

Gauge-Mediation of Supersymmetry Breaking in String Compactifications

Bogdan Florea
SLAC and Stanford

ICTP, Trieste, May 2006

Abstract

Based on

- hep-th/0512170 w/ D.-E. Diaconescu, S. Kachru and P. Svrček
- work in progress w/ S. Kachru, J. McGreevy and N. Saulina

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1. Overview

- Introduction
 - Gauge mediation versus gravity mediation
 - Embedding of gauge mediation scenarios into string theory
- Field Theory Models with Dynamical Supersymmetry Breaking
 - Dynamical supersymmetry breaking in quiver gauge theories
 - Noncalculable models of supersymmetry breaking
- Fractional Brane Supersymmetry Breaking and GUT Models
 - F-theory geometry
 - Dual heterotic compactification
- String Theory Embeddings of the Noncalculable Models
 - Heterotic bundles construction
 - Dual F-theory geometry
- Conclusions

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2. Introduction

- Recent progress in string theory compactifications
 - IIB and IIA constructions where the question of moduli stabilization can be successfully addressed
 - Heterotic constructions that get very close to realizing the MSSM (**Penn**)

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 - Heterotic constructions that get very close to realizing the MSSM (Penn)
- Next steps in the top-down approach
 - Construction of MSSM vacua with all moduli stabilized
 - Engineer moduli-stabilized GUT or MSSM-like configurations that exhibit low-scale supersymmetry breaking
 - This talk
 - * constructions incorporating a toy model of the MSSM or a SUSY GUT and a sector realizing dynamical supersymmetry breaking
 - * tuning of closed string parameters \rightsquigarrow dominant mechanism of transmitting supersymmetry breaking to the Standard Model is gauge mediation

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 - * tuning of closed string parameters \rightsquigarrow dominant mechanism of transmitting supersymmetry breaking to the Standard Model is gauge mediation
 - Type II flux vacua w/ intersecting D-branes \rightsquigarrow calculable SUSY breaking soft terms induced by fluxes have typically too large an order of magnitude \rightsquigarrow lose natural connection between supersymmetry and GUT models

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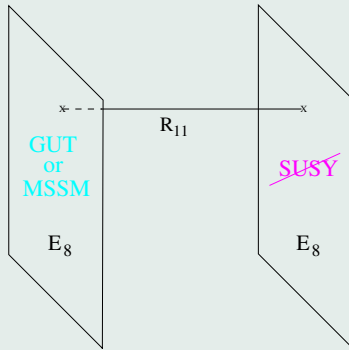
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 - Gravity mediation is sensitive to Planck-scale physics
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 - Gauge mediation solves the SUSY flavor problem: soft-breaking terms do not introduce new sources of flavor violation that would disagree w/ present experimental bounds
 - * gaugino masses $m_\lambda \sim \alpha F/M$ and squark and slepton masses $m_Q^2 \sim \alpha^2 F^2/M^2$; F is the supersymmetry breaking F-term, M is the messenger mass
 - * messenger fields are charged under the Standard Model and contribute to the running of the gauge coupling at energy scales higher than M
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 - Will not be very concerned with numerical considerations (messenger mass, messenger index, strong coupling scale of the hidden gauge group)

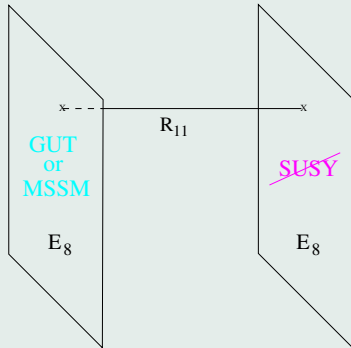
- Embedding of gauge-mediation scenarios into string theory
 - Most natural construction: strongly coupled $E_8 \times E_8$ heterotic string



- * realize a GUT model on the visible end-of-the-world 9-brane and a supersymmetry breaking sector on the hidden 9-brane
- * picture is not suitable for gauge mediation and SUSY breaking is typically transmitted via gravity mediation

