



The Abdus Salam
International Centre for Theoretical Physics



SMR.1771 - 20

Conference and Euromech Colloquium #480

on

High Rayleigh Number Convection

4 - 8 Sept., 2006, ICTP, Trieste, Italy

Rotational effects on turbulent convection

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These are preliminary lecture notes, intended only for distribution to participants

Rotational Effects on Turbulent Convection

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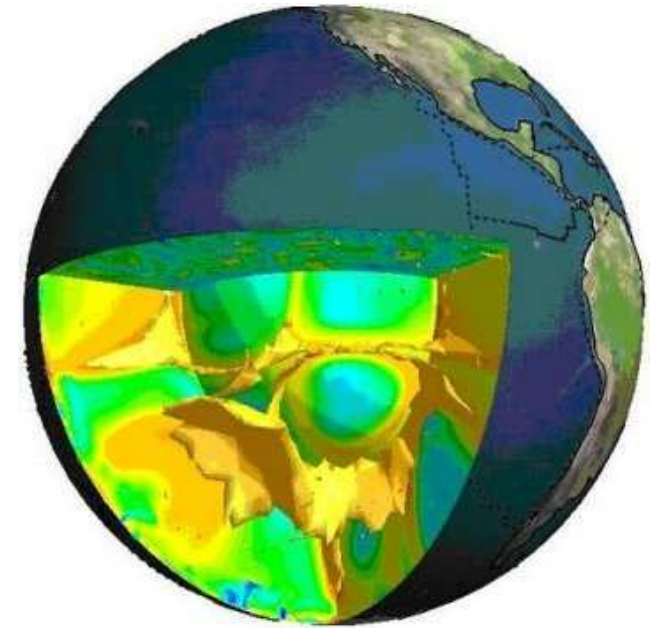
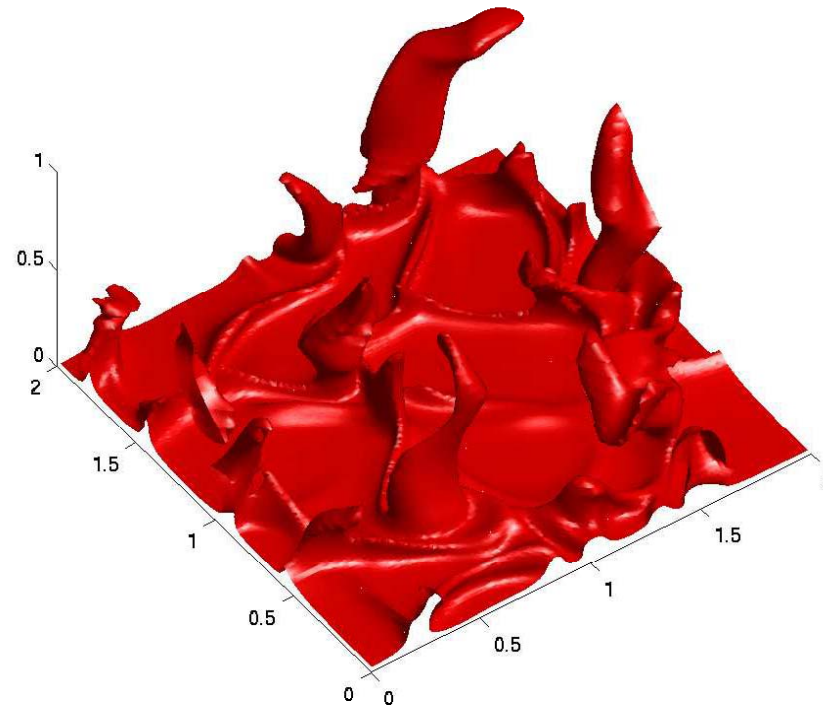
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*Euromech Colloquium on
High Rayleigh Number Convection
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Convection influenced by rotation

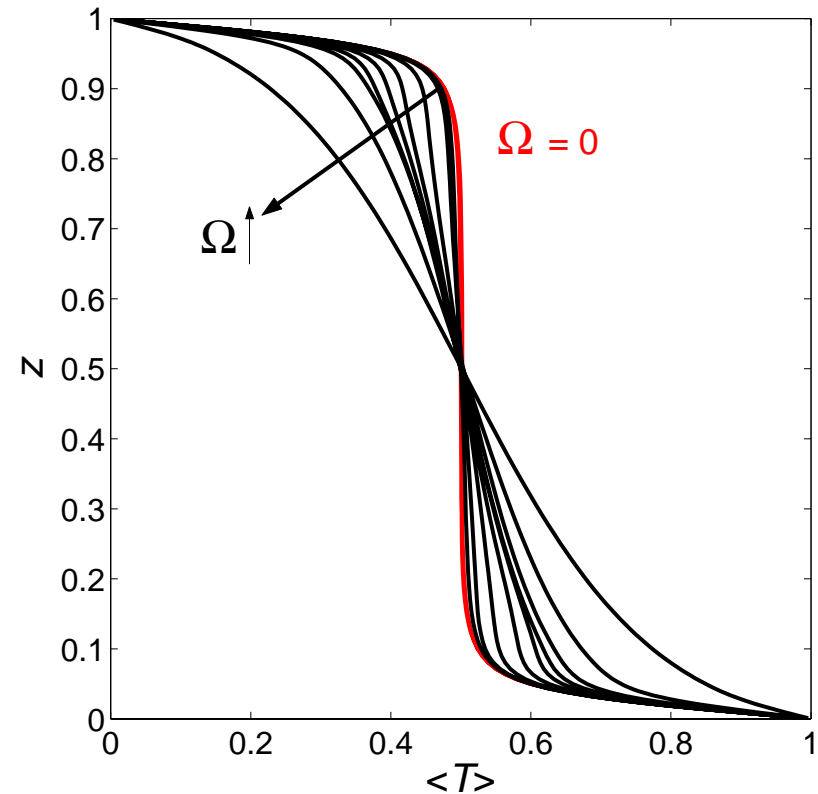
in geophysical flow settings



Rotational effects on convection

found in many statistical quantities using DNS:

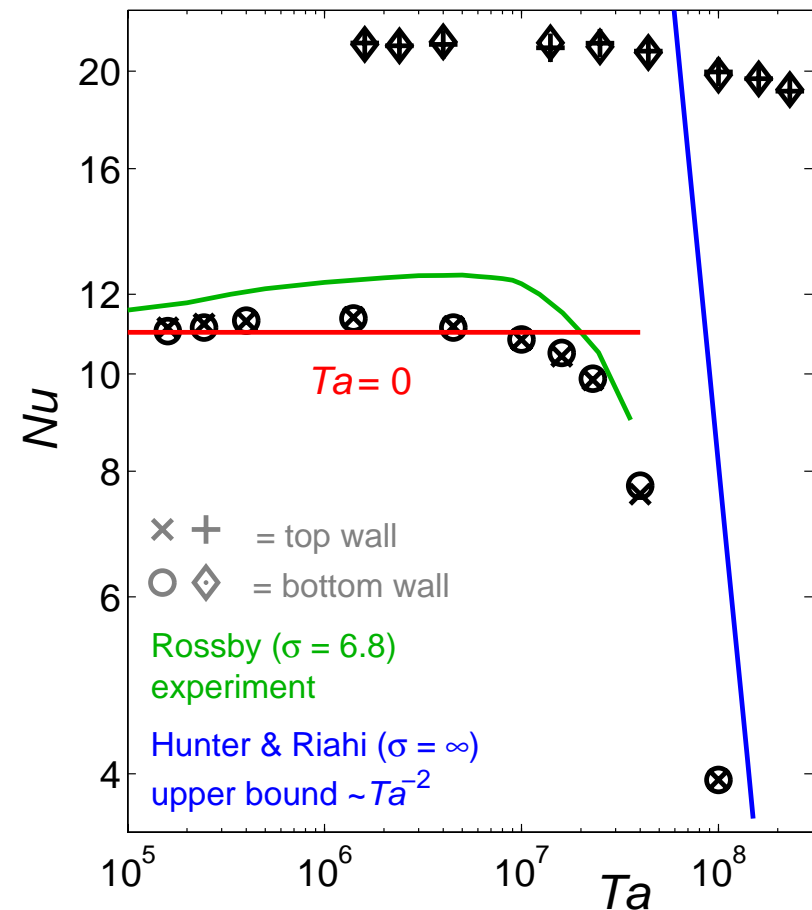
- Temperature gradient over bulk
- Changes in heat transfer
- Skewness of vertical velocity (flow structuring)
- Boundary layers



