





SMR.1771 -7

Conference and Euromech Colloquium #480 on

High Rayleigh Number Convection

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Cascades, Decoherence & Plumes in turbulent thermal convection

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Cascades, Decoherence and Plumes in Turbulent Thermal Convection

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Heng-Dong Xi

Quan Zhou

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Several issues in turbulent convection

- > Heat transport
- > Statistics of turbulent fluctuations

- >Flow structure and dynamics
- > Coherent structures

Specific issues addressed in this talk:

➤ Cascades of velocity and temperature fluctuations

Measurements of real-space velocity and temperature structure functions

De-coherence of LSC:

Cessations and Flow mode transitions

>Plumes:

Extraction and characterization of plumes as individual geometrical and thermal objects.

Part 1

Cascades of velocity and temperature fluctuations

A long-standing issue:

What is the mechanism that drives the velocity and temperature cascades in turbulent thermal convection, or, in general, buoyancy-driven thermal turbulence?

Different dynamics may be manifested as different scaling laws for the velocity and temperature structure functions

What are the true scaling exponents of the structure functions?

Bolgiano-Obukhov Scaling (1959)

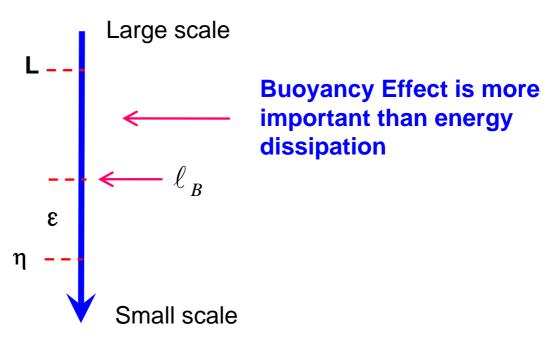
$$\eta << \ell << L$$

$$v_{\ell} = v(x+\ell) - v(x)$$

$$S_{p}(\ell) \equiv \left\langle v_{\ell}^{p} \right\rangle$$

$$T_{\ell} = T(x+\ell) - T(x)$$

$$R_{p}(\ell) \equiv \left\langle T_{\ell}^{p} \right\rangle$$



K41
$$\begin{cases} \ell < \ell_B \\ S_p(\ell) \sim \ell^{p/3} \\ R_p(\ell) \sim \ell^{p/3} \end{cases}$$

BO59
$$\begin{cases} \ell > \ell_B \\ S_p(\ell) \sim \ell^{\frac{3p}{5}} \\ R_p(\ell) \sim \ell^{\frac{p}{5}} \end{cases}$$

Scaling behavior in convective thermal turbulence: previous works

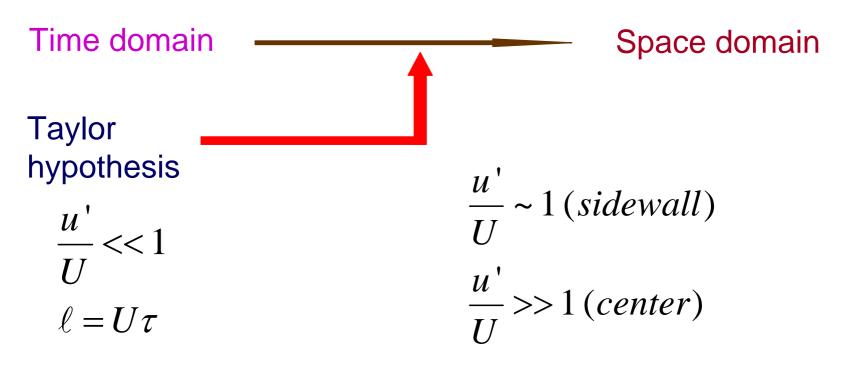
Many studies have been made on this subject.

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Procaccia & Zeitak, RPL(1989); L'vov, PRL (1991)
Wu, Kadanoff, Libchaber & Sano, PRL(1990);
Castaing, PRL (1990)
Shraiman & Siggia, PRA(1990);
Grossmann & Lohse, PRL(1991);
Tong & Shen PRL(1992);
Brandenburg PRL (1992); Yakhot, PRL (1992);
Cioni, Ciliberto & Sommeria, Europhys. Lett. (1995).
Kerr, JFM(1996)
Benzi, Toschi & Tripiccione, J. Stat. Phys. (1998)
Ashkenazi & Steinberg, PRL(1999);
Glazier et al. Nature (1999), Mashiko, Tsuji, Mizuno & Sano, PRE(2004);
Skrbek, Niemela, Sreenivasan & Donnelly, Nature (2000), PRE(2002);
Calzavarini, Toschi & Tripiccione, PRE (2002).
Ching, PRE (2000); Ching et al. JoT(2004)
Zhou & Xia, PRL(2001) Shang & Xia, PRE(2001);
Calzavarini, Toschi & Tripiccione, PRE(2002);
Camussi & Verzicco, Euro. J. Mech. (2004);
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Several theoretical models give BO scaling and many experimental and numerical results found apparent BO scaling exponent

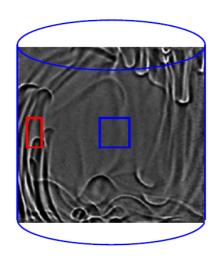
But there are also many theoretical arguments and numerical evidences against it

In the studies that appear to have observed BO59, some are based on very limited scaling range or data precision, while many others based on data obtained in the time/frequency domain. All theoretical predictions are in space domain.



To determine the true scaling properties of the temperature and velocity fields direct real-space measurements of the structure functions are needed.

Experimental Setup:



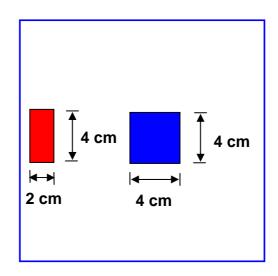
Center: few plumes

Sidewall: plume dominant region

Two regions may have different scaling behavior!

Velocity measurement

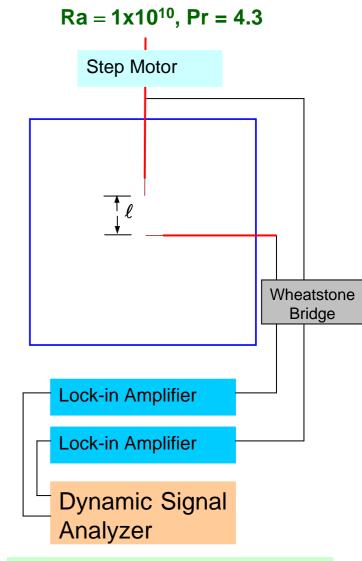
 $Ra=7x10^9$, Pr = 4.3



PIV vector maps: 7500 (1 hour with data rate 2.2 Hz)

Spatial resolution: 0.66 mm

Temperature measurement

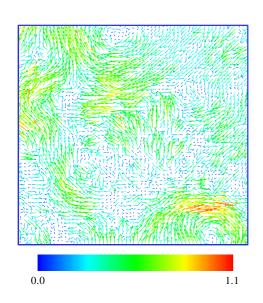


l: from 0.5 mm to 90 mm

Each l: Data rate=32Hz, Data

length:1,152,000

PIV can acquire a large amount of data for statistical calculation over a reasonable time frame

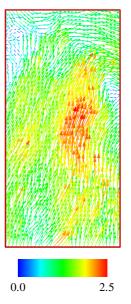




of velocity differences:

24,700,000 for smallest r in inertial region.

12,600,000 for largest r in inertial region



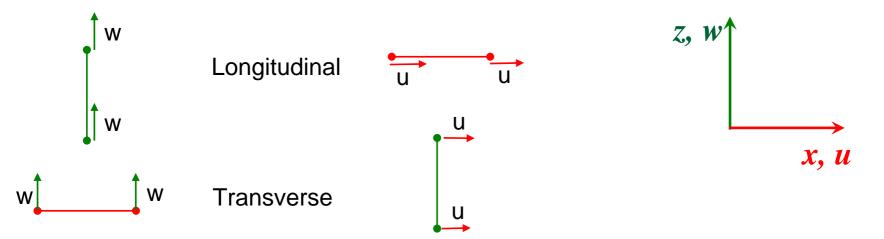
Sidewall:61x30x7500 data points

of velocity differences:

15,100,000 for smallest r in inertial range.

3,720,000 for largest r in inertial region

Definition of structure functions (SF)



Longitudinal SF of vertical velocity

Transverse SF of vertical velocity

Longitudinal SF of horizontal velocity

Transverse SF of horizontal velocity

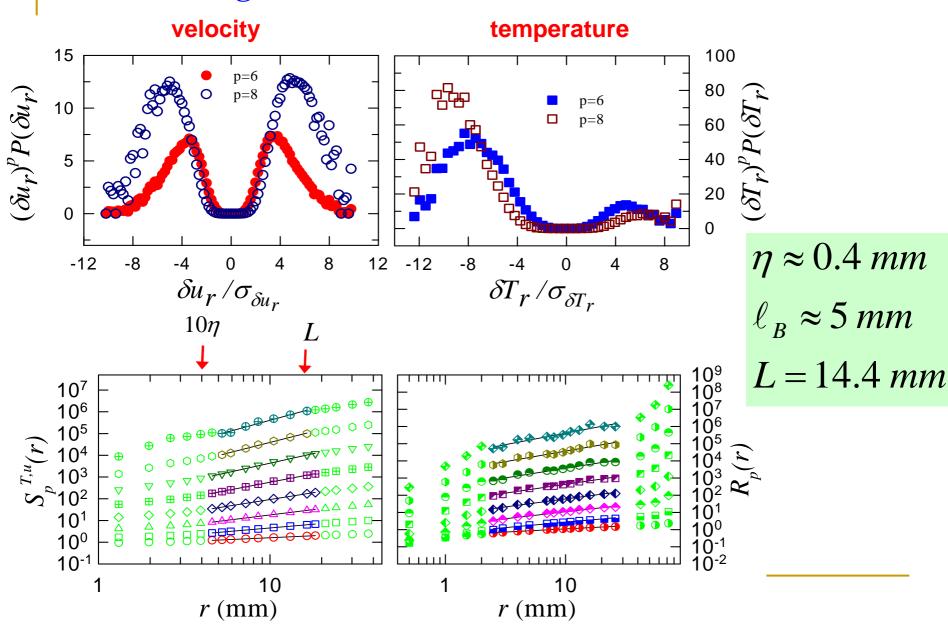
$$S_p^{L,w}(r) = \left\langle \left| w(x,z+r) - w(x,z) \right|^p \right\rangle$$

