

# *Monte Carlo simulations for brachytherapy*

D.W.O. Rogers

Carleton Laboratory for  
Radiotherapy Physics.  
Physics Dept,  
Carleton University  
Ottawa, Canada



<http://www.physics.carleton.ca/~drogers>  
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# Brachytherapy

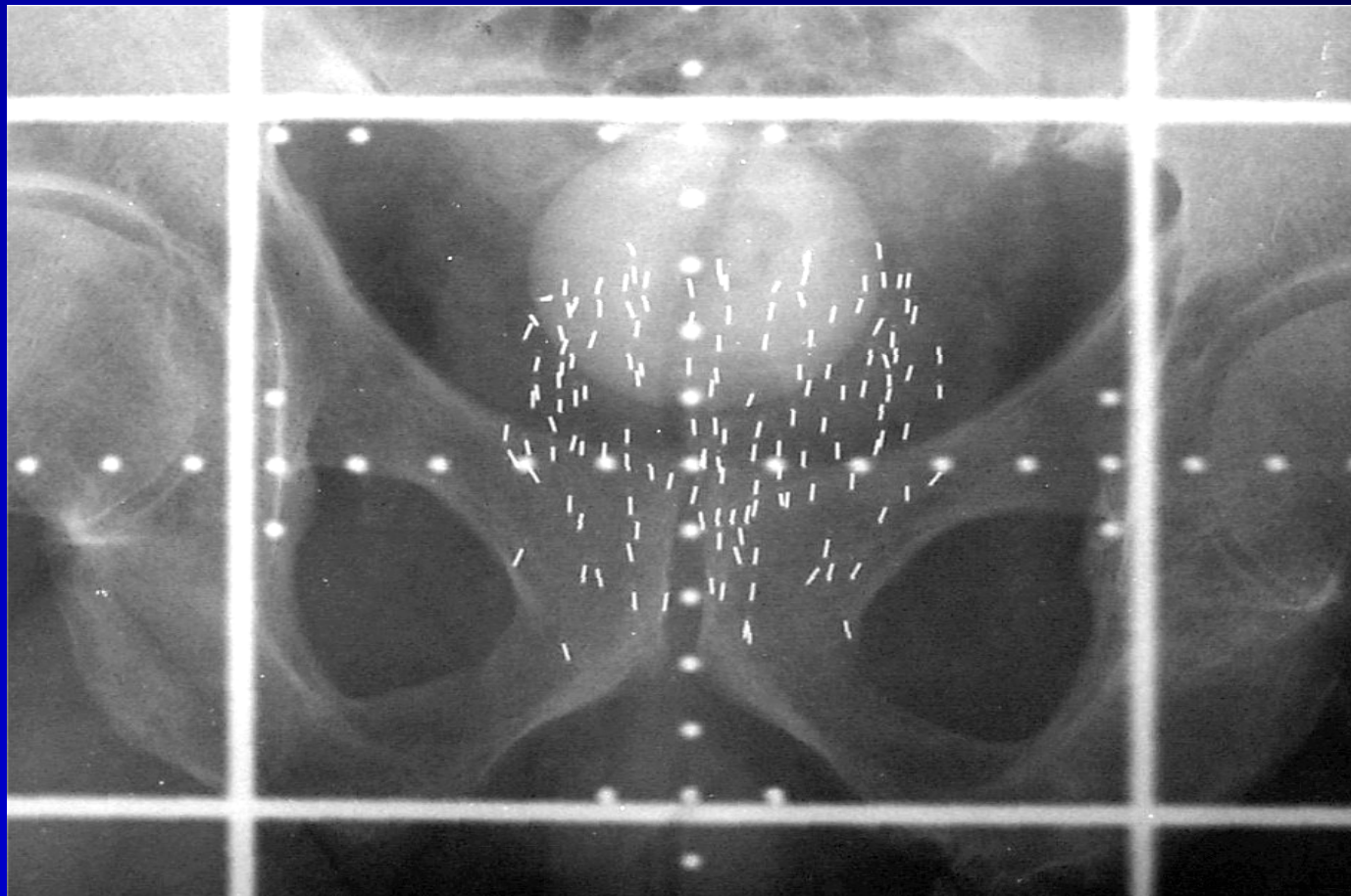
Radiation *therapy given at a short distance*

- Radioactive seeds or sources implanted either permanently or temporarily *inside* tumours
- Commonly used for prostate, breast, cervical and ocular cancers.



# *Typical Prostate Implant*

Prostate implant of  $\sim 150$   $^{125}\text{I}$  brachytherapy seeds



# Characteristics of isotopes used in brachytherapy

missing  
Cs-131  
Yb-169

Isotope	Average <sup>(a)</sup> photon energy (MeV)	Half-life	HVL in lead (mm)	$\Gamma_{AKR}$ <sup>(b,d)</sup> $\left( \frac{\mu\text{Gy} \cdot \text{m}^2}{\text{GBq} \cdot \text{h}} \right)$	$\Lambda$ <sup>(c,d)</sup> $\left( \frac{\text{cGy} \cdot \text{h}^{-1}}{\text{cGy} \cdot \text{cm}^2 \cdot \text{h}^{-1}} \right)$
Co-60	1.25	5.26 yr	11	309	1.11
Cs-137	0.66	30 yr	6.5	77.3	1.11
Au-198	0.41	2.7 d	2.5	56.2	1.13
Ir-192	0.38	73.8 d	3	108	1.12
I-125	0.028	60 d	0.02	-	-0.92-1.012
Pd-103	0.021	17 d	0.01	-	-0.63- 0.69

(a) These are only approximate values, depending on source make and filtration

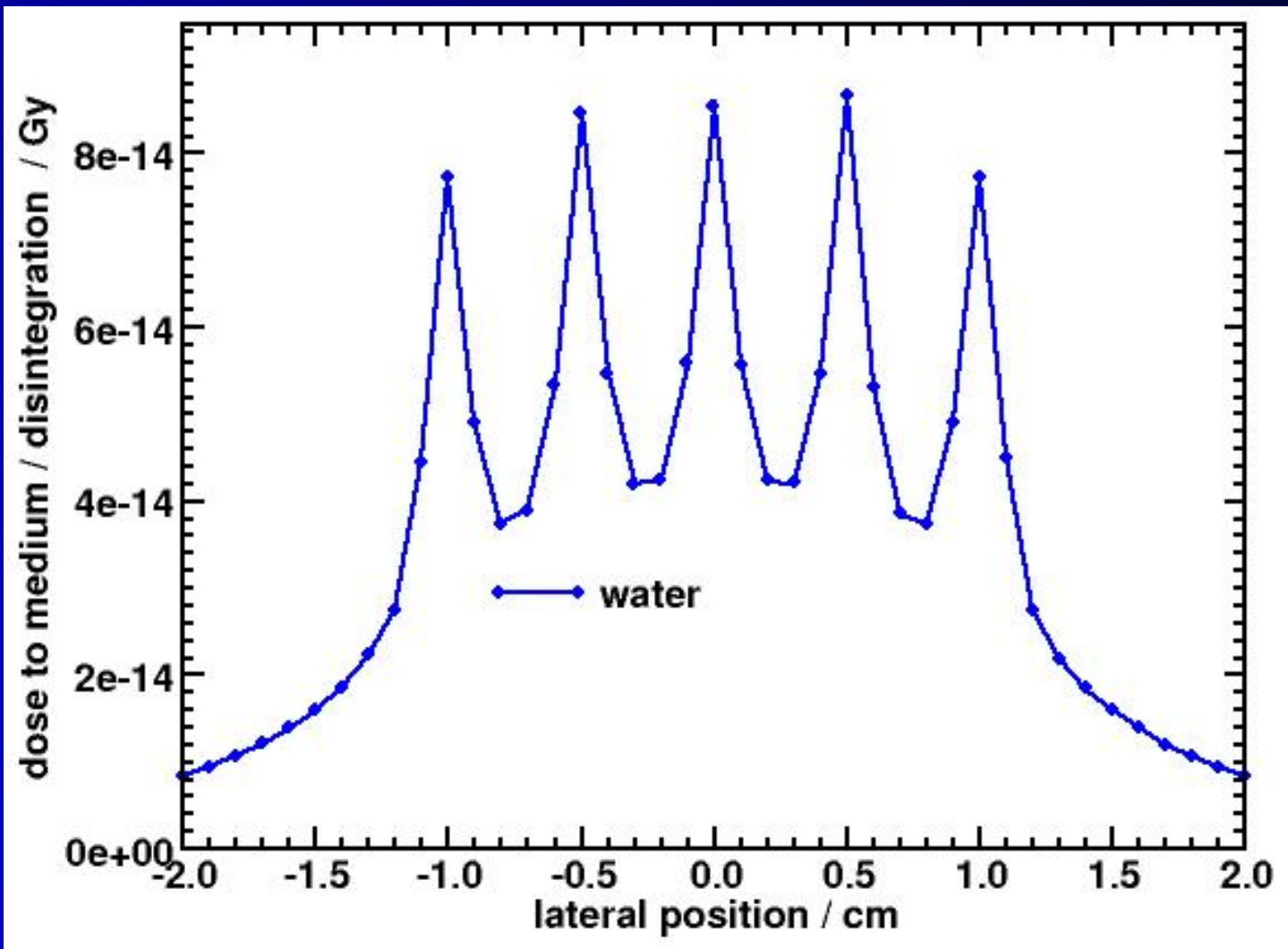
(b)  $\Gamma_{AKR}$  is the air-kerma rate constant

(c)  $\Lambda$  is the dose rate constant.

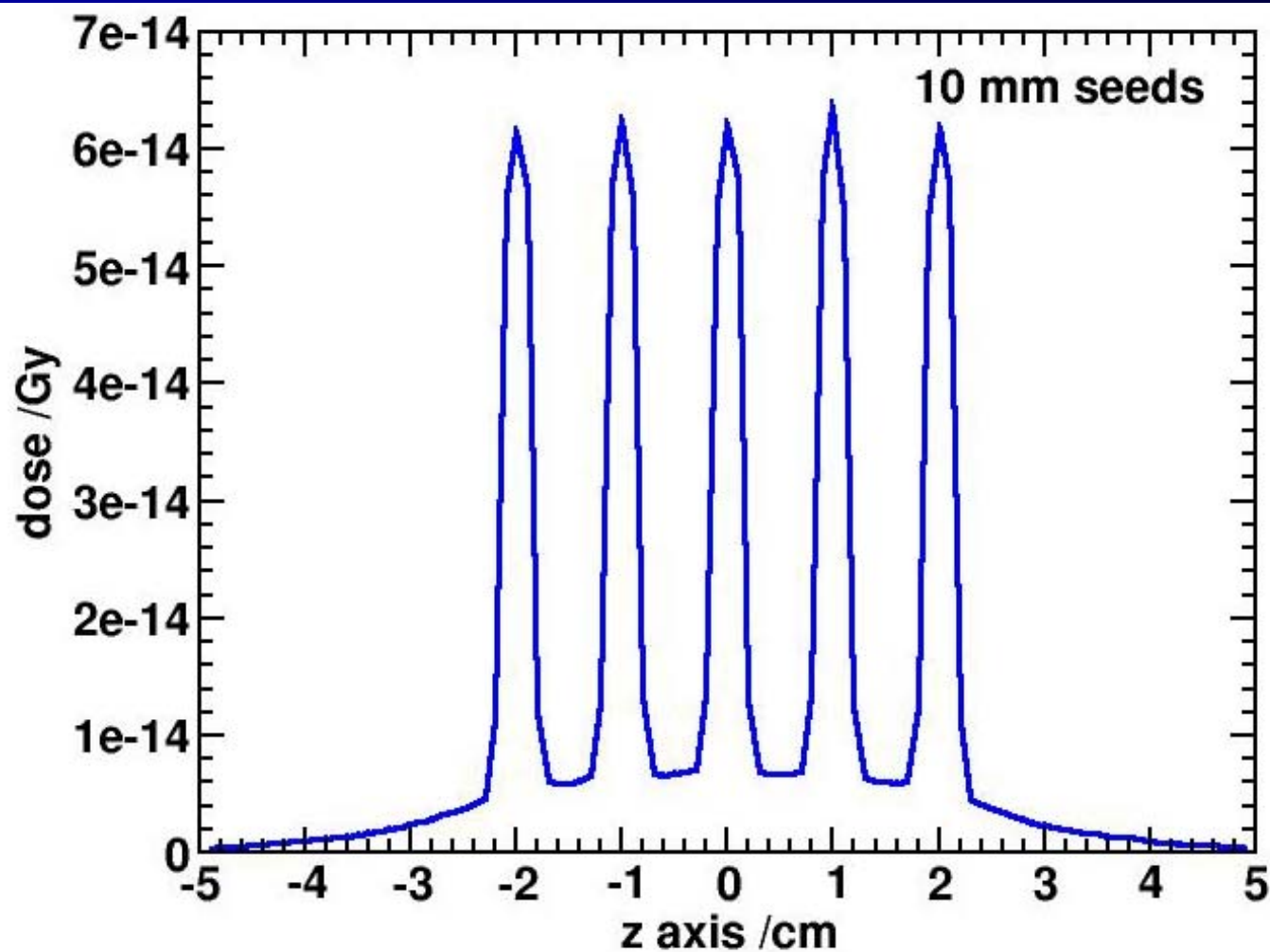
(d) Using generic values of the air-kerma rate constant or dose rate constant for low energy photon source may lead to substantial errors in the dose calculations. They are therefore not given here for iodine-125 and palladium-103.



## *I-125 seeds cause hot spots*



*10 mm spacing  $\Rightarrow$  9 to 1 ratio*

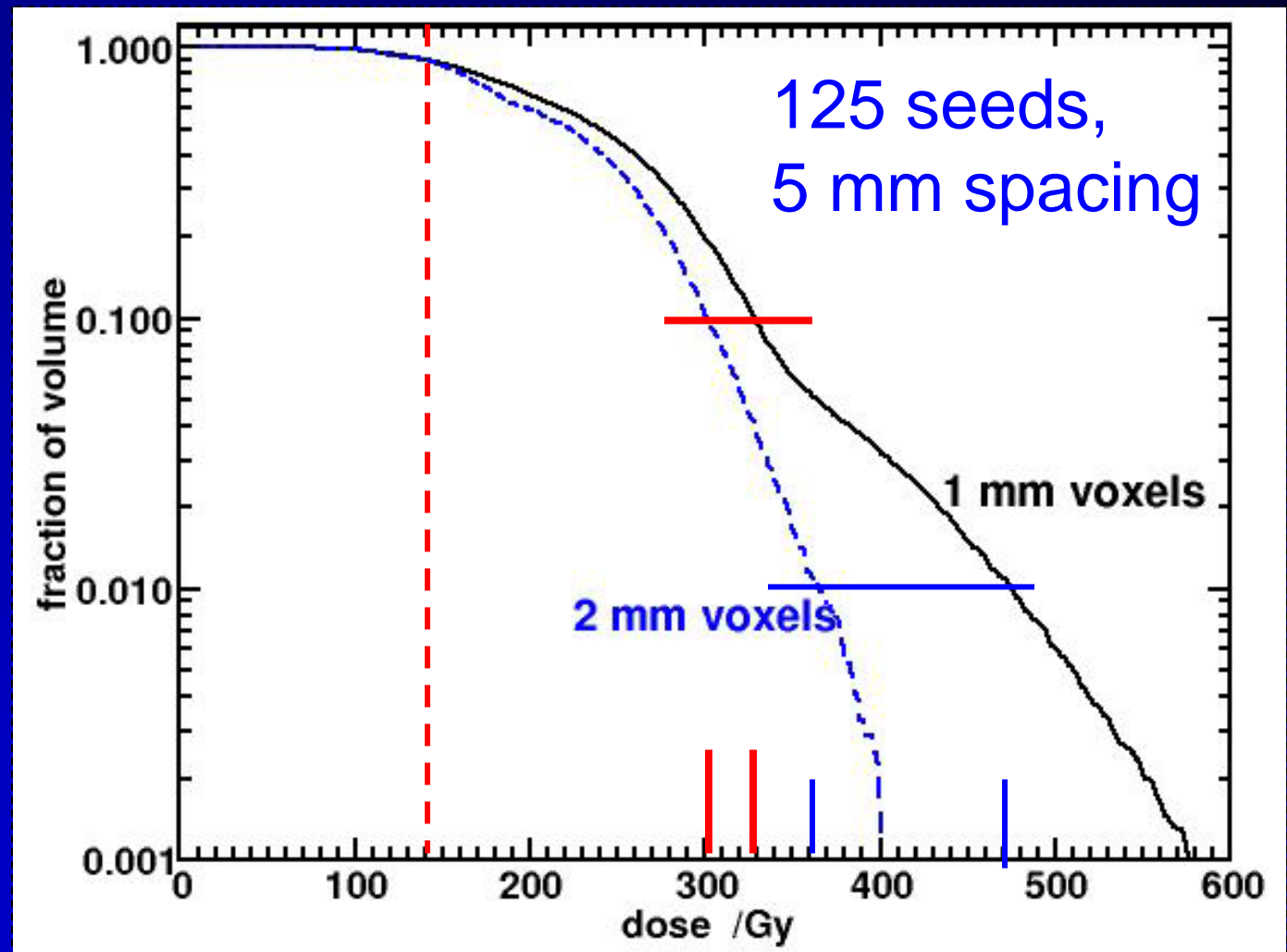


*90% of volume receives > 140 Gy*

## DVH

dose volume  
histogram

fraction of  
volume of  
interest  
(eg prostate)  
receiving  
at least the  
dose on the x-  
axis