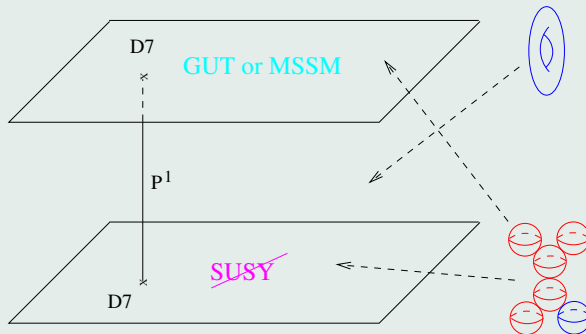
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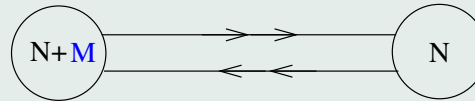
- F-theory picture: the gauge symmetry is realized on the worldvolume of stacks of D7-branes wrapping surfaces in the base of the Calabi-Yau 4fold



- * D7-brane moduli correspond to complex structure moduli of CY 4fold;
- * sometimes possible to bring the two stacks of D7-brane close: $d \ll l_s$
- * messengers: open strings stretched between the D7-brane stacks

3. Dynamical SUSY Breaking in Field Theory

- Dynamical supersymmetry breaking in quiver gauge theories ([Berenstein, Herzog, Ouyang, Pinansky; Franco, Hanany, Saad, Uranga; Bertolini, Bigazzi, Cotrone](#))
 - ([Klebanov, Witten](#)) Place a stack of N D3-branes at the tip of the conifold, $\sum_{i=1}^4 z_i^2 = 0 \rightsquigarrow SU(N) \times SU(N)$ superconformal gauge theory with pairs of bifundamentals in the $(\mathbf{N}, \overline{\mathbf{N}})$ and $(\overline{\mathbf{N}}, \mathbf{N})$ representations



- ([Klebanov, Strassler](#)) Add M D5-branes wrapping the collapsed two-cycle $\rightsquigarrow SU(N+M) \times SU(N)$ gauge theory with pairs of bifundamentals in the $(\mathbf{N} + \mathbf{M}, \overline{\mathbf{N}})$ and its conjugate representations
 - * the theory is no longer conformal \rightsquigarrow flows to a strongly coupled gauge theory in the IR via an infinite series of Seiberg duality transformations
 - * in the IR, the theory exhibits chiral symmetry breaking and confinement
 - * the dual supergravity description is the [warped deformed conifold](#) $\sum_{i=1}^4 z_i^2 = \epsilon$, where the deformation parameter ϵ is related to the gaugino condensate in the field theory

- Consider a more complicated singularity: the cone over del Pezzo surface dP_1
 - * while the singularity admits a first-order deformation, it is obstructed at second order (Altmann)
 - * place N D3-branes and M fractional D5-branes at the singularity \rightsquigarrow conflict between gaugino condensation and other scalar vevs lead to dynamical supersymmetry breaking

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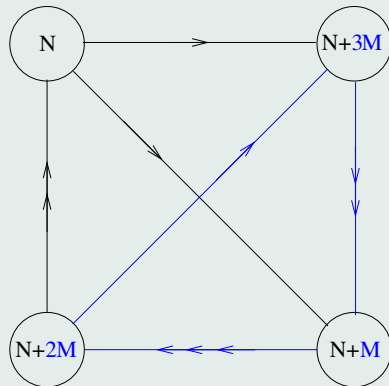
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 - * the gauge theory is described by the following quiver diagram



- * the fractional brane triggers a duality cascade: the effective number of D3-branes decreases while the number of fractional D5-branes remains constant
- * **blue**: the quiver corresponding to the gauge theory of the end of the flow
- * $U(3M) \times U(2M) \times U(M)$ gauge theory with that spectrum of bifundamental matter fields exhibits dynamical breaking of supersymmetry

- Impossible to satisfy all the D-term and F-term constraints

– Wait! This was too fast.

- * in the noncompact geometry, the D-term constraints can not be imposed since the $U(1)$'s are massive (Franco et al; Intriligator, Seiberg) \rightsquigarrow runaway direction and no supersymmetry breaking

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- * once the above configuration is embedded in a compact geometry, the Kähler parameters become dynamical (they play the role of field dependent Fayet-Iliopoulos terms) \rightsquigarrow **need to stabilize the Kähler parameters**. Otherwise, runaway direction and no supersymmetry breaking.

