



The Abdus Salam
International Centre for Theoretical Physics



1833-46

**Workshop on Understanding and Evaluating Radioanalytical
Measurement Uncertainty**

5 - 16 November 2007

Uncertainty in gas proportional counting.

Gyula KIS-BENEDEK
*International Atomic Energy Agency IAEA
Agency's Laboratories Seibersdorf
Chemistry Unit, A-2444 Seibersdorf
AUSTRIA*

Counting Uncertainty in Using Gas Proportional Counters



IAEA

*Atoms for Peace: The First Half Century
1957–2007*

Main Types of Proportional Counters

1. Gas Flow Proportional

- with window (laboratory alpha-beta counters)
- windowless

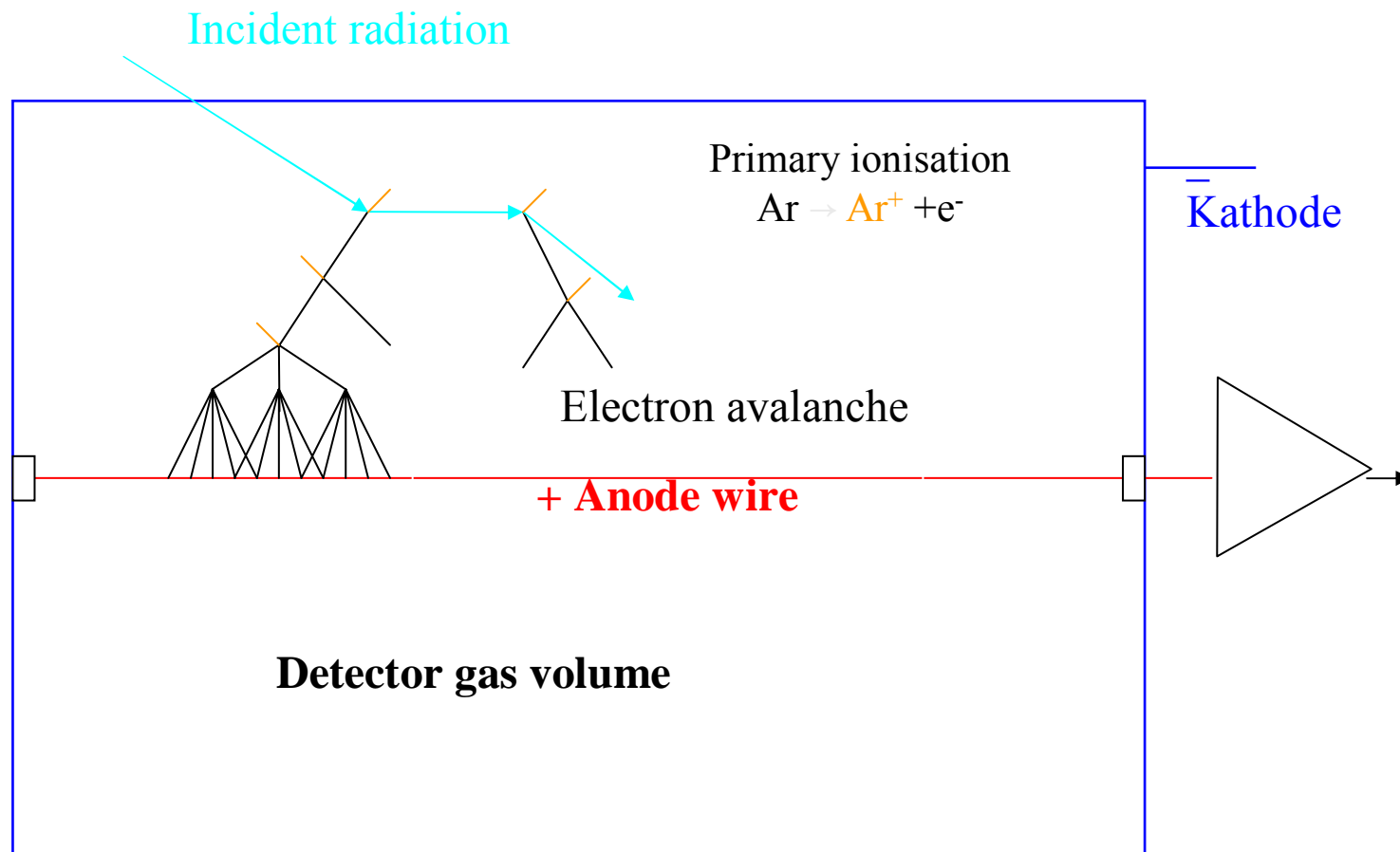
2. Air Proportional (alpha counting only)

