy losses with particles:

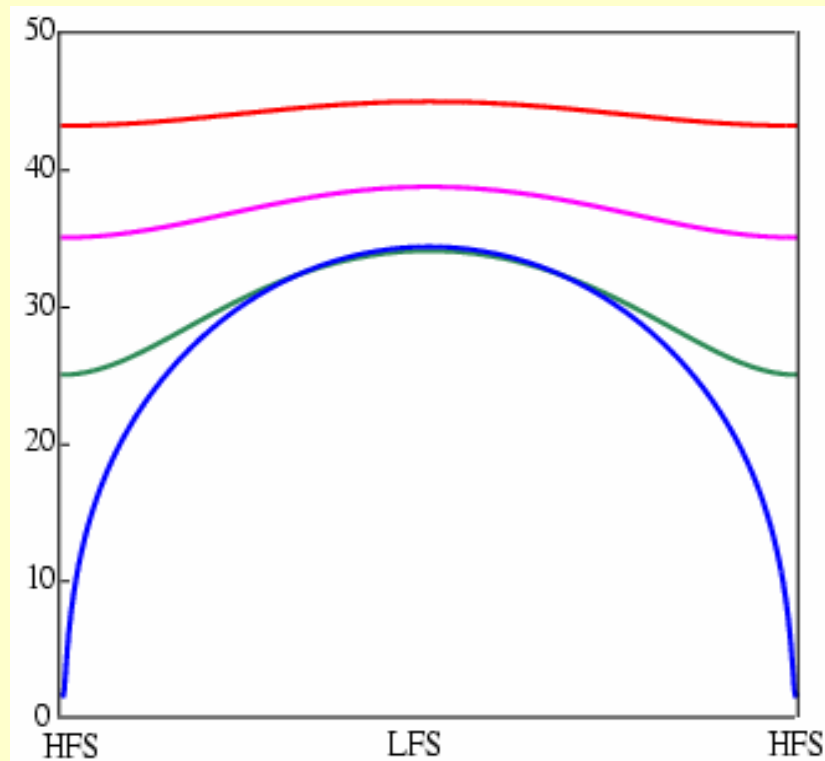
$$q_{conv/rec} = \Gamma_{\perp} (\alpha T + E_i) \approx \propto D_{\perp} n^2 (\alpha T + E_i)$$

Numerical modelling of MARFE onset in TEXTOR particle,  
momentum and heat transport equations are solved

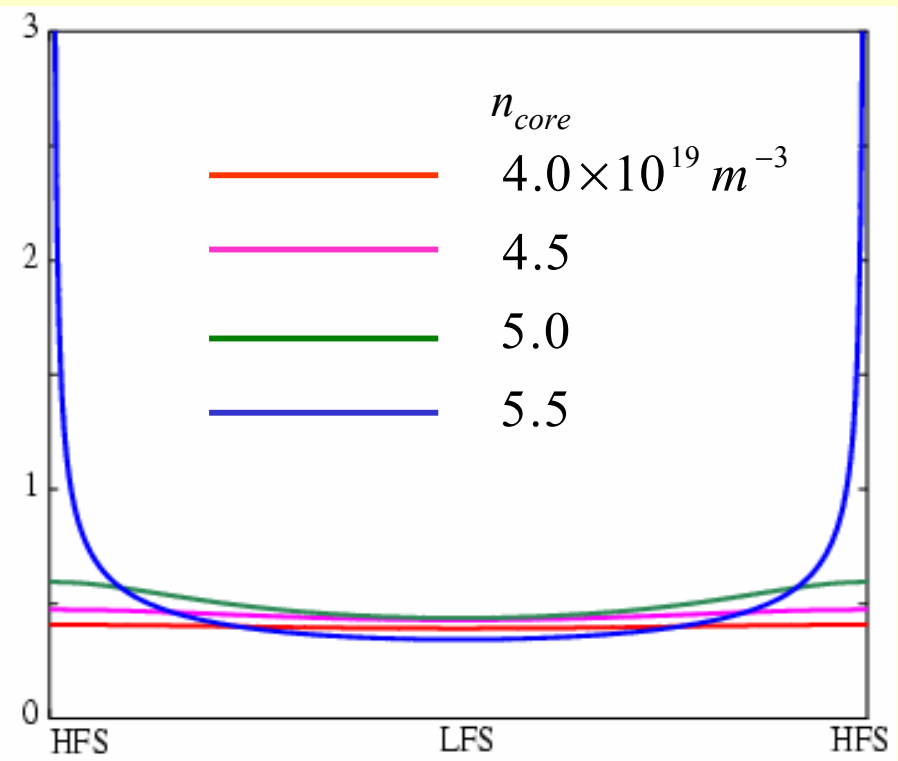
$$P_{heat}(\text{MW})=0.3(\text{OH})+1.3(\text{NBI}), \Lambda=0.8, D_{\perp}=1\text{m}^2/\text{s}, \kappa_{\perp}=3nD_{\perp}$$

