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## *Basic Photochemistry of the Middle Atmosphere*

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These lecture notes are intended only for distribution to participants

# Photochemistry of the Middle Atmosphere

Wednesday, May 17, 2006

8:30-10:30

Dan Marsh

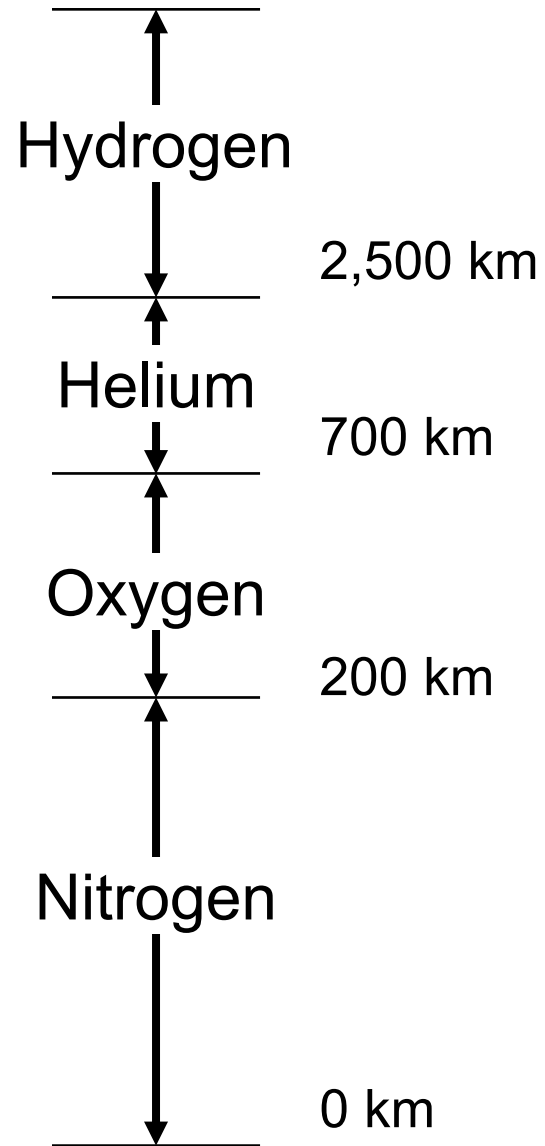
National Center for Atmospheric Research,  
Boulder, USA

# Overview

- Composition
  - Primary constituents
  - Continuity equation
  - Minor constituents - ozone, HO<sub>x</sub>, NO<sub>x</sub>
  - Catalytic cycles
- Energetics
  - Thermal structure
  - Energy deposition
  - Heating and cooling

# Composition

# Primary constituent



# Total density height variation

$$p = nkT \quad \text{Ideal gas law}$$

$$\Delta p = -\rho g \Delta z \quad \text{Hydrostatic balance}$$

$$\frac{\Delta p}{p} = -\frac{\rho}{n} \frac{g}{kT} \Delta z = -\frac{1}{H} \Delta z \quad \text{where } H = \frac{kT}{mg}$$

$$p(z) = p_0 \exp \left( -\int_0^z \frac{dz}{H} \right)$$

$$n(z) = n_0 \frac{T_0}{T} \exp \left( -\int_0^z \frac{dz}{H} \right)$$

Which leads to:

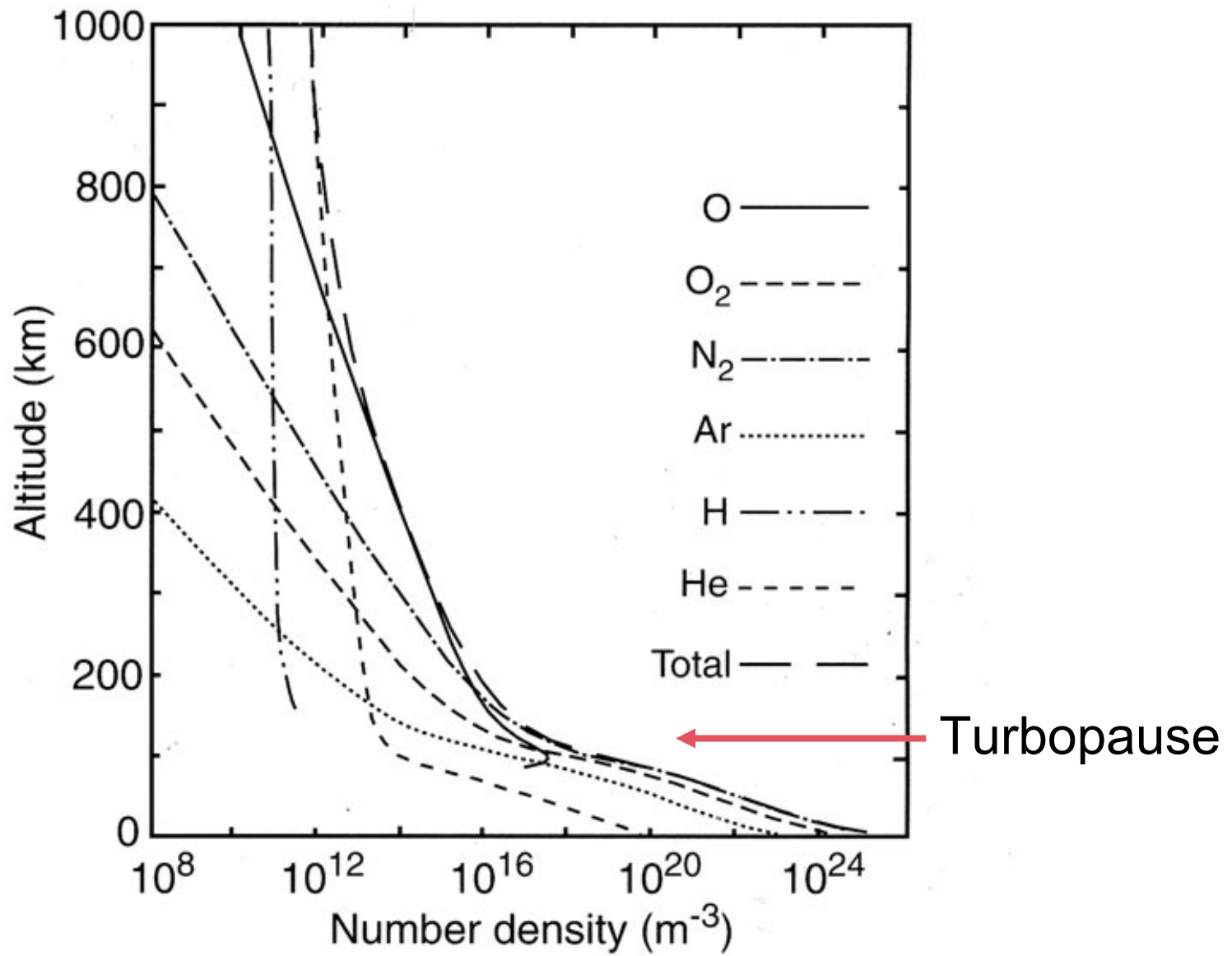
$$\frac{\partial n}{\partial z} = - \left( \frac{1}{T} \frac{\partial T}{\partial z} + \frac{1}{H} \right) n$$

In the “homosphere,” where eddy diffusion tends to mix the atmosphere, the mean molecular weight is almost constant ( $m \sim 28.96$  amu), and the density will decrease with a mean scale height of  $\sim 7$ km.

Above about 90km, constituents tend to diffuse with their own scale height ( $H_i = kT/m_i g$ ) as the mean free path becomes longer. This is the “heterosphere.” The  $i$ th constituent (assuming no significant sources or sinks) will have the following gradient:

$$\frac{\partial n_i}{\partial z} = - \left( \frac{1}{T} \frac{\partial T}{\partial z} + \frac{1}{H_i} \right) n_i$$

Constituents with low mass will fall off less rapidly with height, leading to diffusive separation.



From Richmond [1983]



## To recap...

- Above the turbopause (~105km), molecular diffusion causes constituents to drop off according to their mass.
- Below, the atmosphere is fully mixed:
- 78%N<sub>2</sub>, 21%O<sub>2</sub>, <1% Ar, <0.1% CO<sub>2</sub>
- Density decreases with a mean scale height:  
 $H = kT/mg \sim 7\text{km}$
- The lower thermosphere is also the transition from a molecular to atomic atmosphere.

# What about chemistry?

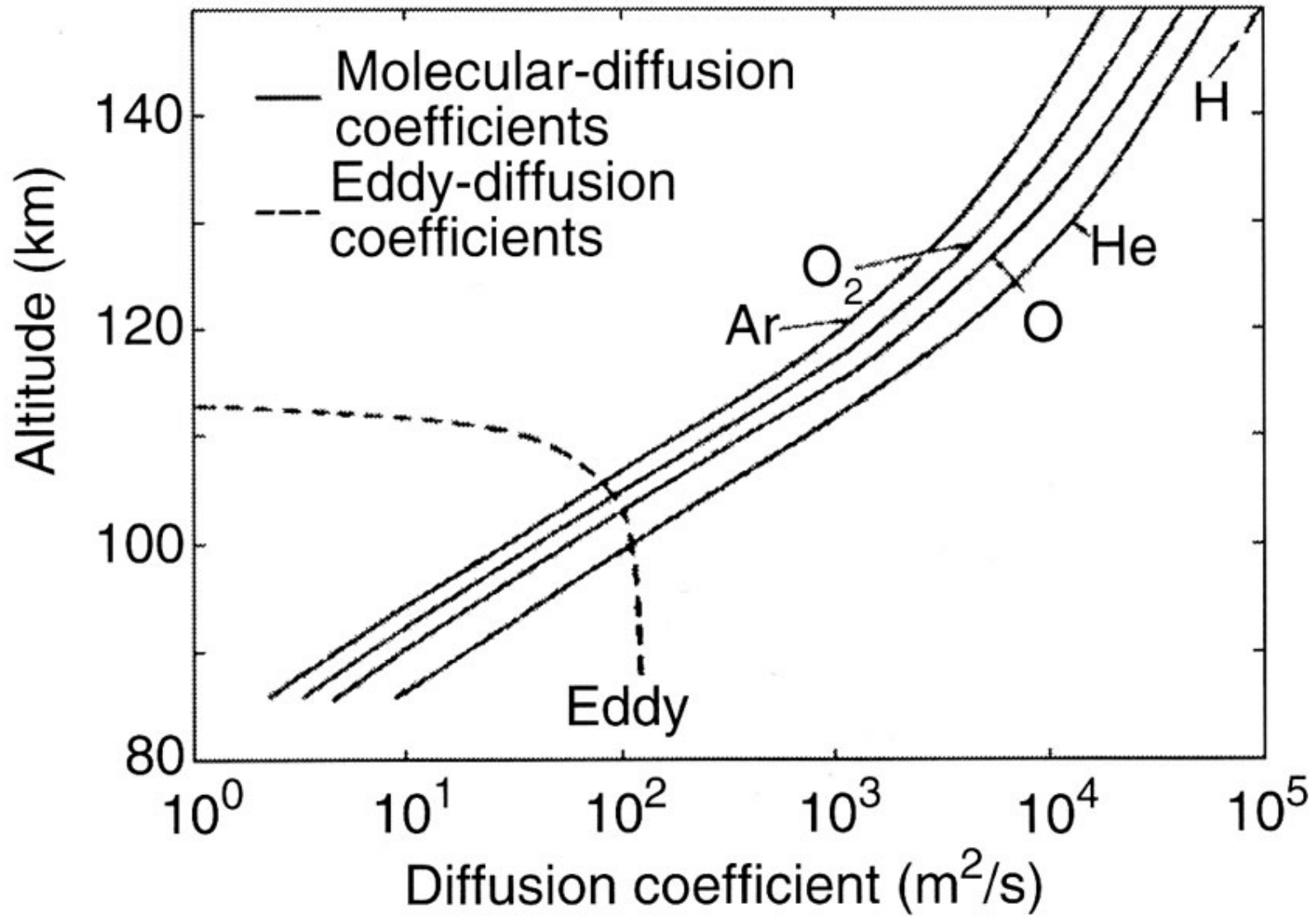
Recall: 
$$\frac{\partial n_i}{\partial z} = - \left( \frac{1}{T} \frac{\partial T}{\partial z} + \frac{1}{H_i} \right) n_i$$

If there's chemical production or loss of a minor constituent then this equality will not hold and a diffusive flux occurs. The flux is proportional to the amount of the inequality. Above the turbopause this will be:

$$\phi_i = w_d n_i = -D_i \left( \frac{\partial n_i}{\partial z} + \left( (1 + \alpha_T) \frac{1}{T} \frac{\partial T}{\partial z} + \frac{1}{H_i} \right) n_i \right)$$

Where  $D_i$  is the diffusion coefficient:

$$D_i = \frac{3}{8n\sigma_i^2} \left\{ \frac{kT(m + m_i)}{2\pi m m_i} \right\}^{1/2}$$



From Richmond [1983]

# Continuity equation

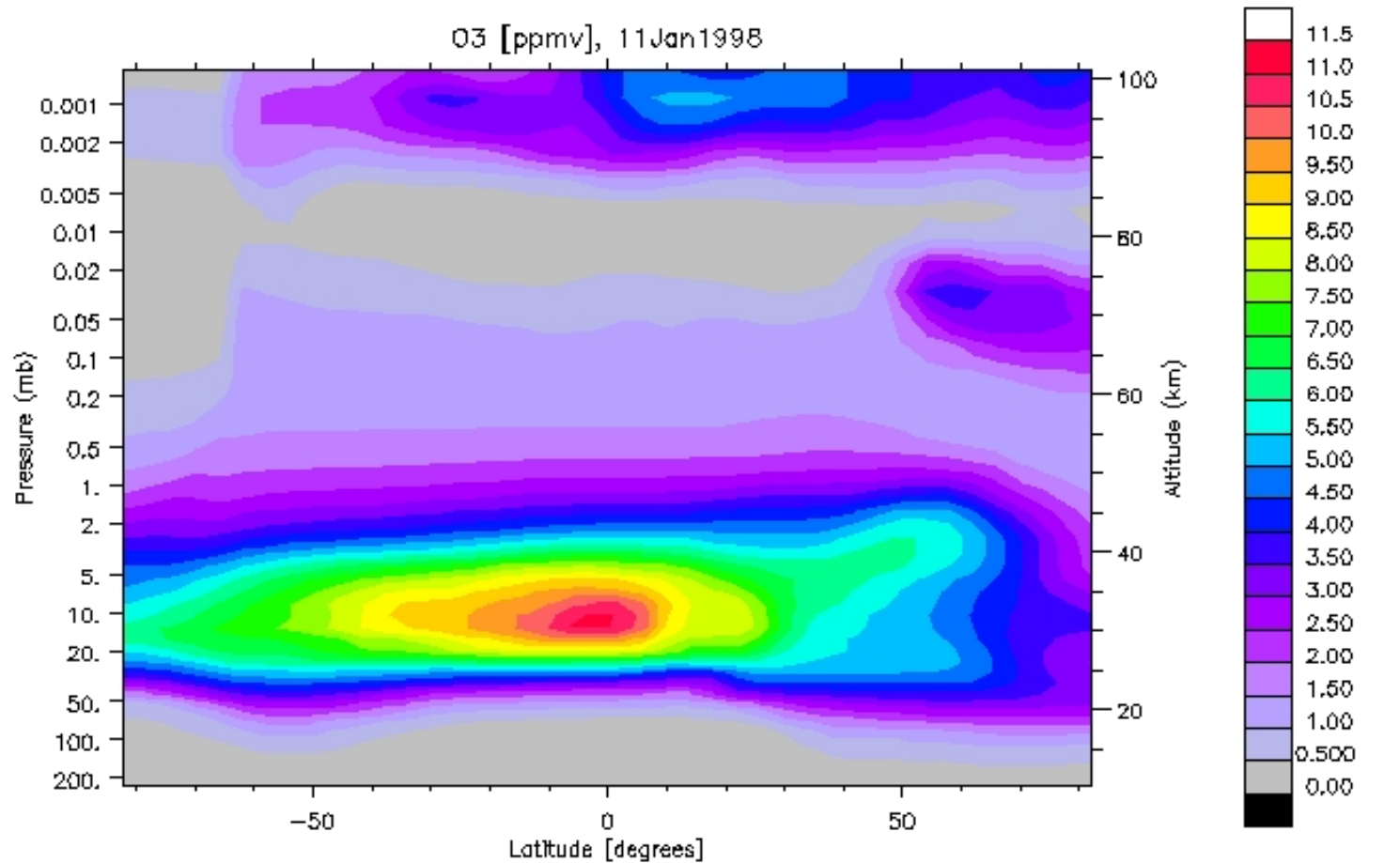
The total diffusive flux will include both molecular and eddy diffusion terms:

$$\phi_i = -K \left\{ \frac{\partial n_i}{\partial z} + \left( \frac{1}{T} \frac{\partial T}{\partial z} + \frac{1}{\bar{H}} \right) n_i \right\} - D_i \left\{ \frac{\partial n_i}{\partial z} + \left( (1 + \alpha_T) \frac{1}{T} \frac{\partial T}{\partial z} + \frac{1}{H_i} \right) n_i \right\}$$