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– Other possibility (**Franco, Uranga**): add noncompact D7-branes to the system

- * the system admits metastable supersymmetry breaking vacua (string theory realization of **Intriligator, Seiberg, Shih**- type vacua)
- * (**Garcia-Etxebarria, Saad, Uranga**): local models of gauge mediation using this construction for the SUSY breaking sector
- * issue of moduli stabilization still open – but (\exists) quite promising compact embedding of the **ISS** model (work w/ **Diaconescu,...**)

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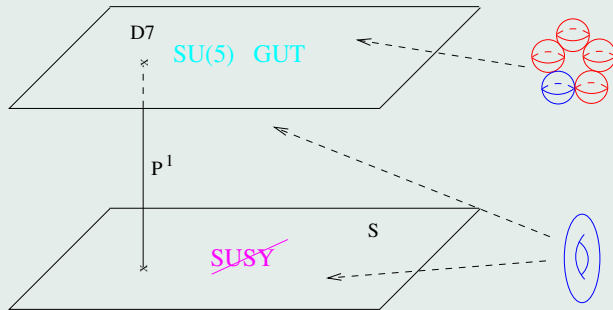
- Noncalculable models of supersymmetry breaking
 - Simple class of models which exhibit dynamical breaking of supersymmetry ([Affleck, Dine, Seiberg](#))
 - * $SU(5)$ gauge theory w/ one generation of $\bar{\mathbf{5}} \oplus \mathbf{10}$
 - * $SO(10)$ gauge theory w/ one generation of $\mathbf{16}$
 - These models do not have any flat directions or adjustable parameters
 - $(\exists) U(1)_R$ symmetry
 - * if the $U(1)_R$ is preserved in the IR \rightsquigarrow implausible charge assignments for the low-energy fields in order to satisfy the anomaly constraints
 - * postulate broken global symmetry in the IR \rightsquigarrow (\exists) Goldstone bosons



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 - If (\exists) unbroken supersymmetry \rightsquigarrow Goldstone bosons are complexified into scalar multiplets whose scalar vevs are not constrained
 - * But this is implausible in theories w/out tree-level flat directions \rightsquigarrow **supersymmetry is dynamically broken**
 - Additional evidence (Murayama): consider models with extra vector-like fields
 - * the Witten index vanishes when the mass is small; obtain the noncalculable model in the decoupling limit

4. Fractional Brane SUSY Breaking and GUT Models

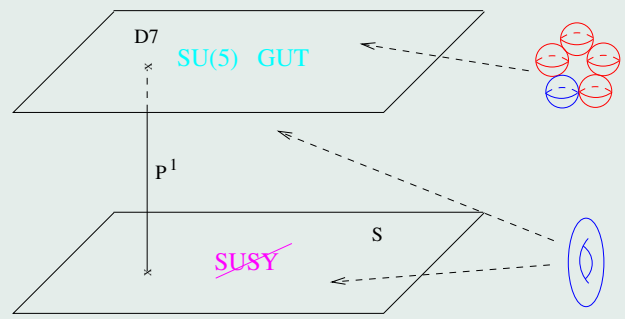
- Engineering Goal of the Section:



- $X \rightsquigarrow$ elliptic Calabi-Yau 4fold fibered over a base P
- P is itself a \mathbb{P}^1 bundle over a del Pezzo surface S (dP_5)
- the elliptic fiber is constant along the negative section S
- the elliptic fiber is Kodaira type I_5 along the positive section S_∞

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- IIB Calabi-Yau orientifolds ...

