



**The Abdus Salam
International Centre for Theoretical Physics**



1833-41

**Workshop on Understanding and Evaluating Radioanalytical
Measurement Uncertainty**

5 - 16 November 2007

In-situ-gamma Spectrometry

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IN SITU GAMMA RAY-SPECTROMETRY



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*Atoms for Peace: The First Half Century
1957-2007*

IN SITU GAMMA RAY-SPECTROMETRY



Applications

- Rapid identification and determination of gamma emitting radionuclides in the environment (in the field)
 - activity concentration (Bqkg^{-1}) or
 - deposition (Bqm^{-2})
 - activity concentration (Bqkg^{-1})
- Indoor radiation studies
 - Analysis of power reactor plumes

NOTE: Spatial distribution of the radionuclide(s) of interest (source geometry) has to be taken into account.

Directly measureable natural radionuclides

Nuclide	E (keV)	Intensity I_r	Comments
Be-7	477.60	10.44%	Spallation product Continuous deposition at varying rate
K-40	1460.83	10.67%	
Pb-210	46.54	4.24	Low-energy Inhomogeneous distribution Note ^{222}Rn
Ra-226	186.10	3.51	Interference with ^{235}U (185.72 keV)
Pa-231	300.07 302.65	2.47% 2.2%	Interference with ^{212}Pb (300.09 keV)
U-235	143.76 185.72	10.96% 57.2%	Interference with ^{226}Ra (186.10 keV)



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Natural radionuclides measurable through daughter products

Nuclide	Gamma-emitting nuclide	E (keV)	Intensity I _γ	Comments
Ra-226	Pb-214 Bi-214	295.22	18.15%	Equilibrium assumed between ²²⁶ Ra, ²²² Rn, ²¹⁸ Po, ²¹⁴ Pb, and ²¹⁴ Bi Note ²²² Rn
		351.93	35.1%	
		609.31	44.6%	
		1120.29	14.7%	
		1764.49	15.1%	
Ac-227	Th-227 Ra-223	235.97	12.3%	Equilibrium assumed between ²²⁷ Ac, ²²⁷ Th, and ²²³ Ra Interference with ²²⁸ Ac at 270.24 keV
		269.46	13.7%	
Th-228	Ra-224 Pb-212 Bi-212 Tl-208	240.99	4.10%	Equilibrium assumed between ²²⁸ Th, ²²⁴ Ra, ²²⁰ Rn, ²¹⁶ Po, ²¹² Pb, ²¹² Bi, and ²⁰⁸ Tl Note ²²⁰ Rn
		238.63	43.3%	
		727.33	6.58%	
		583.19	30.4%	
		2614.35	35.64%	
Th-232	Ac-228	338.32	11.27%	Equilibrium assumed between ²³² Th, ²²⁸ Ra, and ²²⁸ Ac
		911.20	25.8%	
		968.97	15.8%	
U-238	Th-234 Pa-234m	63.28	4.1%	Equilibrium assumed between ²³⁸ U, ²³⁴ Th, and ²³⁴ Pa(m) Note low-energy gamma line of ²³⁴ Th
		766.37	0.316%	
		1001.03	0.839%	



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- **Analyte:** gamma emitting radionuclides
- **Geometry:** HPGe (or other type) gamma detector usually at 1m above the ground
- **Matrix:** Soil and air
- **Measurement time:** usually 20 to 40 min
- **MDA:** about 100 Bqm⁻², depending on detector efficiency, radionuclide of interest and other radionuclides present
- **Accuracy:** 10-50 % depending on calibration accuracy and environmental conditions.
- **Prerequisite:** Calibration of the gamma-ray spectrometric system for in situ measurements

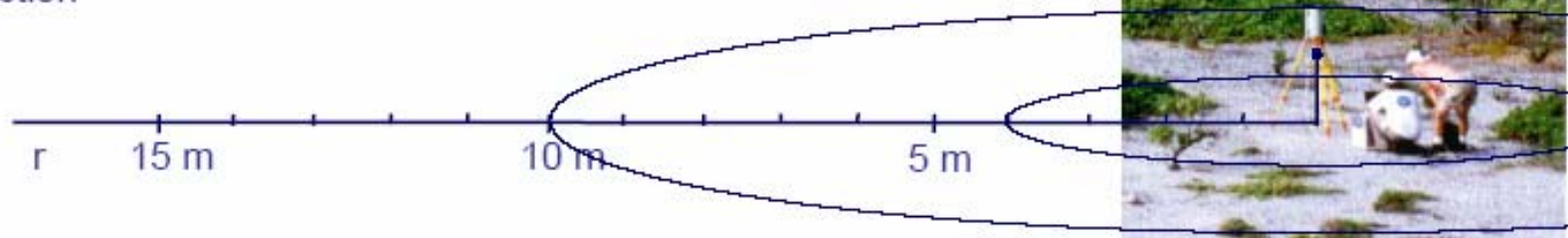
Effective field of view – Sample size

Example

photon energy 662 keV (^{137}Cs)
 detector at height $h=1\text{m}$
 soil density $\rho=1.6\text{ g cm}^{-3}$
 relaxation length $L=3.0\text{ cm}$

r	Fraction of total flux $\Phi(r)/\Phi$	Surface area πr^2
4 m	65%	$\sim 50\text{ m}^2$
10 m	85%	$\sim 310\text{ m}^2$
>10 m	15%#	$\sim 710\text{ m}^2$ (at $r=15\text{m}$)

remaining fraction



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In situ / laboratory measurements

- Shorter measurement time
- Prompt availability of results (without sampling, sample transport and preparation)
- Averaging radionuclide activity over large area
- Often large errors are observed (intercomparison exercises)
- Using laboratory results (soil profiles – depths distribution) better results can be obtained
- Based on in situ results better sampling plan can be prepared



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Basic instrumentation

Detector

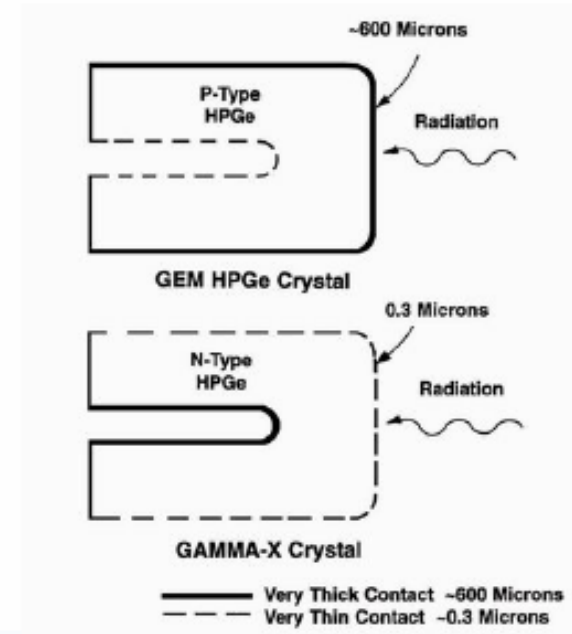
- HPGe (hyper-pure germanium detector)
 - p-type for $E_{\gamma} > 100$ keV (3-60 keV up to 3-10 MeV)
 - n-type for $E_{\gamma} > 45$ keV (3 keV up to 300 keV-3 MeV)
- Efficiency of 20%-50% relative to 3"x3" NaI(Tl) at 1.3 MeV
- Portable (hand-held) cryostat

Electronics

- portable, battery operated, or
- lab instruments and power generator

Detector holder

- tripod, or
- trolley



IN SITU GAMMA RAY-SPECTROMETRY BASIC EQUIPMENT



QA: In-situ γ -ray spectrometry Checklist

Instrumentation

- Detector
- Electronics (MCA, Notebook PC, set of cables, power supply)
- GPS
- Dose rate meter
- Distance meter
- Camera