So, neglecting resolved transport, we now have a continuity equation for the  $i$ th minor constituent:

$$\frac{\partial n_i}{\partial t} = P_i - L_i n_i - \frac{\partial \phi_i}{\partial z}$$

# The distribution of ozone



/data2/marsh/wa3\_v1.5\_smax/h2/wa3\_v1.5\_smax.com2.h2.1997-12-02-0000.nc

marsh 02.06.2005 10:29

Zonal mean volume mixing ratio for January

# Chapman chemistry (Pure oxygen system)

	O	O <sub>3</sub>
J <sub>2</sub> : $O_2 + h\nu \rightarrow O + O$	P	-
k <sub>2</sub> : $O + O_2 + M \rightarrow O_3 + M$	L	P
J <sub>3</sub> : $O_3 + h\nu \rightarrow O_2 + O$	P	L
k <sub>1</sub> : $O + O + M \rightarrow O_2 + M$	L	-
k <sub>3</sub> : $O + O_3 \rightarrow 2O_2$	L	L

Chapman, 1930

J<sub>i</sub>: photolysis rate

k<sub>i</sub>: bimolecular/termolecular rxn rate

# Continuity equation for O, O<sub>3</sub>

$$\begin{aligned}\frac{\partial(O)}{\partial t} &= J_3(O_3) + 2J_2(O_2) \\ &\quad - k_3(O)(O_3) - k_2(M)(O_2)(O) - 2k_1(M)(O)^2\end{aligned}$$

$$\frac{\partial(O_3)}{\partial t} = k_2(M)(O_2)(O) - J_3(O_3) - k_3(O)(O_3)$$

Define Ox = { O, O<sub>3</sub> } “odd-oxygen”

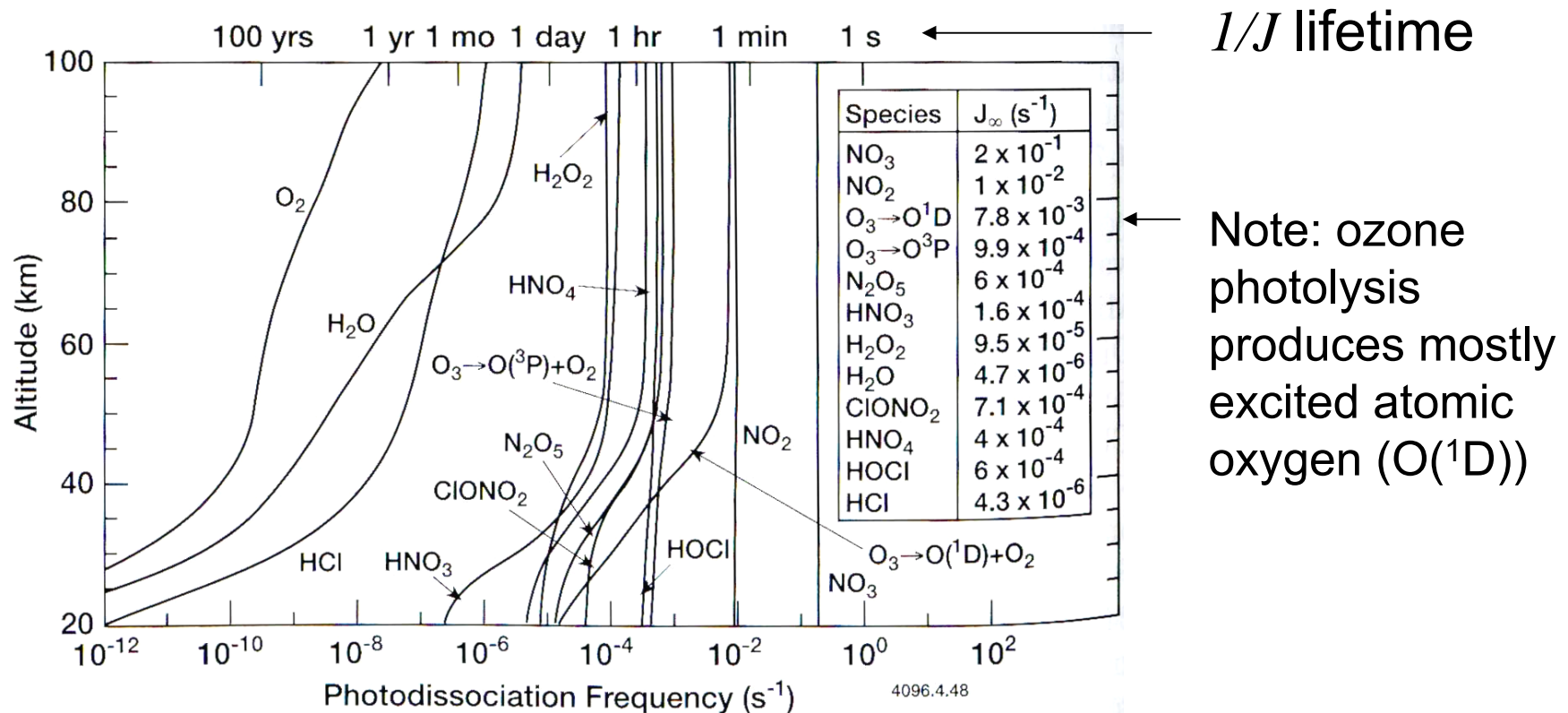
$$\frac{\partial(Ox)}{\partial t} = 2J_2(O_2) - 2k_3(O)(O_3) - 2k_1(M)(O)^2$$

# Calculation of photolysis rates ( $J$ )

$$J_A(\lambda, z, \chi) = \int \epsilon_A(\lambda) \sigma_A(\lambda) q(\lambda, z, \chi) d\lambda$$

'Transmission' factors

e.g.  $J_{O_2}(\lambda, z, \chi) = \int \sigma_{O_2}(\lambda) q_{\infty}(\lambda) T_{O_2}(\lambda, z, \chi) T_{O_3}(\lambda, z, \chi) d\lambda$

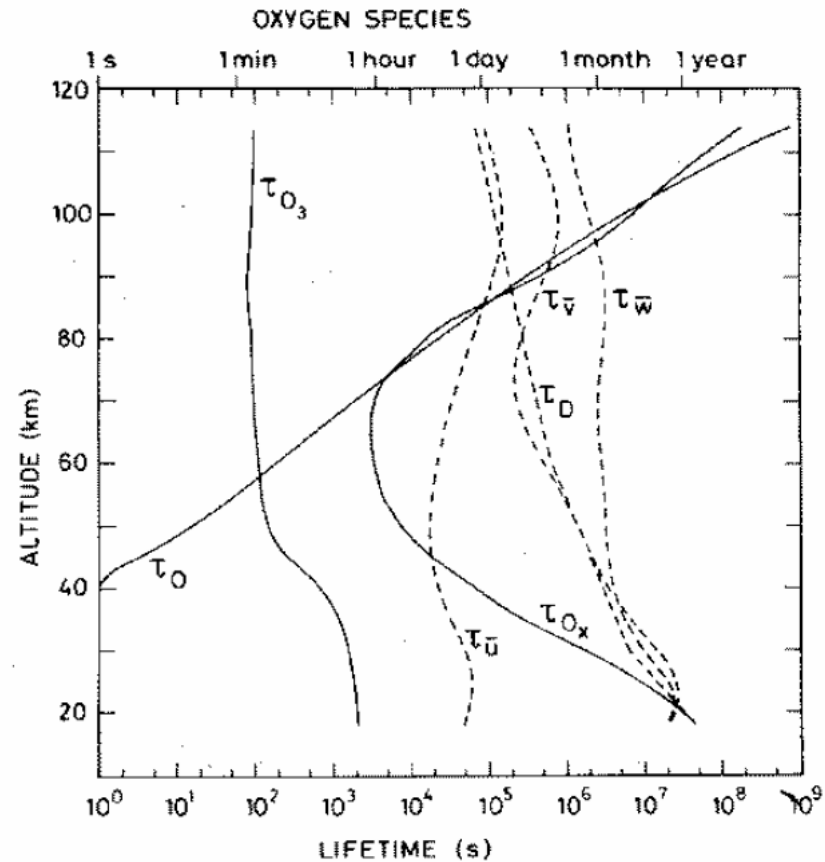




# Photochemical lifetimes

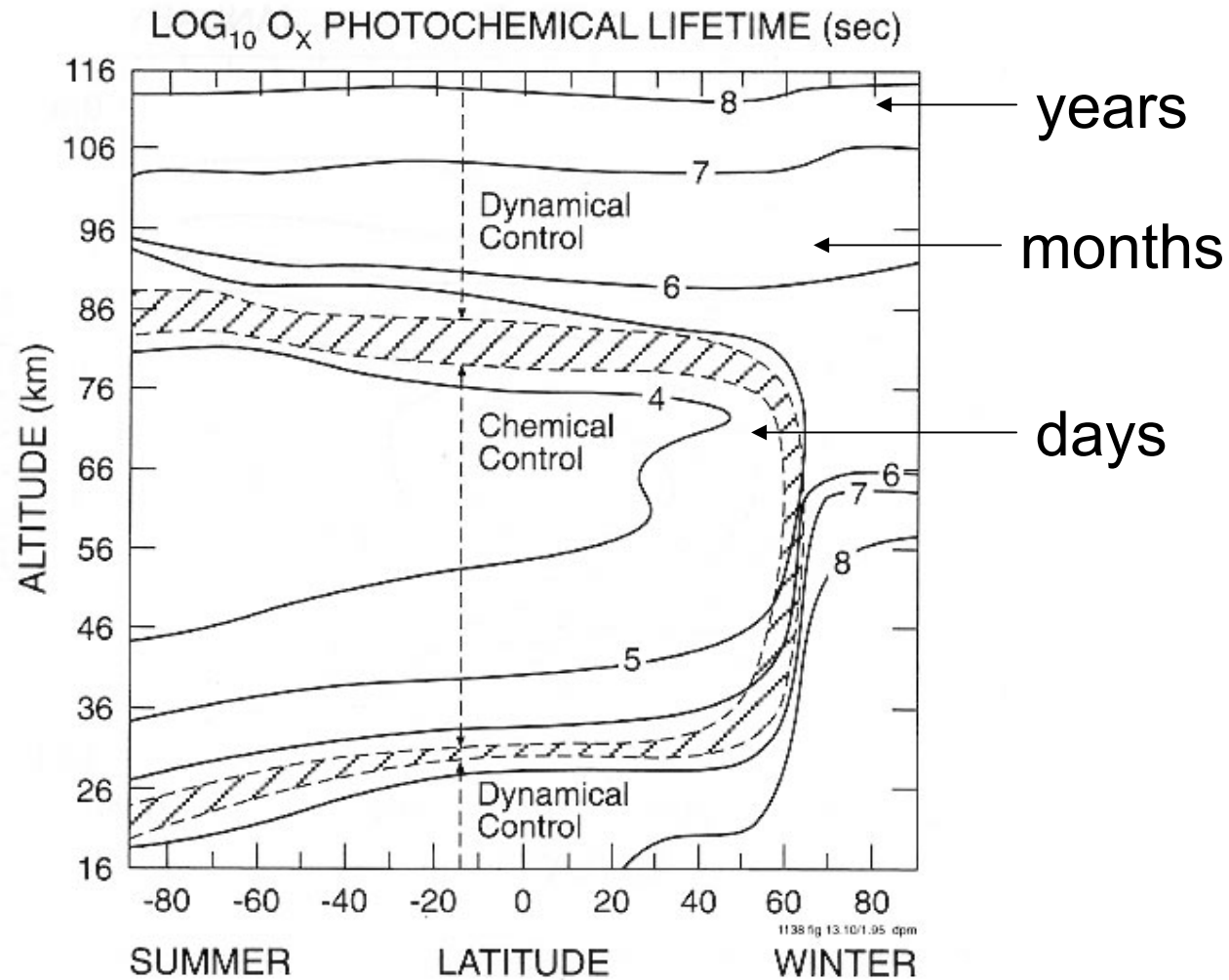
$$\tau = \frac{n_i}{L_i} \quad \tau_{O_3} = \frac{(O_3)}{J_3(O_3) - k_3(O)(O_3)} = \{J_3 - k_3(O)\}^{-1}$$

Q: why is the lifetime for atomic oxygen so long in the thermosphere?



Brasseur & Solomon, 2006

# Chemical/dynamical control



# Ox Partitioning

Below ~80km  $\tau_O$  is small and we can assume  $dO/dt \sim 0$  and that oxygen is in *photochemical equilibrium*. So equating P to L:

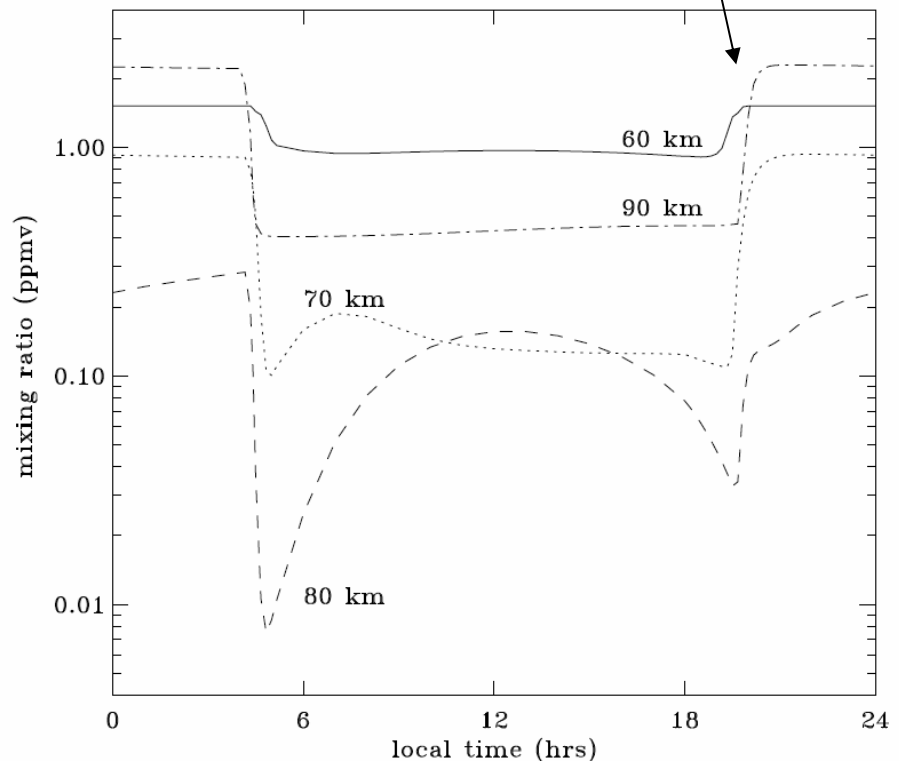
$$(O) \approx \frac{J_3(O_3) + 2J_2(O_2)}{k_2(M)(O_2) + k_3(O_3)} \approx \frac{J_3(O_3)}{k_2(M)(O_2)}$$