# *Large variety of seeds (4-5mm overall)*

$^{125}\text{I}$



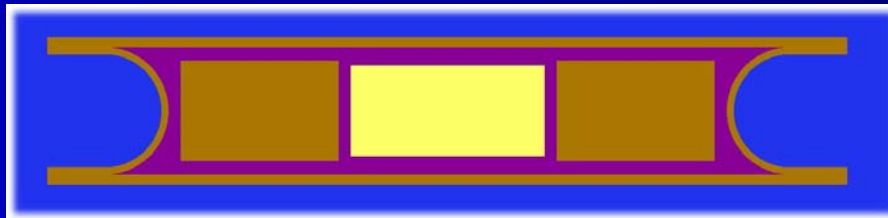
Amersham 6711

$^{103}\text{Pd}$



Best 2335

$^{103}\text{Pd}$



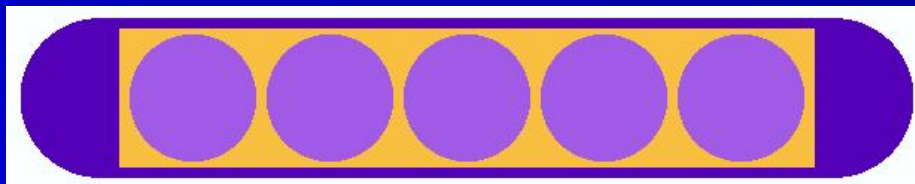
Theragenics 200

$^{125}\text{I}$



Source Tech  
Medical STM125I

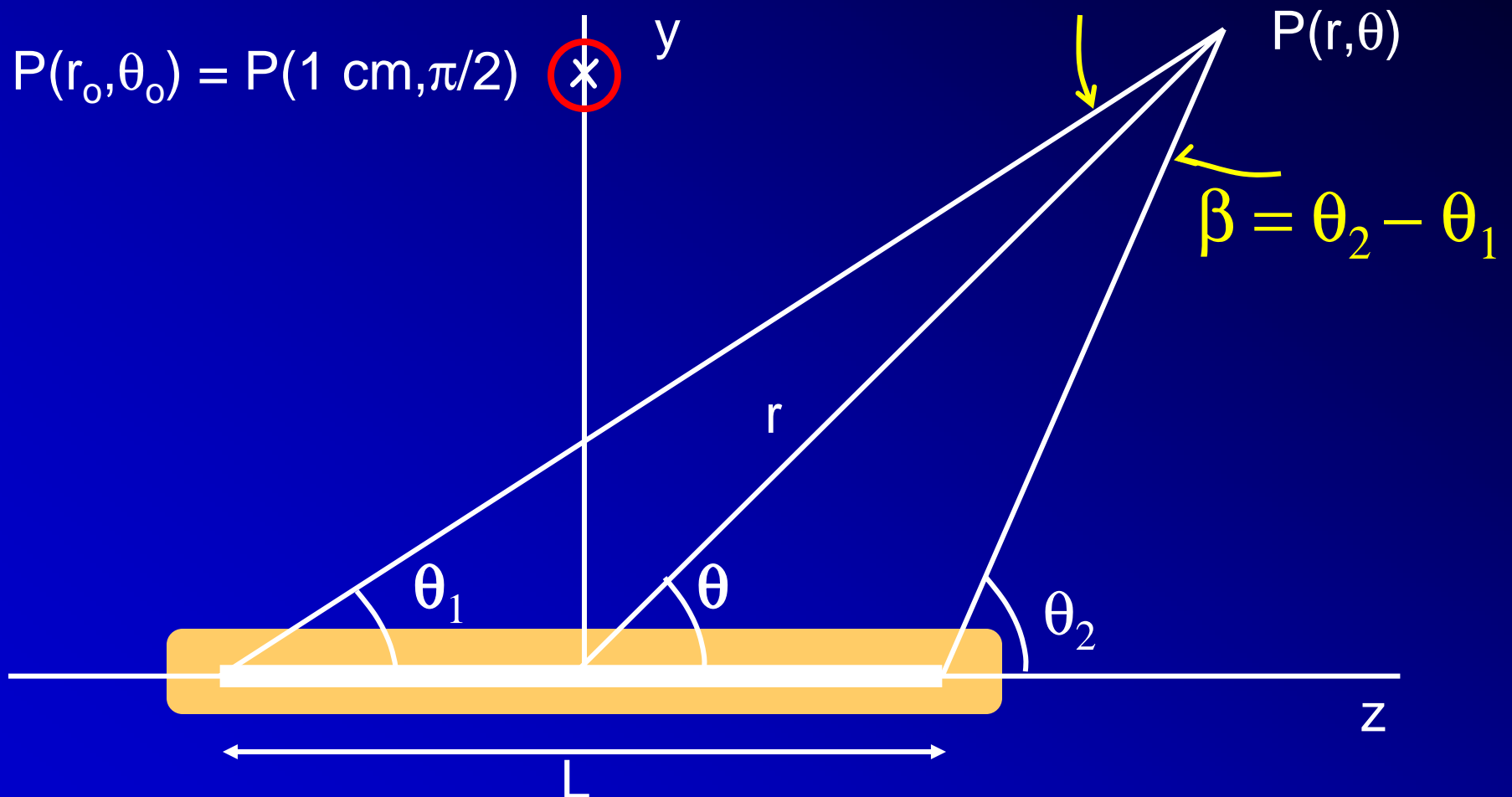
$^{125}\text{I}$



Imagyn  
isoStar 12501



# *TG-43 coordinate system for calculations*



# What are pure geometry effects?

- Consider the source in vacuum. What is the fluence of particles at  $(r, \theta)$ ?  
just  $1/r^2$

$$G_X(r, \theta) = \frac{\int_V \frac{\rho(\vec{r}')}{|\vec{r} - \vec{r}'|^2} dV'}{\int_V \rho(\vec{r}') dV'}$$

- for a point source

$$G_p(r, \theta) = \frac{1}{r^2}$$

- for a line source

$$G_l(r, \theta) = \begin{cases} 1/(r^2 - L^2/4) & \theta = 0 \\ \beta/Lr \sin \theta & \text{if } \theta \neq 0 \end{cases}$$

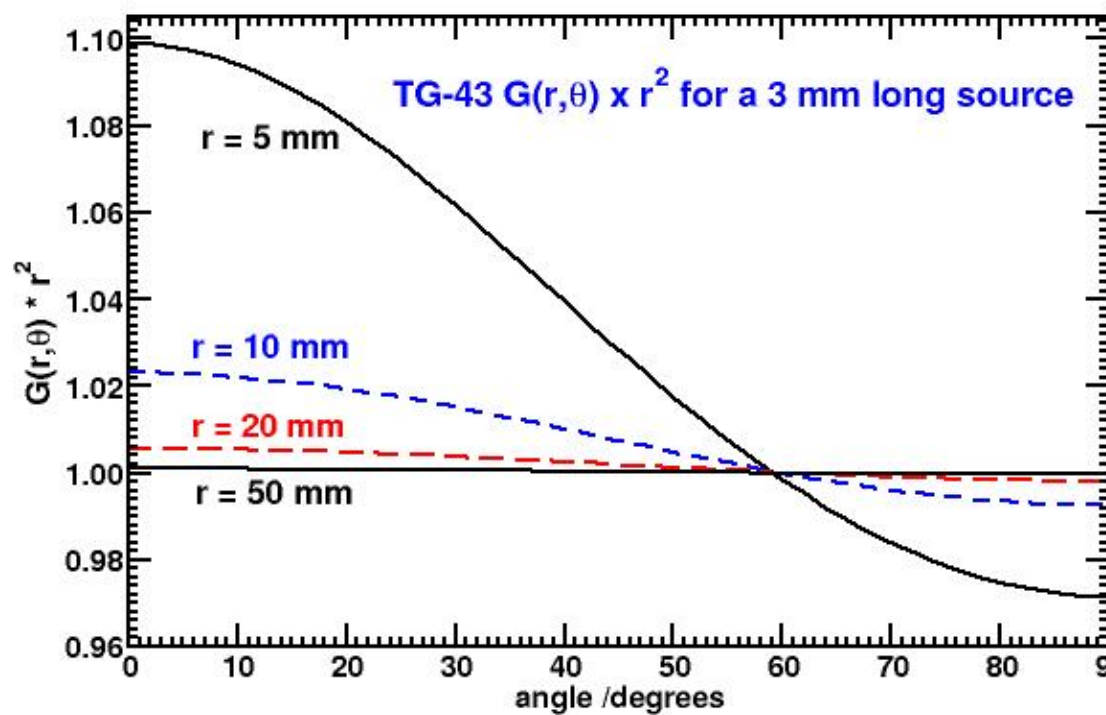
$$\beta = \theta_2 - \theta_1 = \tan^{-1} \left( \frac{r \sin \theta}{r \cos \theta - L/2} \right) - \tan^{-1} \left( \frac{r \sin \theta}{r \cos \theta + L/2} \right)$$

or

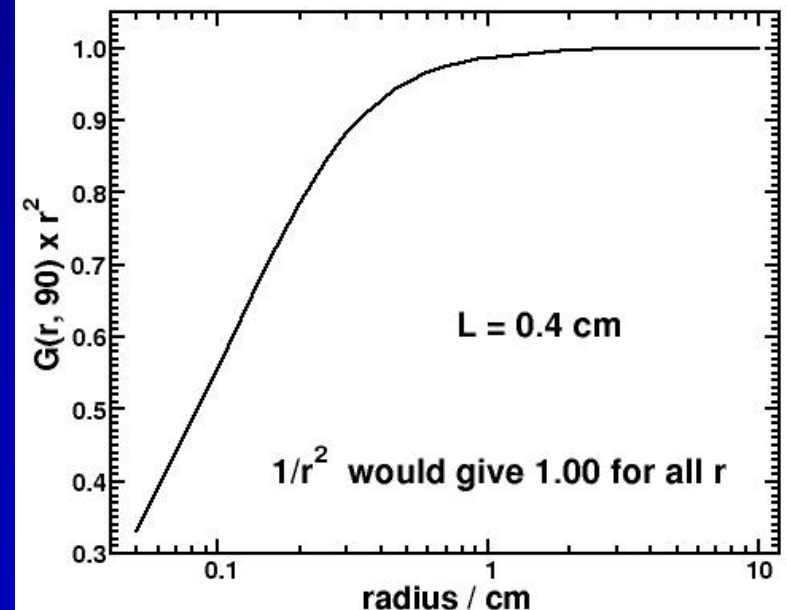
(faster)

$$\beta = \begin{cases} \tan^{-1} \left( \frac{Lr \sin \theta}{r^2 - L^2/4} \right) & r > L/2 \\ \tan^{-1} \left( \frac{Lr \sin \theta}{r^2 - L^2/4} \right) + \pi & r < L/2 \\ \pi/2 & r = L/2 \end{cases}$$

# How big is the geometry factor?



Pure  $1/r^2$  would be unity in both plots



TG43

$$\dot{D}(r, \theta) = S_k \cdot \Lambda \cdot \frac{G(r, \theta)}{G(r_o, \theta_o)} \cdot g(r) \cdot F(r, \theta)$$

## Air-kerma strength

$$S_K = \dot{K}_\delta(d) d^2$$

$$1\text{U} = 1\text{mGy m}^2\text{h}^{-1} = 1\text{ cGy cm}^2\text{h}^{-1}$$

$$\dot{K}_\delta(d)$$

-the air kerma rate at distance d

-in vacuum (i.e., no air attenuation or scatter)

-for photons  $> \delta$  (no effect on dose

but has effect on K, typically 5 keV)

$S_K$  is defined to be independent of d (for  $d \gg L$ ).

Numerically = **reference air kerma rate** of ICRU 38/60

This is a **measured quantity**.

TG43

$$\dot{D}(r, \theta) = S_k \cdot \Lambda \cdot \frac{G(r, \theta)}{G(r_o, \theta_o)} \cdot g(r) \cdot F(r, \theta)$$

## Dose-rate constant (DRC)

$$\Lambda = \frac{\dot{D}(r_o, \theta_o)}{S_K}$$

$$r_o = 1 \text{ cm}, \theta_o = 90^\circ$$

$$\text{cGyh}^{-1}/\text{U} = \text{cm}^{-2}$$

depends on radionuclide & source model

DRCs are measured or **calculated by Monte Carlo**



TG43

$$\dot{D}(r, \theta) = S_k \cdot \Lambda \cdot \frac{G(r, \theta)}{G(r_o, \theta_o)} \cdot g(r) \cdot F(r, \theta)$$

## Radial dose function

$$g_X(r) = \frac{\dot{D}(r, \theta_0)}{\dot{D}(r_o, \theta_0)} \frac{G_X(r_o, \theta_0)}{G_X(r, \theta_0)}$$

X = P or L (point or line)       $g(r_o) = 1$

Aside from geometry ( $1/r^2$ ),  $g(r)$  accounts for  
dose fall off on transverse axis  
due to photon attenuation and scatter.

For a point source:

$$g_p(r) \equiv \frac{\dot{D}(r)r^2}{\dot{D}(r_o)r_o^2}$$

Radial dose functions are measured and  
calculated by Monte Carlo

TG43

$$\dot{D}(r, \theta) = S_k \cdot \Lambda \cdot \frac{G(r, \theta)}{G(r_o, \theta_o)} \cdot g(r) \cdot F(r, \theta)$$

## Dose anisotropy function

$$F(r, \theta) = \frac{\dot{D}(r, \theta)}{\dot{D}(r, \theta_o)} \frac{G_L(r, \theta_o)}{G_L(r, \theta)}$$

$F(r, \theta)$  describes variation in dose vs polar angle relative to transverse plane (above  $G_L$  variations)

$$F(r, \theta_o) = 1.0$$

Dose anisotropy functions are mostly **calculated by Monte Carlo**

TG43

$$\dot{D}(r, \theta) = S_k \cdot \Lambda \cdot \frac{G(r, \theta)}{G(r_o, \theta_o)} \cdot g(r) \cdot F(r, \theta)$$

$$S_K \Lambda = D(r_o, \theta_o)$$

$$D(r_o, \theta_o) \cdot g(r) = D(r, \theta_o) \cdot \text{geom}$$

$$D(r, \theta_o) \cdot F(r, \theta) \cdot \text{geom} = D(r, \theta)$$

i.e. the TG-43 formalism is an identity,

- holds independently of what  $G(r, \theta)$  is.

Clinically, get measured  $S_k$  for your individual seeds  
and use Monte Carlo or measured values for

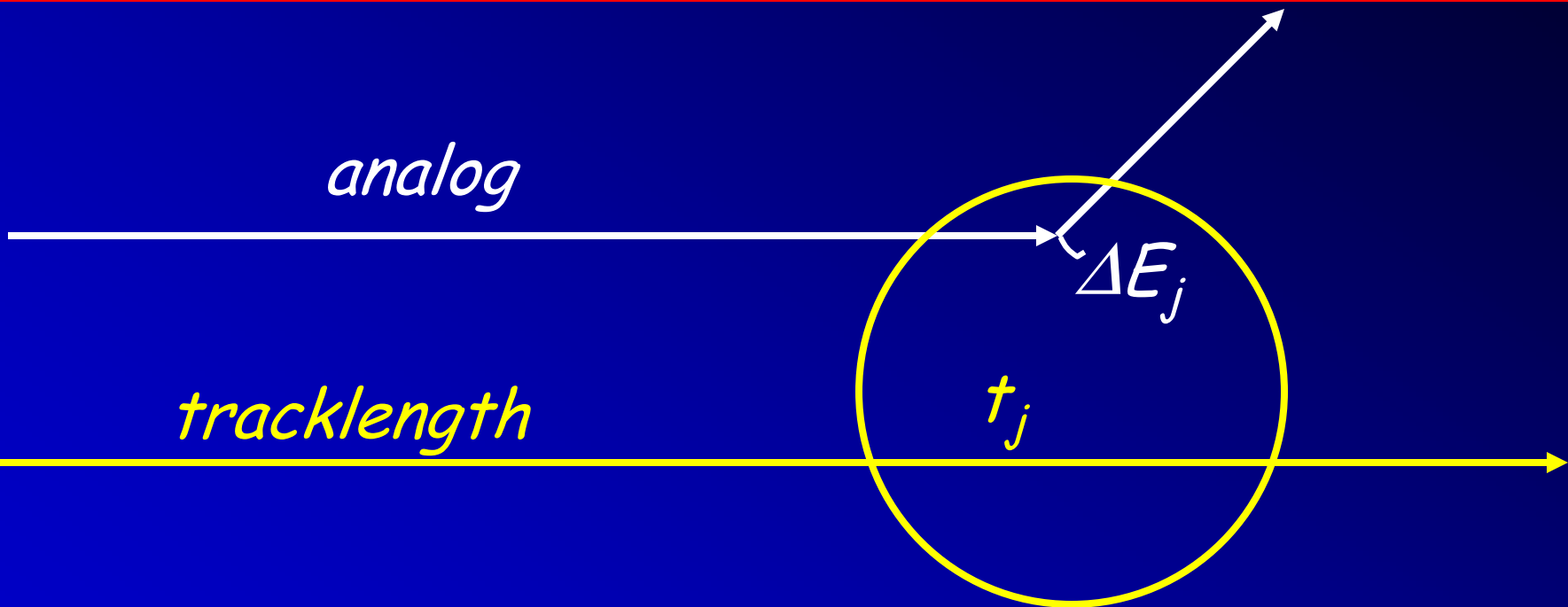
$\Lambda$ ,  $g(r)$ , and  $F(r, \theta)$

# Monte Carlo for TG43 parameters

- Jeffrey F Williamson - **PTRAN\_CCG**
  - this code is responsible for most of the published values (MCNP and EGS4/EGSnrc have also been used)
  - references at end
- Monte Carlo for brachytherapy is, in general a photon transport problem since so low in energy
- Dose = Kerma (strictly the collision kerma)

$$D_{\text{med}} \stackrel{\text{CPE}}{=} K_{\text{col,med}} = E_{\gamma} \phi \left( \frac{\mu_{\text{en}}}{\rho} \right)_{\text{med}}$$

# Kerma estimators





# Kerma estimators

- Analog estimator  $K_i = \frac{1}{m_i} \sum_j \Delta E_j$    
 i-th region   
 j-th interaction region i

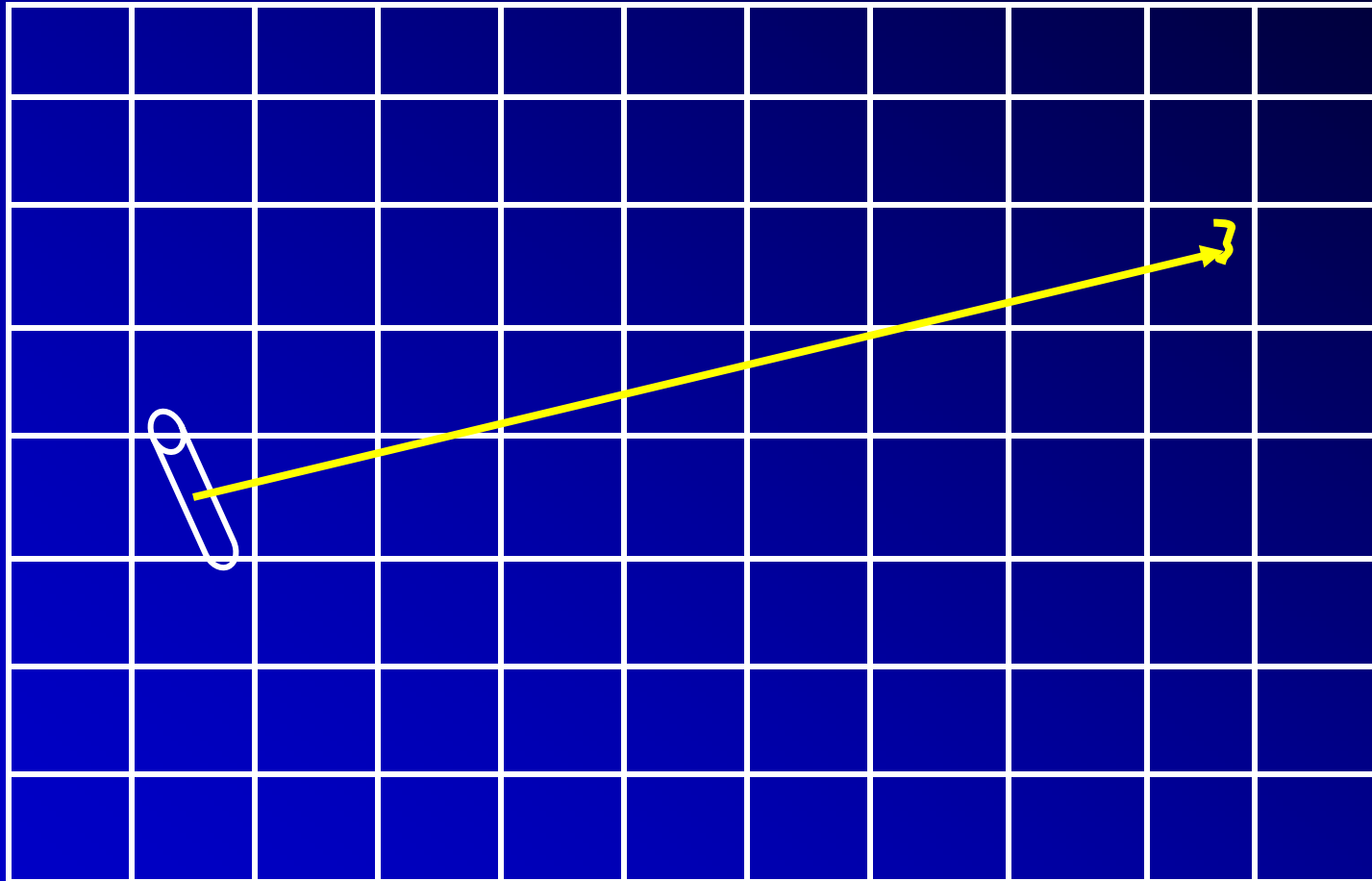
- Tracklength estimator  $K_i = \frac{1}{V_i} \sum_j E_j t_j \left( \frac{\mu_{en}}{\rho} \right)_j$

-uses relationships between fluence  $\phi$  and total tracklength per unit volume  $\phi = \frac{1}{V} \sum_j t_j$    
  $t_j$  tracklengths in i-th region

and between kerma and fluence  $K_{col,med} = E_\gamma \phi \left( \frac{\mu_{en}}{\rho} \right)_{med}$

