



**The Abdus Salam
International Centre for Theoretical Physics**



2030-19

Conference on Research Frontiers in Ultra-Cold Atoms

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Emergence of turbulence in an oscillating Bose-Einstein condensate

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Emergence of “turbulence” in a Bose-Einstein condensate: excitation by external oscillation

BEC project:

Theory :

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M. Caracanhas

Outside Collaborators:

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V. Yukalov (Russia)

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www.cepof.ifsc.usp.br

Experiment :

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E.A.L. Henn
J.A. Seman
R. Shiozaki
C. Castelo Branco
P. Castilho
P. Tavares

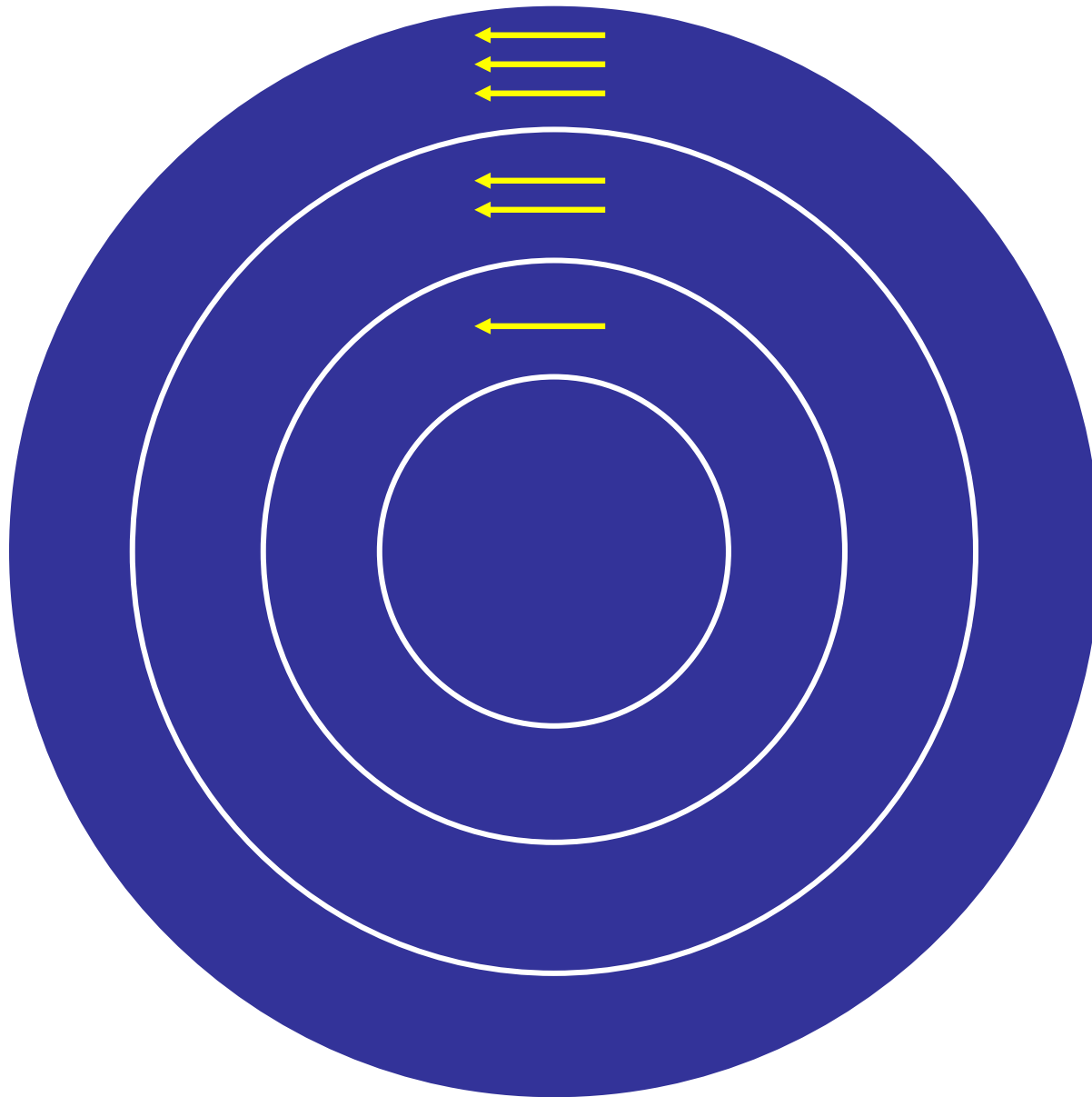
Trapped Bose Condensate and superfluidity

Investigation of Scissors Mode (rotation of the cloud around the symmetry axis)