Rotational effects on convection

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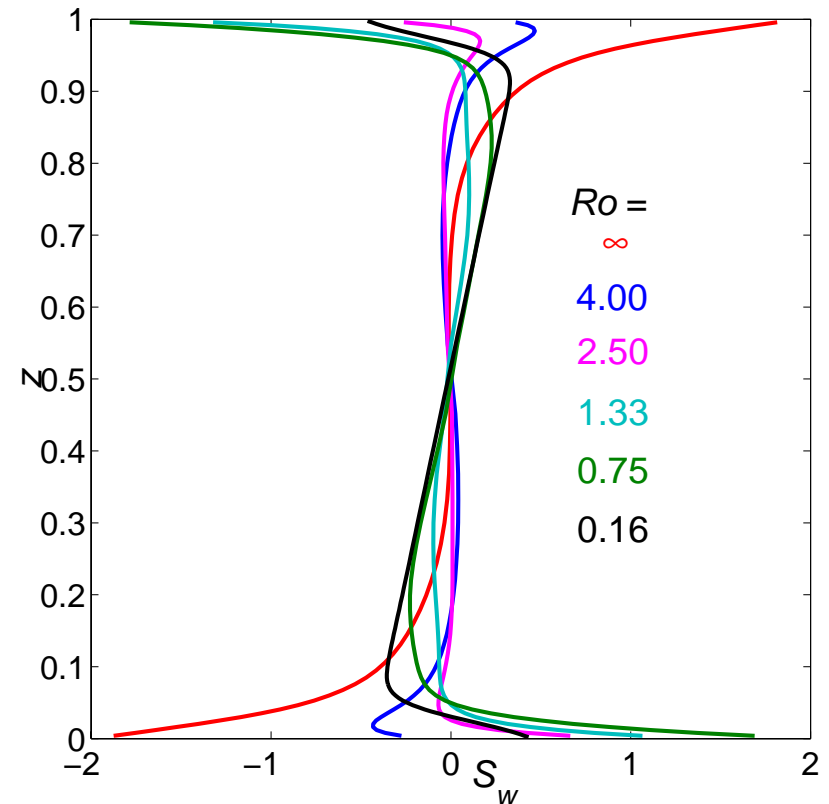
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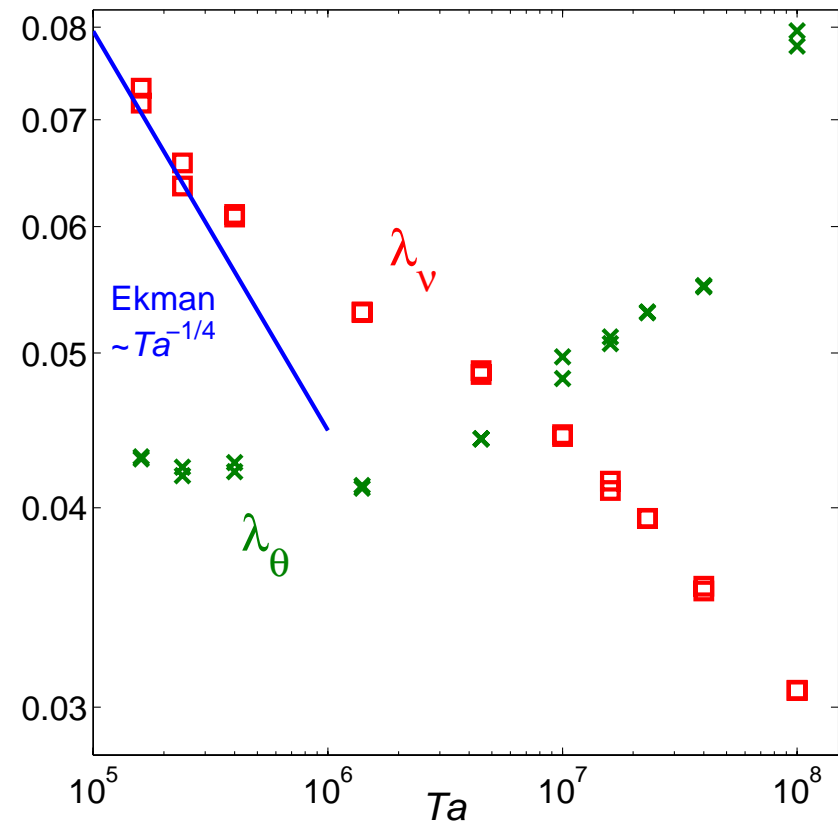
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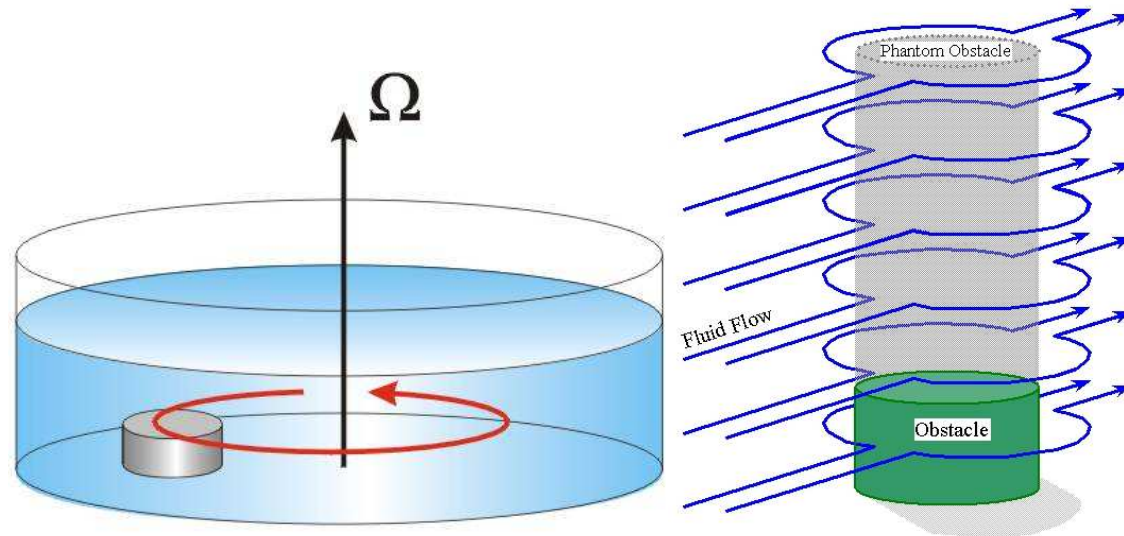


