

Synthesis of full MHD simulation results of neoclassical tearing modes in ITER geometry

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Outline

- XTOR and theory
- NTM: nonlinear thresholds
- NTM: saturation
- NTM: toroidal interaction

XTOR equations:

$$\rho \frac{D\vec{v}}{Dt} = \vec{J} \times \vec{B} - \nabla p + \nabla v \nabla \vec{v}$$

$$\partial_t \vec{B} = \nabla \times (\vec{v} \times \vec{B}) - \nabla \times \eta (\vec{J} - \vec{J}_{boot})$$

$$\partial_t T = -\vec{v} \cdot \nabla T - (\Gamma - 1) T \nabla \vec{v} + \nabla \chi_{\perp} \nabla T + \vec{B} \cdot \nabla \chi_{\parallel} \frac{\vec{B} \cdot \nabla T}{B^2} + H$$

$$\partial_t \rho = -\vec{v} \cdot \nabla \rho - \rho \nabla \vec{v} + \nabla D_{\perp} \nabla \rho + Q$$

$$H = -\nabla \chi_{\perp} \nabla T_{equil}; \quad \eta_{equil} (J_{\phi} - J_{\phi,boot})_{equil} = const.$$

Full toroidal geometry.

$$\text{Mapping:} \quad \eta_{equil}(r); \quad T_{equil}(r) \xrightarrow[\substack{\text{Spitzer,} \\ p_edge}]{\quad} \eta_{equil}(T_{equil}) \xrightarrow[t \neq 0]{\quad} \eta(T(t))$$

$$\text{Bootstrap:} \quad \vec{J}_{boot}(t) = f_{bs} \left\| \vec{J}_{boot,equil} \right\| \cdot \nabla_r p(t) / p'_{equil} \vec{B}(t) / \left\| \vec{B}(t) \right\|$$

Nonlinear theory

- Generalized Rutherford equation

$$1.22 \quad \frac{\tau_r}{dt} \frac{dw}{dt} = \Delta'(w) + \Delta'_{GGJ}(w) + \Delta'_{boot}(w) \quad (+ \textit{non MHD})$$

(Rutherford (1973), White(1977), Thyagaraja (1981)

Militello et al., Escande et al., Hastie et al. (2004),

with Kotschenreuter (1985), Lütjens & al.(2001), Fitzpatrick (1995))

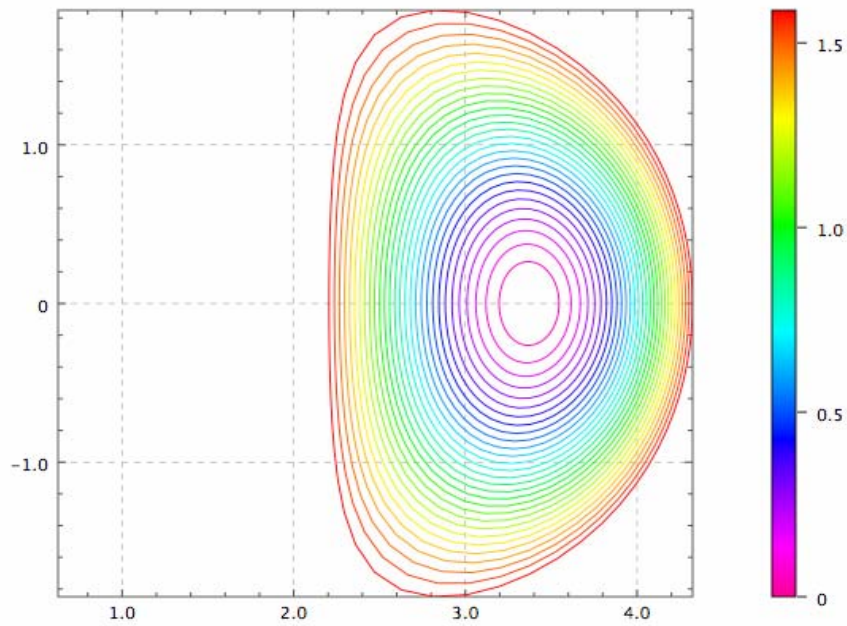
$$\Delta'_{GGJ} = 6.35 \frac{D_R}{\sqrt{w^2 + 0.65w_c^2}} \quad (\textit{curvature})$$

and

$$\Delta'_{boot} = 6.35 \frac{R_o q}{B_o s_s} J_{boot,o} \frac{w}{w^2 + (1.8w_c)^2} \quad (\textit{bootstrap})$$

