

# Entangled States

- entanglement



states:  $|0\rangle \otimes |0\rangle$

$|1\rangle \otimes |1\rangle$

... product states

but also ...

$$\frac{1}{\sqrt{2}} (|0\rangle \otimes |0\rangle + |1\rangle \otimes |1\rangle) \quad \dots \text{entangled}$$

- fundamental aspects of quantum mechanics
- applications
  - quantum computing & communication, quantum simulation
  - precision measurement

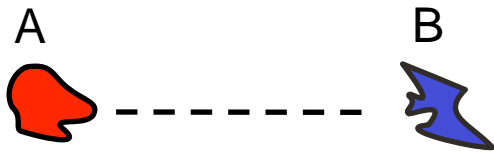
Schrödinger:  
*Verschränkung*



# Engineering Entangled States

We need ...

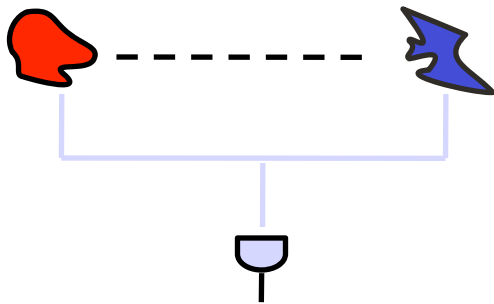
- quantum state engineering



$$|a\rangle_A |b\rangle_B \rightarrow \sum c_{ab} |a\rangle_A |b\rangle_B$$

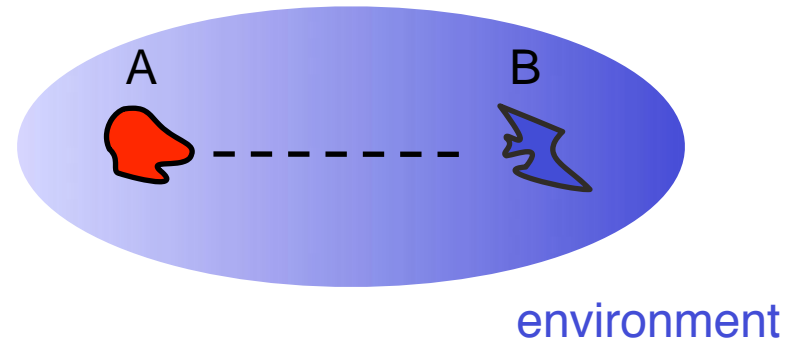
Hamiltonian evolution

- or: “quantum gambling”



measurement

- isolation



$$|\phi\rangle_A |\phi\rangle_B |E\rangle \rightarrow |\Psi\rangle_{ABE}$$

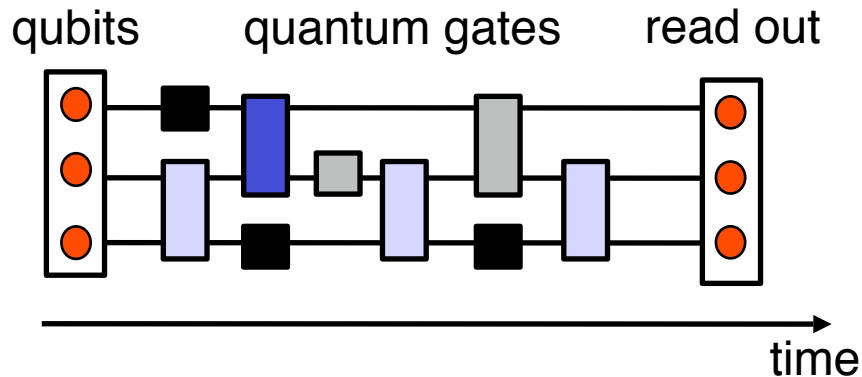
$$\rho_{AB} = \text{tr}_E |\Psi\rangle_{ABE} \langle \Psi|$$

$$\neq |\Psi\rangle_{AB} \langle \Psi|$$

Quantum optical systems provide one of the best set-ups to create entangled states in a controlled way.