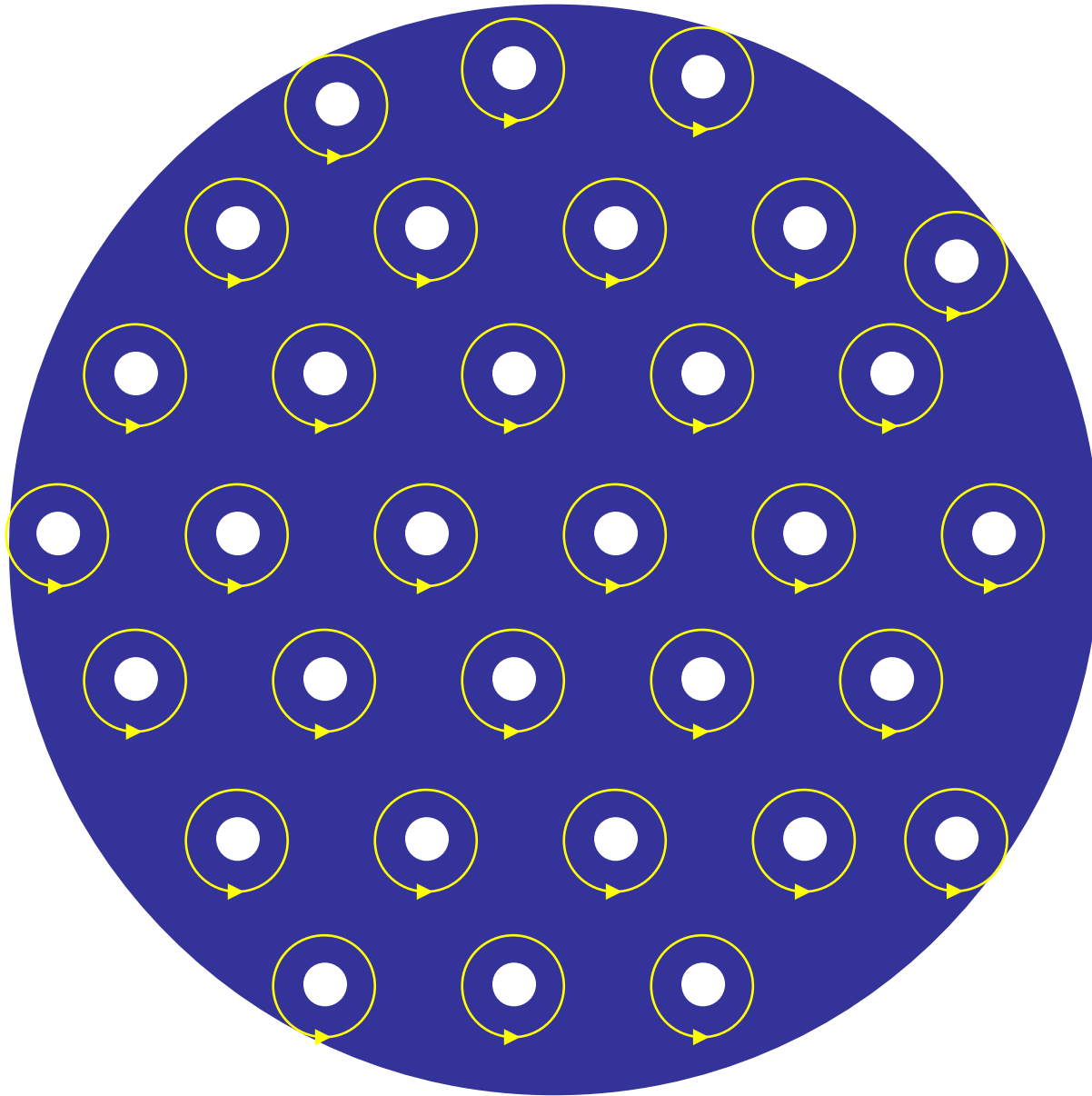
(proposed) Trento – Phys. Rev. Lett. 83,4452(1999)

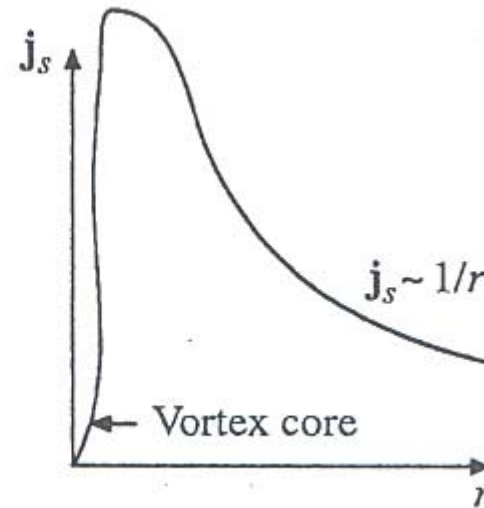
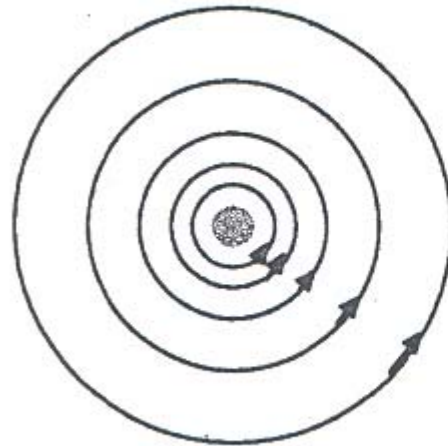
**(experiment) Oxford – Phys. Rev. Lett. 84,2056(2000)
and Phys. Rev. Lett. 86,3938(2001)**

Introducing rotation to the cloud



Vortex structure



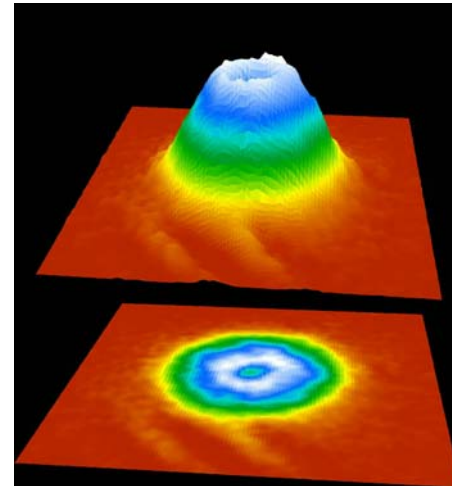
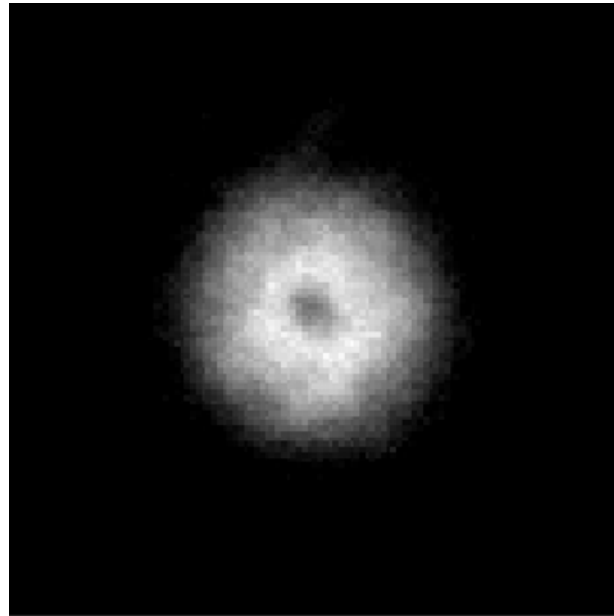