3. Sealed proportional (e.g., BF_3 , ^3He neutron detectors)

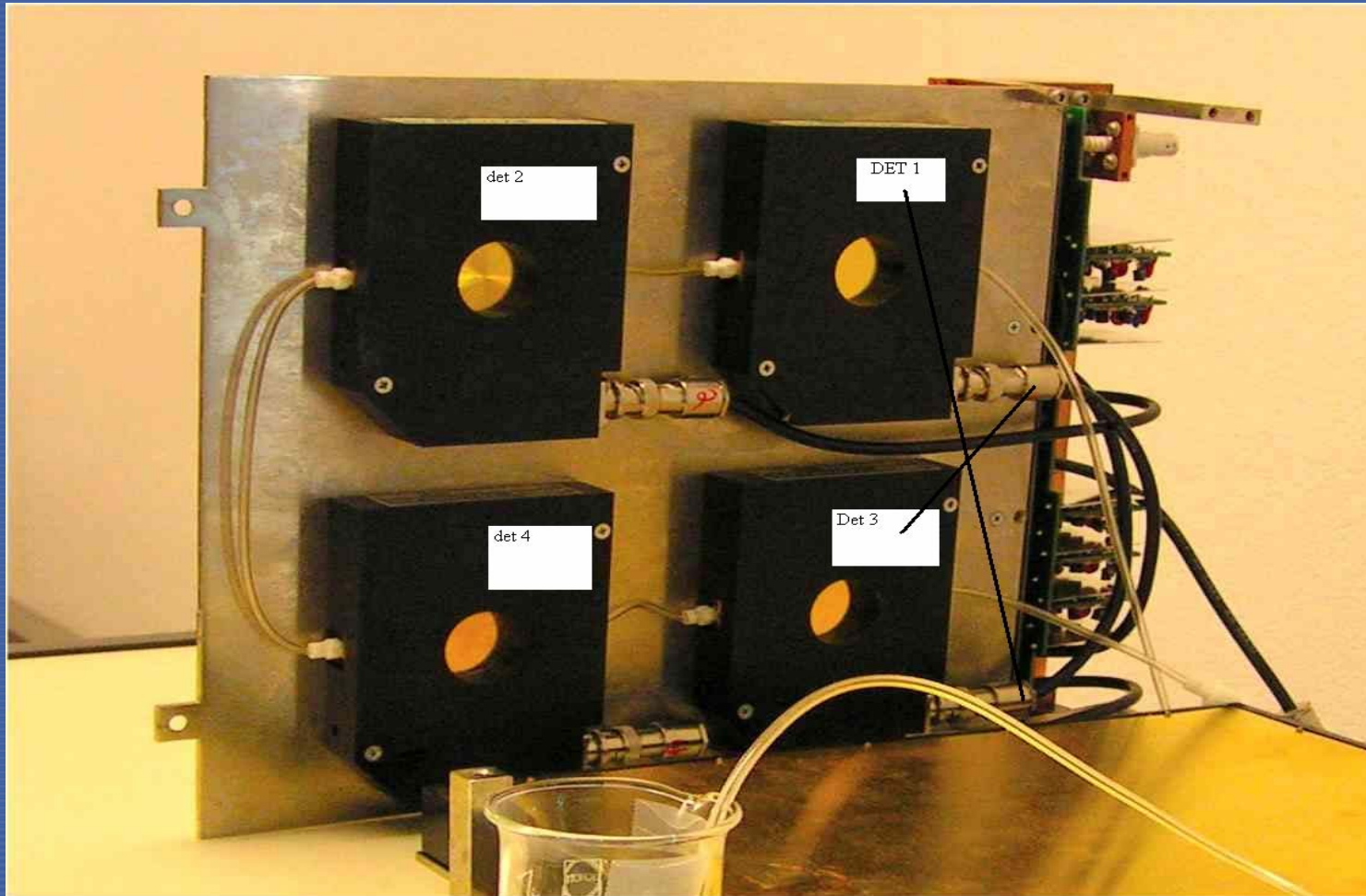
Applications

- Gross alpha and or beta counting
 - Filter
 - Smear (wipe test)
 - Water (residue)
 - Soil,
- Sources from separated alpha or beta emitting radionuclides
 - Sr-90, Y-90 or C-14