$$\frac{(O)}{(O_3)} \approx \frac{J_3}{k_2(M)(O_2)}$$

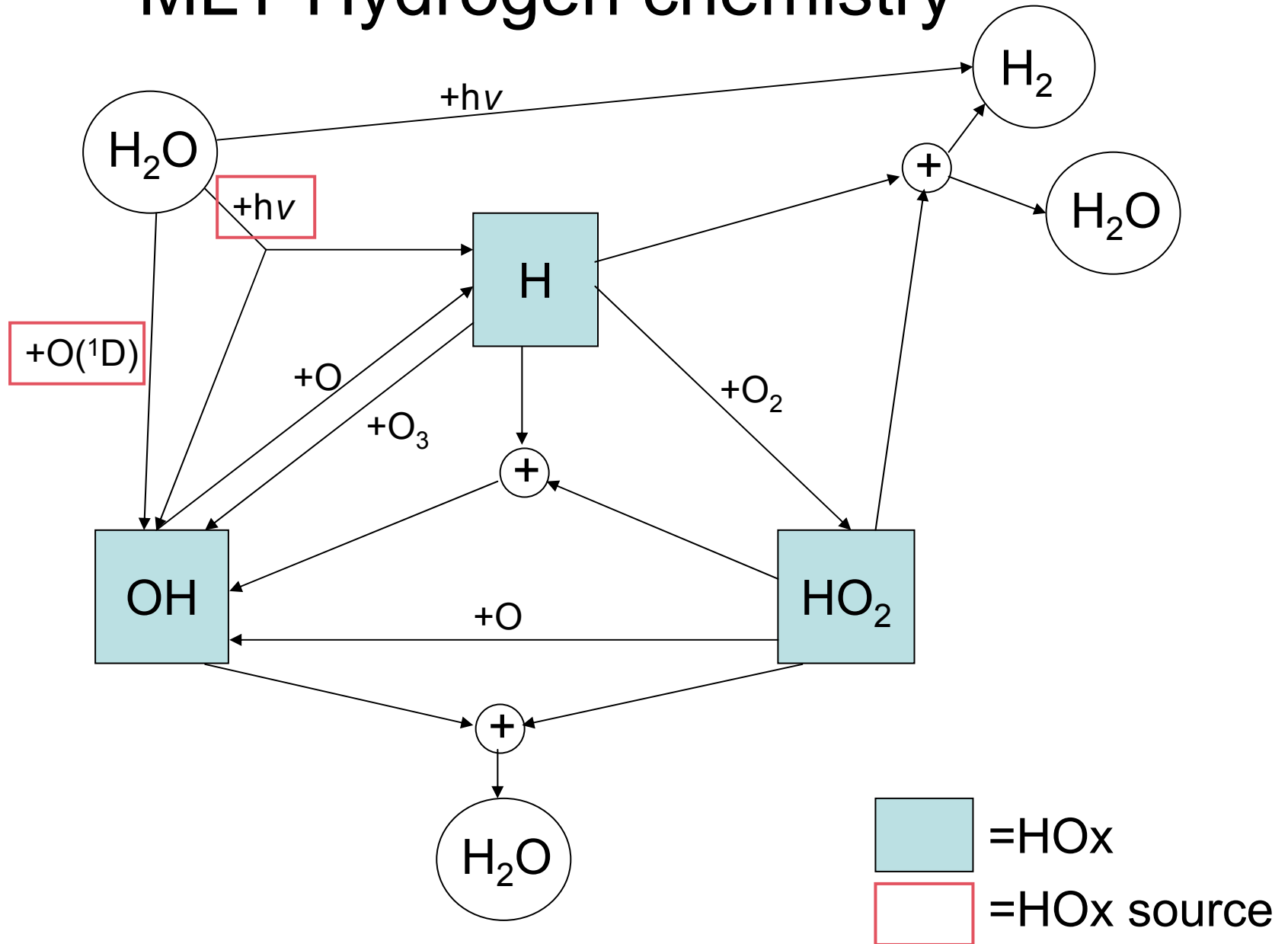
So  $O/O_3$  in the daytime is determined by the ratio of photolysis to recombination

Q: why do day/night differences increase with height? (<2x @ 60 km vs. 10x @ 70km)

Rapid recombination at sunset

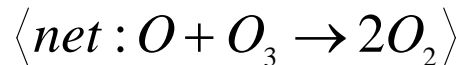
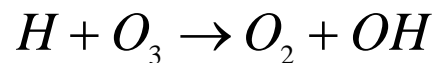
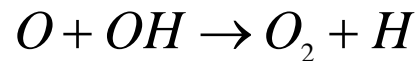
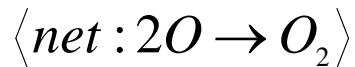
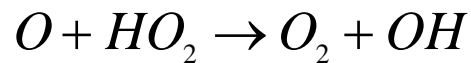
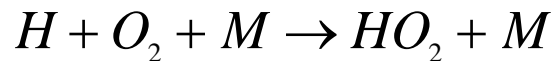
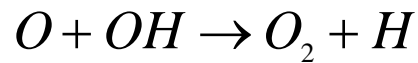


# MLT Hydrogen chemistry

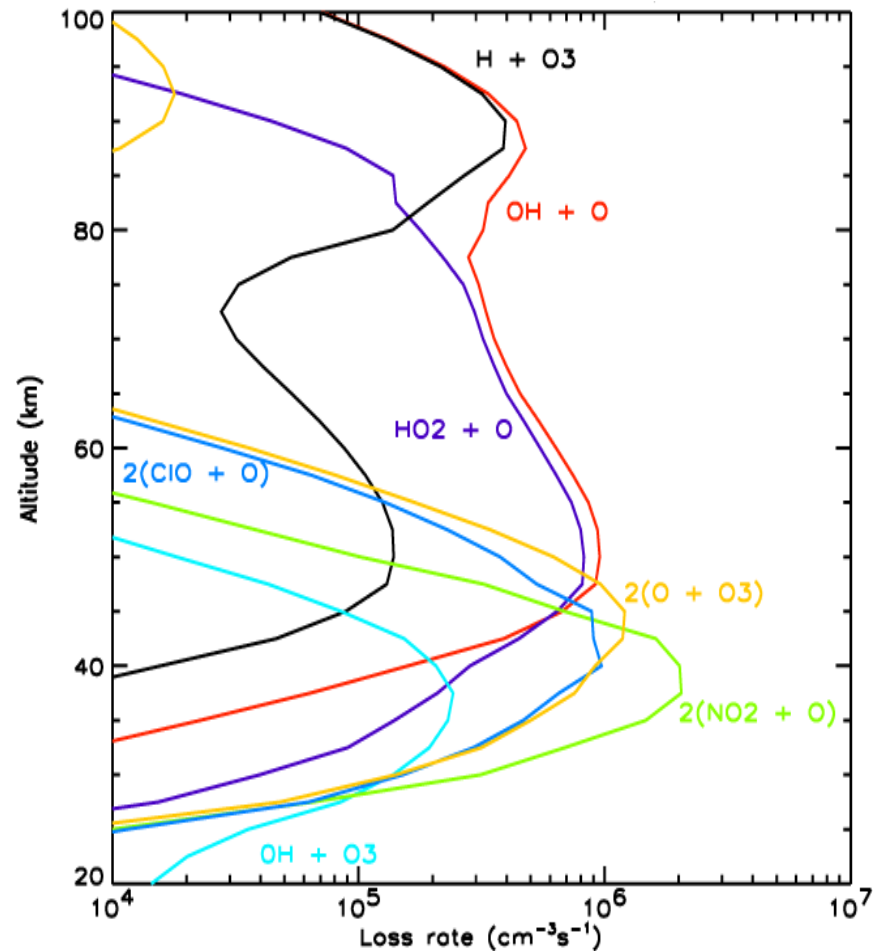


# Catalytic cycles in the mesosphere

## Mesosphere



## Zonal mean Ox loss rates 2.5°N



# Revised Ox continuity eqn.

With some algebra:

$$(O_3)_{80km} \propto \frac{[J_{O_2}(O_2)]^2}{J_{H_2O}(H_2O) \left( J_{O_3} + a \frac{J_{O_2}}{(M)} \right)}$$

$$(O_3)_{70km} \propto \frac{J_{O_2}(M)(O_2)^2}{J_{O_3}[J_{H_2O}(H_2O)]^{1/2}}$$

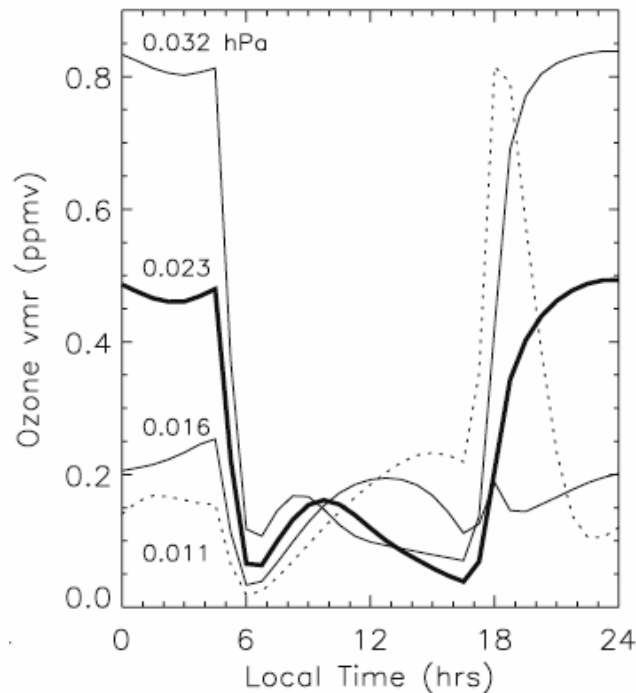
$$(O_3)_{50km} \propto \left( \frac{J_{O_2}(M)}{J_{O_3}} \right)^{2/3} \left( \frac{(N_2)}{J_{O_3}^*(H_2O)} \right)^{1/3} (O_2)^{4/3}$$

Q: why does water vapor dependency increase with height?  
Hint: what are the sources of HOx?

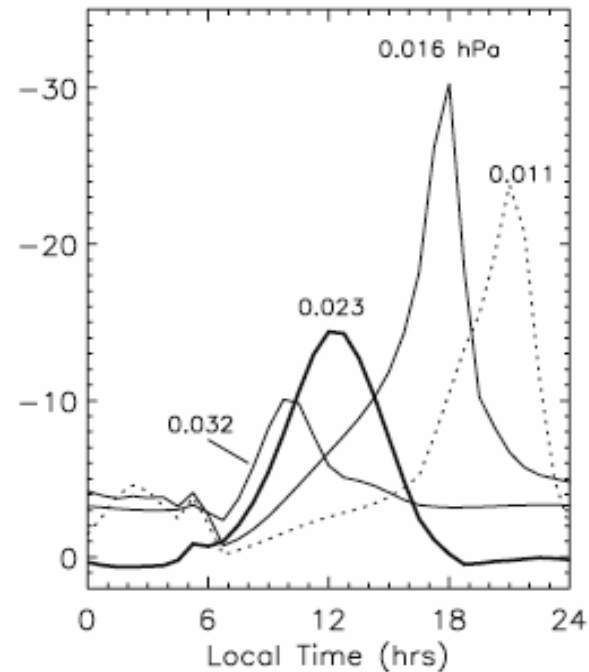
See Allen, 1984

Even these formulae are simplifications. Ozone is usually calculated using a time-dependent model, that does not assume photochemical equilibrium. The response of ozone to water vapor changes with height and time of day:

Ozone

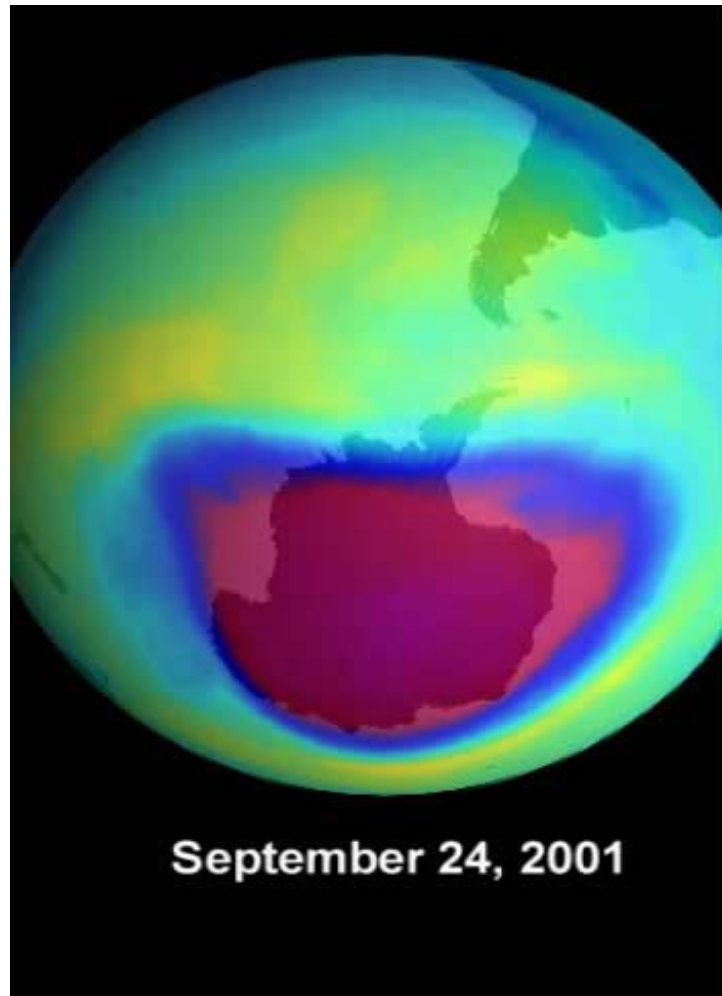


$\% \Delta O_3$  for  $10\% \Delta H_2O$



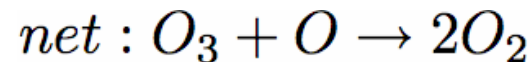
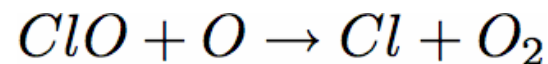
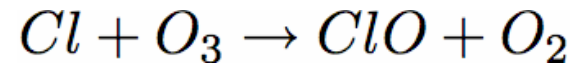
# Catalytic cycles in the stratosphere: ClOx

Total ozone column

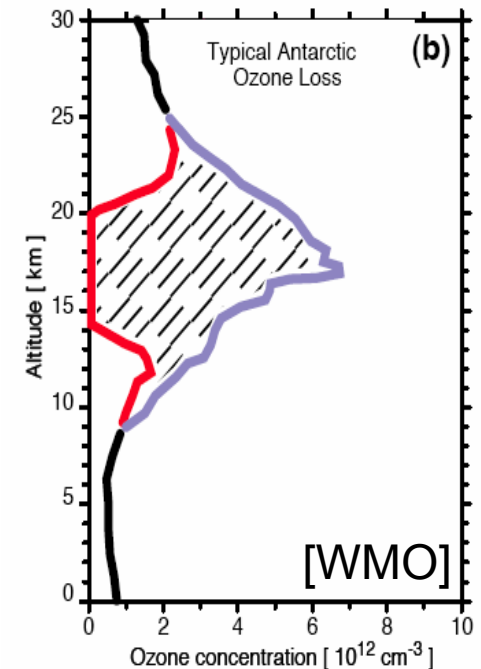


[GSFC, NASA]

40-50 km & Antarctic lower stratosphere

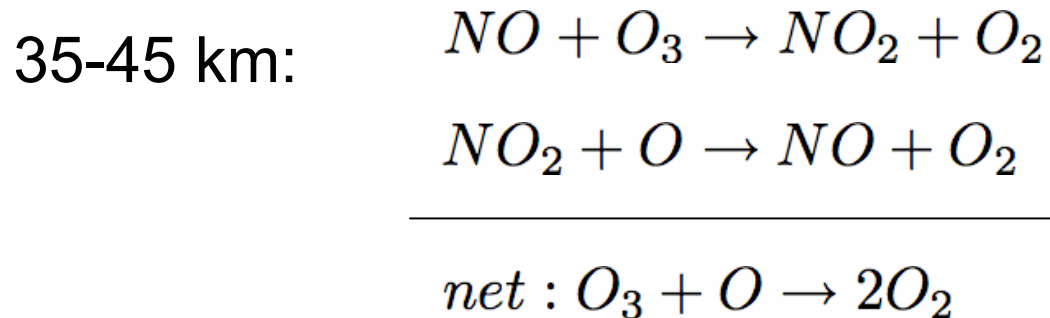


ClOx = Cl + ClO has a large source from chlorofluorocarbons (CFCs) - this leads to the creation of the Antarctic ozone hole. In the mid-1990s approximately 75-85% of stratospheric chlorine was of anthropogenic origin.





