



**The Abdus Salam
International Centre for Theoretical Physics**



1965-11

**9th Workshop on Three-Dimensional Modelling of Seismic Waves
Generation, Propagation and their Inversion**

22 September - 4 October, 2008

**Geophysical modelling and GPS, SAR, GRACE and GOCE
data for the understanding of lithospheric
and mantle processes Part 1 & 2**

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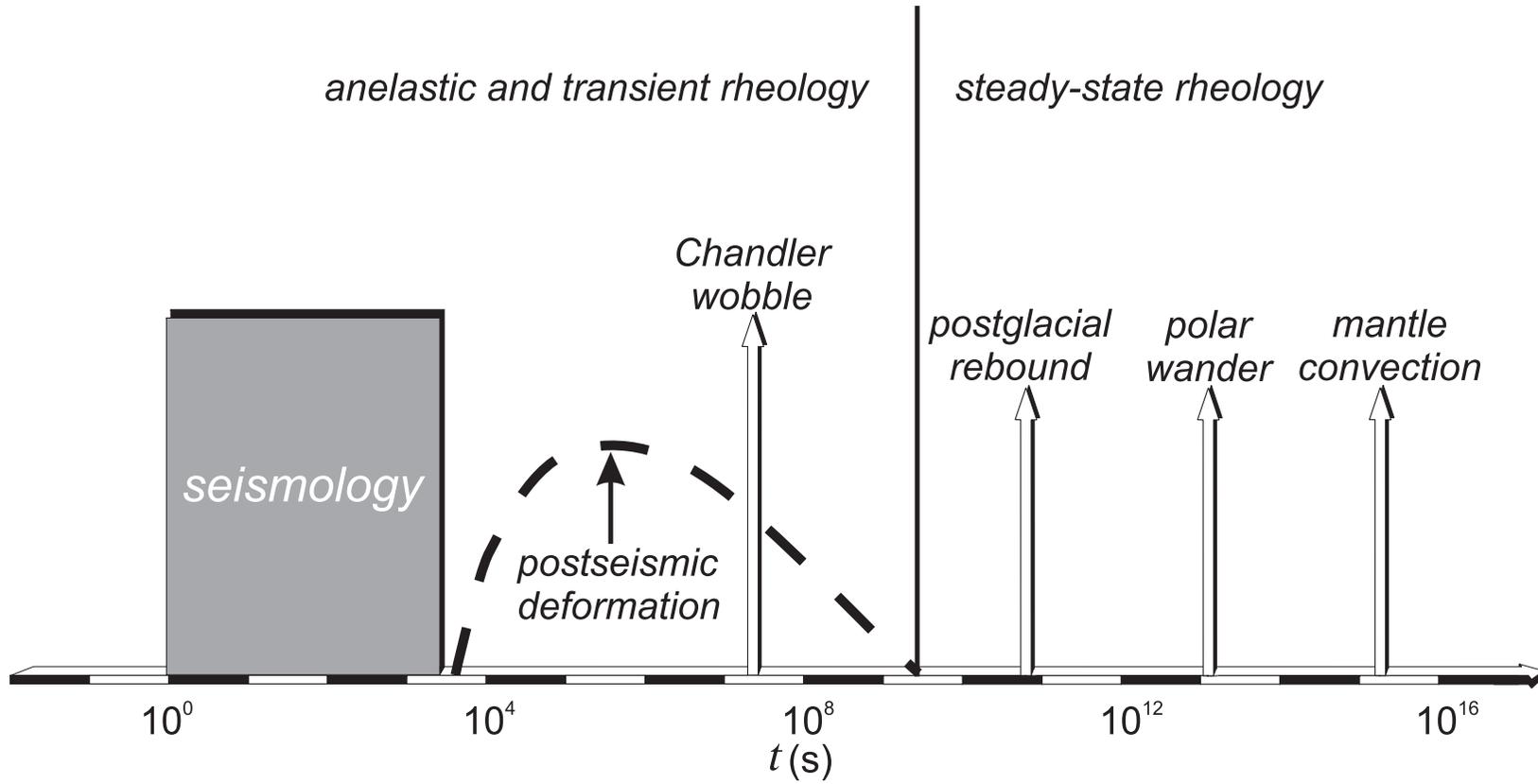


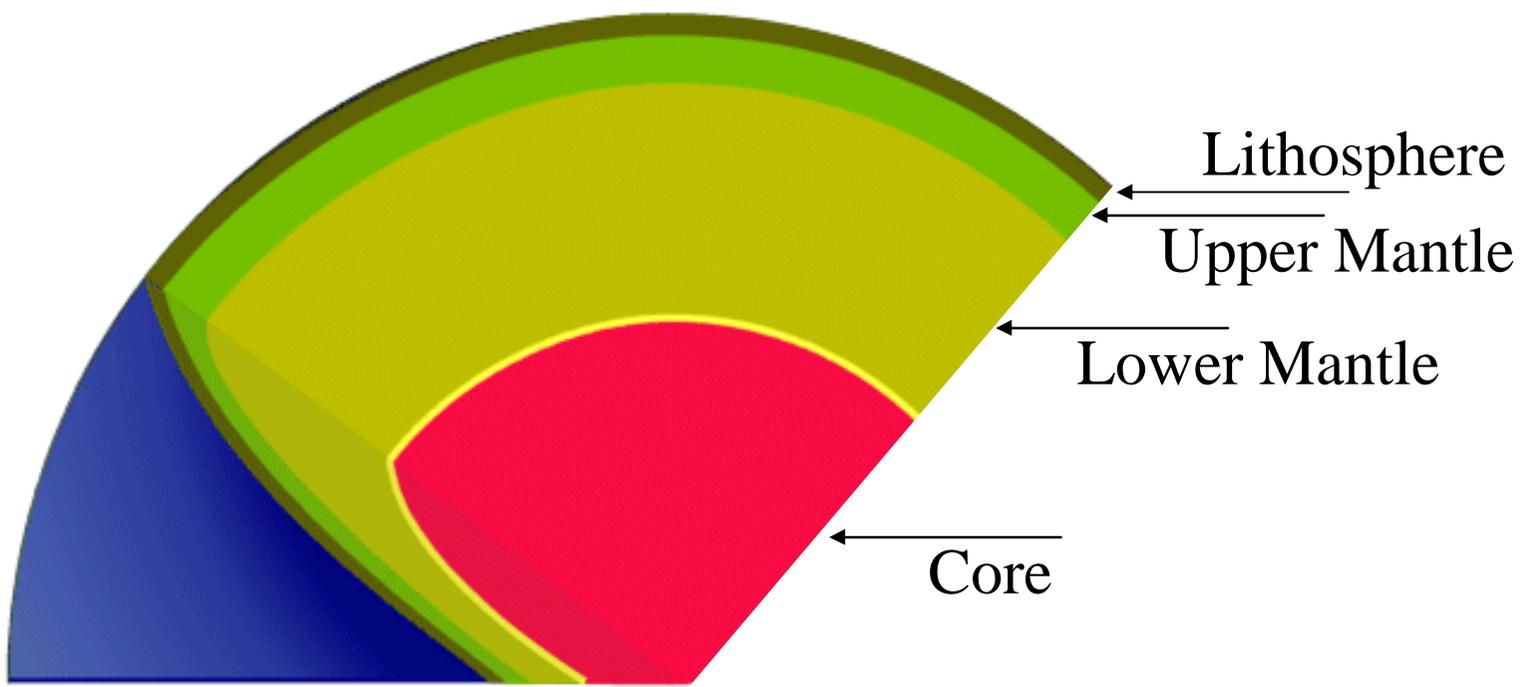
Geophysical modelling and GPS, SAR, GRACE and GOCE data for the understanding of lithospheric and mantle processes - 1

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$$\text{Maxwell time} = \nu_1 / \mu_1 \sim 0 (10^2 \text{ y})$$





$$\nabla \cdot \sigma_1 - \nabla p_0(t_0) - \nabla(\rho_0 g \mathbf{u} \cdot \hat{\mathbf{e}}_r) + \rho \mathbf{F} = 0$$

$$\nabla \cdot \sigma_1 - \nabla(\rho_0 g \mathbf{u} \cdot \hat{\mathbf{e}}_r) - \rho_0 \nabla \phi_1 - \rho_1 g \hat{\mathbf{e}}_r = 0$$

$$\nabla^2 \phi_1 = 4\pi G \rho_1$$

$$\nabla^2 \phi_1 = 0$$

$$\begin{aligned}
& -\rho_0 \partial_r \phi_1 + \rho_0 g_0 \Delta - \rho_0 \partial_r (u g_0) + \partial_r \sigma_{rr} + r^{-1} \partial_\theta \sigma_{r\theta} \\
& + r^{-1} (2\sigma_{rr} - \sigma_{\theta\theta} - \sigma_{\phi\phi} + \sigma_{r\theta} \cot \theta) = 0
\end{aligned}$$

$$\begin{aligned}
& -\rho_0 r^{-1} \partial_\theta \phi_1 - \rho_0 g_0 r^{-1} \partial_\theta u + \partial_r \sigma_{r\theta} + r^{-1} \partial_\theta \sigma_{\theta\theta} \\
& + r^{-1} ((\sigma_{\theta\theta} - \sigma_{\phi\phi}) \cot \theta + 3\sigma_{r\theta}) = 0
\end{aligned}$$

$$\begin{aligned}
& r^{-2} \partial_r (r^2 \partial_r \phi_1) + (r^2 \sin \theta)^{-1} \partial_\theta (\sin \theta \partial_\theta \phi_1) \\
& = -4\pi G (\rho_0 \Delta + u \partial_r \rho_0)
\end{aligned}$$

$$u = \sum_{l=0}^{\infty} U_l(r) P_l(\cos \theta)$$

$$v = \sum_{l=0}^{\infty} V_l(r) \partial_{\theta} P_l(\cos \theta)$$

$$\phi_1 = - \sum_{l=0}^{\infty} \phi_l(r) P_l(\cos \theta)$$

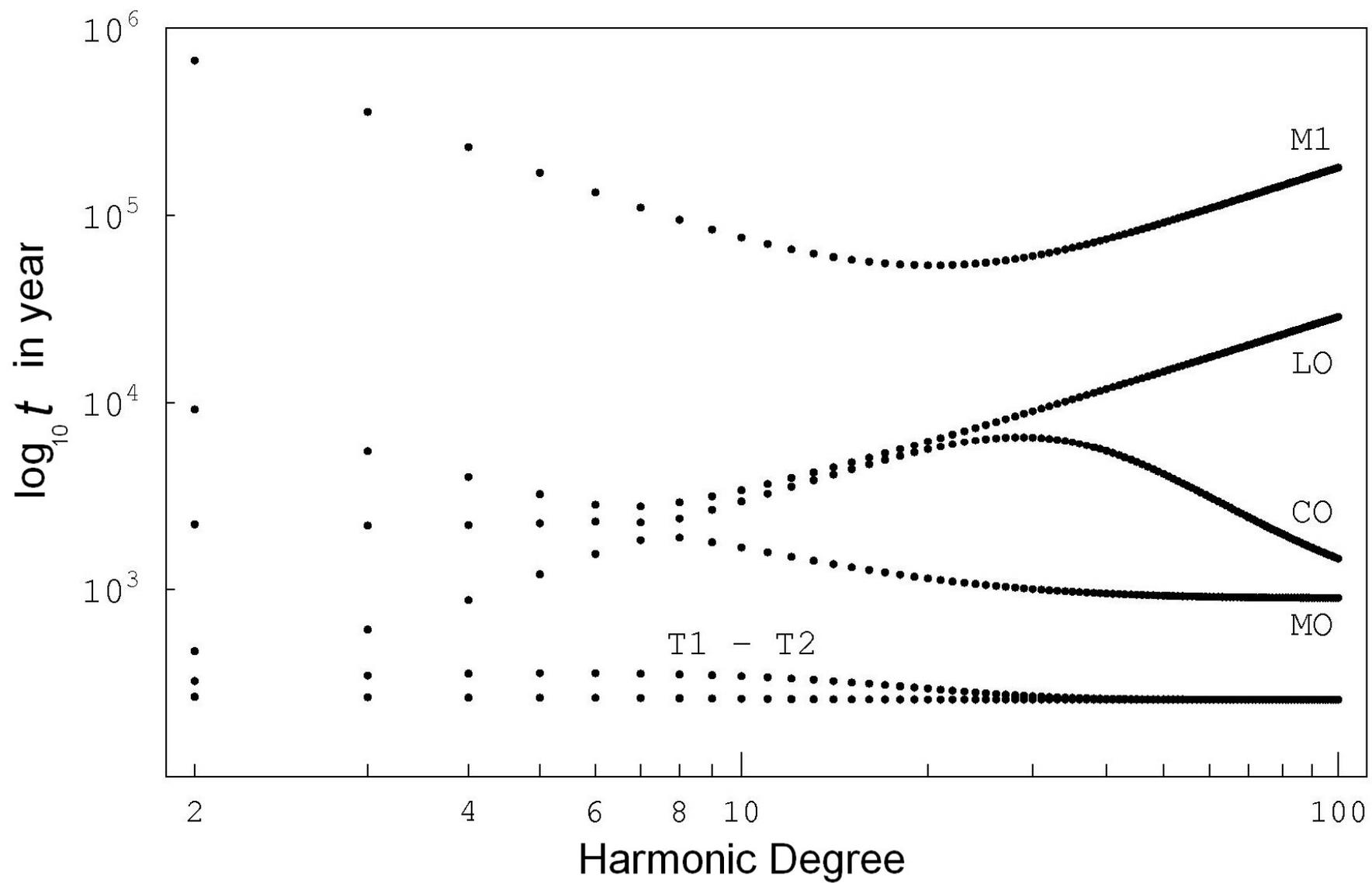
$$P_l(\cos \theta) = \frac{1}{2^l l!} \frac{d^l}{d(\cos \theta)^l} (\cos^2 \theta - 1)^l$$

$$\frac{d\epsilon}{dt} = \frac{\sigma}{2\nu} + \frac{1}{2\mu} \frac{d\sigma}{dt}$$

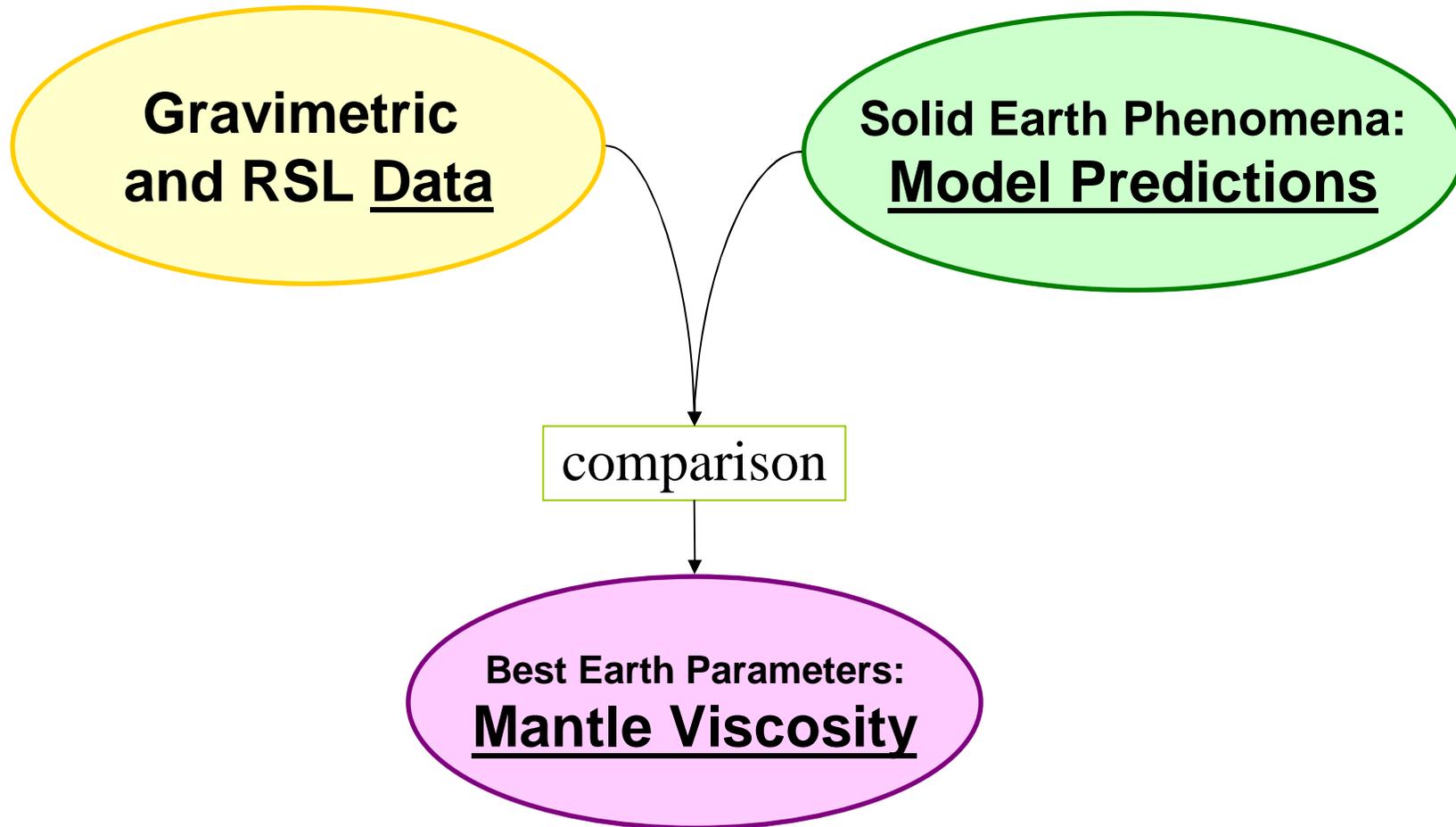
$$\tilde{\mu}(s) = \frac{\mu s}{s + \mu/\nu}$$

$$\tilde{\sigma}_{ij}(s) = 2\tilde{\mu}(s)\tilde{\epsilon}_{ij}(s)$$

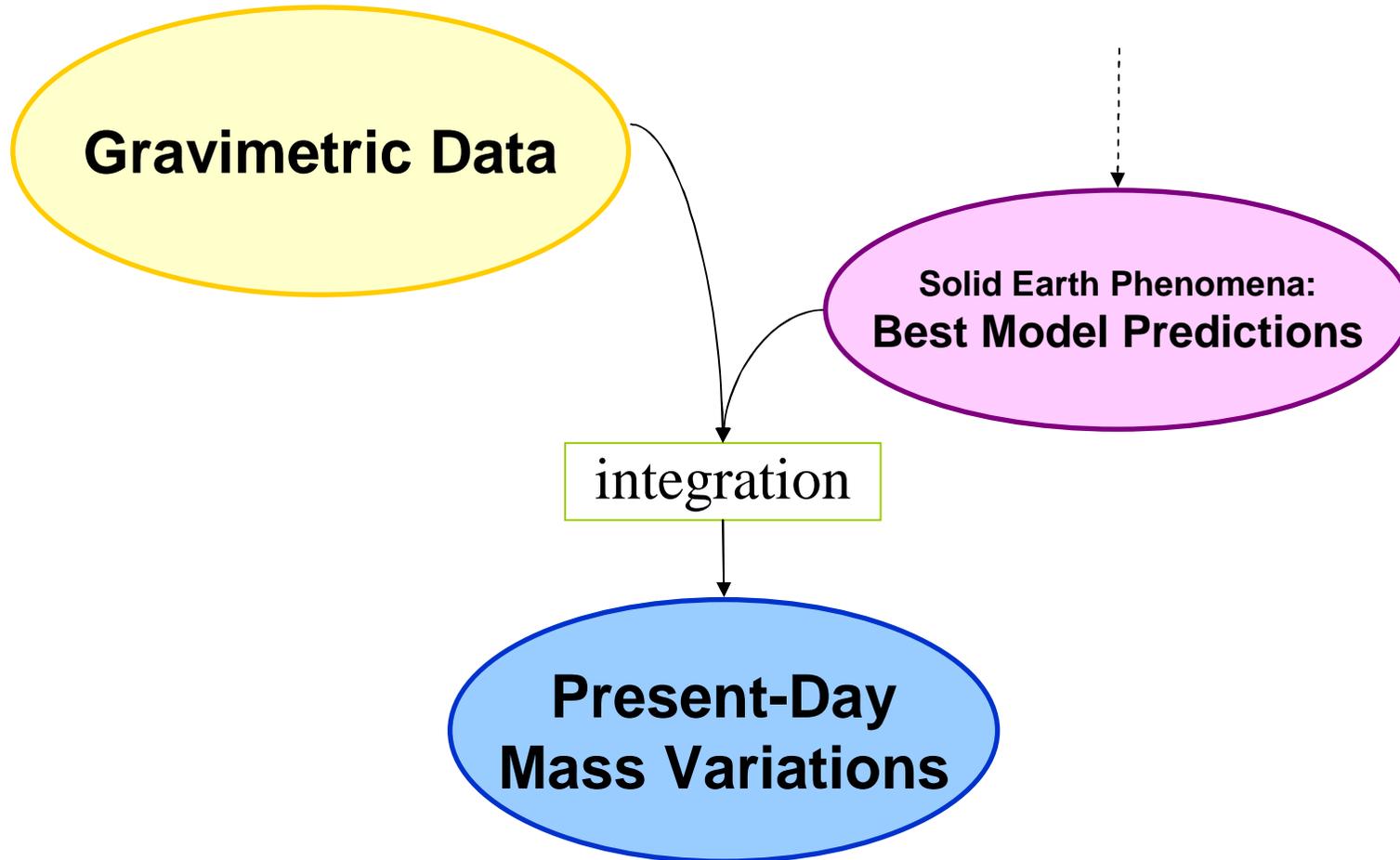
$$U_i(t) = U_{ik}\delta(t) + \sum_{j=1}^M U_{ij}e^{s_j t}$$



General Scheme

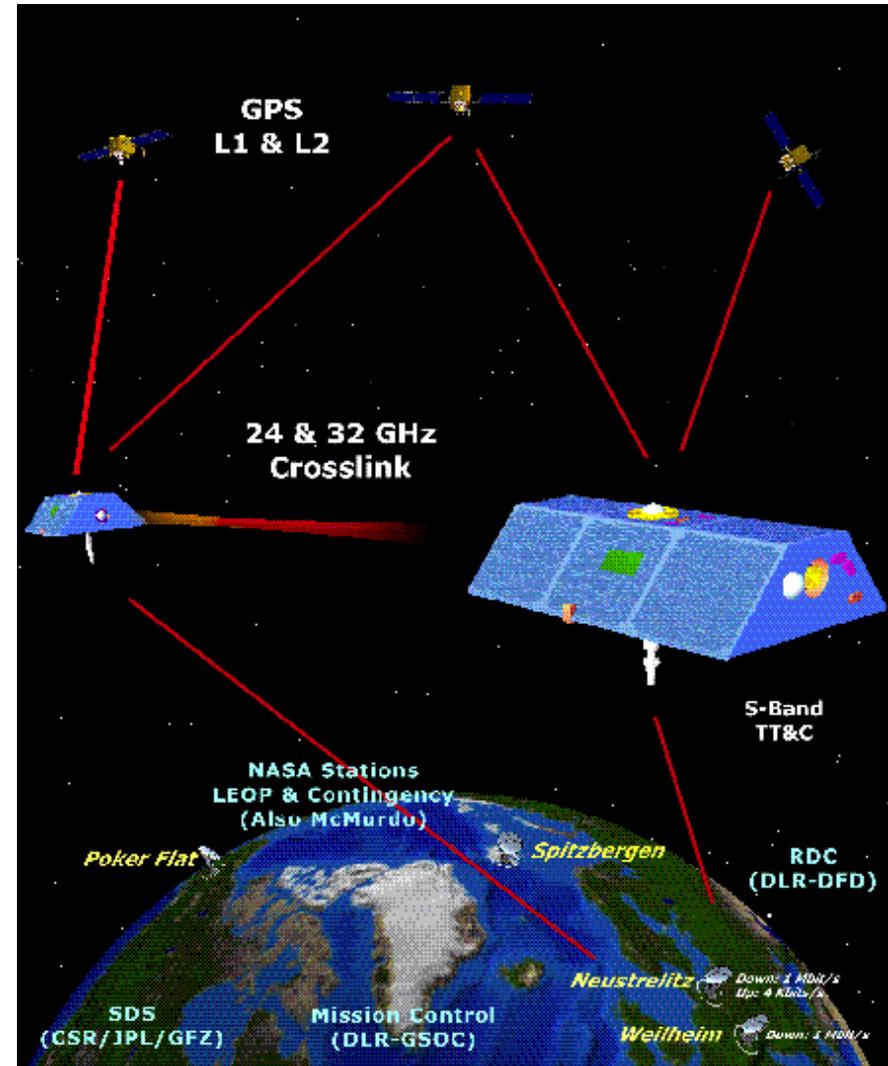


General Scheme

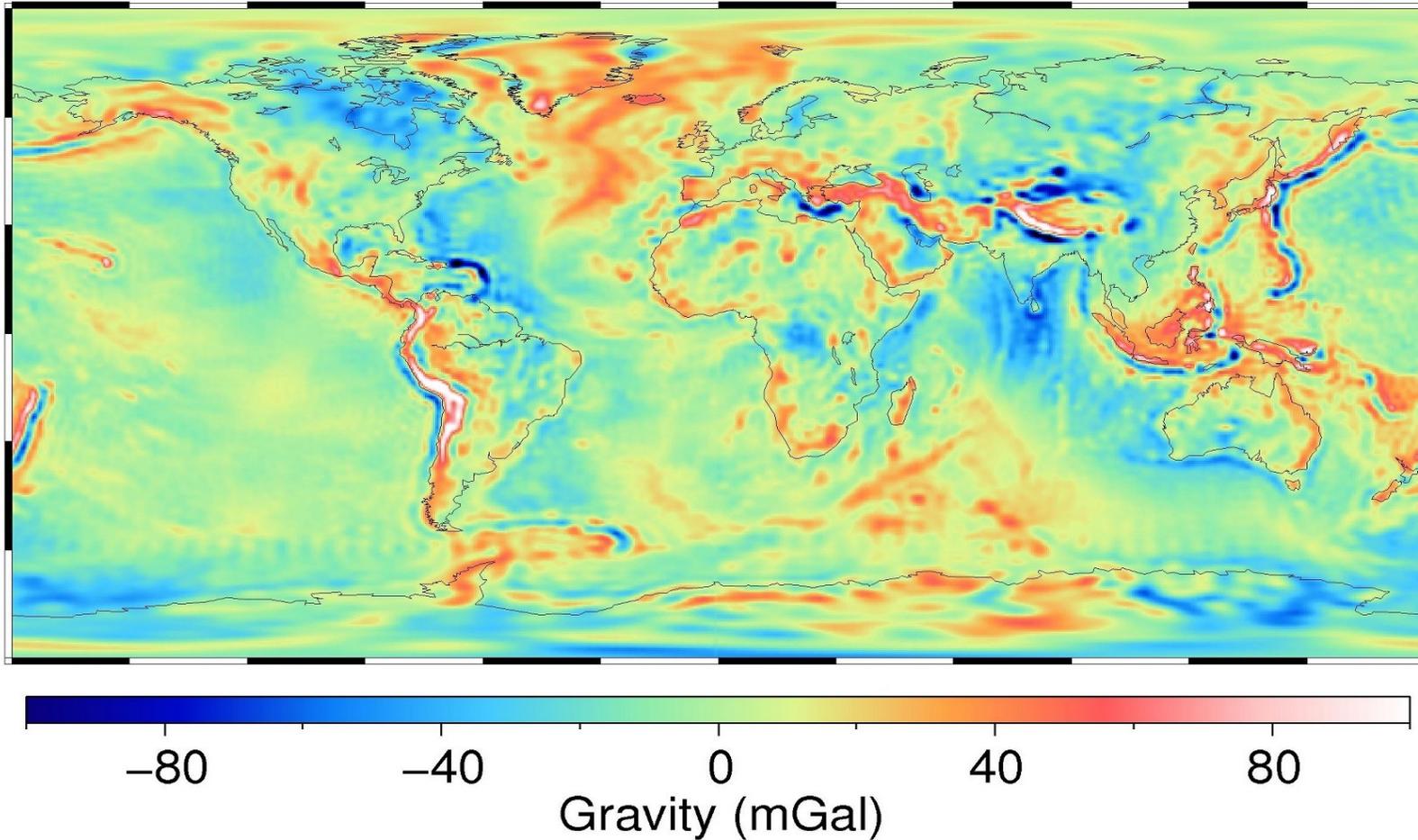


SLR and GRACE

Satellite Laser Ranging

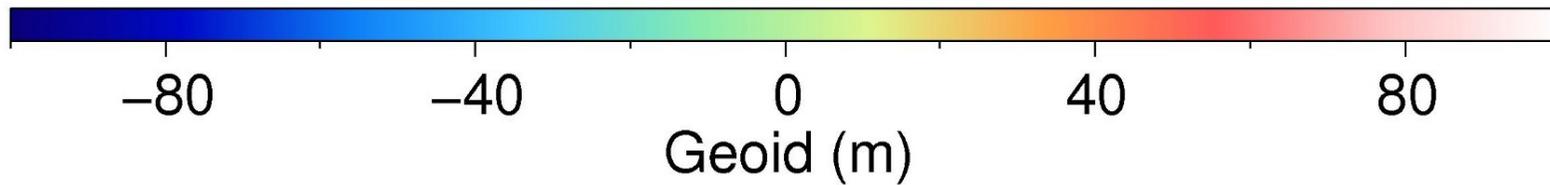
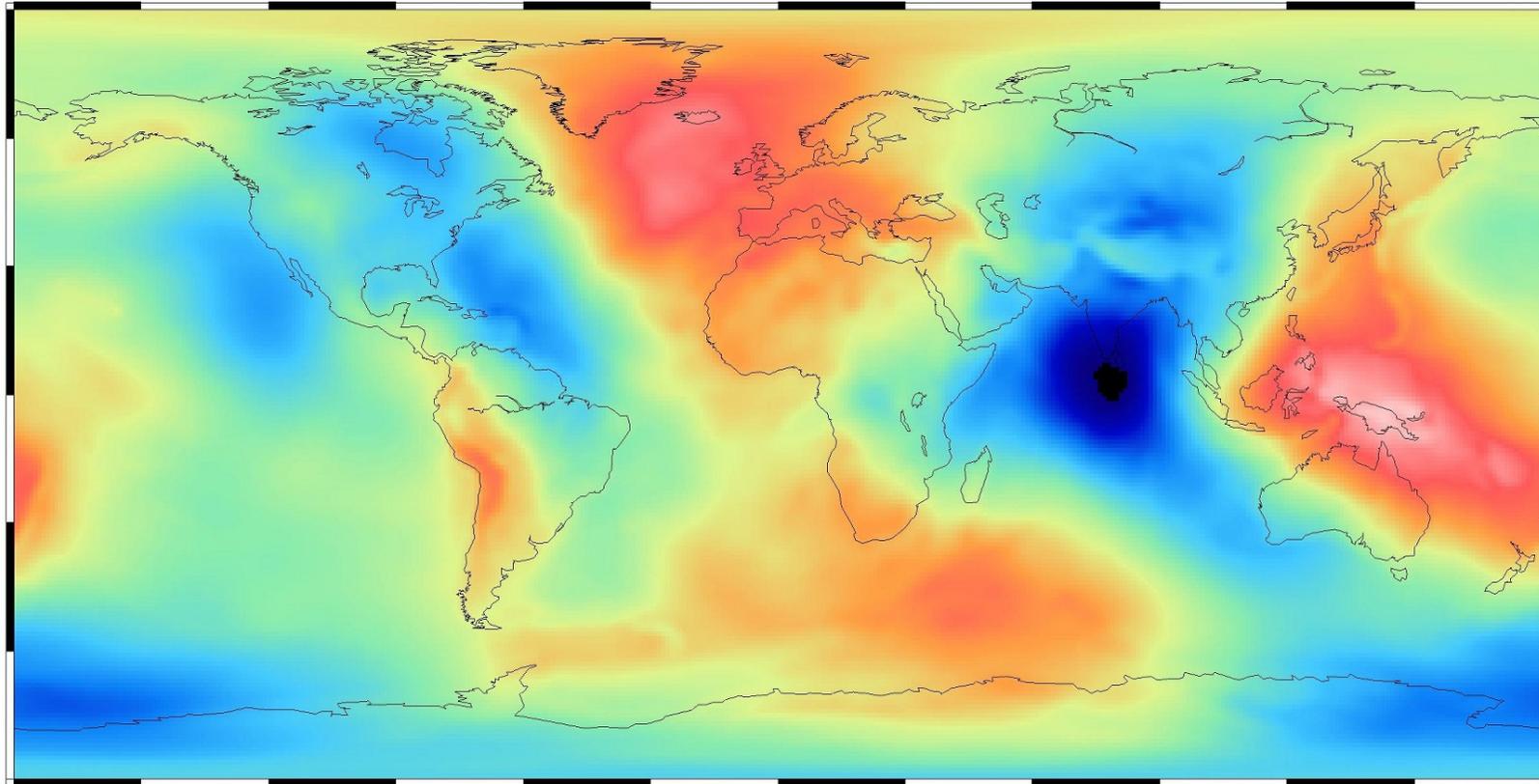


Gravity Anomalies (from GRACE)



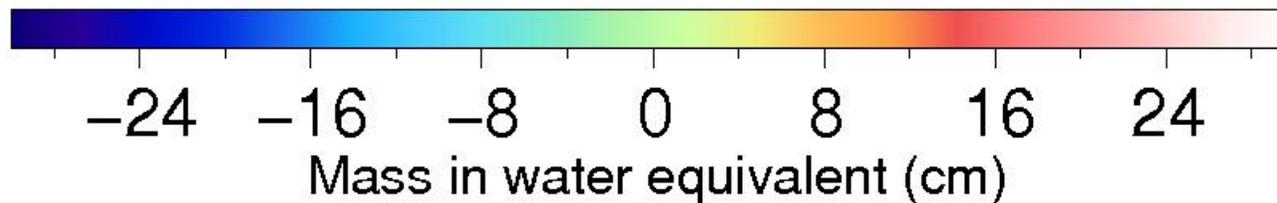
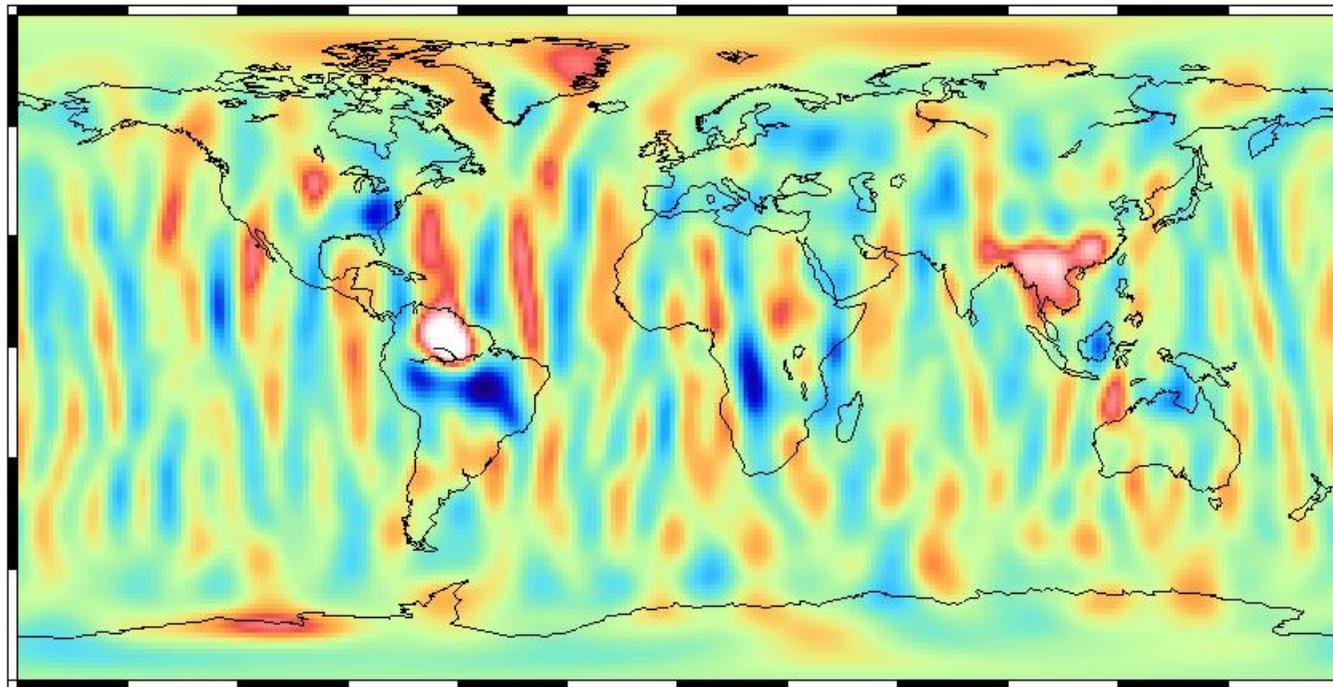
GRACE-LAGEOS 2-year gravity field (EIGEN-GL04S)

Static Geoid (from GRACE)

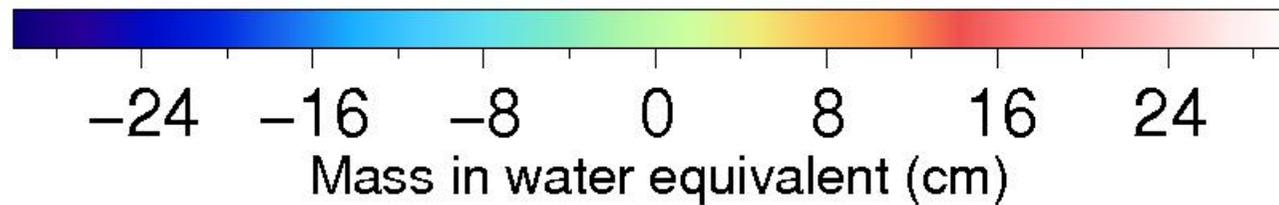
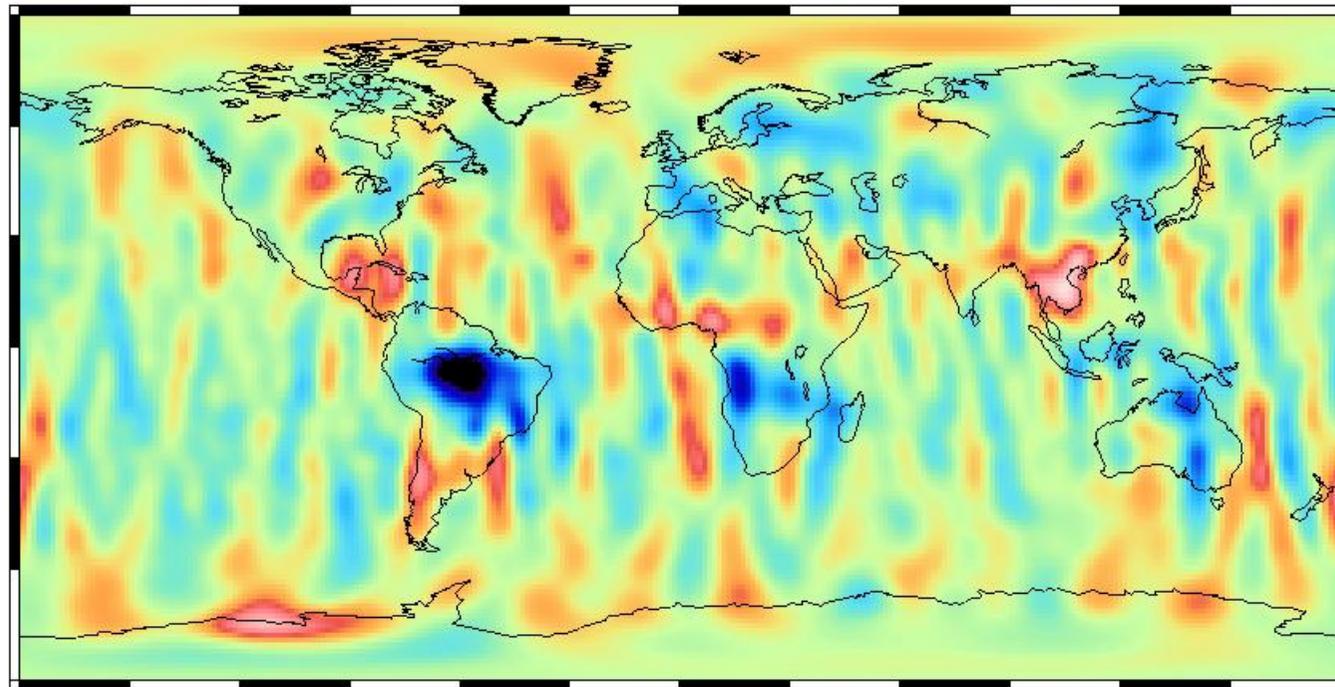


GRACE-LAGEOS 2-year gravity field (EIGEN-GL04S)

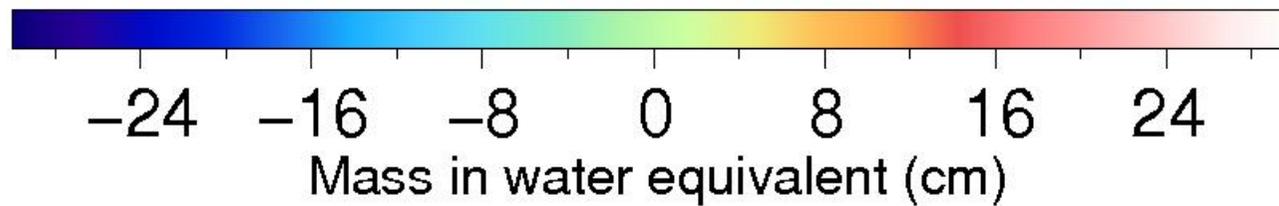
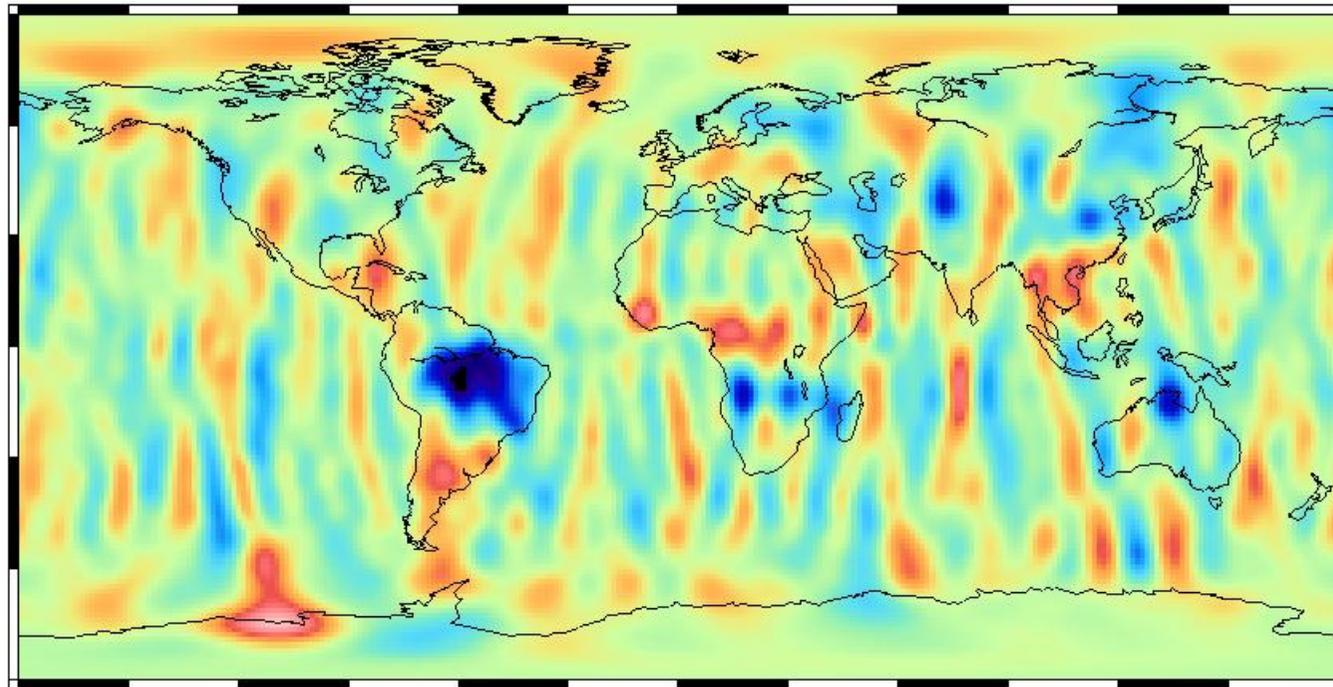
Geoid Variation - August 2002



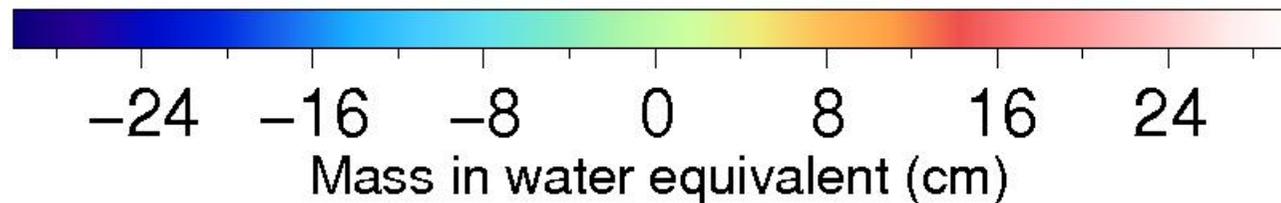
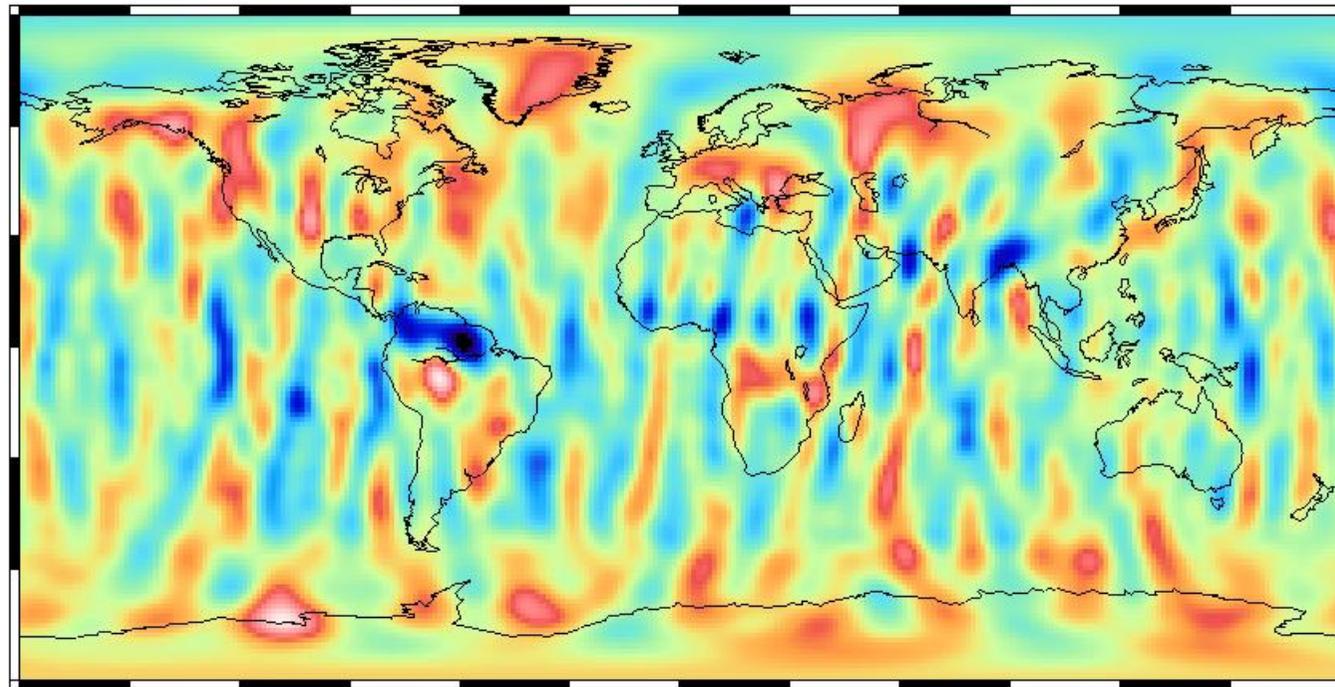
Geoid Variation - October 2002



