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# Ionosphere-Thermosphere Basics: Dynamics and Energetics

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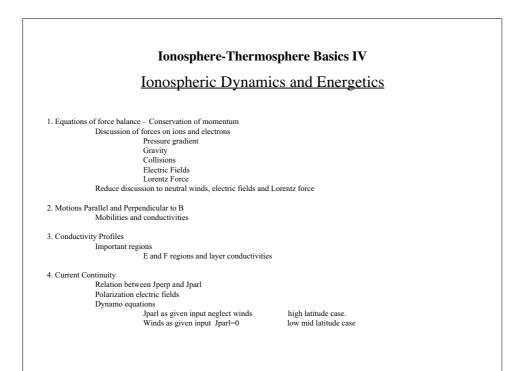
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#### **Ionosphere-Thermosphere Basics IV**

Ionospheric Dynamics and Energetics

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#### **Ionosphere-Thermosphere Basics IV**

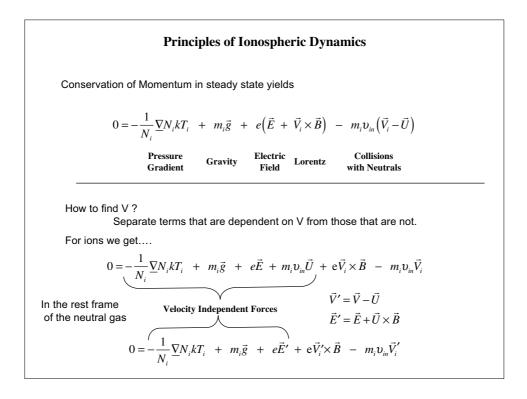
### Ionospheric Dynamics and Energetics

5. Electric fields at low and middle latitudes Drifts perpendicular to B in the meridian (Vperp at equator) Plasma motions including diffusion Fountain effect and horizontal transport Effects of different E-fields Effects of different E-fields Appleton anomaly Reduction of Ion drag Change in layer thickness during the day Reduction in recombination rate at night. Drifts perpendicular to B and perpendicular to the meridian (e-w drifts) Change in effective length of the day for plasma Superrotation of the ionosphere.

6. Plasma motions parallel to B at low and middle latitudes

Effects of neutral winds Effects of neutral winds Importance of magnetic dip angle Seasonal asymmetries Changes in Ion composition and number density Effects on plasma temperatures.

| Principles of Ionospheric Dynamics |  |
|------------------------------------|--|
|                                    | Forces on Charged Particles  |
| • Colli                            | sions with neutral particles.  |
|                                    | Tidal oscillations that propagate up from below.                                   |
|                                    | In-situ circulation due to high-latitude energetic particles, Joule heating,       |
|                                    | and local heating from the sun.  |
| • Colli                            | sions with charged particles.  |
|                                    | Neglect for ions in the ionosphere. Important for electron mobility parallel to B. |
|                                    | Effective resistivity in the magnetosphere.  |
| • Elect                            | ric Fields   |
|                                    | Externally applied from solar wind sources.  |
|                                    | Internally produced to make total current divergence free.                         |
| • Lore                             | ntz Force  |
|                                    | A charged particle in motion feels a force in a uniform magnetic field.            |
| • Grav                             | ity  |
|                                    | Most important for ions in the ionosphere  |
| • Pres                             | sure Gradient  |
|                                    | Perpendicular to the magnetic field dependent on the particle energy distribution. |
|                                    | Parallel to the magnetic field it produces an ambipolar electric field to make     |
|                                    | ions and electrons move together.  |



#### **Principles of Ionospheric Dynamics**

Conservation of momentum can be written as

$$\mathbf{F} \pm e(\mathbf{V} \times \mathbf{B}) - m\upsilon \mathbf{V} = 0$$

We solve this equation to determine the particle velocity perpendicular and parallel to the magnetic field resulting from a force F. Parallel to the magnetic field  $\mathbf{F} = \min \mathbf{V} = 0$ 

 $\mathbf{F}_{\parallel} - m\upsilon\mathbf{V}_{\parallel} = 0$  $\mathbf{V}_{\parallel} = \frac{\omega_B}{\upsilon} \frac{1}{eB} \mathbf{F}_{\parallel}$  $\mathbf{V}_{\parallel} = \kappa_{\parallel} \mathbf{F}_{\parallel}$ 

The coefficient in relating the velocity to the force is called the "mobility"  $\kappa$ 

The particle velocity is proportional to the component of the force parallel to B but may be reduced by collisions between the charged particle and the neutral gas.

