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> Supersymmetry at LHC Part III (Reconstructing SUSY)

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These are preliminary lecture notes, intended only for distribution to participants.

Reconstructing SUSY

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Recall Inclusive analysis



Will determine gluino/squark masses to $\sim 15\%$



Peak in $M_{\rm eff}$ distribution correlates well with SUSY mass scale



 $M_{\rm SUSY} = \min(M_{\widetilde{u}}, M_{\widetilde{g}})$

Use this and similar global distributions to establish that new physics exists and determine its mass scale

Method is slightly model dependent



Generalizations to other models

Similar method works in GMSB and MSSM In MSSM, 15 parameters were varied Events selected to have no isolated leptons, at least 4 jets, large missing E_T More global variables were used; best is

$$\sum_{jets} |E_T| \text{ or } \sum_{jets} |E_T| + \not\!\!\!E_T$$

Error is bigger in MSSM





Model	Var	$ar{x}$	σ	σ/\bar{x}	Prec. (%)
mSUGRA	1	1.585	0.049	0.031	2.9
	2	0.991	0.039	0.039	3.8
	3	1.700	0.043	0.026	2.1
	4	1.089	0.030	0.028	2.5
	5	1.168	0.029	0.025	2.1
MSSM	1	1.657	0.386	0.233	23.1
	2	0.998	0.214	0.215	21.1
	3	1.722	0.227	0.132	12.8
	4	1.092	0.143	0.131	12.8
	5	1.156	0.176	0.152	14.8
GMSB	1	1.660	0.149	0.090	8.1
	2	1.095	0.085	0.077	6.6
	3	1.832	0.176	0.096	9.0
	4	1.235	0.091	0.074	6.1
	5	1.273	0.109	0.086	7.9

 $\sigma(M_{susy} < 13\%)$

Not optimized

Leptonic channels not used

More work on "global signatures" needed



Characteristic SUSY Decays

Illustrate techniques by choosing examples from case studies.

Both \widetilde{q} and \widetilde{g} produced; one decays to the other

Weak gauginos ($\widetilde{\chi_i^0}, \widetilde{\chi_i^\pm}$) then produced in their decay. $e.g. \ \widetilde{q_L} \to \widetilde{\chi}_2^0 q_L$

Two generic features $\chi_2^0 \rightarrow \chi_1^0 h$ or $\chi_2^0 \rightarrow \chi_1^0 \ell^+ \ell^-$ possibly via intermediate slepton $\chi_2^0 \rightarrow \widetilde{\ell^+} \ell^- \rightarrow \chi_1^0 \ell^+ \ell^-$ Former tends to dominate if kinematically allowed.

Use these characteristic decays as a starting point for mass measurements

Many SUSY particles can then be identified by adding more jets/leptons



Decays to Higgs bosons

If $\chi_2^0 \to \chi_1^0 h$ exists then this final state followed by $h \to b\overline{b}$ results in discovery of Higgs at LHC. In these cases $\sim 20\%$ of SUSY events contain $h \to b\overline{b}$





Generally applicable



Over rest of parameter space, leptons are the key...



Starting with Leptons

Isolated leptons indicate presence of t, W, Z, weak gauginos or sleptons Key decays are $\tilde{\chi}_2 \to \tilde{\ell}^+ \ell^-$ and $\tilde{\chi}_2 \to \tilde{\chi}_1 \ell^+ \ell^-$

Mass of opposite sign same flavor leptons is constrained by decay





Decay via virtual slepton: $\widetilde{\chi}_2 \rightarrow \widetilde{\chi}_1 \ell^+ \ell^$ and Z from other SUSY particles



Building on Leptons

Decay
$$\widetilde{q_L} \to q \widetilde{\chi}_2^0 \to q \widetilde{\ell} \ell \to q \ell \ell \widetilde{\chi}_1^0$$

