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**Laboratory Reproduction of Auroral Magnetospheric
Radio Wave Sources.**

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Laboratory Reproduction of Auroral Magnetospheric Radio Wave Sources

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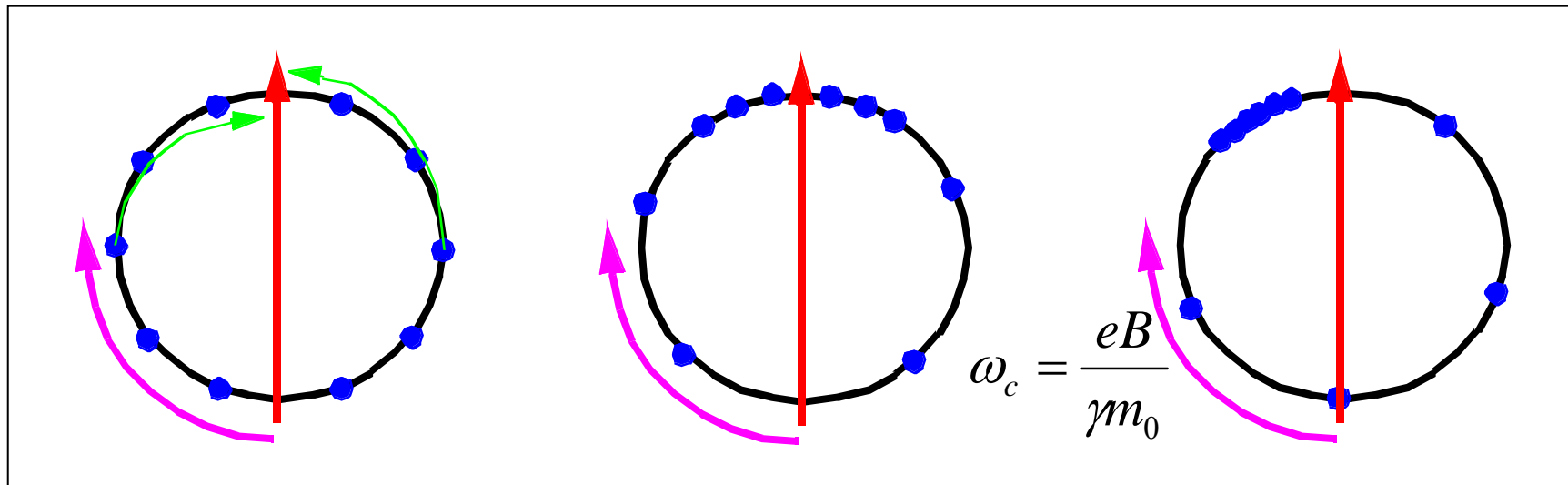
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Introduction - The Auroral Kilometric Radiation

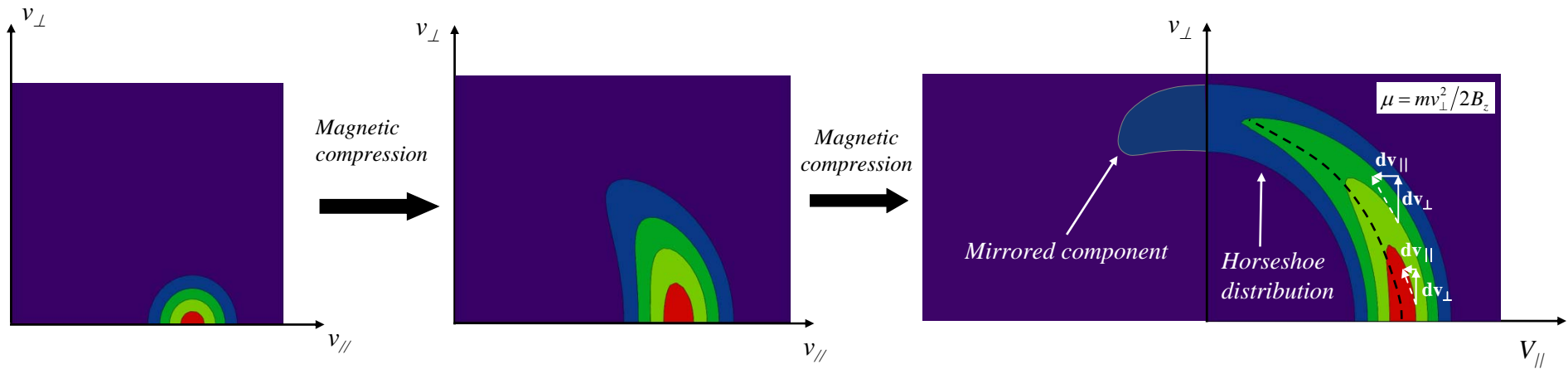
- Intense RF emission at high altitudes ($\sim 1.5 - 3$ Earth radii) within a large region of plasma depletion (the auroral density cavity), at frequencies of ~ 300 kHz
- Discrete components of emission typically ~ 1 kHz in bandwidth
- Within the source region the emissions have been observed to be polarised in the extraordinary (X) mode
- At certain altitudes, frequency components of emission are observed to extend down to the local relativistic electron cyclotron frequency Ω_{ce}/γ
- These emissions are observed in conjunction with the formation of a horseshoe distribution function in electron velocity space
- Total RF output power ranges between $10^7 - 10^9$ Watts. Efficiency of emission is $\sim 1-2\%$ [Gurnett1974]

Cyclotron Resonant Instability



- Electrons gyrate in close synchronism with a rotating electric field vector
- Bunching occurs due to modulation of the electron energy via the relativistic cyclotron frequency- this is fundamentally a relativistic phenomenon
- If the cyclotron frequency is slightly less than the wave frequency then net energy extraction may occur
- Saturation arises when phase trapping occurs

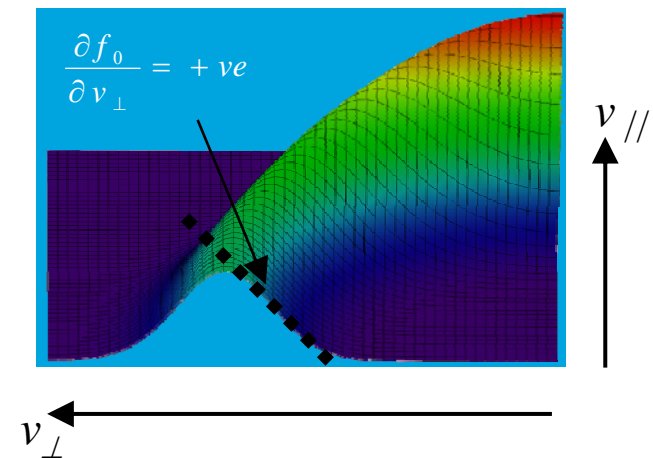
Horseshoe distribution formation



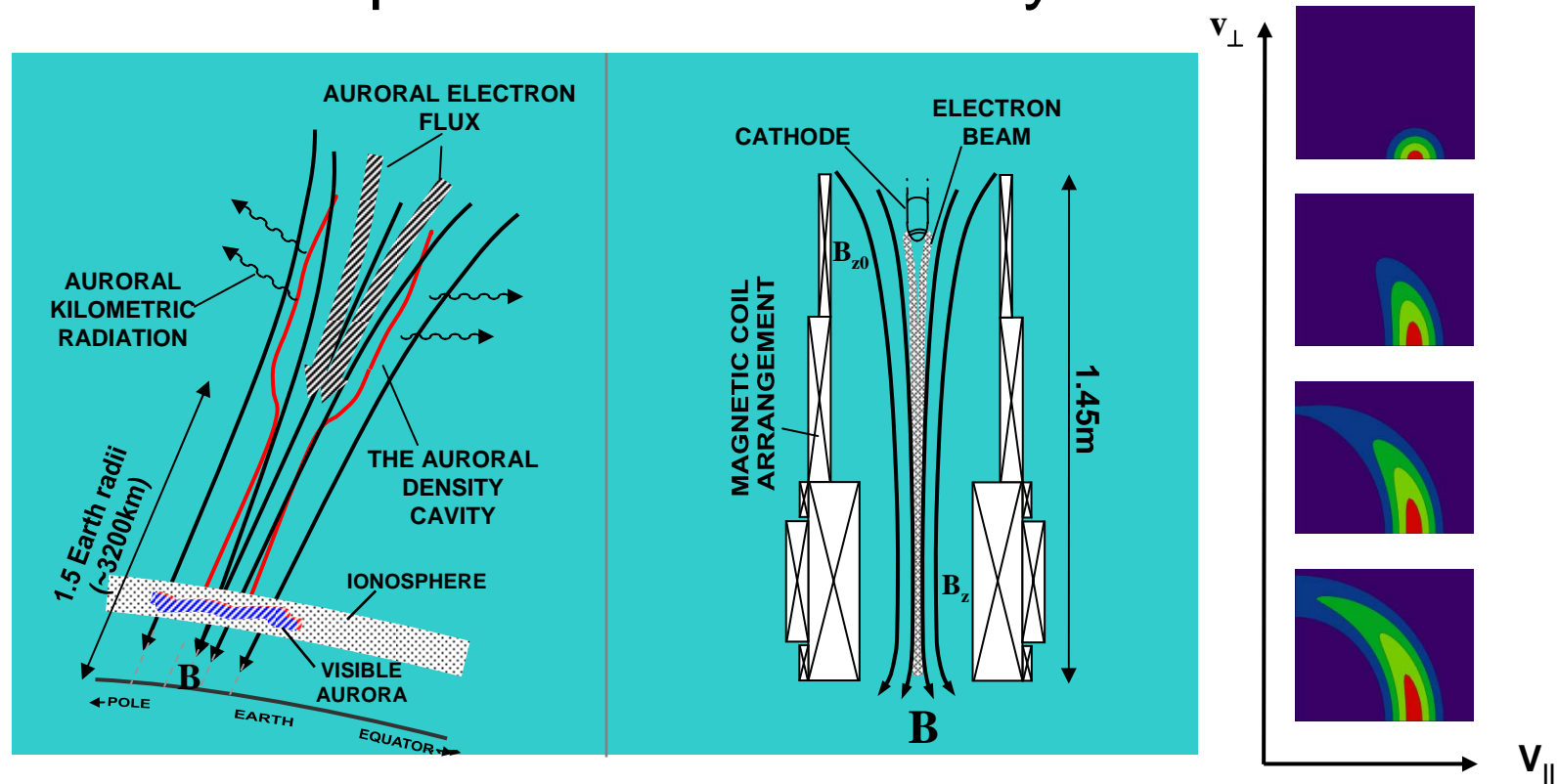
- When an electron propagates into an increasing axial magnetic field a horseshoe distribution may arise
- Reason - conservation of the magnetic moment, μ
- Conversion of axial velocity v_{\parallel} into perpendicular velocity v_{\perp} , results in an increase in electron pitch factor, α .

$$\mu = \frac{mv_{\perp}^2}{2B_0}$$

$$\alpha = v_{\perp} / v_{\parallel}$$



Space : Laboratory

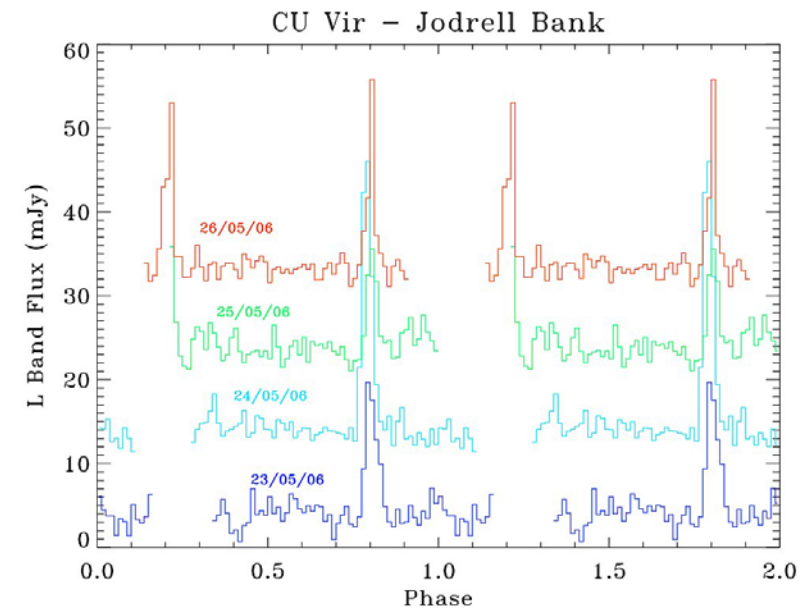
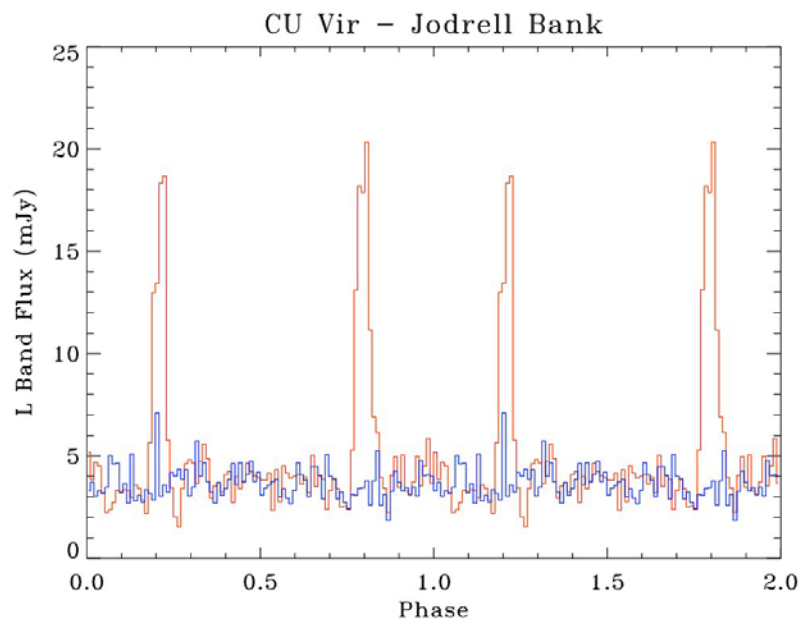


