



**The Abdus Salam
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**Workshop on Understanding and Evaluating Radioanalytical
Measurement Uncertainty**

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Estimation of Uncertainty arising from Sampling - Exercise

Paolo de ZORZI and Sabrina BARBIZZI
*APAT - Agenzia per la Protezione dell'Ambiente e per Servizi Tecnici
Servizio Metrologia Ambientale
Via Castel Romano 100
00128 Roma
ITALY*

Uncertainty arising from sampling Exercises

Sabrina Barbizzi & Paolo de Zorzi

Workshop on "Understanding and Evaluating Radioanalytical Measurement Uncertainty"

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Contents

Two exercises:

1. Empirical method (Duplicate)
2. Modelling method (Gy's Fundamental Error)



Exercise 1

Empirical method-Duplicate

- A soil area was investigated in order to know the content of some trace element (As, Cr, Sc)
- 100 samples (**S1**) were collected by a stratified random strategy (100 sampling targets 10x10 m);
- Each sample was collected in duplicate (**S2**);
- The duplicates were analysed in duplicate (**A1 and A2**)



Exercise 1

Measurand				Uncertainty estimation		
Analyte and technique	Unit	Matrix	Sampling target	Purpose	Design	Statistics
As, Cr, Sc INAA	mg kg ⁻¹	Soil	Cell 10x10 m	<ul style="list-style-type: none">▪ Measurement uncertainty▪ Specific contribution from sampling and analysis	Empirical Duplicate Method	Robust ANOVA



Exercise 1

- Estimate for each and elements:
 - *Measurement uncertainty;*
 - *Sampling and analysis uncertainties;*
 - *The dominant component of uncertainty*

- Report the measurement result for a sampling target with the associated measurement uncertainty



Exercise 1

- Data:

- [DATA BASE_2.xls](#)

- Calculation

- [ROBAN ver. 1.01](#)

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Exercise 1

ROBUST ANOVA RESULTS:

Mean = 231,47298 mg/kg

Standard Deviation (Total) = 15,90858 mg/kg

	Geochemical -----	Sampling -----	Analysis -----	Measurement -----
Standard Deviation	7,7554994	11,738699	7,4255023	13,890109
Percentage Variance	23,766035	54,447398	21,78657	76,233965
Relative Uncertainty (% at 95% confidence)	-	10,142609	6,4158697	12,001495



Exercise 2

Modelling approach

Gy's Fundamental Error

- Particulate material has to be analysed for Pb content (contamination)
- The primary sample is taken from a very large lot
- The study design objectives require:
 - an analysis using a maximum **test portion** of **5 g**;
 - Maximum sampling fundamental error of **8 %**
($S^2_{FE} = 6,4 \times 10^{-3}$) of the mean Pb mass fraction
- Different sub-sampling and comminution steps are performed
- Analytical uncertainty equals to **5%** of the mean Pb mass fraction



Exercise 2

Measurand				Uncertainty estimation		
Analyte and technique	Unit	Matrix	Sampling target	Purpose	Design	Statistics
Pb ICP-OES	mg kg ⁻¹	Soil	Primary sample	Sampling Fundamental Error	Modelling Gy's theory	Propagation of error



Exercise 2

- Estimate :
 - *Contribution of each sampling step to the whole Sampling Fundamental Error;*
 - *Sampling Fundamental Error ;*
 - *The dominant contribution*

- Is the sampling procedure fit-for-purpose ?



Exercise 2

- Data:
 - Template Gy



Exercise 2 - comment

- The dominant contribution to the Fundamental sampling error is attributed to:
- [Template Gy_solved.xls](#)