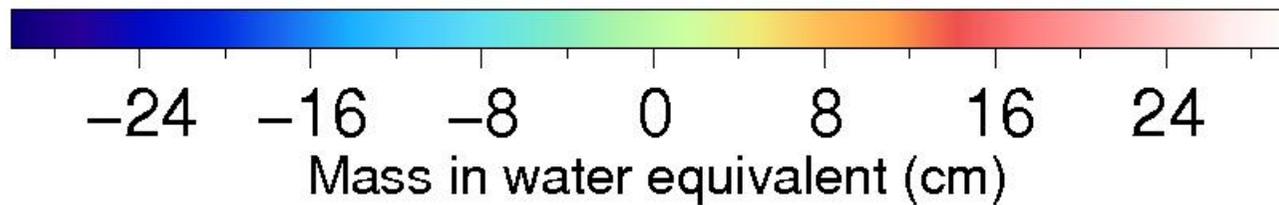
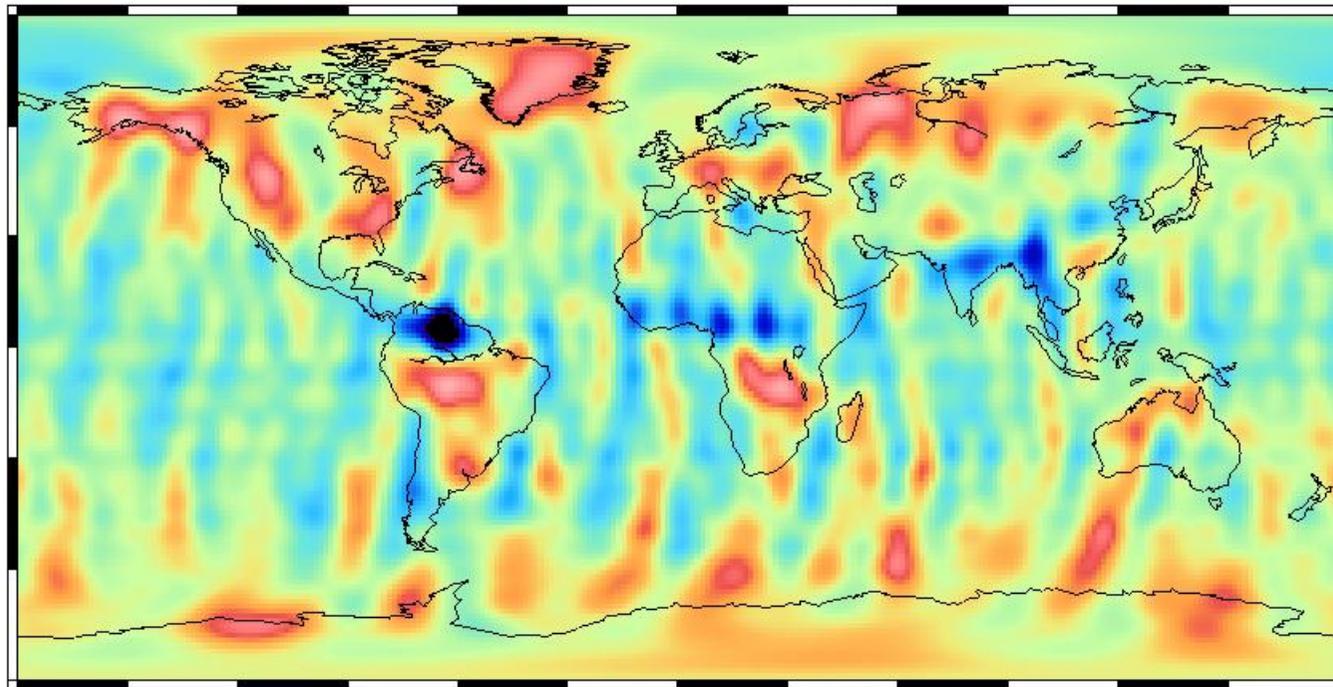
Geoid Variation - November 2002



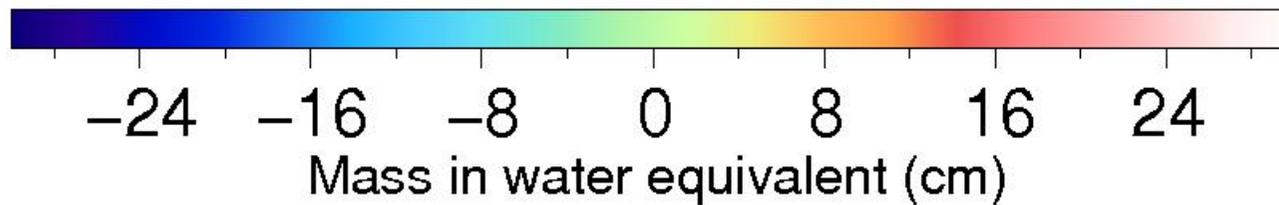
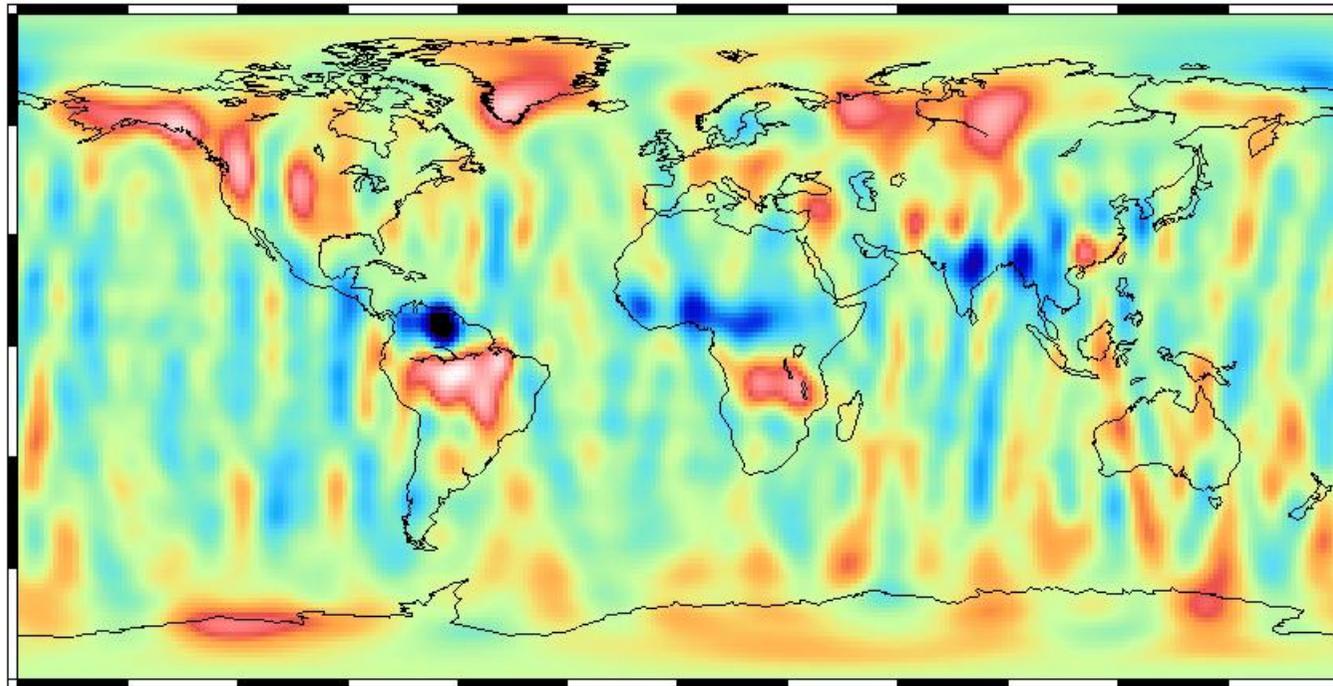
Geoid Variation - February 2003



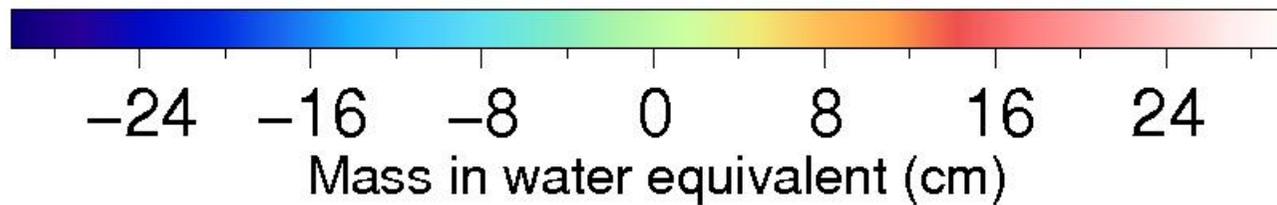
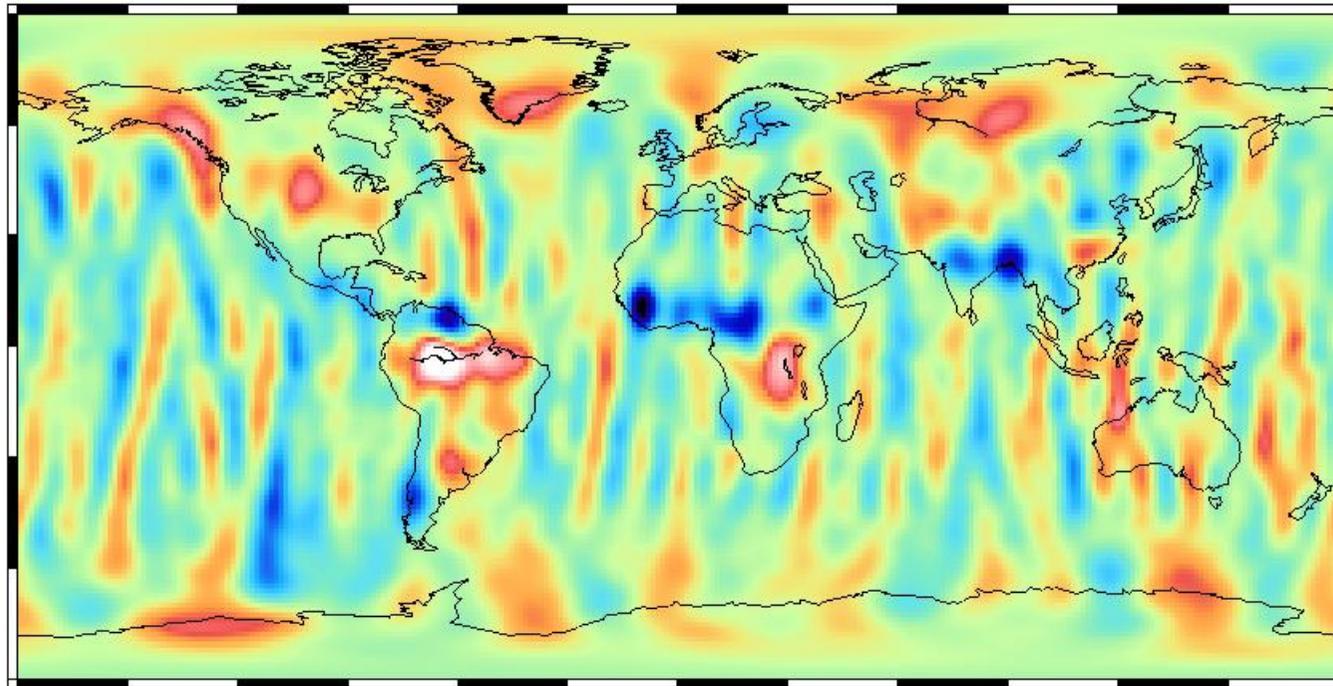
Geoid Variation - March 2003



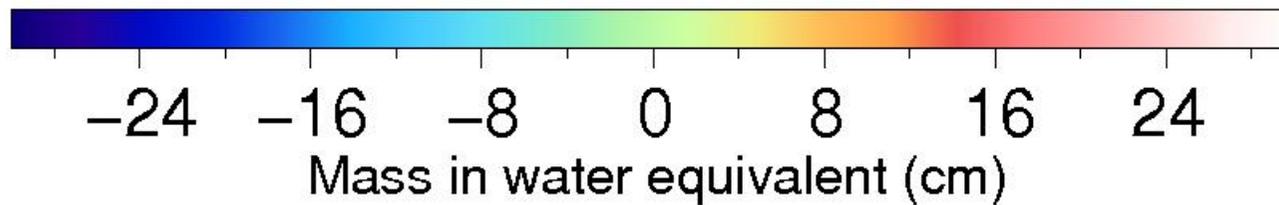
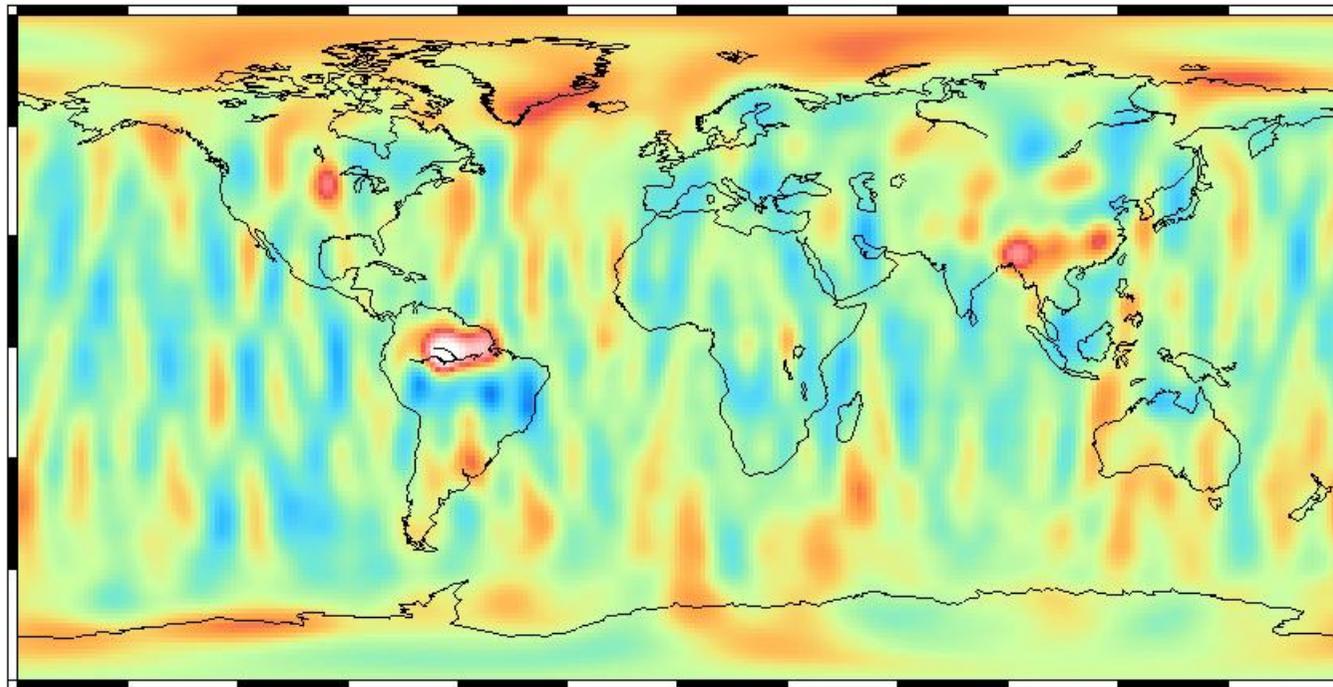
Geoid Variation - April 2003



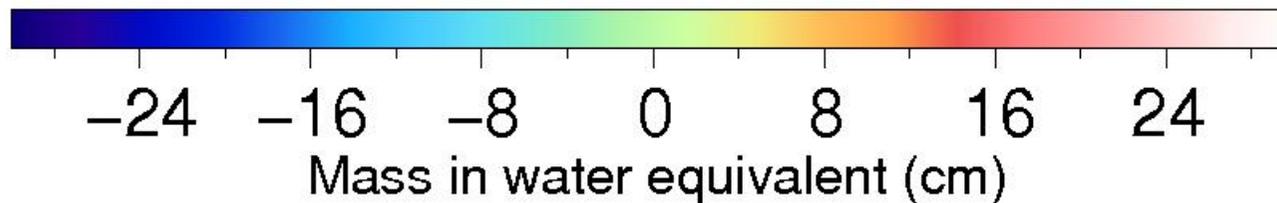
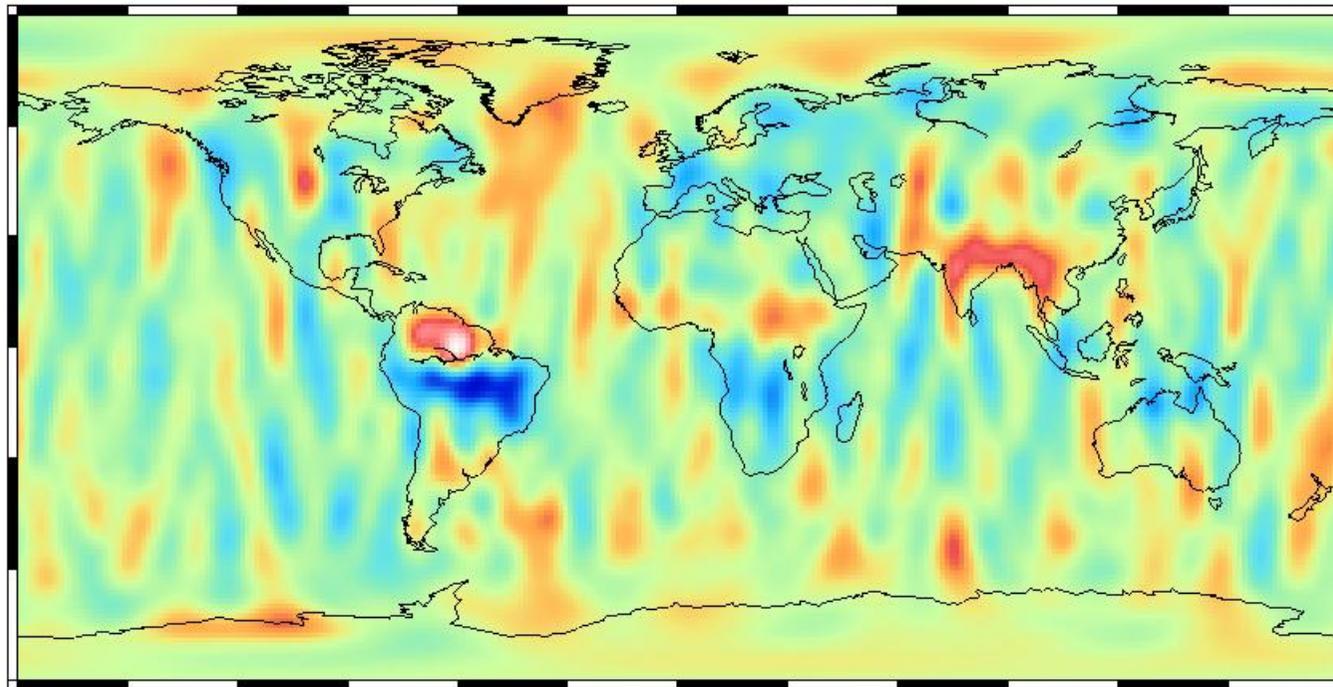
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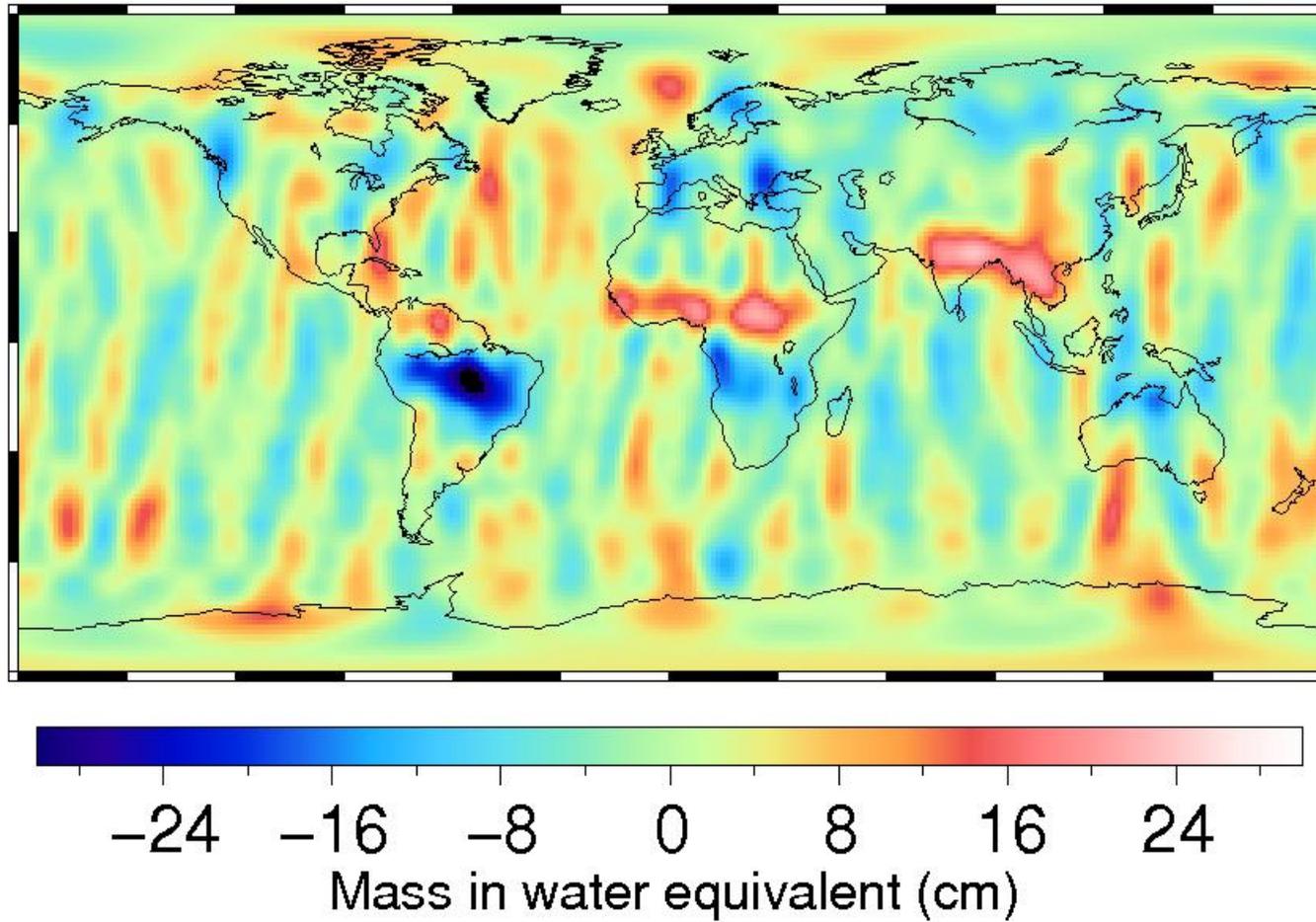
Geoid Variation - July 2003



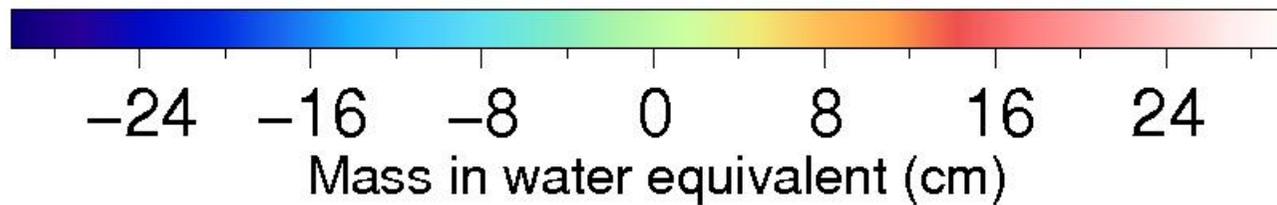
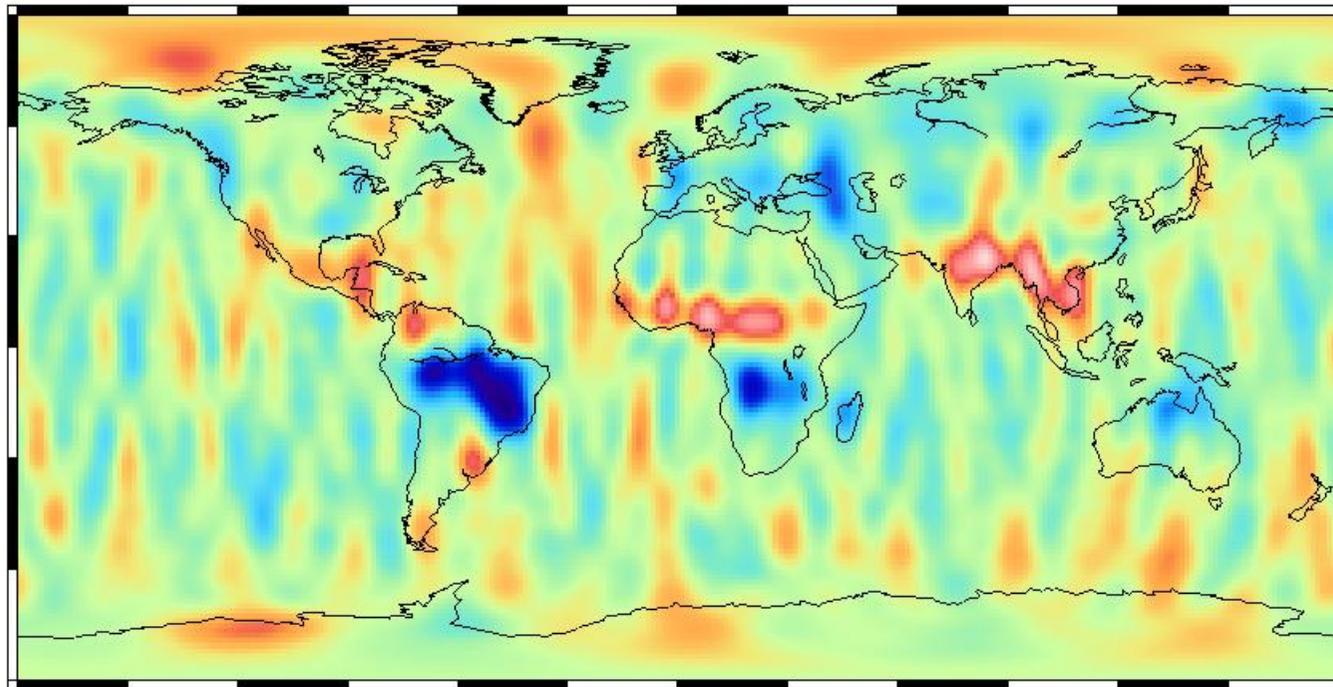
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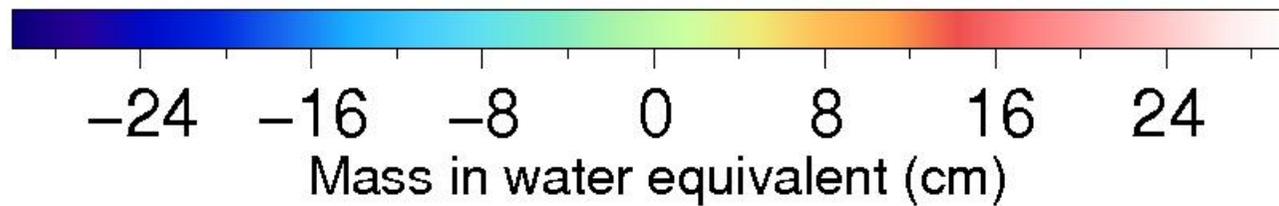
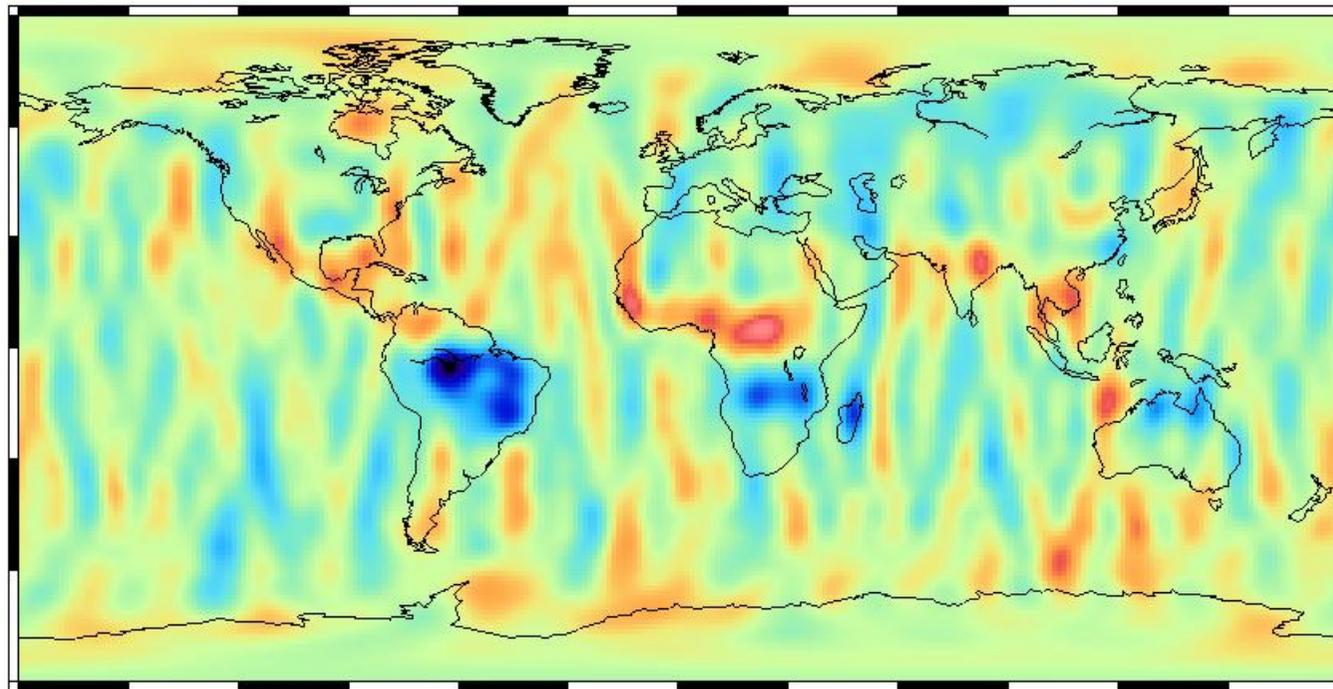
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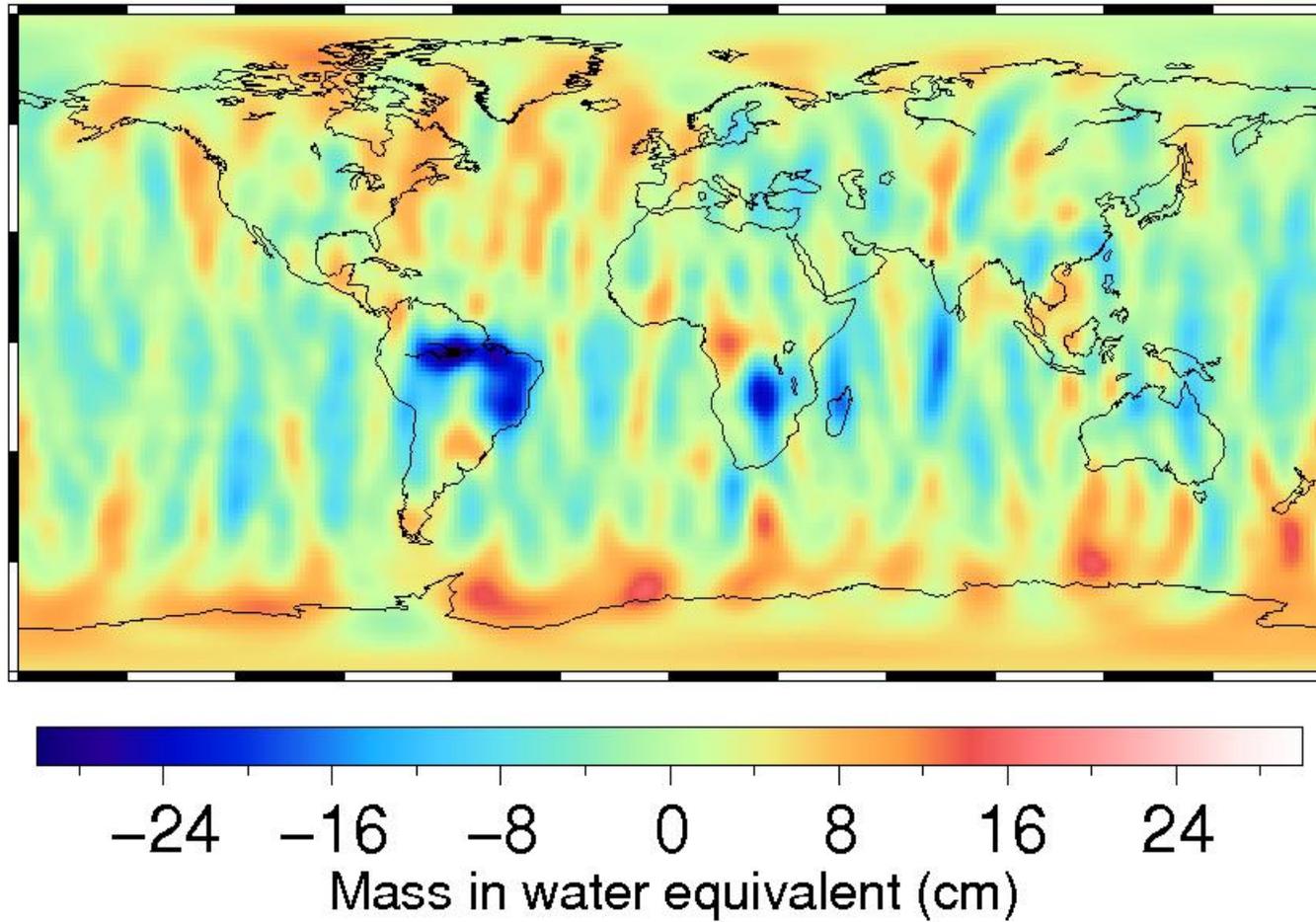
Geoid Variation - October 2003



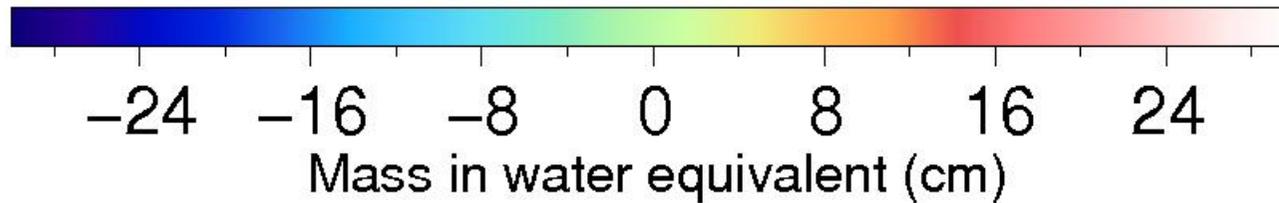
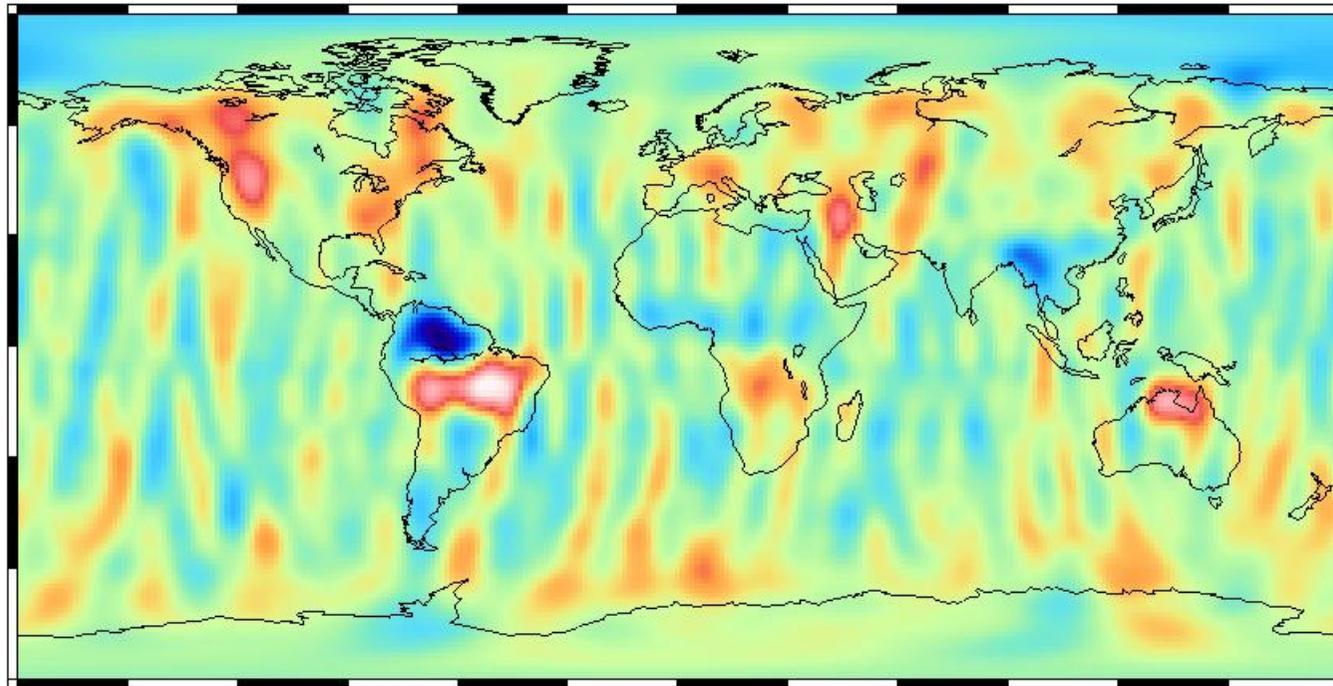
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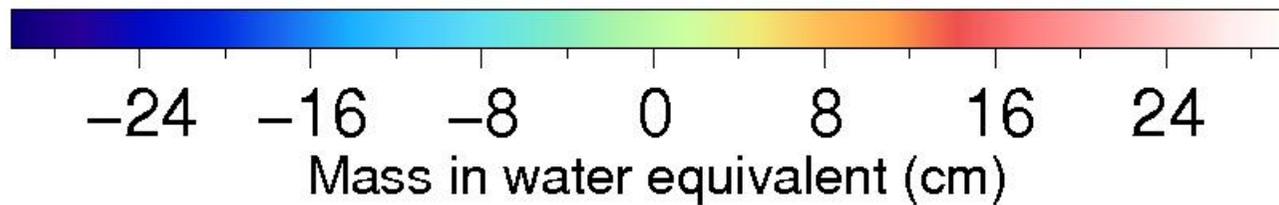
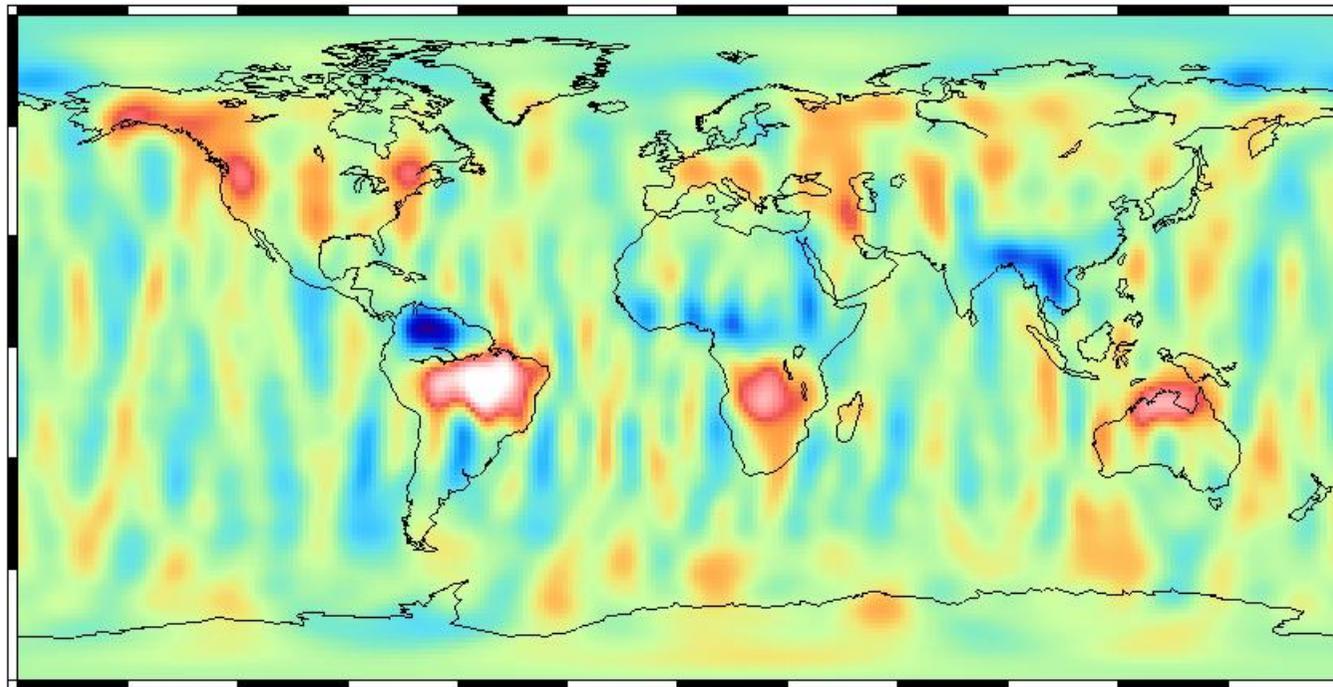
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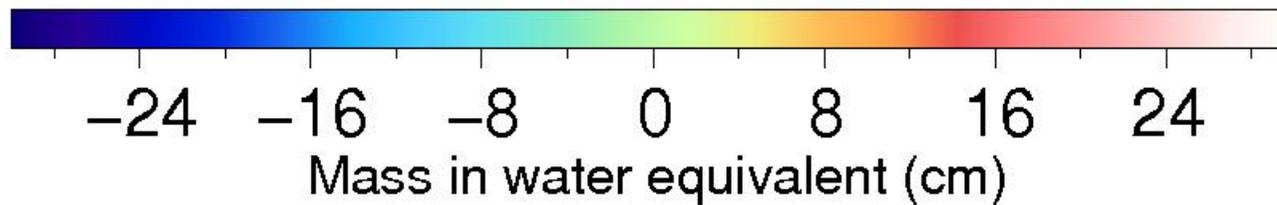
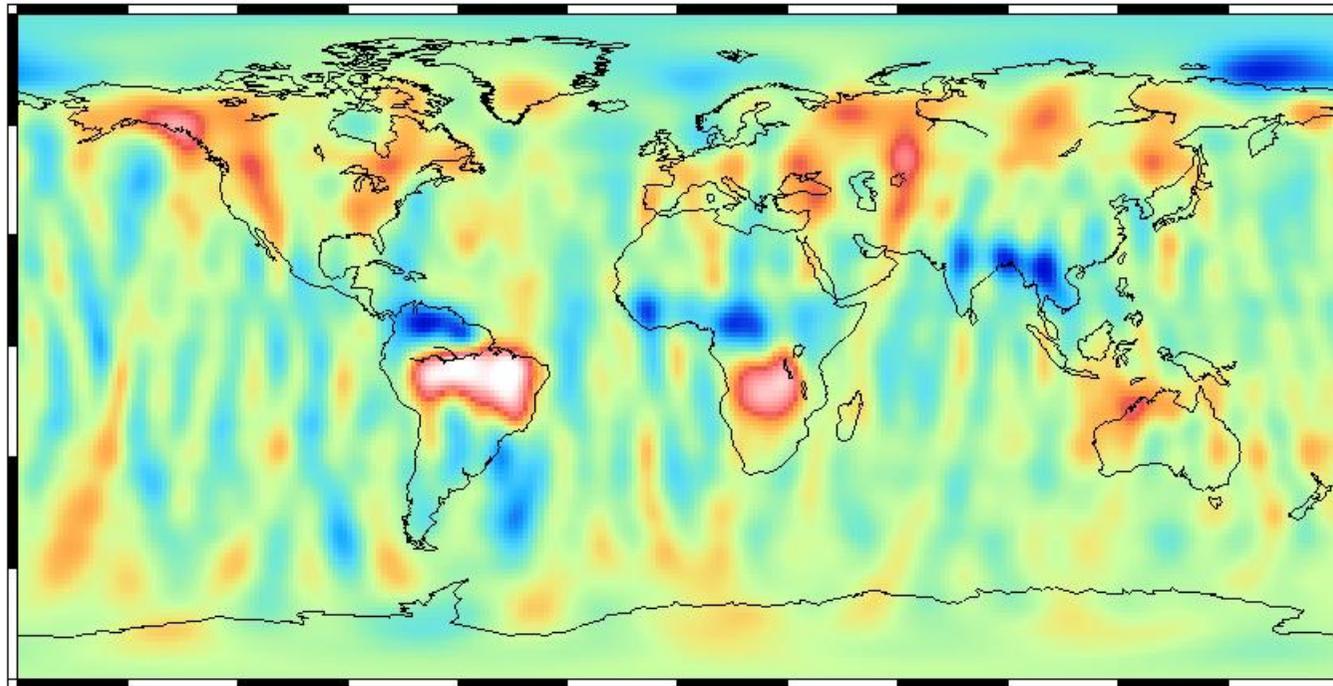
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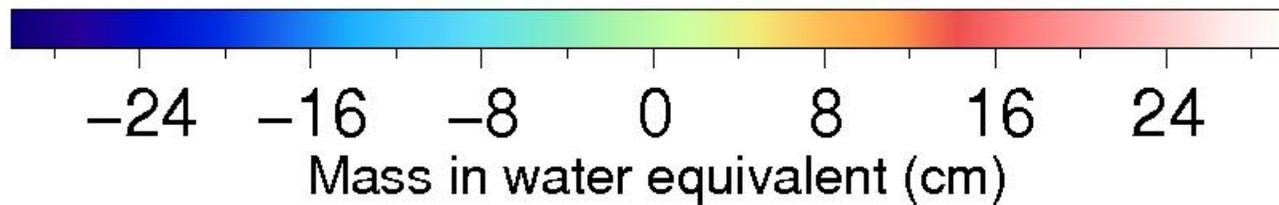
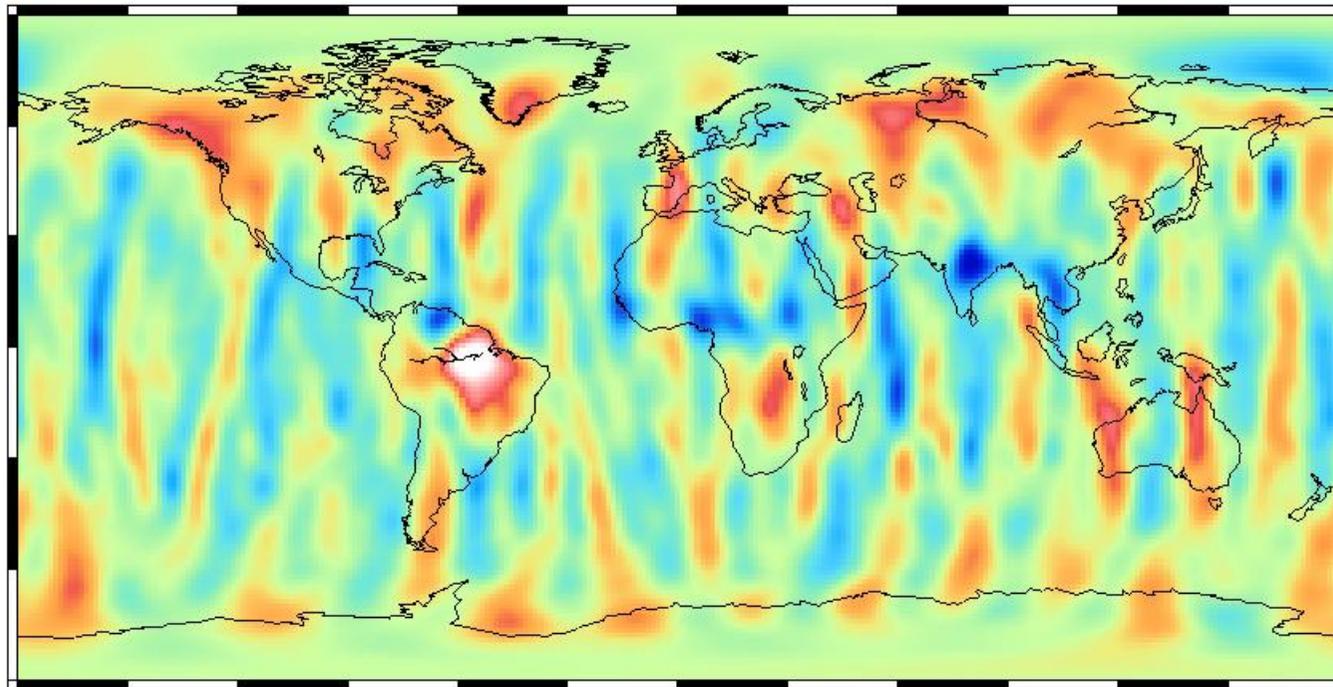
Geoid Variation - March 2004



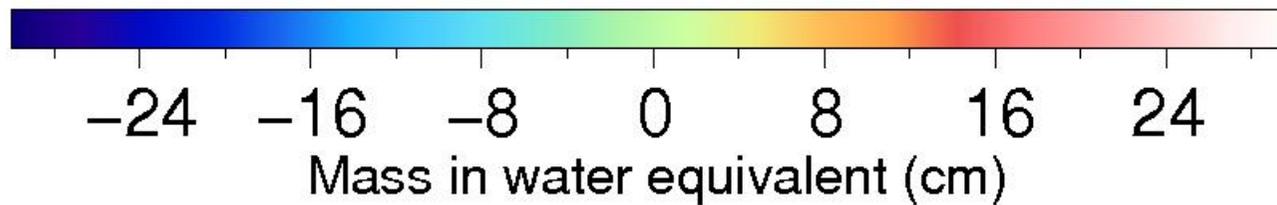
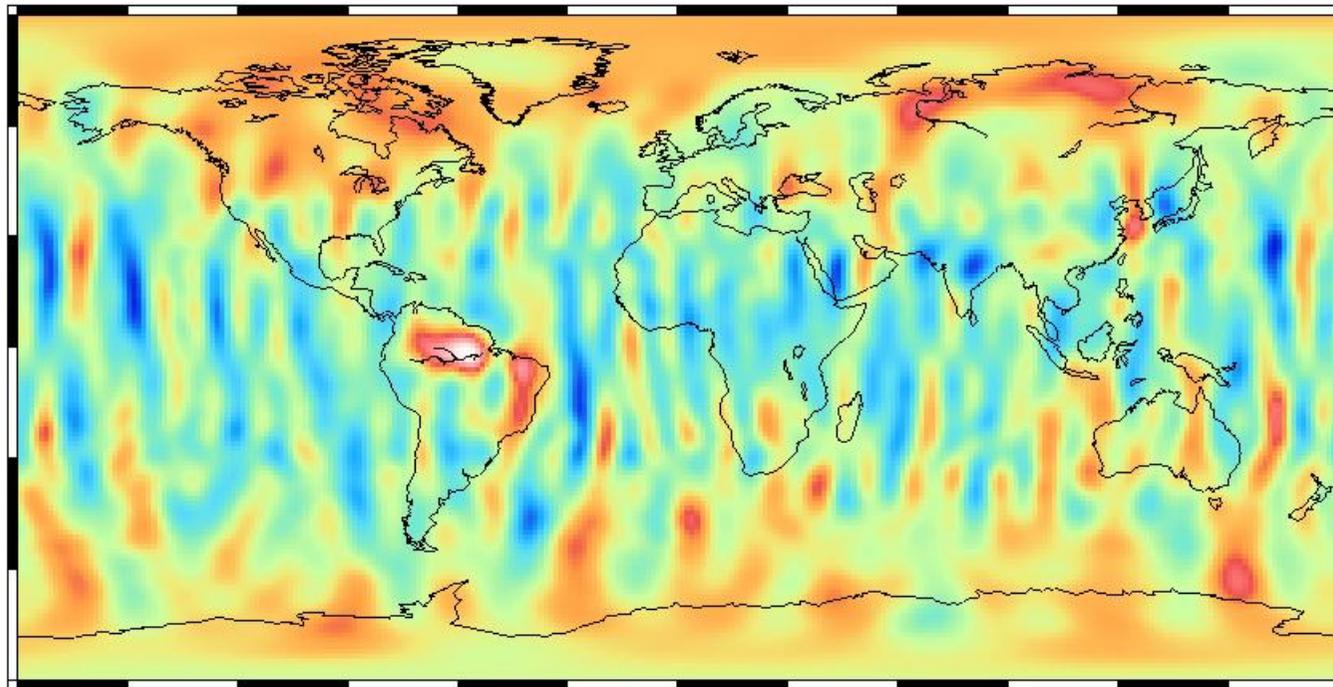
Geoid Variation - April 2004