$$S_p^{T,w}(r) = \left\langle \left| w(x+r,z) - w(x,z) \right|^p \right\rangle$$

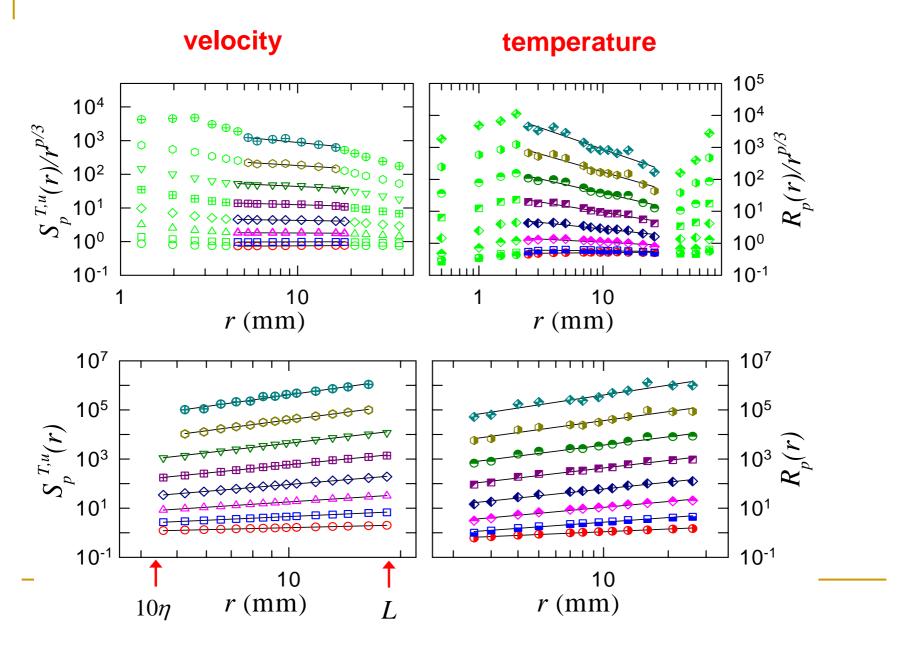
$$S_p^{L,u}(r) = \left\langle \left| u(x+r,z) - u(x,z) \right|^p \right\rangle$$

$$S_p^{T,u}(r) = \left\langle \left| u(x,z+r) - u(x,z) \right|^p \right\rangle$$

Data convergence and SFs in cell center

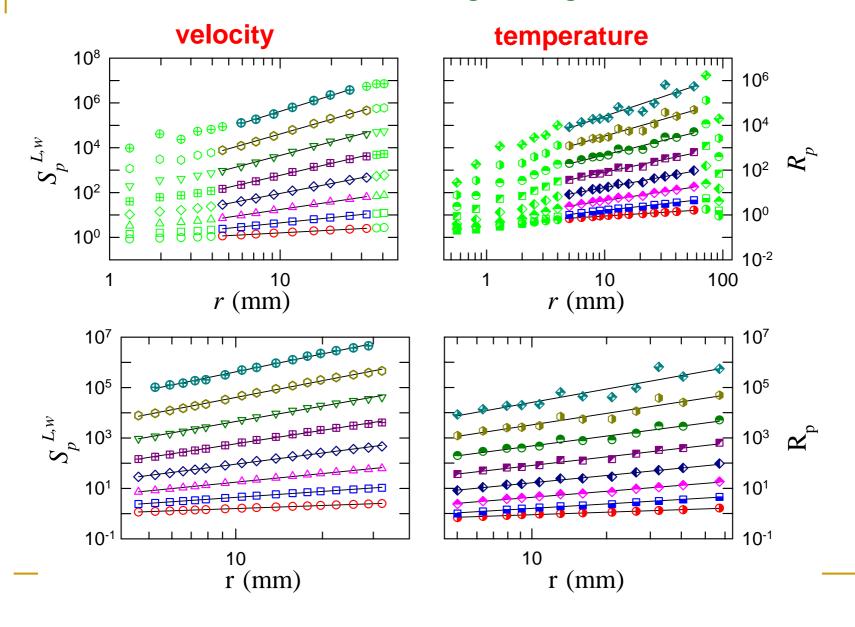


SFs in center



SFs near sidewall

Inertial range is longer than in center



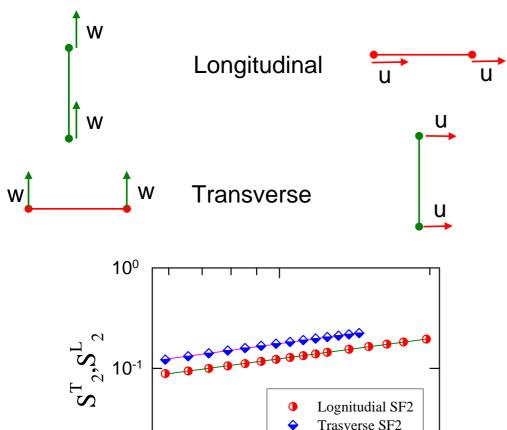
SF exponents

			Center			Sidewall	
р	$\zeta_p^{L,w}$	$\zeta_p^{T,w}$	$\zeta_p^{T,u}$	$\zeta_p^{L,u}$	$\xi_p \qquad \qquad \zeta_p^{L,w}$	$\zeta_p^{T,u}$	ξ^p
1	0.35 ± 0.01	0.35 ± 0.01	0.36 ± 0.01	0.36 ± 0.01	$0.37 \pm 0.01 \mid 0.40 \pm 0.01$	0.38 ± 0.01	0.33±0.01
2	0.68 ± 0.01	0.68 ± 0.01	0.68 ± 0.01	0.68 ± 0.01	0.63 ± 0.01 0.78 ± 0.01	0.72 ± 0.01	0.59 ± 0.01
3	0.99 ± 0.01	1.00 ± 0.01	0.98 ± 0.01	0.98 ± 0.01	0.80 ± 0.01 1.14 ± 0.01	1.01 ± 0.01	0.80 ± 0.01
4	1.25 ± 0.02	1.27 ± 0.02	1.26 ± 0.02	1.25 ± 0.02	$0.93 \pm 0.01 \mid 1.48 \pm 0.02$	1.27 ± 0.02	0.97 ± 0.01
5	1.53 ± 0.03	1.51 ± 0.03	1.52 ± 0.03	1.53 ± 0.03	1.03 ± 0.01 1.78 ± 0.03	1.52 ± 0.04	1.13 ± 0.02
6	1.81 ± 0.04	1.73 ± 0.04	1.76 ± 0.04	1.76 ± 0.04	$1.12\pm0.02 \mid 2.03\pm0.04$	1.70 ± 0.06	1.31 ± 0.02
7	2.02 ± 0.06	1.96 ± 0.06	2.00 ± 0.06	1.99 ± 0.06	$1.22 \pm 0.04 \mid 2.21 \pm 0.06$	1.94 ± 0.08	1.52 ± 0.04
8	2.30 ± 0.10	2.09 ± 0.10	2.14 ± 0.10	2.07 ± 0.10	$1.33 \pm 0.05 \mid 2.36 \pm 0.08$	2.05 ± 0.13	1.77 ± 0.05

Velocity fluctuations in central region appear to be isotropic.

Statistical characteristics in cell center

Condition for local isotropy:



10 *r (mm)*

 10^{-2}

$$S_2^T = S_2^L + \frac{1}{2}r\frac{\partial}{\partial r}S_2^L$$

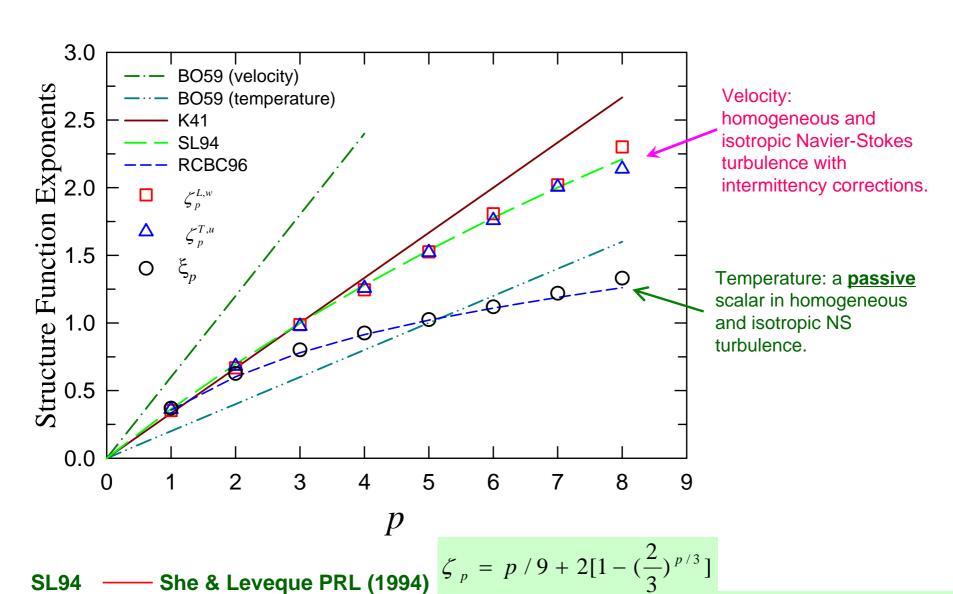
$$S_2^T = (1 + 0.68/2)S_2^L = 1.34S_2^L$$

$$w: S_2^T / S_2^L = 1.31 \pm 001$$

$$u: S_2^T / S_2^L = 1.34 \pm 0.02$$

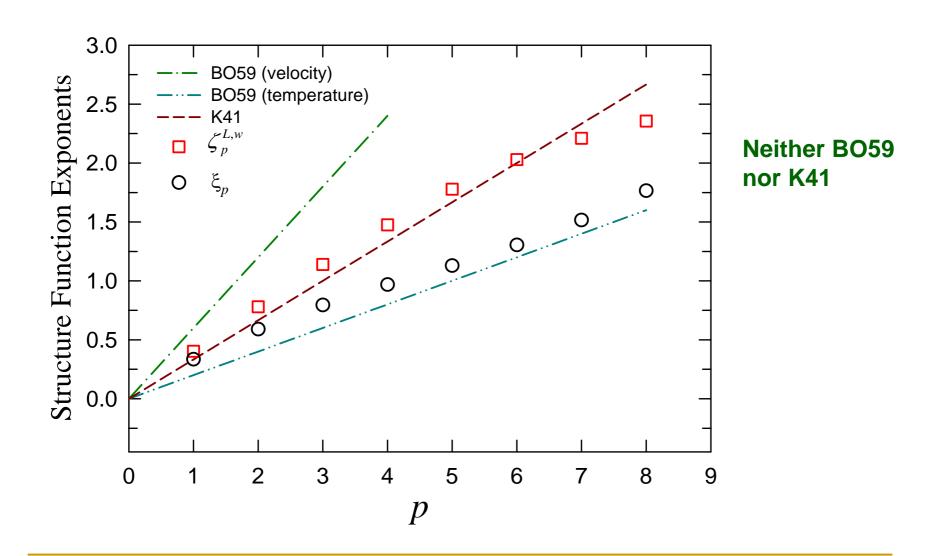
Cell center: nearly isotropic.

