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International Centre for Theoretical Physics



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ICTP-COST-USNSWP-CAWSES-INAF-INFN  
International Advanced School  
on  
Space Weather  
2-19 May 2006

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*Ionosphere-Thermosphere Basics - II*  
*Dynamics of the Thermosphere*

*Jeffrey M. FORBES*  
*Department of Aerospace Engineering Sciences*  
*University of Colorado at Boulder*  
*Boulder, CO 80309-0429*  
*U.S.A.*

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These lecture notes are intended only for distribution to participants

# **Ionosphere-Thermosphere Basics - II**

## **Dynamics of the Thermosphere**

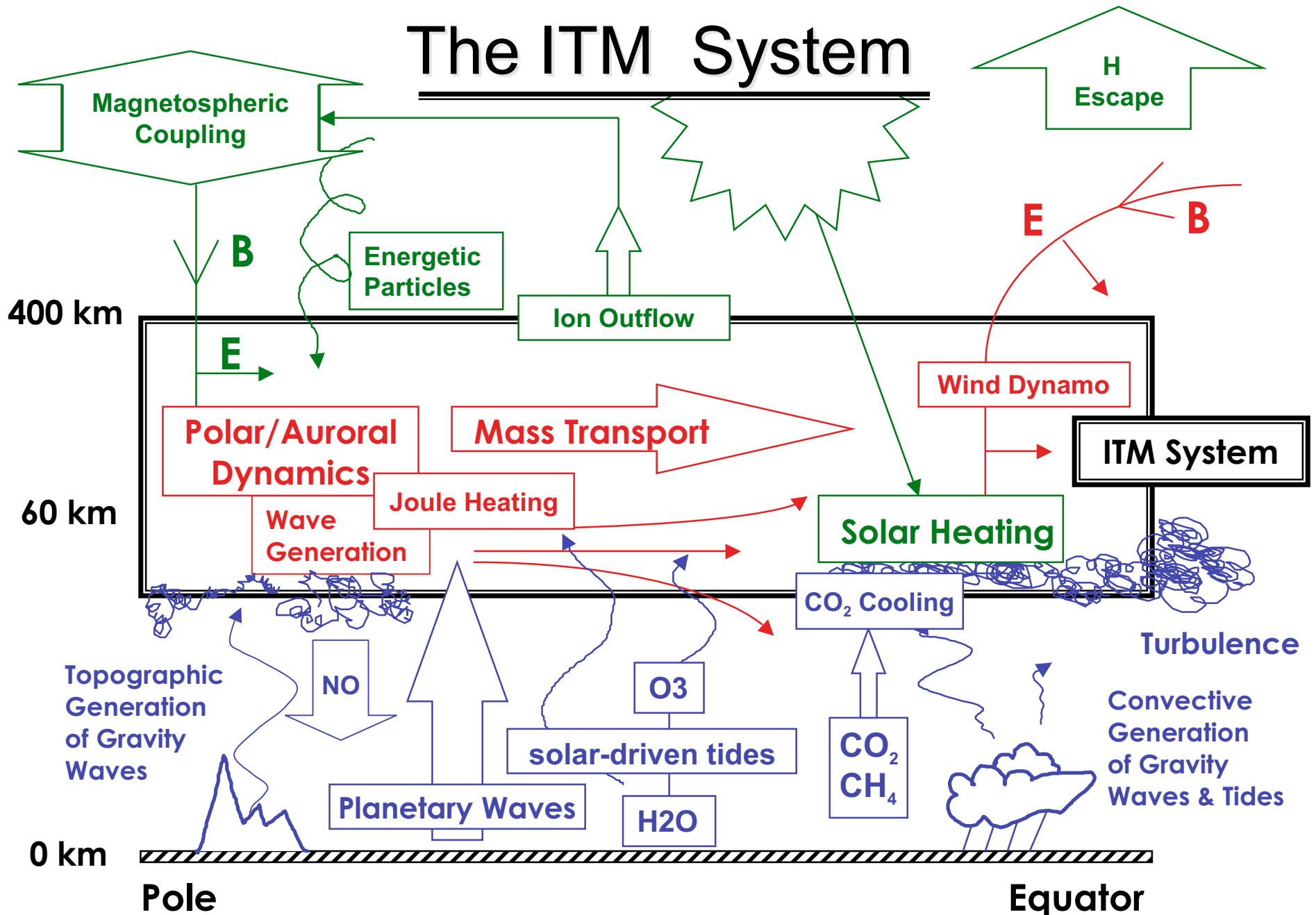
*Jeffrey M. Forbes, University of Colorado*

<http://spot.colorado.edu/~forbes/Home.html>

### **Lecture Topics**

- Momentum Balance
- Winds and Composition: Diurnal Variations
- Winds and Composition: Seasonal Variations
- Thermosphere Weather: Magnetic Storm Response
- Thermosphere Weather: Coupling with the Lower Atmosphere

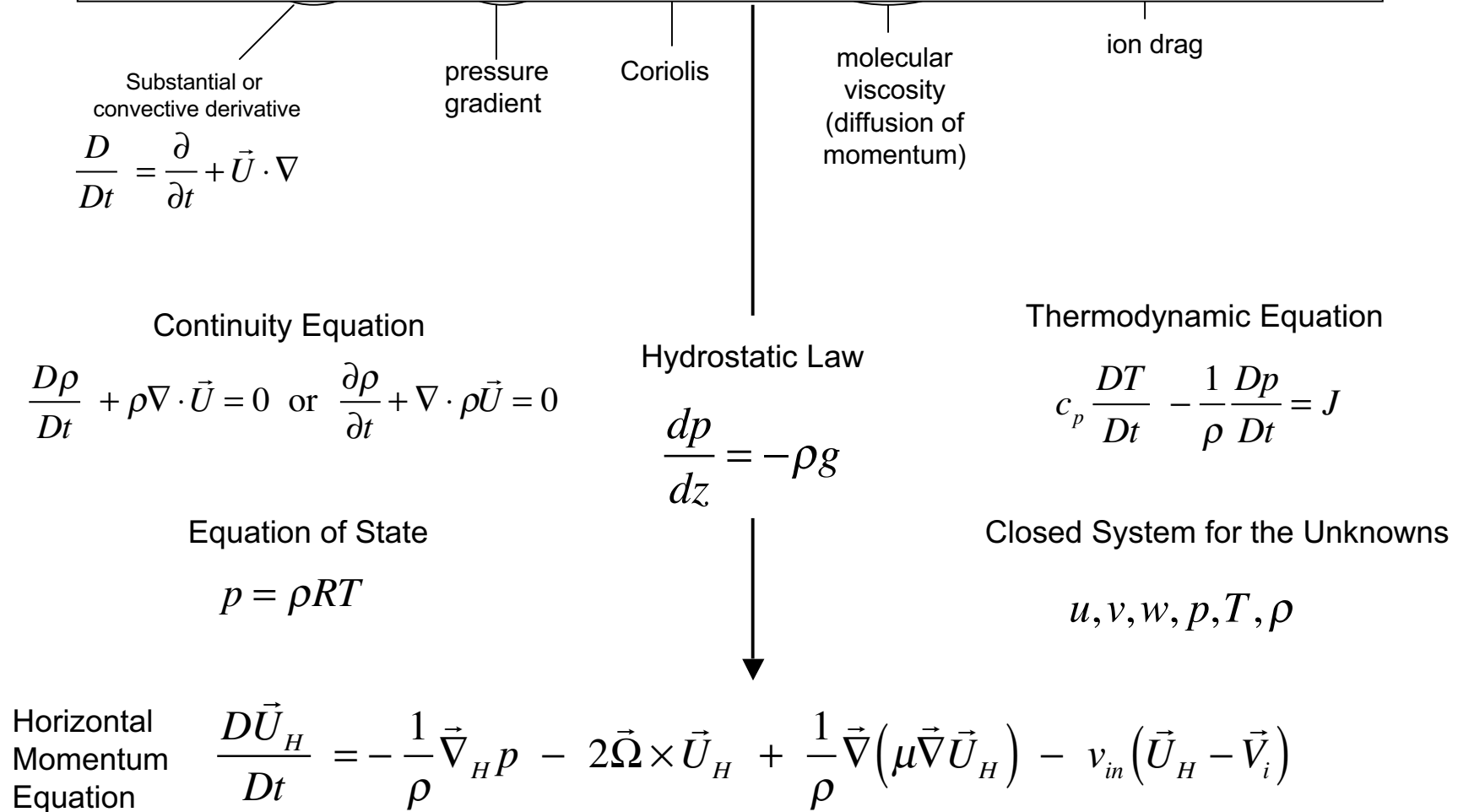
# The ITM System



# Momentum Balance

# Governing Equations

These equations are written in terms of total density & pressure; in practice, must actually consider multi-component equations, and self-consistent coupling between neutral species, and coupling with ionospheric and electrodynamic equations



By considering conservation of mass above a constant pressure surface,  $p_0$  (Dickinson & Geisler, 1968), it can be shown that the total vertical wind may be expressed in terms of two components, the **barometric** wind and the **divergence** wind. The former is due to thermal expansion/contraction of the atmosphere, the latter is caused by diverging horizontal winds and the conservation of mass:

$$w = w_B + w_D = \left( \frac{\partial h}{\partial t} \right)_p + \frac{1}{\rho} \nabla \cdot \int_{h(p_0)}^{\infty} \rho \vec{U}_H dz$$

They furthermore show that  $w_D = -\frac{1}{\rho g} \frac{Dp}{Dt}$  (Vertical motion of air with respect to a fixed pressure surface )

so that the thermodynamic equation  $c_p \frac{DT}{Dt} - \frac{1}{\rho} \frac{Dp}{Dt} = J$  ( $J$  is NET heating from all sources, including conduction)

becomes  $c_p \frac{DT}{Dt} + gw_D = J$

$$c_p \frac{DT}{Dt} + gw_D = J$$

To a first approximation, to explain vertical structure, one can linearize about a mean basic state dependent only on height (overbar);  $w\text{-bar} = 0$

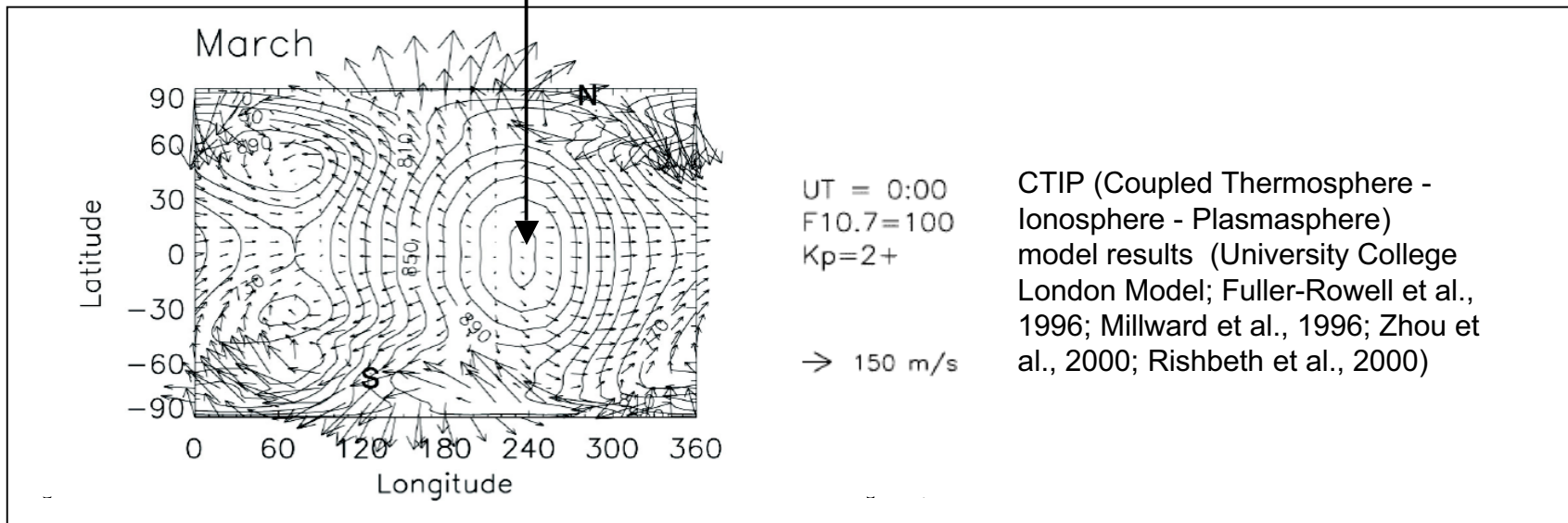
$$\frac{DT}{Dt} \approx \frac{\partial T}{\partial t} + w_D \frac{\partial \bar{T}}{\partial z} \longrightarrow \frac{\partial T}{\partial t} = \frac{J}{c_p} - w_D \Gamma$$

An additional "heat source" as important as direct EUV heating.

$$\Gamma = \frac{\partial \bar{T}}{\partial z} + \frac{g}{c_p}$$

is the mean atmospheric stability

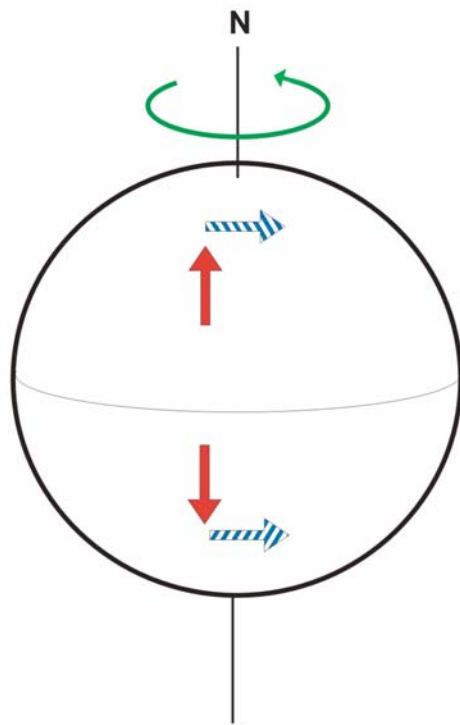
Accounts for much of the observed shift in the time of temperature maximum to late afternoon.



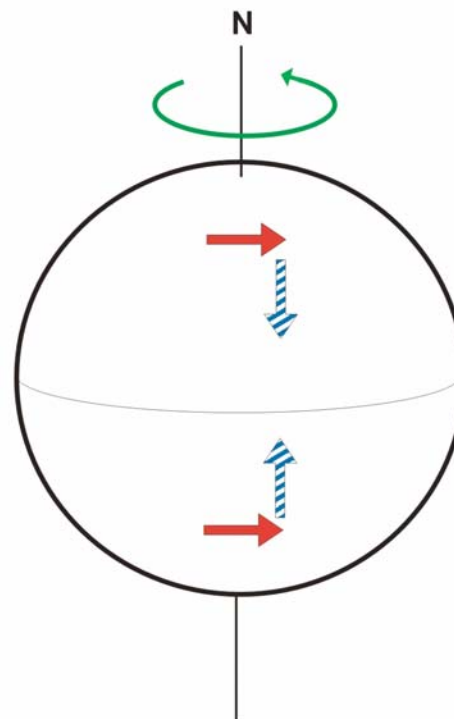
$$\frac{D\vec{U}_H}{Dt} = -\frac{1}{\rho} \vec{\nabla}_H p - 2\vec{\Omega} \times \vec{U}_H + \frac{1}{\rho} \vec{\nabla}(\mu \vec{\nabla} \cdot \vec{U}_H) - v_{in}(\vec{U}_H - \vec{V}_i)$$

 Wind flow  
 Coriolis force

**Coriolis force** acts **perpendicular** to the **wind vector**. It deflects poleward winds towards the east and eastward winds equatorward. So, winds are driven clockwise (anticlockwise) in the northern (southern) hemisphere around pressure minima.



Meridional wind flow

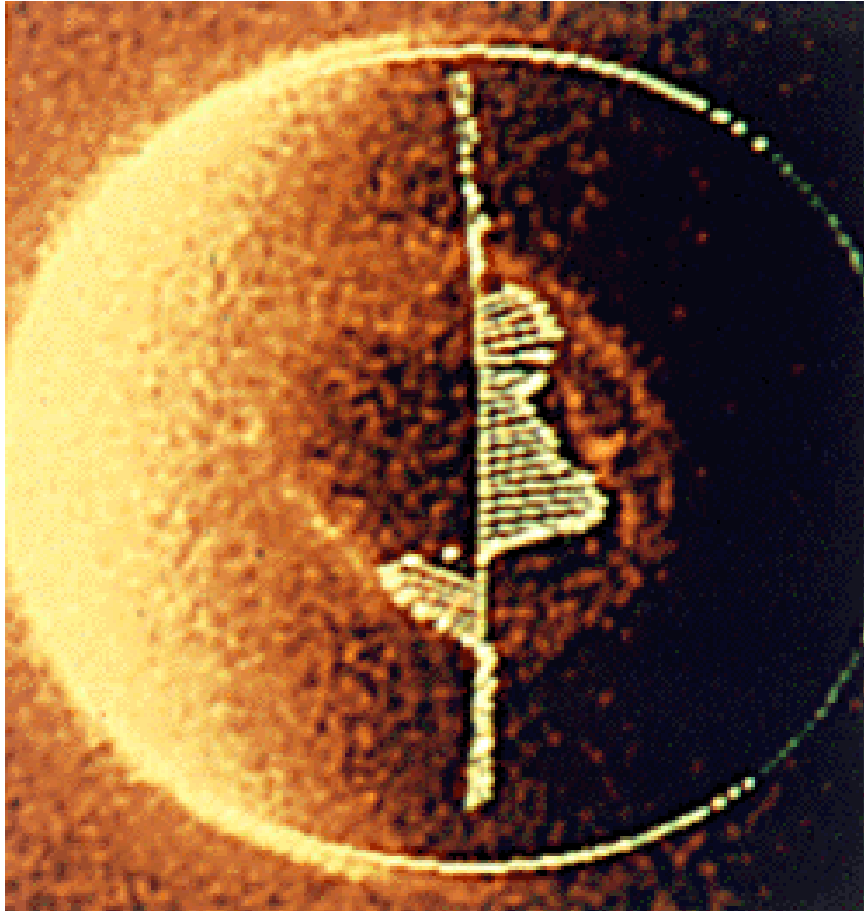


Zonal wind flow

Near steady-state flow below about 150 km is usually involves approximate balance between the pressure gradient and Coriolis forces, leading to the **geostrophic approximation**, where the flow is **parallel to the isobars** (clockwise flow around a **High** in the Northern Hemisphere)



$$\frac{D\vec{U}_H}{Dt} = -\frac{1}{\rho}\vec{\nabla}_H p - 2\vec{\Omega}\times\vec{U}_H + \left(\frac{1}{\rho}\vec{\nabla}(\mu\vec{\nabla}\vec{U}_H)\right) - v_{in}(\vec{U}_H - \vec{V}_i)$$



Neutral winds and auroral oval from Dynamics Explorer measurements (Killeen et al., 1988)

ence of any ion drifts ( $V_i = 0$ ), the  
of ions that are bound to  
field lines act to decelerate the  
nd, due to neutral-ion collisions.