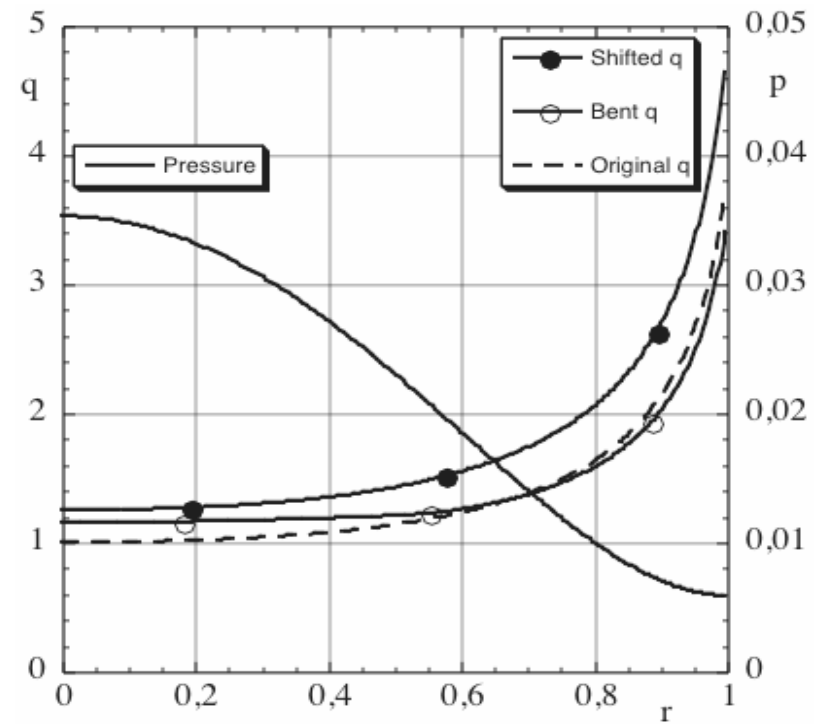
$$w_c = 2\sqrt{2} \left(\frac{\chi_{\perp}}{\chi_{\parallel}} \right)^{1/4} \sqrt{\frac{r_s R}{n s_s}}; \quad s_s = \frac{r_s q'}{q}$$

Equilibrium (CHEASE):

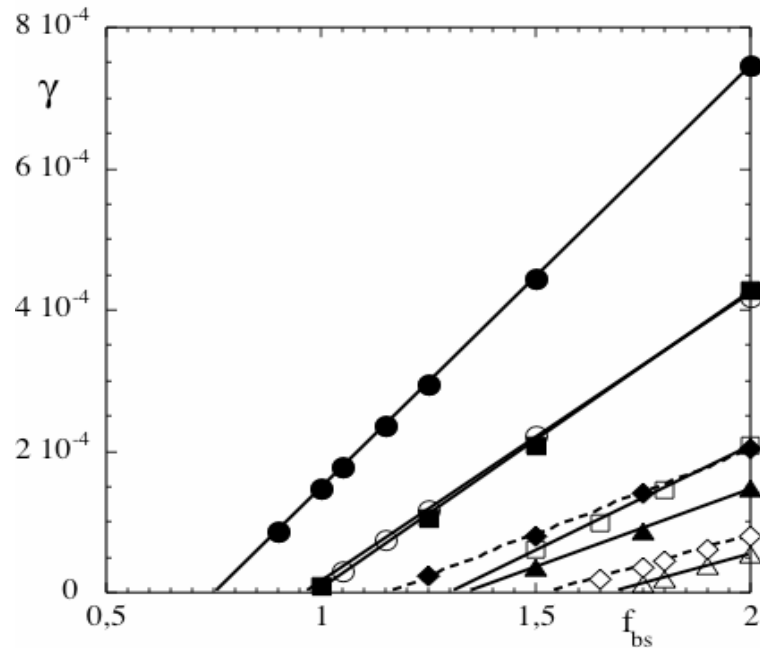


ITER:

$A=3; \kappa=1.75; \delta=0.4$



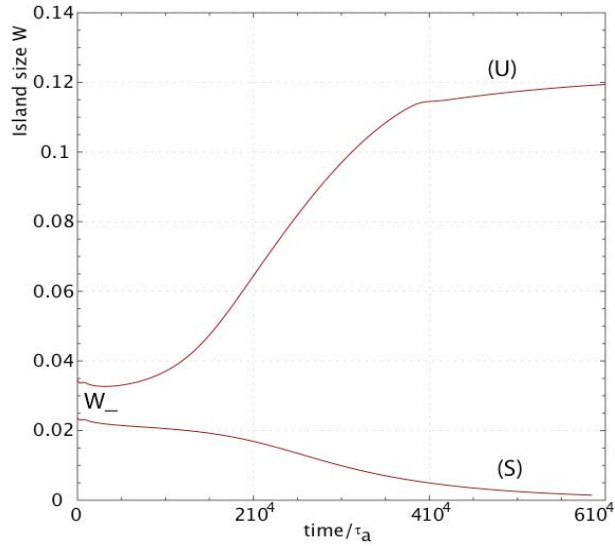
NTM: linear stability thresholds



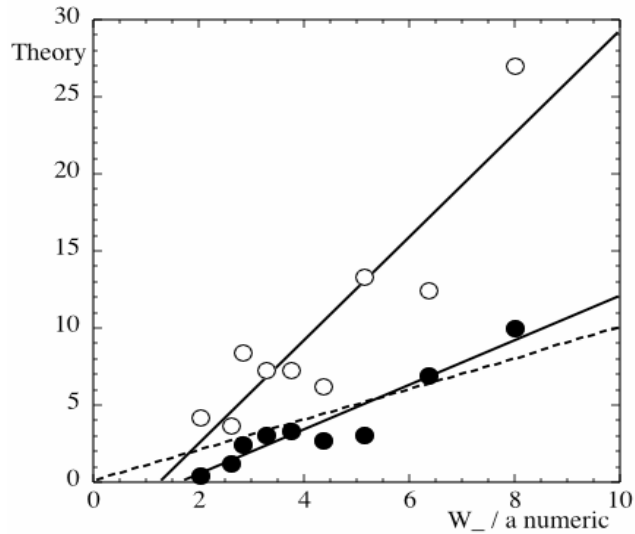
- $S=10^7$
- Open: $\chi_{//} / \chi_{\perp} = 10^8$
- Closed: $\chi_{//} / \chi_{\perp} = 6.25 \cdot 10^6$
- ITER: m/n=4/3 (circles)
 m/n=3/2 (squares)
 m/n=2/1 (triangles)
- TS: m/n=2/1 (diamonds)

- Threshold with given geometry and $\chi_{//} / \chi_{\perp}$ depends on S.
- For ITER, $S > 10^{10}$ ----> threshold at $f_{bs} \gg 2$

NTM: nonlinear stability thresholds



- NTM dynamics ($m=4/n=3$) about its nonlinear threshold (ITER)



- Thresholds: numerics (XTOR) vs. Theory
- Closed symbols: with linear correction i.e