Objectives

- To form in the laboratory an electron beam with velocity distribution comparable to the magnetosphere
- Scale radiation resonance to the microwave range
- Characterise the electron beam parameters and take microwave measurements as function of magnetic compression
- Compare with numerical simulation and magnetospheric results

Similar astrophysical radio sources

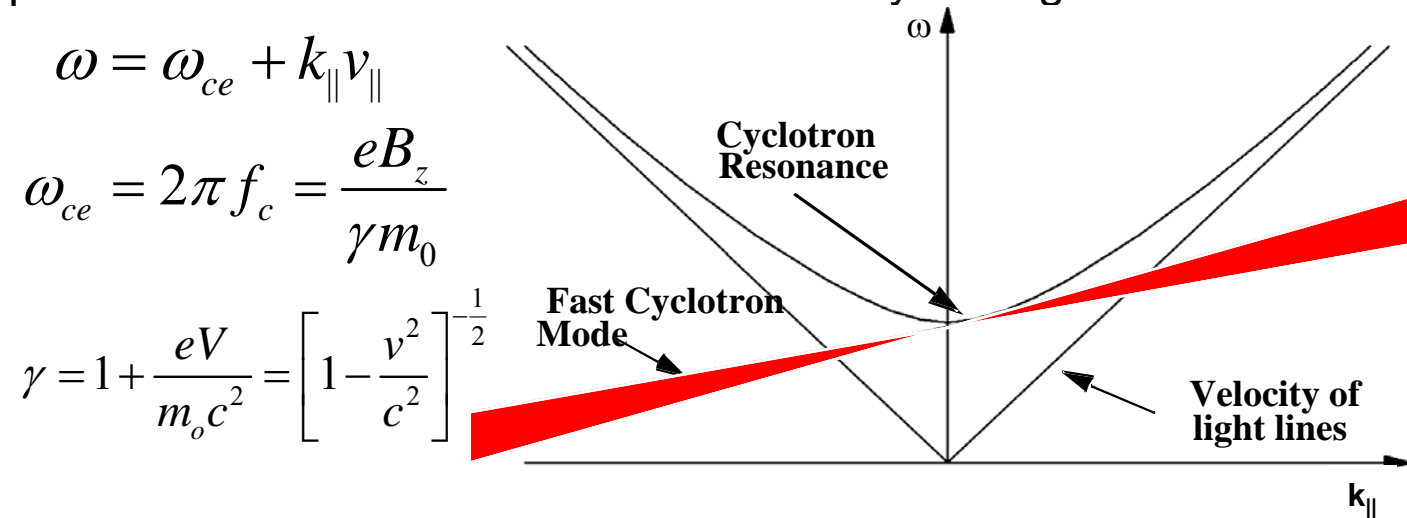
CU Virginis



- Recently observed by the telescopes at Jodrell Bank
- Highly reproducible L Band microwave emission from polar regions
- Strongly circularly polarised

Polarisation and dispersion

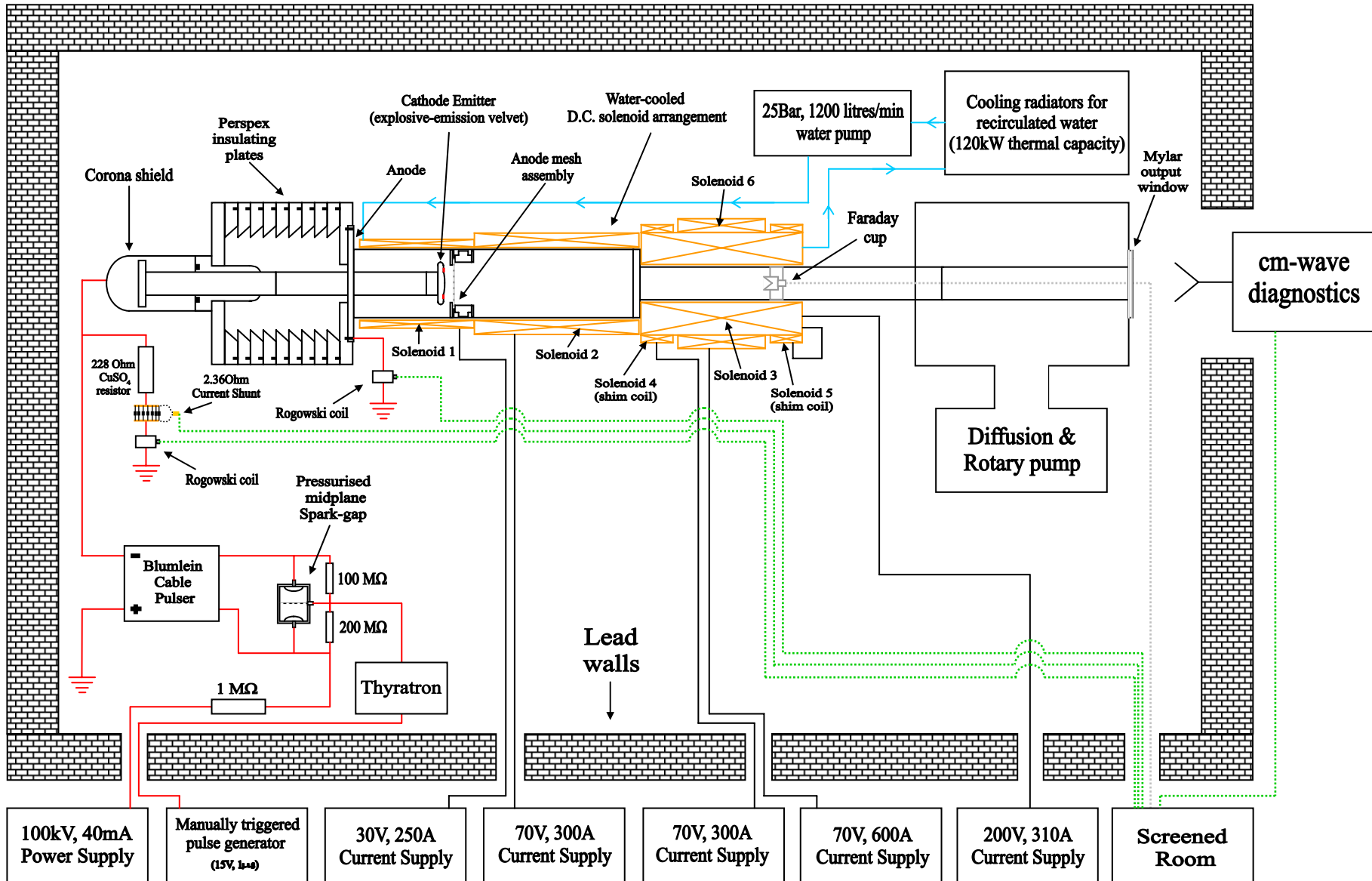
- Natural emission is in the X-mode, AC E-field and wavevector normal to static B-field
- Perpendicular wavevector can be achieved by waveguide modes near cut-off



Transverse field components for modes of cylindrical waveguides

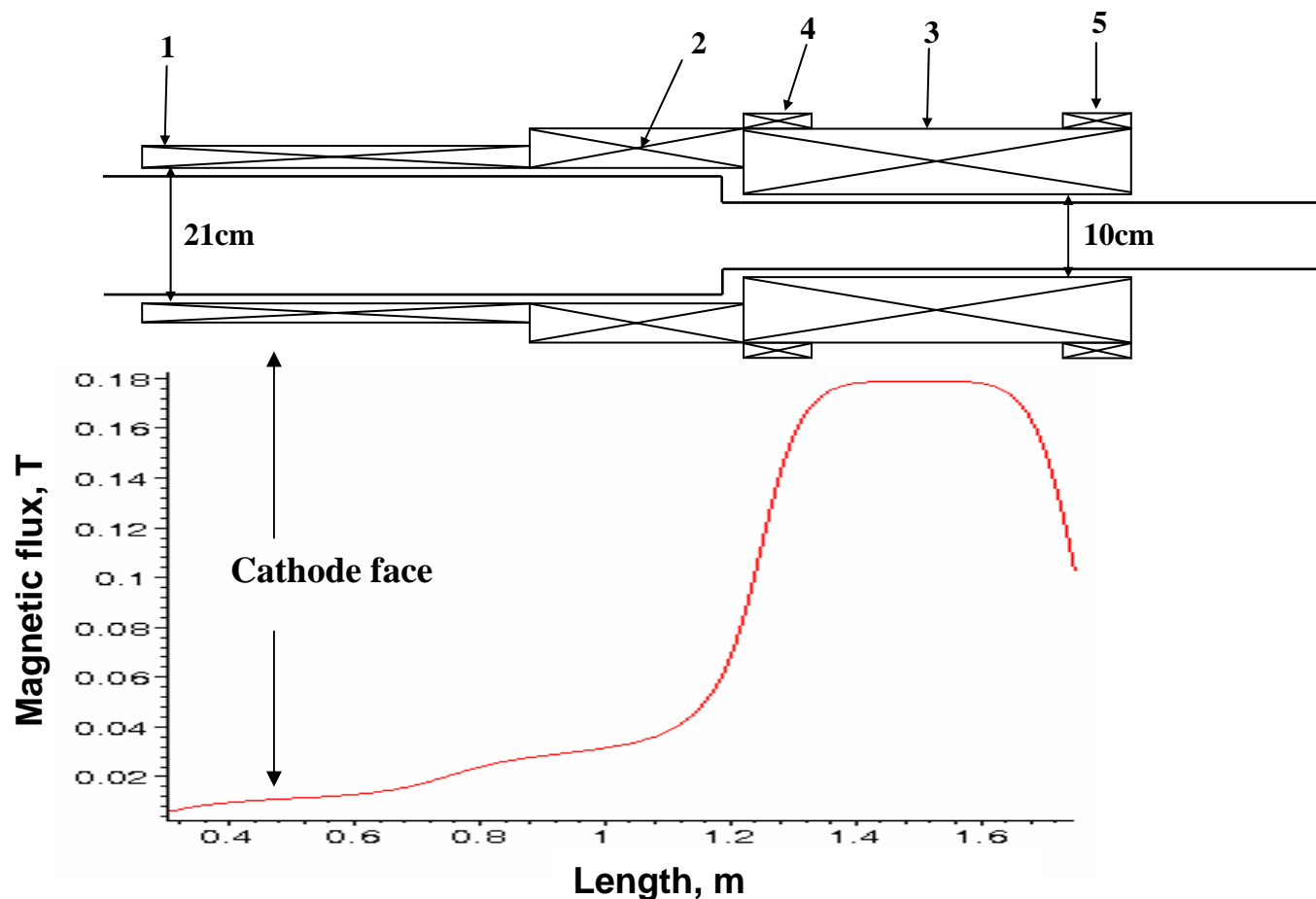
- Near cut-off modes are required to give the correct propagation orientation and minimise the Doppler broadening
- TE modes have finite transverse electric field when $k_{\parallel} \rightarrow 0$
- TM modes have zero transverse electric field when $k_{\parallel} \rightarrow 0$
- Using TE modes near cut-off gives an approximation to the X-mode