If the ion-neutral collision  
frequency is sufficiently  
large, and if the ion drift  
is sufficiently large and  
acts over a sufficient  
length of time, then the  
neutral gas circulation will  
begin to mirror that of the  
plasma.

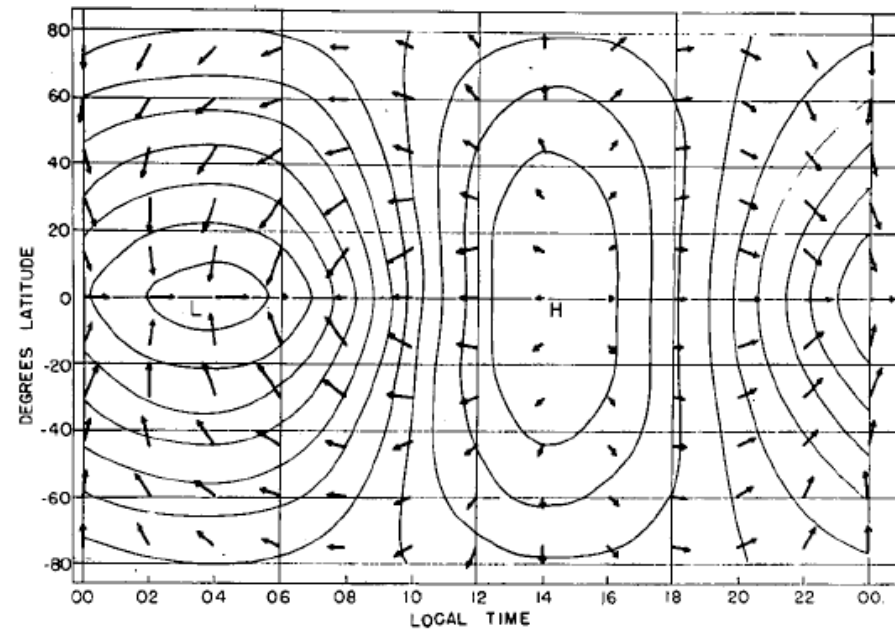
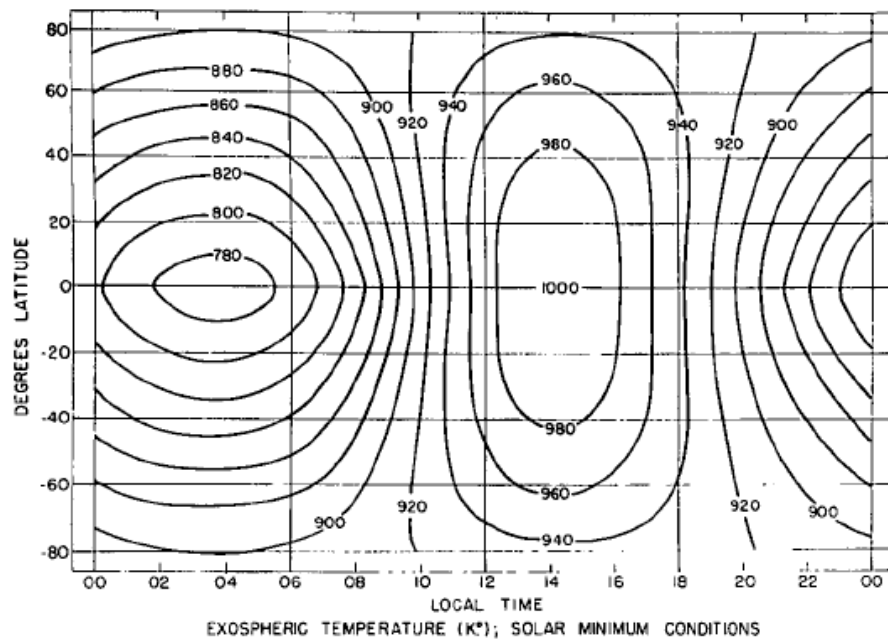
$$\frac{D\vec{U}_H}{Dt} = -\frac{1}{\rho}\vec{\nabla}_H p - 2\vec{\Omega}\times\vec{U}_H + \frac{1}{\rho}\vec{\nabla}(\mu\vec{\nabla}\vec{U}_H) - v_{in}(\vec{U}_H - \vec{V}_i)$$

In the upper thermosphere, balance between pressure gradient, ion drag, and viscous diffusion tends to prevail, such that the flow is **across the isobars**.

September 1968

R. E. Dickinson and J. E. Geisler

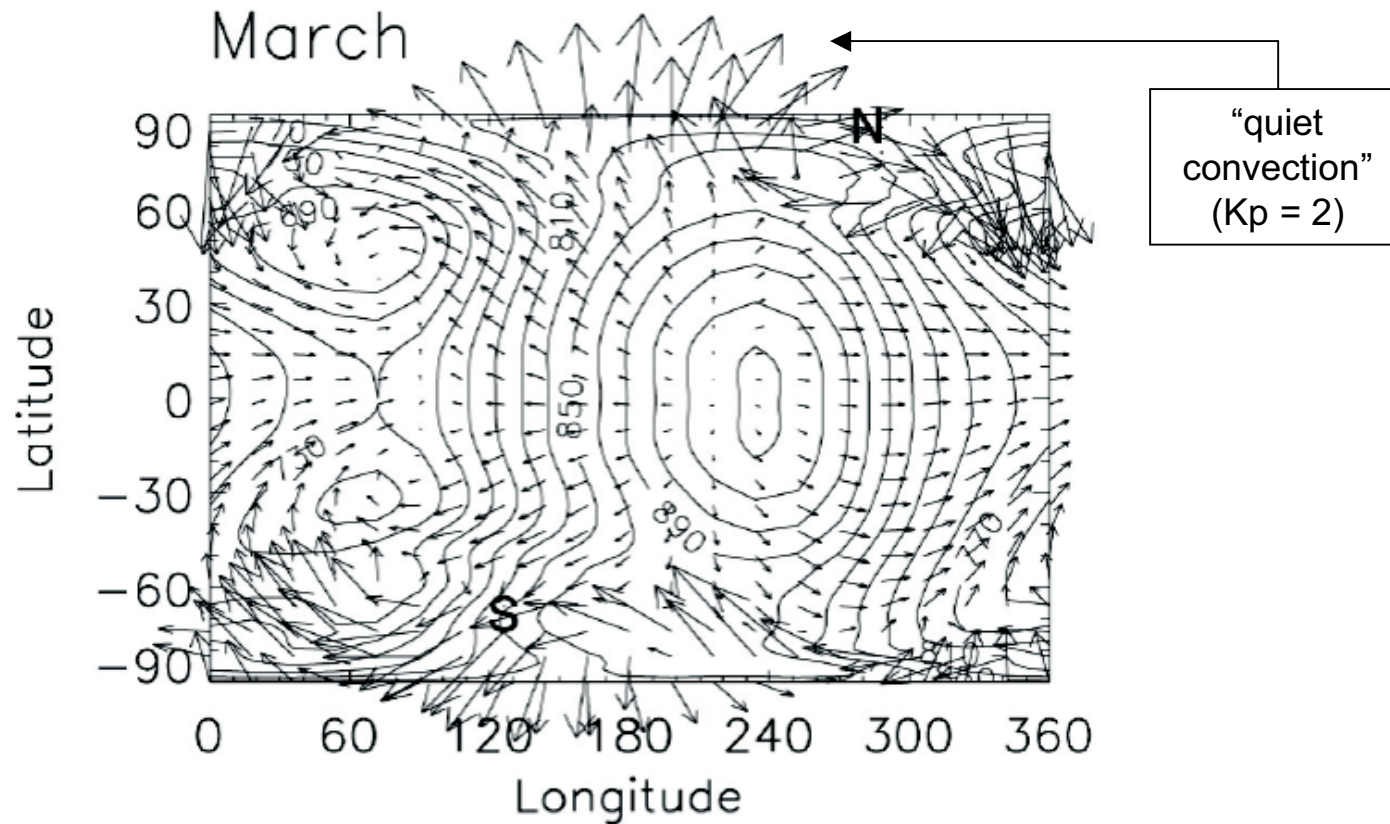
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Exospheric Temperatures from Jacchia 1965 model, used with model densities to derive pressures and pressure gradients

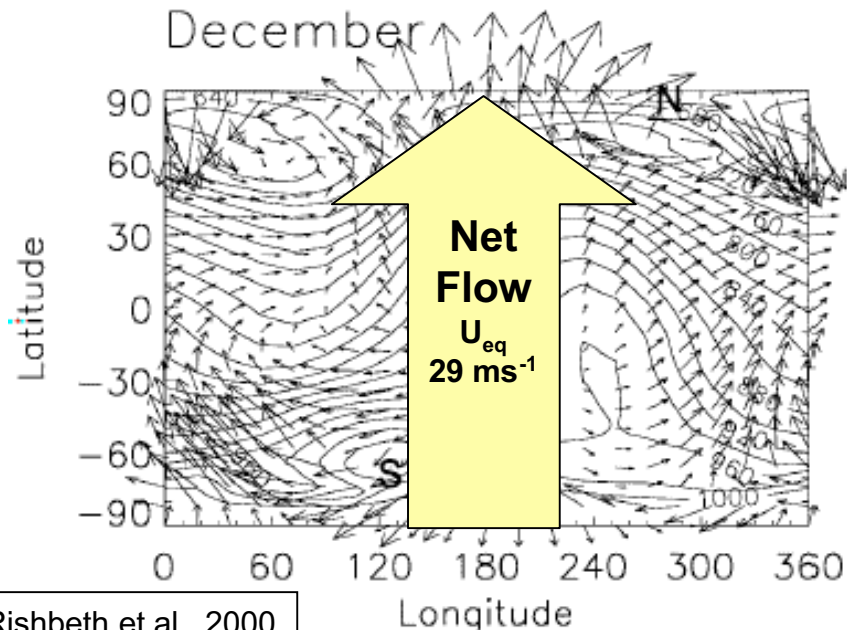
Wind vectors calculated from momentum equation with Jacchia 1965 pressure gradient forcing. Isobars are shown by solid lines

The gross features of this early work are consistent with those embodied in the more recent CTIP modeling



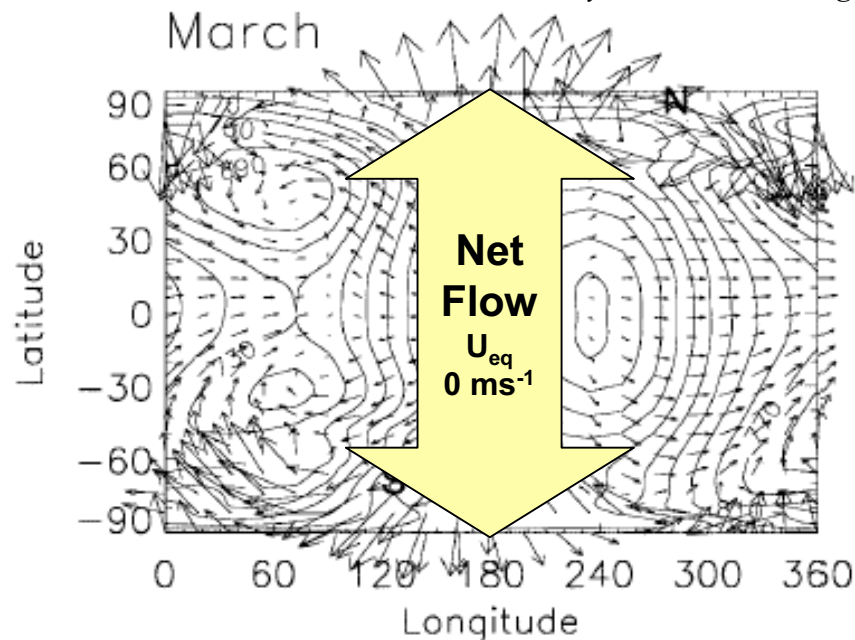
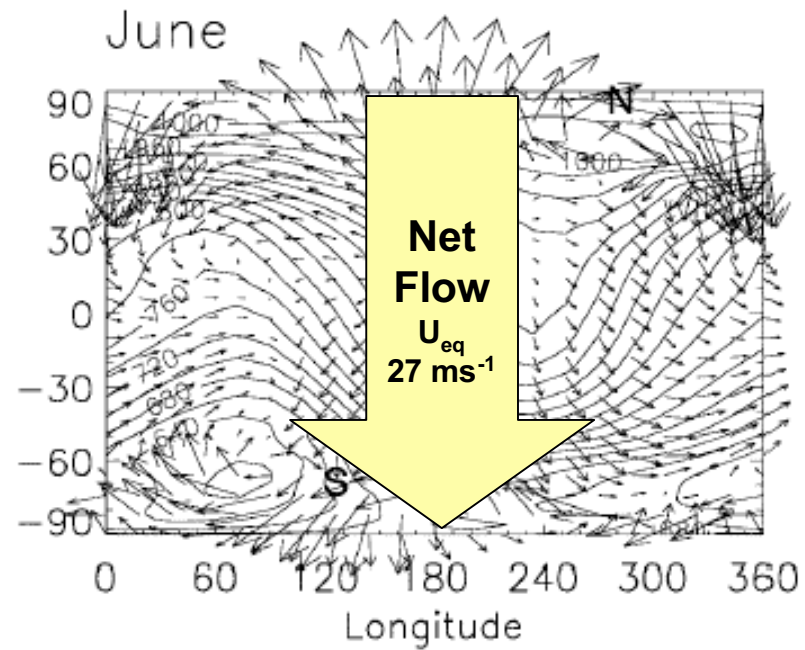
Exospheric temperatures peak near **15:30 h** local time.  
Day-night temperature differences at low latitudes reach around **200 K**.

# Predominantly EUV-Driven Circulation



Rishbeth et al., 2000

Courtesy I. Mueller-Wodarg



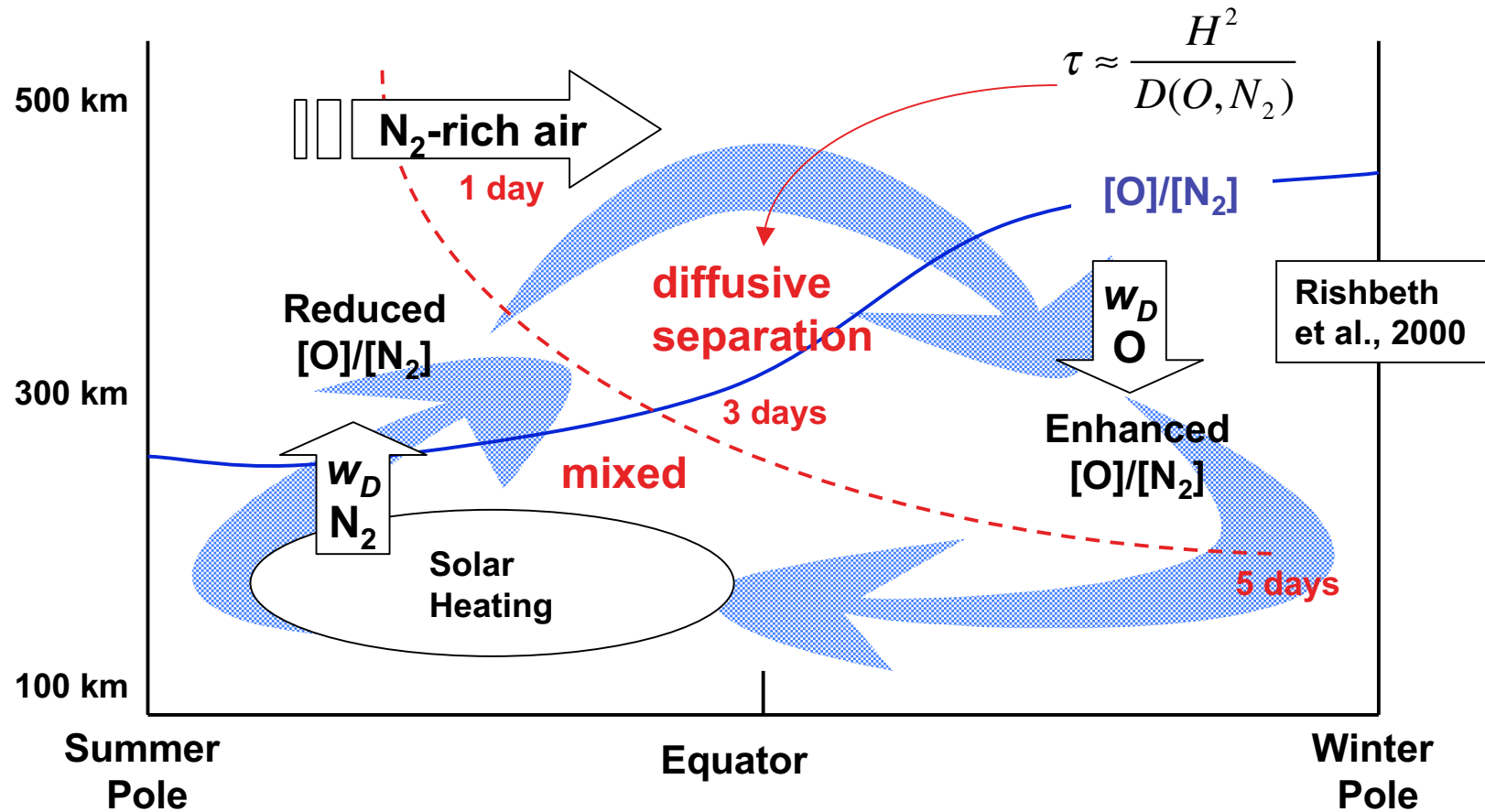
**Winds flow essentially from the summer to the winter hemisphere.**

**At equinox winds are quasi-symmetric, from the equator towards the poles.**

**Polar winds are strongly controlled by ion drag**

# Winds and Composition: Seasonal Variations

# Solar EUV-Driven (Magnetically-Quiet) Circulation and O-N<sub>2</sub> Composition



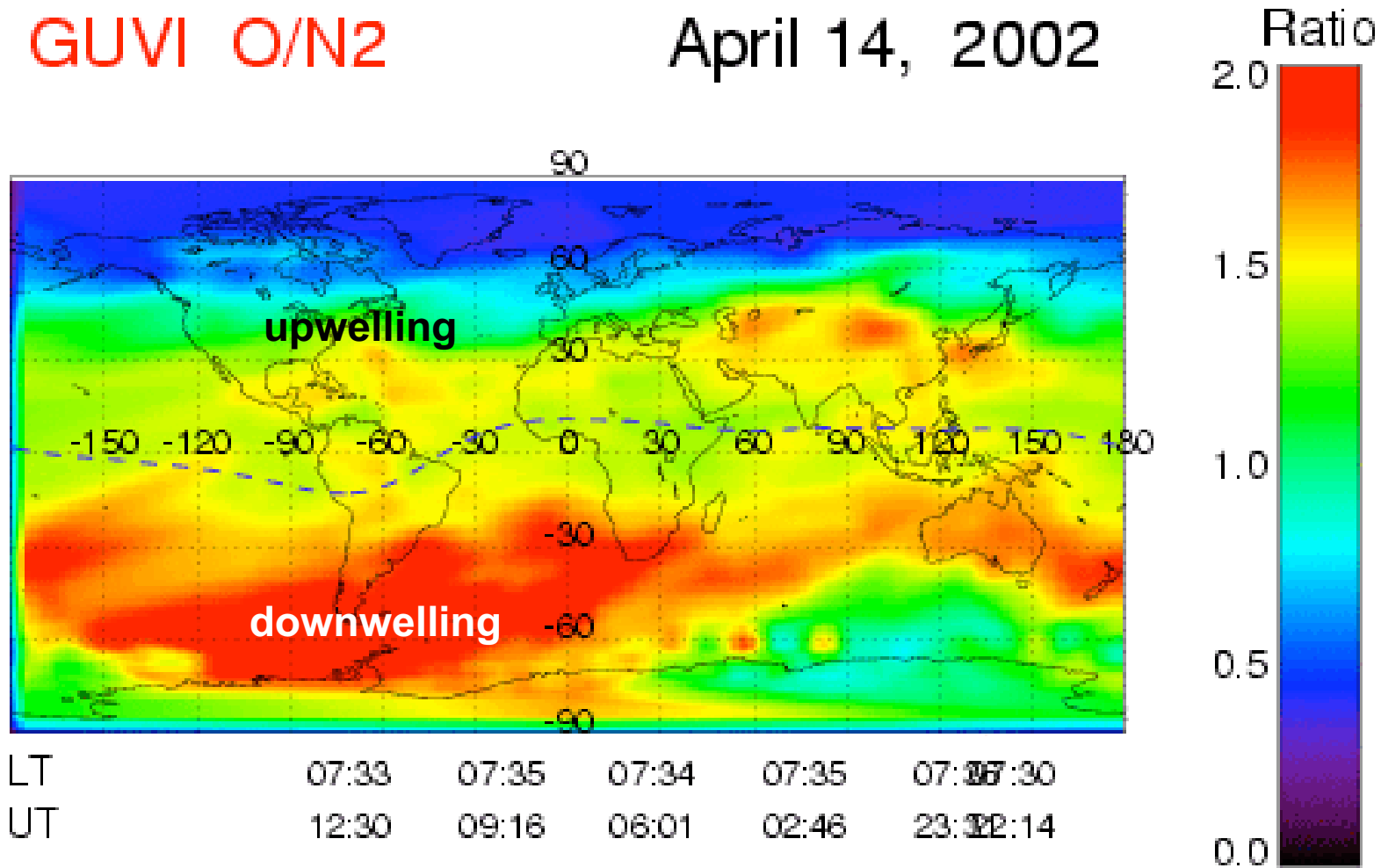
Upwelling occurs in the summer hemisphere, which upsets diffusive equilibrium.