- Let Z be a Calabi-Yau 3fold equipped w/ a holomorphic involution $\sigma : Z \rightarrow Z$

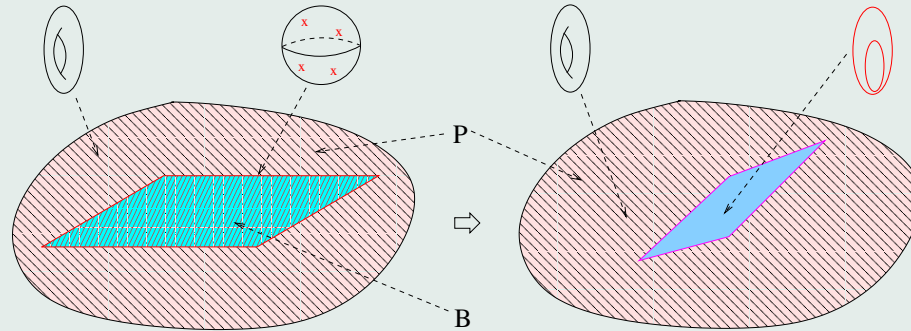
$$\sigma^* \Omega_Z = -\Omega_Z$$

- Z is a double cover of P

$$Z \xrightarrow{2:1} P$$

branched along B , the fixed locus of σ

- IIB orientifold \rightsquigarrow gauge discrete symmetry $(-1)^{F_L} \Omega \sigma$
 - * F-theory compactification on $X = (Z \times T^2) / \mathbb{Z}_2$, where $\mathbb{Z}_2 \equiv (\sigma, -\mathbb{1})$
 - * the Calabi-Yau 4fold $T^2 \rightarrow X \rightarrow P$ has D_4 singularities along B



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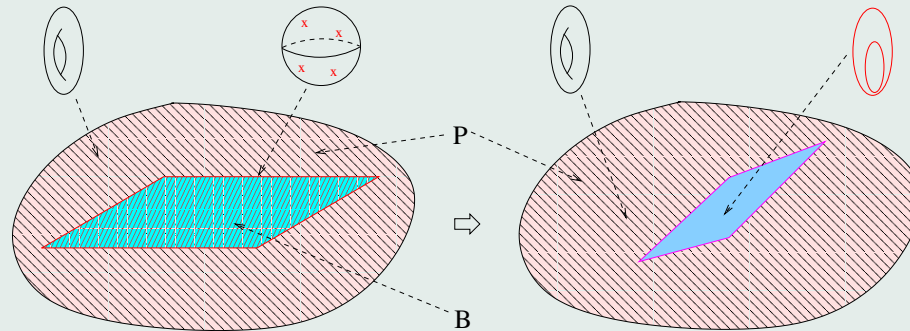
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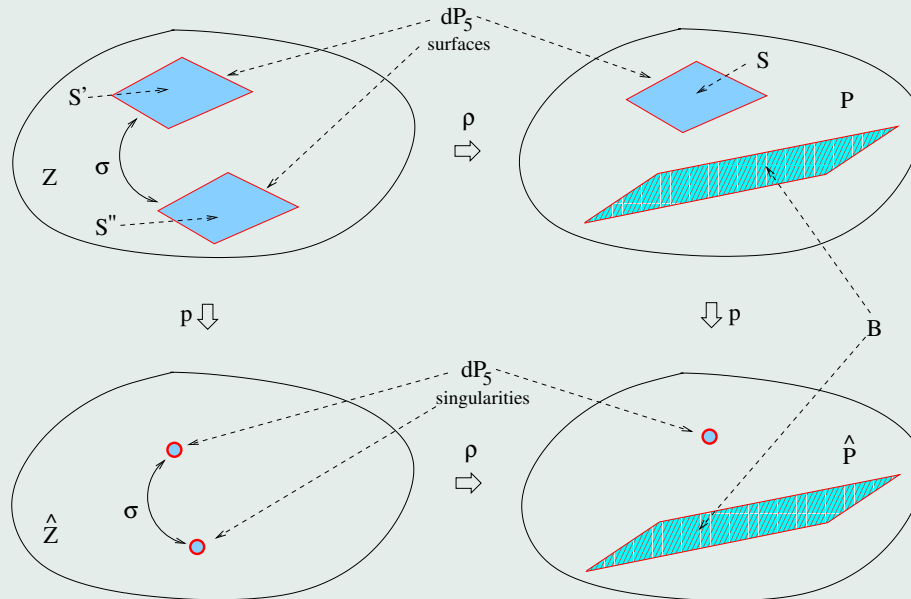
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- ... w/ fractional branes at del Pezzo singularities
 - Engineer models in which P develops del Pezzo singularities away from the branch locus of $\rho: Z \rightarrow P$
 - * del Pezzo surface S on P such that $S \cap B = \emptyset$
 - * map $p: P \rightarrow \hat{P}$ which contracts S to a singular point p on \hat{P}