Healing length = $(8\pi \rho a)^{-1/2}$

Can be macroscopic ~ 1 micron

Vortex

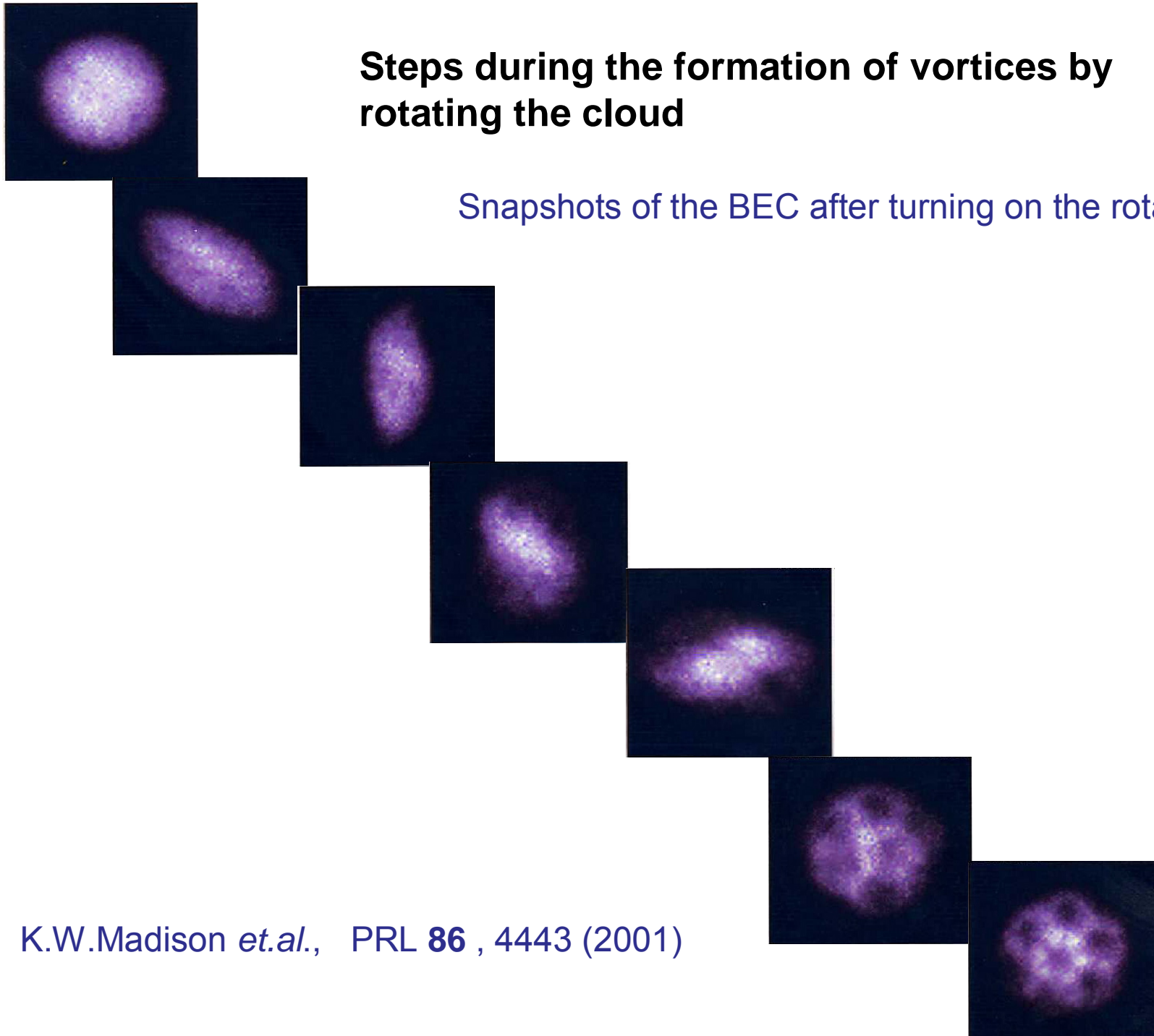
After
time-of-flight
expansion:



J.DALIBARD

Steps during the formation of vortices by rotating the cloud

Snapshots of the BEC after turning on the rotation



K.W.Madison *et.al.*, PRL **86** , 4443 (2001)

There are many studies of vortices in BECs

- Measuring angular momentum – PRL85(2000)
- Nucleation by instabilities in the rotation PRL 86 (2001)
- Phase measurement – PRA 64 (2001)
- Dynamics of single vortex line and observation of Kelvin modes – PRL90(2003)
- Lattices – many

How are the vortices formed and how is the dynamics?

- Many experiments and many theoretical papers
- Tsubota's group : PRA 65(2002), PRA 71(2005)
- Fetter – Rev. Mod. Phys (2008) and reference there in..
- Dalibard's group – Theory and experiment
- Gardiner's group – Theory
- Recent: Anderson – Nature(2008); PRL(2007)
- Etc..

Are there more things to be done
related to vortices in BEC?

