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*Transionospheric Propagation:  
Fundamental processes, total electron content,  
scintillation*

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These lecture notes are intended only for distribution to participants

# Transionospheric Propagation: Fundamental processes, total electron content, scintillation

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# Transionospheric Propagation

- Earth / space communication

## Outline – Lecture 1

- Introduction
  - Ionosphere
  - Radio propagation – magneto-ionic theory
- Effects of bulk ionosphere
  - Total electron content (TEC)
- Effects of small-scale irregularities
  - Scintillation

# Transionospheric Propagation

- Earth / space communication

## Outline – Lecture 2

- Radio tomography
  - Ionospheric imaging
- Effects of space weather
  - High-latitude ionosphere

# Ionospheric Basics

- Vertical profiles of electron density  
N versus h
- Variable structure – vert. and hor.
- Interaction of basic mechanisms

Continuity equation

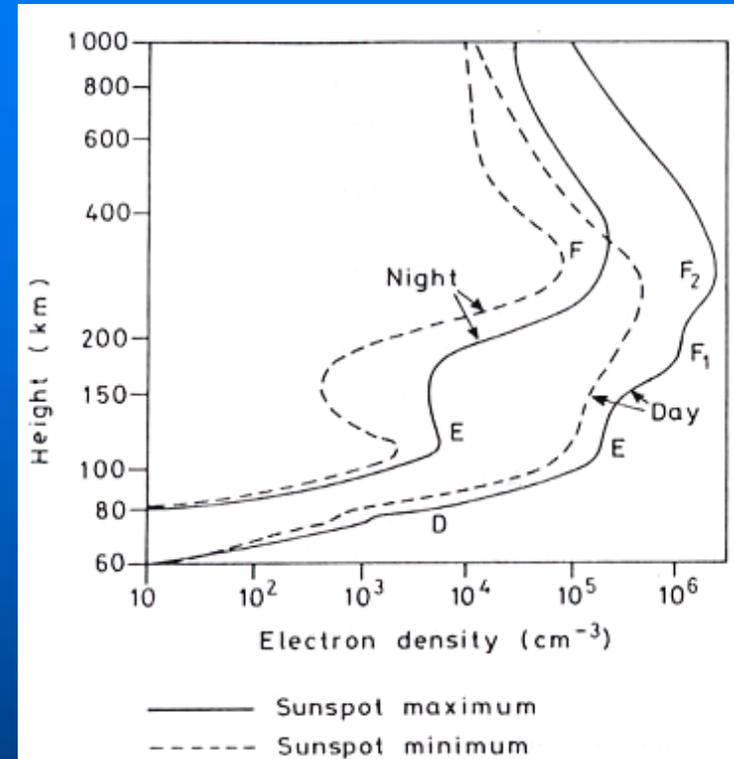
$$\Delta N / \Delta t = q - L - \text{div}(Nv)$$

Electron  
density  
rate change

Production

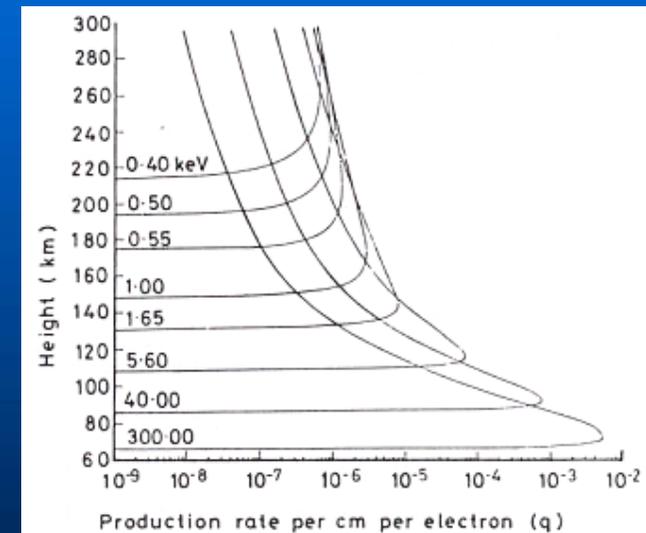
Loss

Transport



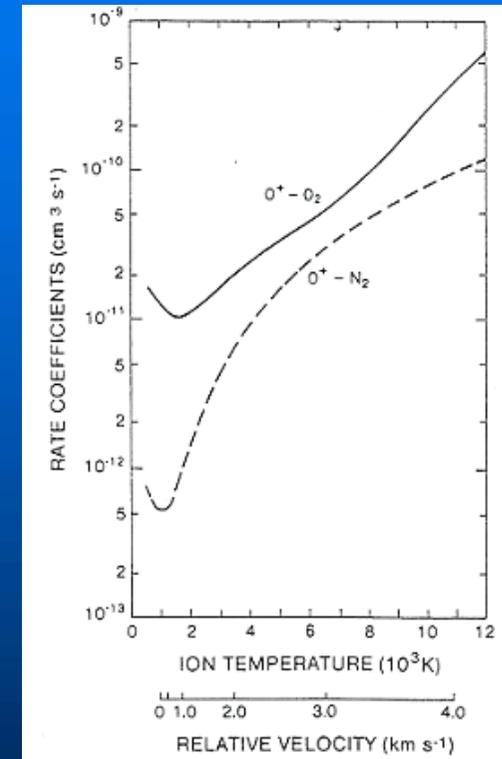
# Ionospheric Basics - Production

- Production (q)
  - solar euv radiation
    - atomic oxygen ( $O^+$ ) plasma in F2-layer
  - particle precipitation
    - impact ionisation
    - high latitudes
    - ionospheric storms



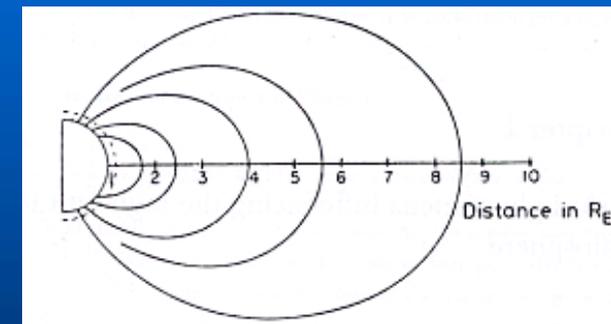
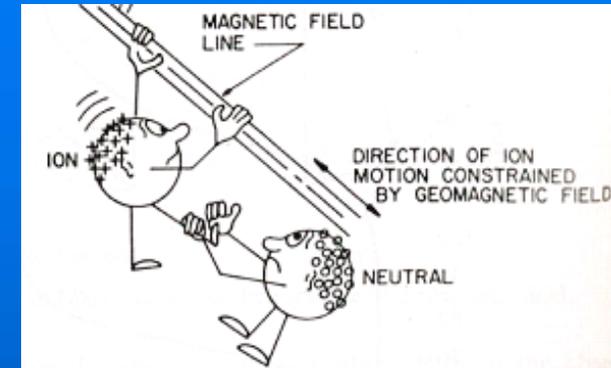
# Ionospheric Basics - Loss

- Loss (L)
  - neutral atmosphere chemistry
    - molecular species ( $N_2$ )
    - reaction rates
      - temperature dependent
      - velocity dependent
  - composition changes
    - $[O] / [N_2]$  ratio
    - production / loss processes
    - storms



# Ionospheric Basics - Transport

- Transport  $\text{div}(N\mathbf{v})$ 
  - motion constrained by magnetic field
    - neutral winds
      - diurnal, seasonal, storm
    - diffusion
      - $\text{O}^+ \leftrightarrow \text{H}^+$  protonosphere
  - electric fields -  $\mathbf{E} \times \mathbf{B}$  convection
    - equatorial anomaly
    - high latitudes



# Ionospheric Structure

- Electron density at any place and time depends on the *balance* between *many different processes*
- Ionosphere has *temporal* variability on many scales
  - solar cycle, seasonal, diurnal, etc
- Ionosphere is structured *spatially* on many different scales
  - from geographic (hundreds of kilometres) to small-scale irregularities (metres)
- *F2-region* of ionosphere is responsible for most of the effects on *transionospheric* radio signals
  - 2/3 of electrons are above F2 peak

# Plasma Basics – Plasma Frequency

- Plasma frequency ( $\omega_N$ )

Natural oscillation frequency of electrons in a plasma

$$\omega_N = (N e^2 / \epsilon_0 m_e)^{1/2}$$

$$\text{or } f_N = (80.6 N)^{1/2} \text{ when } N \text{ is in } m^{-3} \text{ and } f_N \text{ in Hz}$$

- Non-dimensional form of plasma frequency ( $X$ )

For a radio wave of frequency ( $\omega$ ) propagating in a plasma it is useful to express the plasma frequency squared in a non-dimensional form

$$X = (\omega_N / \omega)^2 = (N e^2 / \epsilon_0 m_e \omega^2)$$

# Reflection of a radio wave in a plasma

- Reflection

Radio wave of frequency ( $\omega$ ) is reflected in a plasma at vertical incidence when

$$\omega = \omega_N$$

that is, at the particular height level with the appropriate electron density

- Transionospheric propagation

For radio wave to pass through ionosphere without reflection

- need  $\omega > \omega_N$  at vertical incidence
- and  $\omega \gg \omega_N$  at oblique incidence

so only *vhf and higher frequencies* will cross the ionosphere

# Plasma Basics - Gyrofrequency

- Gyrofrequency ( $\omega_B$ )

Gyration frequency of electrons about a magnetic field

$$\omega_B = B e / m_e \quad \text{or} \quad f_B = B e / 2\pi m_e$$

- for Earth's magnetic field  $B \sim 0.5 \text{ T}$  then  $f_B \sim 1.4 \text{ MHz}$

- Non-dimensional form of gyrofrequency ( $Y$ )

For a radio wave of frequency ( $\omega$ ) propagating in a plasma it is useful to express the gyrofrequency in a non-dimensional form

$$Y = \omega_B / \omega = B e / m_e \omega$$

- Often useful to treat gyrofrequency in terms of components *along* ( $Y_L$ ) and *transverse* to the magnetic field ( $Y_T$ )

For many transionospheric situations the propagation can often to be considered to be *quasi-longitudinal* so that  $Y_T$  can be neglected

# Basic Magneto-ionic Theory

How is radio wave affected by ionosphere?

Need *refractive index* for propagation of radio wave in ionosphere

Appleton Equation (Appleton-Hartree Equation)

$$n^2 = 1 - \frac{X}{1 - jZ - \frac{Y_T^2}{2(1 - X - jZ)} \pm \left( \frac{Y_T^4}{4(1 - X - jZ)^2} + Y_L^2 \right)^{1/2}}$$

*'It is virtually impossible for an ordinary mortal to make much sense of the Appleton equation(s) in their full glory.'*

*(Hunsucker and Hargreaves, 2003)*

# Appleton Equation

$$n^2 = 1 - \frac{X}{1 - jZ - \frac{Y_T^2}{2(1 - X - jZ)} \pm \left( \frac{Y_T^4}{4(1 - X - jZ)^2} + Y_L^2 \right)^{1/2}}$$

- $X = (\omega_N / \omega)^2$   
where  $\omega_N = (Ne^2 / \epsilon_0 m_e)^{1/2}$  is *plasma frequency*  
 $X$  depends on *electron density (N)*
- $Y = \omega_B / \omega$   
where  $\omega_B = Be / m_e$  is *electron gyrofrequency*  
 $Y$  depends on *magnetic field (B)*
- $Z = \nu / \omega$   
 $Z$  depends on the *electron collision frequency ( $\nu$ )*
- Refractive index ( $n$ ) of an ionised medium with electron density ( $N$ ), a magnetic flux ( $B$ ) and electron collision frequency ( $\nu$ )

## Appleton Equation (cont)

$$n^2 = 1 - \frac{X}{1 - jZ - \frac{Y_T^2}{2(1 - X - jZ)} \pm \left( \frac{Y_T^4}{4(1 - X - jZ)^2} + Y_L^2 \right)^{1/2}}$$

- $n = \mu - j\chi$  is complex,
  - real part - phase propagation
  - imaginary part - absorption of wave
  - $Z$  non-dimensional collision frequency
- $\pm$  signs correspond to ordinary and extraordinary waves
- $Y$  has components along ( $Y_L$ ) and transverse ( $Y_T$ ) to the magnetic field

*Fortunately, for most applications approximations can be used that reduce the Appleton equation to very much simpler forms*

# Appleton Equation – Useful Approximations for Transionospheric Propagation

- $Z = 0$  - since collisions are only important in the lower ionosphere (D-layer) where the neutral density is high
- $Y = 0$  - effects of magnetic field can *often* be neglected because radio frequency  $\gg$  gyrofrequency ( $\omega \gg \omega_B$ )
- $Y_T = 0$  - even when magnetic field is included in most circumstances only the component in the propagation direction ( $Y_L$ ) needs to be considered
- $\omega \gg \omega_N$  - for transionospheric propagation the radio frequency must be very much greater than the maximum plasma frequency encountered ( $f_oF2$ )

# Appleton Equation – No Magnetic Field

Neglecting the magnetic field ( $Y=0$ ) and collisions ( $Z=0$ )

$$n = (1 - X)^{1/2} = \{1 - (\omega_N / \omega)^2\}^{1/2} = \{1 - N e^2 / \epsilon_0 m_e \omega^2\}^{1/2}$$

For transionospheric signals with  $\omega \gg \omega_N$  can expand binomially and neglect higher order terms so that the refractive index

$$n = 1 - X/2 = 1 - N e^2 / 2\epsilon_0 m_e \omega^2 = 1 - 40.3 N / f^2$$

*(with  $N$  in  $m^{-3}$  and  $f$  in Hz)*

While  $n = 1 - X/2$  is the approximation currently used for most transionospheric propagation applications, it must be noted that for super-resolution (< 2cm error) use of GPS positioning consideration of higher-order terms involving the magnetic field is becoming of interest

# Phase velocity of radio wave

The phase velocity of the radio wave will be given by

$$v_p = c / n = c / (1 - N e^2 / 2 \epsilon_0 m_e \omega^2)$$

- phase velocity  $> c$
- phase of carrier wave will advance wrt free space
- Doppler shift in frequency

Consider a radio wave of frequency ( $f$ ) and wavelength ( $\lambda$ ) propagating along a path ( $l$ ) through the ionosphere:

# Carrier Phase Advance and Doppler Shift

After travelling a distance  $dl$  (ie  $dl/\lambda$  wavelengths) *phase of the wave* has changed by

$$2\pi dl/\lambda = 2\pi f n dl / c$$

Thus over a path  $l$  through the ionosphere the *phase change* will be

$$-(2\pi f / c) \int n dl / c = -2\pi f l / c + (2\pi \times 40.3 / cf) \int N dl$$

Change in phase of a wave  
travelling at the speed of light

Phase *advance*  
due to the *medium*

- phase advance is *cumulative* along path
- depends on the *Total Electron Content (TEC)* along slant path

$$N_T = \int N dl$$

Numerically, *phase advance* (in radians) due to the ionosphere is

$$\varphi = (8.45 \times 10^{-7}) N_T / f \quad (\text{with } N_T \text{ in } m^{-2} \text{ and } f \text{ in } Hz)$$

Since *frequency* is *rate of change of phase*, ionosphere imposes *Doppler shift* on the wave

# Group Propagation

Group propagation – group refractive index ( $n_g$ )

$$n_g = c / u = c (\partial k / \partial \omega) = c (\partial (n\omega) / \partial \omega) = c(n + \omega (\partial n / \partial \omega))$$

Group velocity ( $u$ )

$$u = c / n_g = c (1 - N e^2 / \epsilon_0 m_e \omega^2)^{1/2}$$

- group velocity ( $u$ )  $< c$
- group delay of modulation phase
- time delay of pulse