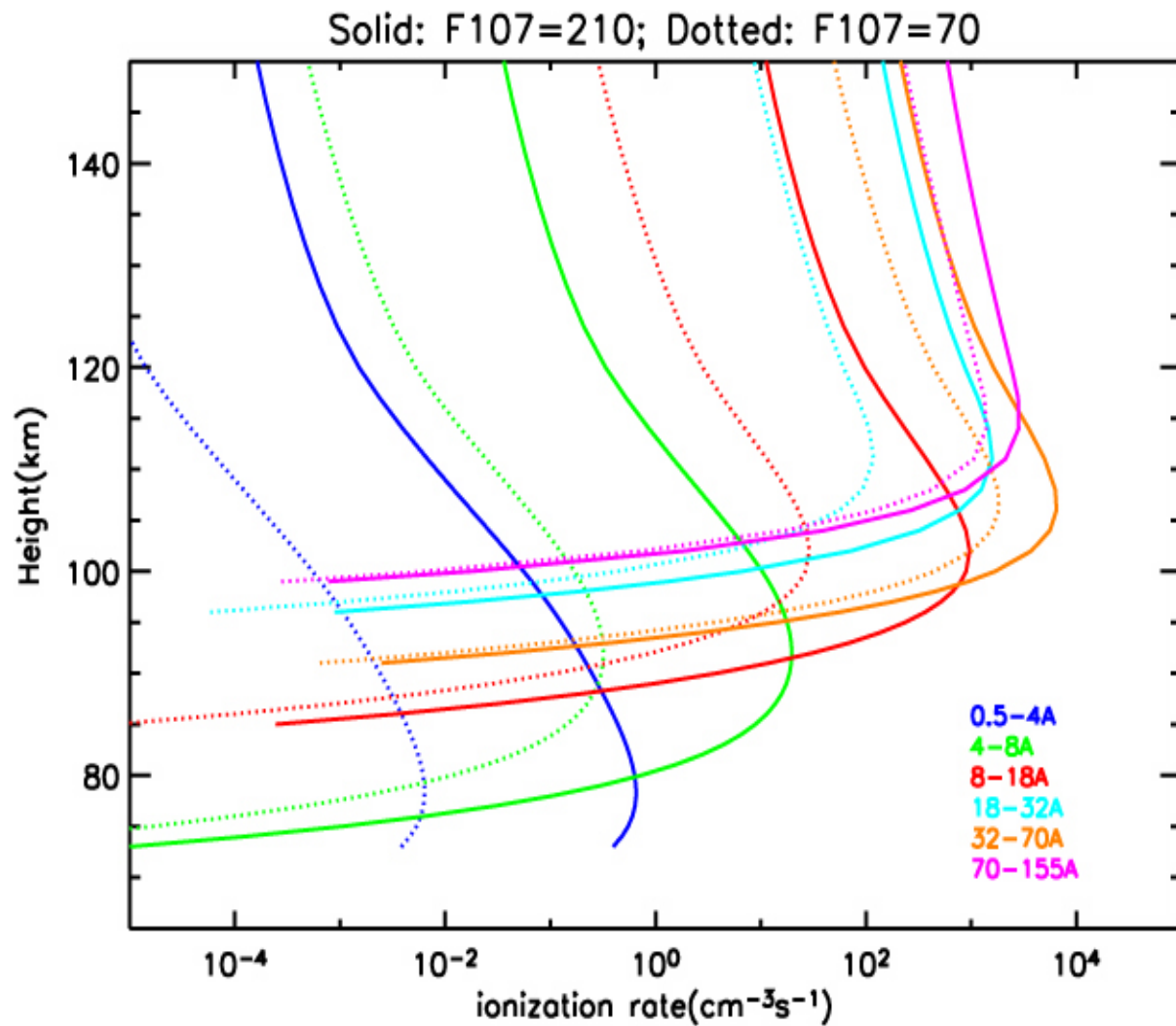
# Catalytic cycles in the stratosphere: NO<sub>x</sub>



Sources of stratospheric NO<sub>x</sub> = NO + NO<sub>2</sub>:

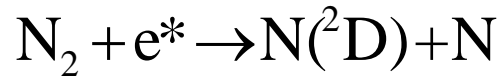
- Oxidation of N<sub>2</sub>O produced in the troposphere
- Ionization of N<sub>2</sub> by GCR & solar energetic particles
- Stratospheric aircraft
- NO<sub>x</sub> transported from the mesosphere/thermosphere

# EUV/x-ray ionization rates



# Ionization leads to N(<sup>2</sup>D) production

electron impact



(e\* secondary/photoelectron

Produced by (1-10 keV)  
precipitating electrons and  
solar soft X-rays (2-7 nm)

dissociative recombination

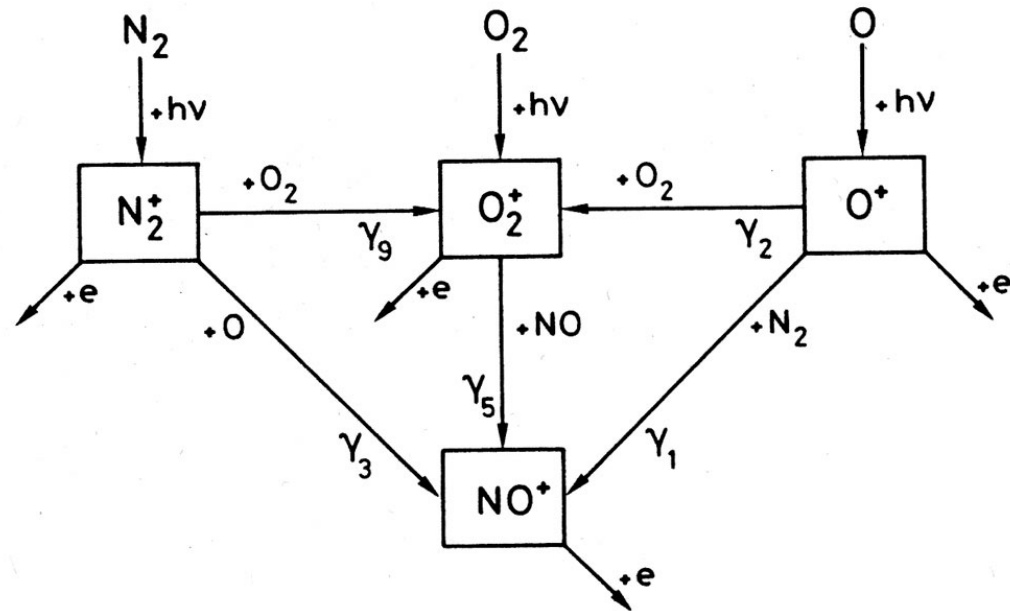
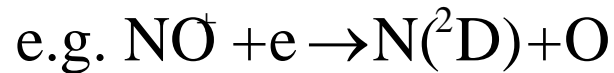
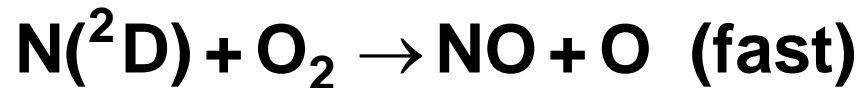


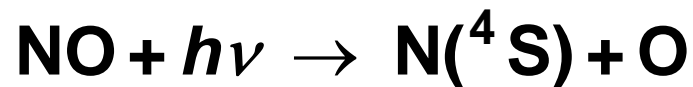
Fig. 6.12. Schematic diagram of E-region ion chemistry.

# Nitric Oxide in the lower-thermosphere

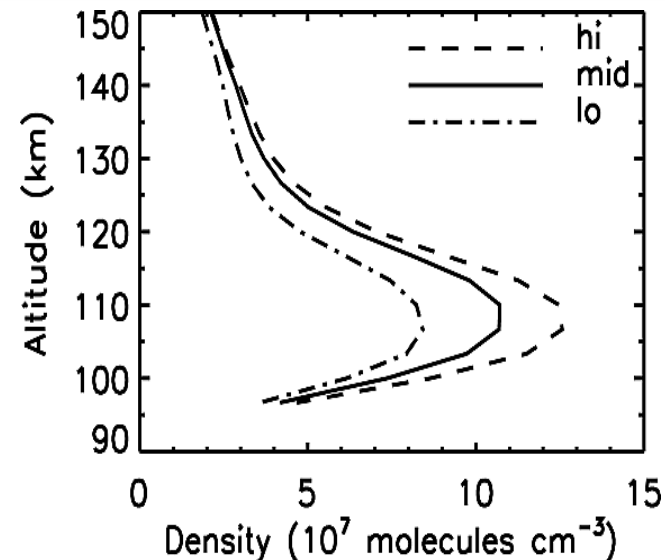
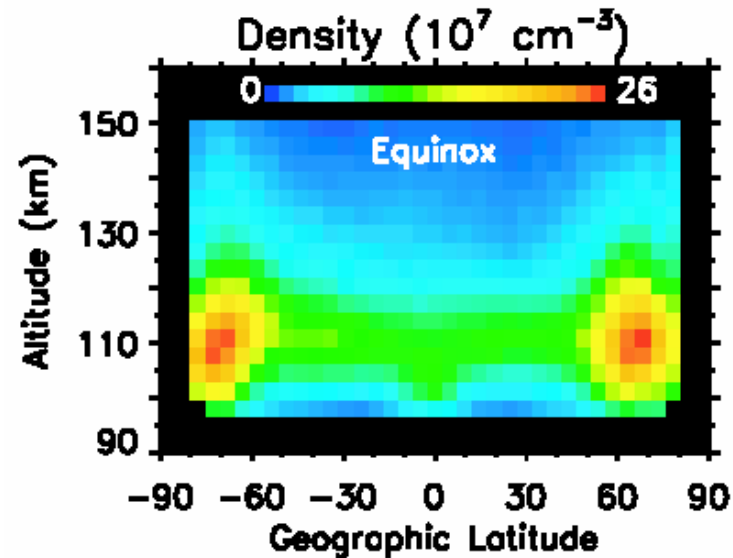
## Production:



## Loss:



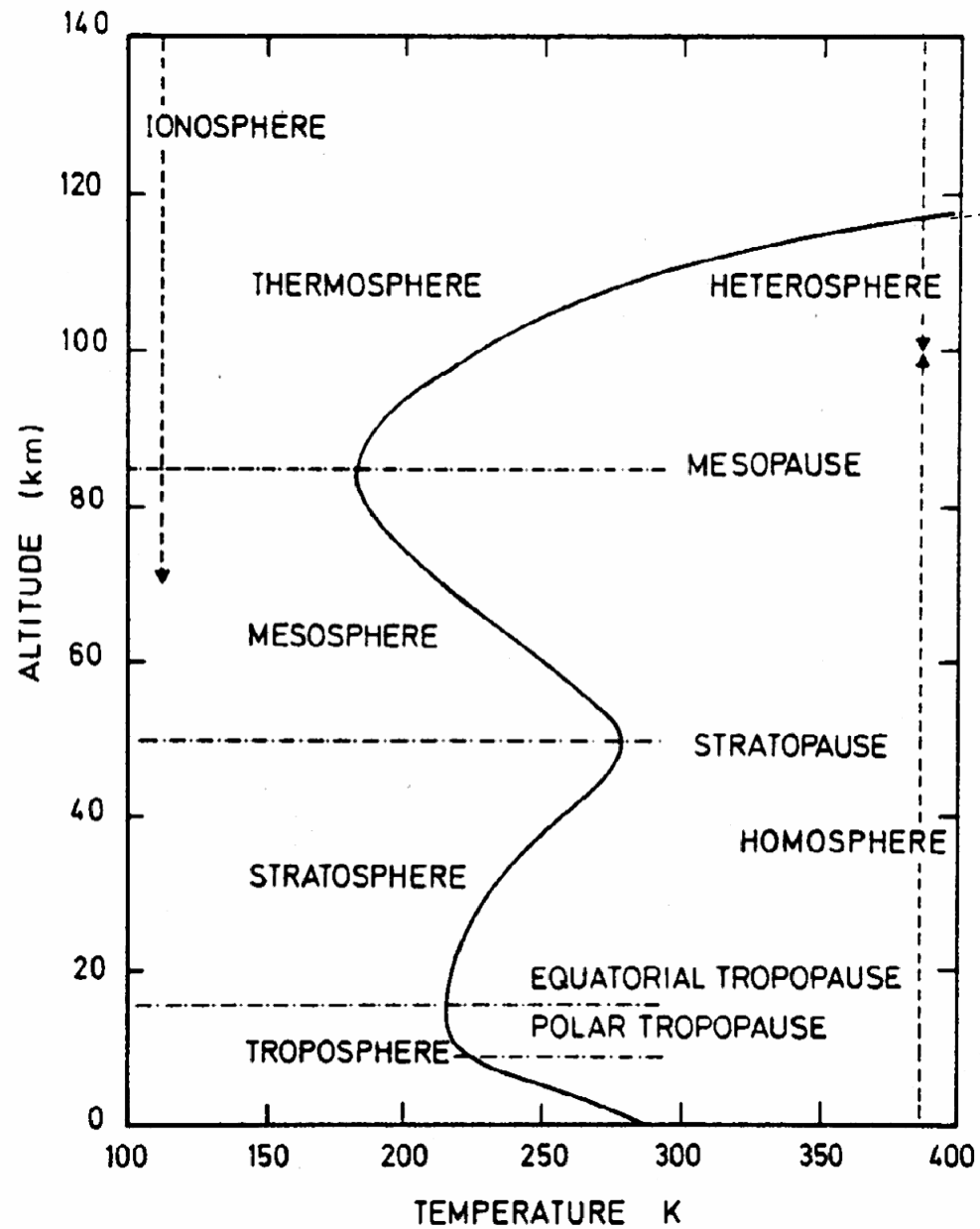
[a "canabalistic" reaction]



(Barth et al., 2003)

# Energetics

# Thermal structure



# Thermodynamic equation

$$\frac{\partial T}{\partial t} = -\left(\Gamma_d + \frac{\partial T}{\partial z}\right)w - \mathbf{v} \cdot \nabla T + \frac{Q}{c_p} + \dots$$