YES

Turbulence like in superfluid He

PRESENTATION

OUTLINE

1 - INTRODUCTION

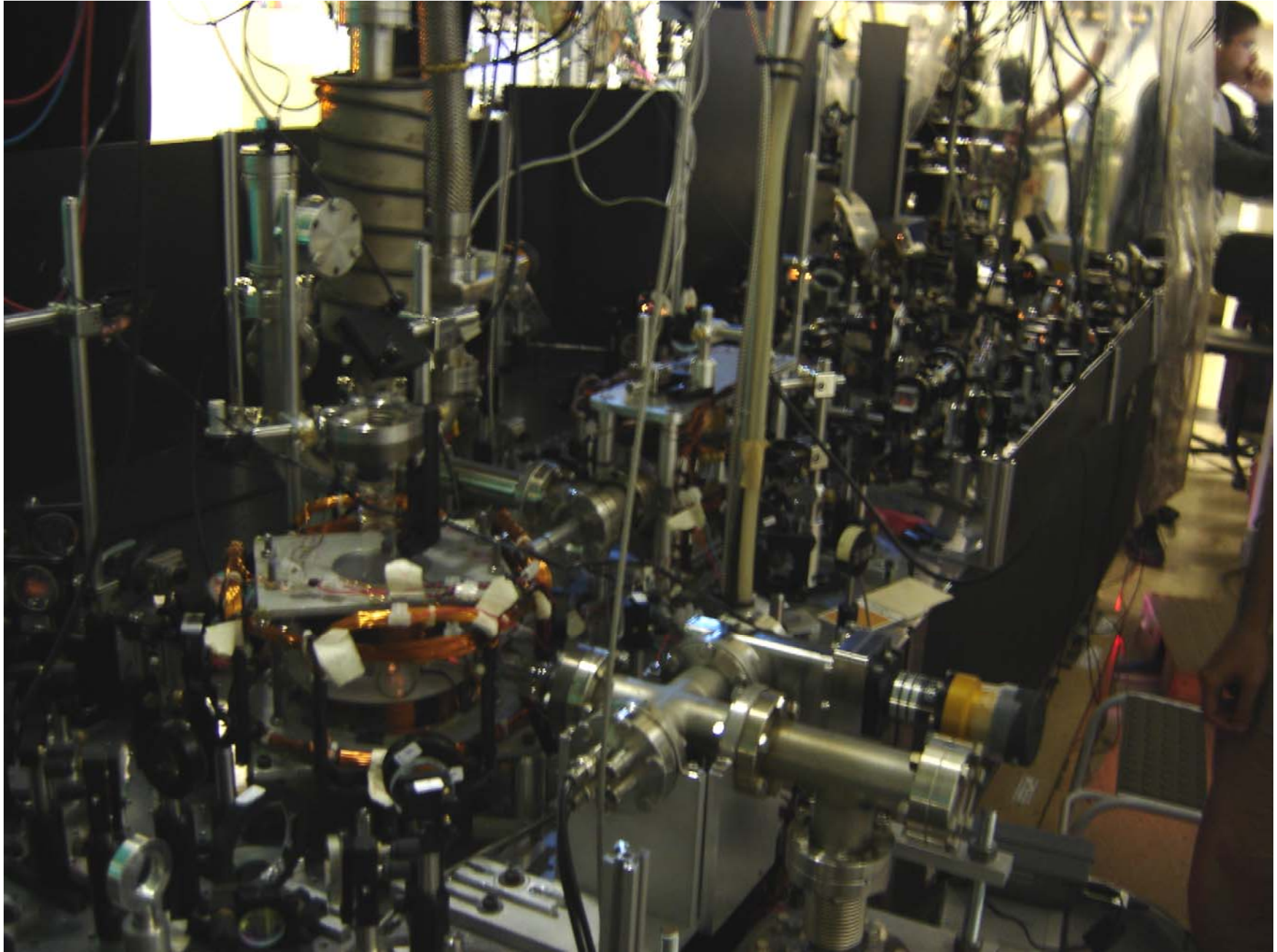
2 - VORTICES FORMED BY OSCILLATIONS

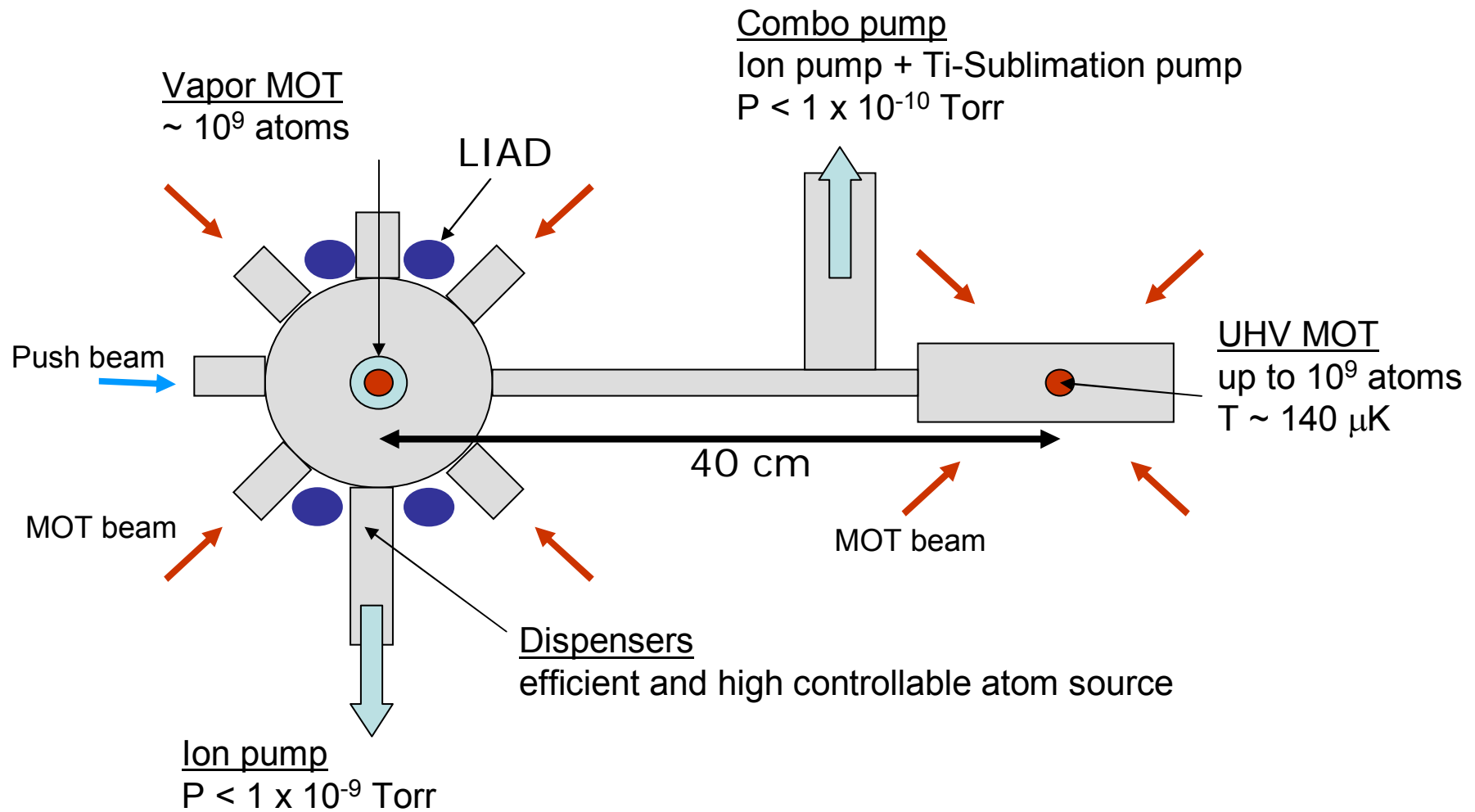
3 – CLUSTERS OF VORTICES: TRIPOLE

4 - EMERGENCE OF VORTICES TANGLE –
“TURBULENCE ? “

5 - FRAGMENTATION