Software

- MCA and Evaluation
- Databases
- Nuclide library, conversion factors

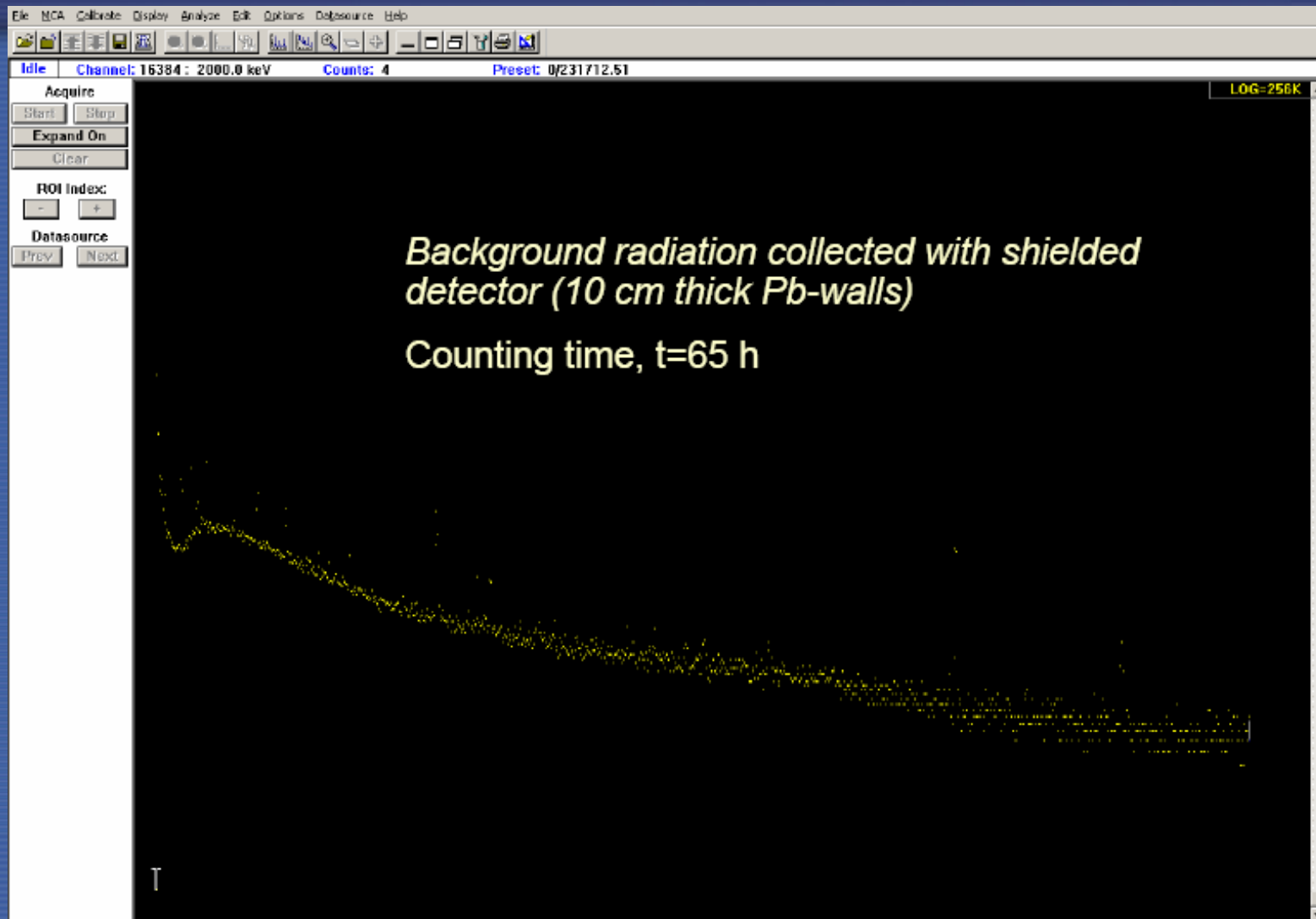
Supplies

- Detector support (tripod)
- Spare batteries, Spare cables, Check sources
- Liquid nitrogen (fittings for filling)
- Protective clothes, plastic bags,
- Basic tools

Documentation

- Manuals (operation, procedures)
- Logbook
- Nuclide library tables, conversion factors
- Map