Molecular-rich gases are transported by horizontal winds towards the winter hemisphere, where diffusive balance is progressively restored, from top (where diffusion is faster) to bottom

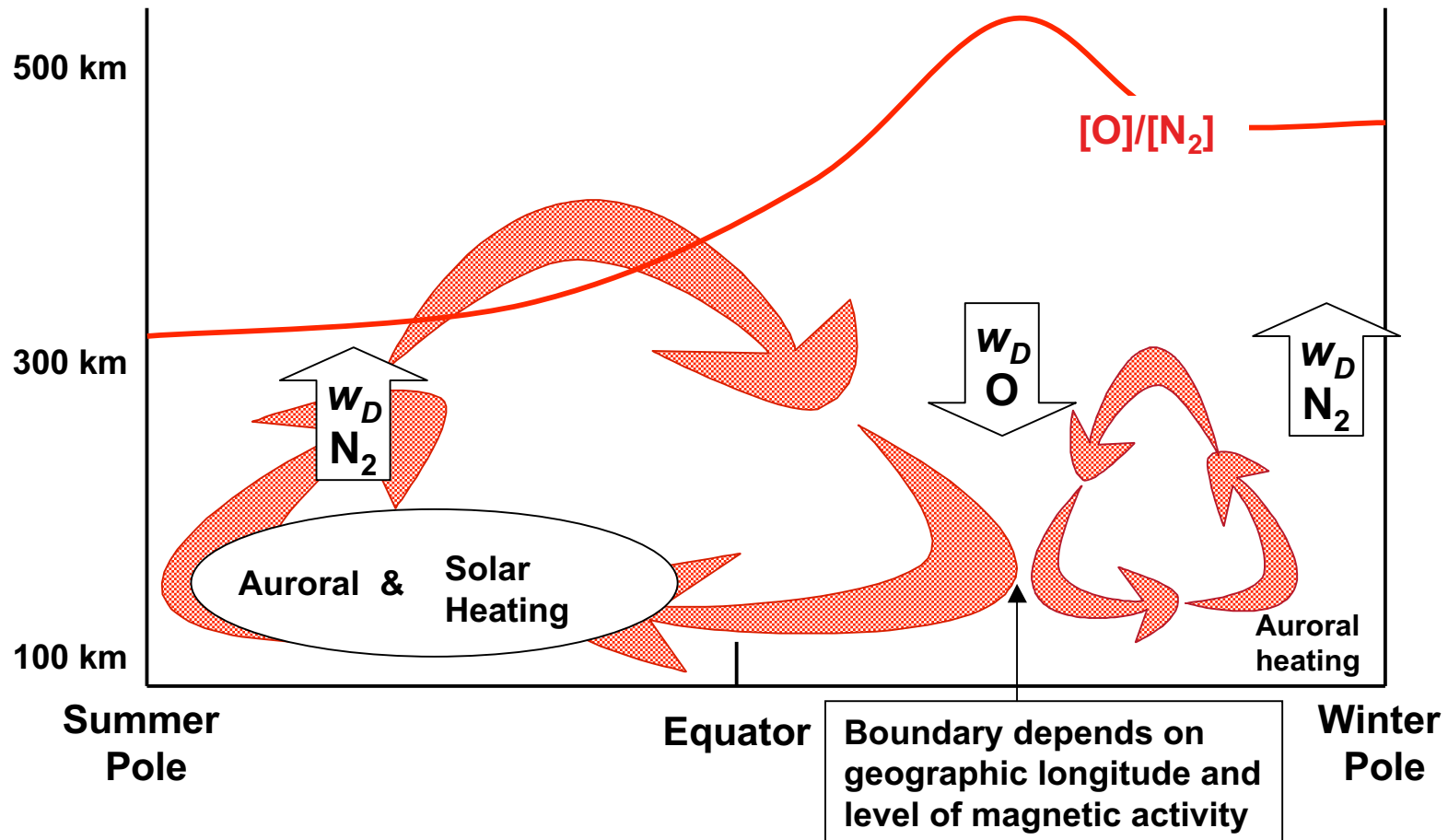
# Shift Between “Summer” and “Winter” Occurs in a Short Period Around Equinox

**GUVI O/N2**

**April 14, 2002**



# Solar EUV & Aurorally-Driven Circulation and O-N<sub>2</sub> Composition



A secondary circulation cell exists in the winter hemisphere due to upwelling driven by aurora heating. The related O/N<sub>2</sub> variations play an important role in determining annual/semiannual variations of the thermosphere & ionosphere.



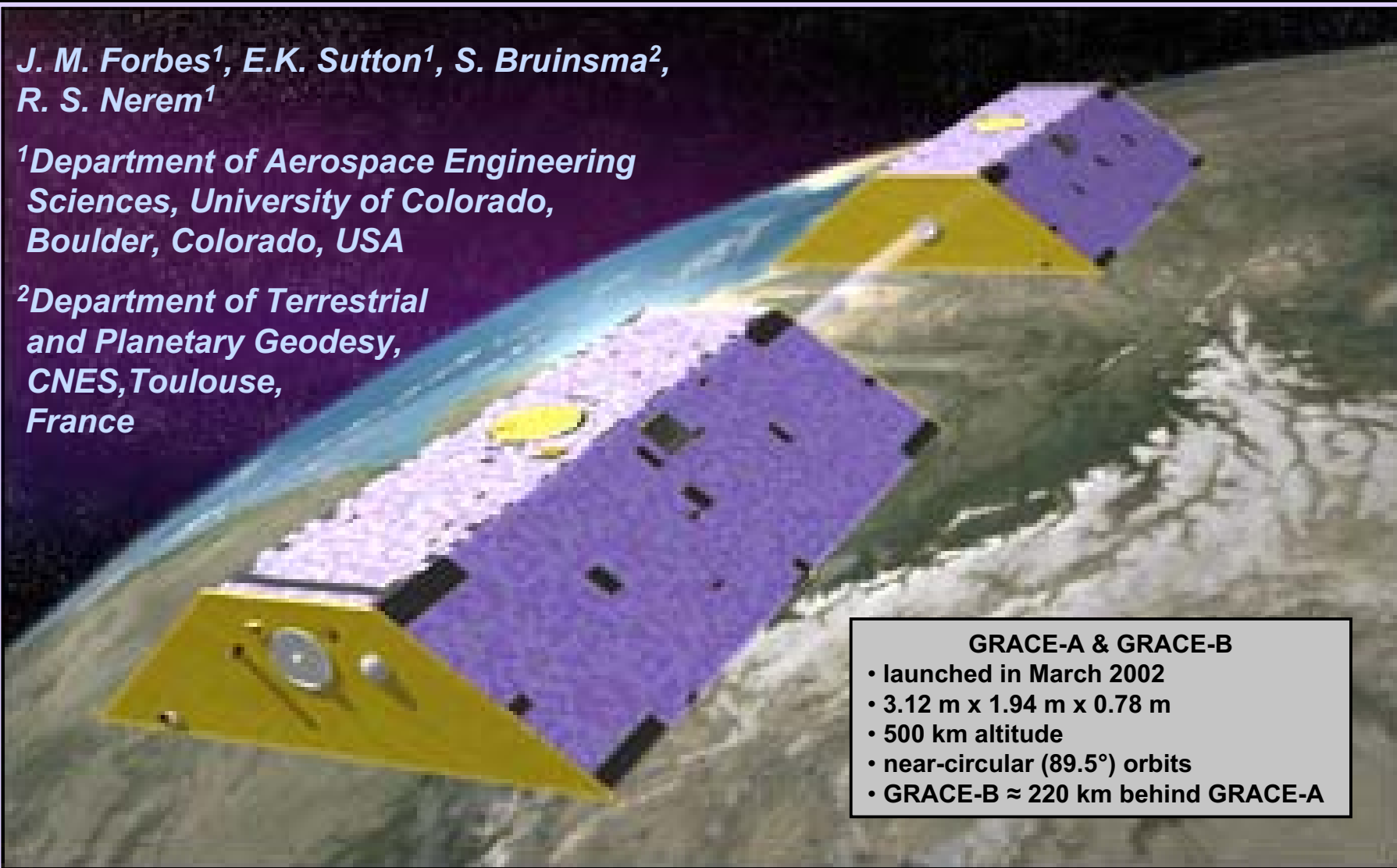
# Thermosphere Weather: Magnetic Storm Response

# Solar-Terrestrial Coupling Effects in the Thermosphere: New Perspectives from CHAMP And GRACE Accelerometer Measurements of Winds And Densities

*J. M. Forbes<sup>1</sup>, E.K. Sutton<sup>1</sup>, S. Bruinsma<sup>2</sup>,  
R. S. Nerem<sup>1</sup>*

*<sup>1</sup>Department of Aerospace Engineering  
Sciences, University of Colorado,  
Boulder, Colorado, USA*

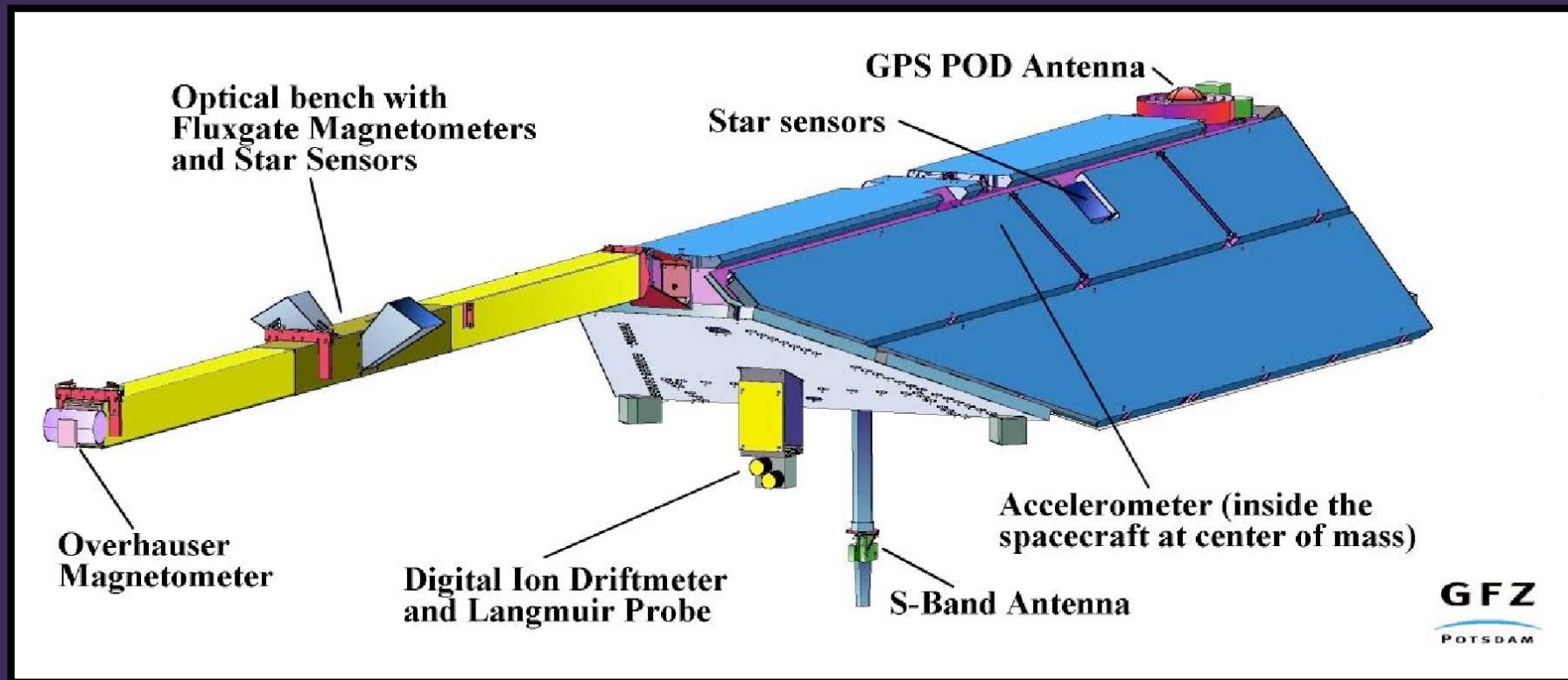
*<sup>2</sup>Department of Terrestrial  
and Planetary Geodesy,  
CNES, Toulouse,  
France*



## **GRACE-A & GRACE-B**

- launched in March 2002
- 3.12 m x 1.94 m x 0.78 m
- 500 km altitude
- near-circular (89.5°) orbits
- GRACE-B  $\approx$  220 km behind GRACE-A

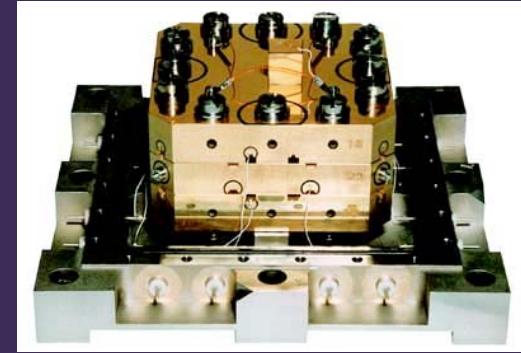
*The CHAMP satellite was launched in July 2000  
at 450 km altitude in a near-circular orbit  
with an inclination of 87.3°*



The physical parameters of the CHAMP satellite are:

- Total Mass 522 kg
- Length (with 4.044 m Boom) 8.333 m
- Area to Mass Ratio 0.00138 m<sup>2</sup>kg<sup>-1</sup>
- Height 0.750 m
- Width 1.621 m

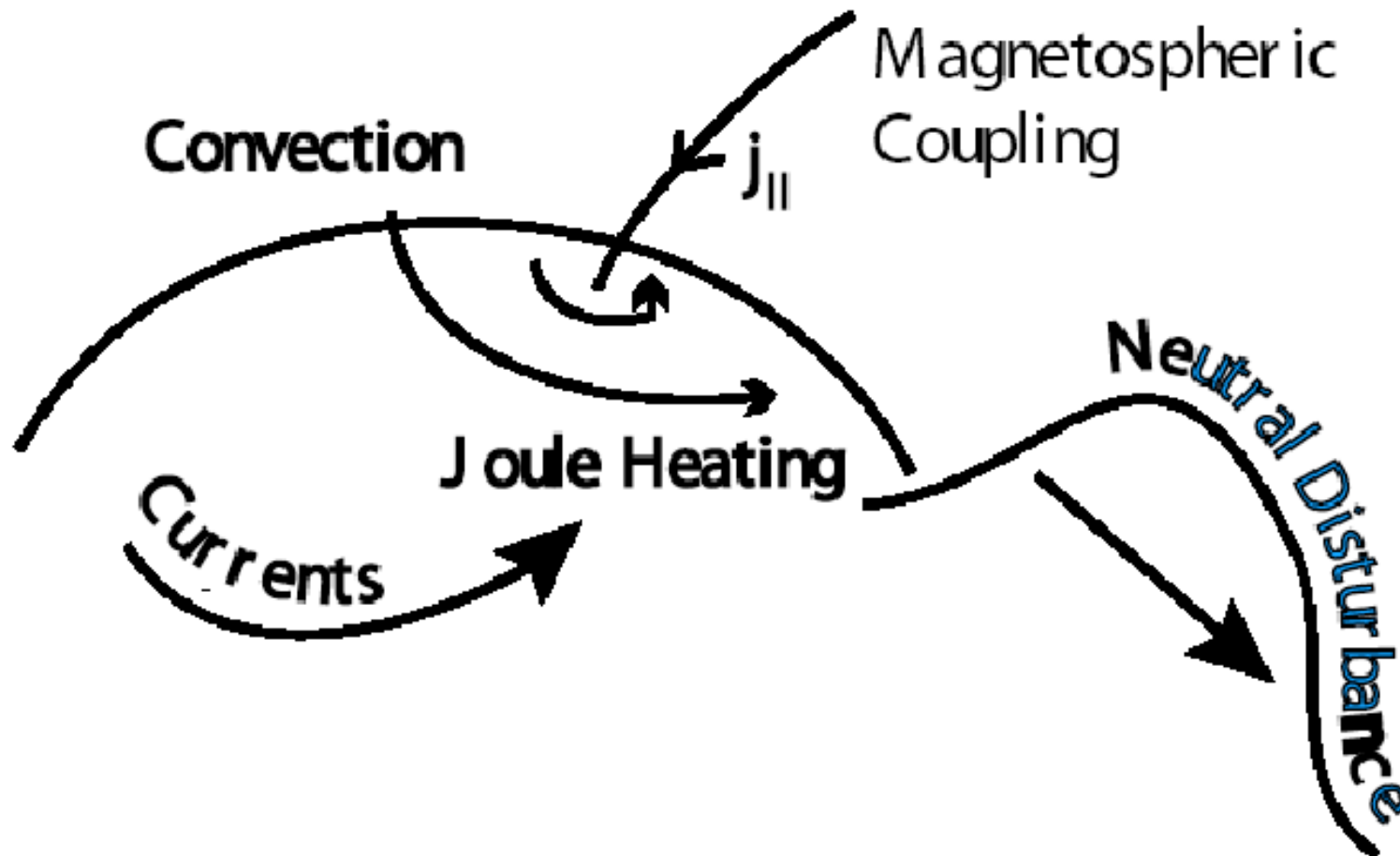
- ***Non-gravitational forces acting on the CHAMP and GRACE satellites are measured in the in-track, cross-track and radial directions by the STAR accelerometer***