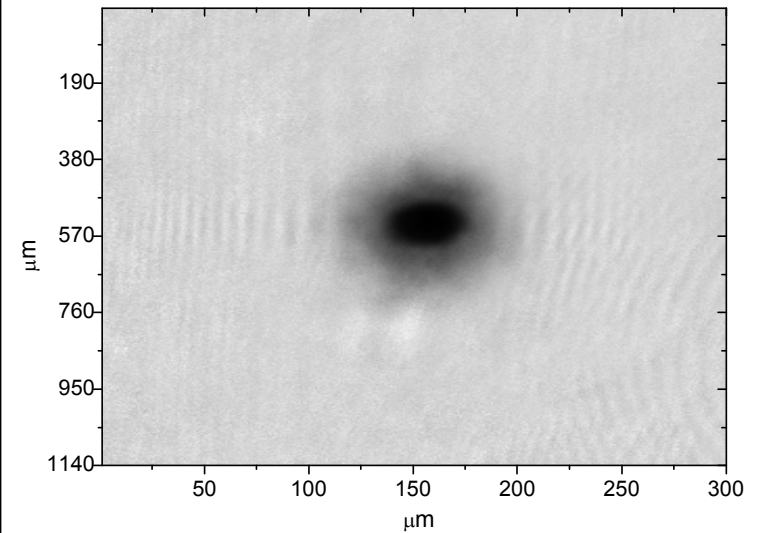
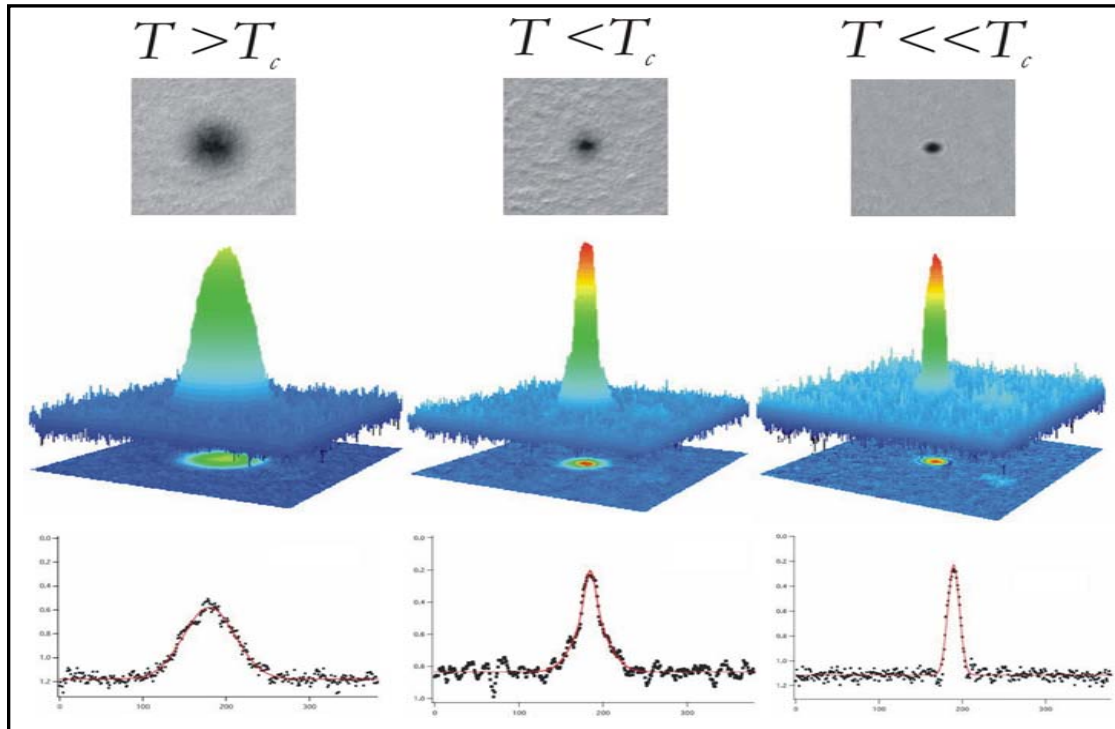
BEC OF Rb





OUTCOME: 1 to 3 x 10⁵ condensate Atoms

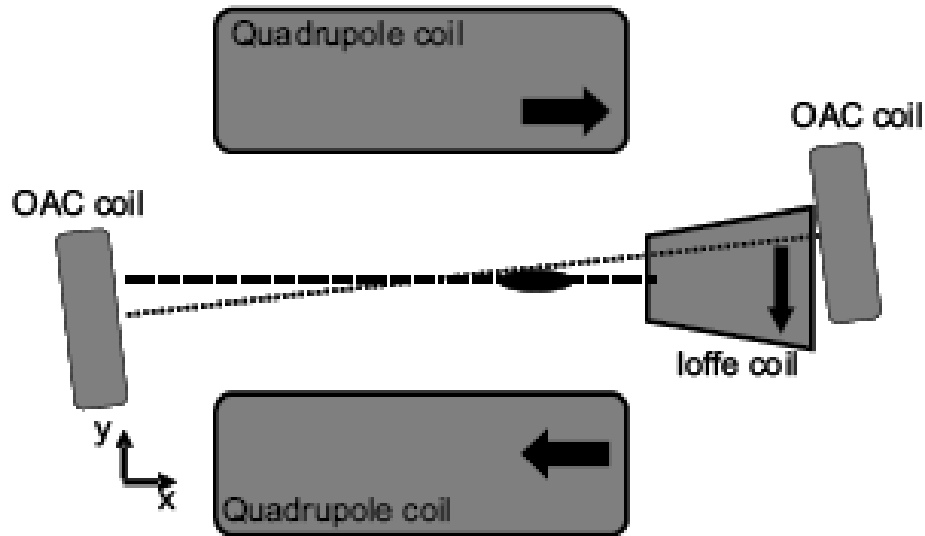
T ~ 80 to 200 nK



Frequencies: $\omega_x = 2\pi \cdot 23 \text{ Hz}$ $\omega_y = \omega_z = 2\pi \cdot 210 \text{ Hz}$