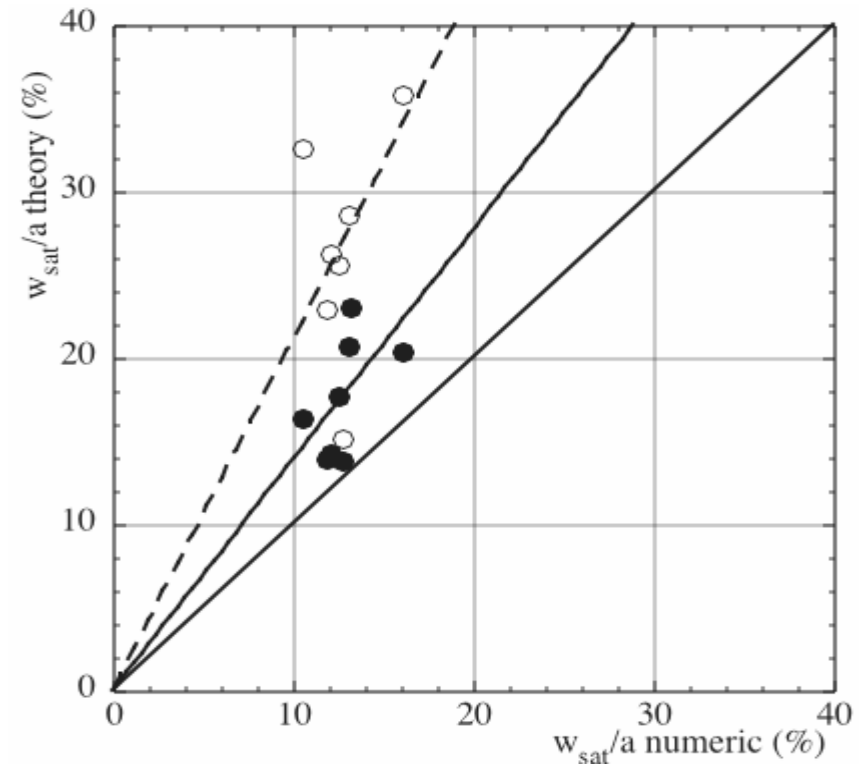
$$\cdot \frac{\tau_r}{1.22} \frac{dw}{dt} = \Delta'_{eff} \frac{w}{w + w_{lin}} + \Delta'_{boot}; \quad \Delta'_{eff} = \Delta' + \sqrt{2} \pi^{\frac{3}{2}} \frac{D_R}{W_c}$$

- Open symbols: without linear corrections

NTM: saturation

- Comparison of NTM saturation levels in ITER geometry with leading edge theory:

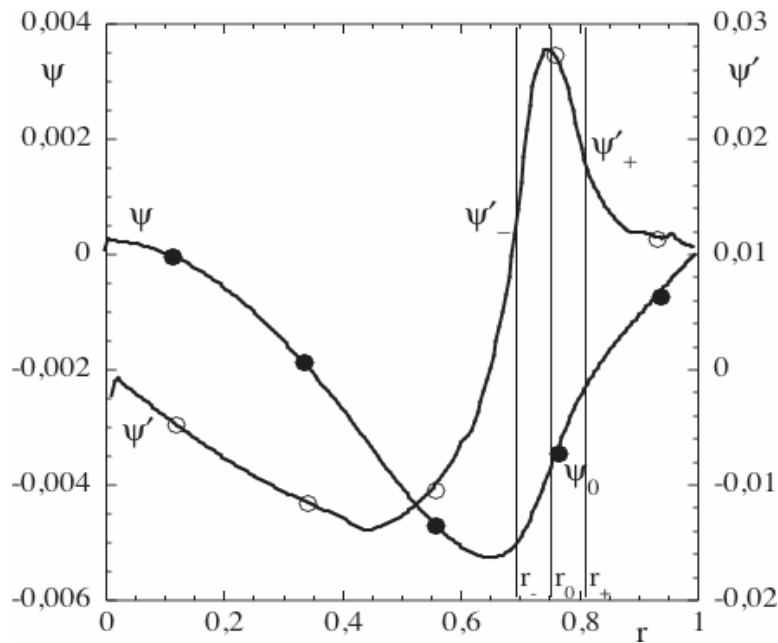
XTOR gives much smaller saturation sizes than predicted with Rutherford



Validity field of Rutherford vs. Numerical XTOR results:

- Rutherford ---> Boundary layer approximation
 ---> w and Δ' are small

- XTOR saturation: $\frac{m}{r_s} w \approx 1$; $\frac{\psi'}{\psi} w \approx 1$



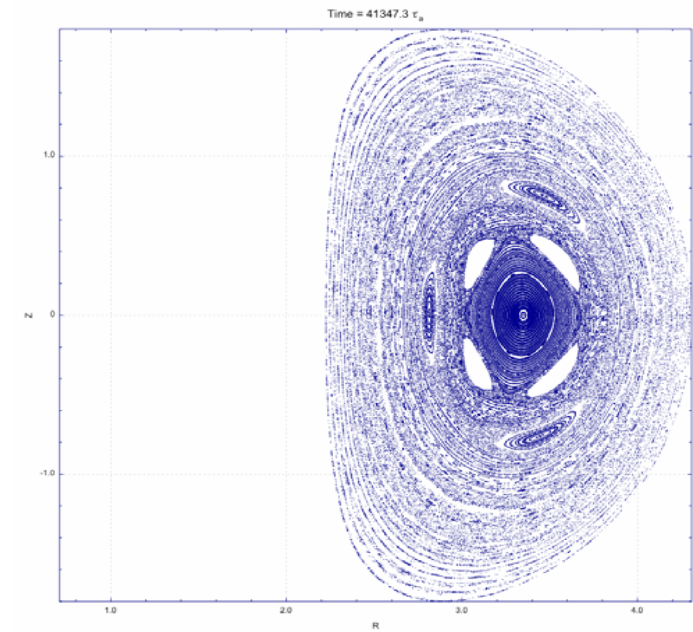
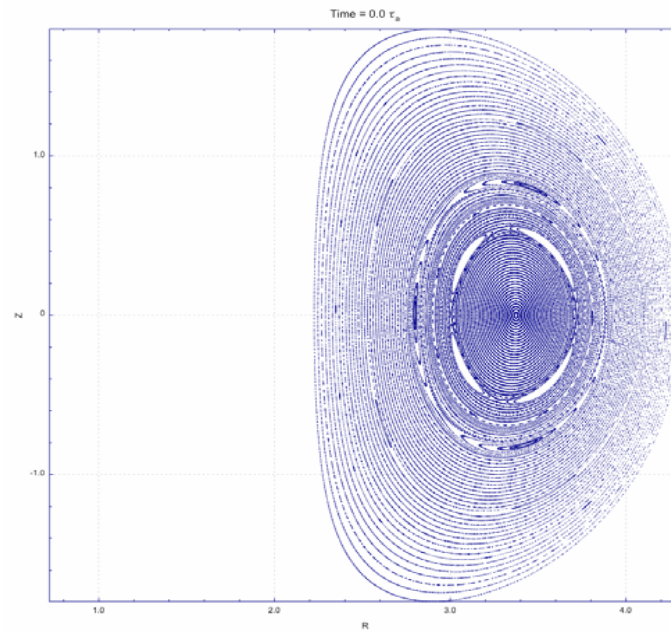
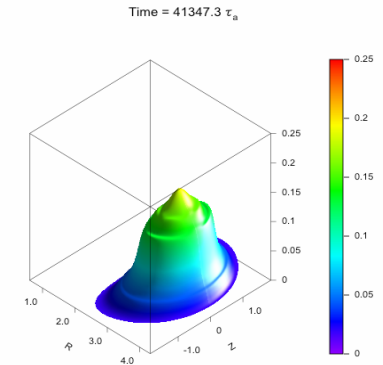
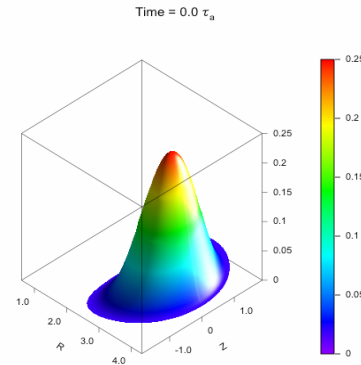
- Theory derived with constant Ψ approx. Shape of $\Psi(r)$
- XTOR does not satisfy these assumption.

NTM: toroidal interactions

Equilibrium bootstrap: (~20%)

Example:

Growth of 2 NTM's
 $m/n=4/3$ et $3/2$



- NTM's with $m/n=2/1,3/2,4/3$
- Single, double or triple mode simulations
- Initial perturbation $W_{\bar{}}$ or W_{sat} .
- $S=10^7$ and $\chi_{//}/\chi_{\perp} = 10^8$
- Iter geometry

Observations:

- Within the framework of the XTOR model, and the Simulations times (about $60000 \tau_a$), no toroidal coupling was observed. No interaction as measured in experiments
- In multiple mode simulations, island overlap cause large stochastic zones, which empty the central pressure.

Conclusions

- Full numerical simulations show a reasonable agreement with generalized Rutherford's equation in the small island regime. Acceptable results are obtained for nonlinear NTM thresholds.
- In the NTM saturation regime, simulation results and theory disagree. XTOR results give much smaller saturation sizes than theory.
- We have not observed toroidal mode coupling effects in multiple NTM runs.