Shielded background

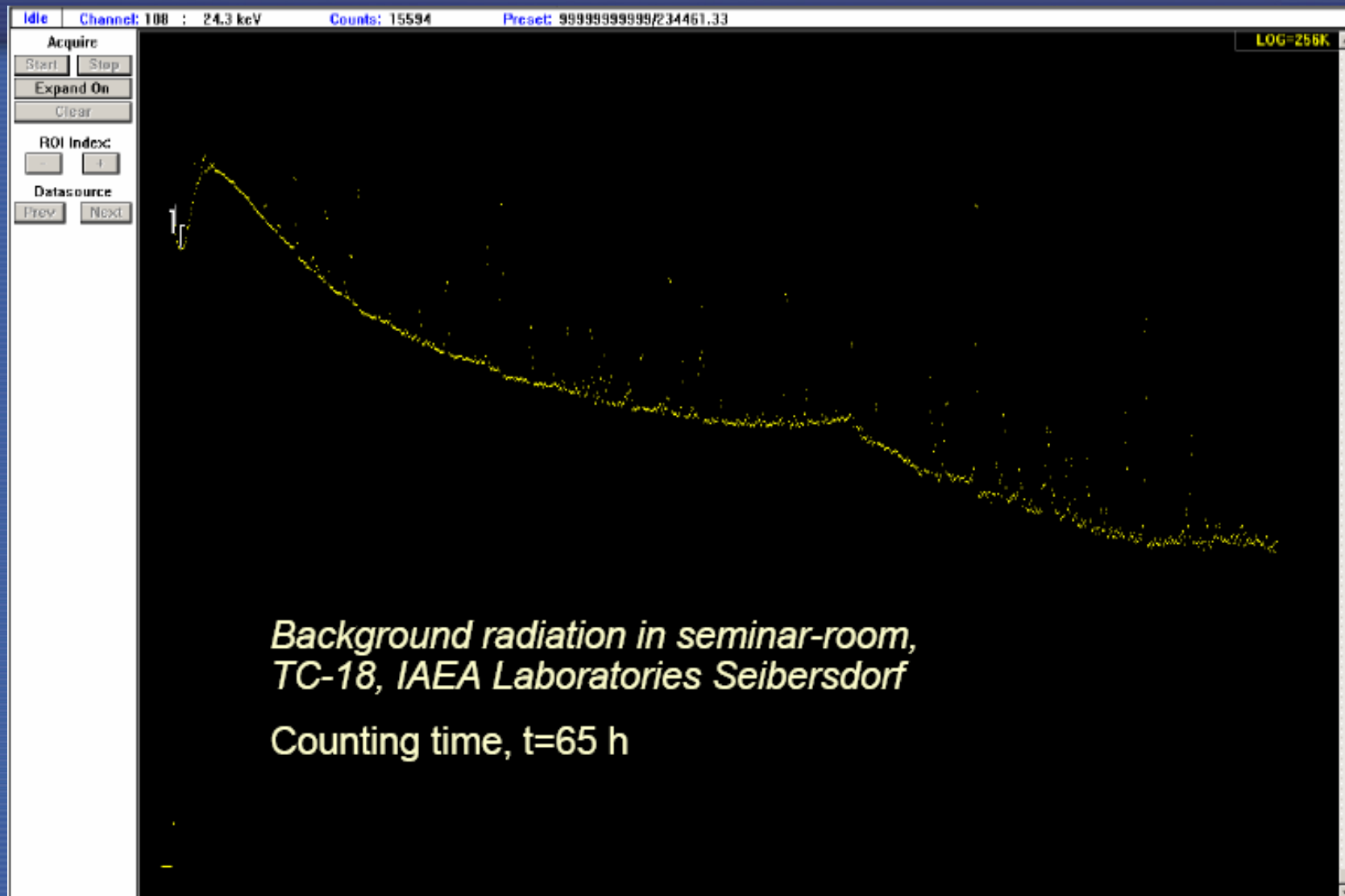


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Seminar room

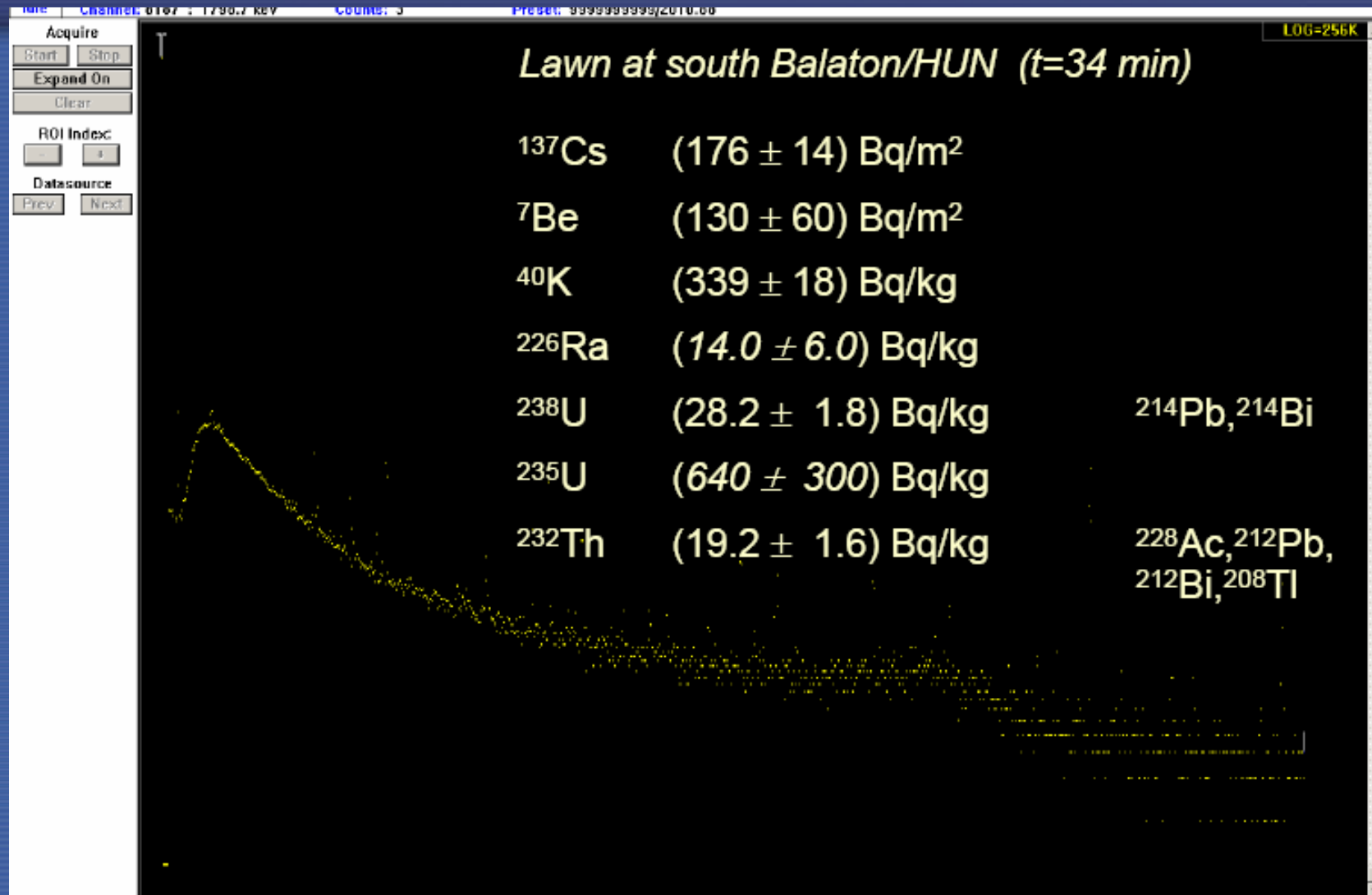


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Typical environment

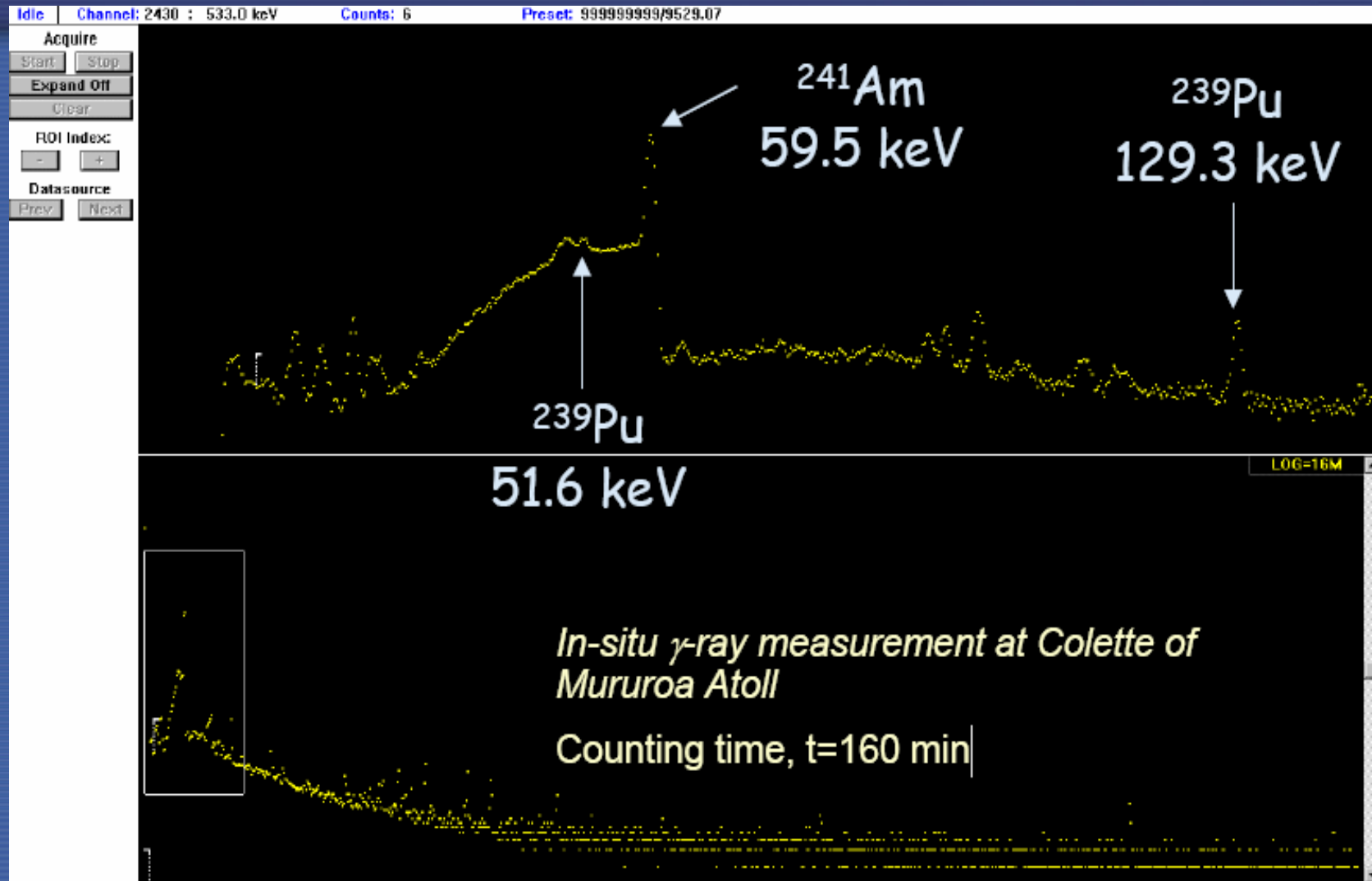


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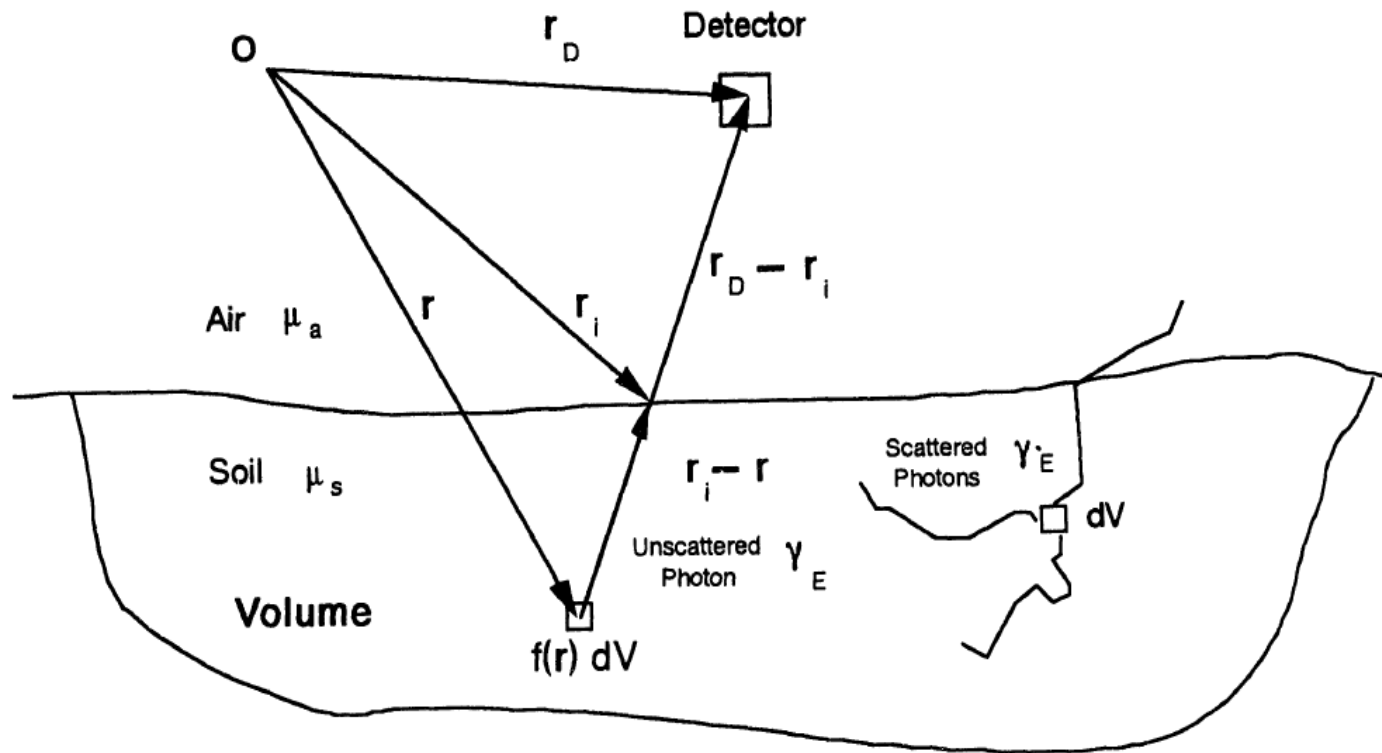
Mururoa