Tracklength estimator: much more efficient - it uses all paths through a volume, not just interactions in it

# *Analog vs pathlength estimators*



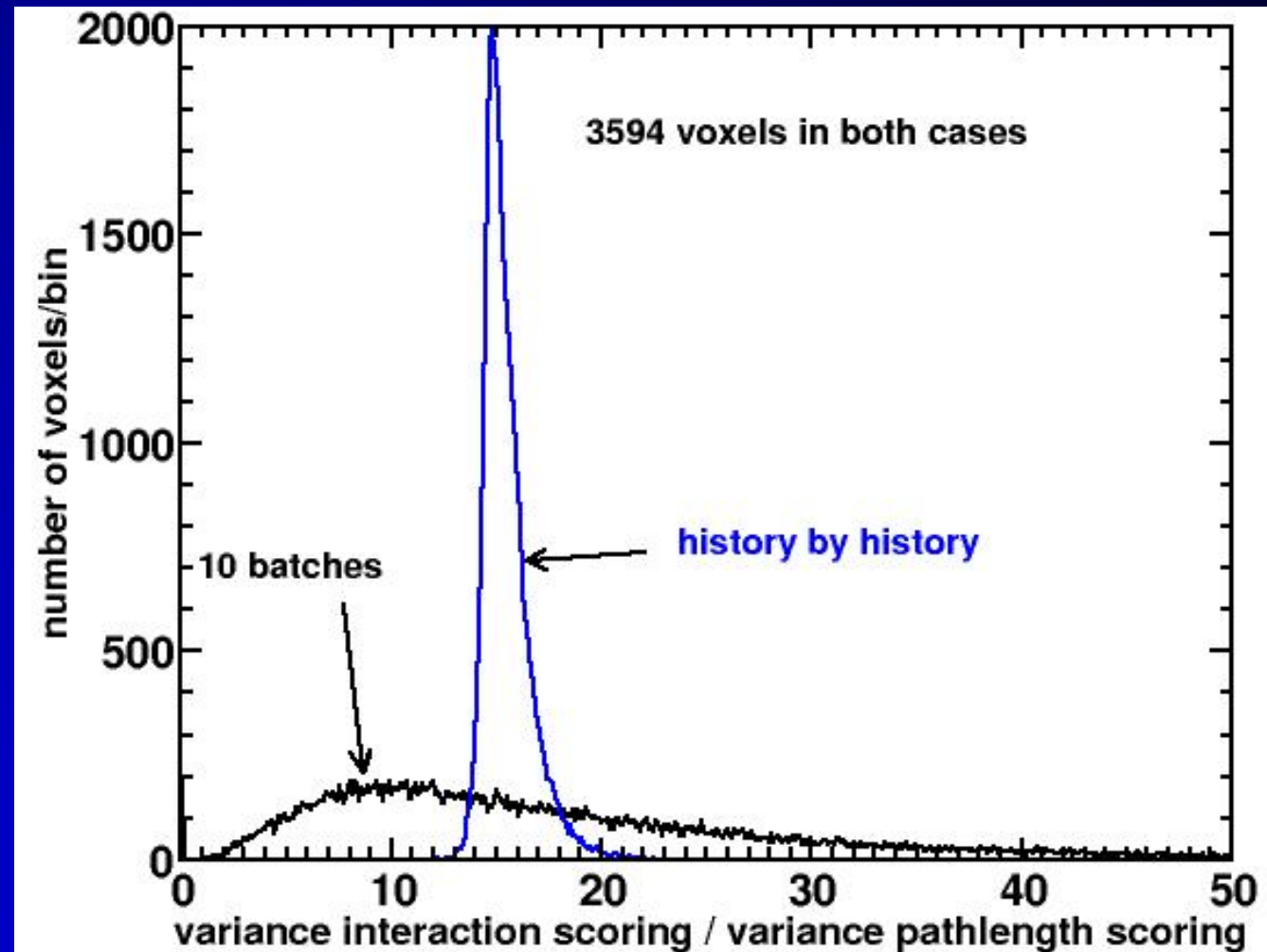
analog estimator (interaction) contributes to 1 voxel  
pathlength estimator contributes to 11 voxels

# *Efficiency increase from tracklength estimator*

125 <sup>125</sup>I seeds,  
5 mm spacing  
2 mm voxels

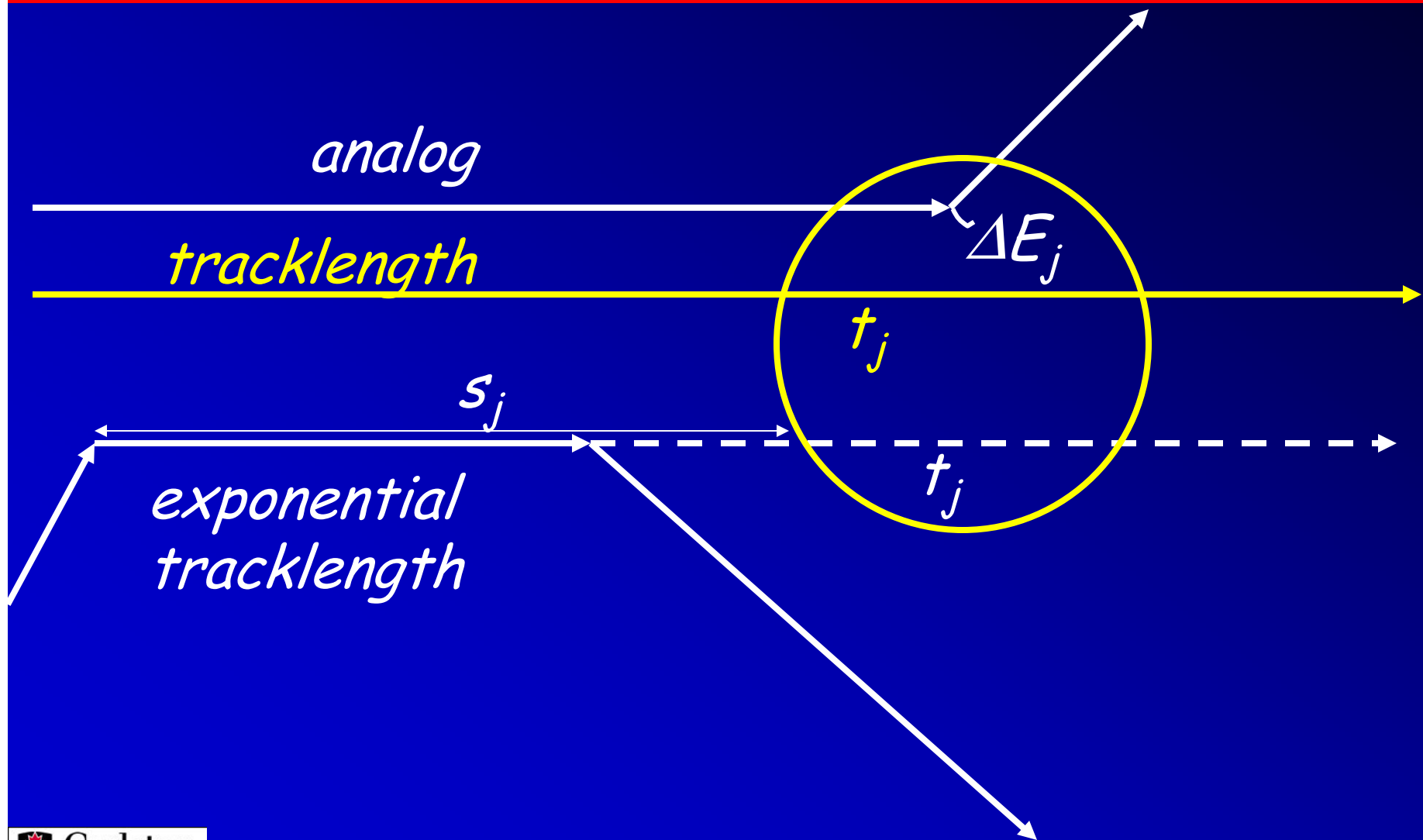
CPU time same

BrachyDose  
code



use history by history scoring

# Kerma estimators



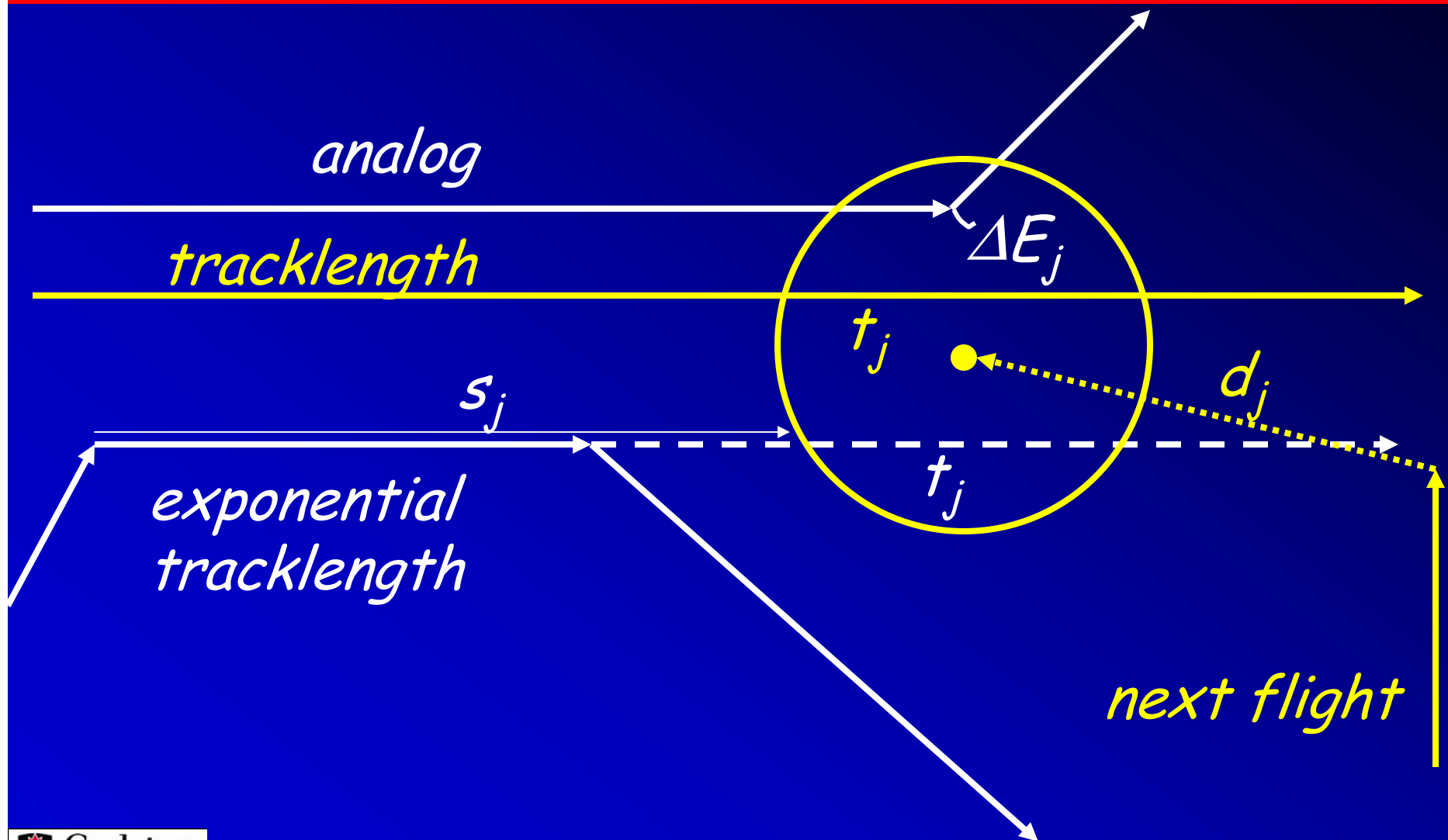
# Exponential tracklength estimator

$$K_i = \frac{1}{m_i} \sum_j E_j \left( \frac{\mu_{en}}{\mu} \right) e^{-\mu s_j} (1 - e^{-\mu t_j})$$

- tracklength estimator scores for every track which actually crosses the region
- exponential tracklength estimator scores on every track which would have crossed the region
- if interaction in or past volume  $s_j = 0 \Rightarrow e^{-\mu s_j} = 1.0$
- 'thin voxel'  $\Rightarrow \mu t_j \ll 1 \Rightarrow (1 - e^{-\mu t_j}) \approx \mu t_j$
- for interaction in a thin voxel, same as tracklength estimator



# Next flight estimators



## Next flight estimators (cont)

$$K = \frac{\sum_i E(\theta_i) P(\theta_i | E_{i-1}) e^{-\mu d_i} \left( \frac{\mu_{en}}{\rho} \right)}{d_i^2}$$

Estimates the **kerma at a point** - previous are **voxel averages**

At each interaction, determine angle,  $\theta_i$ , **to point of interest** & **probability per unit solid angle** of a photon of energy  $E_{i-1}$  scattering to that direction. Energy-angle relationship  $\Rightarrow E(\theta_i)$

$$P(\theta_i | E_{i-1}) = \frac{\frac{d\sigma}{d\Omega}(\theta_i, E_{i-1})}{\sigma}$$

**Problem:** interactions for which  $d_i$  near 0

**$\Rightarrow$  large fluctuations**

# *Bounded next flight (BNF) estimators*

Consider a sphere of radius  $R$  around point of interest

$d_i < R$

$$K = \frac{\sum_i 3E(\theta_i)P(\theta_i|E_{i-1}) \left(1 - e^{-\mu R}\right) \left(\frac{\mu_{en}}{\rho}\right)}{\mu R^3}$$

$d_i > R$

$$K = \frac{\sum_i E(\theta_i)P(\theta_i|E_{i-1})e^{-\mu d_i} \left(\frac{\mu_{en}}{\rho}\right)}{d_i^2}$$

where we have replaced  $e^{-\mu d}/d^2$  with its mean value within  $R$ , assuming there are **uniform interactions within  $R$** .

**This is the workhorse method used in Williamson's code for TG43 parameters.**

# *Once more collided flux estimators (OMCFE)*

- **BNF** requires uniform interactions within  $R$ 
  - does not work **close to small sources** with steep gradients
  - does not work **near interfaces**
- **OMCFE** is basically a **next flight estimator**
  - resamples a step if it ends within  $R$
  - changes the weight and then does next flight estimate for that collision
  - but tracks the history using the originally sample collision point

# *No photo-electric absorption*

- improve efficiency by not terminating histories via photo-electric events
  - sample distance to interaction from  $\sigma_+$
  - select interaction type ignoring  $\sigma_{pe}$
  - reduce weight = probability particle has escaped a terminal event
$$W_i = W_{i-1} \left( 1 - \frac{\sigma_{pe}(E_{i-1})}{\sigma_t(E_{i-1})} \right)$$
  - energy deposition
$$\Delta E = W_{i-1}E_{i-1} - W_iE_i$$
    - consider compton scatter
$$E_i \approx E_{i-1} \Rightarrow \Delta E = W_{i-1}E_{i-1} \frac{\sigma_{pe}}{\sigma_t}$$
  - other estimators, multiply by  $W_i$



# Calculating TG43 parameters: $S_K$

$K_{\text{air}}$  at 10 cm on the bisector, in vacuum

- issues
  - air attenuation or not? - definition is in vacuum
  - low energy (4.5 keV) Ti x-rays
    - no effect in water
    - large effect on  $K_{\text{air}}$  since  $(\mu_{\text{en}}/\rho)$  large at 5 keV
    - decision to exclude using thin Al sheet
  - on-axis or area of wide angle free air chamber (WAFAC)
    - definition, TLDs, clinical ion chambers all on-axis
    - primary standard is WAFAC

# Calculating TG43 parameters: $g(r), F(r, \theta)$

$K_{\text{water}}$  throughout the medium  $D(r, \theta)$

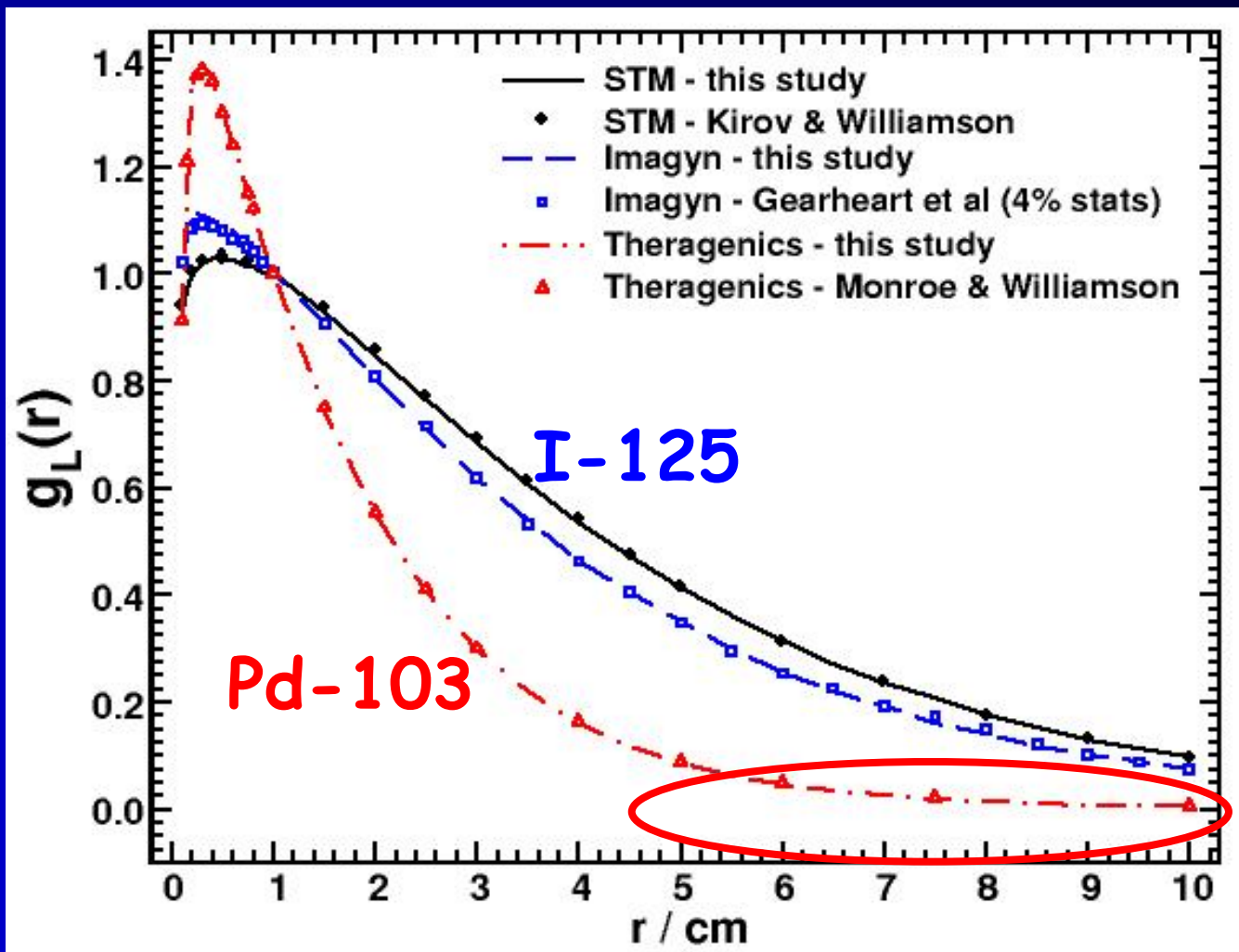
$$g_X(r) = \frac{\dot{D}(r, \theta_0)}{\dot{D}(r_0, \theta_0)} \frac{G_X(r_0, \theta_0)}{G_X(r, \theta_0)}$$

$$F(r, \theta) = \frac{\dot{D}(r, \theta)}{\dot{D}(r, \theta_0)} \frac{G_L(r, \theta_0)}{G_L(r, \theta)}$$

$$r_0 = 1 \text{ cm}, \theta_0 = 90^\circ$$

- issues
  - what  $G(r, \theta)$  to use: line or point: **consistency critical**
  - **voxel size effects** if using voxels
  - what is the **medium**?
    - water for the TG43 parameters (is this the best?)
    - experiments in plastics/"solid-virtual water" etc
  - **size of phantom** (must be big enough)