Influence of background rotation

Under geostrophic conditions no vertical variation of velocity

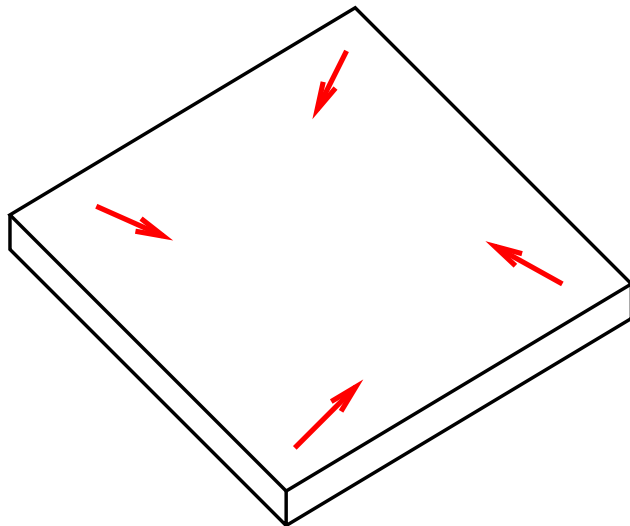


Taylor–Proudman theorem



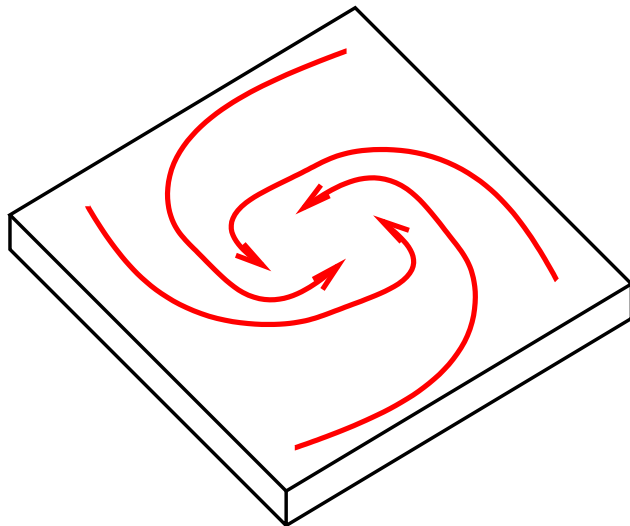
“Taylor column” above object dragged through rotating fluid

Thermal plumes under rotation



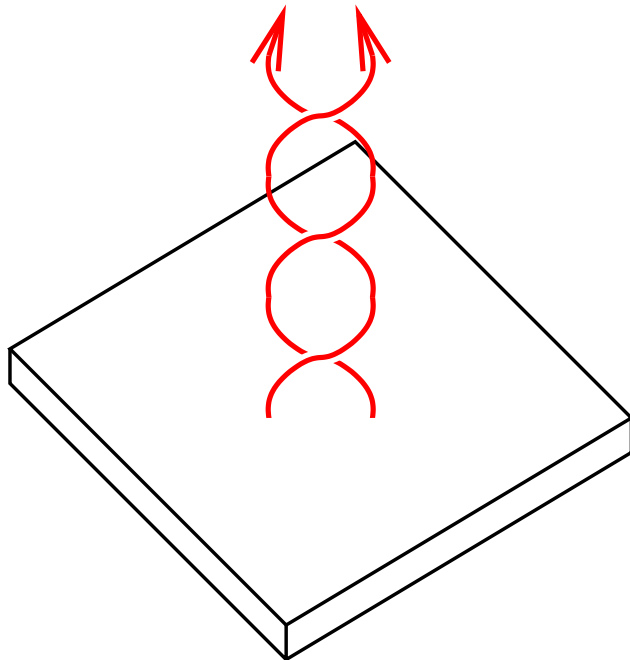
Thermal plumes spin up cyclonically → called **thermal vortices**

Thermal plumes under rotation



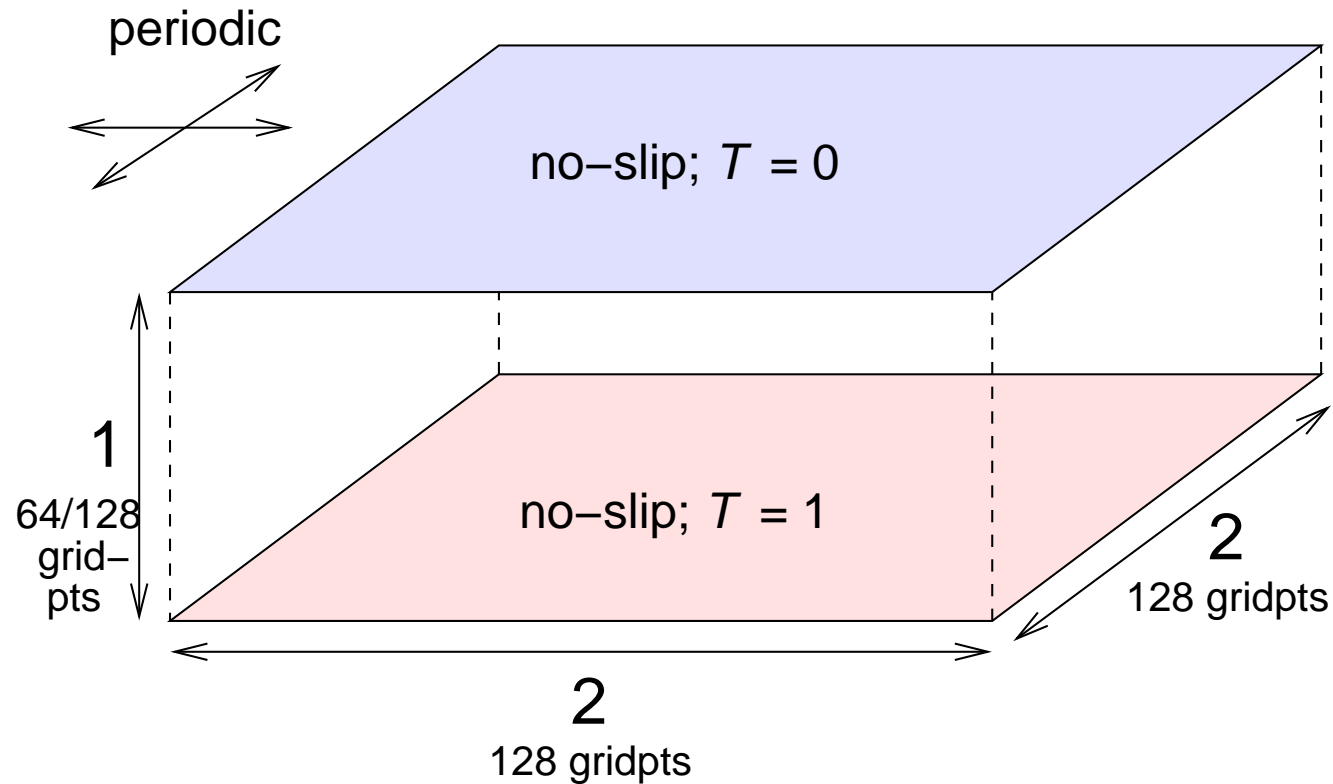
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Thermal plumes under rotation



Thermal plumes spin up cyclonically → called **thermal vortices**

DNS: Domain and boundary conditions



- Symmetry-preserving fourth-order finite-volume discretisation
- Details: Verstappen & Veldman *J. Comput. Phys.* **187** (2003) 343–368