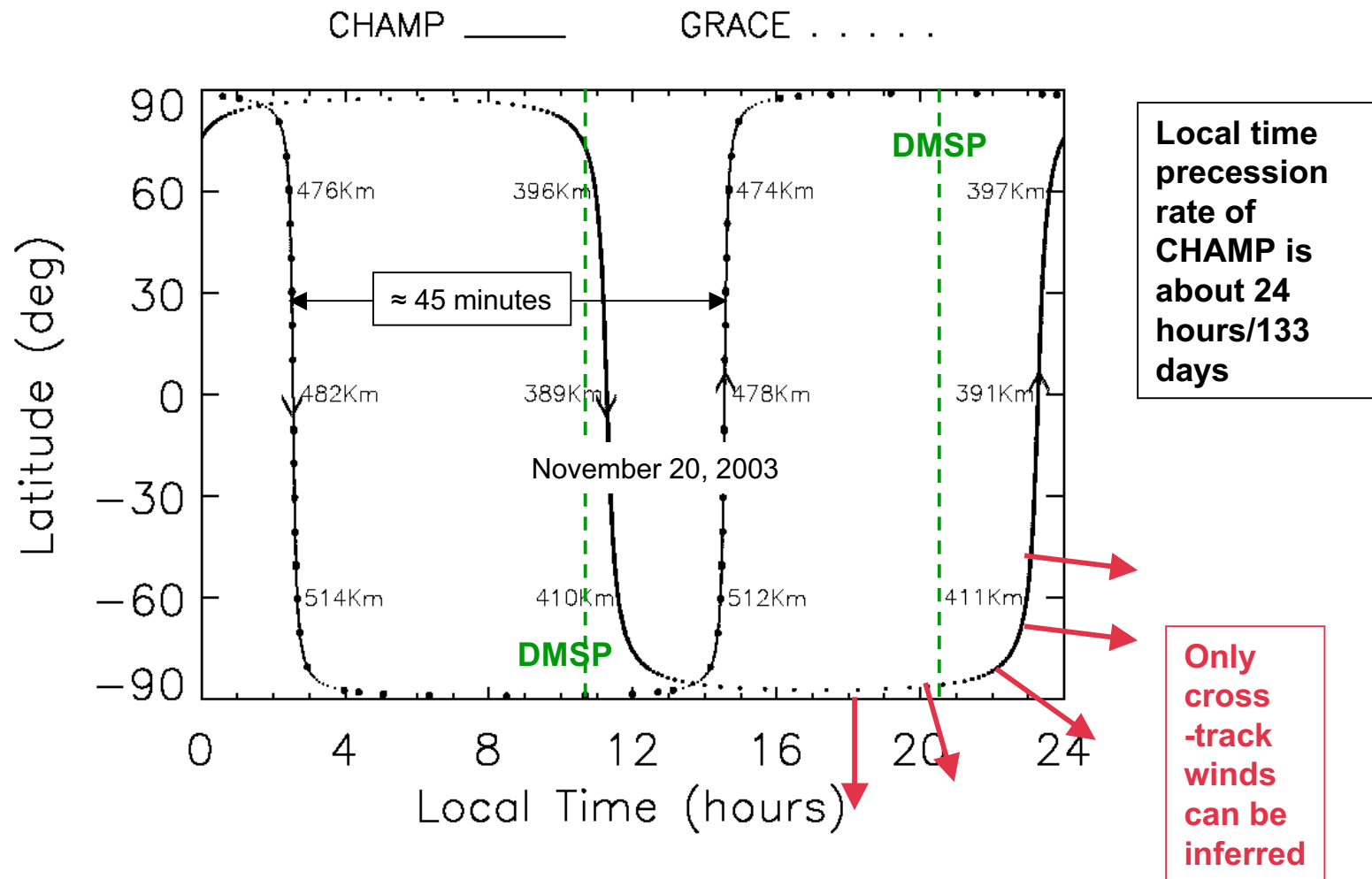
STAR accelerometer by Onera

- ***Separation of accelerations due to mass density (in-track) or winds (cross-track and radial) require accurate knowledge of***
  - » ***spacecraft attitude***
  - » ***3-dimensional modeling of the spacecraft surface (shape, drag coefficient, reflectivity, etc.)***
  - » ***accelerations due to thrusting***
  - » ***solar radiation pressure***
  - » ***Earth albedo radiation pressure***

# *CHAMP & GRACE in the Context of Magnetosphere-Ionosphere- Thermosphere Coupling*

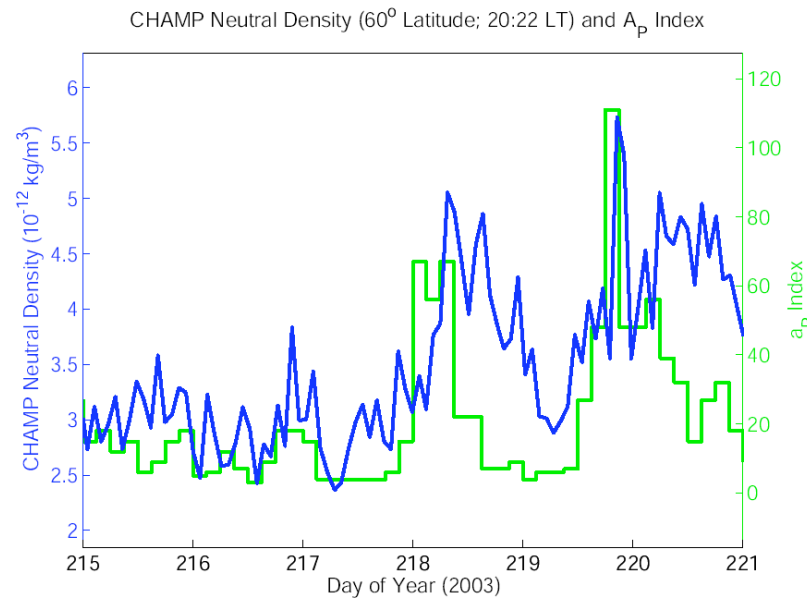
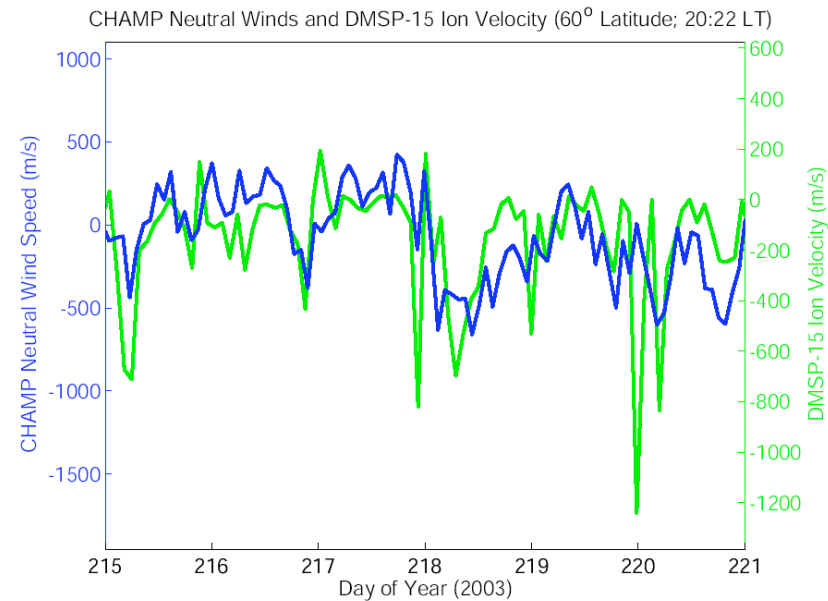


# ***CHAMP and GRACE offer new perspectives on thermosphere density response characterization: latitude, longitude, temporal and local time sampling***



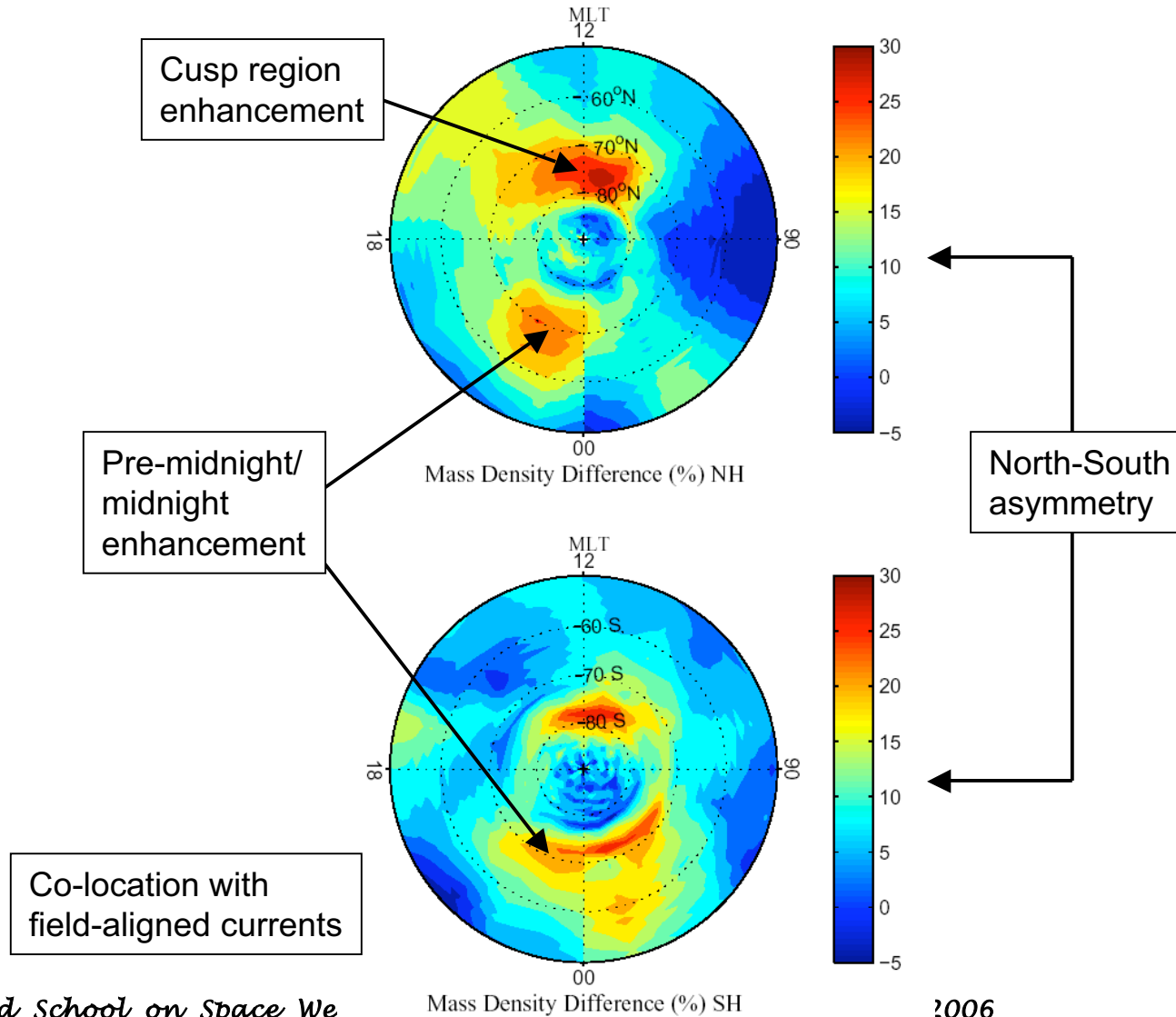
$$\frac{\partial \vec{U}_n}{\partial t} \sim -v_{in} (\vec{U}_n - \vec{V}_i) + \dots$$

CHAMP and GRACE orbits periodically intersect with those of the DMSP satellites, offering the opportunity to study ion-neutral coupling processes.



*Liu et al., JGR, 2005: "Global Distribution of the Thermospheric Mass Density Derived from CHAMP"*

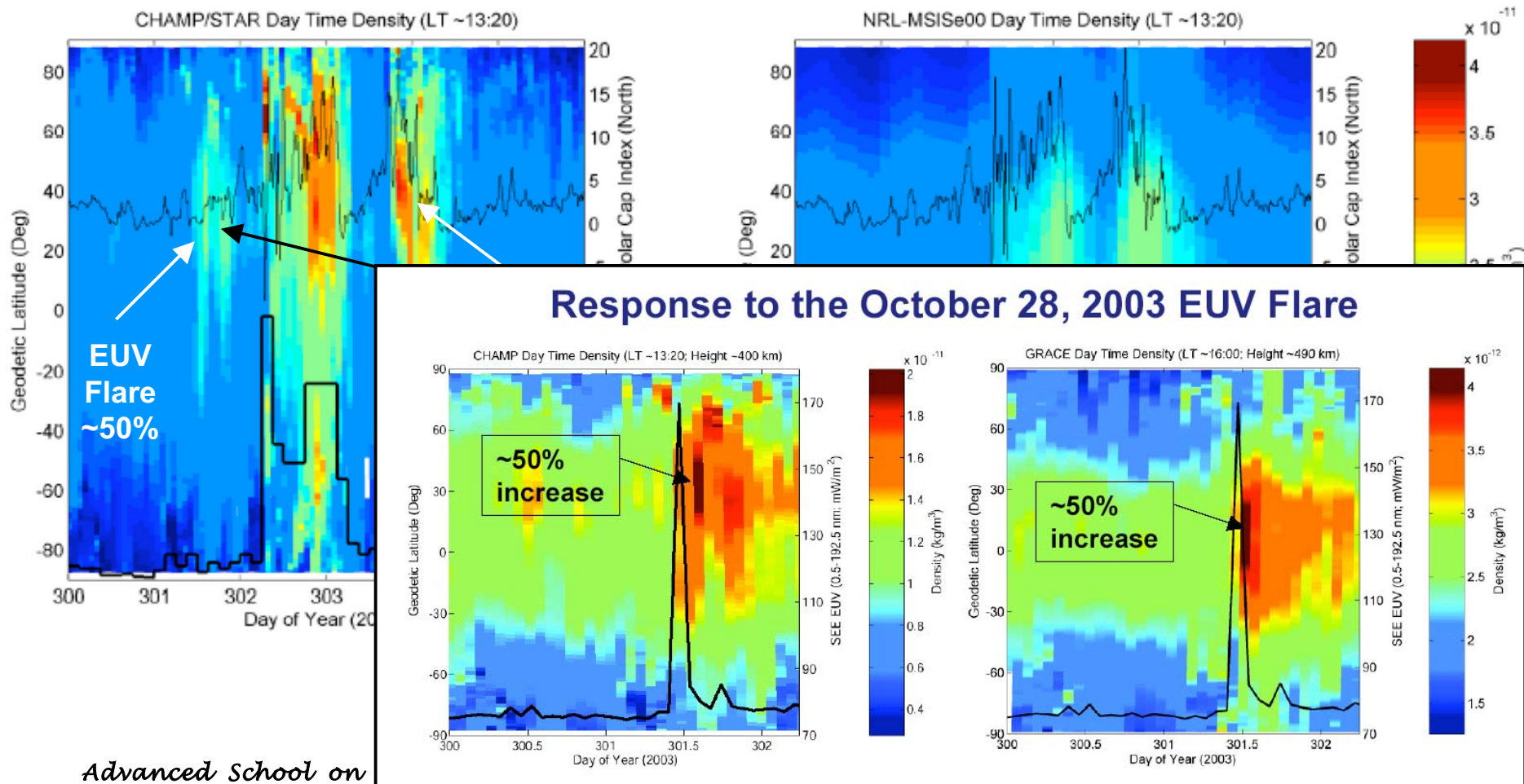
**Percent Differences from MSIS90 for  $K_p = 0-2$  during 2002  $> 50^\circ$  Latitude**



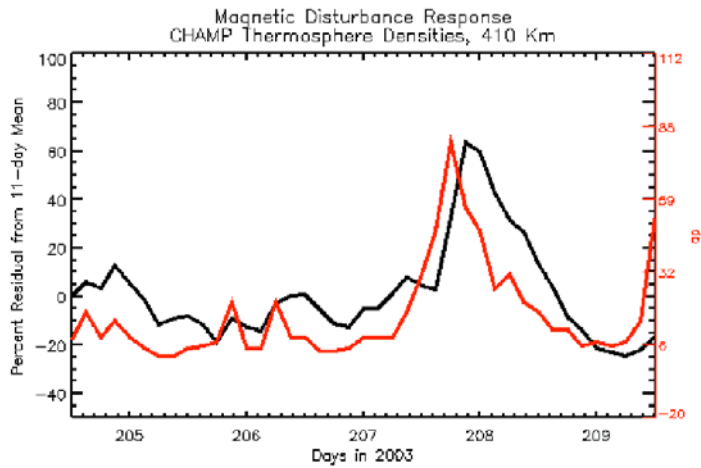
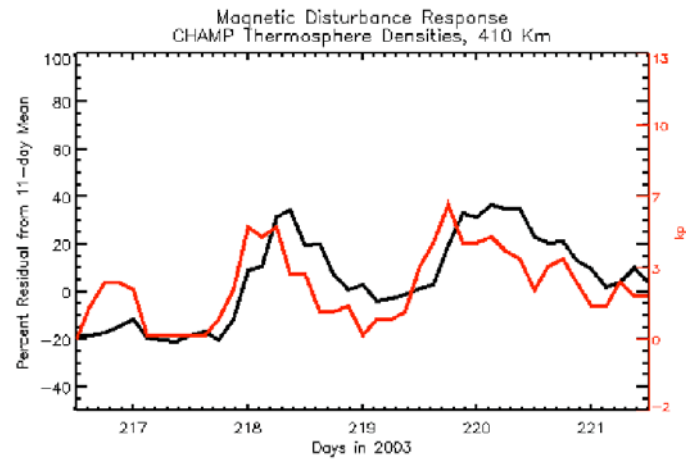