Experimental schematic

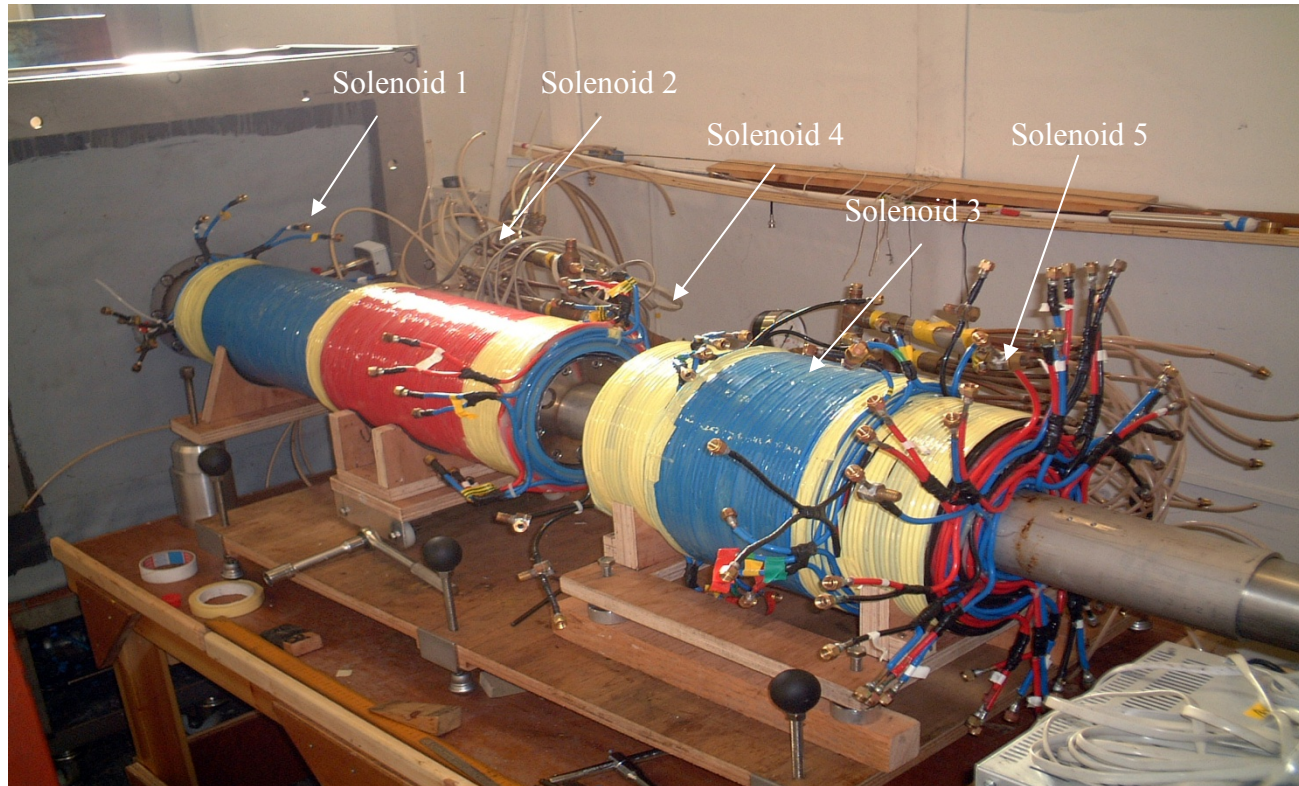


Solenoid configuration

- Insulated OFHC copper tubing, 7mm OD, 2mm ID (total length >1km) wound on non-magnetic formers, tubing is core cooled by water at 20Bar
- Drive 5 solenoids independently up to 300A with 120kW DC power supplies
- Flexible control of the magnetic field configuration



Experimental apparatus



Solenoid 1: 4 Layers, Length = 0.5m, $R_i = 0.105\text{m}$, Current = 75A.

Solenoid 2: 2 Layers, Length = 0.45m, $R_i = 0.105\text{m}$, Current = 60A.

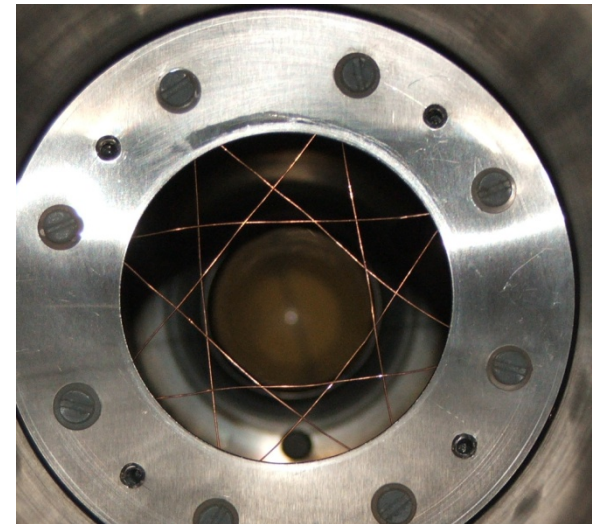
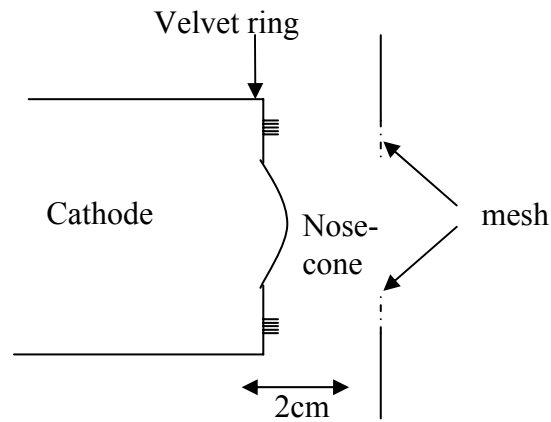
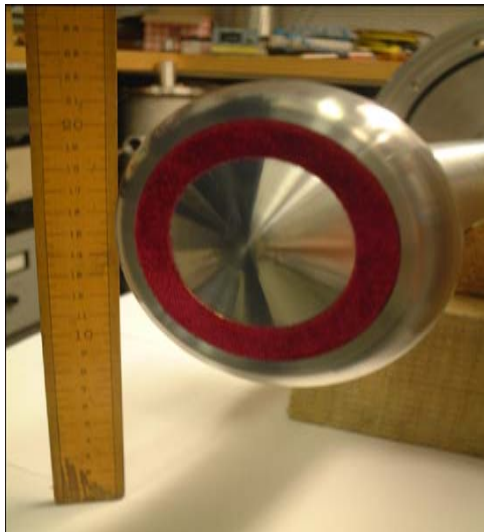
Solenoid 3: 10 Layers, Length = 0.5m, $R_i = 0.05\text{m}$, Current = 250A.

Solenoid 4: 2 Layers, Length = 0.11m, $R_i = 0.12\text{m}$, Current = 250A.

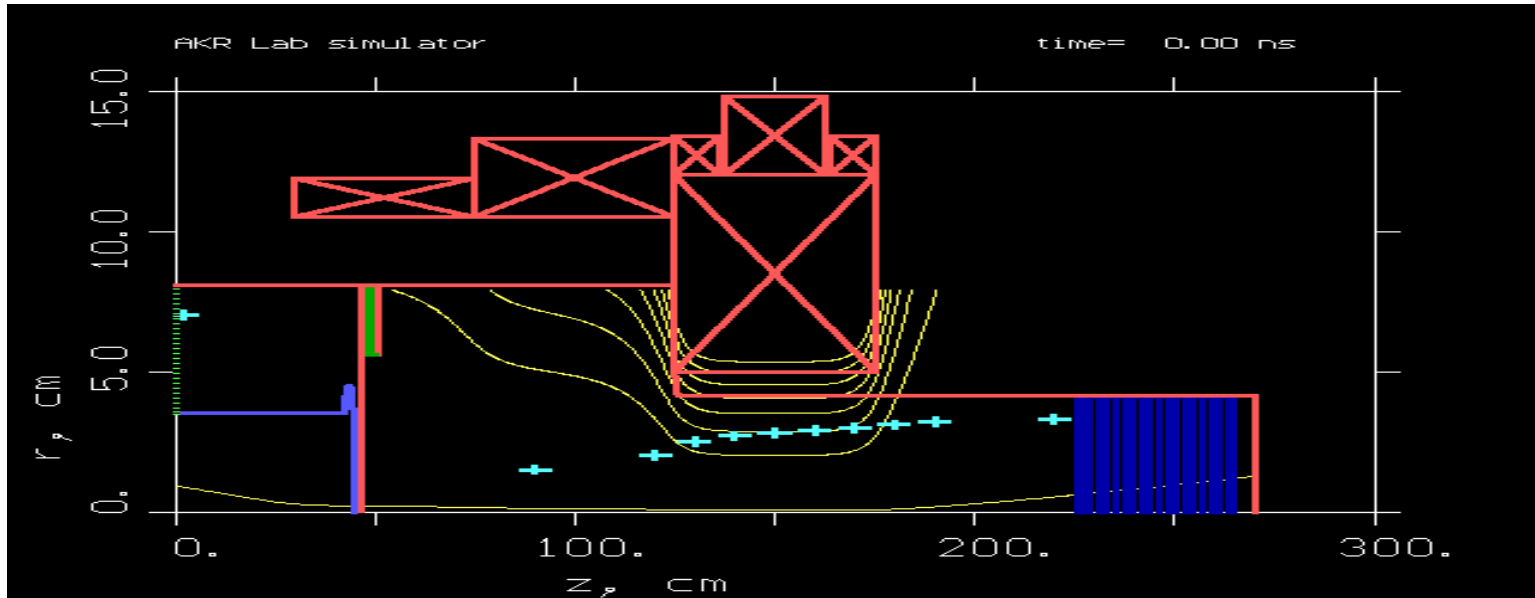
Solenoid 5: 2 Layers, Length = 0.11m, $R_i = 0.12\text{m}$, Current = 250A.

Vacuum spark electron injector

- Velvet electron emitter secured to a planar metallic surface facing a sparse mesh
- Cathode energised by a double Blumlein pulser generating over 75kV
- Field emission from velvet fibres combined with dielectric avalanche and surface flashover leads to a cathode plasma flare
- Space charge limited emission into vacuum gap
- Mesh concentrates electric field close to cathode



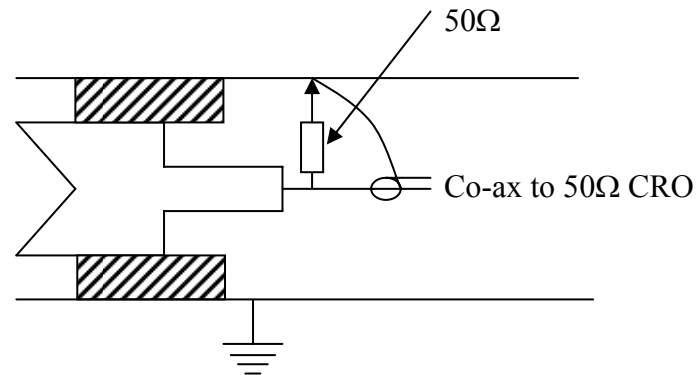
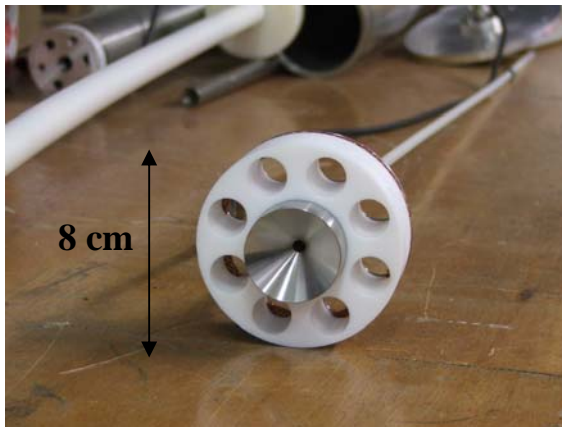
Experimental geometry



- Solenoid sizes set by power and cooling constraints
 - Sets dimensions of the rest of the apparatus
 - Electron gun region 16cm in diameter
 - Resonant region 8cm diameter and 20cm length
- Maximum possible fill factor ~50% (radius)
- Evacuated to $<10^{-6}$ mBar