# Quantum Computing

- quantum computing: logic network

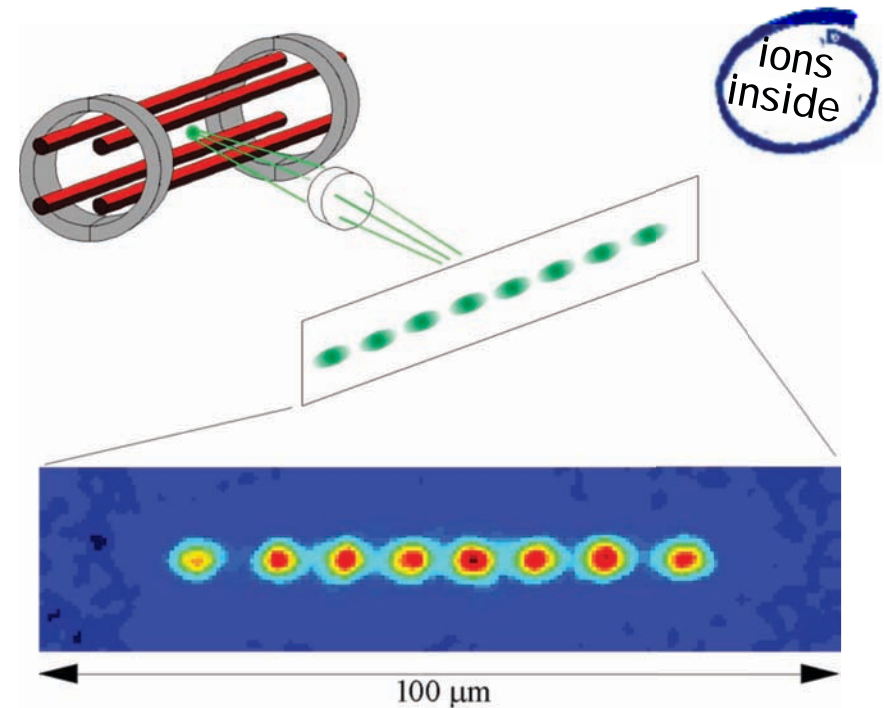


- general purpose quantum processor

- ✓ qubits
- ✓ single qubit gate
- ✓ two qubit gate = entanglement
- ✓ read out
- ✓ (no decoherence)

# Quantum Optics

- laser cooled trapped ions [I. Cirac & P.Z.](#)



... 2 internal state / ion

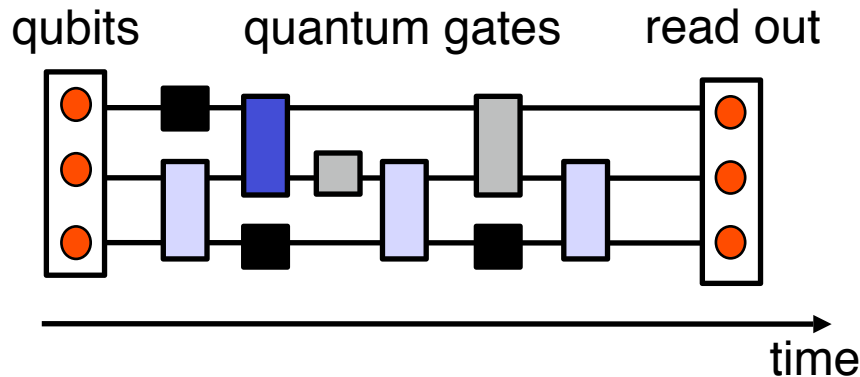
... with laser pulses

... via collective phonon modes

... with quantum jump technique

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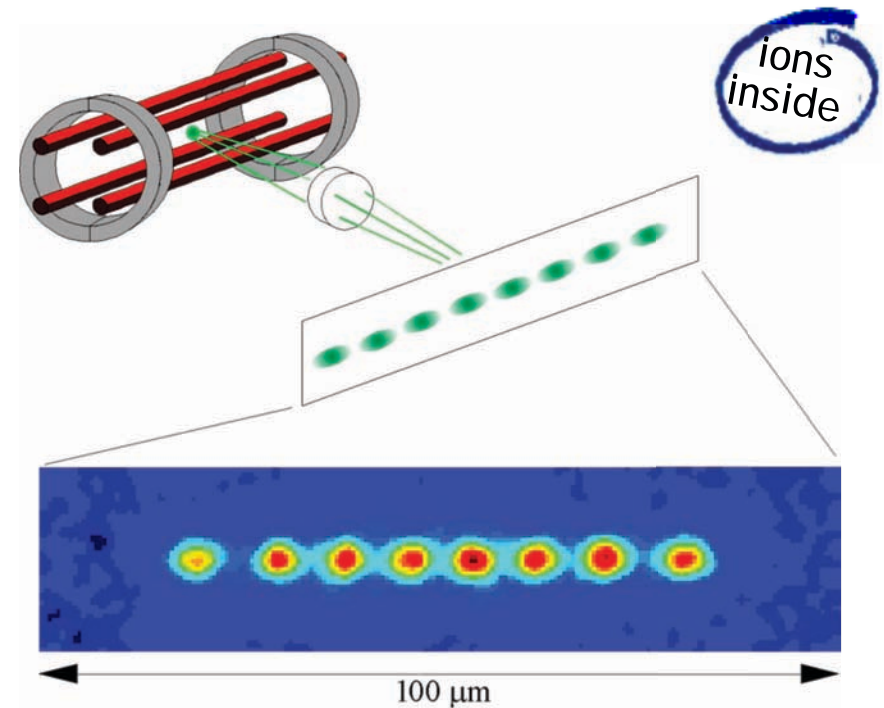