EXCITATION BY EXTERNAL OSCILLATION

**POSSIBILITY TO EXCITE VORTICES OF BOTH SIGNS:
VORTEX AND ANTI-VORTEX**



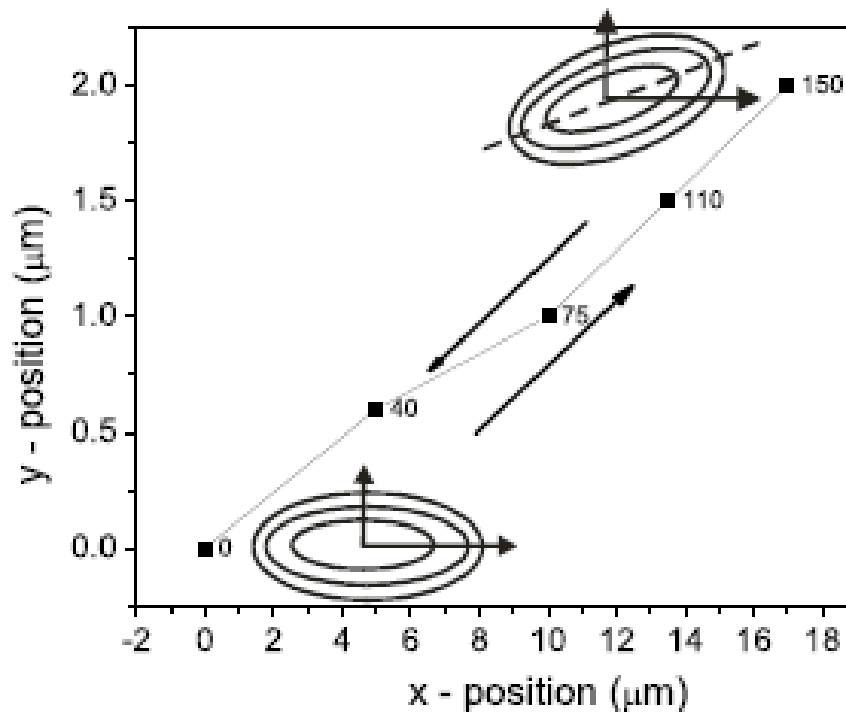
Max add field : 190 mG/cm

Frequency : 0 to 400 Hz

Displacement

Rotation

Deformation of the potential



Larger amplitude of oscillation implies in:

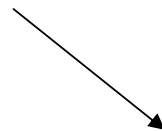
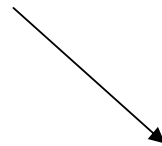
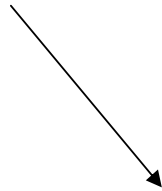
- Larger displacement
- Larger deformation of the potential
- Higher acceleration in the rotation

PRODUCING BEC (1 MIN)

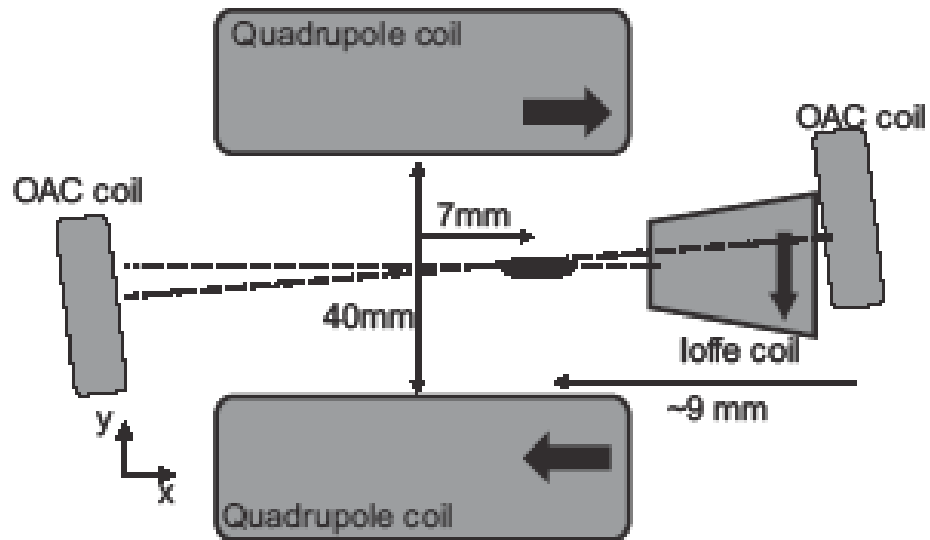
EXCITATION (0 TO 70 ms)

Rest (20 ms)