DNS: equations

Navier–Stokes and heat equations in Boussinesq approximation with incompressibility:

$$\begin{aligned}\frac{D\mathbf{u}}{Dt} + \sqrt{\frac{\sigma Ta}{Ra}} \hat{\mathbf{z}} \times \mathbf{u} &= -\nabla p + T \hat{\mathbf{z}} + \sqrt{\frac{\sigma}{Ra}} \nabla^2 \mathbf{u} \\ \frac{DT}{Dt} &= \frac{1}{\sqrt{\sigma Ra}} \nabla^2 T \\ \nabla \cdot \mathbf{u} &= 0\end{aligned}$$

Extra control parameter: Taylor number $Ta = \left(\frac{2\Omega H^2}{\nu}\right)^2$

Buoyancy/Coriolis ratio: Rossby number $Ro = \sqrt{\frac{Ra}{\sigma Ta}}$

Simulation values

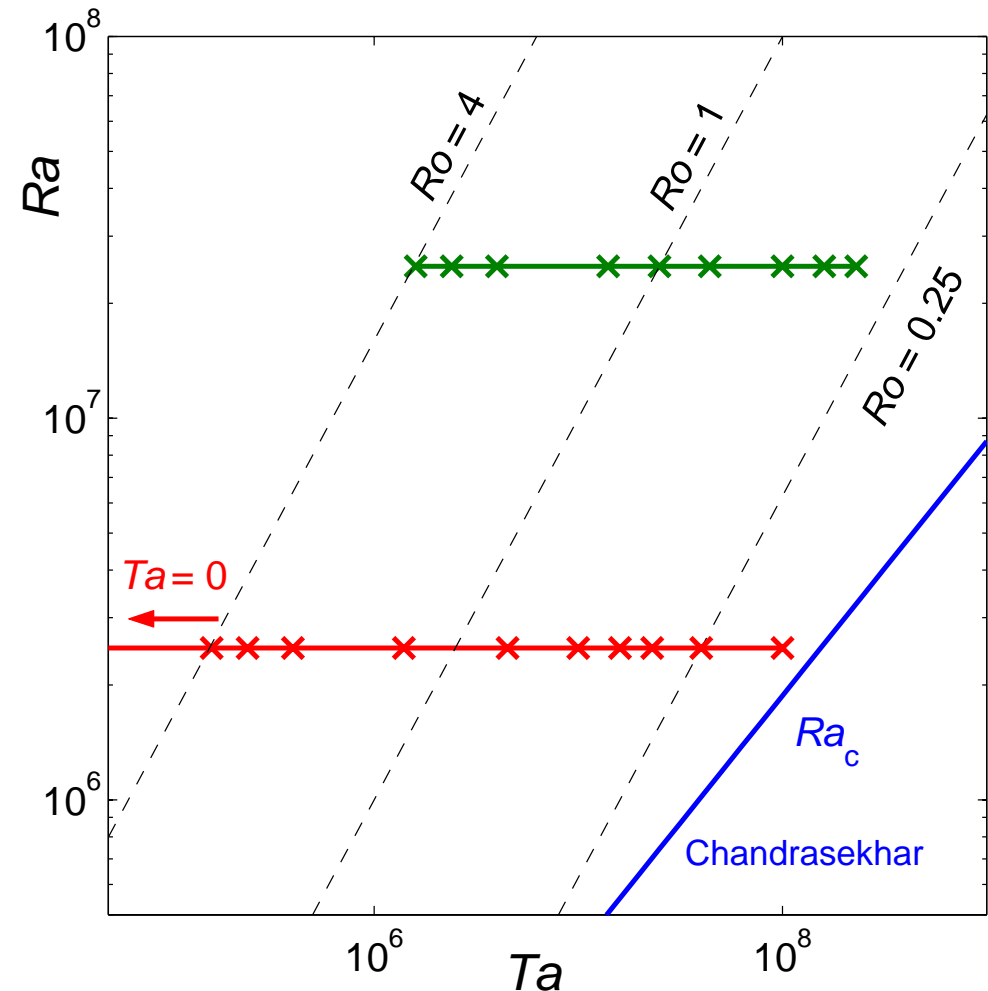
Two series: (both at $\sigma = 1$)

Red:

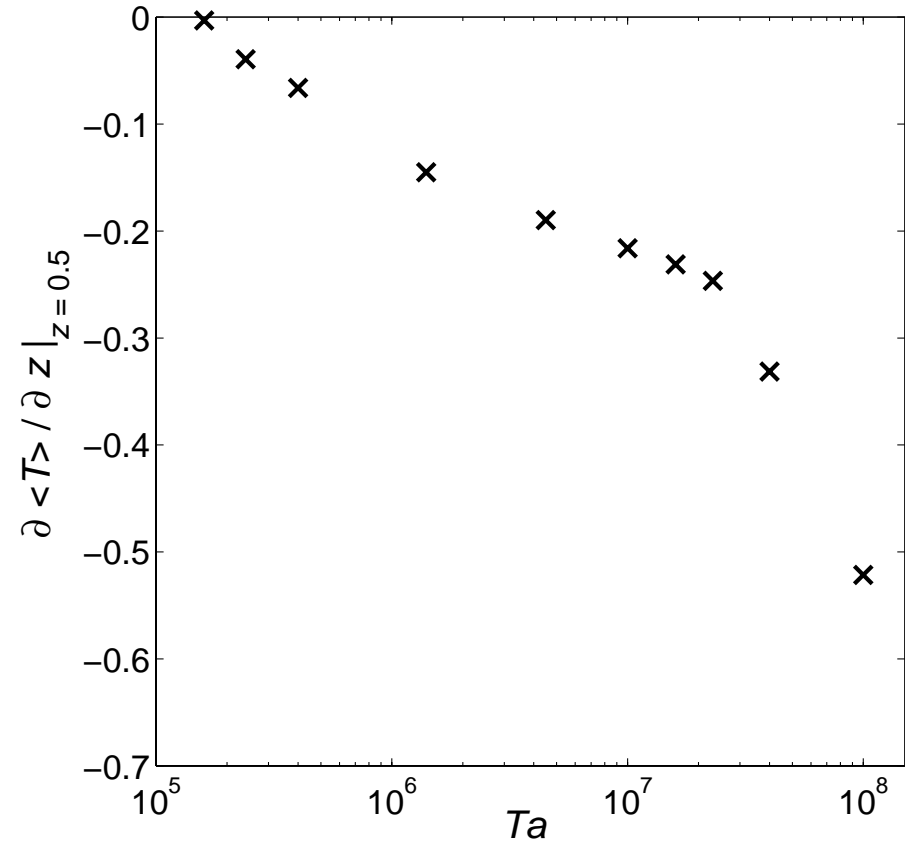
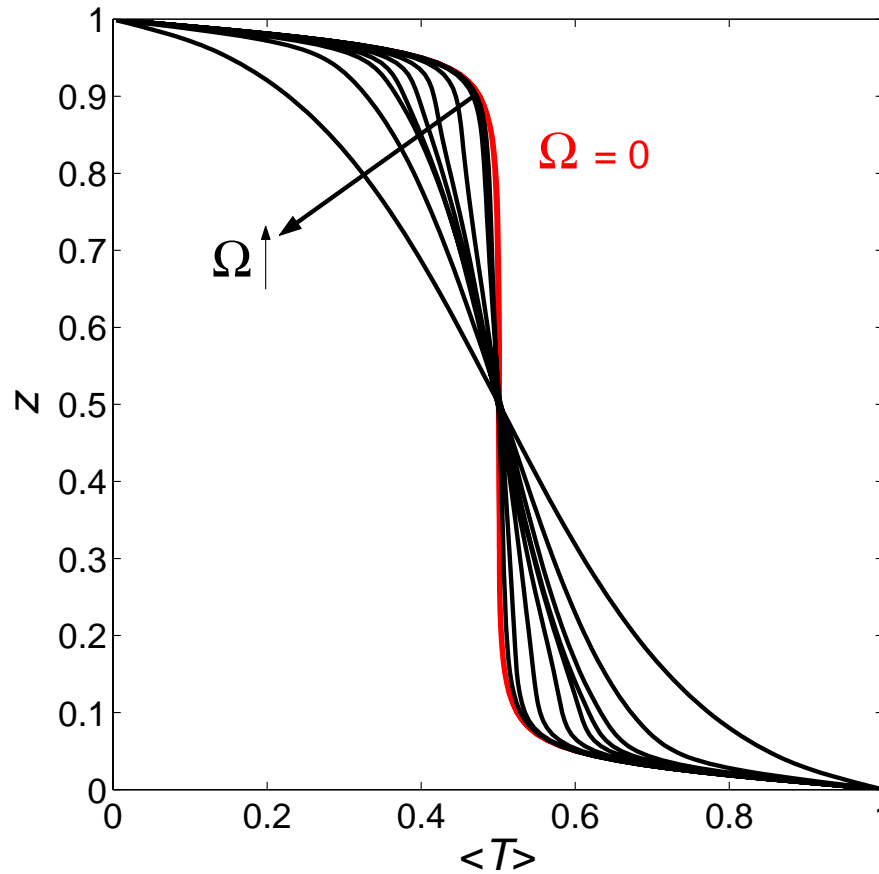
- $Ra = 2.5 \times 10^6$
- $Ta = 0 \dots 10^8$
- $Ro = \infty \dots 0.16$