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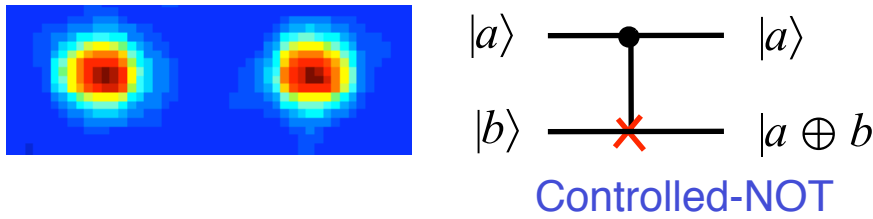
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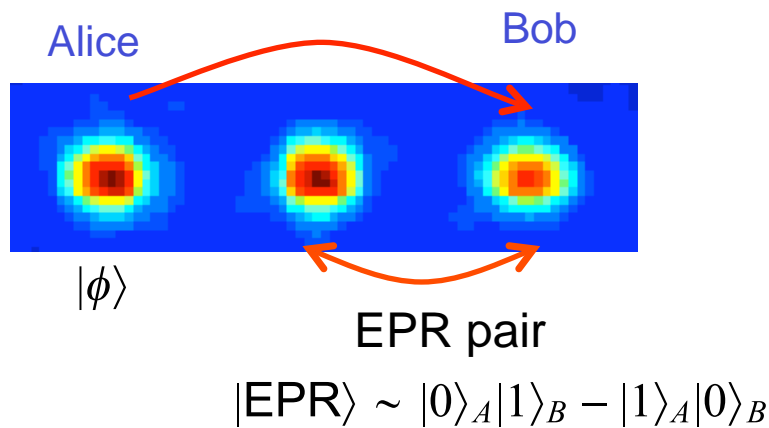
"phonon data bus"