Electrical diagnostics

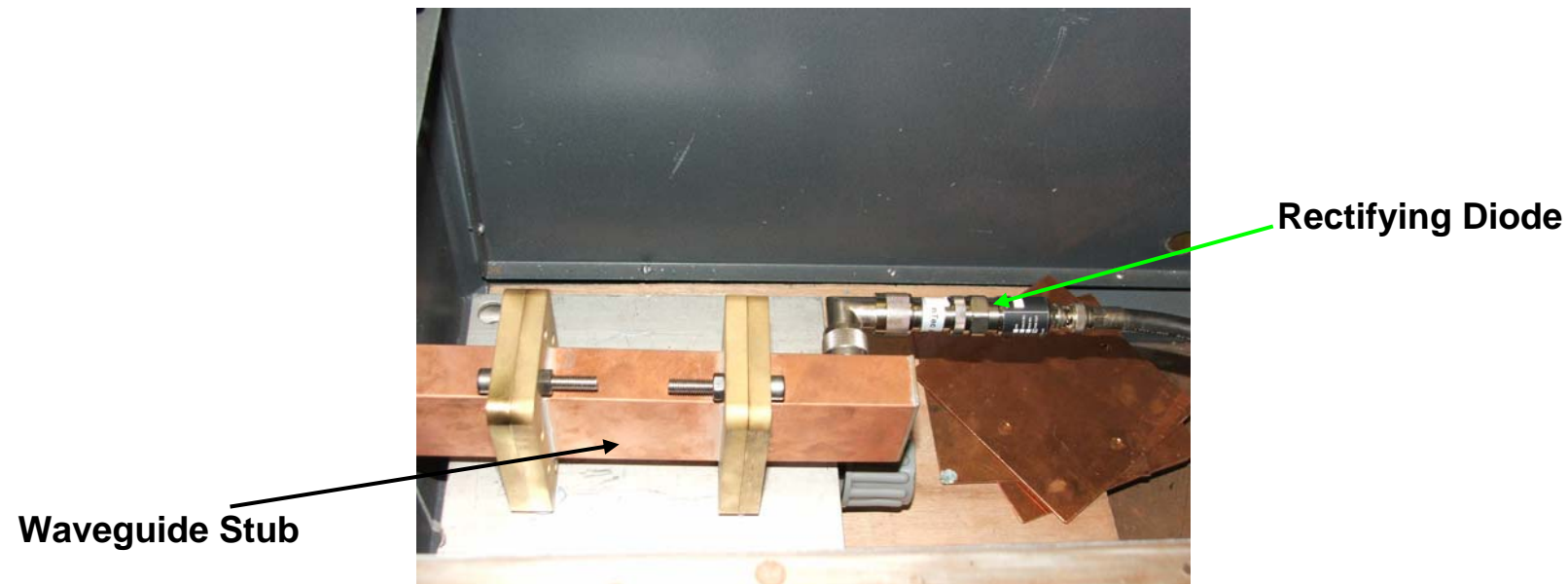
- Diode voltage:
 - Matching resistor (230Ω) in shunt with accelerator
 - Current measured by a Rogowski belt
- Diode current:
 - Rogowski belt (in ground connection of anode)
- Beam current:
 - Faraday cup feeding 50Ω shunt resistor



- Cup shaped to inhibit secondary escape

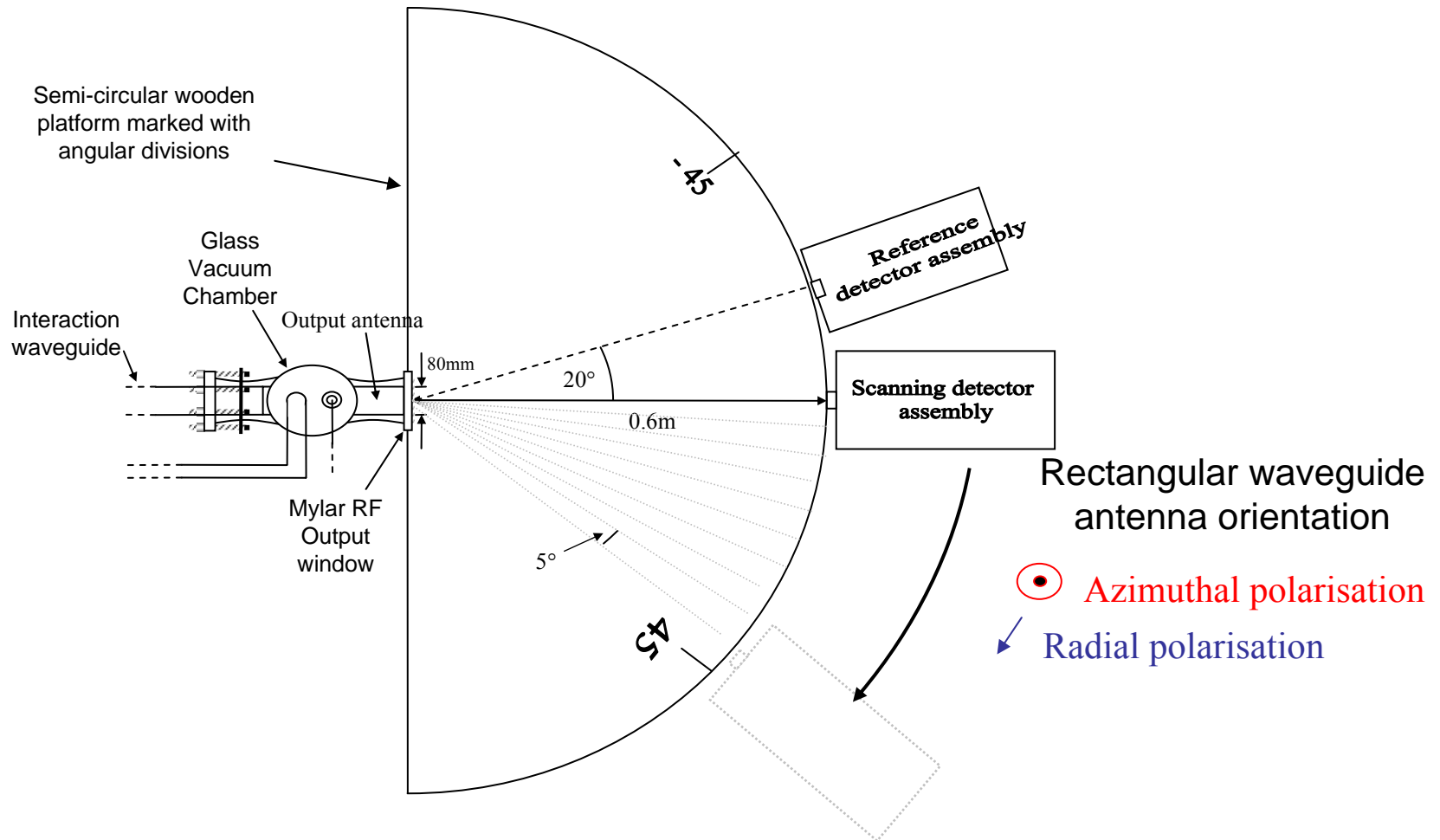
Microwave detection: Amplitude and Spectrum

- Waveguide 12 (single mode at 4.42GHz) or Waveguide 18 (single mode at 11.7GHz) antenna in far field of experiment output
- Fitted with calibrated attenuators
- Signals delivered to calibrated rectifying diodes
- Rectified signals measured on a 1.5GHz digital oscilloscope
- Spectrum measured by FFT of AC waveform captured by 12GHz DSO



Microwave detection: Polarisation and Propagation

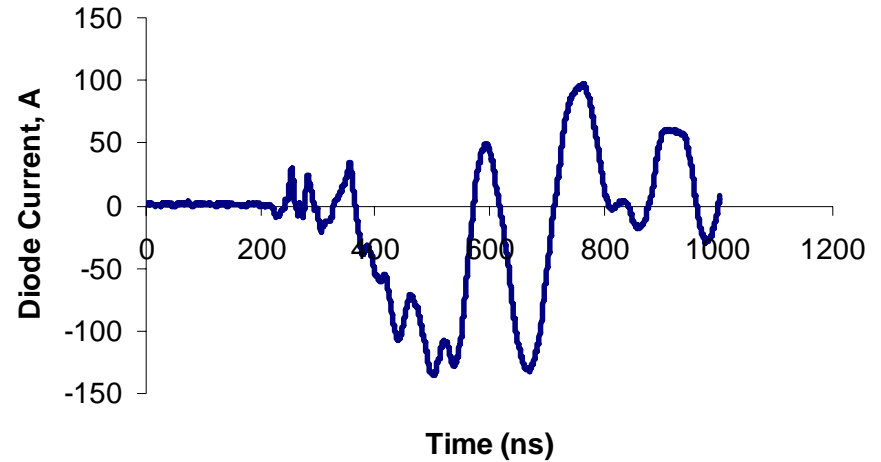
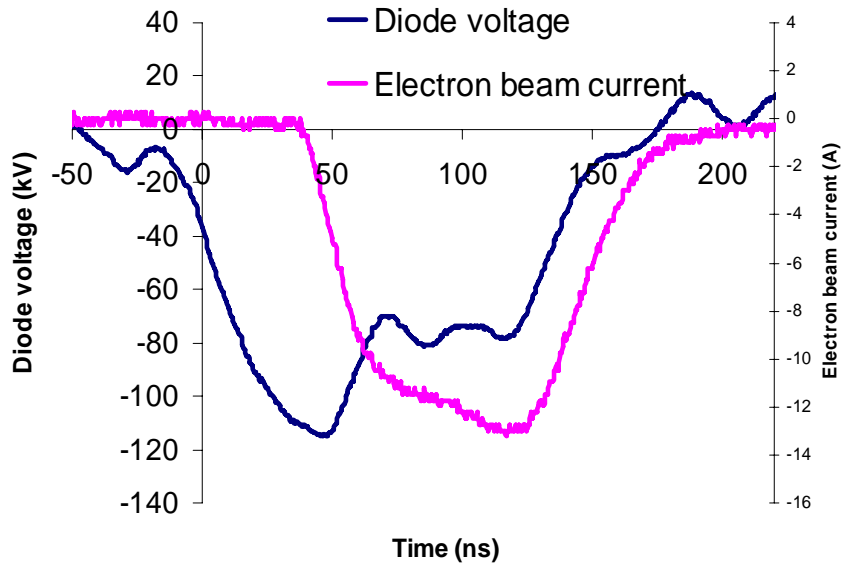
- Waveguide stub receiving antenna - output pattern and polarisation
- Waveguide attenuators and rectifying diodes - operating efficiency



Experimental and numerical studies

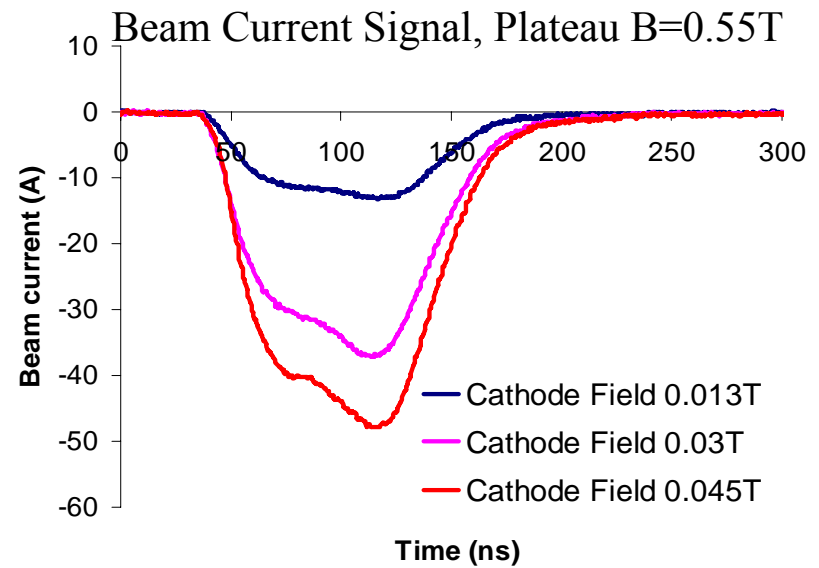
- Beam formation investigated, numerically and experimentally
- Two regimes of radiation generation were studied:
 - 4.42GHz resonance, plateau $B=0.18\text{T}$
 - Expected mode $\text{TE}_{0,1}$
 - Relatively low order mode and magnetic flux density
 - Potential to measure the electron velocity distribution
 - 11.7GHz resonance, plateau $B=0.48\text{T}$
 - Resonant mode $\text{TE}_{0,3}$
 - Highly overmoded, $\lambda \ll D$, high magnetic flux density
 - Chosen as most representative of magnetosphere