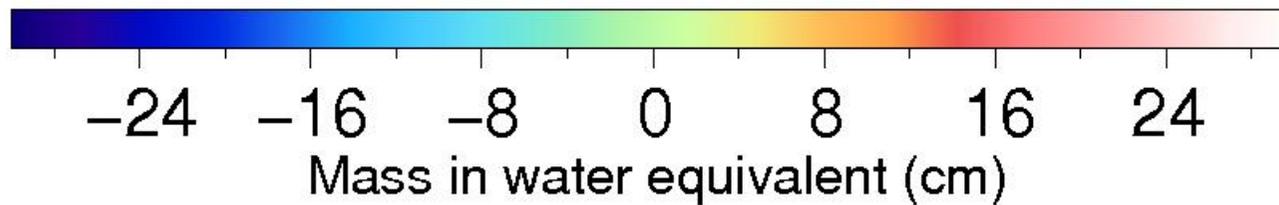
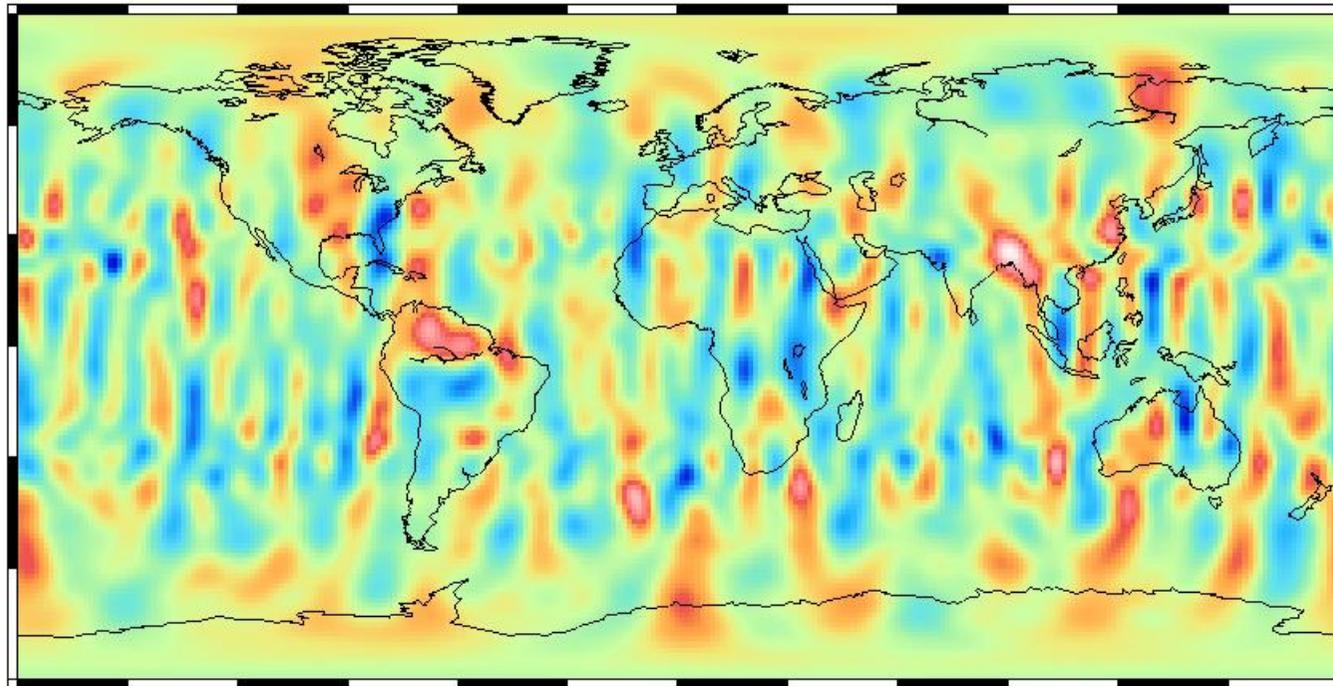
Geoid Variation - May 2004



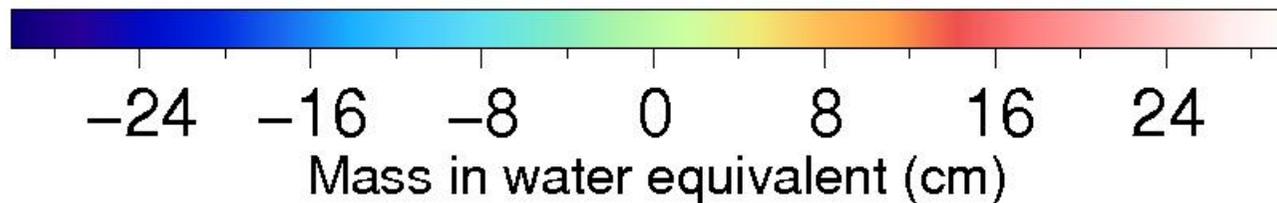
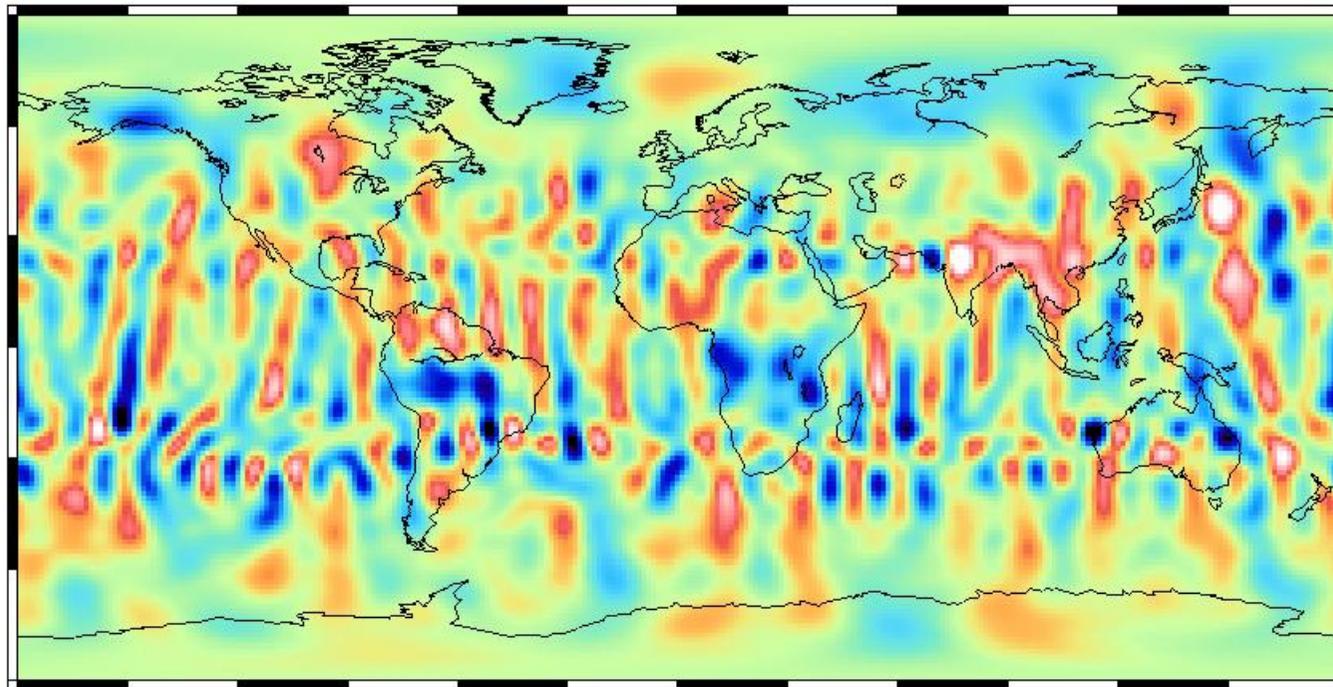
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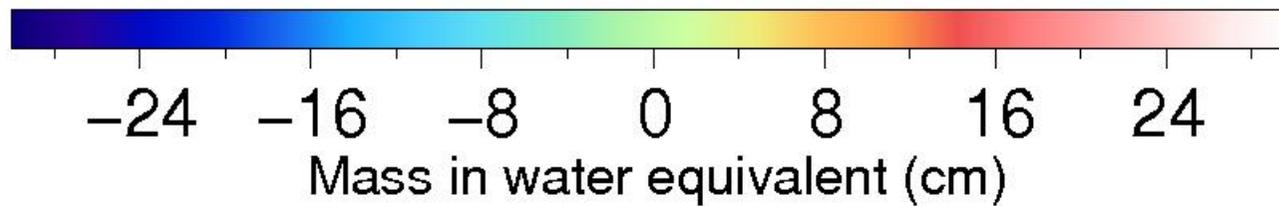
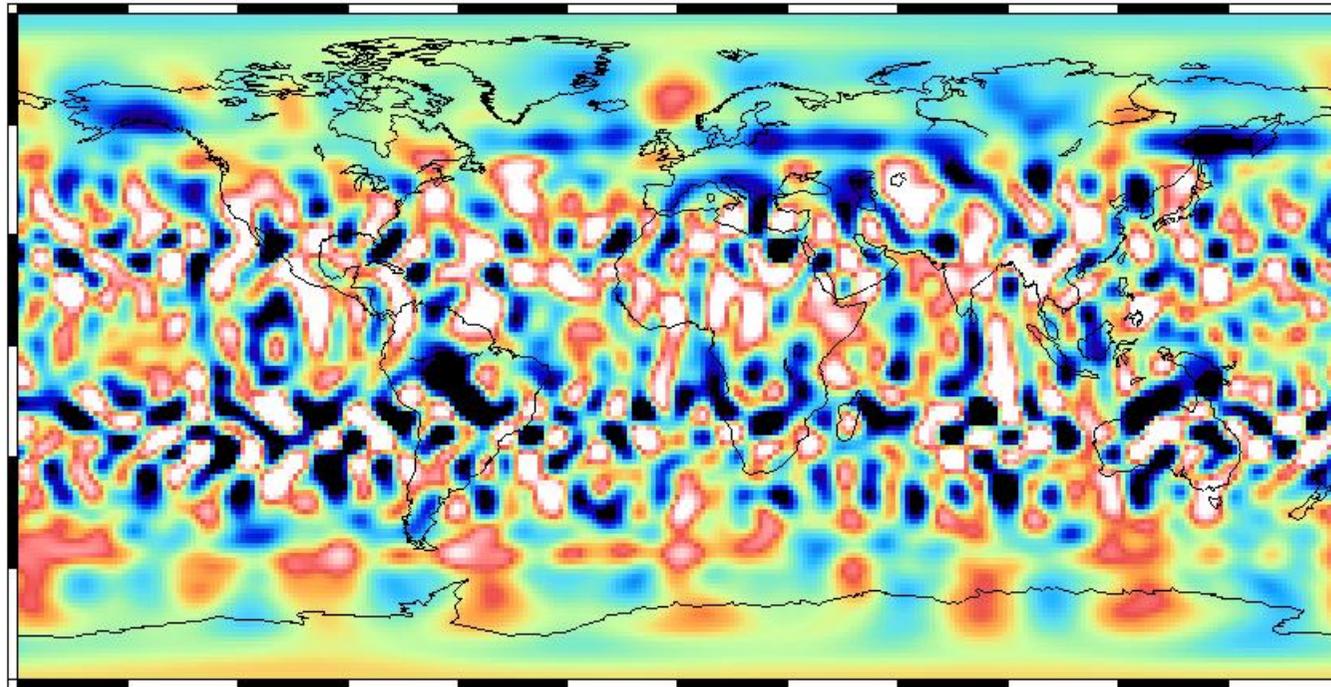
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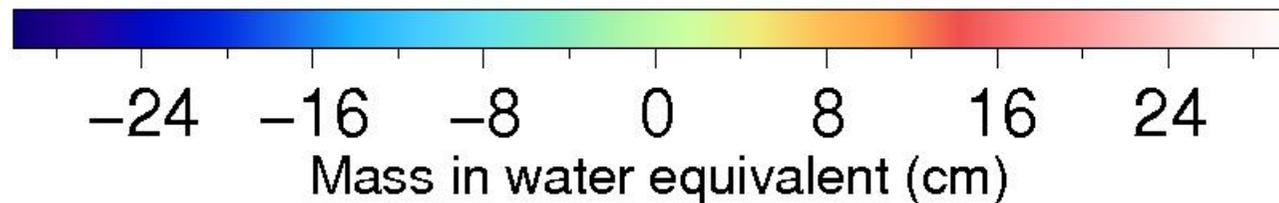
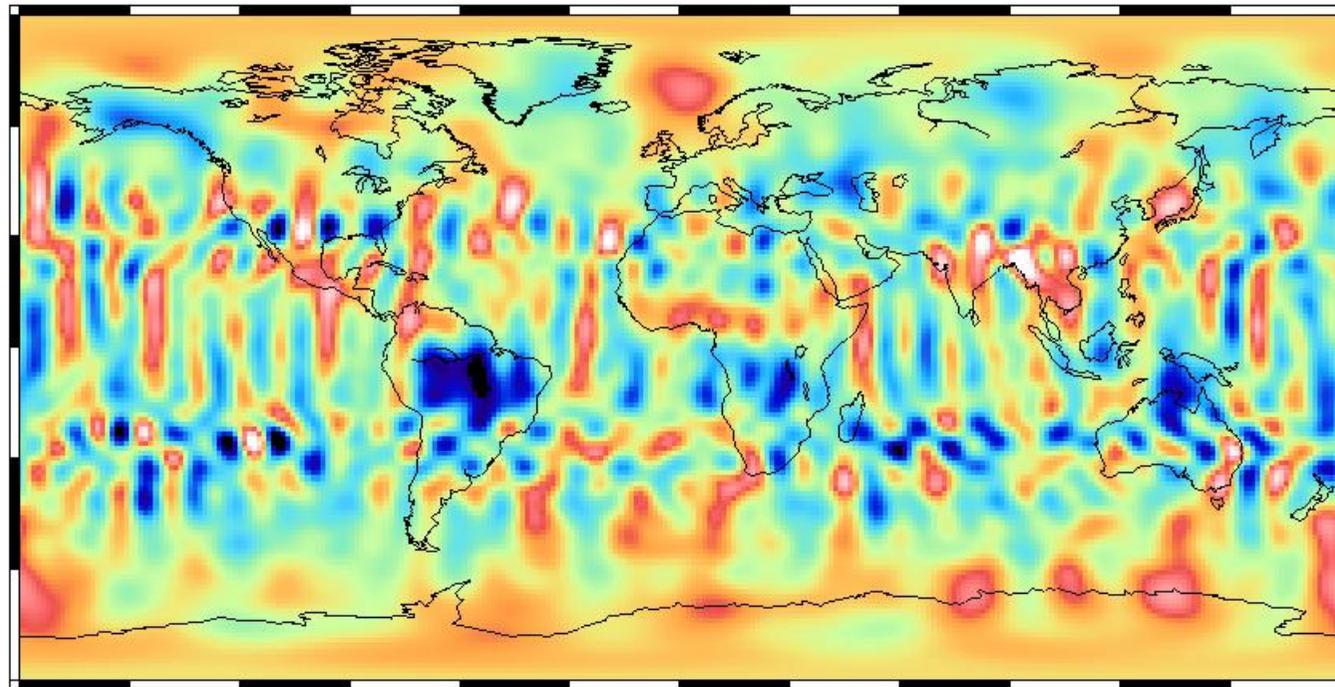
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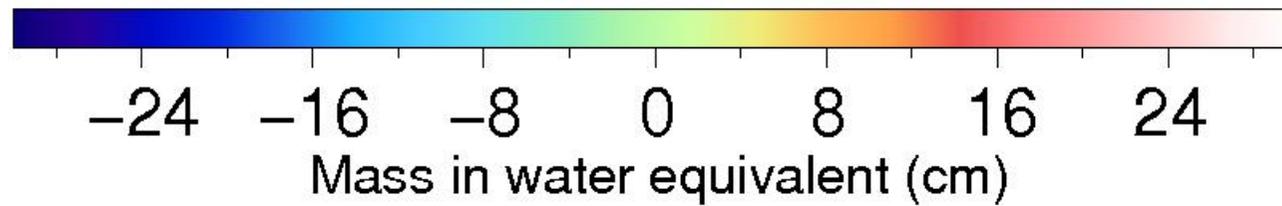
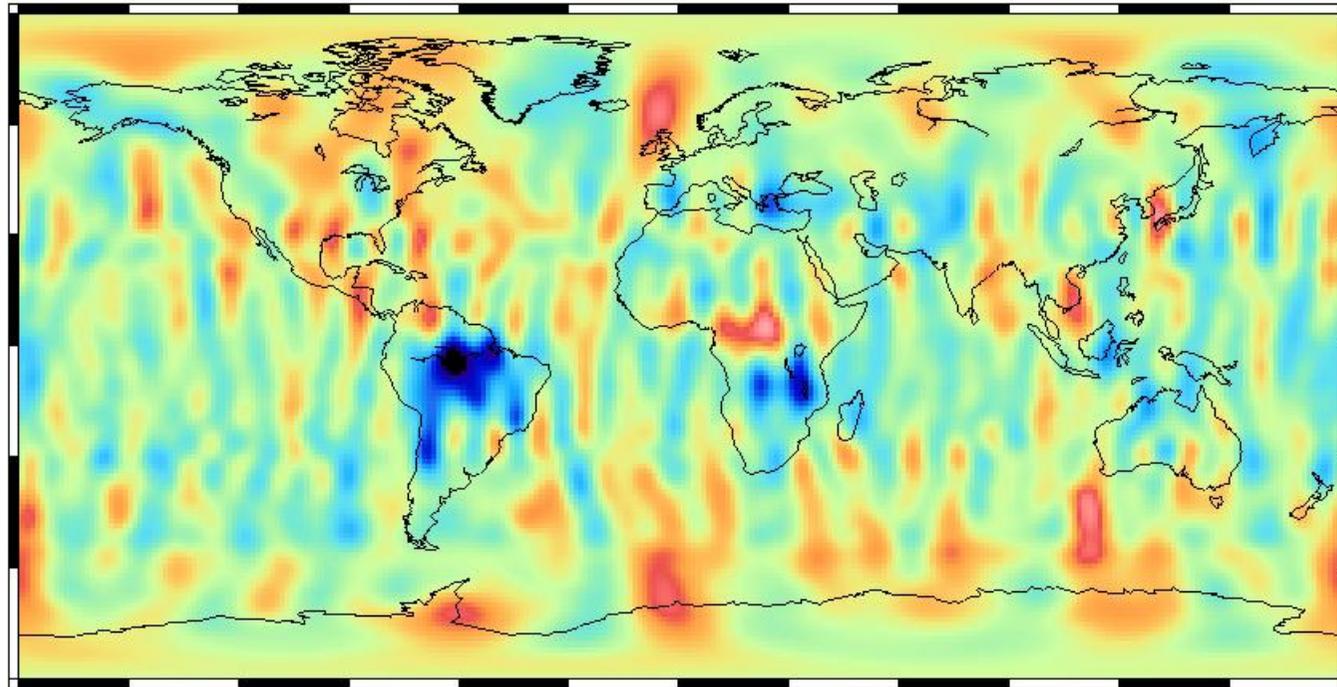
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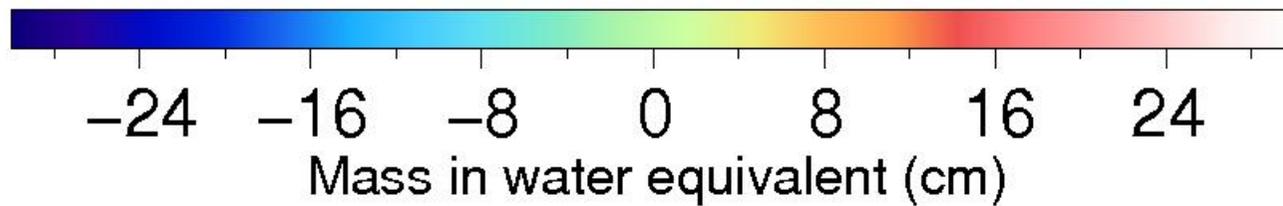
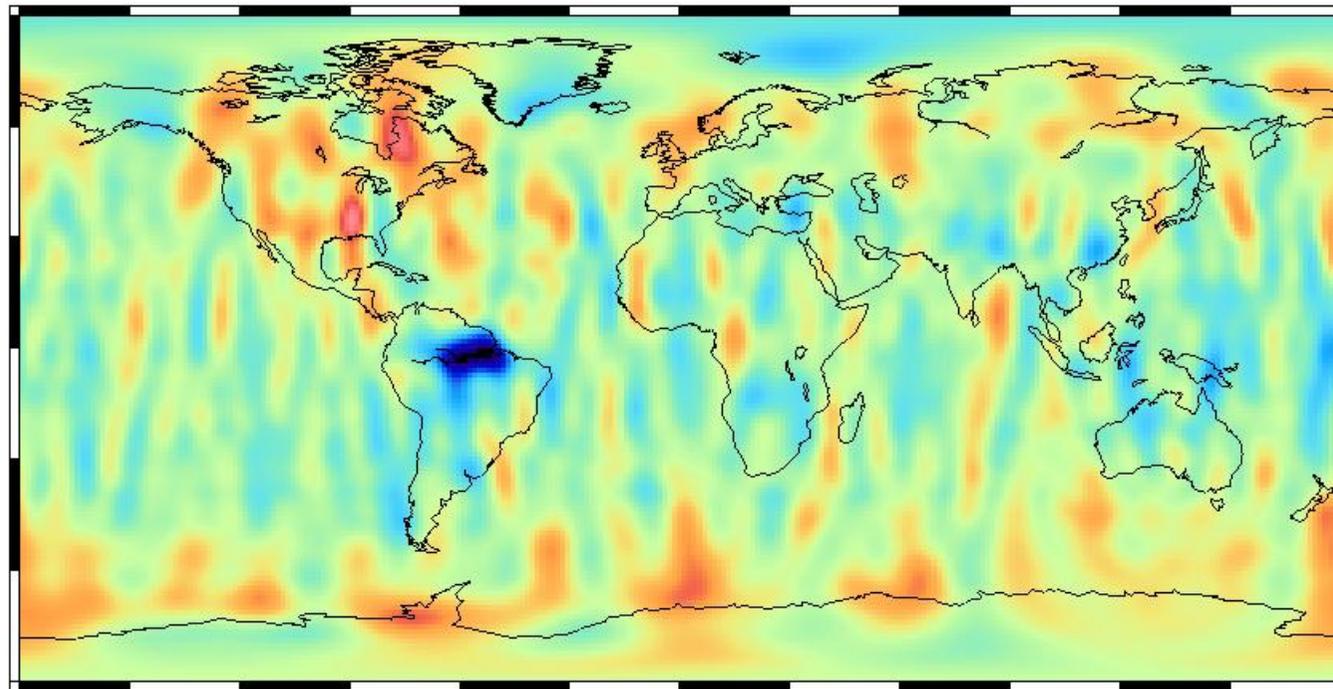
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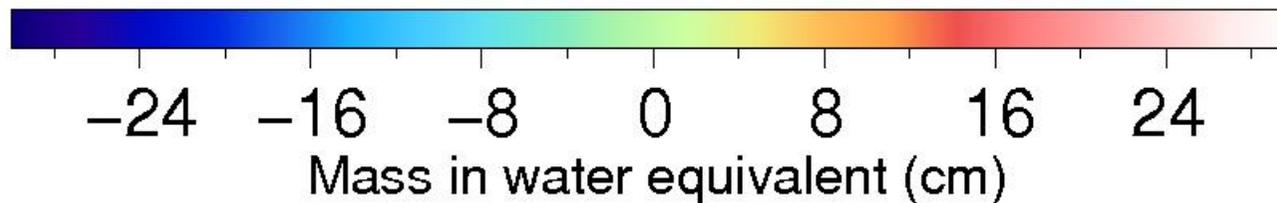
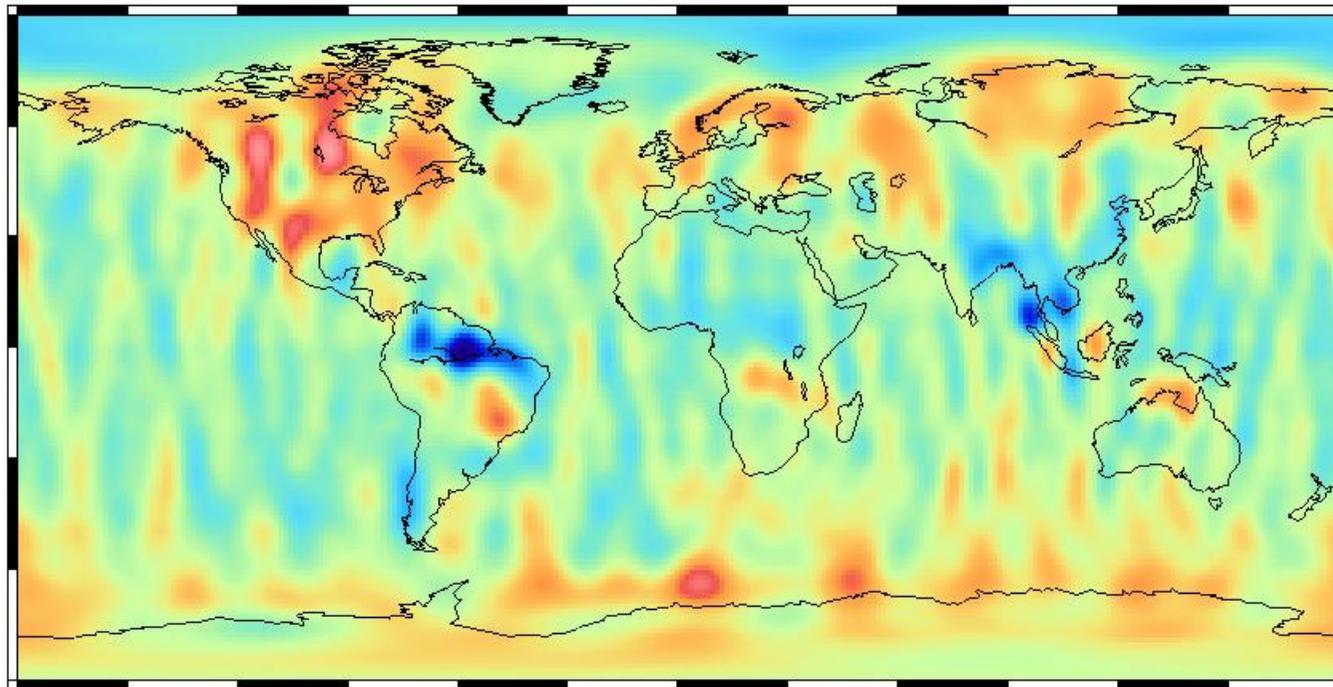
Geoid Variation - November 2004



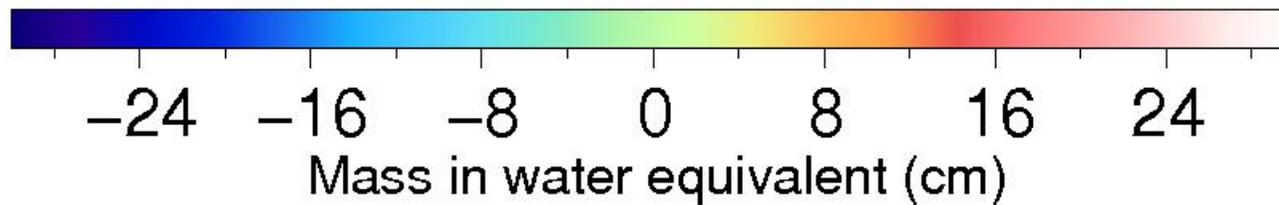
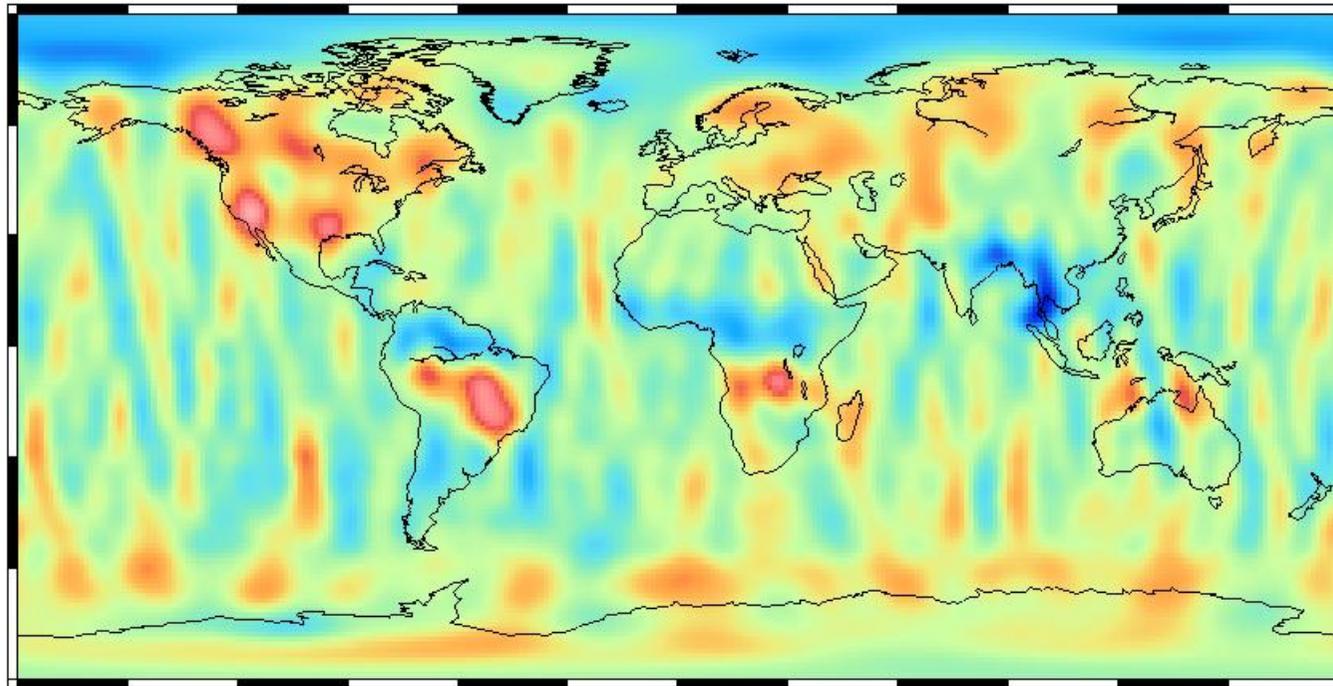
Geoid Variation - December 2004



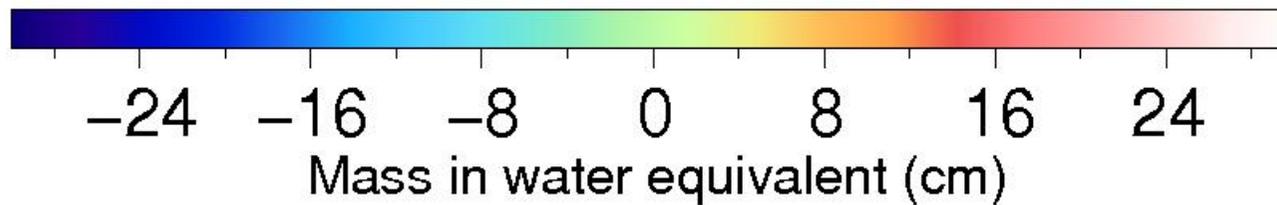
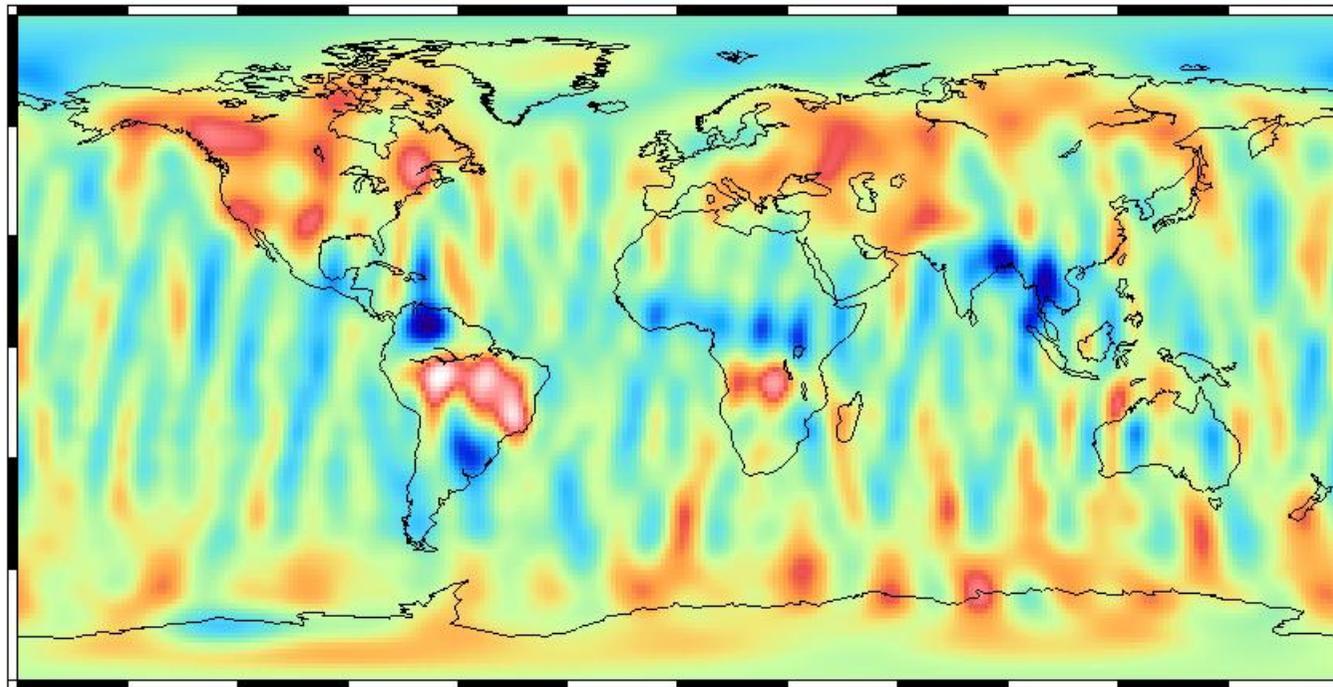
Geoid Variation - January 2005



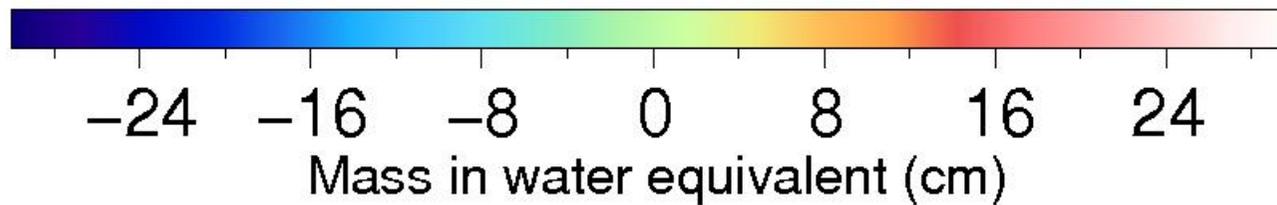
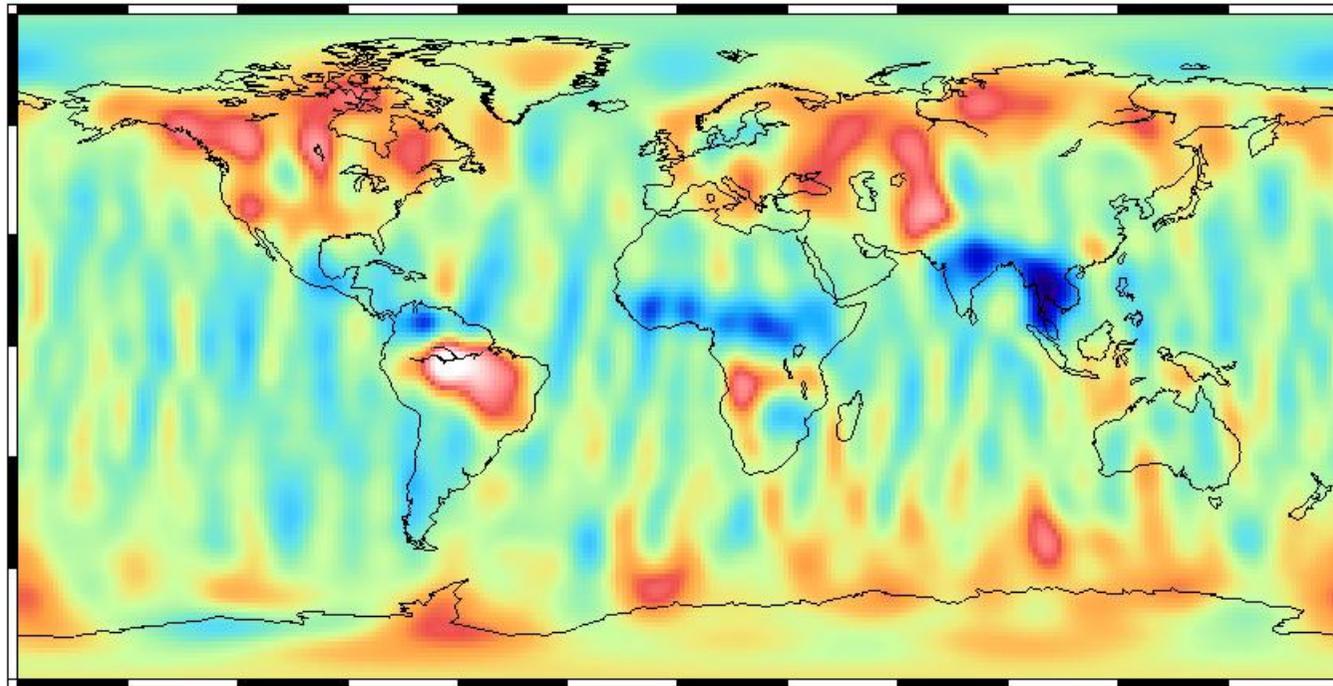
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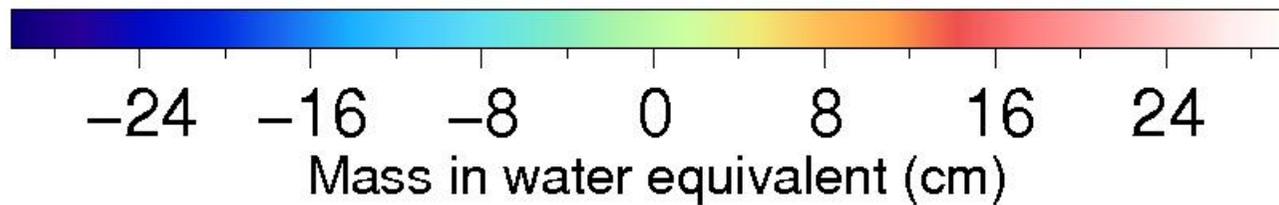
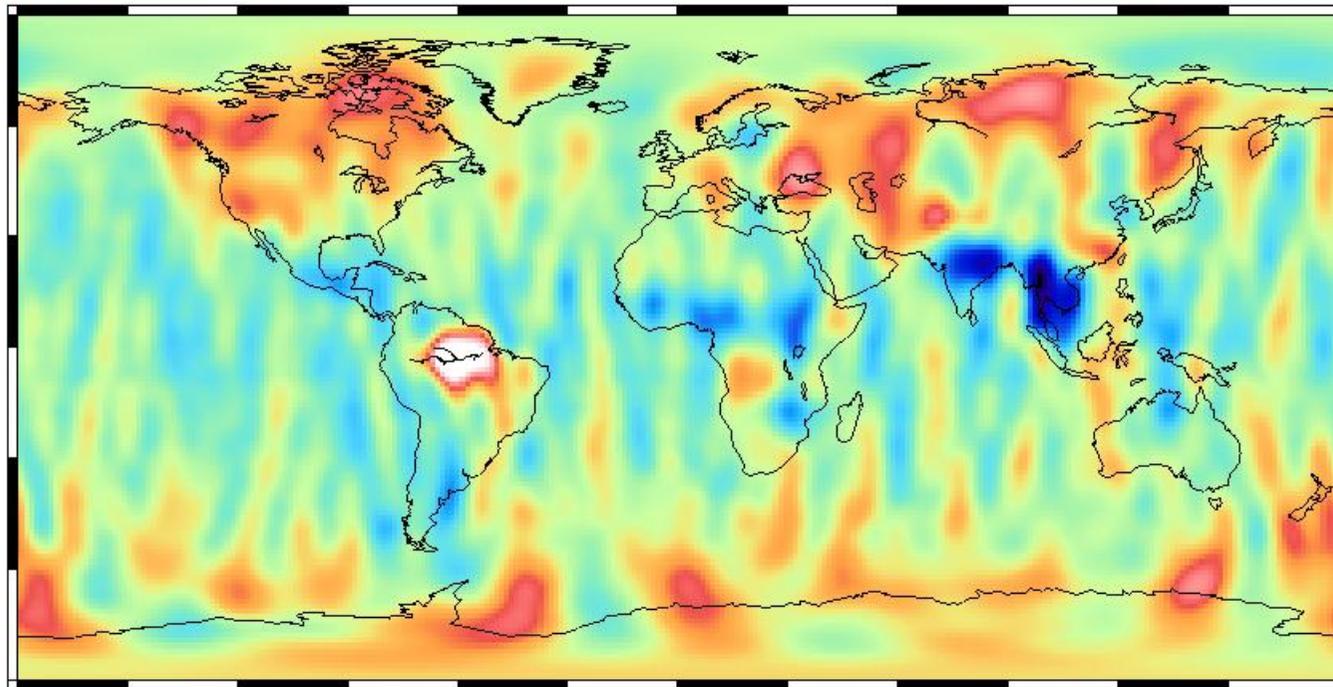
Geoid Variation - March 2005



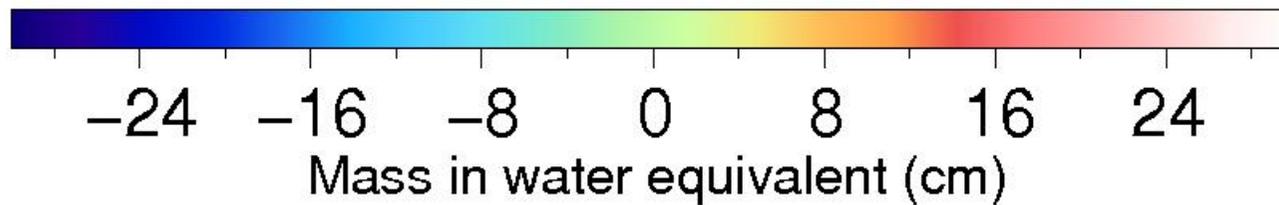
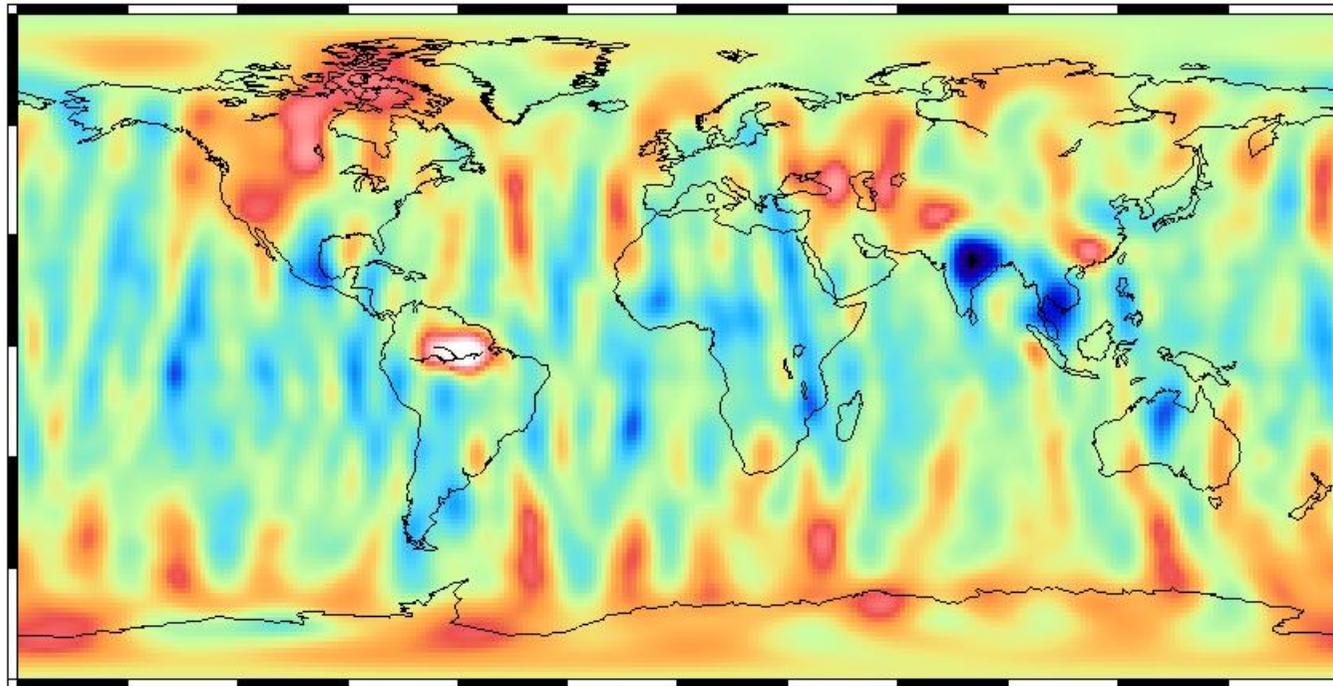
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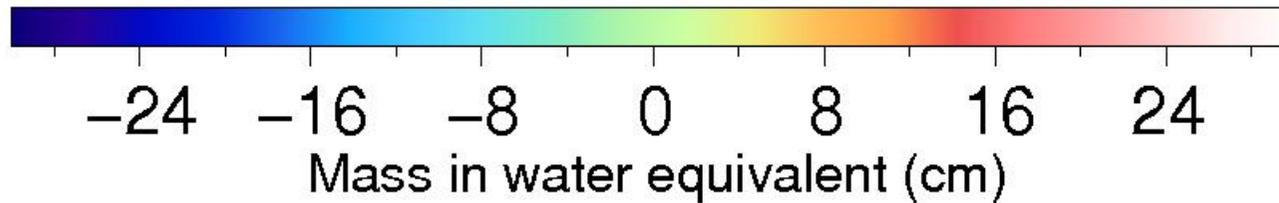
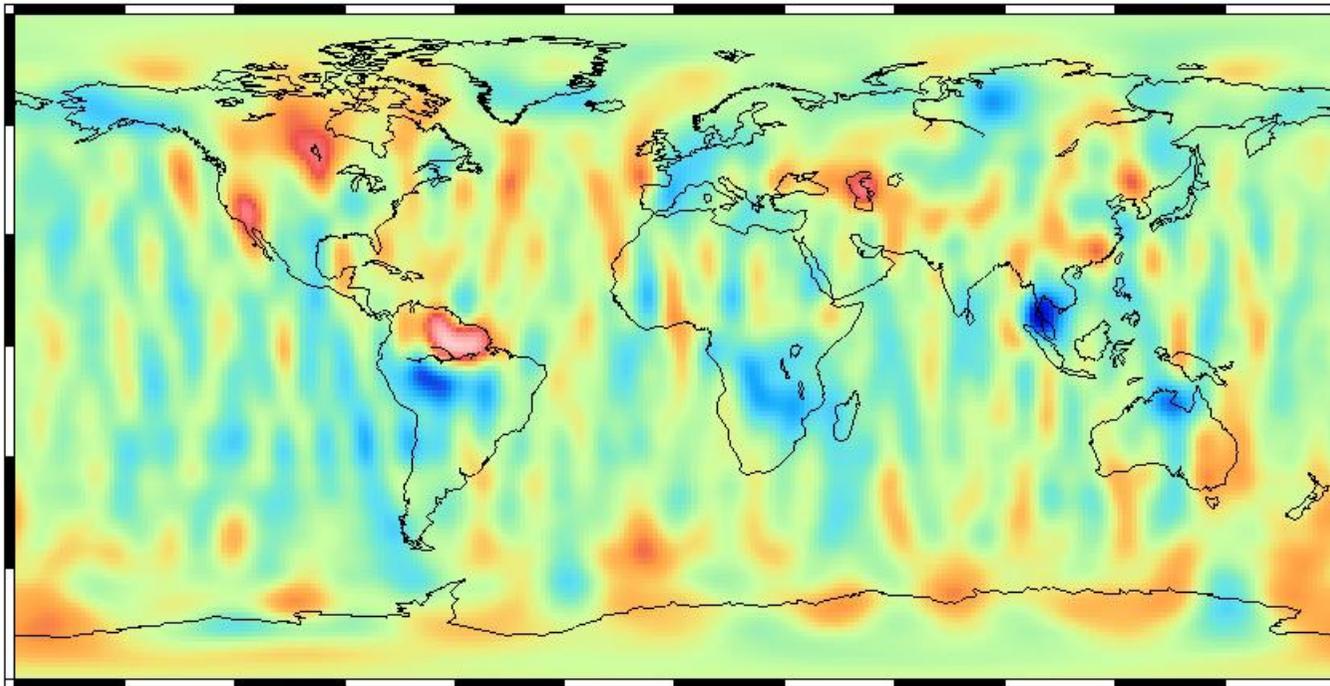
Geoid Variation - May 2005