# Group Delay and Time Delay

If carrier wave of frequency  $f$  is modulated at a frequency  $f_m$  the phase of the modulation is *retarded* by

$$\varphi_m = - 8.45 \times 10^{-7} (f_m / f^2) N_T$$

There is a *group delay* because the modulation travels at the group velocity ( $u < c$ )

Hence, there is a *time delay* of a pulse

$$\Delta t = - (8.45 \times 10^{-7} / 2\pi f^2) N_T$$

Both *group and time delays* depend directly on Total Electron Content (*TEC*) – line integral of electron density along the ray path  $N_T = \int N dl$

# Ionospheric Time Delay

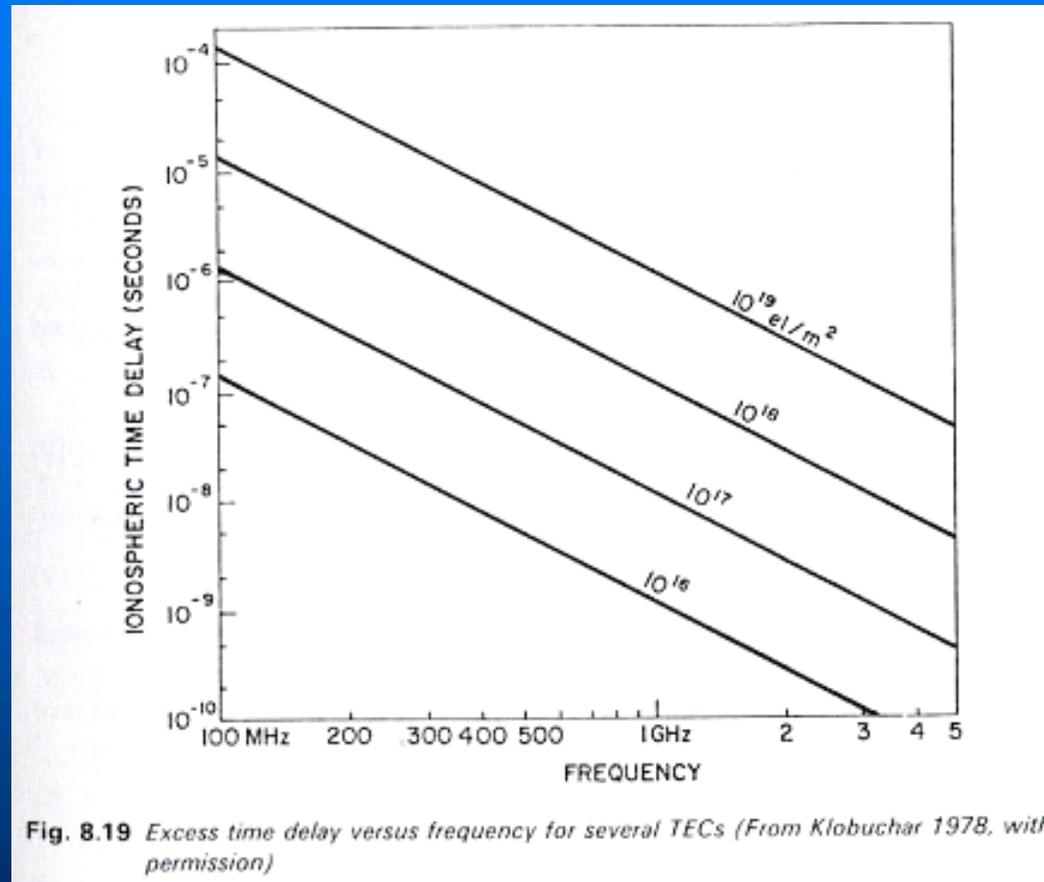


Fig. 8.19 Excess time delay versus frequency for several TECs (From Klobuchar 1978, with permission)

# Appleton Equation – Magnetic Field

Effect of magnetic field

$$n^2 = 1 - X / (1 \pm Y_L)$$

or  $n = 1 - \frac{1}{2} X \pm \frac{1}{2} XY_L$  for transionospheric propagation

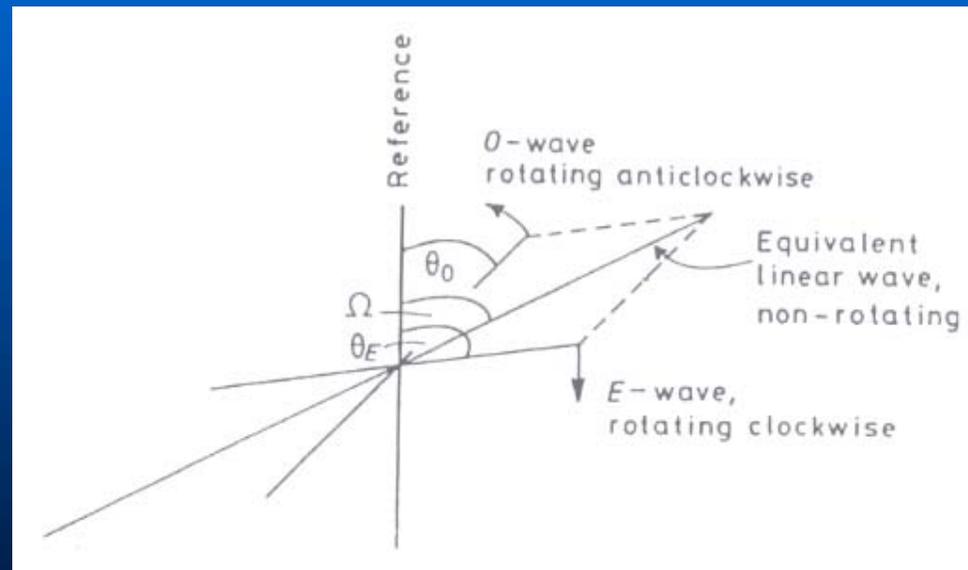
- field component in propagation direction
- longitudinal approximation -  $Y_L$  only
- $\pm$  ordinary and extraordinary waves
- o and e waves travel at different speeds
- leads to polarisation (Faraday) rotation
- $n_O - n_E = XY_L$  if radio frequency ( $f$ )  $\gg$  gyrofrequency ( $f_B$ )

# Faraday Effect – Polarisation Rotation

When geomagnetic field is taken into account the propagation comprises *ordinary and extraordinary* waves - circularly polarised in opposite directions

If  $\theta_O$  and  $\theta_E$  are the respective instantaneous angles of the ordinary and extraordinary components, these combine to give a linearly polarised wave at an angle

$$\Omega = (\theta_O + \theta_E) / 2$$



# Faraday Rotation (continued)

Ordinary and extraordinary waves have different refractive indices and travel at different speeds, so after distance  $dl$  in the medium the polarisation of resultant wave will have rotated by

$$d\Omega = (\pi f / c) (n_O - n_E) dl = (\pi f / c) XY_L dl = (\pi f / c) ((f_N)^2 f_L / f^3) dl$$

Thus for a path through the ionosphere where both the electron density and the magnetic field vary, the polarisation rotation will be

$$\Omega = (8.45 \times 10^{-7} / f^2) \int f_L N dl = (2.36 \times 10^4 / f^2) \int B_L N dl$$

where  $B_L$  is the component of magnetic field in the propagation direction

If an appropriate mean value of  $B_L$  can be assumed then

$$\Omega = 2.36 \times 10^4 \langle B_L \rangle / f^2 \int N dl = 2.36 \times 10^4 \langle B_L \rangle / f^2 N_T$$

that is *Faraday rotation* depends on *TEC*

# Ionospheric Faraday Rotation

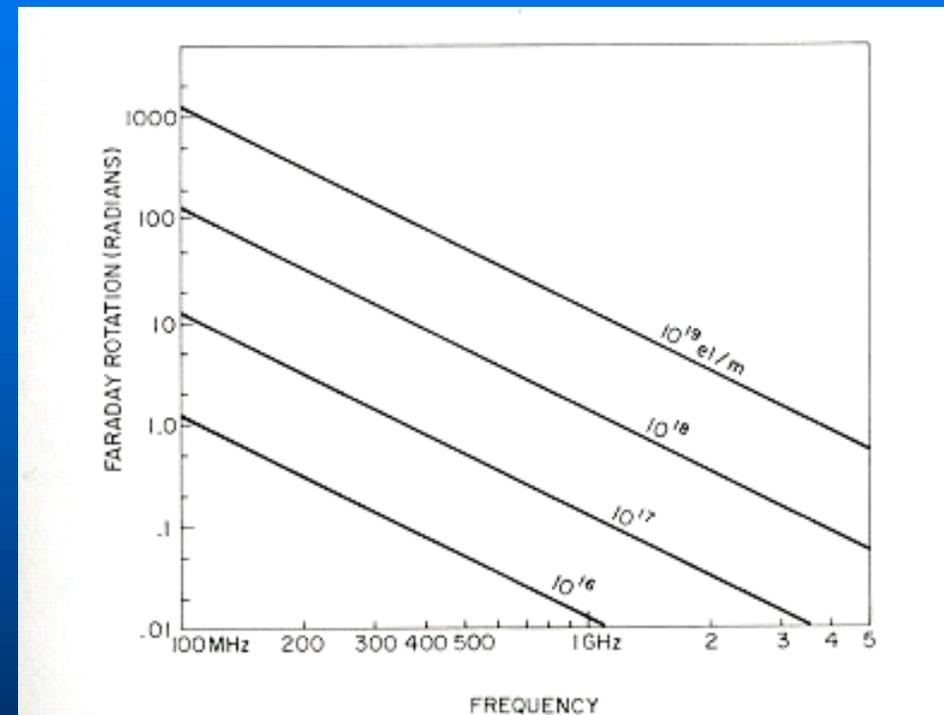
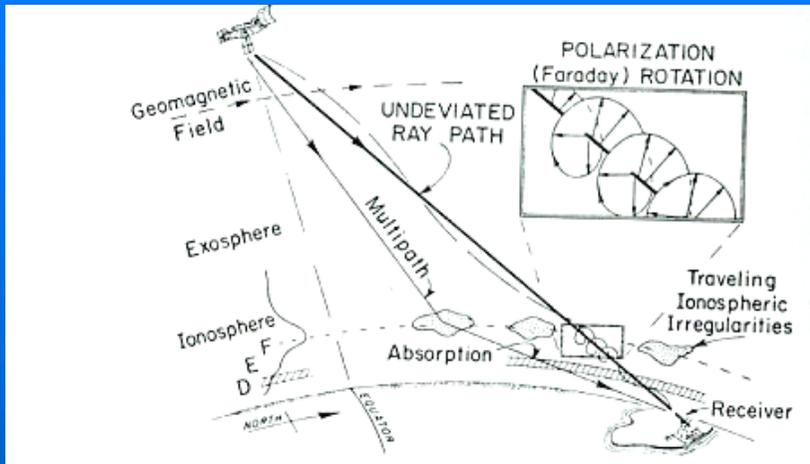


Fig. 8.18 Approximate Faraday rotation as a function of frequency and TEC for a ray path in a magnetic meridian (From Klobuchar 1978, with permission)

For particular station and geometry ie mean  $B_L$

# Importance of Total Electron Content

For a radio wave crossing the ionosphere

- Carrier phase advance
- Group delay
- Faraday rotation
- Refraction

all depend on

- Total Electron Content (TEC)
- line integral of electron density along ray path
- $N_T = \int N dl$

# Practical Significance of TEC

Radio systems using signals from satellites or natural sources that cross the ionosphere will be subject to errors due to the line integral of the electron density, that is, the *total electron content (TEC)* along the ray path

Applications include:

- Navigation
- Positioning
- Time transfer
- Radar
- Radio astronomy

Mitigation of the effects requires measurement or modelling of TEC

# Total Electron Content (TEC) –some definitions

- *Slant total electron content*  $N_T = \int N dl$ 
  - TEC along slant ray path  $l$
- *Vertical total electron content*  $N_T = \int N dh$ 
  - measure using incoherent scatter radar
  - integrate through tomographic image
- *Equivalent vertical electron content*
  - assume thin-layer ionosphere at chosen height
  - simple geometrical mapping function  $dl = dh \sec \chi$
  - usually what is meant by TEC
- *Faraday electron content*
  - assume mean magnetic field  $\langle B_L \rangle$
  - upper limit usually taken  $\sim 2000$  km

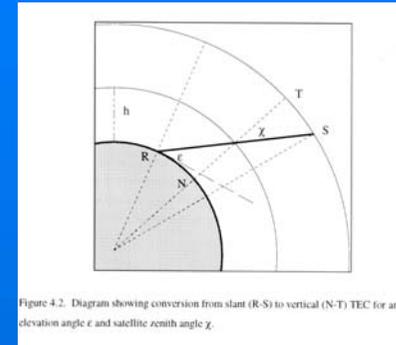


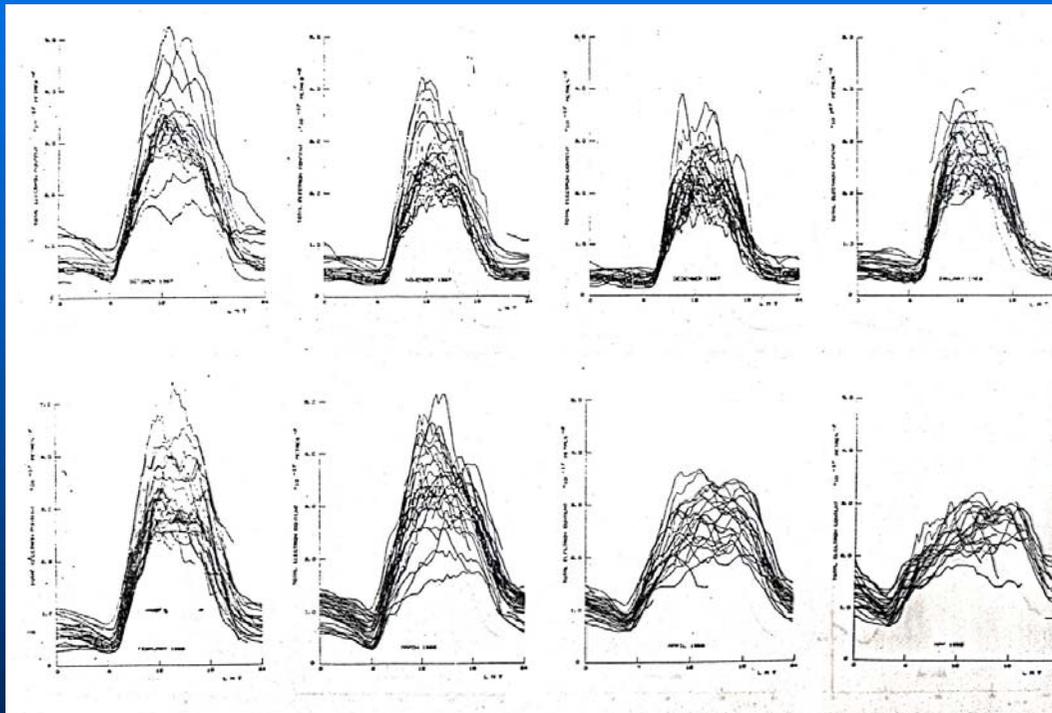
Figure 4.2. Diagram showing conversion from slant (R-S) to vertical (N-T) TEC for an elevation angle  $\epsilon$  and satellite zenith angle  $\chi$ .