# Ion Trap QC: Achievements

- 2 ion addressable Controlled-NOT

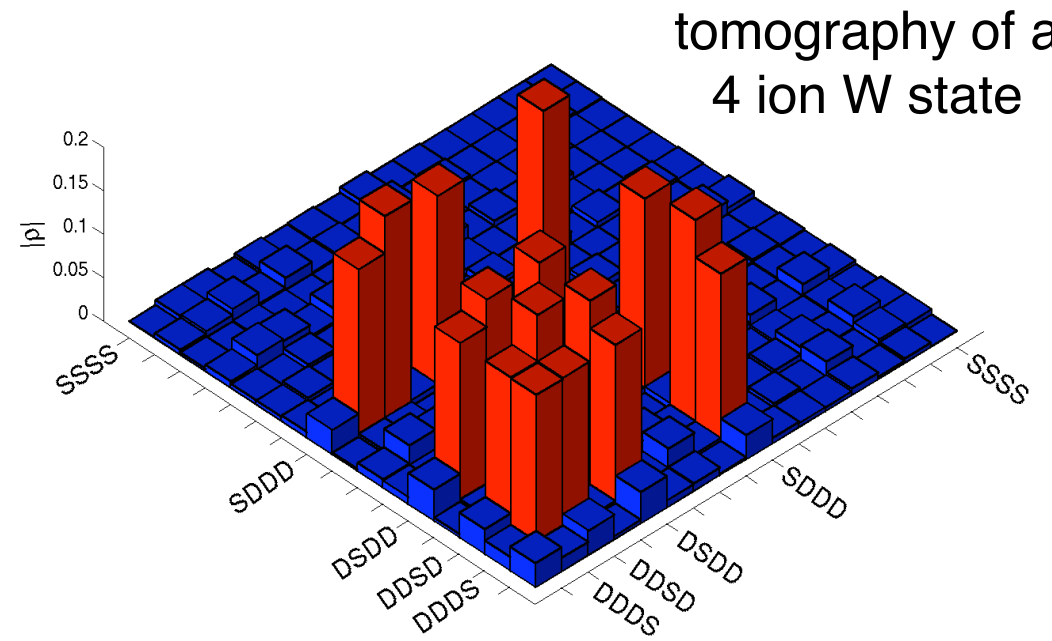


- 3 ions: deterministic teleportation, error correction



- lifetime of EPR states ~ 60 sec

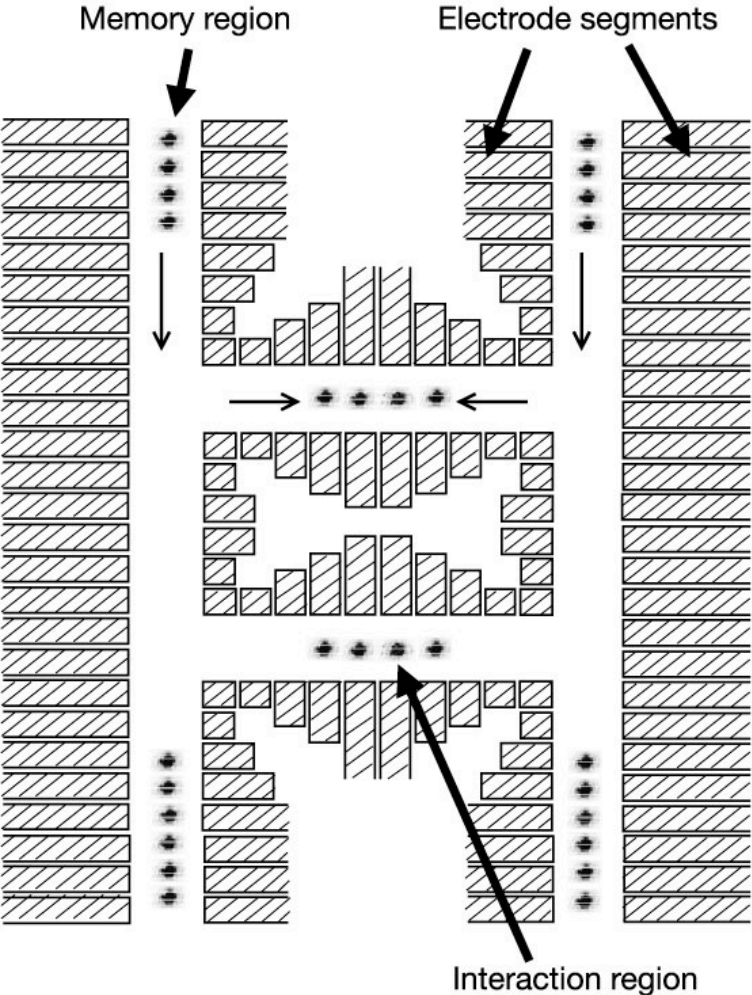
- 6 ions GHZ state
- 8 ions: W-state



$$|\Psi_4\rangle = \frac{1}{2} (|SDDD\rangle + |DSDD\rangle + |DDSD\rangle + |DDDS\rangle)$$