# $g(r)$ - radial dose function



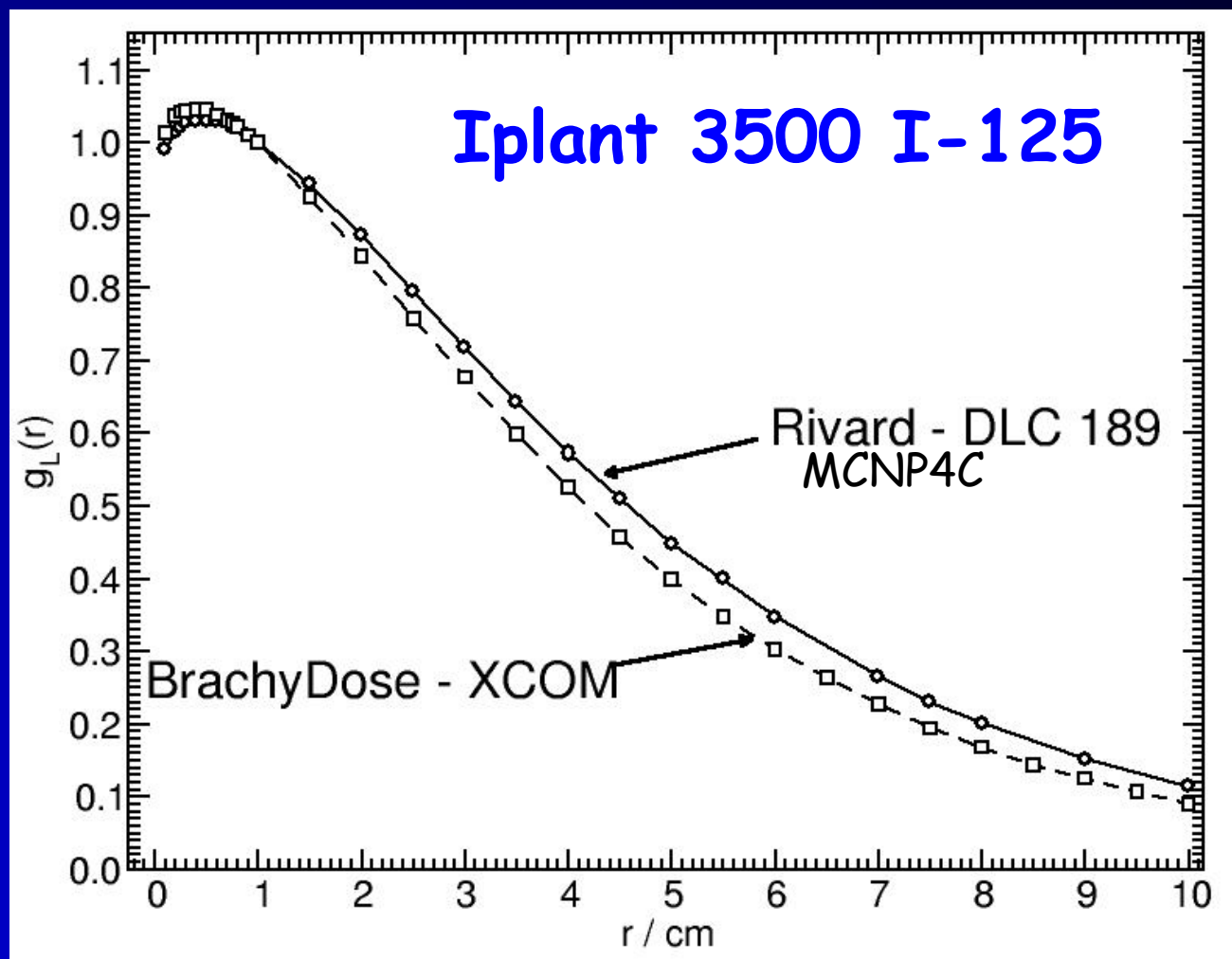
$\Delta =$   
3%, 6%,  
16%

# Effect of cross sections

DLC-189/200  
in MCNP4B/C

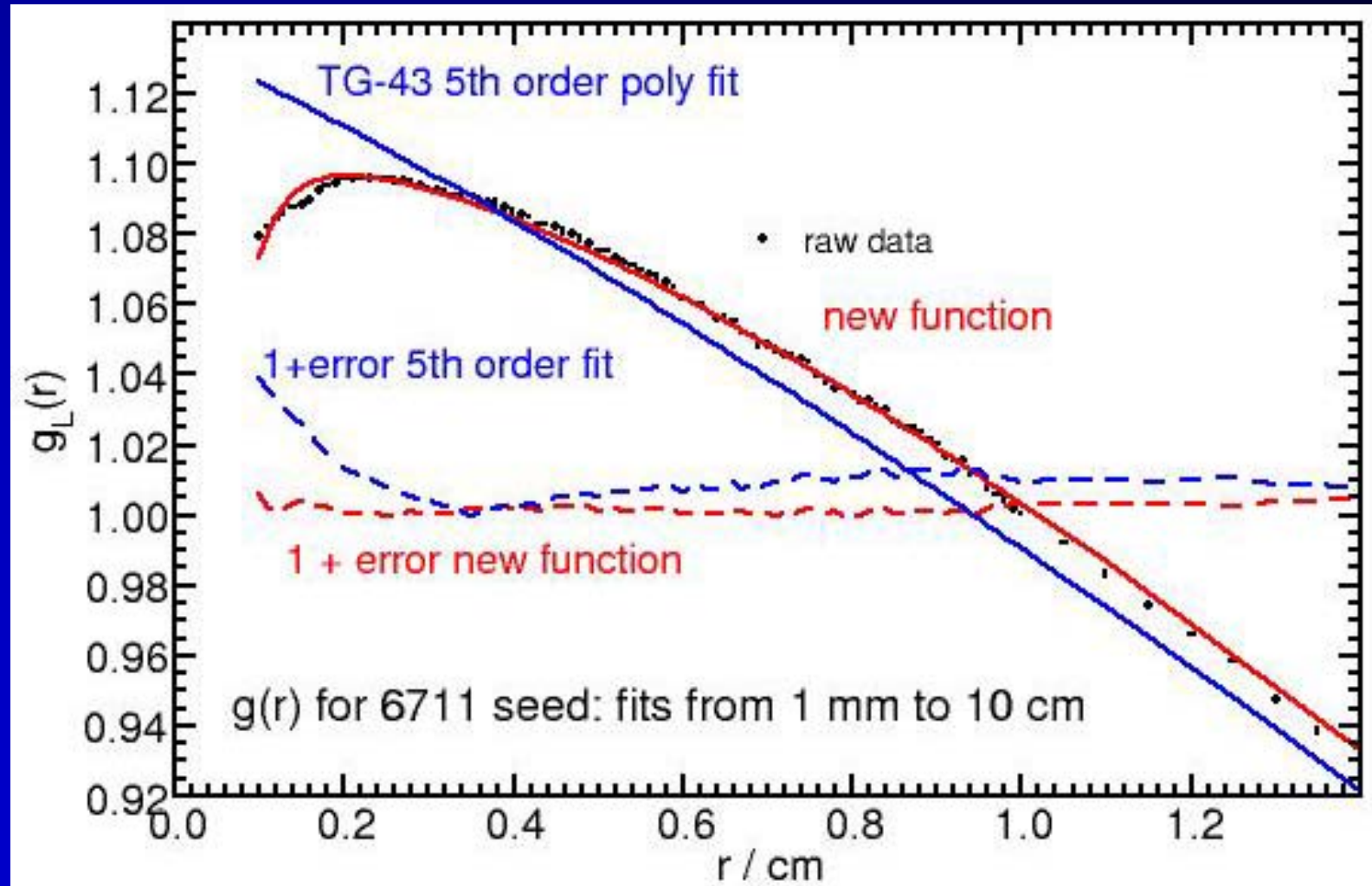
$\mu$  low by 5-6%  
DeMarco et al  
PMB 47 (2002)1321

XCOM  
considered  
state-of-art  
(DLC-136/146/174)



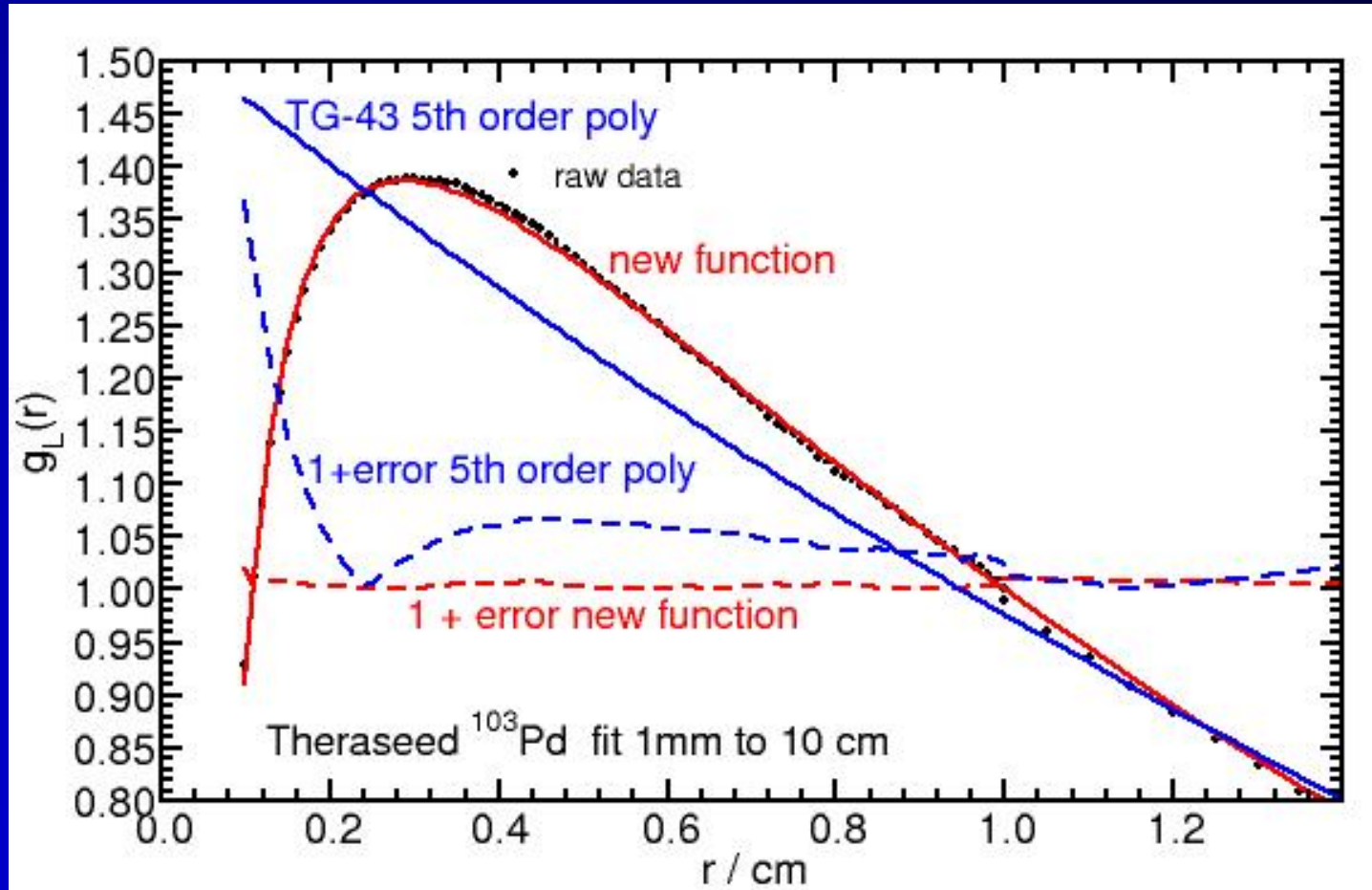
$\Lambda$  is 2% too high for this seed with MCNP 32/69

# *Improved fitting function for $g(r)$ data*





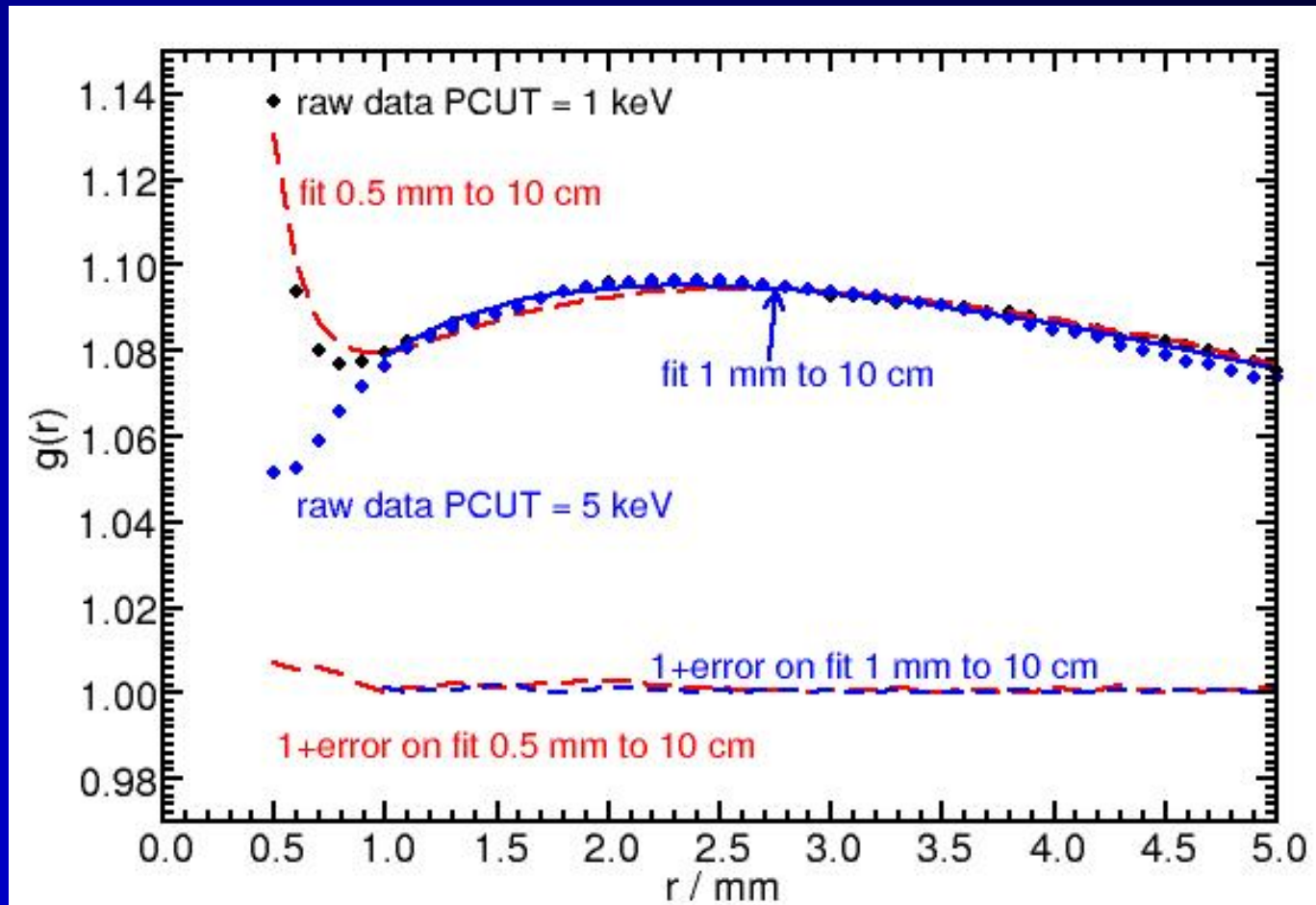
# *Improved fitting function for $g(r)$ data*



If fitting from 5 mm to 10 cm, then 5-th order polynomial is perfect.