Green:

- $Ra = 2.5 \times 10^7$
- $Ta = 1.6 \times 10^6 \dots 2.3 \times 10^8$
- $Ro = 4.00 \dots 0.33$



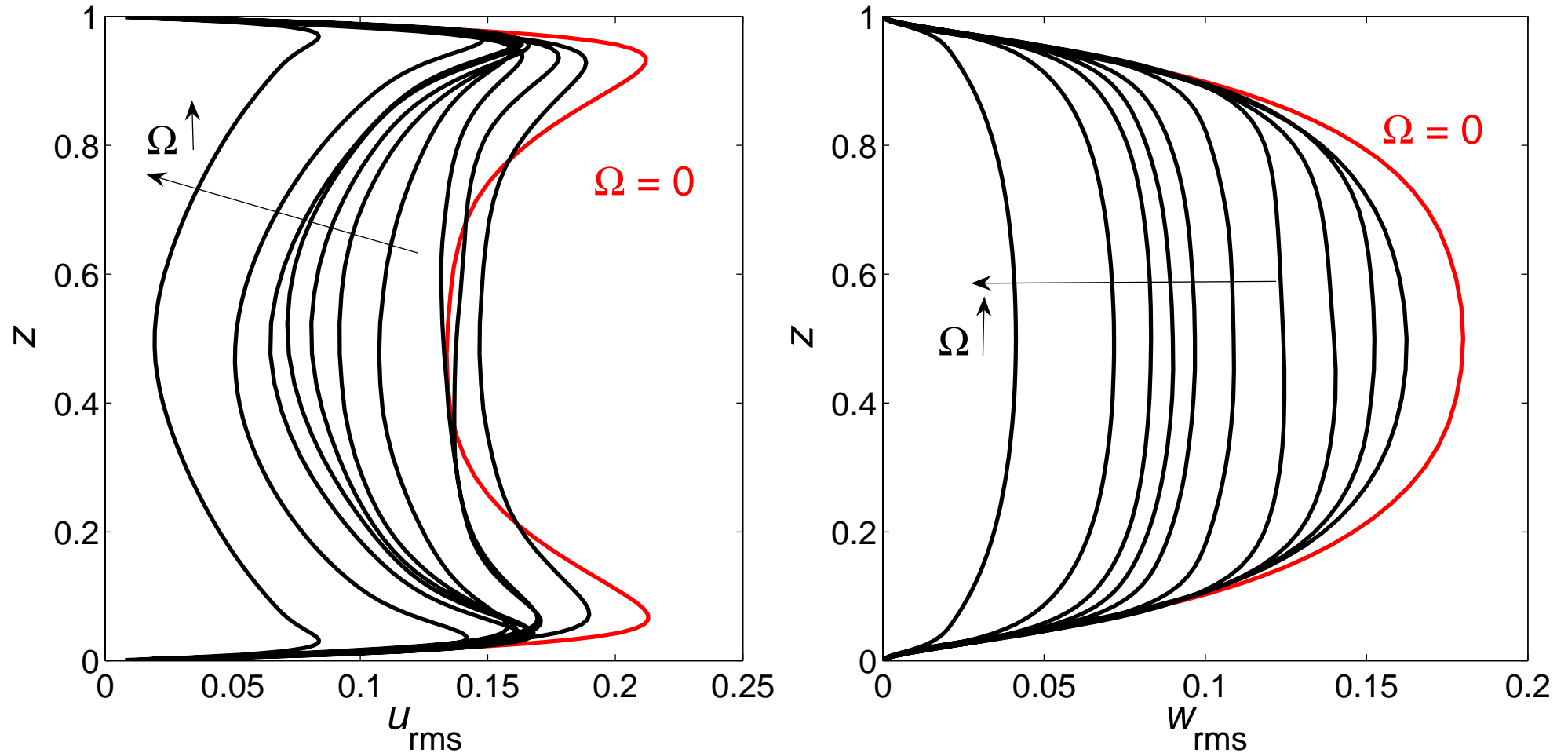
Average temperature and midplane gradient



$$Ra = 2.5 \times 10^6$$

Temperature gradient develops over bulk;
goes towards stable conductive state at high Ta