# Ion Trap QC: Future

- scalable quantum computing



move ions

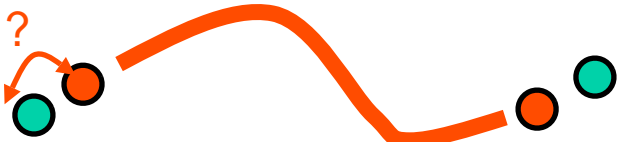
Wineland et al., I. Cirac and PZ

- interfaces

-quantum optics / solid state interfaces

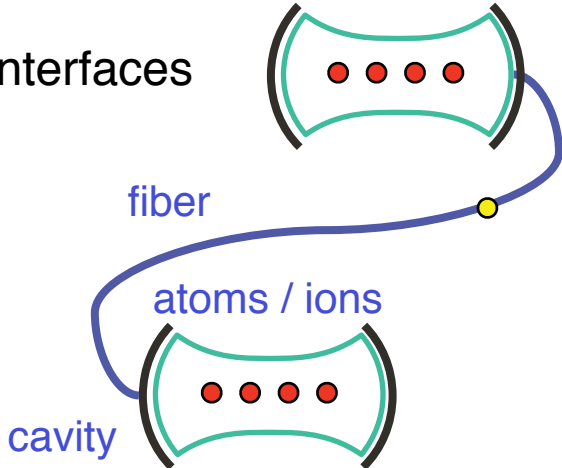


connecting two quantum optical qubits by a (passive) solid state bus



interfacing active devices

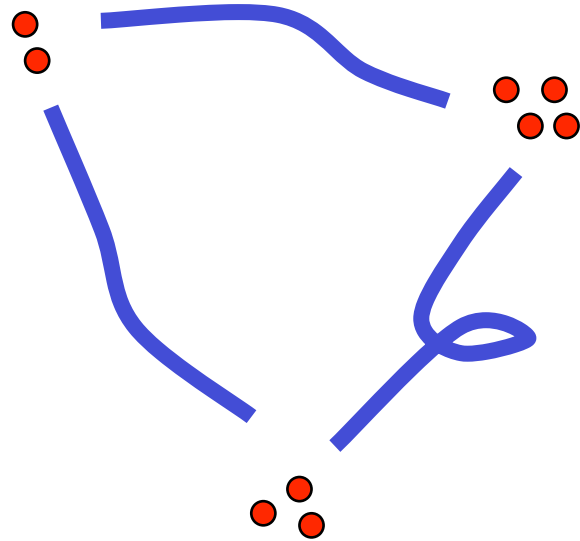
-ion / photon interfaces



I. Cirac, PZ,  
J Kimble, H. Mabuchi

# Quantum Communication

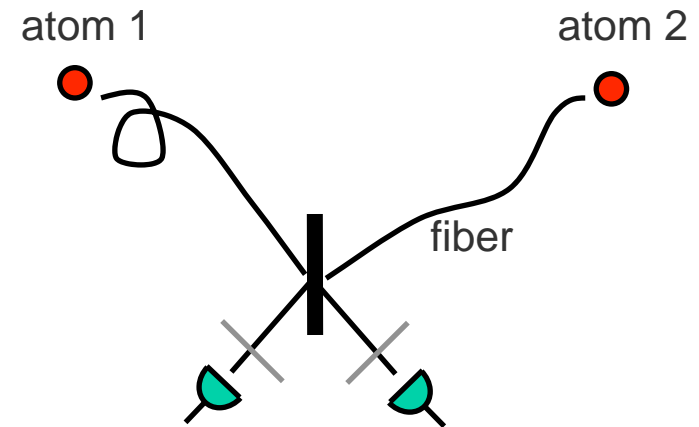
- quantum communication & quantum networks



- **Nodes: local quantum computing**
  - store quantum information
  - local quantum processing
- **Channel: quantum communication**
  - transmit quantum information

# Quantum Optics

- entanglement over a distance



$$|\Psi\rangle \sim |01\rangle - |10\rangle$$

*probabilistic* generation of EPR state

- quantum repeater protocols** for long distance quantum communication
  - generation and purification of long distance EPR pairs
  - teleportation

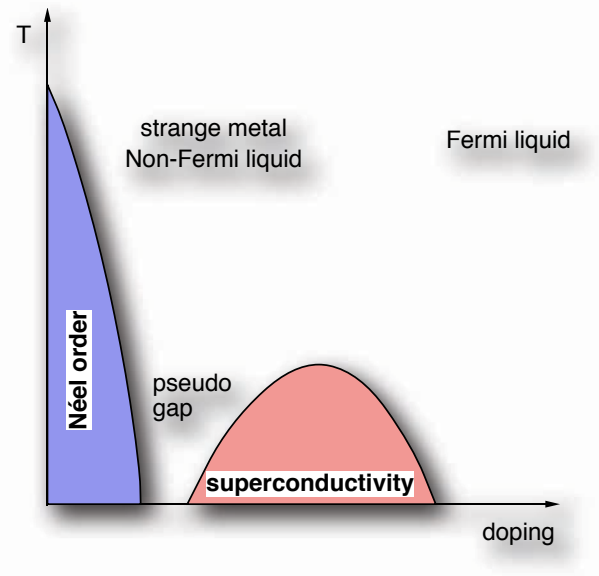
Duan, Cirac,  
Lukin & PZ

exp: Kimble, Kuzmich, Lukin, Polzik;  
Monroe



# Condensed Matter Physics

- cond mat models: strong correlation ...

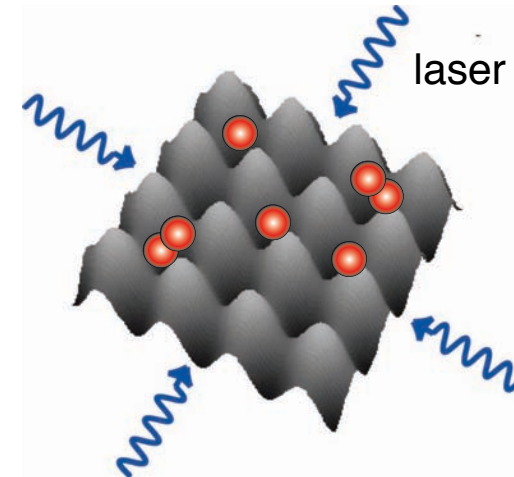


Fermi Hubbard in 2D

$$H = -t \sum_{i,j,\sigma} (c_{i\sigma}^+ c_{j\sigma} + c_{j\sigma}^+ c_{i\sigma}) + U \sum_i n_{i\uparrow} n_{i\downarrow}$$

# Quantum Optics

- atoms in an optical lattices



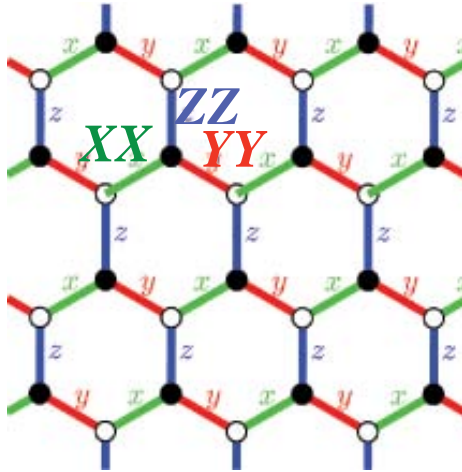
Bose & Fermi Hubbard

## AMO Hubbard toolbox

- ✓ engineer interactions
- ✓ controllable parameters  
(1D/2D/3D, time dependence, ...)