# *Improved fitting function for $g(r)$ data*

The new  
fitting  
function  
handles the  
upturn

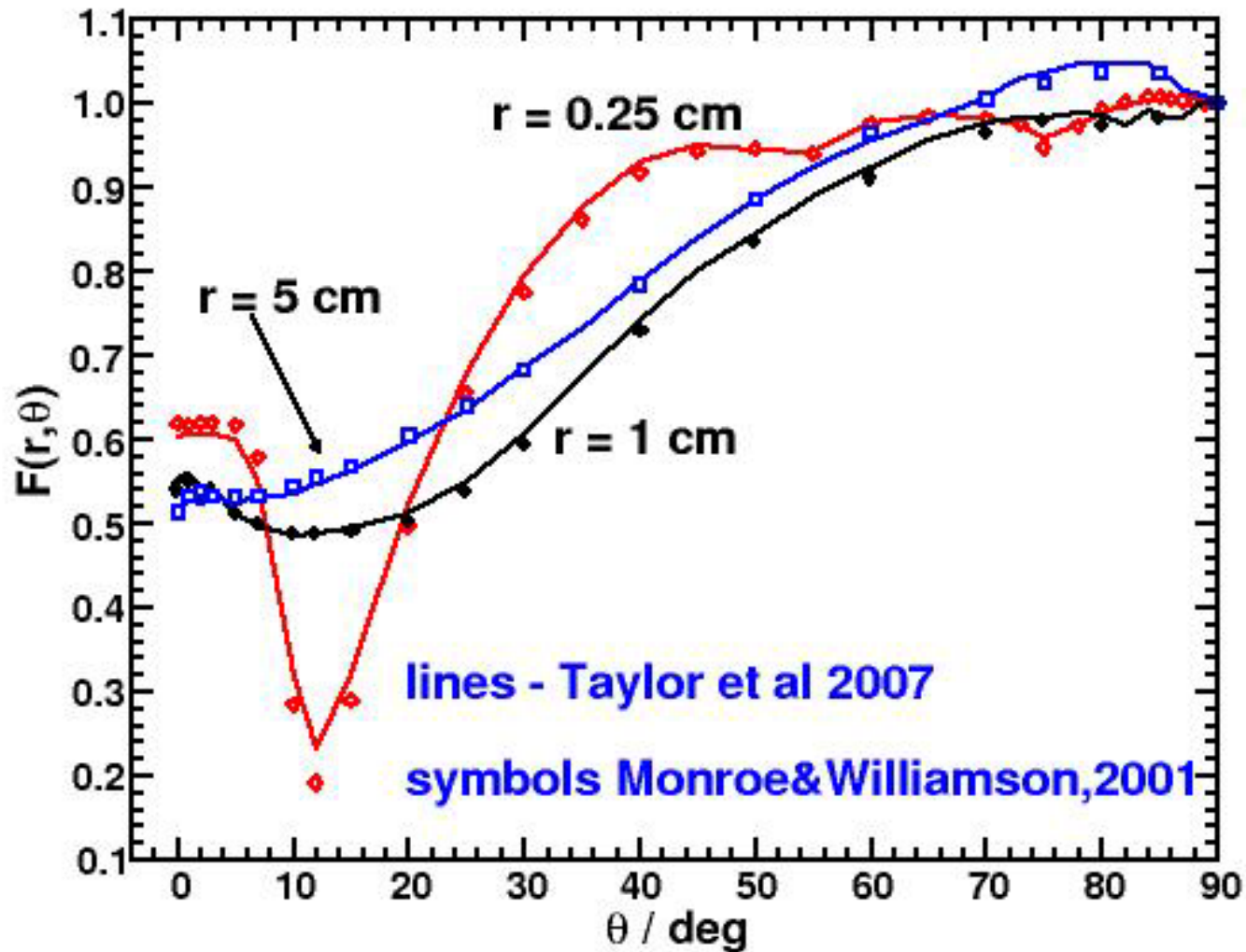


Upturn is from Ti x-rays and/or from geometry effects



# $F(r, \theta)$ : Theragenics 200 Pd-103

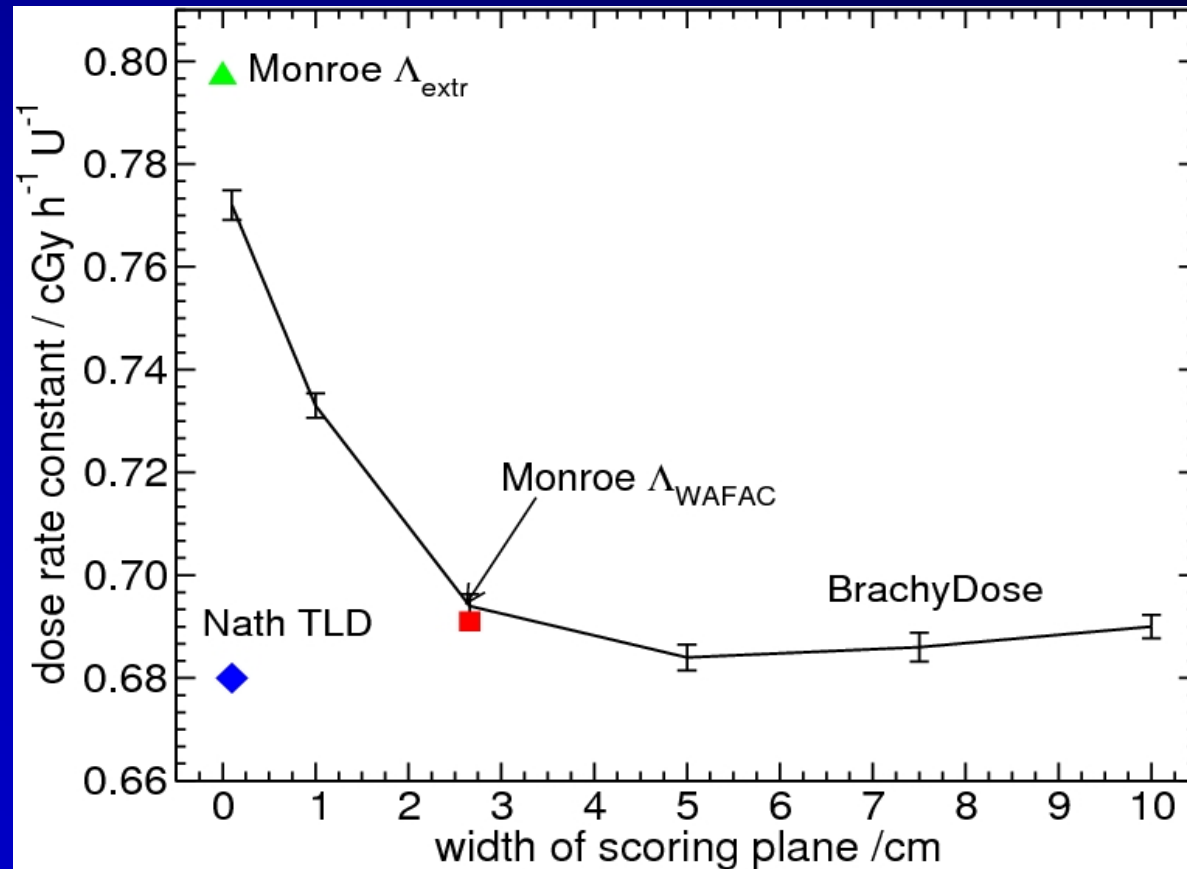
$^{103}\text{Pd}$  Source  
Theragenics  
Model 200



# $\Lambda$ - dose-rate constant

Dose to water at reference point divided by air-kerma strength

$^{103}\text{Pd}$  Source  
Theragenics  
Model 200



scoring plane at 10 cm from source

# BrachyDose

- a code for calculating **dose distributions** in a voxel CT phantom with brachytherapy sources
- code is based on Yegin's **MG (multi-geometry) package** and **EGSnrc**
- detailed models of **multiple seed types** at multiple locations and orientations
- can handle **x-ray sources** since based on EGSnrc
- code is **very fast**

Similar code: MCPI Chibani & Williamson

Med Phys 32(2005)3688-3698

# *Yegin's Multi-Geometry package*



Available online at [www.sciencedirect.com](http://www.sciencedirect.com)

SCIENCE @ DIRECT®

Nuclear Instruments and Methods in Physics Research B 211 (2003) 331–338

**NIM B**  
Beam Interactions  
with Materials & Atoms

[www.elsevier.com/locate/nimb](http://www.elsevier.com/locate/nimb)

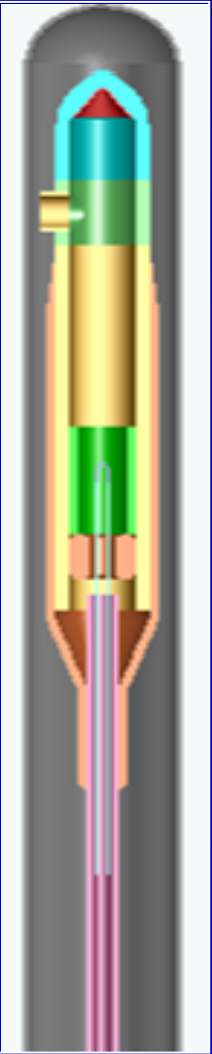
## A new approach to geometry modeling for Monte Carlo particle transport: An application to the EGS code system

Gultekin Yegin \*

*Department of Physics, Faculty of Arts and Sciences, Celal Bayar University, TR-45030 Manisa, Turkey*

Received 22 May 2002; received in revised form 10 April 2003

# Features of BrachyDose



- have modelled **most (all?) major seeds**
- ability to extract TG-43 parameters easily
  - **benchmarked** against previous TG-43 work
  - studied **voxel size effects** (Taylor et al, Med Phys 34(2007) 445-457)
- ability to use a **CT dataset**
- scores **spectrum** in any voxel
- models **50 kV brachytherapy x-ray source**
  - **VRT** increased efficiency by factor of  $10^4$
- ability to use a **phase space source**
- models **Ir-192 HDR** in **catheters**
- adjust cross sections for **sensitivity analysis**

# *BrachyDose: speed-up features*

- use pathlength scoring (factor of 15 over analog)
- reuse photons escaping from one seed for every seed (20% for 1mm, 28% for 3mm)
- fast table lookups of mass energy absorption coefficients (5% speed up)
  - use same approach as EGSnrc (log interpolation, small energy increments)
  - use XCOM data base for EGSnrc
- virtual geometry to reduce checks on seeds (large speed up)

# *BrachyDose: timing*

- for **average uncertainty of 2%** on dose  
in each voxel in implant  
(**g77** compiler - single 3.0 GHz 64 bit CPU)
  - 3 mm voxels: 14 s
  - 2 mm voxels: 30 s
  - **1 mm voxels: 228 s**
- i.e., **3.5 min for 1 mm voxels**
- and with an Intel compiler it is expected to be faster based on previous experience



# Voxel size effects

- Williamson's code uses a **point estimator**
- when using voxels one must be careful

$$D_{\text{vox}} = \frac{1}{\Delta r} \int_{r_o - \frac{\Delta r}{2}}^{r_o + \frac{\Delta r}{2}} dr D(r) \text{ i.e., dose is averaged over voxel}$$

$$D_{\text{vox}} = D(r_o) \left[ 1 + \frac{D''(r_o)}{24D(r_o)} \Delta r^2 + O(\Delta r^4) \right]$$

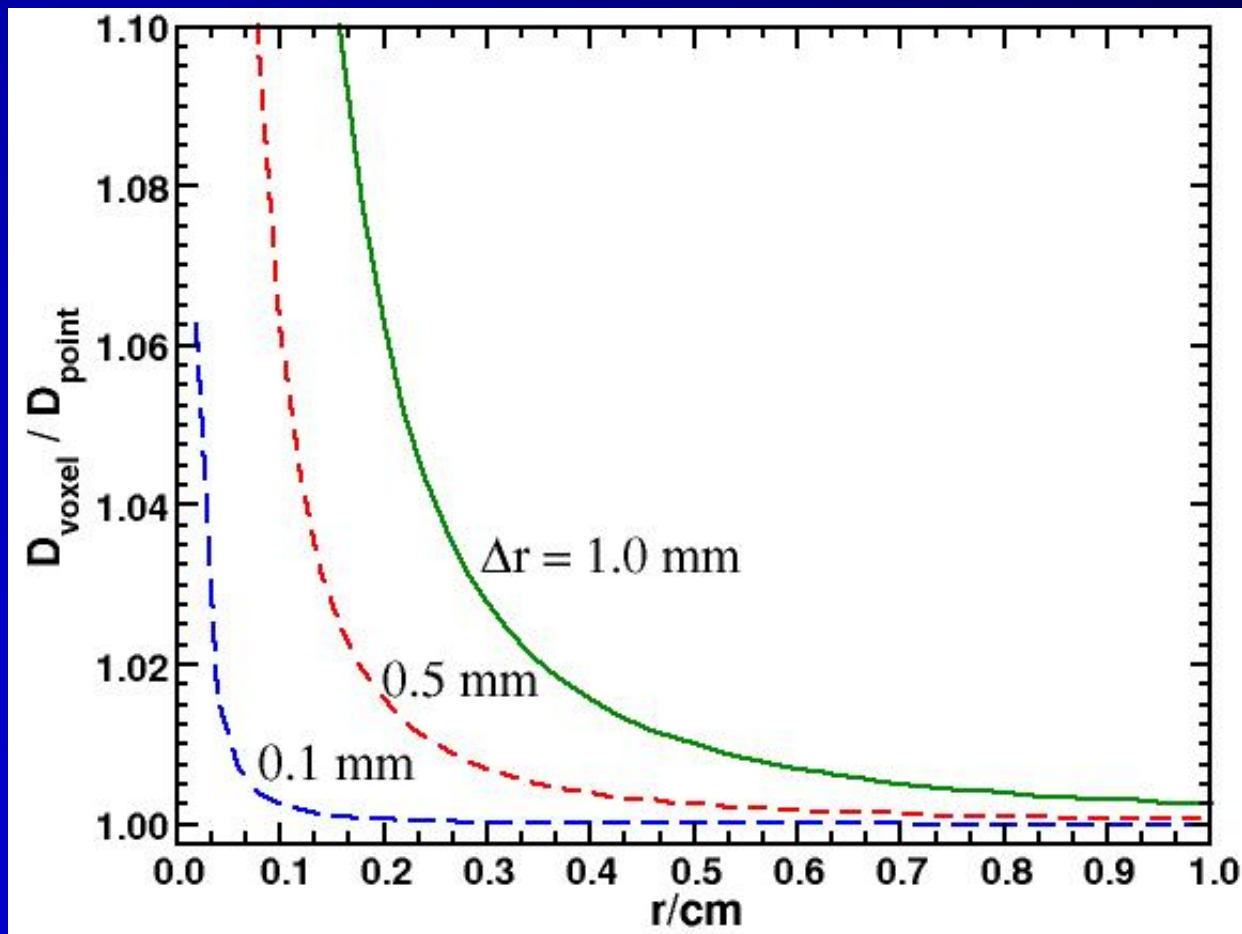
Kawrakow  
MP 33(2006)1829

For  $1/r^2$

$$D_{\text{vox}} \approx D(r_o) \left[ 1 + \frac{\Delta r^2}{4r_o^2} \right]$$

# Voxel size effects

Size of error in associating the **average dose** in the voxel with the **dose at the mid-point** (near a point source)

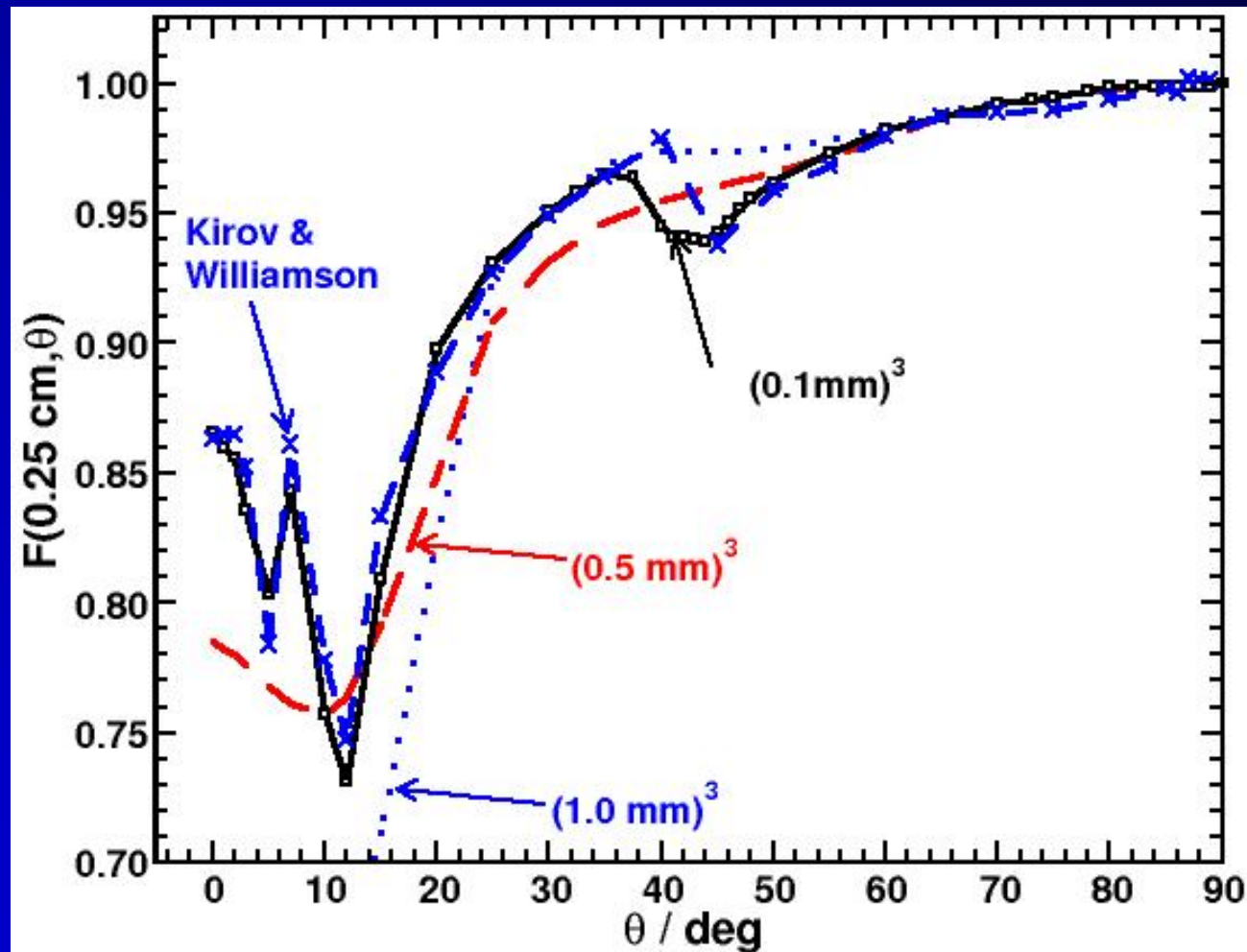


# Voxel size effects

$^{125}\text{I}$



Source Tech  
Medical STM125I



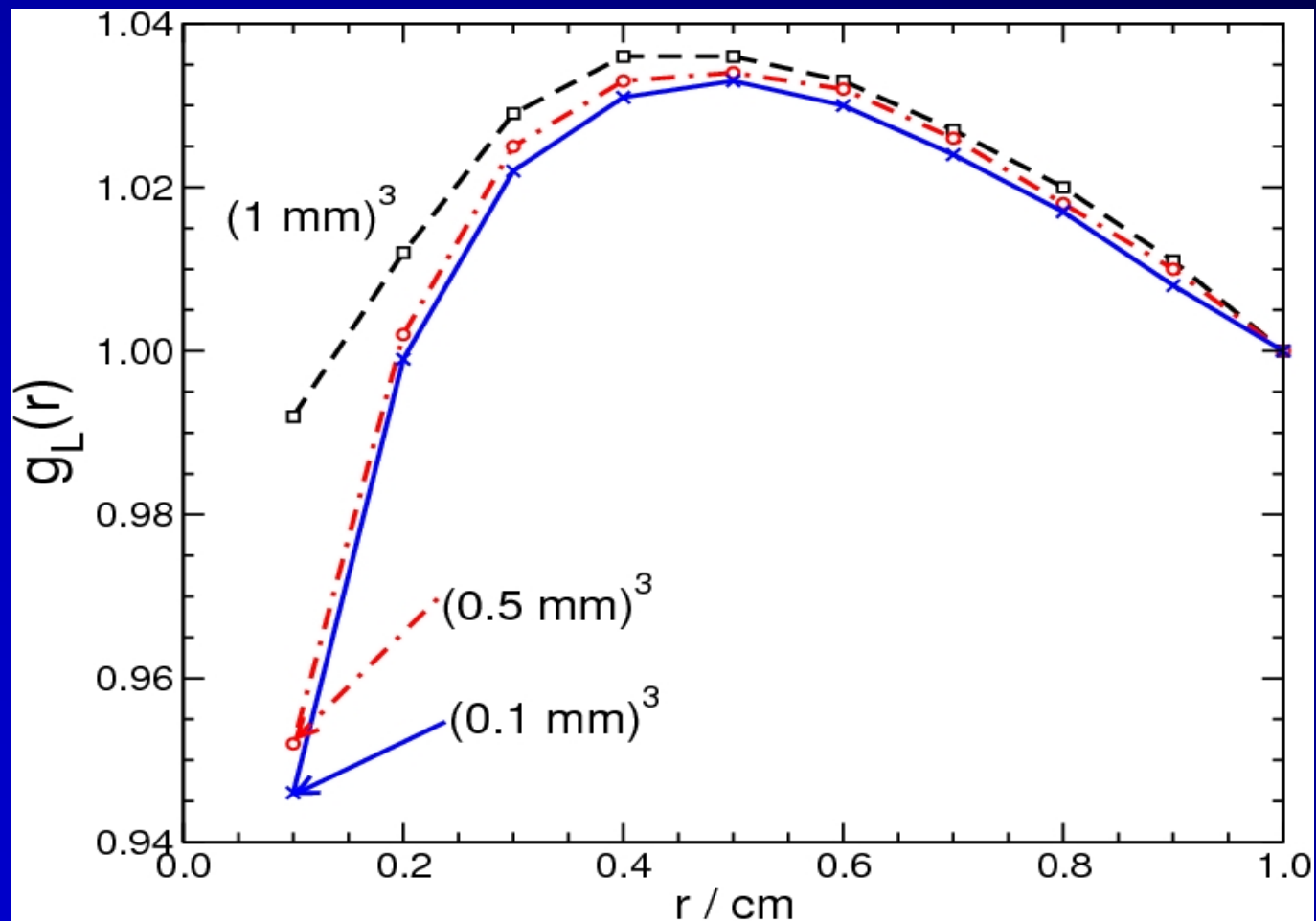
Taylor et al,  
Med Phys  
34 (2007)  
445 - 457