Experimental results: Beam formation

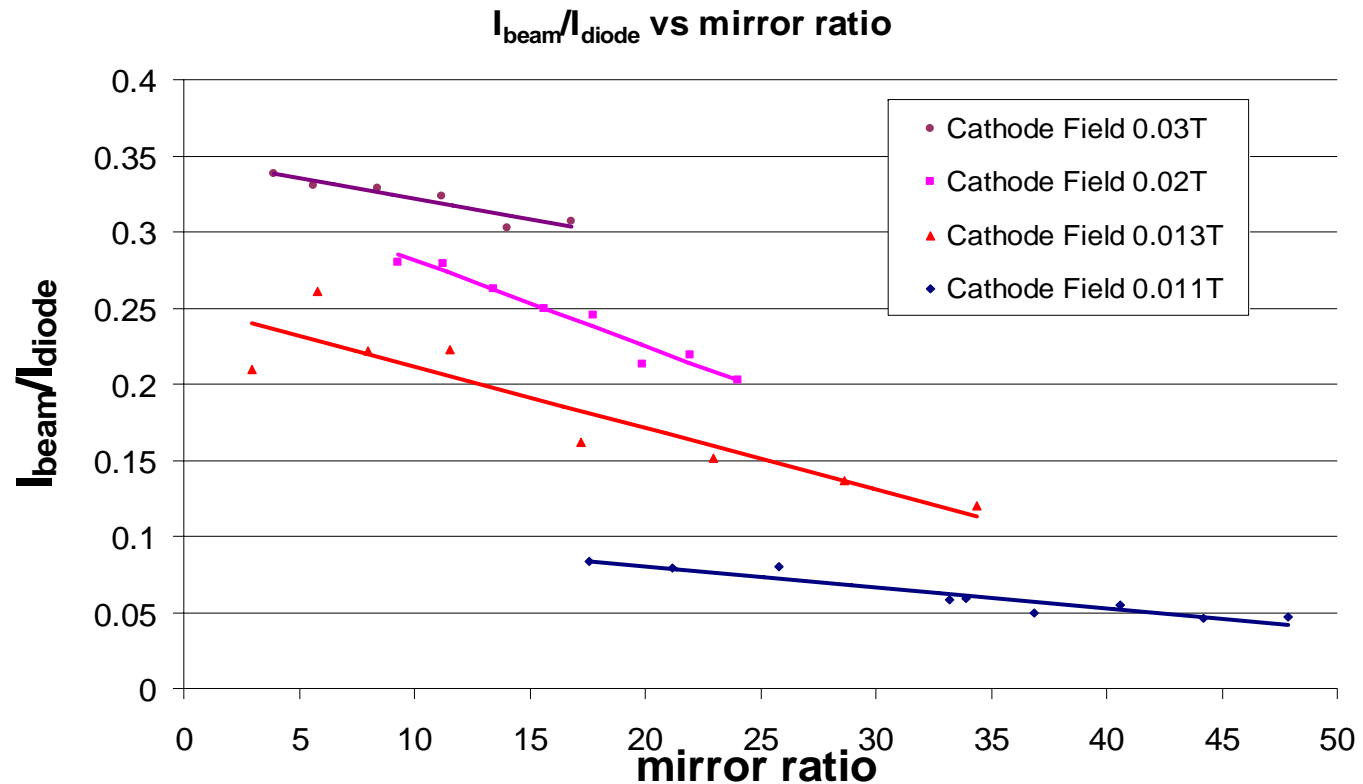


0.18T on main coil, beam voltage 75kV:

- Mirror Ratio of 17 gave I_{beam} of 12A
- Mirror Ratio of 9 gave I_{beam} of 34A
- Mirror Ratio of 4 gave I_{beam} of 44A

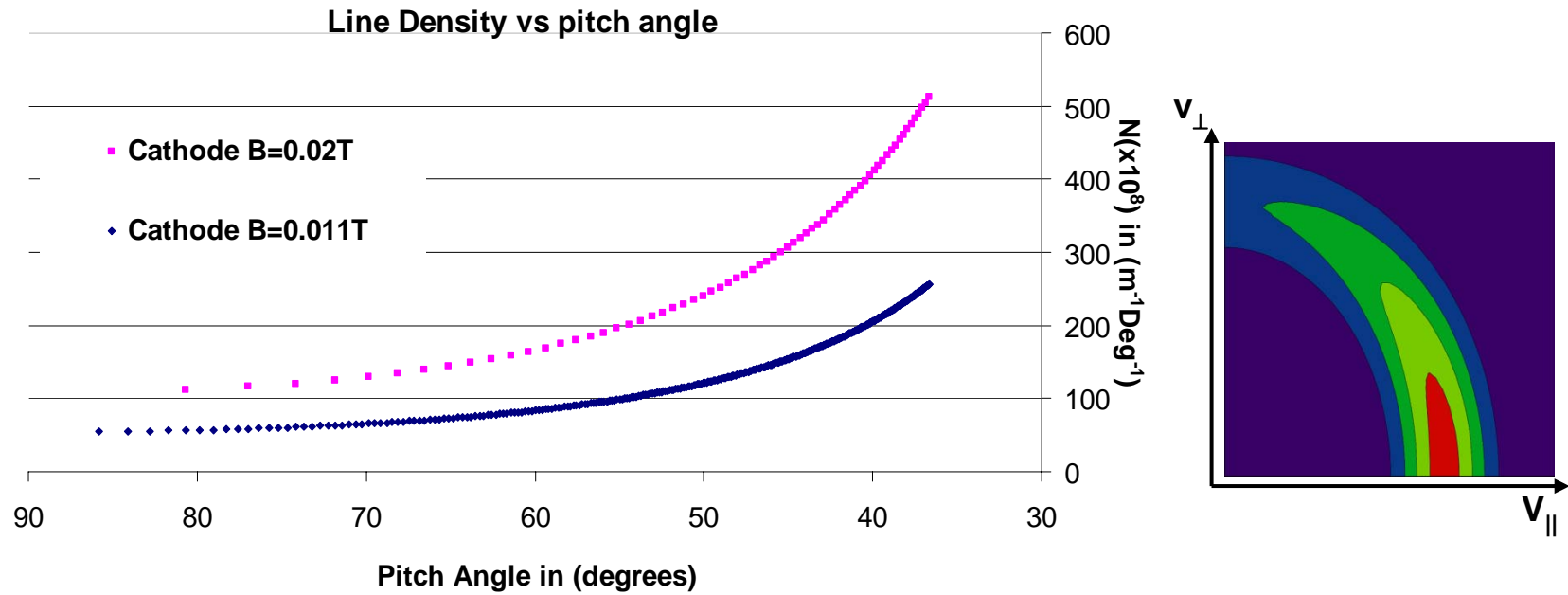


Beam transport measurements



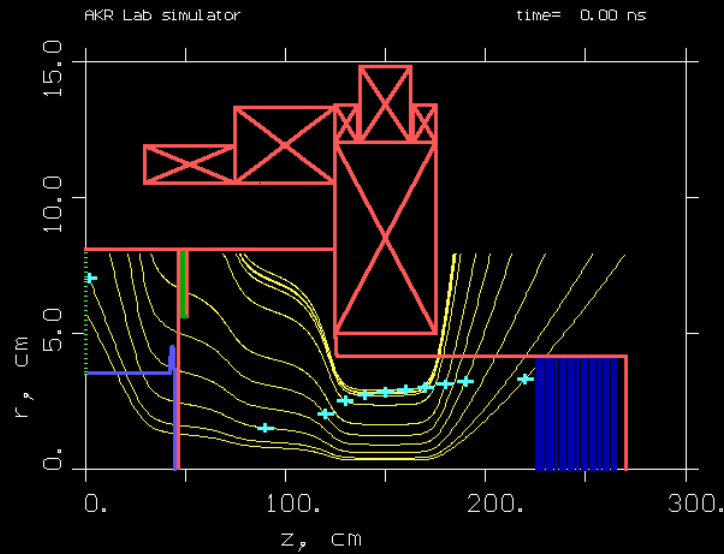
- Progressive decrease in current with increasing mirror ratio
- Demonstrates formation of horseshoe distribution

Estimation of 1D number density

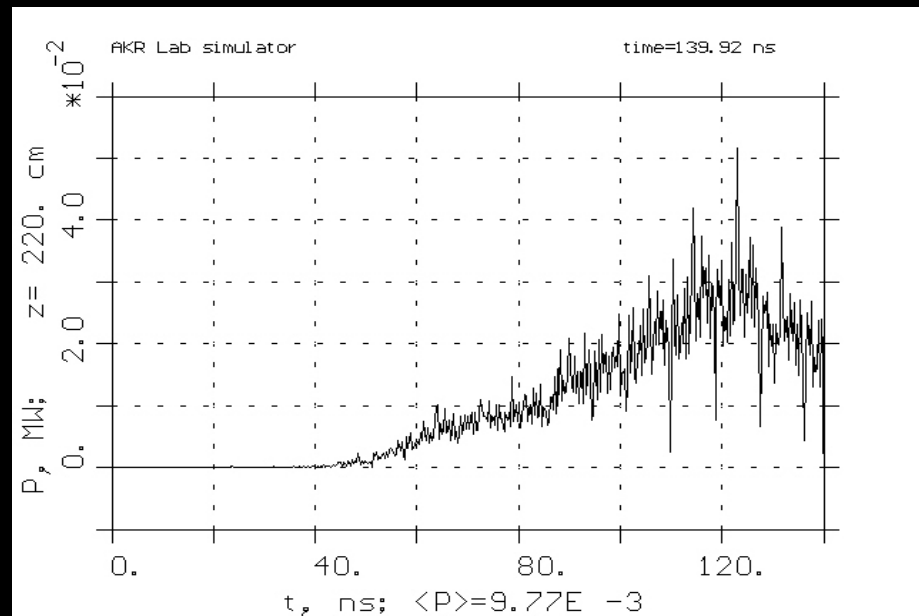
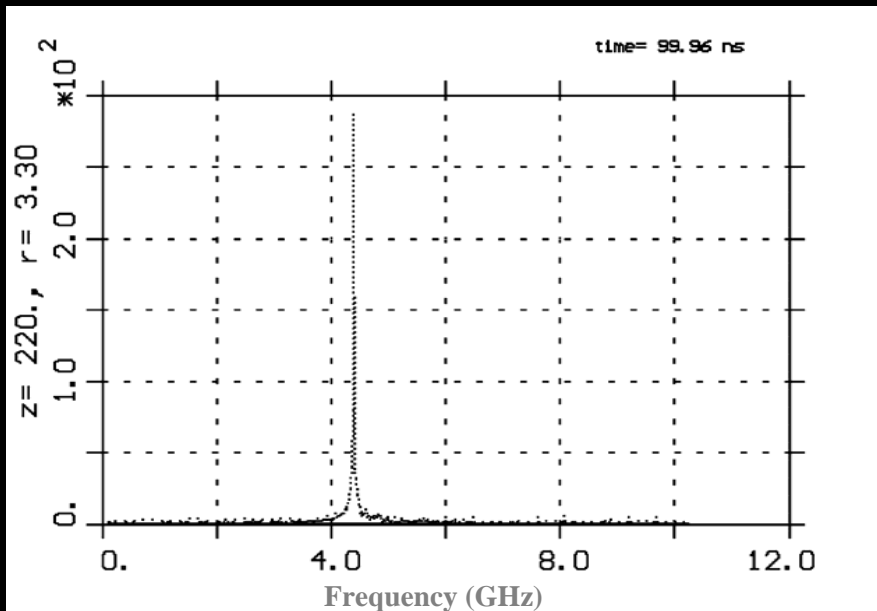