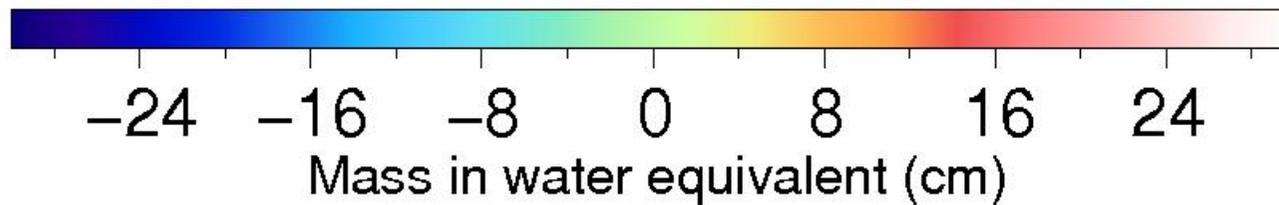
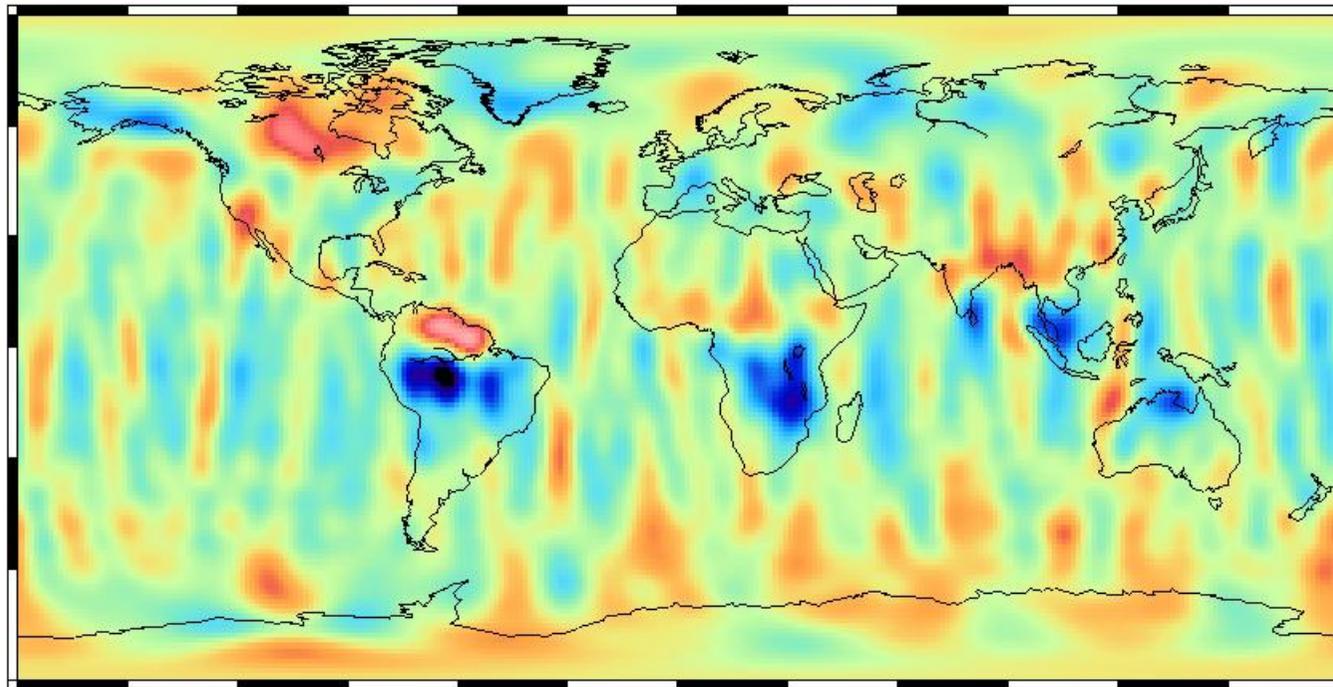
Geoid Variation - June 2005



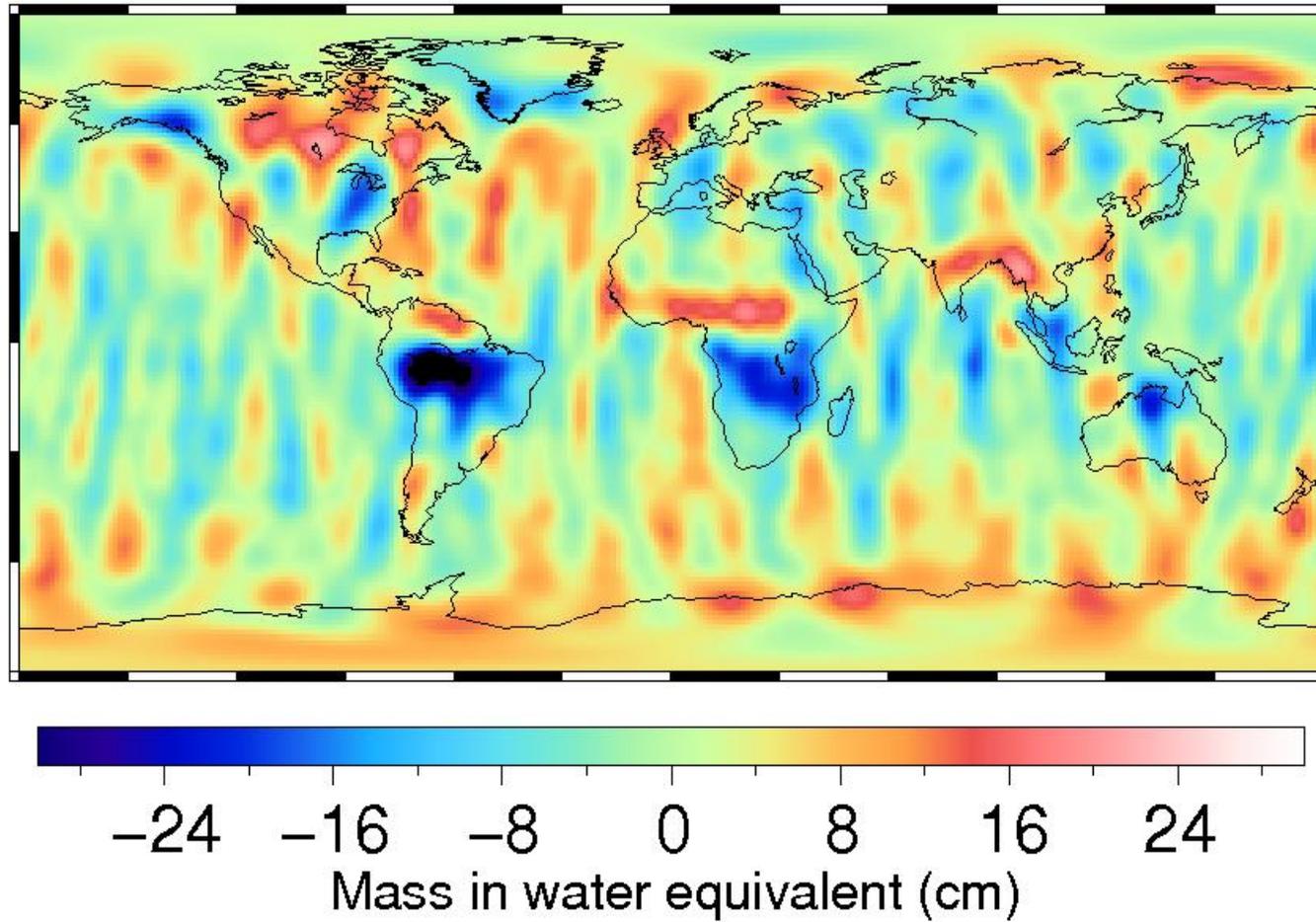
Geoid Variation - July 2005



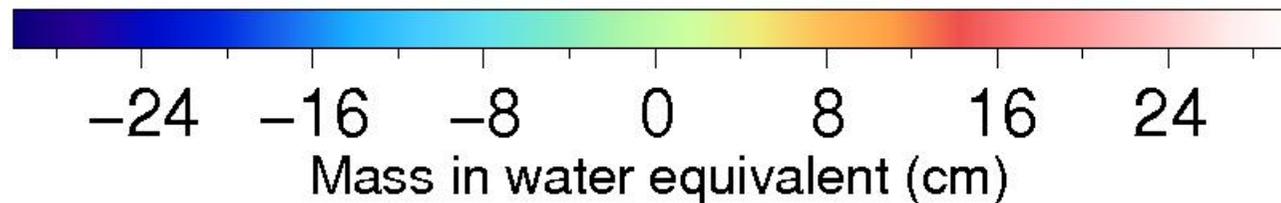
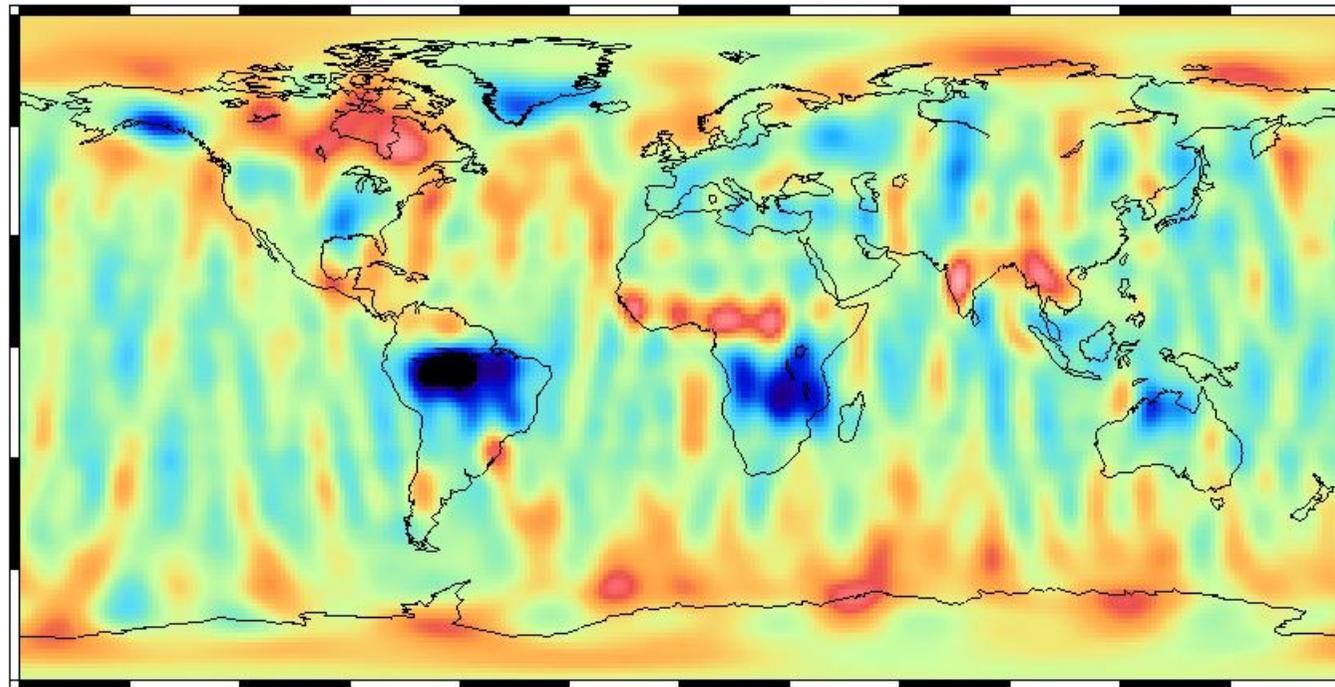
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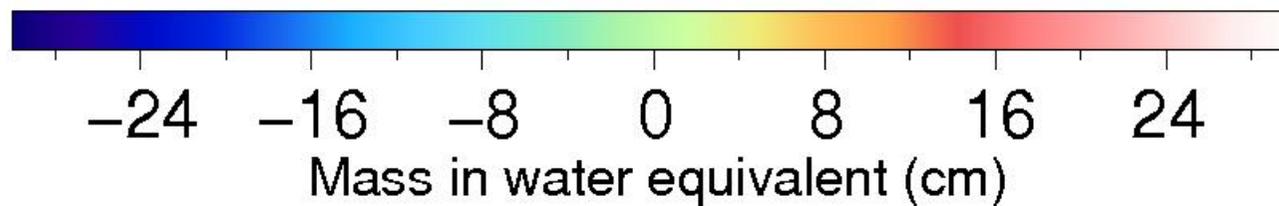
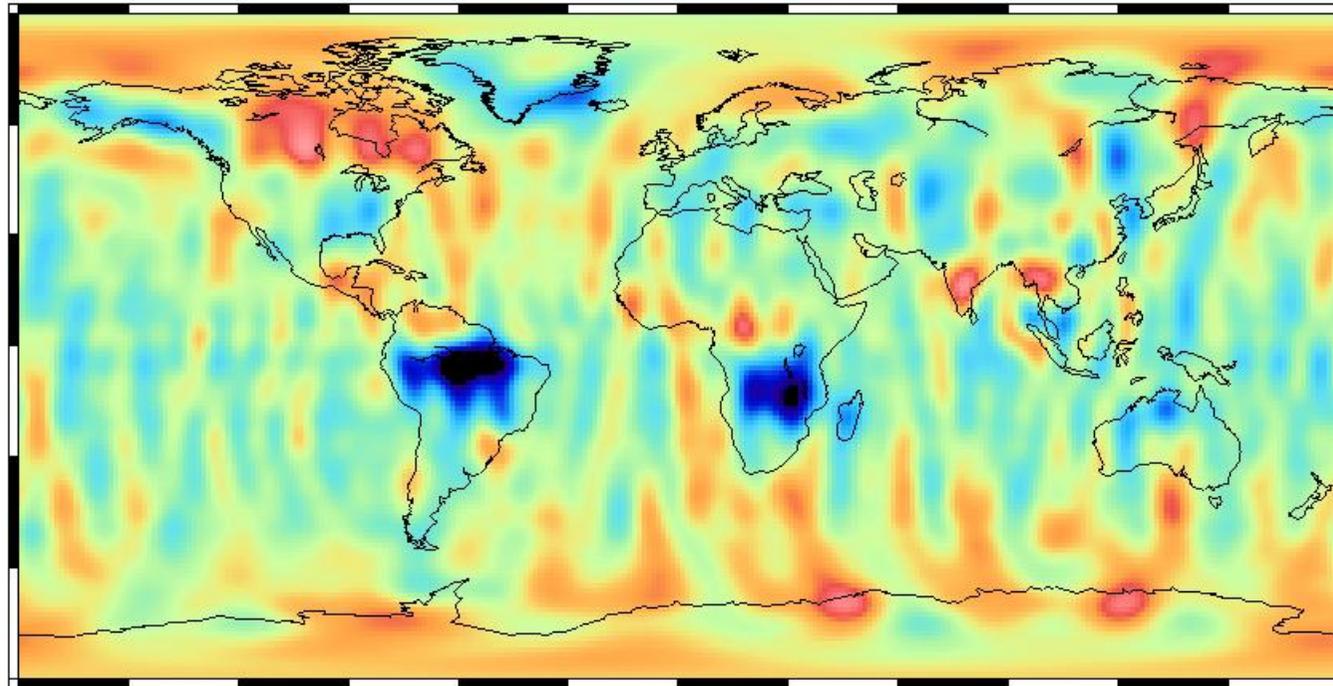
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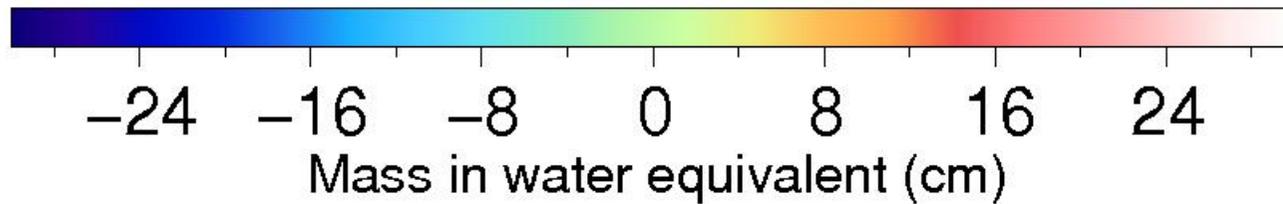
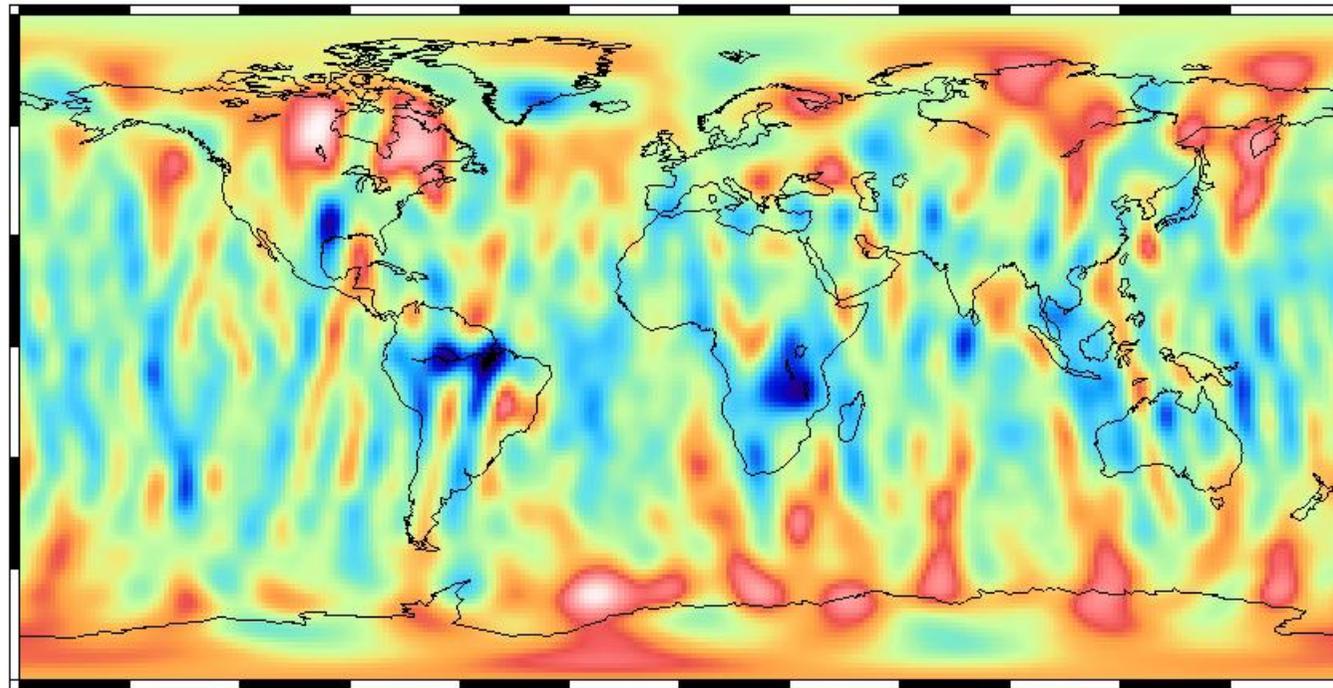
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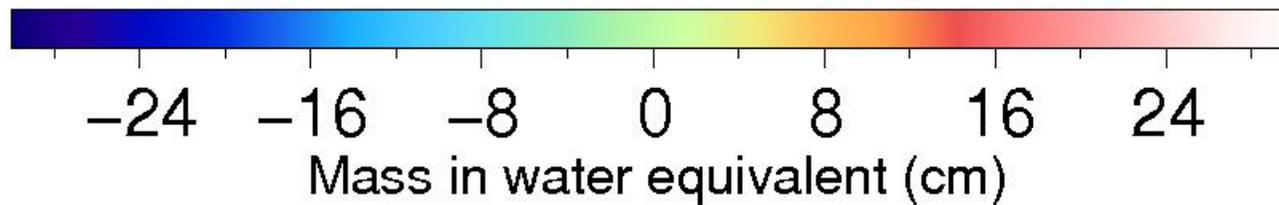
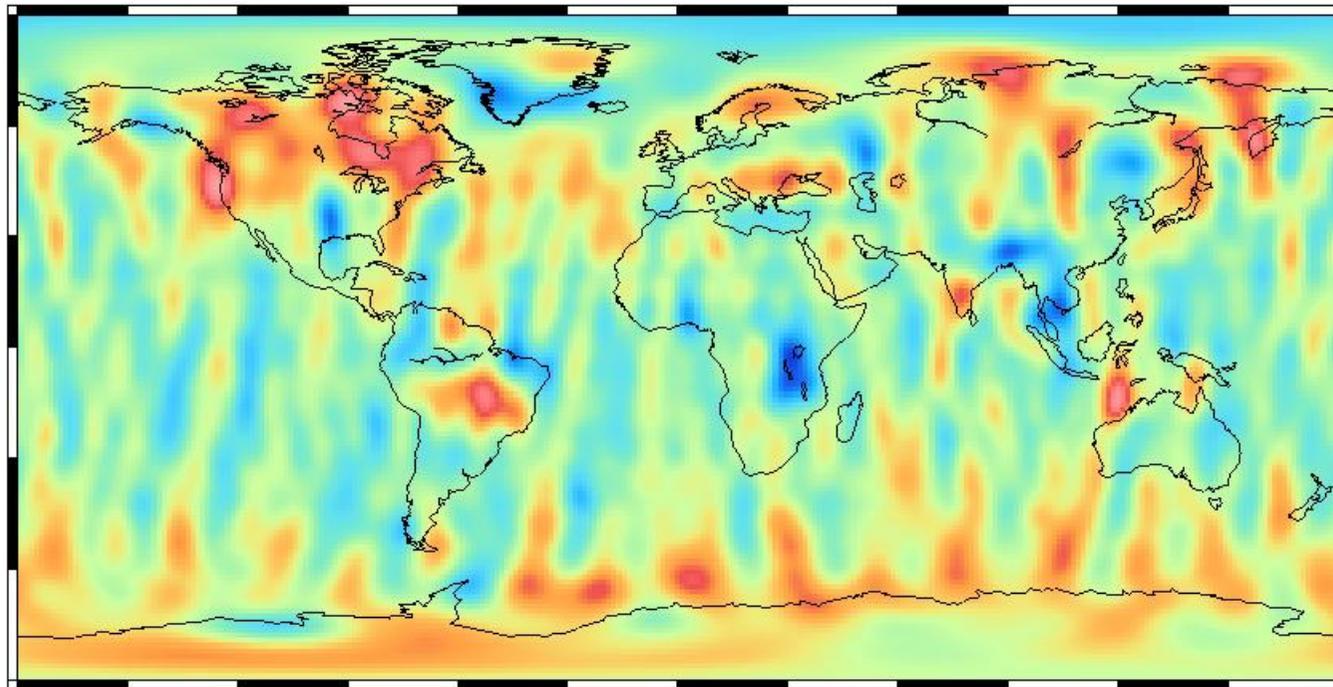
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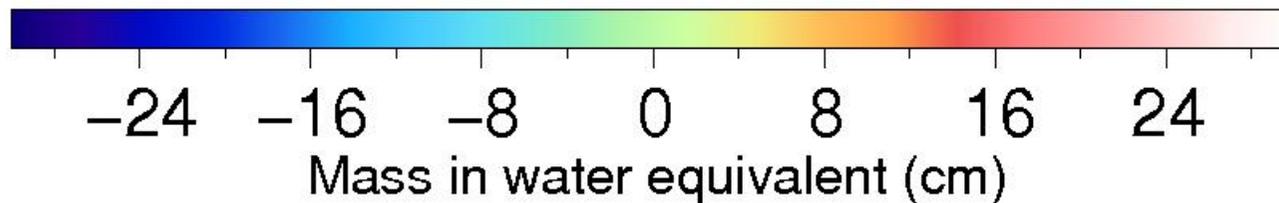
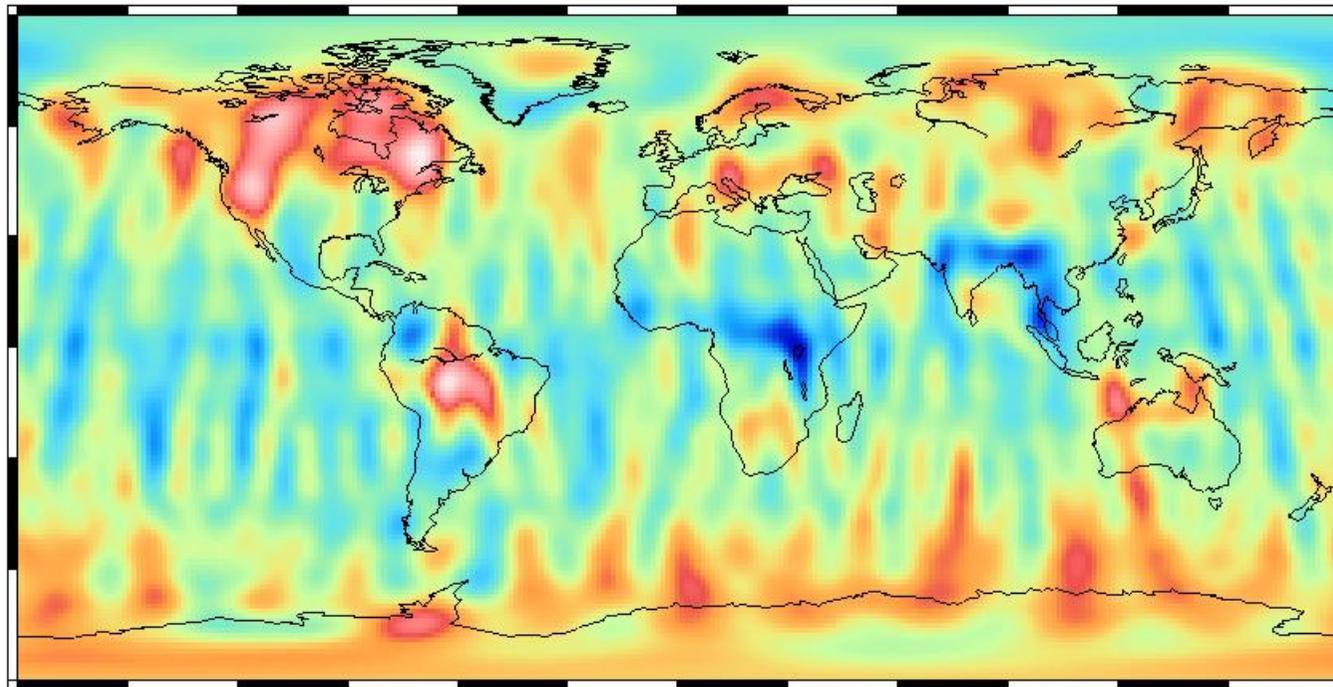
Geoid Variation - December 2005



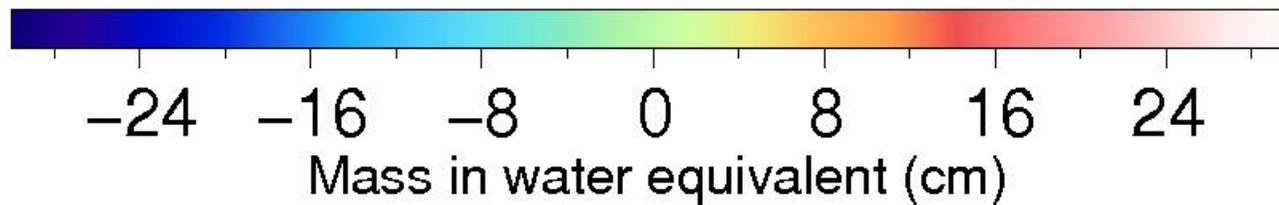
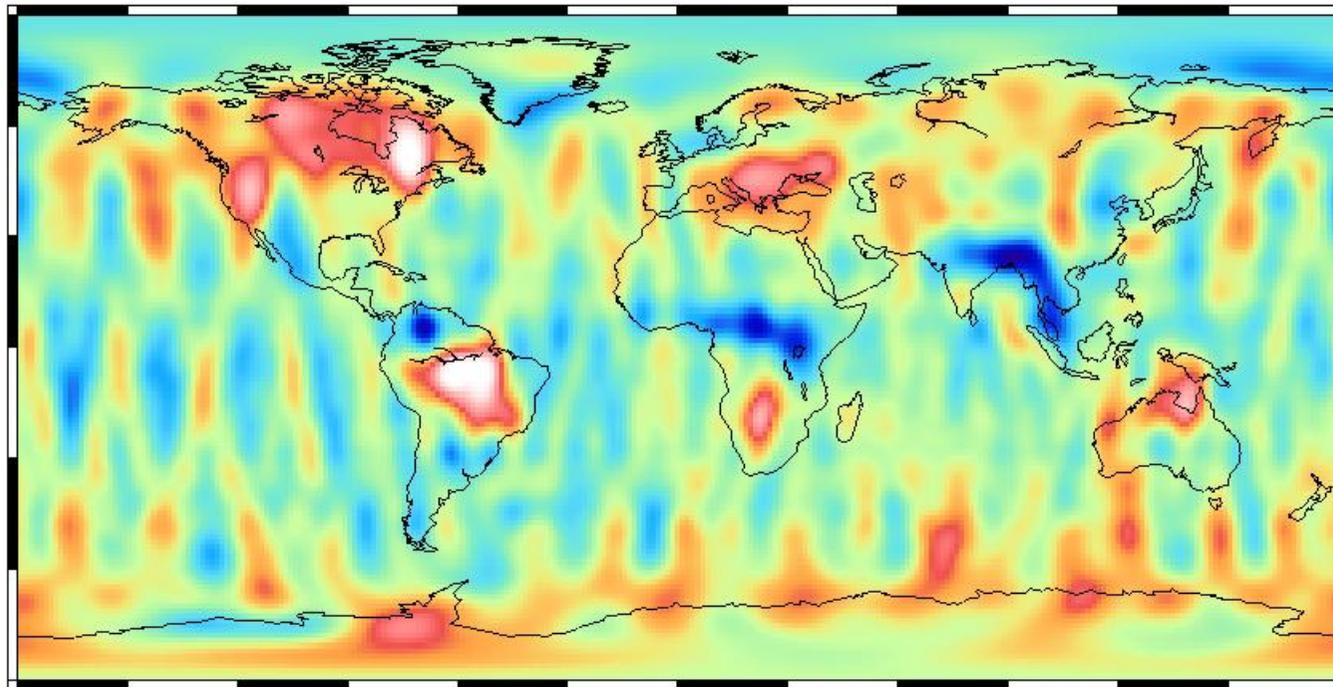
Geoid Variation - January 2006



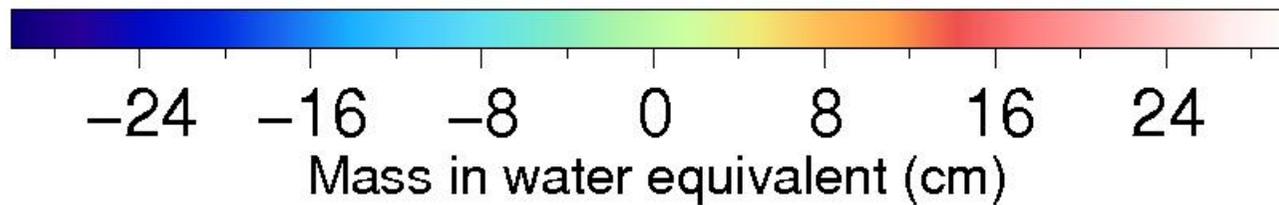
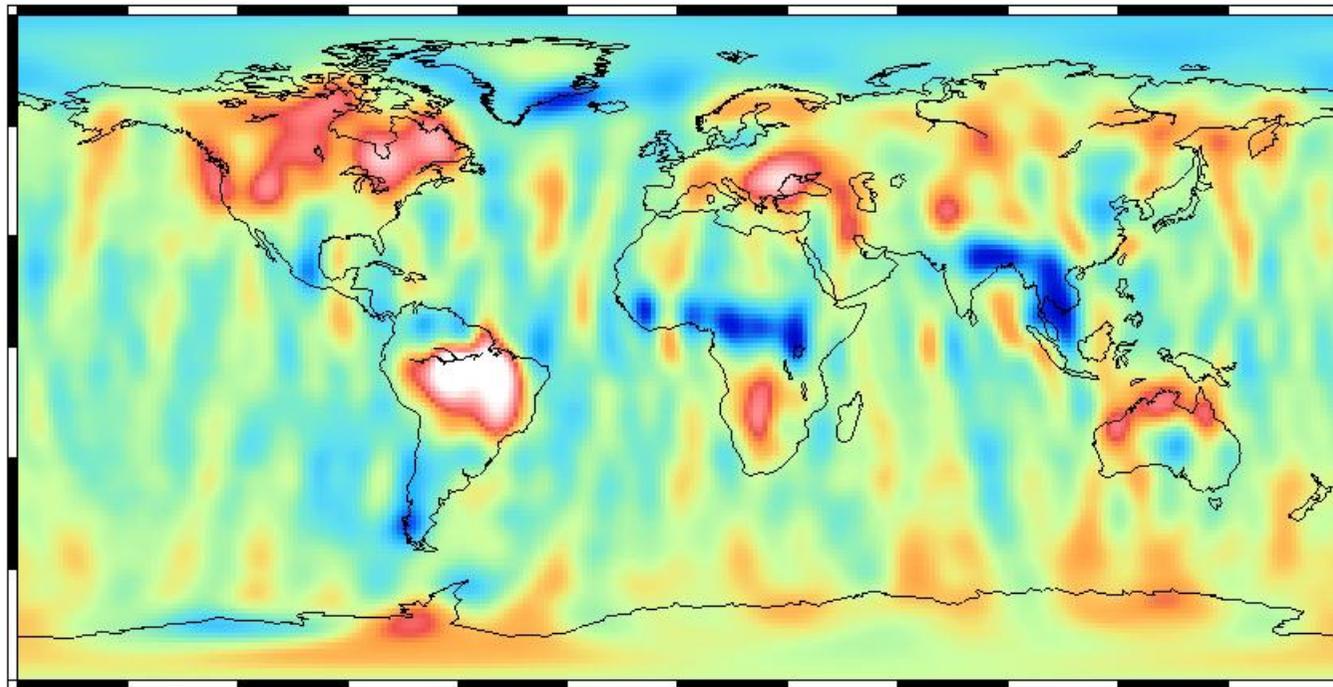
Geoid Variation - February 2006



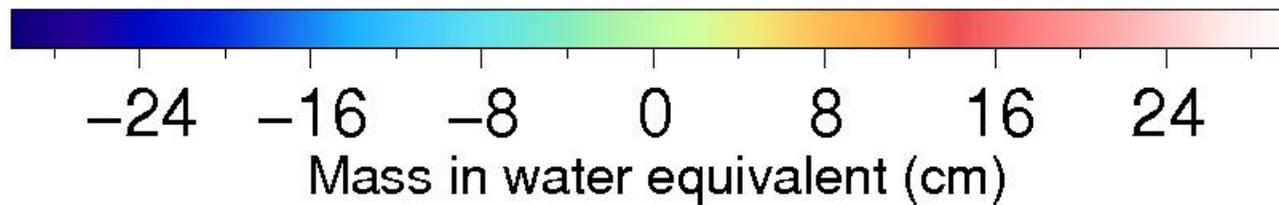
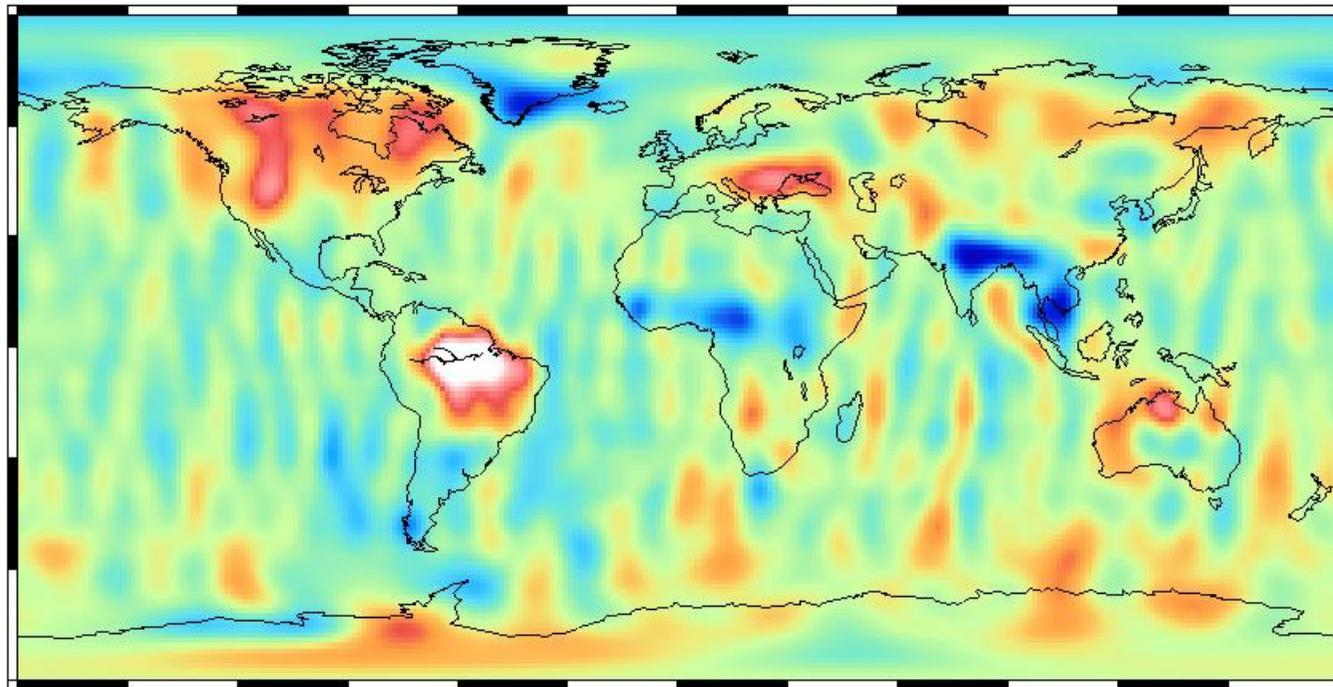
Geoid Variation - March 2006



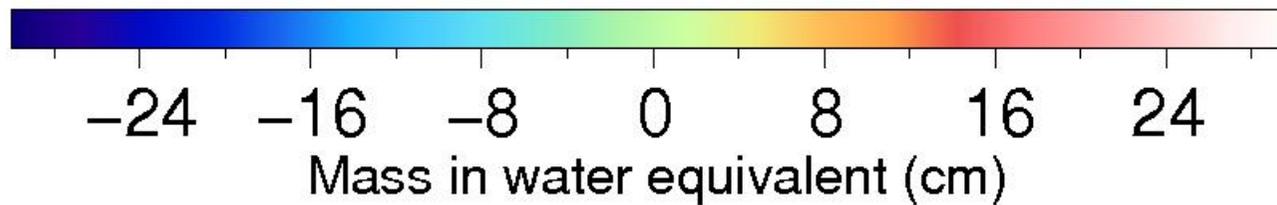
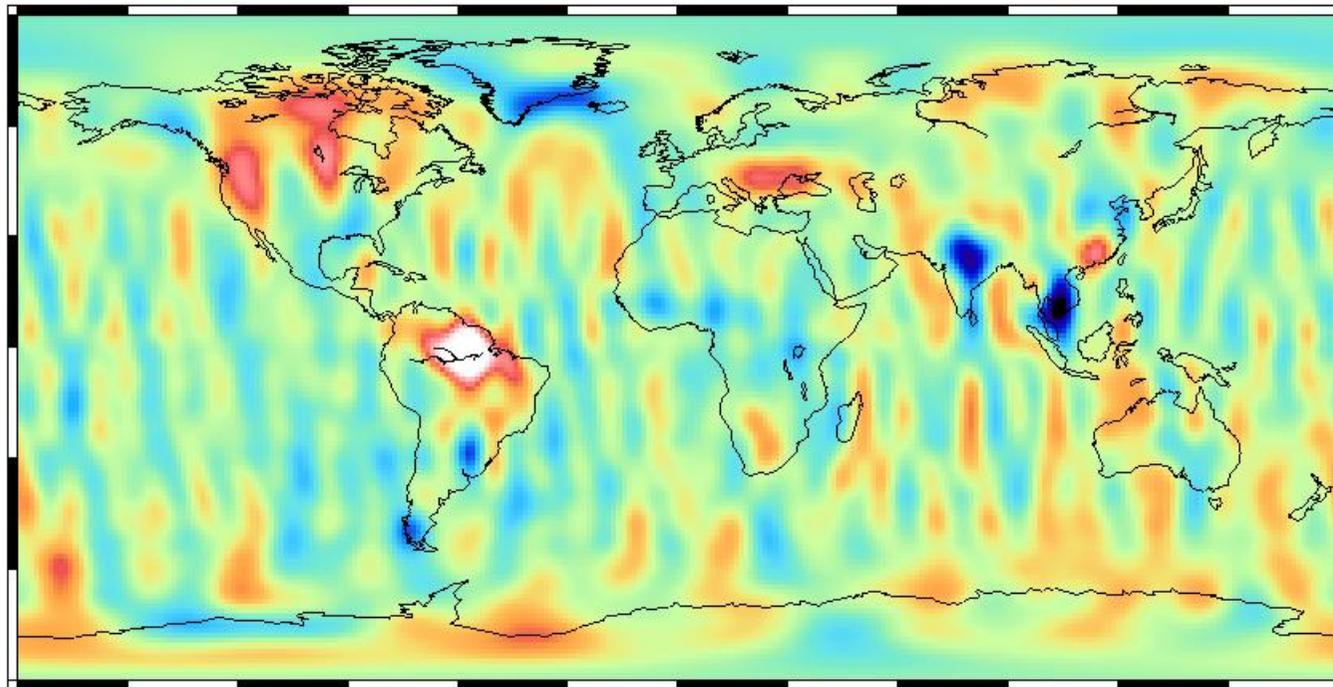
Geoid Variation - April 2006



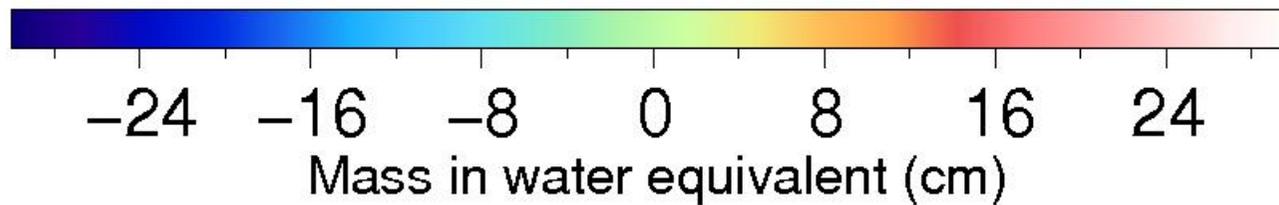
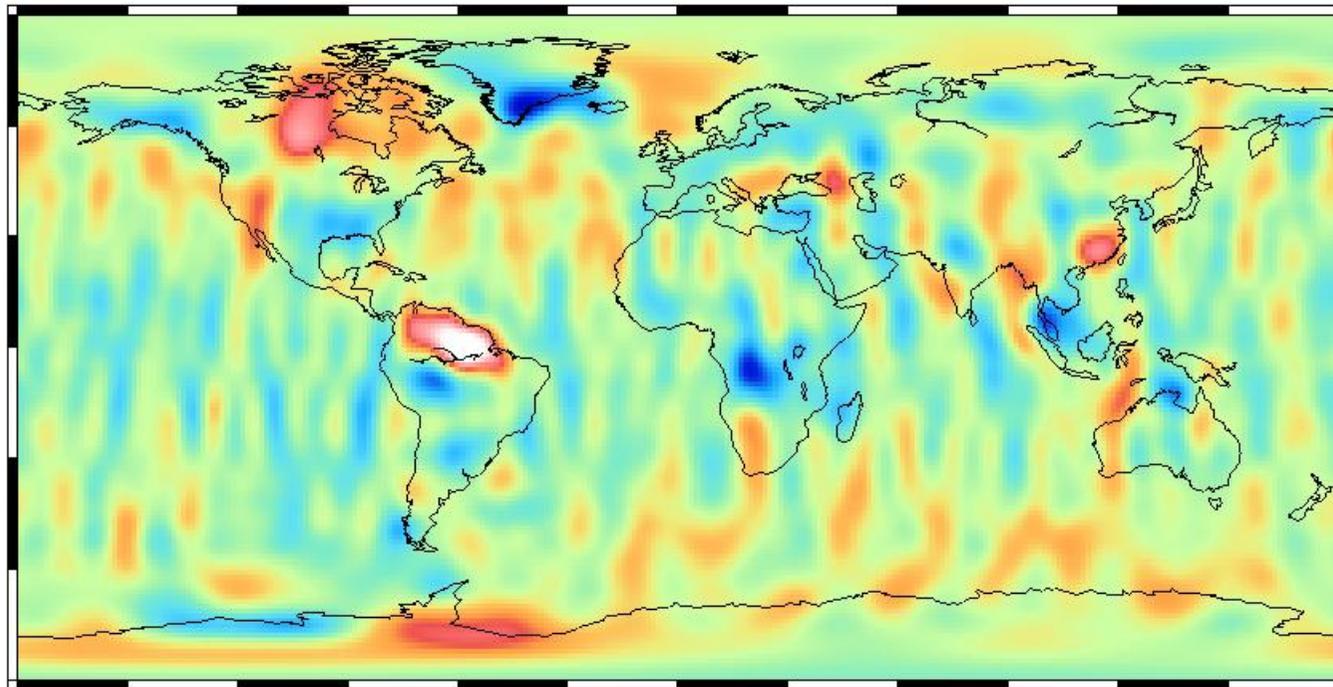
Geoid Variation - May 2006



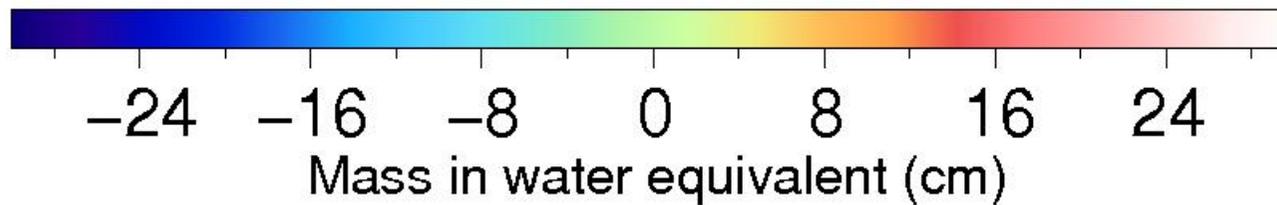
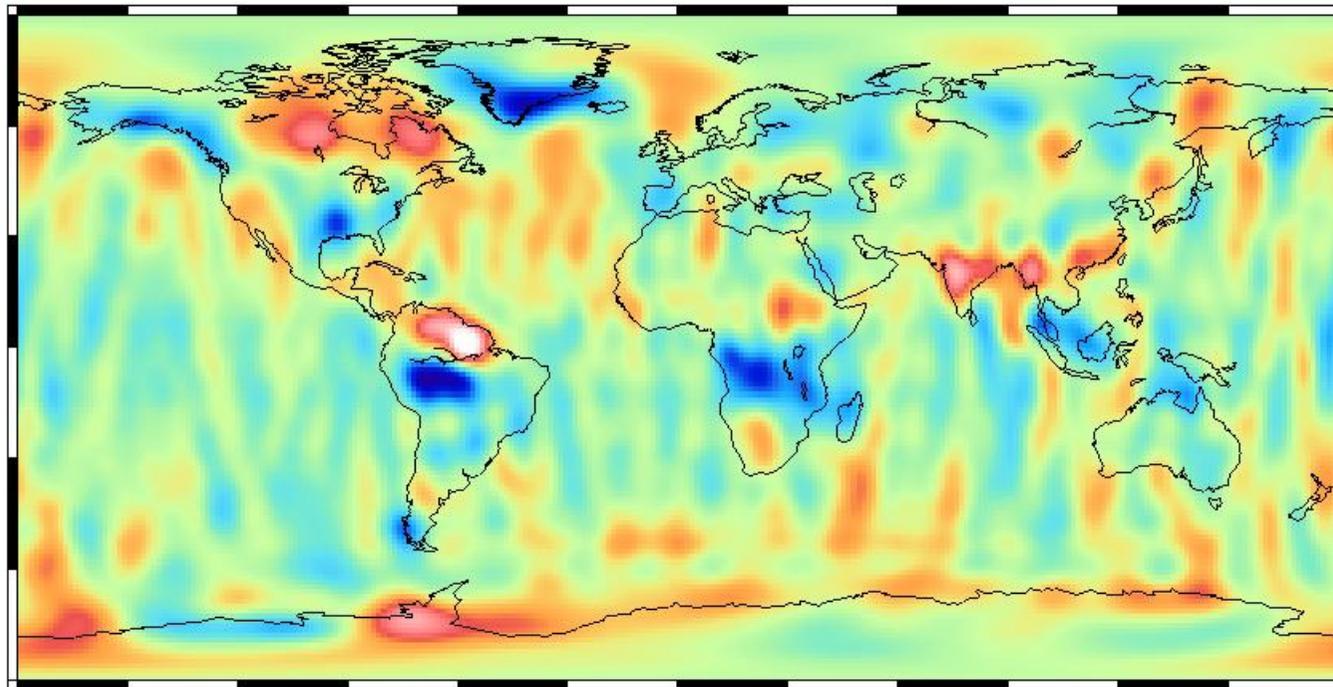
Geoid Variation - June 2006