# Voxel size effects

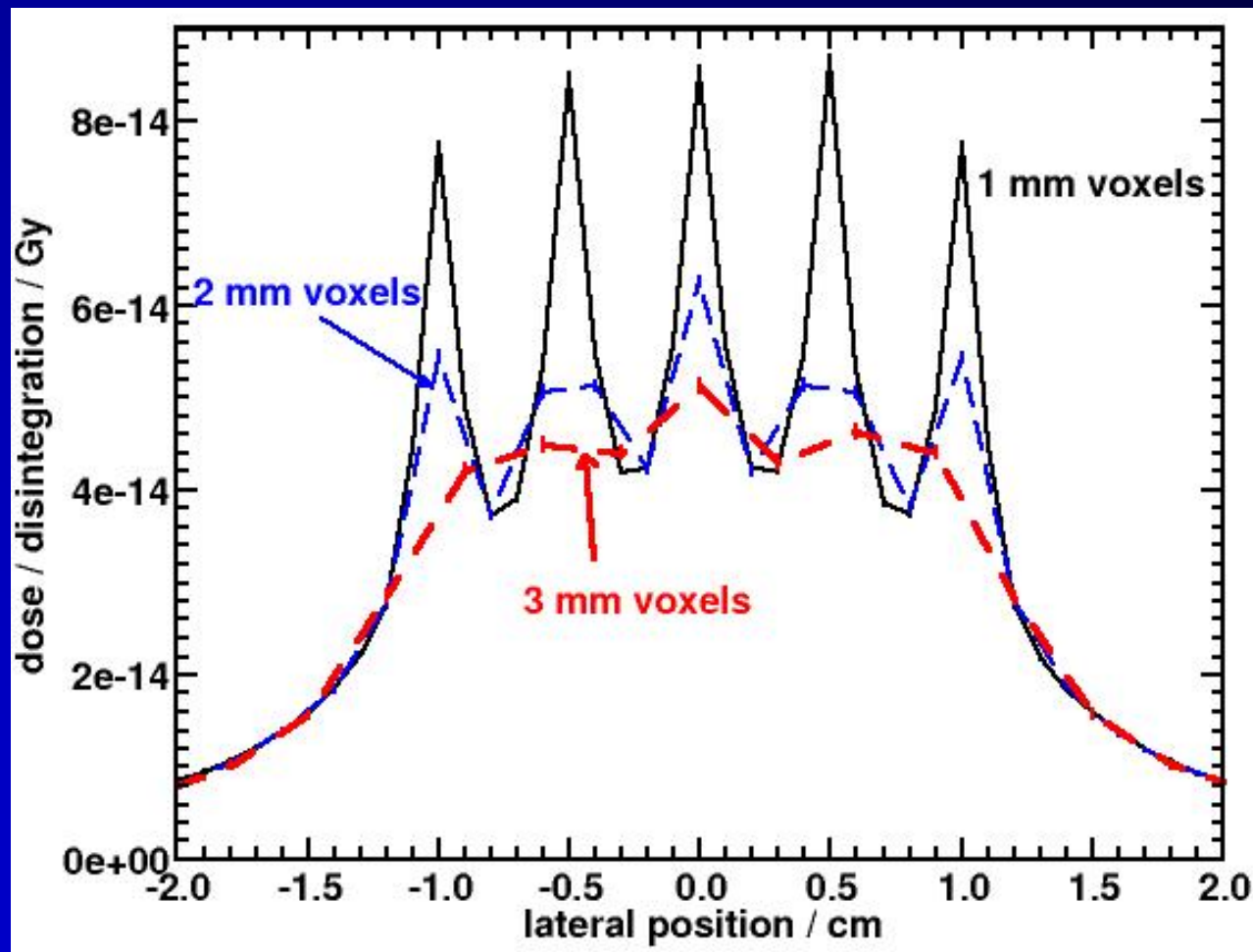
$^{125}\text{I}$



Source Tech  
Medical STM125I

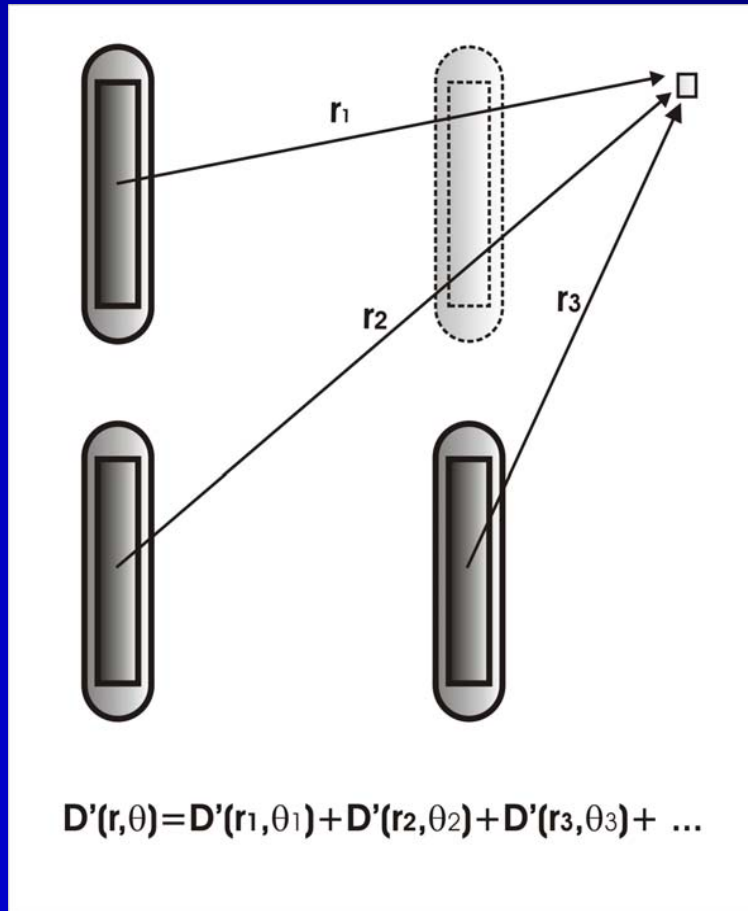


# Voxel size effects



recall slide 7 showed voxel size effects on DVHs

# *Inter-seed effects in brachytherapy*

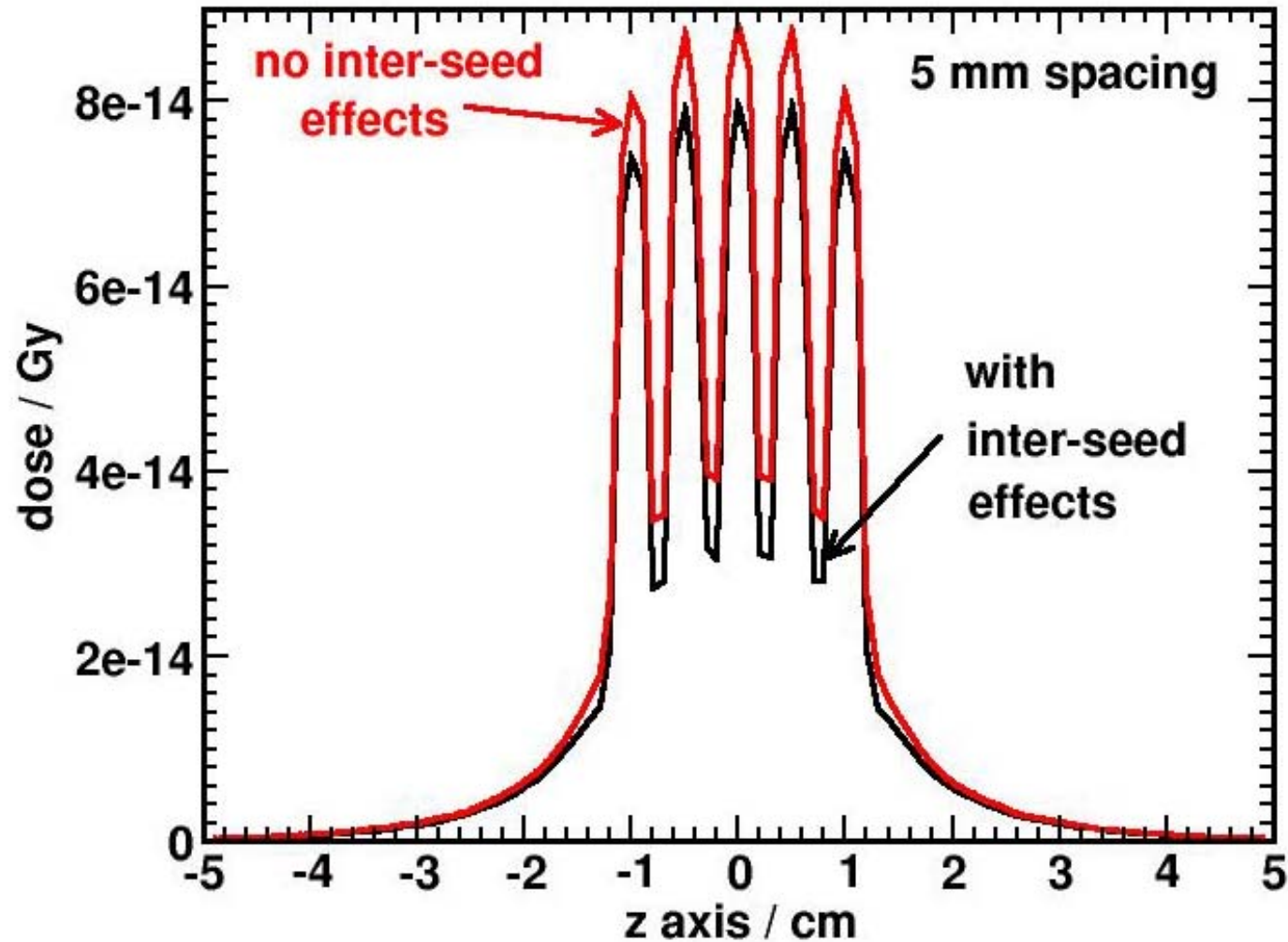


Standard planning systems  
**ignore self-shielding**

A few papers have investigated  
**inter-seed effects.**

Chibani and Williamson, (Med  
Phys 2005) used MCNP. Each  
calculation **took 3 days.**

## *central axis dose for 5 mm spacing*





# *inter-seed effects*

---

- doses vary by as much as
  - 27% in valley
  - 10% near peak
- can be misleading since volumes near peaks are often small in these regular patterns
- close to **worst case** (seeds are 3.6% of volume compared to 0.5% for 10 mm spacing)

## *inter-seed effects (cont)*

- total energy deposited in implant
  - 5 mm spacing -down 13%
  - 10 mm spacing -down 2.8%
- total energy deposited in nearby "critical organ"
  - 5 mm spacing -down 13%
  - 10 mm spacing -down 3%
- difference is more important than the absolute value since dose prescription determined by experience

# *$^{192}\text{Ir}$ source in catheters*



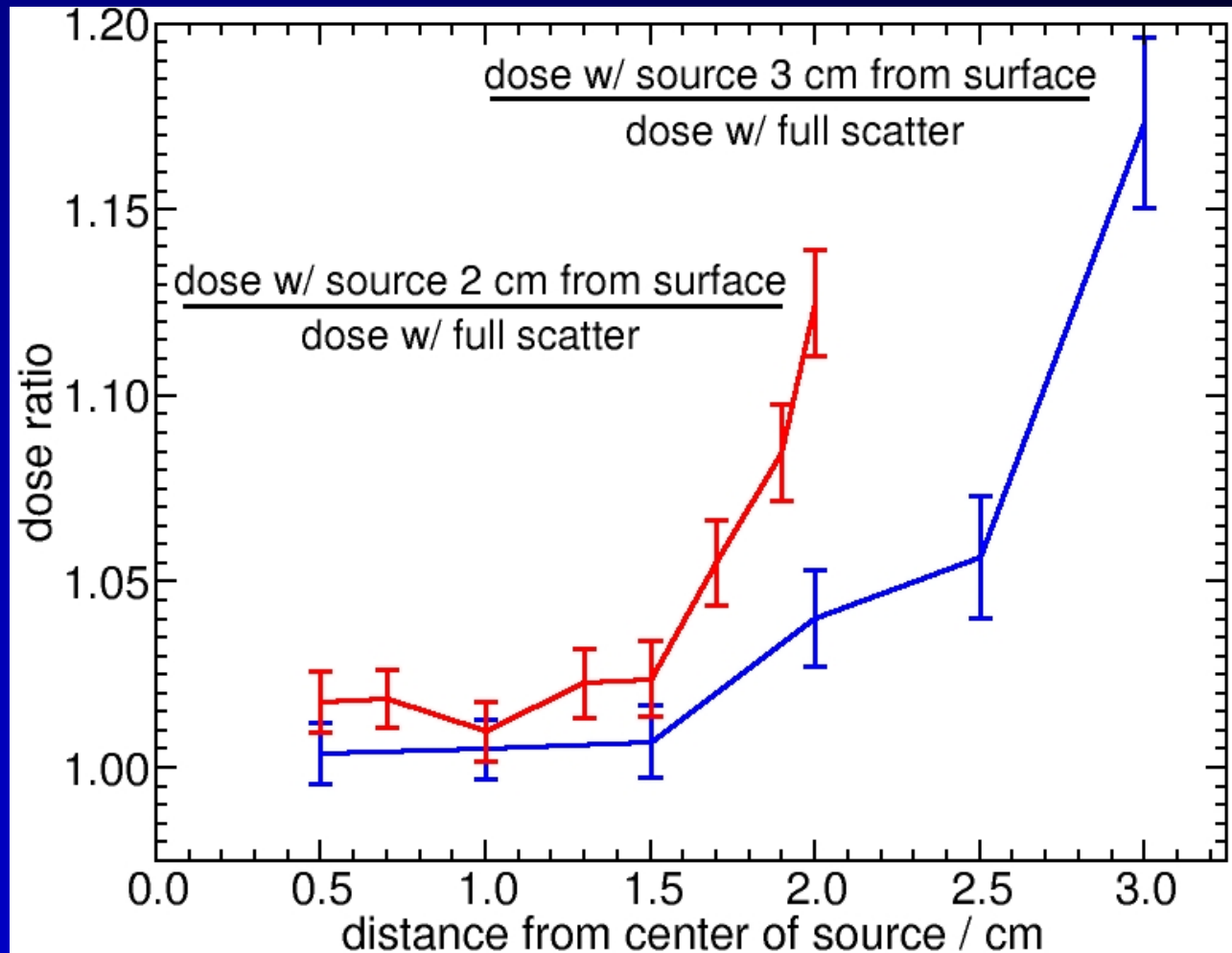
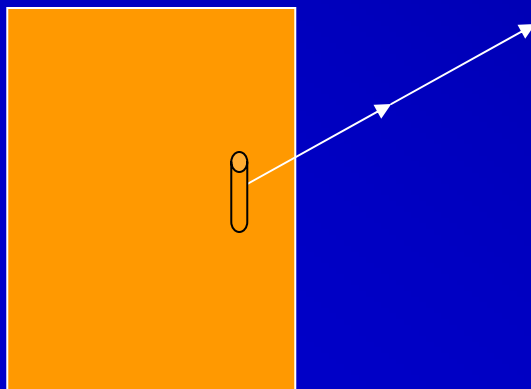
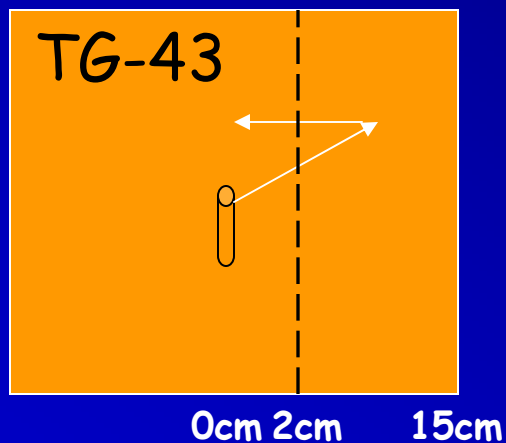
- can model an HDR source inside a catheter
- the source moves to an arbitrary number of positions in an arbitrary number of catheters
- we see **no significant effect** of the catheters.

# *Need for treatment planning*

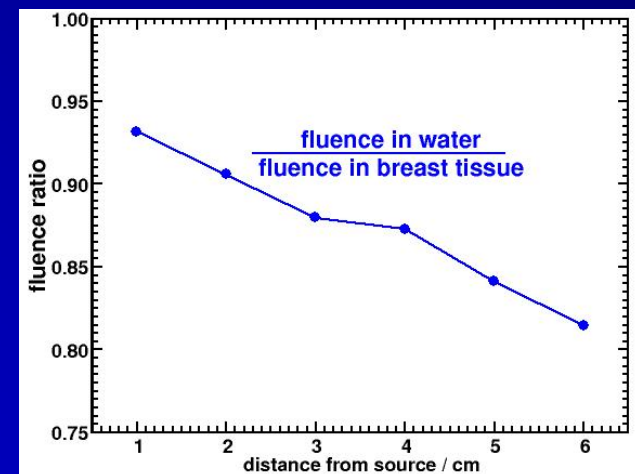
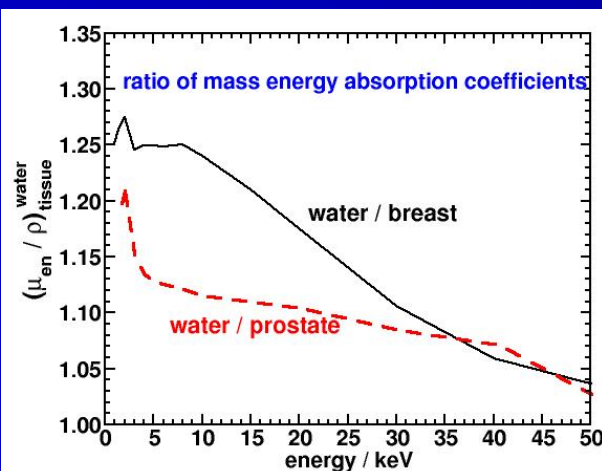
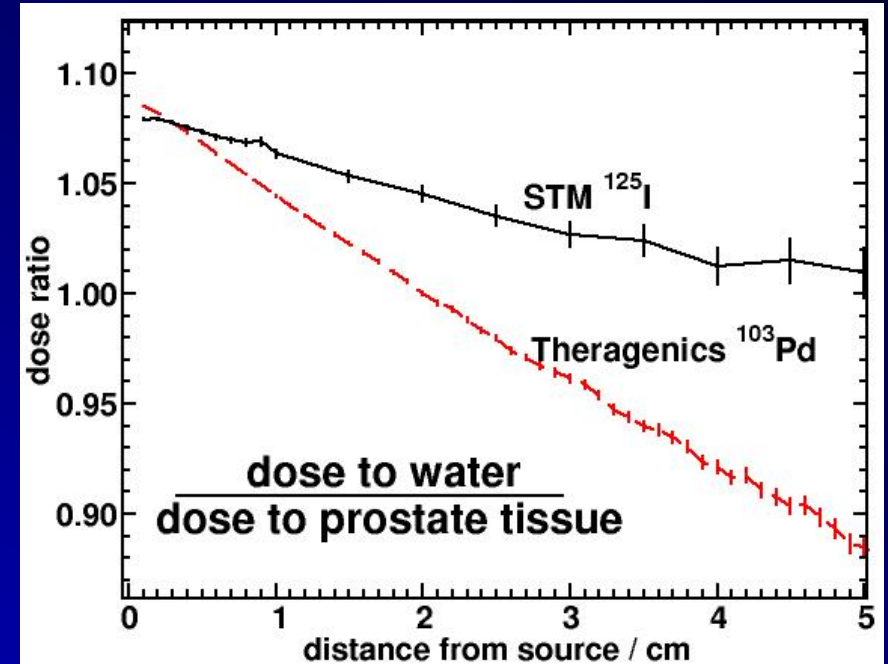
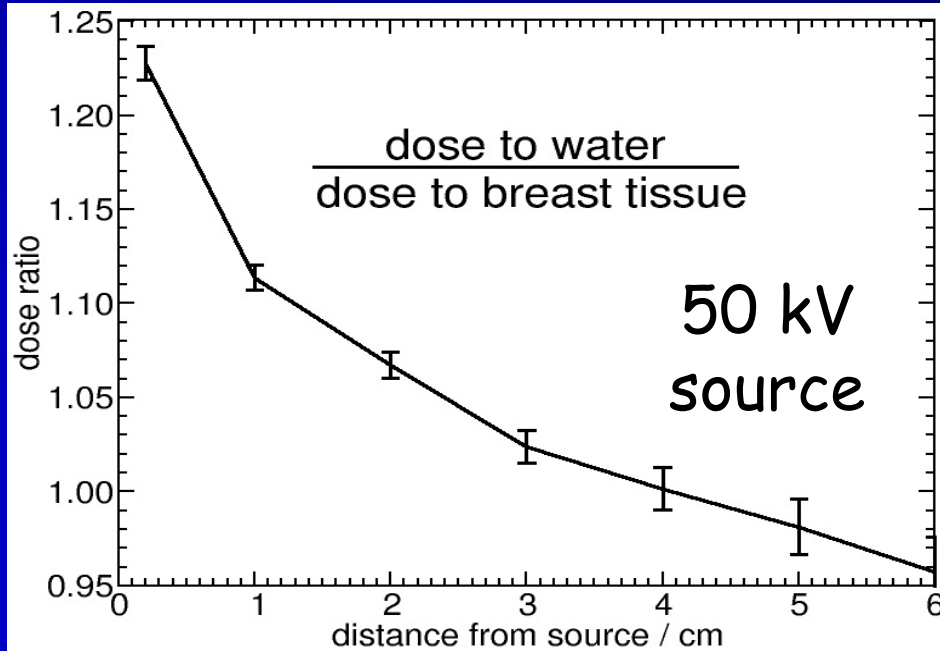
- TG-43 treatment planning assumes **infinite water** patient with one source at a time
- what are the magnitudes of the effects of
  - **other tissues and calcifications**
  - air surfaces (for breast treatments)
  - **inter-seed attenuation** (up to 5-10%)
- treatment planning with **BrachyDose** based on 3 D CT data sets **handles all of these**

# *Effect of finite irradiated volume*

50kV X-Ray Source




# Effect of realistic tissue



# CLRP TG-43 web resource

[http://www.physics.carleton.ca/clrp/seed\\_database](http://www.physics.carleton.ca/clrp/seed_database)

- Full set of **tabulated dosimetry data** for each source studied
- Description of calculation methods
- Descriptions & **scale drawings** of sources
- Plots compare values calculated in this study to other results
- Links to relevant papers & websites

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## The CLRP TG-43 Parameter Database

*R. E. P. Taylor and D. W. O. Rogers*

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### About the Database:

This is the home of the [Carleton Laboratory for Radiotherapy Physics \(CLRP\)](#) Database of TG-43 brachytherapy dosimetry parameters. The dosimetry parameters presented here were calculated using the [EGSnrc](#) usercode BrachyDose<sup>1,2</sup>, a Monte Carlo code for doing rapid brachytherapy treatment planning calculations. The code is capable of calculating the full 3D dose distribution with (1 mm)<sup>3</sup> voxels from 125 <sup>125</sup>I seeds in a prostate implant with 2% statistics in under 5 minutes on a single Xeon processor.

