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International Centre for Theoretical Physics**



**2030-20**

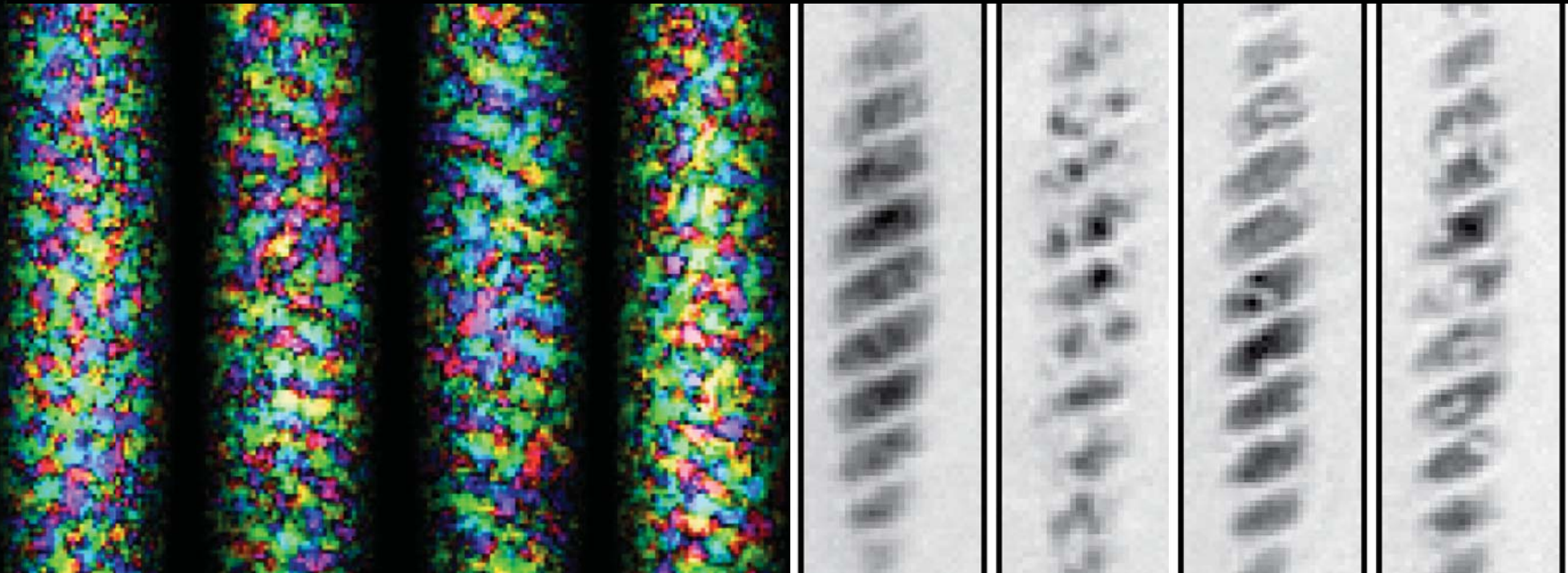
**Conference on Research Frontiers in Ultra-Cold Atoms**

*4 - 8 May 2009*

**Evidence for supersolid behavior in a spin-1 Rubidium gas**

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# Evidence for supersolid behavior in a spin-1 rubidium gas



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UC Berkeley

Conference on Research Frontiers in Ultra-Cold Atoms  
ICTP May 2009

## Outline

### ● To read

◆ Chan specific heat measurement 2007

◆ ⇒ Yi and Pu, PRL 97, 020401 (2006); Kawaguchi, Saito, Ueda PRL 97, 130404 (2006)

◆ ⇒ Pfau, Santos, Lewenstein, others:  $^{52}\text{Cr}$  ( $6 \mu_B$ )  
⇒ Jin, Ye (JILA): polar molecules ( $>137 \mu_B$ )

◆ Barnett, Turner, Demler  
[PRL **97**, 180412 (2007)]

● Lamacraft, PRA 77, 062622 (2008),  
Cherng, et al., PRL 100, 180404 (2008)

# Outline

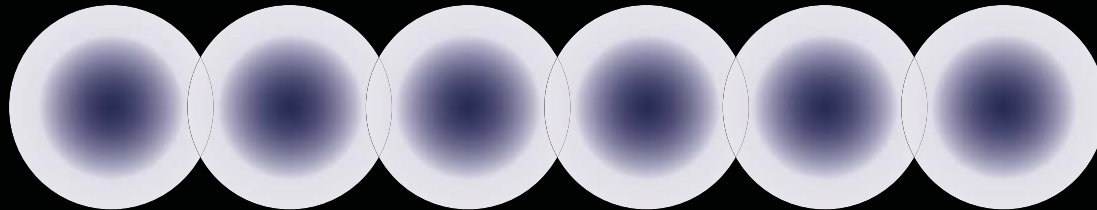
- Rb  $F=1$  phase diagram (slides leading up to it)
- How to image magnitization (experimental interlude)
- 3 experiments
  - ◆ Wind up experiment (following experimental observation)
  - ◆ Evaporation; "121"
  - ◆ Evaporation "111"
- Probing coherence of these gases:
  - ◆ Looks like a BEC in TOF: furthermore if you look closely we see phase fluctuations and vorticies; phase defects show up in TOF.
  - ◆ From original interference experiment to Heterodyne AI
  - ◆ Heterodyne Atom interferometry
  - ◆ Applying this probe to scalar system; Imaging Resolution limits measurement
  - ◆ Mean field chirp
  - ◆ Short distance measurements, interpretation.
- Current work; experimental upgrade, longer equilibration time, different geometries, better quantification of crystal, cancel expansion of gas.

## Supersolid?

particles "localized" at lattice sites

⇒ translational symmetry breaking

real-space regular structure (density, magnetization, ...)



but particles may be simultaneously "delocalized": superposition of locations

$$\Psi = (|\text{site 1}\rangle + |\text{site 2}\rangle + |\text{site 3}\rangle + \dots)^N$$

delocalization may lead to superfluidity

⇒ long-range phase coherence

"off-diagonal long-range order"

some number uncertainty per site ⇒ phase certainty at each site

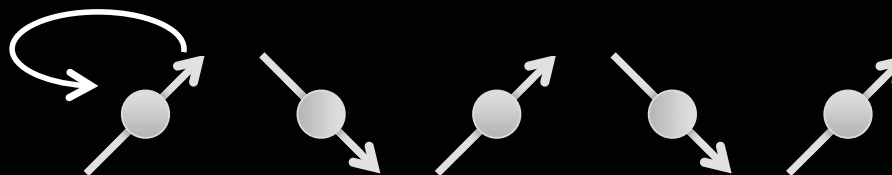
First suggestions: [Andreev & Lifshitz, Reatto, Chester, Leggett ] ~1970

theory:  
ingredients, characteristics,  
variants, candidates

experiments:  
solid  $^4\text{He}$   
2D helium films  
solid  $\text{H}_2$   
"Quantum crystals"

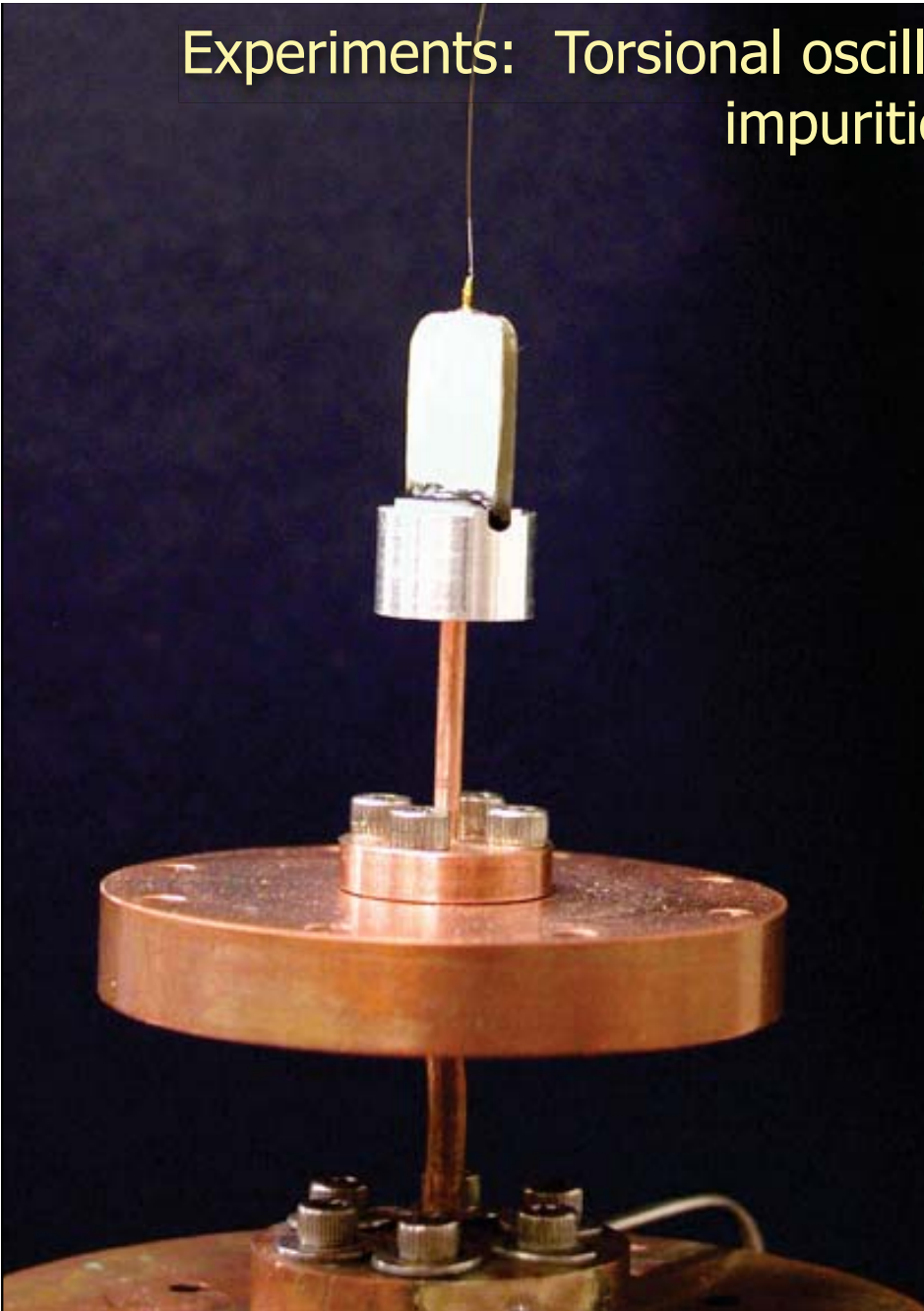
- Bosons with long-range interactions
  - ◆ Pomeau & Rica (1994): start from fluid and increase interactions, see rotons and instability (cf Cherng & Demler)
- "Lattice supersolids": Bosons on lattice
  - ◆ Liu & Fisher (1972) [also Bruder, Fazio, Schon; van Otterlo, Wagenblast; Batrouni, Scalettar; ...]
  - ◆ Bose-Hubbard models, related to JJ arrays, cold atoms
- "Spin supersolids": Quantum magnets
  - ◆ Fisher & Nelson (1974) + lots of work 90's onwards: "spinflop" = "boson"

XY: SF phase

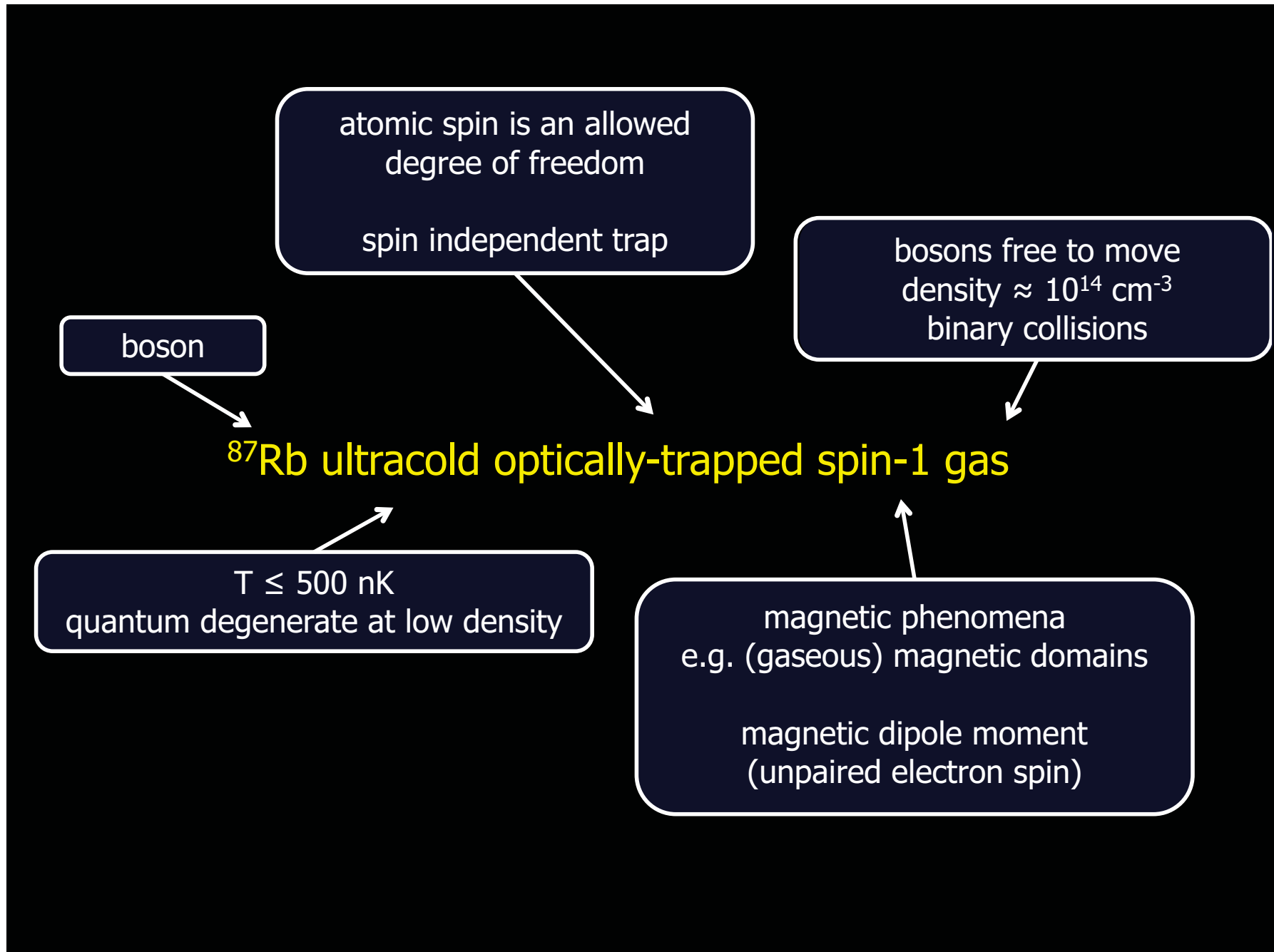


Z: solid

## Experiments: Torsional oscillators, vycor, dislocations, impurities...



- Kim & Chan (2004 + on)
  - ◆ non-classical rotational inertia – superfluid decouples from motion
  - ◆ strongly affected by annealing... (Rittner & Reppy, Chan, ...)
- Anomalous shear modulus
  - ◆ role of dislocations... (Day & Beamish 2007)
- $\Delta$  specific heat (Lin, Clark & Chan 2007)
- "Unusual mass transport" in solid (Ray & Hallock 2008)



atomic spin is an allowed  
degree of freedom  
spin independent trap

bosons free to move  
density  $\approx 10^{14} \text{ cm}^{-3}$   
binary collisions

boson

**$^{87}\text{Rb}$  ultracold optically-trapped spin-1 gas**

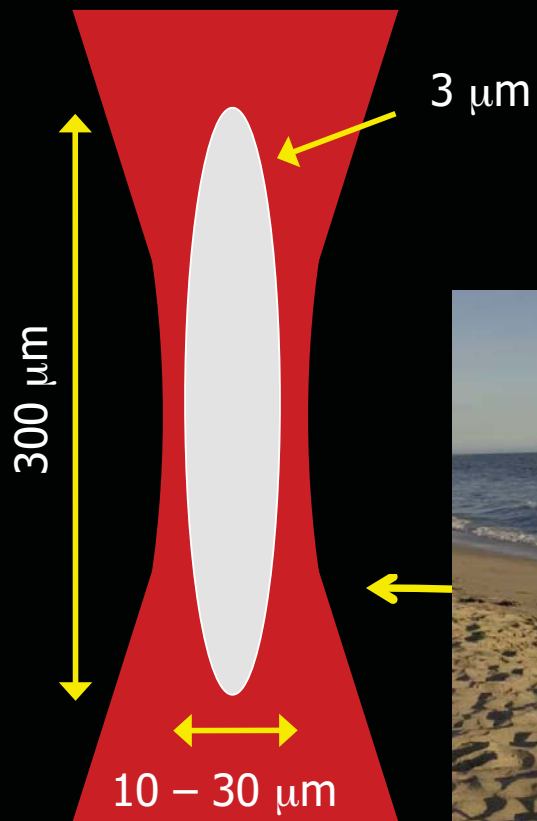
$T \leq 500 \text{ nK}$   
quantum degenerate at low density

magnetic phenomena  
e.g. (gaseous) magnetic domains  
magnetic dipole moment  
(unpaired electron spin)

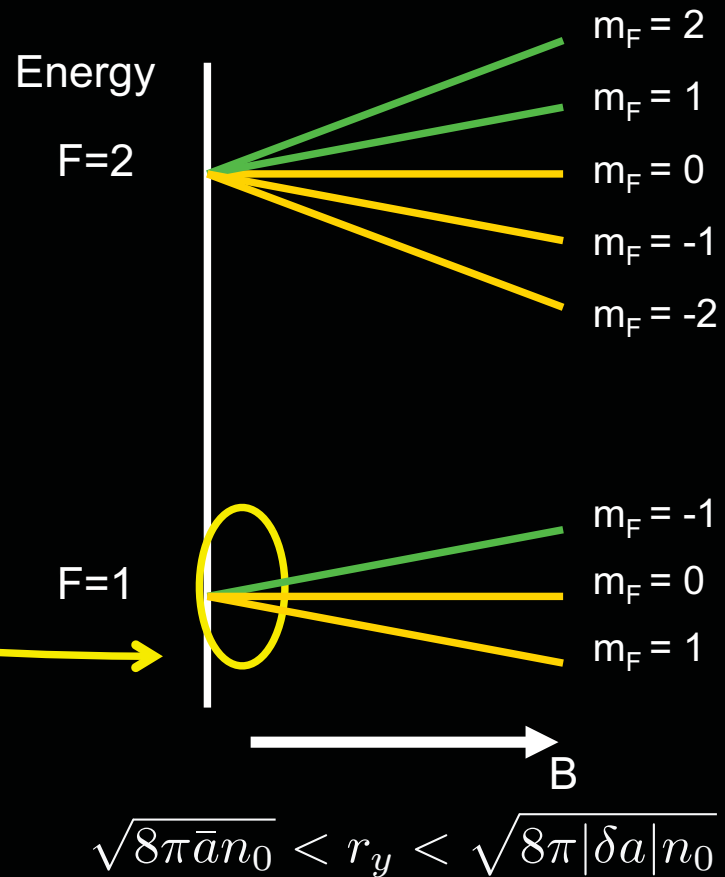


# Optically trapped spin-1 gas

$N \geq 2 \times 10^6$  atoms  
 $T \geq 50$  nK



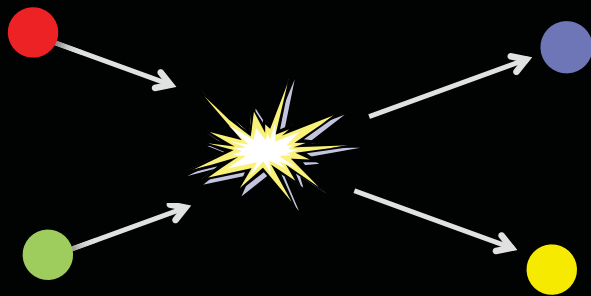
geometry  $\approx$  surfboard



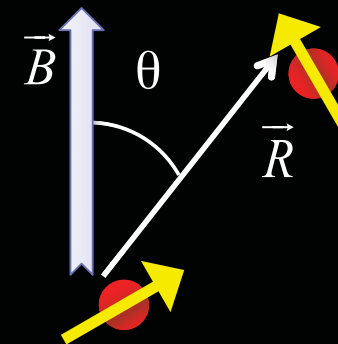
2D spin dynamics  
 3D condensate

# Interatomic interactions

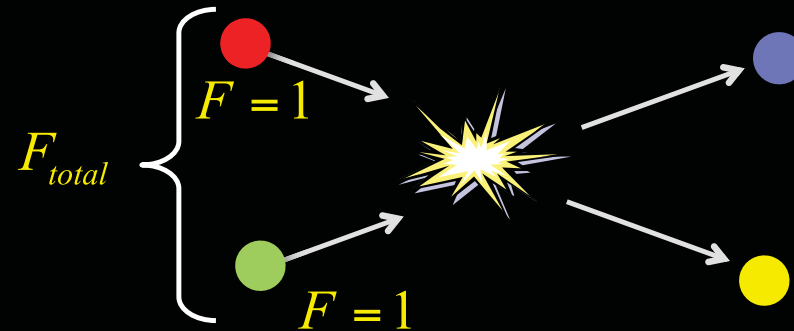
contact interactions



magnetic dipolar interactions

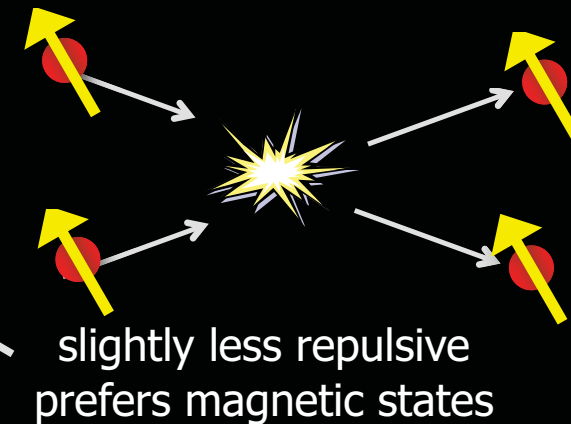


# Interatomic interactions



- Low energy
  - ◆ only s-wave collisions occur; characterized by scattering length
- Rotational symmetry: interactions depend on total spin, not its orientation

$F_{total} = 0$	$F_{total} = 2$
$^{87}\text{Rb}: a_0 = 5.39 \text{ nm}$	$a_2 = 5.31 \text{ nm}$
interactions are repulsive	



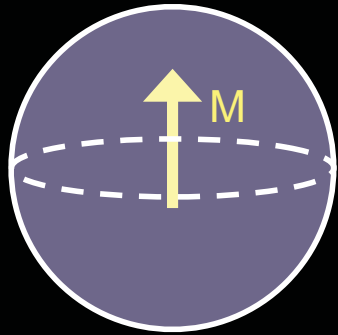
in dense BEC:

$$\mu = c_0 n \approx 2000 \text{ Hz, or } 100 \text{ nK}$$

$$\Delta\mu = -|c_2| n \langle \vec{F} \rangle^2 \approx 10 \text{ Hz, or } 0.5 \text{ nK}$$

# Dipolar interactions: magnetism in a quantum fluid

## "Quantum ferrofluids"



self-field:

$$B \approx \mu_0 M = (\mu_0 g_F \mu_B) n$$

@  $3 \cdot 10^{14} \text{ cm}^{-3}$

17  $\mu\text{G}$

energy per particle:

$$U_d = (\mu_0 g_F^2 \mu_B^2) n$$

$h \times 12 \text{ Hz}$

### Comparison to other energy scales:

◆ total interaction energy:  $\mu \sim h \times 2000 \text{ Hz}$

⇒ Pfau, Santos, Lewenstein, others:  $^{52}\text{Cr}$  ( $6 \mu_B$ )

⇒ Jin, Ye (JILA): polar molecules ( $>137 \mu_B$ )

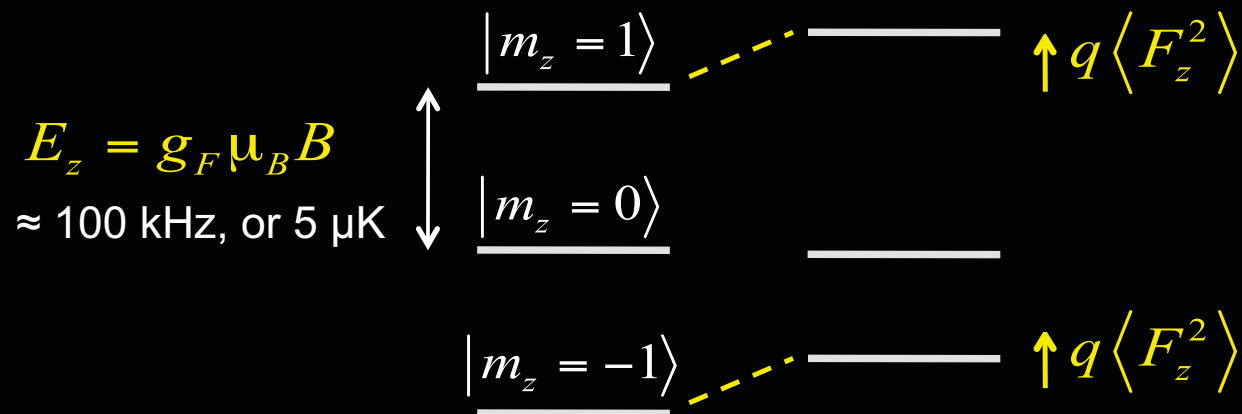
◆ spin-dependent interaction energy:  $\mu \sim h \times 12 \text{ Hz}$

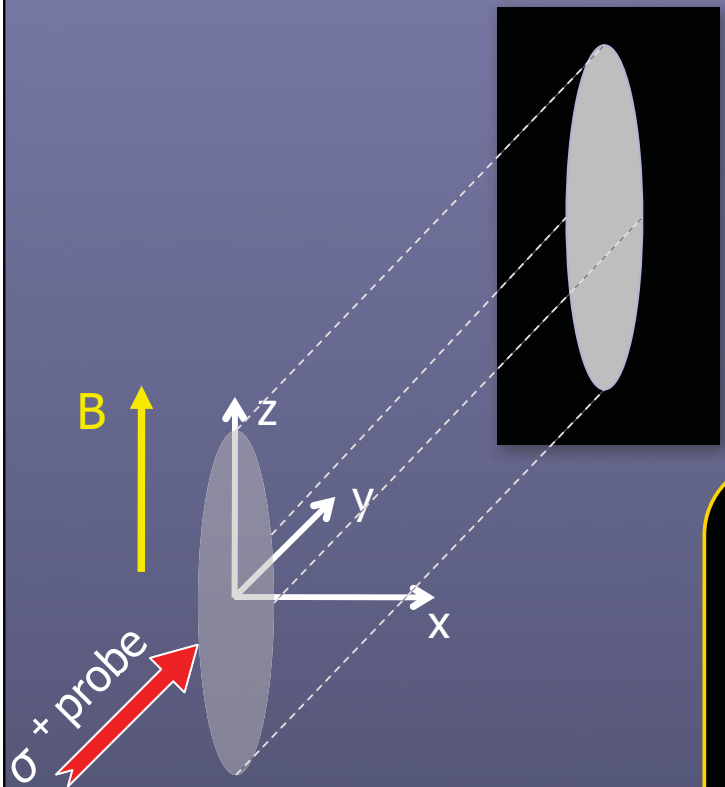
⇒ Yi and Pu, PRL 97, 020401 (2006); Kawaguchi, Saito, Ueda PRL 97, 130404 (2006)

⇒  $^{87}\text{Rb}$  is an essentially dipolar spinor quantum fluid

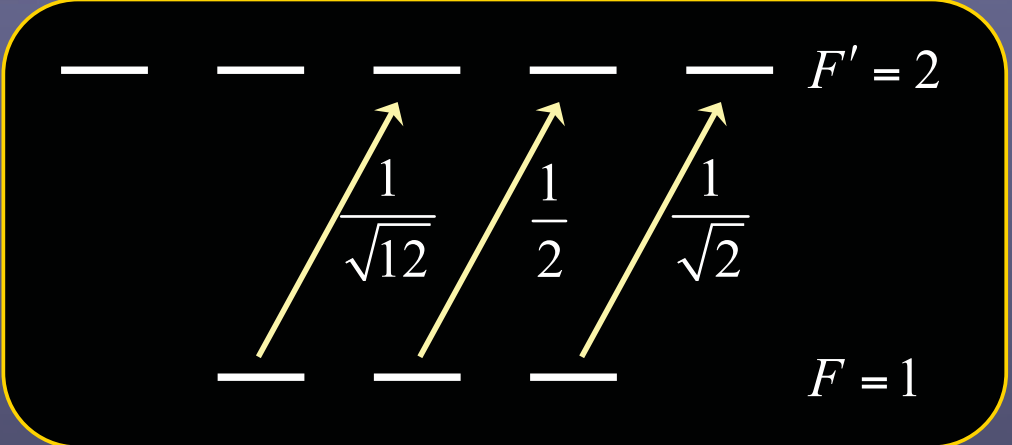
## Effects of magnetic field

- linear Zeeman shift
  - ◆ Transverse coherences rapidly precess
- quadratic Zeeman shift:  $q$ 
  - ◆  $m=0$  condensate favored at high  $q$





phase-contrast image;  
dispersive (minimally destructive)



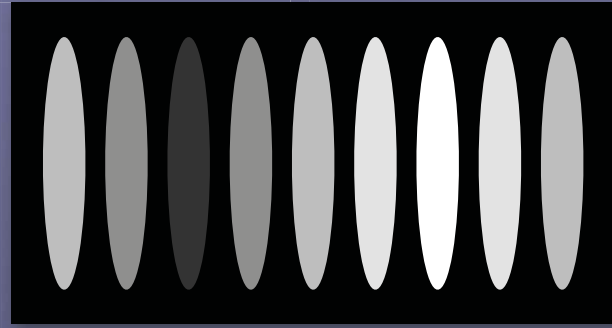
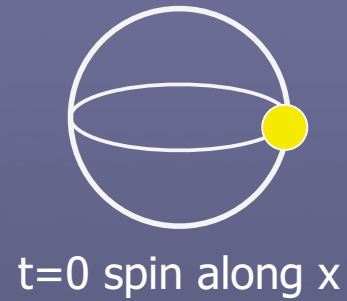
signal  
(normalized # photons/pixel)

$$S \propto 1 + \frac{\gamma}{\Delta} \sigma_0 \left[ s_0 n_{2D} + s_1 n_{2D} \langle F_y \rangle + \dots \right]$$

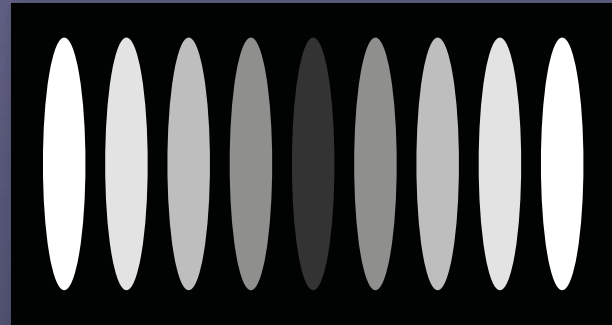
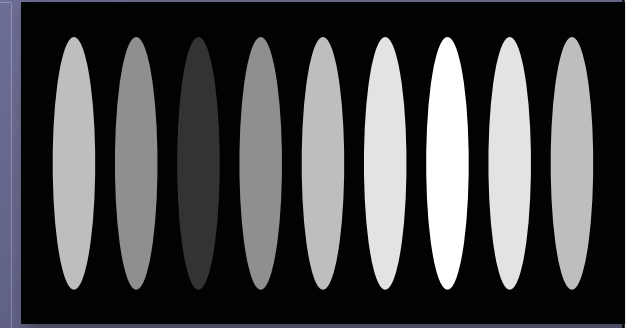
small

# Measuring the vector spin

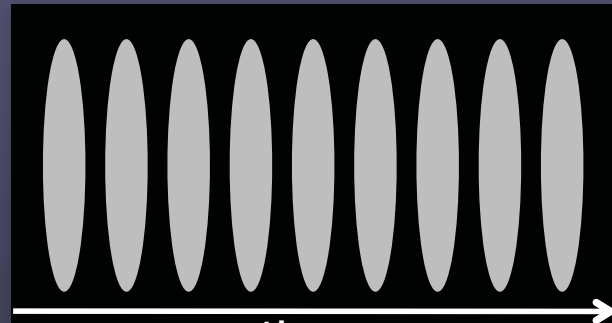
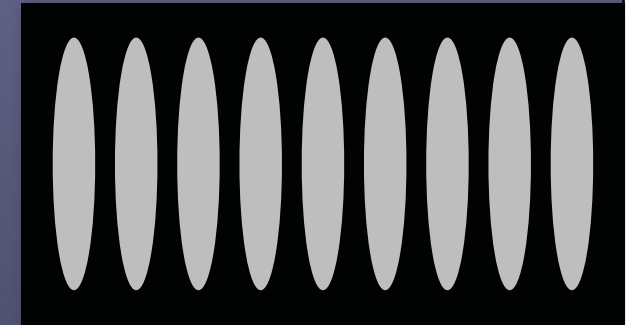
- Larmor precession: continuous spin rotation about z-axis
- resonant RF pulses: a  $\pi/2$  spin rotation about x-axis



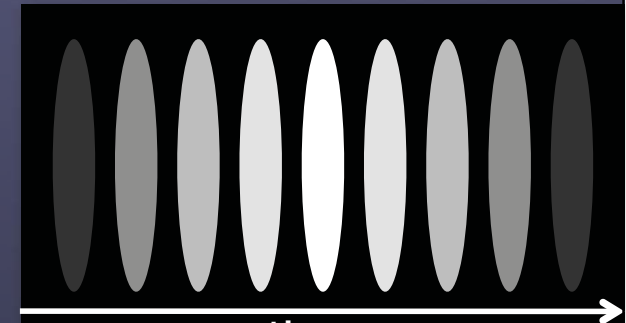
$\pi/2$



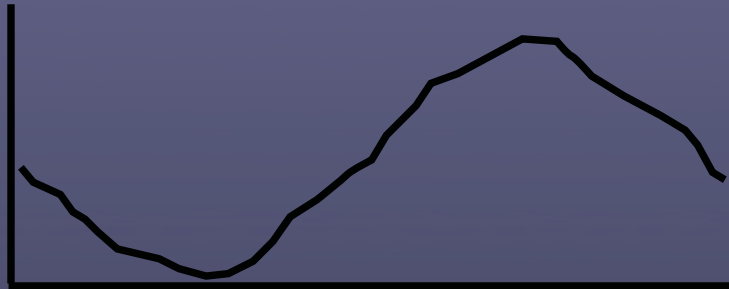
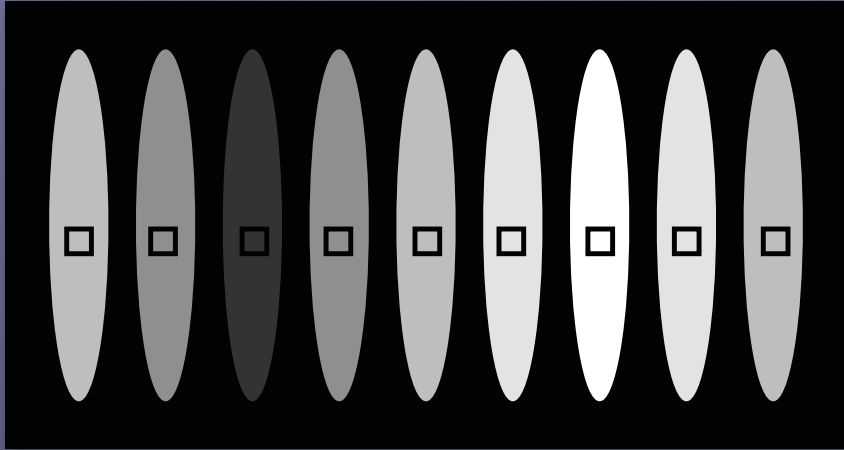
$\pi/2$



$\pi/2$



## Displaying the vector spin



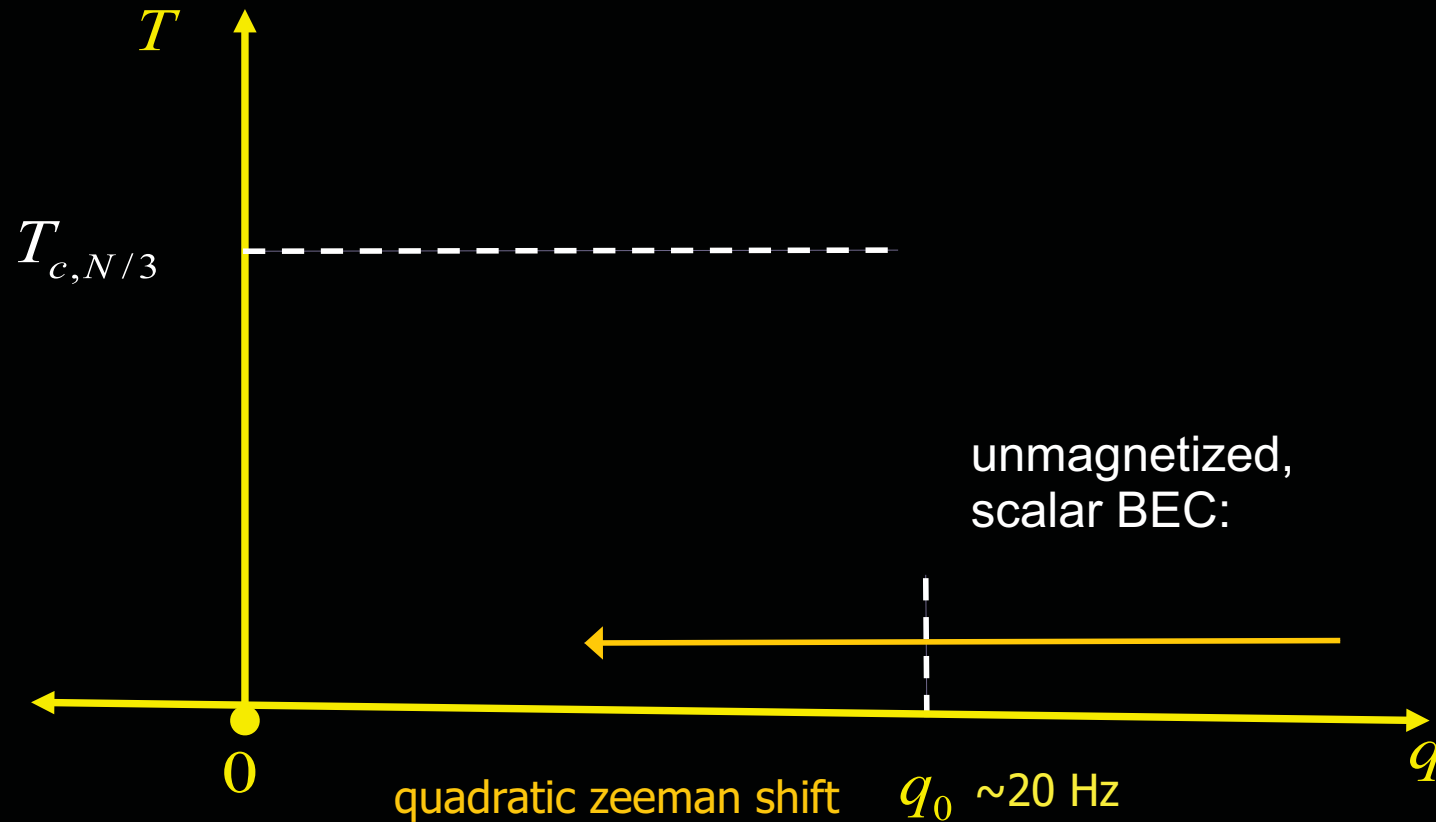
Least squares estimate of  
phase and amplitude which  
obtains the CR bound



Phase-  
Amplitude  
map



# F=1 <sup>87</sup>Rb gas phase diagram: overview



nature

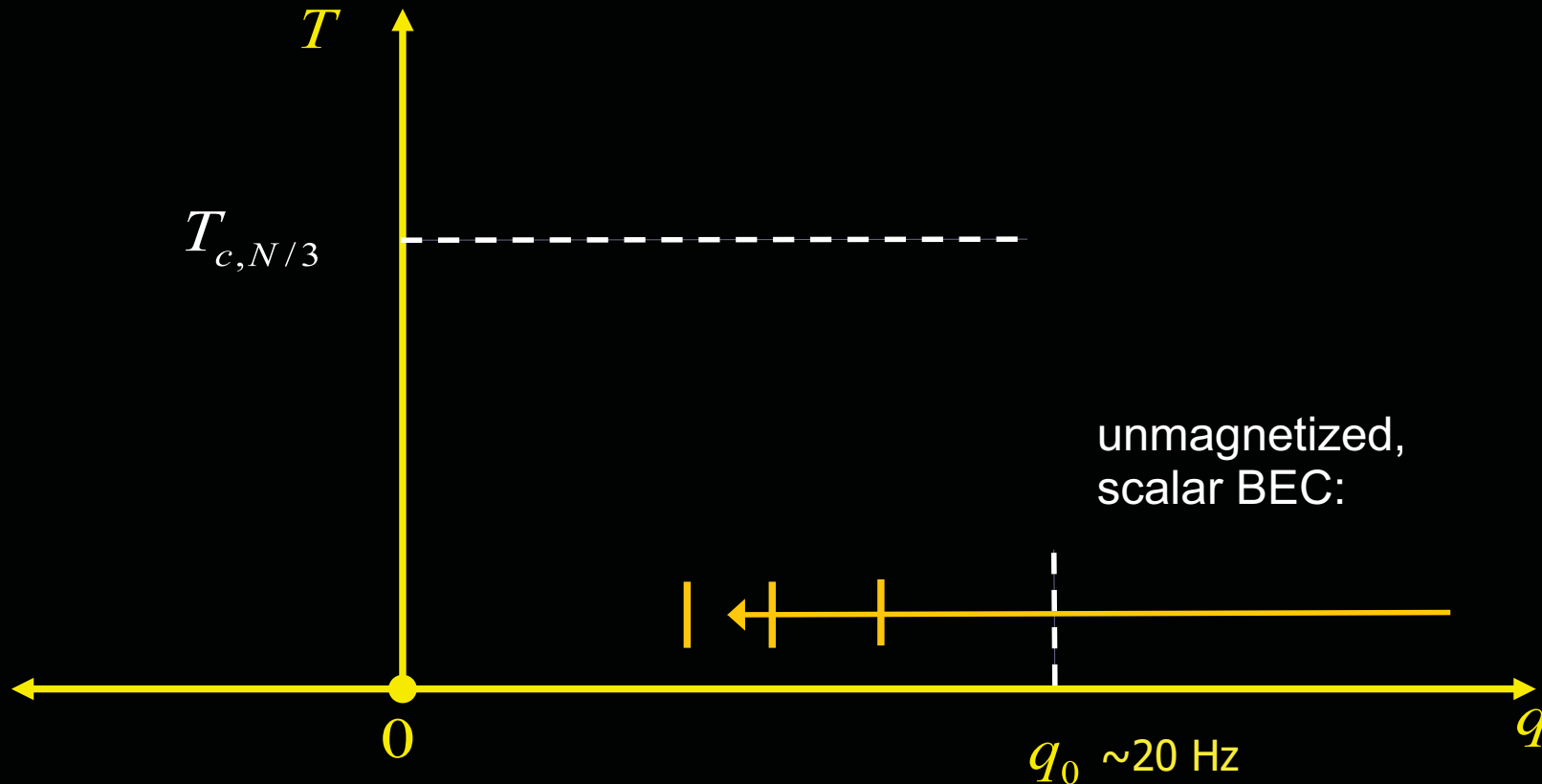
Vol 443|21 September 2006|doi:10.1038/nature05094

LETTERS

**Spontaneous symmetry breaking in a quenched ferromagnetic spinor Bose-Einstein condensate**

L. E. Sadler<sup>1</sup>, J. M. Higbie<sup>1</sup>, S. R. Leslie<sup>1</sup>, M. Vengalattore<sup>1</sup> & D. M. Stamper-Kurn<sup>1</sup>

# F=1 <sup>87</sup>Rb gas phase diagram: overview



## Amplification of Fluctuations in a Spinor Bose Einstein Condensate

S. R. Leslie<sup>1,\*</sup>, J. Guzman<sup>1,2</sup>, M. Vengalattore<sup>1</sup>, Jay D. Sau<sup>1</sup>, Marvin L. Cohen<sup>1,2</sup>, and D. M. Stamper-Kurn<sup>1,2</sup>

<sup>1</sup>Department of Physics, University of California, Berkeley CA 94720

<sup>2</sup>Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720

(Dated: November 9, 2008)

[arXiv:0806.1553](https://arxiv.org/abs/0806.1553)

Dynamical instabilities in a <sup>87</sup>Rb  $F = 1$  spinor Bose-Einstein condensate are used as a parametric amplifier of quantum spin fluctuations. We demonstrate the spectrum of this amplifier to be tunable, in quantitative agreement with theory. We quantify the microscopic spin fluctuations of the initially

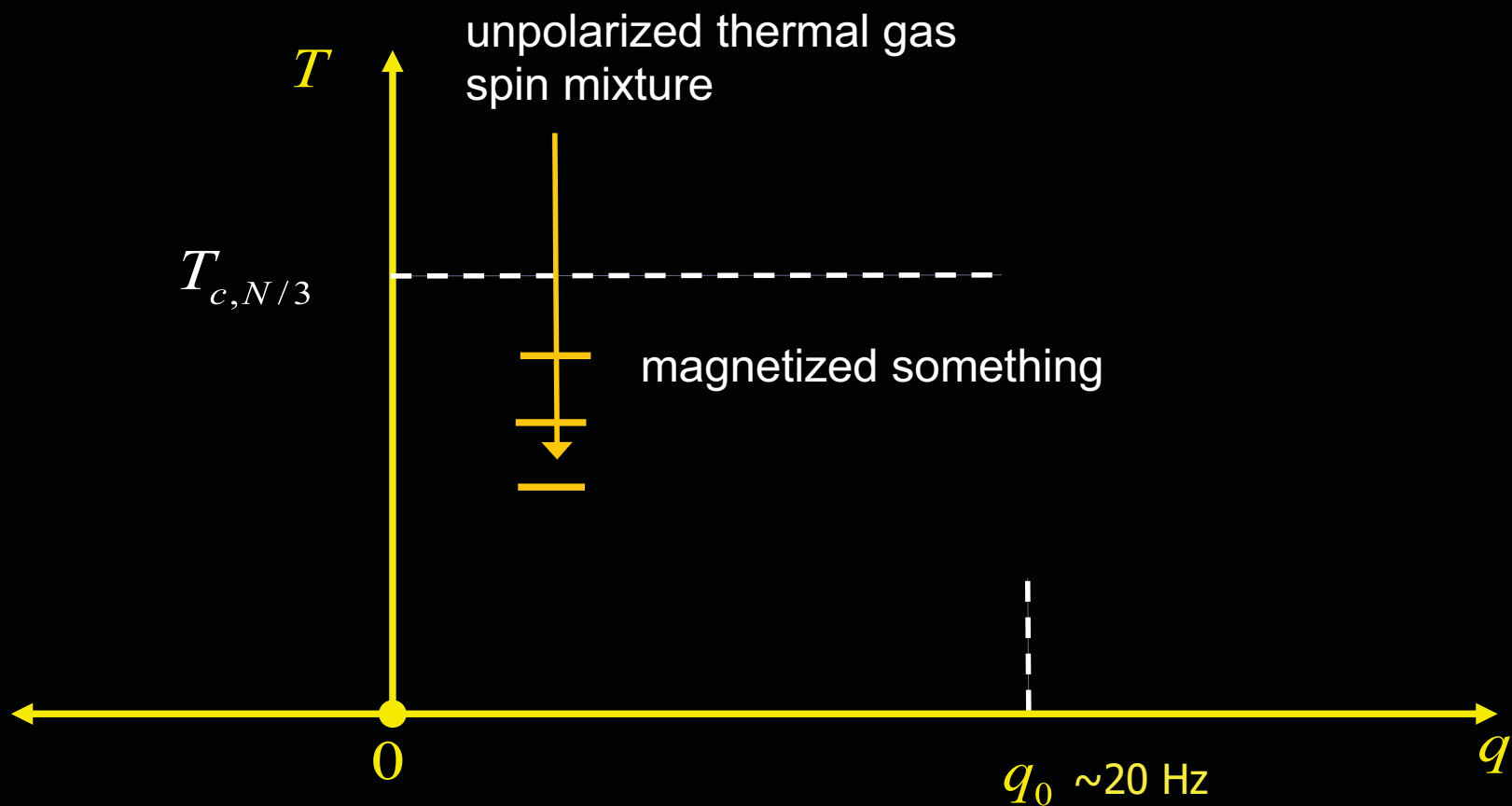
LETTERS

Spontaneous symmetry breaking in a quenched ferromagnetic spinor Bose-Einstein condensate

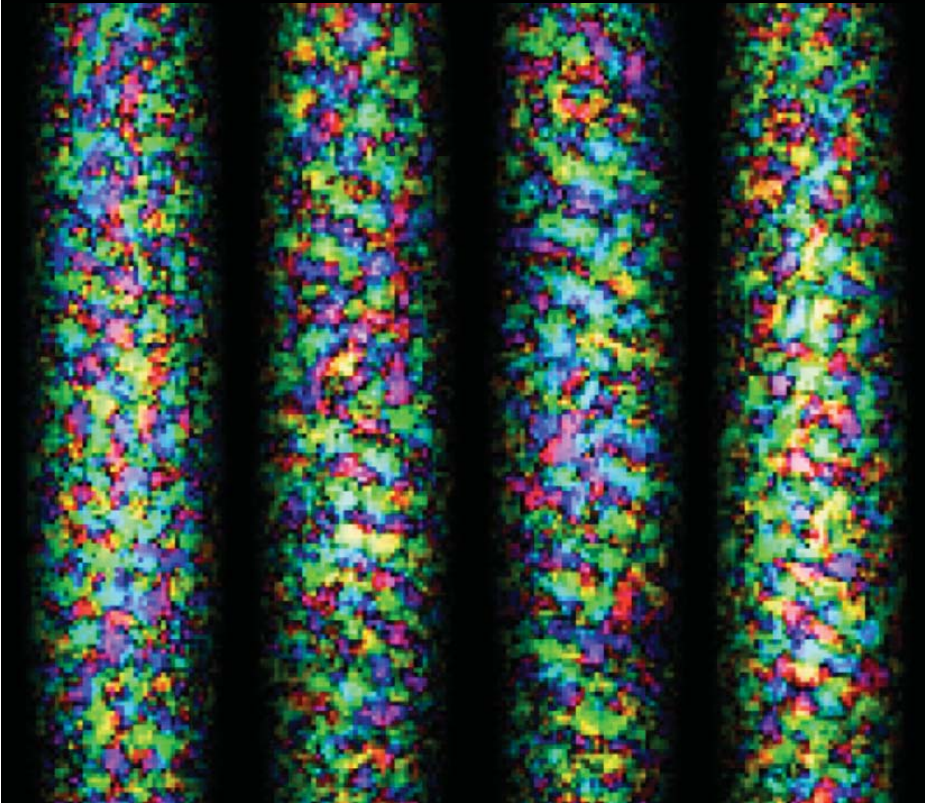
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## Experiment: $F=1$ $^{87}\text{Rb}$ gas at thermal equilibrium

- prepare fully depolarized thermal gas in uniform magnetic field
- lower temperature
- take pictures



"Crystalline magnetic order in a dipolar spinor quantum gas," arXiv:0901.3800 (2009)

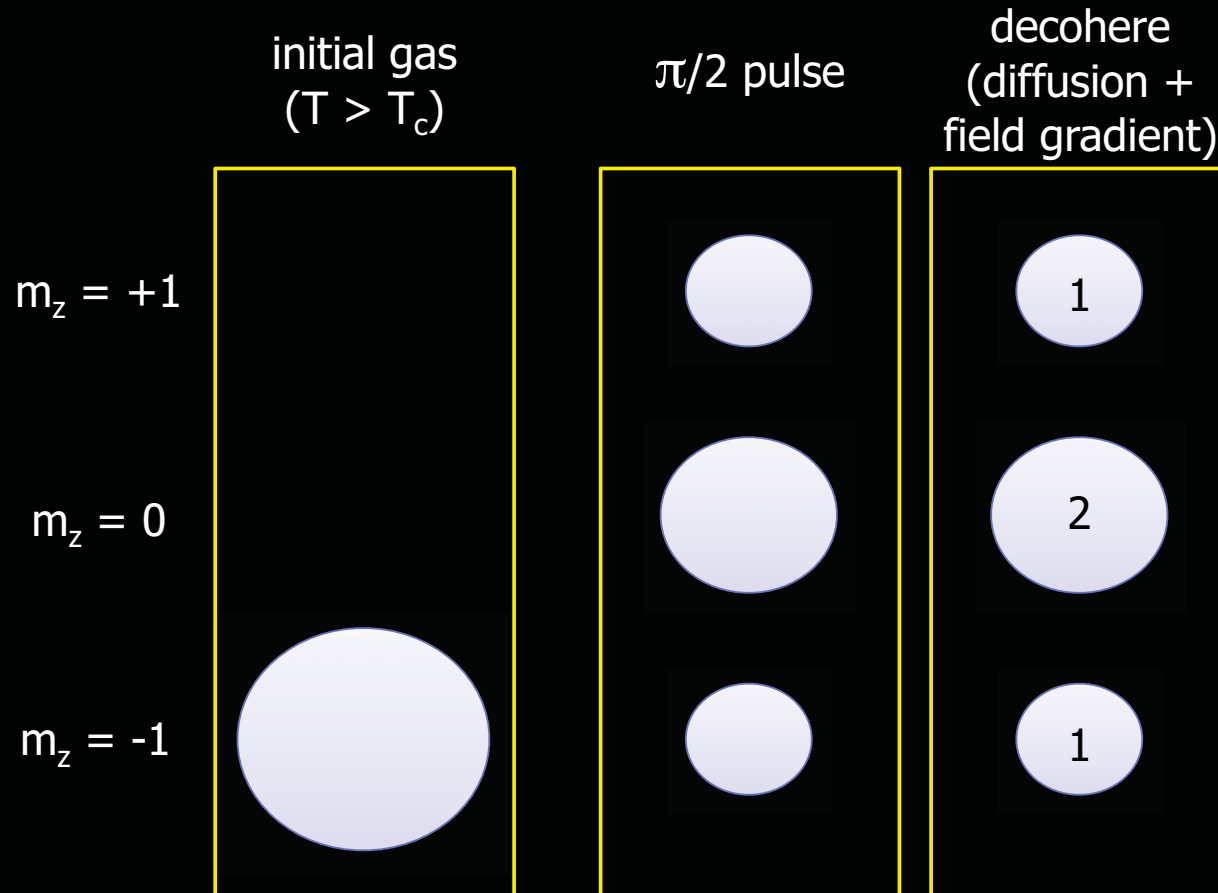


## Observation #1

direct imaging of low-temperature  
spatially patterned magnetization in  
gas produced by slow evaporative  
cooling

Spontaneous breaking of  
translational symmetry

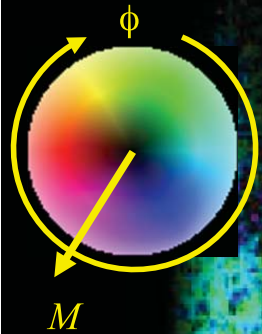
# preparing unmagnetized gases



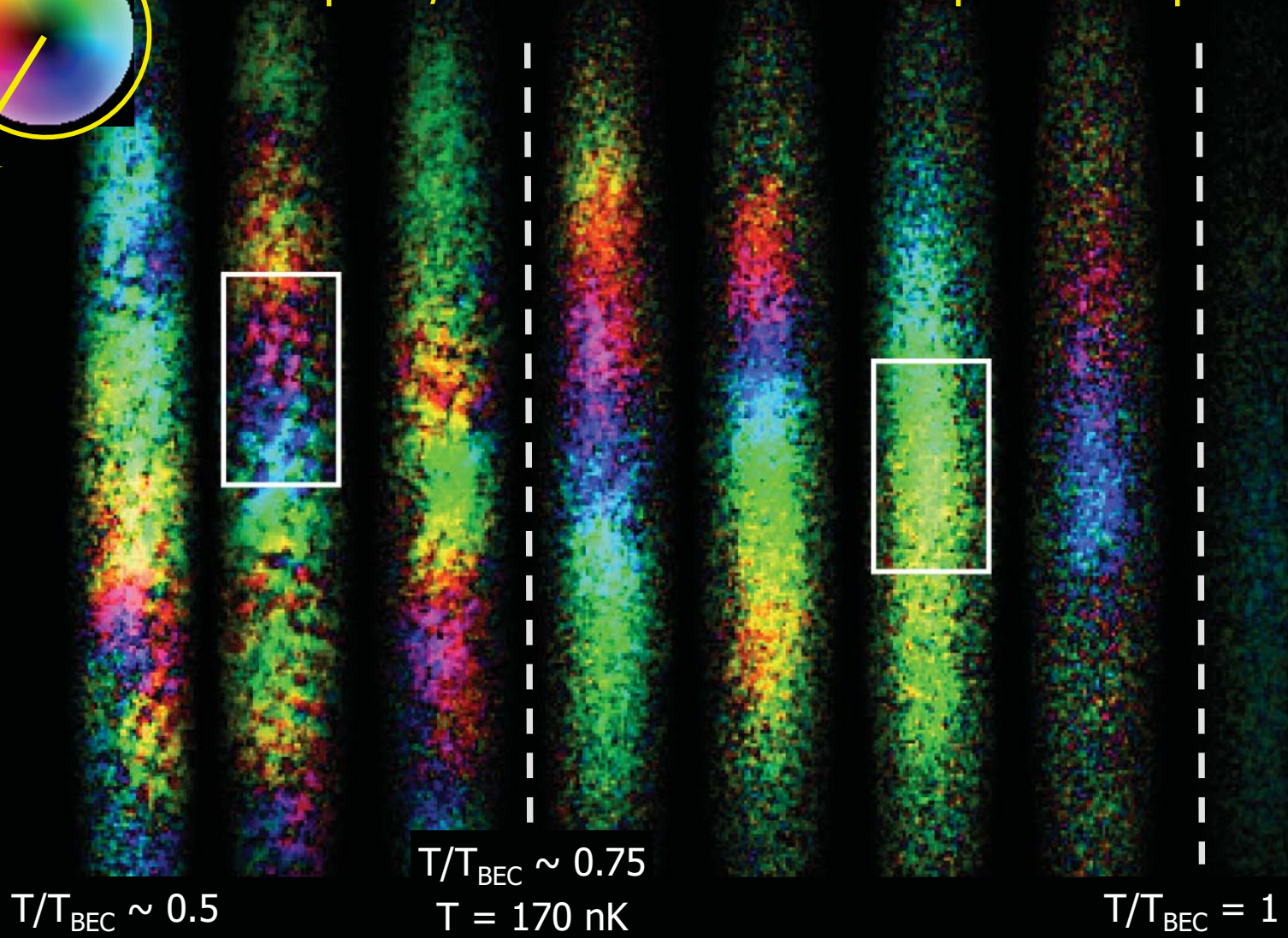
1:2:1 mixture

$$\eta = 1/4$$

Quadrupole moment (nematicity): related to  $\eta = [m=0] - [m=1]$



initial  $\eta = 1/4$  mixture – thermal equilibrium phases



$T/T_{\text{BEC}} \sim 0.5$

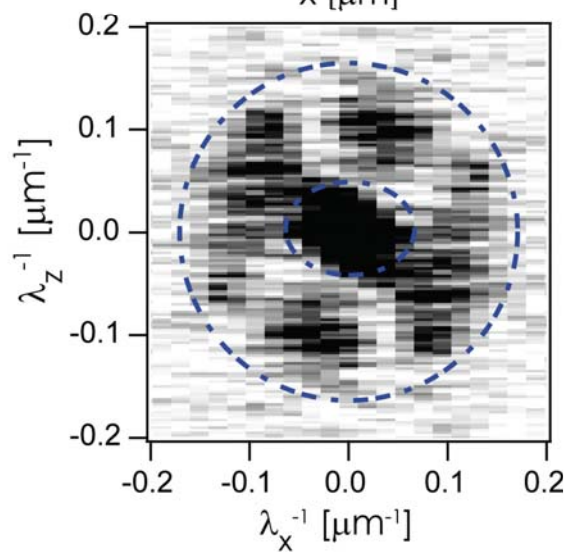
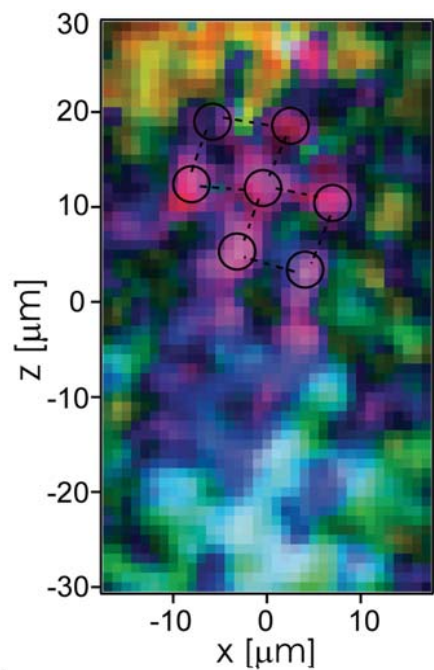
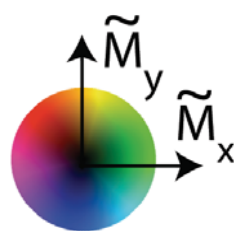
$T/T_{\text{BEC}} \sim 0.75$

$T = 170 \text{ nK}$

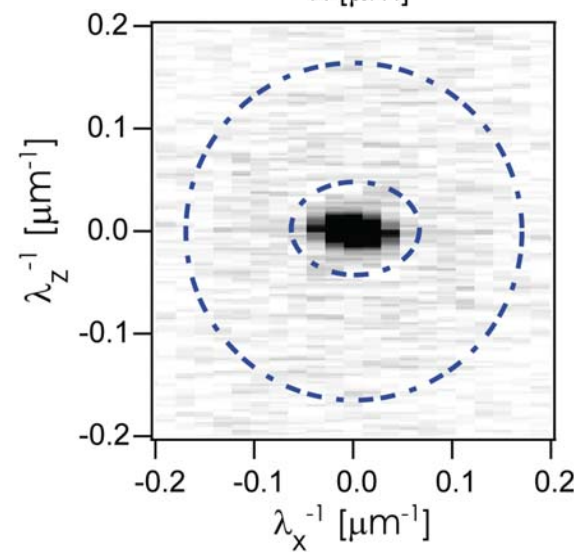
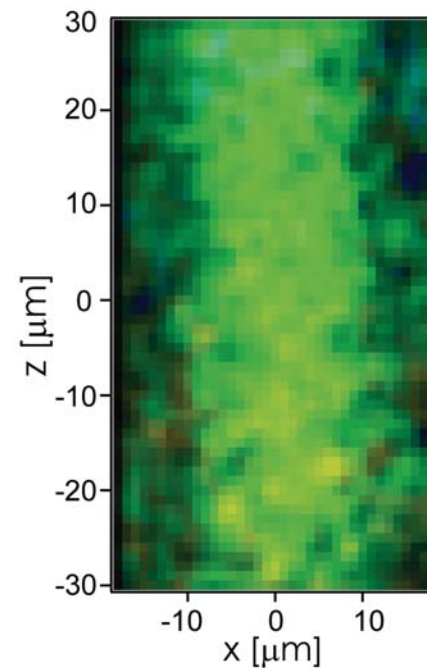
$T/T_{\text{BEC}} = 1$

●  $\sim$  no long. magnetization – spins lie exclusively in transverse plane

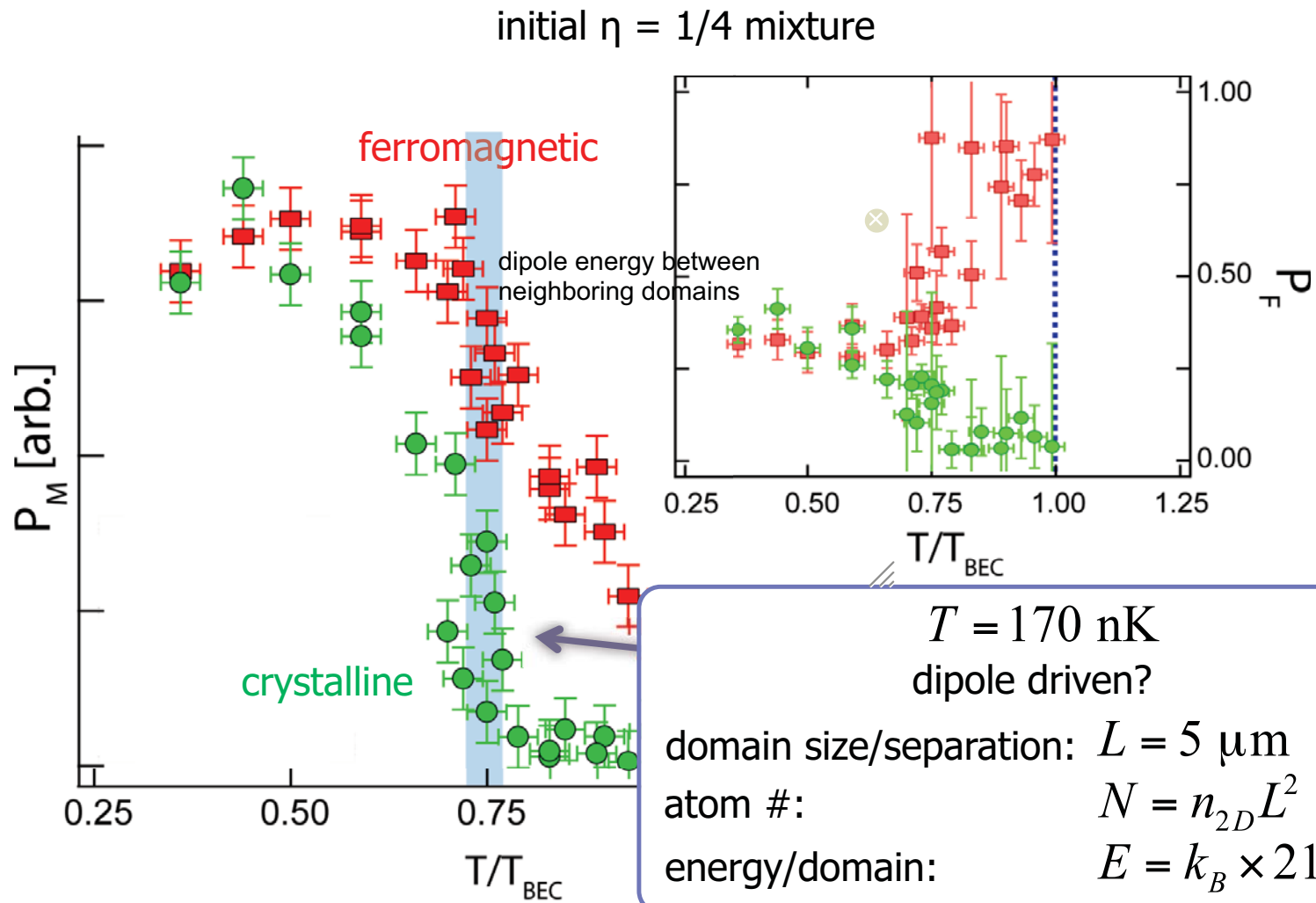
initial  $\eta=1/4$ , low temperature



initial  $\eta=1/4$ , high temperature

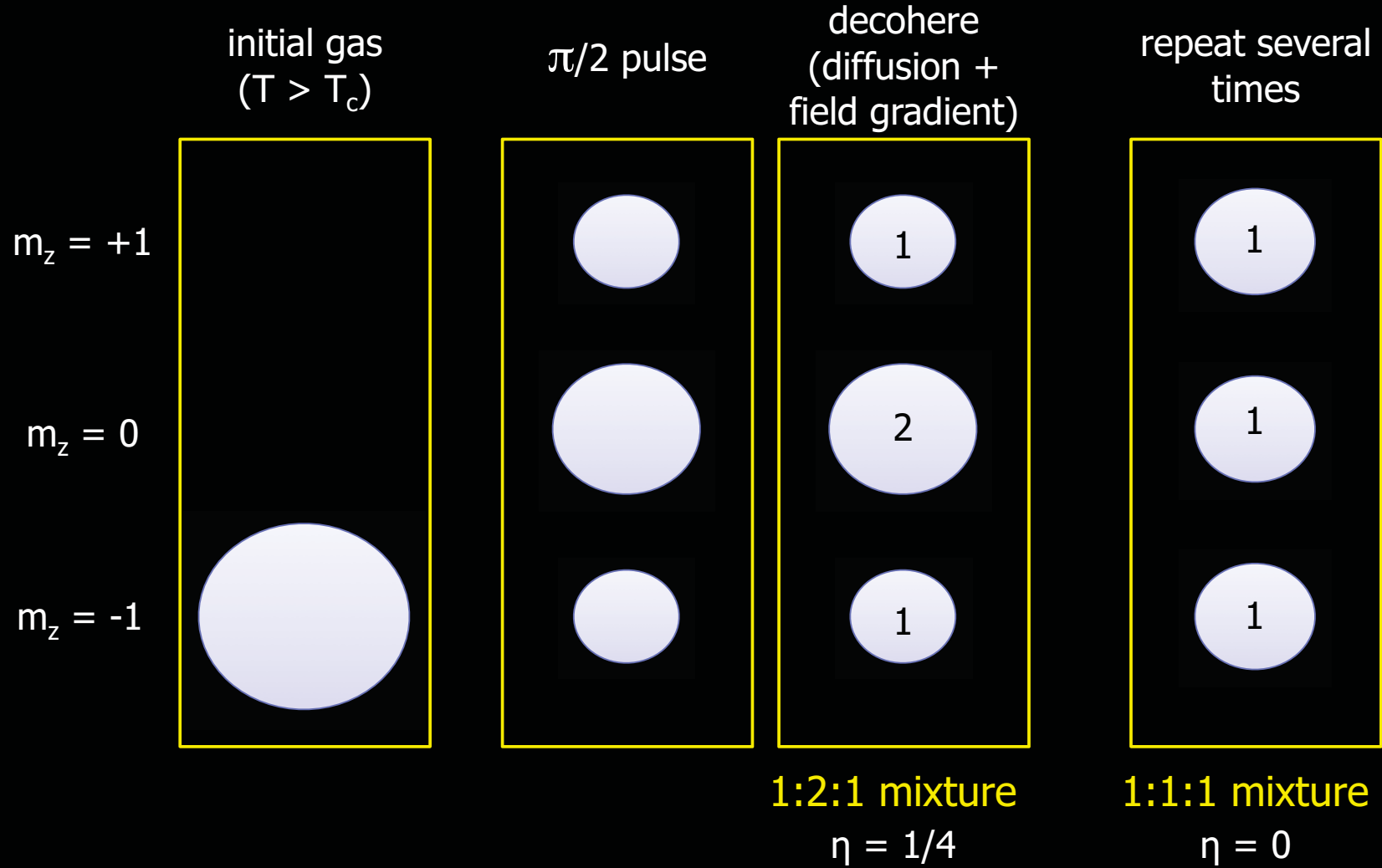


# Ferromagnetic and crystalline order parameters

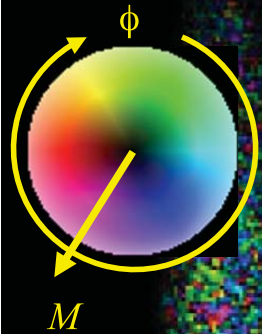




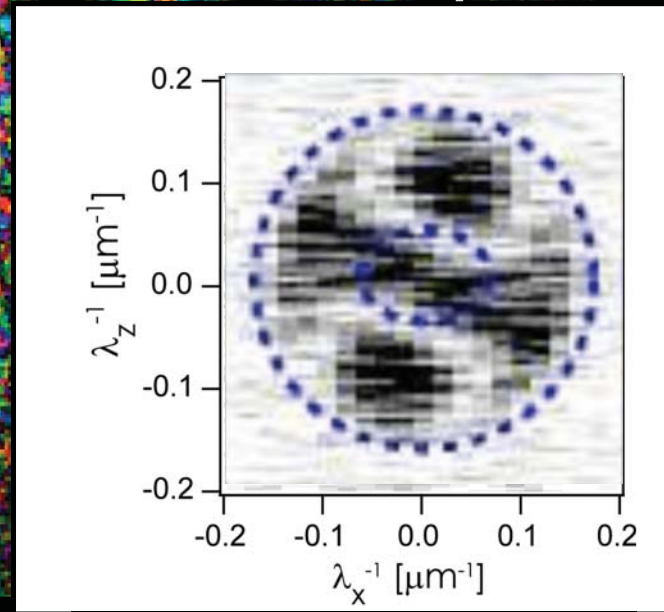
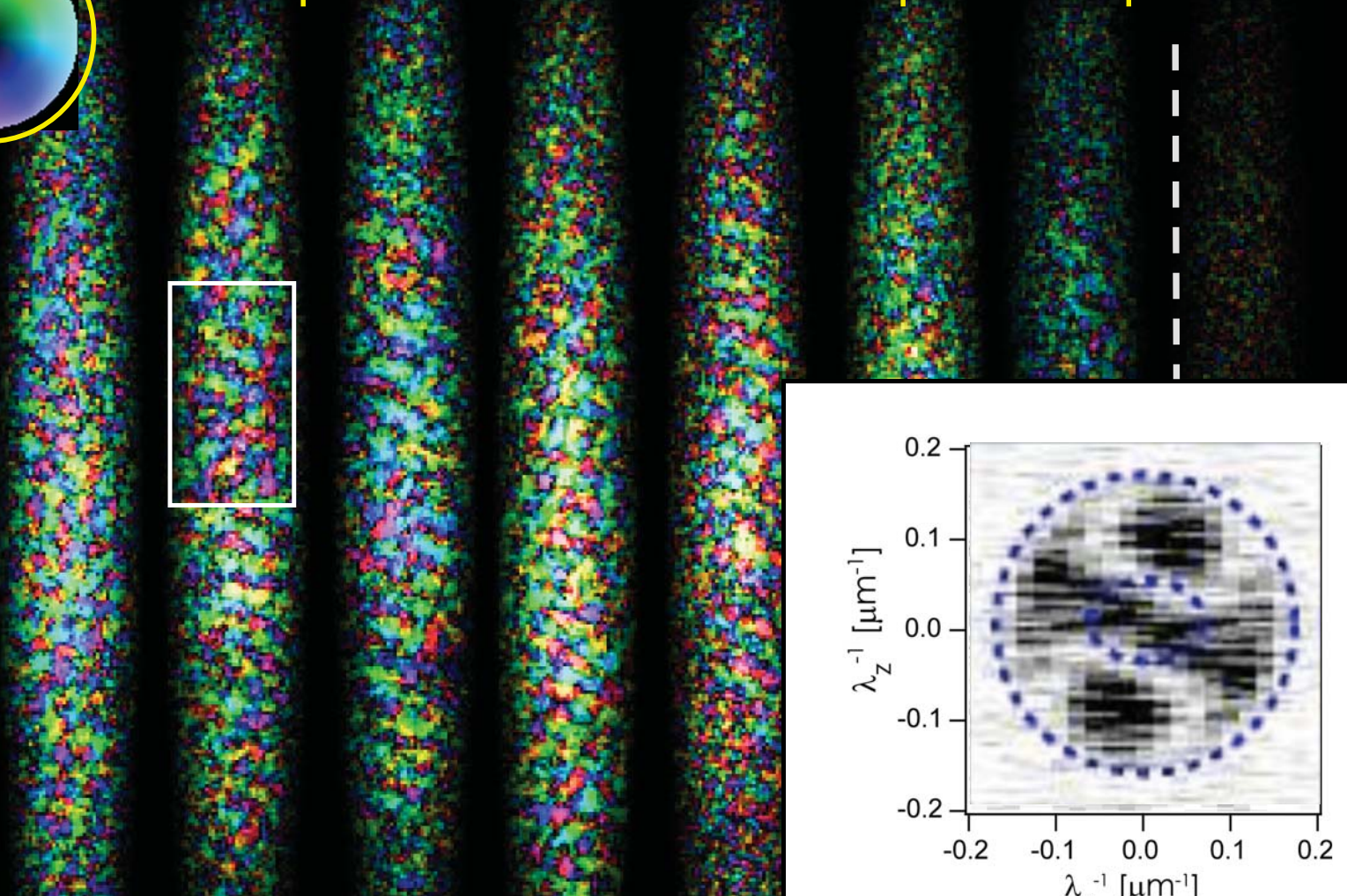
# preparing unmagnetized gases



Quadrupole moment (nematicity): related to  $\eta = [m=0] - [m=1]$



initial  $\eta = 0$  mixture – thermal equilibrium phases



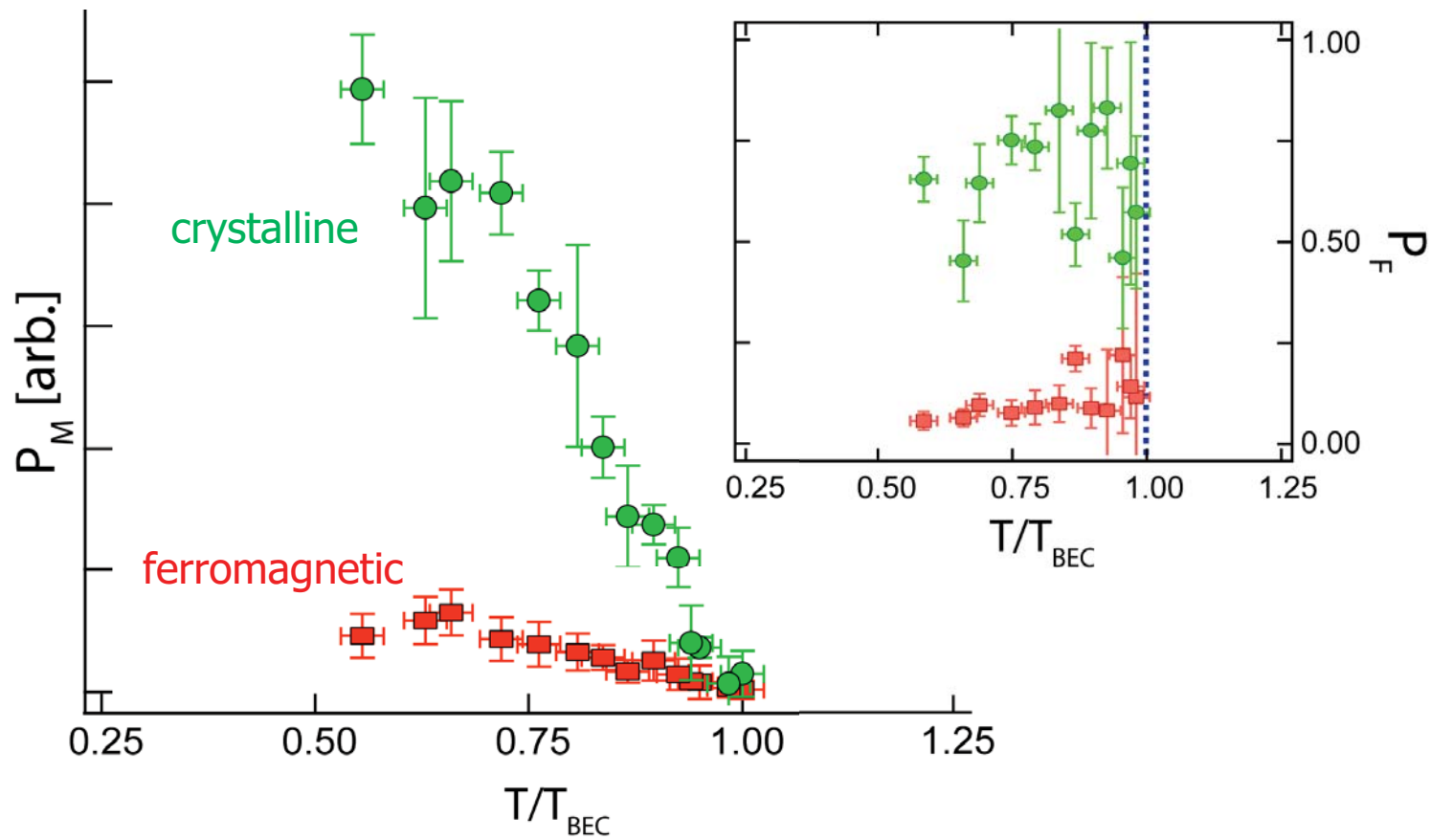
$T/T_{\text{BEC}} = 0.55$

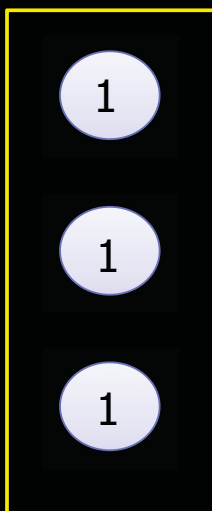
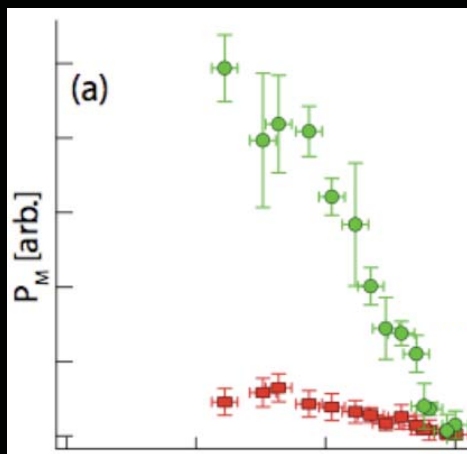
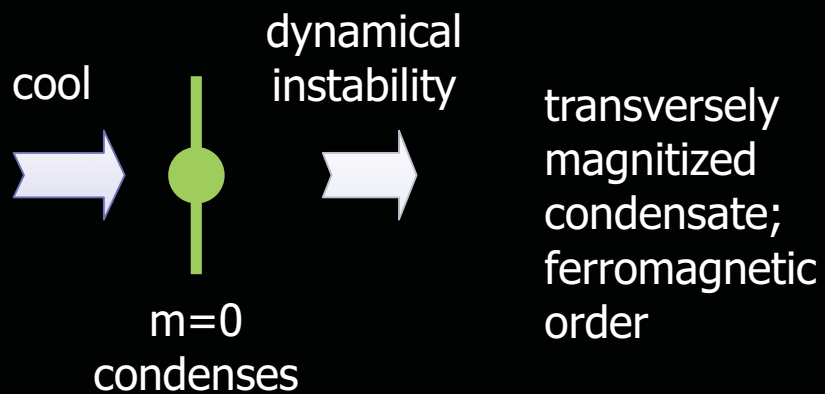
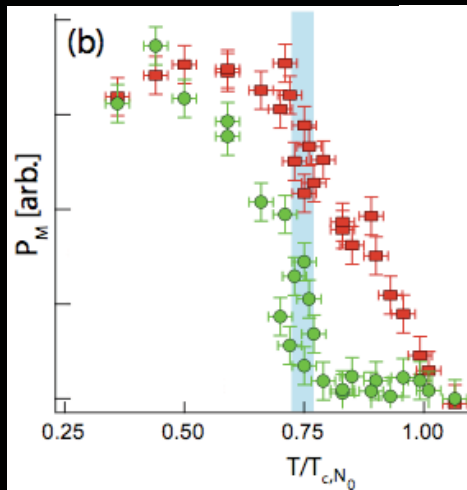
$T/T_{\text{BEC}} = 1$

● similar spatial variation in long. magnetization – no globally preferred spin direction

# Ferromagnetic and crystalline order parameters

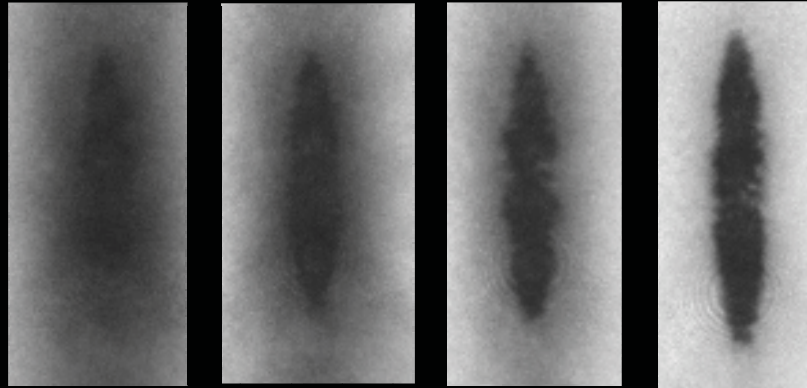
initial  $\eta = 0$  mixture





## Both spinors ( $\eta=0$ and $1/4$ ) exhibit hallmarks of Bose condensation

◆ Looks like a BEC in TOF:



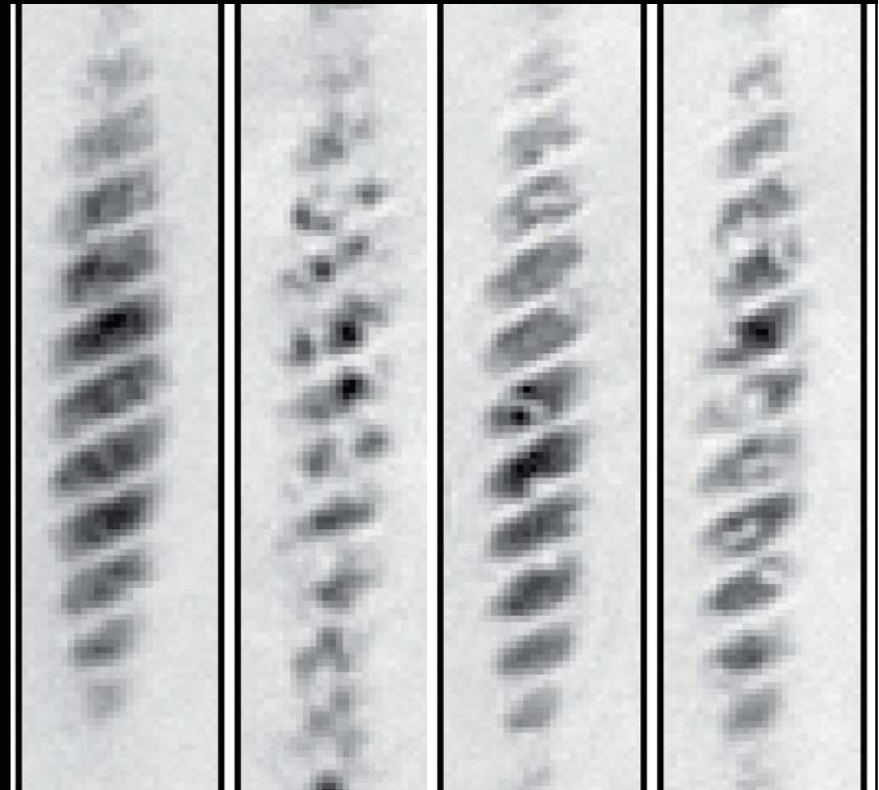
$m=0$  component  
of  $\eta=1/4$  spinor

Is it a superfluid?  
(long range off-diagonal order)

## Observation #2

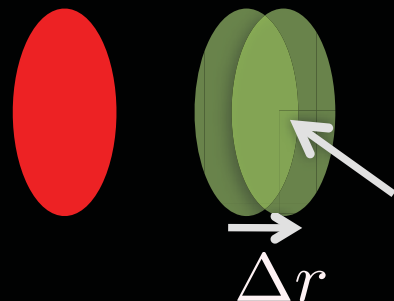
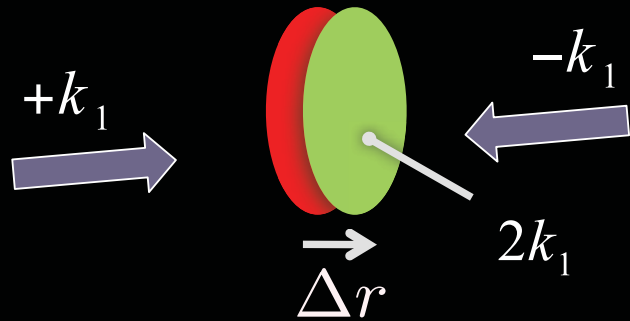
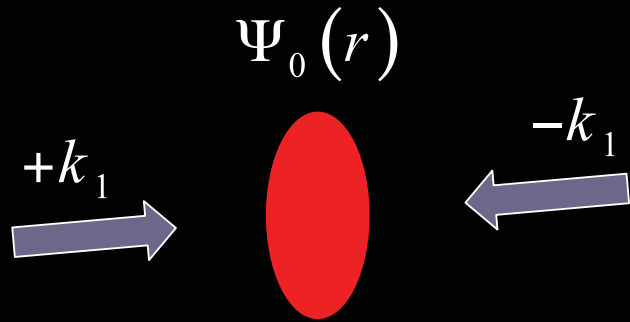
off-diagonal density operator, i.e. first-order correlation function, measured by atom interferometry

Spontaneous establishment of off-diagonal long-range order

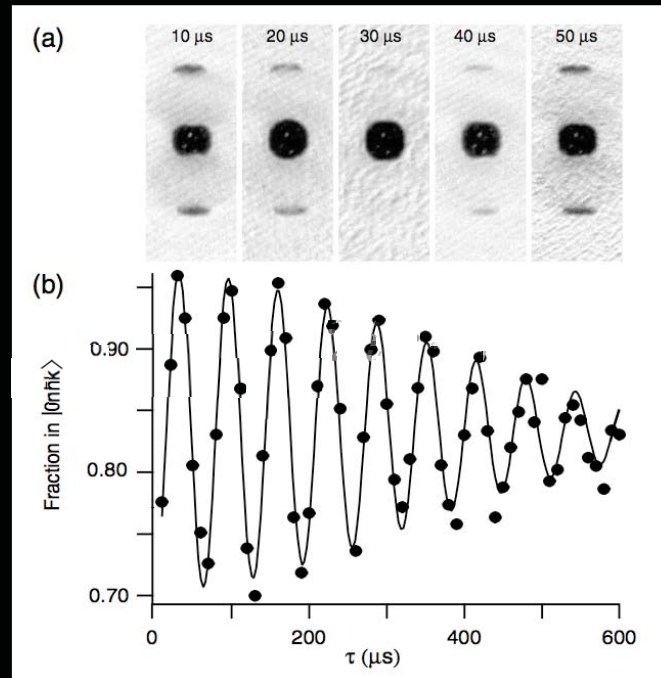


# Measuring coherence via atom interferometry

Ramsey-type (two pulse) Bragg scattering:



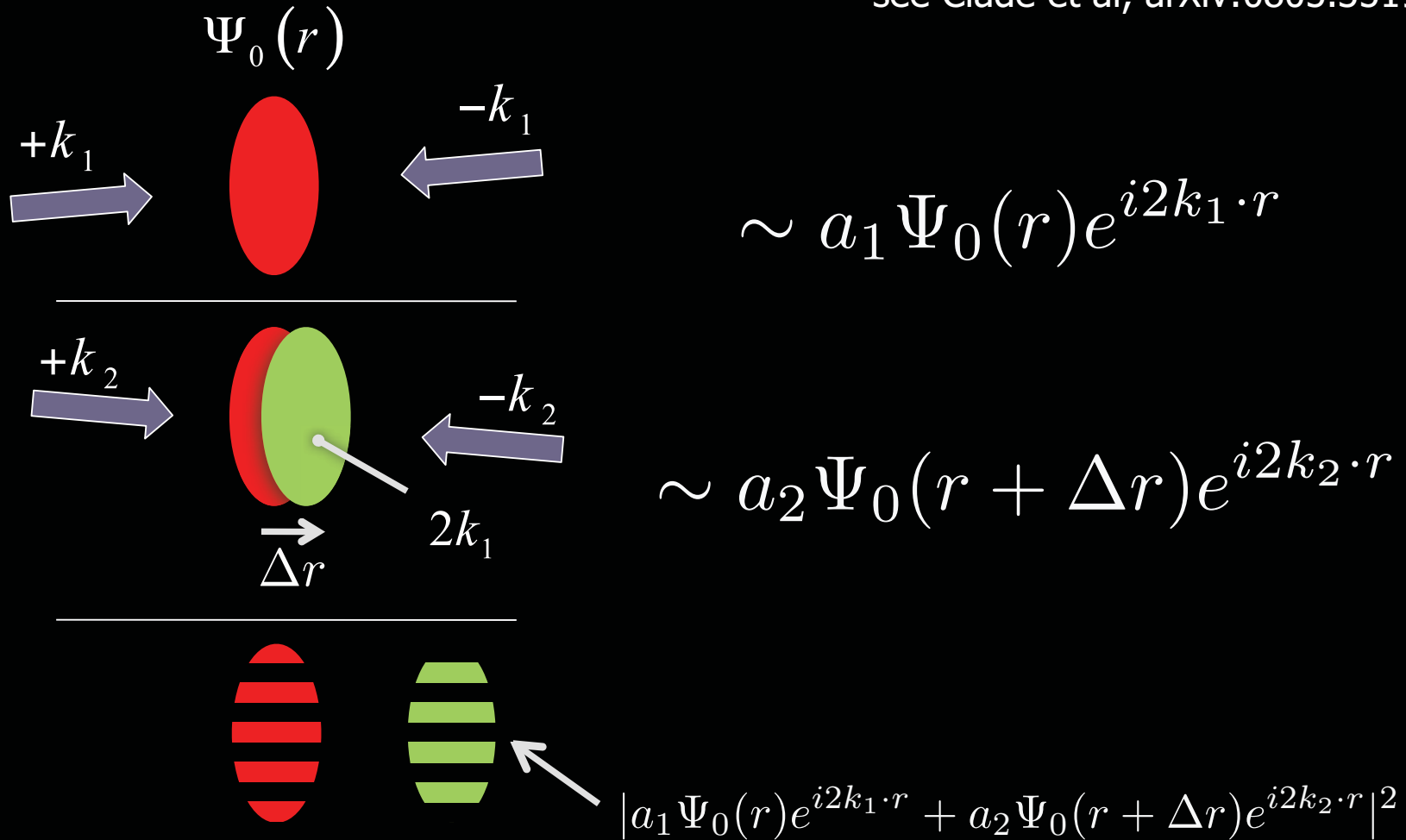
$$|\Psi_0(r) + e^{i\phi} \Psi_0(r + \Delta r)|^2$$



Campbell 2005

## Spatial heterodyne atom interferometry

Ramsey-type (two pulse) Bragg scattering with 2 different wavevectors:  
see Cladé et al, arXiv:0805.3519







$$|a_1 \Psi_0(r) e^{i2k_1 \cdot r} + a_2 \Psi_0(r + \Delta r) e^{i2k_2 \cdot r}|^2$$

$$a_1^2 \Psi_0^*(r) \Psi_0(r) + a_2^2 \Psi_0^*(r + \Delta r) \Psi_0(r + \Delta r) + \left( a_1 a_2 \Psi_0^*(r) \Psi_0(r + \Delta r) e^{i\Delta k \cdot r} + c.c. \right)$$

Density from first pulse

Density from second pulse

Interesting quantity

$$F(\Delta k) = \int dr \left[ \cancel{(n_1 + n_2)} e^{-i\Delta k \cdot r} + a_1 a_2 \Psi_0^*(r) \Psi_0(r + \Delta r) + \cancel{c.r.t} \right]$$

"good heterodyne" approximation

$$F(\Delta k) \sim \langle \Psi_0^*(r) \Psi_0(r + \Delta r) \rangle$$

"First order correlation function":

$$\tilde{g}^{(1)} = \frac{F(\Delta k) + F(-\Delta k)}{N_1 + N_2} = g^{(1)} \times f(\Delta r)$$

# test run: scalar BEC

Kapitza-Dirac pulses in Raman-Nath regime

absorption image after time of flight

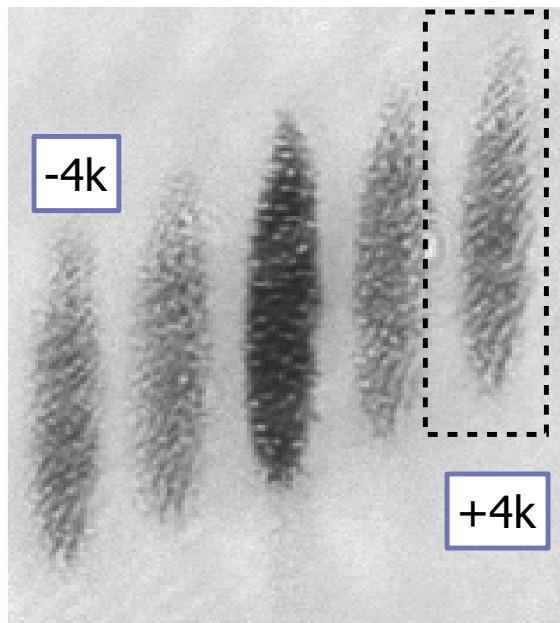
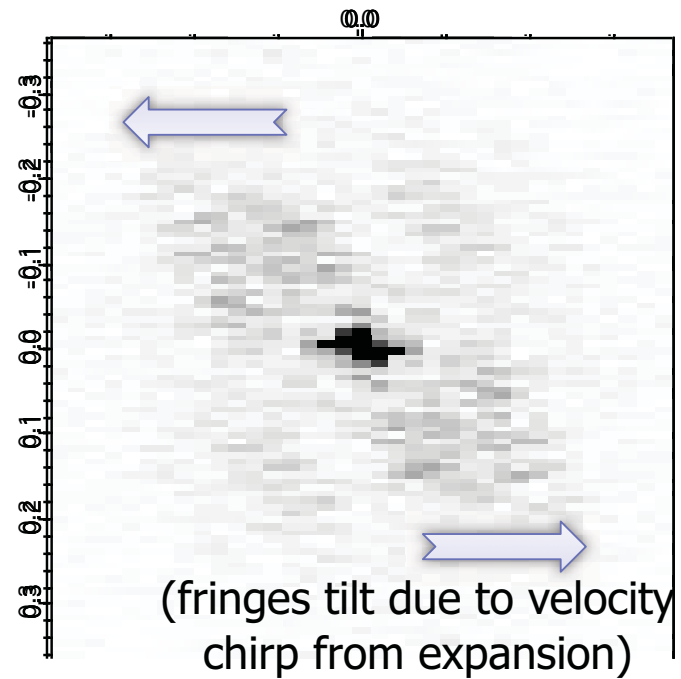
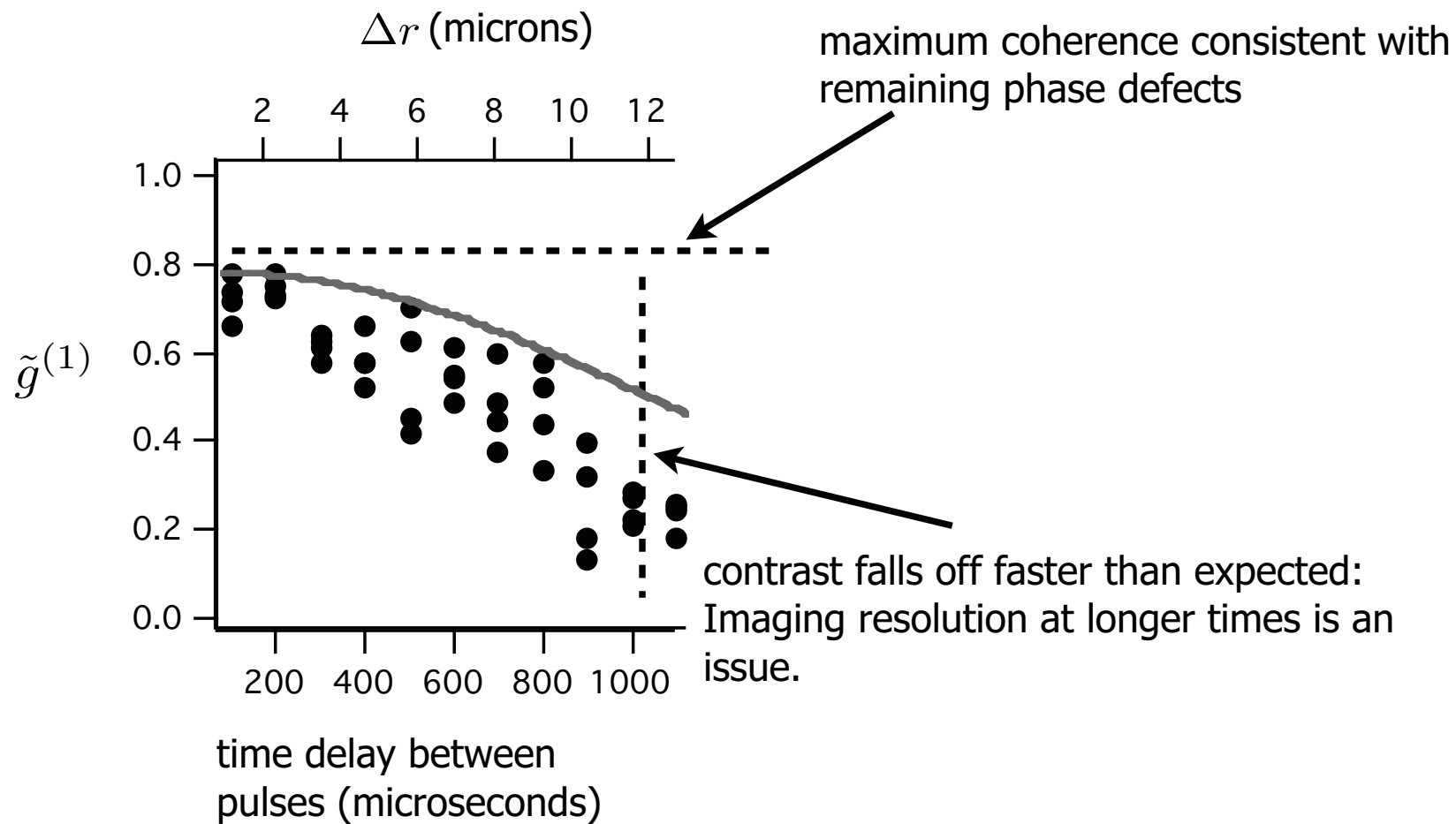


image Fourier transform

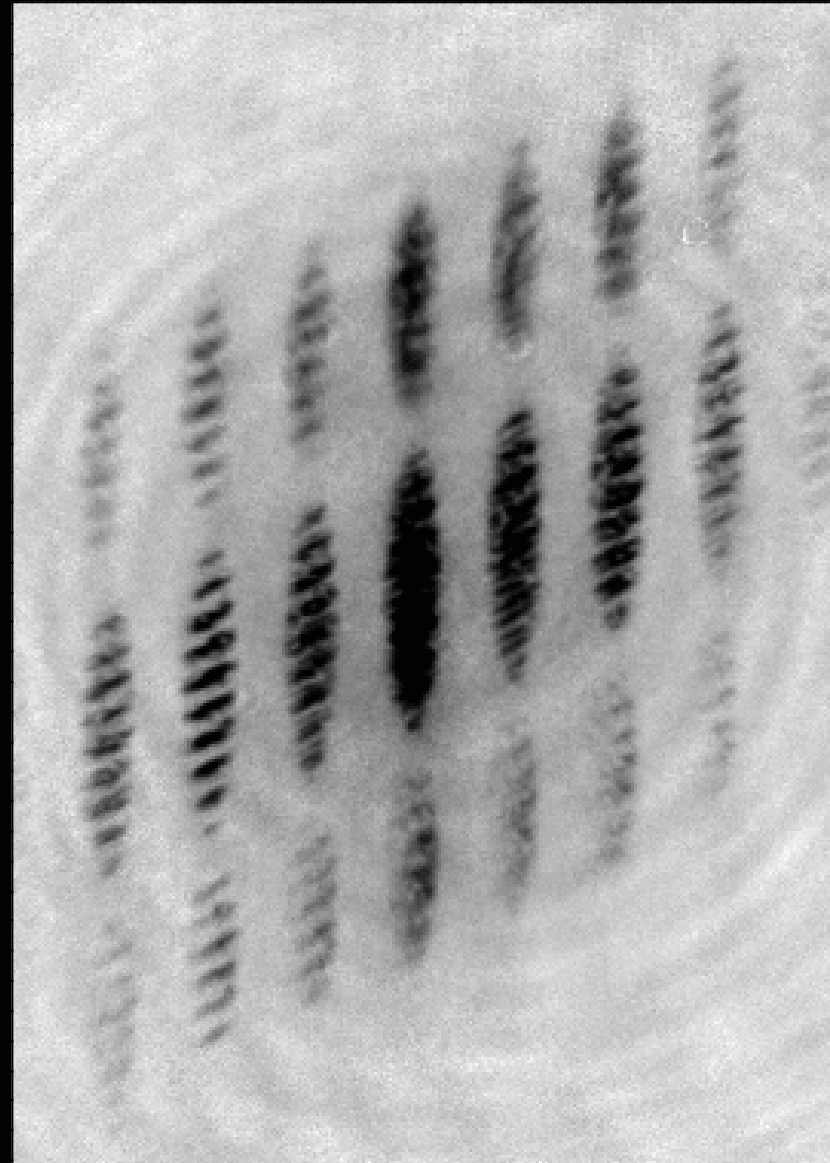


# test run: scalar BEC



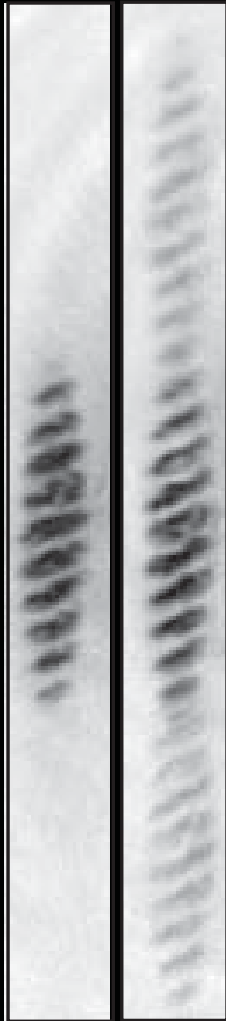
## Atom interferometry: with spinors

- Stern-Gerlach separation
- Many orders diffracted
- Challenge to keep everything in focus
- Very cool!



# Spinor gases in crystalline phase

without Stern-Gerlach spin separation



Transversely magnetized  
no crystal

with Stern-Gerlach spin separation

$m_z = +1$

$m_z = 0$

$m_z = -1$

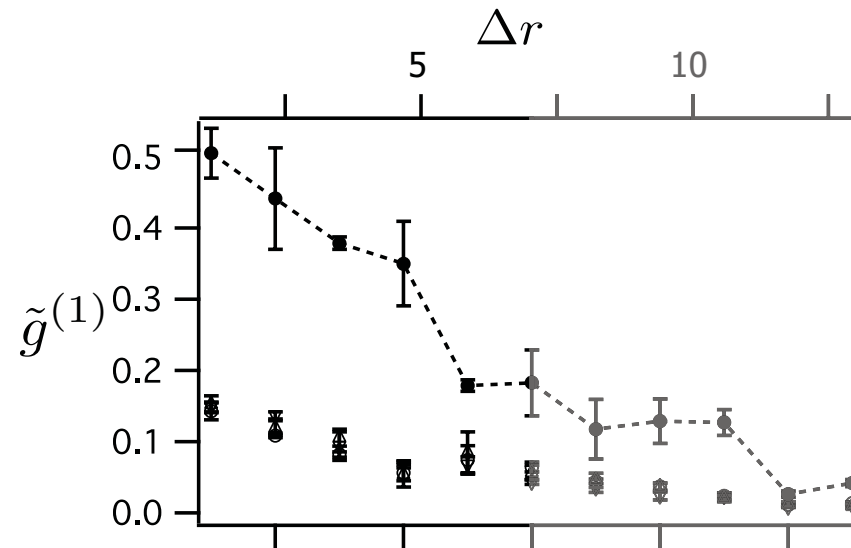


$\eta = 1/4$

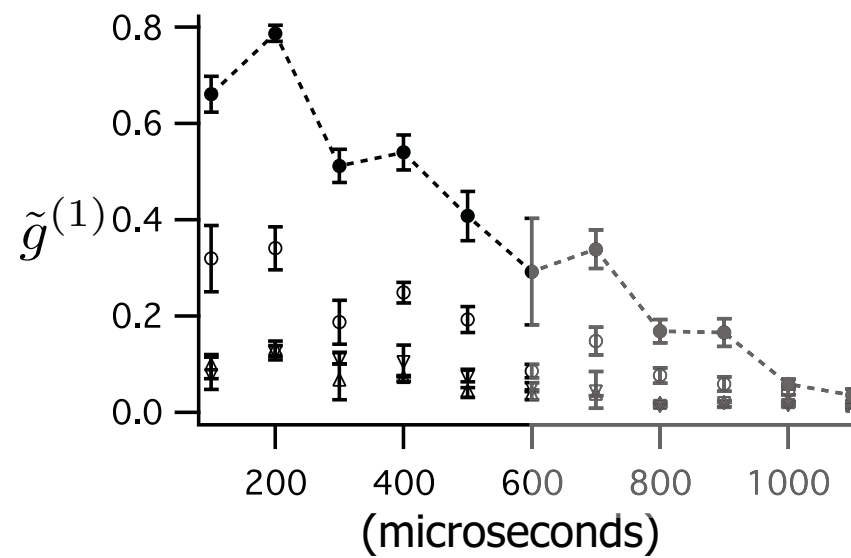


$\eta = 0$

# Spinor gases in crystalline phase



$\eta=0$ : coherence is shared equally between three components

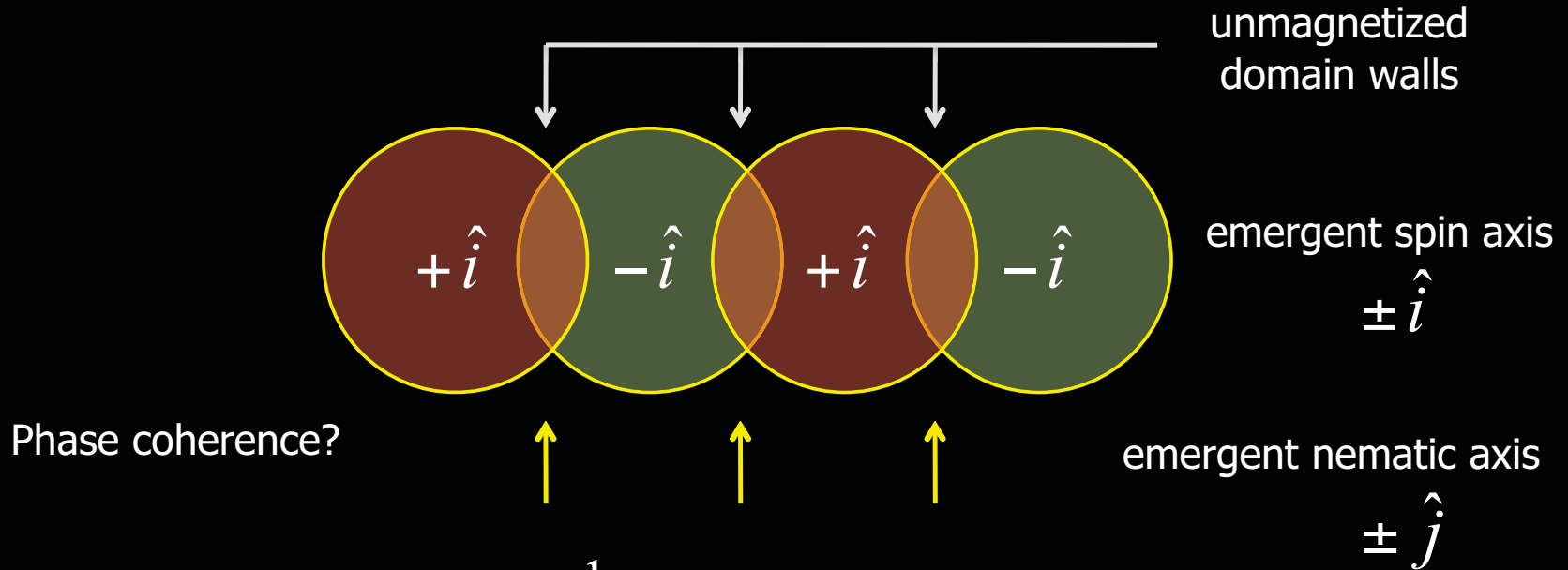


$\eta=1/4$ :  $m=0$  component has majority of coherence (also majority of atoms)

Generally: we see long range coherence for crystalline phase

## Possible coherence in the crystalline phase

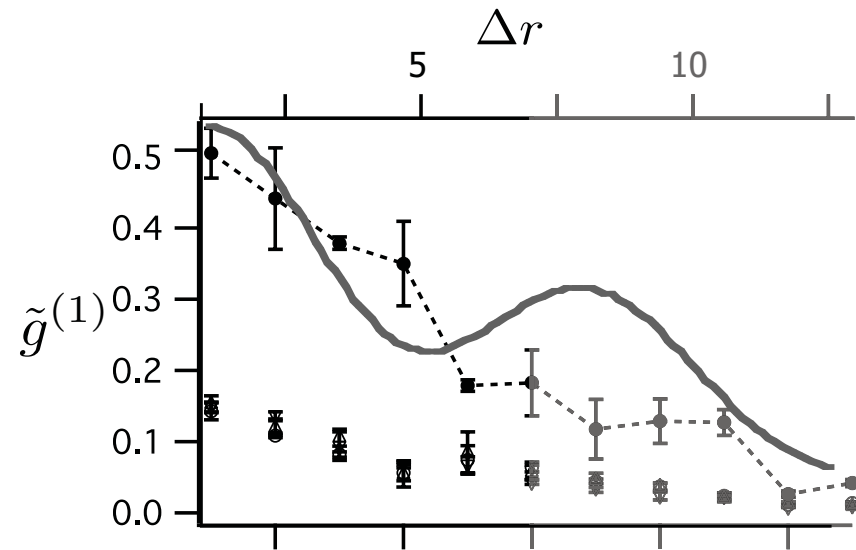
Observed checkerboard lattice:



$$\Psi(\text{wall}) = \frac{1}{\sqrt{2}} \left( |+\hat{i}\rangle + e^{i\phi} |-\hat{i}\rangle \right) = |m_{\hat{j}} = 0\rangle$$

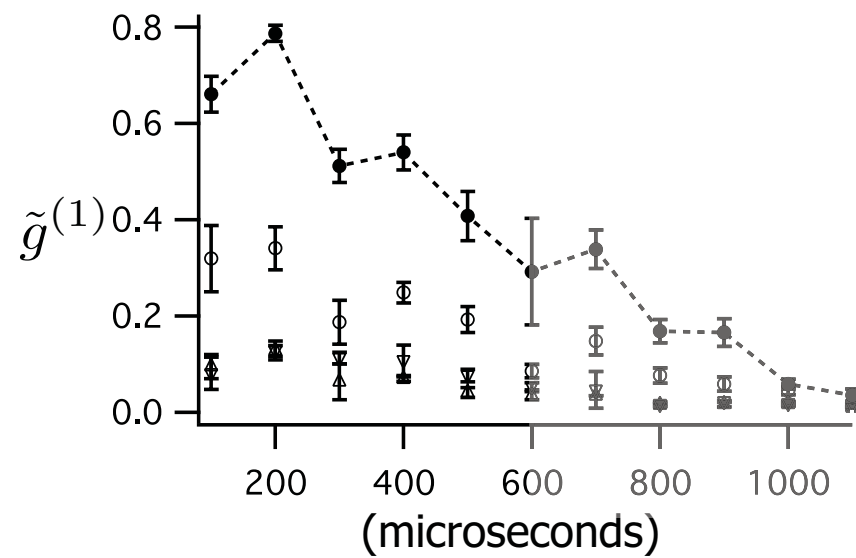
1. Latent long-range magnetic order: a second nematic axis
2. Long-range off-diagonal order of nematic background

# Spinor gases in crystalline phase



about half of the  $m = \pm 1$  atoms  
contribute to the crystal

$\lambda = 2\pi (10\mu\text{m})$  crystal





## Summary

- Is  $^{87}\text{Rb}$   $F=1$  spinor gas a supersolid at low temperature?
  - ◆ Not certain...
- Ingredients: mobile bosons (exchange) + long-range interactions (dipolar)
- Evidence for crystalline ordering from direct imaging
  - ◆ thermal equilibrium?
  - ◆ initial state dependence: hysteresis? metastability?
  - ◆ small system size ( $\sim 6$  domains wide). “quasi-long-range?” hexatic?
  - ◆ other properties of a solid not yet probed.
  - ◆ crystal not observed in interferometry experiment.
- Evidence for superfluidity from atom interferometry
  - ◆ measured across 30 micron dimension
  - ◆ other properties of superfluid not yet probed

## Current status

● Is  $^{87}\text{Rb}$   $F=1$  spinor gas a supersolid at low temperature?

◆ Not certain...

◆ thermal equilibrium?

◆ small system size ( $\sim 6$  domains wide). “quasi-long-range?” hexatic?

◆ other properties of a solid not yet probed

Constructed a new experimental apparatus:

Longer equilibration times,

Faster duty cycle

Better magnetic field control

Better optical access

Cancel mean-field expansion



E1: Spinor BEC  
Jennie Guzman  
(Sabrina Leslie)  
Kater Murch  
(Friedhelm Serwane)  
(Mukund Vengalattore)

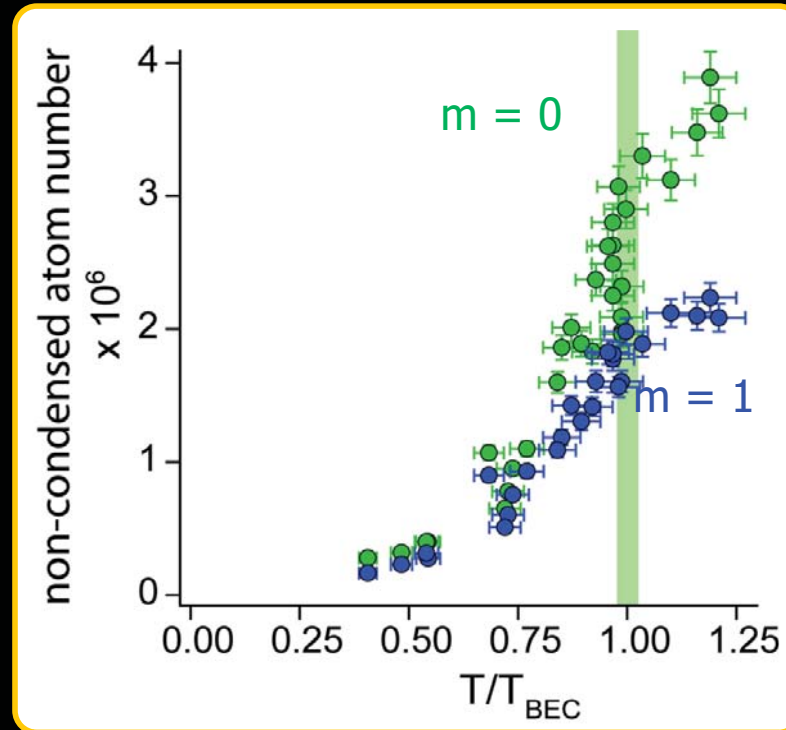
E2,E3: Cavity QED  
Thierry Botter  
Nathan Brahams  
Daniel Brooks  
Gee-Na Kim  
Zhao-Yuan Ma  
Guil Miranda  
Tom Purdy

E4: Ring-trap interferometry  
Ed Marti  
Ryan Olf  
Tony Oettl  
Enrico Vogt



## non-equilibrium? metastable? extrinsic?

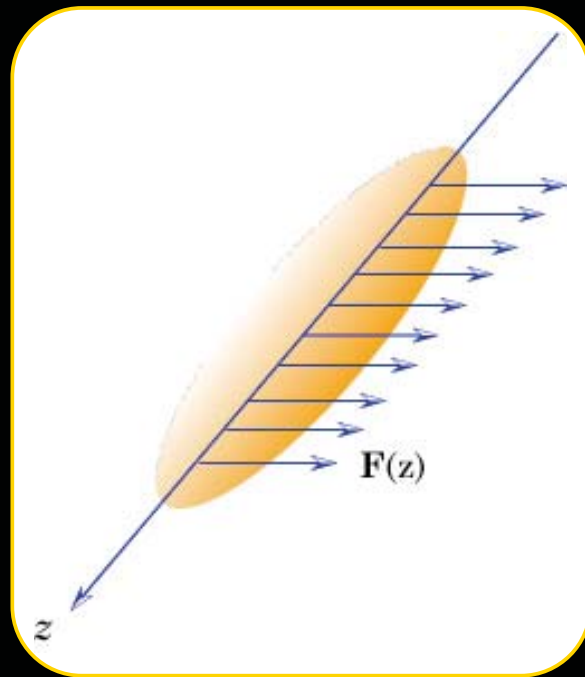
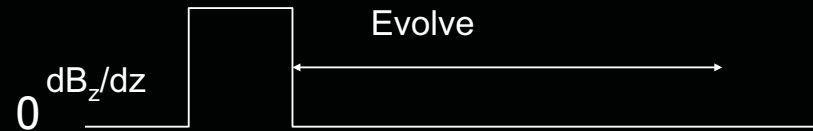
- non-equilibrium thermal spin mixture persists only above  $T_{\text{BEC}}$



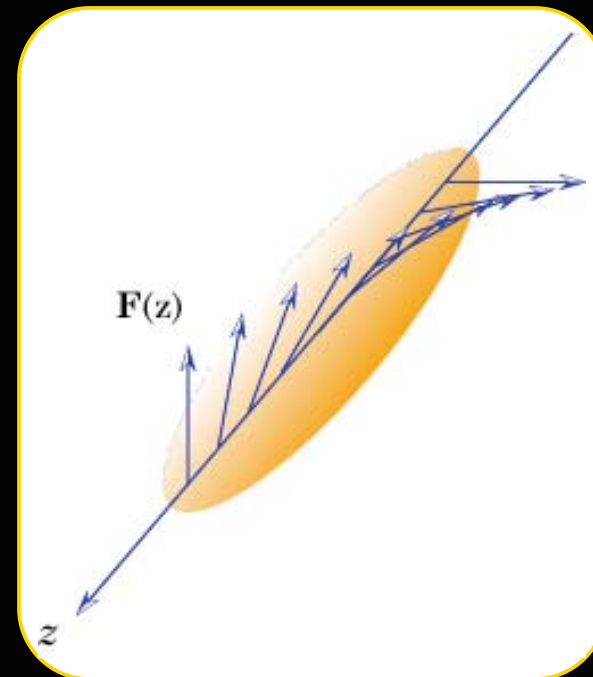
- no variation with cooling time, equilibration time
- crystalline pattern seen in relaxation from other states (quench, helix)
- low-temperature, small atom-number gases are crystalline

## Experiment 1: Dissolution of ferromagnetic spin textures

- generate helical spin pattern (uniform spin current) using inhomogeneous field

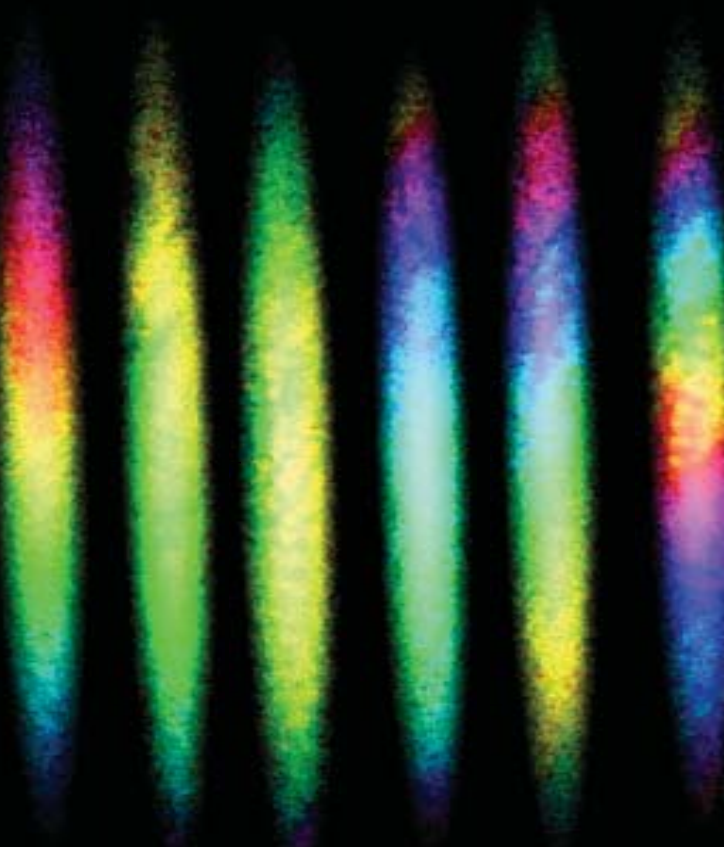


w/o gradient  
zero-wavevector helix



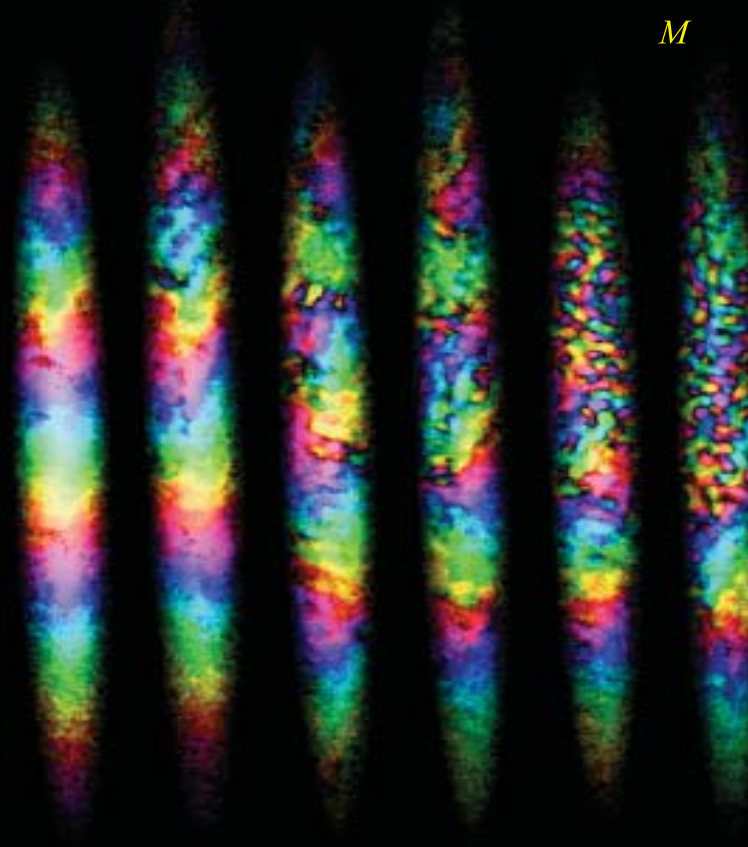
with gradient  
non-zero-wavevector helix

# Dissolving spin textures



30 60 90 120 150 180

initial texture = uniform

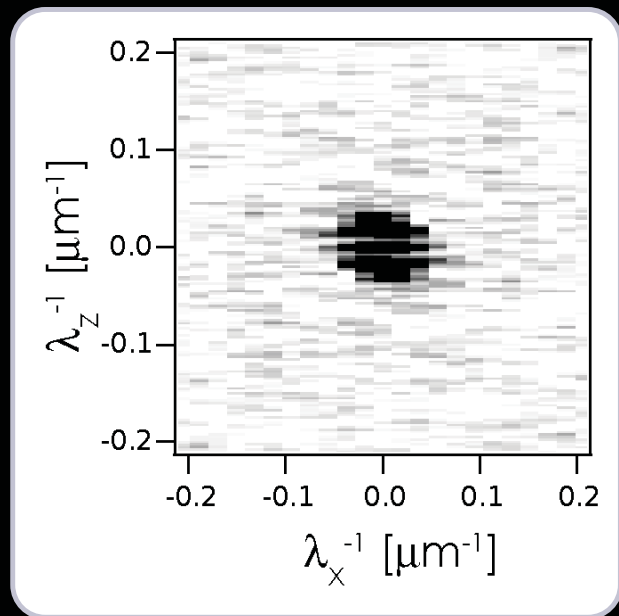


30 60 90 120 150 180 ms

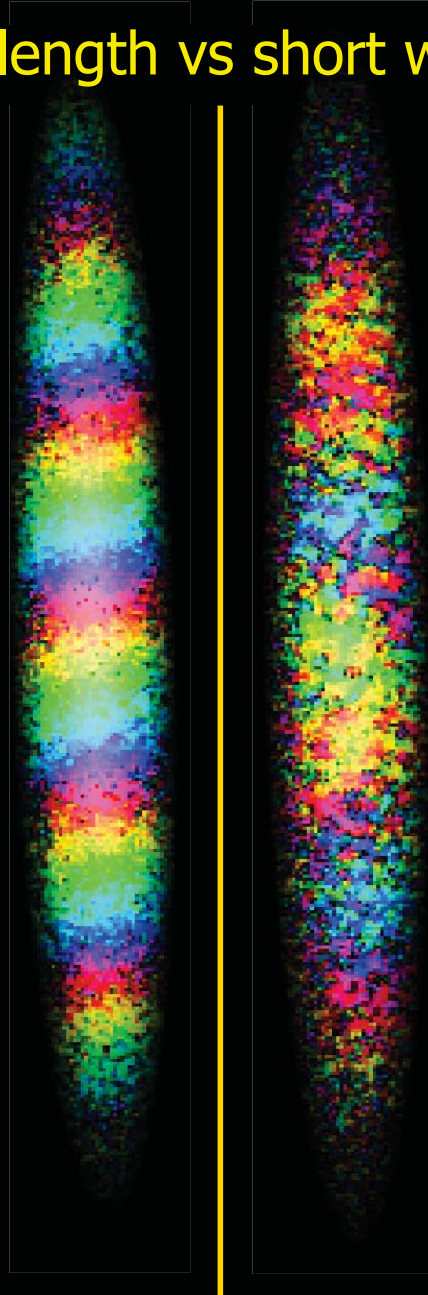
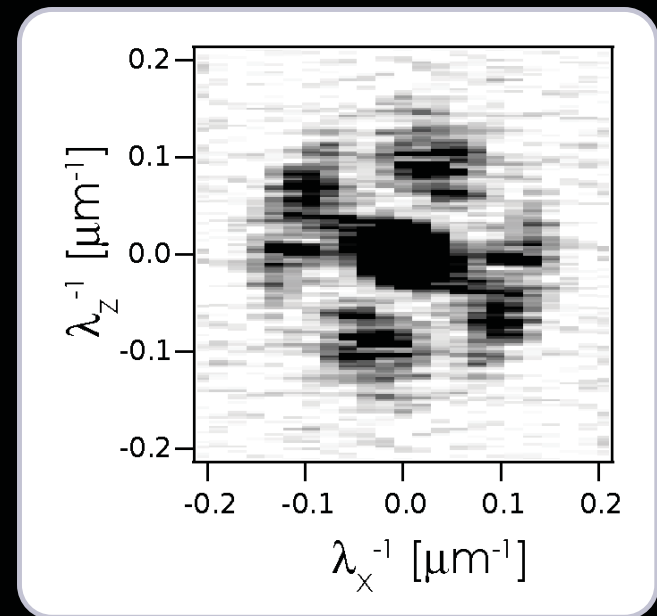
initial texture = wound up

## Long wavelength vs short wavelength order

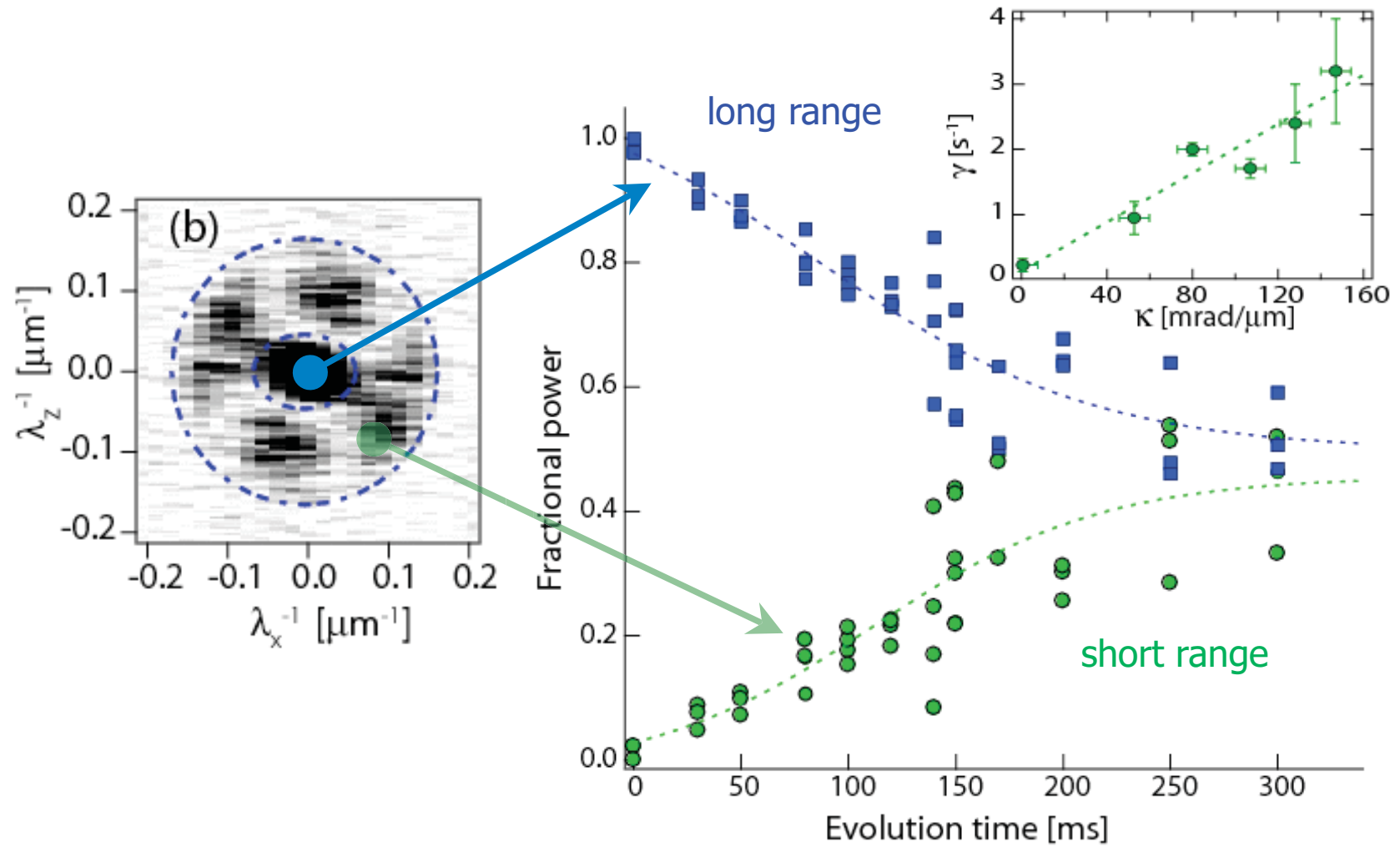
Initial texture



Final texture

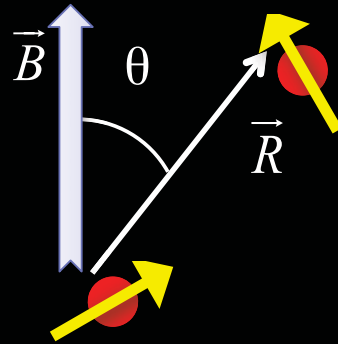


# Long wavelength vs short wavelength order





## tempering dipolar interactions



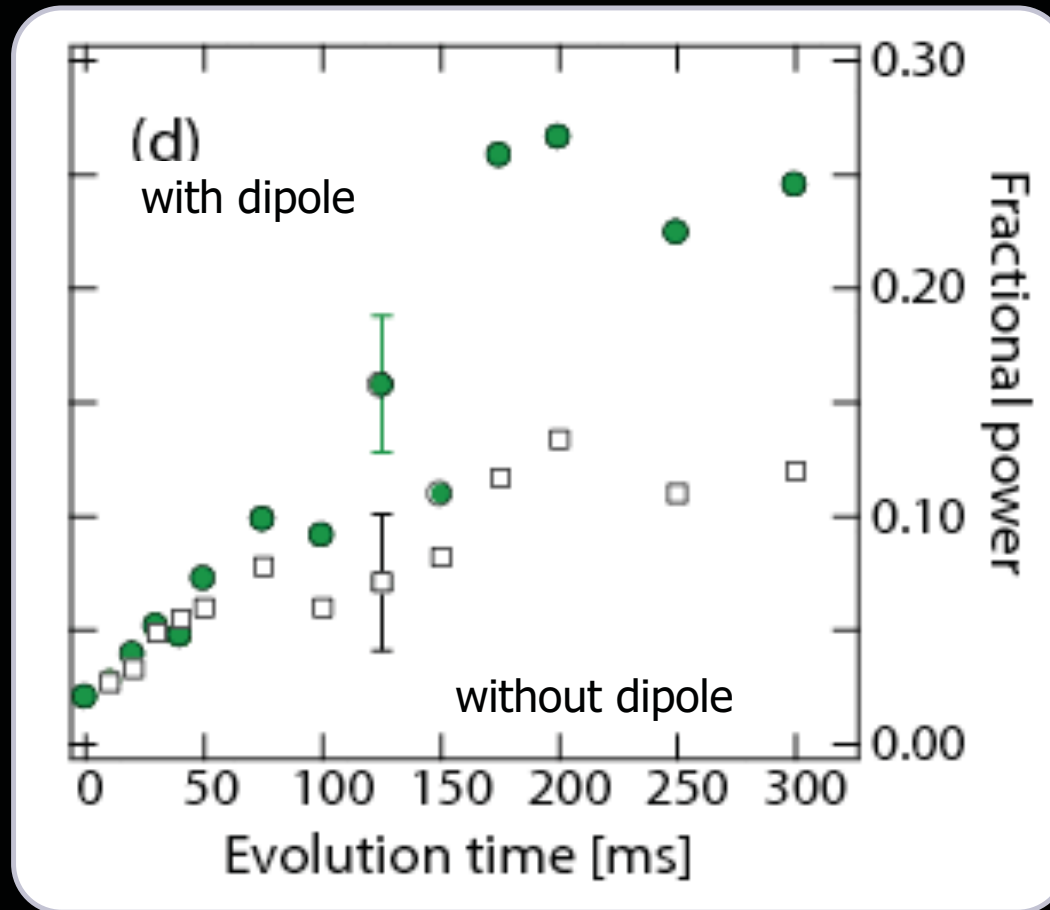
$$U = -J \left( \frac{3}{2} \cos^2 \theta - \frac{1}{2} \right) \left[ F_{1,z} F_{2,z} - \frac{1}{2} (F_{1,x} F_{2,x} + F_{1,y} F_{2,y}) \right]$$

- Magic angle spinning (hard for us)
- Stochastic spin-flip narrowing: repeated RF ( $\pi/2$ ) pulses with random phase (easy for us)

## Evolution with/without dipolar interactions

with  
dipole

without  
dipole



Strength of short lengthscale modulation

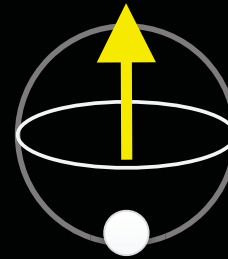
"Spontaneously modulated spin textures in a dipolar spinor BEC,"  
PRL **100**, 170403 (2008)

# Quantum states of an F=1 atom

Examples:

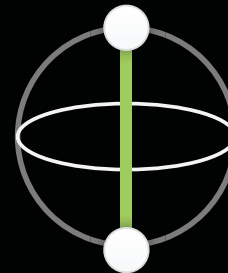
"magnetic"  
"oriented"

$$\Psi = \hat{R} |m_z = 1\rangle$$



"non-magnetic"  
"nematic"  
"aligned"

$$\Psi = \hat{R} |m_z = 0\rangle$$



# Ferromagnetic spin textures

energy budget:

● spin-dependent contact interaction:

$$-|c_2|n|\langle\vec{F}\rangle|^2 \quad \sim -0.5 \text{ nK, minimized}$$

● quadratic Zeeman shift:

$$qF_z^2 = \frac{q}{2} \quad \text{excess} \sim 30 \text{ pK; } \lambda = 60 \text{ } \mu\text{m}$$

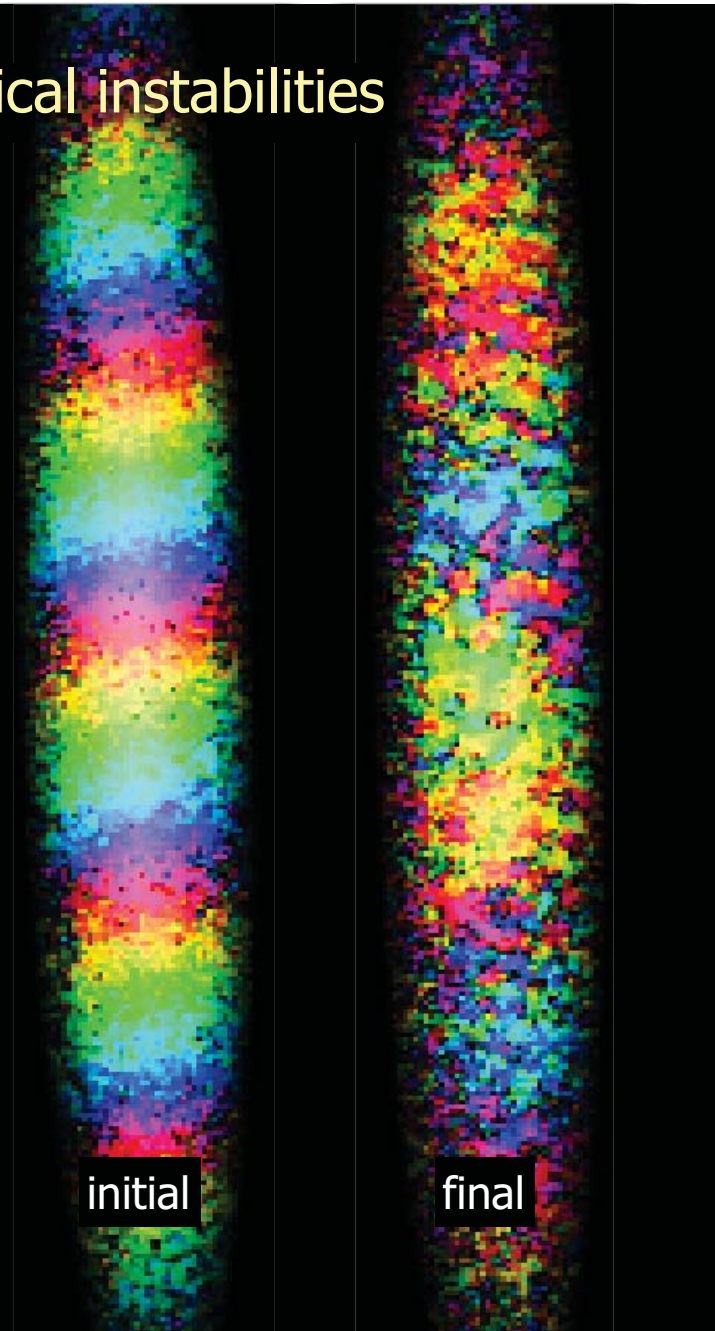
● spin current kinetic energy

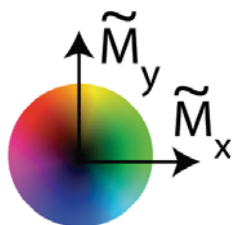
$$\lambda \geq 50 \text{ } \mu\text{m} \quad \nu \leq 1 \text{ Hz}$$

## Possible role of dynamical instabilities

- Lamacraft, PRA 77, 062622 (2008),  
Cherng, et al., PRL 100, 180404 (2008)
- ◆ spiral state is dynamically unstable

But whence the energy?

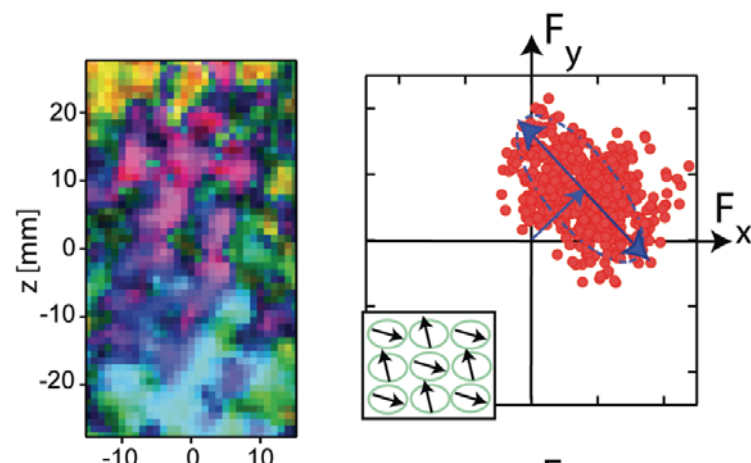
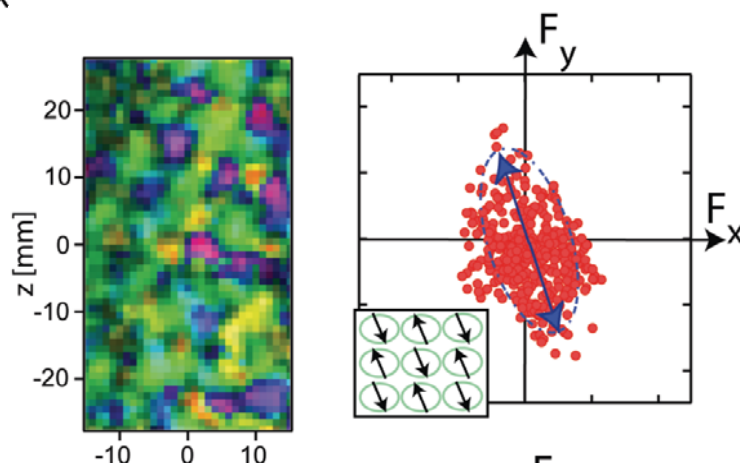




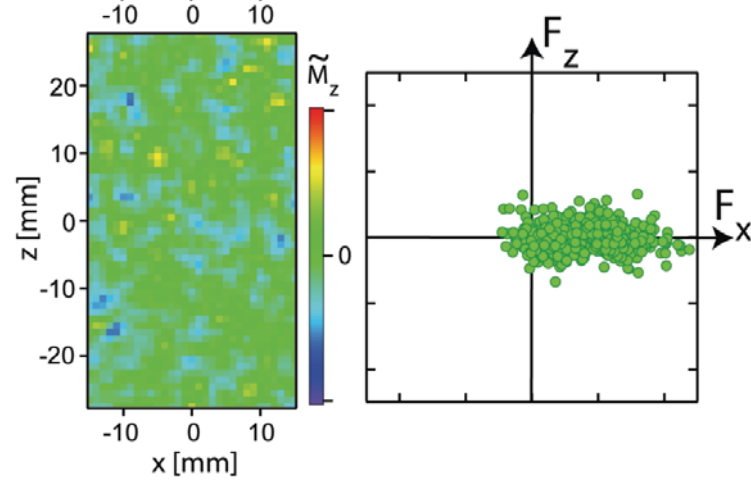
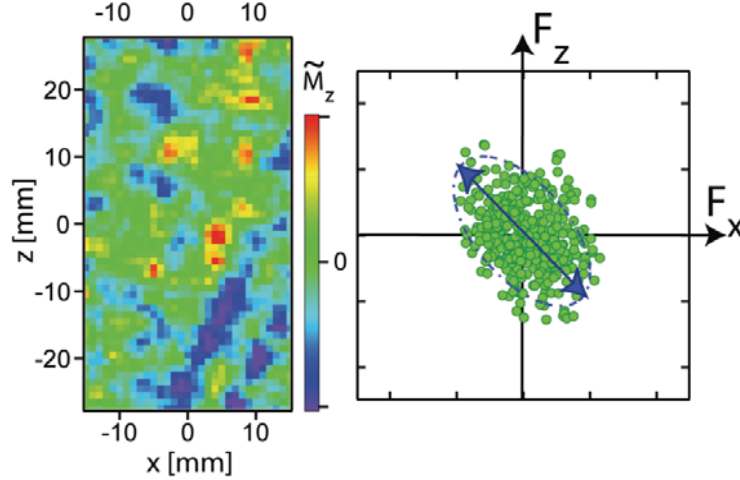
initial  $\eta=0$

initial  $\eta=1/4$

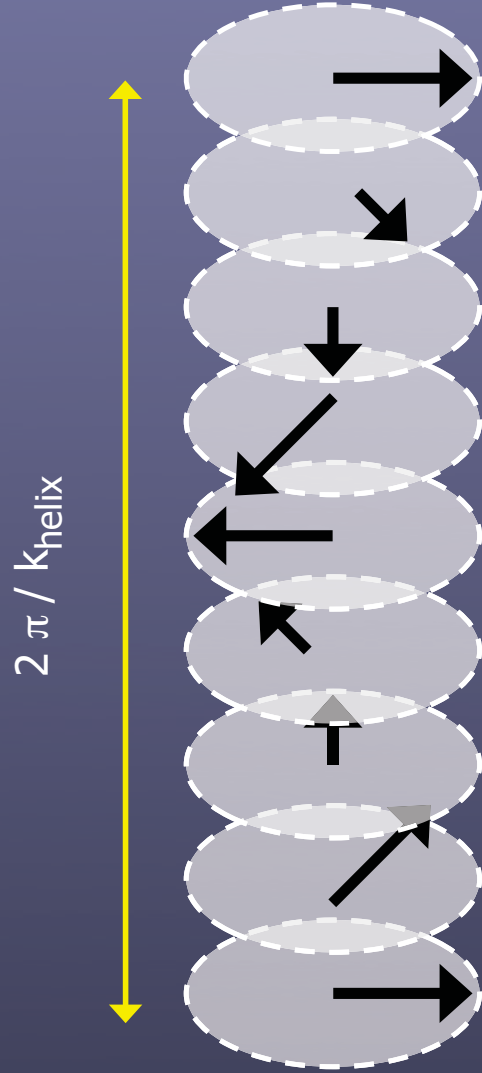
transverse



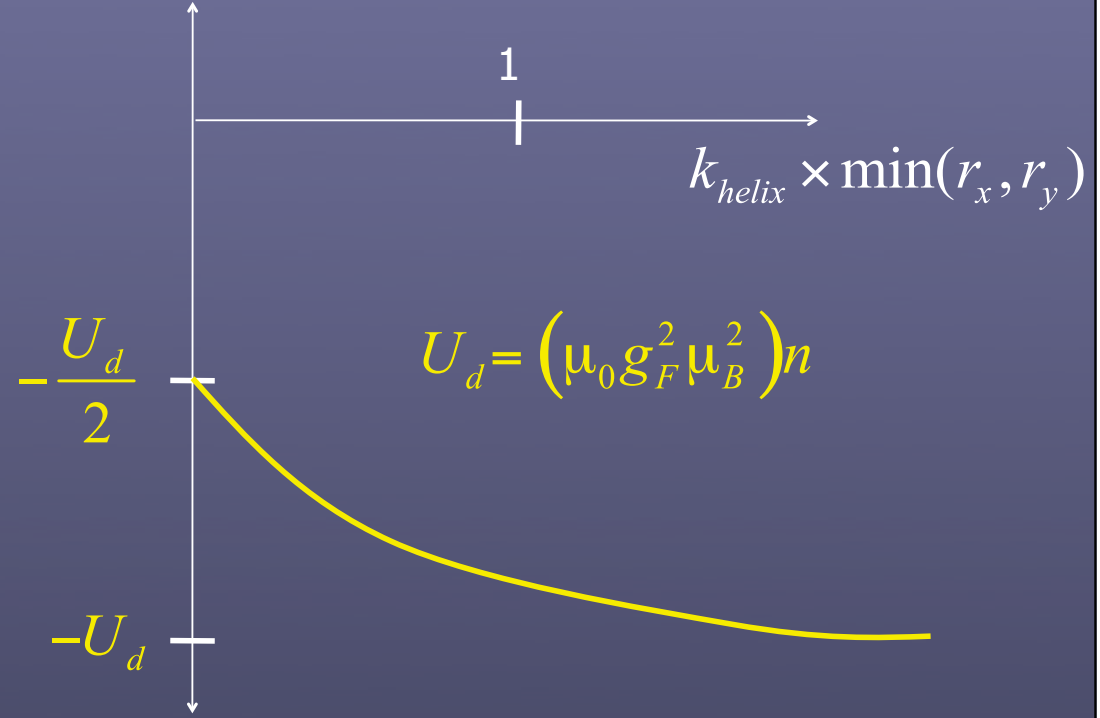
longitudinal

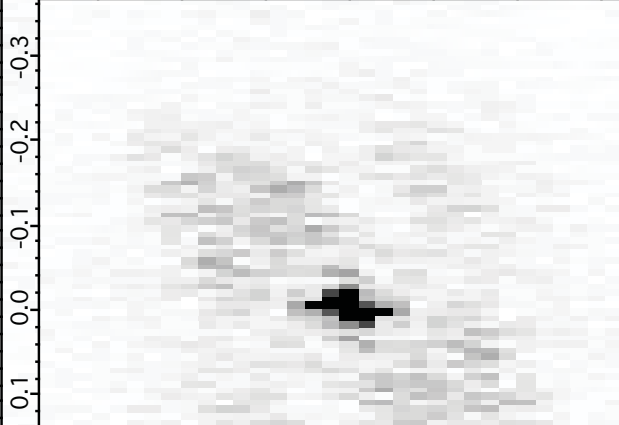
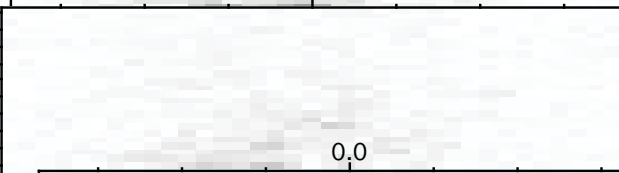
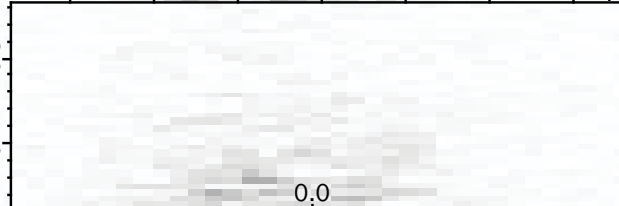
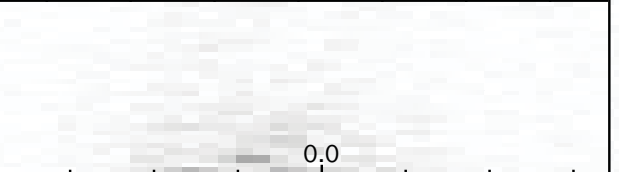
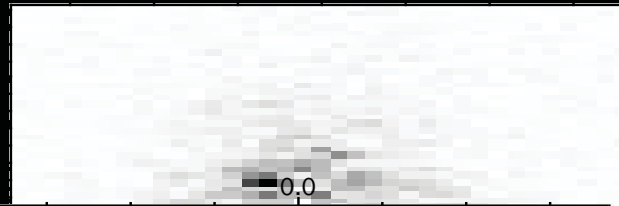
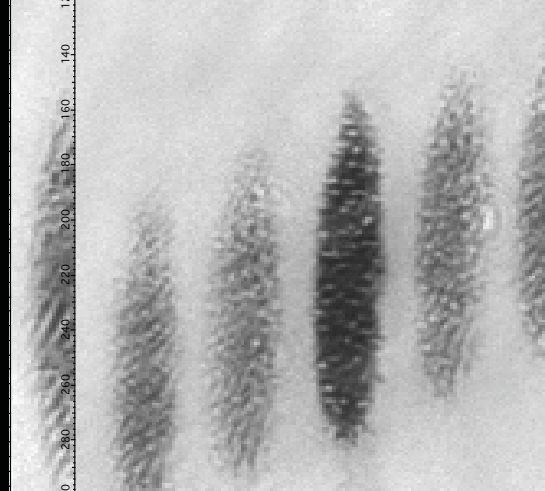
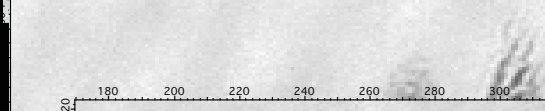
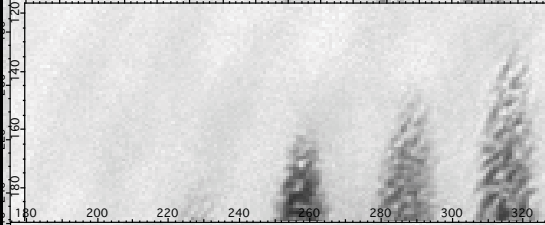
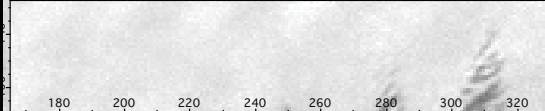
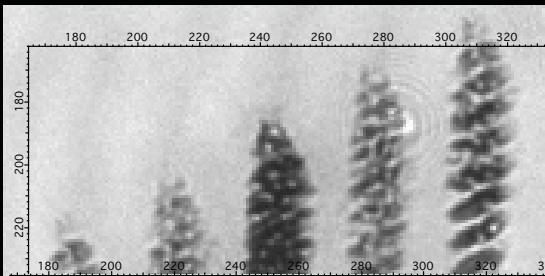


## Dipolar interactions in the spin helix



magnetic dipole energy







## Supersolid = superfluid + solid?



"stiff" – shear modulus  
spatially ordered  
constituents "localized"



"flows"  
not ordered  
constituents "delocalized"

- Does quantum mechanics blur the distinction between these at  $T=0$ ?