Theoretical model for photon flux calculation in an in situ measurement

$$\Phi = \int_V \frac{f(r)}{4\pi(r_D - r)^2} \exp\left[-\frac{\mu_s}{\rho} \rho(r_i - r) - \frac{\mu_a}{\rho_a} \rho_a(r_D - r_i)\right] dV \quad (2.2)$$

where $f(r)$ is the source strength at r , μ_s/ρ is the mass attenuation coefficient for soil ($\text{cm}^2 \text{g}^{-1}$) and μ_a/ρ_a is the mass attenuation coefficient for air.



Commonly used depth distributions and units

Exponential	$f(z) = \frac{S_0}{L} e^{-z/L}$	S_0 in (Bq m ⁻²)
Uniform L=∞	$f(z) = S_V$	S_V in e.g. (Bq m ⁻³), (Bq cm ⁻³), or (Bq kg ⁻¹)
Plane L=0	$f(z) = S_A$	S_A in (Bq m ⁻²)
Plane at depth z_0	$f(z) = S_A \delta(z - z_0)$	S_A in (Bq m ⁻²)
In general	$f(z) = \sum_i S_i \delta(z - z_i)$	S_i in (Bq m ⁻²)



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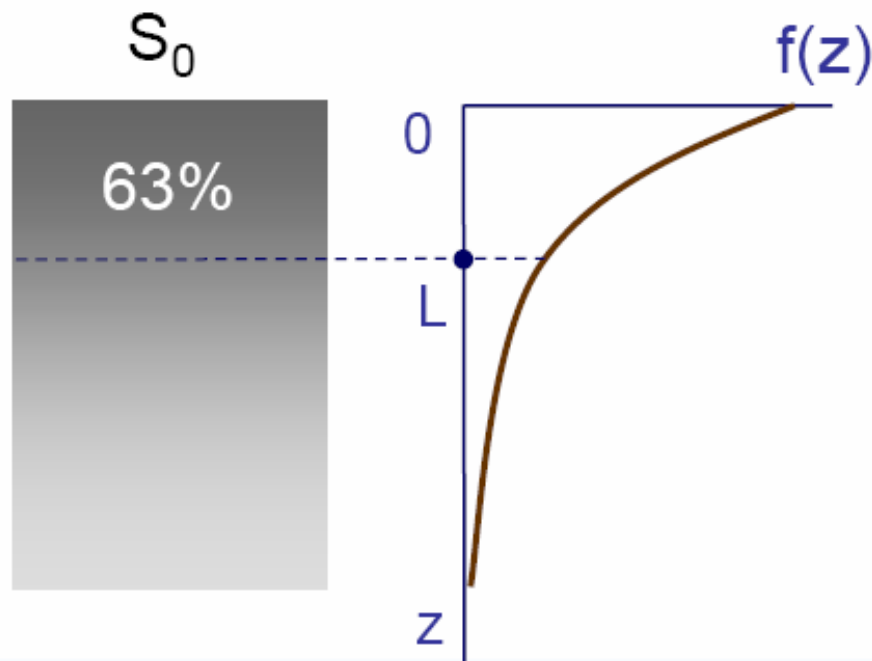
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Exponential distribution of a radionuclide

$$f(z) = \frac{S_0}{L} e^{-z/L}$$

S_0 – activity in a soil column, total inventory (Bq m⁻²)

L – relaxation length, e.g. (cm)



Interpretation of S_0 :

$$\int_0^{\infty} f(z) dz = S_0$$

Interpretation of L :

$$\int_0^L f(z) dz \approx 0.63 S_0$$

Example values for relaxation length (Soil density: 1.6 gcm⁻³)

L (cm)	Applications
0.10	used for fresh fallout where all the radioactivity is deposited on the soil surface
1.25	used for global fallout on wooded or desert sites (1.25 cm – 3.1 cm)
12.5	used for global fallout on open undisturbed fields (7 cm – 12.5 cm)
infinity	used for uniformly distributed radionuclides, e.g. natural radioactivity

Calculation of unscattered photon flux for different radionuclide depth distributions

Exponential

$$\Phi = \frac{1}{2} S_0 \left\{ E_1(\mu_a h) - e^{\frac{\mu_a h}{\mu L}} E_1 \left[\left(1 + \frac{1}{\mu L} \right) \mu_a h \right] \right\}$$

Uniform

$$\Phi = \frac{1}{2} S_V \frac{\mu_a}{\mu} \left[\frac{1}{\mu_a h} e^{-\mu_a h} - E_1(\mu_a h) \right]$$