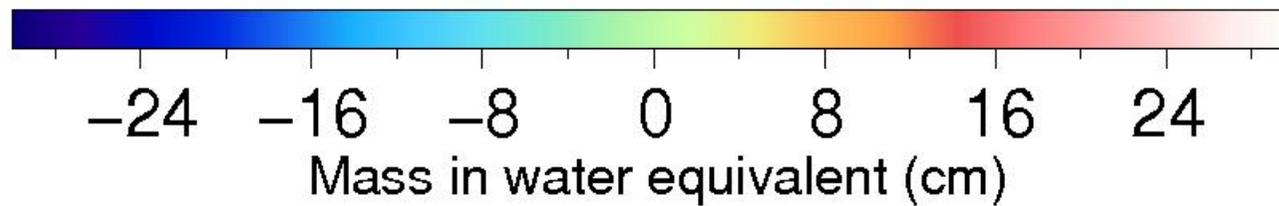
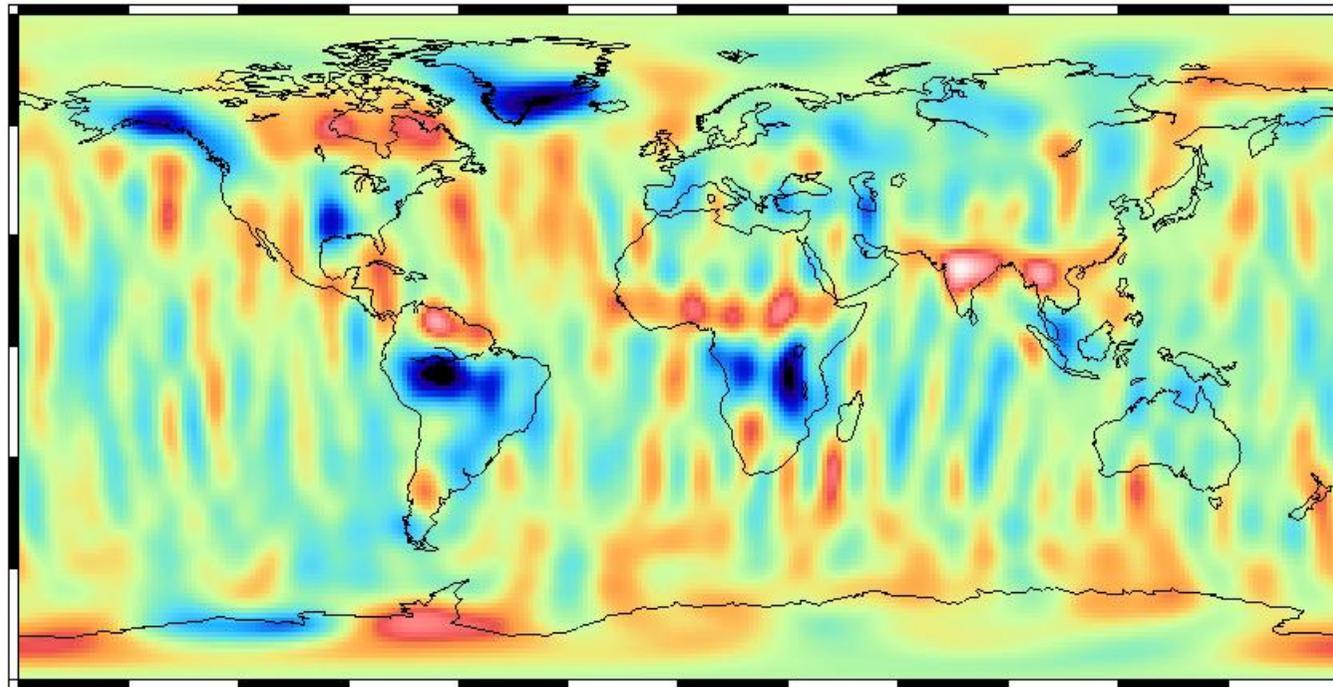
Geoid Variation - July 2006



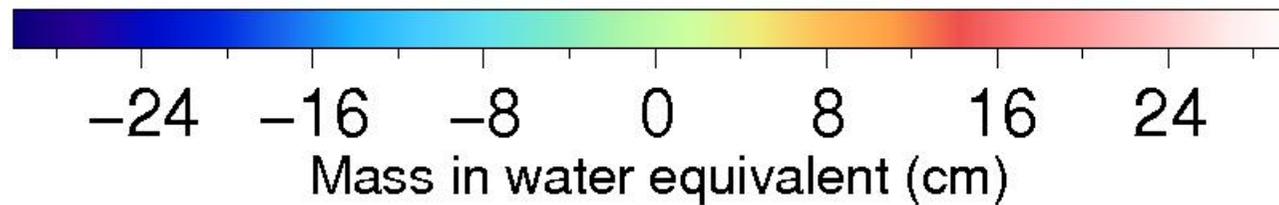
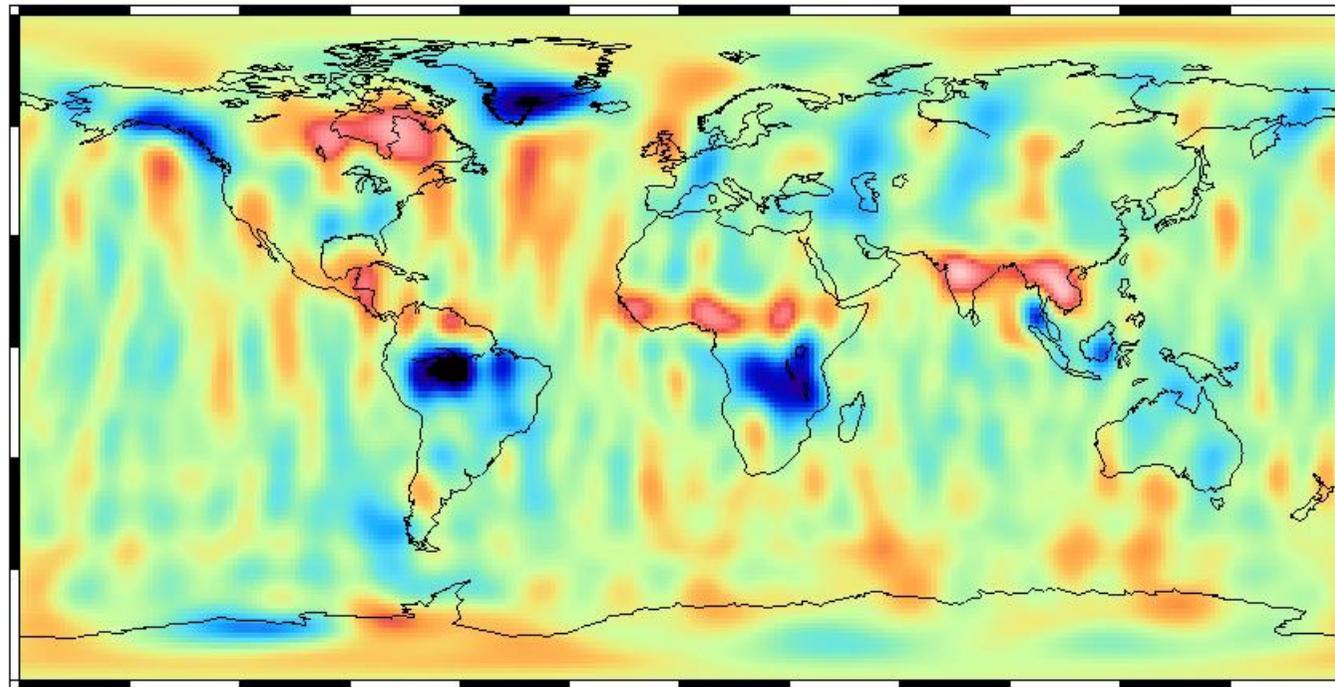
Geoid Variation - August 2006



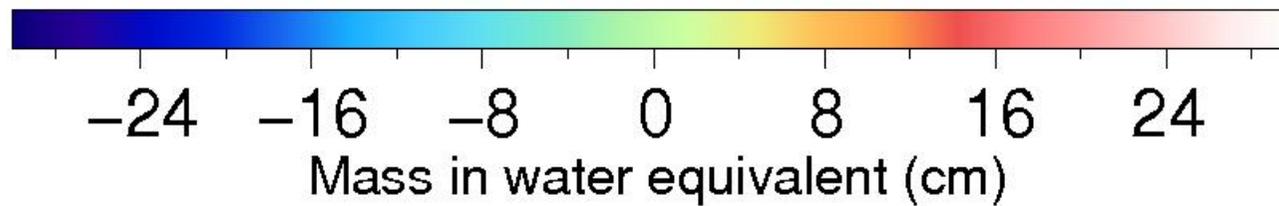
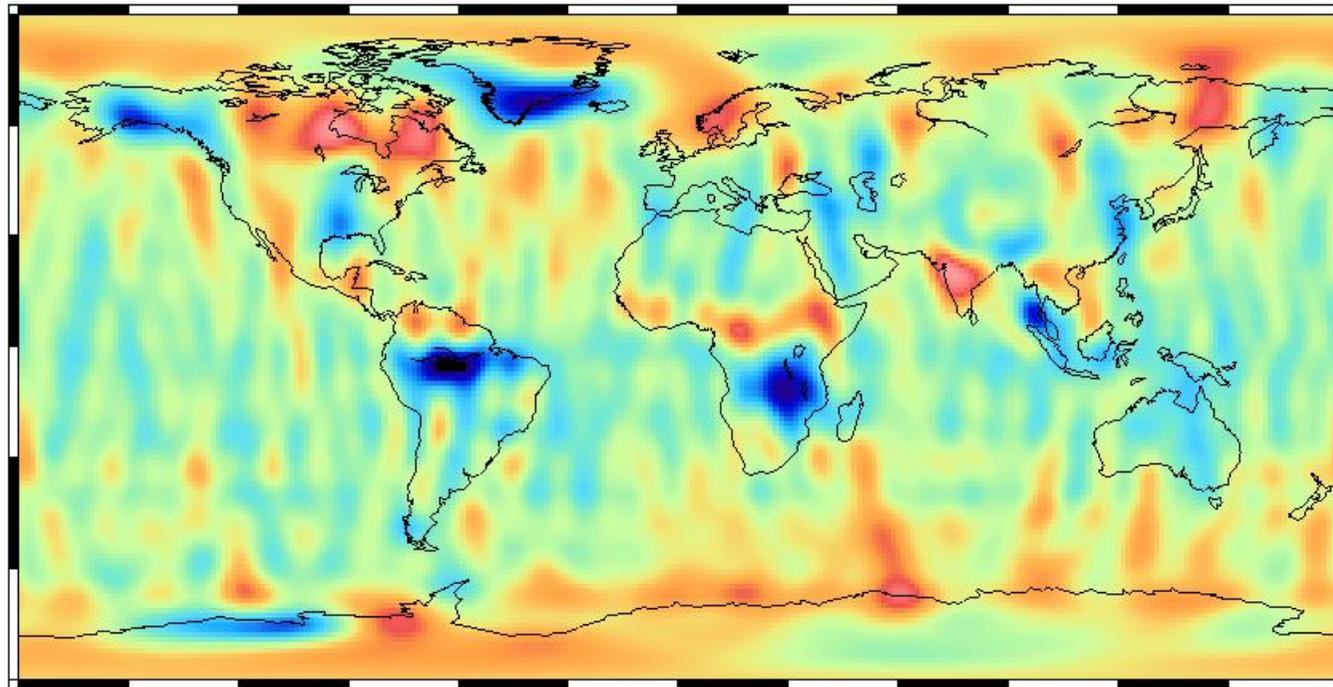
Geoid Variation - September 2006



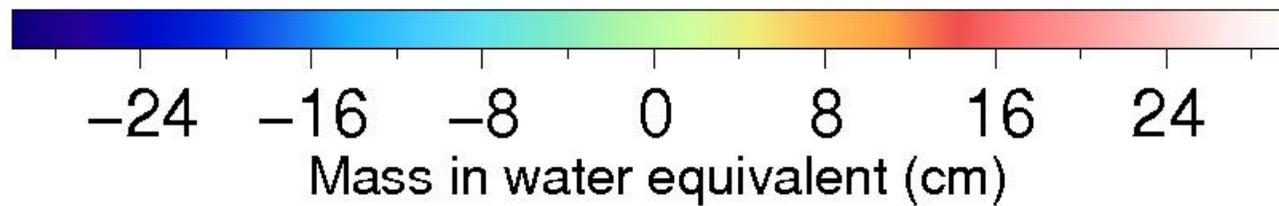
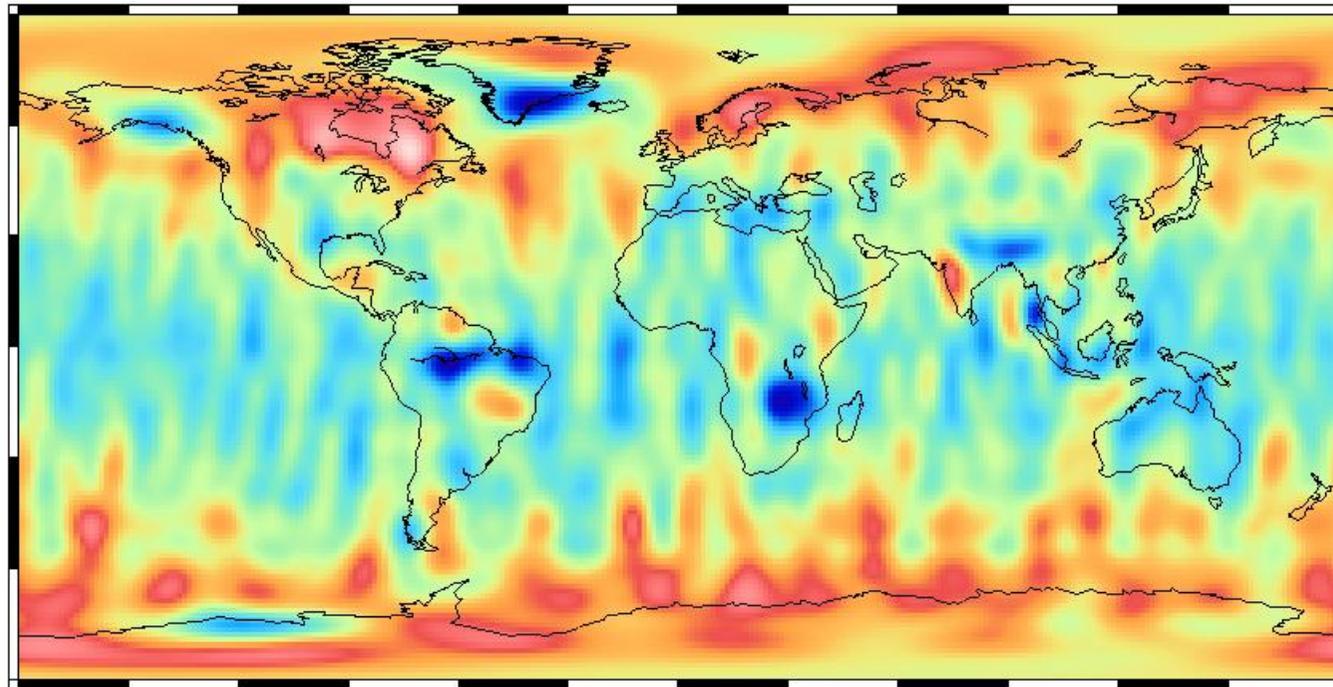
Geoid Variation - October 2006



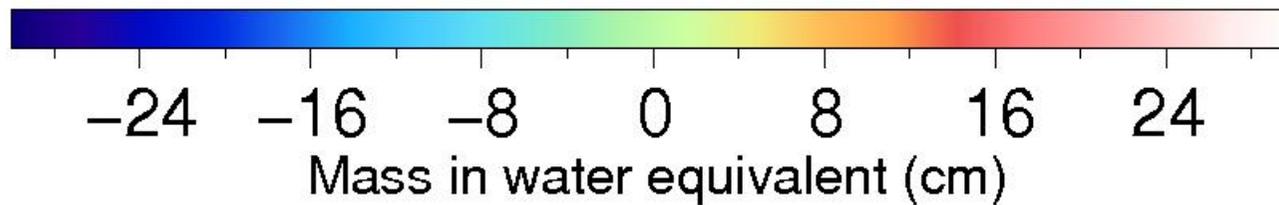
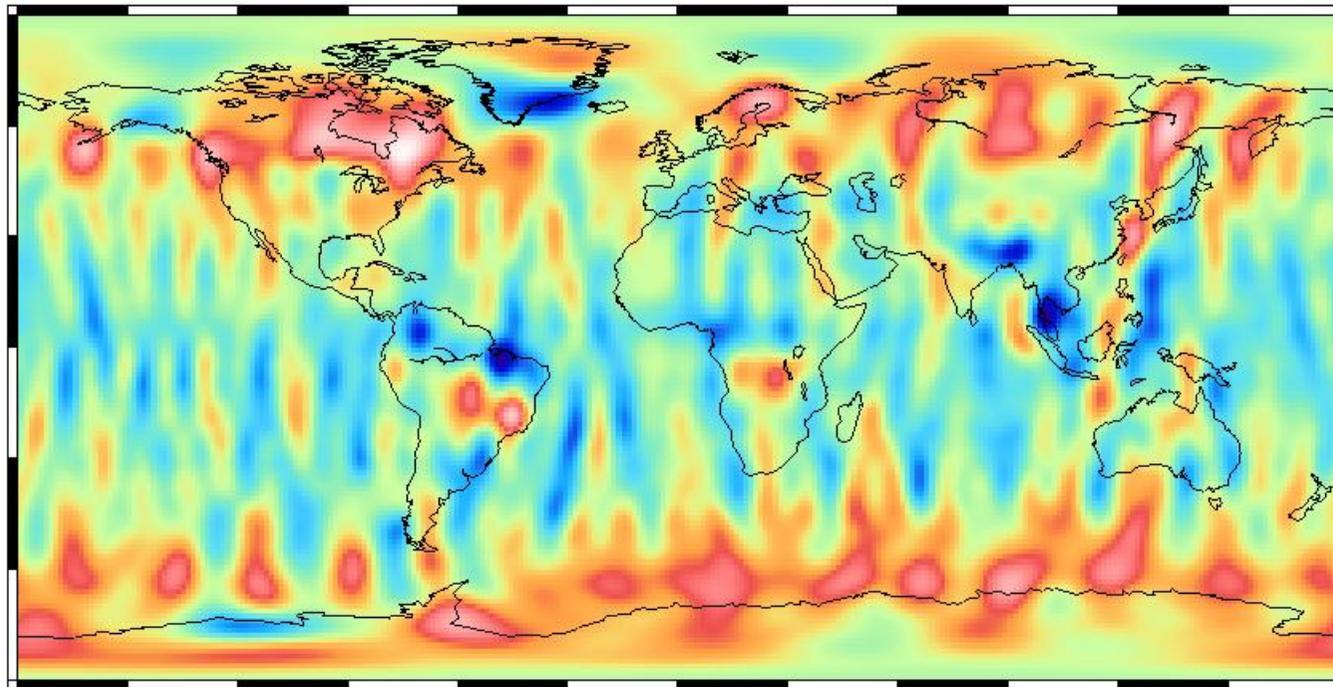
Geoid Variation - November 2006



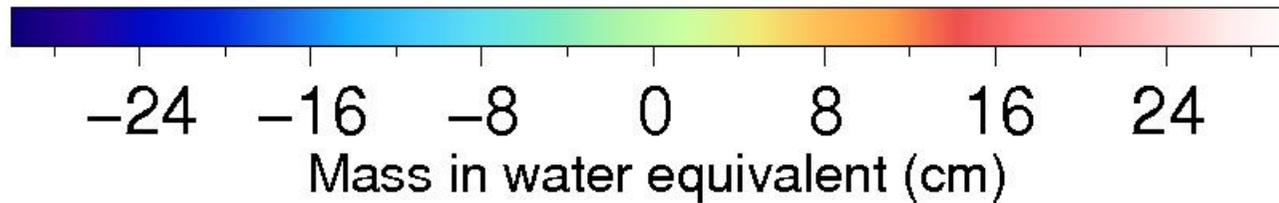
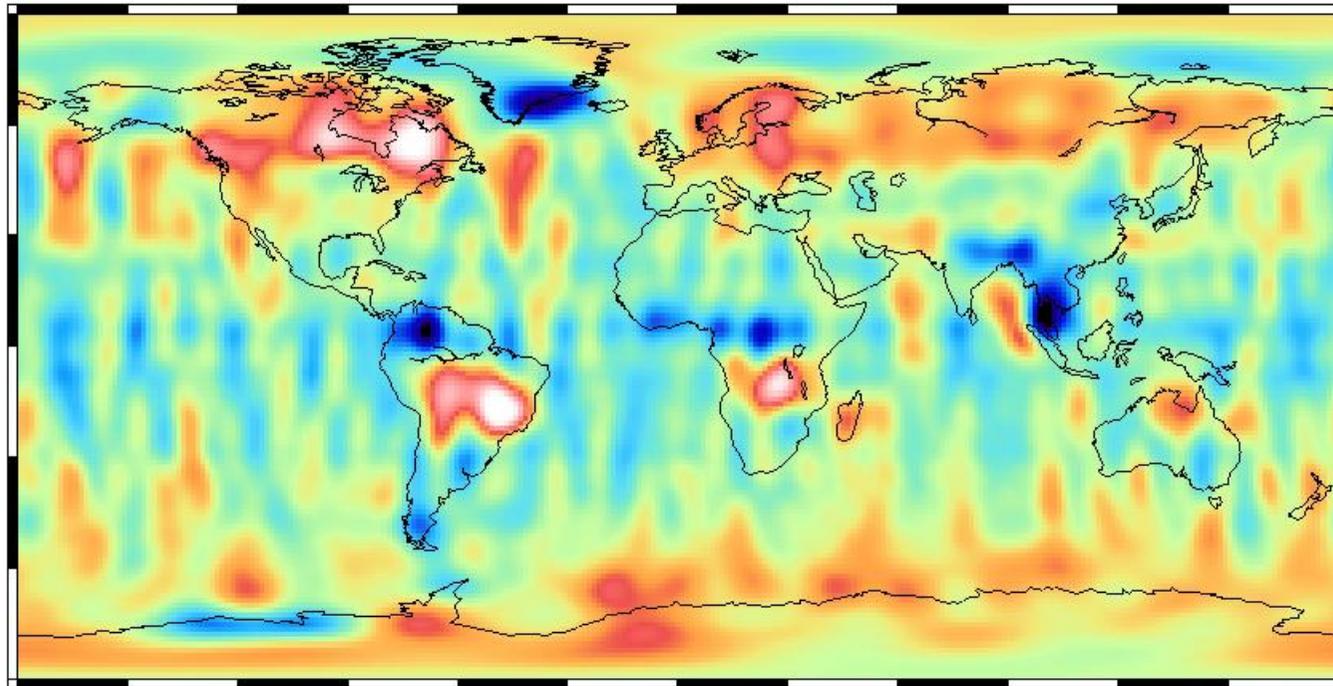
Geoid Variation - December 2006



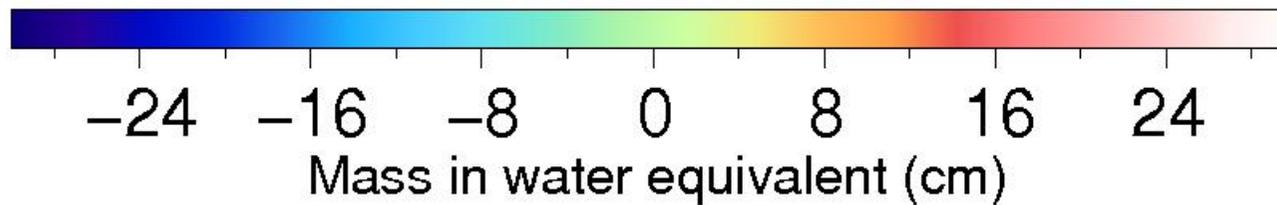
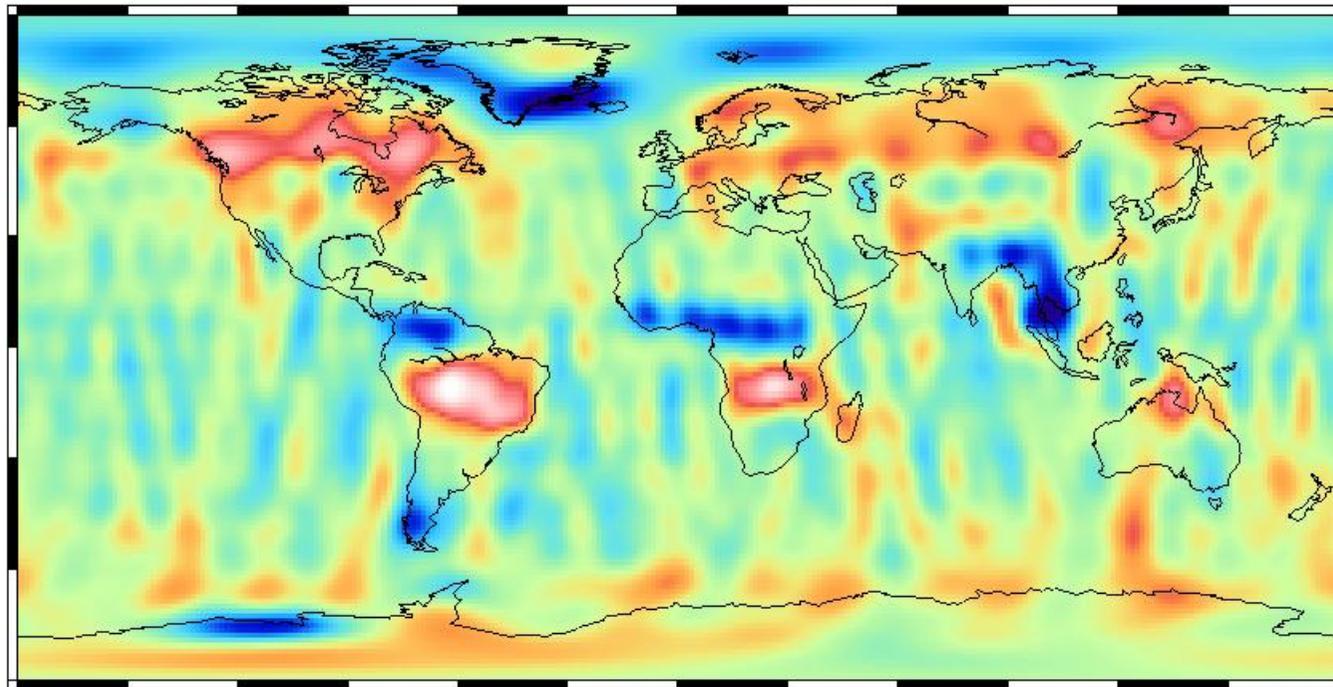
Geoid Variation - January 2007



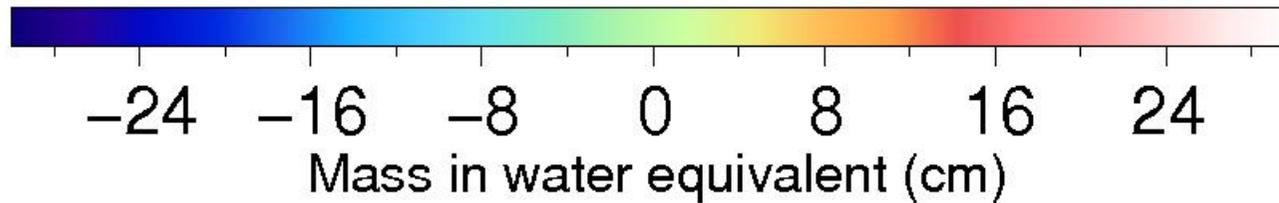
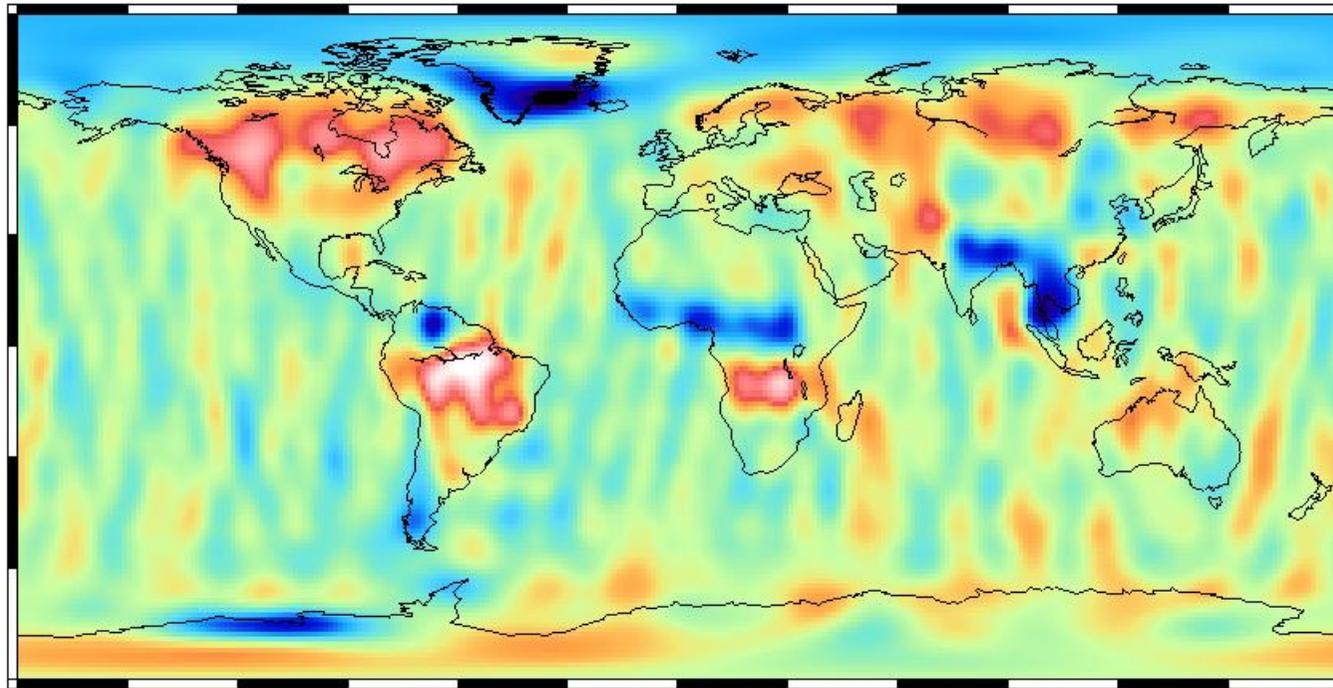
Geoid Variation - February 2007



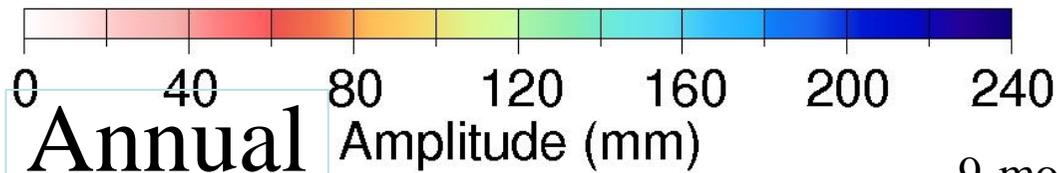
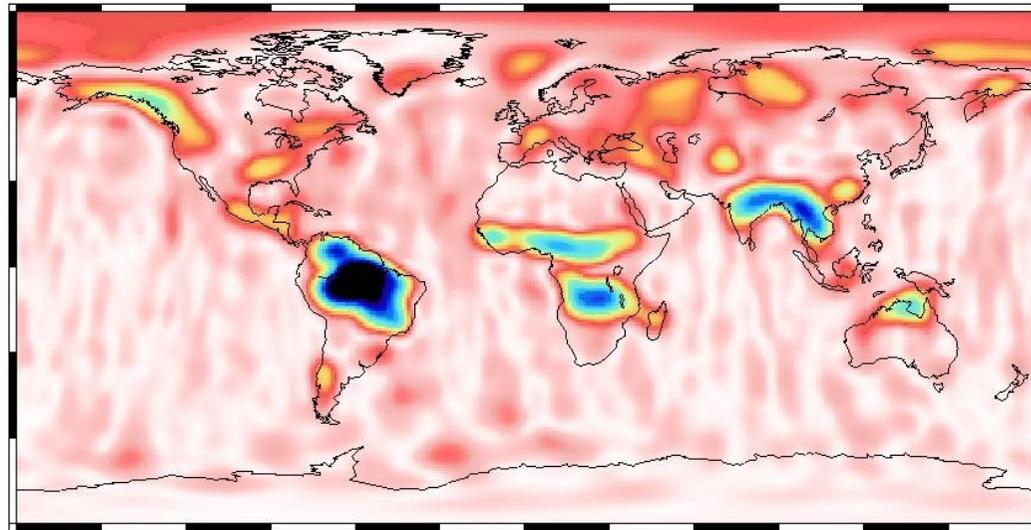
Geoid Variation - March 2007



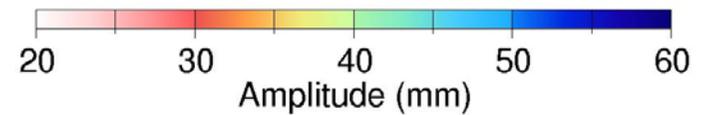
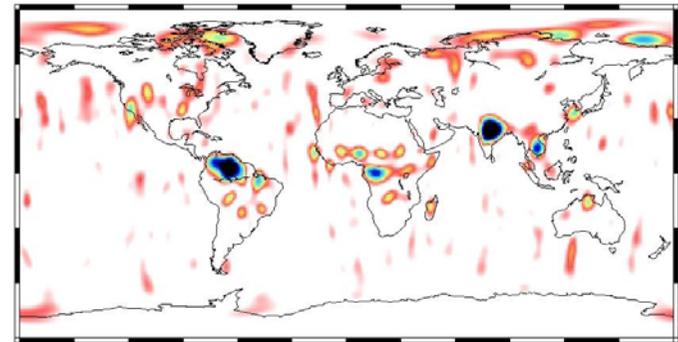
Geoid Variation - April 2007



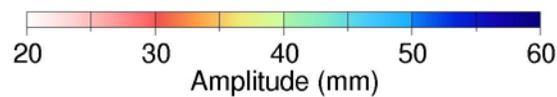
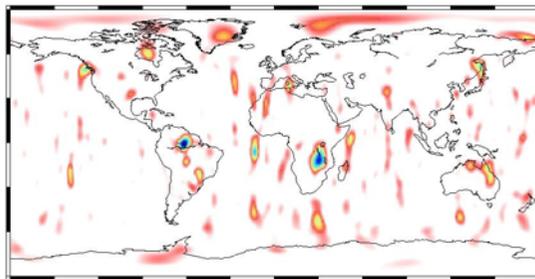
Periodic Signal



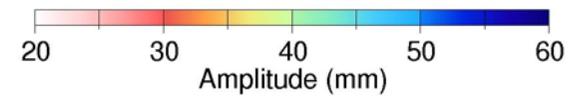
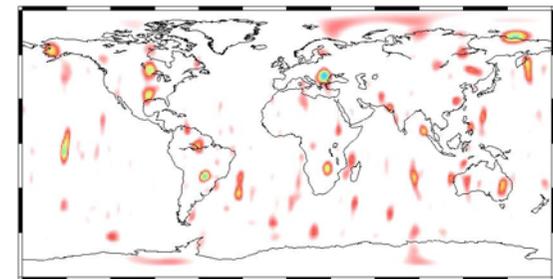
Semi-Annual



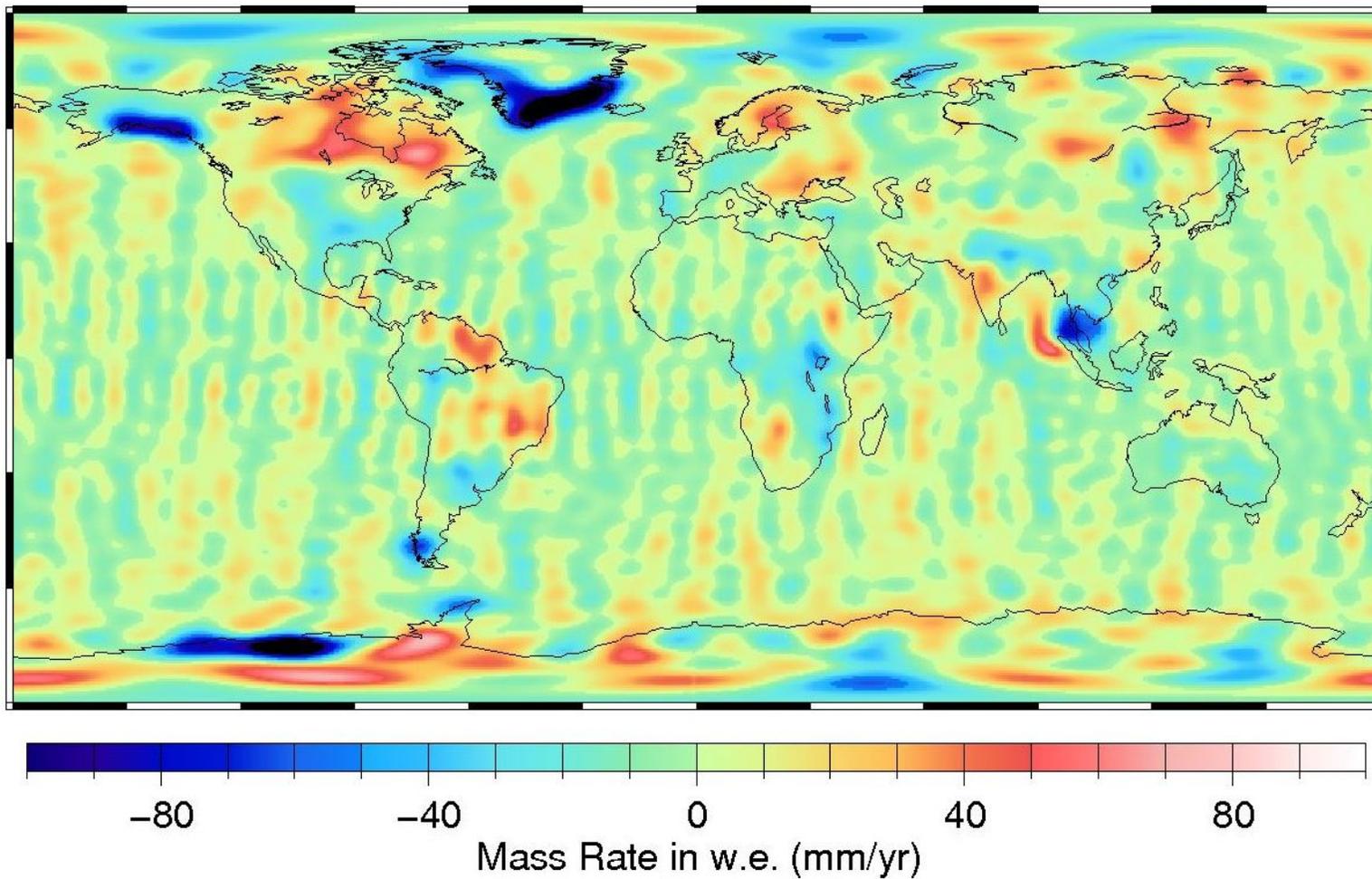
9-month



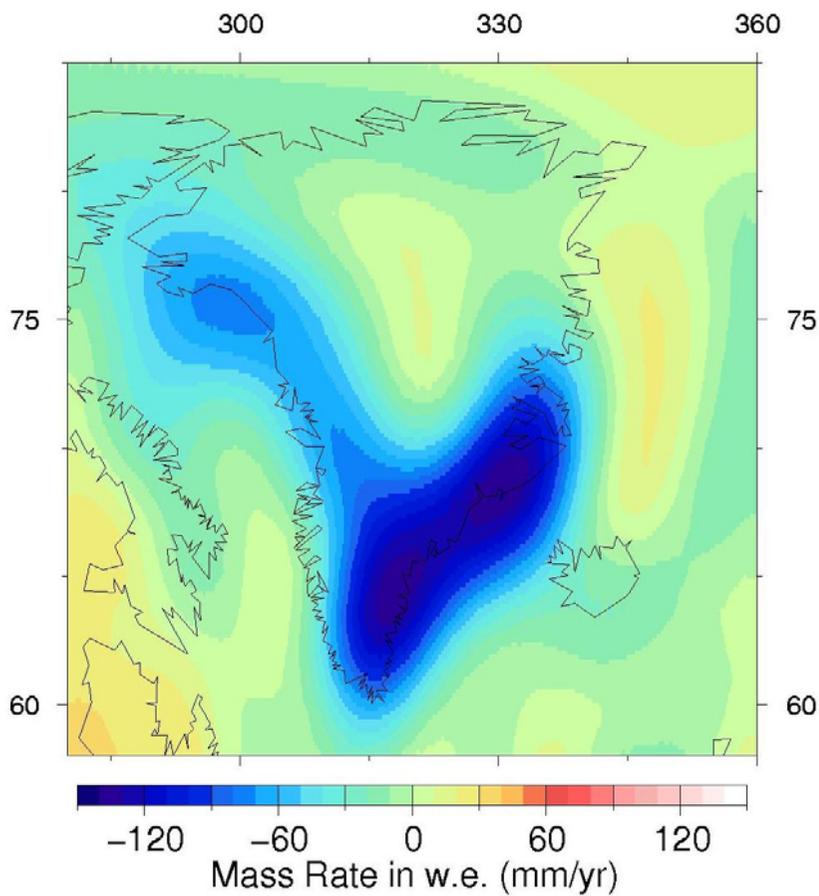
7.2-month



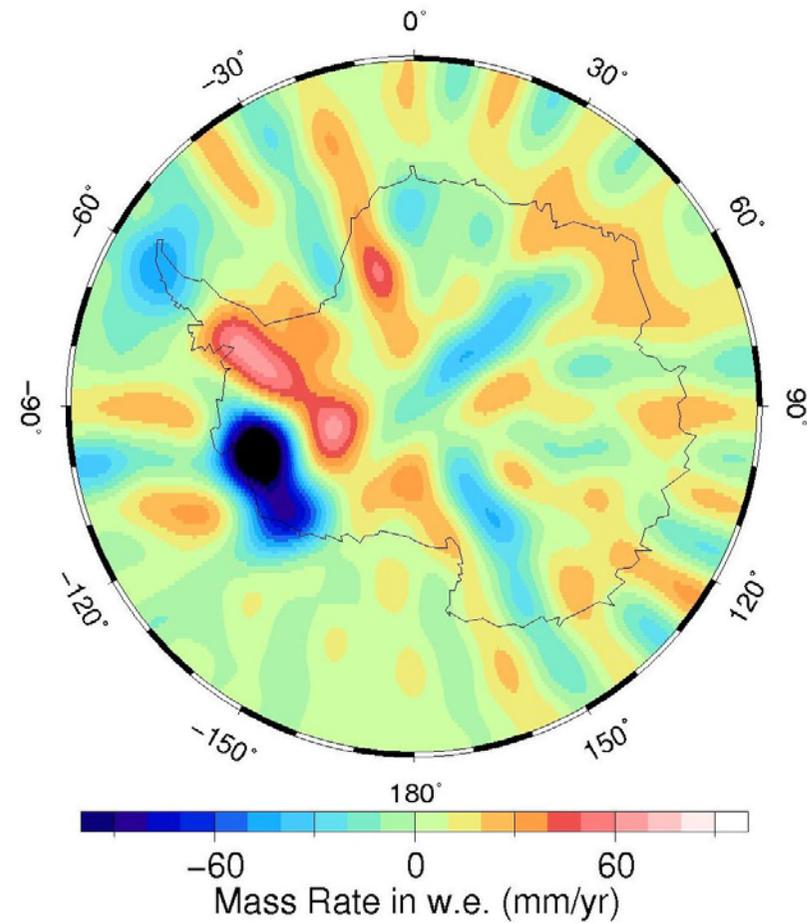
The Map of Mass Variation Trend - Filtered



Details: Greenland and Antarctica

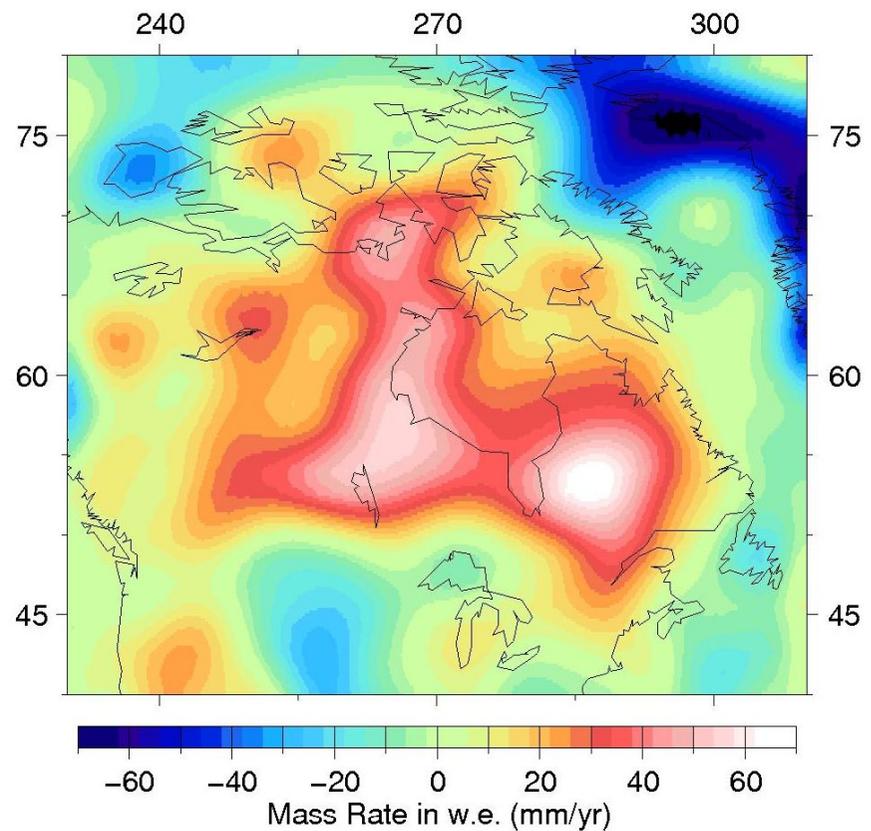
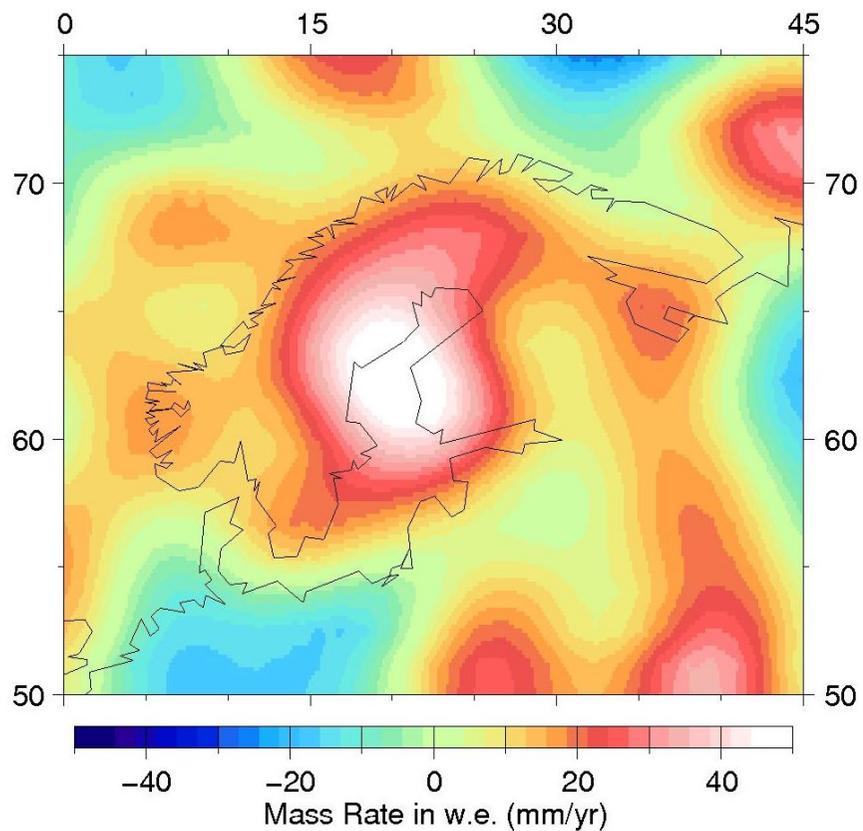