Adiabatic heating



Heat advection



Diabatic heating/cooling

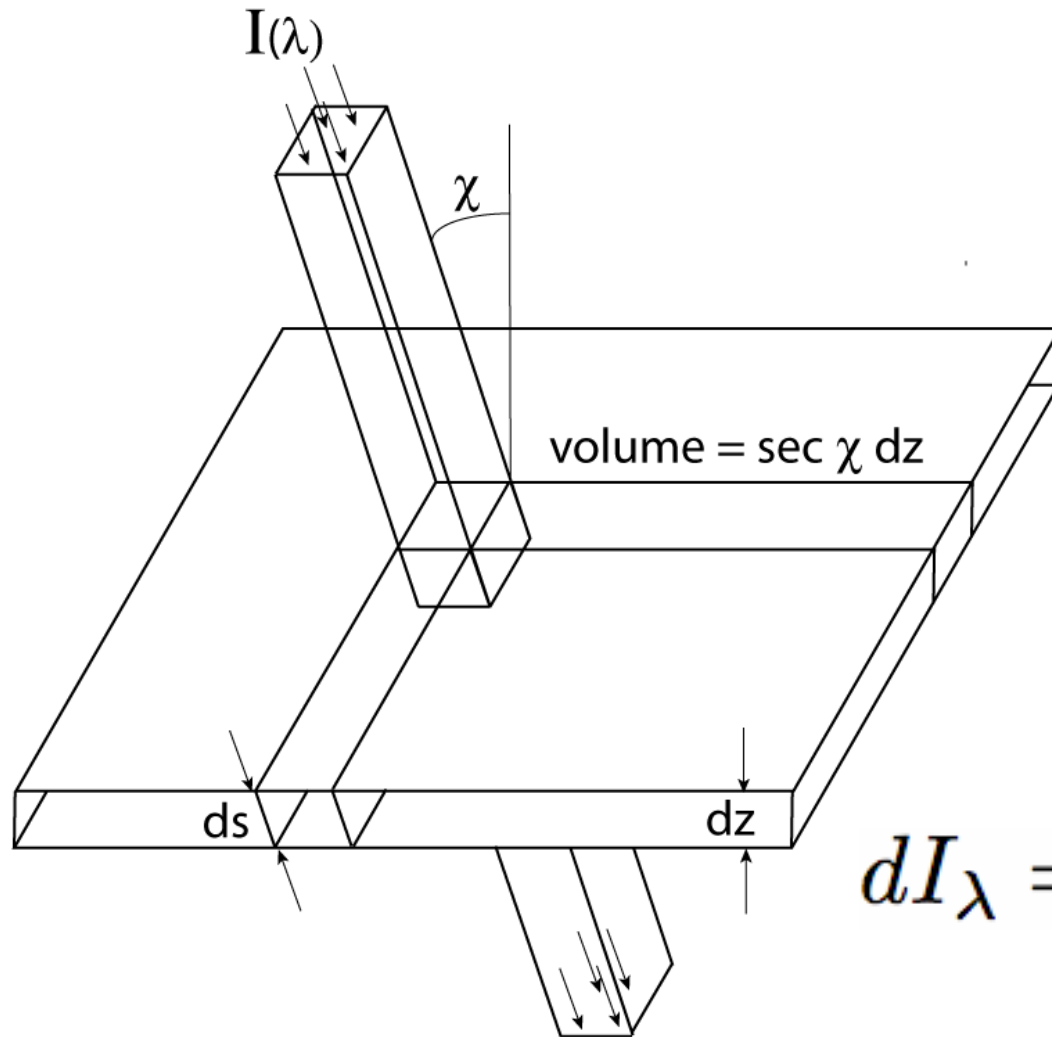


# Sources of diabatic heating/cooling

- Absorption of solar radiation and energetic particles (e.g. ozone)
- Chemical heating through exothermic reactions ( $A + B \rightarrow AB + \text{Energy}$ )
- Collisions between ions and neutrals (Joule heating)
- IR cooling (e.g.  $\text{CO}_2$  and NO)
- Airglow



# Absorption of solar radiation



Beer-Lambert Law:

$$dI_{\lambda} = -I_{\lambda} \sigma_a(\lambda) n_a ds$$

For a plane-parallel atmosphere:

$$ds = dz \sec \chi$$

Integrating:

$$I(z) = I_0 \exp \left( -\sec \chi \int_z^\infty \sigma_a n(z') dz' \right)$$

The optical depth is defined as:

$$\tau_a(\lambda, z) = \sec \chi \int_z^\infty \sigma_a n(z') dz'$$

Recall:  $n(z) = n_0 \frac{T_0}{T} \exp\left(-\int_0^z \frac{dz}{H}\right)$

const. T:  $n(z) = n_0 e^{-(z-z_0)/H}$

Under the assumption we have one absorbing species, with fixed scale height:

$$\tau = \sec\chi \int_z^\infty \sigma_a n_0 e^{-z'/H} dz'$$

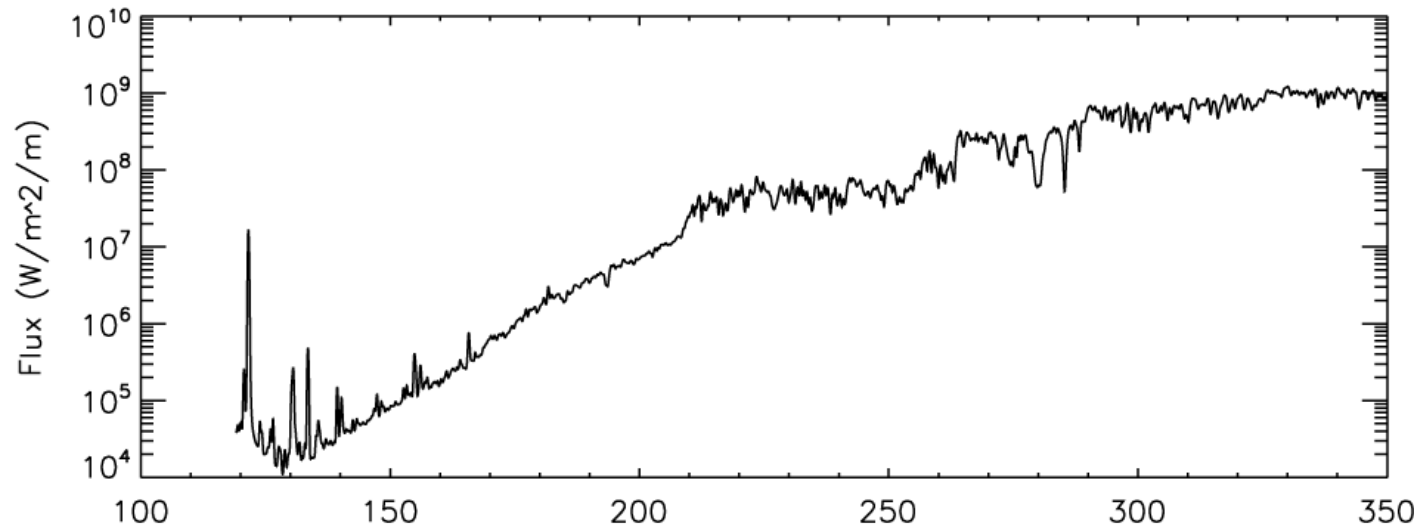
$$\tau = \sec\chi \sigma_a n(z) H$$

$$I(z) = I_\infty e^{-\sec\chi \sigma_a n(z) H}$$

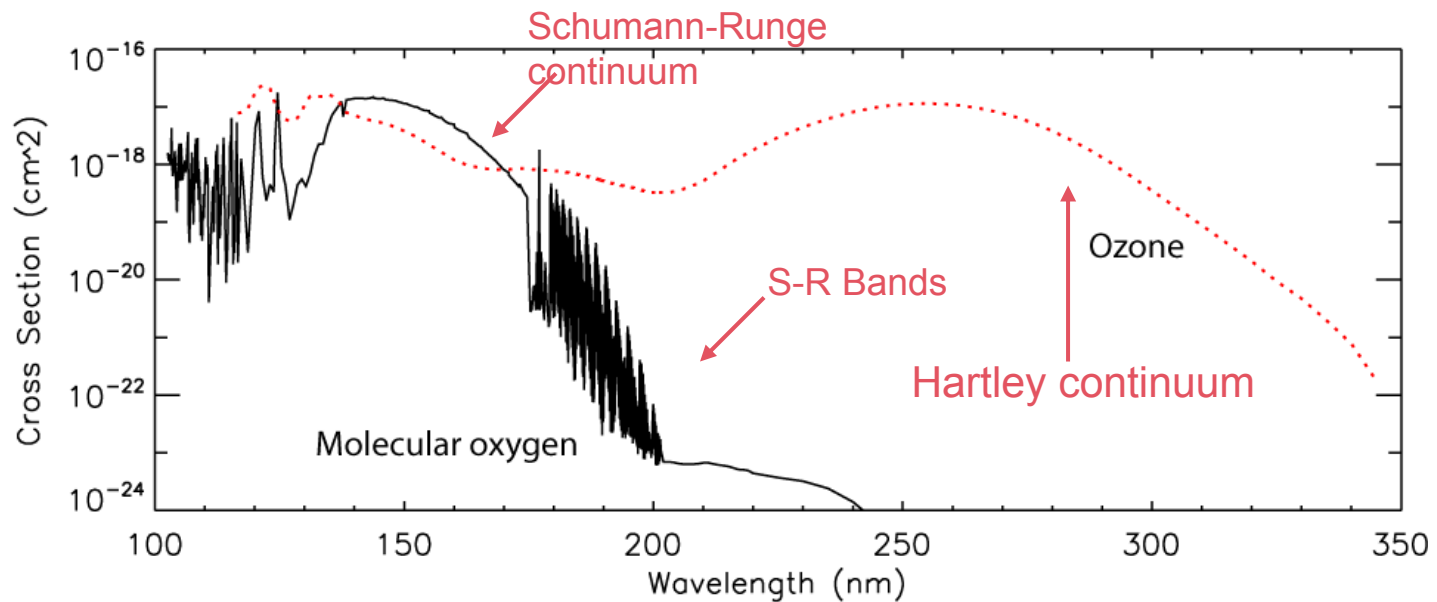
Note: the height at which the exoatmospheric flux decrease by a factor of 1/e corresponds to  $\tau(z)=1$

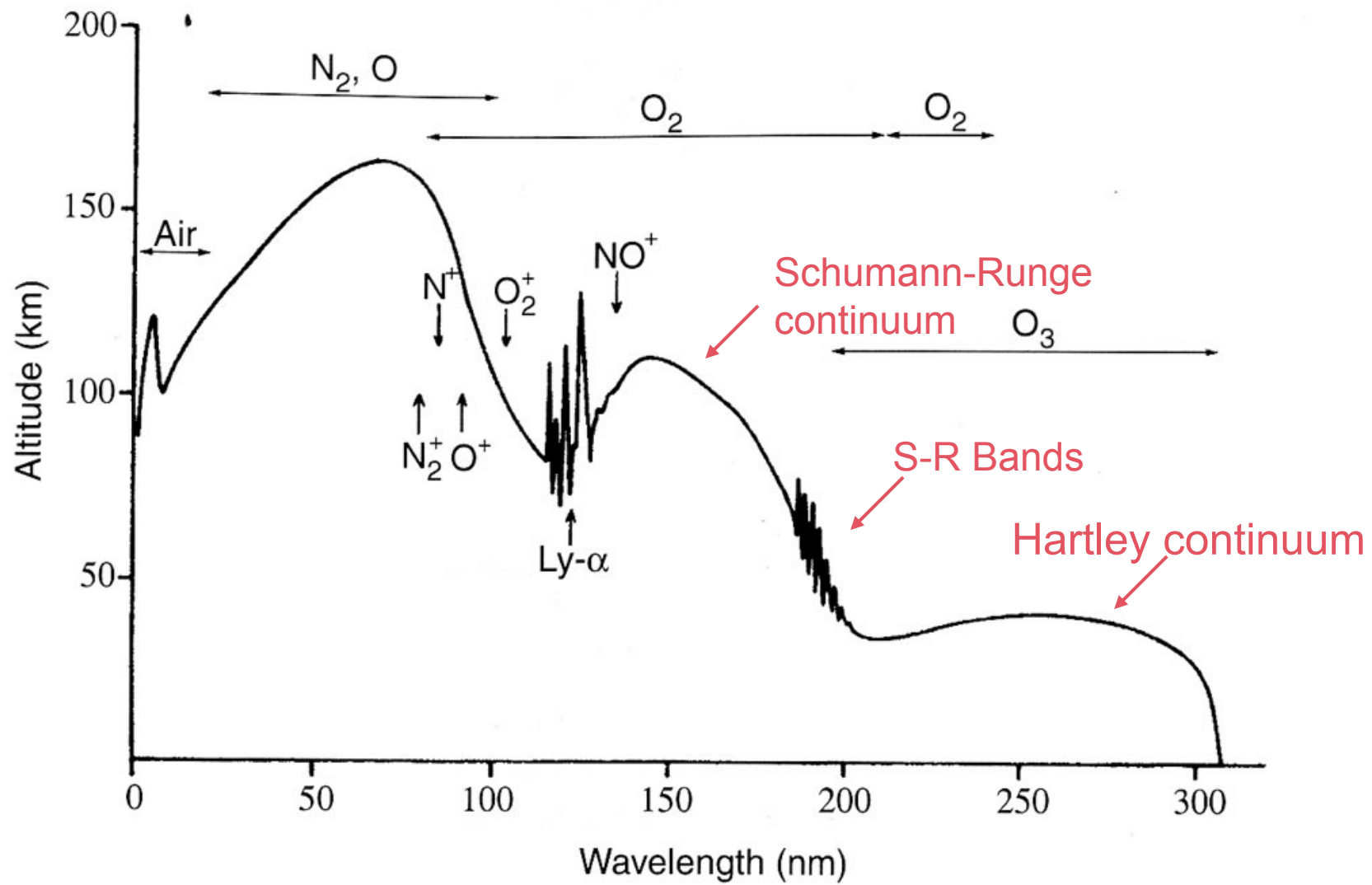
In practice there are multiple (overlapping) absorbers:

$I_\lambda$



$\sigma_{O_2/O_3}$





PRACTICUM: calculate  $\tau=1$  height vs.  $\lambda$

## Energy deposition rate due to solar absorption

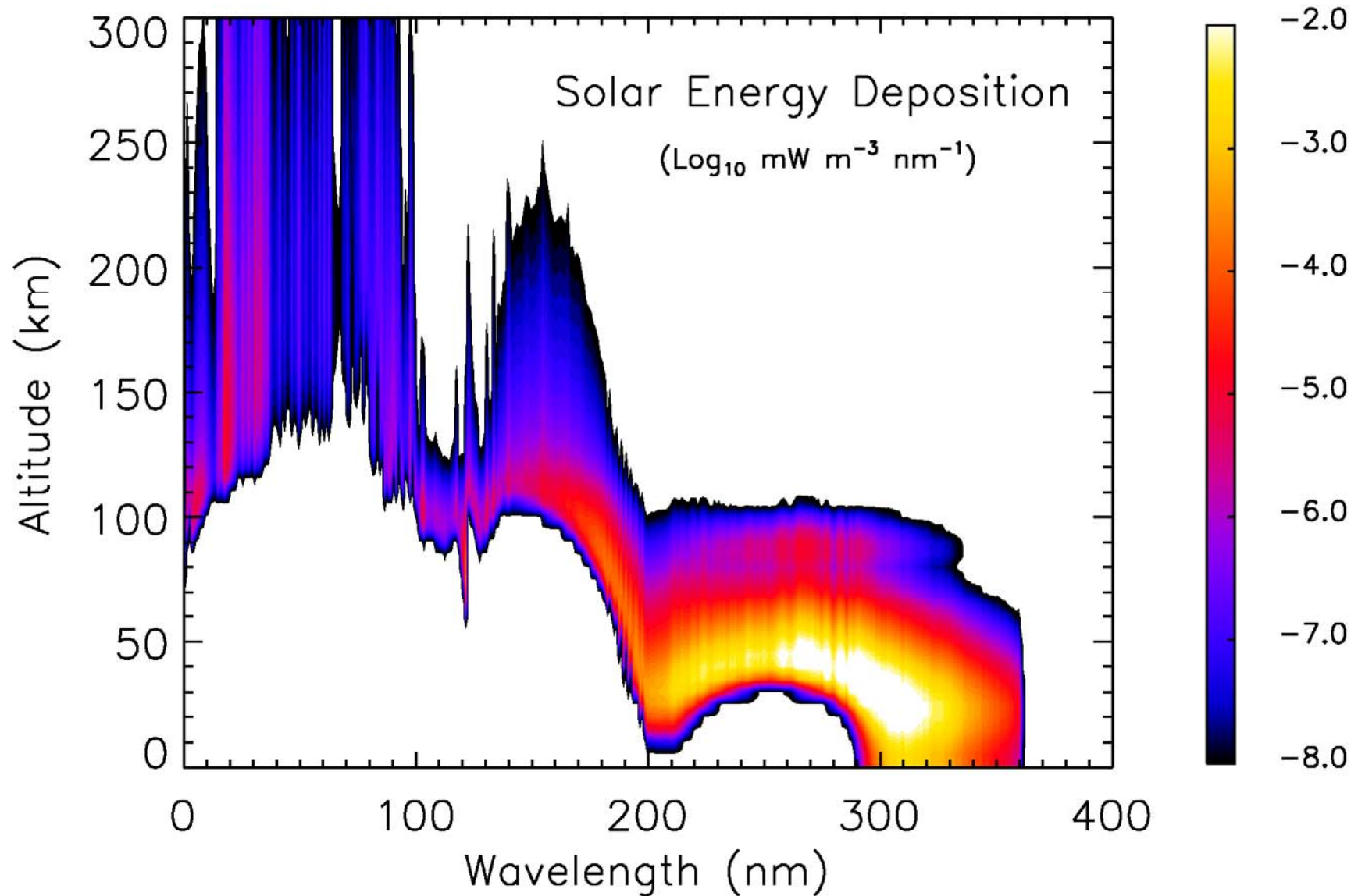
If we assume all absorbed radiation is thermalized at the location it is absorbed, then the energy deposition rate is the divergence of the vertical component of the total flux (spectral flux integrated over all wavelengths):

$$Q = \frac{\partial F}{\partial z}$$

The heating rate is then:

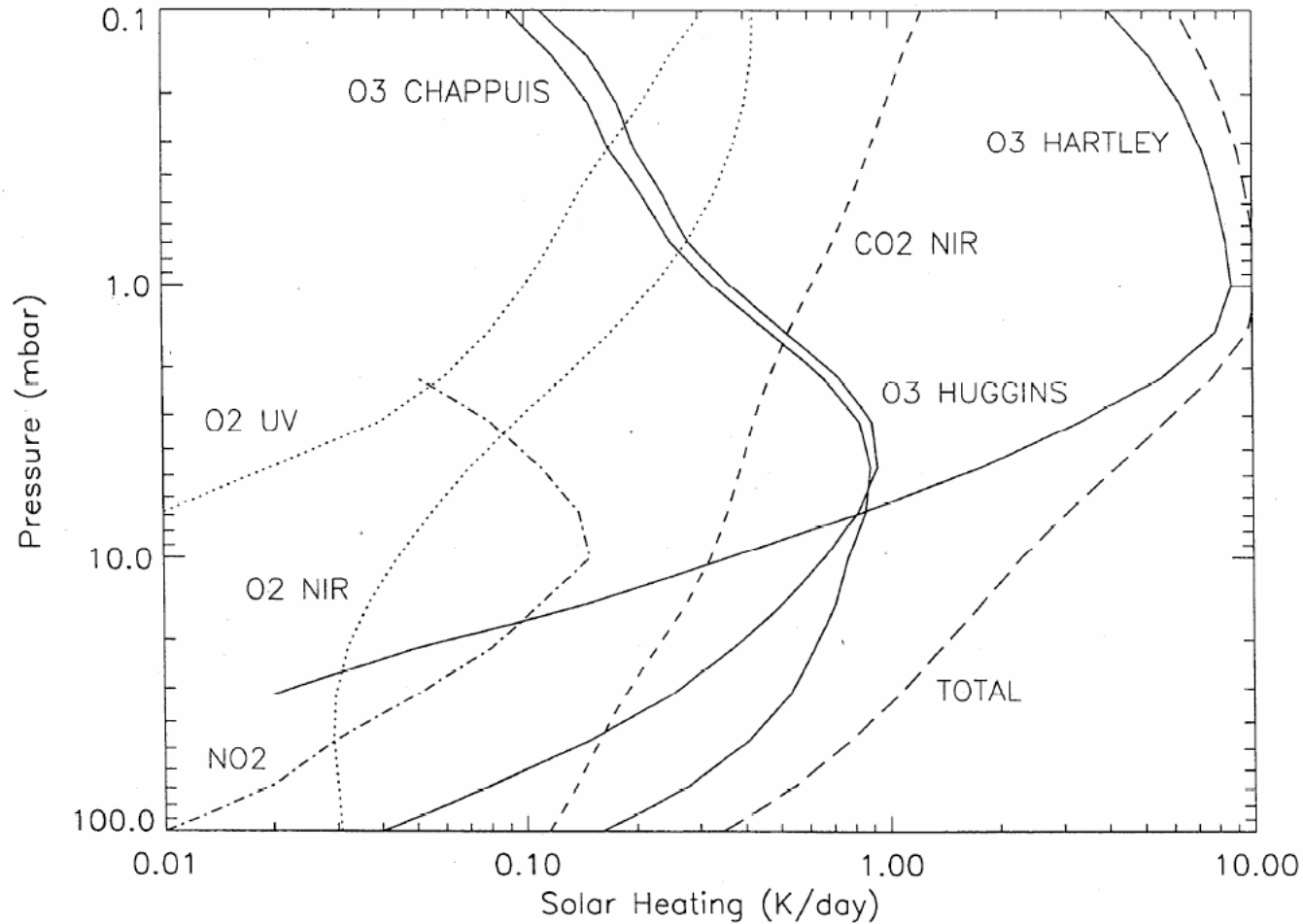
$$\frac{\partial T}{\partial t} = \frac{1}{\rho c_p} \frac{\partial F}{\partial z}$$

# Solar UV Energy Deposition



Courtesy Stan Solomon

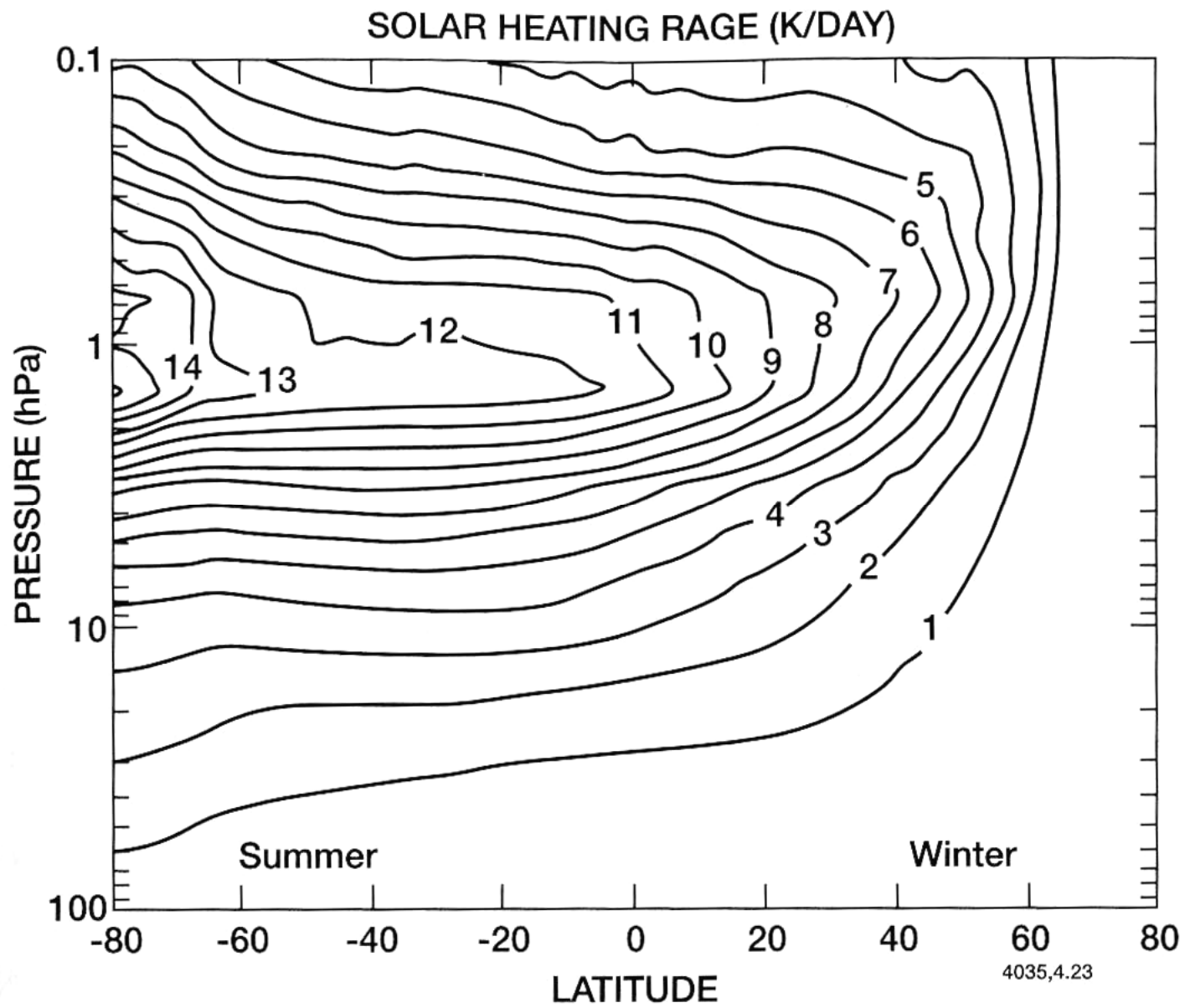
# Stratospheric heating



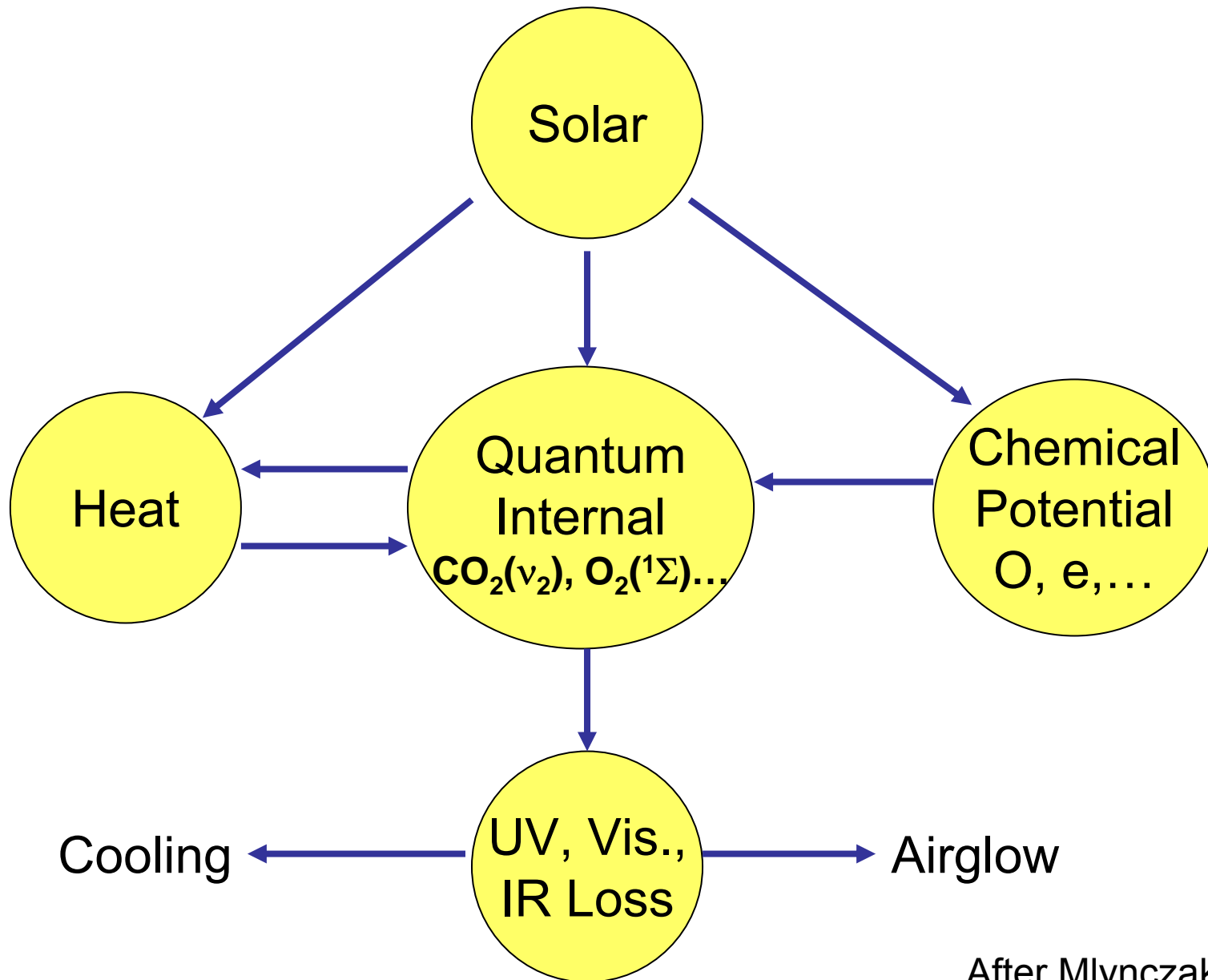
Mertens et al., 1999

Absorbed energy is thermalized locally



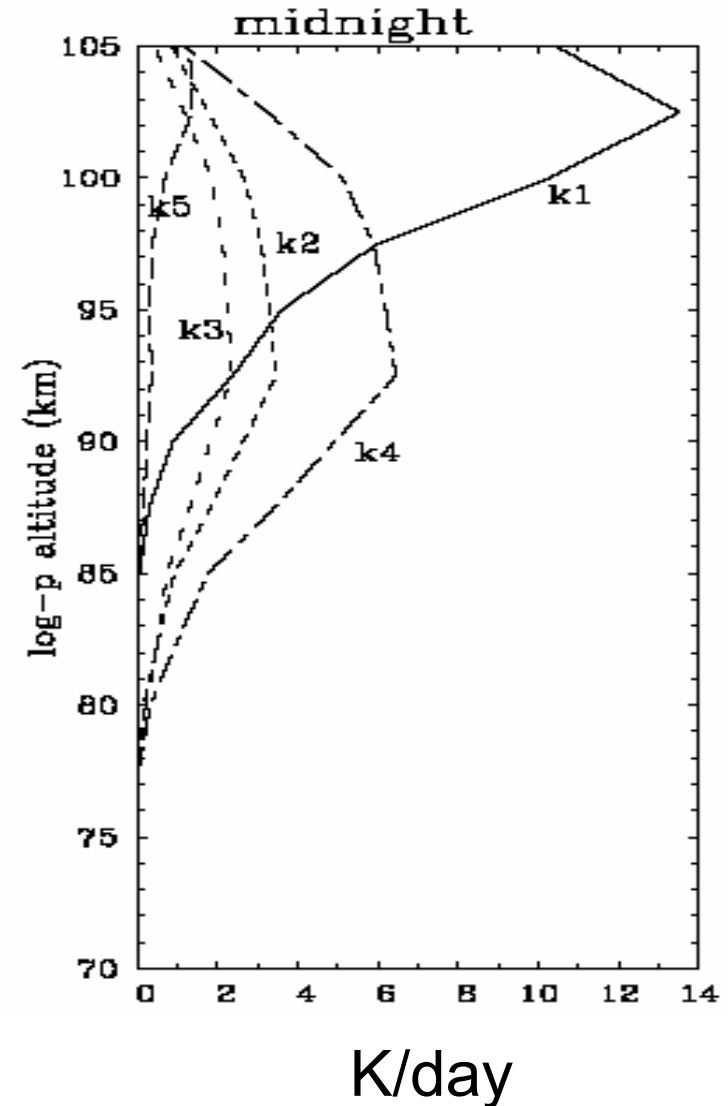


Not all absorbed radiation is directly thermalized

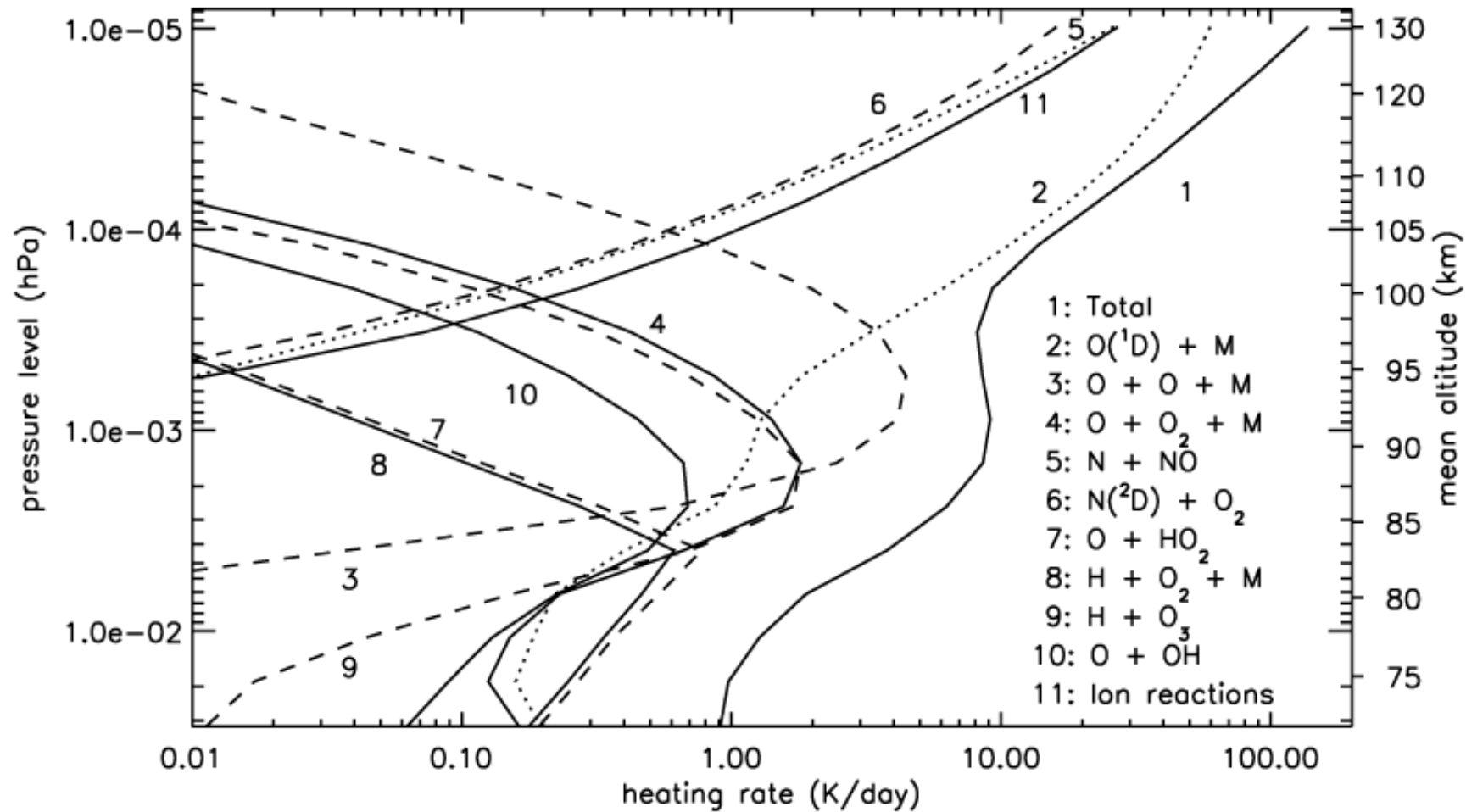


After Mlynczak et al.