➤ Pitch angle is $\arctan(v_{\perp} / v_z)$

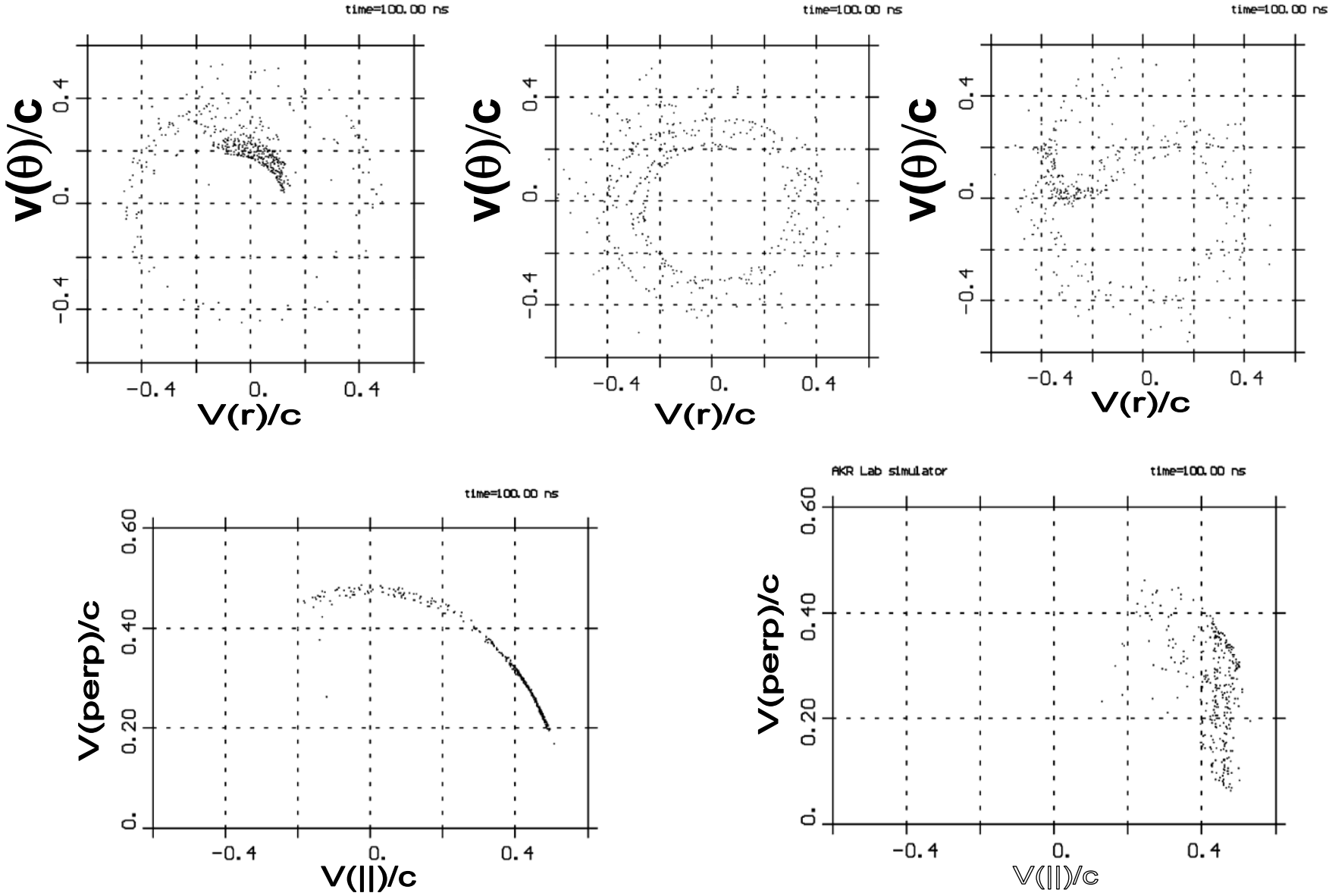
4.42GHz Numerical simulations



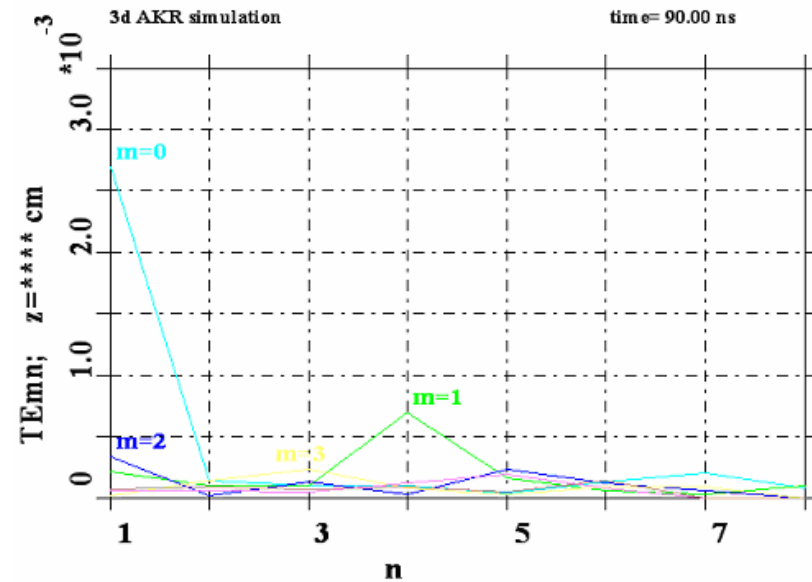
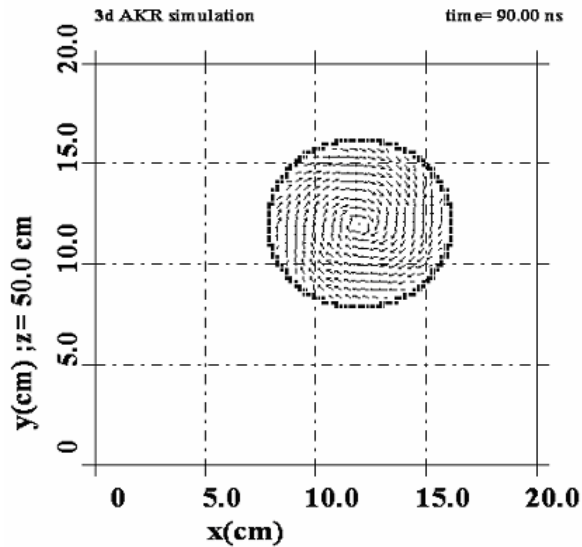
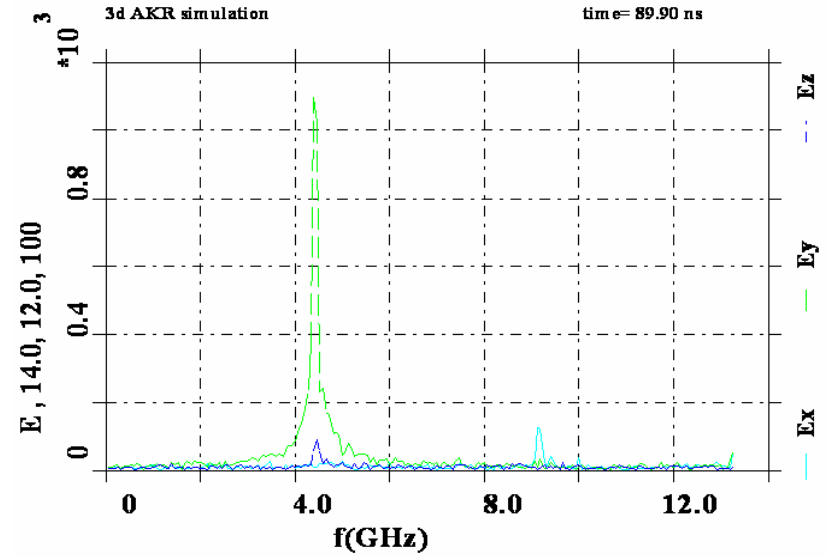
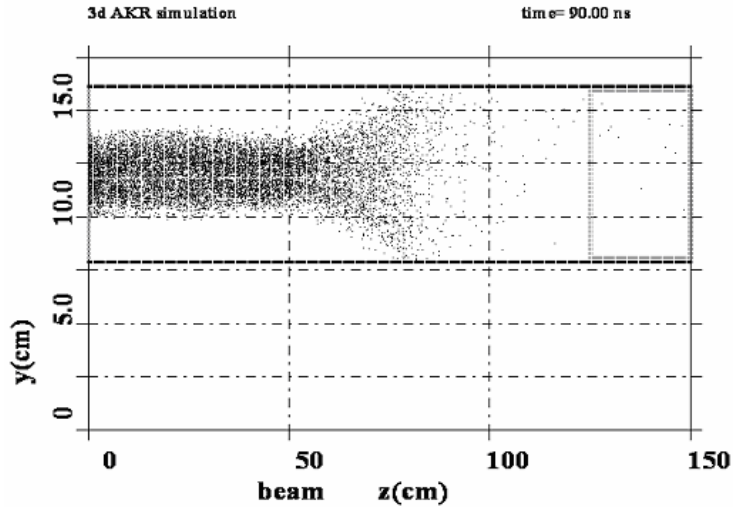
- Geometry programmed into KARAT, a 2D axisymmetric PiC (Particle in Cell) code
- Highest η at 1% cyclotron detuning
- Cathode $B=0.011T$, power ~ 20 kW, $\eta=1.7\%$
- Cathode $B=0.02T$, power ~ 50 kW, $\eta=2\%$



2D Simulations: Electron velocity distributions

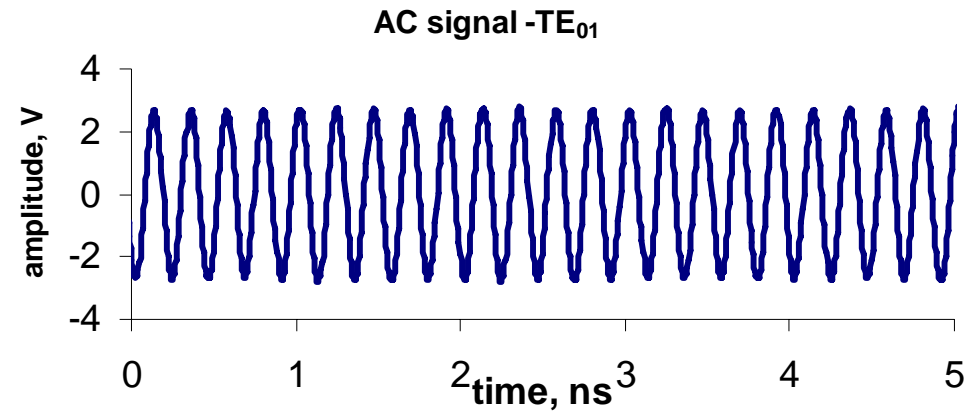


4.42GHz 3D Simulations

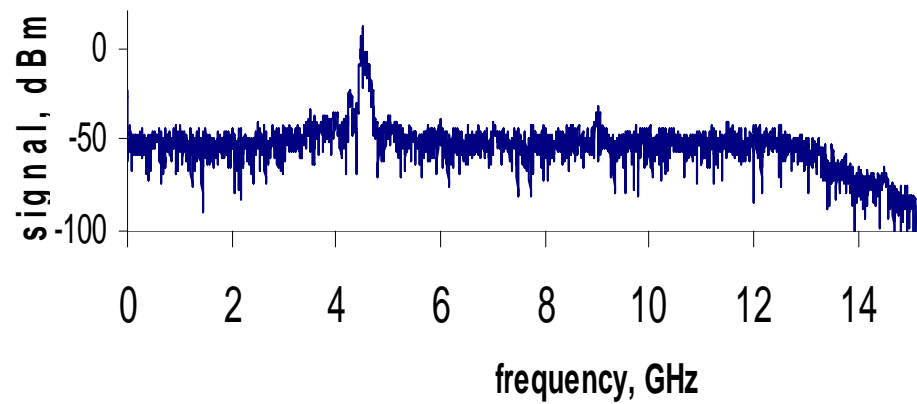


Microwave spectral measurements - 4.42GHz

- 12GHz Real-time oscilloscope
- AC waveform captured
- Fourier transform gives frequency