Identify and measure decay chain

- 2 isolated opposite sign leptons; $p_t > 10 \text{ GeV}$
- $\bullet \geq 4$ jets; one has $p_t > 100~GeV$, rest $p_t > 50~{
 m GeV}$
- $E_T > max(100, 0.2M_{eff})$

\tilde{q} $\tilde{\chi}_2$ e^+ \tilde{e} $\tilde{\chi}_1$ e^-

Mass of $q\ell\ell$ system has max at

$$M_{\ell\ell q}^{\max} = \left[\frac{(M_{\tilde{q}_L}^2 - M_{\tilde{\chi}_2^0}^2)(M_{\tilde{\chi}_2^0}^2 - M_{\tilde{\chi}_1^0}^2)}{M_{\tilde{\chi}_2^0}^2}\right]^{1/2} = 552.4 \,\text{GeV}$$

and min at 271 ${\rm GeV}$





smallest mass of possible $\ell \ell j e t$ combinations

Kinematic structure clearly seen Can also exploit ℓjet mass





Can now solve for the masses. Note that no model is needed

Very naive analysis has 4 constraints from $lq, llq_{upper}, llq_{lower}, ll$ masses 4 Unknowns, $m_{\tilde{q_L}}, m_{\tilde{e_R}}, m_{\tilde{\chi}^0_2}, m_{\tilde{\chi}^0_1}$



Errors are 3%, 9%, 6% and 12% respectively



Right squarks

s-tranverse mass. Definition



• Partition $\vec{E}_T = \vec{E}_{T,1} + \vec{E}_{T,2}$ in all possible ways and compute:

$$M_T^2 = \min_{\vec{k}_{\mathrm{T},1}, \vec{k}_{\mathrm{T},2}} \left[\max\{m_T^2(P_{T,j1}, \vec{k}_{\mathrm{T},1}, M_{\tilde{\chi}_1^0}), m_T^2(P_{T,j2}, \vec{k}_{\mathrm{T},2}, M_{\tilde{\chi}_1^0})\} \right]$$

• M_T^2 depends on the choice of $M(\tilde{\chi}_1^0)$



s-tranverse mass for the SU5 point

Fit the end-point with a straight line and extrapolate to the x-axis Use "true" value of $\mathsf{M}(\tilde{\chi}^0_1)$

(Ola Kristoff Oye)



Again Limited by LSP mass uncertainty





Final states with taus

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Large 	an \beta implies that m(\tilde{\tau}) < m(\tilde{\mu})
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Real signal visible above fakes (dashed) and SM (solid)

Can use peak position to infer end point in decay $\tilde{\chi}_2^0 \rightarrow \tau \tau \tilde{\chi}_1^0$ (61 GeV) Estimate 5% error

Large $\tan\beta \Rightarrow {\rm light\ sbottom\ - Look\ for\ these}$



$$\tilde{g} \to b\tilde{b} \to bb\tau^{\pm}\tau^{\mp}\tilde{\chi}_1^0$$

Previous sample with 2 b-jets having $p_t > 25$ GeV

Lots of missing E_T : tau decays and $\widetilde{\chi}_1^0$'s

Select $40 < m_{\tau\tau} < 60 \text{ GeV}$

Combine with b jets

Look at $\tau\tau bb$ and $\tau\tau b$: should approximate gluino and sbottom use partial reconstruction technique assuming mass of $\tilde{\chi}_1^0$

Peaks are low; should be expected due to missing energy



Plot of $m(\widetilde{\chi}_2^0 bb)$ vs $m(\widetilde{\chi}_2^0 bb) - m(\widetilde{\chi}_2^0 b)$



Projections





Gauge Mediated Model

Aims to solve FCNC problem by using gauge interactions instead of Gravity to transmit SUSY breaking

Messenger Sector consists of some particles (X) that have SM interactions and are aware of SUSY breaking.