TOF FOLLOED BY ABSORPTION IMAGE

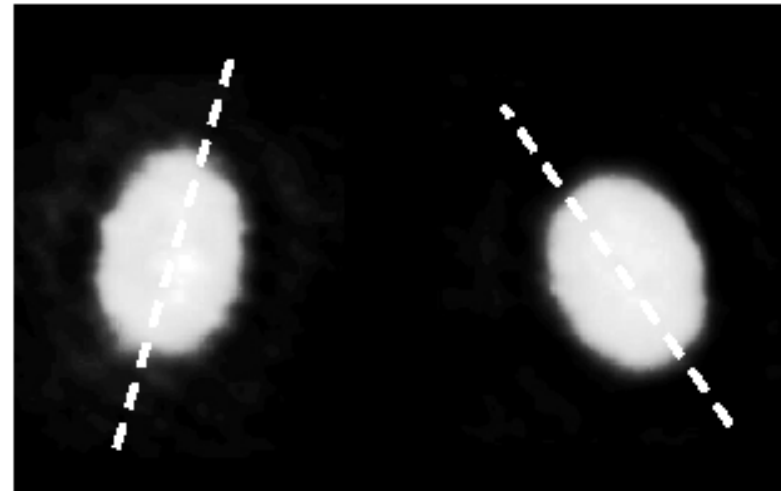


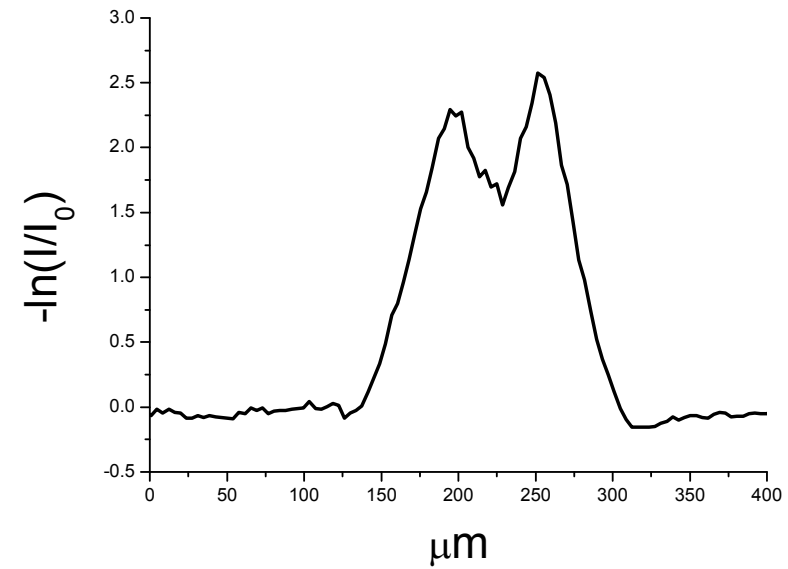
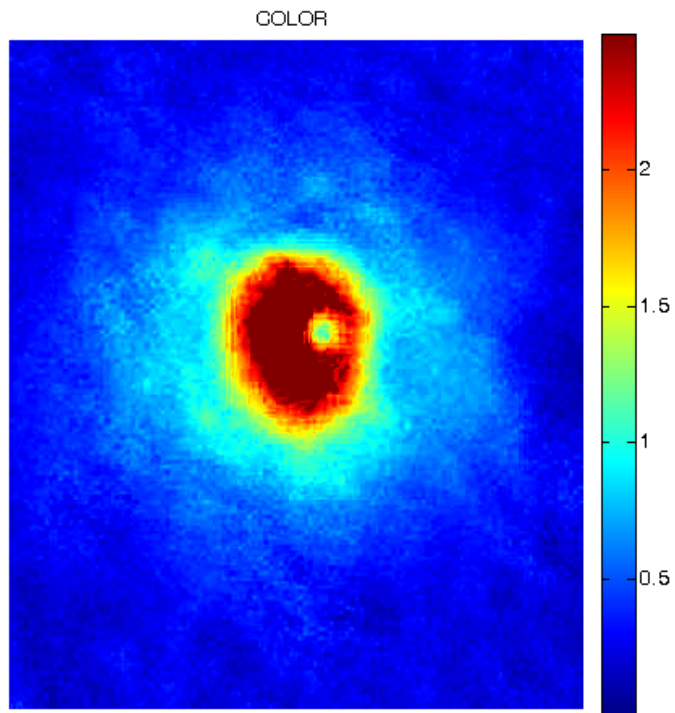
Small amplitudes and/or small times of excitation



Oscillatory banding

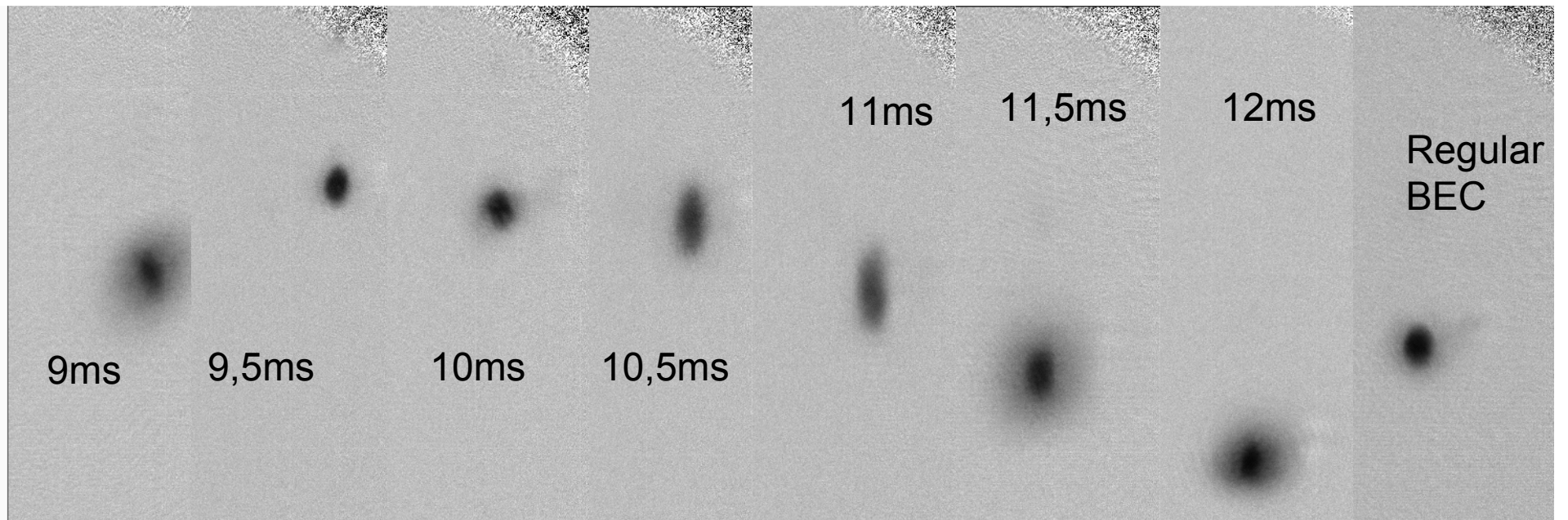
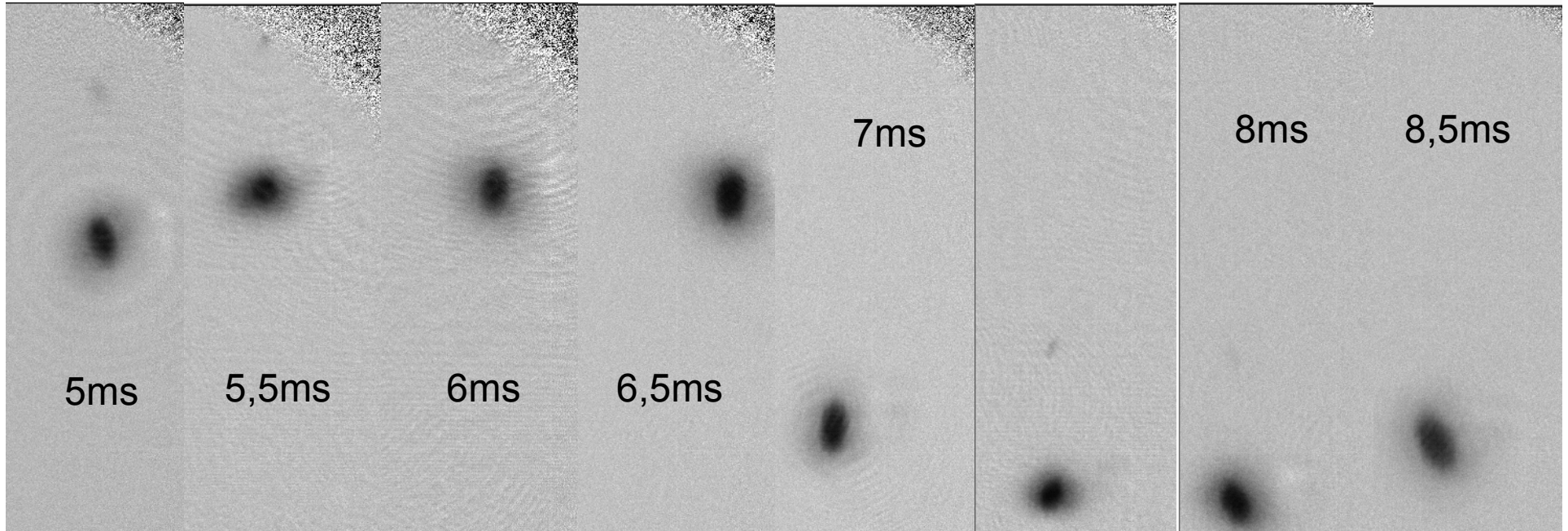
Equivalent to oscillations
generated by sudden rotations →
Scissors Mode