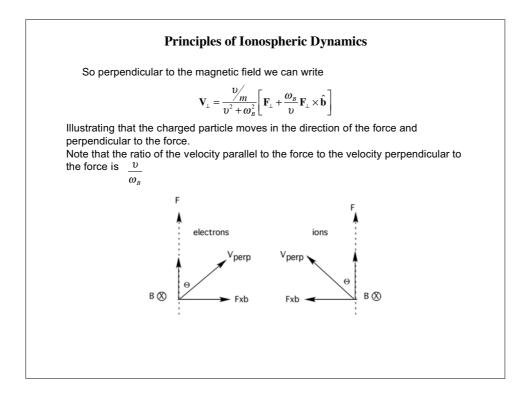
Notice MAY be reduced. This will not be true if the force itself is due to collisions with the neutral gas.

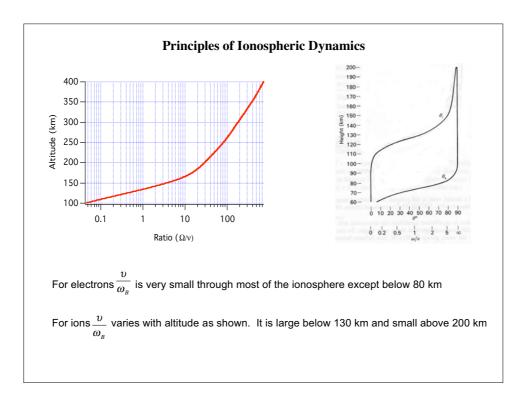
#### **Principles of Ionospheric Dynamics**

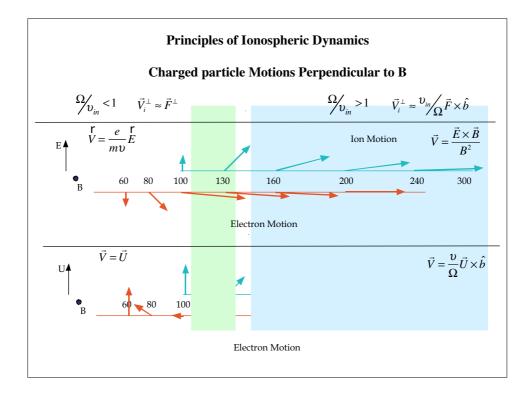
Conservation of momentum can be written as

$$\mathbf{F} \pm e(\mathbf{V} \times \mathbf{B}) - m\upsilon \mathbf{V} = 0$$

Perpendicular to the magnetic field the situation is more complicated and we proceed as follows







#### **Principles of Ionospheric Dynamics**

Forces can produce different ion and electron velocities ..... Currents

If we express the force as an equivalent electric field, then we can express the current density in terms of the equivalent electric field. The matrix of coefficients is called the conductivity tensor.

Parallel to B  $\mathbf{j}_{\parallel} = Ne(\mathbf{V}_{\parallel}^{i} - \mathbf{V}_{\parallel}^{e})$ 

$$\mathbf{V}_{\parallel} = \frac{\omega_B}{\upsilon} \frac{1}{B} \mathbf{E}_{\parallel} = \frac{e}{m\upsilon} \mathbf{E}_{\parallel}$$
$$\mathbf{j}_{\parallel} = Ne^2 \left(\frac{1}{m_i \upsilon_i} + \frac{1}{m_e \upsilon_e}\right) \mathbf{E}_{\parallel} \Longrightarrow \sigma_0 \mathbf{E}_{\parallel}$$

 $\sigma_0$  is called the Direct Conductivity

$$\sigma_0 = Ne^2 \left[ \frac{1}{m_i v_i} + \frac{1}{m_e v_e} \right]$$

Note that the electron collision frequency is dominated at high altitudes by ionelectron collisions and that this term is linearly proportional the charged particle number density. Thus the direct conductivity becomes constant at high latitudes.