# Thermosphere Density Response to the October 29-31 2003 Storms from CHAMP Accelerometer Measurements

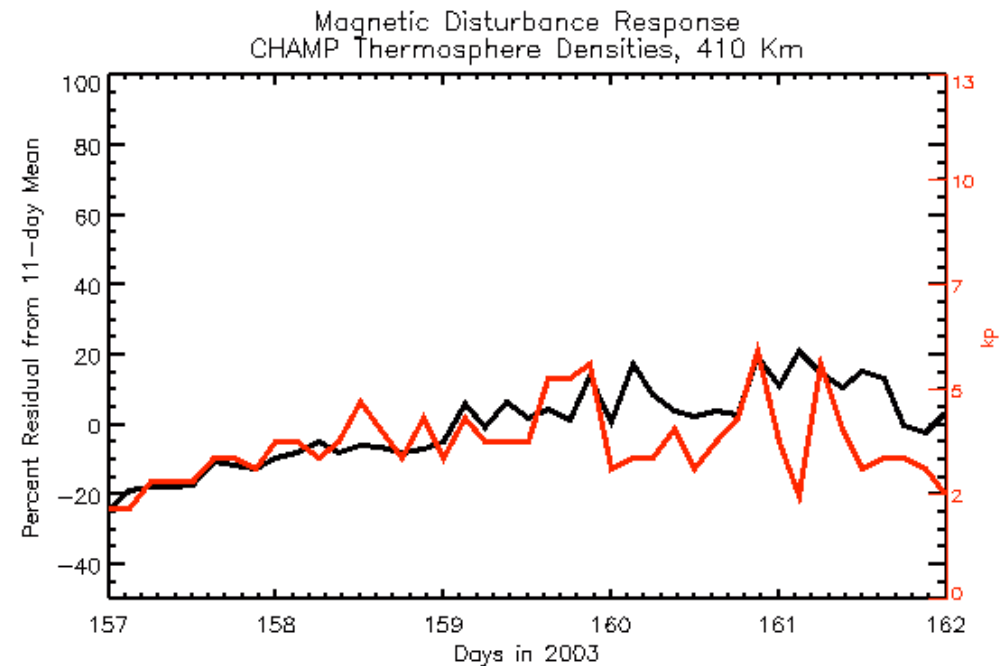
(Sutton et al., JGR, 2005)



# “Integrated (Orbit-Average) Response”



## 90-minute avg densities last half of 2003



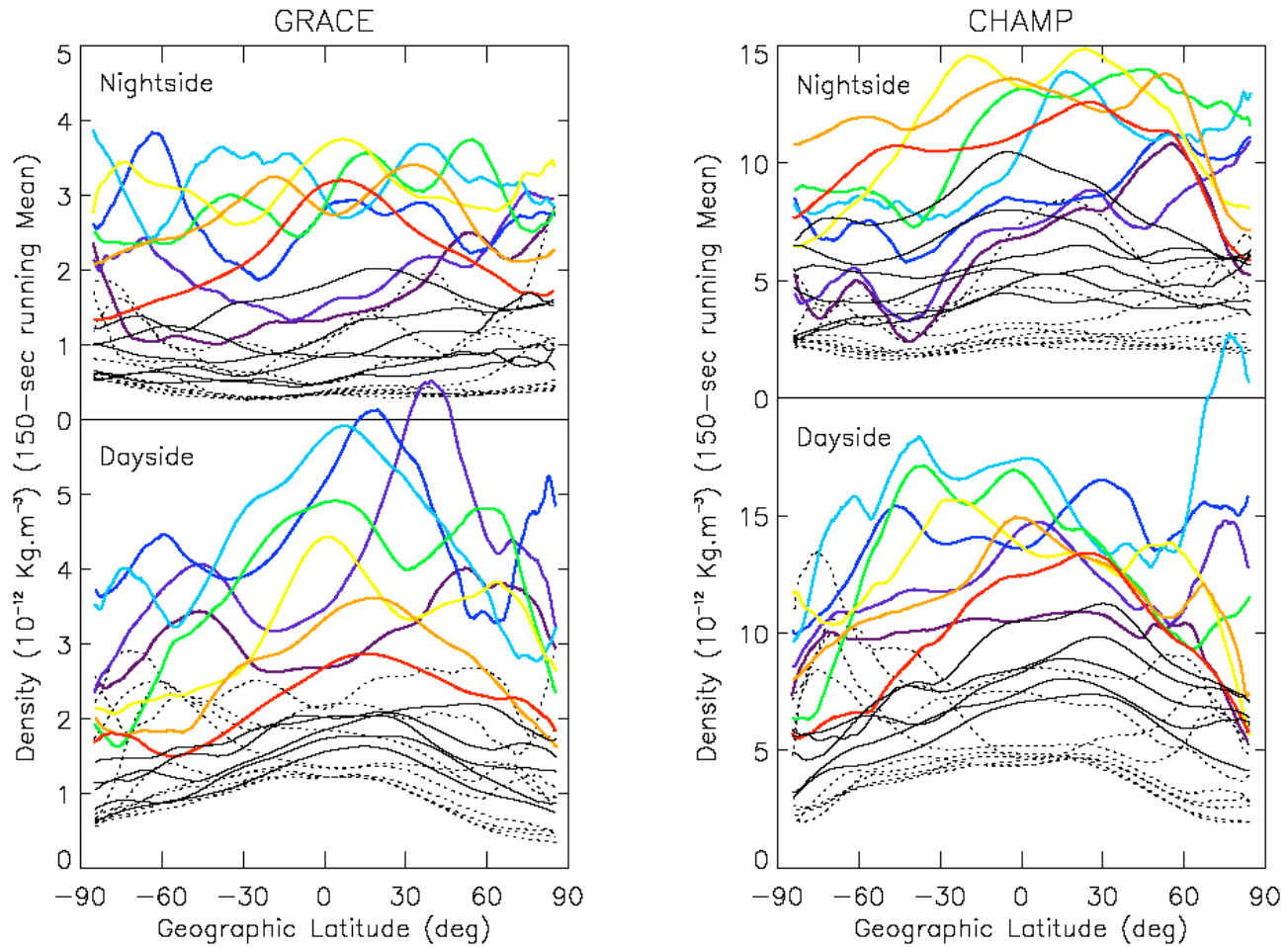
# November 19-21 2003 Storm

## Density Structures at Scales $> 1200$ km: “Large-Scale” Waves

.....  
before

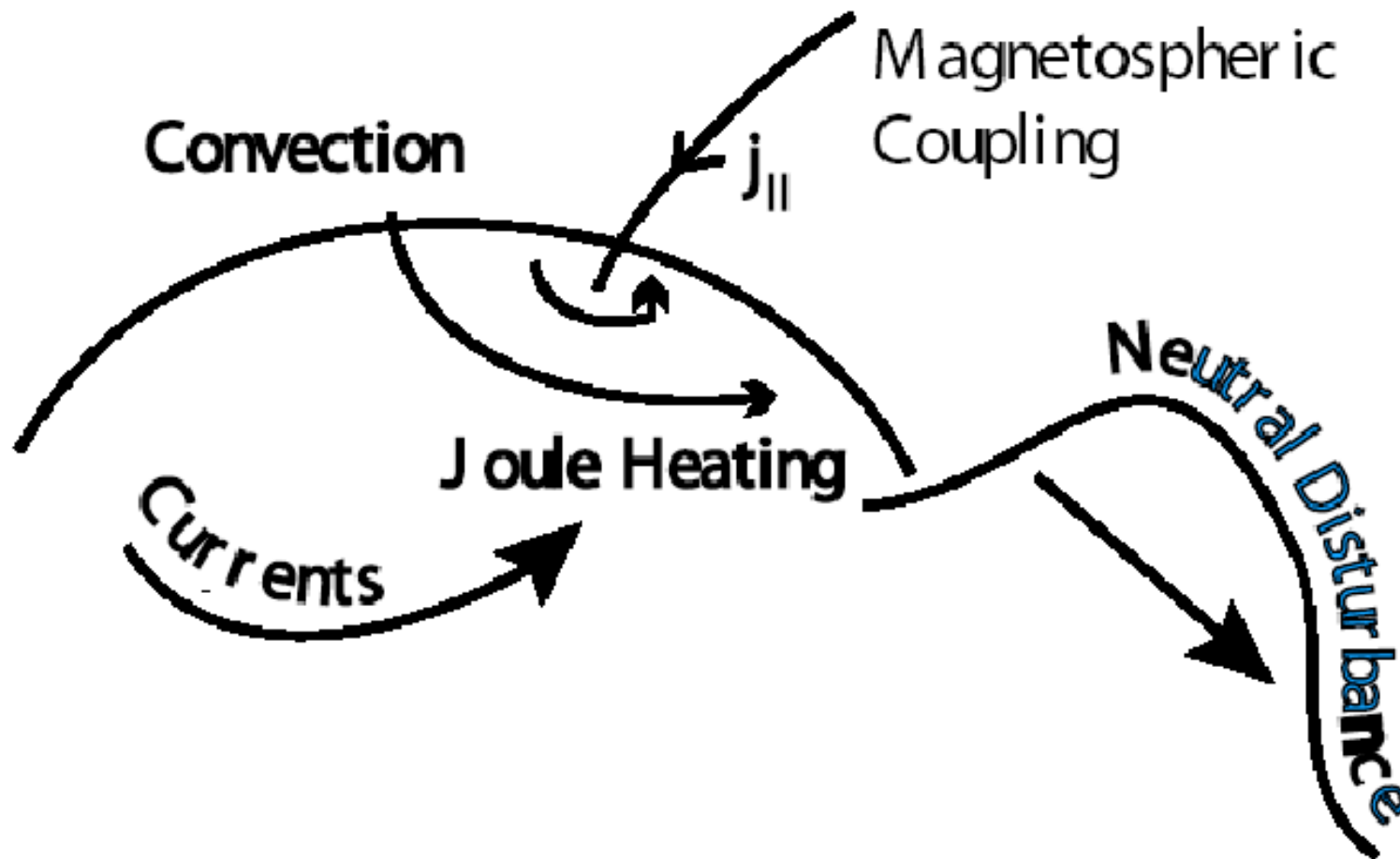
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after

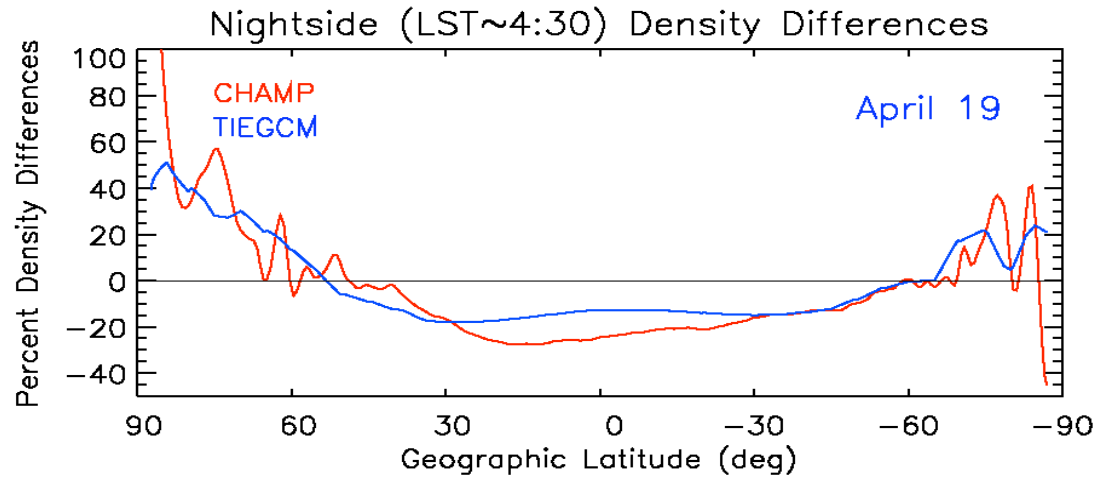


(150-sec (~1200 km) running means applied to raw data)

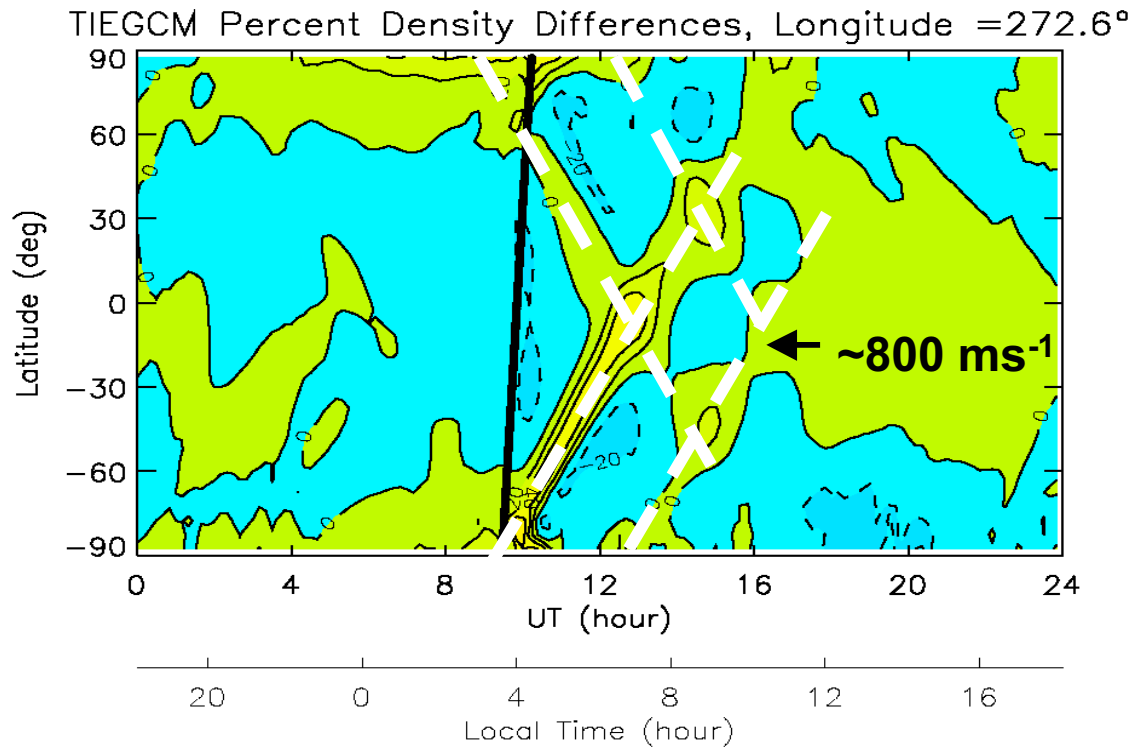
# Time Delay and Traveling Atmospheric Disturbances

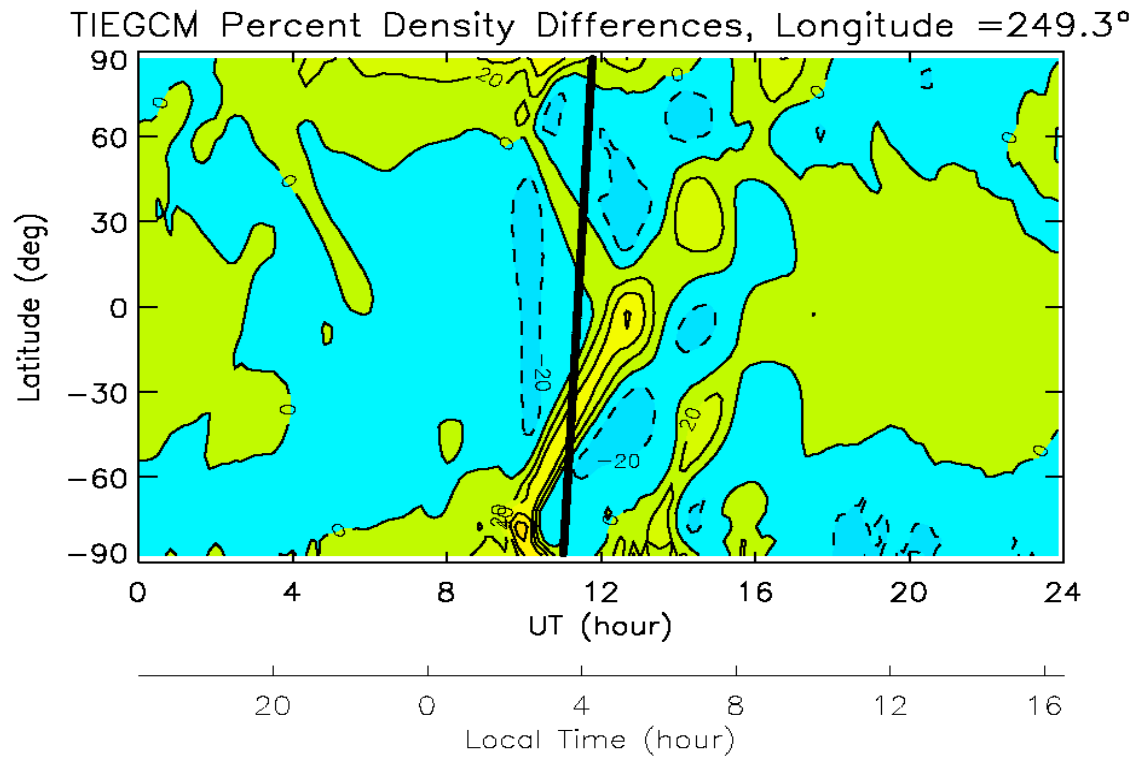
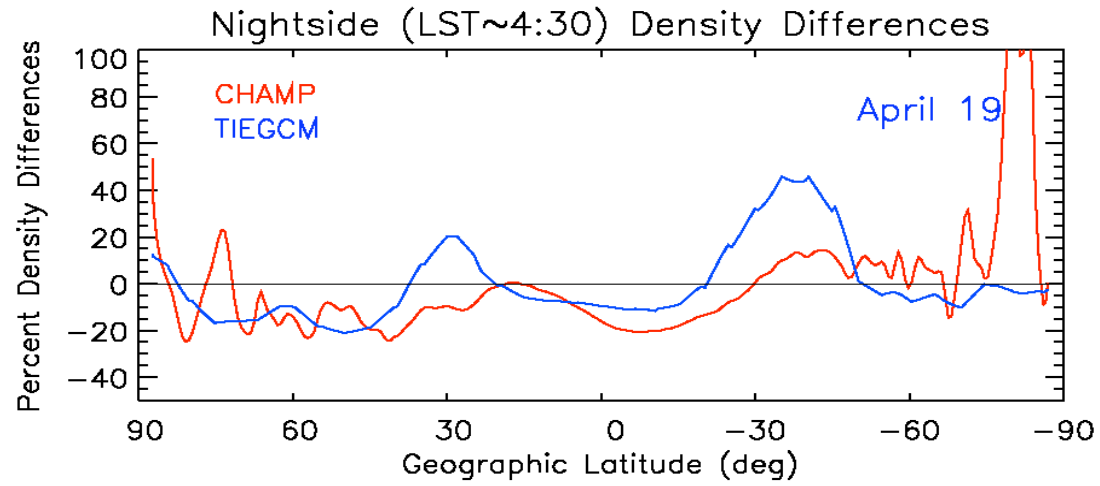