Scaling behavior in cell center



RCBC96 — Ruiz-Chavarria, Baudet & Ciliberto, Physica D (1996) $\xi_p = 0.06p + 0.8(1 - 0.63^p)$

Scaling behavior near sidewall: vertical direction



Dimension model

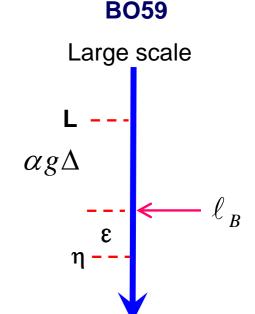
$$\frac{\partial \vec{u}}{\partial t} + \vec{u} \cdot \nabla \vec{u} = -\frac{1}{\rho} \nabla p + \nu \nabla^2 \vec{u} - g \alpha \Delta T \hat{z}$$

Both dissipation and buoyancy influence the cascade.

Assume ε_v and $\alpha g \Delta$ are equally important:

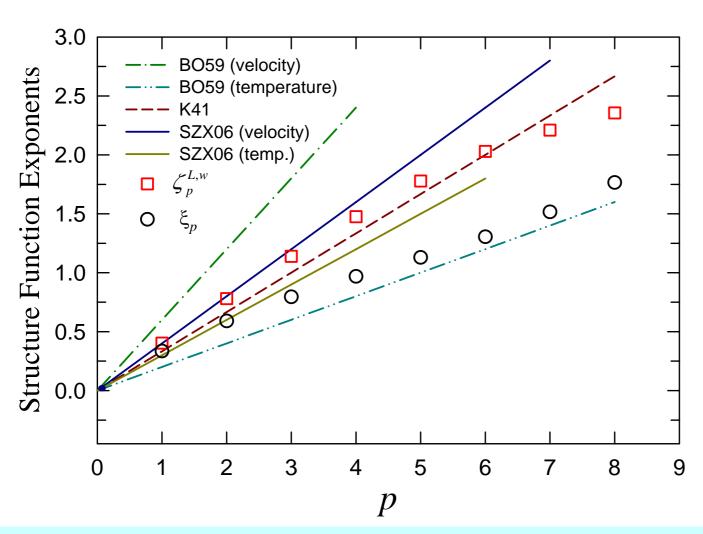
$$v_{\ell}^{p} \sim \ell^{\alpha} (\alpha g \Delta \varepsilon_{v})^{\beta} = \ell^{\frac{2p}{5}} (\alpha g \Delta \varepsilon_{v})^{\frac{p}{5}} \sim \ell^{\frac{2p}{5}}$$

$$T_{\ell}^{p} \sim \ell^{a} (\alpha g \Delta \varepsilon_{v})^{b} \varepsilon_{\theta}^{c} = \ell^{\frac{3p}{10}} (\alpha g \Delta \varepsilon_{v})^{-\frac{p}{10}} \varepsilon_{\theta}^{\frac{p}{2}} \sim \ell^{\frac{3p}{10}}$$



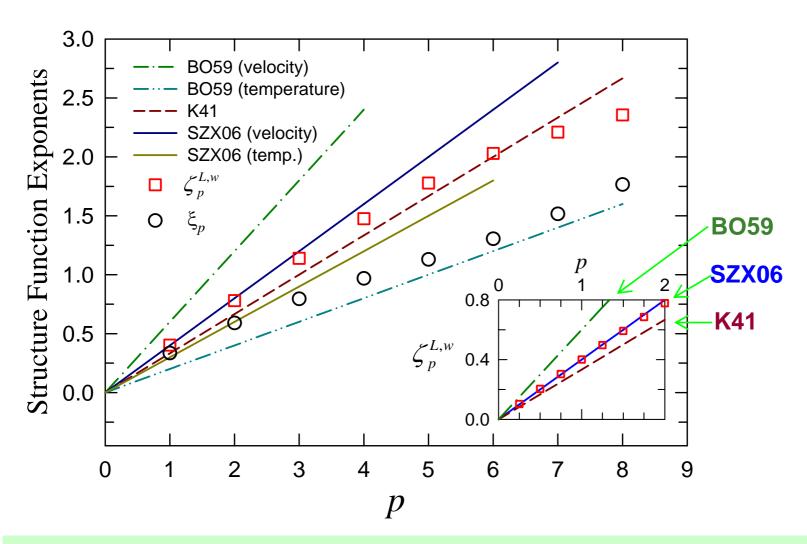
Small scale

Scaling behavior near sidewall: vertical direction



High order structure functions are influenced by intermittency effect, low order SFs can better test the dimensional model.

Fractional SFs



Excellent agreement between our model with experimental results for fractional SFs,

Summary for Part 1

Cell center: Turbulent flow is locally isotropic

Velocity behaves the same as in homogeneous and isotropic NS turbulence. SF exponents may be described by the hierarchy model for velocities (SL94).

Temperature behaves as a passive scalar in NS turbulence. SF exponents may be described by the hierarchy model for passive Scalars (RCBC96).

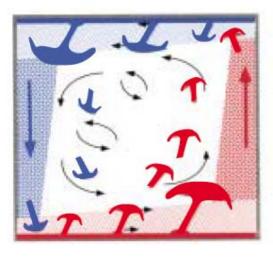
Sidewall: Turbulent flow is locally anisotropic.

Vertical velocity and temperature follow neither BO59 nor K41. SF exponents may be described by a dimension model treating buoyancy and viscous dissipation on an equal footing.

High order SF deviate from dimensional model due to intermittency.

Part 2

Cessations and Decoherence of the Large-scale Circulation



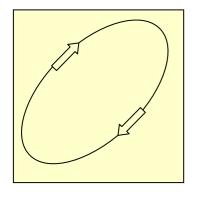
Kadanoff, Physics Today (2001)

- ➤ A large-scale-circulation (LSC) exists in RB system
- Cioni et al observed azimuthal rotation of the LSC in mercury convection (*JFM 1997*).
- ➤ Niemela et al found reversals of LSC in helium (*JFM* 2001).

Flow reversal occurs in many turbulent flow systems.

Reversal of the LSC in turbulent convection may be related to natural phenomena such as the reversal of the geomagnetic polarity.

Reversal phenomenon



Two scenarios

In-plane reversal

180° azimuthal rotation

Statistical analysis and physical models:

Sreenivasan, Bershadskii and Niemela, *PRE 2002, Physica A 2004, Physics Lett. 2004, Hwa et al, PRE 2005*

Benzi, PRL 2005.

Araujo, Grossmann and Lohse, *PRL* 2005.

More recent experiments:

Brown, Nikolaenko & Ahlers, *PRL* 2005; Brown & Ahlers, JFM 2006 Sun, Xi & Xia, PRL 2005, Xi, Zhou, & Xia (PRE 2006)

Ahlers group found both the in-plane reversal and 180° azimuthal rotation can occur and identified the 'cessation' phenomenon.

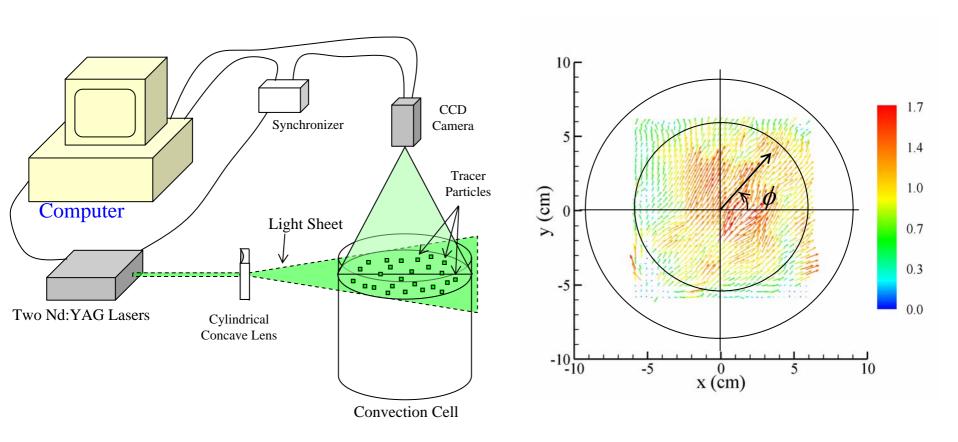
Xia group found the azimuthal motion of LSC plane consists of net rotations and erratic fluctuations. The residents phenomenon is observed.

Motivation

- The physical pictures in theoretical models appear to apply to unity aspect ratio geometry.
- > Can cessations occur in small aspect ratio geometry?

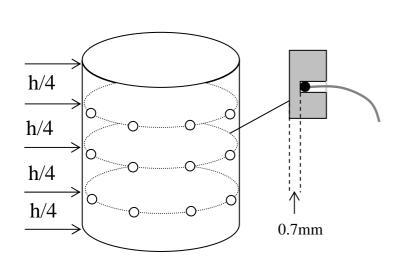
➤ What happens to the LSC during a cessation?

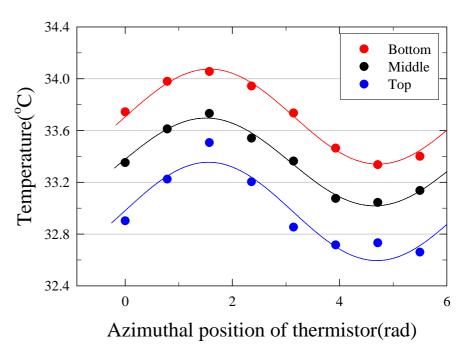
The PIV measurement



Xi, Zhou and Xia, PRE (2006)

The Multi-thermistor measurement





$$T_i = T_0 + A\cos(i\pi/4 - \phi)$$

- A(t) measures the flow strength (amplitude of the LSC)
- $\phi(t)$ is the azimuthal postion where the hot side of the LSC goes up.