 $M_i^2 = M^2 \pm F_A$ Simplest X is complete SU(5) 5 or 10 to preserve GUT

Fundamental SUSY breaking scale $F > F_A$, but $\sqrt{F} \lesssim 10^{10}$ GeV or SUGRA breaking will dominate Gaugino masses at 1-loop

 $M_{\widetilde{g}} \sim \alpha_s N_X \Lambda$

Squark and Slepton masses at 2-loop

 $M_{\widetilde{e}} \sim \alpha_W \sqrt{N_X} \Lambda$

True LSP is a (almost) massless Gravitino Sparticles decay as in SUGRA, then "NLSP" decays to \tilde{G} lifetime model dependent NLSP does not have to be neutral



6 parameters

 Λ , M, N_5 , $\tan\beta$,

 $sign\mu$

 $10 \text{ TeV} \lesssim \Lambda \equiv F_A/M \lesssim 400 \text{ TeV}$: Scale for SUSY masses.

 $M > \Lambda$: Messenger mass scale.

 $N_5 \ge 1$: Number of equivalent $5 + \overline{5}$ messenger fields.

 $1 \lesssim \tan \beta \lesssim m_t/m_b$: Usual ratio of Higgs VEV's.

 $\operatorname{sgn} \mu = \pm 1$: Usual sign of μ parameter.

 $C_{\text{grav}} \geq 1$: Ratio of $M_{\widetilde{G}}$ to value from F_A , controls lifetime of NLSP.

Point	Λ	M_m	N_5	aneta	$\operatorname{sgn}\mu$	$C_{\rm grav} \ge 1$	σ
	(TeV)	(TeV)				J.	(pb)
G1a	90	500	1	5.0	+	1.0	7.6
G1b	90	500	1	5.0	+	10^{3}	7.6
G2a	30	250	3	5.0	+	1.0	23
G2b	30	250	3	5.0	+	5×10^3	23



C	C1	60	0	<u>C1</u>	<u> </u>
Sparticle	G1	G2	Sparticle	G1	G2
$\widetilde{g}_{_{\perp}}$	747	713			
$\widetilde{\chi}_1^{\pm}$	223	201	$\widetilde{\chi}_2^{\pm}$	469	346
$\widetilde{\chi}_1^0$	119	116	$\widetilde{\chi}_2^0$	224	204
$\widetilde{\chi}_3^0$	451	305	$\widetilde{\chi}_4^0$	470	348
\widetilde{u}_L°	986	672	\widetilde{u}_R	942	649
${\widetilde d}_L$	989	676	\widetilde{d}_R	939	648
\widetilde{t}_1	846	584	\widetilde{t}_2	962	684
\tilde{b}_1	935	643	\widetilde{b}_2	945	652
\widetilde{e}_L	326	204	\widetilde{e}_R	164	103
$\widetilde{ u}_{e}$	317	189	$\widetilde{ au}_2$	326	204
$\widetilde{ au}_{1}$	163	102	$\widetilde{ u}_{\mathcal{T}}$	316	189
h^0	110	107	H^0	557	360
A^0	555	358	H^{\pm}	562	367

Mass spectrum more spread out than in SUGRA m(squark)/m(slepton) bigger



New signals in GMSB

Lightest superpartner is unstable and decays to Gravitino (\tilde{G}) Either neutral

 $\chi_1^0 \to \gamma \tilde{G} : c\tau \sim C^2 (100 \text{ GeV}/M_{\chi_1^0})^5 (\Lambda/180 \text{TeV})^2 (M_M/180 \text{TeV})^2 \text{mm}$ $\Rightarrow \text{ over a photons or similar signals to SUCRA depending on lifetime.}$

 \Rightarrow extra photons or similar signals to SUGRA depending on lifetime

Or charged

Almost always slepton: $\tilde{e_R} \rightarrow e\tilde{G}$

No Missing E_T if $c\tau$ large, events have a pair of massive stable charged particles ("G2b")

Large lepton multiplicity if $c\tau$ small ("G2a").