Basic Detector Theory



Gas proportional detectors



IAEA

Atoms for Peace: The First Half Century

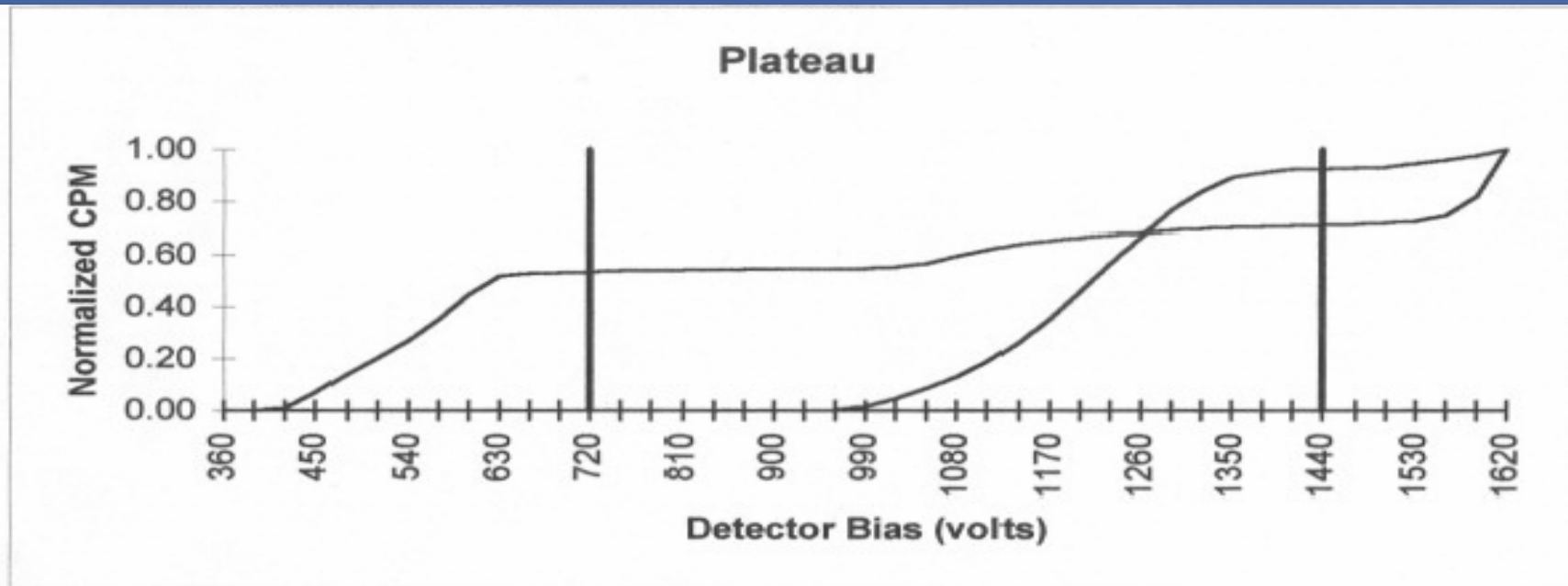
1957-2007

Basic Detector Theory

$$\textit{Gain} = \frac{N}{n}$$

- Gain
- Number of electrons reaching the anode wire
~ U (applied detector voltage bias)
- number of electrons produced by the particle
~ Energy of the particle/ E_{igas}