Convective, recycling and radiation losses are included

Edge temperature (eV):



Edge density ( $10^{20} \text{ m}^{-3}$ ):



## Some preliminary conclusions:

### Behavior and role of impurity radiation

- Radiation of locally released impurities increases dramatically in MARFE
- MARFE threshold is influenced only weakly by impurity radiation
- MARFE is triggered mostly by “recycling” instability, radiation growth is a consequence

### Density limit with fixed transport coefficients: $D_{\perp} = 1 m^2/s$

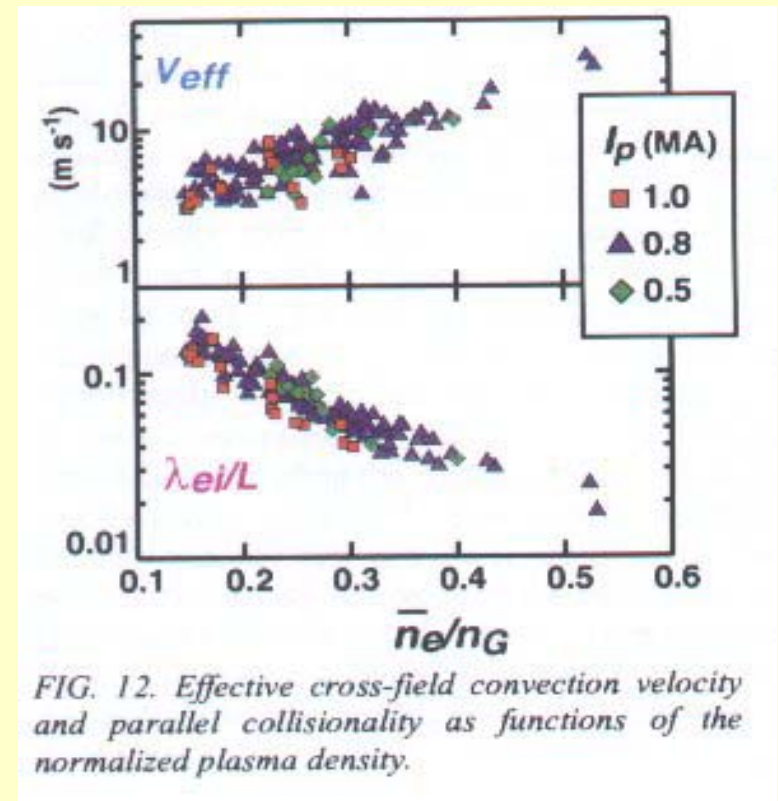
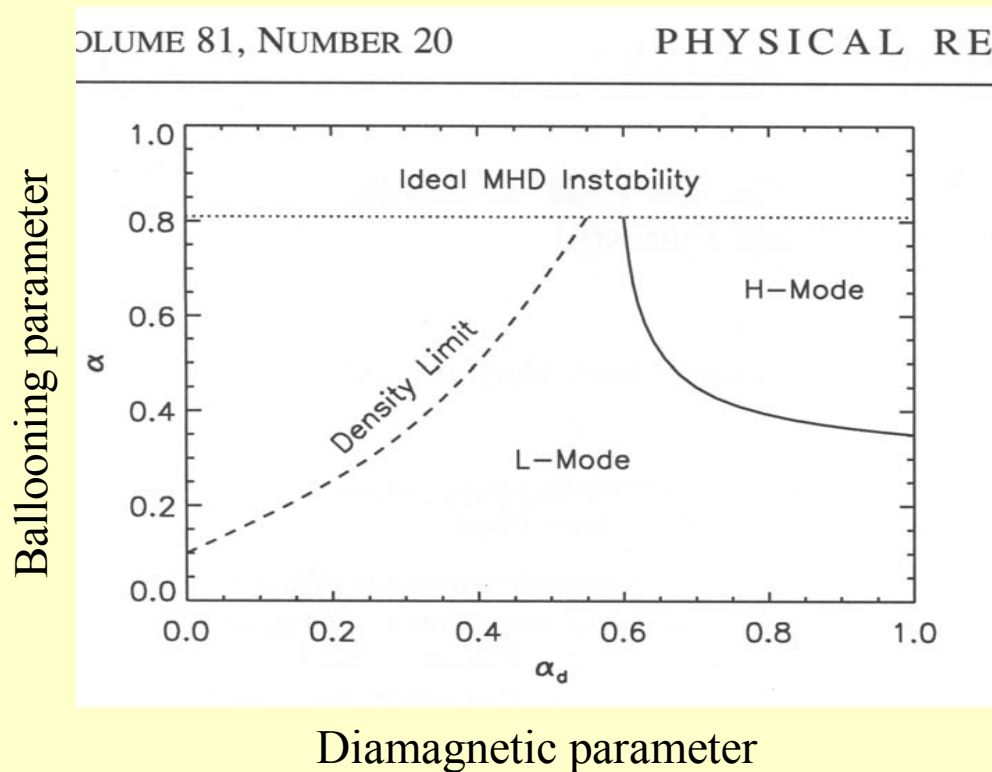
- For any level of heating and Shafranov shift, density limit is due to MARFE
- Simulations do not reproduce detachment at ohmic conditions with low heating and shift

# Role of anomalous transport nature

Change in the nature of edge turbulence can also lead to density limit

“Phase Space of Tokamak Edge Turbulence...”  
*B.N.Rogers et al.*, PRL 81(1998) 4396

“Overview of Recent Alcator C-Mod Research”, *E.S.Marmor et al*





# Model for edge anomalous transport

Linearized parallel Ohm's, Faraday's and Ampere's law, ion momentum balance, quasi-neutrality, ion continuity equation  $\Rightarrow$  Eigen function equation for electric potential perturbation of Mathieu's type:

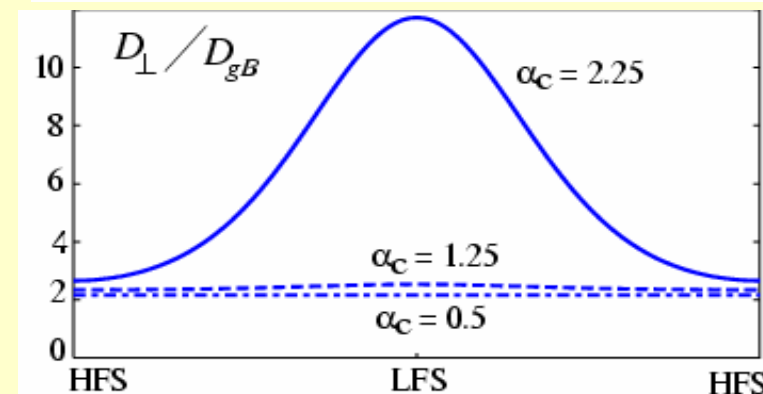
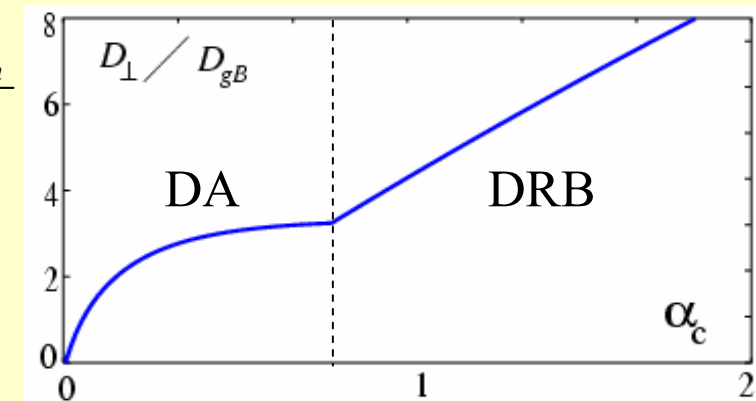
$$\frac{\partial^2 \tilde{\varphi}}{\partial \vartheta^2} + [A(\omega, k_{\perp}, \alpha, \alpha_c, \varepsilon_n) - 2Q(\omega, k_{\perp}, \alpha, \alpha_c, \varepsilon_n) \cos \vartheta] \tilde{\varphi} = 0$$

$$\alpha = q^2 R \left| \frac{d\beta}{dr} \right|, \alpha_c = \frac{2q^2 R}{\lambda_e} \sqrt{\frac{m_e}{m_i}} \propto \frac{1}{\alpha_d}, \varepsilon_n = \frac{2L_n}{R}$$

Importance of different modes:

Moderate collisionality,  $\alpha_c \leq 1$  drift-Alfven mode described by  $ce_2$  w/o localization on magnetic surface

High collisionality,  $\alpha_c \geq 1$ : drift-resistive ballooning mode described by  $ce_0$  with maximum on LFS