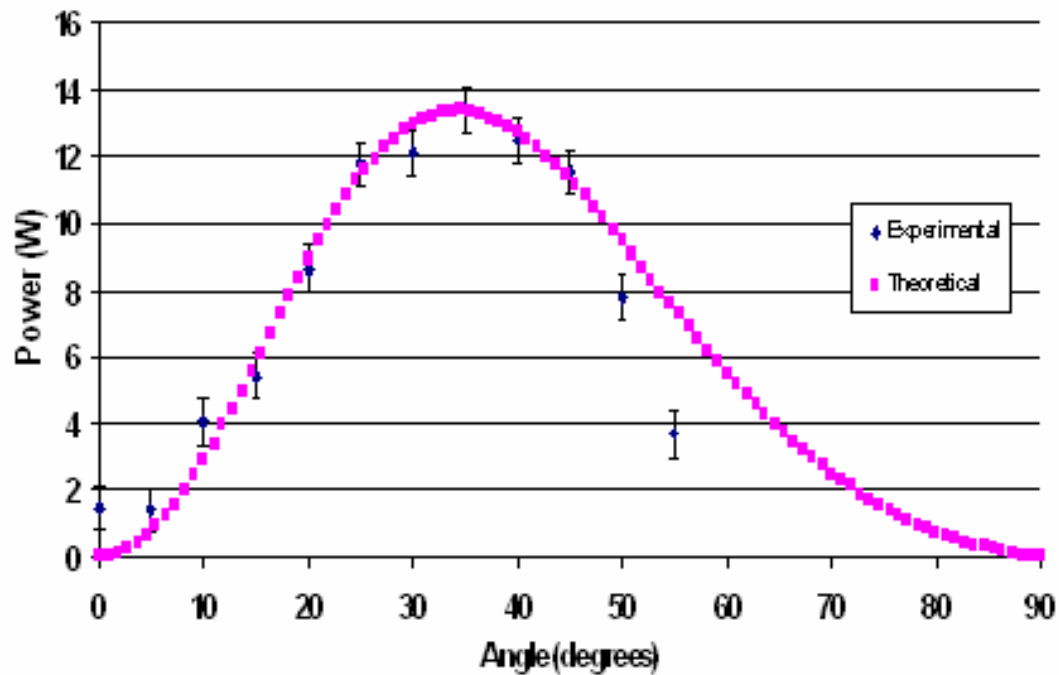
Fourier Transform



- Spectral peak at ~4.42GHz
- Close to cut-off for TE₀₁
- Second harmonic at ~8.84GHz

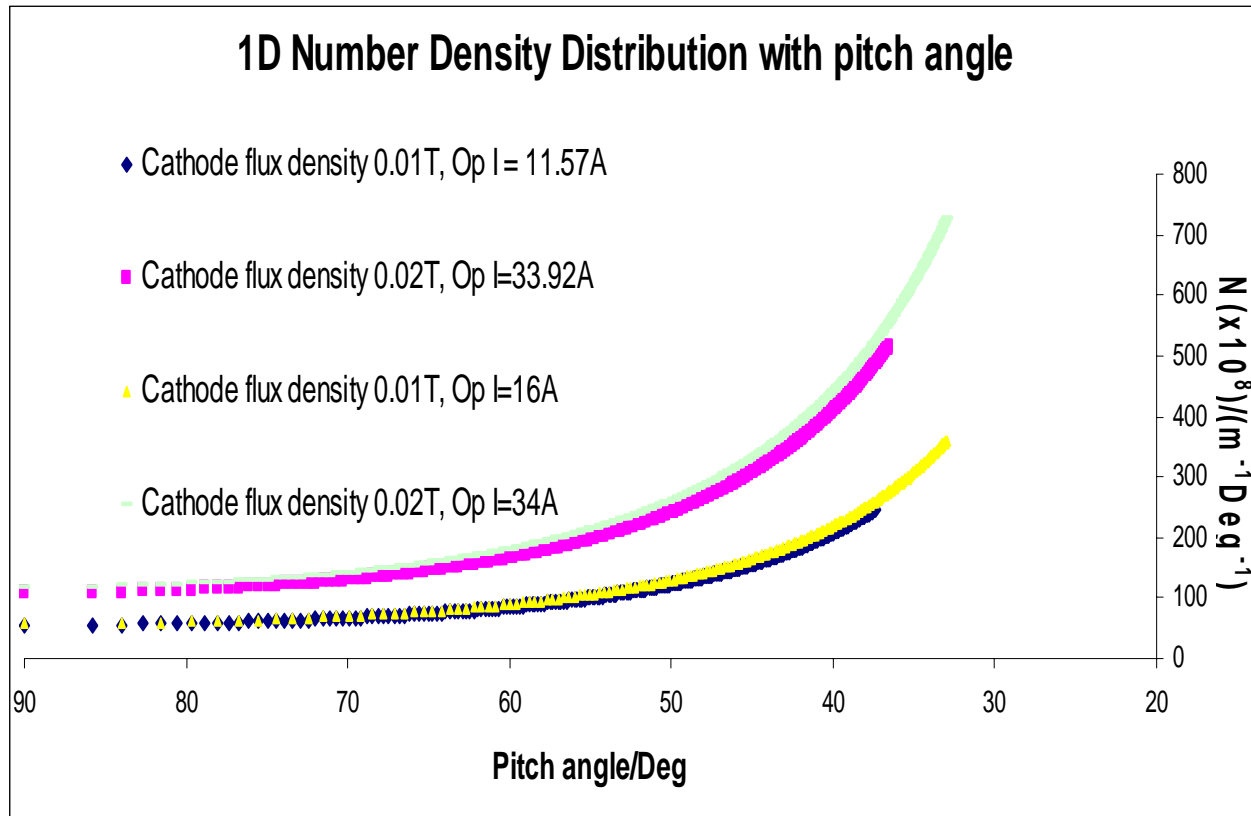
Microwave amplitude and polarisation measurements at 4.42GHz

Antenna Pattern: Mirror Ratio 9



- Integrated antenna pattern:
- Radial polarisation gave no output
- Azimuthal polarisation:
 - Cathode $B=0.011T$ ~ 19 kW
 - Cathode $B=0.02T$ ~ 35 kW
- Results consistent with 1D number density measurements
- Max efficiencies of ~2% for mirror ratio of 17, despite lower power
- Highest η at cyclotron detuning 2.4%

Comparison of numerical and experimental results

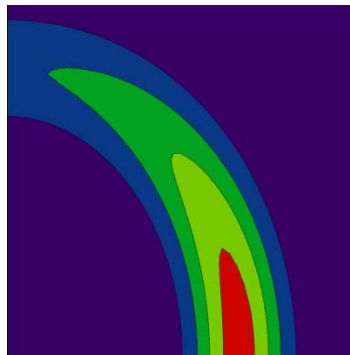


For cathode flux density 0.01T

<u>Exp</u>	<u>Num</u>
$I_{in}=121A$	$I_{in}=18A$
$I_{out}=11.57A$	$I_{out}=16A$
$P_{out}=19kW$	$P_{out}=20kW$

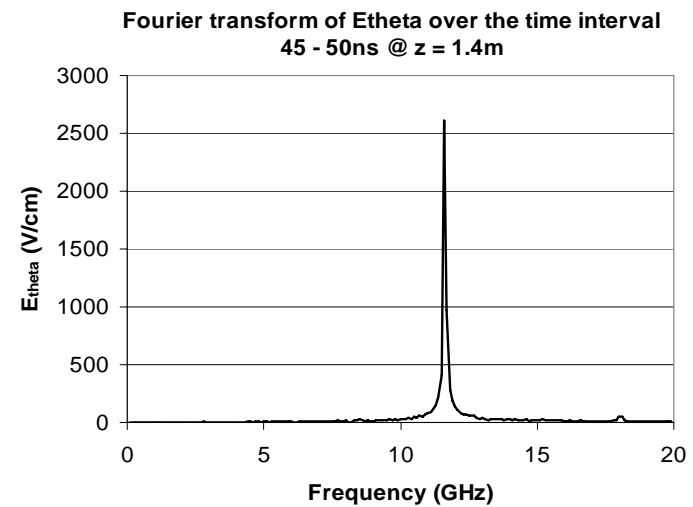
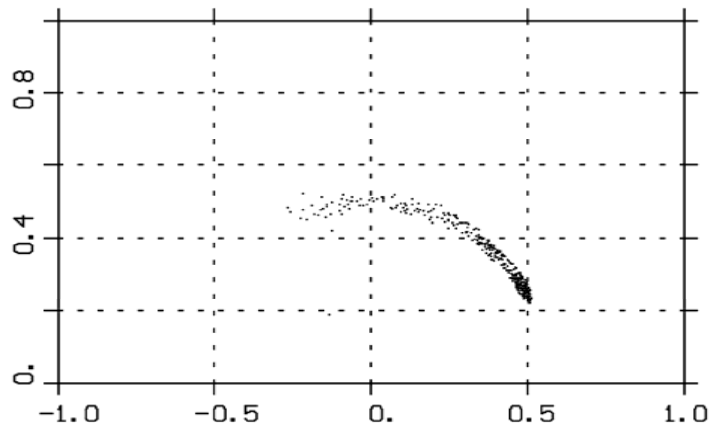
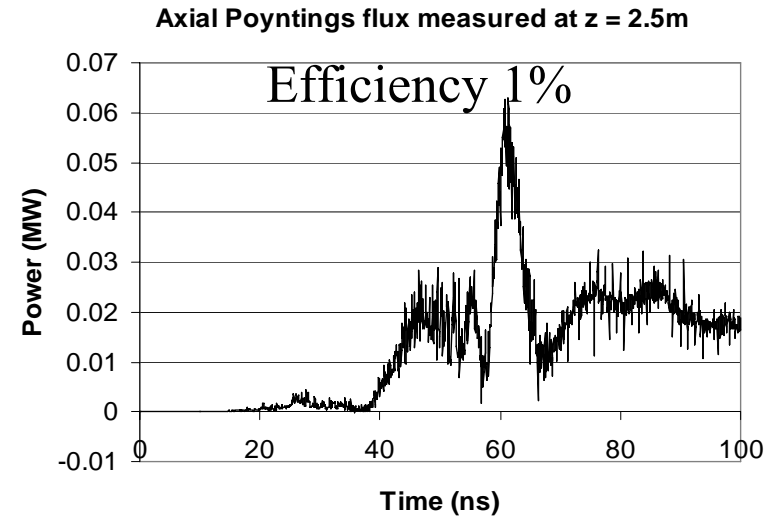
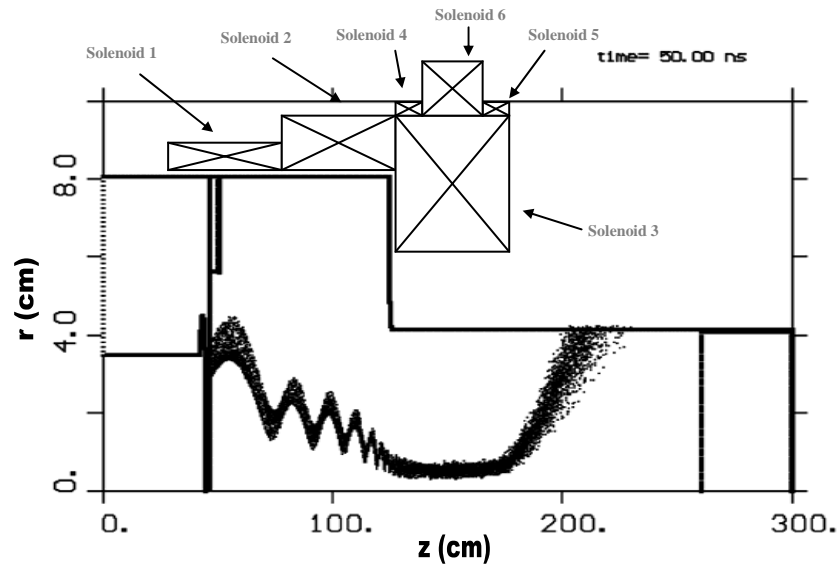
For cathode flux density 0.02T

<u>Exp</u>	<u>Num</u>
$I_{in}=208A$	$I_{in}=35A$
$I_{out}=33.92A$	$I_{out}=34A$
$P_{out}=35kW$	$P_{out}=50kW$