On these pages you will find a set of TG-43 dosimetry parameters for all of the brachytherapy seeds listed in the Joint AAPM/RPC brachytherapy source [registry](#). The aim of this work was to create a comprehensive database of TG-43 dosimetry parameters using a consistent set of methods for all seeds. This data is made freely available to the public and we hope it will prove to be a valuable resource for the Medical Physics Community.

If you have questions or comments please [Contact](#) us!

---

### Brachytherapy Seed Data:

1. Seeds listed in the Joint AAPM/RPC brachytherapy source [registry](#)

<sup>125</sup>I Seeds:

- Amersham, OncoSeed, 6711 [html](#) [pdf](#)
- Amersham, EchoSeed, 6733 [html](#) [pdf](#)
- Bebig GmbH, IsoSeed I-125, I25.S06 / Theragenics Corporation, I-Seed I-125, I25.S06 [html](#) [pdf](#)

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# CLRP TG-43 web resource

## Amersham OncoSeed 6711 $^{125}\text{I}$ Source TG-43 data



### Source Description:

The 6711 source consists of radioactive AgI and AgBr coated on a 2.8 mm long cylindrical silver rod. The silver rod has conical sections beveled at  $45^\circ$  and the end faces of the rod have a coating assumed to have a uniform thickness of  $1.75\text{ }\mu\text{m}$  on the cylindrical surface. The composition is given in ref. 1. The silver rod is encapsulated in a titanium tube with  $0.375\text{ mm}$  thick end welds. The inside of the capsule is filled with air. Overall source length is  $3.5\text{ mm}$ .

### Dose Rate Constant - $\dot{\Lambda}$ :

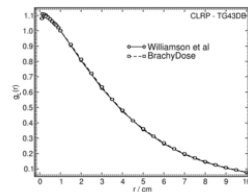
Dose rate constants,  $\dot{\Lambda}$ , are calculated by dividing the air kerma strength per history  $(0.1\text{-mm})^3$  voxel centered on the reference position,  $(1\text{ cm}, 1/2)$ , in the  $30 \times 30 \times 30$  voxel grid. Constants are provided for air kerma strength calculated using voxels of  $2.7 \times 2.7 \times 0.05\text{ mm}^3$  and  $2.7 \times 2.7 \times 0.1\text{ mm}^3$  source. The larger voxel size averages the air kerma per history over a region comparable to the primary collimator of the WAFAC<sup>bc</sup>. The small voxel serves to estimate the air kerma at the reference position.

Author	$\dot{\Lambda}$ (cGy/h)
this study - $0.1 \times 0.1 \times 0.05\text{ mm}^3$ voxel at $10\text{ cm}$	
this study $2.66 \times 2.66 \times 0.05\text{ mm}^3$ voxel at $10\text{ cm}$	
Williamson <sup>1</sup> (DLC 146)	
Williamson <sup>1</sup> TLD	

### Radial dose function - $g(r)$ :

The radial dose function,  $g(r)$ , is calculated using both line and point source models. The line source model is used for distances less than  $1\text{ cm}$  from the source and the point source model is used for distances greater than  $1\text{ cm}$ .

Click image for higher res version

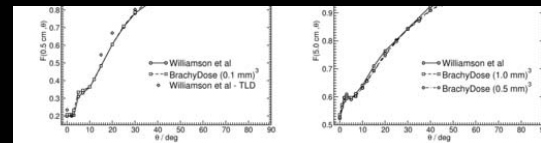
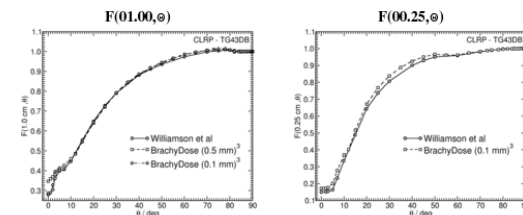


Tabulated  $g(r)$  data: [html](#) [Excel](#)

### Anisotropy function - $F(r, \theta)$ :

Anisotropy functions are calculated using the line source approximation and 32 unique polar angles with a minimum resolution of  $5^\circ$ . The anisotropy factor,  $\phi_{an}(r)$ , was calculated by integrating the weighted dose rate over  $0^\circ \leq \theta \leq 90^\circ$ .

Click images for higher res versions



Tabulated  $F(r, \theta)$  data: [html](#) [Excel](#)

### References:

#### Seed Specific References

1. J. Dolan, Z. Li, and J.F. Williamson, Monte Carlo and experimental dosimetry of an  $^{125}\text{I}$  brachytherapy seed, Med. Phys **33** 4675 (2006)

#### Other References

- R. E. P. Taylor, G. Yegin, D.W.O. Rogers, Benchmarking BrachyDose: voxel-based EGSnrc Monte Carlo calculations of TG-43 dosimetry parameters, Med. Phys **34**, 445 (2006)
- R. Loevinger, Wide-angle free-air chamber for calibration of low-energy brachytherapy sources, Med. Phys **20** 907 (1993)
- S. M Seltzer *et al*, New National Air-Kerma-Strength Standards for  $^{125}\text{I}$  and  $^{103}\text{Pd}$  Brachytherapy Seeds, J. Res. Natl. Inst. Stand. Technol., **108**, 337 (2003)
- R. E. P. Taylor, D.W.O. Rogers, An EGSnrc Monte Carlo calculated TG-43 parameter database, *in preparation*

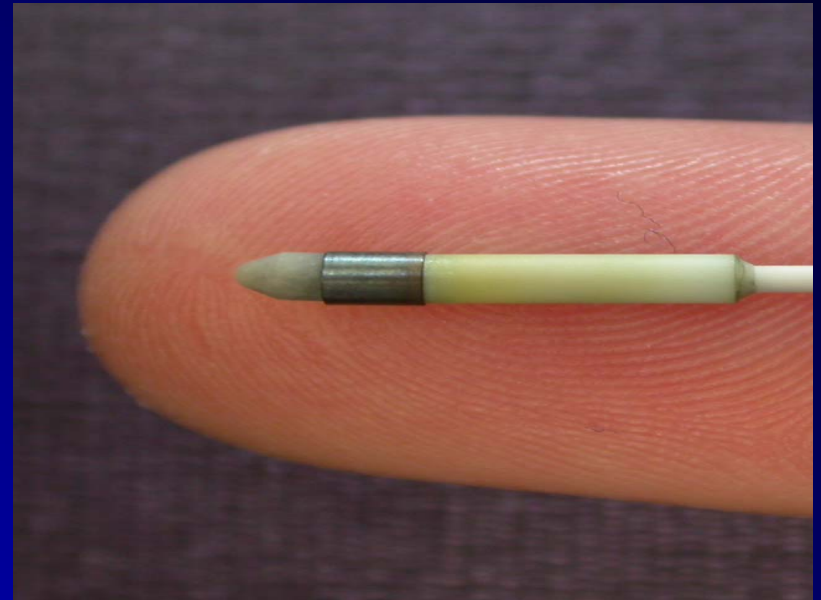
[Back to seed index](#)

[Carleton Laboratory for Radiotherapy Physics](#)

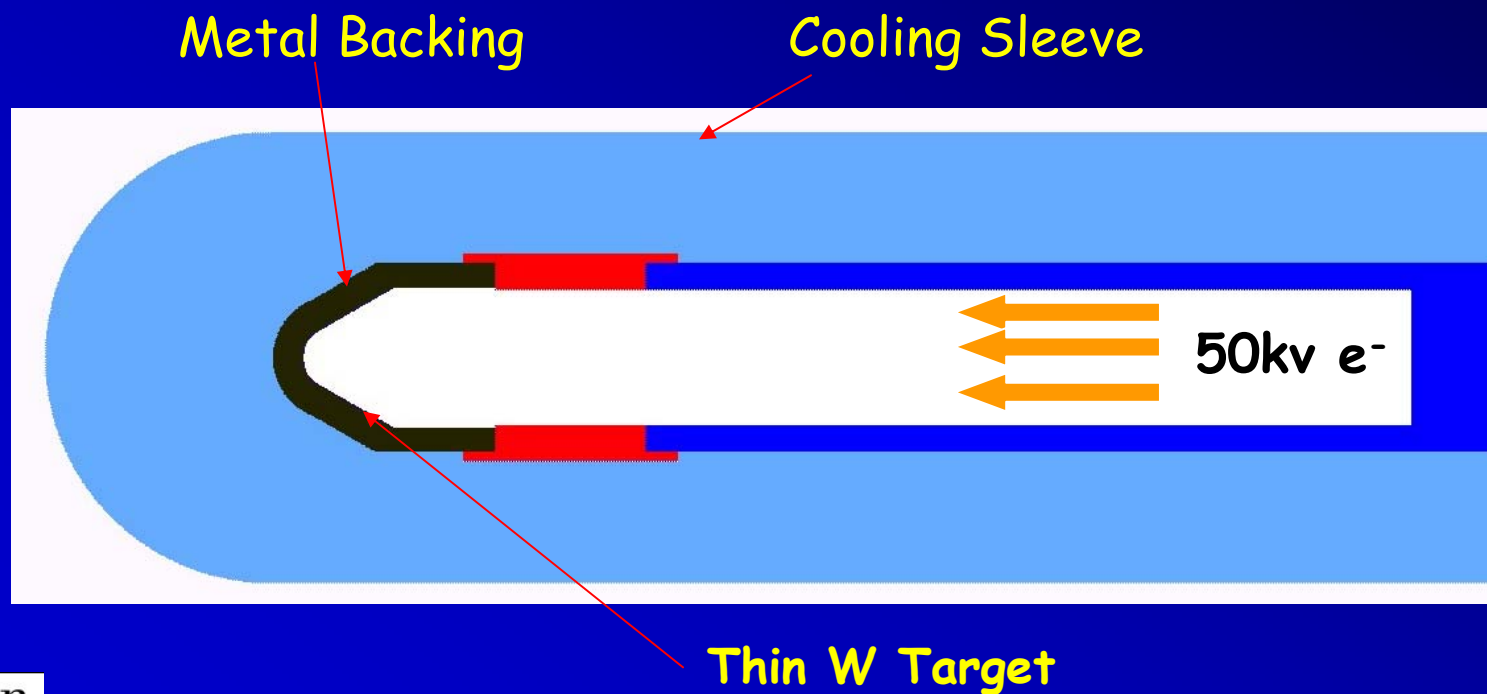
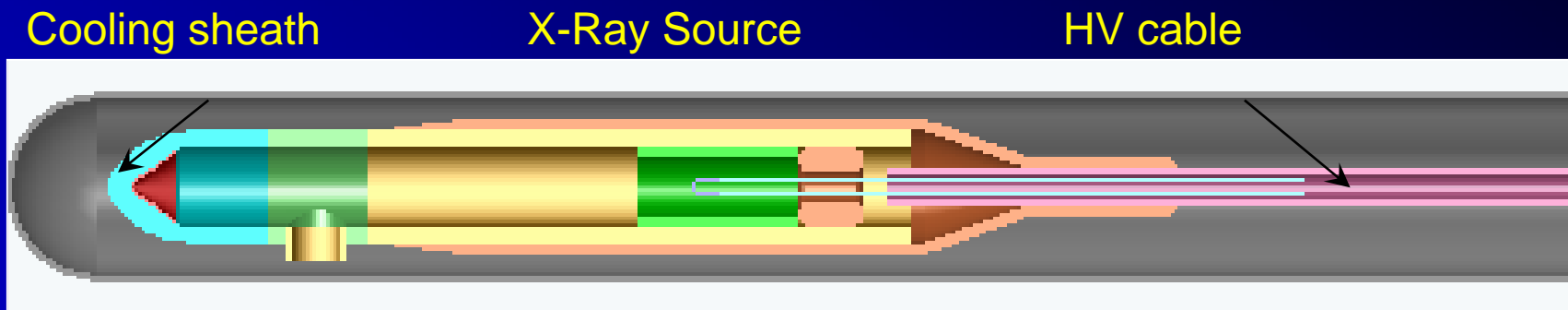
March 30 2007.

# *Xoft Axxent X-ray source*

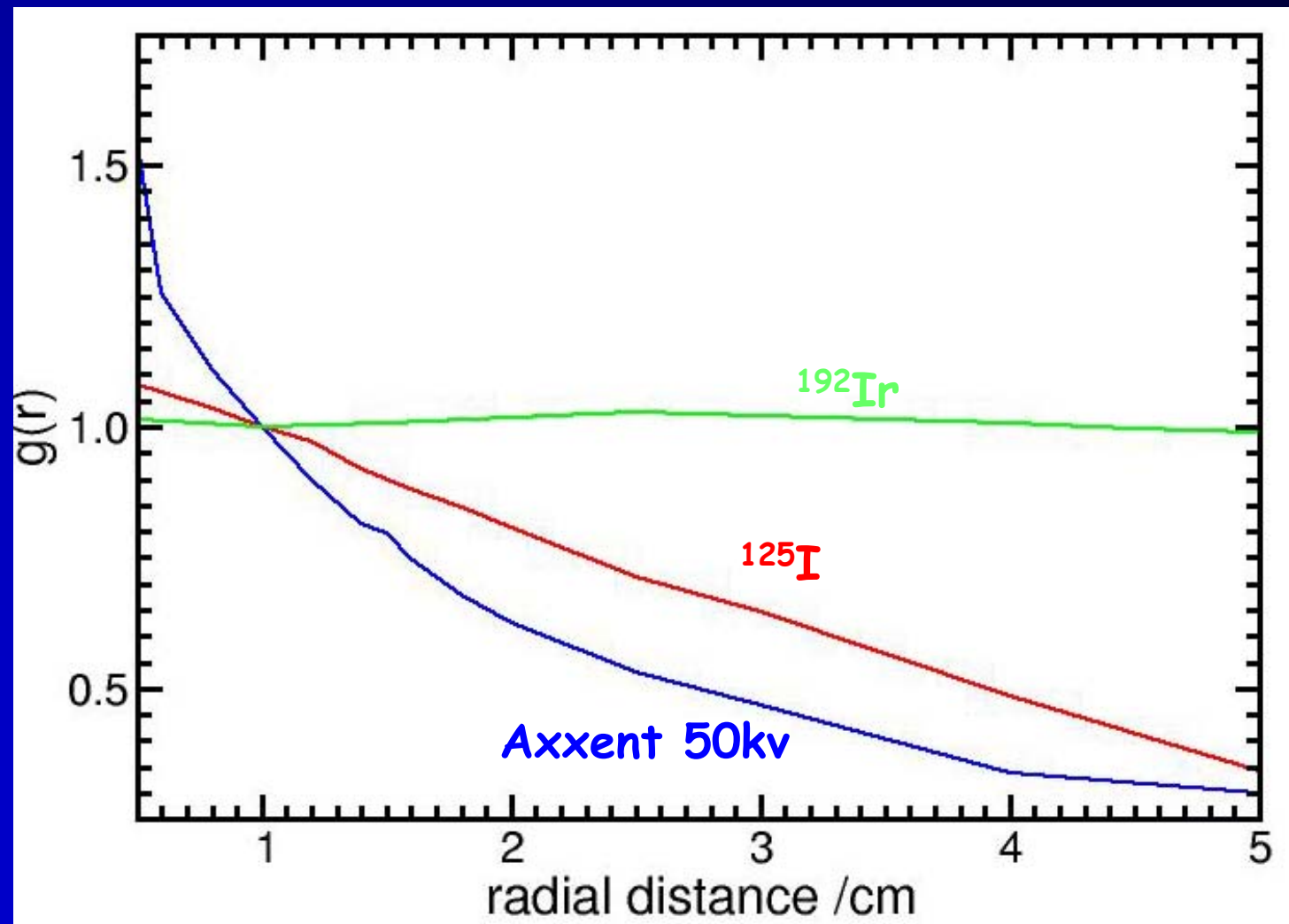
- Miniature X-Ray Source
  - 25-50 kV  $e^-$  on W target.
  - Lifetime of 5h w/ beam on
- "Tunable" dose rates
- Reduced shielding requirements
- Source can be turned on/off
- FDA Approved - Jan 2006
- EGSnrc can handle this unlike other brachytherapy codes