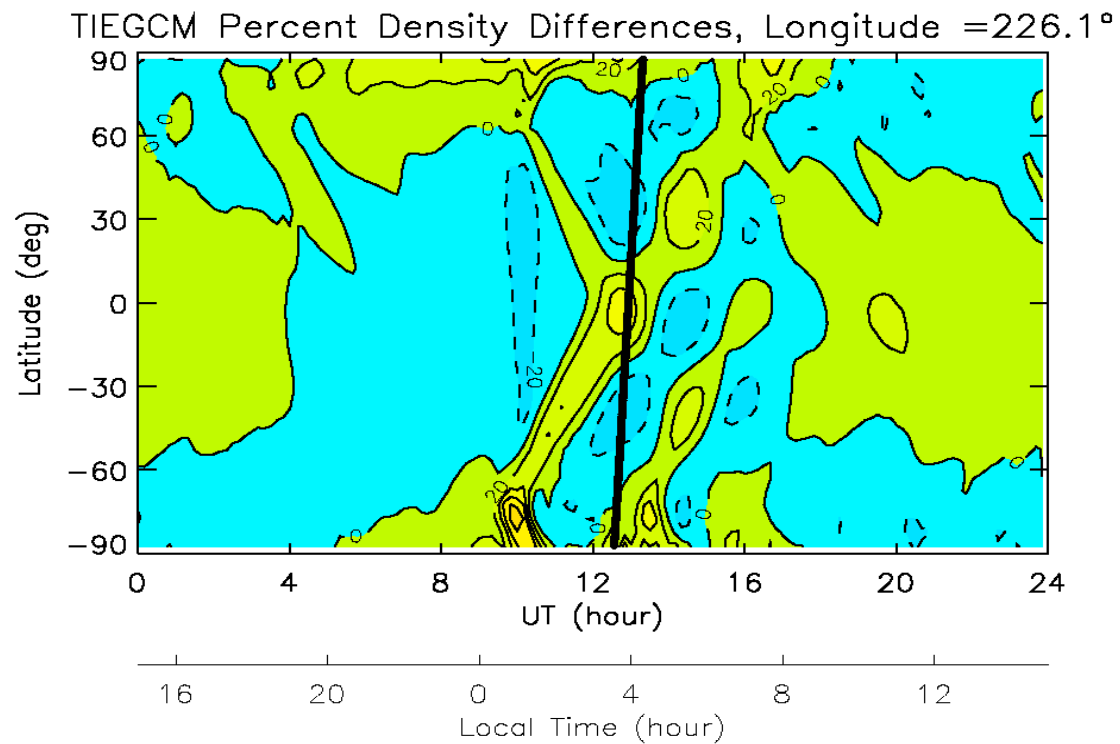
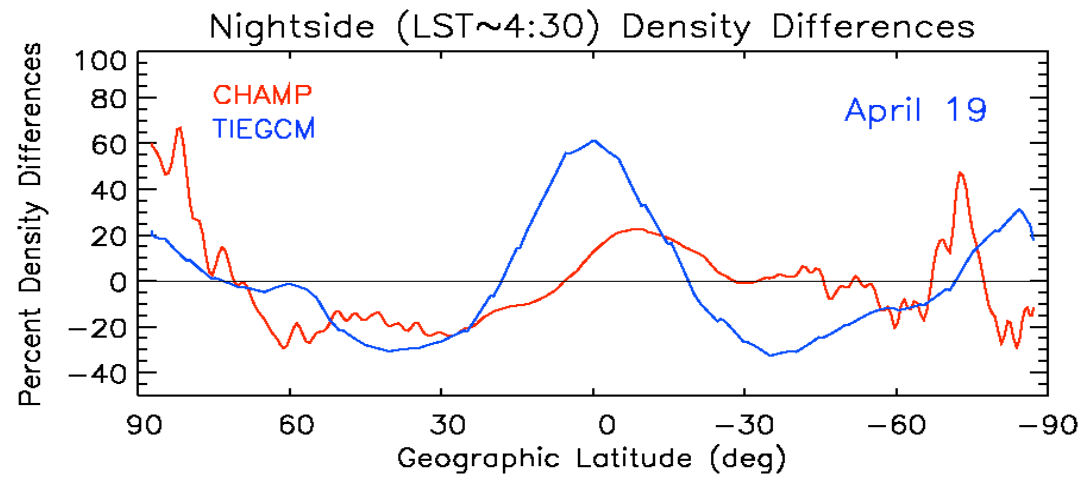
% density difference from orbit average

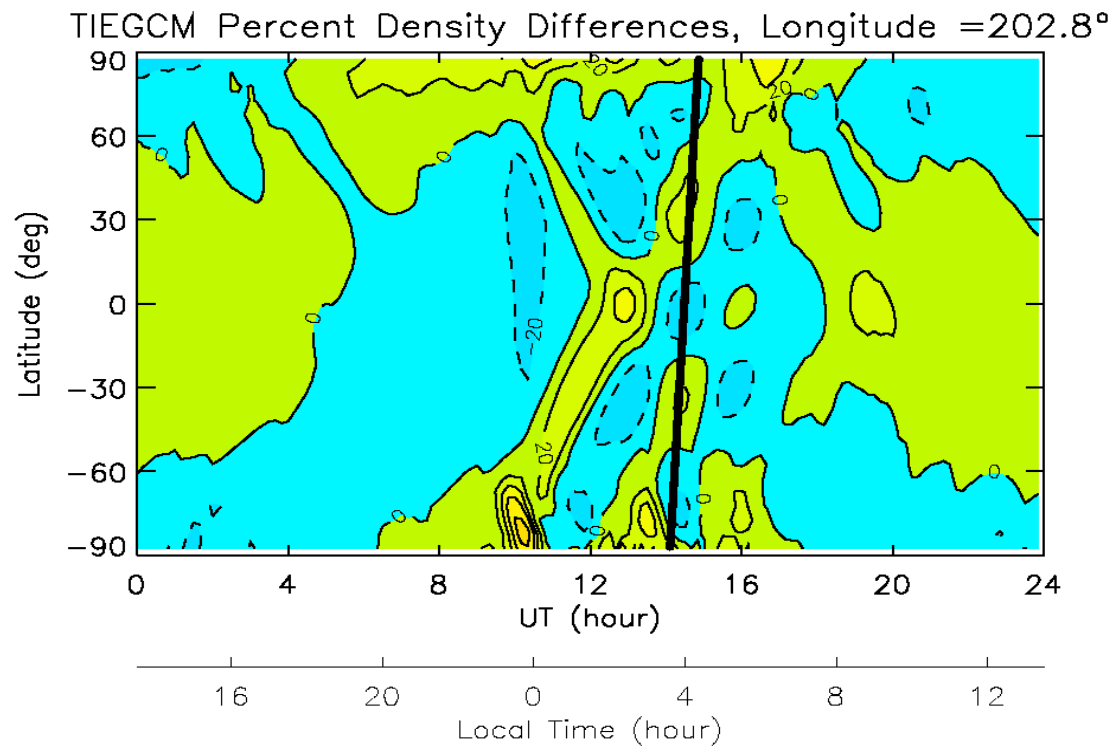
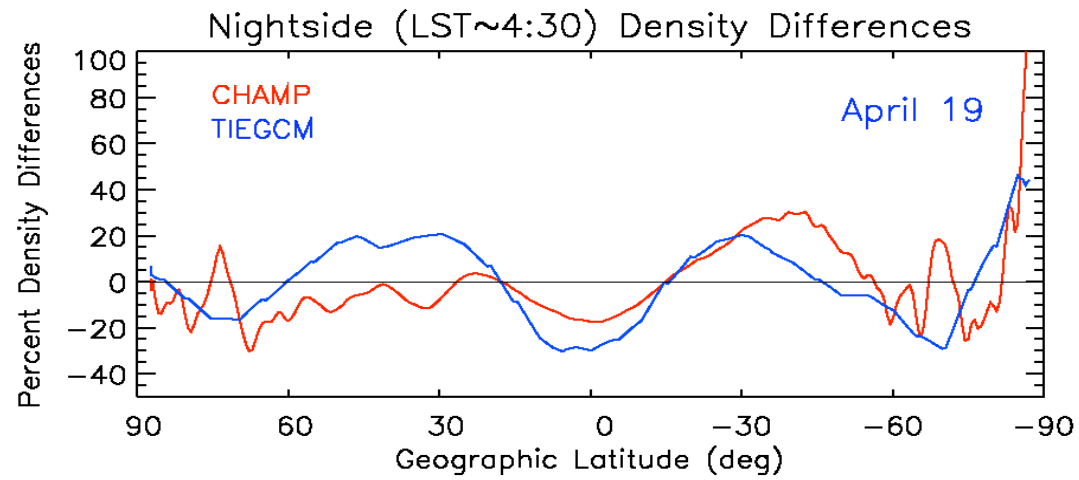


April 2002 storm period

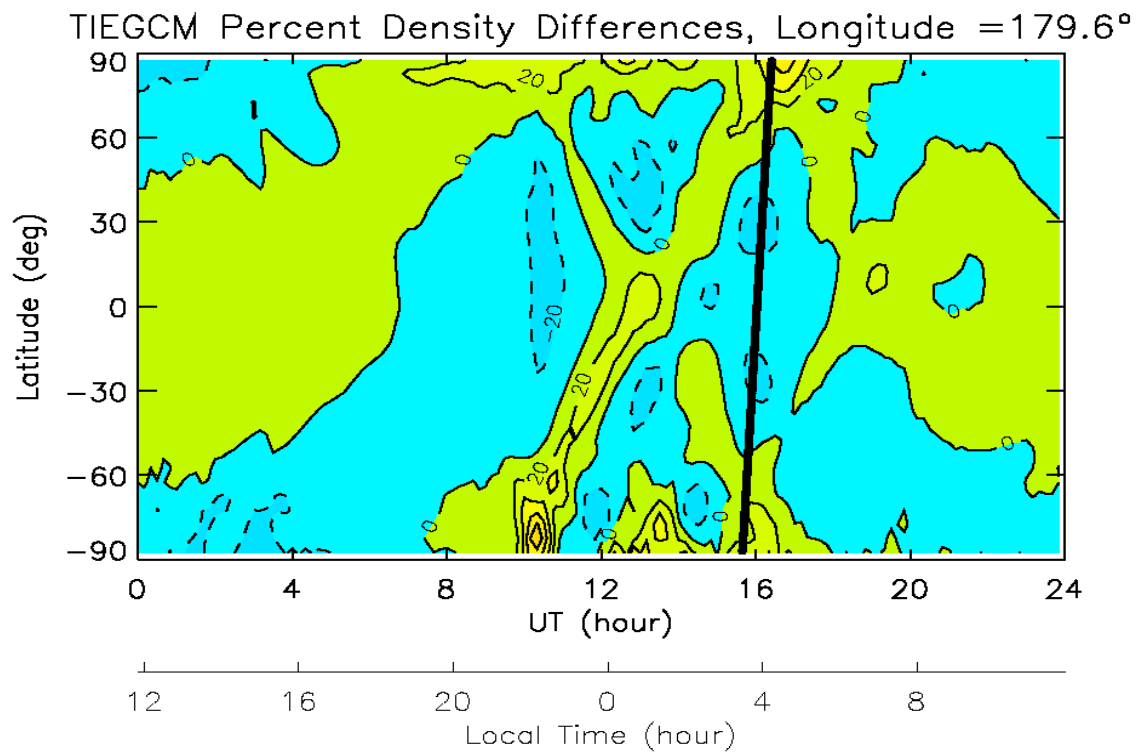
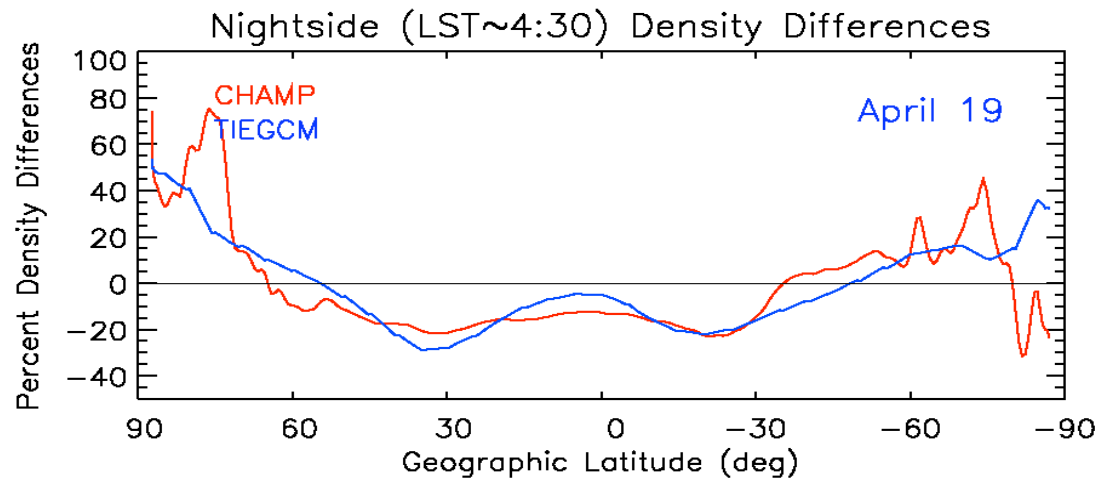


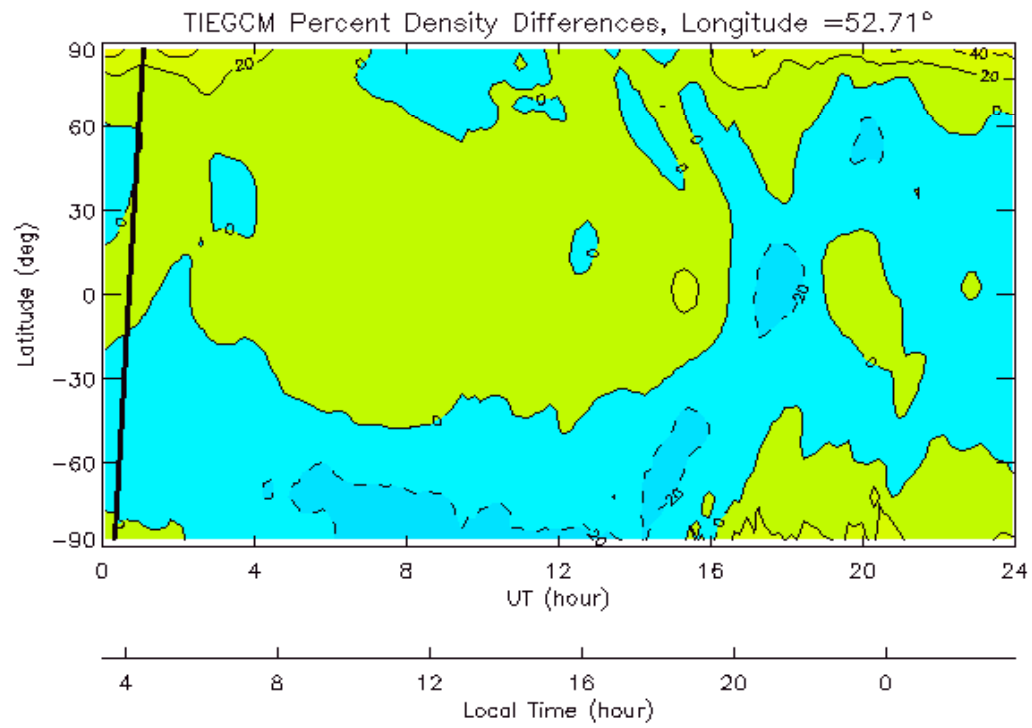
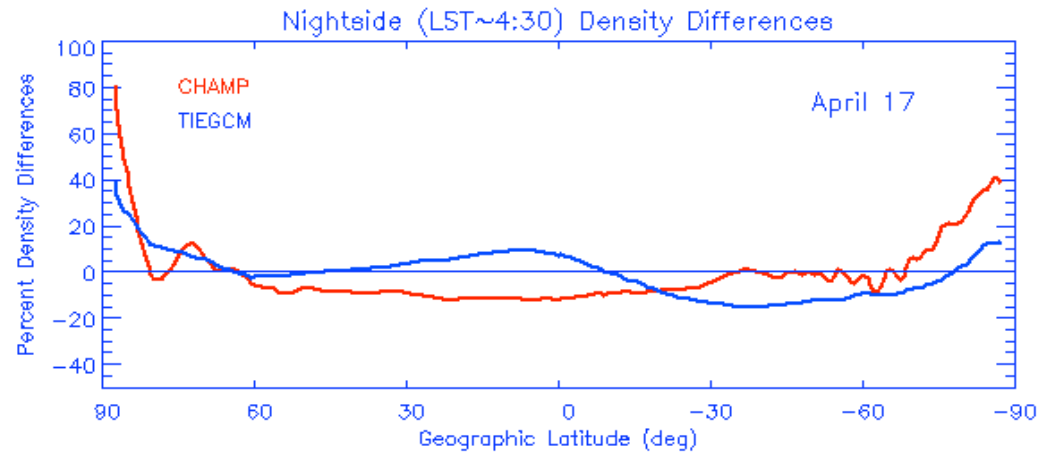