# Condensed Matter Physics

- cond mat models: strong correlation ...

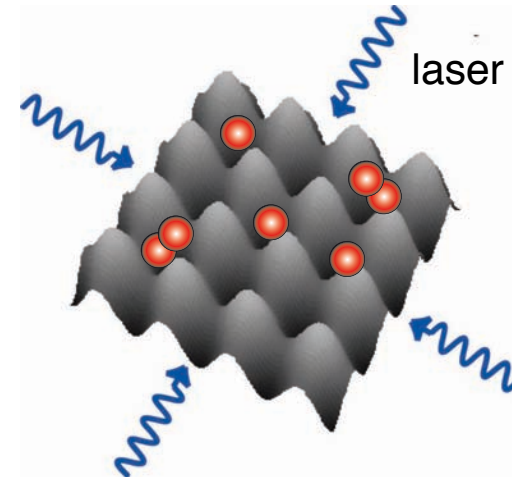


exotic “materials” and quantum phases

- “quantum simulators”
  - analog & digital
- measurement based quantum computing
- topological phases and qc (?)

# Quantum Optics

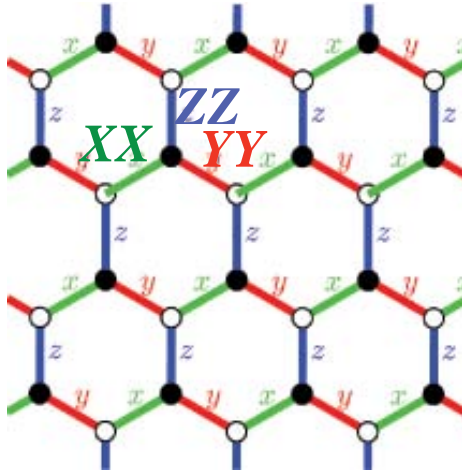
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Bose & Fermi Hubbard

# Condensed Matter Physics

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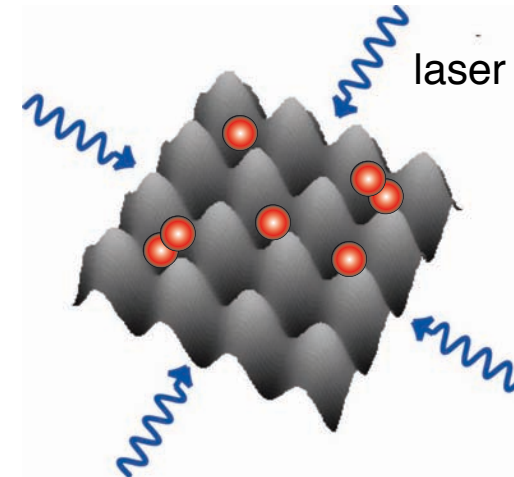


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# Quantum Optics

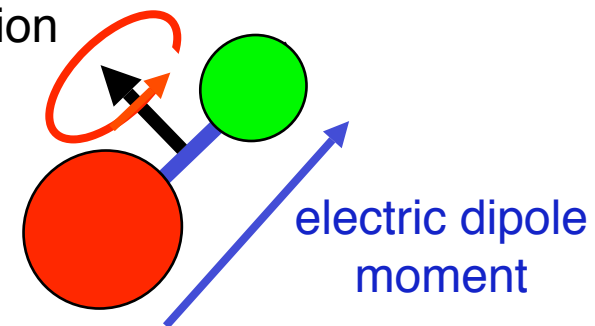
- atoms in an optical lattices



Bose & Fermi Hubbard

- polar molecules

rotation

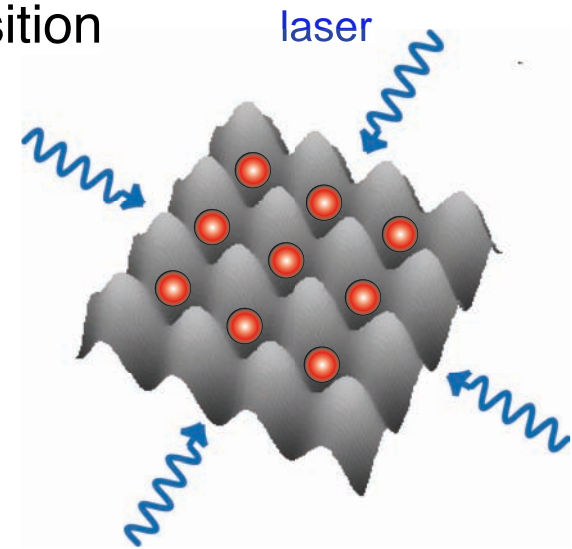


new system

# Atoms in Optical Lattices: Achievements

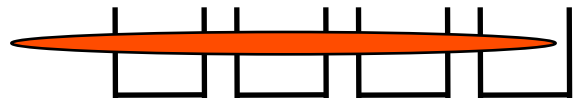
- Superfluid - Mott insulator quantum phase transition