Water Equivalent in mm/yr

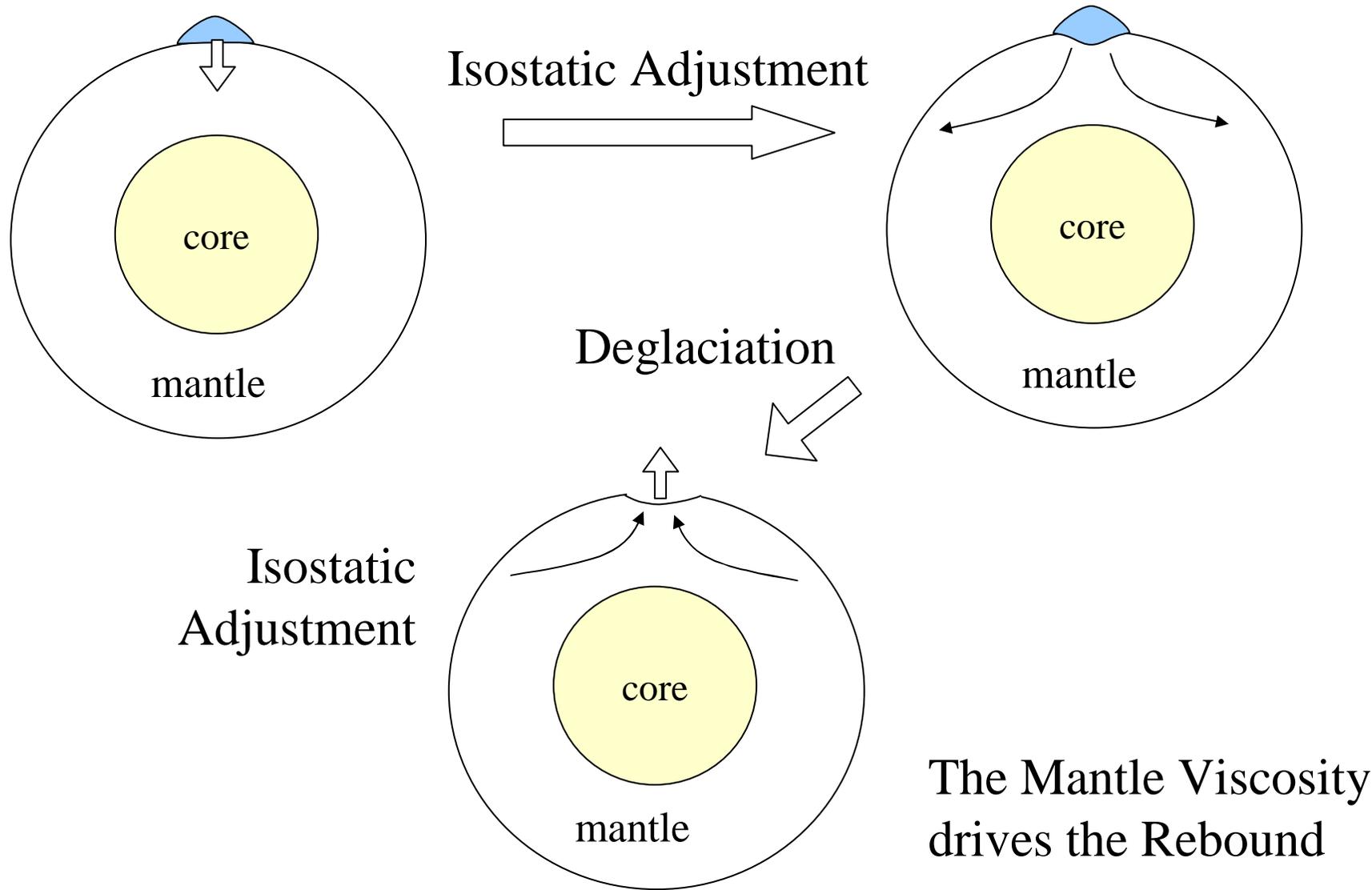


Water Equivalent in mm/yr

Details: Fennoscandia and Hudson Bay



The Post Glacial Rebound

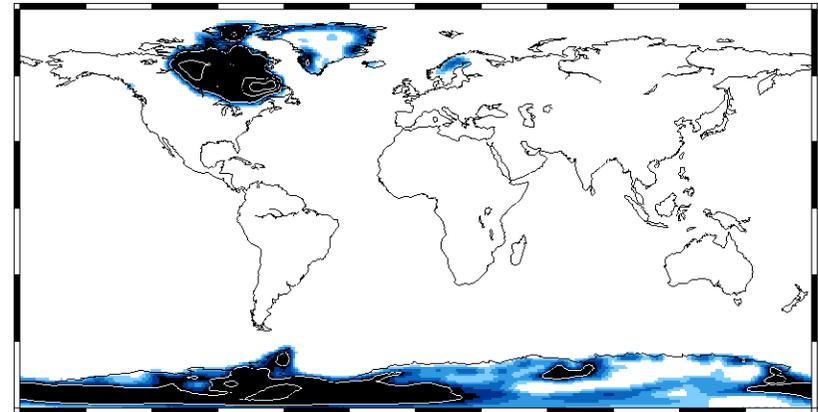
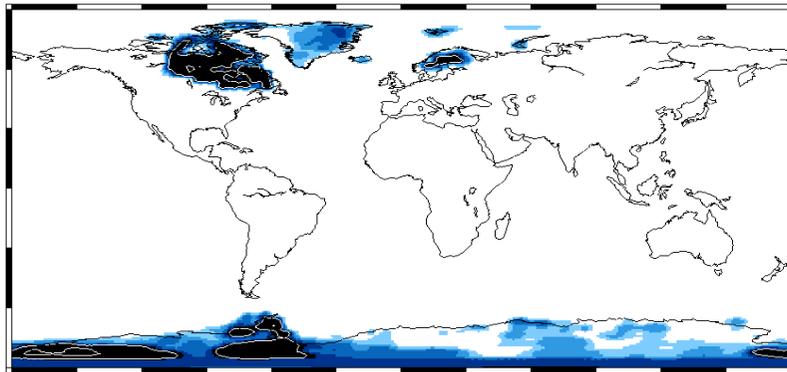


Pleistocene Deglaciation Model

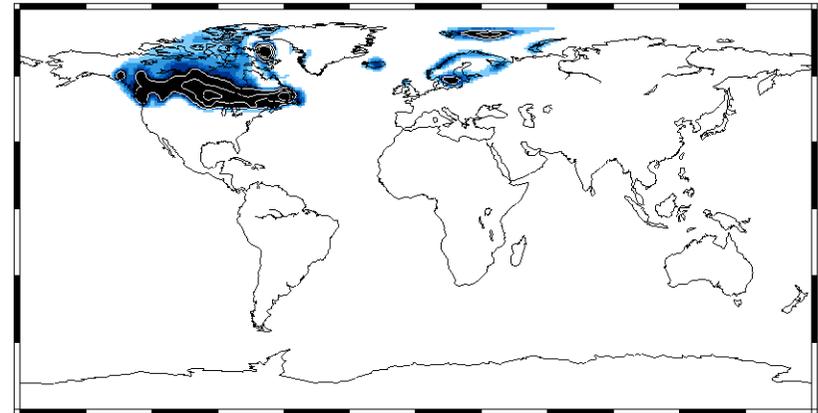
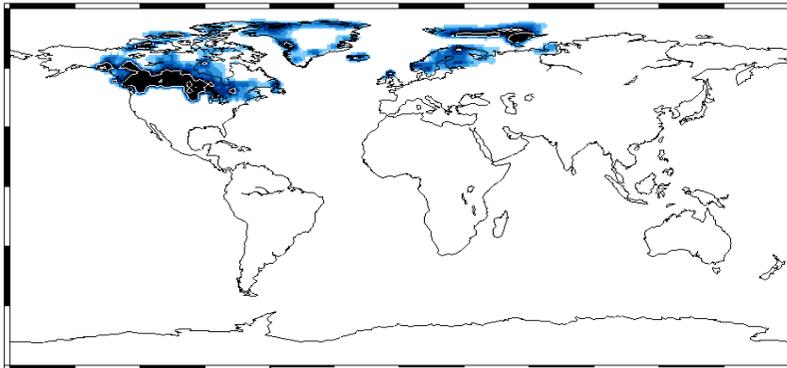
ICE-3G

Lambeck (ANU)

9 kyr BP



14 kyr BP



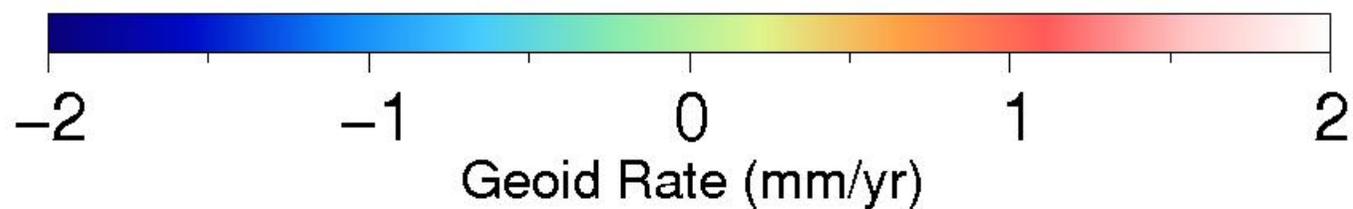
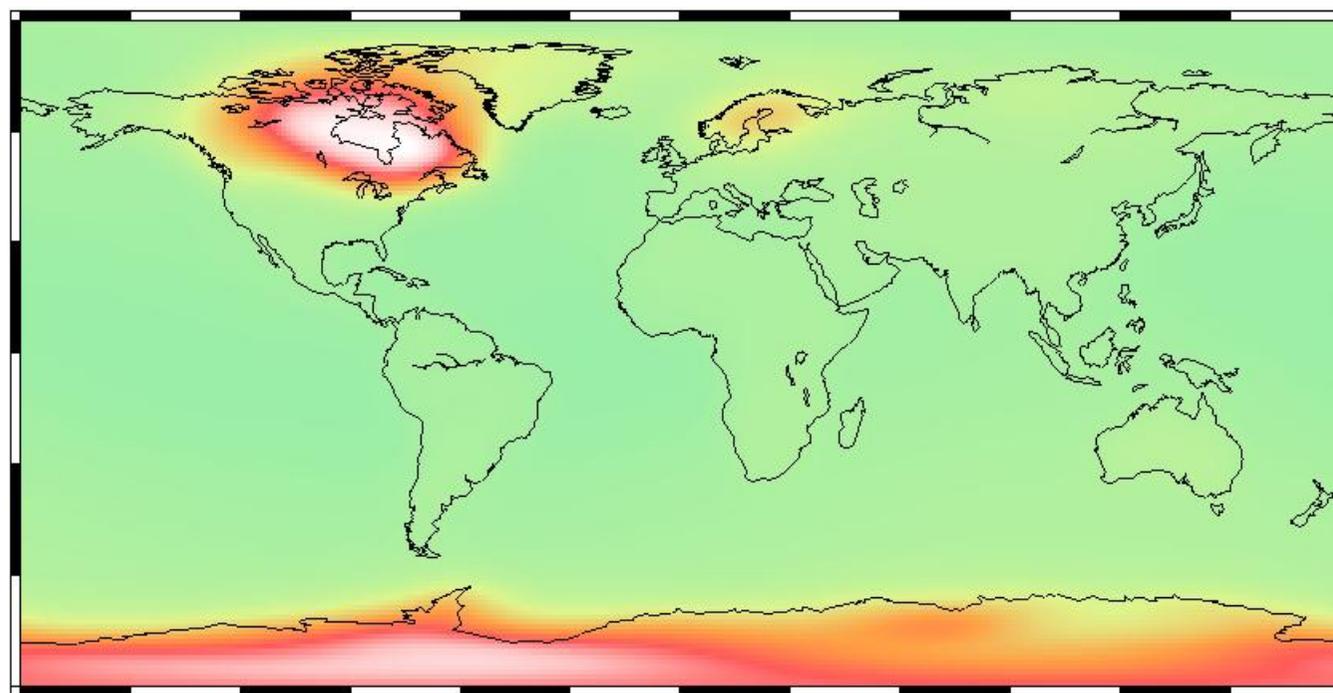
0 100 200 300

Ice (m/kyr)

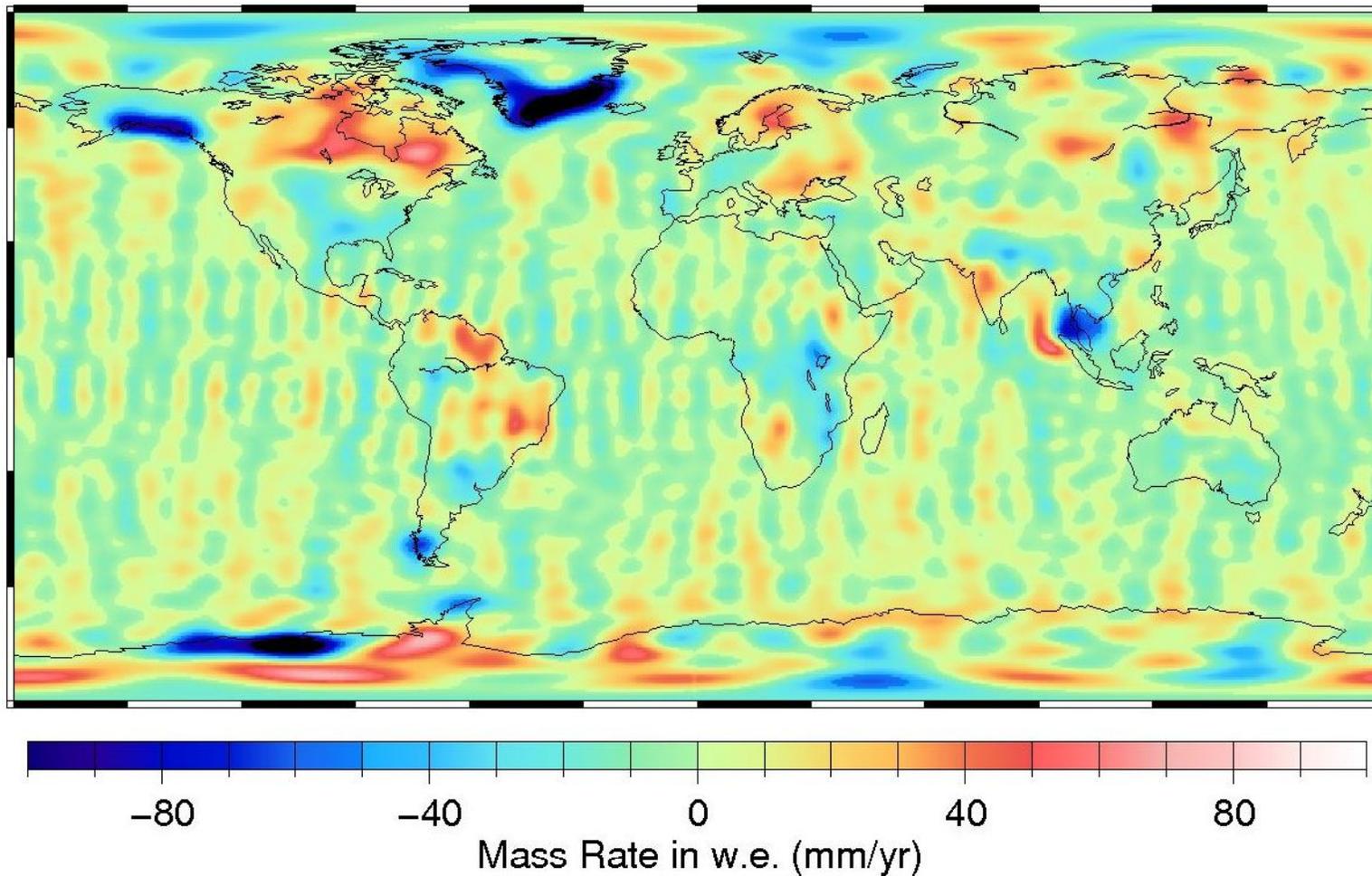
The Post Glacial Rebound: *Geoid Rate*

Lambeck (ANU)

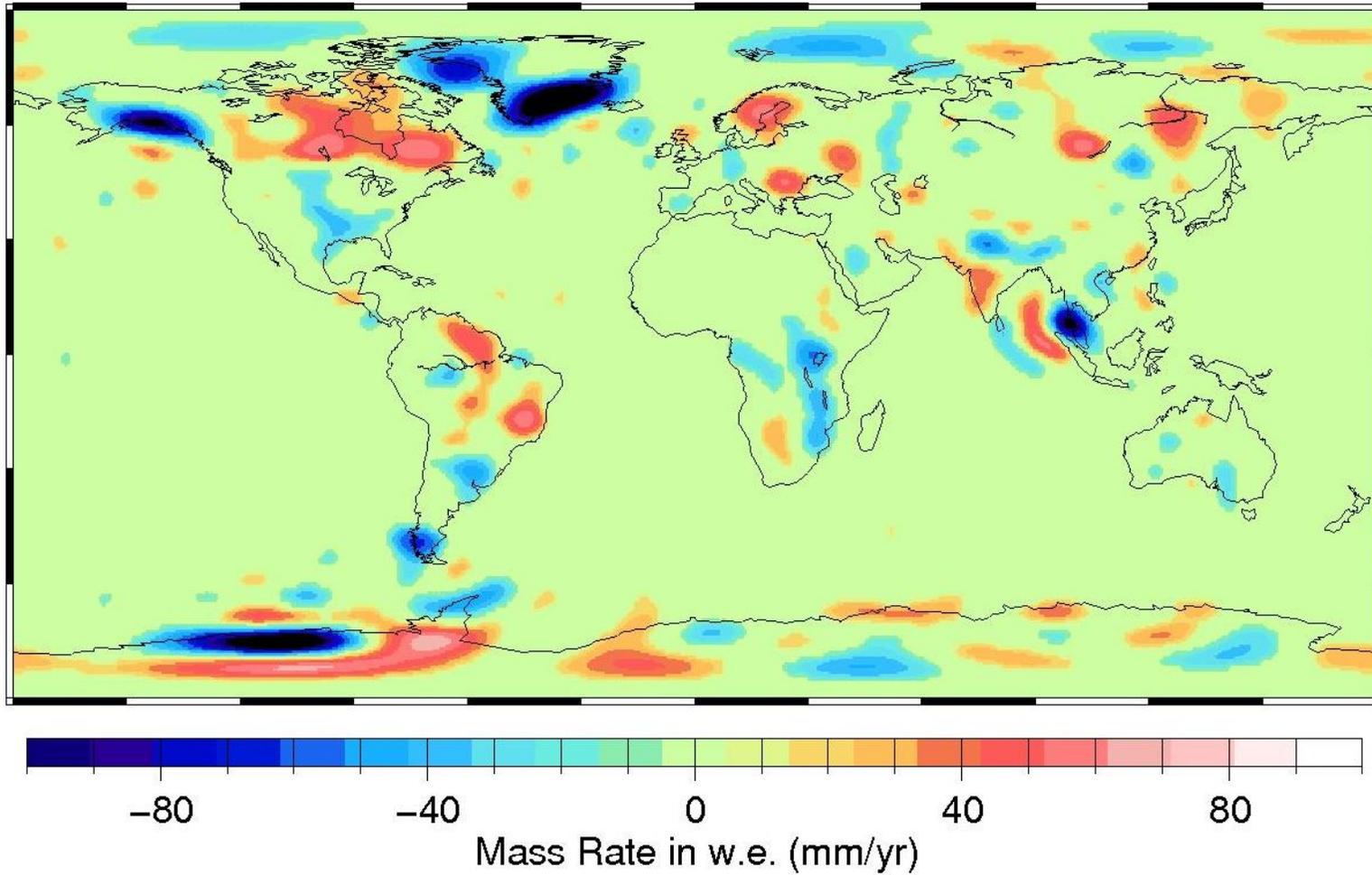
$$\nu_{UP} = 5 \times 10^{20} \text{ Pa s} \quad \nu_{LW} = 2.5 \times 10^{21} \text{ Pa s}$$



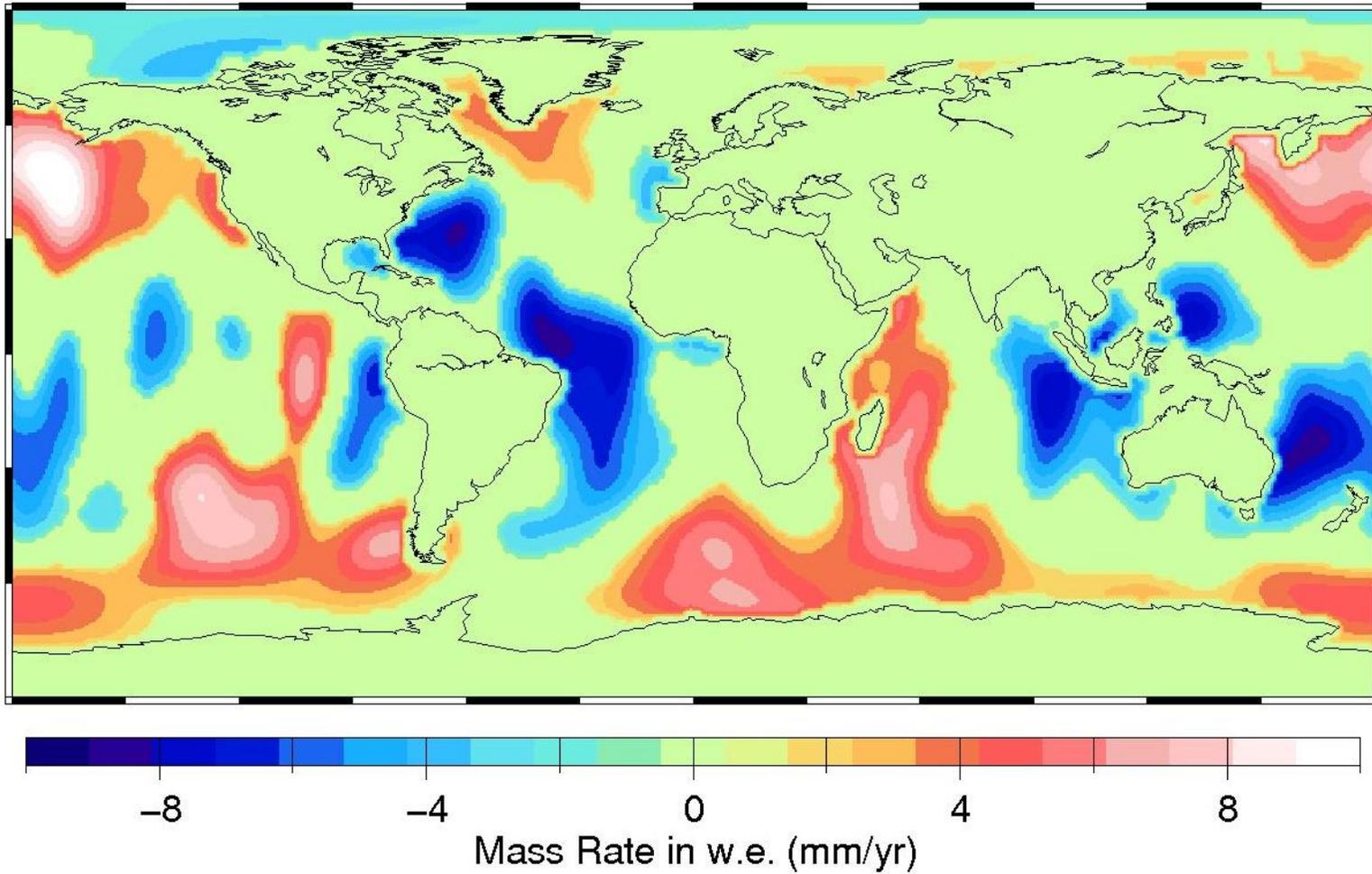
The Map of Mass Variation Trend - Filtered



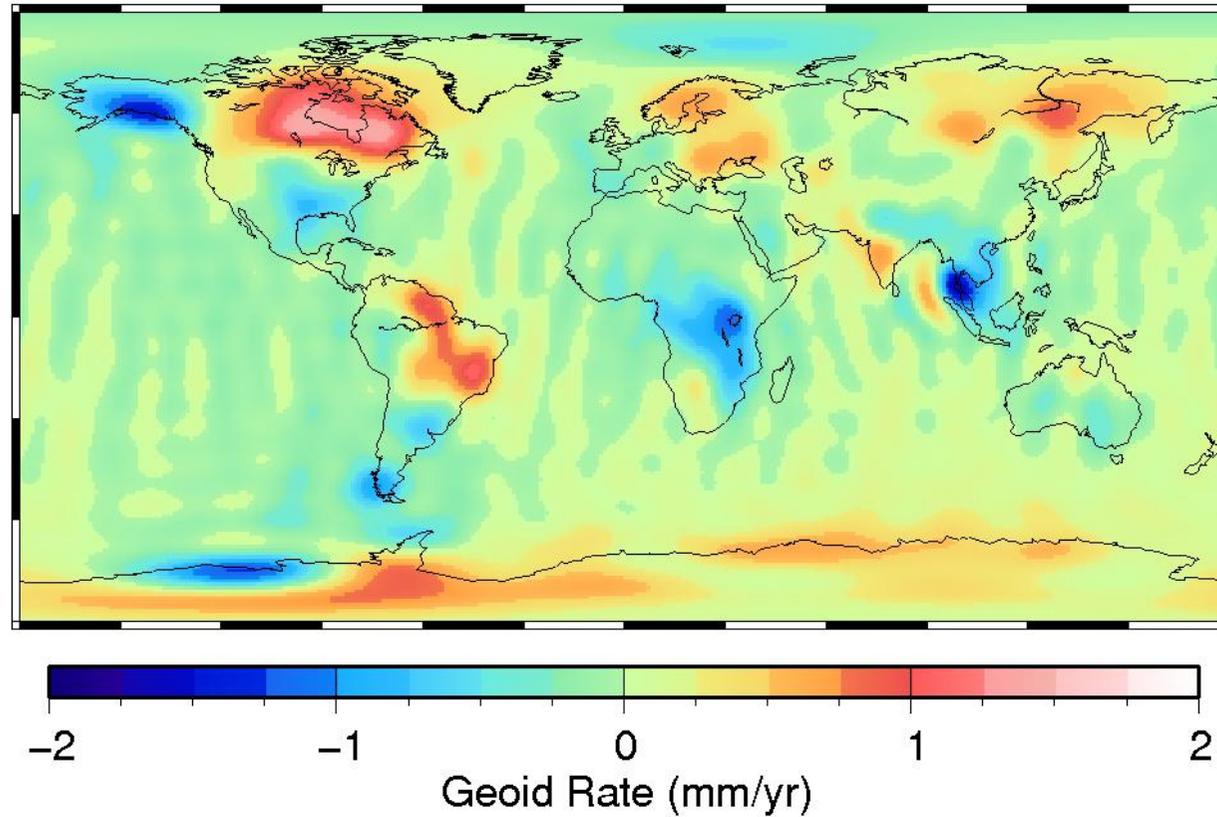
Mass Distribution



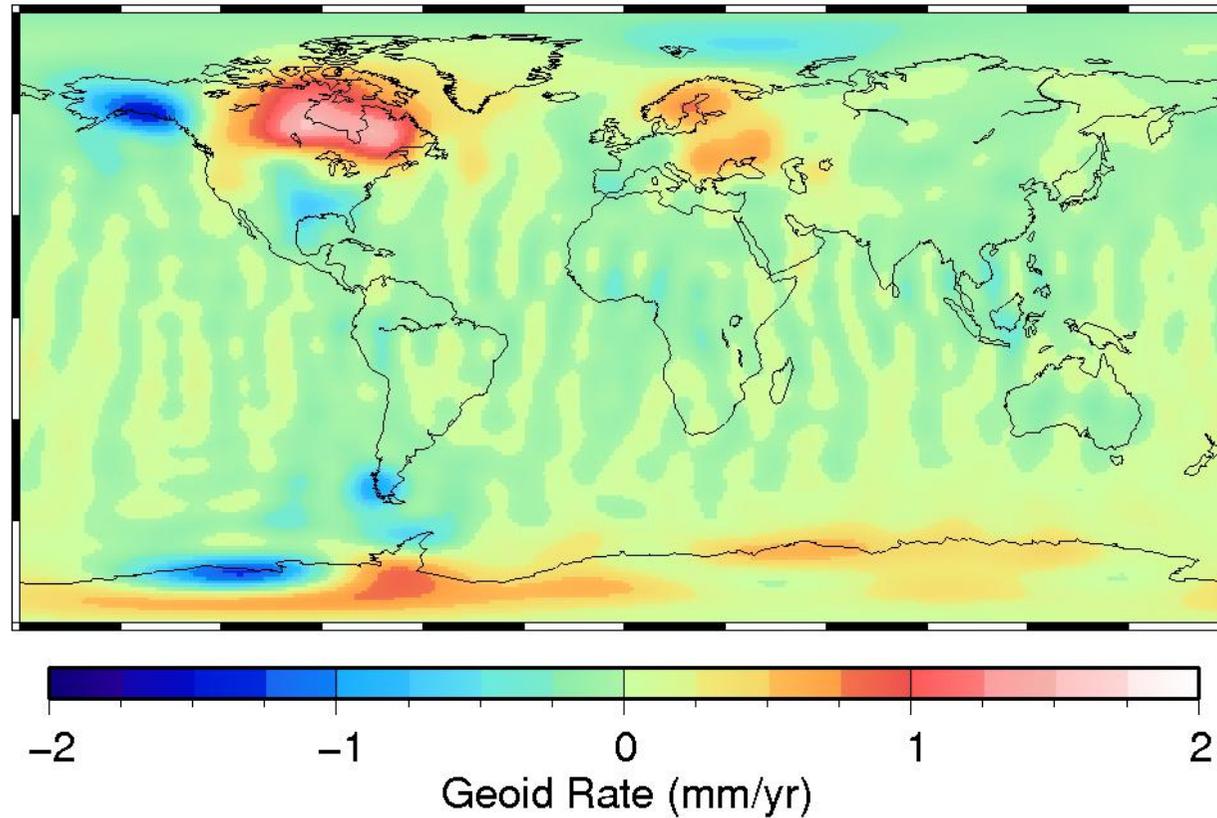
Mass Distribution over Oceans



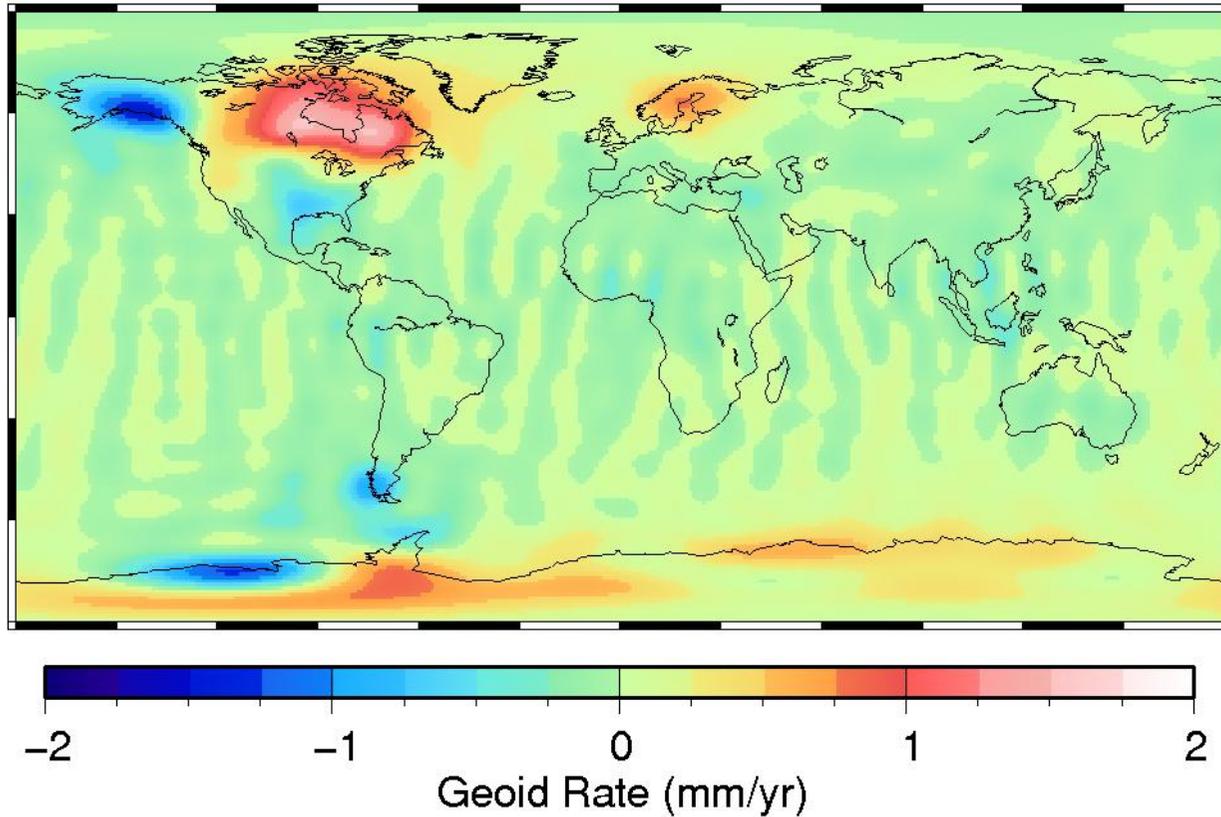
GRACE up 30 - Sea *Removed*



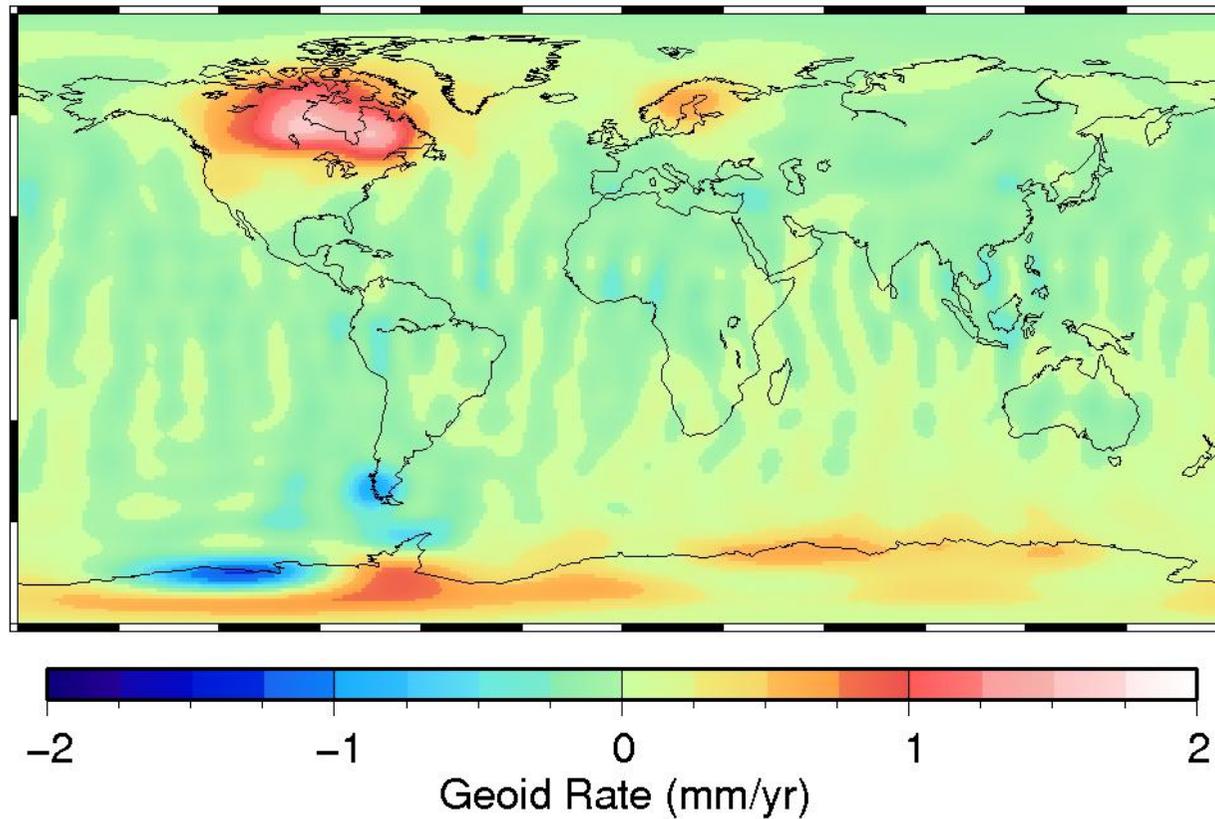
GRACE up 30 - Far from PGR *Removed*



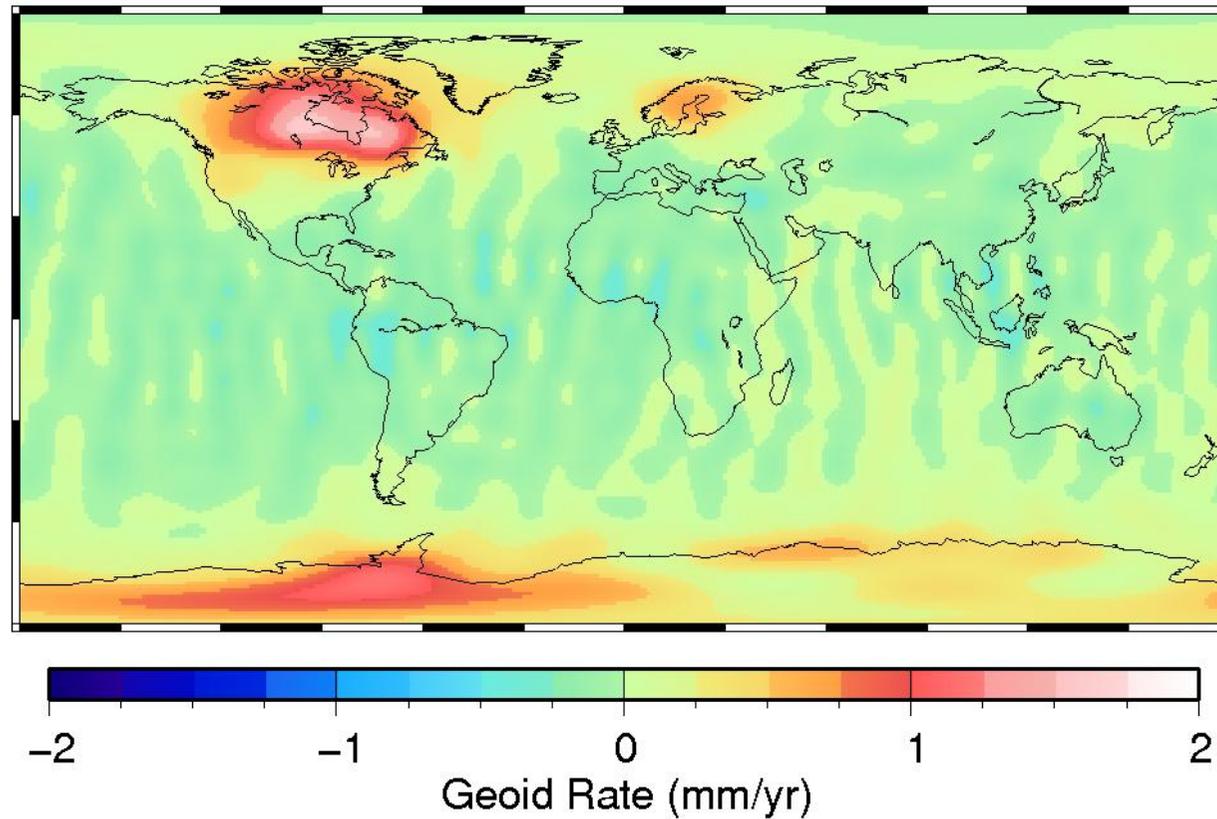
GRACE up 30 - Nearby Fennoscandia *Removed*



GRACE up 30 - Nearby Hudson Bay *Removed*

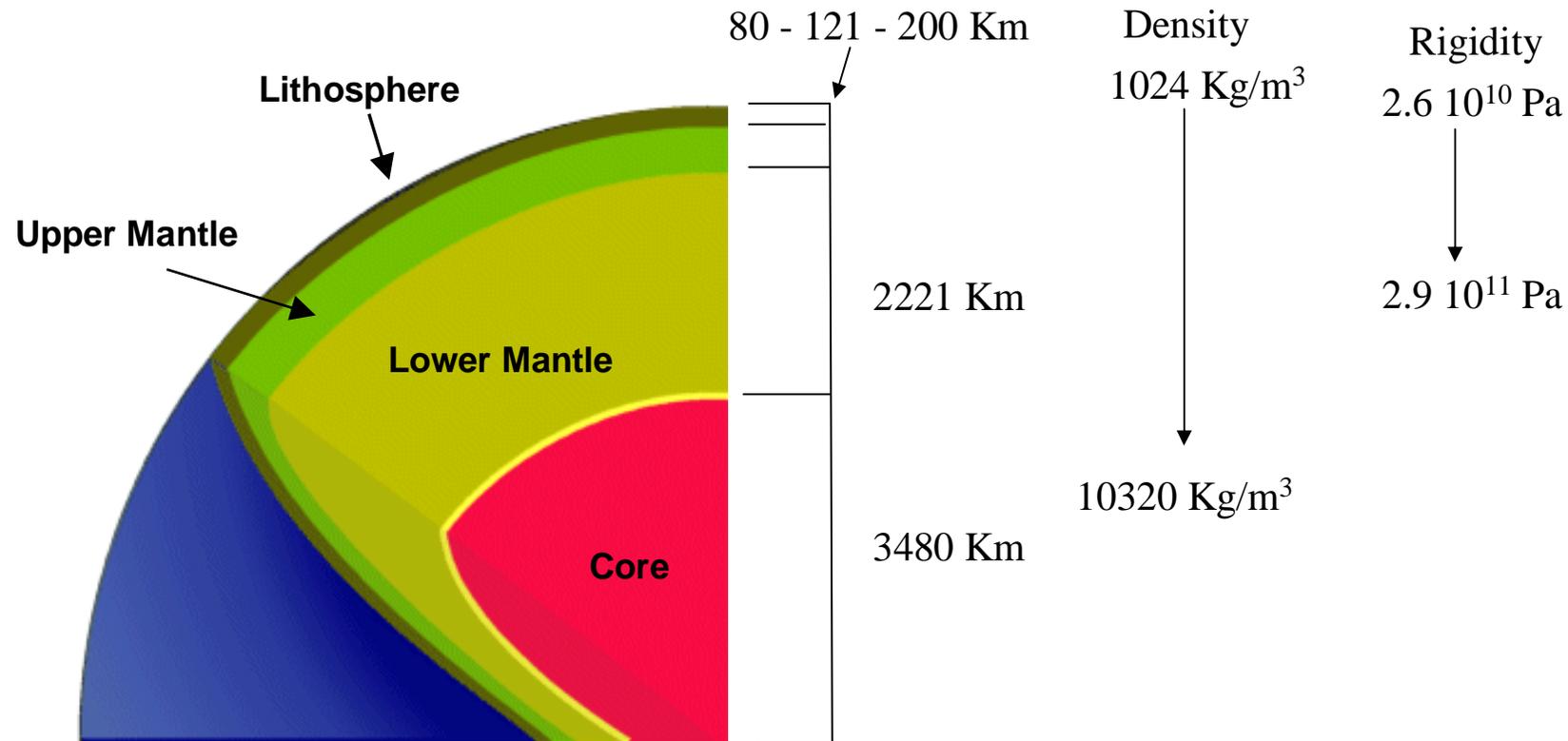


GRACE up 30 - West Antarctica *Removed*



The Earth Model

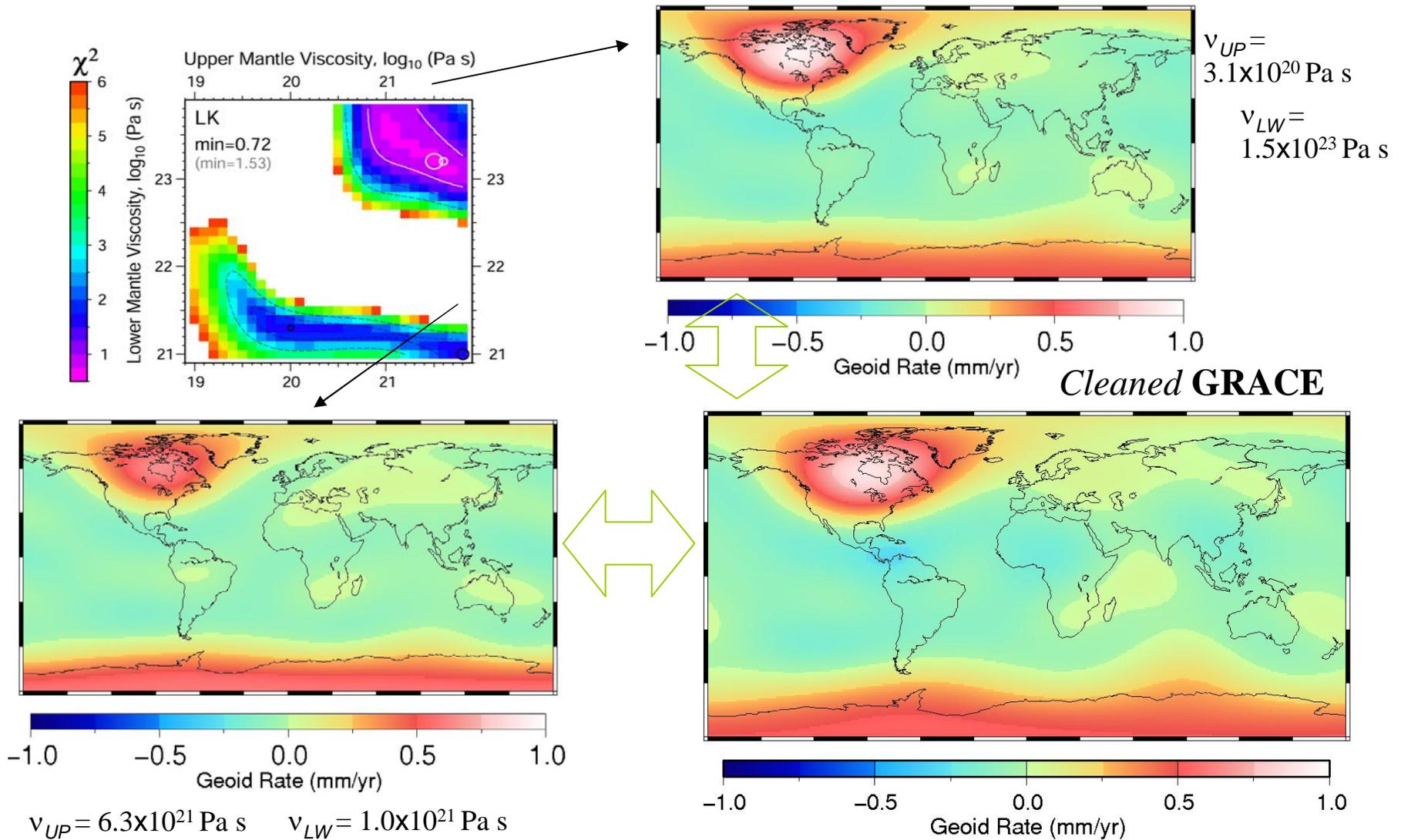
Incompressible, Viscoelastic Maxwell Rheology



Upper Mantle Viscosity $\nu_{UP} = 10^{19}-6 \times 10^{21}$ Pa s

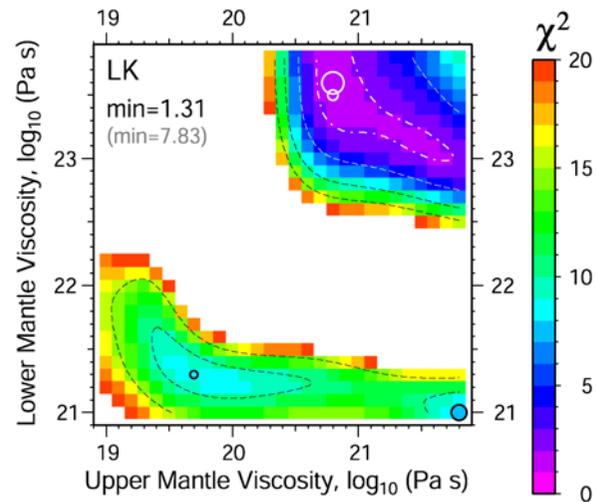
Lower Mantle Viscosity $\nu_{LW} = 10^{21}-6 \times 10^{23}$ Pa s