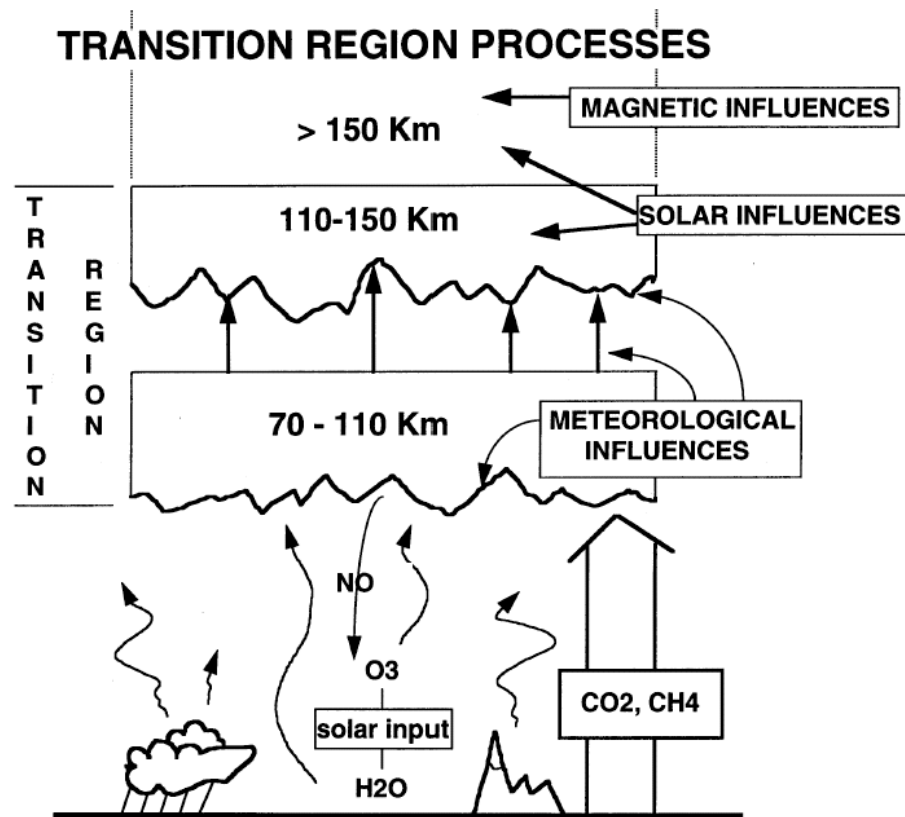




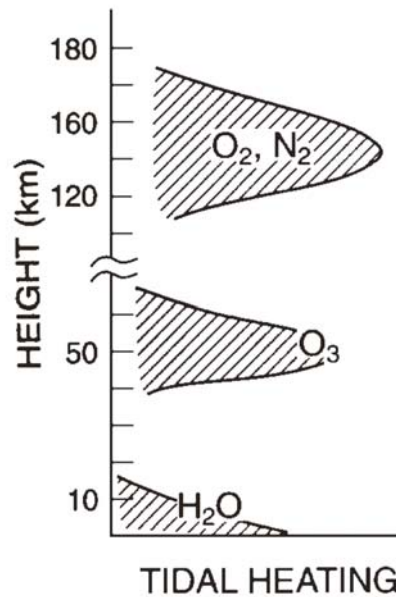
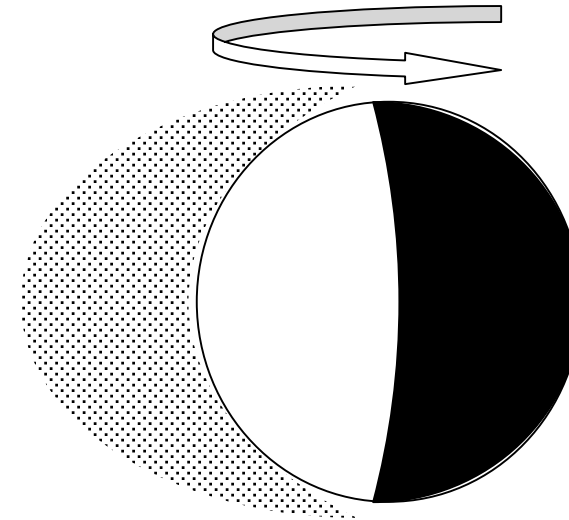
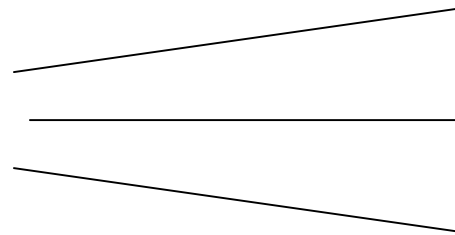
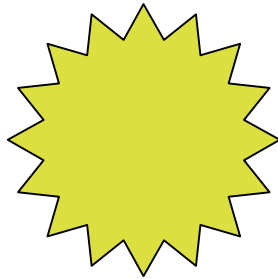




# Thermosphere Weather: Coupling with the Lower Atmosphere



# Solar Thermal Tides



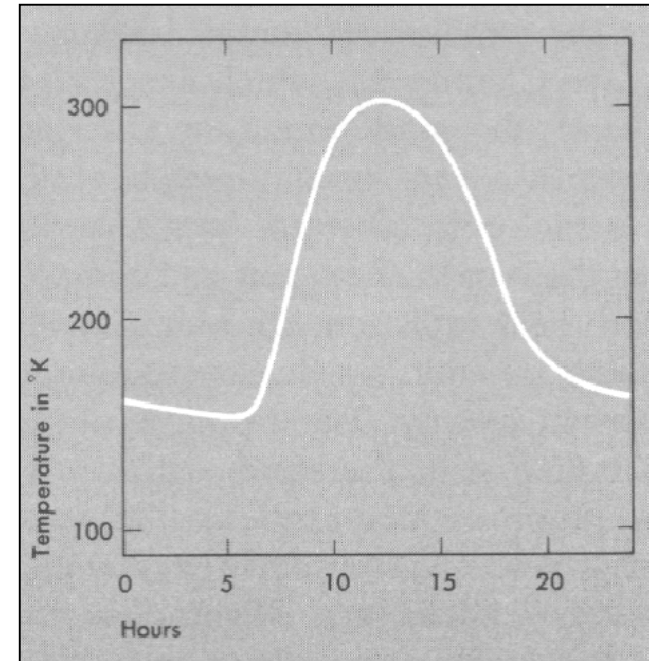
**Solar thermal tides are excited in a planetary atmosphere through the periodic (local time, longitude) absorption of solar radiation.**

**In general, tides are capable of propagating vertically to higher, less dense, regions of the atmosphere; the oscillations grow exponentially with height.**

**The tides are dissipated by molecular diffusion above 100 km, their exponential growth with height ceases, and they deposit mean momentum and energy into the thermosphere.**

In the local (solar) time frame, the heating, or changes in atmospheric fields due to the heating, may be represented as

$$\begin{aligned} \text{heating} &= Q_o + \sum_{n=1}^N a_n \cos n\Omega t_{LT} + b_n \sin n\Omega t_{LT} \\ &= Q_o + \sum_{n=1}^N A_n \cos(n\Omega t_{LT} - \phi) \end{aligned}$$



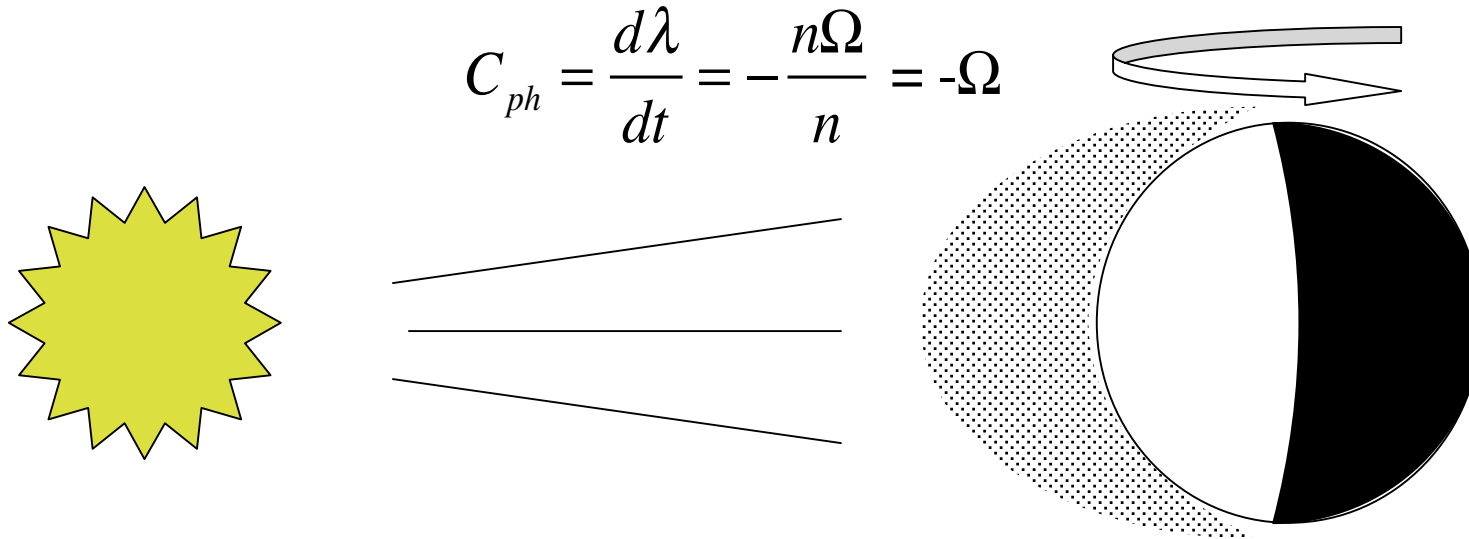
Local time

Converting to universal time  $t_{LT} = t + \lambda/\Omega$ , we have

$$\text{heating} = Q_o + \sum_{n=1}^N A_n \cos(n\Omega t + n\lambda - \phi)$$

n = 1	“diurnal”
n = 2	“semidiurnal”
n = 3	“terdiurnal”

Implying a zonal phase speed  $C_{ph} = \frac{d\lambda}{dt} = -\frac{n\Omega}{n} = -\Omega$



**To an observer in space, it looks like the heating or response bulge is fixed with respect to the Sun, and the planet is rotating beneath it.**

**To an observer on the ground, the bulge is moving westward at the apparent motion of the Sun, i.e.,  $2\pi \text{ day}^{-1}$ . It is sometimes said that the bulge is ‘migrating’ with the apparent motion of the Sun with respect to an observer fixed on the planet.**

**This is what things look like if the solar heating is the same at all longitudes.**

However, if the excitation depends on longitude, the spectrum of tides that is produced is more generally expressed as a linear superposition of waves of various frequencies ( $n$ ) and zonal wavenumbers ( $s$ ):

$$\sum_{s=-k}^{s=+k} \sum_{n=1}^N A_n \cos(n\Omega t + s\lambda - \phi)$$

implying zonal phase speeds

$$C_{ph} = \frac{d\lambda}{dt} = -\frac{n\Omega}{s} \quad \therefore \quad s > 0 \quad \Rightarrow \quad \text{westward propagation}$$

The waves with  $s \neq n$  are referred to as non-migrating tides because they do not migrate with respect to the Sun to a planetary-fixed observer.

## Non-Migrating Tides are Not Sun-Synchronous

Thus, they can propagate westward

around the planet both faster than the Sun, i.e.,  $\frac{\sigma}{s} < -\Omega$

or slower than the Sun, i.e.,  $-\Omega < \frac{\sigma}{s} < 0$  ,

and opposite in direction to the Sun, i.e.,  $\frac{\sigma}{s} > 0$  ,

or just be standing:  $s = 0$  (i.e., the whole atmosphere breathes in and out at the frequency  $\sigma$  .

*The total atmospheric response to solar forcing is some superposition of migrating and nonmigrating tidal components, giving rise to a different tidal response at each longitude.*



# “Weather” due to Tidal Variability

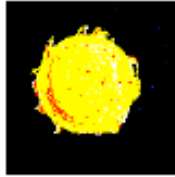
## Eastward Winds over Saskatoon, Canada, 65-100 km

Note the  
predominance  
of the  
semidiurnal  
tide at upper  
levels, with  
downward  
phase  
progression.

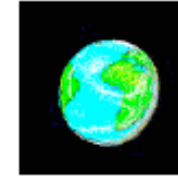


Note the  
transition  
from  
easterlies  
(westerlies)  
below ~80-85  
km to  
westerlies  
(easterlies)  
above  
during  
summer  
(winter), due  
to GW  
filtering and  
momentum  
deposition.

Courtesy of C. Meek and A. Manson

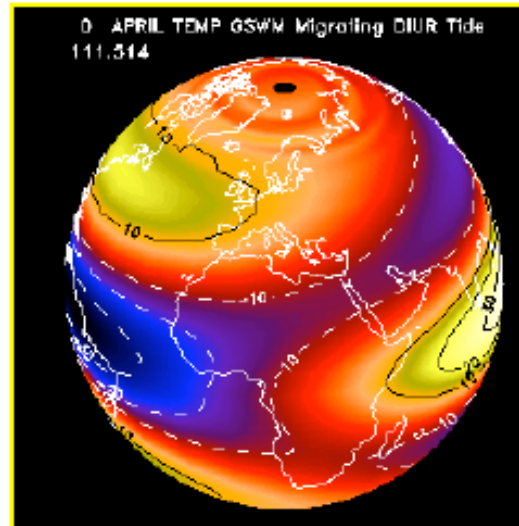


# GSWM: Global Scale Wave Model



A Numerical Model of Planetary Waves and Solar Tides in the Earth's Atmosphere

*High Altitude Observatory (HAO)  
National Center for Atmospheric Research (NCAR)*



GSWM-98 24-hr Tidal Temperature Perturbation (K) for April, 111km.  
Click for animation with alternating "Earth" vs. "Space" frame of reference (1.5M).  
(Animation runs 4 loops; [ESC] stops it!)

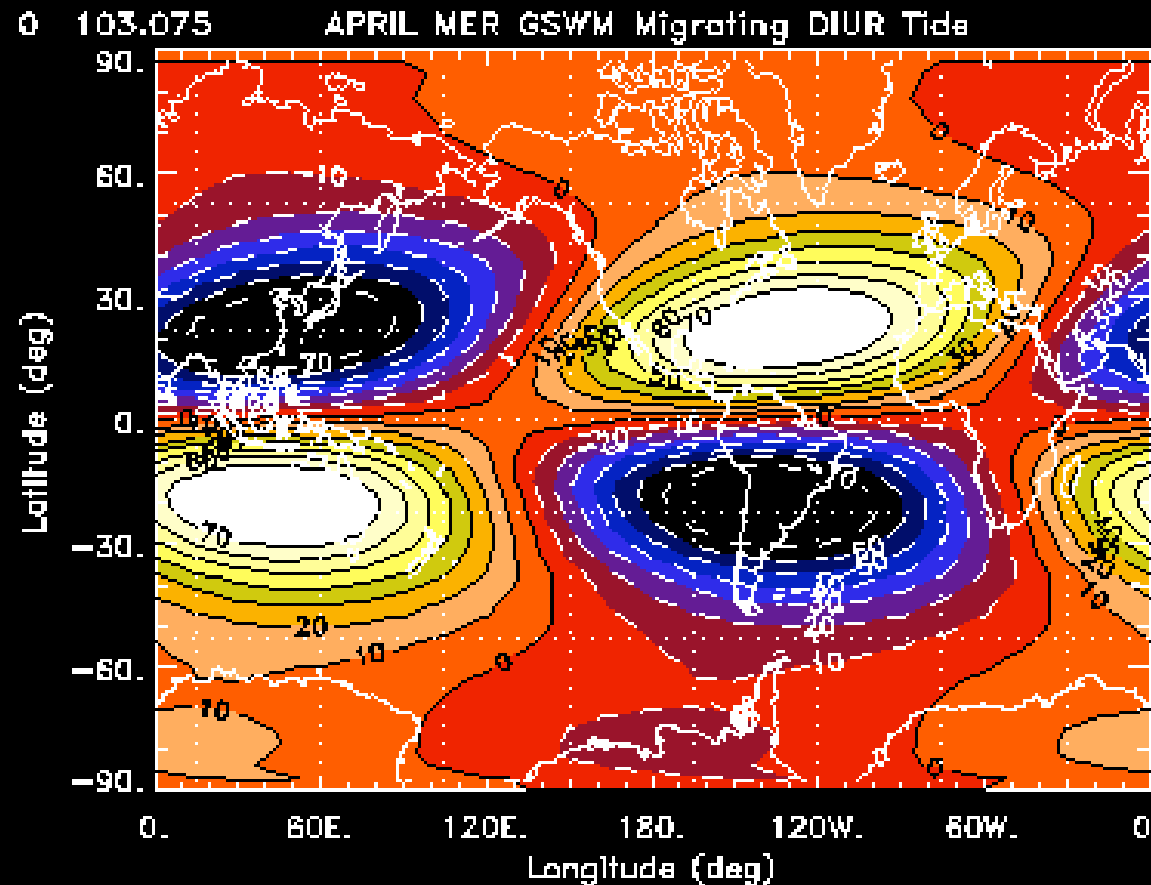
Download tables of monthly GSWM-00 migrating diurnal and semidiurnal results.

Download monthly GSWM-02 migrating and nonmigrating diurnal and semidiurnal results at user specified locations.

Download netcdf files of GSWM-02 results that mimic TIMED/CEDAR observations

<http://web.hao.ucar.edu/public/research/tiso/gswm/gswm.html>

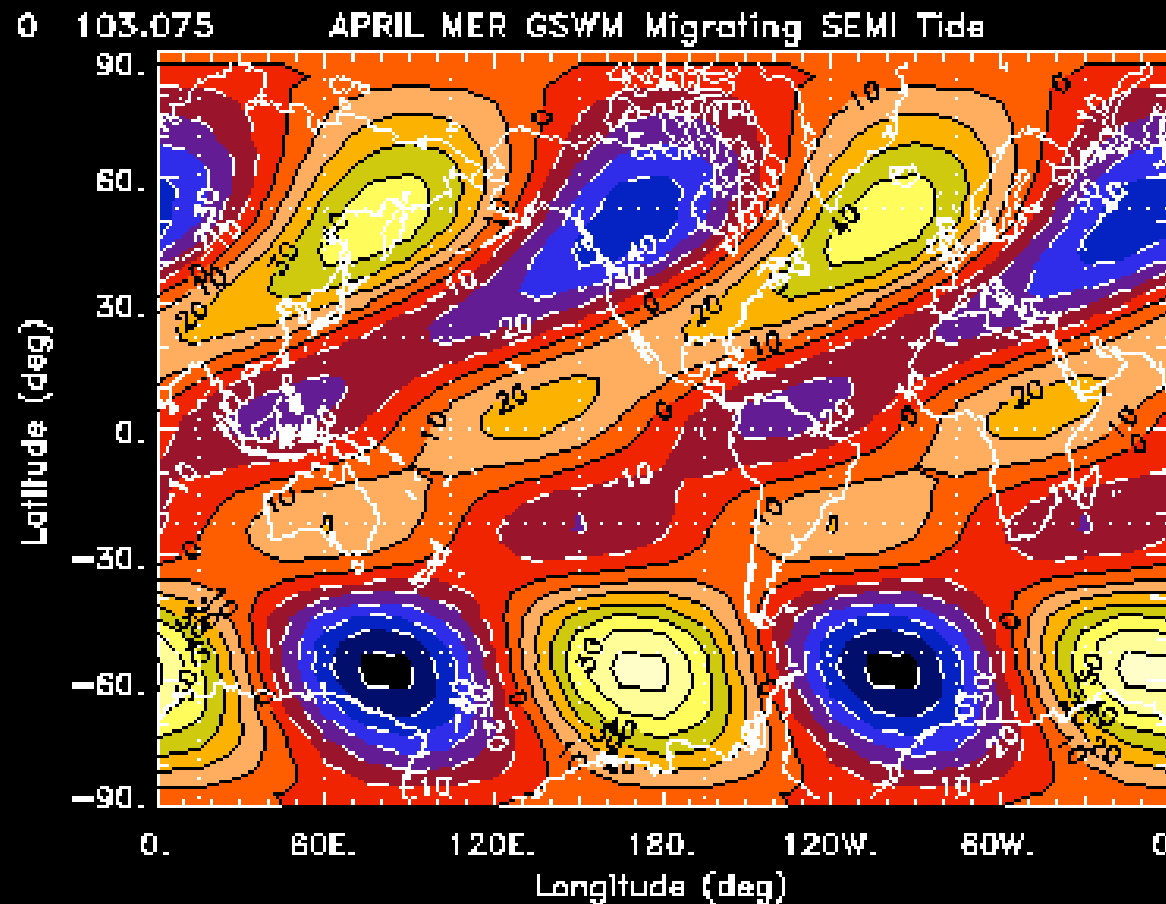
Meridional wind field at 103 km (April) associated with the **diurnal tide** propagating upward from the lower atmosphere, mainly excited by near-IR absorption by  $H_2O$  in the troposphere



*Courtesy M. Hagan*

The tide propagates westward with respect to the surface once per day, and is locally seen as the same **diurnal** tide at all longitudes.