$$H = - \sum_{\alpha \neq \beta} J_{\alpha\beta} b_{\alpha}^{\dagger} b_{\beta} + \frac{1}{2} U \sum_{\alpha} b_{\alpha}^{\dagger} b_{\alpha}^{\dagger} b_{\alpha} b_{\alpha}$$



- shallow lattice: superfluid  $t \gg U$

- deep lattice: Mott insulator  $t \ll U$



$$\left( b_1^{\dagger} + \dots + b_M^{\dagger} \right)^N |\text{vac}\rangle$$

delocalized atoms: BEC

(weakly interacting)



quantum phase  
transition



$$b_1^{\dagger} b_2^{\dagger} \dots b_M^{\dagger} |\text{vac}\rangle$$

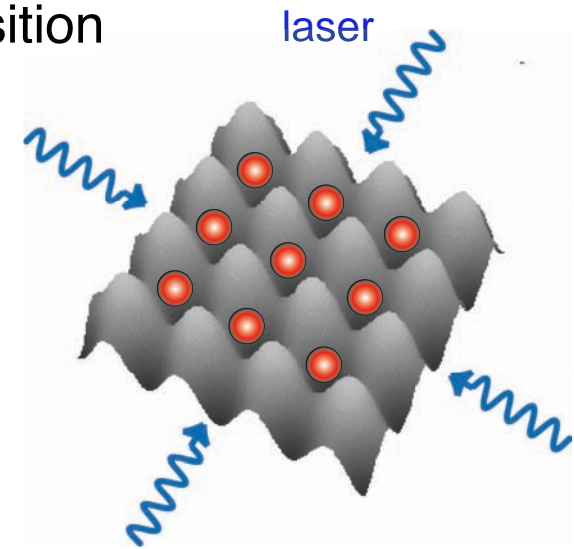
"Fock states"

(strongly interacting)

# Atoms in Optical Lattices: Achievements

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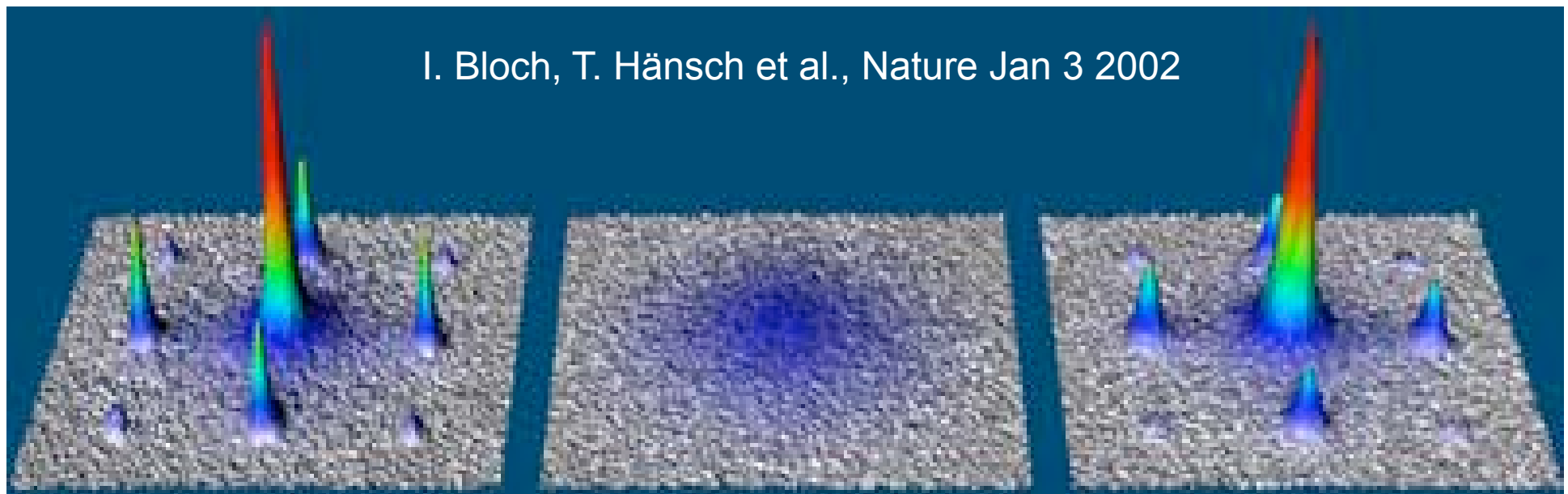
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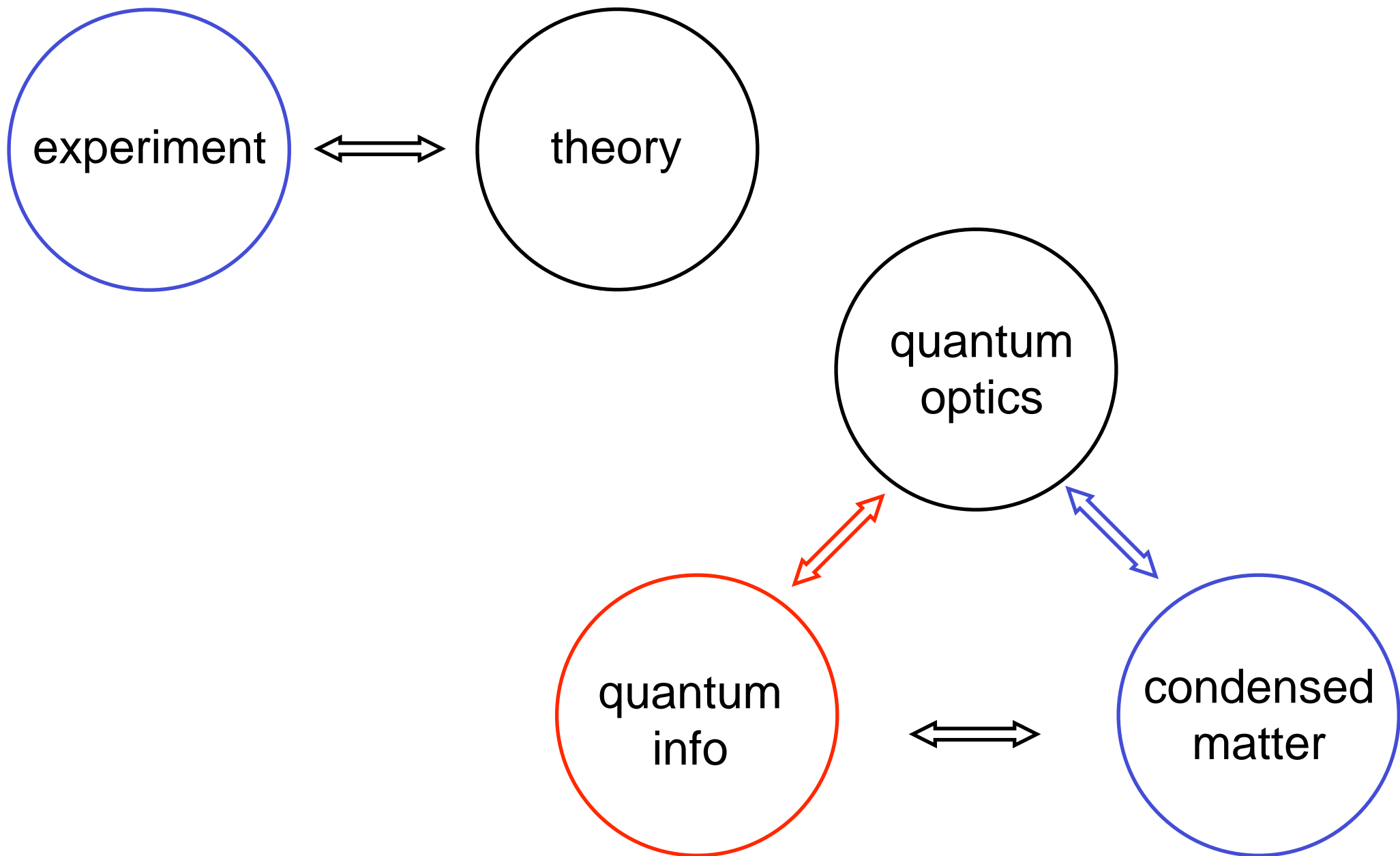
interference: SF

NO interference: Mott

interference: SF



## Summary & Outlook



## Innsbruck:

Andrea Micheli (PhD)

M. Ortner (PhD)

Peter Rabl (PhD->Harvard)

Gavin Brennen (Postdoc-> Prof. Sydney)

Hanspeter Büchler (Postdoc->Prof. Stuttgart)

Guido Pupillo (Postdoc)

## Theory Collaborations:

MPQ: **I. Cirac**

Harvard: E. Demler, M Lukin

Oxford: D. Jaksch

Michigan: L.M. Duan

Barcelona: M Lewenstein