Global Problem - Search for best viscosity

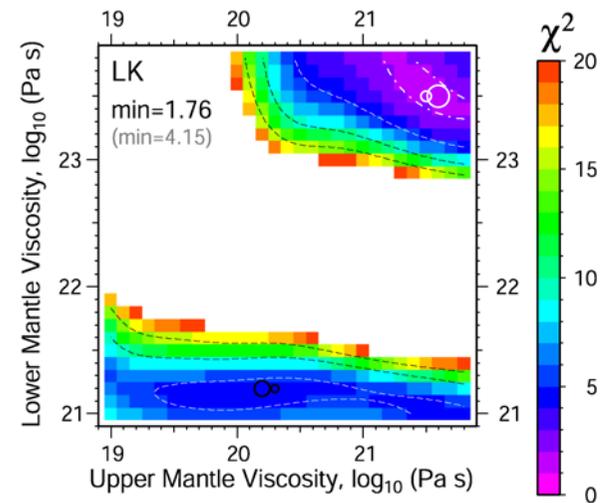


Global Problem - Search for Zonals j best viscosity

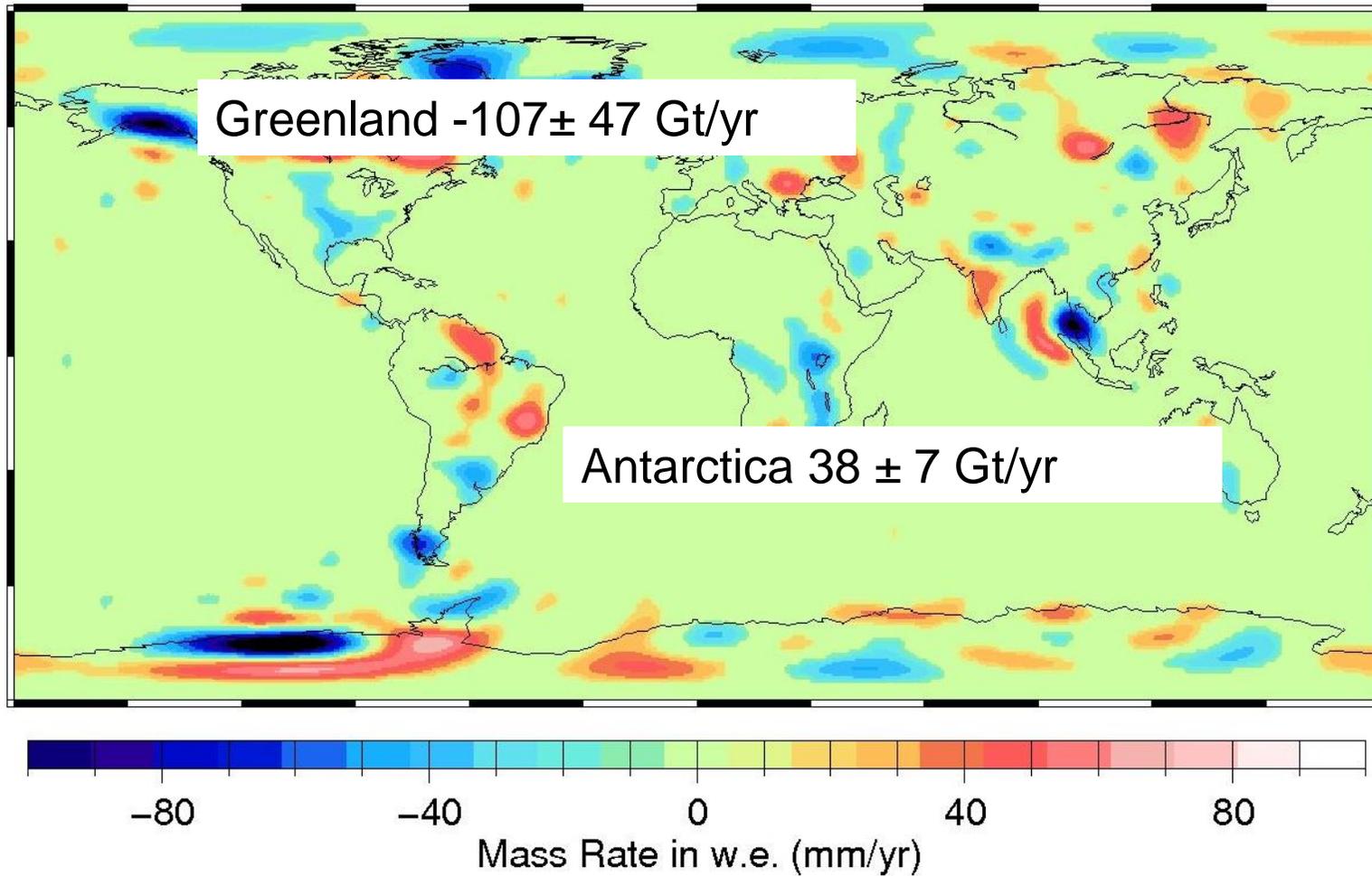
GRACE



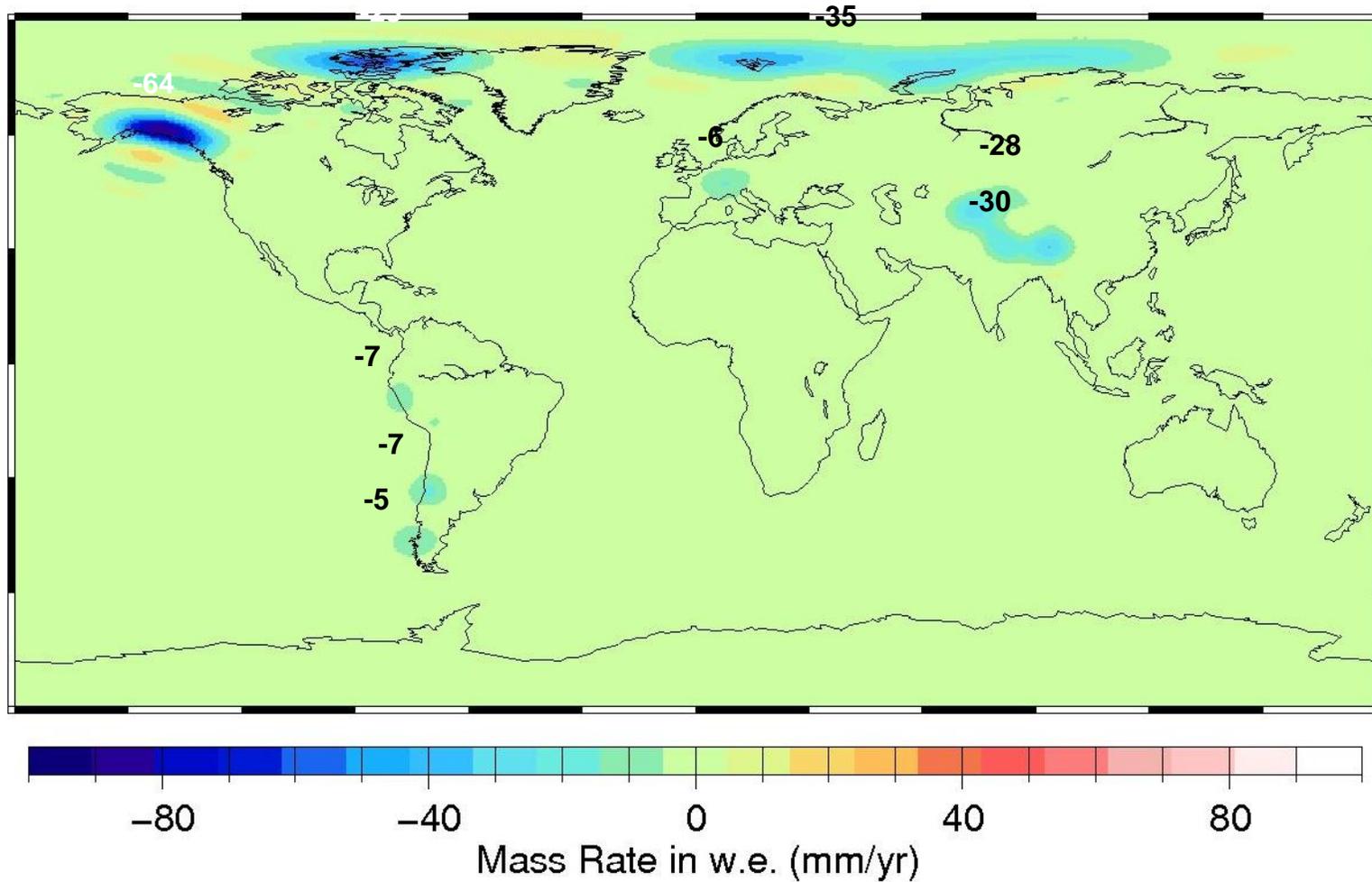
SLR



Polar Region Mass Balance from GRACE



Worldwide Glacier Shrinkage





UNIVERSITA' DEGLI STUDI DI MILANO

Dep. of Earth Sciences - Sec. Geophysics

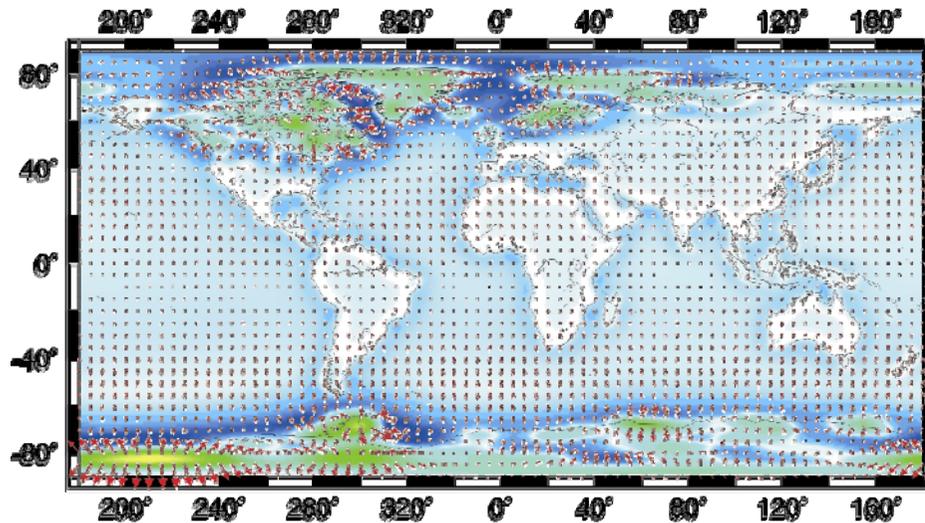
Lithosphere=80 Km

MOD 21

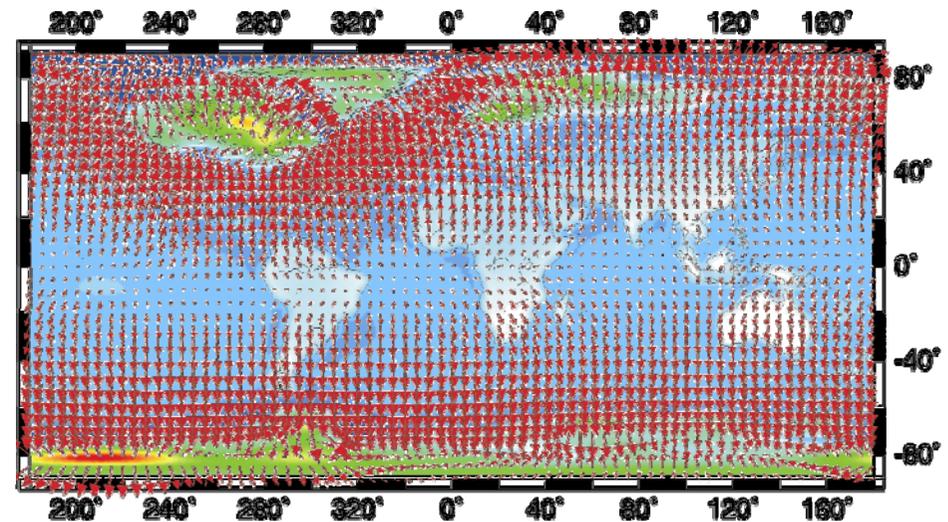
$$v_{UM}=0.5 \times 10^{21} \text{ Pa s} \quad v_{LM}=1.0 \times 10^{21} \text{ Pa s}$$

MOD 26

$$v_{UM}=0.5 \times 10^{21} \text{ Pa s} \quad v_{LM}=1.0 \times 10^{22} \text{ Pa s}$$



Radial velocity cm/yr



Tangential Velocity \rightarrow 0.3 cm/yr



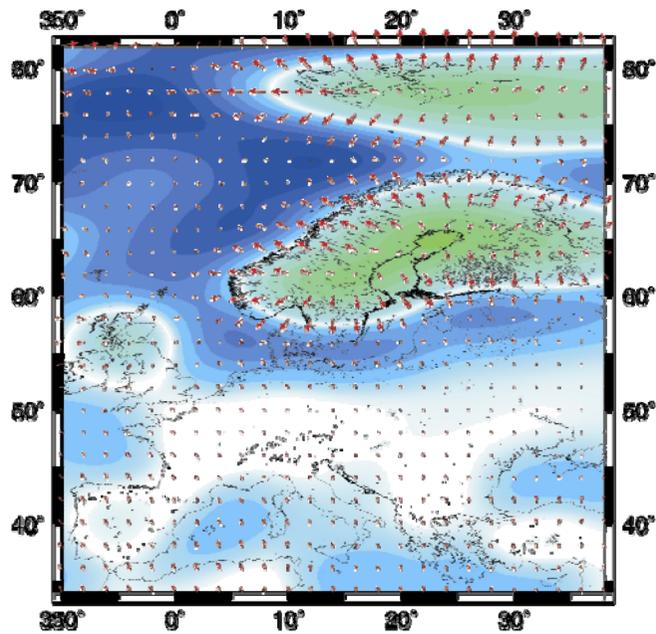
UNIVERSITA' DEGLI STUDI DI MILANO

Dep. of Earth Sciences - Sec. Geophysics

Lithosphere=80 Km

MOD 21

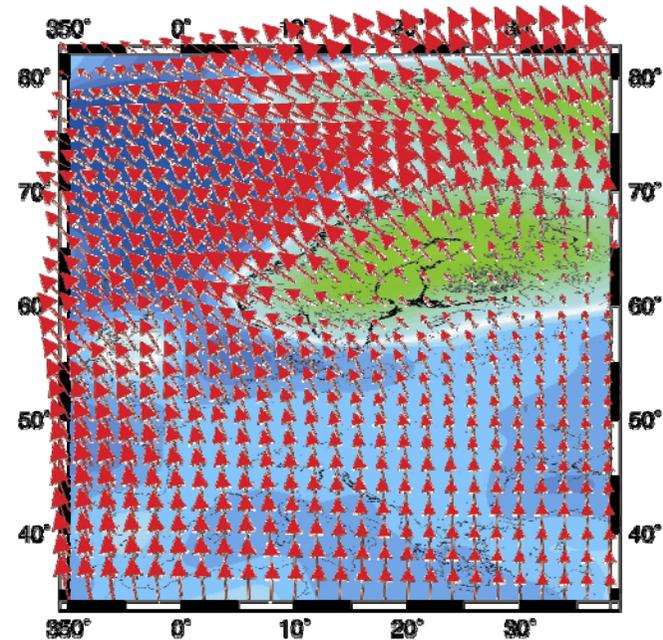
$$v_{UM}=0.5 \times 10^{21} \text{ Pa s} \quad v_{LM}=1.0 \times 10^{21} \text{ Pa s}$$



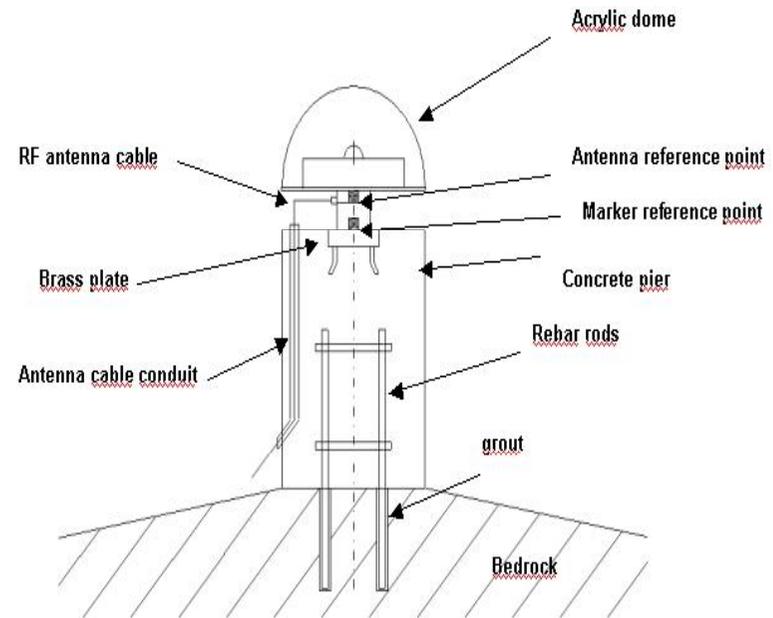
-0.8 -0.4 0.0 1.0 2.0
Radial velocity cm/yr

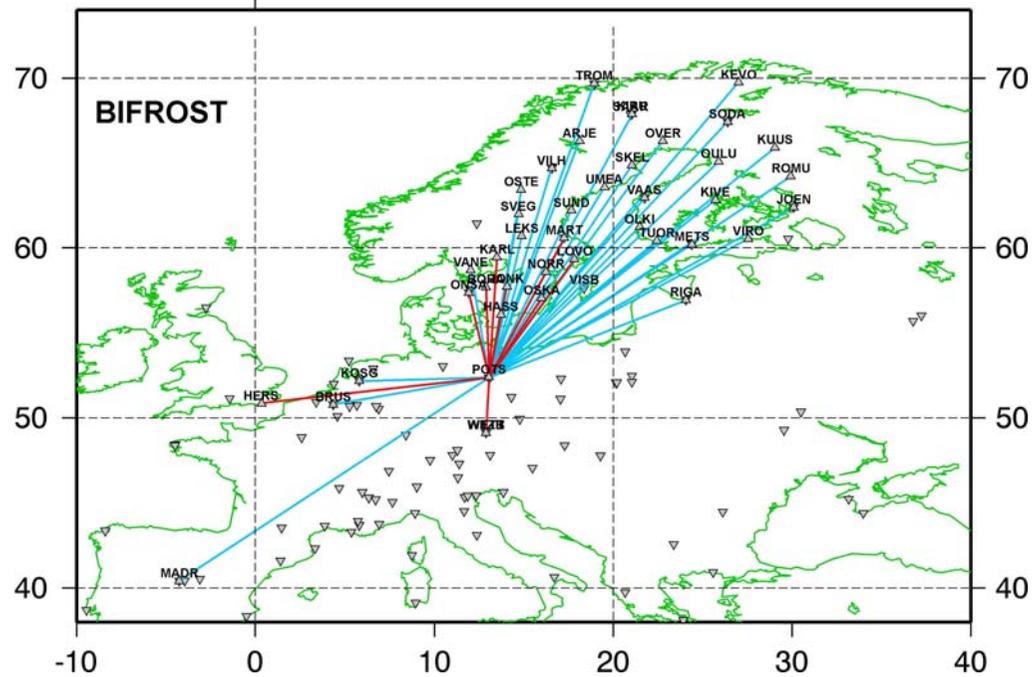
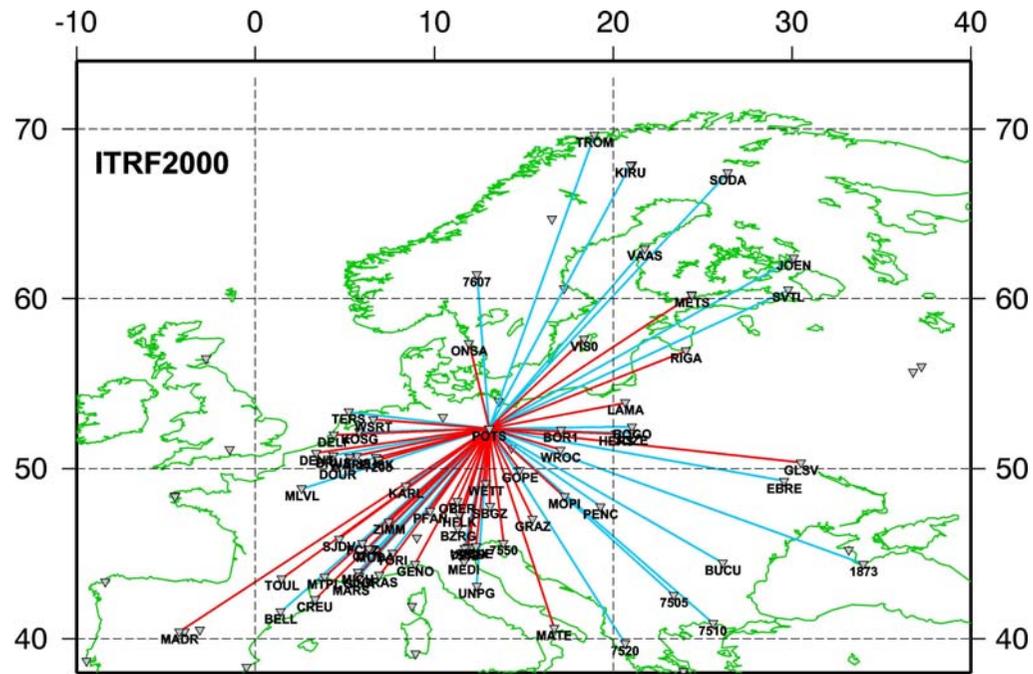
MOD 26

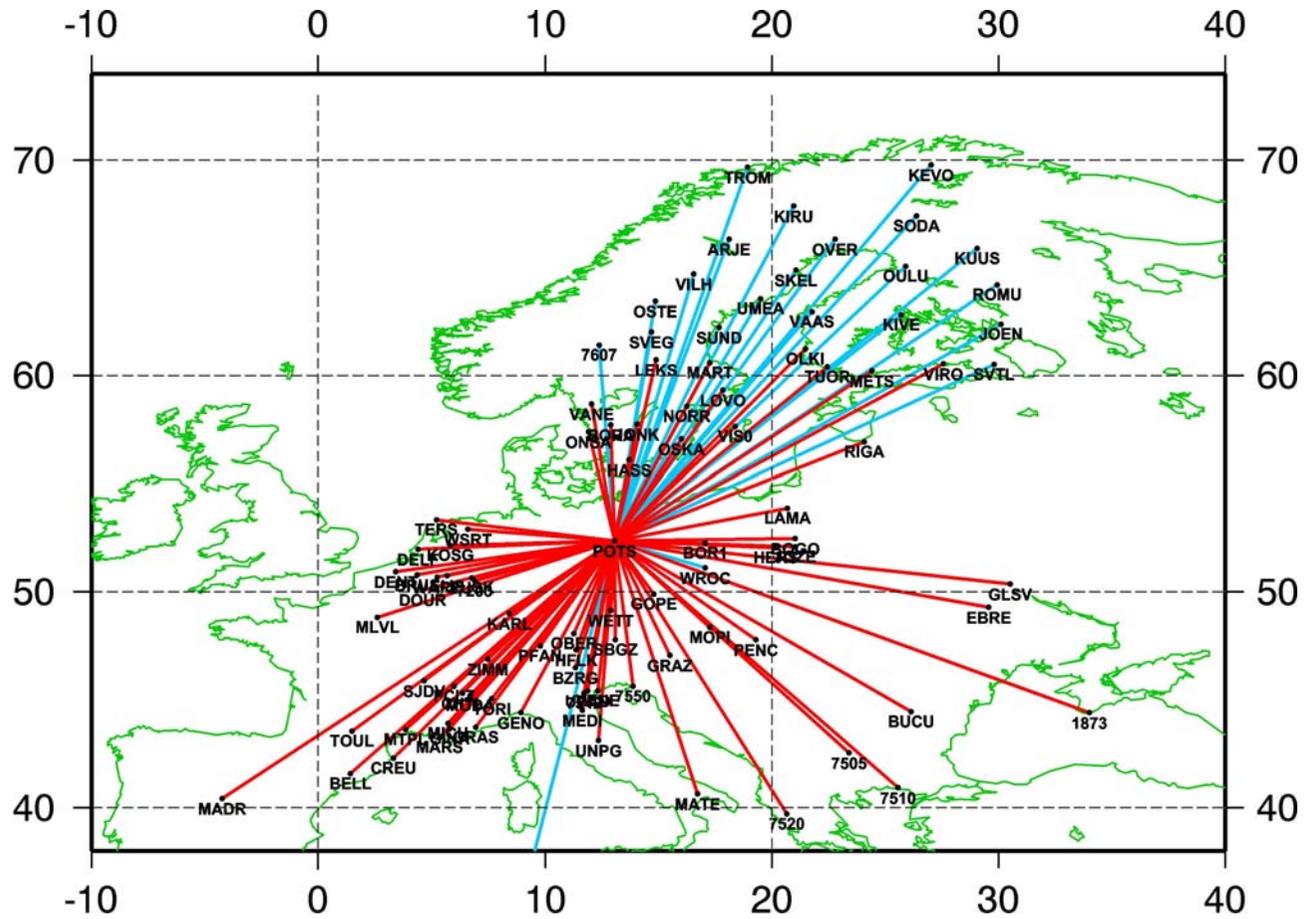
$$v_{UM}=0.5 \times 10^{21} \text{ Pa s} \quad v_{LM}=1.0 \times 10^{22} \text{ Pa s}$$

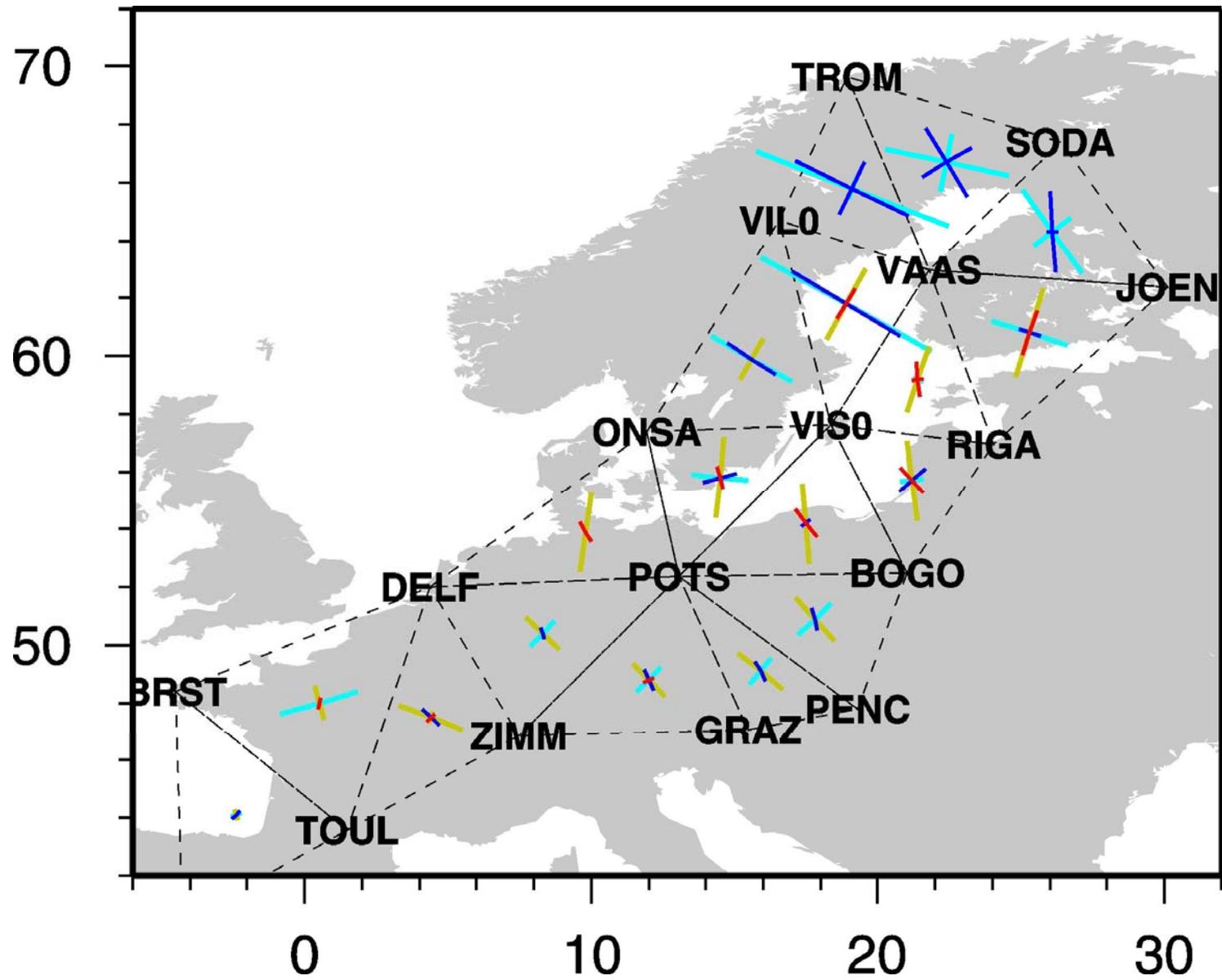


Tangential Velocity → 0.3 cm/yr







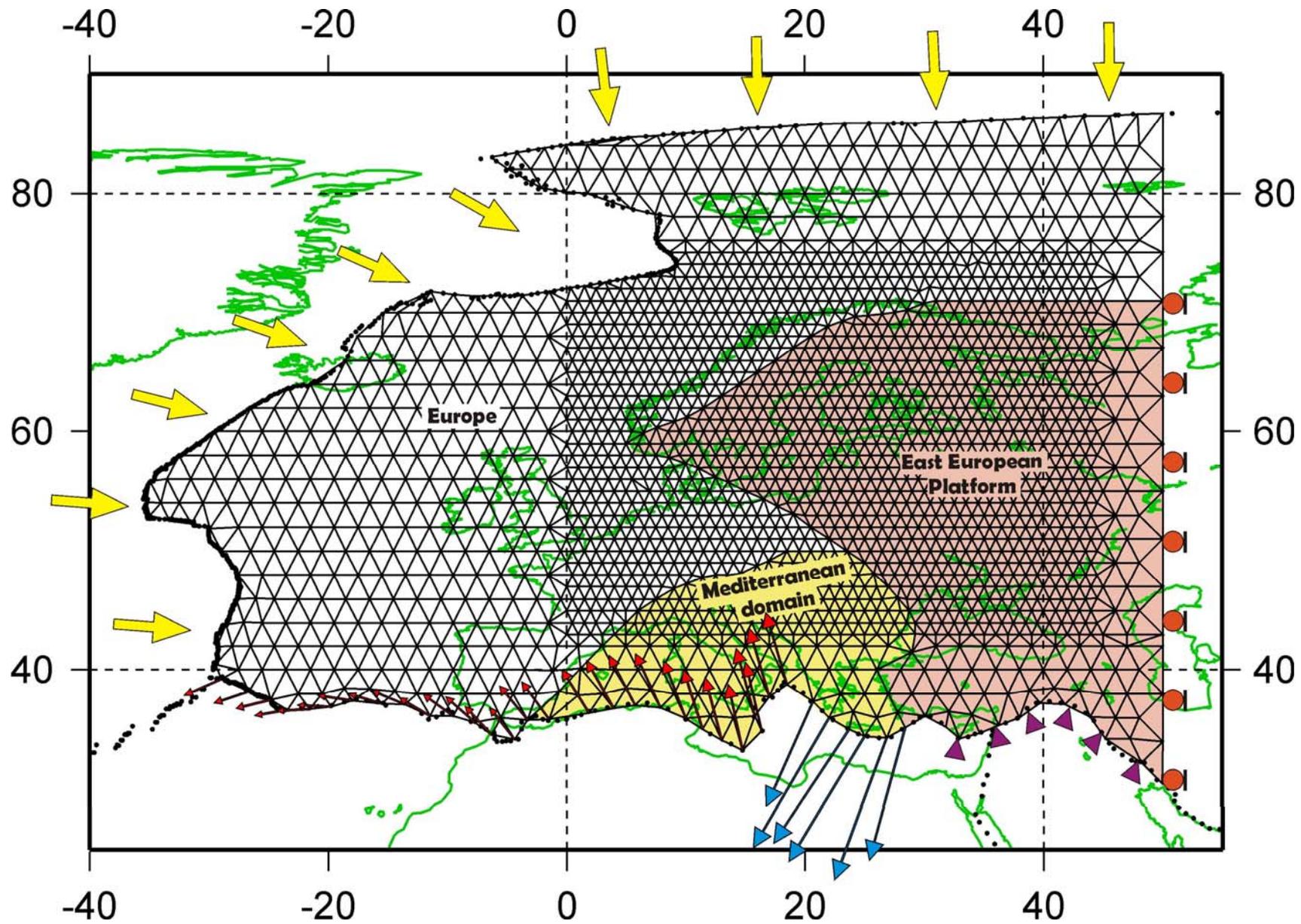


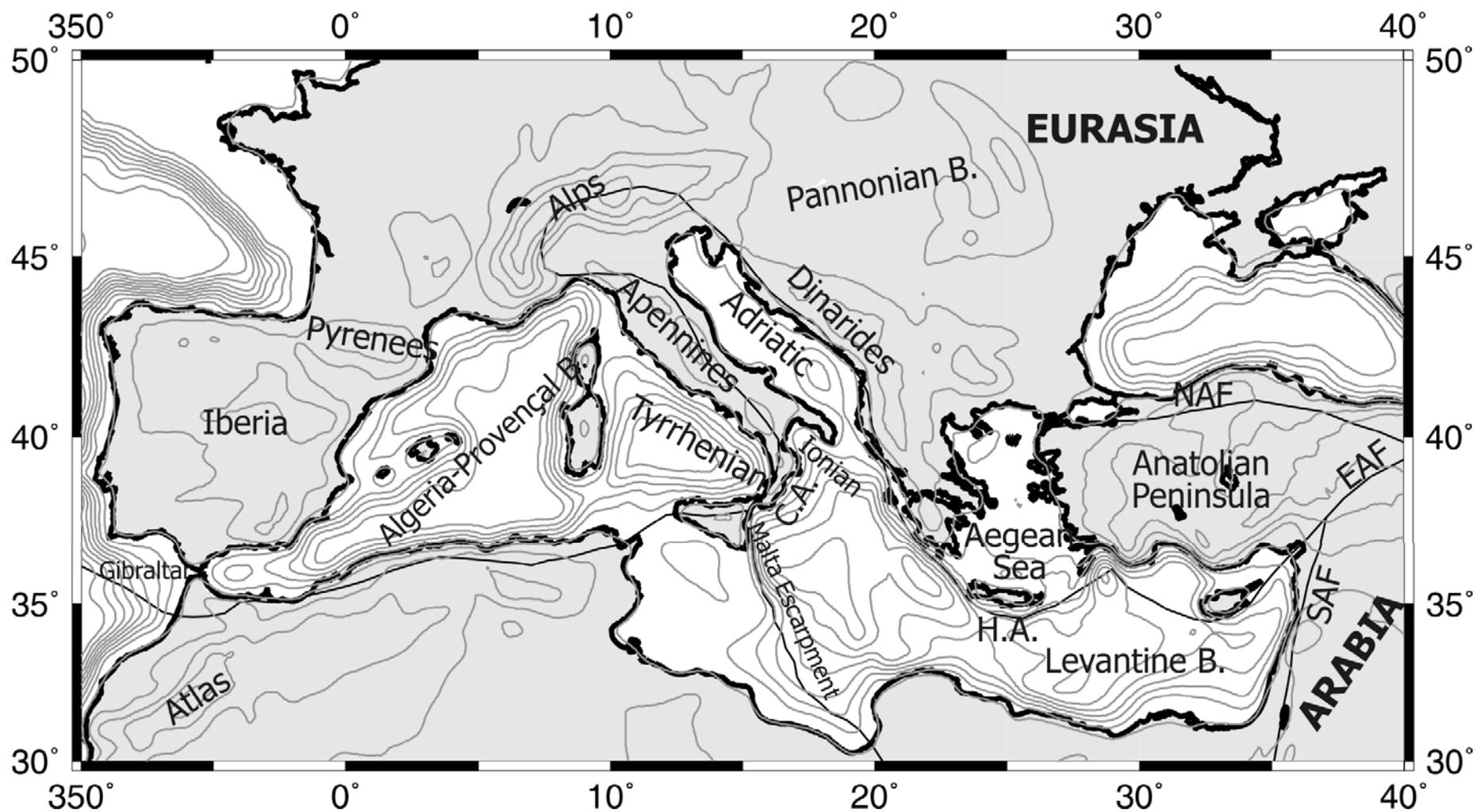


**Geophysical modelling and GPS, SAR, GRACE and GOCE
data for the understanding of lithospheric
and mantle processes - 2**

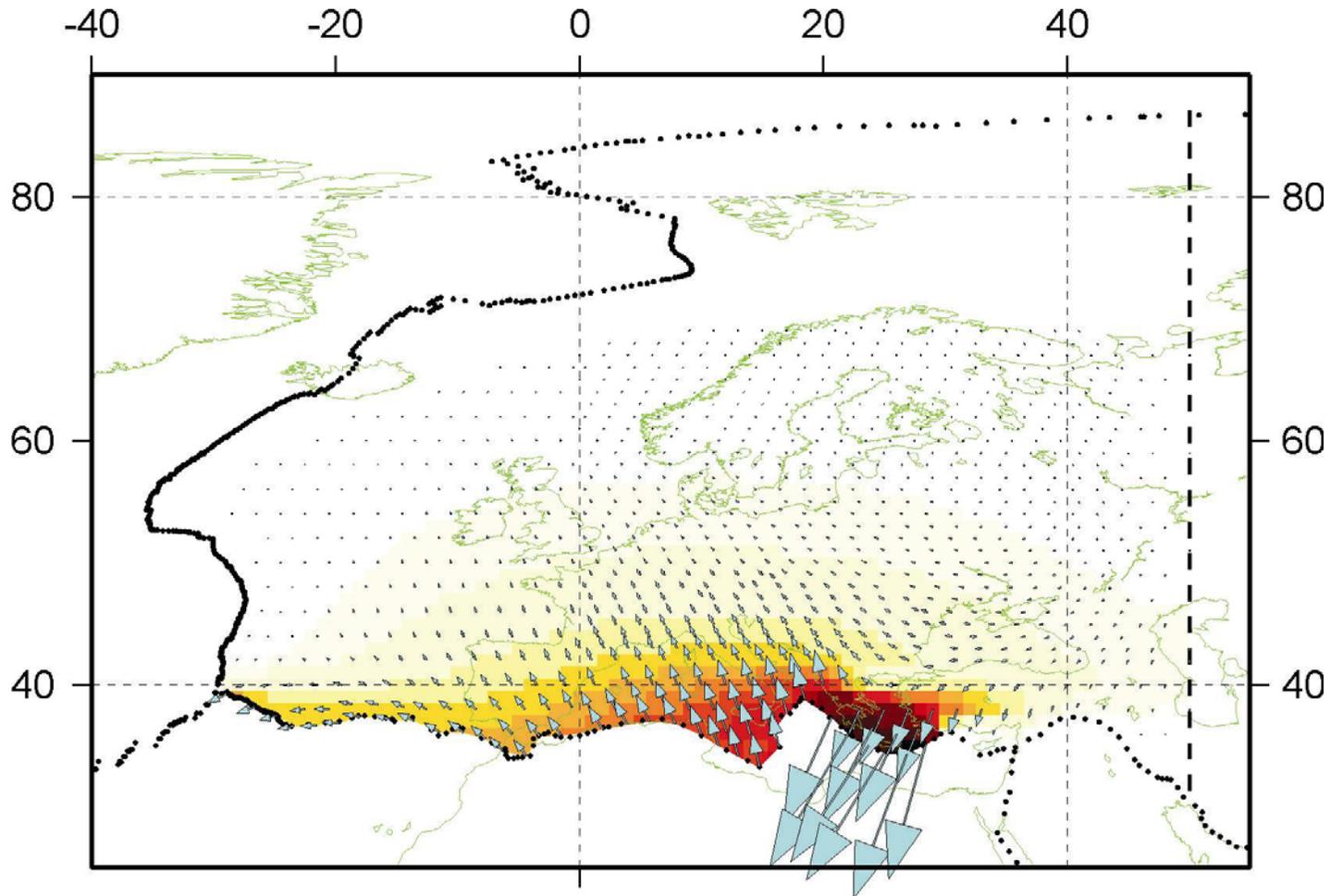
Roberto Sabadini

Dipartimento di Scienze della Terra "A. Desio"
Università di Milano

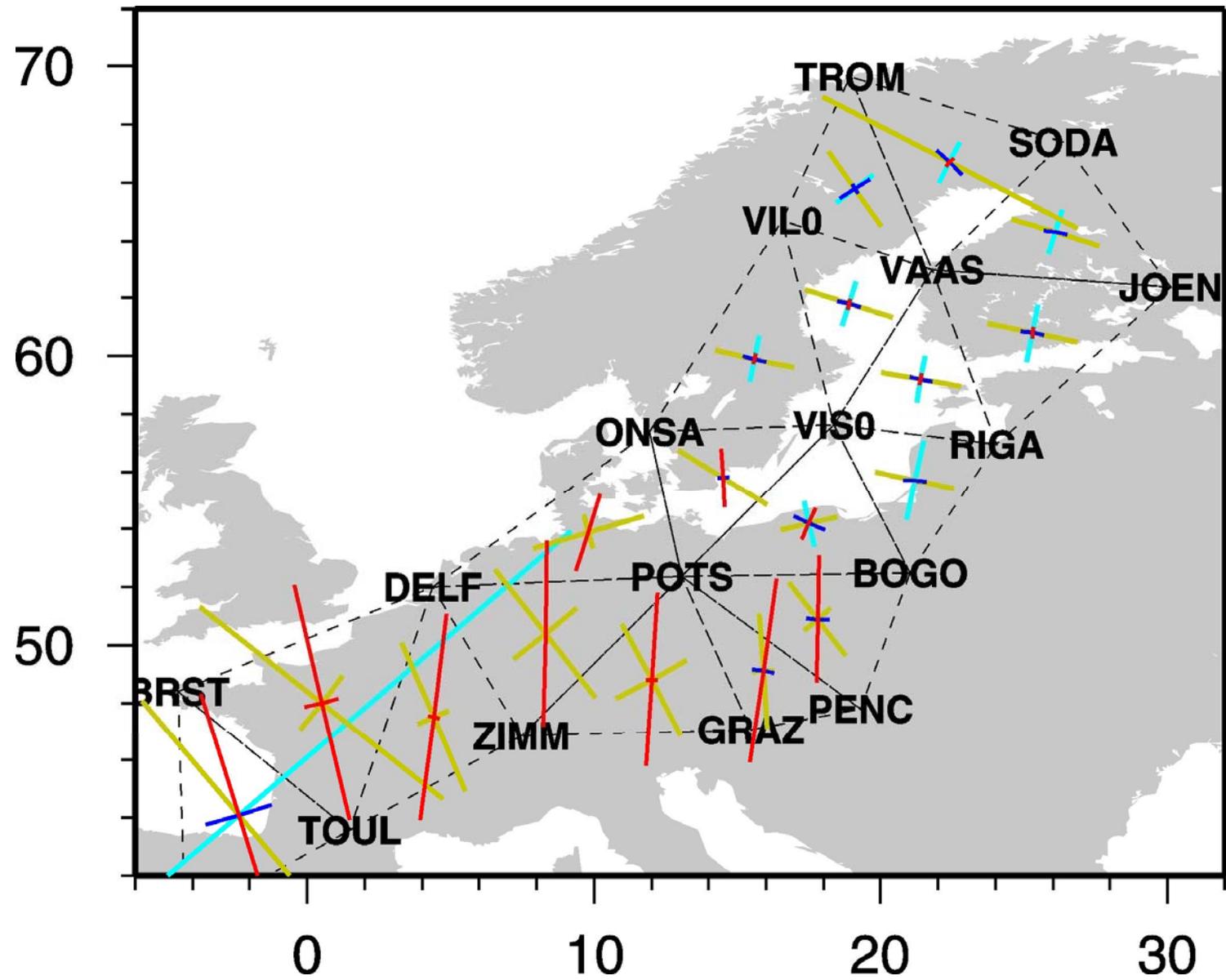


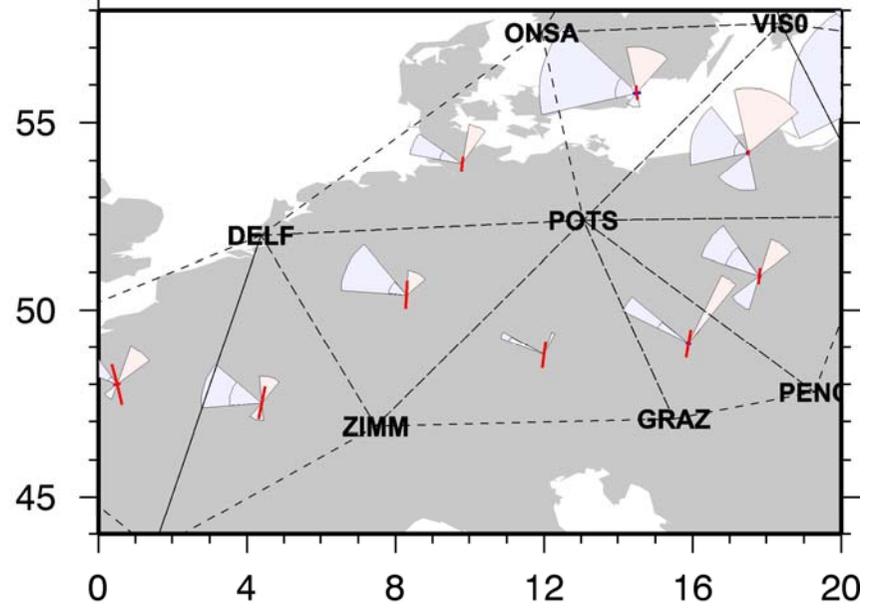
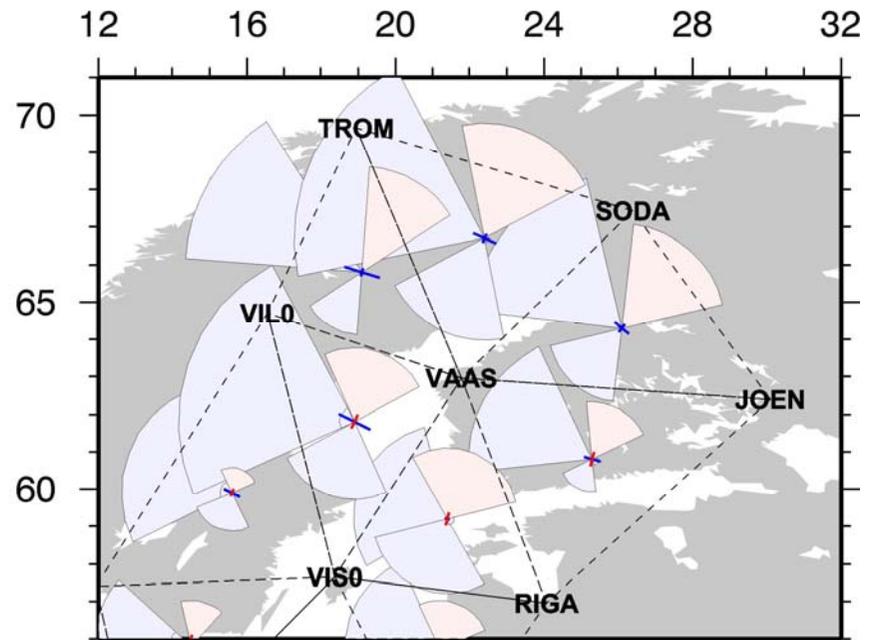


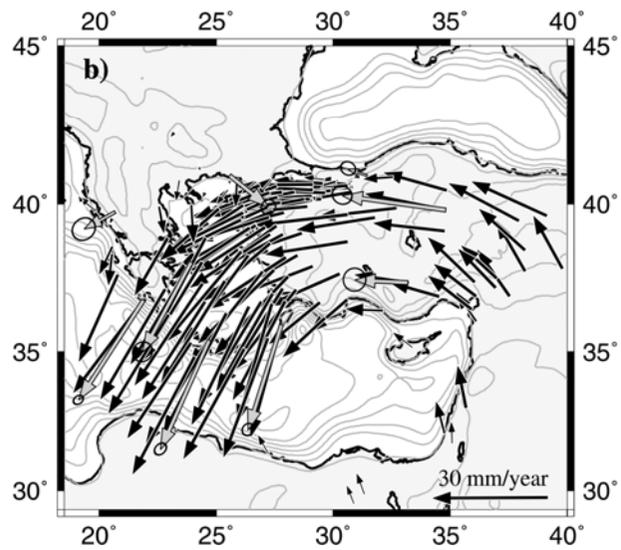
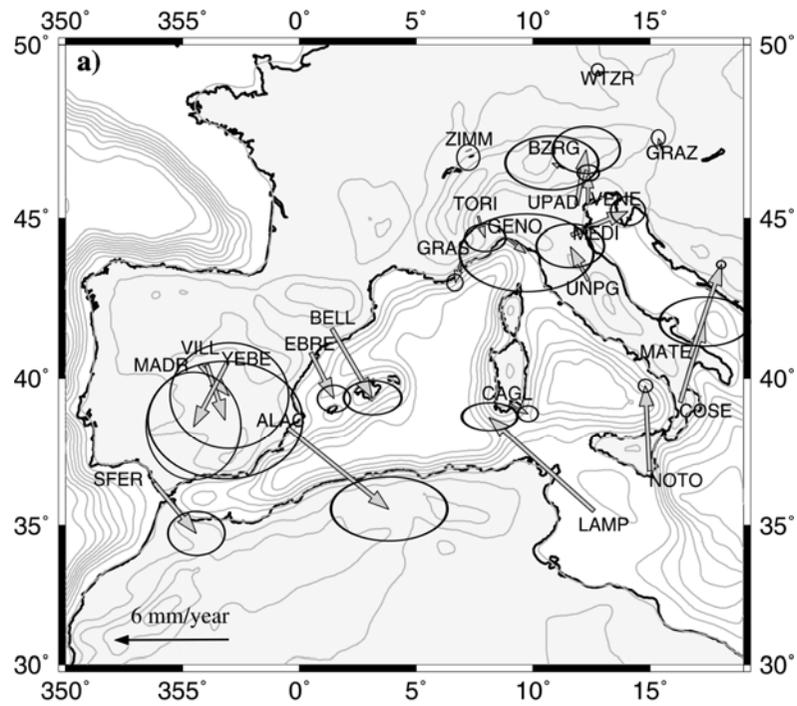
Implementation of numerical and analytical forward and inverse modeling of crust and lithosphere deformation

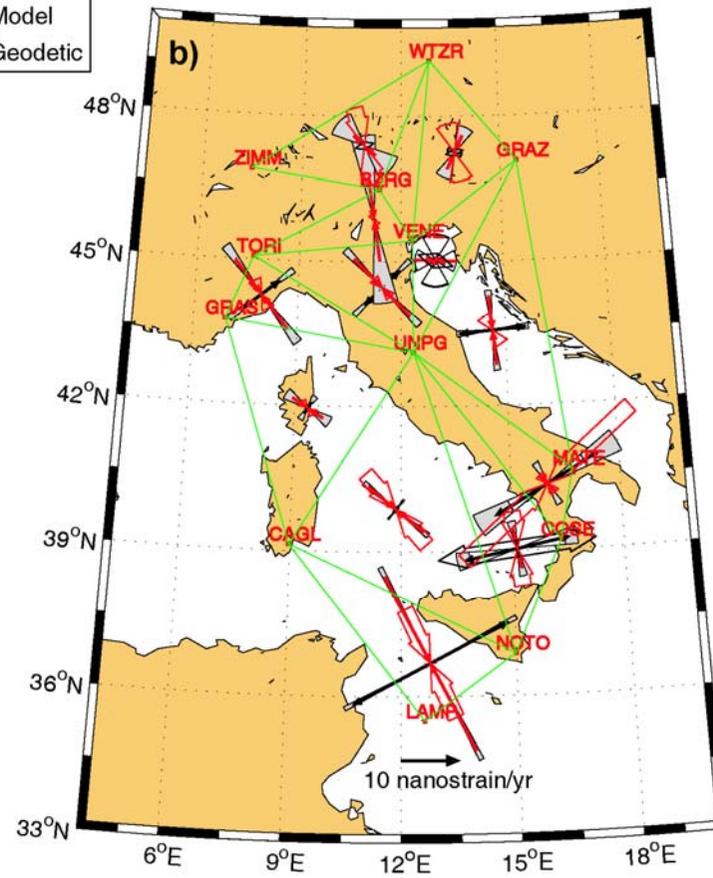
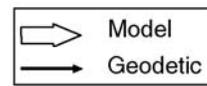
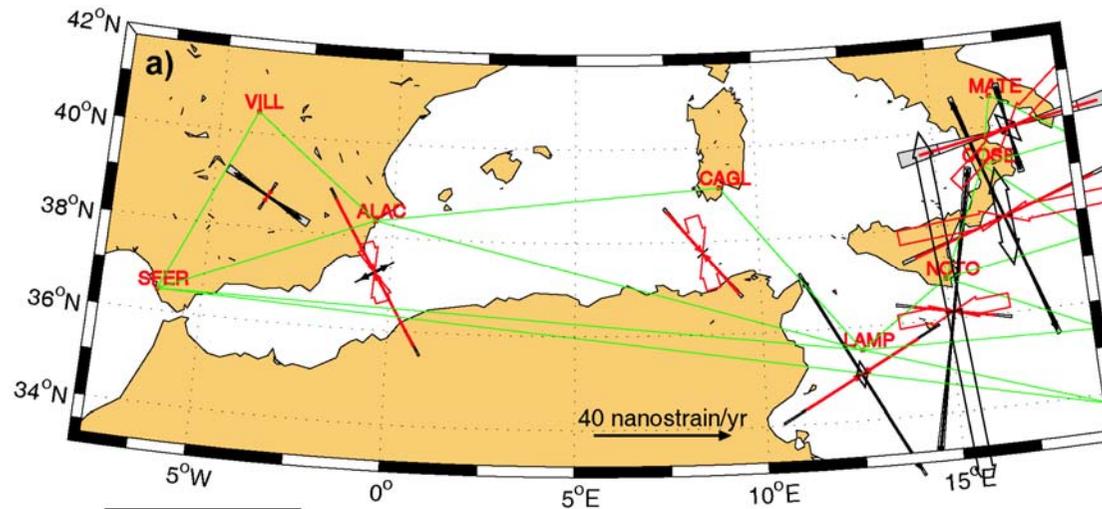


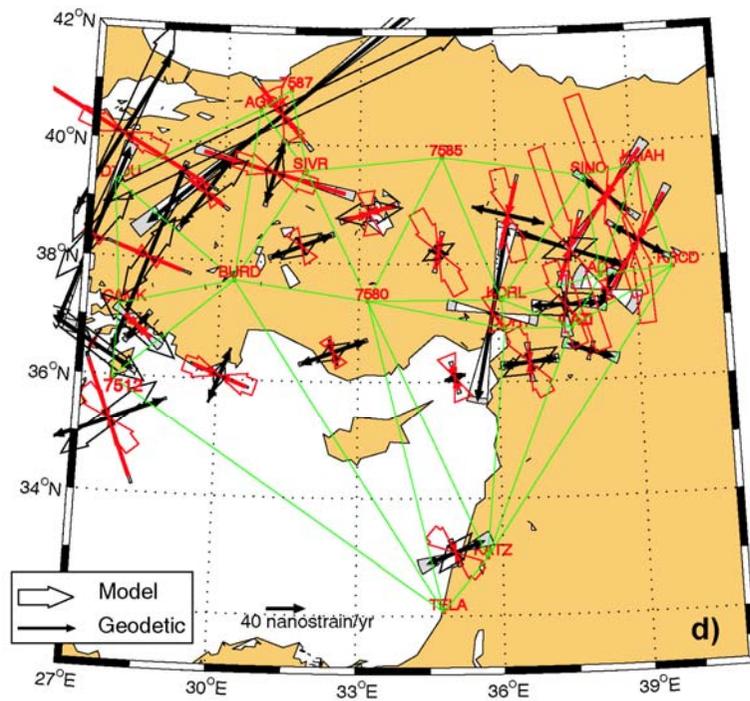
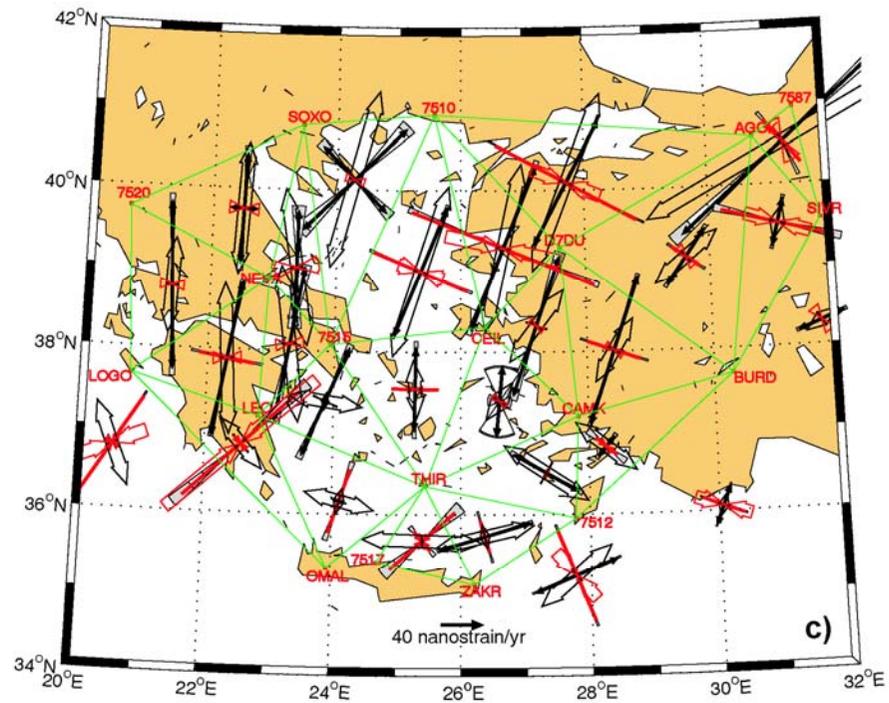
Marotta, A. M. et al., JGR 2004 – Combined effects of tectonics and glacial isostatic adjustment on intraplate deformation in central and northern Europe: Application to Geodetic baseline analysis.