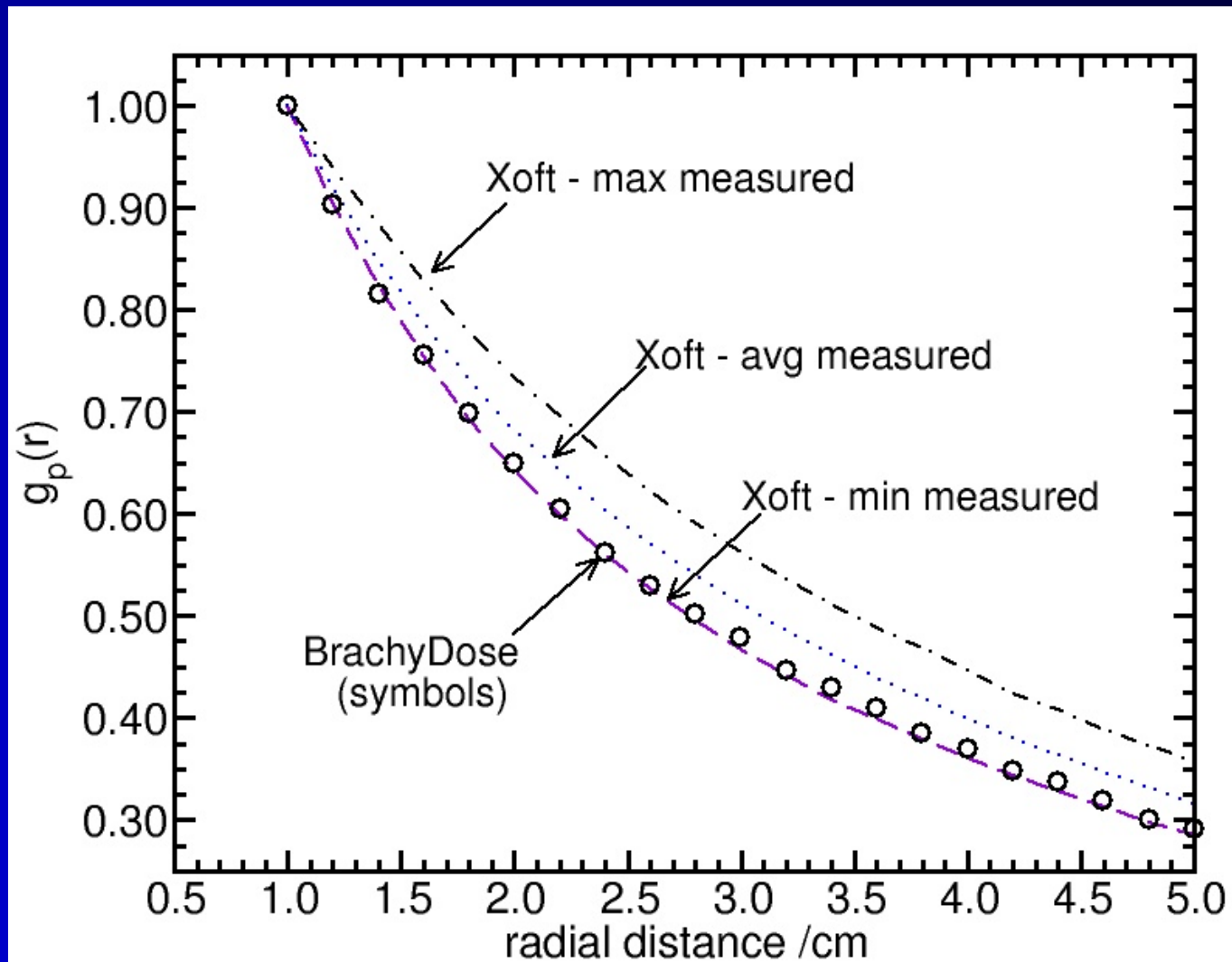
# *Model for Monte Carlo simulation*



# Radial dose function comparison



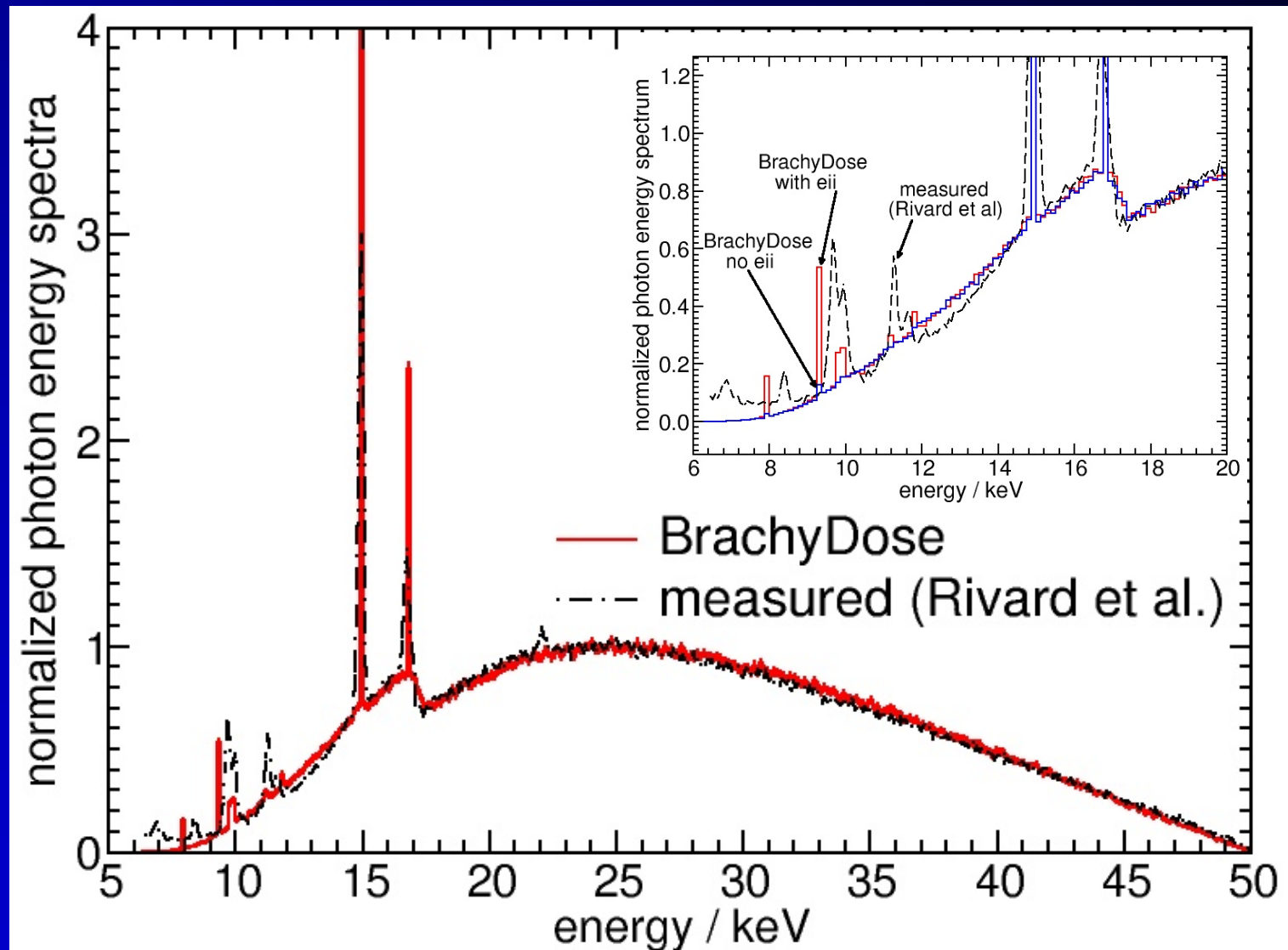
# $g(r)$ - radial dose function



# Energy spectrum with EII

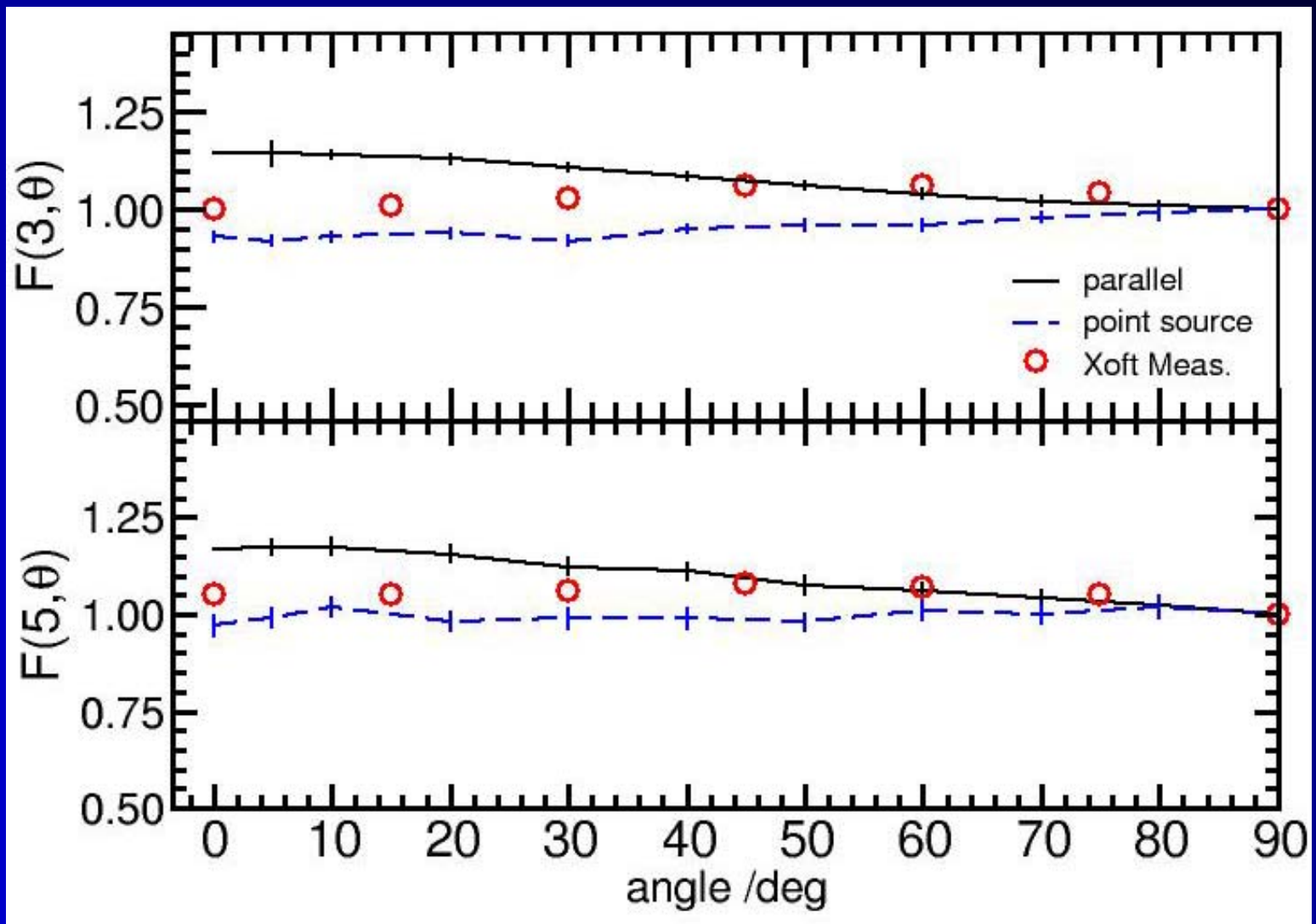
spectrum  
calculated  
in air

including  
detector  
response  
explains  
7 keV  
"peak"





# $F(r, \theta)$ - anisotropy function





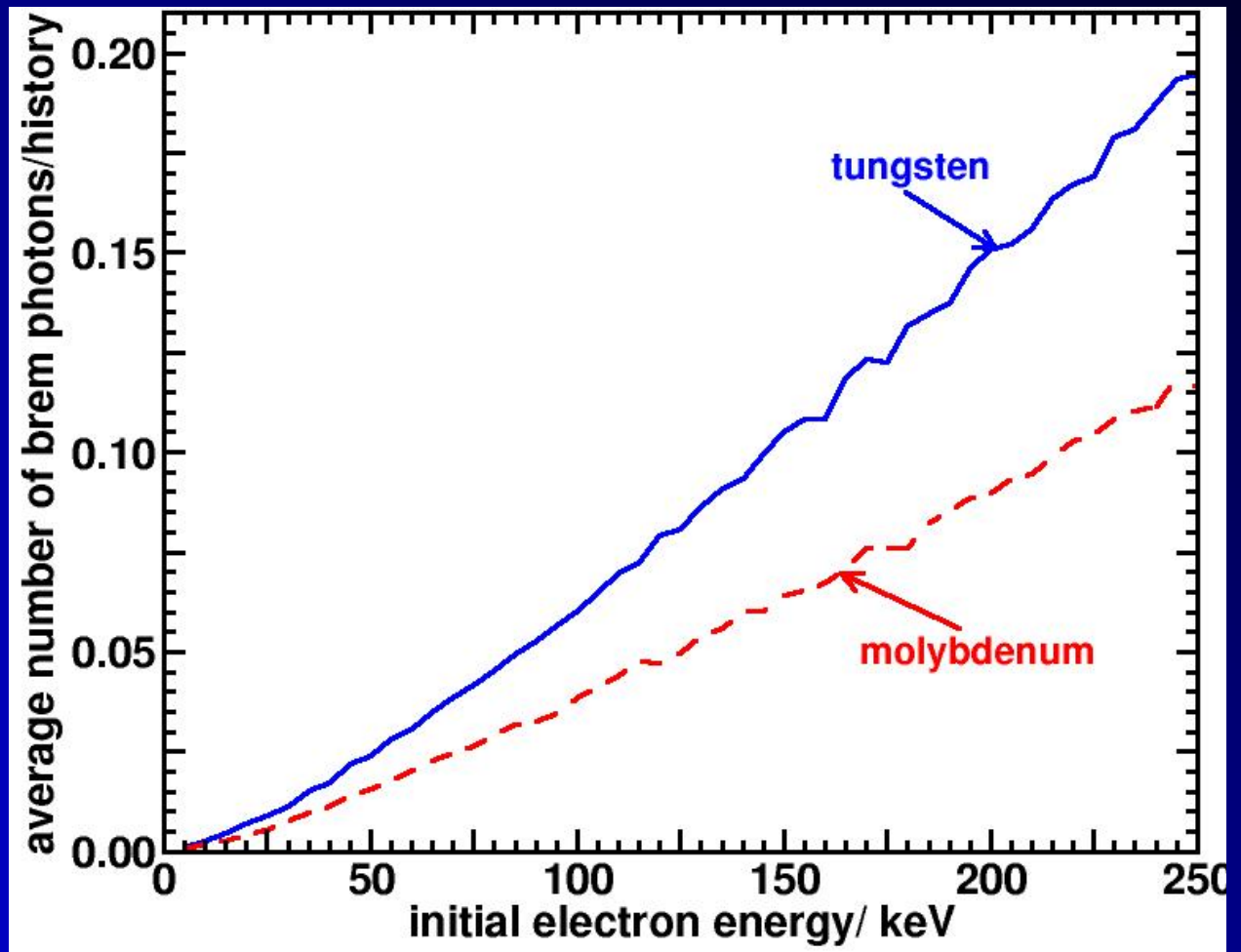
# BCSE

## *brem cross section enhancement*

low-energy  
electrons produce  
**very few** brem  
photons

=> **waste time**  
tracking electrons  
with no effect

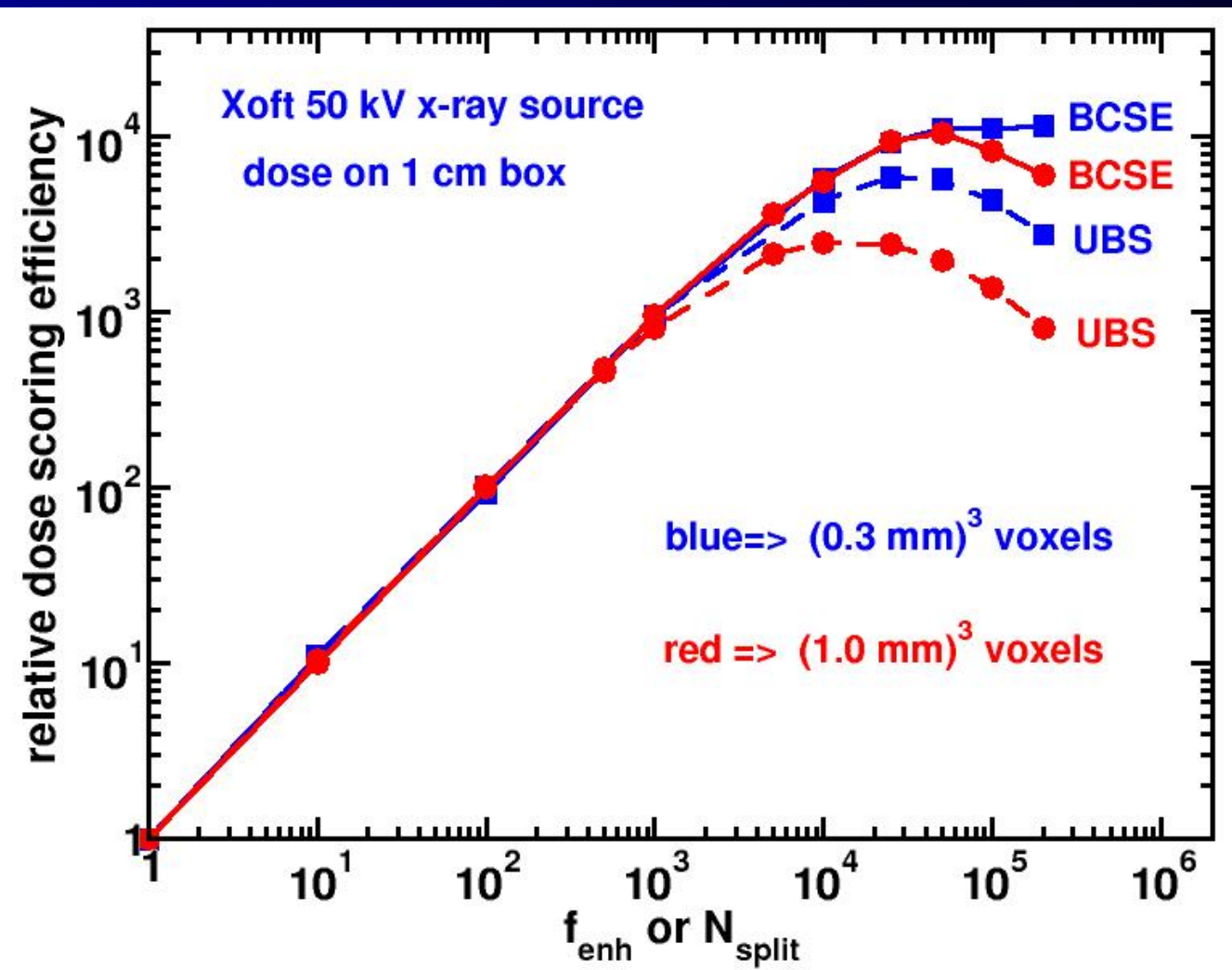
**Solution: enhance  
the cross section  
for brem**



# BCSE

UBS = uniform  
brem splitting

UBS "saturates"  
sooner because  
many photons in  
the same history.  
Optimal approach  
is hybrid(500,100)  
 $1 \text{ mm}^3 \epsilon=15,000$



# *Phase-space source*

- electrons take much longer to transport than photons
- in the patient we only care about photons
- score the phase space data outside the source and inside the "balloon" and re-use
- saves a factor of 4 in the calculation
- will be able to recycle as in BEAMnrc
- not needed for seeds since already reuse each photon with every seed

# Summary

- Monte Carlo has played a central role in brachytherapy dosimetry, especially in calculating TG43 parameters
- Monte Carlo dose calculations are needed in brachytherapy
  - interseed attenuation
  - realistic materials
  - lack of full backscatter
- BrachyDose does a 2% cal'n in 1 mm voxels in 4 min.
  - extensive benchmarking for different seeds
  - EGSnrc inherently can model the x-ray sources

# Acknowledgments

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**OIT**

**OGSST**

**TomoTherapy**

**MDS-Nordion**

**Varian**

**Nucletron**



**Elsayed  
Ali**



**Gultekin  
Yegin**



**Randy  
Taylor**

*Thank you*

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# *Bibliography re Williamson's work*

- PTRAN\_CCG (Williamson group's code)
  - Monte Carlo evaluation of kerma at a point for photon transport problems Med Phys 14(1987)567-576
  - Volume-based geometric modeling for radiation transport calculations, Med Phys 19 (1992) 667-677
  - Comparison of calculated and measured heterogeneity factors... Med Phys 20 (1993) 209-222
  - Monte Carlo calculations of kerma to a point in the vicinity of media interfaces, PMB 38 (1993) 1825-1840
- Quantitative dosimetry methods for brachytherapy, Williamson and Rivard, pp 233-294 in AAPM 2005 Summer School: Brachytherapy Physics, Medical Physics Publishing



# *Bibliography re TG43*

- Dosimetry of interstitial brachytherapy sources:  
Recommendations of the AAPM Radiation Therapy  
Committee Task Group 43  
*Med Phys* 22 (1995) 209-234
- Update of AAPM TG43 Report: A revised protocol for  
brachytherapy dose calculations  
*Med Phys* 31 (2004) 633 -674
- Supplement to the 2004 update of the AAPM TG43 Report  
*Med Phys* 34 (2007) 2187-2205