# Measurement of total electron content (TEC)

- Faraday rotation
  - Early measurements
  - Geostationary satellites
  - Diurnal variations
  - TEC morphology
- Differential carrier phase (differential doppler)
  - NNSS or NIMS satellites in low Earth orbit
  - TEC versus latitude
  - Radio tomography
- Combinations of techniques
  - Protonospheric content
  - GPS - phase and code measurements
- TEC Units
  - $1 \text{ TECU} = 10^{16} \text{ m}^{-2}$

# Mid-latitude TEC – temporal variations

Diurnal TEC plots from geostationary satellite Faraday rotation of radio signals at about 136MHz



Aberystwyth 52° N Europe

- Daytime maximum
- Low nighttime values
- Equinox maximum
- Summer daytime bite-out
- Day-to-day variability

# Mid-latitude TEC - temporal variations

## Diurnal TEC plots from geostationary satellite Faraday rotation

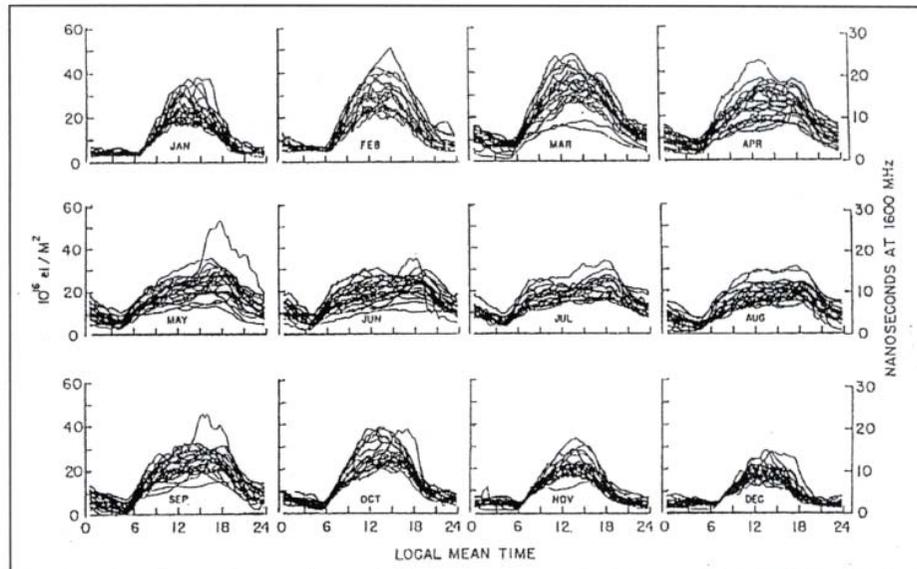


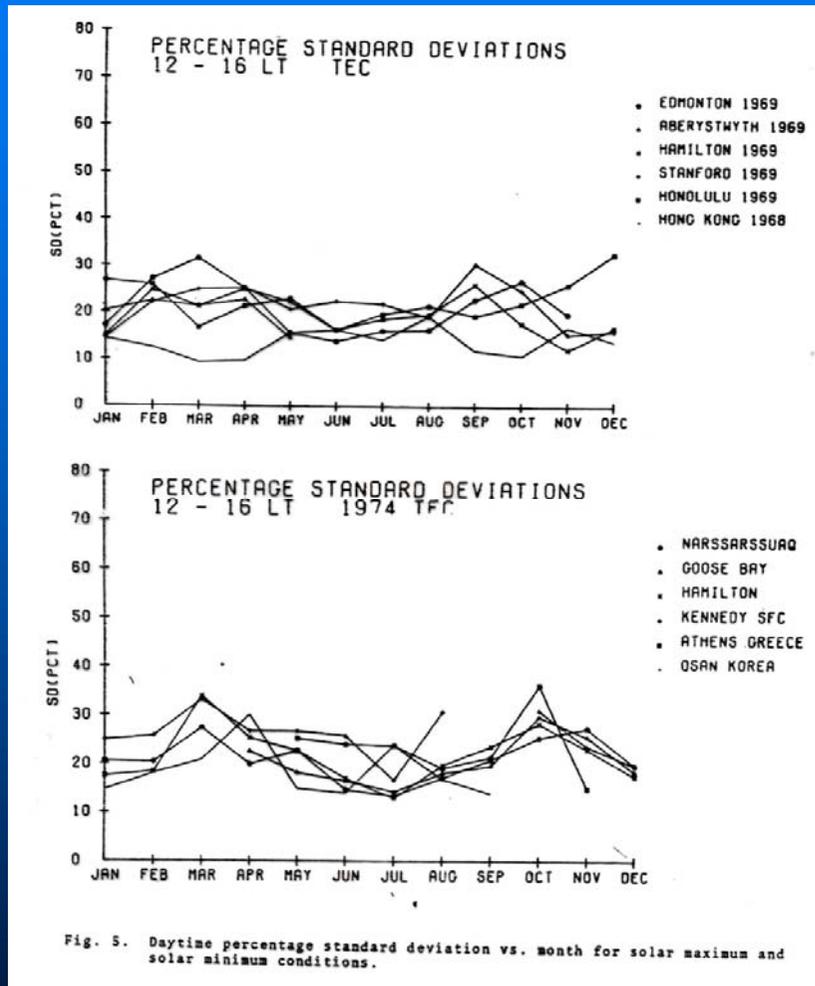
Figure 2.2. Equivalent vertical total electron content, in over-plot format, from observations of ATS-3 made at the Sagamore Hill Radio Observatory, Hamilton, Massachusetts, in 1972 (Mendillo and Klobuchar, 1974).

### Hamilton 42° N USA

- Daytime maximum
- Nighttime decline
- Equinox maximum
- Low summer daytime
- Day-to-day variability

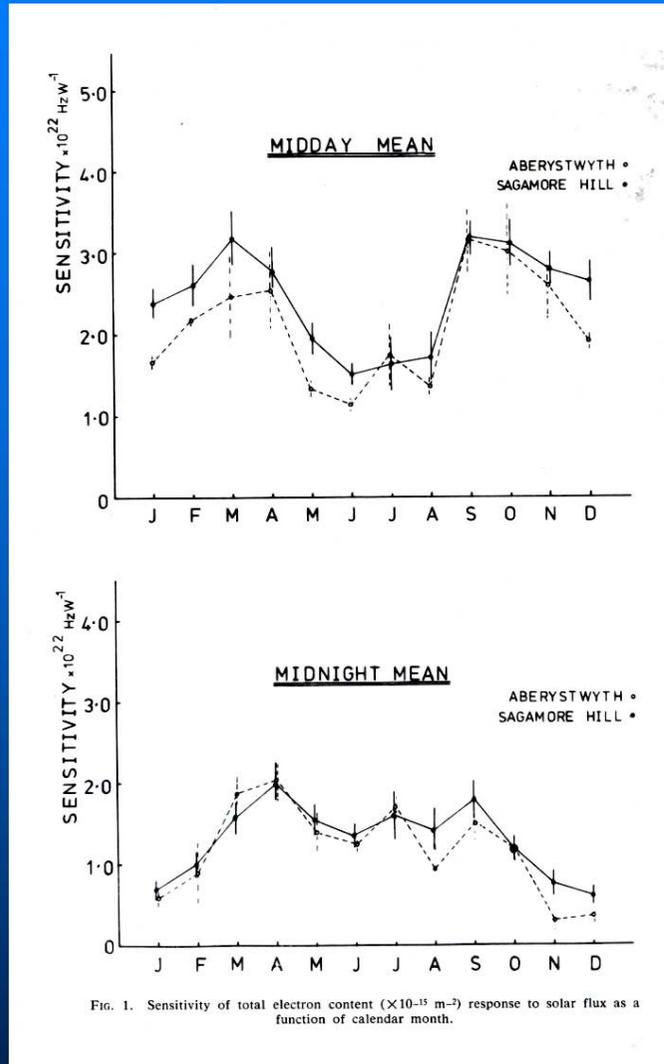
# TEC Variability

## Percentage Standard Deviations



- Day-to day variability
- Standard deviations ~ 25%

# Mid-latitude TEC and Solar Activity



$$\text{TEC} = \text{TEC}(80) + a(\bar{S} - 80) \times 10^{15} \text{ m}^{-2}$$

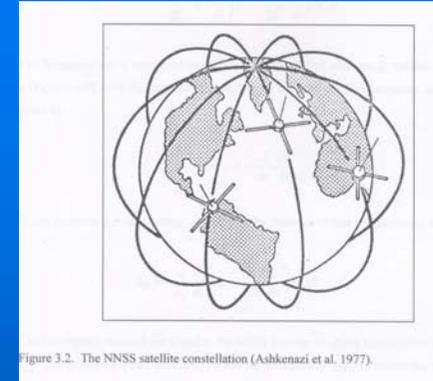
where  $\text{TEC}(80)$  = total electron content at  $80 \times 10^{-22} \text{ W m}^{-2} \text{ Hz}^{-1}$   
 $a$  = sensitivity of TEC to change in solar flux  
and  $\bar{S}$  = monthly mean solar flux at 10.7 cm.

- Seasonal dependence during daytime
- Latitudinal dependence in winter

- Highest TECs are found at the equatorial anomaly latitudes at solar maximum

# NIMS Satellites - spatial TEC gradients

- NIMS – Navy Ionospheric Monitoring Satellites
- up to six satellites, formerly NNSS
- circular polar orbits at 1100 km altitude
- coherent transmissions at 150 MHz and 400 MHz
- differential carrier phase (differential Doppler) technique
- measure total electron content along ray paths
- TEC as a function of latitude



# Differential Carrier Phase (Differential Doppler) Technique

Satellite transmits two *coherent* frequencies  $f$  and  $pf$ , where  $p$  is constant (NIMS satellites transmit on 150MHz and 400MHz so that  $p = 8/3$ )

Compare *received phase of lower frequency* with that of the *higher frequency divided by  $p$*

$$\Delta\varphi = \varphi_f - \varphi_{pf} = \{-2\pi f l / c + 2\pi \times 40.3 N_T / f c\} - \{(1/p)(\{-2\pi p f l / c + 2\pi \times 40.3 N_T / p f c\})\}$$

The *first and third terms cancel* because they represent the phase changes for *free space propagation* of the two signals along the path

Thus the *differential phase shift* due to the ionospheric TEC is

$$\Delta\varphi = \{1 - 1 / p^2\} (8.45 \times 10^{-7}) N_T / f$$

Can measure *relative phase accurately* but still have  $2\pi$  ambiguity to solve to get *absolute TEC*

# Absolute TEC from Differential Carrier Phase Measurements

- With two or more stations separated in latitude can match the observation in the region of overlap to give the same equivalent vertical TEC
- Hence obtain *absolute* TEC measurements versus latitude

Equivalent  
Vertical TEC

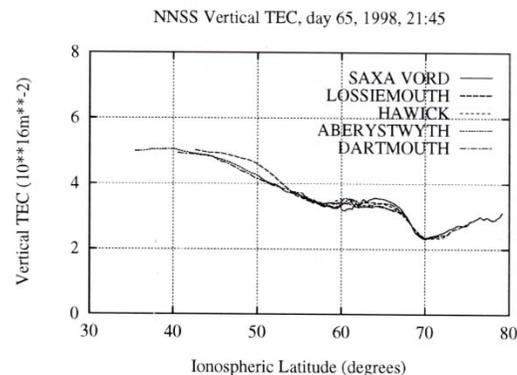
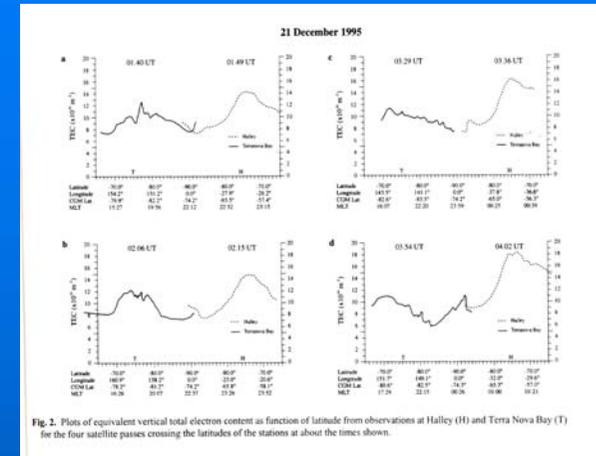


Figure 4.4. Equivalent Vertical TEC obtained from the multi-station method from NNSS observations at 5 stations in the UK of the satellite pass at 21:45 UT on 6 March 1998.

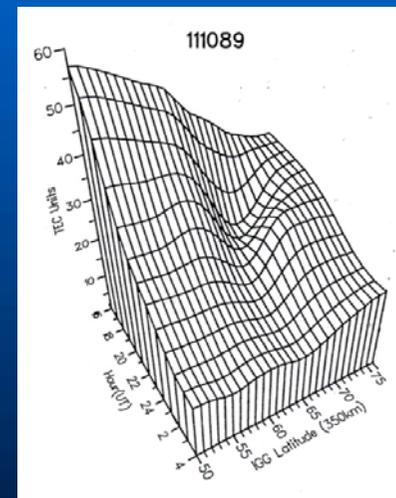
Latitude

# Importance of NIMS TEC studies

- Latitudinal TEC gradients
- Spatial structure
- Remote regions – polar cap
- Equatorial anomaly region
- Main (mid-latitude) trough
- Radio tomography



TEC across Antarctica



TEC in main trough

# GPS Satellites

- > 24 satellites in 6 orbital planes
- circular orbits at  $55^\circ$  inclination
- 20200 km altitude
- 12 siderial hours period
- same track 237 s earlier each day
- L1 frequency 1575.42 MHz
- L2 frequency 1227.60 MHz
- pseudo random noise (PRN) modulation
- coarse acquisition (C/A) code on L1 carrier
- precision (p) code on both L1 and L2
- receiver uses PRN code to estimate travel time of signal
- calculate distance or pseudo-range from satellite
- receiver also determines phase pseudo-range for carrier
- RINEX (receiver independent exchange) data format
- observables – phases, code ranges, Doppler shifts on 2 freqs
- navigation message – orbit parameters

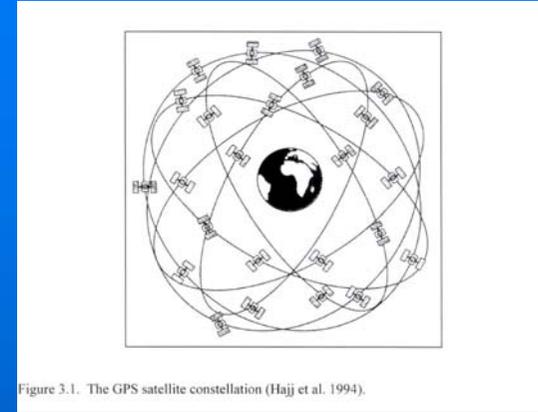


Figure 3.1. The GPS satellite constellation (Hajj et al. 1994).

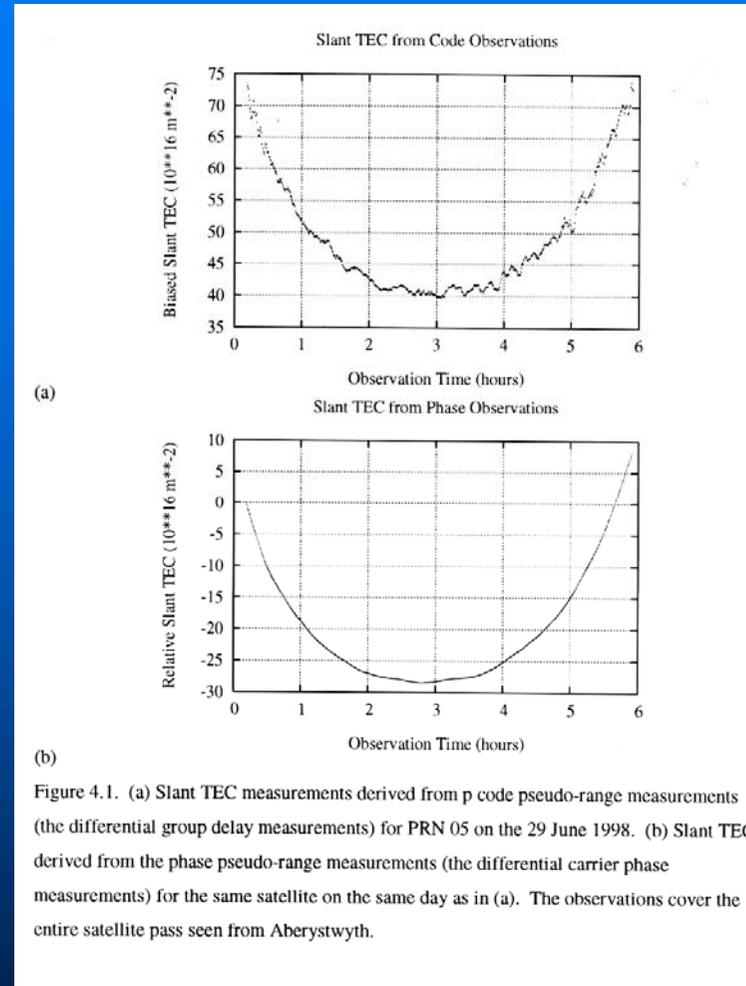
# GPS slant TEC during pass

‘p code pseudo range’  
(differential group delay)  
measurements

‘phase pseudo range’  
(differential carrier phase)  
measurements

Processing to determine  
many bias errors and  
find absolute TEC

multipath



# GPS TEC – diurnal plots

Data from many passes  
with differing geometries

Processing – eg SCORE

Solve for unknowns to get  
absolute TEC

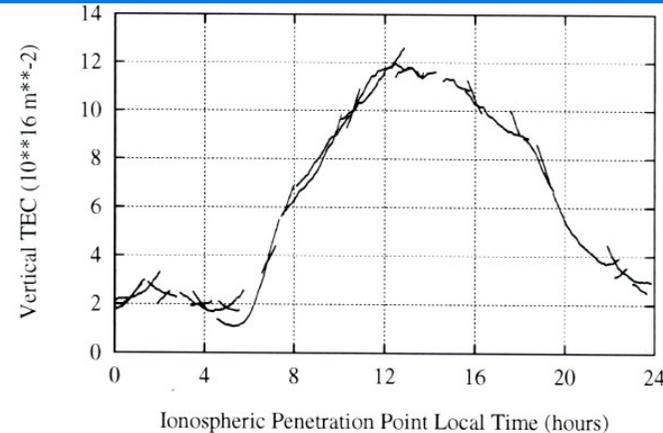
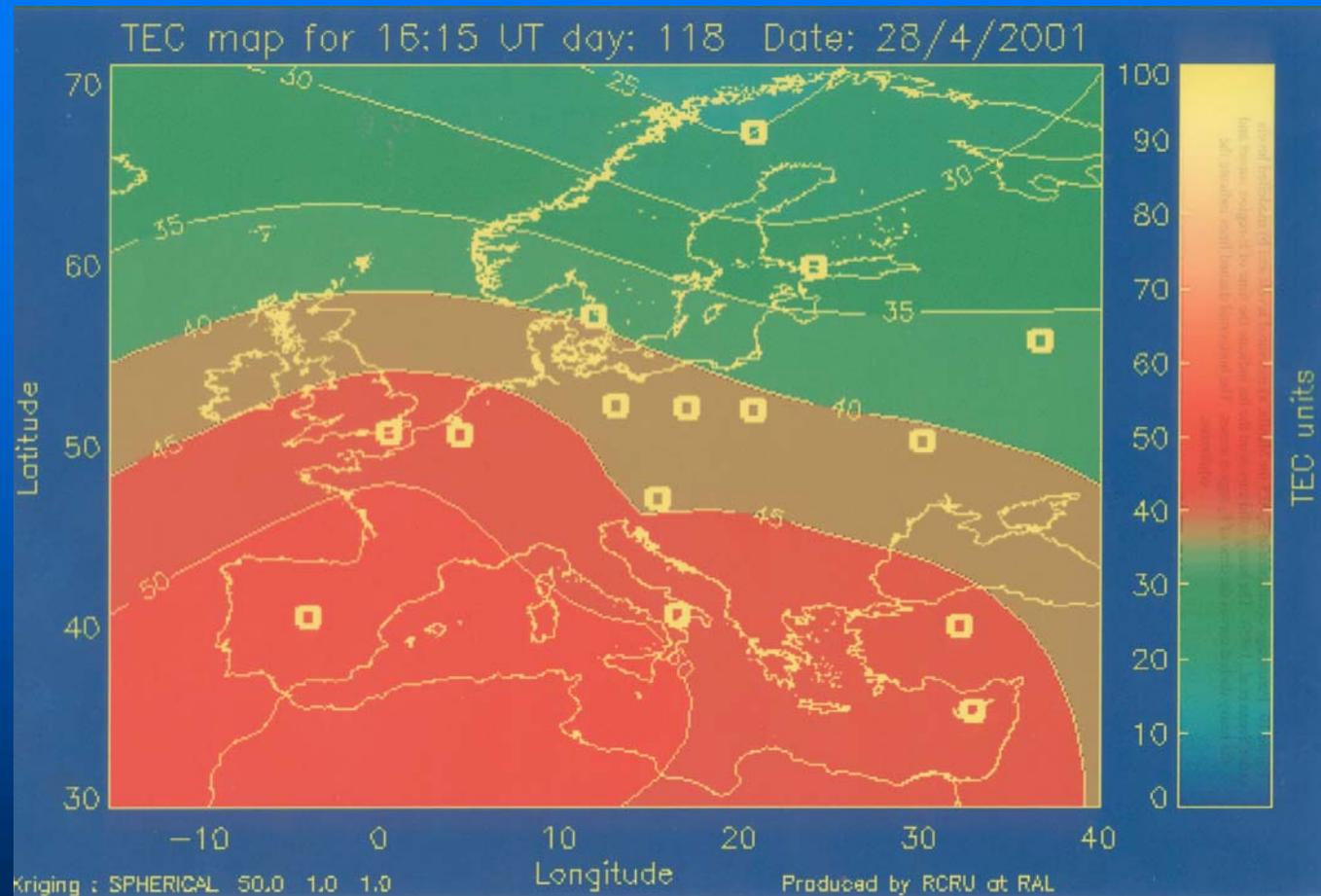


Figure 4.3. Equivalent Vertical TEC obtained from SCORE processed GPS observations on 6 March 1998 for the one degree wide latitude band centred over Aberystwyth.

1 TECU represents a range error of  $\sim 16$  cm for GPS L1 frequency

# TEC Maps from GPS



# Effects of space weather on mid-latitude TEC

## - ionospheric storms

- strong enhancements on first day
- sudden collapse
- very steep spatial gradients
- depressed values for several days
- composition changes
- contraction of plasmapause
- storm enhanced densities (SEDs)
- slow refilling of plasmasphere

# Mid-latitude TEC during Geomagnetic Storms

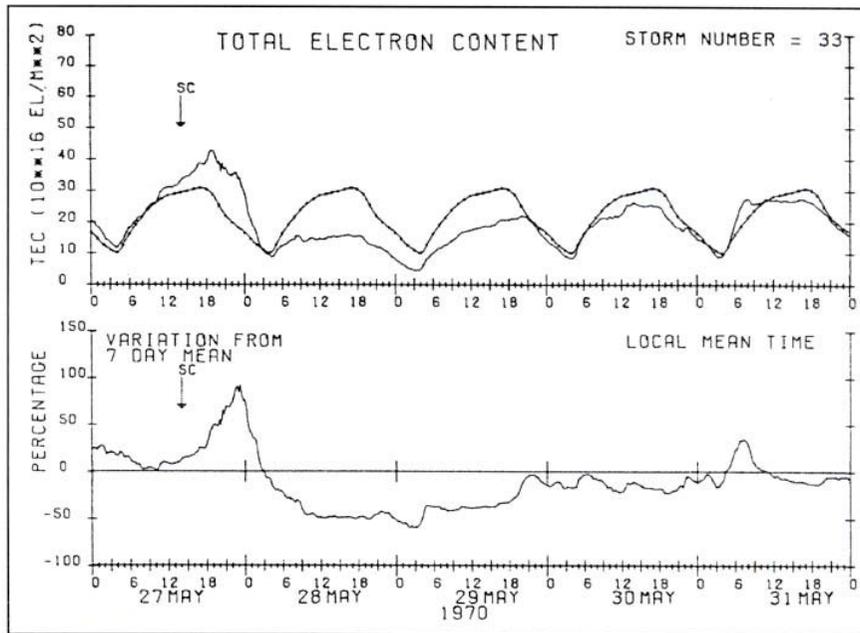


Figure 2.3. The development of an ionospheric storm. The top plot shows the TEC for the first few days of a storm plotted with the mean TEC values of the seven days prior to the commencement of the storm. The lower plot is the difference between the recorded and mean values (Mendillo and Klobuchar, 1974).

- Initial positive phase
- Collapse around 1800 LT on first day of storm
- Depleted TEC for several days subsequently
- Low nighttime values
- Composition changes
- $[O] / [N_2]$  ratio
- Plasmapause contraction

# Storm Contraction of Plasmapause

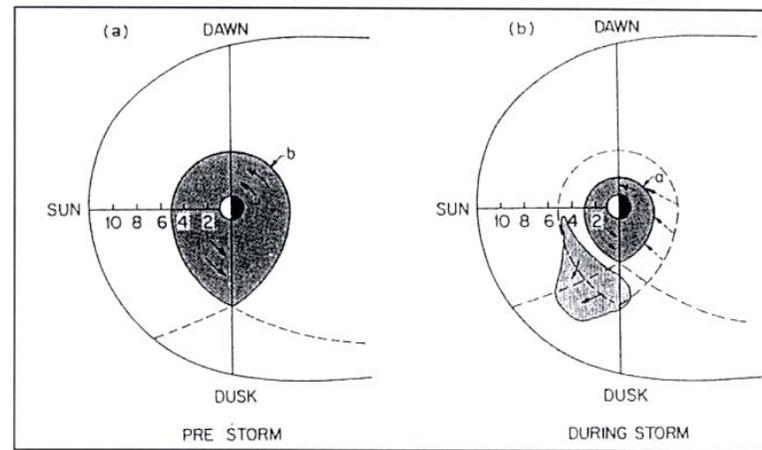
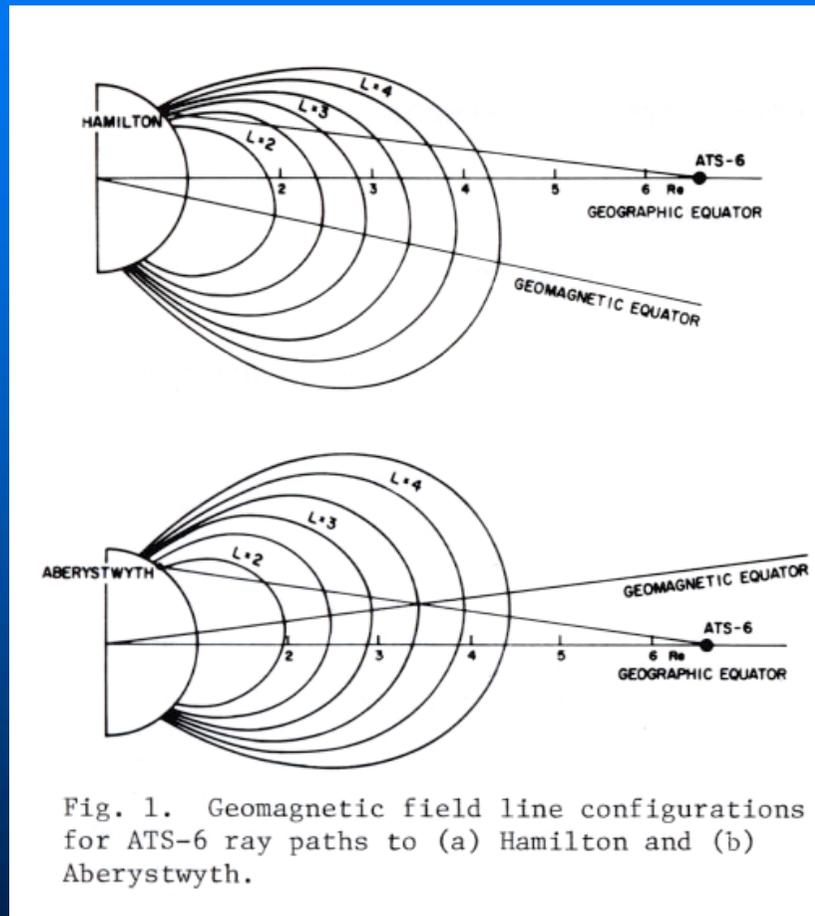


Figure 2.5. Diagram of the plasmasphere, a) quiet period before storm, b) after increased convection has peeled off the outer layers of the region. The grey areas denote high plasma concentrations, filled arrows denote plasma motion, the dotted arrows show the movement of the plasmapause and the scale is in L (Chappell, 1972).

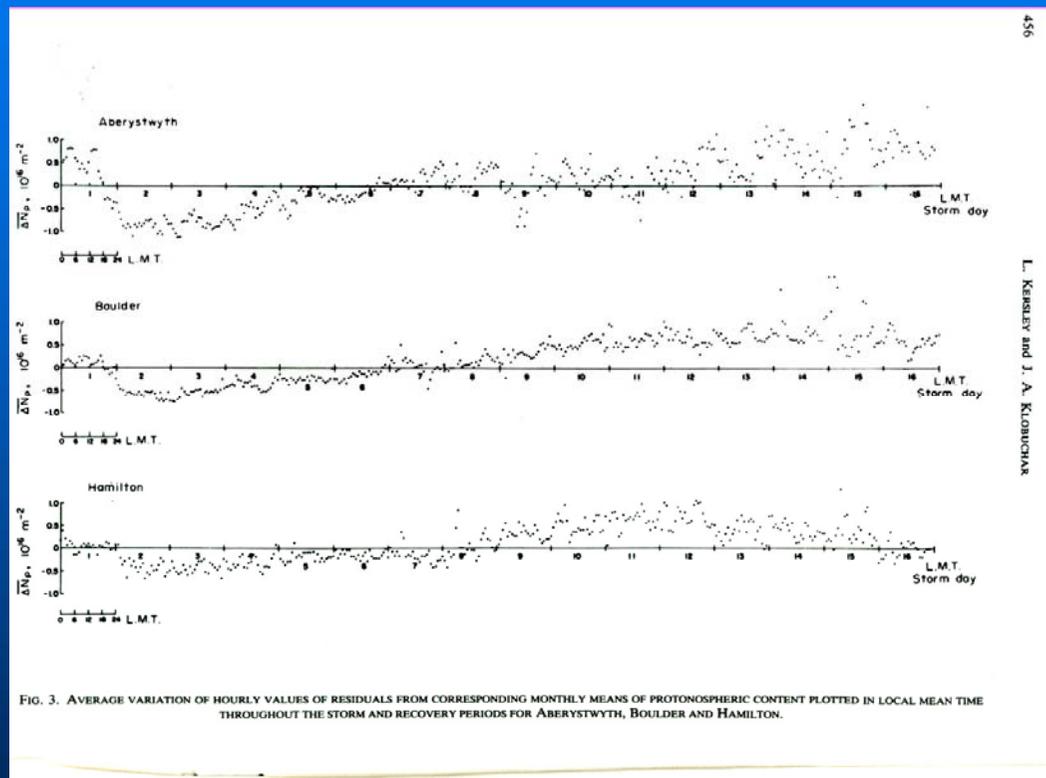
- Can result in very severe spatial gradients in mid-latitude ionosphere - storm enhanced densities (SEDs)
- Problems for GPS applications (eg WAAS & EGNOS)

# Protonospheric Content - Flux-Tube Geometry



- Flux tubes replenished by diffusion from ionosphere
- $O^+ / H^+$  transition
- Flux Tube Volume  $\sim L^3$
- Low L-shells – diurnal exchange with ionosphere
- Higher L-shells – never fill completely between storms

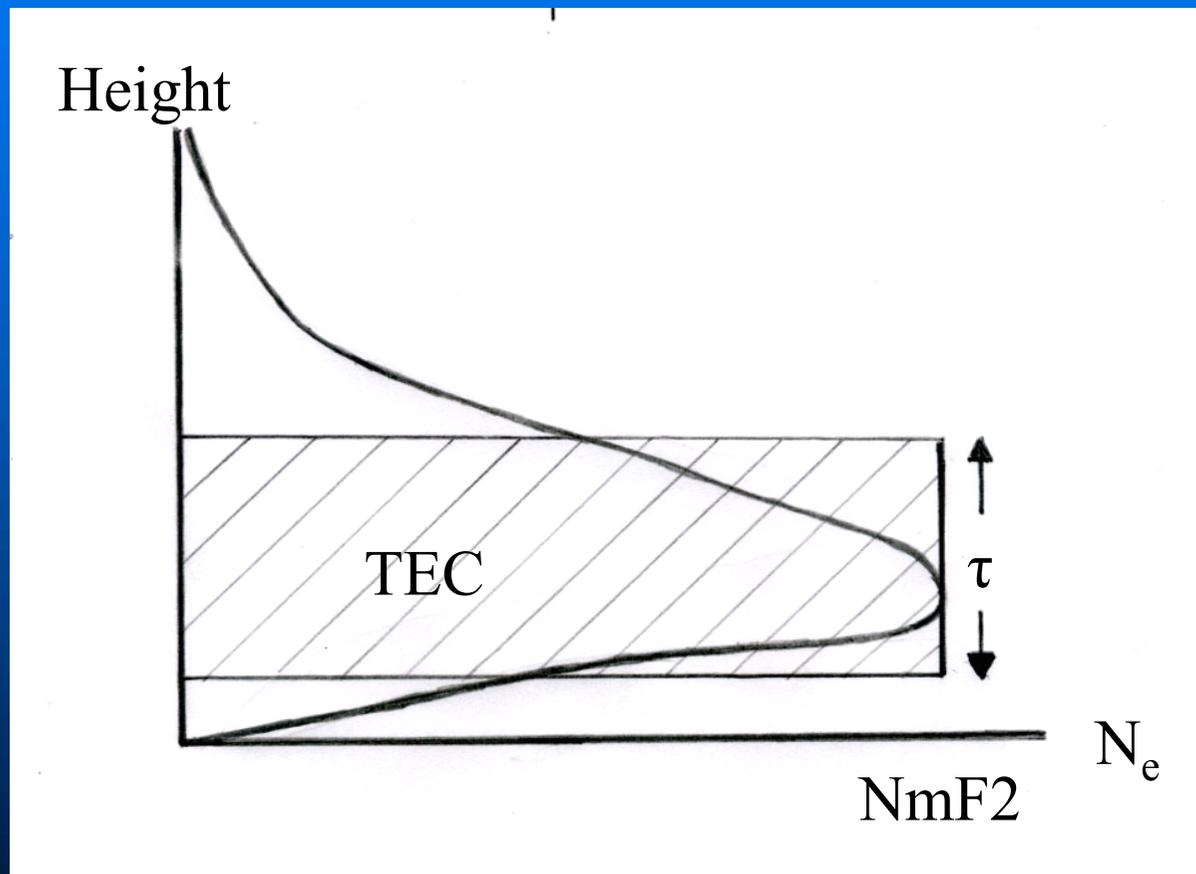
# Protonospheric Content Storm Collapse and Slow Recovery



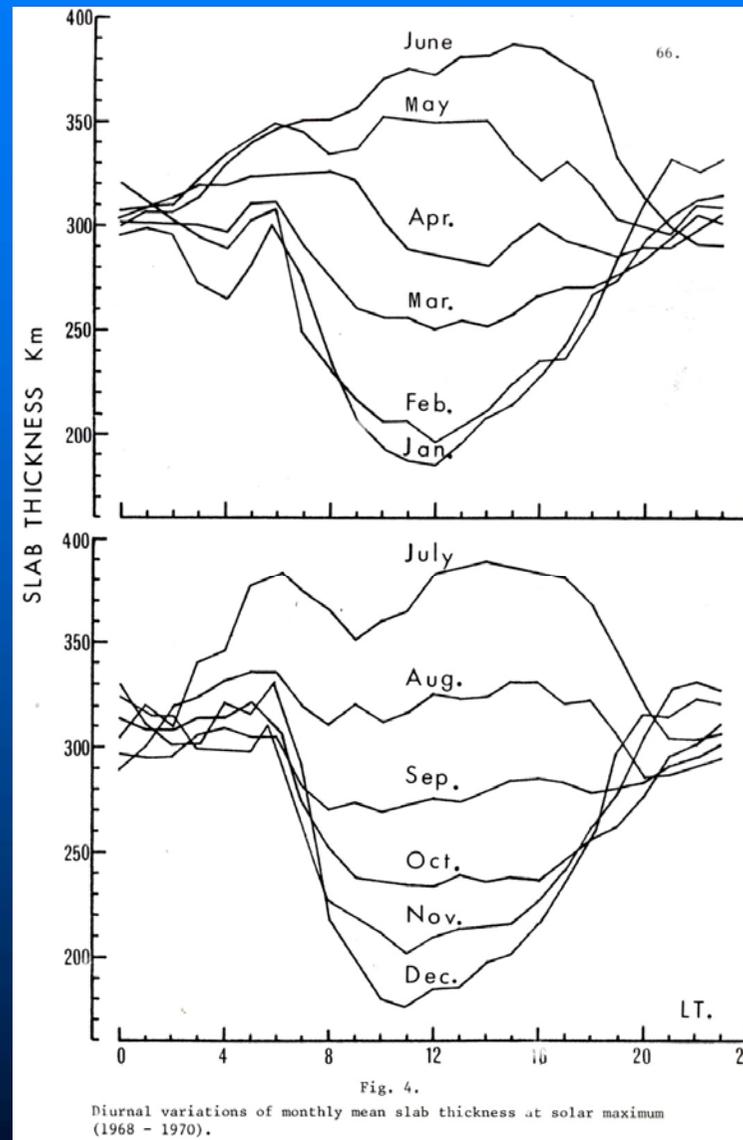
- Collapse in evening of storm day
- Slow replenishment over many days

# Slab Thickness ( $\tau$ )

Slab Thickness ( $\tau$ ) = TEC / Maximum Electron Density (NmF2)



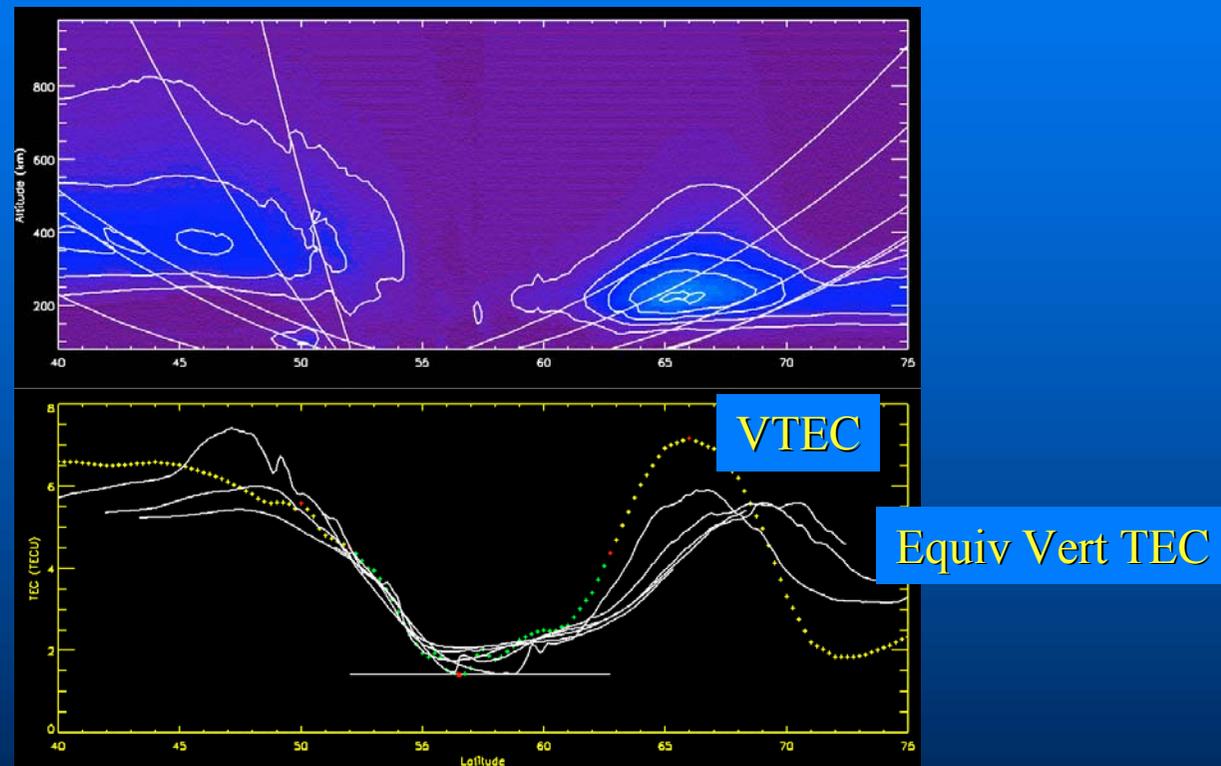
# Slab Thickness Variations



- ~ 300 km at night
- max summer daytime
- min winter daytime

# Accuracy of TEC measurements

## Problems with layer height assumption in equivalent vertical TEC

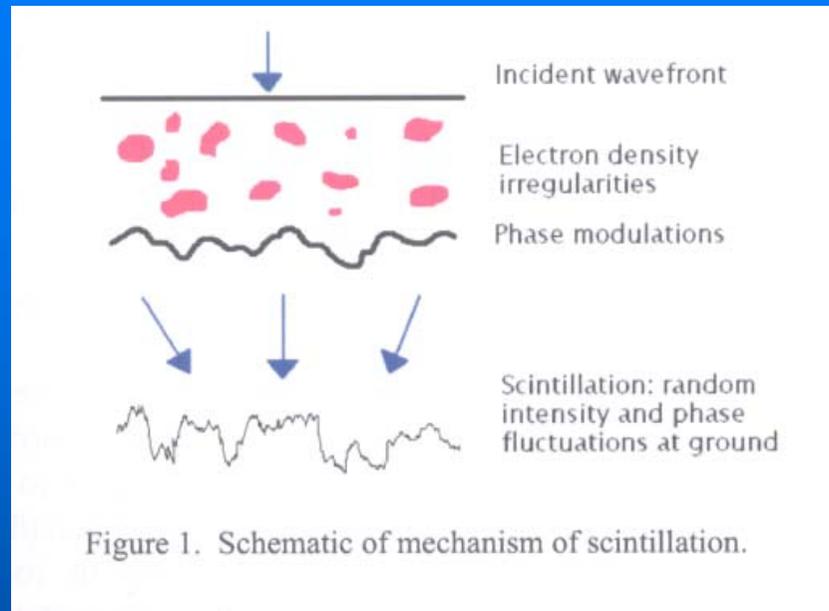


- In practice, all measurements limited to accuracy of a few TECU

# Ionospheric Scintillation

Effects of small-scale irregularities in  
ionospheric electron density on  
transionospheric propagation

# Scintillation – basic ideas



- diffraction pattern on ground
- satellite motion or irregularity motion
- random temporal fluctuations of received signal
- both phase and amplitude (intensity)
- intensity may fade below receiver margin
- phase shifts can cause signal loss

# Irregularity Spectrum

- perturbations in electron density ( $\Delta N$ )
- *spatial* spectrum of irregularities has *power-law* form

$$\Phi_{\Delta N}(k_x) \propto k_x^{-p_{1D}} \quad \text{where } k_x \text{ is wave number} \\ \text{and } p_{1D} \text{ is 1-D spectral index}$$

- for *isotropic* irregularities

$$\Phi_{\Delta N}(k_x, k_y, k_z) \propto K^{-p} \quad \text{where } K \text{ is 3-D wave number} \\ \text{and } p = p_{1D} + 2$$

- range of wave numbers
  - inner scale - set by diffusion processes - metres
  - outer scale - ? - tens of km

# Scintillation Spectra

- *temporal* spectra for weak scintillation
- *phase* ( $\varphi$ ) fluctuations

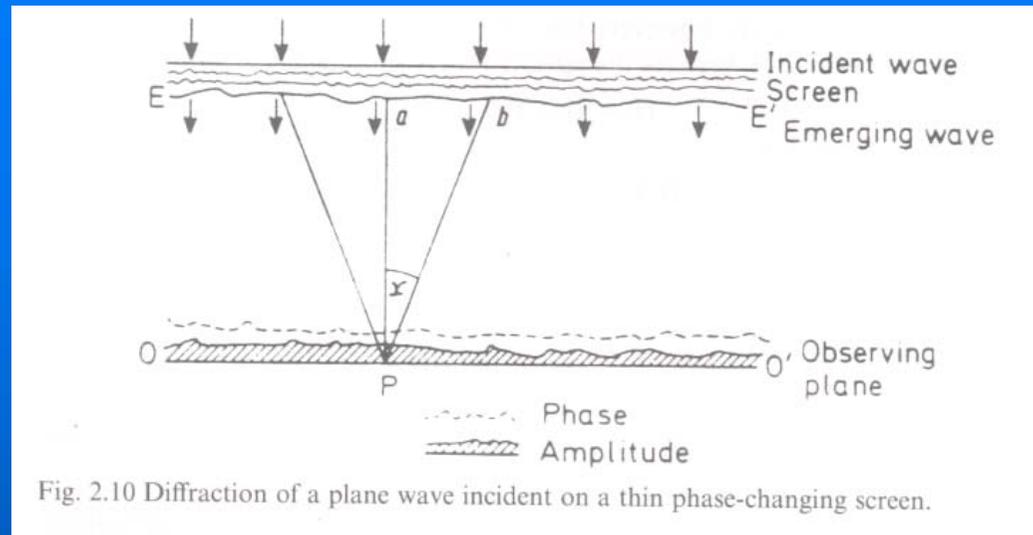
$$\Phi_{\varphi}(\Omega) \propto \Omega^{-p_s} \quad \text{where } \Omega \text{ is fluctuation frequency} \\ \text{and } p_s = p - 1$$

- *intensity* (I) fluctuations

$$\Phi_I(\Omega) \propto \Omega^{-p_s} \quad \text{for } \Omega \gg \Omega_F$$

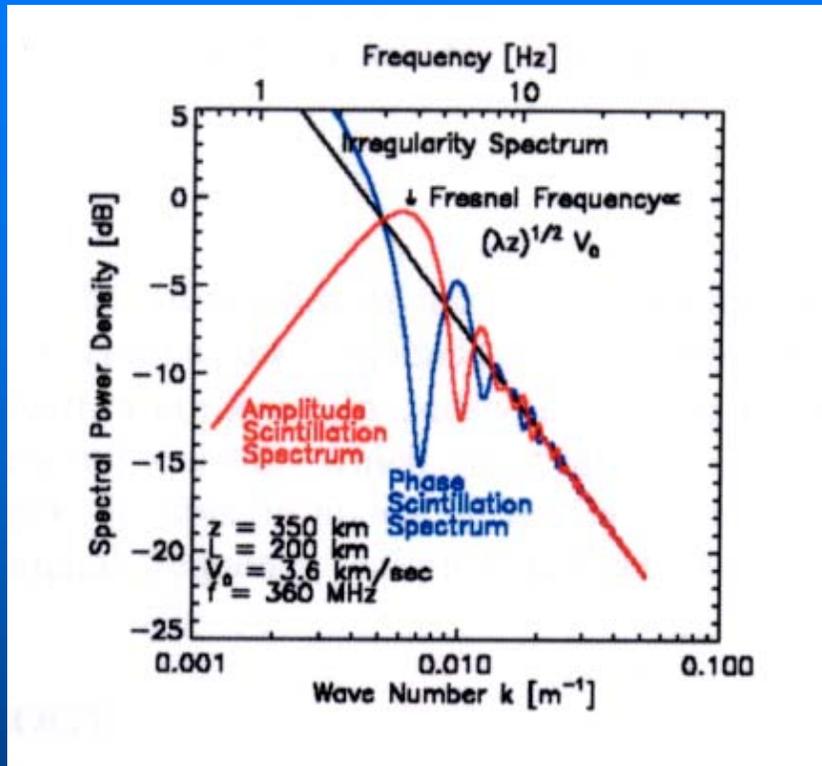
- $\Omega_F$  is *Fresnel frequency*

# Fresnel cut-off



- constructive interference for  $Pb < Pa + \lambda/2$
- irregularities of Fresnel zone size will contribute most to amplitude (intensity) scintillation
- $r_F \sim \sqrt{\lambda z}$  where  $\lambda$  is radio wavelength and  $z$  is altitude of irregularities
- scintillation caused by sub-kilometre irregularities (eg GPS L1:  $\lambda \sim 0.2 \text{ m}$ , so for  $z \sim 350 \text{ km}$ ,  $r_F \sim 250 \text{ m}$ )

# Spectra



Theoretical (Wernik et al., 2003)

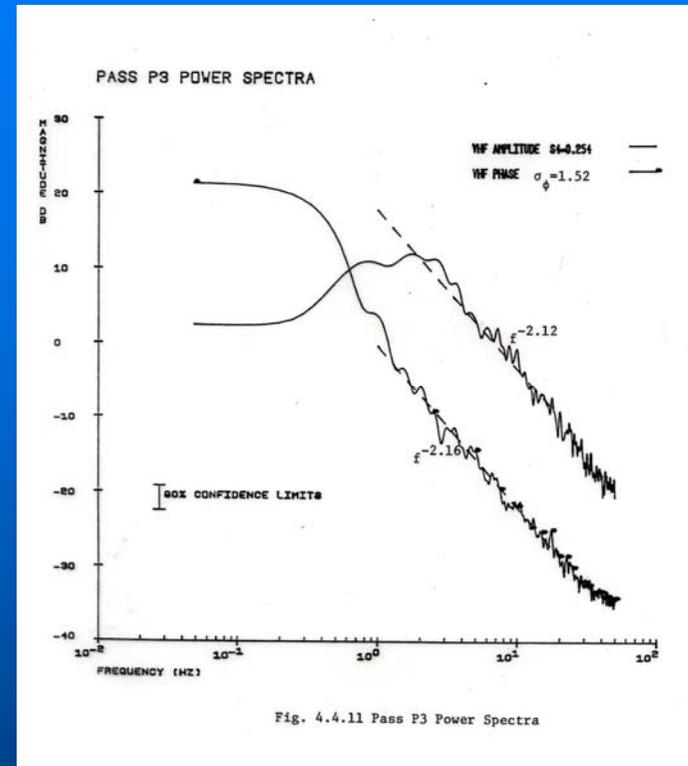
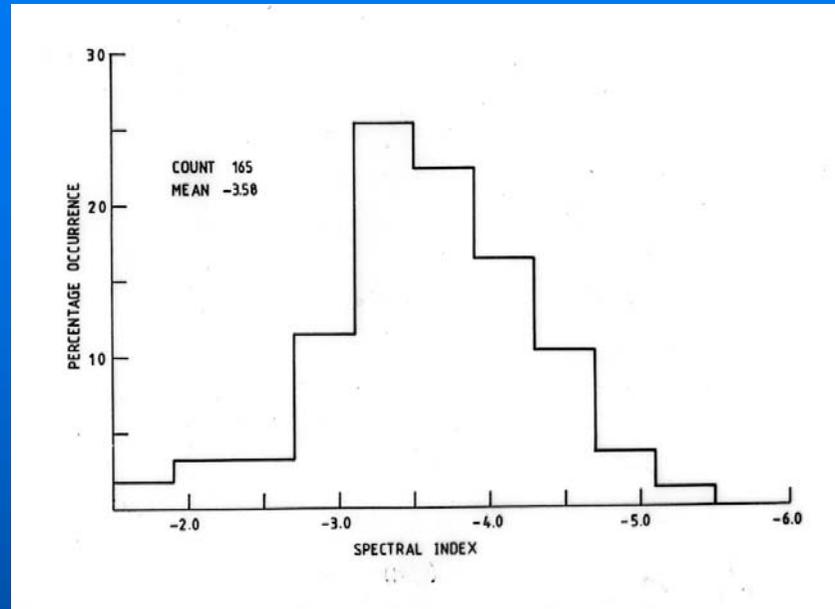


Fig. 4.4.11 Pass P3 Power Spectra

Experimental

# Spectral index – spectral slope



- range ~2 to ~5
- $p_s$  often taken to be 3

# Scintillation indices – measurements of scintillation

- Intensity fluctuations ( $S_4$ )

$$S_4 = \{ (\langle I^2 \rangle - \langle I \rangle^2) / \langle I \rangle^2 \}^{1/2}$$

- Phase fluctuations *sigma phi* ( $\sigma_\phi$ )

$$\sigma_\phi = \{ \langle \phi^2 \rangle - \langle \phi \rangle^2 \}^{1/2}$$

- in practice, signal processing involves filtering to remove effects of large-scale TEC structures
- must specify de-trend cut-off used
- $S_4$  and  $\sigma_\phi$  depend on
  - $\langle \Delta N^2 \rangle$
  - irregularity anisotropy
  - propagation geometry

# Scintillation Theory

## Intensity

$$S_4^2 = r_e^2 \lambda^2 (L \sec \theta) C_s Z^{\nu-1/2} \left[ \frac{\Gamma((2.5-\nu)/2)}{2\sqrt{\pi}\Gamma((\nu+0.5)/2)(\nu-0.5)} \right] \mathcal{J}$$

where

$$\mathcal{J} = \frac{ab}{\sqrt{A''C''}} {}_2F_1 \left( \frac{1}{2} - \nu, \frac{1}{2}; 1; \frac{A'' - C''}{A''} \right)$$

$S_4$  depends on

- strength of irregularities ( $C_s$ )
- spectral slope ( $p = 2\nu$ )
- irregularity shape
- propagation geometry (irregularities are field aligned)
- Fresnel zone size ( $Z$ )

## Phase

$$\langle \delta\phi^2 \rangle = r_e^2 \lambda^2 (L \sec \theta) G C_s \frac{q_0^{-2\nu+1} \Gamma(\nu - 1/2)}{4\pi\Gamma(\nu + 1/2)}$$

where

$$G = \frac{ab}{\sqrt{AC - B^2/4 \cos \theta}}$$

$\sigma_\phi$  depends differently on

- strength of irregularities ( $C_s$ )
- spectral slope ( $p = 2\nu$ )
- irregularity shape
- propagation geometry
- *but not Z*

# Dependence on radio frequency

- Intensity scintillation

$$S_4 \propto f^{-(3+p_s)/4}$$

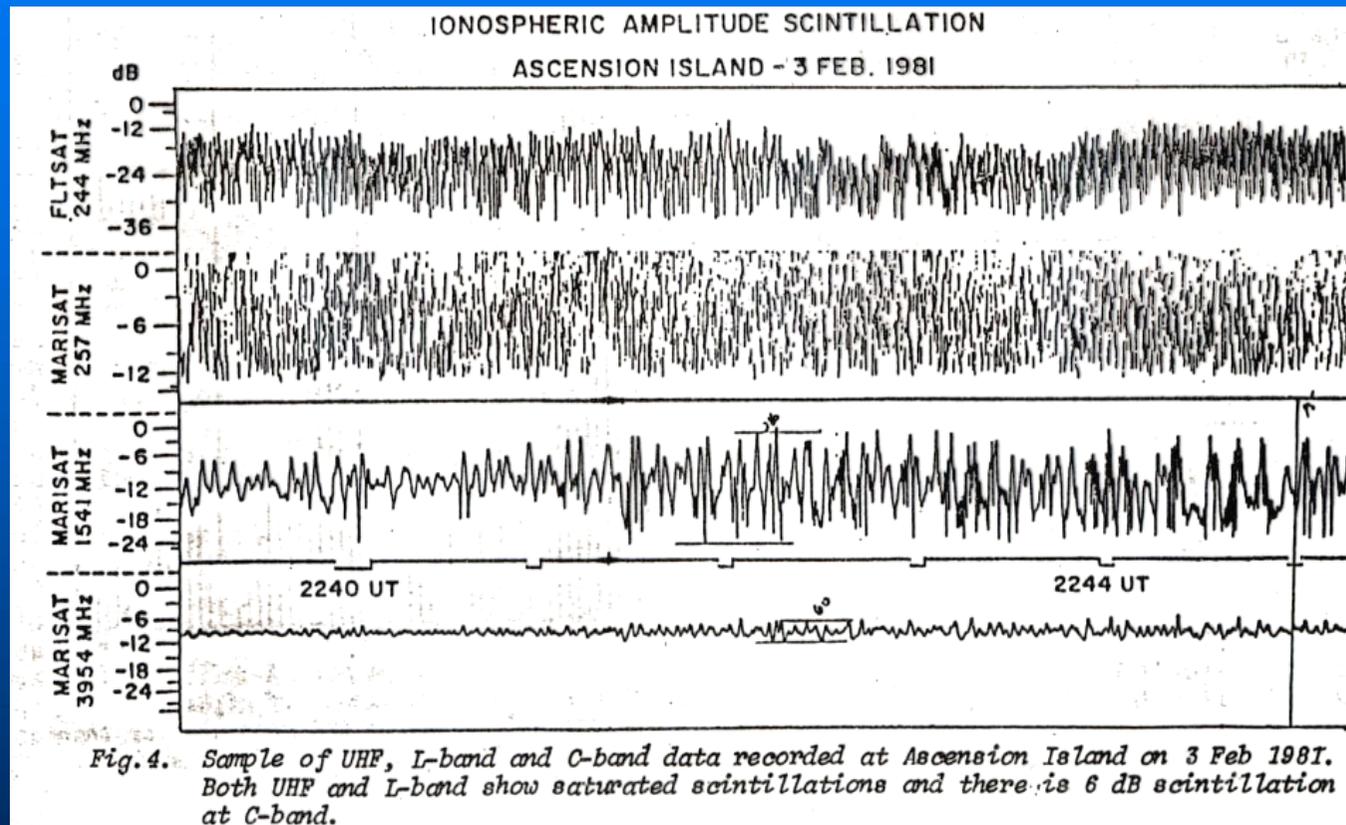
$$S_4 \sim f^{-1.5} \quad \text{for } p_s \sim 3$$

- Phase scintillation

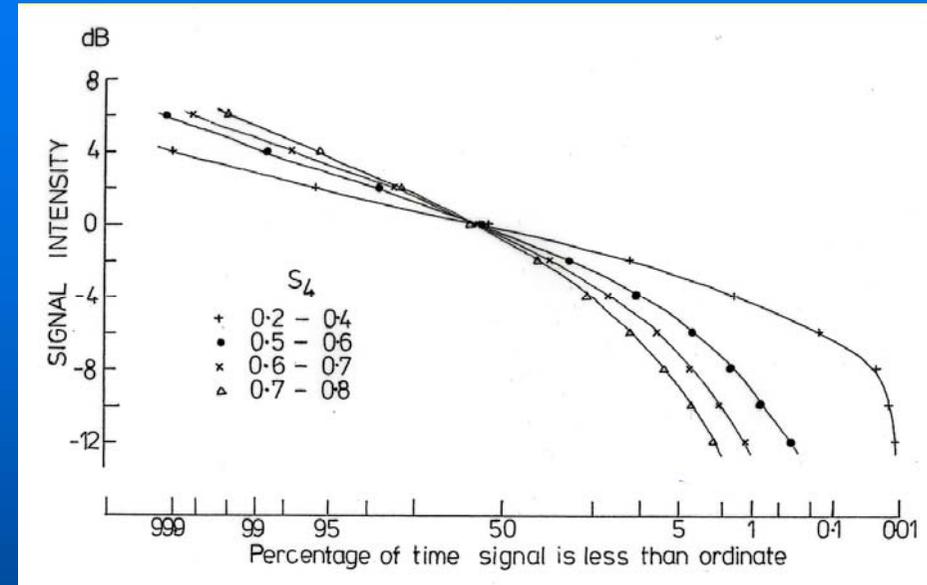
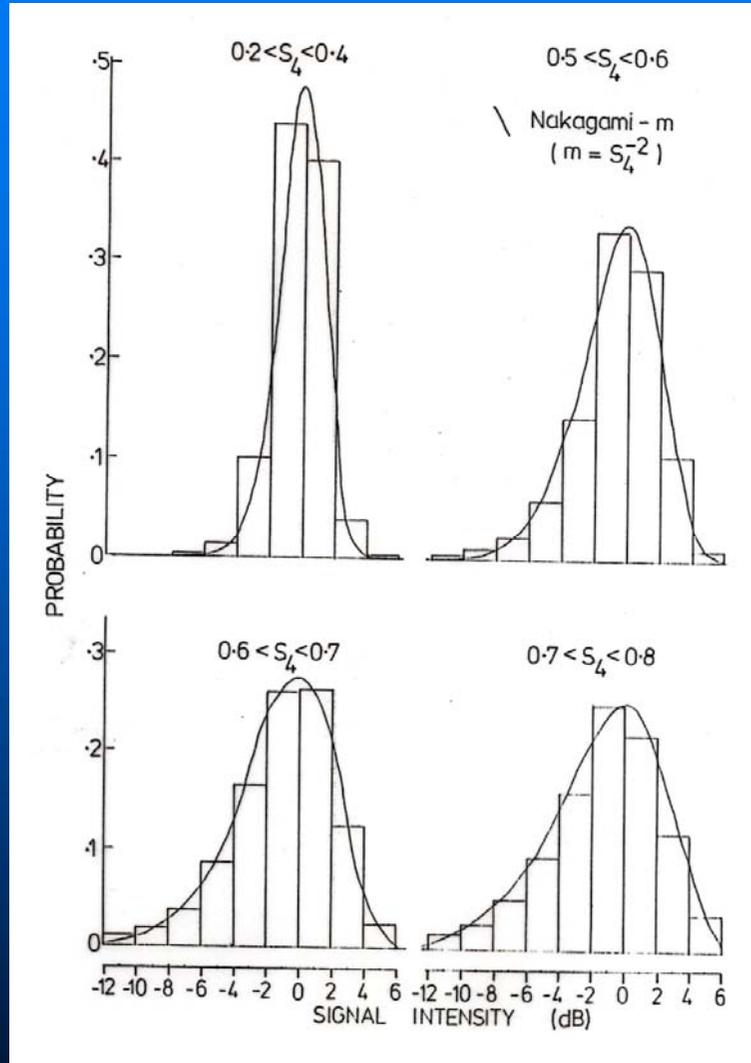
$$\sigma_\phi \sim f^{-1}$$

not limited by Fresnel zone size

# Scintillations on various carrier frequencies



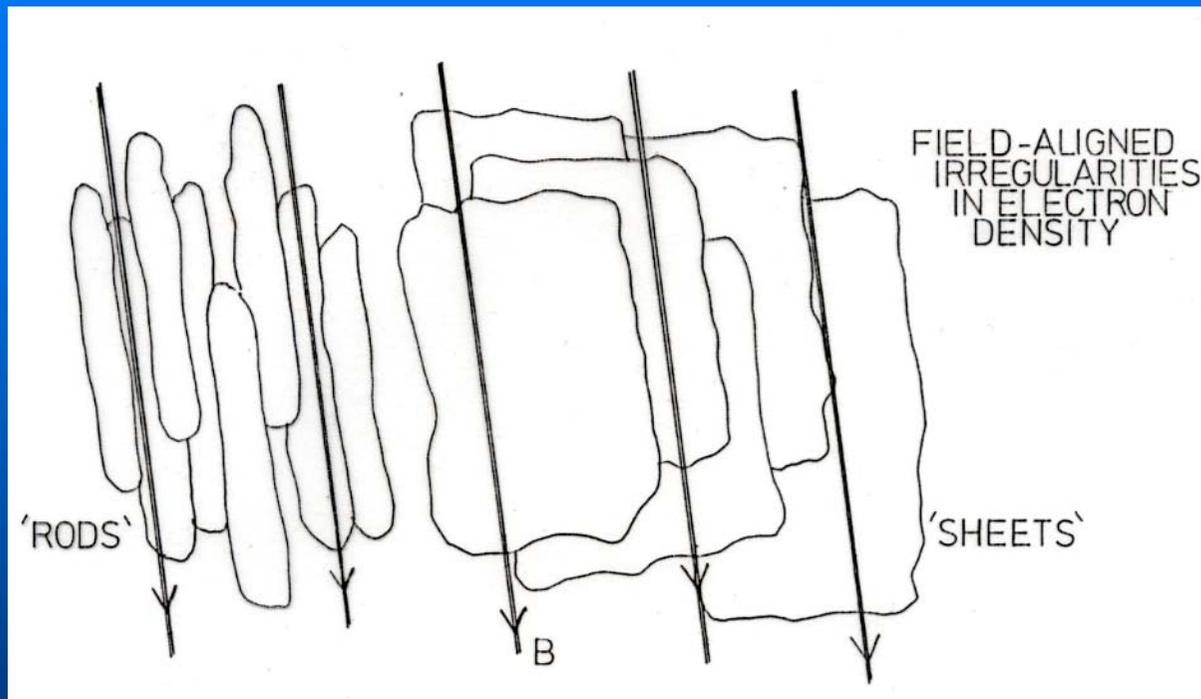
# Structure of scintillating signal



Depth of fading related to  $S_4$

# Irregularity anisotropies

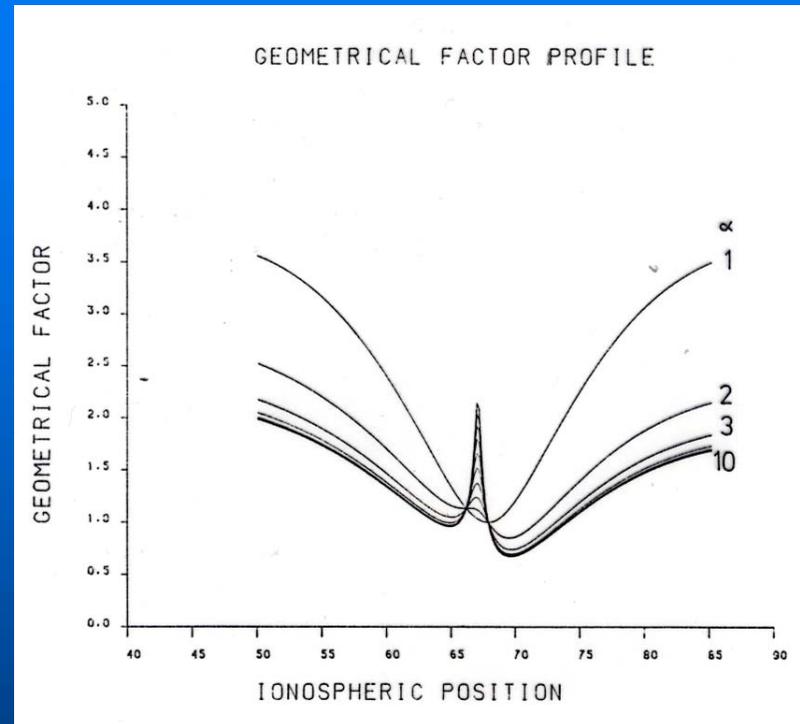
Plasma constrained by magnetic field



- field-aligned 'rods'
- axial ratio (x : 1 : 1)
- sub-auroral latitudes
- L-shell confined 'sheets'
- axial ratio (x : y : 1)
- auroral zone

# Geometrical effects

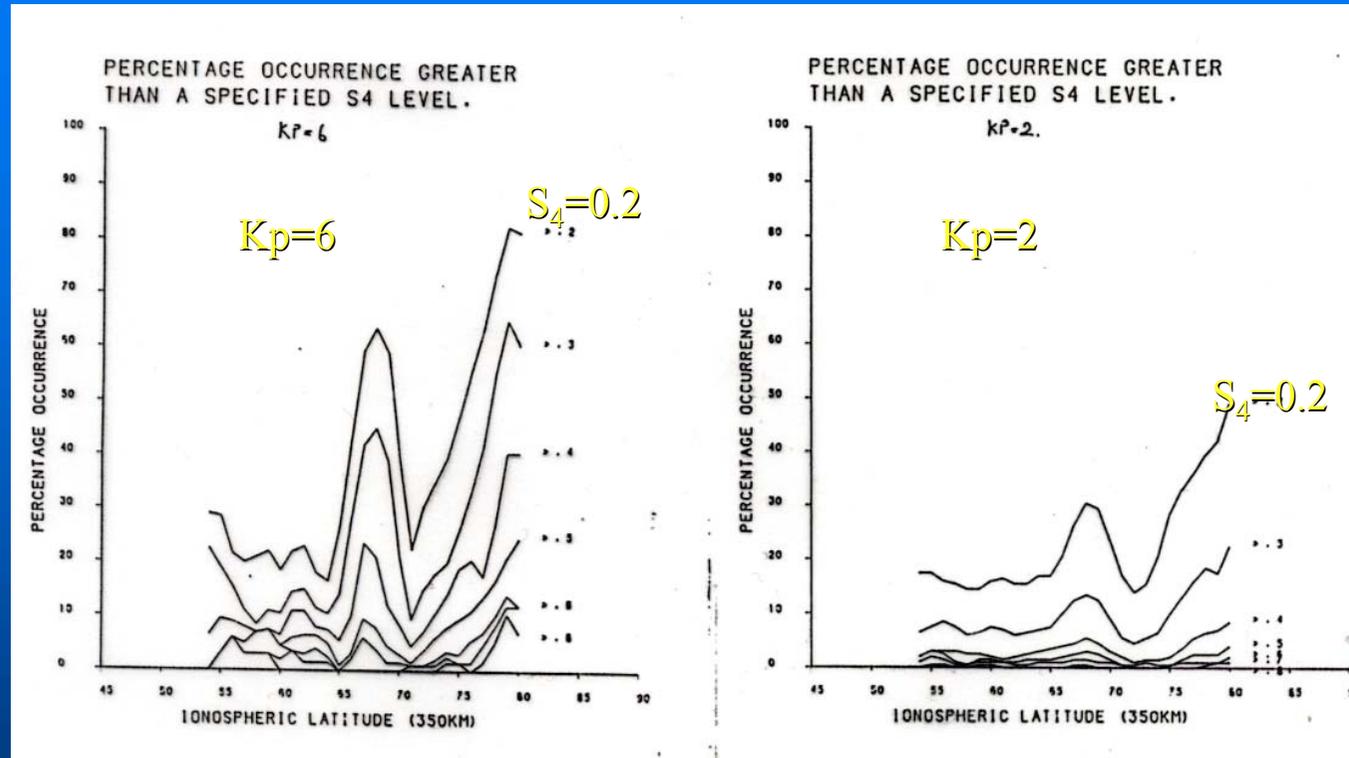
Theoretical estimates for Kiruna as a function of latitude



- multiplying factor normalised to overhead
- rod-like irregularities
- axial ratios up to  $\alpha = 1 : 10$
- function of latitude

# Geometrical effects on $S_4$

Experimental observations on 150 MHz at Lerwick  
– a *sub-auroral* station



- enhancement looking up field line
- evidence for *rod-like* irregularities
- scintillation boundary
- irregularity zone moves equatorwards with Kp



# Geometrical effects on scintillation

## Phase scintillation at Kiruna – an *auroral* zone station

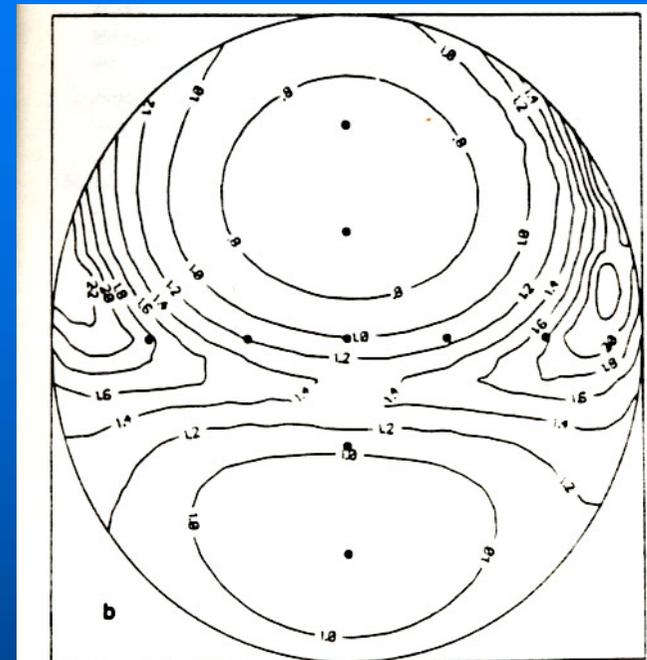
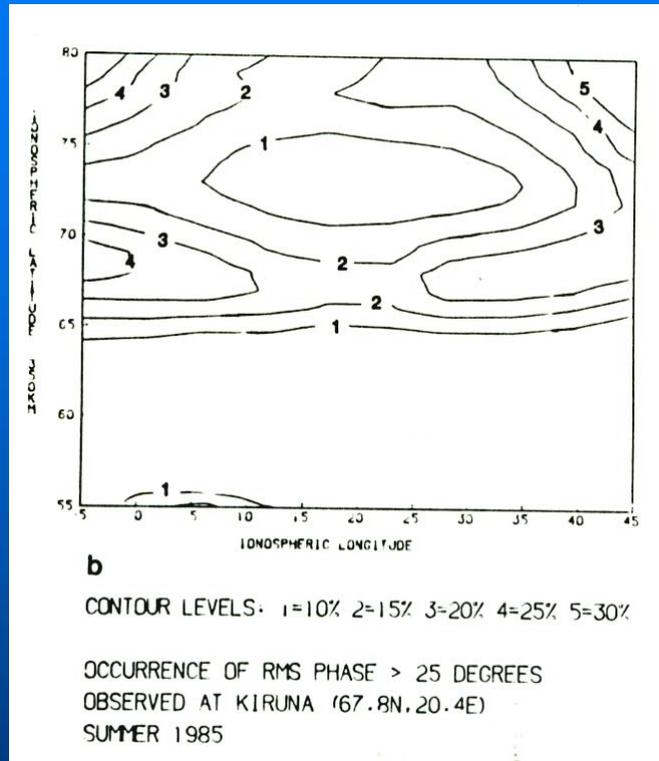


Fig. 8. Estimates of the geometrical factor in  $\sigma_p$  normalized to overhead measurements.

- phase scintillation occurrence
- experimental results at 150MHz
- different propagation directions
- Evidence for sheet-like irregularities in auroral zone
- geometrical factor
- irregularity sheets (8:8:1)

# Global scintillation morphology

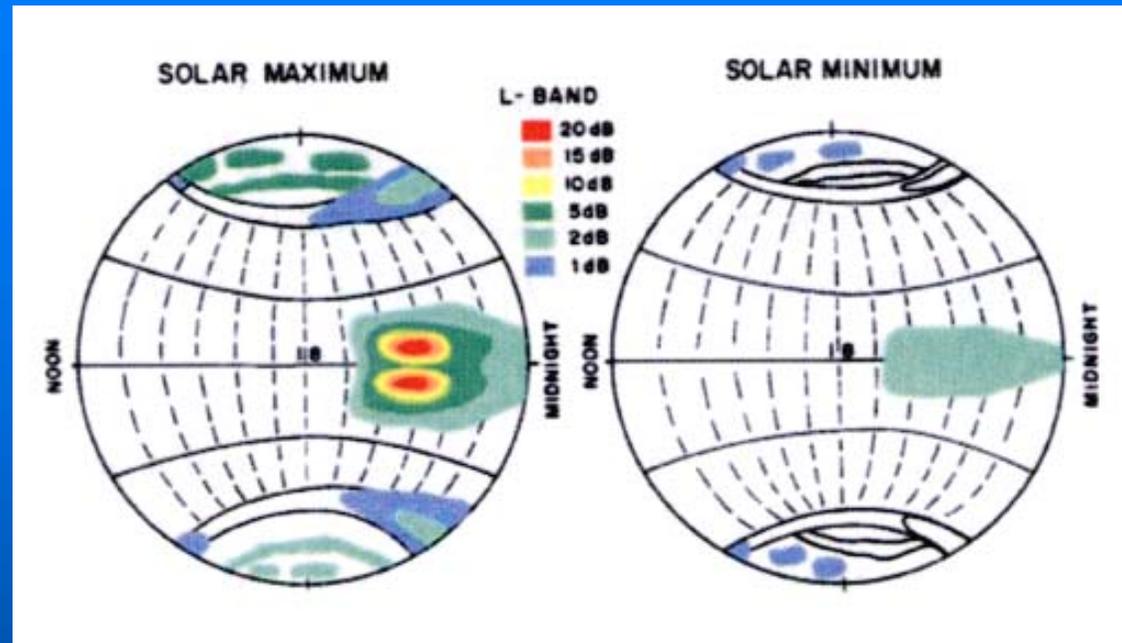


Figure 3. Global variation of scintillation fades during solar maximum and solar minimum conditions. Understanding of these patterns was developed in a series of papers over many years by Aarons, though the figure above has been taken from Basu et al. (1988).

- the most severe scintillation effects are found in the post-sunset equatorial ionosphere
- equatorial morphology is longitude dependent

# Auroral scintillation

## Kiruna 150 MHz

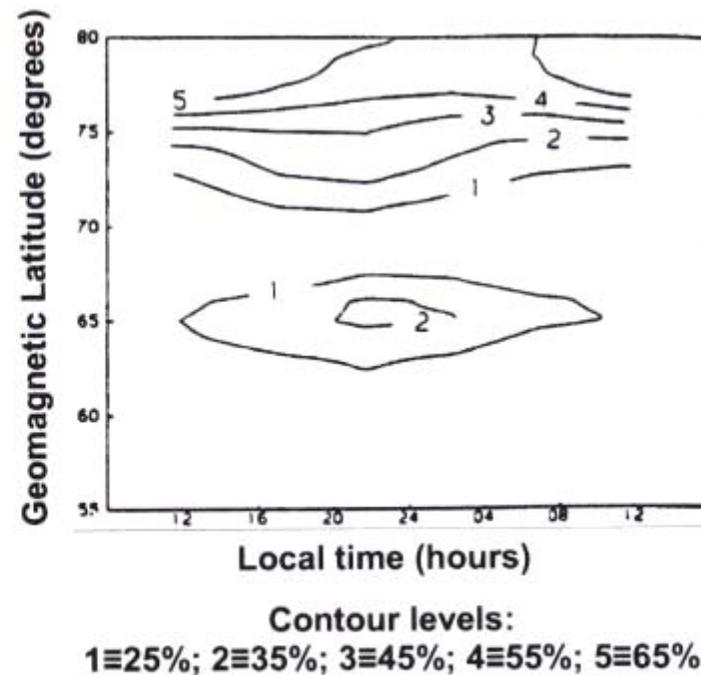


Figure 5. Diurnal variation of occurrence  $S_4 > 0.2$  at Kiruna ( $64.3^\circ$ CGM Lat,  $102.8^\circ$ CGM Lon) during winter 1985/1986 (after Kersley et al., 1988c).

- Nighttime maximum

# Sub-auroral scintillation

## Lerwick 150MHz

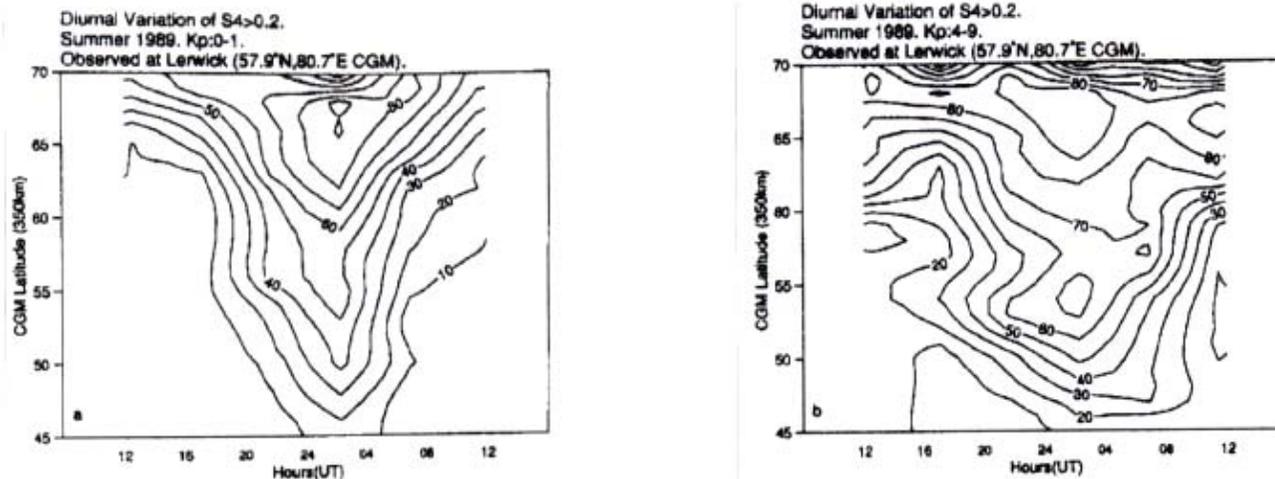


Figure 6: Diurnal variation of occurrence of S4 > 0.2 measured at Lerwick during summer 1989, under a) quiet and b) disturbed geomagnetic conditions (after Pryse et al., 1991).

- scintillation boundary
- evening equatorwards advance
- extension with geomagnetic disturbance

# Auroral scintillation

## Kiruna 150 MHz

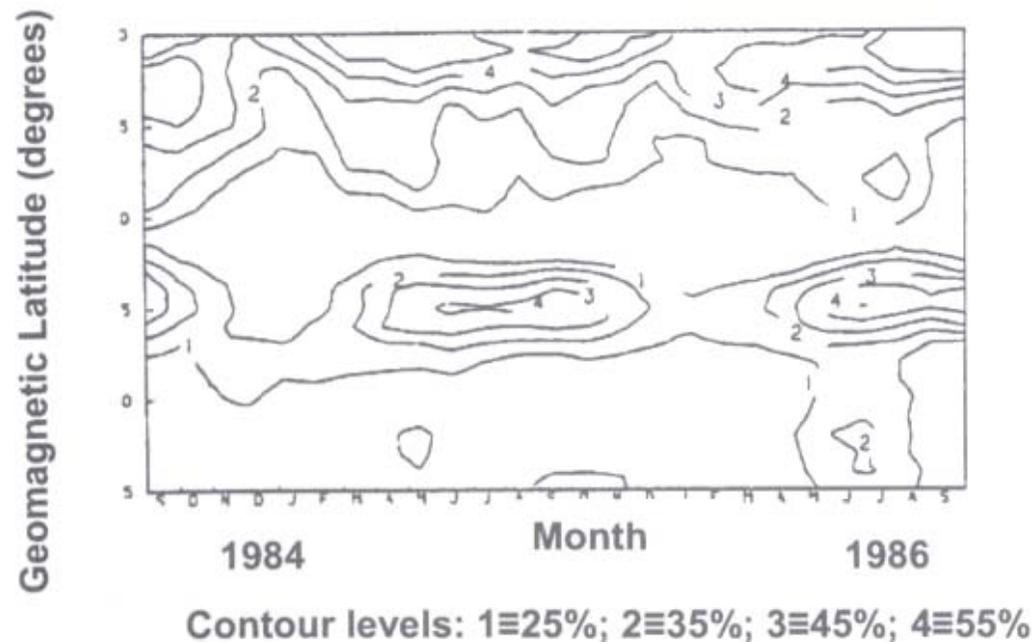


Figure 7. Occurrence of S4>0.2 measured at Kiruna between September 1984 and September 1986 (after Kersley et al., 1988c).

- summer maximum at solar minimum

# Sub-auroral scintillation

## Lerwick 150 MHz

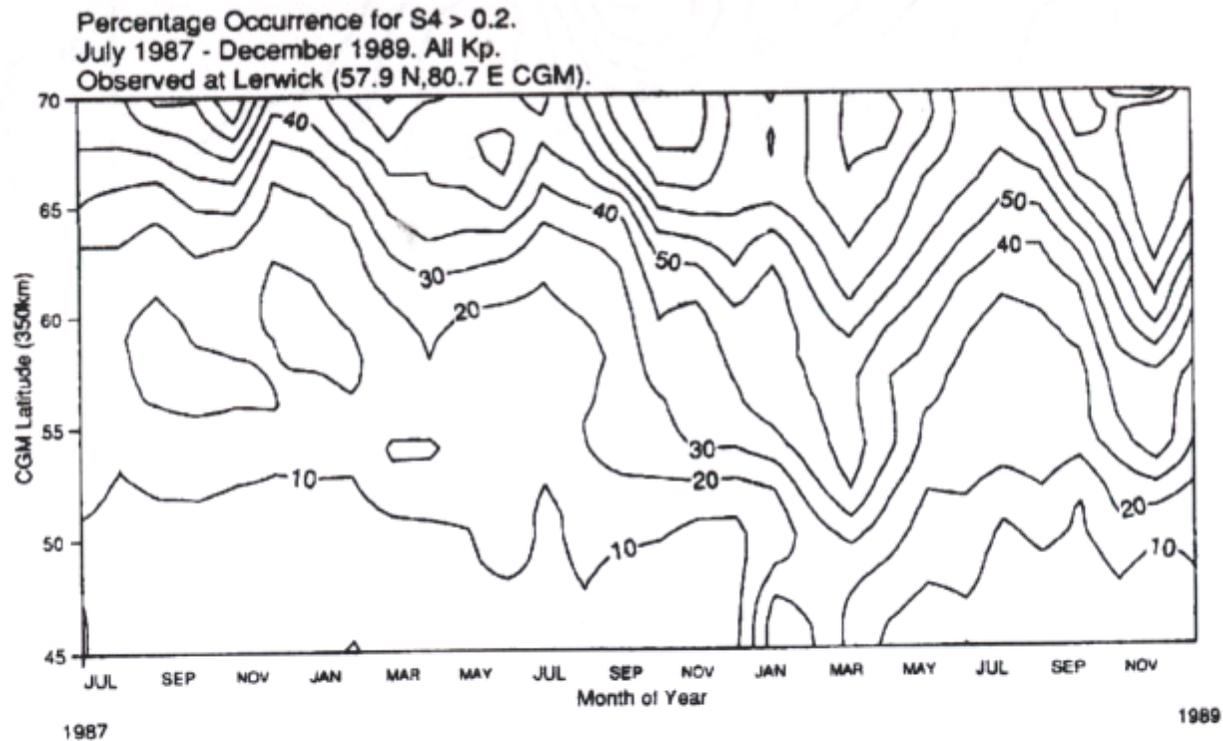


Figure 8. Occurrence of  $S_4 > 0.2$  measured at Lerwick between July 1987 and November 1989 (after Pryse et al., 1991).

- equatorwards extension with rising solar activity

# Polar-cap scintillation

## Ny Alesund 150 MHz

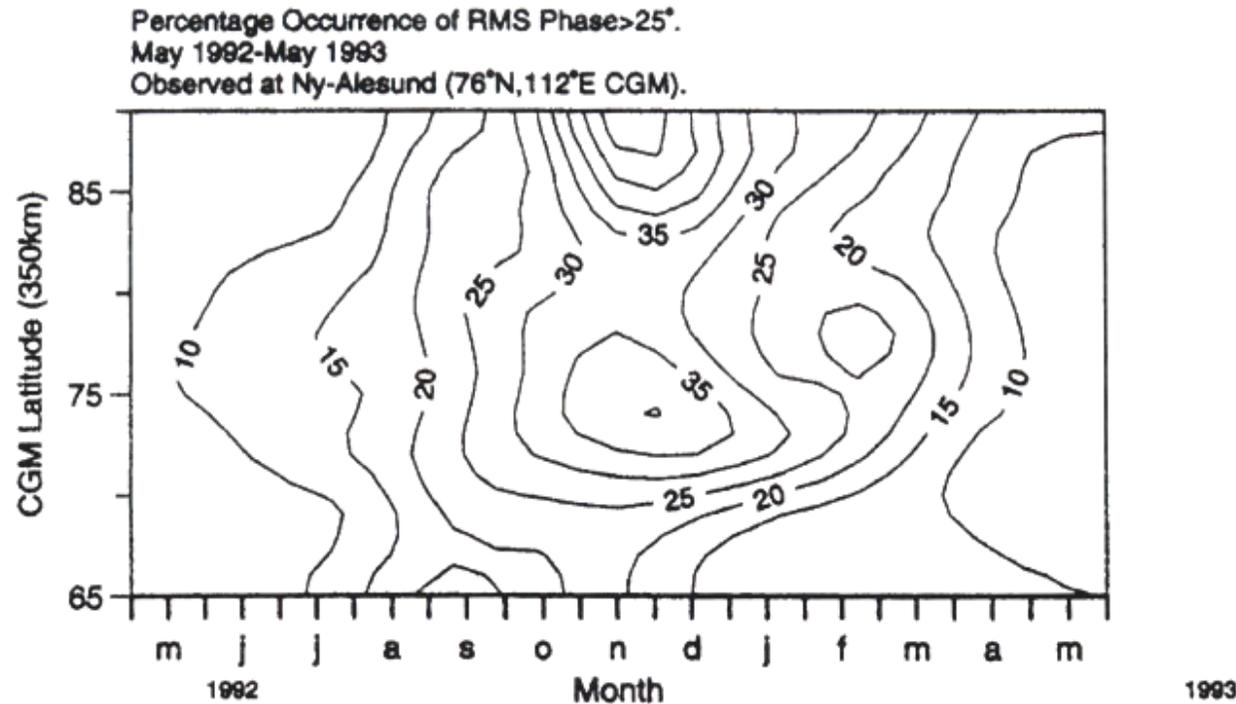


Figure 9. Occurrence of  $\sigma_{\phi} > 25^{\circ}$ , measured at Ny Ålesund between March 1992 and March 1993 (after Kersley et al., 1995).

- winter maximum
- evidence for wing-like irregularities

# Scintillation modelling and forecasting

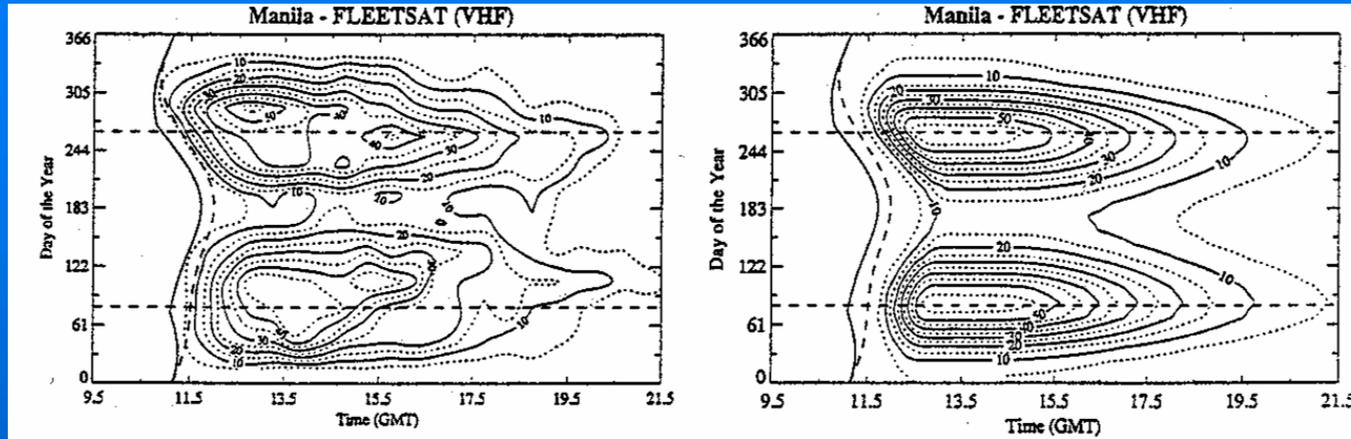


Figure 10. Percentage occurrence of  $S_4 > 0.5$  for Manila: a) measured levels and b) modelled levels (after Secan et al., 1995). The heavy solid curves on the lhs indicate the time of E-region sunset and the heavy dashed curves the time of  $F_2$  region sunset. The horizontal dashed lines indicate the equinoxes.

## Scintillation models

- WBMOD
- GISM

# Irregularity mechanisms

## What causes the irregularities?

- Plasma instabilities
  - Equatorial scintillation
    - Rayleigh-Taylor gravitational instability
  - High-latitude scintillation
    - ExB gradient drift instability
    - velocity shears
- Soft-particle precipitation
  - Auroral scintillation
    - in-situ fine-structured

# Transionospheric propagation - conclusions

- *Total electron content (TEC) along ray path is a key parameter*
- *Carrier phase, group delay and polarisation of received signal are modified by crossing ionosphere*
- *TEC has large temporal and spatial variability on many different scales*
- *Small-scale irregularities in electron density cause scintillation of received signal*
- *TEC and scintillation introduce errors and cause problems for operation of applied radio systems like GPS*