Cessations in $\Gamma = \frac{1}{2}$ convection cell

Setup and parameter range:

Sapphire cell

■ PIV, Multi-thermistor simultaneously

$$Ra = 5.7 \times 10^9$$
, 1.5×10^{10} , 3.3×10^{10} , $Pr = 5.3$

Multi-thermistor

$$Ra = 1.4 \times 10^{10}, \ 1.5 \times 10^{10}, \ 1.6 \times 10^{10}, \ 3.0 \times 10^{10}, \ 3.3 \times 10^{10}, \ 4.3 \times 10^{10}, \ 7.2 \times 10^{10}$$

$$Pr = 4.9 - 5.3$$

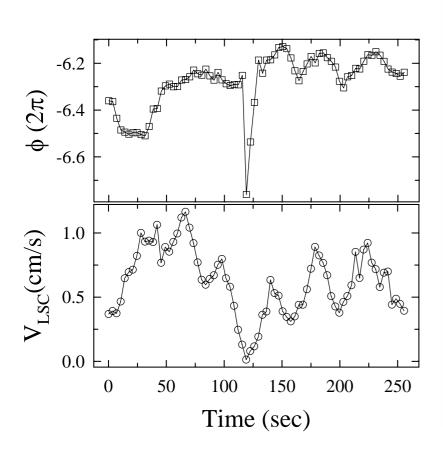
Copper cell

■ Multi-thermistor, 34-day measurement. Ra = 5.6x10¹⁰

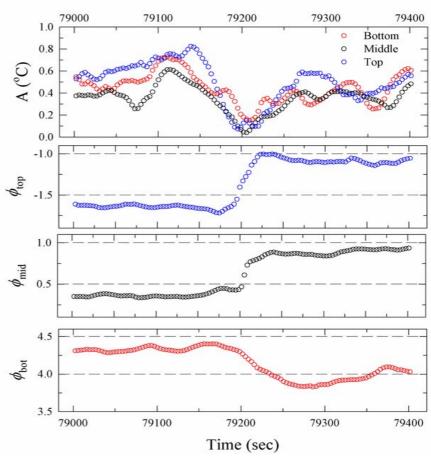
The same statistical results are obtained from all these measurements

The examples of cessation in $\Gamma = \frac{1}{2}$ cell

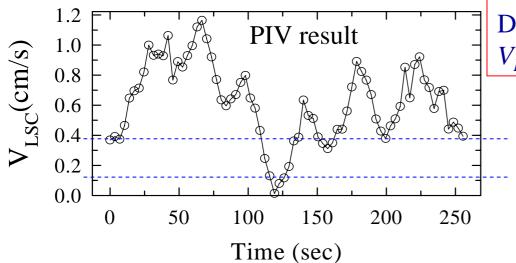
PIV result



Muti-thermistor result



The definition of a cessation



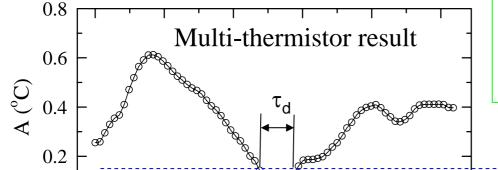
Cessation is defined by $V_{LSC} < (V_{LSC})_L$

Duration τ_d of cessation is defined by $V_{LSC} < (V_{LSC})_h$

$$(V_{LSC})_h$$

$$(V_{LSC})_l = 0.1 < V_{LSC} >$$

$$(V_{LSC})_h$$
 $(V_{LSC})_l = 0.1 < V_{LSC} >$
 $(V_{LSC})_l$ $(V_{LSC})_h = 0.3 < V_{LSC} >$



100

150

Time (sec)

200

250

50

0.0

0

Cessation is defined by $A < (A)_{I}$

Duration of cessation τ_d is defined by $A < (A)_h$

$$A_h$$

$$A_l = 0.1 < A >$$
 $A_h = 0.3 < A >$

$$A_h = 0.3 < A >$$

Thresholds explored

$$(V_{LSC})_l = (0.05 \sim 0.2) < V_{LSC} > 0.05 \sim 0.2$$

$$(V_{LSC})_h = (0.2 \sim 0.8) < V_{LSC} >$$

Similar statistics are obtained

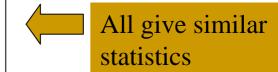
$$A_1 = (0.05 \sim 0.2) < A >$$

$$A_l = (0.05 \sim 0.2) < A >$$

 $A_h = (0.2 \sim 0.8) < A >$

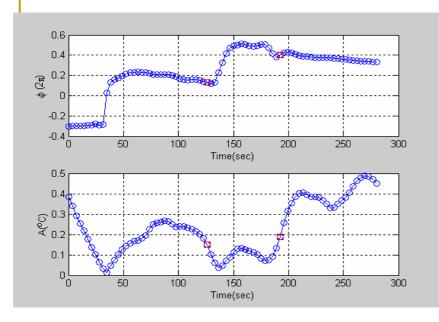
Similar statistics are obtained

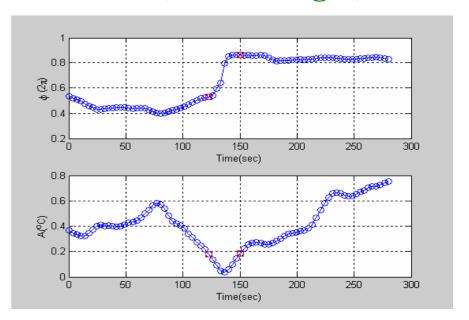
- PIV, multi-Ra: **466** cessations
- Multi-thermistor, multi-Ra: 1778 cessations
- ■Single-Ra, 34-day measurement: **1071** cessations

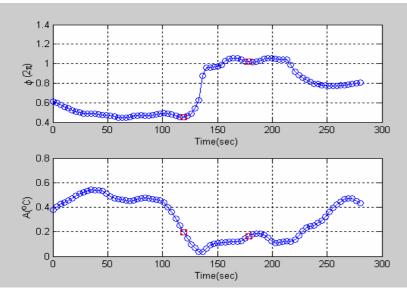


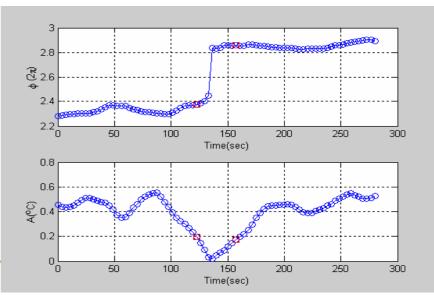
The number of cessations identified by the 3 rows of thermistors at different heights differ by less than 3%, and the statistics are all the same.

Examples of cessations, multi-thermistor (middle height)

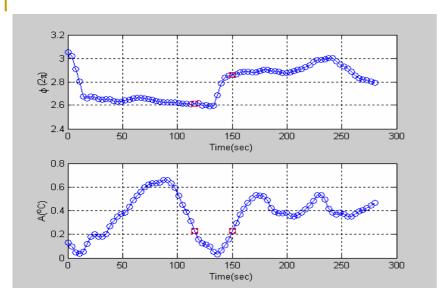


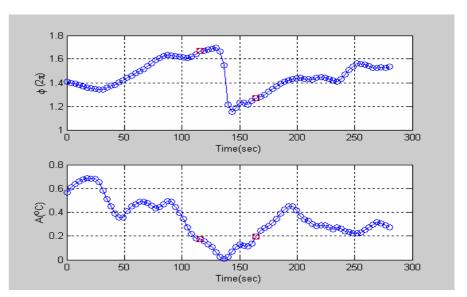


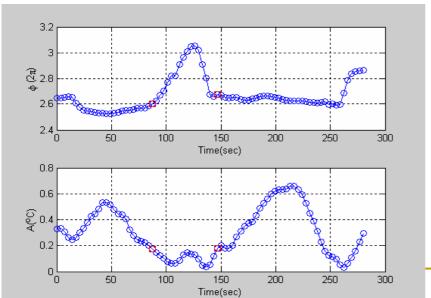


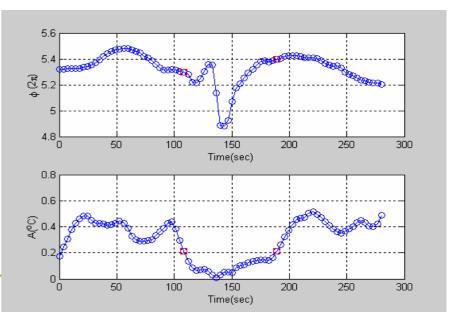


Examples of cessations, multi-thermistor (bottom row)

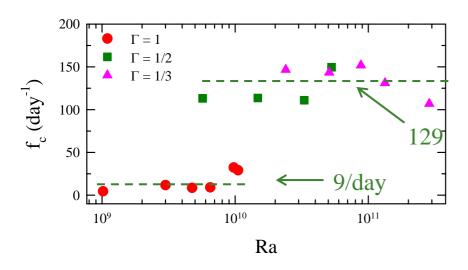








PIV result

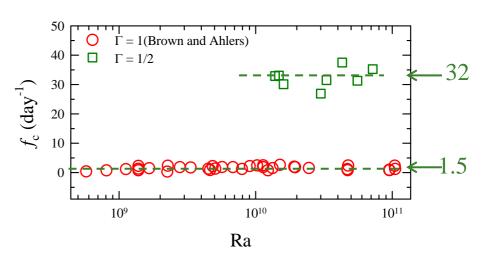


$$\frac{f_c(\Gamma = 1/2, 1/3)}{f_c(\Gamma = 1)} = 14$$

$$f_c(PIV)/f_c(therm) = 3.7 \sim 6$$

 Γ = 1 PIV data is reanalyzed using new definition (96 now vs. 28 in Xi et al, PRE 2006)

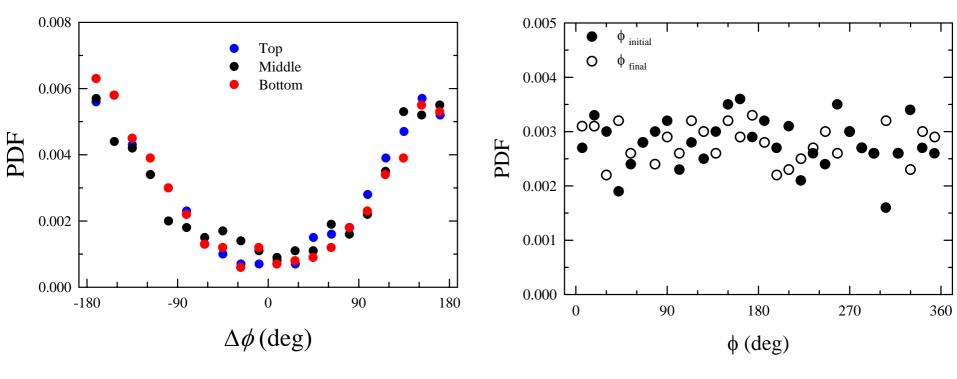
Multi-thermistor result



$$\frac{f_c(\Gamma=1/2)}{f_c(\Gamma=1)} = 20$$

Cessations in Γ < 1 cells occur an order of magnitude more frequent than in Γ = 1 cells.