- Inverse image of the surface S via the double cover $\rho : Z \rightarrow P$ is a pair of disjoint surfaces $S', S'' \subset Z$
 - * the involution $\sigma : Z \rightarrow Z$ maps isomorphically S' to S''



- The infinitesimal neighborhood of S in P is isomorphic to the infinitesimal neighborhood of S' (or S'') in Z

- * S is a locally Calabi-Yau surface on P
- * the local physics of fractional D5-branes at the singularities of \widehat{P} is identical to the local physics of Calabi-Yau del Pezzo singularities
- * the local physics is independent of complex structure deformations that preserve the singularities \rightsquigarrow deform X away from the orientifold limit

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– Physical configuration

- * place N D3-branes and M D5-branes at the singularity in \widehat{Z} obtained by collapsing S'
- * orientifold projection \rightsquigarrow N D3-branes and M anti-D5-branes at the singularity in \widehat{Z} obtained by collapsing S''

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– What about tree-level supersymmetry?

- * at the quiver point, the D3-brane and D5-brane central charges are aligned
- * the central charges of the two configurations are

$$Z' = NZ_{D3} + MZ_{D5}, \quad Z'' = NZ_{D3} - MZ_{D5}$$

- * Z' and Z'' will also be collinear if $N \gg M$

- Concrete example

- Consider S a del Pezzo dP_5 surface and take the base $P = \mathbb{P}(\mathcal{O}_S \oplus K_S)$

- * P has two canonical sections S, S_∞ with normal bundles

$$N_{S/P} \simeq K_S, \quad N_{S_\infty/P} \simeq -K_S$$

- $\rightsquigarrow S$ is locally Calabi-Yau in P

- * pick B a generic smooth divisor in the linear system $|-2K_P| = |4S_\infty|$

- * the double cover $\rho: Z \rightarrow P$ of P branched along B is a smooth Calabi-Yau 3fold containing two disjoint surfaces S', S'' isomorphic to dP_5

- (\exists) a toric contraction map $p: P \rightarrow \widehat{P}$ which contracts S to a point

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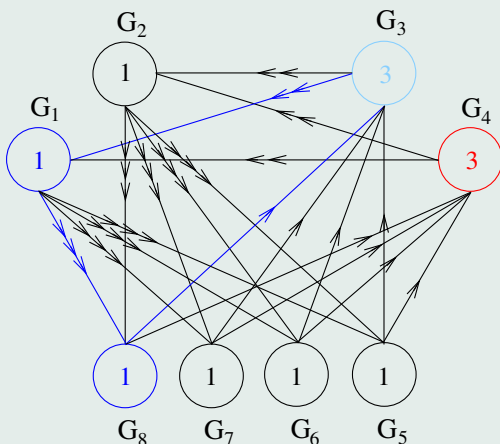
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- * the diagram describes the quiver gauge theory associated with a collapsing dP_5 surface

- * the quiver gauge theory accommodates the desired supersymmetry breaking model; choose the following multiplicities:

$$n_1 = M, \quad n_3 = 3M, \quad n_5 = 2M$$

and all the other n_i vanishing

- Enforce an A_4 singularity of the elliptic fibration along the S_∞ section \rightsquigarrow on S_∞ , D7-brane w/ $SU(5)$ gauge theory on its worldvolume
 - * S_∞ does not intersect S_0 , but can be brought arbitrarily close to S_0 by complex structure deformations
 - * mass of the open strings between fractional branes at the dP_5 singularity and GUT D7-branes is controlled by a complex structure moduli of the 4fold
- Dual heterotic description \rightsquigarrow realize a three-generation $SU(5)$ theory on S_∞