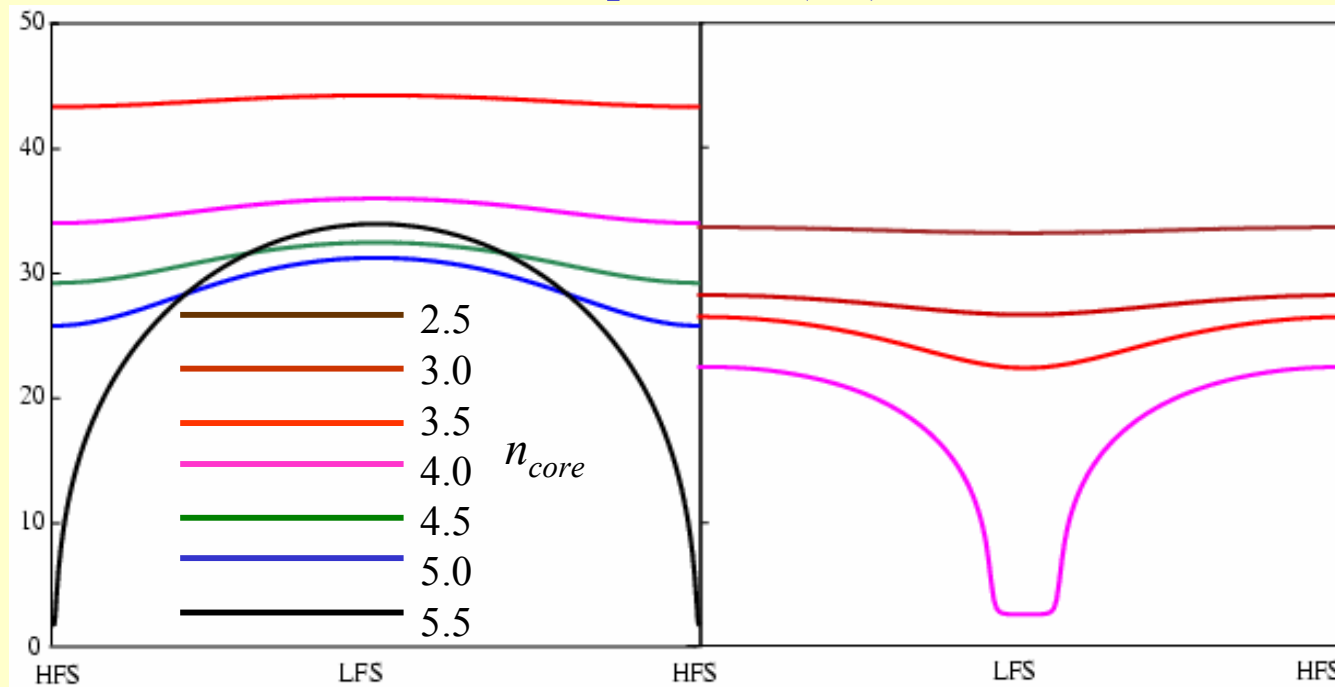


# Edge temperature poloidal profiles computed with theory-based transport model

NBI heated plasma with  $P_{heat} = 1.6 \text{ MW}$ ,  $\Lambda = 0.8$

Ohmic heated plasma with  $P_{heat} = 0.3 \text{ MW}$ ,  $\Lambda = 0.4$

Temperature (eV):



Recycling instability leads to MARFE at HFS

Transition to DRB-driven transport results in detachment at LFS

## What determines scenario of density limit?

**MARFE:** stimulated by  $\vartheta$ -variation of heat influx from the core due to Shafranov shift  $\Delta$ :

$$\propto 1 + 2|\Delta'| \cos \vartheta$$

**Detachment:** promoted by ballooning nature of anomalous transport losses:

$$\propto \exp\left(4\sqrt{\alpha_c} \cos \vartheta\right)$$

**MARFE develops if:** at the threshold shift asymmetry  $>$  ballooning asymmetry:

$$\frac{1 + 2\Delta'}{1 - 2\Delta'} > \exp\left(8\sqrt{\alpha_c}\right)$$

Impact of heating power on asymmetries:

$$W_{heat} \uparrow \Rightarrow \Delta' \uparrow \Rightarrow \frac{1 + 2\Delta'}{1 - 2\Delta'} \uparrow$$

$$\alpha_c \propto \frac{1}{\lambda_c} \propto \frac{n}{T^2} \downarrow \Rightarrow \exp\left(8\sqrt{\alpha_c}\right) \downarrow$$

Density limit scenario abruptly changes at a critical heating power

## Peculiarities of divertor geometry

### Differences:

- Recycling is localized in divertor
- Presence of X-points leads to new drift modes

### Similarities:

- Most favorite mechanism for MARFE (*Borrass, ...*): is due to recycling, but charged particles hit divertor plates  $\parallel \mathbf{B}$
- Transport  $\perp \mathbf{B}$  starts to play important role close to the density limit (*Xu et al.*: BOUT code)
- New drift modes are of DRB nature (*Xu et al.*: BOUT code)

A self-consistent picture does not exist yet

# Conclusion

Synergy of several mechanisms for DL have been analyzed:

- radiative instability
- recycling instability
- transition to ballooning anomalous transport

**MARFE at HFS:** result of **recycling instability** at **high heating power** when **Shafranov shift** dominates poloidal asymmetry

**Detachment at LFS:** develops at **lower heating power** because of transition to **anomalous transport due to DRB-modes**

# Plans

Present model is very approximate in many respects

Further development is needed in all directions

**include divertor geometry**

First: