



*The Abdus Salam  
International Centre for Theoretical Physics*



**2030-8**

**Conference on Research Frontiers in Ultra-Cold Atoms**

*4 - 8 May 2009*

**Impurities in a Bose gas**

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# Impurities in a Bose gas

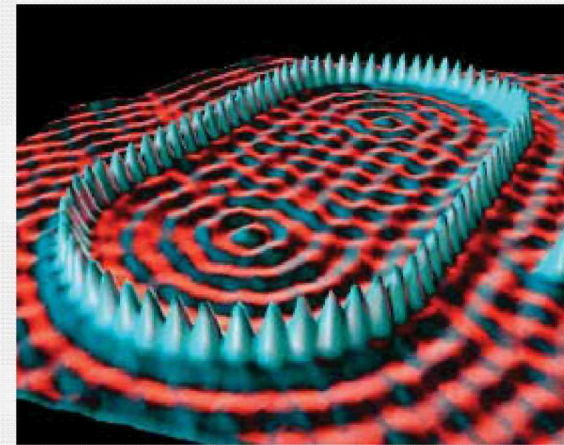
Michael Köhl



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# Impurities: why spoiling a clean system?

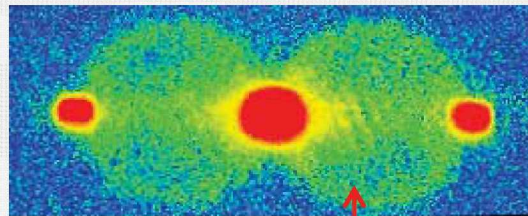
- Understanding real world systems
- Test & measurement:  
Impurities as probes and tools
- Transport experiments





# Transport experiments in cold atoms

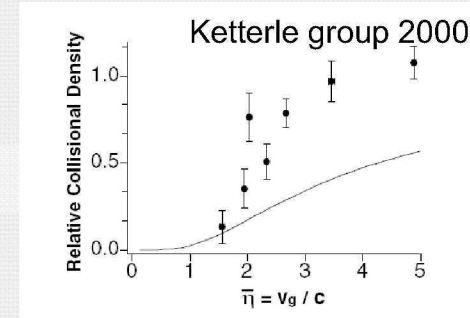
A simple transport experiment



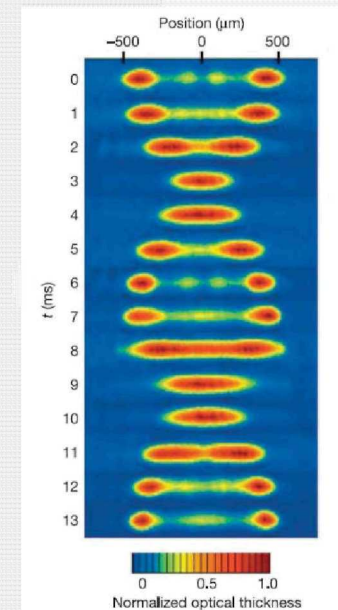
$-2\hbar k$        $0$        $+2\hbar k$

Scattered atoms with spherical (s-wave) symmetry

Three dimensions



One dimension



Weiss group 2006

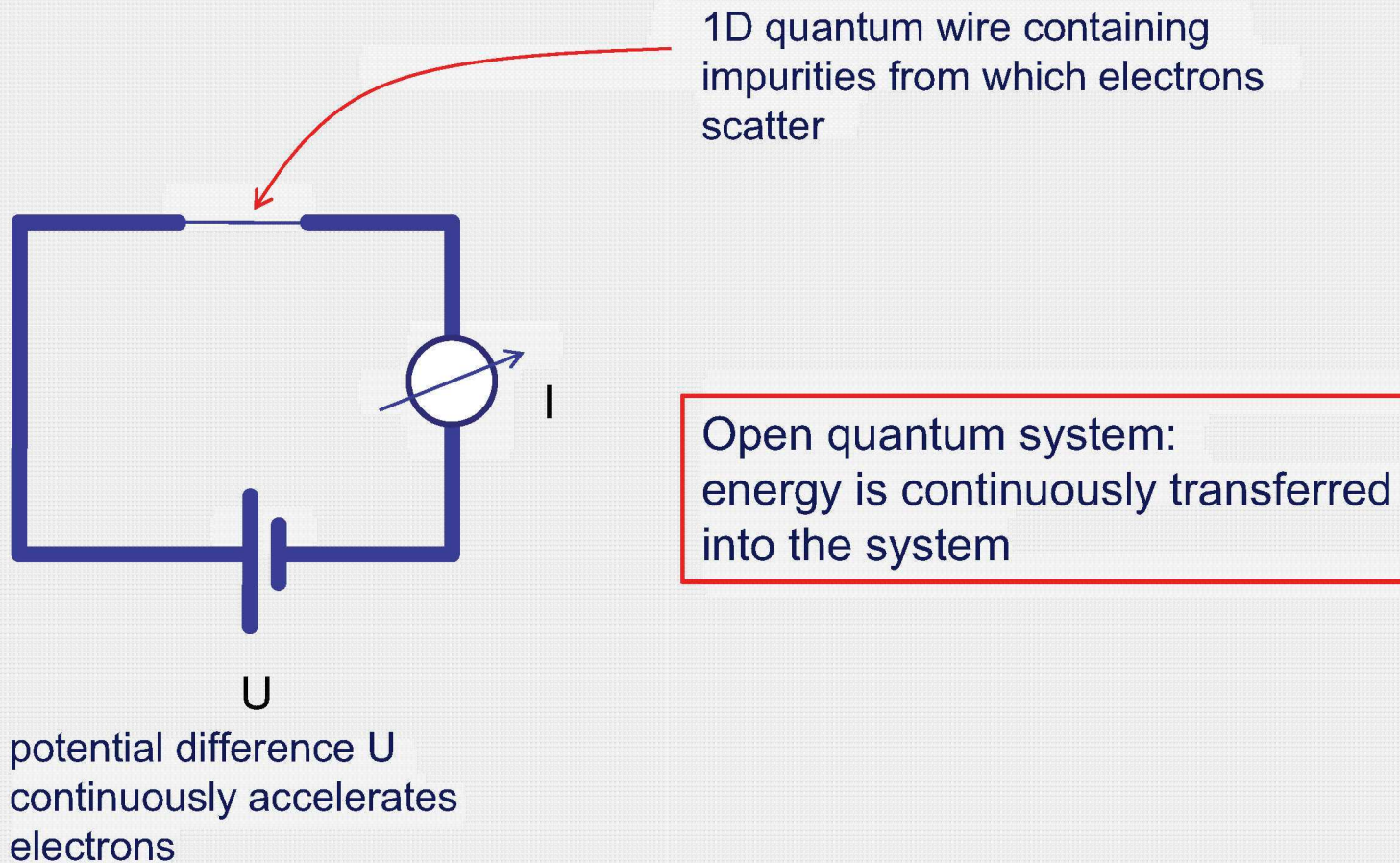
Other transport experiments: ETH, LENS, NIST, Orsay, Pisa, Stanford, ...



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# Transport in the solid state



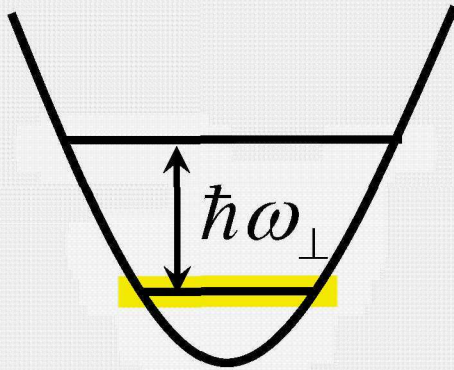
# Quantum transport in a strongly interacting 1D Bose gas





# What is a one-dimensional gas?

- transverse degrees of freedom are frozen out



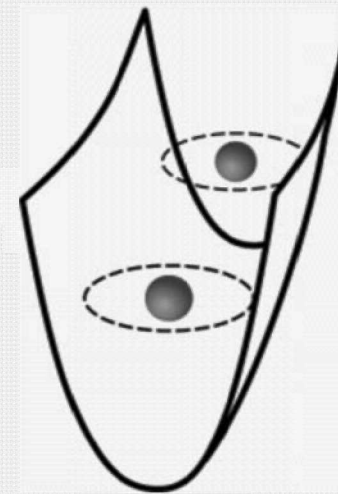
## Conditions for 1D

$$k_B T < \hbar\omega_{\perp}$$

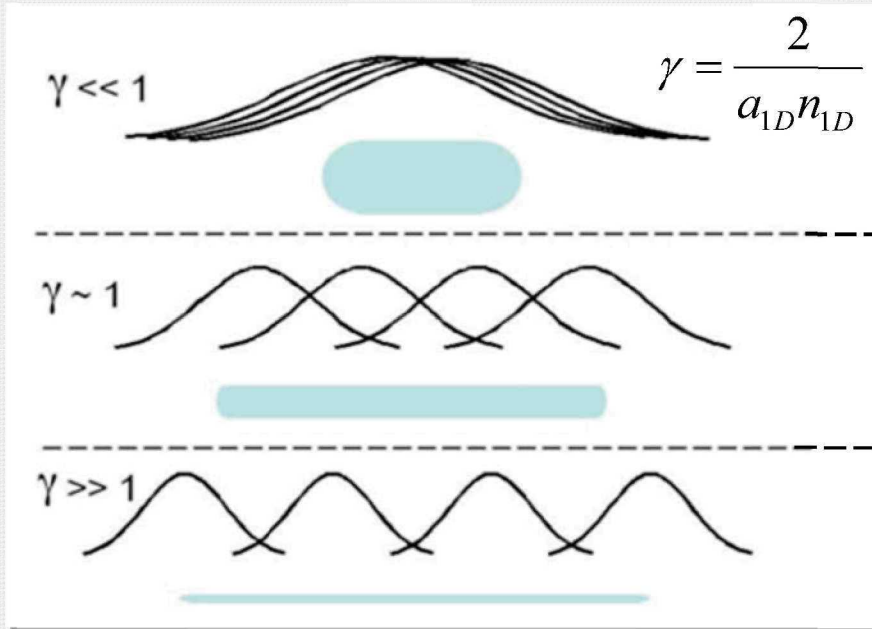
$$\text{Bosons: } \mu < \hbar\omega_{\perp}$$

$$\text{Fermions: } E_F = N \hbar\omega_z < \hbar\omega_{\perp}$$

- asymptotic scattering states are one-dimensional wave functions



# Regimes of degeneracy in 1D



weakly interacting Bose gas

$$\psi_{Bose}(r) = \prod_{i=1 \dots N} \psi_i(r); \quad mc^2 = \mu$$

crossover

Tonks-Girardeau gas  
("Fermionized Bosons")

$$\psi_{Bose}(r) = |\psi_{Fermi}(r)|$$

$$k_F = \pi n = mc / \hbar$$

1960:  $\gamma \rightarrow \infty$  limit solved by Girardeau

1963: Exactly solved for all values of  $\gamma$  by Lieb & Liniger

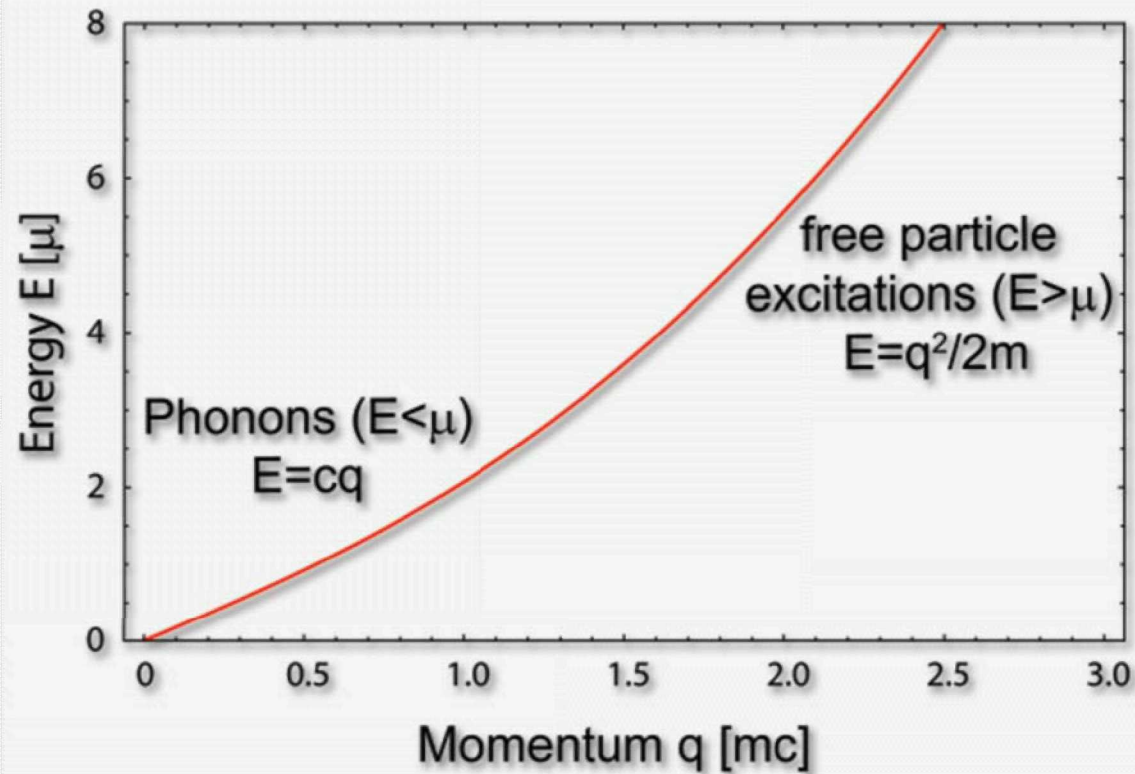
2003: 1D Bose gases first realized by Esslinger et al. (ETH Zürich).

2004: Tonks gas experimentally realized by Weiss et al. (Penn State) & Bloch et al. (Mainz)

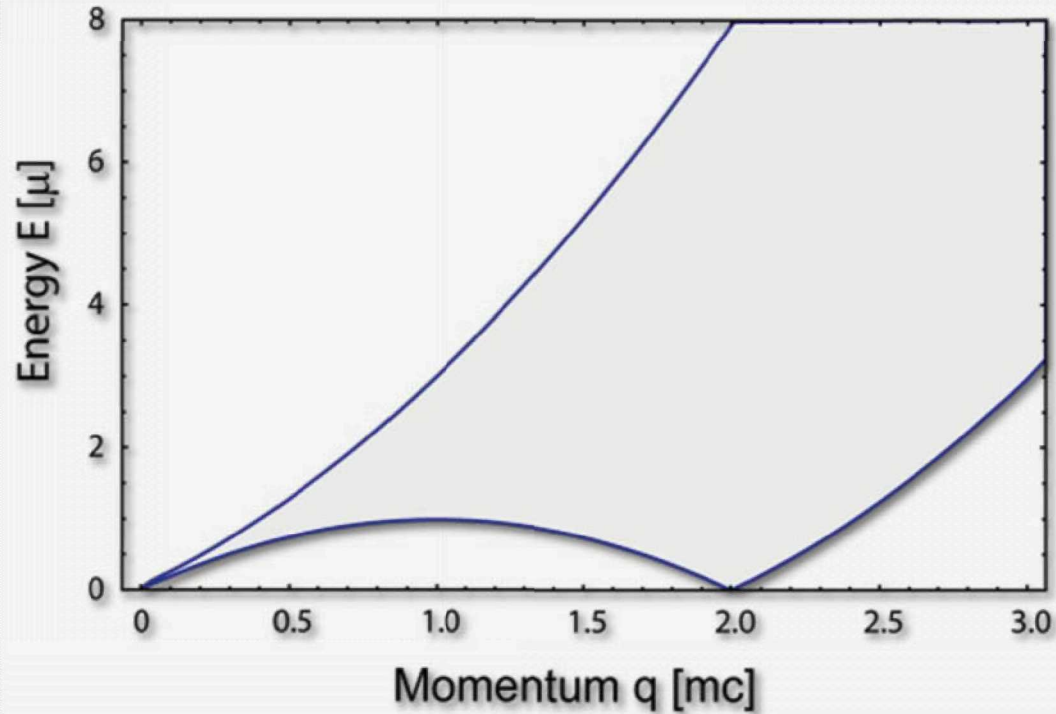


# Excitations in a weakly interacting Bose gas

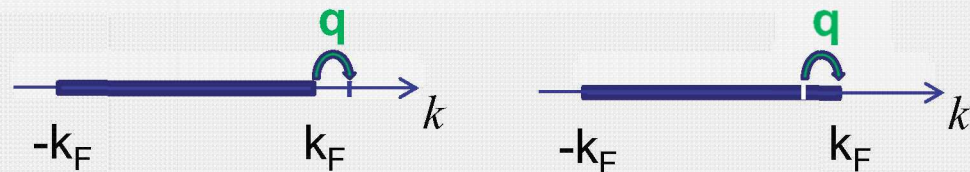
## Bogoliubov spectrum



# Excitations in a Tonks gas

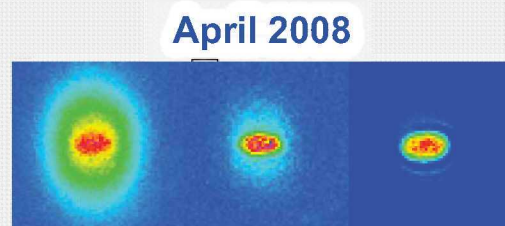


Two branches of excitations: “particle” excitations and “hole” excitations

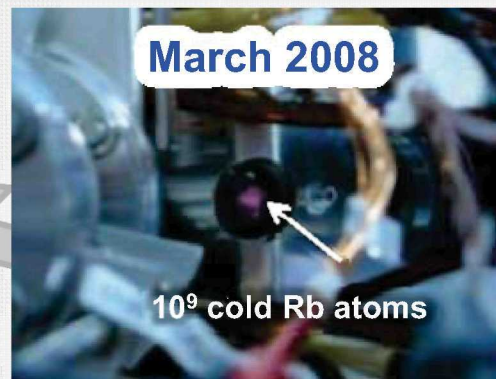




# Making a Bose-Einstein condensate



Bose-Einstein condensation





# Generating tight confining potentials

Induced electric dipole potential:

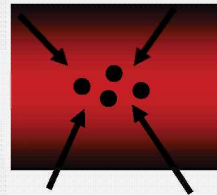
$$V = -\frac{1}{2}\alpha|E|^2$$

ac polarizability of the atom

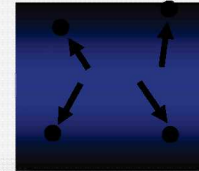
electric field of the laser

Two options:

$\omega_L < \omega_A$   
„red detuned“



$\omega_L > \omega_A$   
„blue detuned“



Optical lattice



$\lambda/2 = 380 \text{ nm}$

Energy scale:

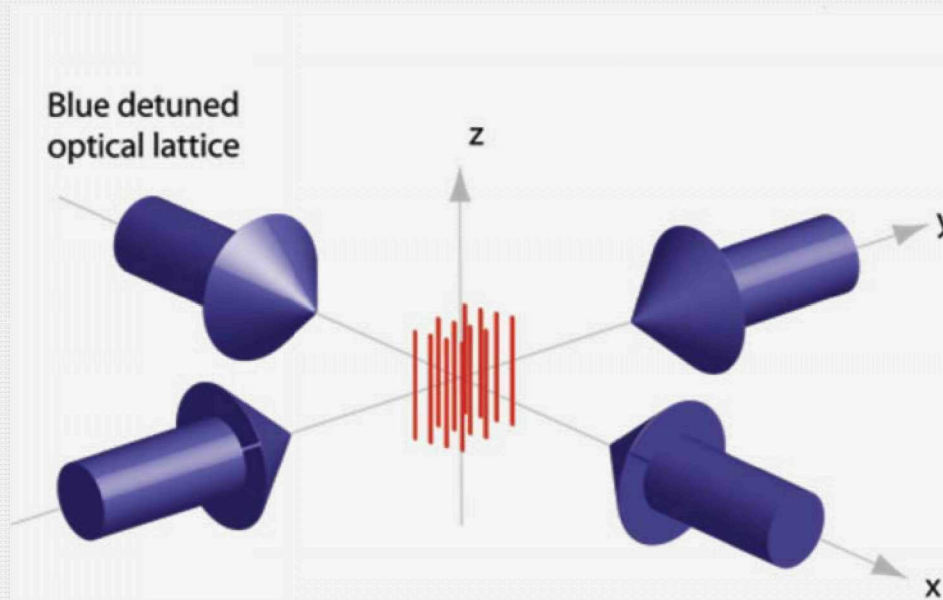
$$E_{rec} = \frac{\hbar^2 k^2}{2m}$$



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# Hybrid optical/magnetic trap



## Experimental parameters:

Atoms:  $^{87}\text{Rb}$  (bosons)

Wavelength of lattice: 764 nm

$\omega_x = \omega_y \leq 2\pi \cdot 65 \text{ kHz}$  (optical lattice)

$\omega_z = 2\pi \cdot 39 \text{ Hz}$  (magnetic trap)

$N < 120$  per tube

$0.5 < \gamma < 5$

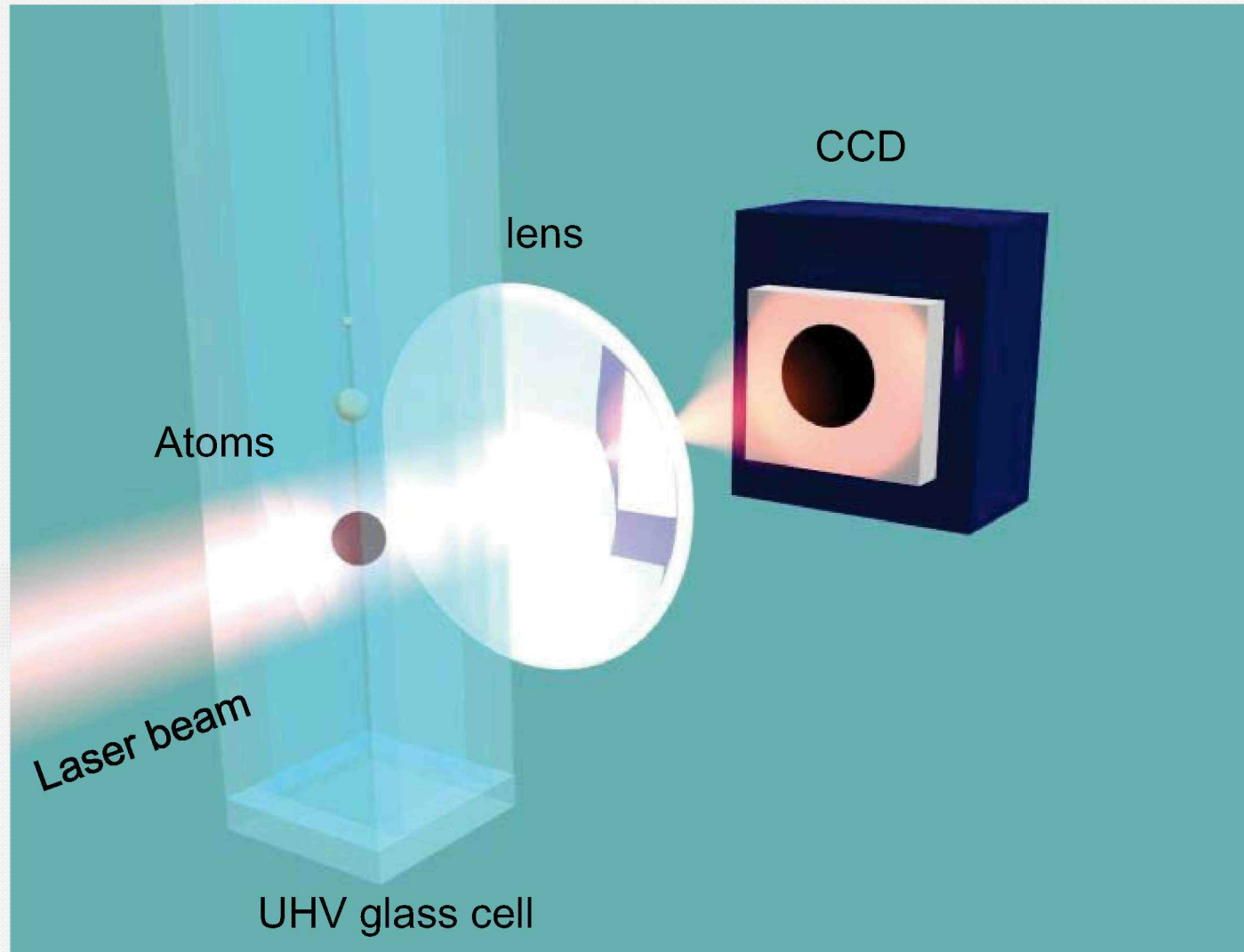
Other experiments in 1D: ENS, ETH, LENS, Mainz, MIT, NIST, Orsay, Penn State, Rice, Vienna ...



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# Detection

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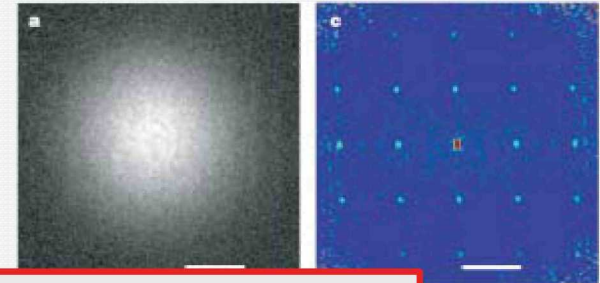




# More advanced detection techniques

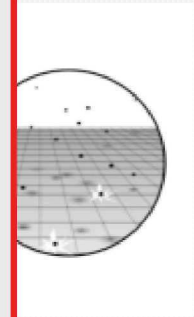
## Noise-correlation measurements

[Altman et al. PRA (2004); Bloch group (Mainz), Nature (2005 & 2006)]



Hank  
of m  
[Aspect

**high resolution *in-situ* measurements  
remain a challenge  
(the cloud is too small and dense)**

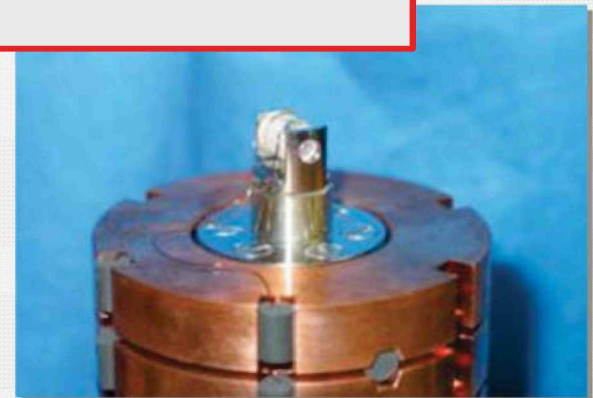


## Single atom counting by cavity QED

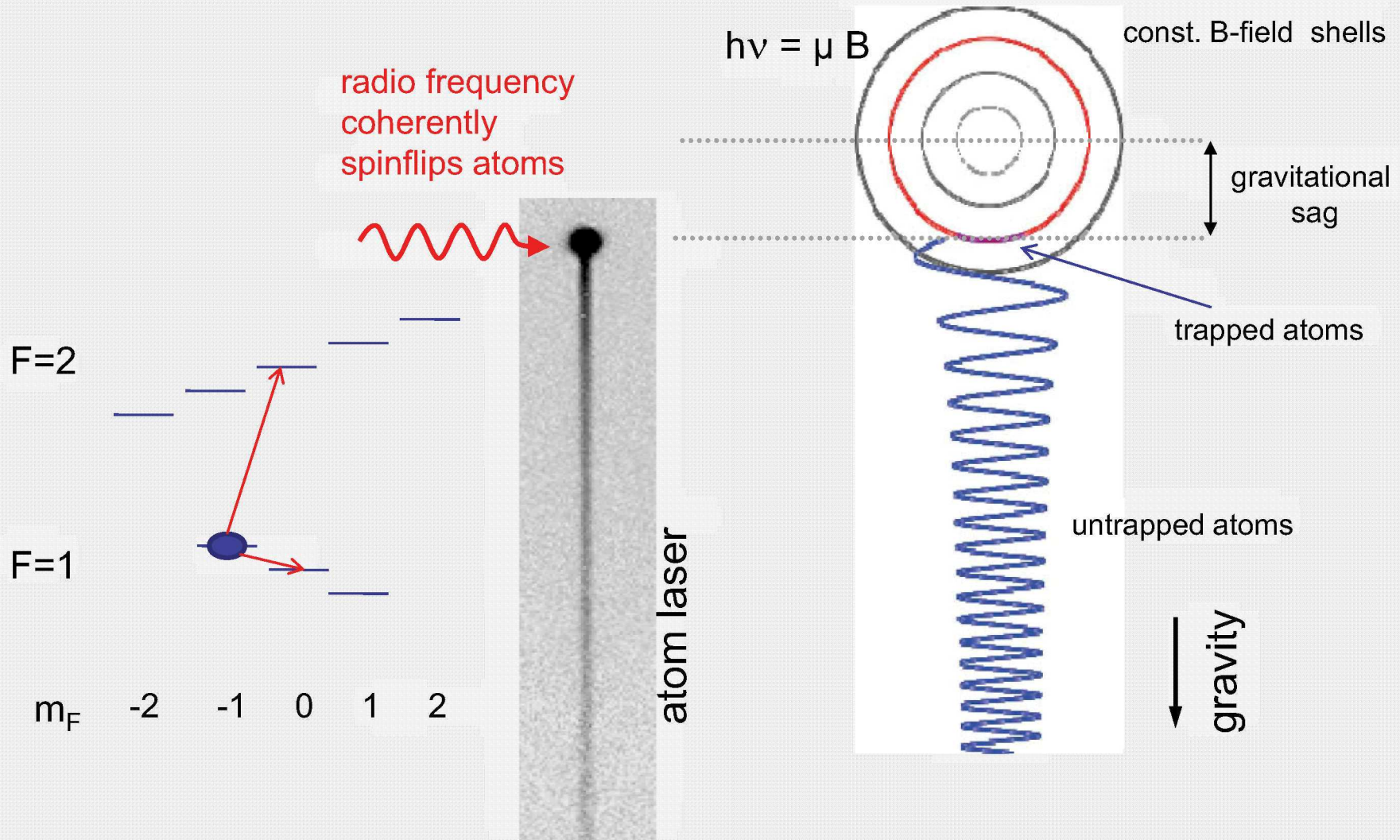
[A. Öttl, S. Ritter, M. Köhl, T. Esslinger, PRL (2005)]

S. Ritter, T. Donner, A. Öttl, M. Köhl, T. Esslinger, PRL (2007)

T. Donner, S. Ritter, T. Bourdel, A. Öttl, M. Köhl, T. Esslinger, Science (2007)].

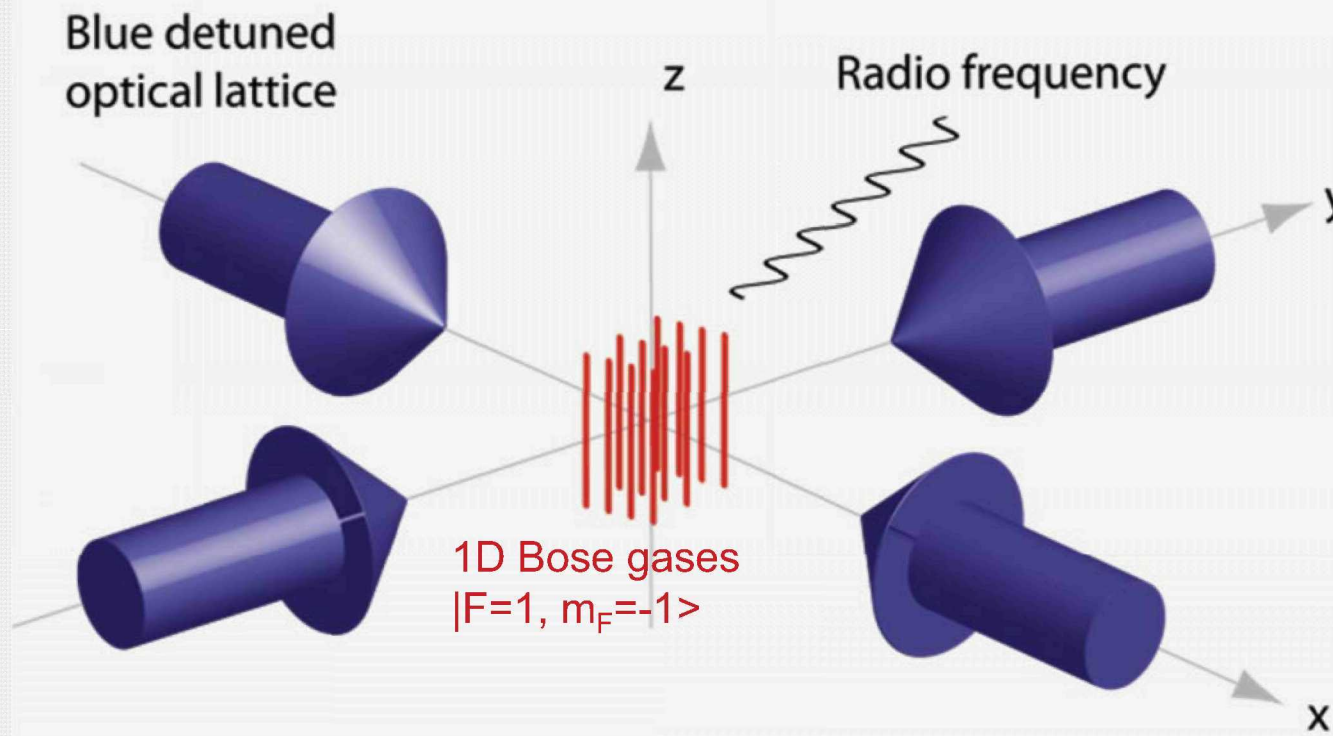


# Tomographic in-situ measurements





# Spatial addressing



Radio frequency resonance:  $|F=1, m_F=-1\rangle \rightarrow |F=1, m_F=0\rangle$   
at  $\hbar\nu_{\text{RF}} = g_F\mu_B B(x,y,z) \approx \mu_B B(z)/2$

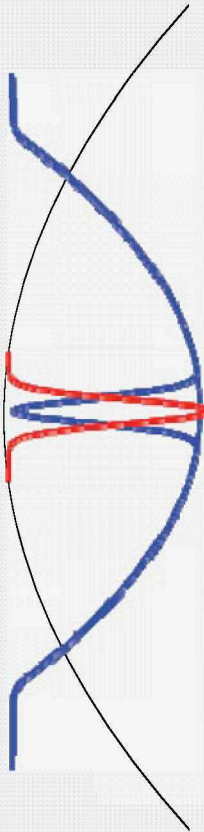


# Generation of spin impurities

$$|F=1, m_F=-1\rangle$$
$$V = m/2 \omega_z^2 z^2 - m g z$$

$$|F=1, m_F=0\rangle$$
$$V = -m g z$$

quick transfer  
(RF  $\pi$ -pulse, 200  $\mu\text{s}$ )

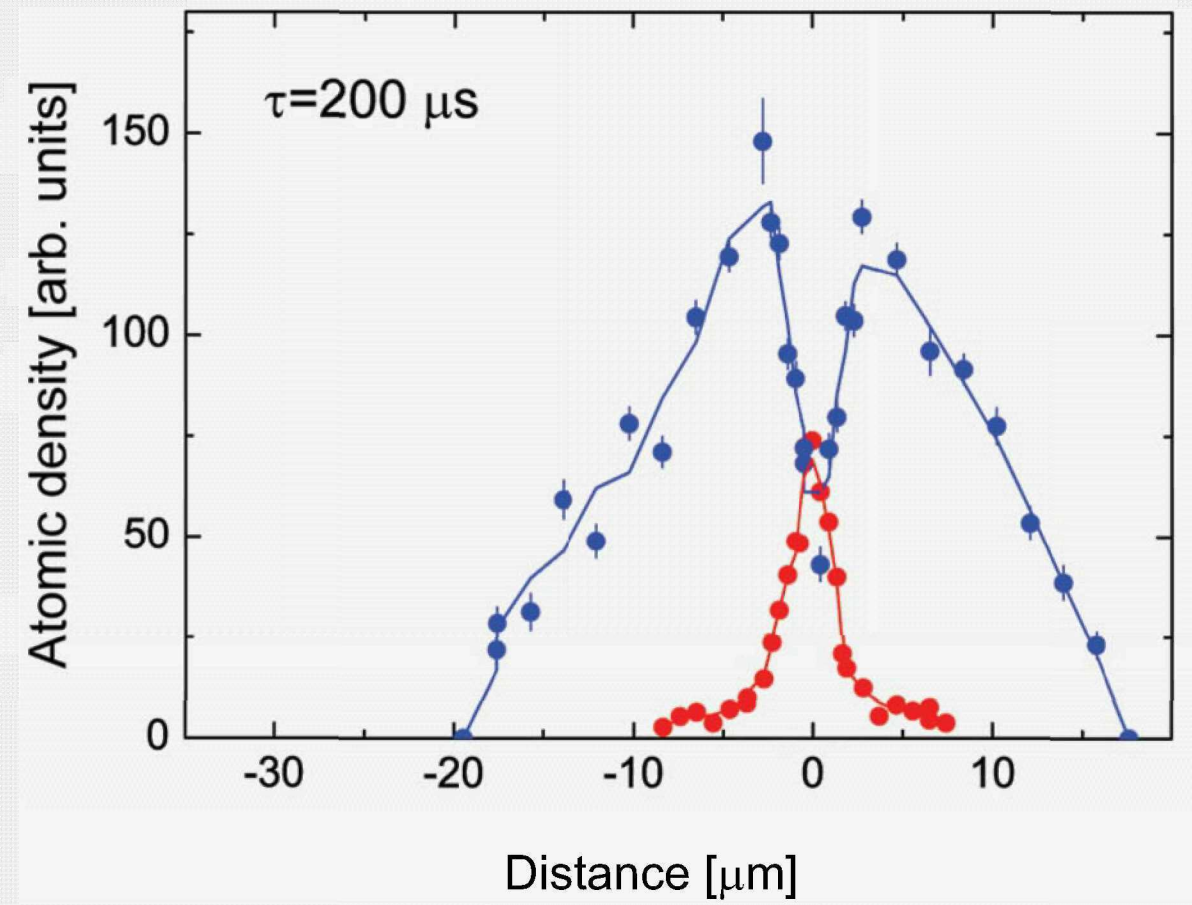
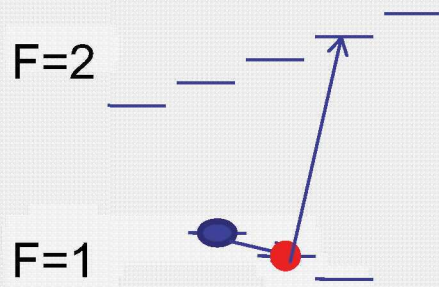
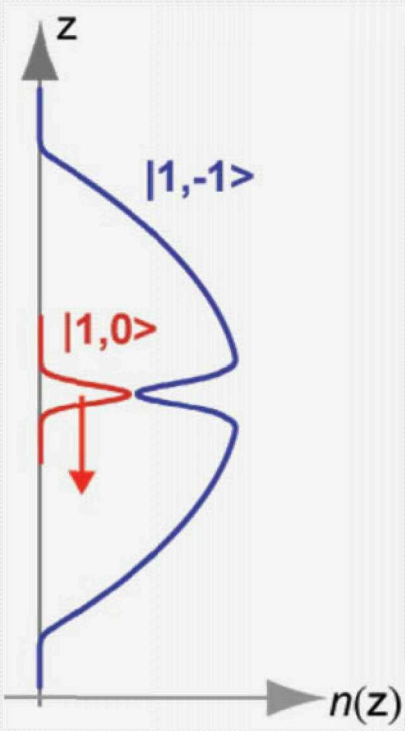


- width of impurity wave packet:  
2.5  $\mu\text{m}$  ( $\approx 3$  atoms)
- same transverse confinement:  
propagation of impurities is  
purely one-dimensional
- same scattering lengths:  
 $a_{-1,-1} \approx a_{-1,0} \approx a_{0,0}$
- accelerated impurity breaks  
integrability of the 1D Bose  
gas  $\rightarrow$  **interesting dynamics**

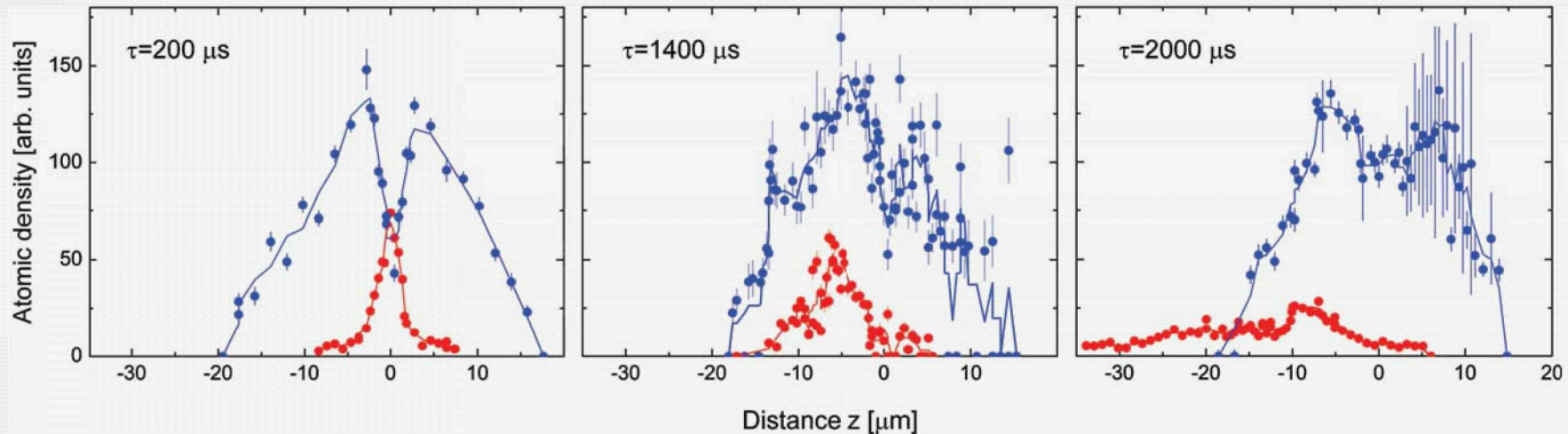




# In situ detection of the spin wave packet



# Time evolution



- strong interaction-induced dynamics
- significant back action of the impurity onto the majority component
- open quantum system: impurity atoms can transfer continuously energy into trapped component by collisions

S. Palzer, C. Zipkes, C. Sias, M.K., arXiv:0903.4823



# Dynamic structure factor

Scattering rate of an impurity (Fermi's golden rule):

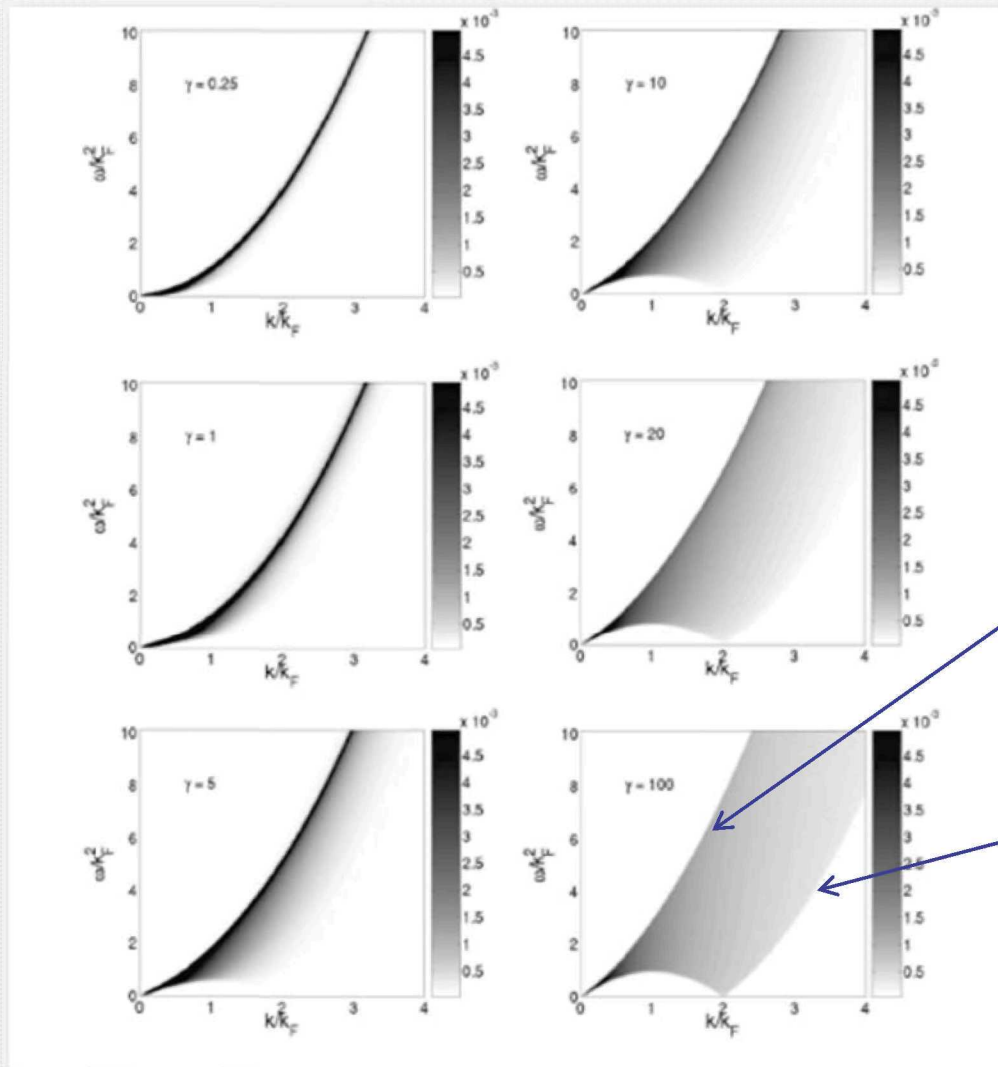
$$\Gamma \propto \int dq d\omega S(\omega, q) \delta(\varepsilon(k_i) - \varepsilon(k_f) - \hbar\omega(q))$$

$S(q, \omega)$ : dynamic structure factor

$k_i, k_f$ : initial and final momentum of the impurity

$\omega(q)$ : excitation spectrum of the gas

# Dynamic structure factor in 1D



$$E_{particle}(q) = \left| \frac{\hbar k_F}{m} q + \frac{q^2}{2m} \right|$$

$$E_{hole}(q) = \left| \frac{\hbar k_F}{m} q - \frac{q^2}{2m} \right|$$

Dynamic structure factor calculation:  
Brand & Cherny, PRA (2004);  
Caux & Calabrese, PRA (2006).



# Collision rate and energy dissipation

For equal masses:  
impurities move collisionless through a superfluid **and** a Tonks-Girardeau gases for  $v < c$ .

Collision rate ( $v > c$ )

$$\Gamma = \begin{cases} \frac{\hbar^2 n_{1D}}{m^2 a_{1D}^2 v} & \text{weakly interacting Bose gas} \\ \frac{\hbar n_{1D}}{2m a_{1D}^2 k_F} \ln \left( \frac{k_i / k_F + 1}{k_i / k_F - 1} \right) & \text{Tonks - Girardeau gas} \end{cases}$$

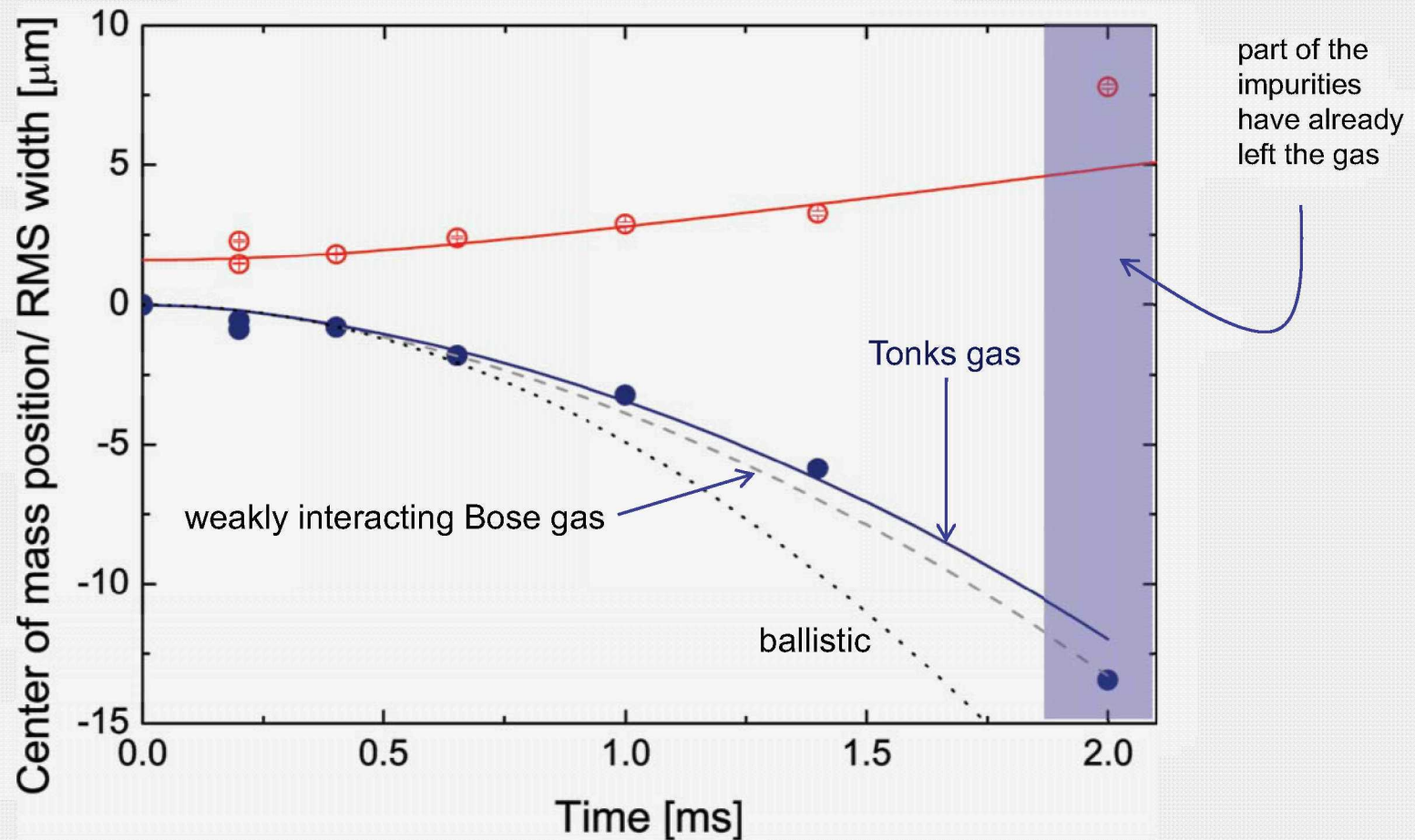
Energy dissipation ( $v > c$ )

$$\dot{E} = \begin{cases} \frac{\hbar^2 n_{1D}}{m a_{1D}^2} \frac{v}{2} \left( 1 - \left( \frac{c}{v} \right)^4 \right) & \text{weakly interacting Bose gas} \\ \frac{\hbar^2 n_{1D}}{m a_{1D}^2} \frac{v}{2} & \text{Tonks - Girardeau gas} \end{cases}$$

**constant force  
≈ 50% of gravity**

for heavy impurities: Astrakharchik & Pitaevskii, Davis et al., ...

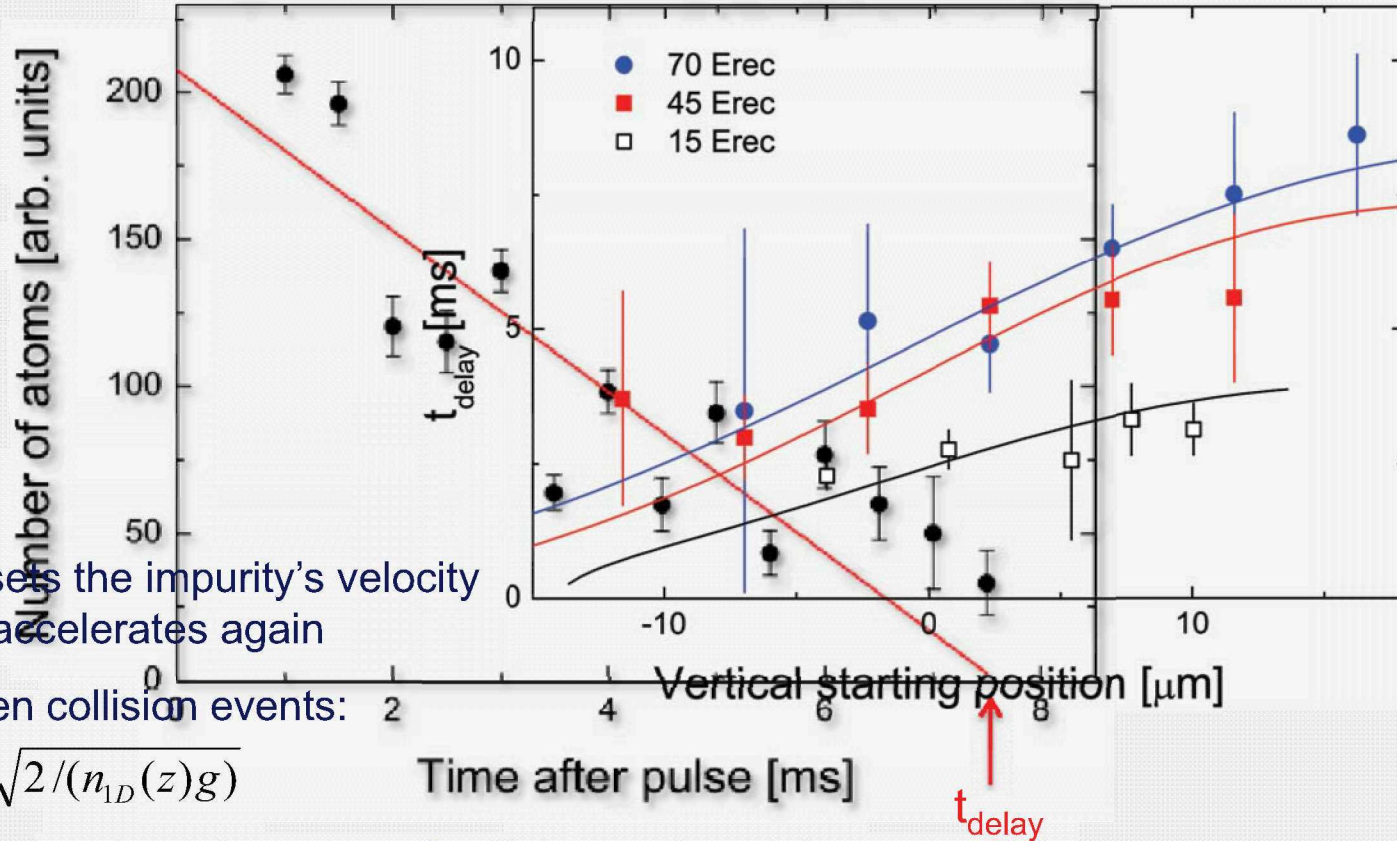
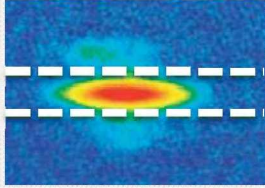
# Center-of-mass motion of the impurities



S. Palzer, C. Zipkes, C. Sias, M.K., arXiv:0903.4823



# Release measurement



## Simple model

Every collision resets the impurity's velocity to 0, then gravity accelerates again

Mean time between collision events:

$$t_{coll} \approx \sqrt{2/(n_{1D}(z)g)}$$

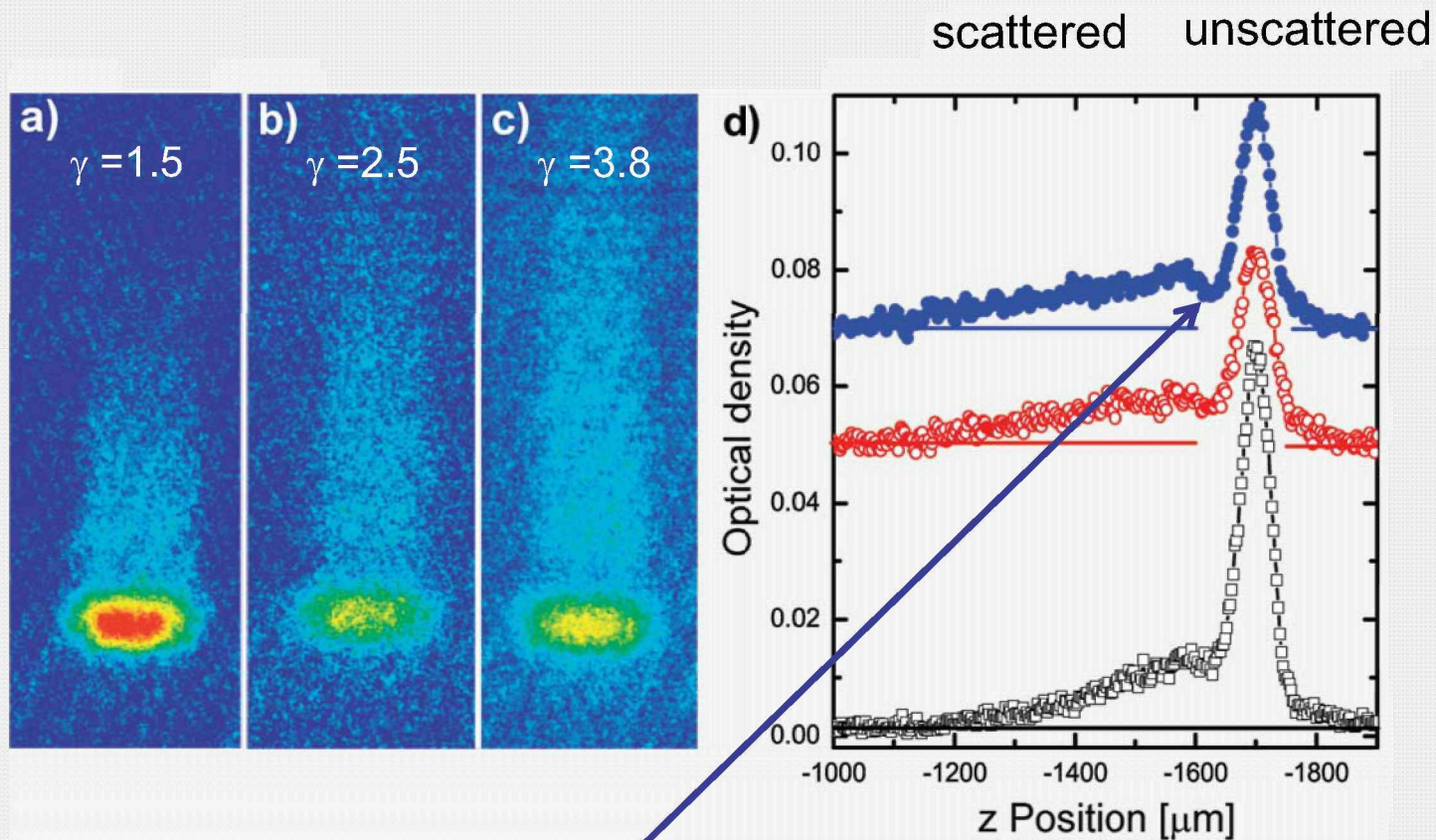
Time delay accumulated: total number of collisions x time delay per collision

$$t = \int_{-R}^{z_0} dz n_{1D}(z) \Gamma(z) t_{coll}^2$$

S. Palzer, C. Zipkes, C. Sias, M.K., arXiv:0903.4823



# “Far field” distribution of the impurities

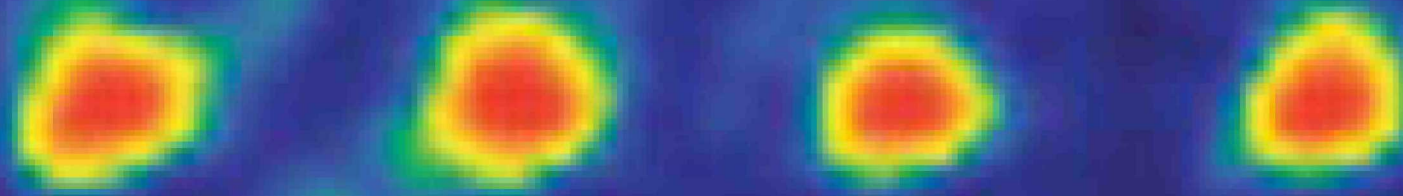


- Fermionization?
- Enhancement of multiple collision events due to strong interactions?
- ?

S. Palzer, C. Zipkes, C. Sias, M.K., arXiv:0903.4823



**Towards immersing charged impurities  
into a Bose-Einstein condensate**



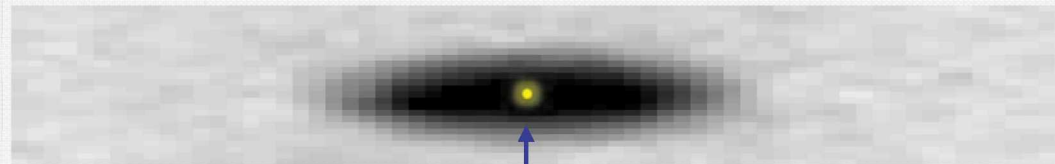
# A new hybrid system: Atoms and ions

## Quantum technology

- Cooling ions by superfluid immersion
- Ion as scanning probe

## Fundamental physics

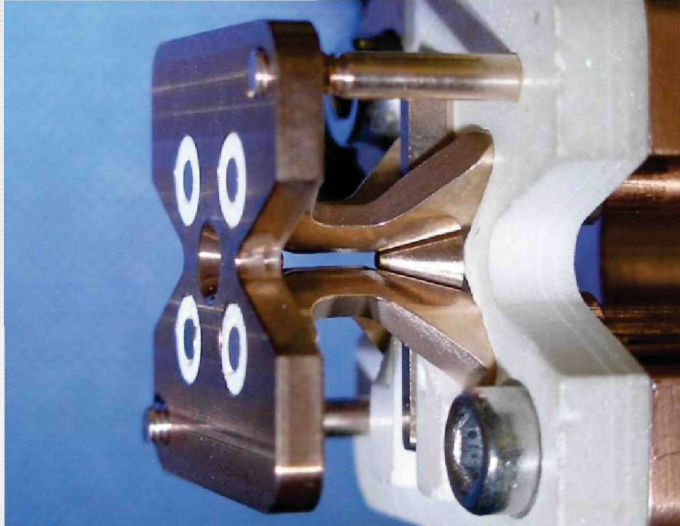
- Ultracold atom-ion interactions
- Ions provide tunable nano-potential



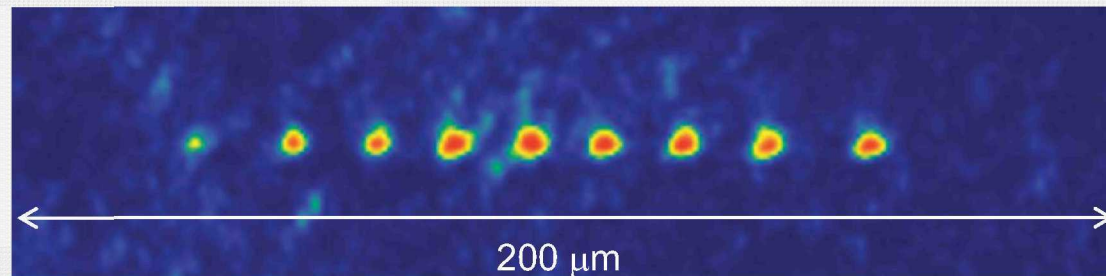
position accuracy  
of the ion: <10 nm



# Ion crystals of $^{174}\text{Yb}^+$



- Linear Paul trap with 0.8 mm spacing between electrodes
- Axial trap frequency:  $\omega_z = 2\pi \cdot 45 \text{ kHz}$   
Radial trap frequency:  $\omega_{\perp} = 2\pi \cdot 1 \text{ MHz}$
- Preparation of a deterministic number of impurities



One-dimensional Coulomb crystal of singly charged ions



# Summary

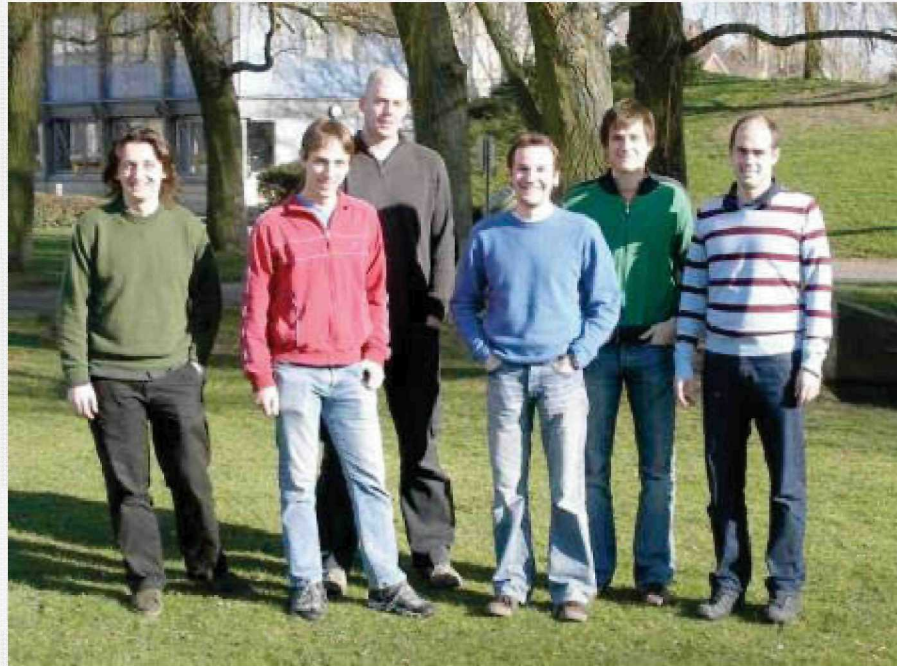
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- Quantum transport in a strongly interacting Bose gas with an accelerated impurity
- High resolution tomography
- Strong dynamics and back action of the impurity
- Work towards deterministic implantation of impurities is on the way



# Thanks!

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Carlo Sias (Postdoc), Christoph Zipkes (PhD), Stefan Palzer (PhD),  
Michael Feld (PhD), Bernd Fröhlich (PhD), M.K.

[www.quantumoptics.eu](http://www.quantumoptics.eu)

**Postdoc position available.**

£££: EPSRC, University of Cambridge, Herchel-Smith Fund