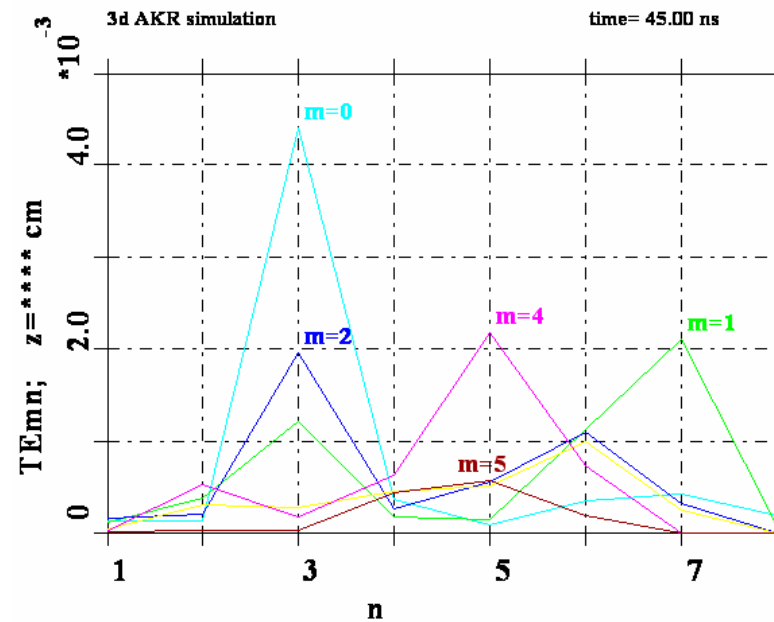
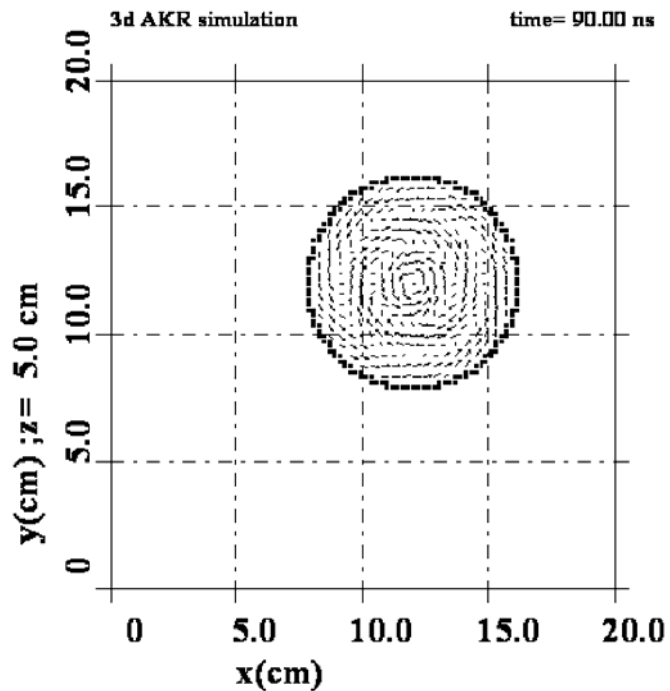
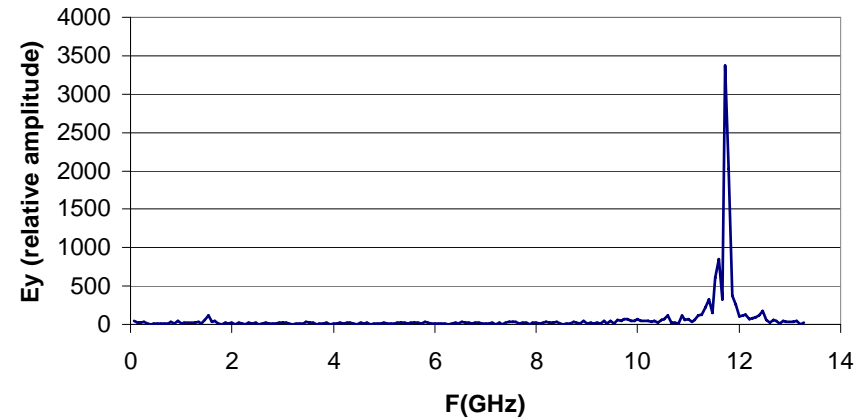
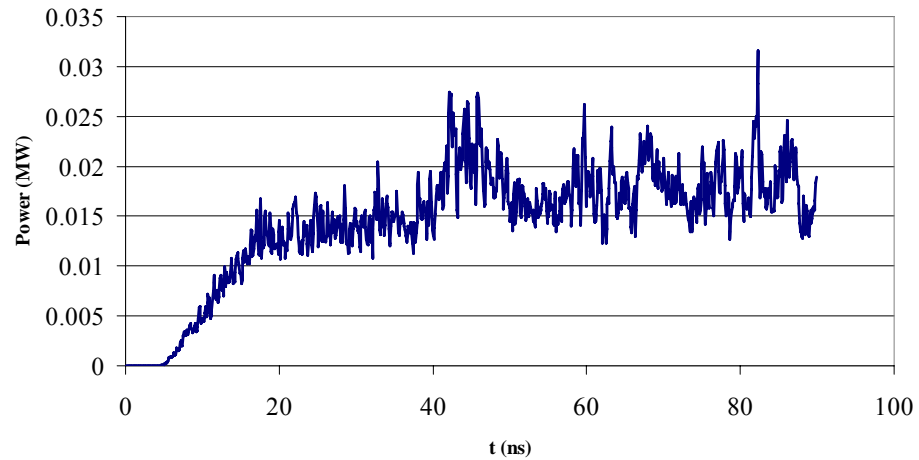


➤ Pitch angle is $\arctan(v_{\perp} / v_z)$

11.7GHz 2D Numerical Results

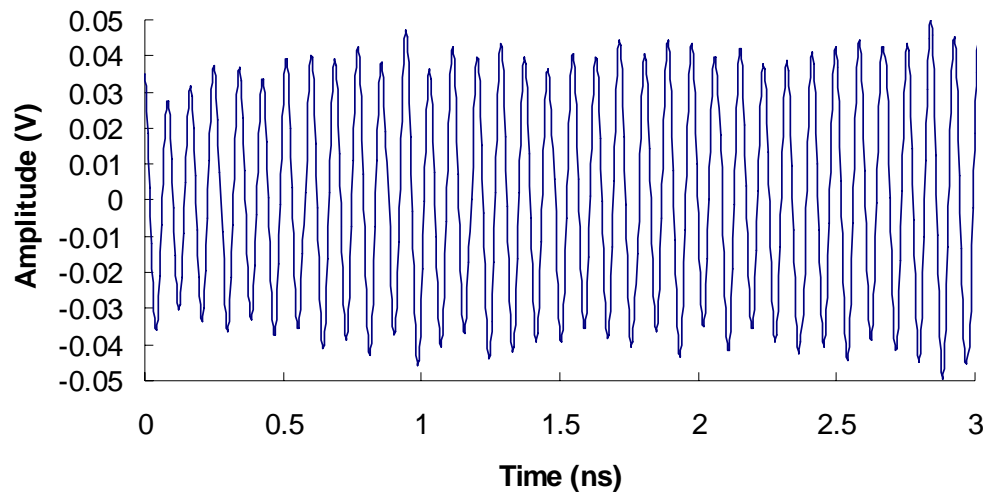


11.7GHz 3D Numerical Simulations

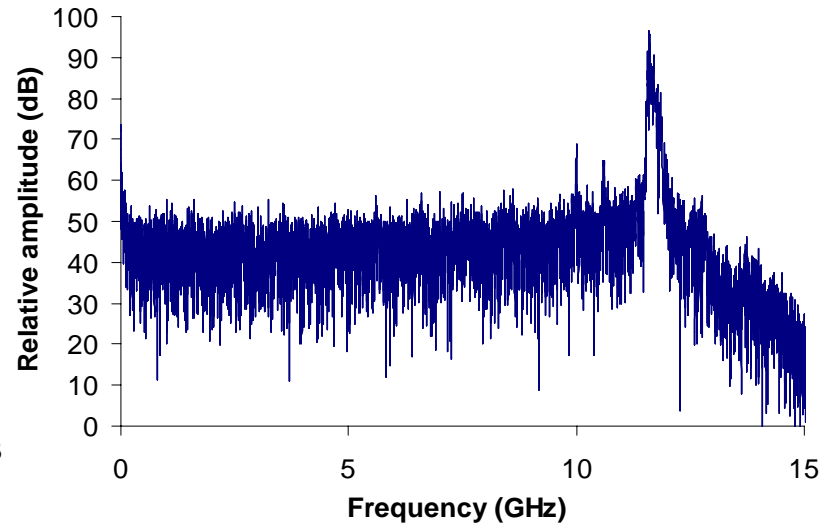


Microwave Spectral Measurements- 11.7GHz

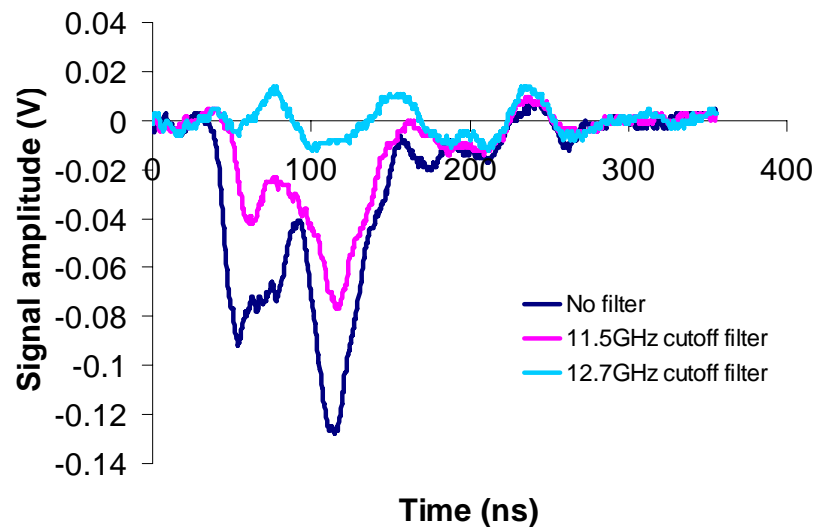
AC output 0.48T
($B_z/B_{z0} = 16$)



Fourier Transform of AC wave

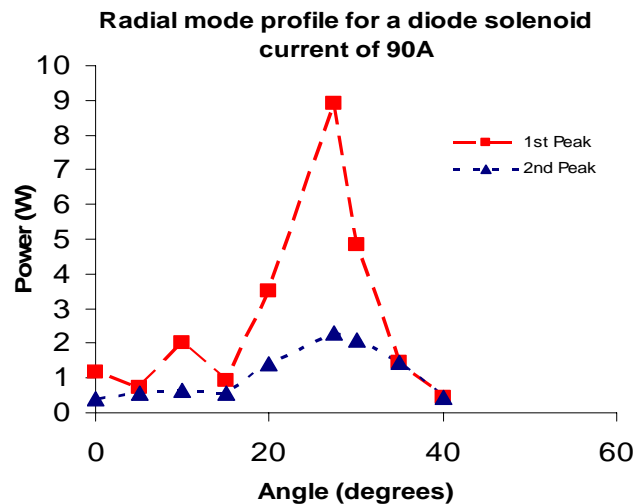
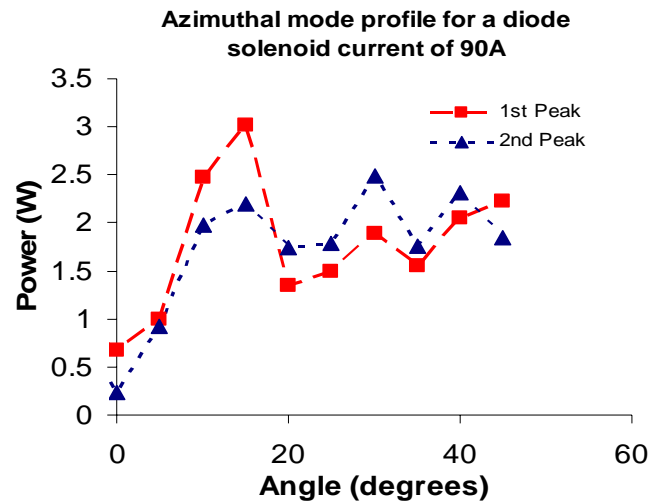


Rectifying crystal output with filters



- Spectral peak at 11.7GHz
- Evidence of backward wave Doppler downshift component
- Close to cut-off for TE_{03}
- Close to CRO Bandwidth
- Check with waveguide filters

Microwave amplitude and polarisation measurements at 11.7GHz



- Antenna Pattern indicated complex mode mixture
- Dominant mode changed with time
 - mode competition and hopping
- Radiation in both polarisations
- TE_{03} and TE_{23} modes present
- Integration of antenna pattern
- Max efficiencies of ~1% with peak output power ~20kW

Conclusion

- Succeeded in forming electron beam with Horseshoe velocity distribution
 - Number density mapped as a function of pitch angle
- Numerical simulations predict instabilities with efficiencies ~1-2%
- Microwave measurements confirmed instability of distribution to cyclotron emissions
 - Radiation frequency slightly $>$ relativistic cyclotron frequency
- The antenna pattern measurements illustrated near cut-off TE modes as numerically predicted
- Experimental efficiencies comparable with the numerical predictions
- Wave polarisation, propagation similar to X mode
- Generation efficiencies compare well with some auroral estimates

Future work

- Investigate Doppler shifted regimes of resonance
 - Measure the resilience of the instability to parallel propagation
 - Build convective experiment to measure spatial growth rate
- Bridge gap to unbounded geometry
 - Numerical simulations underway to study cyclotron instabilities in the absence of 'hard' radiation boundaries
- Investigate influence of background plasma
 - Numerical studies underway of magnetised-plasma loaded waveguides
 - Experimental modification to include a plasma background- possibly a quasi-Penning trap

Acknowledgements

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