Orientational change $\Delta \phi$ of LSC before and after a cessation



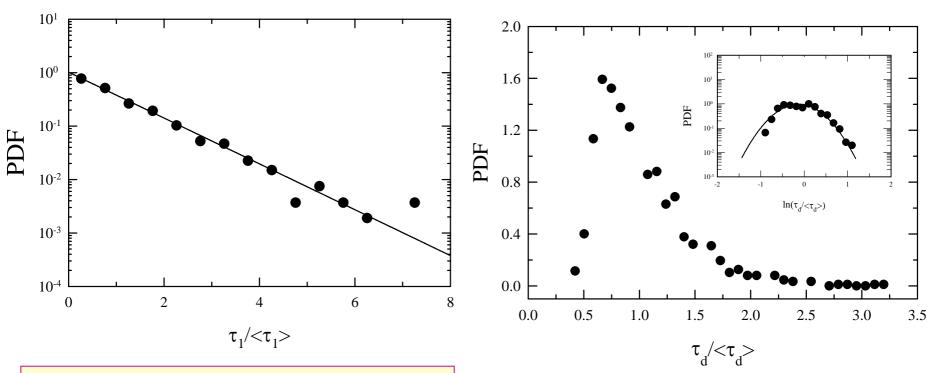
Uniform distribution in $\Gamma = 1$ cell (Brown and Ahlers, PRL05, JFM 2006; Xi, et al PRE 2006)

 $\phi_{initial}$ and ϕ_{final} --- orientation of LSC before and after a cessation

Cessations with $|\Delta \phi|$ close to 180 is 6 times more likely to occur than cessations with small $|\Delta \phi|$

Statistics of cessation

Cessation statistics in $\Gamma=1/2$ are similar to the $\Gamma=1$ case, except that of $\Delta \phi$



 τ_1 ---- time between successive cessations.

The straight line is: $p(\tau_1/\langle \tau_1 \rangle) = \exp(-\tau_1/\langle \tau_1 \rangle)$

$$<\tau_1> = 46 \text{ min.}, <\tau_1>_{\text{max}} = 342 \text{ min}, <\tau_1>_{\text{min}} = 0.7 \text{ min}$$

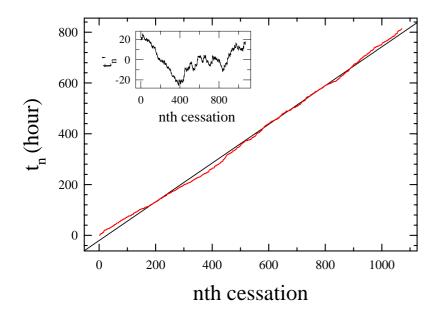
 τ_d --- duration of a cessation

$$<\tau_{\rm d}> = 46 \text{ s}, \text{ max} = 150 \text{ s}, \text{ min} = 18 \text{ s}$$

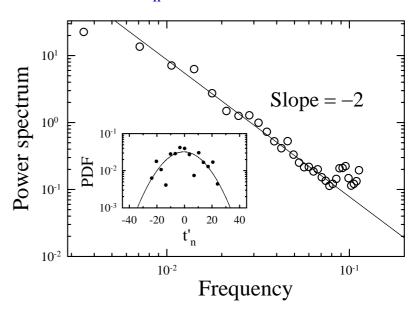
Benzi, PRL, 2005; Brown and Ahlers, JFM 2006.

Statistics of cessation

t_n --- the time that nth cessation occurs



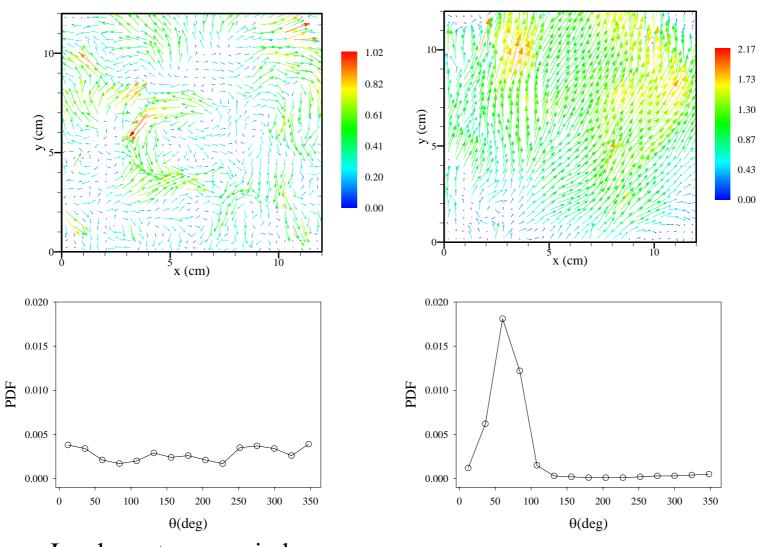
The PDF and power spectrum of detrended t_n .



The statistics for t_n are consistent with those of "reversals" found by Sreenivasan, Bershadskii and Niemela (PRE2002), and "crossings" by Xi, Zhou and Xia (PRE2006). But not those for τ_1 (no power law for small τ_1).

What happens during the cessation?

$$\Gamma = 1$$

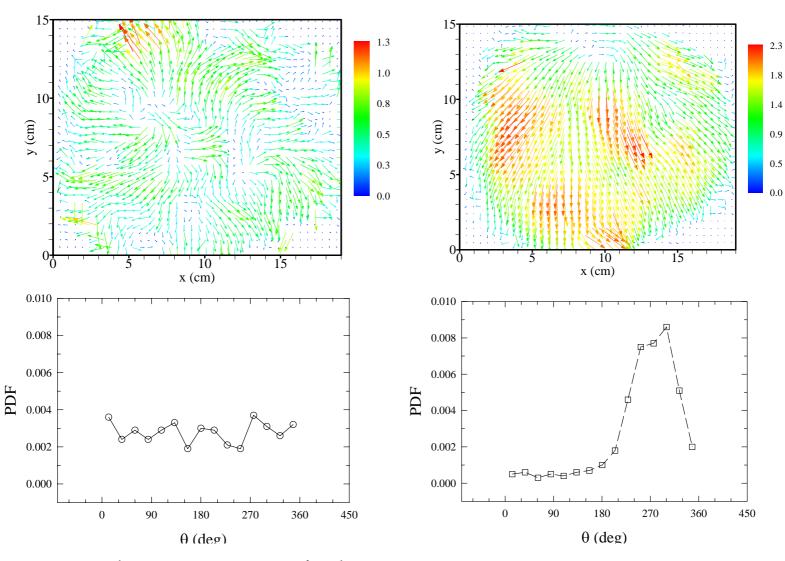


Incoherent mean wind

coherent mean wind



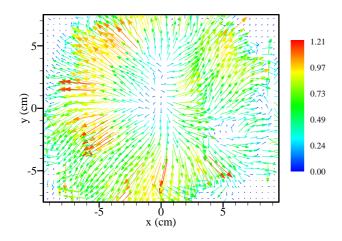
$$\Gamma = 1/2$$



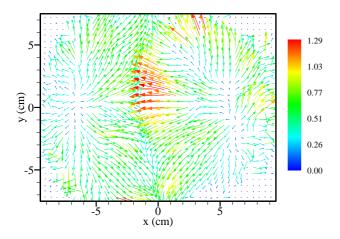
Incoherent mean wind

coherent mean wind

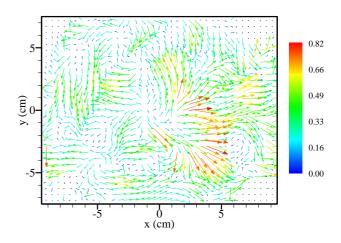
Three incoherent modes causing cessations