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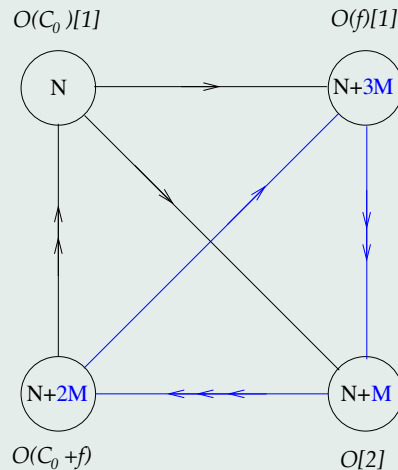
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- Kähler moduli stabilization: possible way out; return to the dP_1 model



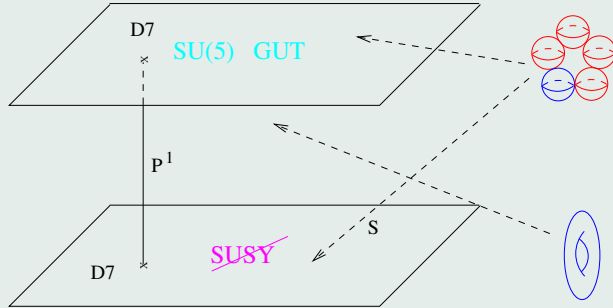
- * consider all axions obtained by integrated RR forms over even cycles in the geometry preserved by the orientifold action which are charged under the $U(1)$ gauge symmetries

- * determine their charges by demanding that the $U(1)$ anomalies are canceled by Green-Schwarz mechanism

- * write down gauge invariant contributions to the superpotential of the form Be^{iS} and understand if and how these can be generated by D3-brane instantons

5. String Theory Embeddings of Noncalculable Models

- Engineering Goal of the Section:



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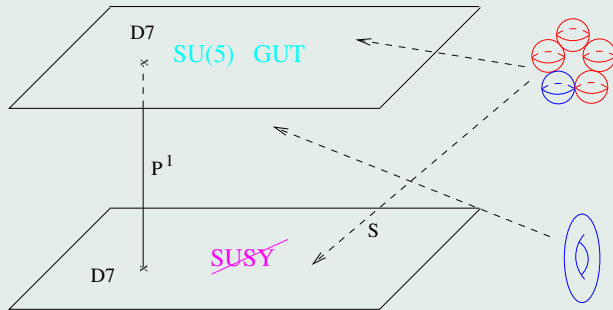
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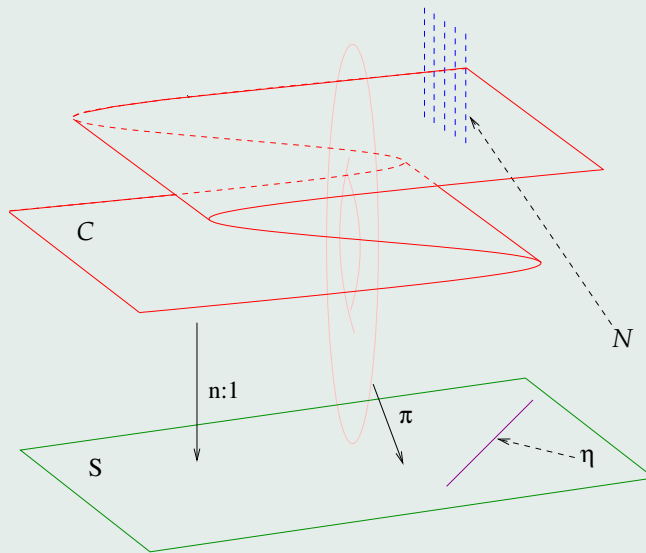


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- Dual heterotic wish list:

- Heterotic $E_8 \times E_8$ compactification on smooth Weierstrass model $\pi : Y \rightarrow S$;
- Background bundle $V_1 \times V_2 \rightarrow Y$, with V_1, V_2 stable $SU(5)$ bundles
 - * required number of generations: $\text{ch}_3(V_1) = \pm 1$, $\text{ch}_3(V_2) = \pm 3$
 - * anomaly cancellation: $c_2(V_1) + c_2(V_2) + \Lambda = c_2(Y)$, Λ effective curve on Y
- Kähler moduli stabilization \rightsquigarrow if $\Lambda = \Xi + N_5 E$, then the connected components of Ξ are smooth irreducible (-1) curves on S