Plane

$$\Phi = \frac{1}{2} S_0 E_1(\mu_a h)$$

The function $E_1(x)$ is the 1st order exponential integral

$$E_1(x) = \int_x^{\infty} \frac{e^{-t}}{t} dt$$

Series expansion

$$E_1(x) = -\gamma - \ln x - \sum_{n=1}^{\infty} \frac{(-1)^n x^n}{n n!}$$

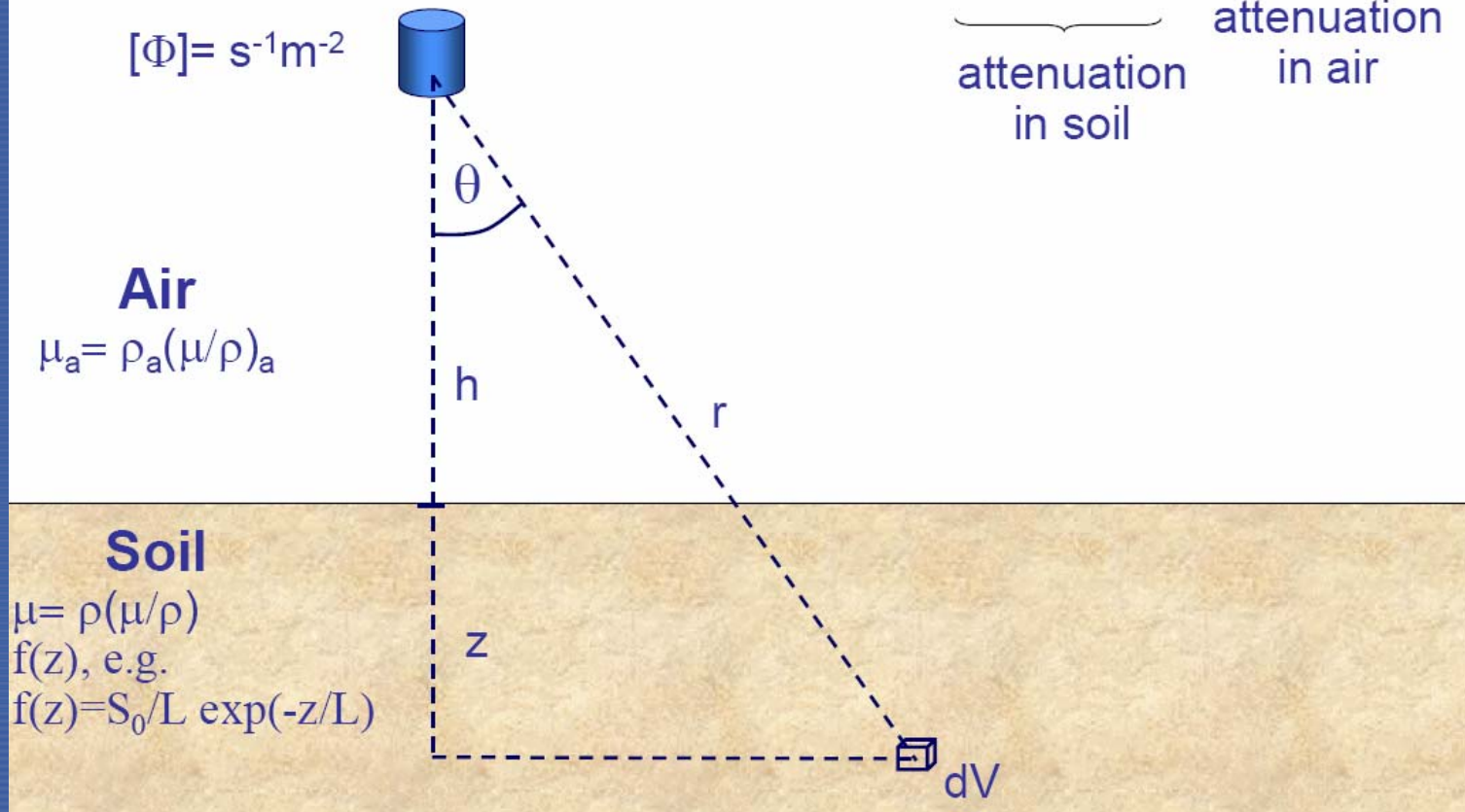
$$\gamma = 0.5772156649\dots$$

Theoretical model for photon flux calculation in an in situ measurement

$$\Phi = \int_0^{\pi/2} d\theta \int_{h/\cos\theta}^{\infty} \frac{S_0}{4\pi r^2} e^{-z/L} \cdot 2\pi r^2 \sin\theta \cdot e^{-\mu(r-h/\cos\theta)} \cdot e^{-\mu_a h/\cos\theta} dr$$

$[\Phi] = \text{s}^{-1}\text{m}^{-2}$

attenuation in soil attenuation in air



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Calculation of radionuclide deposition

$$C = 10 \frac{N}{t} \frac{1}{C_f I_\gamma}$$

unit conversion factor

net counts in the full-energy peak at energy E

deposition – surface concentration of a radionuclide, (kBq m⁻²)

counting time, live time, (s)

detector calibration factor at energy E, (cm²)

intensity of a gamma line at energy E (emission probability)

Detector calibration factor

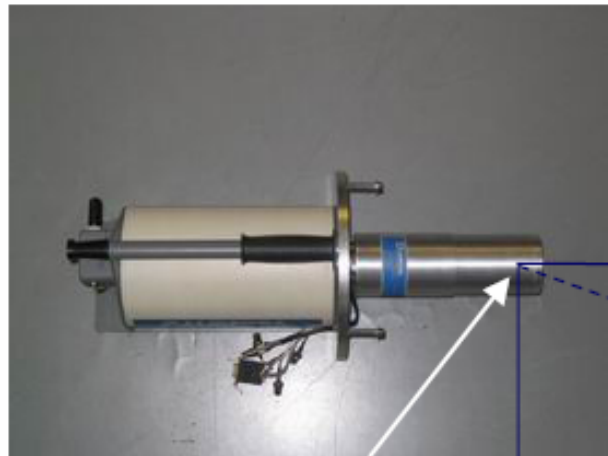
$$C_f = \frac{R_f}{A_s} = \left(\frac{R_f}{R_0} \right) \left(\frac{R_0}{\Phi} \right) \left(\frac{\Phi}{A_s} \right)$$

angular correction factor –
correction factor required to account
for the detector angular response

geometrical factor – total photon
flux density at the detector per unit
concentration or deposition
inventory of the radionuclide

response factor - neat peak count
rate due to a unit primary photon flux
density of energy E incident on the
detector (normal to the detector face)

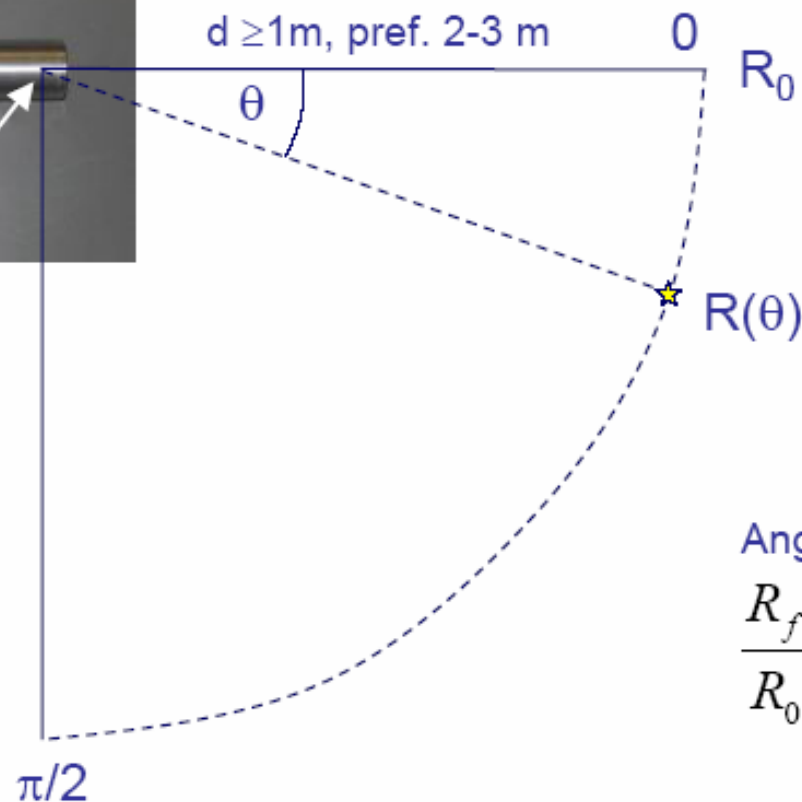
Calibration – detector characteristics



Flux at the detector's effective center:

$$\Phi_0 = \frac{AI_\gamma}{4\pi r^2} e^{-\mu_a(r-x)}$$

$R(\theta)$ – net count rate in a full-energy peak, at angle θ

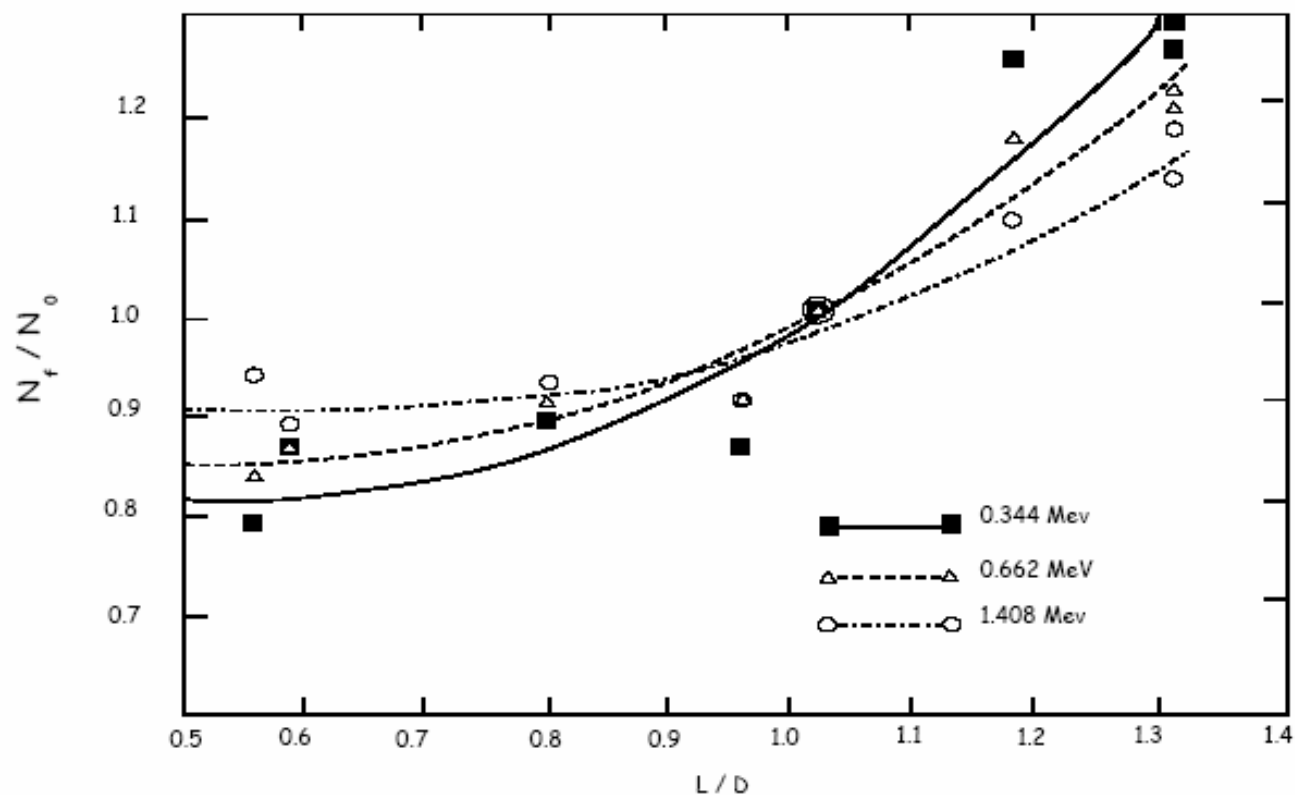


Angular correction factor:

$$\frac{R_f}{R_0} = \int_0^{\pi/2} \frac{\Phi(\theta) R(\theta)}{\Phi R_0} d\theta$$