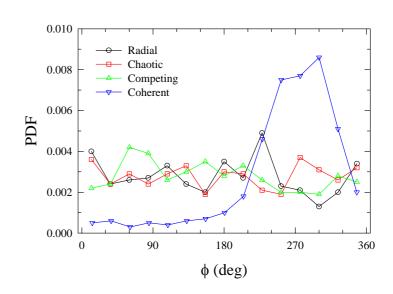
Incoherent flow, radial mode



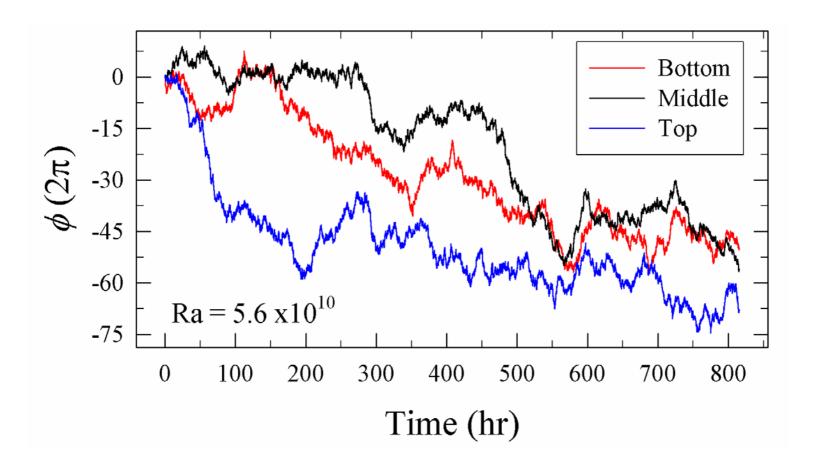
Incoherent flow, competing mode



Incoherent flow, chaotic mode

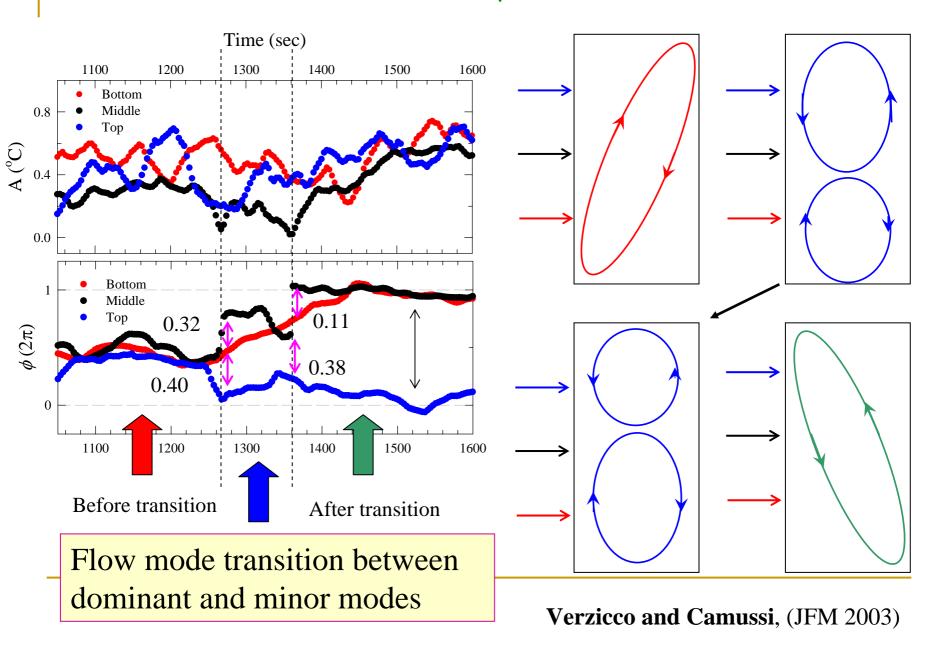


The measured time trace of orientation of LSC plane

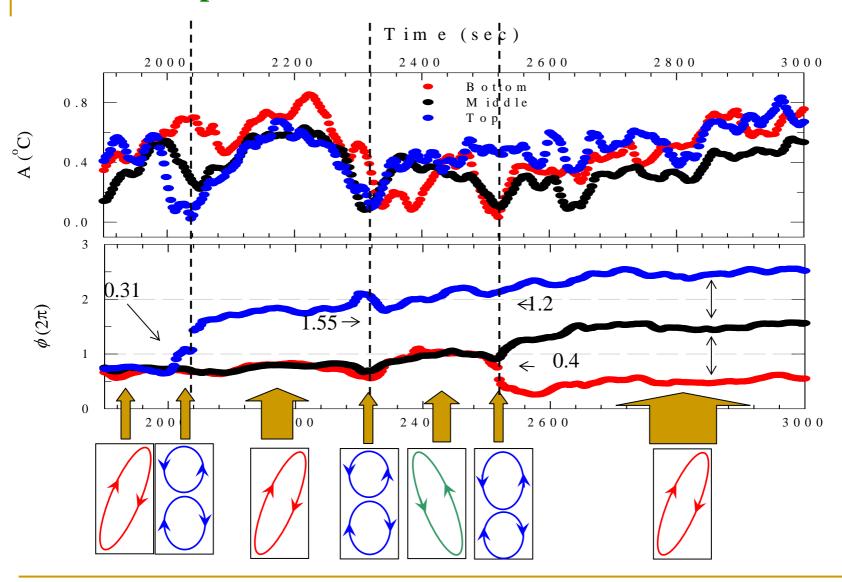


Positive is counterclockwise

Possible scenario for the divergence of ϕ obtained at different heights

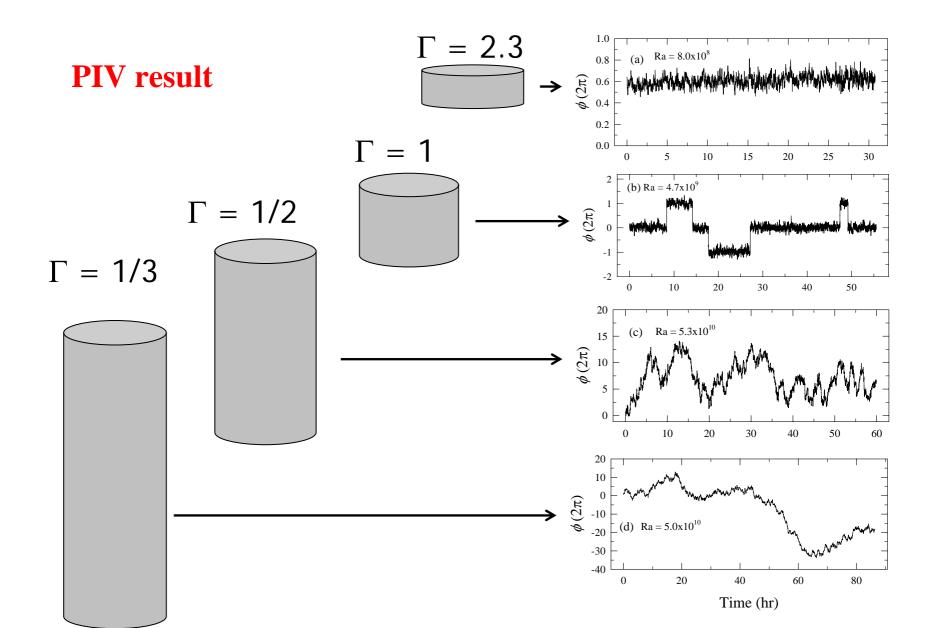


More examples of flow-mode transitions

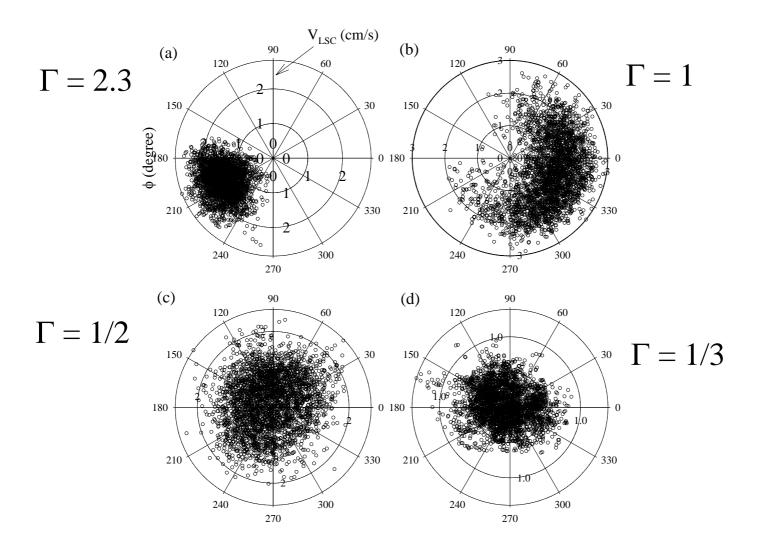


Duration of flow mode transition is less than 100 second.

The orientation trace in cells of different Γ

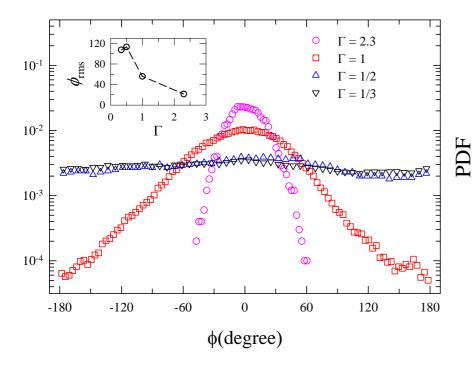


The plots of the traces in polar coordinate

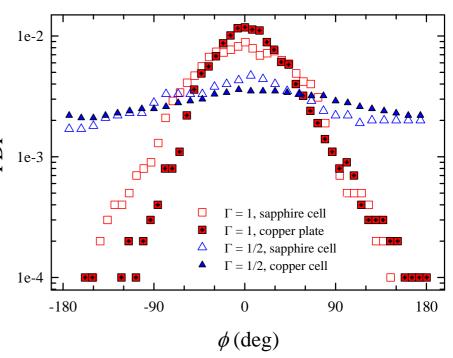


The PDF of the orientation of LSC for different aspect ratio





Multi-thermistor result



Summary of Part 2

- Cessations occur an order of magnitude more frequently in small Γ cells than in cell with $\Gamma = 1$. The frequency of occurrence has no obvious dependence on Ra.
- The LSC likes to reverse its direction after a cessation in cells with $\Gamma = 1/2$.
- Common features of the statistics properties based on pure-cessation events, rotations/reorientations, reversals, and crossings suggest that all these phenomena may share the same origin.
- Constraints for theoretical models (SOC, dynamical systems, stochastic).
- A cessation event is a process of de-coherence, or disorganization and reorganization of the LSC.
- Flow-mode transitions may have been observed indirectly by temperature measurement.

Part 3

Morphological evolution and geometrical properties of turbulent thermal plumes

Mushroom-like Plumes





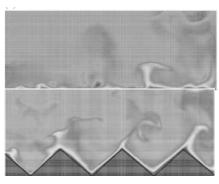
Werne (1994)



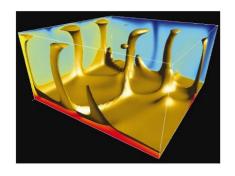
Zhang, Childress, Libchaber (1997)



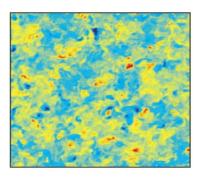
Du & Tong (1998)



Stringano, Pascazio & Verzicco (2006)



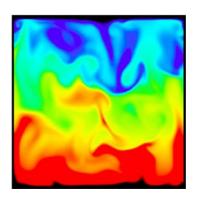
Breuer, Wessling, Schmalzl & Hansen (2004)



Parodi et al. (2004)



Xi, Lam & K.-Q. Xia (2004)

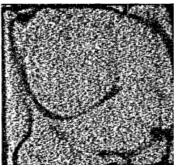


Toschi (2006)

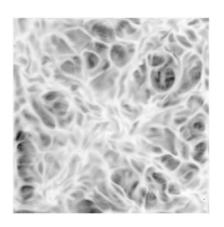
Sheet-like Plumes



Zocchi, Moses, Libchaber (1990)



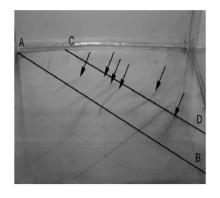
Gluchman, Willaime, Gollub (1993)



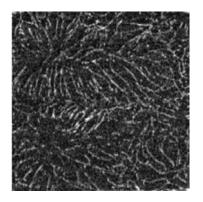
Kerr (1996,2000)



Funfschilling & Ahlers (2004)



String-like coherent structure
Haramina and Tilgner (2004)



Puthenveettil & Arakeri (2005)



Sheet-like plumes



Mush-like plumes

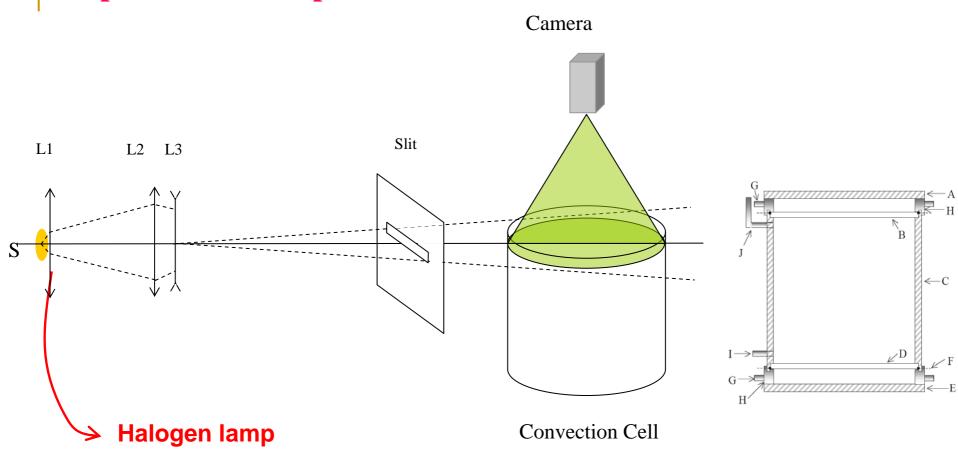
Motivation

What are the geometrical and thermal properties of the plumes as individual objects?