Discovery and measurement in these cases is trivial

In case "G2b", every decay product can be measured

In case "G1a" \tilde{G} momenta can be inferred and events fully reconstructed.



GMSB case 1a: Event selection (not optimized) Decay $\widetilde{\chi}_2^0 \rightarrow \ell^+ \ell^- \widetilde{\chi}_1^0 \rightarrow \ell^+ \ell^- \gamma \tilde{G}$ is key Lifetime of $\widetilde{\chi}_1^0$ is short

Find jets

Require

$$\widetilde{\chi}_2^0 \to \widetilde{\ell}^{\pm} \ell^{\mp} \to \widetilde{\chi}_1^0 \ell^{\pm} \ell^{\mp} \to \widetilde{G} \gamma \ell^{\pm} \ell^{\mp} \,,$$

Electrons and photons : $p_T > 20 \text{ GeV}$ Muons : $p_T > 5 \text{ GeV}$. Require at least 2 photons and two leptons.



Dilepton mass distribution, flavor subtracted $e^+e^- + \mu^+\mu^- - e^\pm\mu^\mp$



End is at

$$M_{\tilde{\chi}_2^0} \sqrt{1 - \left(\frac{M_{\tilde{\ell}_R}}{M_{\tilde{\chi}_2^0}}\right)^2} \sqrt{1 - \left(\frac{M_{\tilde{\chi}_1^0}}{M_{\tilde{\ell}_R}}\right)^2} = 105.1 \,\text{GeV}$$





Form $\ell^+\ell^-\gamma$ mass and take smallest combination. Linear vanishing at

$$\sqrt{M_{\widetilde{\chi}^0_2}^2 - M_{\chi^0_1}^2} = 189.7 \,\mathrm{GeV}\,,$$





Form $\ell^{\pm}\gamma$ mass also. Two structures at

$$\sqrt{M_{\tilde{\ell}_R}^2 - M_{\chi_1^0}^2} = 112.7 \,\mathrm{GeV}$$

 $\quad \text{and} \quad$

$$\sqrt{M_{\chi_2^0}^2 - M_{\tilde{\ell}_R}^2} = 152.6 \,\mathrm{GeV}$$



These four measurements are sufficient to determine the masses of the particles $(\tilde{\chi}_2^0, \tilde{\ell}_R, \text{ and } \tilde{\chi}_1^0)$ in this decay chain without assuming any model of SUSY breaking.

Now use this to reconstruct the decay chain and measure the \tilde{G} momenta despite the fact that there are two in each event and both are invisible!



Full reconstruction of SUSY events



Know masses \Rightarrow can calculate p assuming $p^2 = 0$:

$$\begin{array}{rcl} 2p_0k_0 - 2\vec{p}\cdot\vec{k} &=& M_{\widetilde{\chi}_1^0}^2 \\ \\ 2p_0l_0 - 2\vec{p}\cdot\vec{l} &=& M_{\widetilde{\ell}_R}^2 - M_{\widetilde{\chi}_1^0}^2 - 2k\cdot l \\ \\ 2p_0k_0 - 2\vec{p}\cdot\vec{q} &=& M_{\widetilde{\chi}_2^0}^2 - M_{\widetilde{\ell}_R}^2 - 2(k+l)\cdot q \end{array}$$

0C fit with 2×2 solutions.

Event has two of these decays so require 4 leptons and 2 gammas



Calculate missing E_T Form a χ^2 using measured missing E_T to resolve ambiguities

use $\Delta \not\!\!E_x = \Delta \not\!\!E_x = 0.6 \sqrt{E_T} + 0.03 E_T$.