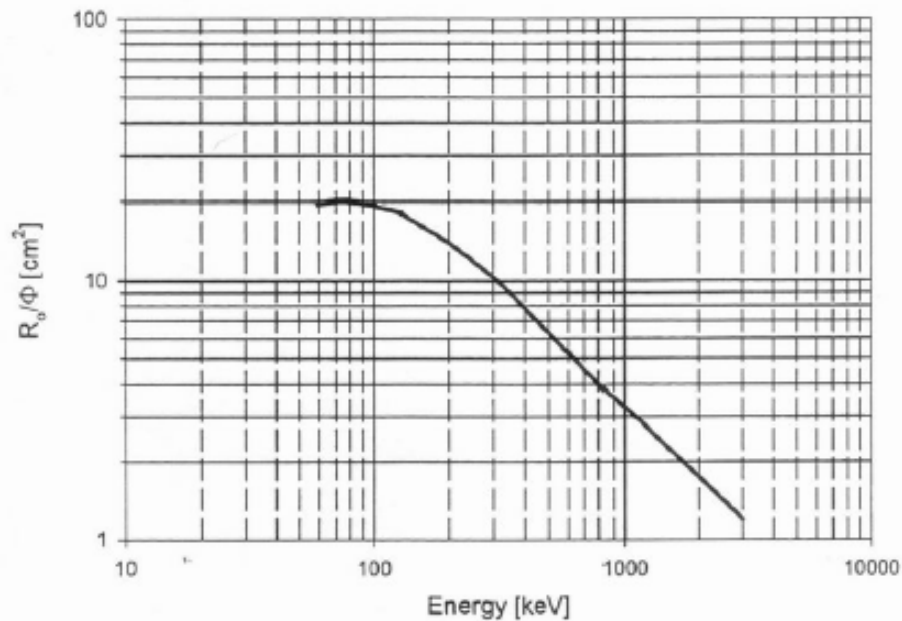
Angular correction factor

Angular correction factor R_f/R_0 as a function of Ge crystal length/diameter L/D ratio at three different energies for a downward facing detector for a uniform with depth source profile in the soil.

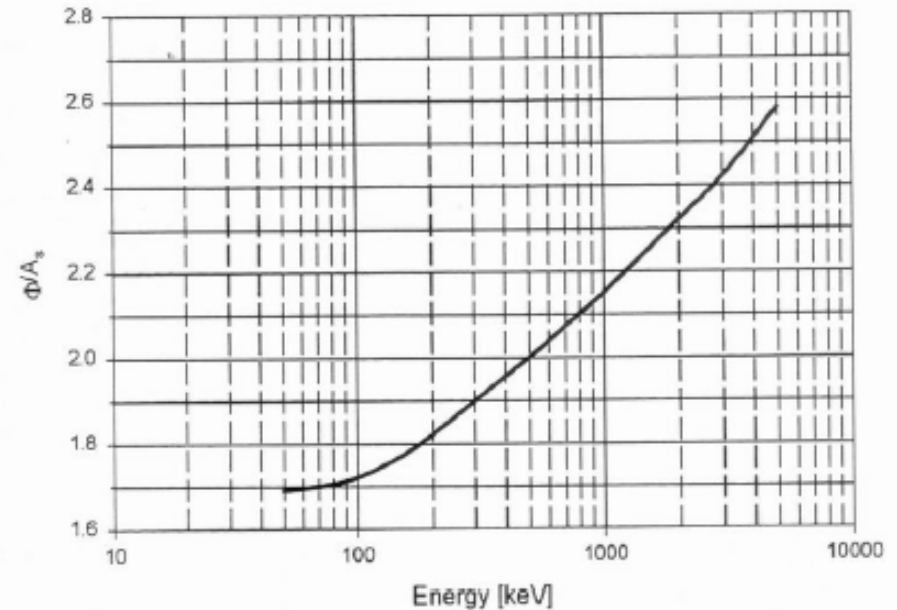


Examples of a detector characteristics

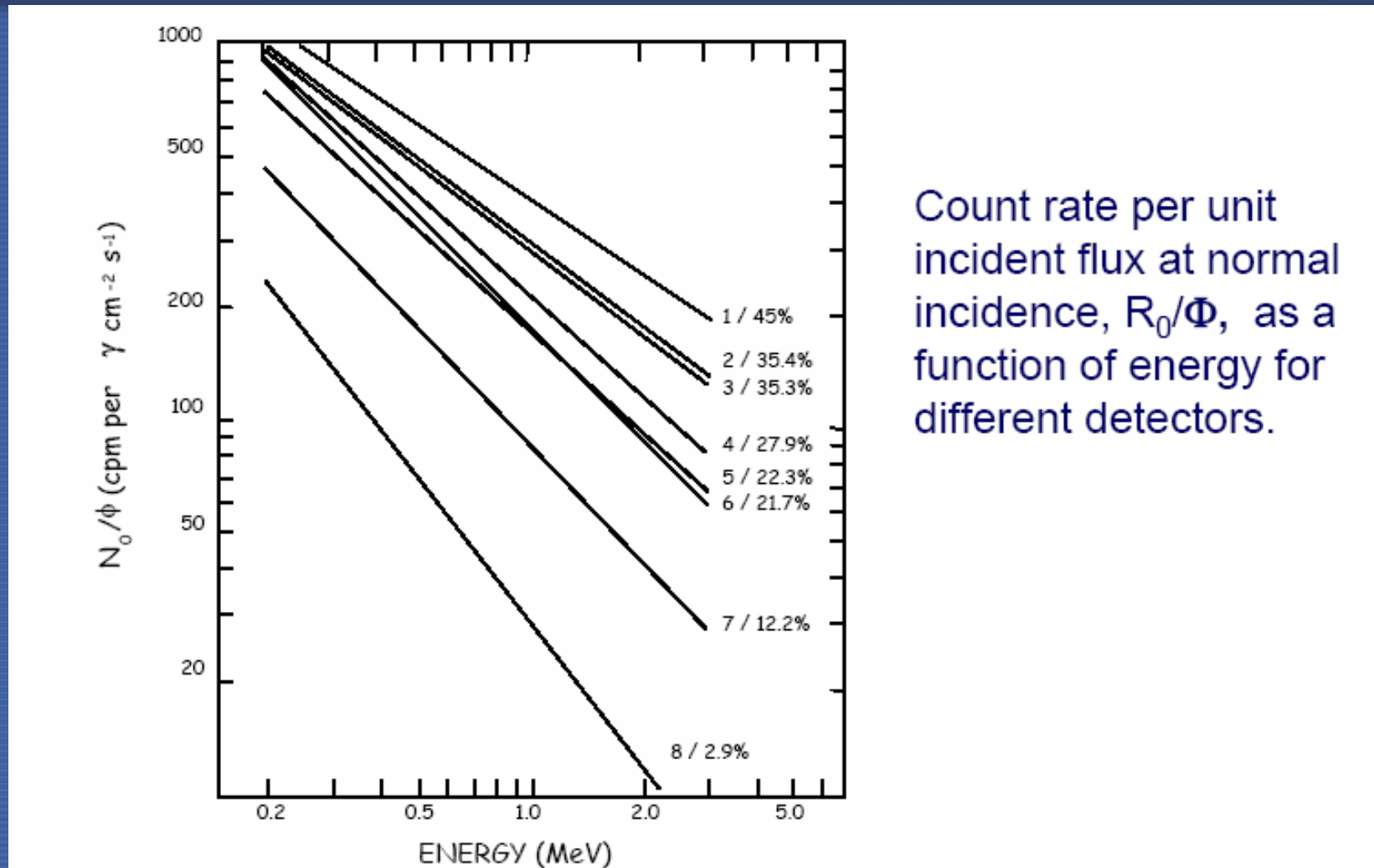
Typical response factor, R_0/Φ , for a Ge detector of 22% relative efficiency