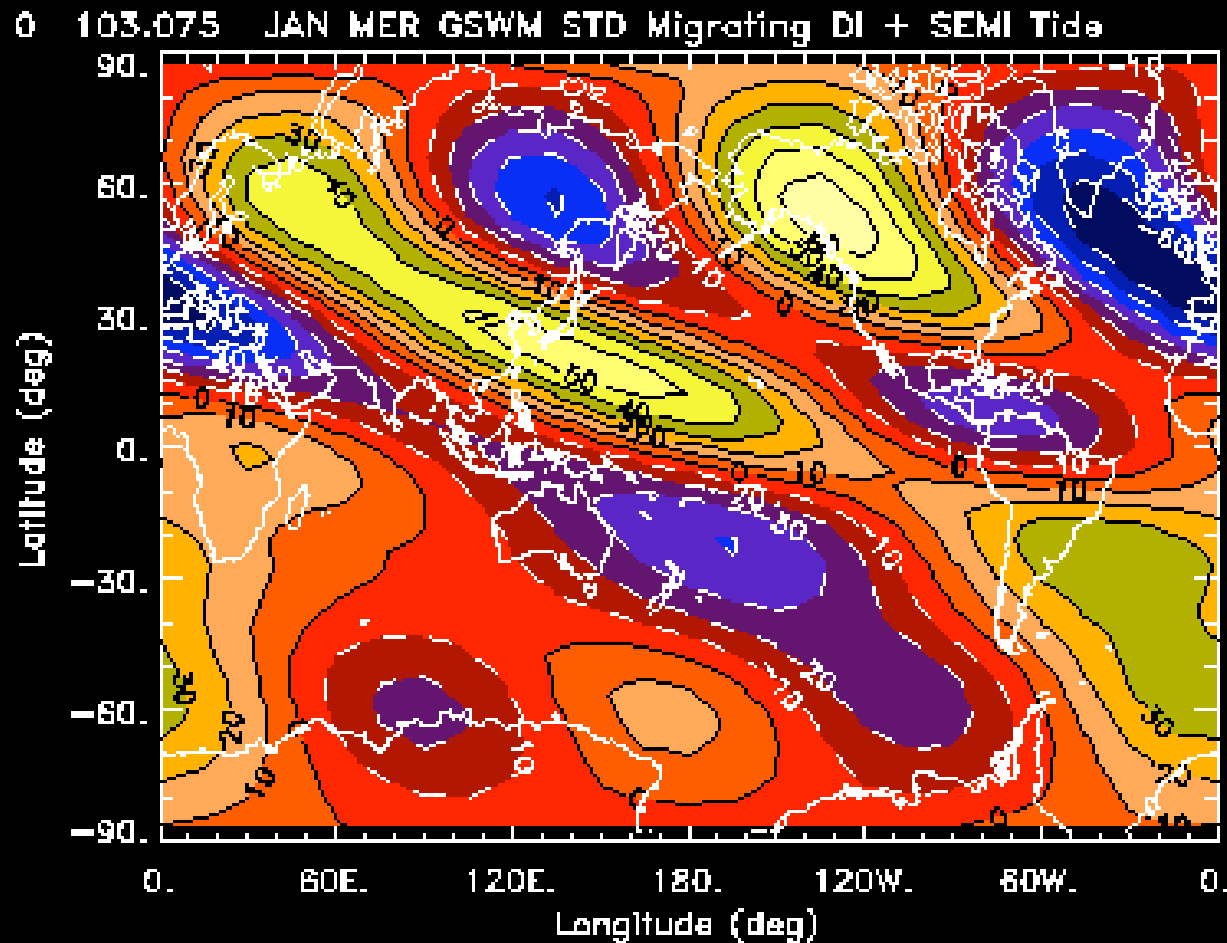
Meridional wind field at 103 km (April) associated with the semidiurnal tide propagating upward from the lower atmosphere, mainly excited by near-IR absorption by  $O_3$  in the troposphere



*Courtesy M. Hagan*

The tide propagates westward with respect to the surface once per day, and is locally seen as the same semidiurnal tide at all longitudes.

Meridional wind field at 103 km (January) associated with the combined diurnal and semidiurnal tides propagating upward from the lower atmosphere



*Courtesy M. Hagan*

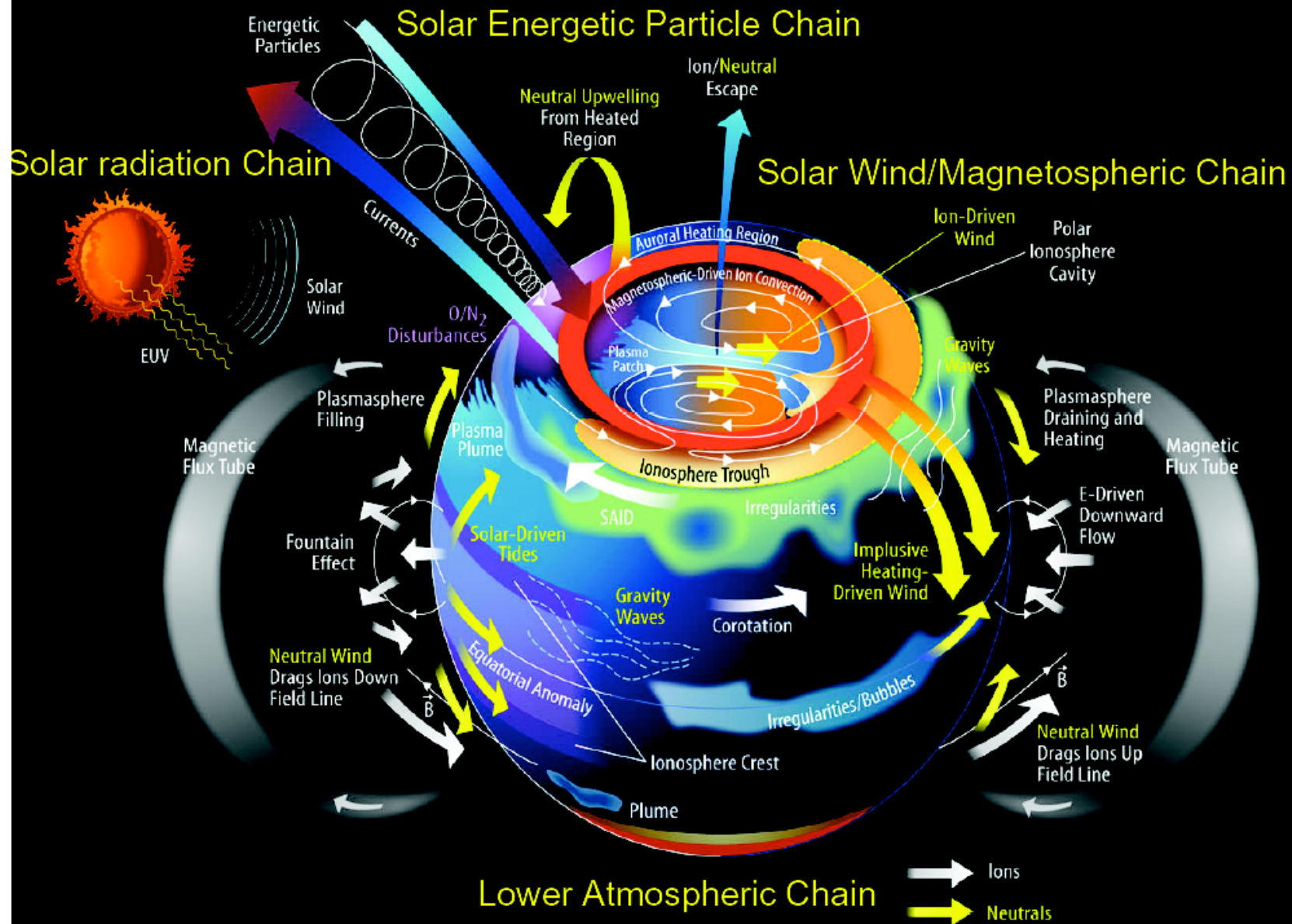
Both tides propagate westward with respect to the surface once per day, and is locally seen as the same **local time structure** at all longitudes.

# Summary of Basic Thermosphere Characteristics

- Solar heating is main energy source
- Main cooling is through molecular conduction; secondary, radiative cooling by O, CO<sub>2</sub>, NO
- Main gases: O, O<sub>2</sub>, N<sub>2</sub>, He (high altitudes only)
- Strong variability of temperature, winds and composition with solar cycle, season, local time, geomagnetic activity
- The seasonal composition changes are controlled primarily by global winds, the diurnal ones by photochemistry
- At low latitudes effects of upward propagating tides, planetary waves and gravity waves are important
- **At high latitudes, heating from the magnetosphere occurs in the form of Joule heating and precipitating particles**

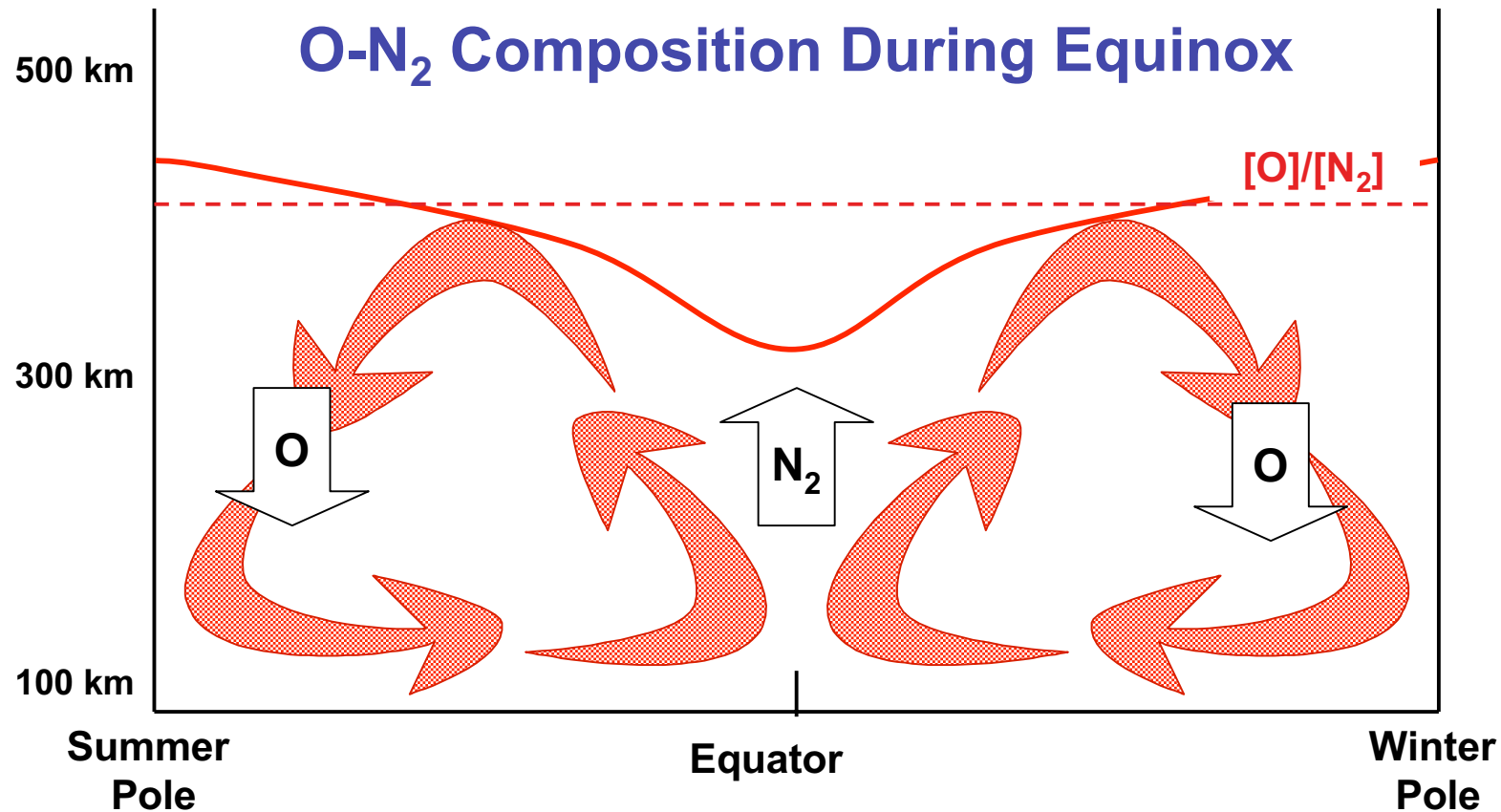
# Additional Slides

# Terrestrial Atmosphere ITM Processes





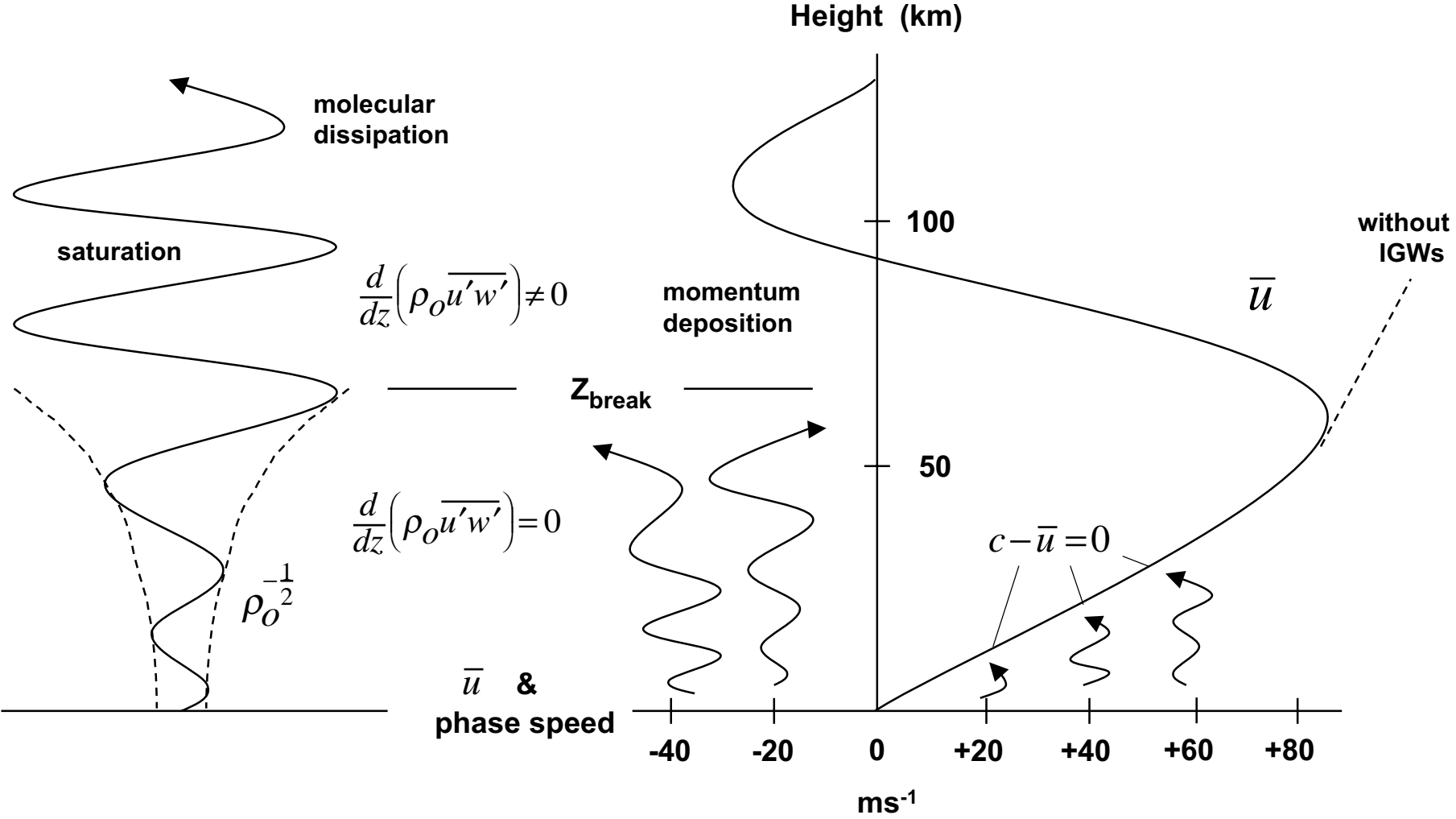
## Solar EUV-Driven Circulation and O-N<sub>2</sub> Composition During Equinox



The increased mean mass ( $M$ ) over regions of upwelling (and beyond) reduces the total density scale height  $H = R \cdot T / Mg$  at a given altitude, essentially “mixing” and “compressing” the atmosphere.

However, from model simulations (Fuller-Rowell, 1998), this effect is more important during solstice, even at low latitudes, such that a semiannual variation in total density results, with maxima at the equinoxes.

# Gravity Wave Coupling in Earth's Atmosphere



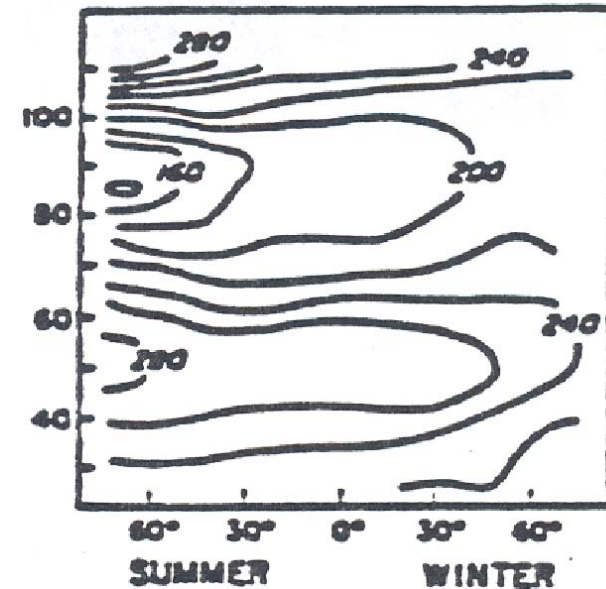
# Gravity Waves and Effects on the Mean Thermal Structure

Due to the exponential decrease of density, amplitudes of gravity waves grow exponentially with height --- in the "reentry" regime they become so large that they go unstable, generate turbulence, and deposit heat and momentum into the atmosphere.

The generated turbulence accounts for the "turbulent mixing" and the turbopause (homopause) that we talked about before.

The deposited momentum produces a net meridional circulation, and associated rising motions (cooling) at high latitudes during summer, and sinking motions (heating) during winter, causing the so-called "mesopause anomaly" in temperature.

$$\frac{\partial \bar{u}}{\partial t} + \dots - f v = -\frac{1}{\rho} \frac{\partial}{\partial z} (\rho \overline{u'w'})$$



# WAVE/MEAN-FLOW/THERMAL INTERACTIONS