#### **Principles of Ionospheric Dynamics**

Perpendicular to B we consider the current in the direction of the force and perpendicular to the force. ĥ

$$\mathbf{j}_{\perp} = \boldsymbol{\sigma}_{p} \mathbf{E}_{\perp} - \boldsymbol{\sigma}_{h} \mathbf{E}_{\perp} \times \hat{\mathbf{b}}$$

 $\sigma_{\!\scriptscriptstyle D}$  is called the Pedersen Conductivity  $\sigma_{\!\scriptscriptstyle h}$  is called the Hall Conductivity

$$\begin{split} \mathbf{V}_{\perp} &= \frac{1}{\upsilon^2 + \omega_B^2} \left[ \frac{\omega_B \upsilon}{eB} \mathbf{F}_{\perp} + \frac{\omega_B^2}{eB} \mathbf{F}_{\perp} \times \hat{\mathbf{b}} \right] \qquad \mathbf{V}_{\perp} = \frac{1}{\upsilon^2 + \omega_B^2} \left[ \frac{\upsilon}{m} \mathbf{F}_{\perp} \pm \frac{\omega}{m} \mathbf{F}_{\perp} \times \hat{\mathbf{b}} \right] \\ \mathbf{J}_{\perp} &= \frac{Ne}{\upsilon_i^{2^+} + \omega_B^2} \left[ \frac{\upsilon_i}{m_i} e \mathbf{E}_{\perp} + \frac{\omega_B}{m_i} e \mathbf{E}_{\perp} \times \hat{\mathbf{b}} \right] - \frac{Ne}{\upsilon_e^2 + \omega_B^2} \left[ \frac{\upsilon_e}{m_e} (-e) \mathbf{E}_{\perp} - \frac{\omega_B}{m_e} (-e) \mathbf{E}_{\perp} \times \hat{\mathbf{b}} \right] \\ \mathbf{J}_{\perp} &= Ne^2 \left[ \frac{\upsilon_i}{m_i} (\upsilon_i^{2^+} + \omega_B^2) + \frac{\upsilon_e}{m_e} (\upsilon_e^{2^+} + \omega_B^2) \right] \mathbf{E}_{\perp} + Ne^2 \left[ \frac{\omega_B}{m_i} (\upsilon_i^{2^+} + \omega_B^2) - \frac{\omega_B}{m_e} (\upsilon_e^{2^+} + \omega_B^2) \right] \mathbf{E}_{\perp} \times \hat{\mathbf{b}} \\ & \sigma_p = \sigma_1 = Ne^2 \left[ \frac{\upsilon_i}{m_i} (\upsilon_i^{2^+} + \omega_B^2) + \frac{\upsilon_e}{m_e} (\upsilon_e^{2^+} + \omega_B^2) + \frac{\upsilon_e}{m_e} (\upsilon_e^{2^+} + \omega_B^2) \right] \\ & \sigma_h = \sigma_2 = Ne^2 \left[ \frac{\omega_B}{m_e} (\upsilon_e^{2^+} + \omega_B^2) - \frac{\omega_B}{m_i} (\upsilon_i^{2^+} + \omega_B^2) \right] \end{split}$$

#### **Collision Frequencies**

$$\upsilon_{i} = \upsilon_{in} \approx 2.6 \times 10^{-9} N_{n} A^{-1/2}$$

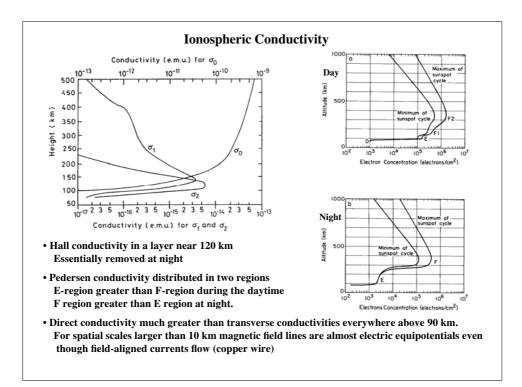
$$A = \frac{m_{i} m_{n}}{m_{i} + m_{n}}$$

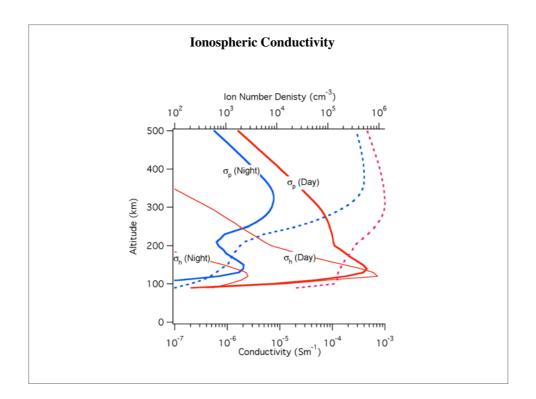
$$\upsilon_{e} = \upsilon_{en} + \upsilon_{ei}$$

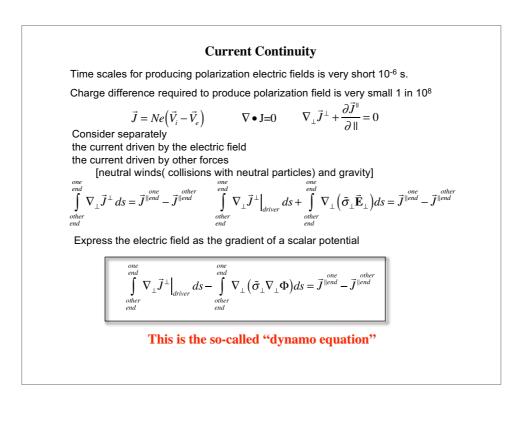
$$\upsilon_{en} \approx 5.4 \times 10^{-10} N_{n} T_{e}^{-1/2}$$

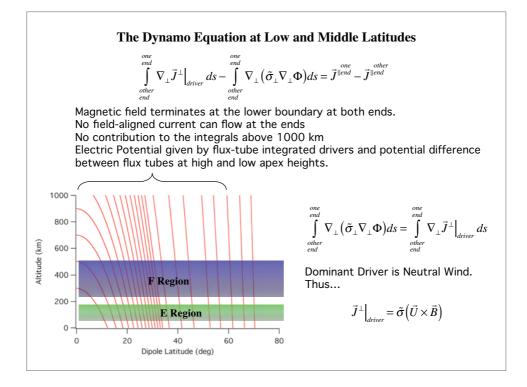
$$\upsilon_{ei} \approx \left[ 34 + 4.18 \ln \left( \frac{T_{e}^{3}}{N_{e}} \right) \right] N_{e} T_{e}^{-3/2}$$

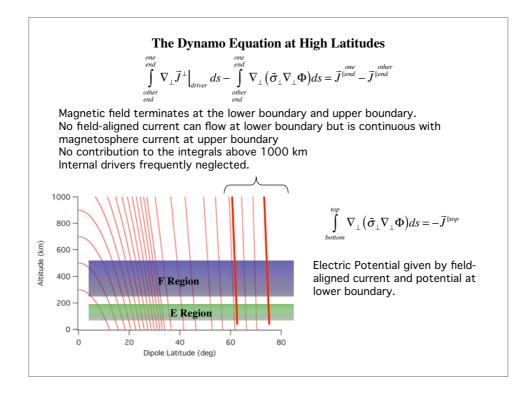
Number density in number per cubic centimeter Mean mass in amu

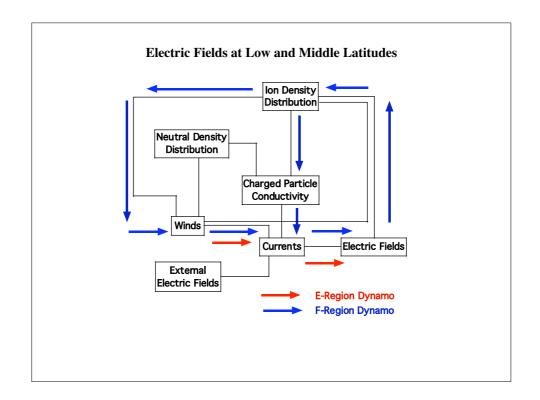


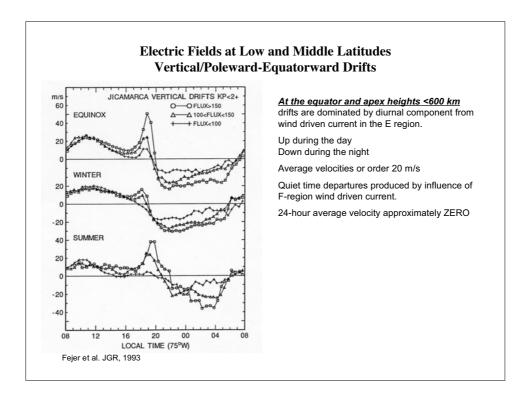


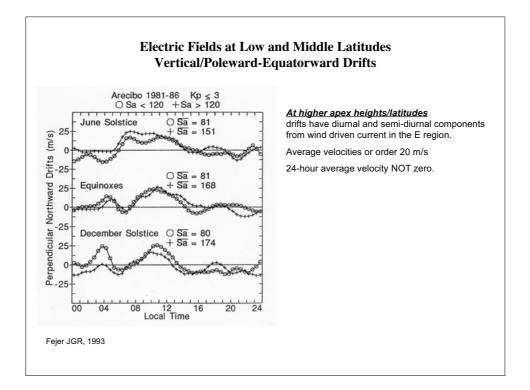


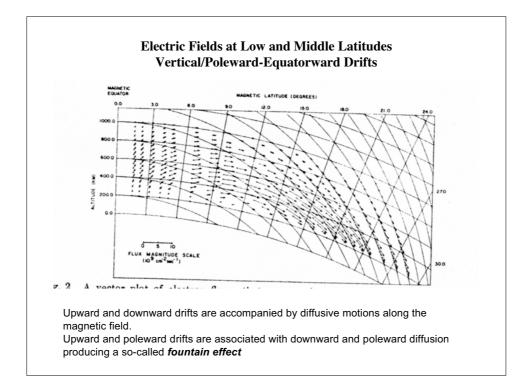


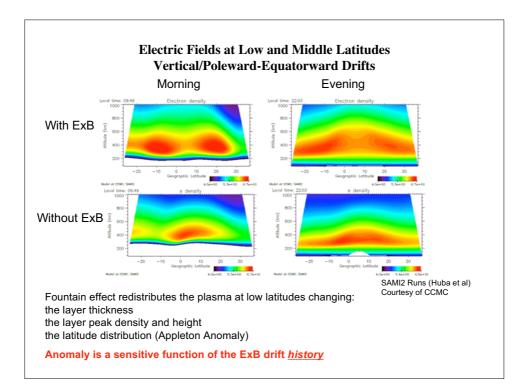


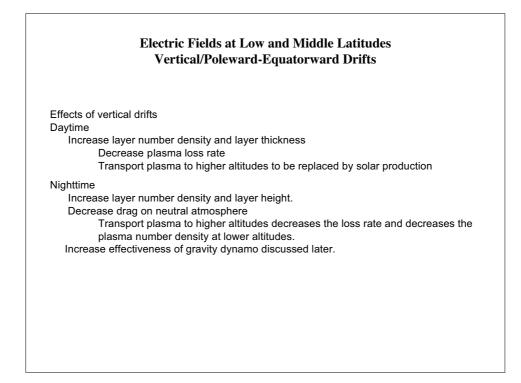


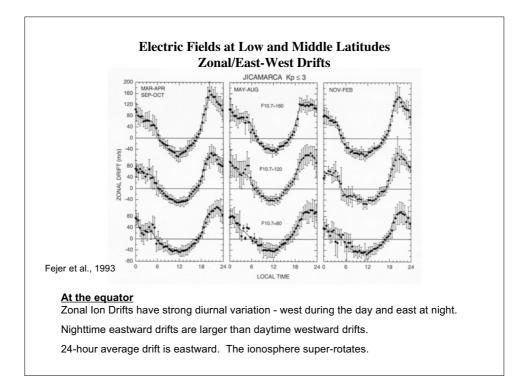


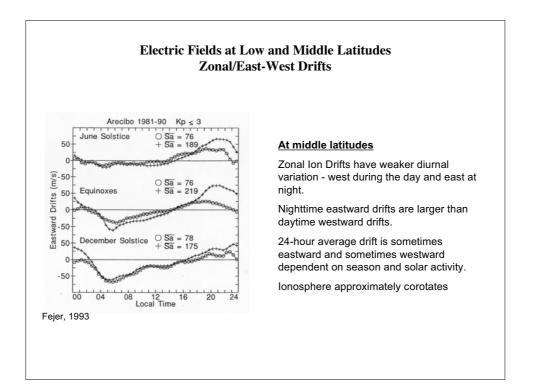


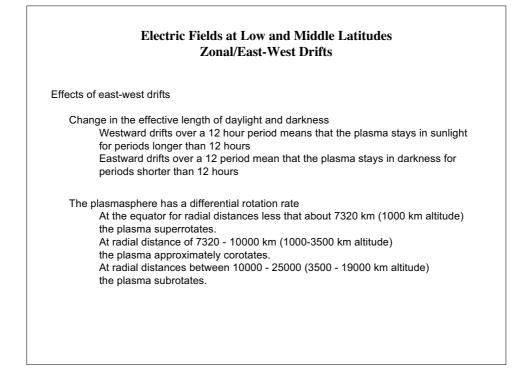


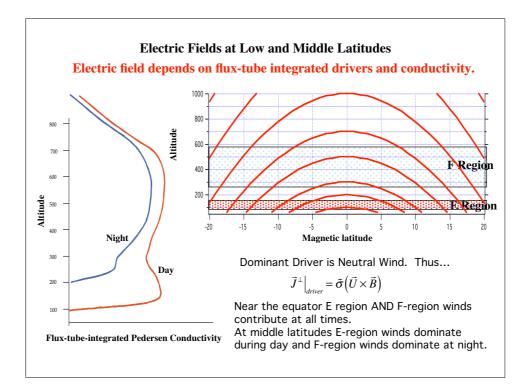


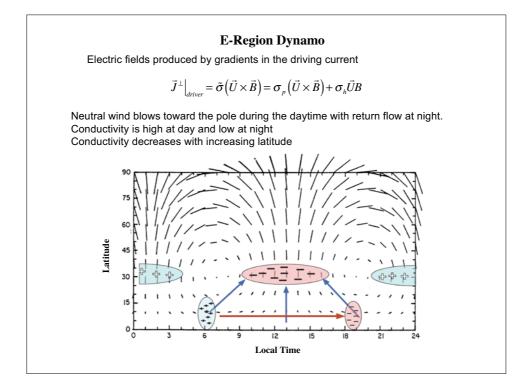












# **The Equatorial Electrojet** It is convenient to consider the E region as a layer where the Hall and Pedersen conductivities are important and where the layer only allows horizontal currents to flow. Near the equator an east-west electric field ( neutral wind) will drive a vertical current that cannot close anywhere and therefore must be suppressed by a vertical polarization electric field. $\int \int \int X \quad J_x = \sigma_p E_x + \sigma_h E_z$ $J_z = -\sigma_h E_x + \sigma_p E_z$ $J_z = 0 \Rightarrow \sigma_h E_x = \sigma_p E_z \Rightarrow J_x = \sigma_p E_x + \sigma_h \frac{\sigma_h}{\sigma_p} E_x$ $J_x = \sigma_3 E_x \qquad \sigma_3 = \sigma_p + \frac{\sigma_h^2}{\sigma_p}$ This enhanced Pedersen conductivity is called the Cowling conductivity and results from making the vertical current zero.

The resulting enhancement in the east west current at the equator is called the equatorial electrojet.

#### **E-region Layer Conductivities**

With the assumption that the vertical current is suppressed in the layer it is possible to write the horizontal current in terms of the north-south (y) and east-west (x) components of the electric field. The e-field can easily include a UxB wind driver.

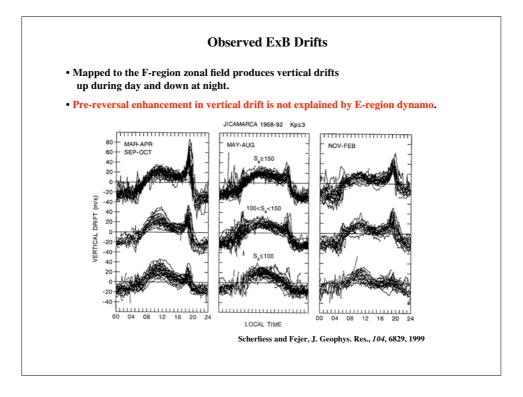
$$J_{x} = \sigma_{xx}E_{x} + \sigma_{xy}E_{y}$$
$$J_{y} = \sigma_{yy}E_{y} - \sigma_{xy}E_{x}$$

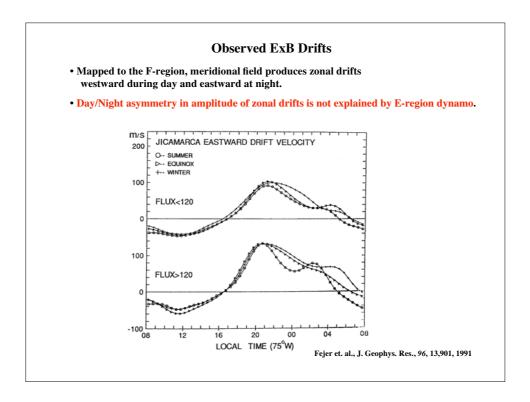
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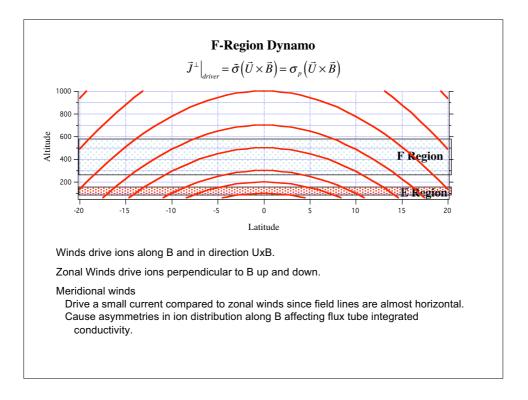
The so called layer conductivities can be expressed as

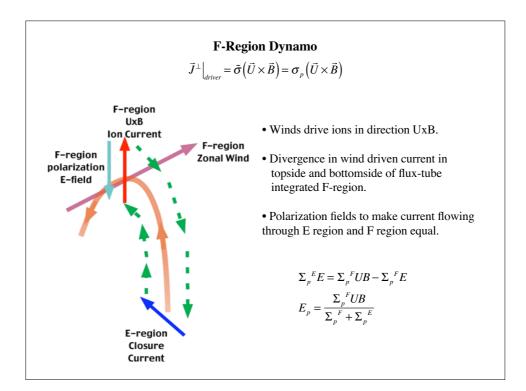
$$\sigma_{xx} = \frac{\sigma_0 \sigma_1}{\left(\sigma_1 \cos^2 I + \sigma_0 \sin^2 I\right)}$$
$$\sigma_{yy} = \frac{\sigma_0 \sigma_1 \sin^2 I + \left(\sigma_1^2 + \sigma_2^2\right) \cos^2 I}{\left(\sigma_1 \cos^2 I + \sigma_0 \sin^2 I\right)}$$
$$\sigma_{xy} = \frac{\sigma_0 \sigma_2 \sin I}{\left(\sigma_1 \cos^2 I + \sigma_0 \sin^2 I\right)}$$

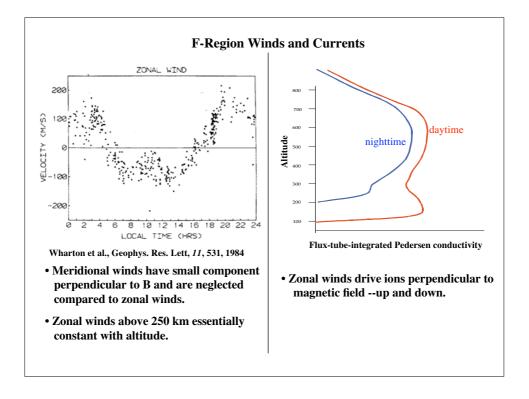
Note that these layer conductivities reduce to just the direct and cowling conductivity at the equator.

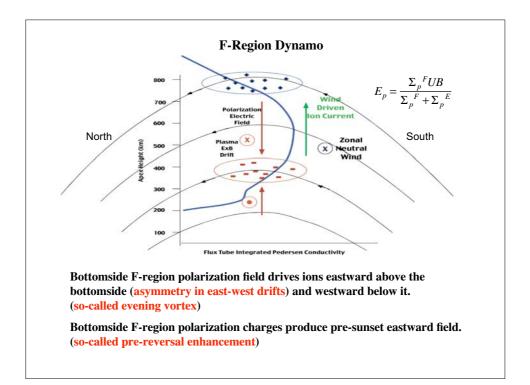


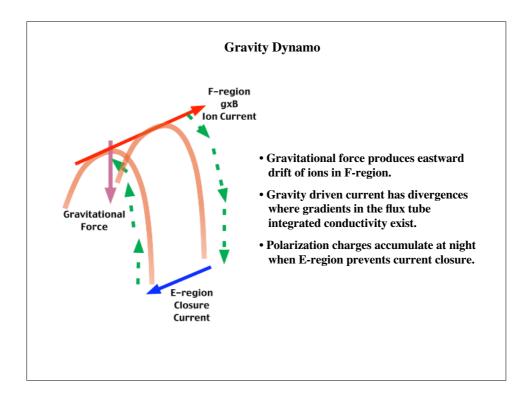


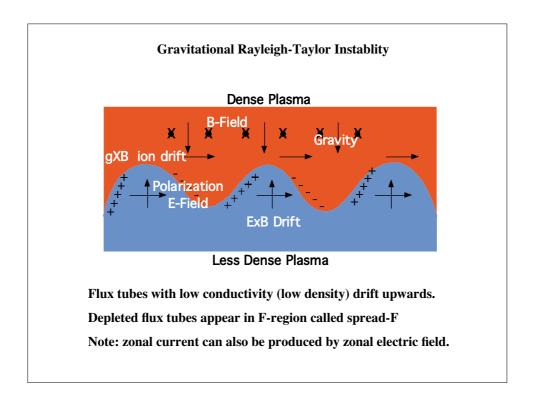


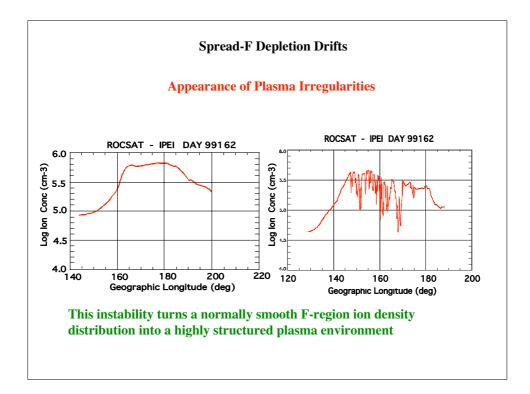


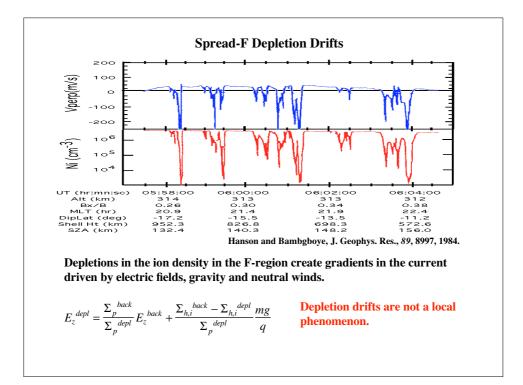












Force Parallel to B $\mathbf{F}_{\parallel} - mv\mathbf{V}_{\parallel} = 0$ <br/> $\mathbf{V}_{\parallel} = \frac{\omega_{\scriptscriptstyle B}}{v} \frac{1}{eB} \mathbf{F}_{\parallel}$ Large neutral winds are always horizontal so if U denotes the wind in the magnetic meridian<br/>then the component along the magnetic field is  $U \cos I$ This velocity will move the plasma along the magnetic field line in latitude and also move it<br/>vertically up and down.<br/>For a neutral wind  $\mathbf{F} = mv\mathbf{U}$   $\mathbf{V}_{\parallel} = U_{\parallel} = U\cos I$ If the magnetic field has an inclination I then the vertical ion velocity is<br/> $\mathbf{V}_{\scriptscriptstyle E} = U\cos I \sin I = \frac{1}{2}U\sin 2I$ A neutral wind is most effective in lifting the charged particles when the inclination is 45 deg

**Plasma Motions Parallel to B** 

If the force is applied by an electric field then  $\mathbf{F} = e\mathbf{E}$ 

$$\mathbf{F}_{\parallel} - m\upsilon\mathbf{V}_{\parallel} = 0$$
$$\mathbf{V}_{\parallel} = \frac{\omega_B}{\upsilon} \frac{1}{B} \mathbf{E}_{\parallel}$$

Electric fields parallel to the magnetic field are rare in the ionosphere except where the collision frequency is very large. We will not discuss them further.