How do sheet-like plumes transform into mush-like ones?

This work represents the an attempt to quantitatively characterize these coherent structures, which remain largely unexplored.

Experimental setup



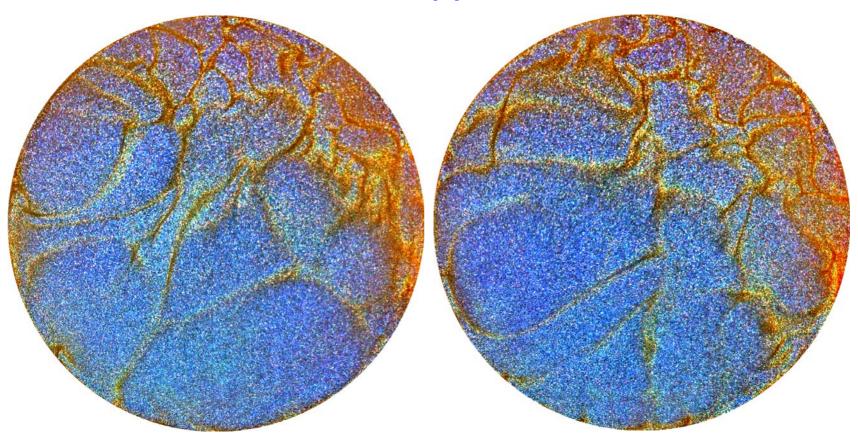
TLC: Thermochromic liquid crystal microspheres (R29C4W), 50 μ m mean diameter.

Red: 29-29.5°C; Green: 29.5-29.7°C; Blue: 29.7-33°C

Zocchi, Moses & Libchaber (1990); Gluchman, Willaime & Gollub (1993); Du & Tong (1998)

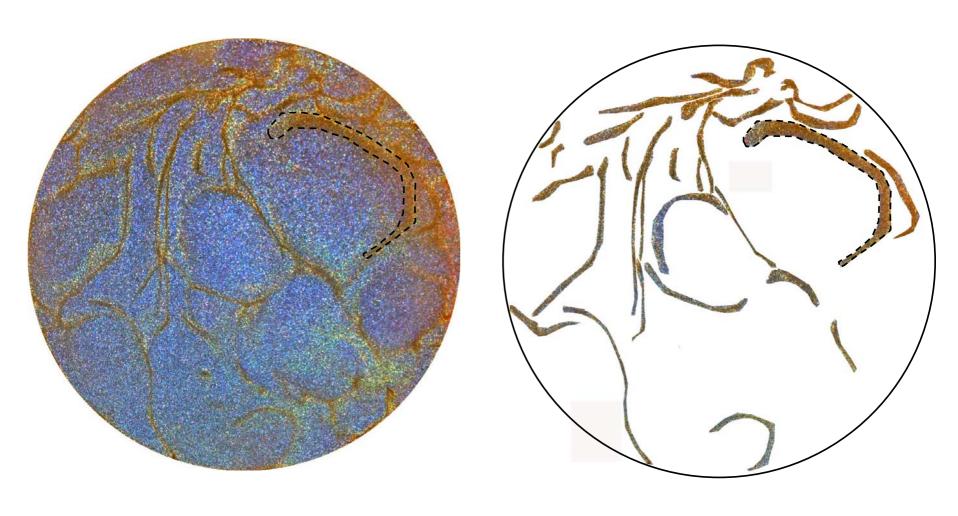
Sheet like plumes

3 mm from top plate

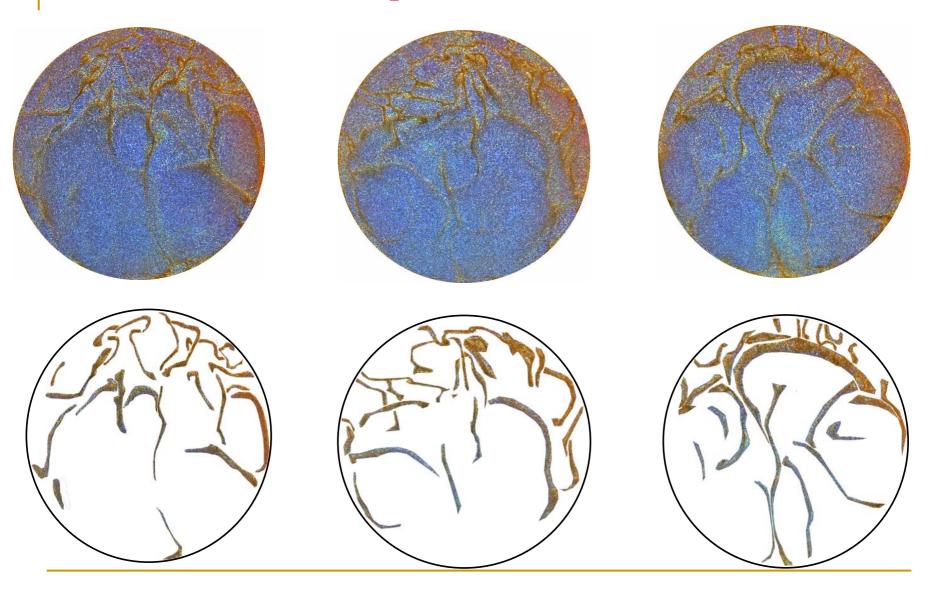


Sheet like plumes were observed near boundary layer.

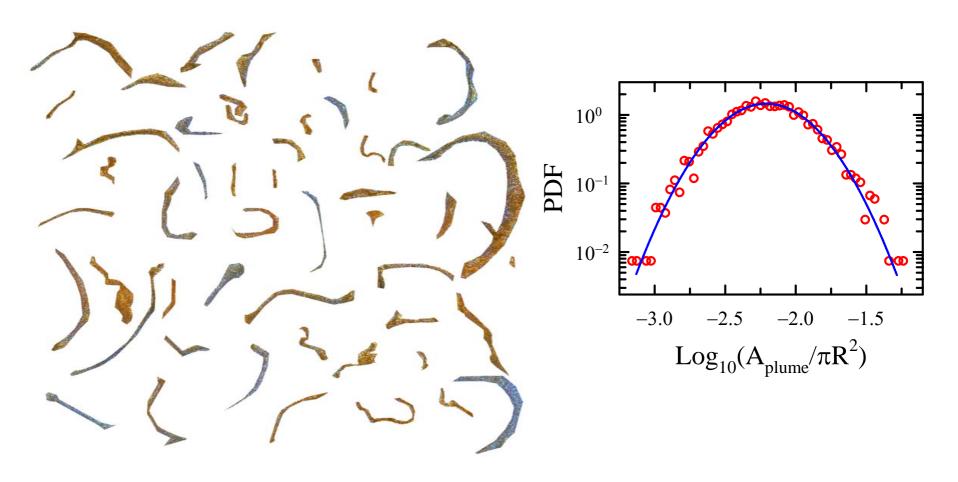
Extraction of sheet-like plumes



Extraction of sheet-like plumes



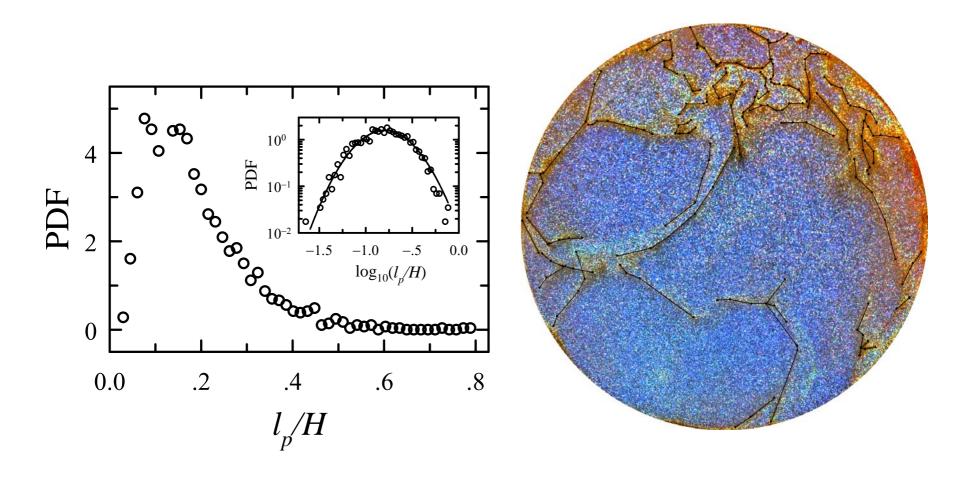
Geometric characteristics: Area



4001 plumes extracted from 200 images.

Areas of plumes follow log-normal distribution: both sheet-like and mush-like plumes (Zhou and Xia, PRL 2002).

Geometric characteristics: Length



The lengths of sheet-like plumes also follow log-normal distribution.

Temperature of a plume

Red-Green-Blue (RGB)



Hue-Saturation-Intensity (HSI)

Hue: a measure of the peak wavelength
→ temperature

Saturation: a measure of the color contrast

Intensity: a measure of the total light intensity

Plumes statistics

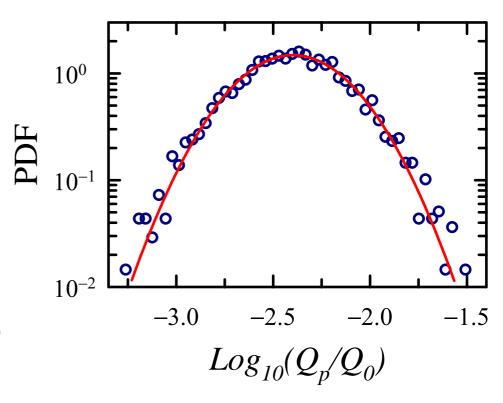
'heat' contained in a plume

$$Q_p = \sum c_p(T_i) \rho(T_i) S_{pix}(T_i - T_0)$$

Area of a pixel:

$$S_{pix} = 0.16 \times 0.16 mm^2$$

'heat' contained in a plume also has log-normal distribution.