Basic Detector Theory



Optimum alpha & beta simultaneous operating voltage: **1440**

Beta slope per 100 volts at beta voltage: 1.85%

Alpha slope per 100 volts at beta voltage: 1.53%

Optimum alpha only operating voltage: **720**

Alpha slope per 100 volts at alpha voltage: 1.82%



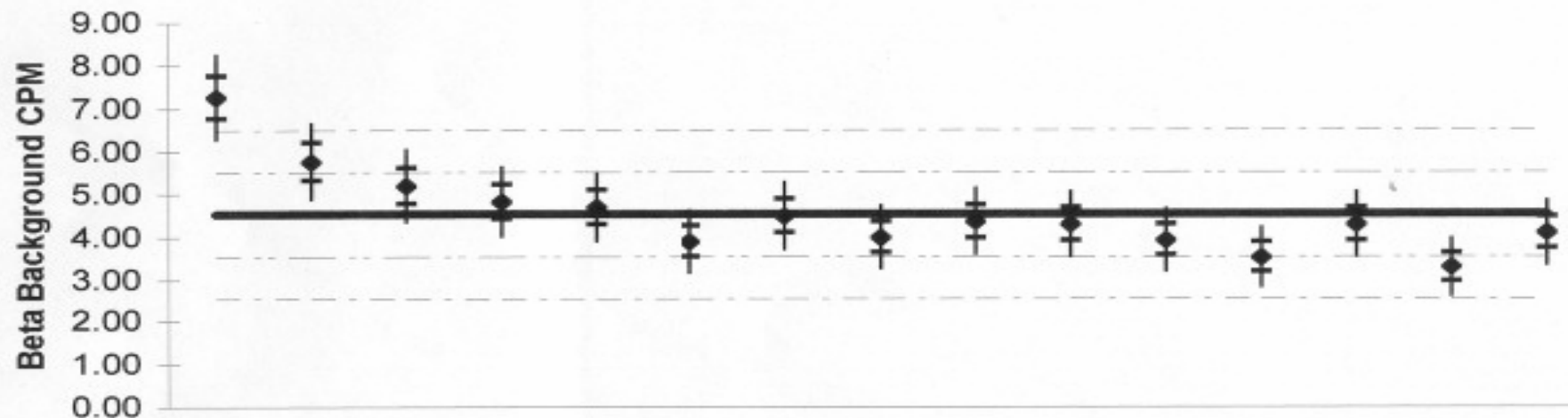
IAEA

Atoms for Peace: The First Half Century

1957-2007

Beta background

LB5100-W Beta Background



legend -- mean

1 σ

2 σ

Mean background: 4.53

Error for mean background: 0.10 1 σ

Actual standard deviation: 0.98

Predicted standard deviation: 0.39

Number of individual measurements: 15

Chi-square: 88.99

Reduced chi-square: 6.36



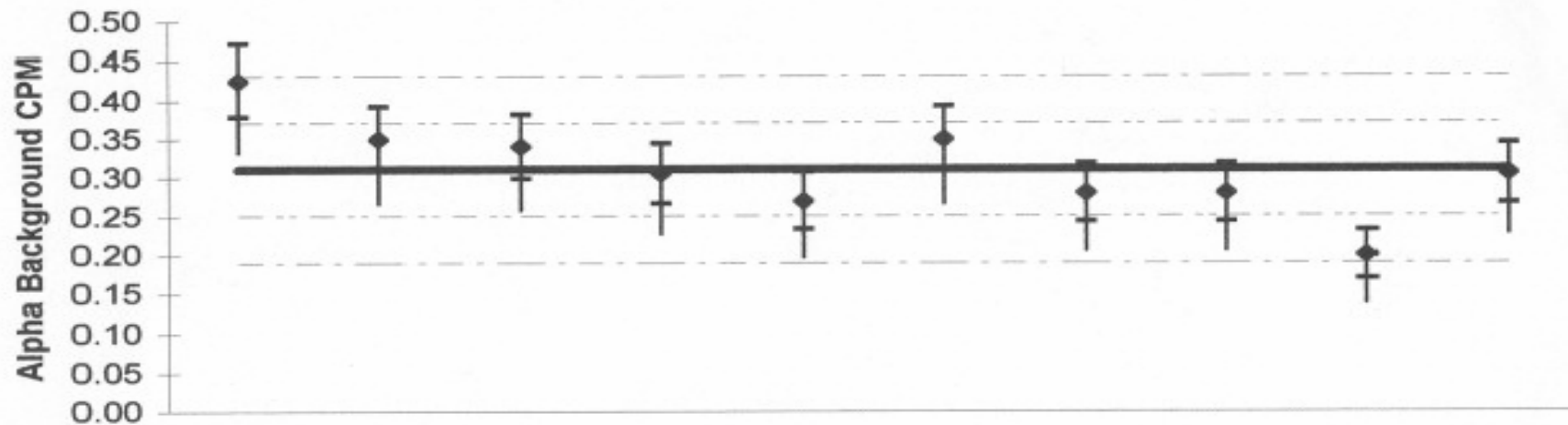
IAEA

Atoms for Peace: The First Half Century

1957-2007

Alpha background

LB5100-W Alpha Background



legend -- mean 1σ 2σ

Mean background:	0.31	
Error for mean background:	0.01	1σ
Actual standard deviation:	0.06	
Predicted standard deviation:	0.04	
Number of individual measurements:	10	
Chi-square:	21.17	
Reduced chi-square:	2.35	



IAEA

Atoms for Peace: The First Half Century

1957-2007

Chi Square test for variances – equipment performance

Expected counting uncertainty :

$$\sigma_N = \sqrt{N}$$

Calculated standard deviation
of n counting:

$$s_N = \sqrt{\frac{n * \sum_i^n N_i^2 - (\sum_i^n N_i)^2}{n * (n - 1)}}$$

Chi square:

$$\chi^2 = \frac{s_N^2}{\sigma_N^2} * (n - 1)$$

Hypothesis:

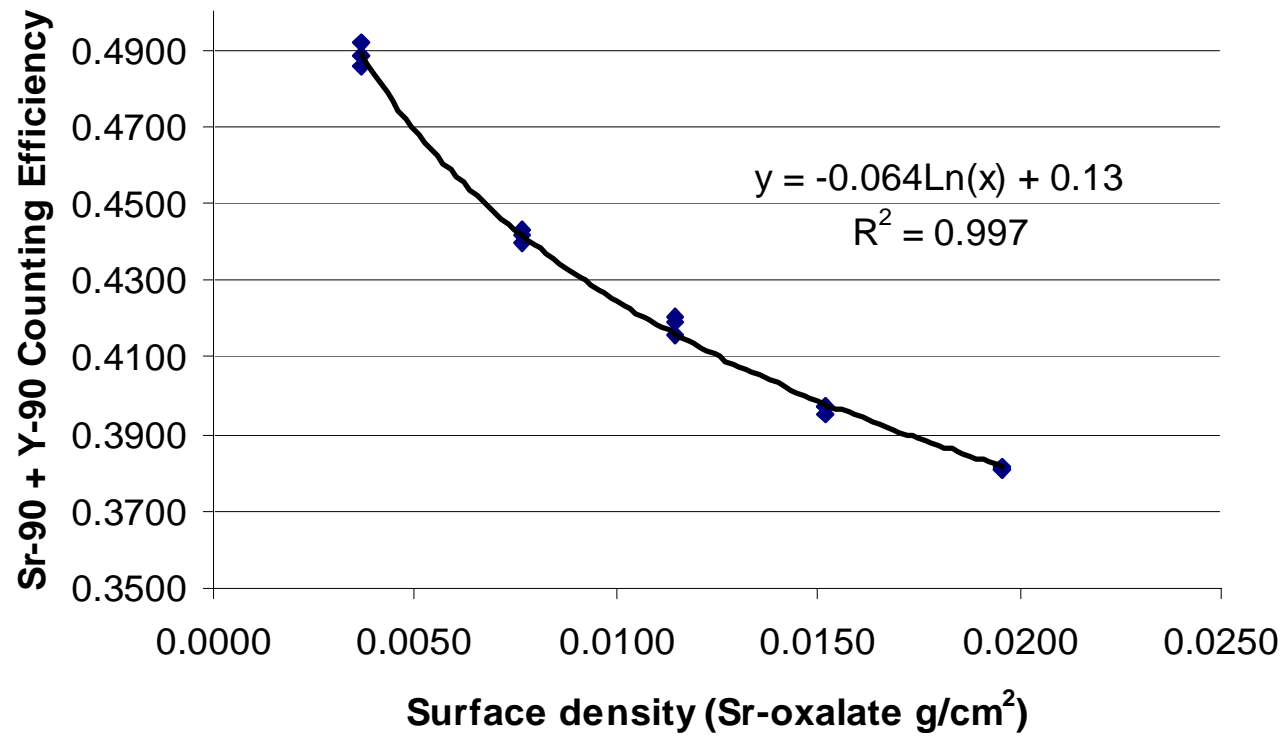
Degree of freedom: n-1

$$H_0 : \sigma_N = s_N ; H_1 : \sigma_N < s_N$$

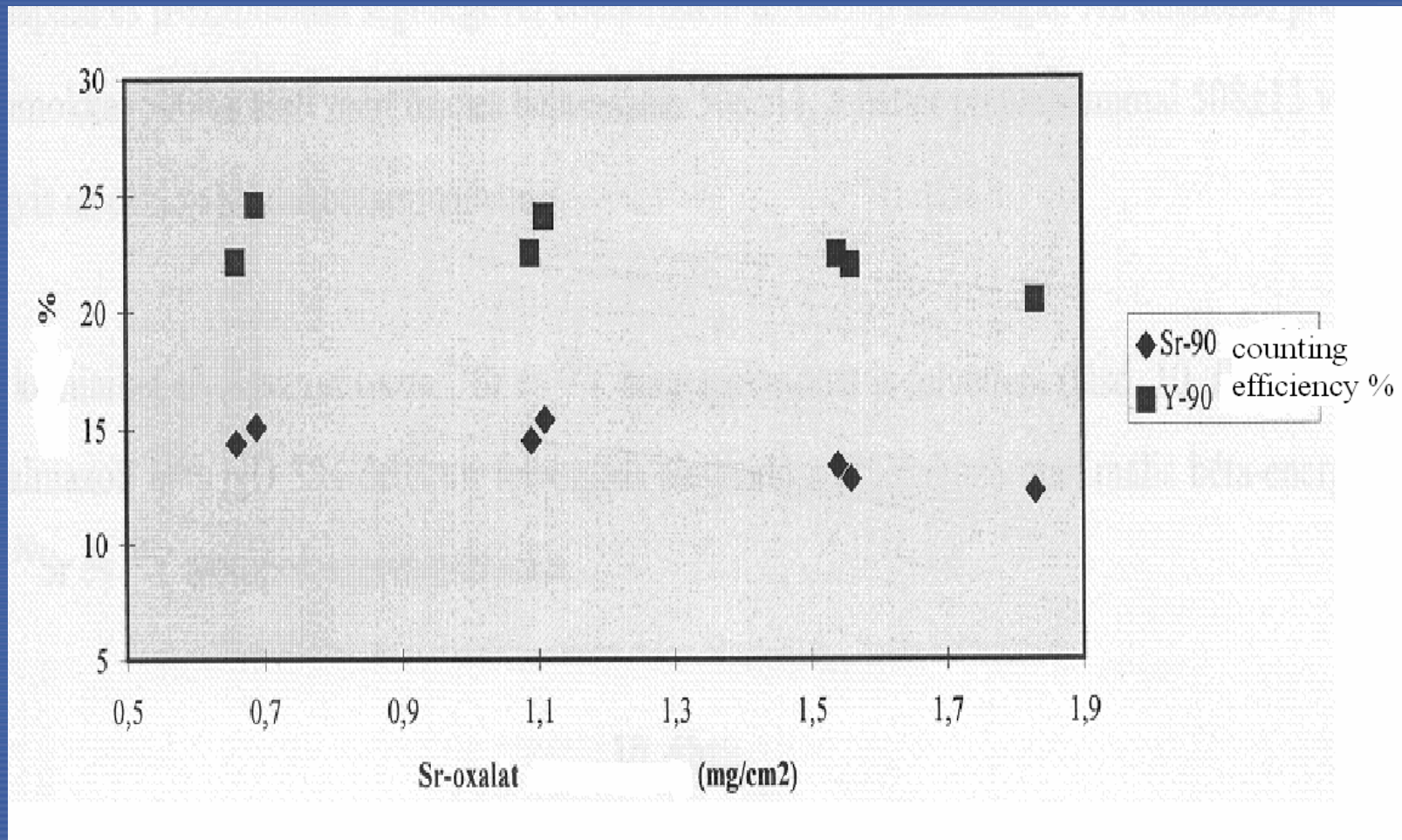
Sources

- Thick source – infinite thickness, saturation layer thickness
 α : 0.02 gcm^{-2} , <3% efficiency, effect of humidity, structure of surface
- Fixed source size
- Variable source thickness
Mass attenuation curve, Standard addition