Squark and Gluino Masses

Use measured $\tilde{\chi}_2^0$ momenta and combine with jets $\tilde{q} \rightarrow \tilde{g}q \rightarrow \tilde{\chi}_2^0 \overline{q}qq$ Require at least 4 jets with $p_T > 75 \,\text{GeV}$



Figure shows mass of $\tilde{\chi}_2^0+2$ jets; peak is below gluino mass (747 GeV); no correction applied for small jet cone.

Much easier than the SUGRA cases; masses measured directly



Measuring the fundamental scale of SUSY breaking

Lifetime of $\widetilde{\chi}^0_1 \to \widetilde{G}$ is important as it measures the fundamental scale of SUSY breaking Measure lifetime of $\chi_1^0 (\to \widetilde{G}\gamma)$ using Dalitz decay $\chi_1^0 \to e^+ e^- \gamma \widetilde{G}$ Works for short lived $\widetilde{\chi}_1^0$ Statistics limited (~few-K events) Measure lifetime of $\chi_1^0 (\to \widetilde{G}\gamma)$: photon pointing. Angular resolution of photons from primary vertex (ATLAS) $\Delta \theta \sim 60 mr/\sqrt{E}$ Detailed study of efficiency for non-pointing photons Important for long lived $\widetilde{\chi}_1^0$ Decays are uniformly distributed in the detector Cross check from time delay of decay Failure to see photons $\Rightarrow c au > 100$ km or $\sqrt{F} > 10^4$ TeV



Mass measurement of quasi-stable sleptons – ATLAS

Sleptons are produced at the end of decay chains \Rightarrow large velocity Most of these will pass the Muon Trigger Measure the velocity using TOF in Muon system, then infer mass Time resolution ~ 65 ns

 $\Rightarrow \Delta M/M \sim 3\%$ for $M=100~{\rm GeV}$





R-parity broken

Implies either Lepton number or Baryon number is violated and LSP decays Either $\tilde{\chi}_1^0 \rightarrow qqq$, or $\tilde{\chi}_1^0 \rightarrow q\bar{q}\ell$ or $\tilde{\chi}_1^0 \rightarrow \ell^+\ell^-\nu$ First two have no $\not\!\!E_T$, last 2 have more leptons and are straightforward First case is hardest, Global S/B is worse due to less $\not\!\!E_T$ Example, SUGRA with $\tilde{\chi}_1^0 \rightarrow qqq$ Leptons are essential to get rid of QCD background ≥ 8 jets with $p_t > 50$ GeV 2 OSSF isolated leptons. $S_T > 0.2$, selects "ball like" events $\Sigma_{jets+leptons}E_T > 1$ TeV





As nothing is lost, should be possible to reconstruct $\widetilde{\chi}_1^0$

Difficult because jet multiplicity is very high and $\widetilde{\chi}^0_1$ mass is usually small, so jets are soft





Nominal mass 122 GeV



Can cut around peak and combine with either leptons or quarks



Plot shows $\tilde{\chi}_2^0$ Note that tight cuts imply low event rate (analysis not optimized)







Explicit flavor violation is also possible

Neutrino oscillations imply lepton number is violated Atmospheric muon neutrino deficit implies $\nu_{mu} \leftrightarrow \nu_{\tau}$ with maximal mixing In a SUSY model, expect significant flavor violation in slepton sector Simplest model of lepton number violation involves addition of right handed neutrino N with SUSY conserving Majorana mass mNN and coupling to lepton left doublet and Higgs of the form LNHIncluding only $\mu \leftrightarrow \tau$ mixing gives

$$M_{\widetilde{\ell}\widetilde{\ell}}^{2} = \begin{bmatrix} M_{L}^{2} + D_{L} & 0 & 0 & 0 & 0 & 0 \\ 0 & M_{L}^{2} + D_{L} & M_{\mu\tau}^{2} & 0 & 0 & 0 \\ 0 & M_{\mu\tau}^{2} & M_{\tau_{L}}^{2} + D_{L} & 0 & 0 & m_{\tau}\bar{A}_{\tau} \\ 0 & 0 & 0 & M_{R}^{2} + D_{R} & 0 & 0 \\ 0 & 0 & 0 & 0 & M_{R}^{2} + D_{R} & 0 \\ 0 & 0 & m_{\tau}\bar{A}_{\tau} & 0 & 0 & M_{\tau_{R}}^{2} + D_{R} \end{bmatrix}$$