The distribution of Q_p is determined by the geometric properties of the plume

Mush-like plumes

9.3 cm from top plate 2.5 cm from top plate

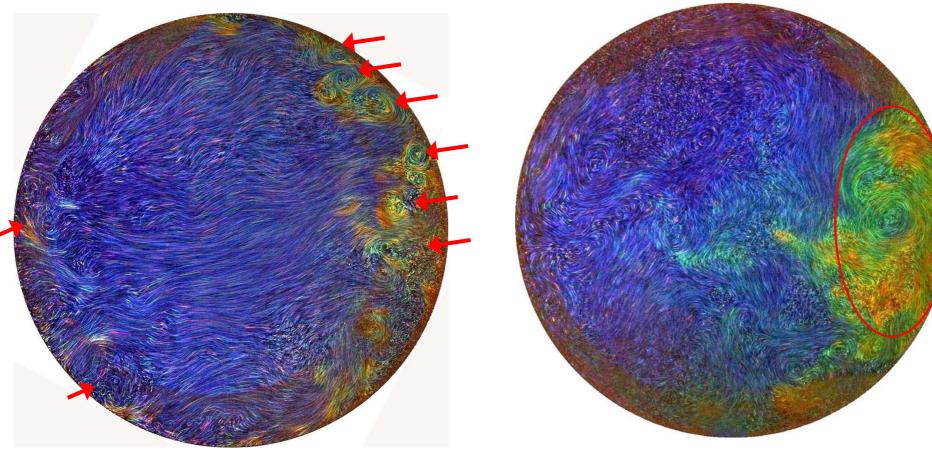
Mush like plumes were observed in bulk region.

Vortical plumes

Long-exposure shot gives both temperature and trajectories of the TLC particles.

2.5 cm from top plate

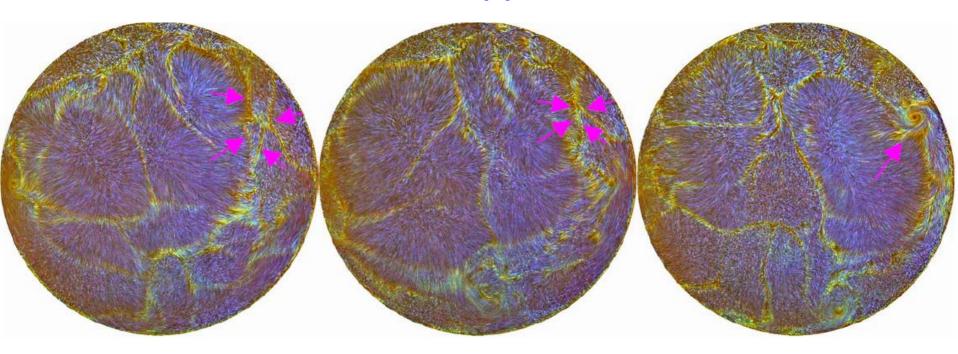
9.3 cm from top plate



Mush like plumes have intense vortical structures! - Where does vorticity come from?

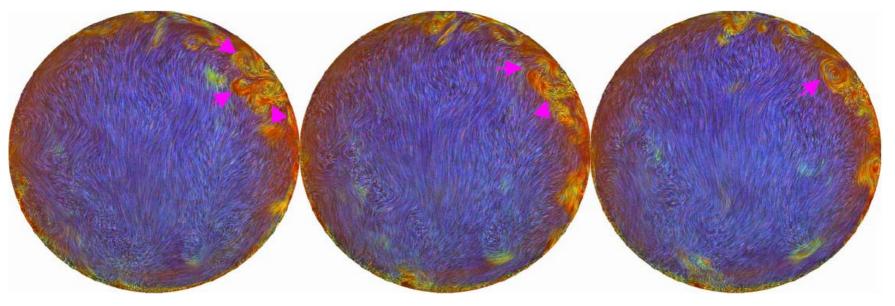
Formation of mushroom-like plumes: interaction between sheet like plumes

3 mm from top plate

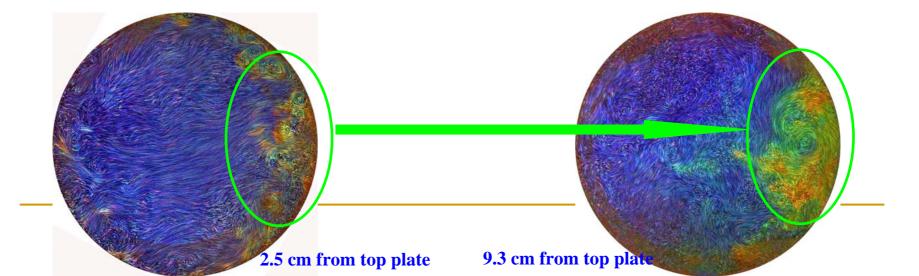


Sheet-like plumes collide and convolute to form swirls that spiral down to become mushroom-lime plumes.

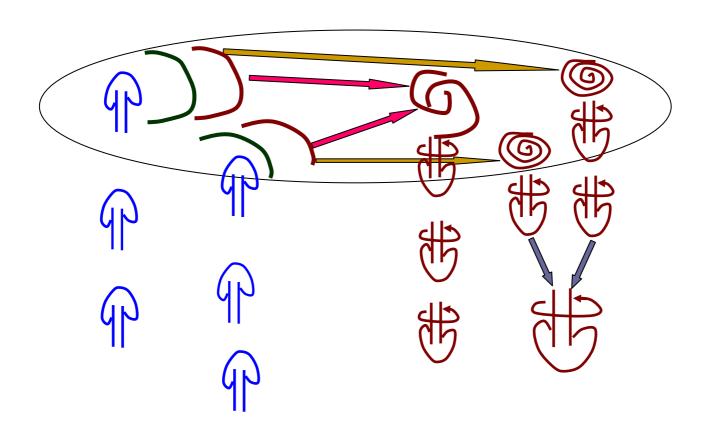
Plume clustering



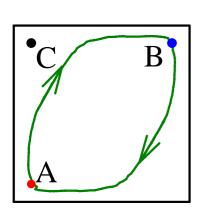
Plumes merge and cluster as they move upward/downward.



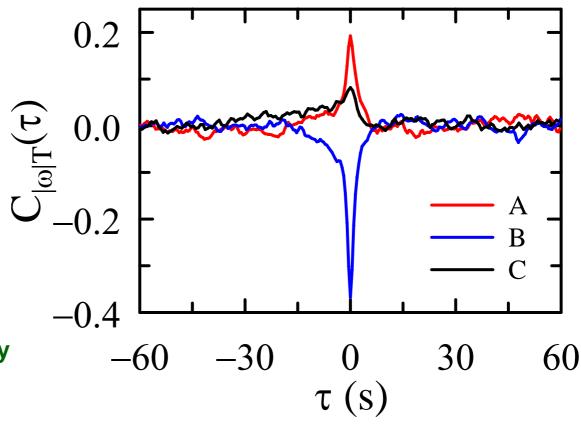
Morphological evolution of sheet-like to mushroom-like plumes



Simultaneous vorticity & temperature measurement



The fluctuations of vertical vorticity and temperature are strongly correlated.



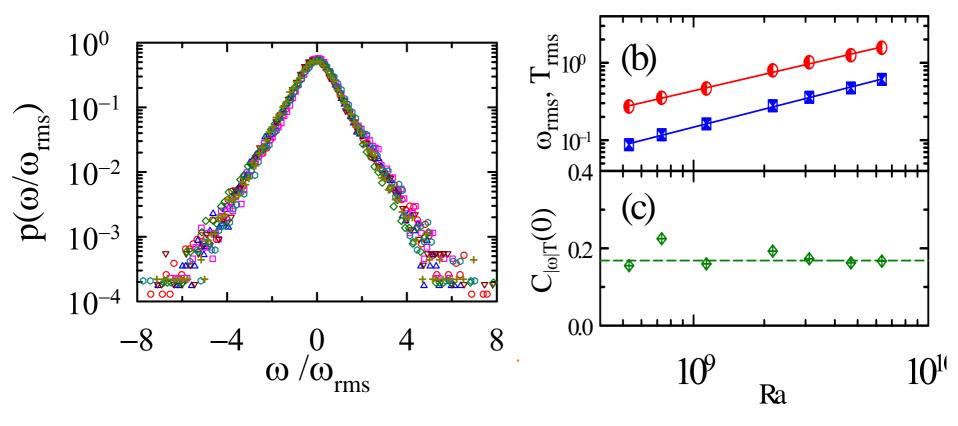
PDF of temperature, velocity and vorticity

Temperature: Exponential

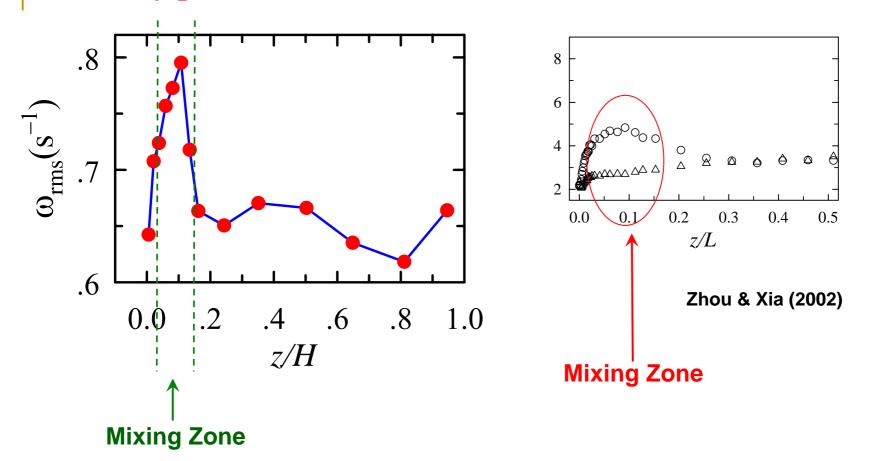
Velocity: Gaussian

Vorticity share the same characteristics with temperature rather than with velocity.

Ra-dependence of vorticity and temperature fluctuations share similar behavior.



Vorticity profile



The maximum ω_{rms} suggests that strong vorticity fluctuations are associated with merging and clustering of plumes.

The mixing zone is roughly the same as that found from the skewness of plus and minus temperature increments.

Summary for Part 3

- ➤ Individual sheetlike plumes are extracted as 2D individual geometrical and thermal objects and their area, circumference, and `heat content' are found to all exhibit log-normal distributions.
- As the sheetlike plumes move across the plate they collide and convolute into spiraling swirls. These swirls then spiral downward to become mushroom-like plumes accompanied by strong vertical vorticity.
- The measured vorticity profile reveals a mixing region within which most of plume merging and clustering take place.
- ➤ The fluctuating vorticity is found to have the same exponential distribution and scaling behavior as the fluctuating temperature.