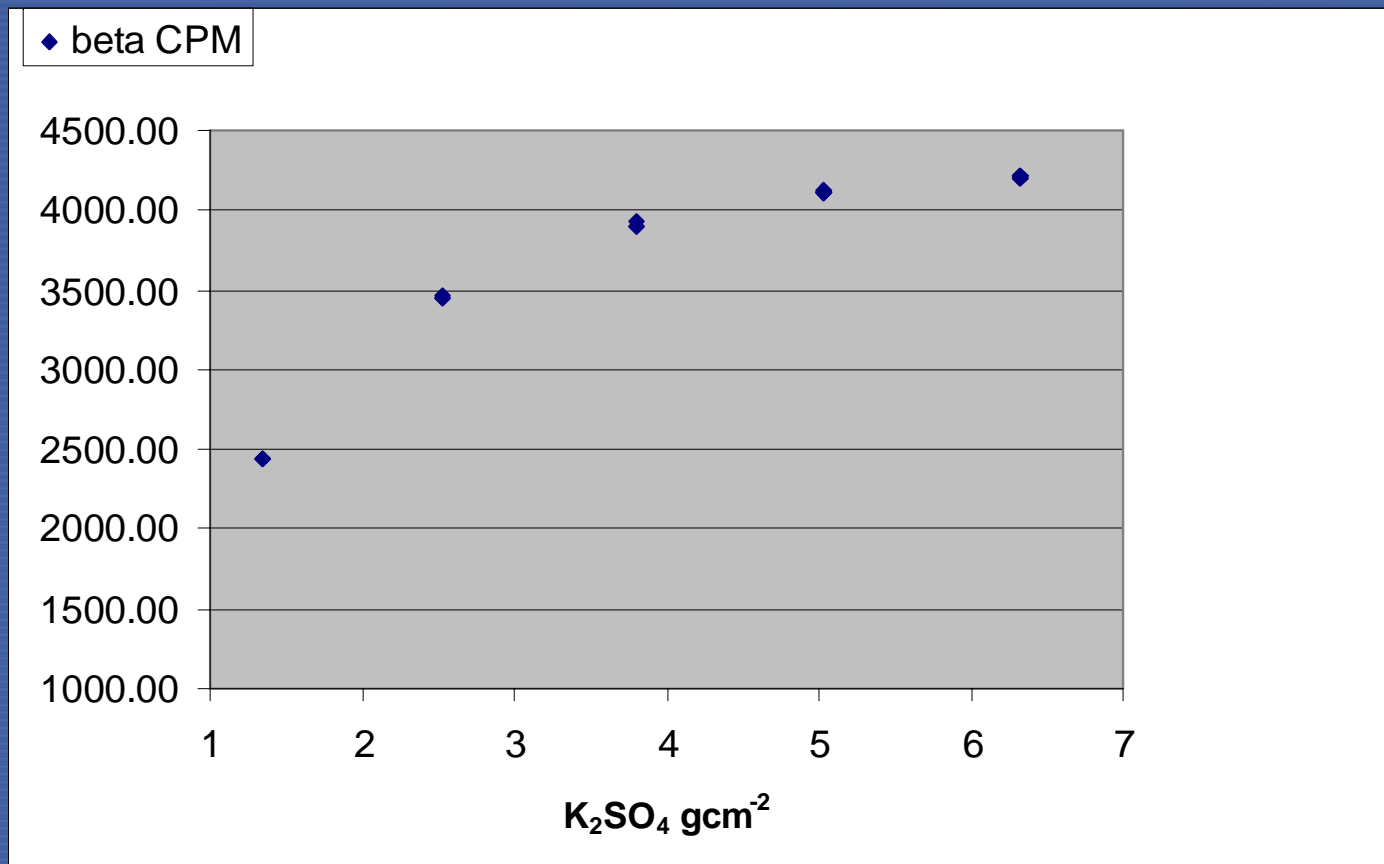
Attenuation Curve



Efficiency – beta energy

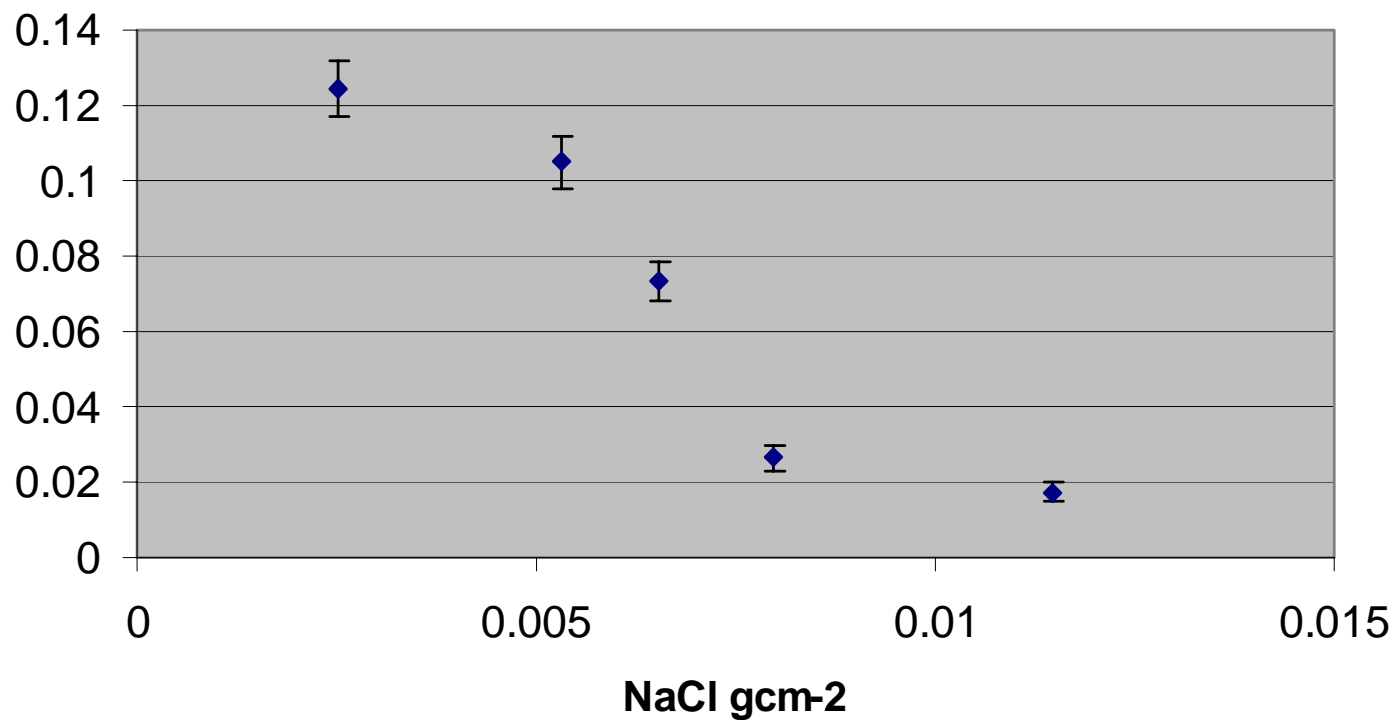


Determination of saturation layer thickness



Alpha attenuation curve

Alpha counting efficiency



IAEA

Atoms for Peace: The First Half Century

1957-2007

Magnified picture of a ^{210}Po / NaCl source



Calibration

$$\varepsilon = \frac{I_{st} - I_{Bg}}{A_{st} * p_{\beta}}$$

Depends on layer thickness, composition, source/sample distribution on plate

Saturation layer thickness:

$$f_{cal} = \frac{(I_{st} - I_{Bg})}{A_m}$$

$$A_m \quad \text{Bq/g}$$

Calculation of activity

$$A_{source} = \frac{i_{sample} - i_{BG}}{\epsilon * p_{\beta}}$$

$$A_{msource} = \frac{i_{sample} - i_{BG}}{f_{cal}} \quad \text{Bq/g}$$

Corrections

- Decay
 - Calibration source/tracer
 - Reporting result to a reference date

$$A = A_0 e^{-\lambda * \Delta t}; \lambda = \frac{\ln 2}{t_{1/2}}$$

- Decay/ingrowth during counting

$$i_0 = i_c * \frac{1 - e^{-\lambda * t_c}}{\lambda * t_c};$$

- Recovery

Crosstalk Spillover

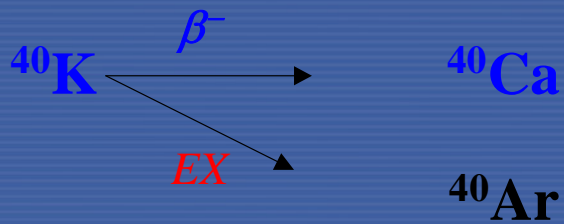
$$X_{\alpha \rightarrow \beta} = \frac{i_{\alpha \text{in} \beta}}{i_{\alpha \text{in} \beta} + i_{\alpha \text{in} \alpha}}$$