Horizontal and vertical rms velocities



Rotation lowers both horizontal
and vertical rms velocities

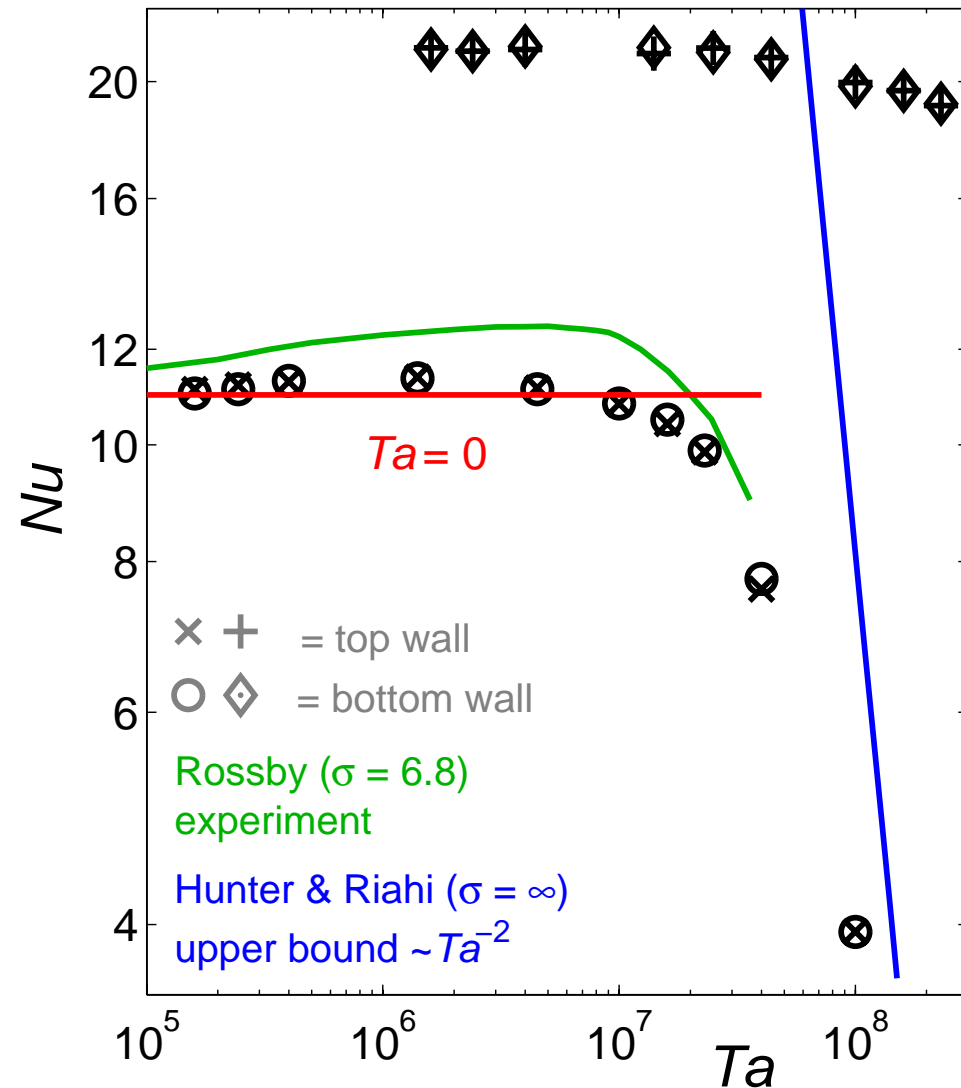
Heat transport — Nusselt number

$$Nu = \frac{\partial \langle T \rangle}{\partial z} \Big|_{\text{wall}}$$

\circ, \times $Ra = 2.5 \times 10^6$
 $\diamond, +$ $Ra = 2.5 \times 10^7$

Rossby *J. Fluid Mech.* **36** (1969)

Hunter & Riahi *J. Fluid Mech.* **72** (1975)

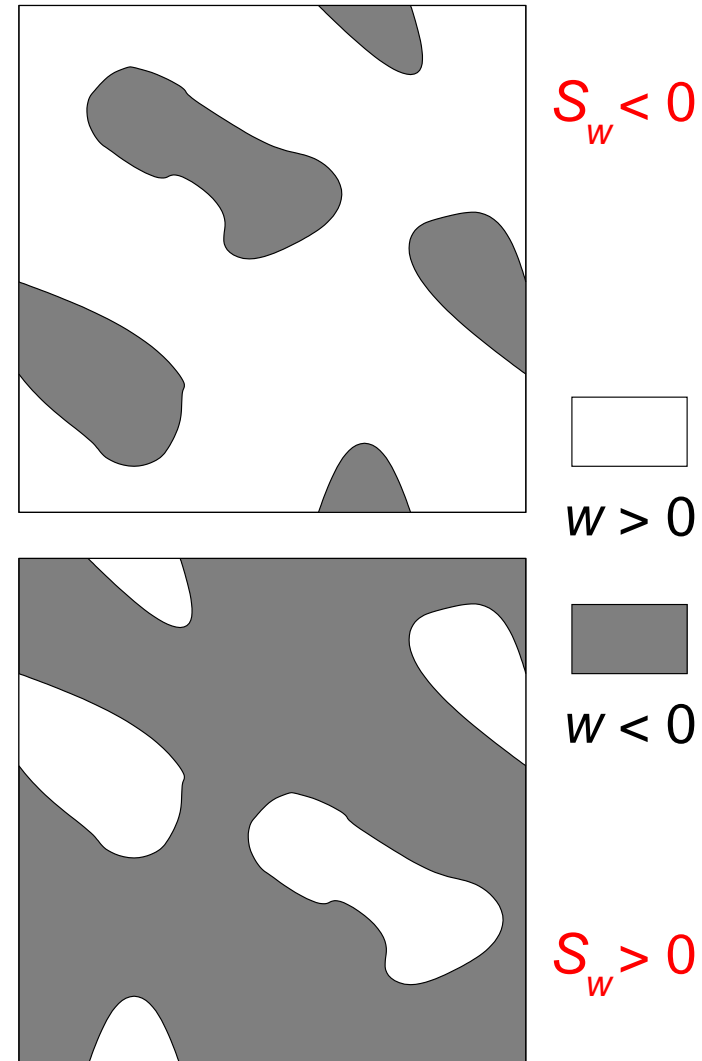


Vertical-velocity skewness

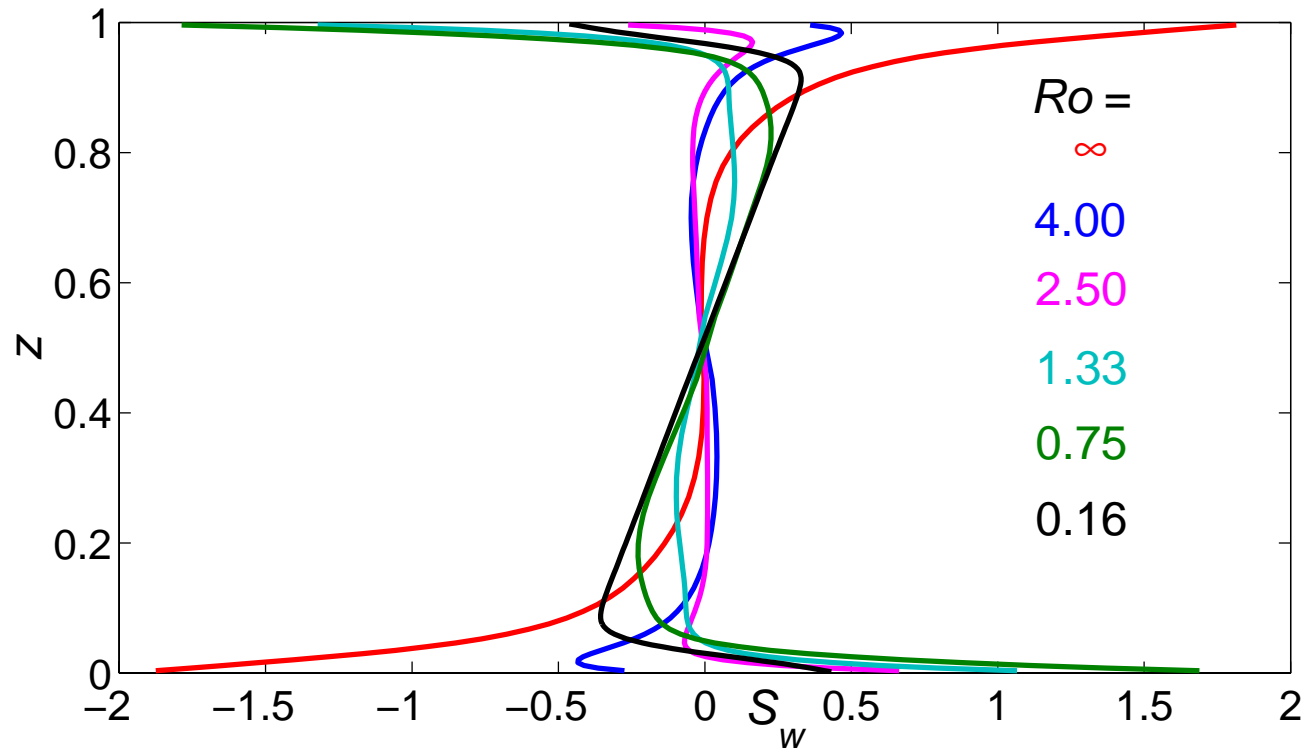
$$S_w = \frac{\langle (w - \langle w \rangle)^3 \rangle}{\langle (w - \langle w \rangle)^2 \rangle^{3/2}}$$

Indicates **area fraction** of horizontal cross-sections containing upward/downward motion.