Geometrical factor, Φ/A_s , as a function of photon energy in case of surface source distribution for 1m above ground



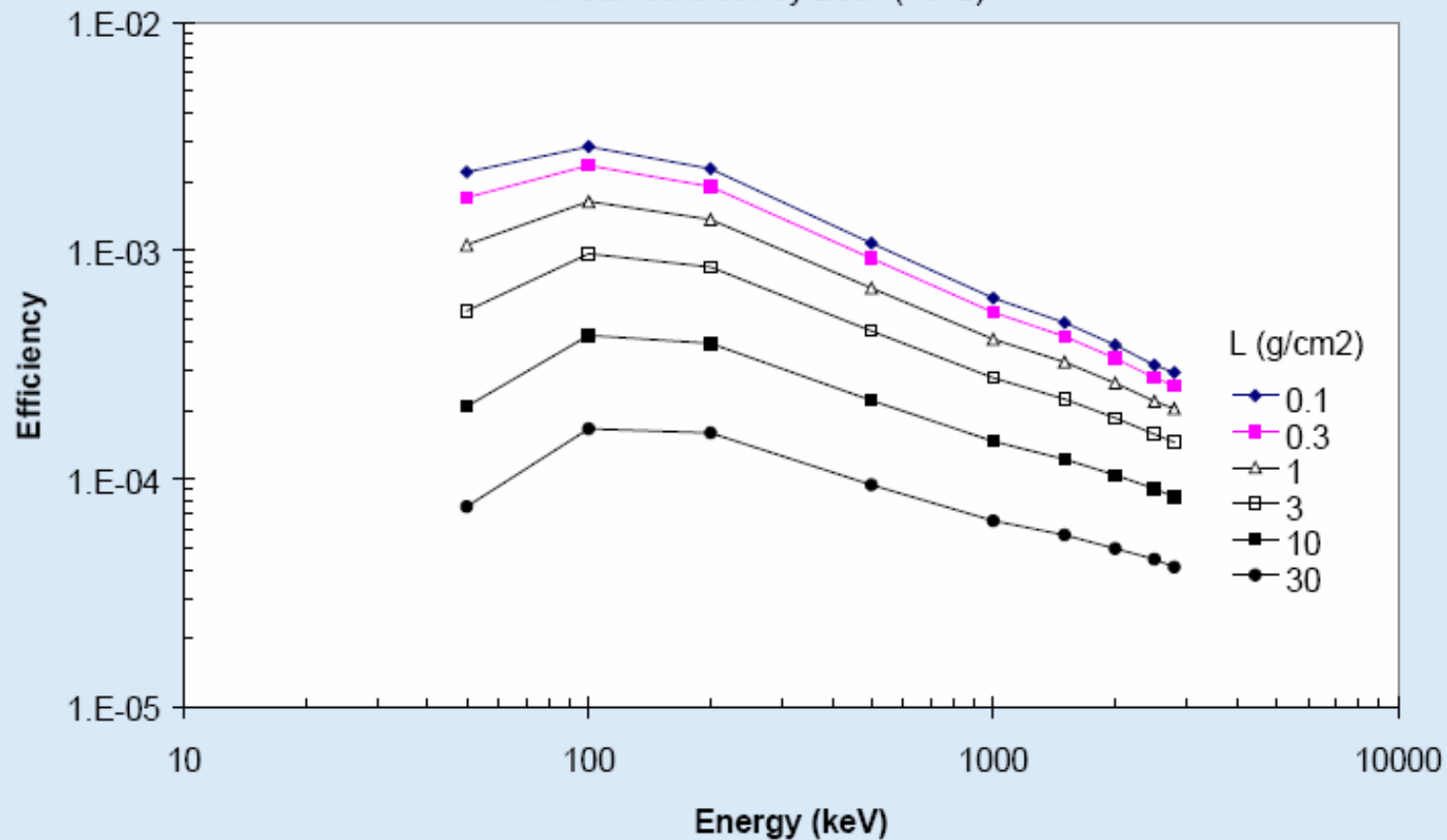
Response factor – a quick reference



Different approach – mathematical detector efficiency calculation

Efficiency of HPGe detector GX2018

generated with MCNP code (Canberra)
for standard soil by Beck (1972)

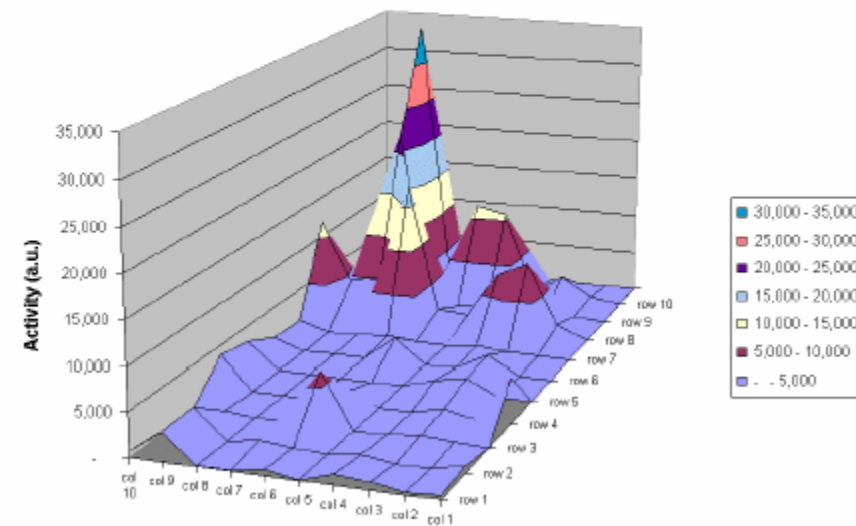
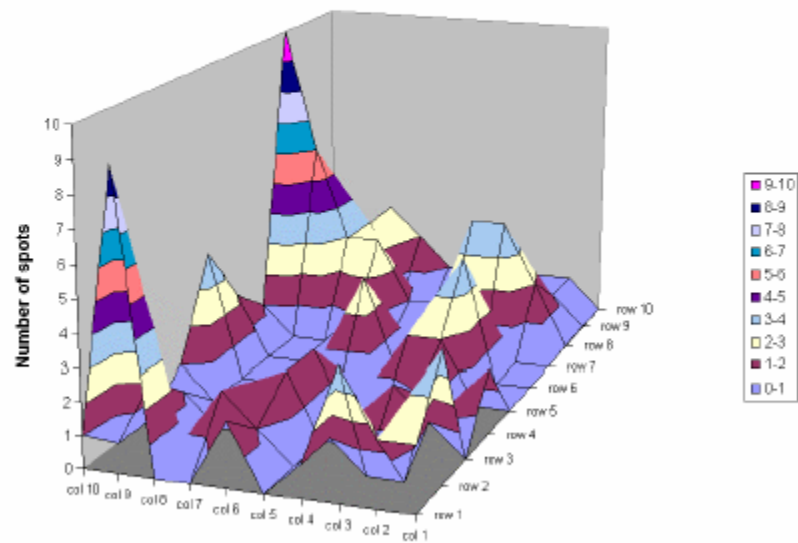


Sources of errors

	Error
<ul style="list-style-type: none">• Radiation situation is not adequately well described by a mathematical model used/available (lack of proper model)<ul style="list-style-type: none">- departure of real depth distribution from the model used,- obstacles, e.g. building, wall, etc. (modified "field-of-view" –departure from a conical shape)- nonuniform surface, e.g. grassland and a road in the field-of-view- roughness of the soil surface (if not considered in the model)	10%-50% (larger are not uncommon)
<ul style="list-style-type: none">• Poor experimental arrangement in the field (geometry)• Incorrect or poor calibration for in-situ measurements• Human errors due to e.g. typing for reporting• Counting statistics of net count rate• Nuclear constants used	10%-20% 15%-20% (?) a factor > 10 5%-10% 1%-5%