$$X_{\beta \rightarrow \alpha} = \frac{i_{\beta \text{in} \alpha}}{i_{\beta \text{in} \alpha} + i_{\beta \text{in} \beta}}$$

$$i_{\alpha_c} = \frac{i_{\alpha} - i_{\alpha} * X_{\beta \rightarrow \alpha} - i_{\beta} * X_{\beta \rightarrow \alpha}}{1 - X_{\beta \rightarrow \alpha} - X_{\alpha \rightarrow \beta}}$$

$$i_{\beta_c} = \frac{i_{\beta} - i_{\beta} * X_{\alpha \rightarrow \beta} - i_{\alpha} * X_{\alpha \rightarrow \beta}}{1 - X_{\beta \rightarrow \alpha} - X_{\alpha \rightarrow \beta}}$$

^{40}K



$t_{1/2}$: 1.277E9 Y

$E_{\beta\text{MAX}}$: 1.311 MeV
(89.3%)

E_{γ} : 1460.8 keV
(10.7%)

Isotopic abundance: 0.000117

A_m : 30.9 Bq/g K



IAEA

Atoms for Peace: The First Half Century

1957-2007

Calculation of uncertainties 1

Approach 1

The combined uncertainties were obtained from the components as using the

$$u_{A \pm B} = \sqrt{u_A^2 + u_B^2}, \quad u_{A * B} = A * B \sqrt{\frac{u_A^2}{A^2} + \frac{u_B^2}{B^2}} \quad \text{and} \quad u_{A/B} = \frac{A}{B} \sqrt{\frac{u_A^2}{A^2} + \frac{u_B^2}{B^2}} \quad \text{and}$$

$u_{A_0 * e^{\lambda * t}} = e^{\lambda * t} \sqrt{u_{A_0}^2 + t^2 u_{\lambda}^2 + \lambda^2 * u_t^2}$, $\lambda = \ln 2 / t_{1/2}$, formulae, breaking the used to formulae for calculation of the activity concentration to expressions covered by one of the ones above.