$S_w > 0$: Fraction of cross-section containing upward motion **smaller** than fraction containing downward motion.



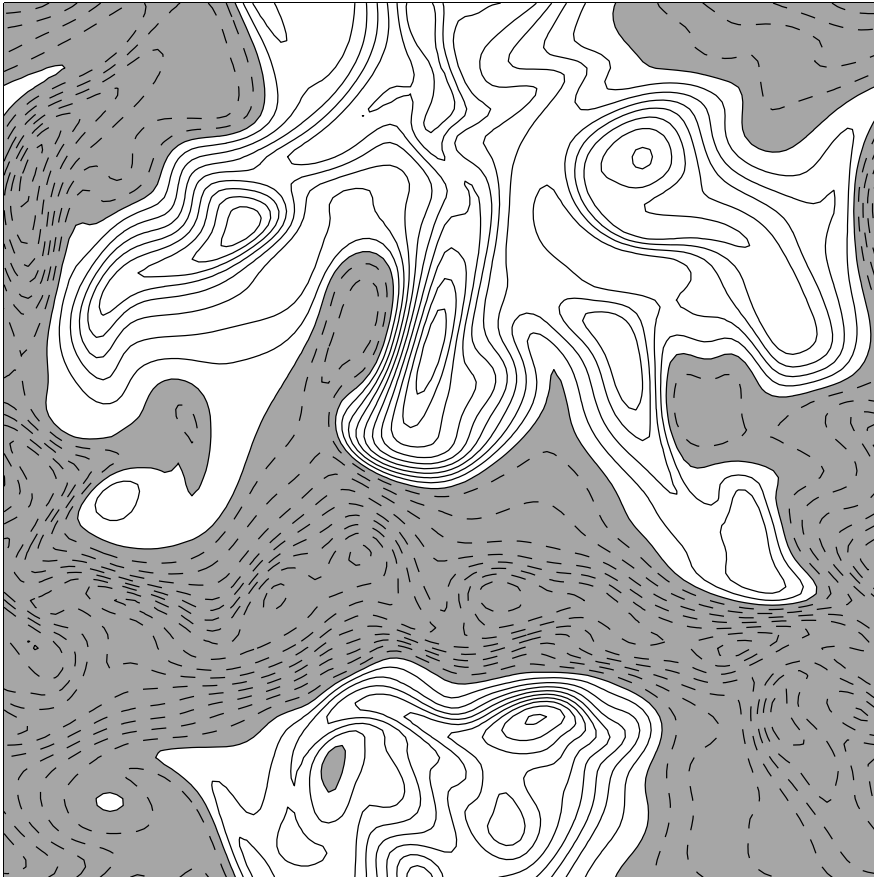
Vertical-velocity skewness for $Ra = 2.5 \times 10^6$



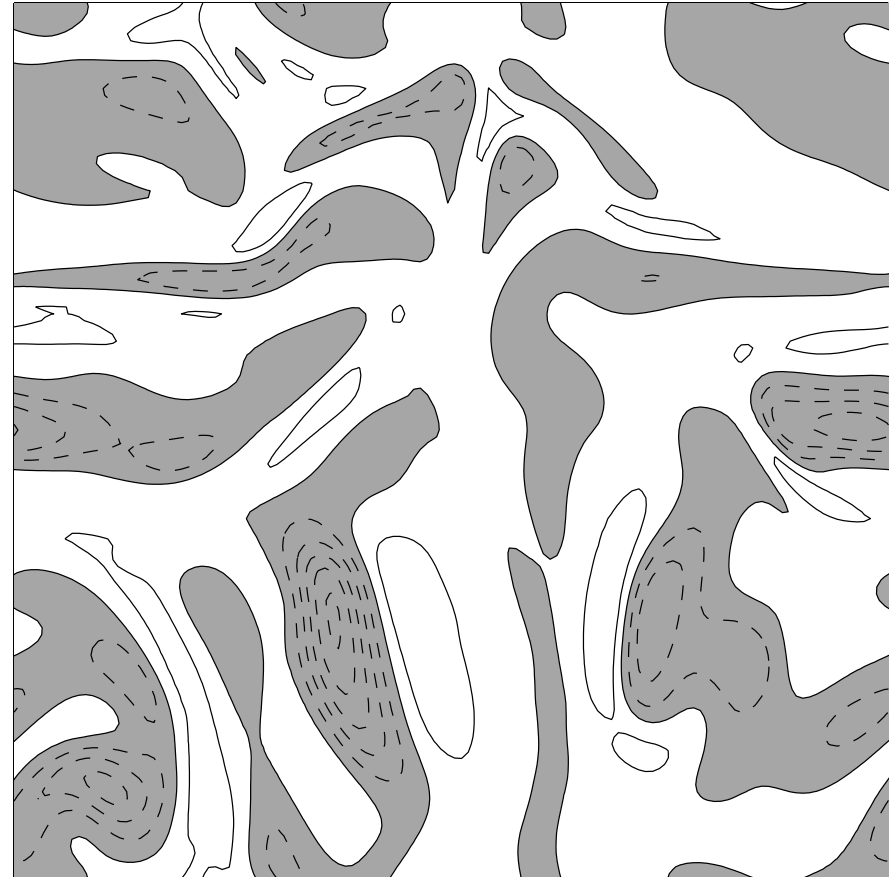
‘Switch’ of S_w near the walls points to different near-wall flow structure under rotation

No rotation ($Ro = \infty$)