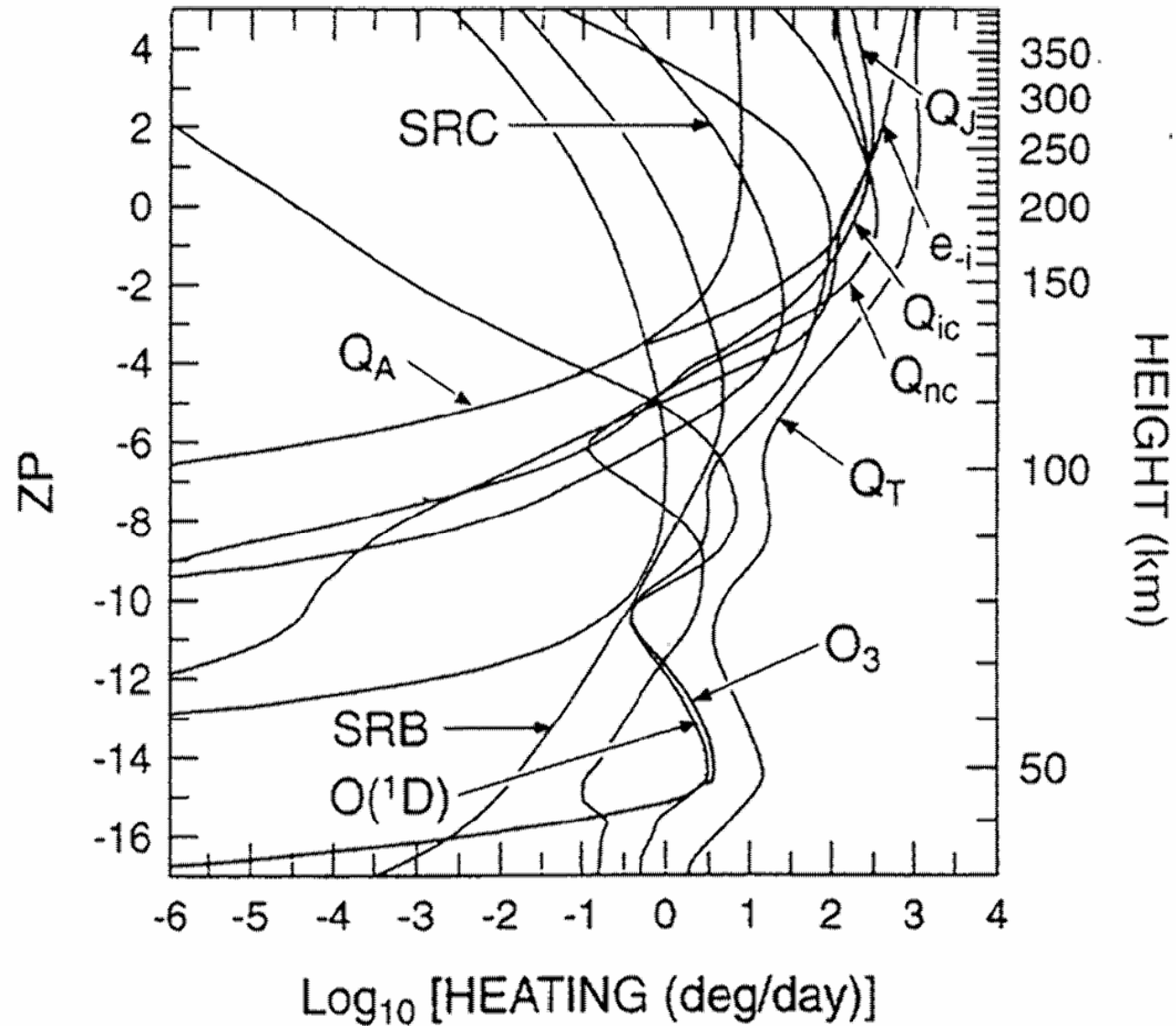
# Chemical heating through exothermic reactions



# Global mean chemical heating rates

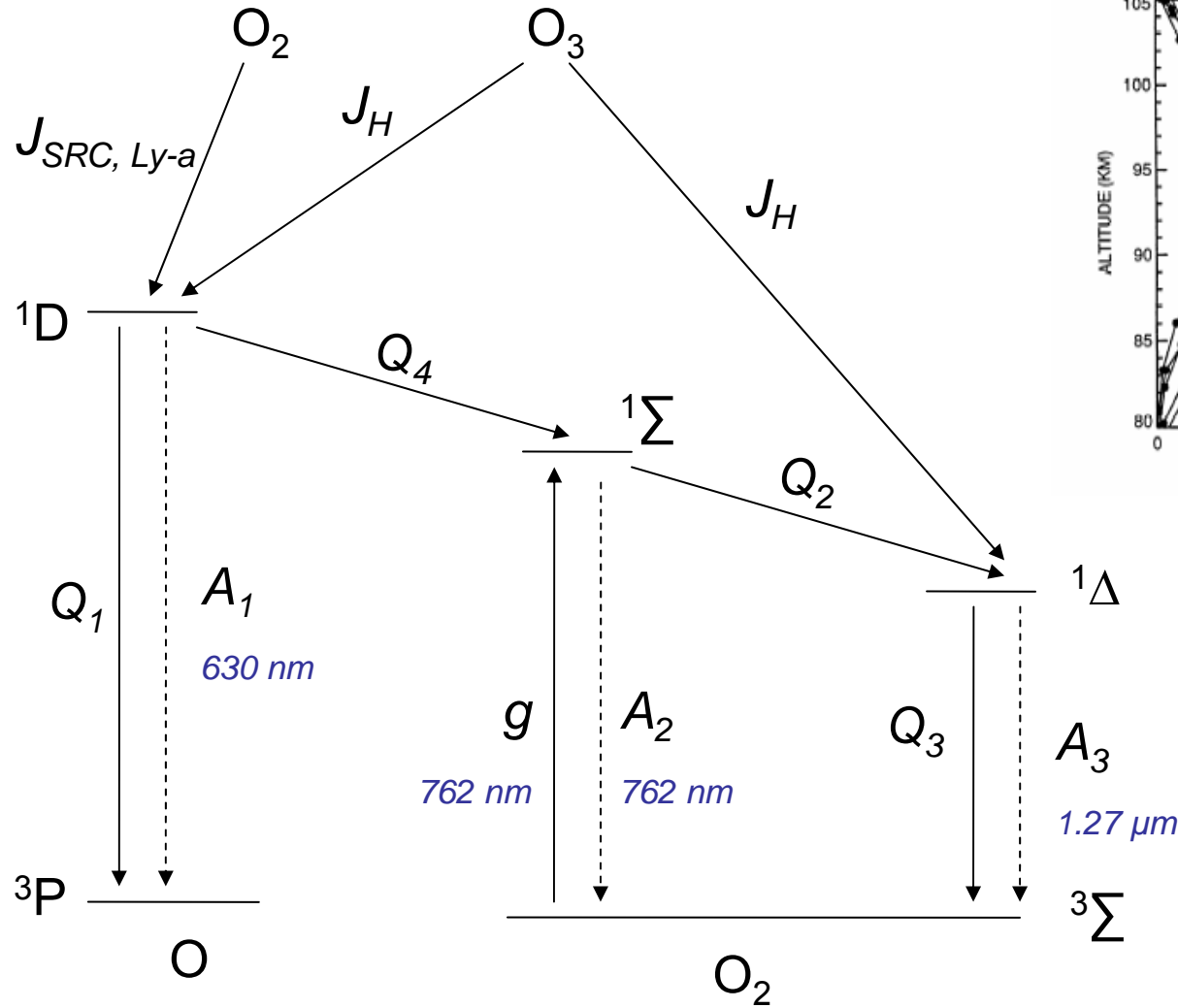


# MLT Global average heating rates



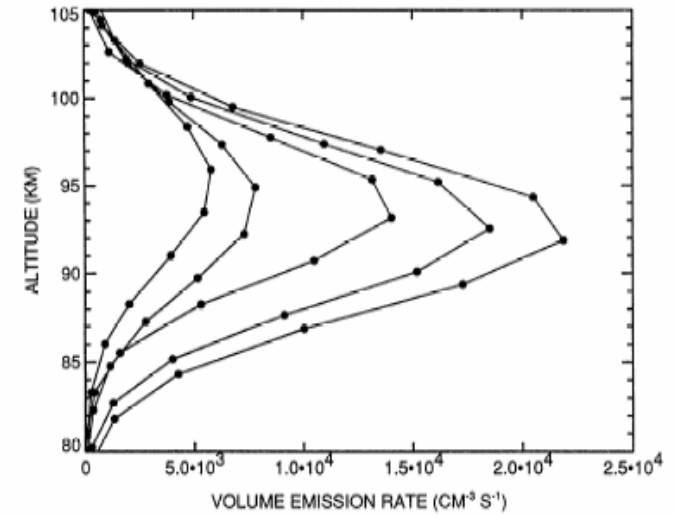
From [Roble, 1995]

# Airglow



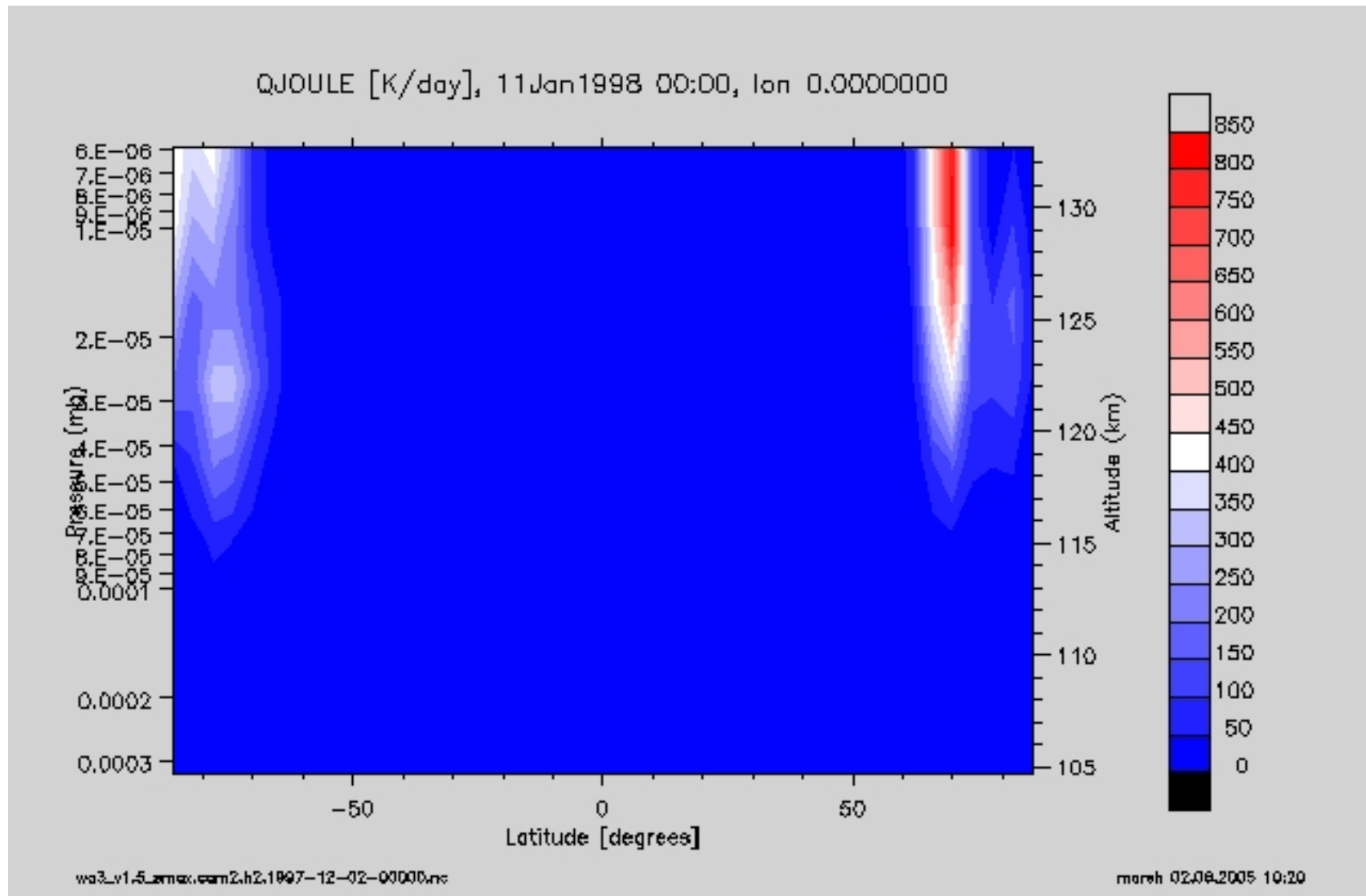
After Mlynczak et al. [1993]