- Spectral cover construction for $SU(n)$ bundles (Friedman, Morgan, Witten; Donagi)
 - (\exists) 1 : 1 correspondence between flat bundles $V \rightarrow Y$ and spectral data $(\mathcal{C}, \mathcal{N})$
 - * $\mathcal{C} = n\sigma + \pi^*\eta$ is an effective divisor on Y ; σ is the section of $\pi : Y \rightarrow S$ and η is a divisor class on S
 - * $\mathcal{N} \rightarrow \mathcal{C}$ is a torsion free rank one sheaf



- The topological invariants of V are determined by the linear equivalence class of \mathcal{C} and the Chern class of \mathcal{N} .
- Stability
 - * If \mathcal{C} is irreducible, (\exists) a polarization J such that V is stable with respect that polarization
 - * (Batyrev, Popov) \rightsquigarrow sufficient conditions on η for the spectral cover to be irreducible



- The GUT bundle

- Obtain a stable bundle V_2 with $\text{ch}_1(V_2) = 0$, $\text{ch}_3(V_2) = -3$ by taking $S \simeq dP_8$ and picking a spectral cover \mathcal{C} and line bundle \mathcal{N}

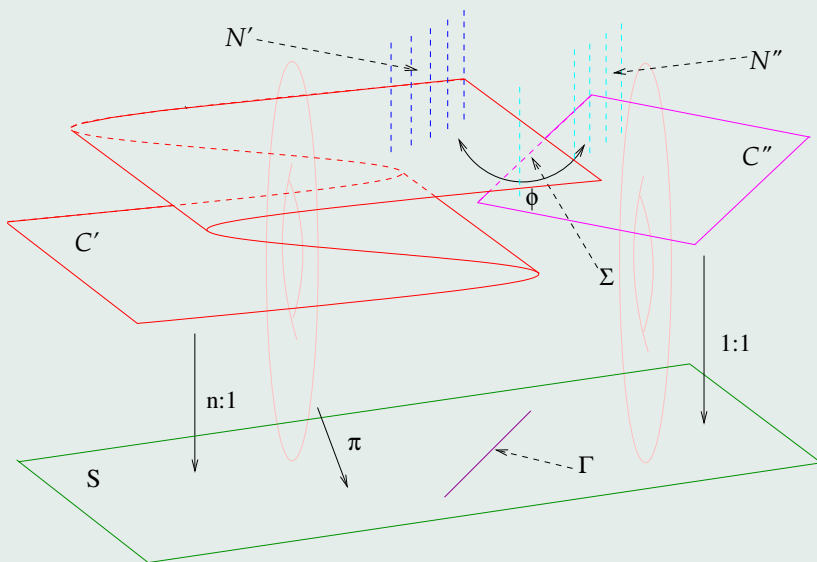
$$\mathcal{C} \in |5\sigma - 6\pi^*K_S|, \quad \mathcal{N} = \pi^*K_S^{-4}|_{\mathcal{C}}$$

- The GUT bundle

- Obtain a stable bundle V_2 with $\text{ch}_1(V_2) = 0$, $\text{ch}_3(V_2) = -3$ by taking $S \simeq dP_8$ and picking a spectral cover \mathcal{C} and line bundle \mathcal{N}

$$\mathcal{C} \in |5\sigma - 6\pi^*K_S|, \quad \mathcal{N} = \pi^*K_S^{-4}|_{\mathcal{C}}$$

- Above construction: not possible to obtain a single generation bundle \rightsquigarrow reducible spectral covers and extensions (Bershadsky, Johansen, Pantev, Sadov)



- $\mathcal{C} \rightsquigarrow$ reducible spectral cover with two smooth irreducible components

$$\mathcal{C} = \mathcal{C}' + \mathcal{C}''$$

intersecting along a smooth irreducible curve $\Sigma = \mathcal{C}' \cap \mathcal{C}''$.