Inhomogeneous radionuclide distribution

Surface-distribution of Am-241 at Colette of Mururora Atoll
10m x 10m square

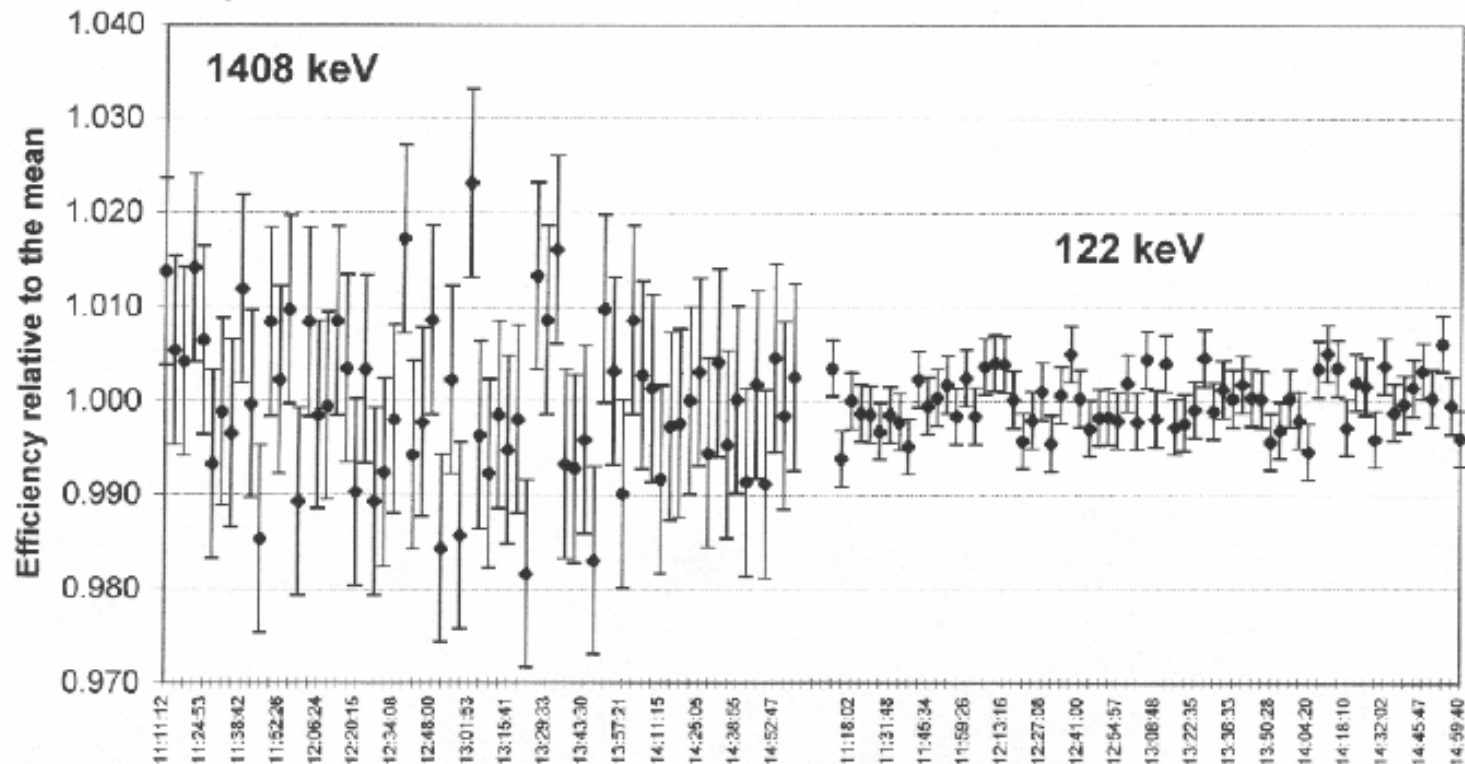


Monitoring the system performance

QC

Stability test of the gamma spectrometer for in-situ measurements

GX2018, InSpector (2)
Geo: Eu-152 IAEA ps set #103; std dist of 6 cm
Counting time RT=10min, DT=33%



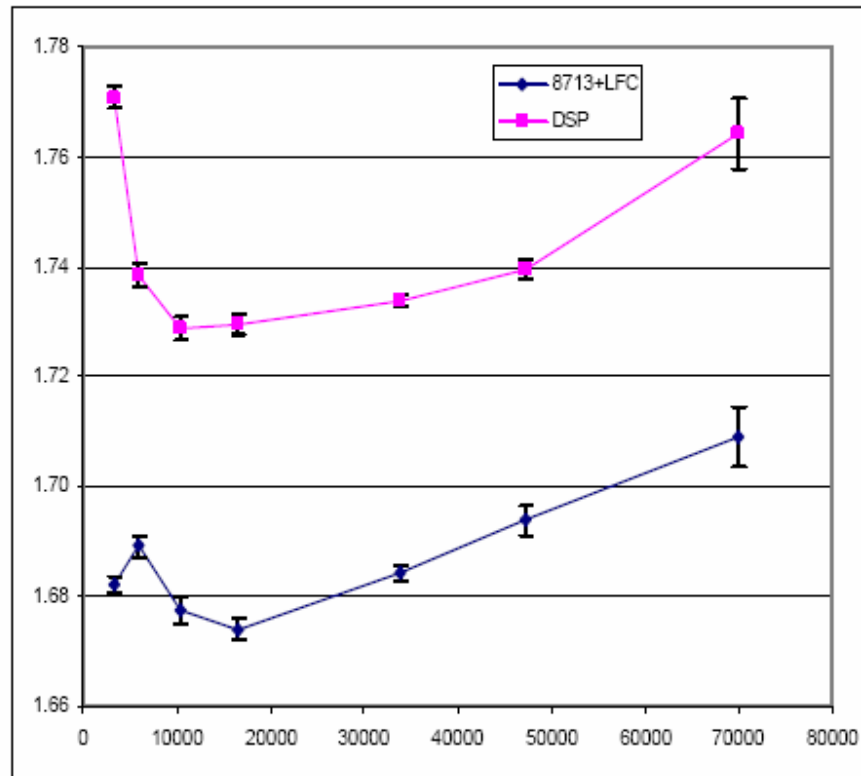
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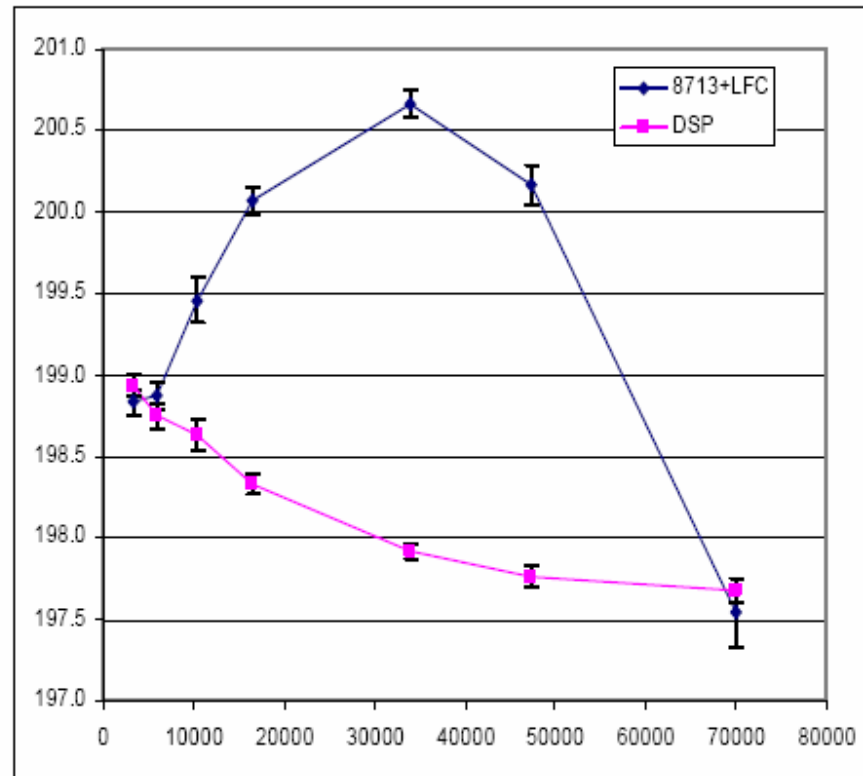
Effect of count rate in well adjusted sytem

Resolution, FWHM (keV)



Input count rate (cps)

Net peak area (cps)



Input count rate (cps)

References

Field measurements of radioactivity: introduction to
in-situ γ -ray spectrometry,

Marek Makarewicz IAEA

References

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- A theoretical comparison of methods of quantification of radioactive contamination in soil using in situ gamma spectrometry; J. MacDonald et. al; J. of Radiol. Prot. 1997 Vol. 17 No.1 3-15
- Uncertainties of in situ gamma spectrometry for environmental monitoring, W. Sowa et. al, Radiation Protection Dosimetry Vol. 27 No. 2 pp. 93-101 (1989)