Calculation of uncertainties 2

Using the partial derivatives method

$$SF = (\delta y / \delta x_i), \quad u_y = \sqrt{\sum SF_i^2 \cdot u_i^2}$$

Analysis and evaluation of uncertainty sources:

$$\text{Contribution, \%} : [(\delta \varepsilon / \delta x_i)^2 \cdot u_{x_i}^2 \cdot 100] / u_\varepsilon^2$$



IAEA

Atoms for Peace: The First Half Century

1957–2007

Calculation of uncertainties 3

- using the spreadsheet (Kragten) method

Quantulus CAL2-05/1										
Table 1 Spreadsheet Method for Uncertainty Calculation in the Efficiency, Calibration of Quantulus for the Determination of ²¹⁰ Pb										
Parameter x _i	Unit	t _{s,CAL} min	m _{mat} g	m _{mat+cont.sol} g	C _{Pb} g/g	m _{mat} g	m _{mat+standard} g	A _p ²¹⁰ Pb -	f _{gravimetry} -	m _{filter} g
Value x _i		60	14.9364	16.03654	0.0274	16.03672	17.1326	12.45	0.70185	0.03654
u _{x_i}		0	0.00010	0.00010	0.000020565	0.00010	0.00010	0.26	0.00041	0.00010
Parameter x _i										
m _{mat}	14.93635		14.93645	14.93635	14.93635	14.93635	14.93635	14.93635	14.93635	14.93635
m _{mat+cont.sol}	16.03654		16.03654	16.03654	16.03654	16.03654	16.03654	16.03654	16.03654	16.03654
C _{Pb}	0.0274		0.0274	0.0274	0.0274	0.0274	0.0274	0.0274	0.0274	0.0274
m _{mat}	16.03672		16.03672	16.03672	16.03672	16.03672	16.03672	16.03672	16.03672	16.03672
m _{mat+standard}	17.13260		17.13260	17.13260	17.13260	17.13260	17.13260	17.13260	17.13260	17.13260
A _p ²¹⁰ Pb	12.4500		12.4500	12.4500	12.4500	12.4500	12.4500	12.7100	12.4500	12.4500
f _{gravimetry}	0.70185		0.70185	0.70185	0.70185	0.70185	0.70185	0.70185	0.70226	0.70185
m _{filter}	0.03654		0.03654	0.03654	0.03654	0.03654	0.03654	0.03654	0.03654	0.03654
m _{filter+Pb(C2O4)}	0.07377		0.07377	0.07377	0.07377	0.07377	0.07377	0.07377	0.07377	0.07377
t _{CAL}	349.654		349.654	349.654	349.654	349.654	349.654	349.654	349.654	349.654
t _{ABS}	1.772		1.772	1.772	1.772	1.772	1.772	1.772	1.772	1.772
t _{CAL}	24.957		24.957	24.957	24.957	24.957	24.957	24.957	24.957	24.957
t _{ABS}	0.703		0.703	0.703	0.703	0.703	0.703	0.703	0.703	0.703
t _{ABS}	1.049		1.049	1.049	1.049	1.049	1.049	1.049	1.049	1.049
t	391564800		391564800	391564800	391564800	391564800	391564800	391564800	391564800	391564800
λ ²¹⁰ Pb	9.85E-10		9.85E-10	9.85E-10	9.85E-10	9.85E-10	9.85E-10	9.85E-10	9.85E-10	9.85E-10
ε _{Pb-210}	0.669		0.669	0.669	0.669	0.669	0.669	0.665	0.668	0.671
u _y Kragten	0.01511									
u _y parc. Der.	0.01537									
		ε _{1,Pb} - ε _{Pb}	-6.078E-05	6.078E-05	5.016E-04	6.103E-05	-6.102E-05	-1.368E-02	-3.904E-04	1.801E-03
Σ(ε _{1,Pb} - ε _{Pb}) ²	2.283E-04	(ε _{1,Pb} - ε _{Pb}) ²	3.695E-09	3.695E-09	2.516E-07	3.725E-09	3.723E-09	1.871E-04	1.524E-07	3.244E-06
u _y /ε, %	2.26	(ε _{1,Pb} - ε _{Pb}) ²	3.69E-09	3.69E-09	2.52E-07	3.72E-09	3.72E-09	1.95E-04	1.53E-07	3.23E-06
SF by Kragten	δe/δx _i		-0.6078	0.6078	24.3888	0.6103	-0.6102	-0.0526	-0.9523	18.0108
SF by Parc. Deriv.	δe/δx _i		-0.608	-0.608	24.389	0.610	-0.6102	-0.0537	-0.9528	17.96244
Contribution, %	Kragten		1.62E-03	1.62E-03	0.11	1.63E-03	1.63E-03	81.96	0.07	1.42
Contribution, %	parc. Der.		1.56E-03	1.56E-03	0.11	1.58E-03	1.58E-03	82.57	0.06	1.37
Contribution, % =	[(δe/δx _i) ² · u _{x_i} ² · 100] / u _y ²									



IAEA

Atoms for Peace: The First Half Century

1957-2007