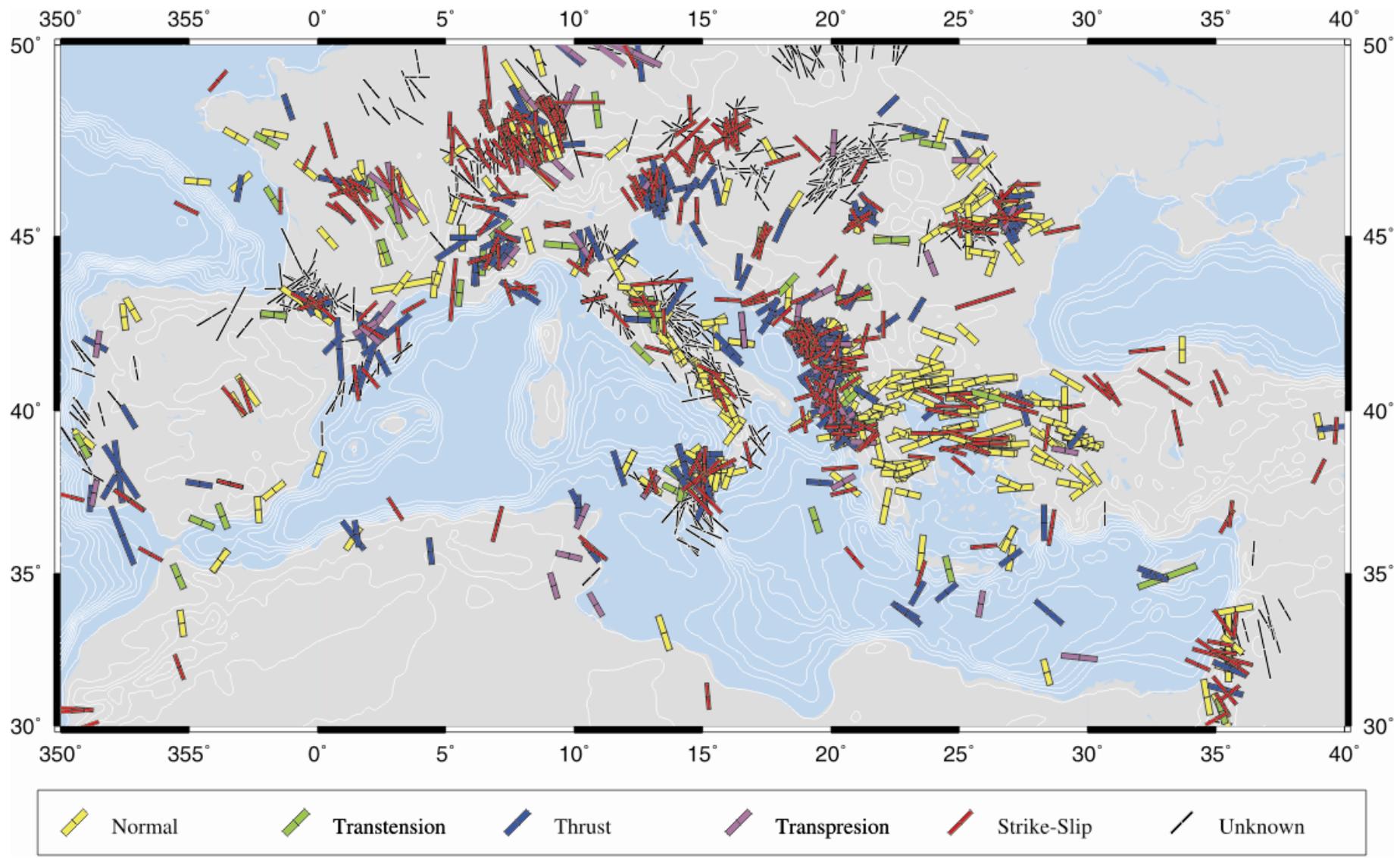




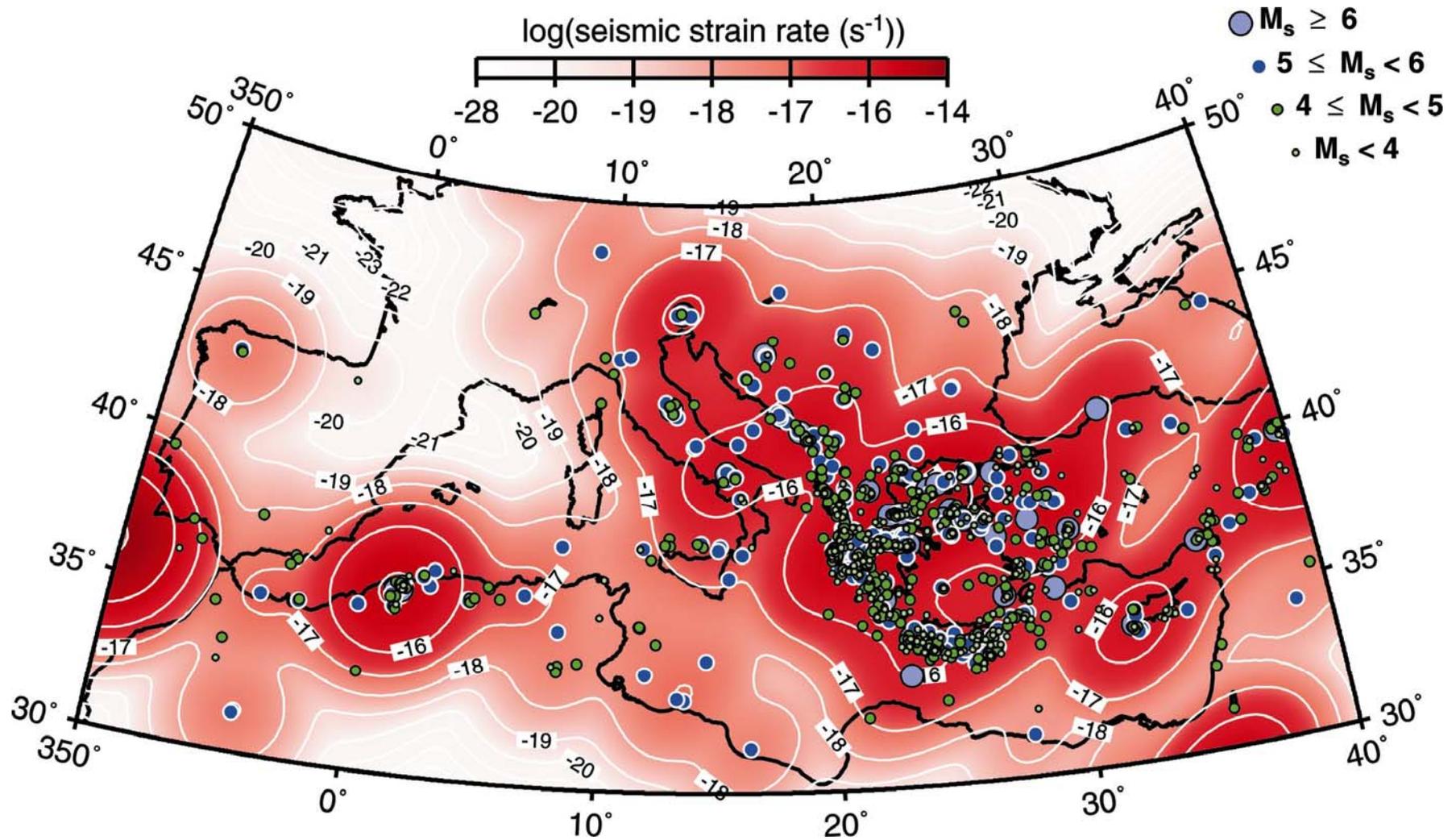




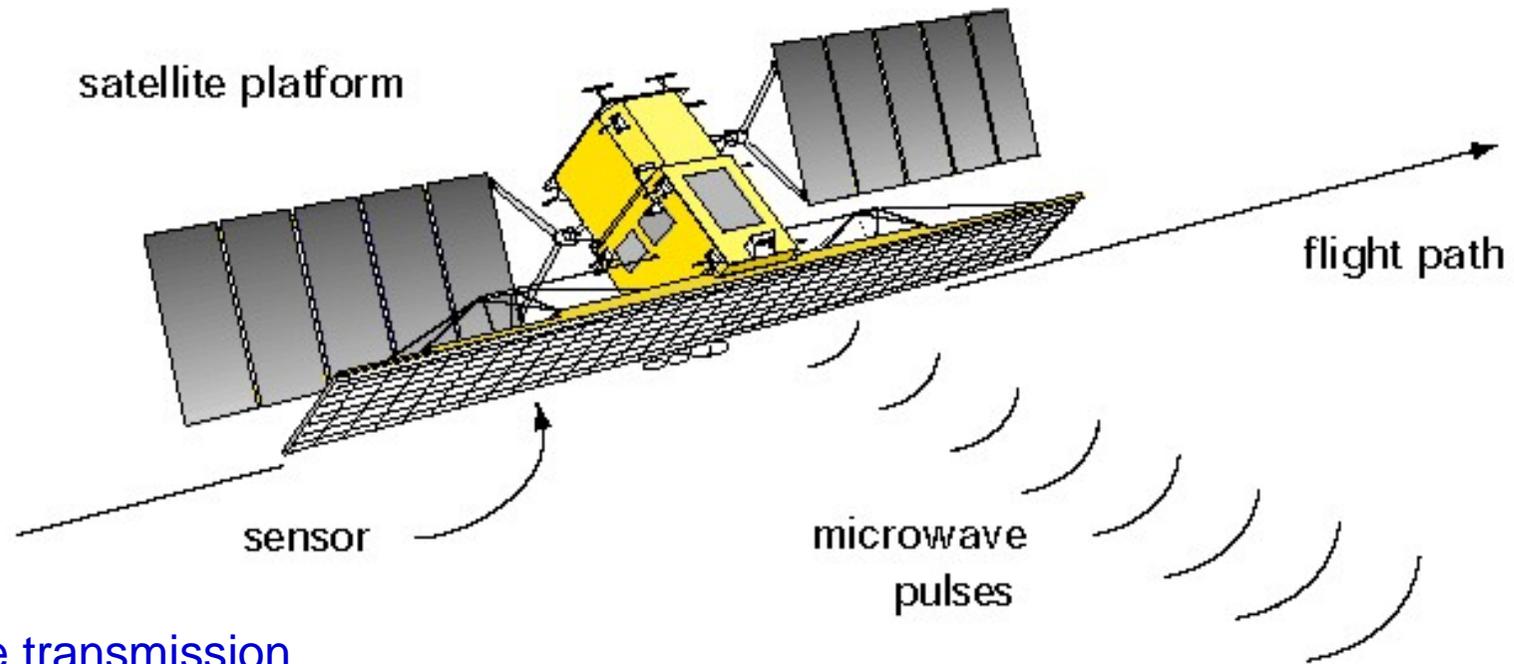




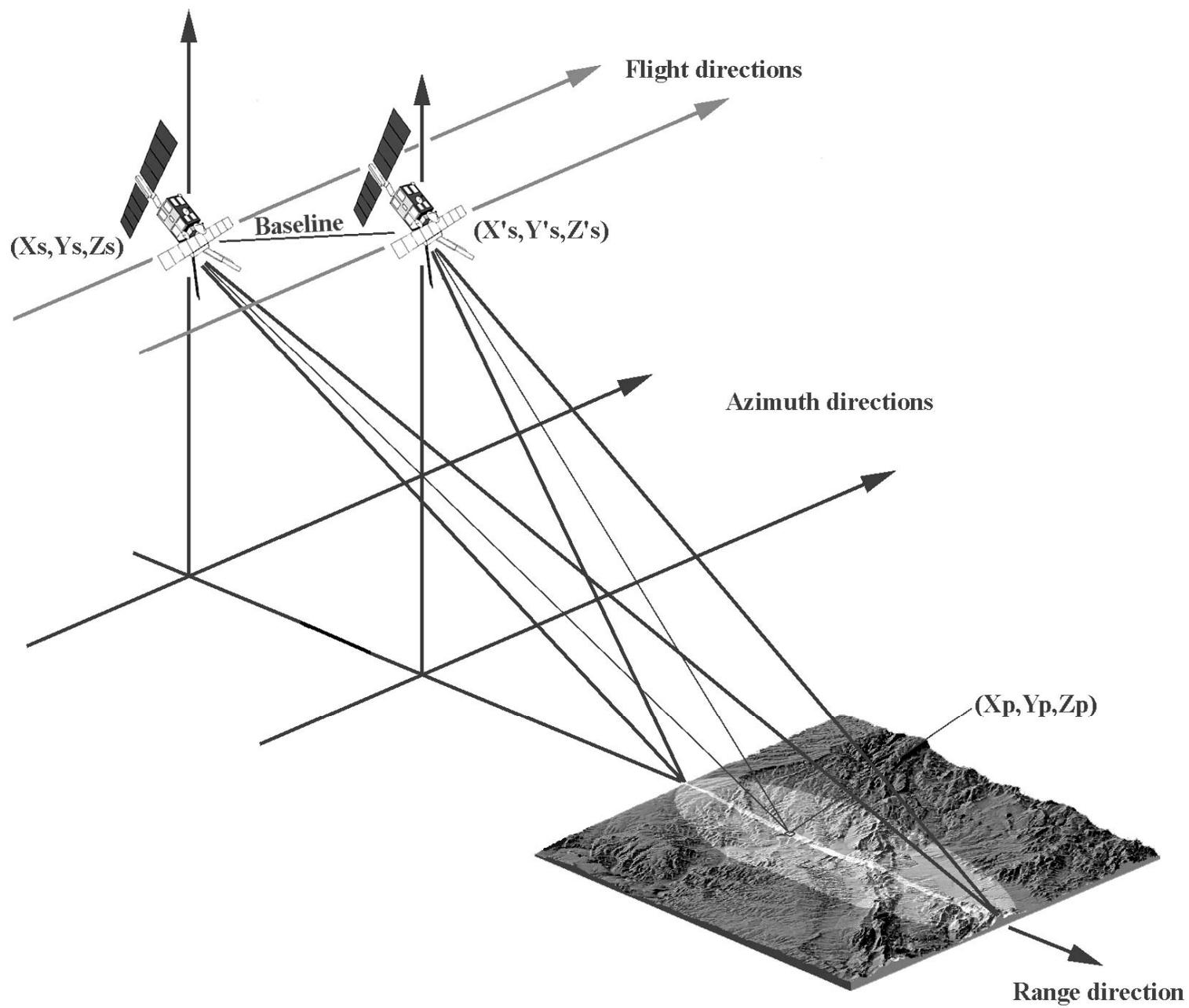
Seismicity (M_s , NEIC 1903-1999) and calculated seismic strain rate



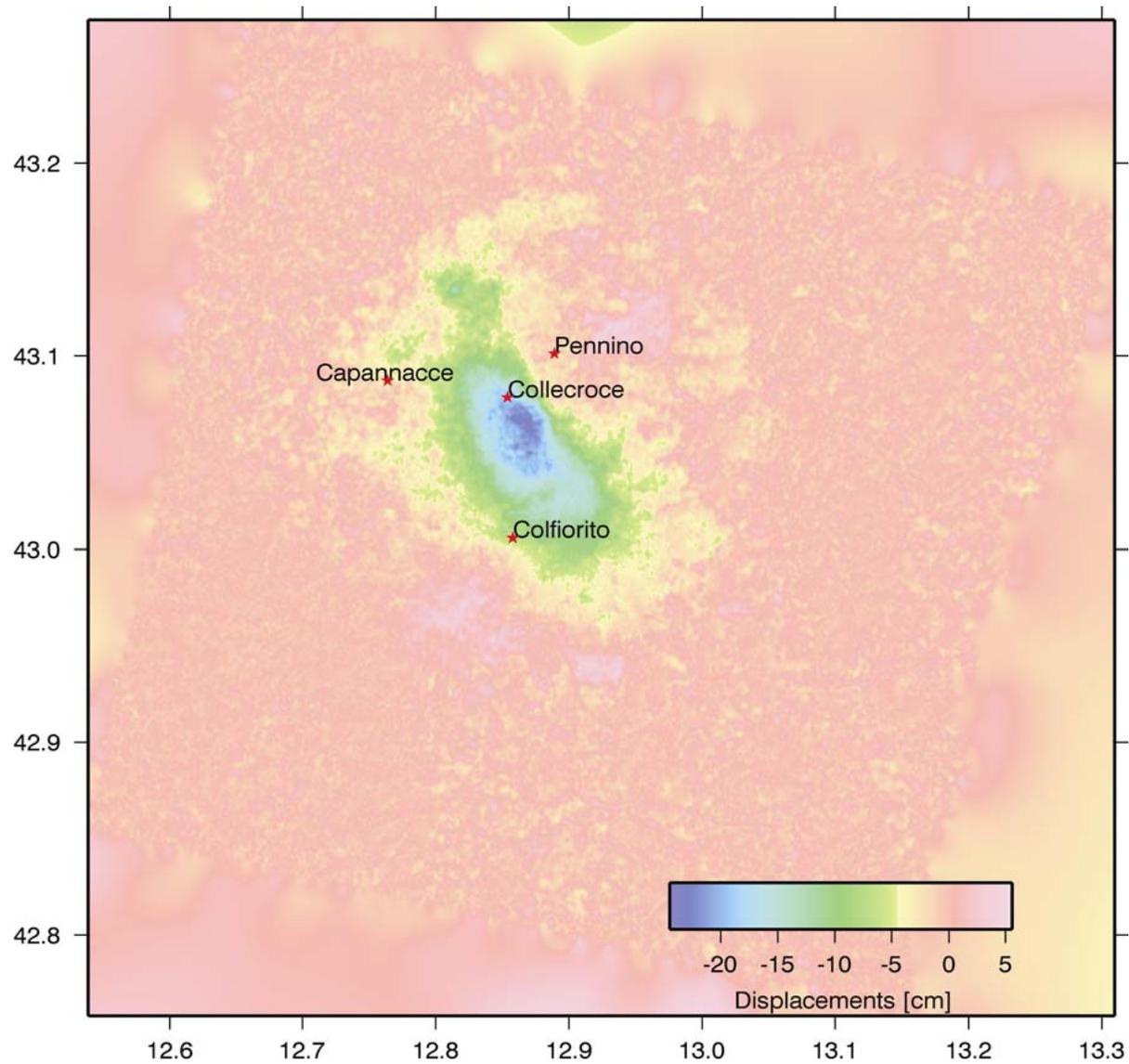
SAR: data acquisition

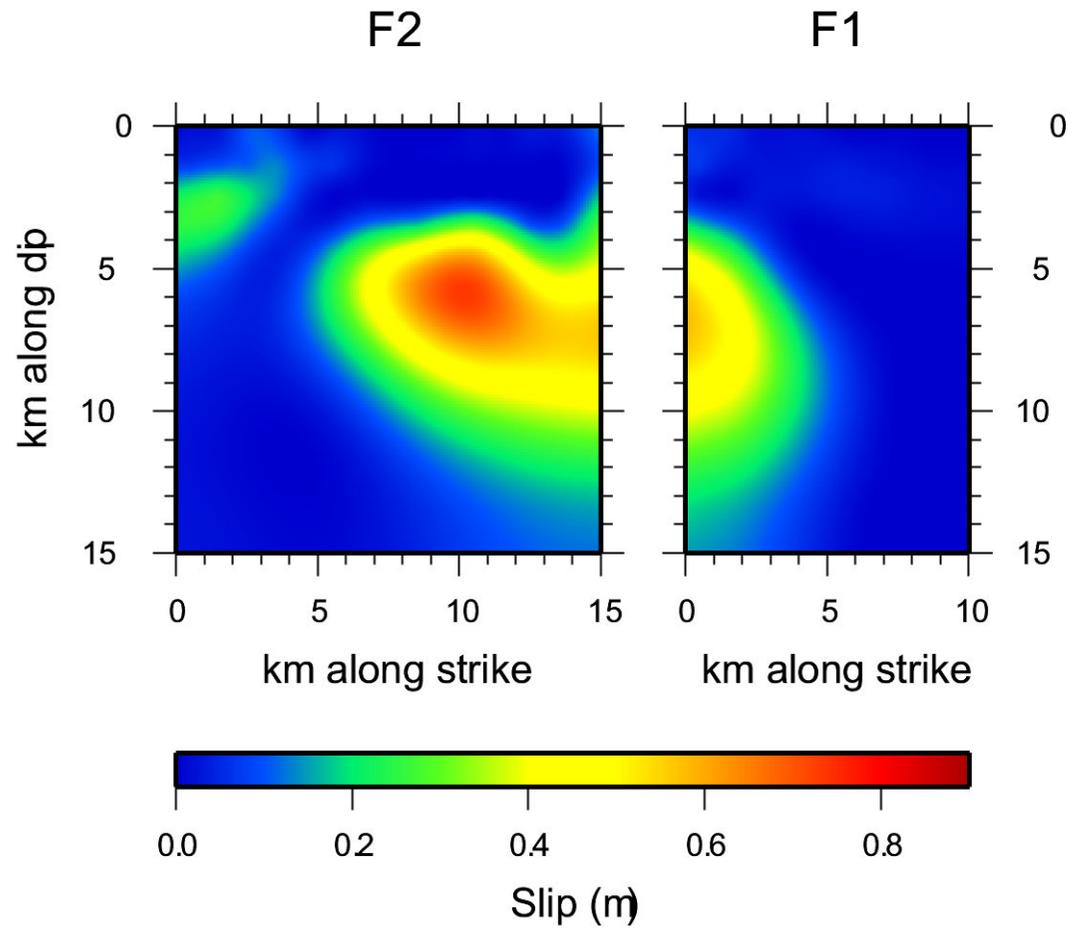


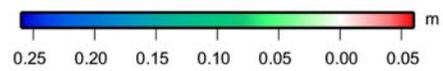
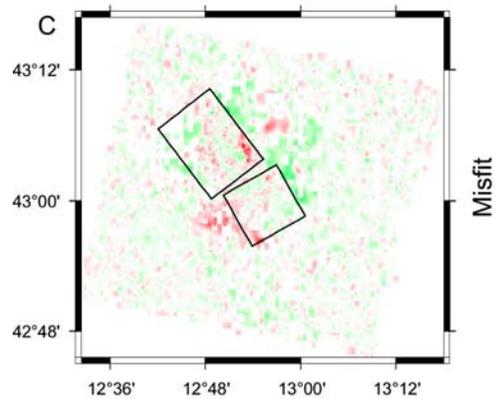
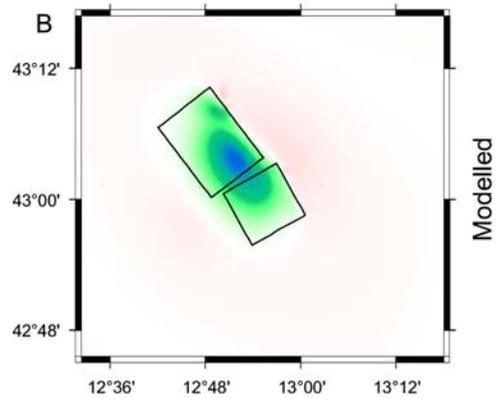
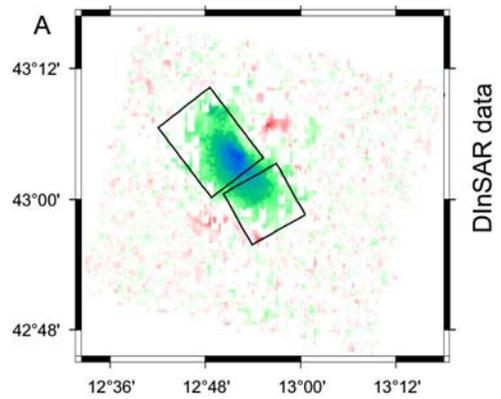
- Pulse transmission
 - Propagation, interaction with surface → echoes
 - Acquisition of echoes, with a delay: $t = 2 R / c$
→ the system measures distances
 - Transmission of pulses along the orbit → 2D sampling of terrain
-

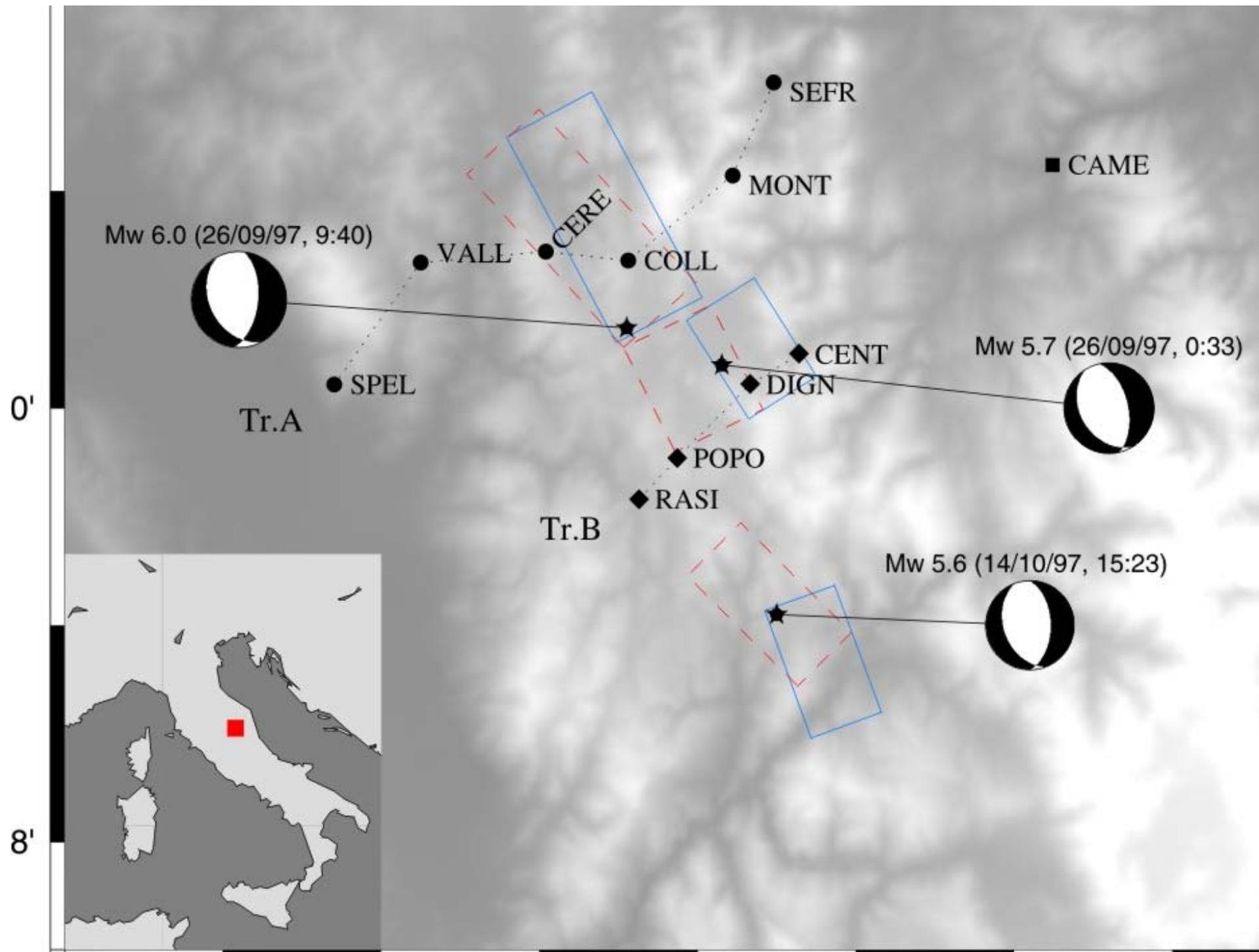


Methodology for detecting the vertical movements during the
pre-seismic, co-seismic and post-seismic phases in earthquake prone areas
(Crippa B. et al., **An advanced slip model for the Umbria-Marche earthquake sequence: coseismic displacements observed by SAR interferometry and model inversion, GJI, 2005, in press**).

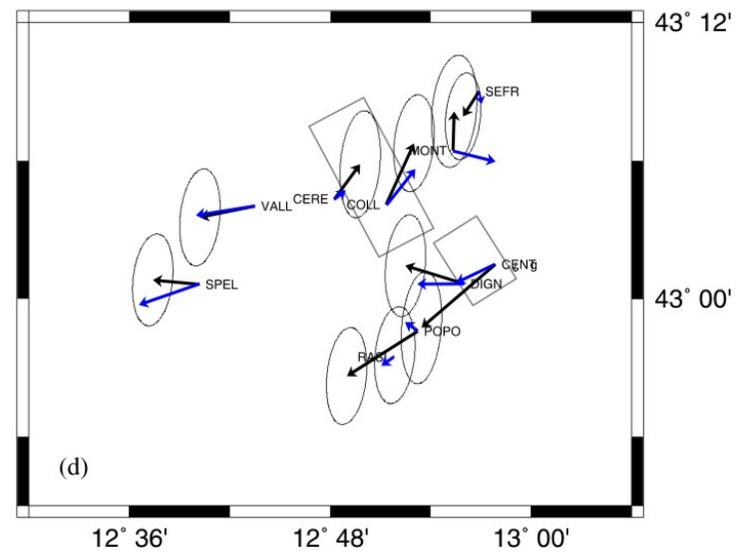
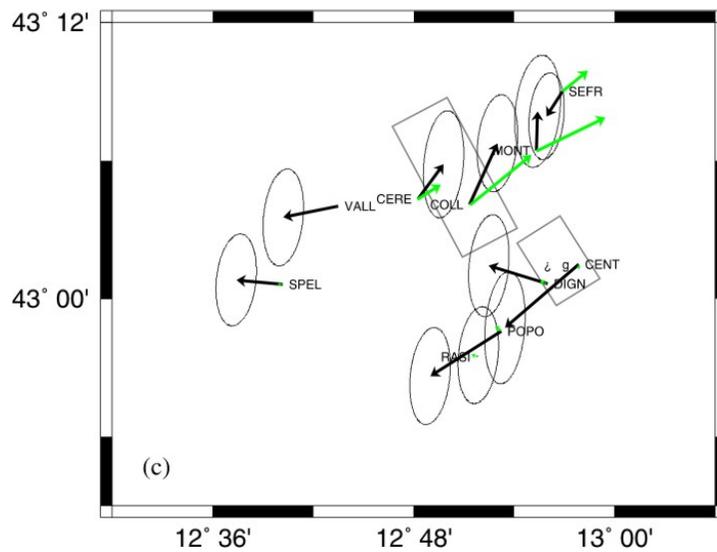
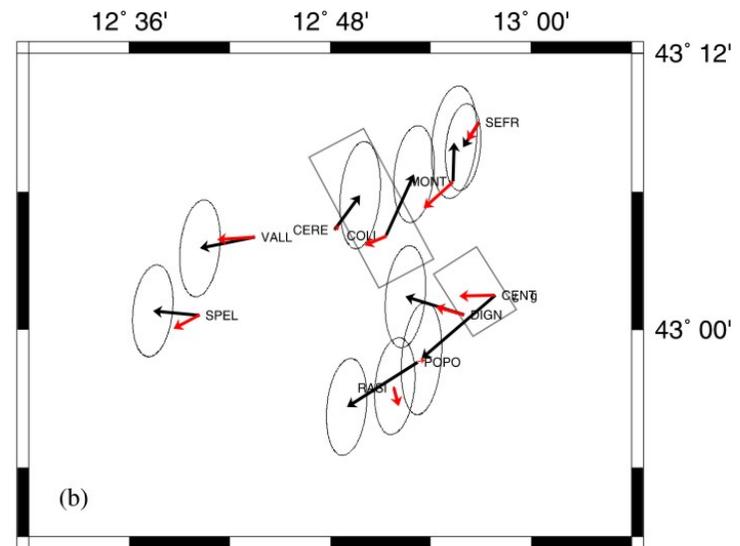
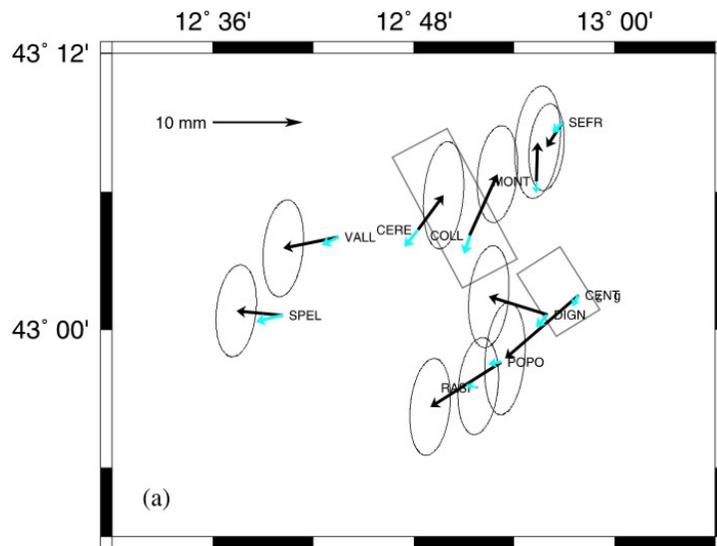






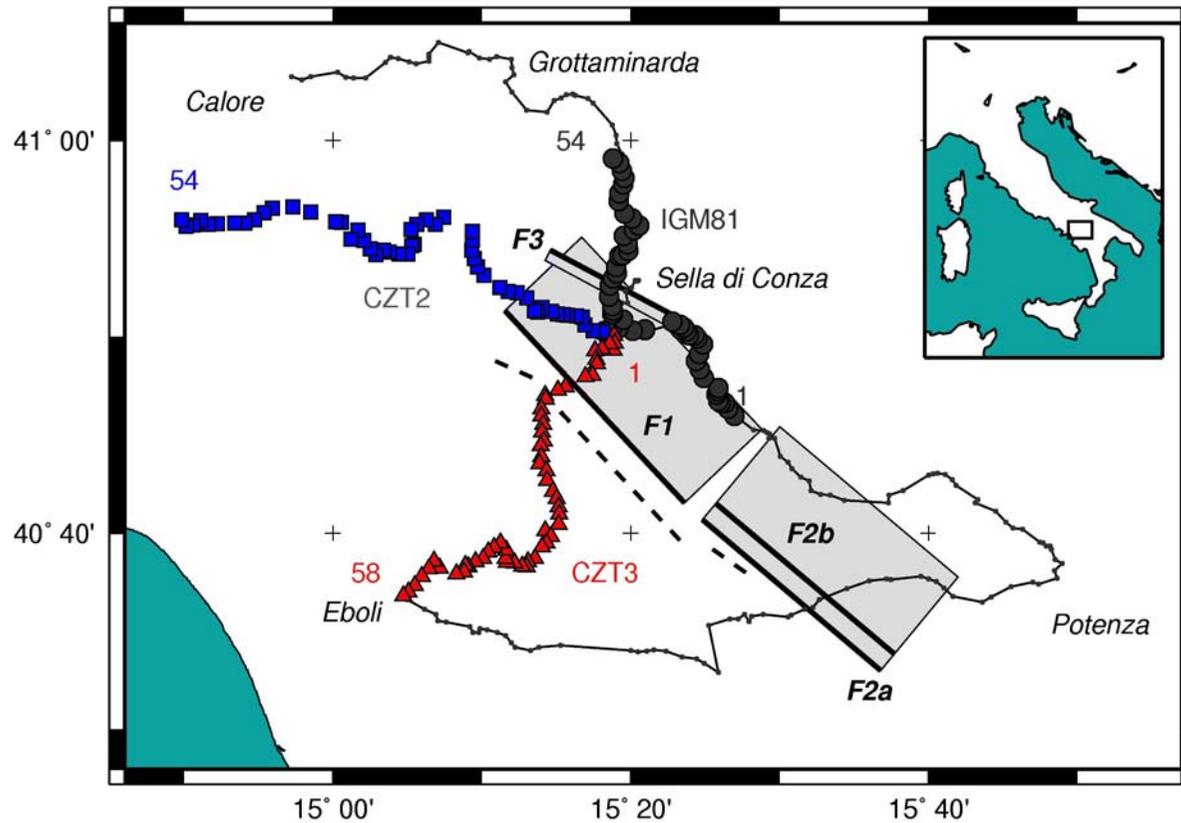


Non-permanent GPS networks

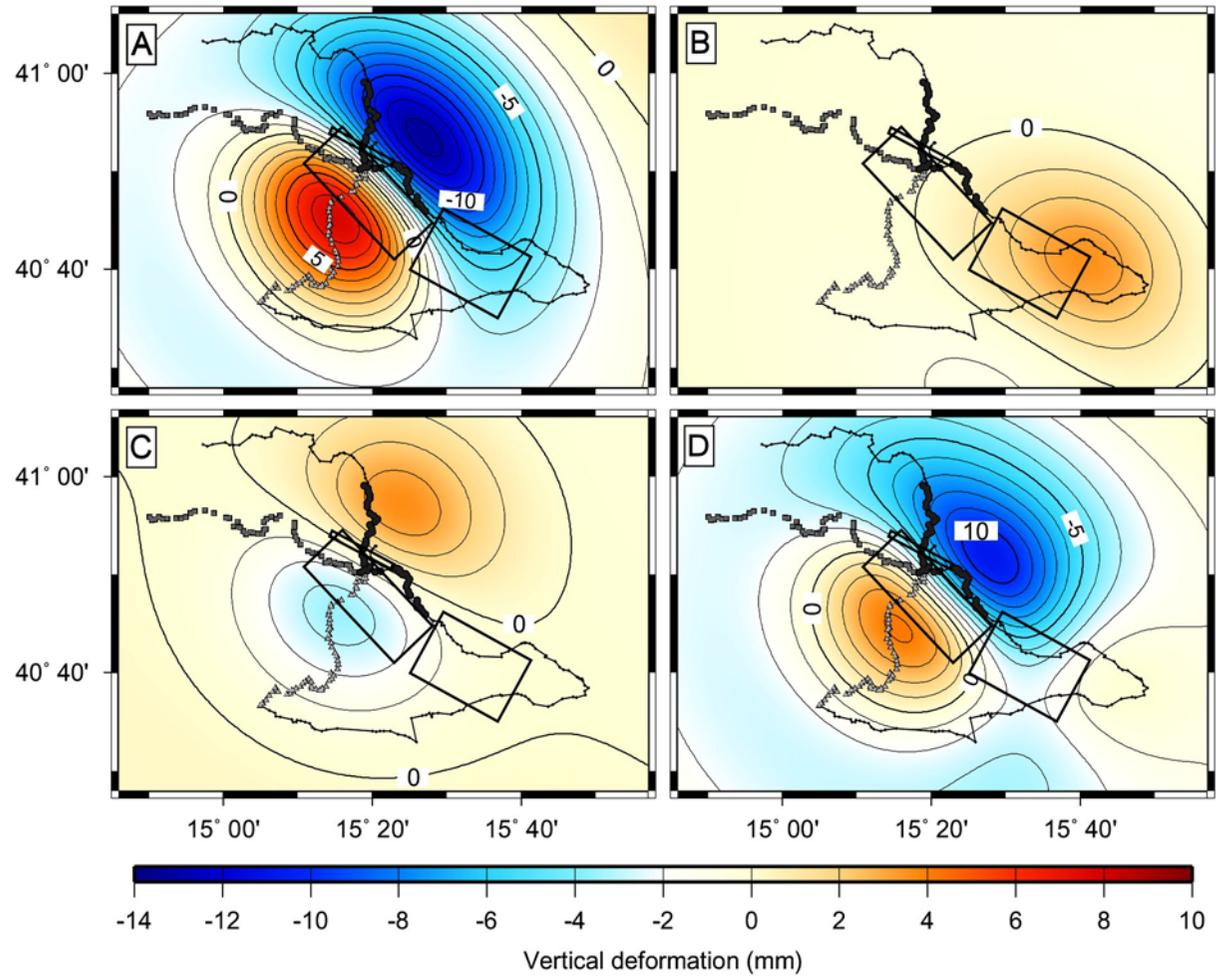


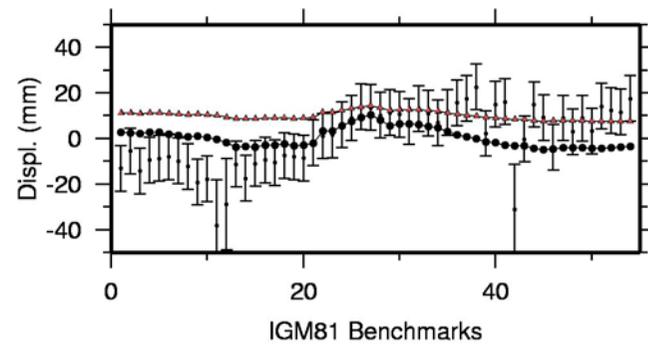
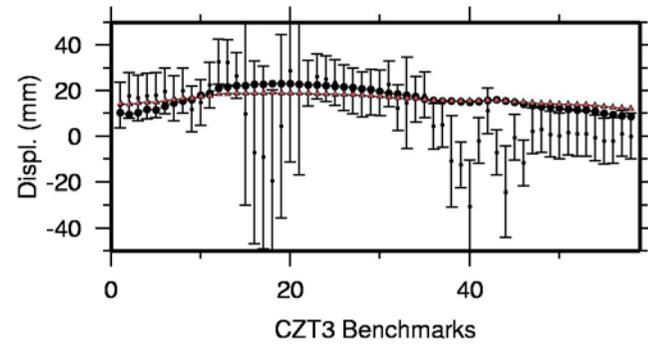
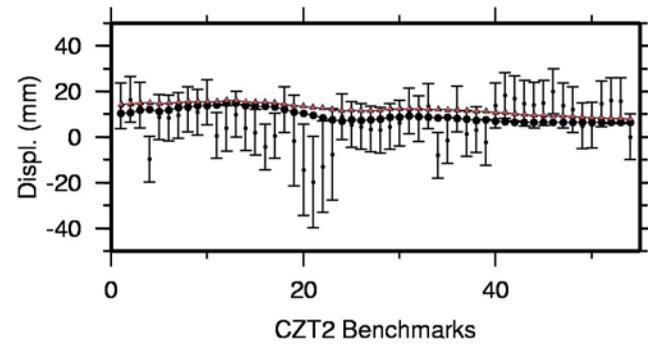
3B: Dignano

4B: Centare



Dalla Via, G. et al., Lithospheric rheology in southern Italy inferred from postseismic viscoelastic relaxation following the 1980 Irpinia earthquake, JGR, 2005





Dalla Via, G. et al., Lithospheric rheology in southern Italy inferred from postseismic Viscoelastic relaxation following the 1980 Irpinia earthquake, JGR, 2005

CONCLUSIONS (1)

- **Although the seismic classification of the Italian territory has been recently revised, the evaluation of seismic hazard continue to be based on the traditional probabilistic approach, i.e. on the probabilistic analysis of earthquake catalogue and of ground motion information, retrieved by macroseismic observations and instrumental recordings, that may lead to severe underestimations of seismic hazard.**
- **Recently this approach showed its limitation in providing a reliable seismic hazard assessment, possibly due to the insufficient information about historical seismicity, which can introduce relevant errors in the purely statistical approach mainly based on the seismic history. Indeed, some areas where low seismic hazard was foreseen, and consequently were not included in the seismic classification, have been subsequently struck by relatively strong and damaging earthquakes (e.g. the Sicily, September 2002, and the Molise, October 2002, earthquakes).**

CONCLUSIONS (2)

- **To overcome the mentioned limitations and, above all, to improve the pre-seismic information which may lead to an effective mitigation of seismic risk, we are proposing an innovative approach, that combines EO data and new advanced approaches in seismological and geophysical data analysis.**
- **The proposed system, in fact, is proposing a deterministic approach to the estimation of seismic ground motion, integrated with the space and time dependent information provided by EO data analysis through geophysical forward modeling. The reason of the proposed integration of different geophysical observables appears almost obvious analyzing the earthquake “life cycle”, i.e. its process of preparation and occurrence: the lithosphere accumulates stress, according to strain and strain rates fields due to tectonic movements, which is partly released during the earthquake occurrence.**