Horizontal cross-sections, vertical-velocity contour plot



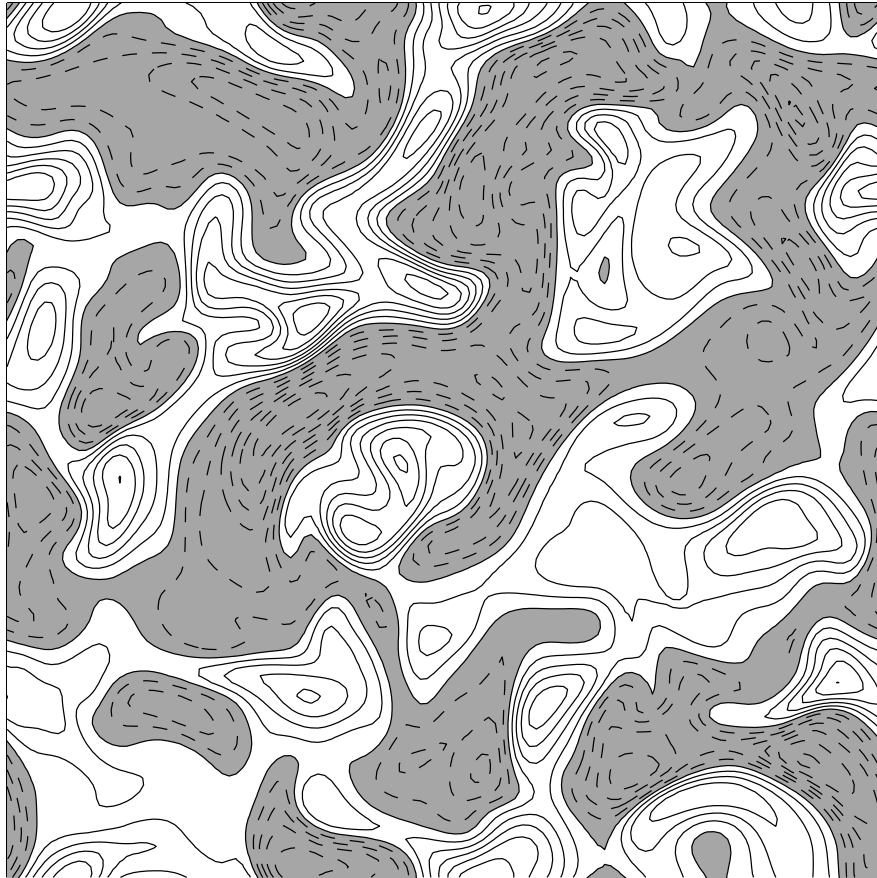
centre: $S_w = 0$



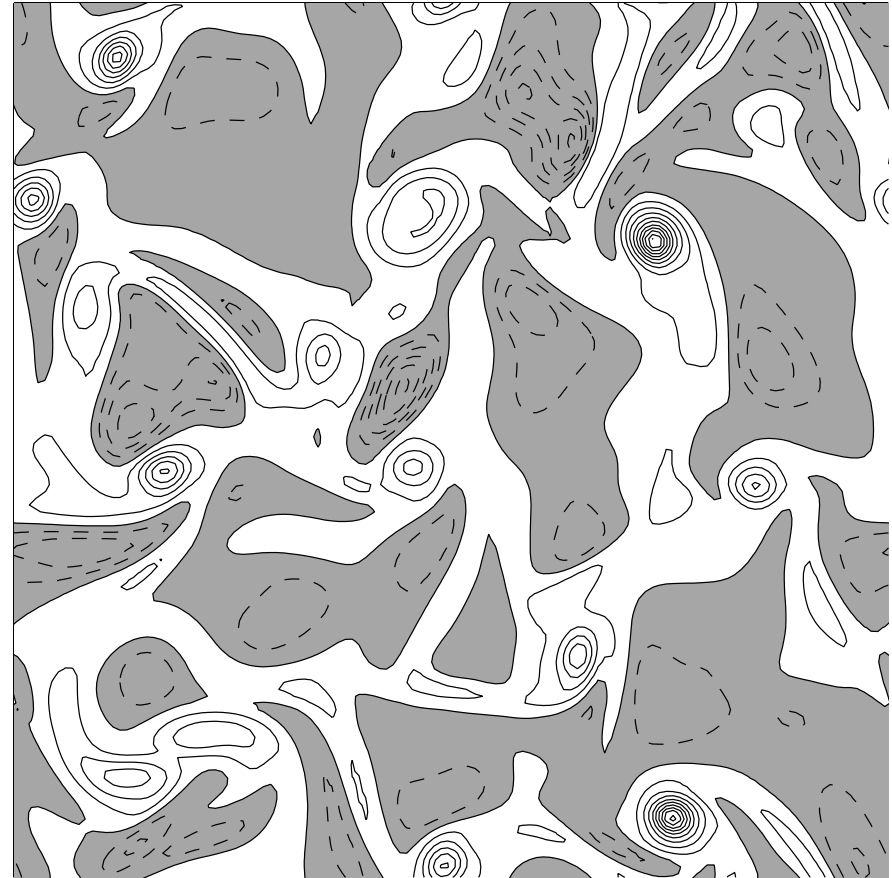
near-wall: $S_w = -1.5$

With rotation ($Ro = 0.75$)

Horizontal cross-sections, vertical-velocity contour plot



centre: $S_w = 0$



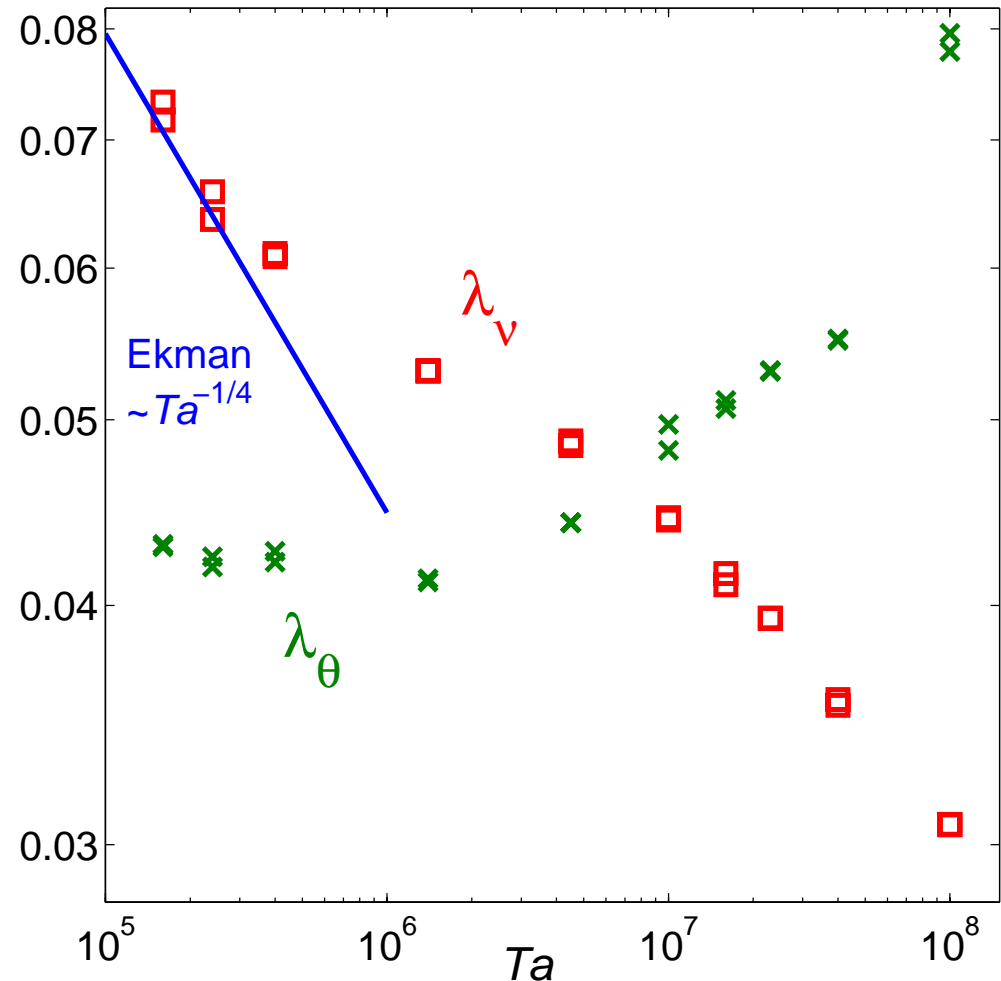
near-wall: $S_w = +0.5$

Boundary layer thicknesses ($Ra = 2.5 \times 10^6$)

λ_ν = viscous BL

λ_θ = thermal BL

BL thickness defined as height at which RMS value is largest



Conclusions

- Rotation alters flow structuring considerably → **vortical plumes**
- At moderate rotation rates heat flux is increased by **Ekman pumping**
- At high rotation rates heat flux decreases rapidly due to **geostrophic damping**
- Rotation stabilises flow → **temperature gradient over bulk**

Outlook

- Investigation of **vortex structures** and **relation with heat transfer**
- DNS on a **cylindrical domain**
→ effect of sidewall;
comparison with experiments
- Local velocity **measurements**
in a cylindrical
rotating-convection cell

