



Kinetic simulations of the NTM polarisation current

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2nd IAEA Technical Meeting on the Theory of Plasma Instabilities



Motivations

• Reliable description of NTMs necessary in order to determine onset conditions and stabilisation requirements (\rightarrow ITER)

• Problem at the meeting point of MHD and kinetic theory (\rightarrow required for accurate predictions, e.g. NTM polarisation current)

Outline

- Polarisation current in the presence of a magnetic island
- Solving the drift kinetic equation
- Single-particle motion and full 3D simulations: new conditions for island stability

The Neoclassical Tearing Mode



• Island evolution connected with the parallel currents flowing near the resonant surface

$$\frac{\mathrm{d}W}{\mathrm{d}t} = c_1 \Delta' + \frac{c_2}{W} \int_{-1}^{\infty} \mathrm{d}\Omega \oint \frac{\mathrm{d}\xi \cos\xi}{\sqrt{\cos\xi + \Omega}} j_{||}^{n.i.}$$

New flux coordinates: helical flux $\Omega \equiv 2(\psi - \psi_s)^2 / W_{\psi}^2 - \cos \xi$ helical angle $\xi \equiv m\theta - n\zeta$



The Neoclassical Tearing Mode





The island polarisation current



Island motion with respect to the plasma
⇒ electric field induced (Faraday)

• $E \times B$ motion in the island rest frame: plasma acceleration and deceleration around the *O*-point

 Variation of plasma inertia balanced by a Lorentz force provided by

 $j_{\rm pol}^{\rm class} = \frac{en}{\omega_c} \frac{{\rm d}v_E}{{\rm d}t}$

Polarisation current

(⇒ mainly carried by the ions) [Smolyakov, PPCF 1993]

• Current continuity (∇·J=0) ensured by an electron parallel current contributing to the Rutherford equation



Solving the drift kinetic equation



• Analytical determination of $j_{\parallel}^{n.i.}$ from the drift kinetic equation possible employing the expansion parameters W/r, $W_b/W \ll 1$ (and further simplifications...)

• Drift kinetic equation in toroidal geometry with an island structure to be solved $\frac{\mathrm{d}f}{\mathrm{d}t} = \frac{\partial f}{\partial t} + \left(v_{||} \hat{\mathbf{b}} + \mathbf{v}_{d} + \mathbf{v}_{E} \right) \cdot \frac{\partial f}{\partial \mathbf{r}} - \frac{e}{m} \frac{\mathbf{v}_{d} \cdot \nabla \Phi}{v} \frac{\partial f}{\partial v} = C(f)$ parallel motion magnetic & electric drift electric field collisions

• Representation of the distribution function: $f = f_0 + \delta f = f_M(\psi, \mathcal{E}) + \delta f$ if $\delta f \ll f_0$: reduction of the numerical noise

• The equation for
$$\delta f$$
 is $\frac{\mathrm{d}(\delta f)}{\mathrm{d}t} = C(\delta f) - \mathbf{v}_d \cdot \nabla f_M - \frac{ef_M}{T} \mathbf{v}_d \cdot \nabla \Phi$

Solution: • $\delta f \rightarrow$ markers (ions) \rightarrow Hamiltonian equations of motion in Boozer coordinates (\rightarrow HAGIS) [Pinches et al., CPC 1998]

• Collisions: Monte Carlo procedure [Bergmann et al., PoP 2001]

Current profiles from the drift kinetic equation





• Binning in velocity space also possible

the distribution function

Flux surface averages → cells

$$\langle A \rangle = \lim_{\delta\Omega \to 0} \frac{\int A \mathrm{d}^3 \mathbf{r}}{\int \mathrm{d}^3 \mathbf{r}} \Rightarrow \frac{1}{n} \left\langle \int A \delta f \, \mathrm{d}^3 \mathbf{v} \right\rangle \simeq \frac{\int_{\Omega - \delta\Omega}^{\Omega + \delta\Omega} A \delta f \, \mathrm{d}^3 \mathbf{r} \mathrm{d}^3 \mathbf{v}}{\int_{\Omega - \delta\Omega}^{\Omega + \delta\Omega} f_0 \, \mathrm{d}^3 \mathbf{r} \mathrm{d}^3 \mathbf{v}}$$

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Stabilising or destabilising?





Numerical results ("standard" polarisation current) in agreement with the current understanding (flat pressure): polarisation current
stabilising if the separatrix is excluded from the radial integration
destabilising if it is included in the radial integration
[Waelbroeck and Fitzpatrick, PRL 1997]

Perpendicular current vs. island rotation frequency

 \bullet Scan over ω important because of theoretical and experimental uncertainties about its actual value

IJЪ



Perpendicular current vs. ω : low frequencies





Perpendicular current vs. ω : low frequencies



• Toroidal precession compensated by the $E \times B$ drift (island frame) when $2\omega_{tp} \approx \omega$

• Different sign of the current for particles drifting slower or faster than the island

IDD

• Motion dominated by the radial component of the $E \times B$ velocity

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Perpendicular current vs. ω : transition to higher frequencies



Transition to higher frequencies
→ toroidal precession less and less important

• Bounce motion along the perturbed surfaces \rightarrow polarisation current sets on

IPP

Perpendicular current vs. ω : transition to higher frequencies



Transition to higher frequencies
→ toroidal precession less and less important



Ibb

• Bounce motion along the perturbed surfaces \rightarrow polarisation current sets on (cf. fluid picture)

Perpendicular current vs. ω : the ''standard'' polarisation current



• High frequencies: polarisation current close to "fluid" behaviour \rightarrow quadratic dependence on ω found

 \bullet Superposition of island motion and bounce motion \rightarrow current reduction due to slower particles

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Polarisation current vs. island width



• Simulation parameters: (3,2) mode, R = 8 m, $B_0 = 2 \text{ T}$, $n_i = 10^{20} \text{ m}^{-3}$, $T_i = 5 \text{ keV}$, flat temperature and density profiles

• Local effects "smeared out" by trapped particles overlapping the island



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• Sign of the polarisation current influenced by competition between electric and magnetic drift

 Polarisation current strongly reduced for small island widths (comparable to banana width)

Conclusions

- Kinetic effects are essential to capture the whole dynamics of the NTM
- Our present model needs to be extended to include self-consistent electron response