- $\mathcal{N}', \mathcal{N}'' \rightsquigarrow$ spectral line bundles such that (\exists) an isomorphism

$$\phi : \mathcal{N}'|_{\mathcal{C}} \rightarrow \mathcal{N}''|_{\mathcal{C}}$$

* the data $(\mathcal{N}', \mathcal{N}'', \phi)$ determines a line bundle $\mathcal{N} \rightarrow \mathcal{C}$

- The hidden sector bundle

- Possible to pick spectral data such that $(\exists)!$ rank 5 stable bundle V_1 with

$$\text{ch}_1(V_1) = 0, \quad \text{ch}_3(V_1) = -1$$

- Need to introduce a horizontal fivebrane wrapping a (-1) curve $\Gamma \subset S$.

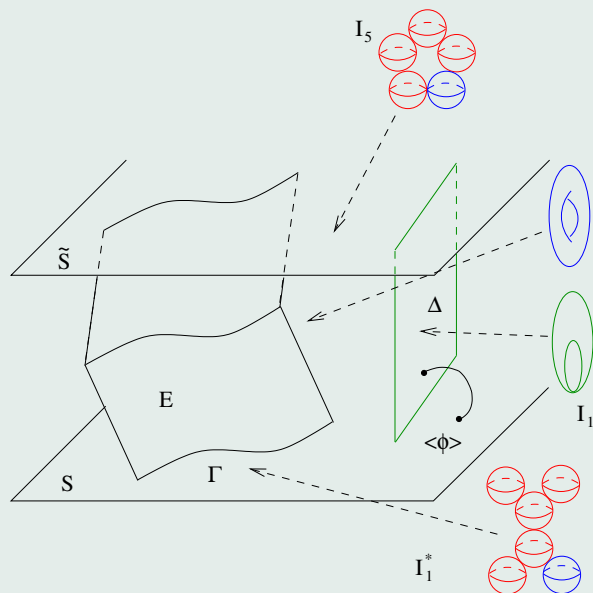
- The hidden sector bundle

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- Need to introduce a horizontal fivebrane wrapping a (-1) curve $\Gamma \subset S$.

- Dual F-theory geometry



- Horizontal heterotic fivebranes wrapped along $\Gamma \subset S \rightsquigarrow$ to blow-ups of the base B along a curve isomorphic to Γ

- \tilde{S} has trivial normal bundle in the base B and moves in a one dimensional system

- Heterotic enhanced gauge symmetry \rightsquigarrow singular elliptic fibers along the sections S and \tilde{S}

- D7-D7 strings localized at the intersection of S with nodal component of discriminant locus condense and break the apparent enhanced $SO(10)$ gauge symmetry to $SU(5)$

- Complex structure moduli stabilization
 - Possible to pick fluxes such that the movable section supporting the $SU(5)$ GUT bundle is brought arbitrarily close to the section supporting the hidden $SU(5)$
 - * tune the messenger masses such that gauge mediation is the dominant source of supersymmetry breaking in the visible sector
- Kähler moduli stabilization
 - F-theory \rightsquigarrow D3-brane instantons which correspond to holomorphic Euler characteristic 1 divisors in the Calabi-Yau 4fold X ; there \exists enough contributions to the nonperturbative superpotential to stabilize the Kähler moduli
 - * the \mathbb{P}^1 bundle over the 240 generators of the Mori cone of S
 - * the exceptional divisor E contributes since Ξ is a (-1) curve
 - * gaugino condensation on the worldvolume of the D7 brane wrapping S_0

6. Conclusions

- Provided examples of string theory compactifications incorporating a toy model of a supersymmetric GUT along with a gauge sector that breaks supersymmetry dynamically
 - Possible to arrange for the dominant mediation mechanism transmitting supersymmetry breaking to the visible sector to be gauge mediation
- Would like to have a better understanding of the stabilization of the Kähler moduli
- Would like to find models with smaller strong coupling scale Λ_H of the hidden gauge theory, messenger mass M and messenger index
- Realize similar constructions incorporating the **Penn** Heterotic Standard Models
- Statistical analysis of such models