O<sub>2</sub> ( $^1\Sigma$ ) emission



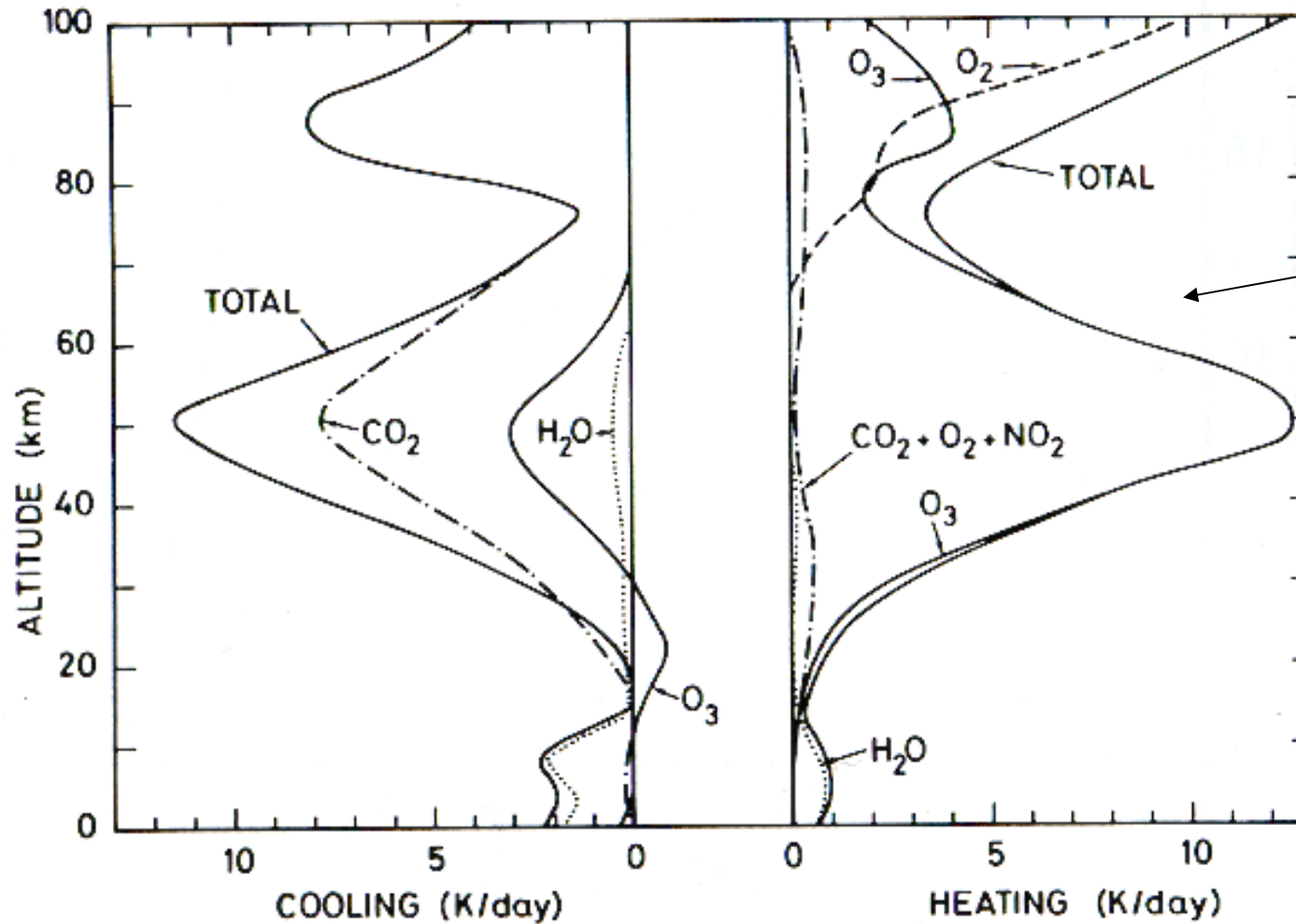
Burrage et al. [1994]

# Joule Heating (K/day) due to ion/neutral collisions



Heating from collisions between ions and neutrals

# Heating in the middle atmosphere must be balanced by cooling



Practicum:  
calculate  
this curve

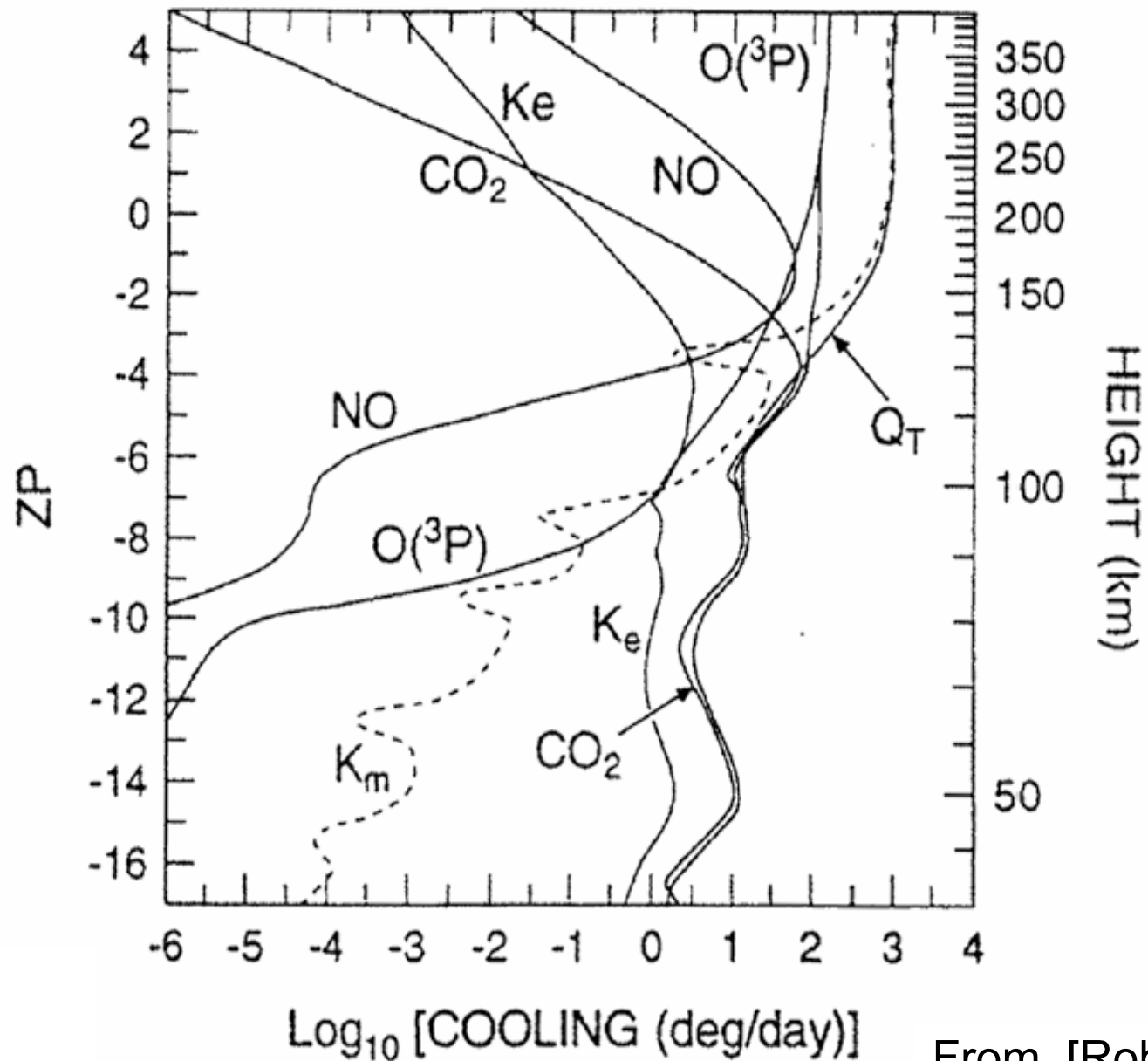
London (1980)



# Radiative cooling

- IR atomic oxygen emission ( $63\ \mu\text{m}$ ) in the upper thermosphere
- Non-LTE IR emission of NO ( $5.3\ \mu\text{m}$ ) 120 to 200 km
- CO<sub>2</sub>  $15\ \mu\text{m}$  (LTE and non-LTE) important below 120km
- IR emission by ozone and water vapor in the middle atmosphere

# Global average cooling rates

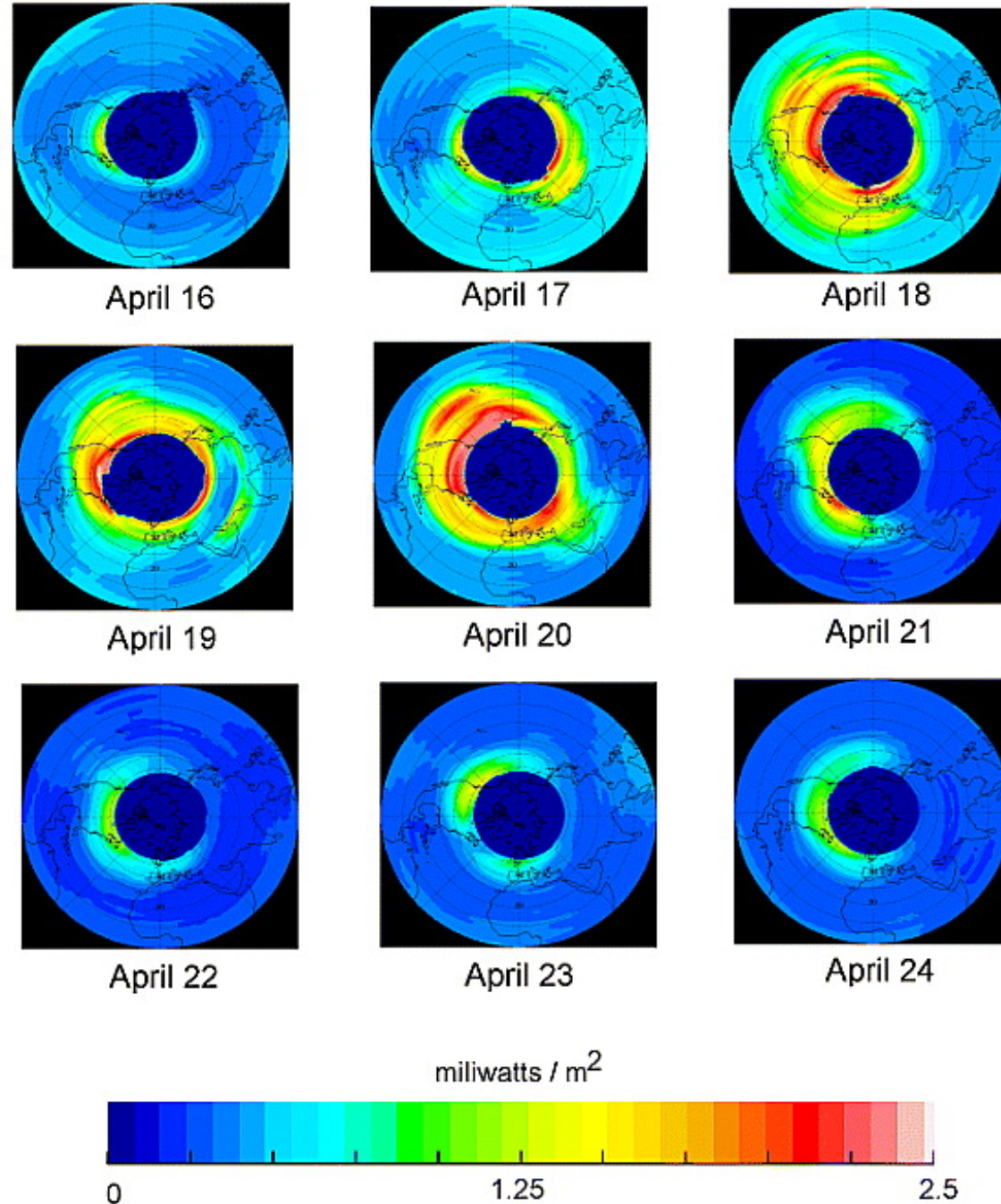


From [Roble, 1995]

# TIMED/SABER observations of NO cooling

Response to the  
solar storm  
during April, 2002

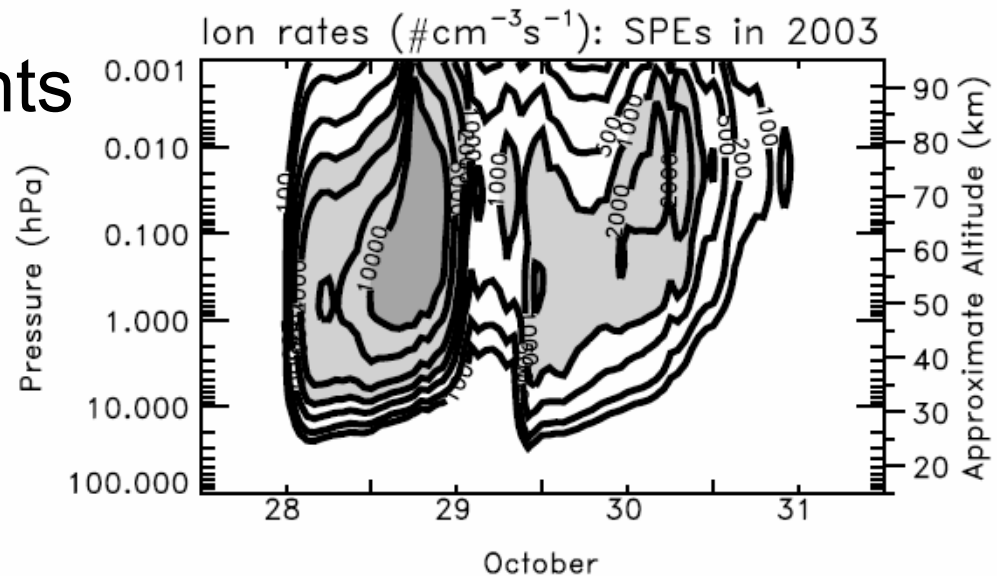
NO 5.3  $\mu\text{m}$  Radiated Flux (Northern Hemisphere)



Mlynczak et al., *Geophys. Res. Lett.*, 30(21), 2003.

# Additional forcing of the neutral atmosphere

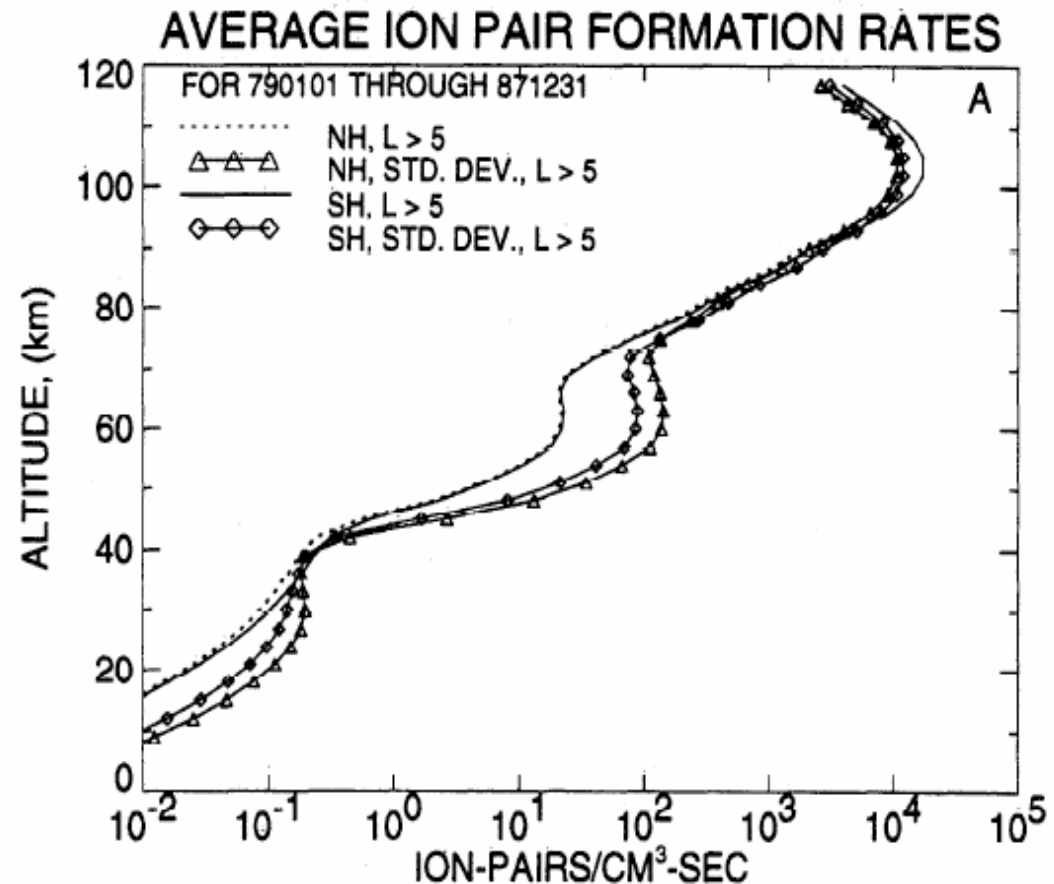
- Energetic particle precipitation
  - Solar proton events (SPEs)
  - Medium energy electrons
  - Highly-relativistic electrons (HREs) >1MeV
- Galactic cosmic rays



Jackman et al., 2005

# Energetic Electron Precipitation

- Thermosphere
  - <30 keV
- Mesosphere
  - 30-300 keV
- Stratosphere
  - >300 keV



Callis et al., 1998

The End