Atmospheric neutrinos suggest maximal mixing *i.e.* $\delta = O(1)$



Two types of flavor violation production ($\tilde{\chi}_2^0 \to \tilde{\tau} \mu$) and decay ($\tilde{\tau} \to \tilde{\chi}_1^0 \mu$).



Signal for lepton number violation comes by comparing $\mu \tau_h$ and $e \tau_h$ final states





 $\ell^{\pm}\tau_{h}^{\mp}$ signal (red), $\ell^{\pm}\tau_{h}^{\pm}$ signal (blue), $\mu^{\pm}\tau_{h}^{\mp}$ from LFV decays with BR = 10%(magenta), and Standard Model $\ell^{\pm}\tau_{h}^{\mp}$

Lepton number violating decay $\widetilde{\chi}_2^0 \to \mu \tau_h \widetilde{\chi}_1^0$ give harder $\mu \tau$ mass distribution than that from $\widetilde{\chi}_2^0 \to \tau \tau \widetilde{\chi}_1^0 \to \mu \tau_h \widetilde{\chi}_1^0$



Subtraction removes background



 $\ell^{\pm}\tau_{h}^{\mp} - \ell^{\pm}\tau_{h}^{\pm}$ (red) and $\mu^{\pm}\tau_{h}^{\mp}$ from LFV decays with BR = 10% (magenta) Signal is established from $E = N(\mu^{\pm}\tau_{h}^{\mp}) - N(e^{\pm}\tau_{h}^{\mp})$ $N(e^{\pm}\tau_{h}^{\mp})$ 10 fb⁻¹ and 5σ implies BR=2.3% or $\delta \sim$ 0.1 well within value needed for neutrino data

Sensitive provided that $\tilde{\chi}_2^0$ production is large enough (large fraction of parameter space More sensitive than $\mu \to e\gamma$



Odd Ball: R-hadron (split susy)

Long lived or quasi stable gluino produces "cannon ball" that charge exchanges as it PYTHIA R-hadron event from ATLSIM



passes through detector



Spin measurements at LHC?

Conventional wisdom says that you need LC for this but...



Angle between q and e^- in $\tilde{\chi}_2^0$ rest frame is sensitive to spin correlations. But effect washes out if we do not know which lepton comes out first: Use kinematics But effect washes out if average over q and \overline{q} : LHC is a pp machine: more \tilde{q} than $\tilde{\overline{q}}$



Form an asymmetry from invariant mass distribution of lepton and jet

$$A = \frac{(l^+q) - (l^-q)}{(l^+q) + (l^-q)}$$

Green:spin correlation off Yellow: No detector ($\times 0.6$) Needs at least 100fb^{-1}







Difficult cases I: Small mass gaps

Co-annihilation region: Near degeneracy between LSP and sleptons.Soft leptons and more messy decays. $\tilde{q_L} \to q \tilde{\chi}_2^0$ then $\tilde{\chi}_2^0(260) \to \tilde{\ell}_R(153)\ell \to \ell \ell \tilde{\chi}_1^0(136)$ and $\tilde{\chi}_2^0 \to \tilde{\ell}_L(255)\ell \to \ell \ell \tilde{\chi}_1^0(136)$

200 <u> אן אן אן אן אויאס אן אויאס אן אויאס א</u> 150 100 Leptons can still be found despite small mass gaps 50 50 100 150 200 0 M_{II} (GeV) **ATLAS** An era is about to end



Low energy SUSY has provided employment for > 20 years It will be discovered or die in the next 6 years.