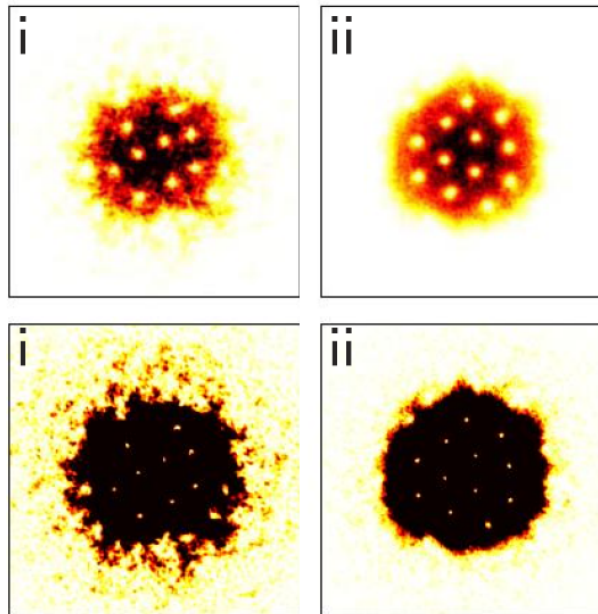
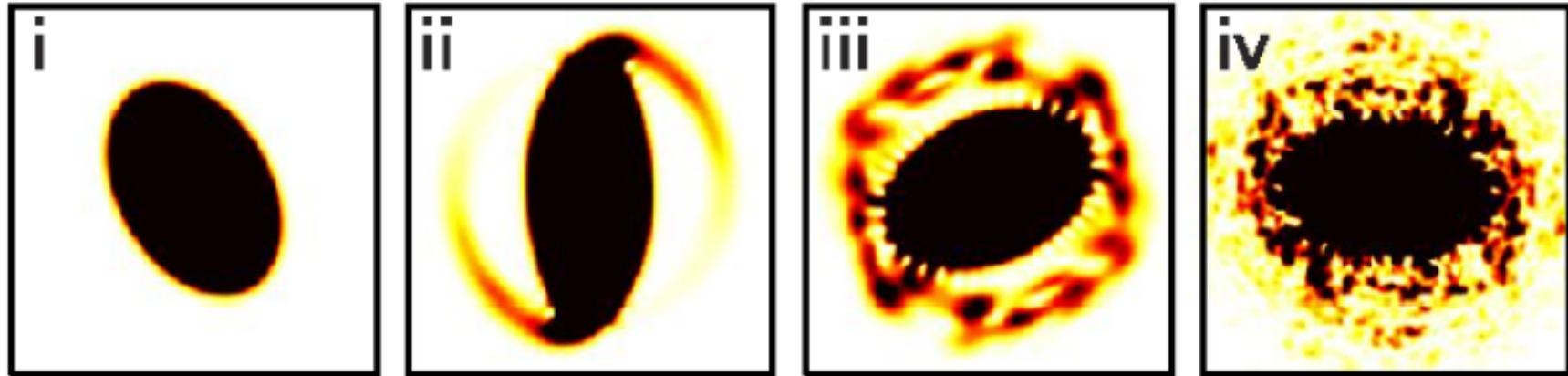
NEXT STEP AFTER BANDING AXIS IS THE OBSERVATION OF A DEEP IN THE ABSORPTION → VORTEX

QUADRUPOLE and dipole EXCITATION



Parker- Adams PRL95(2005) – Stirring BEC

- 1 – Quadrupolar mode breaks down, ejecting energetic atoms to form an outer cloud
- 2- Turbulent cloud containing vortices is formed with a Kolmogorov energy spectrum
- 3- Dissipation and crystallization



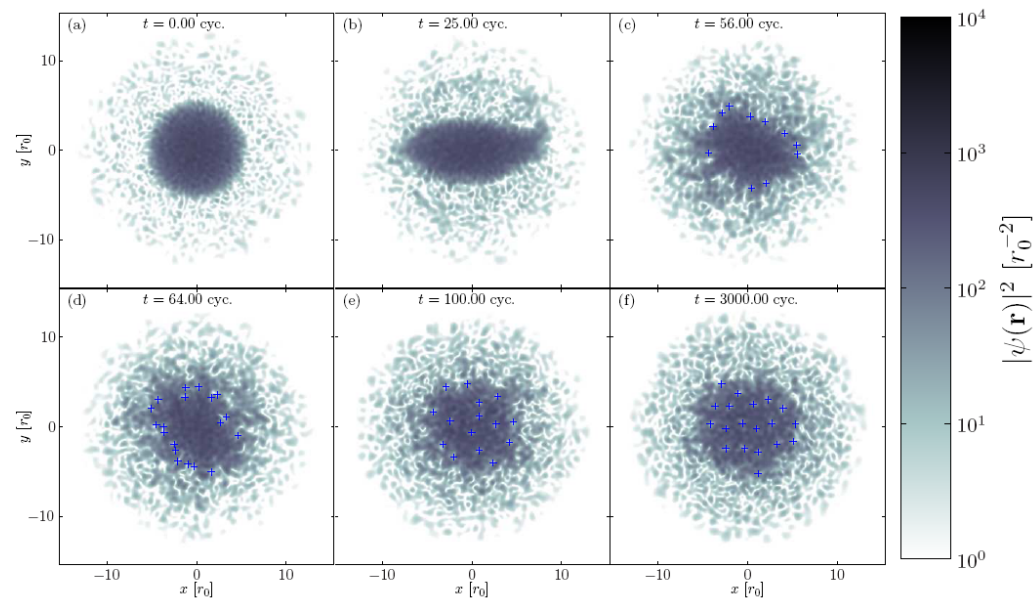
Gardiner et al – arXiv:0808.3553v2

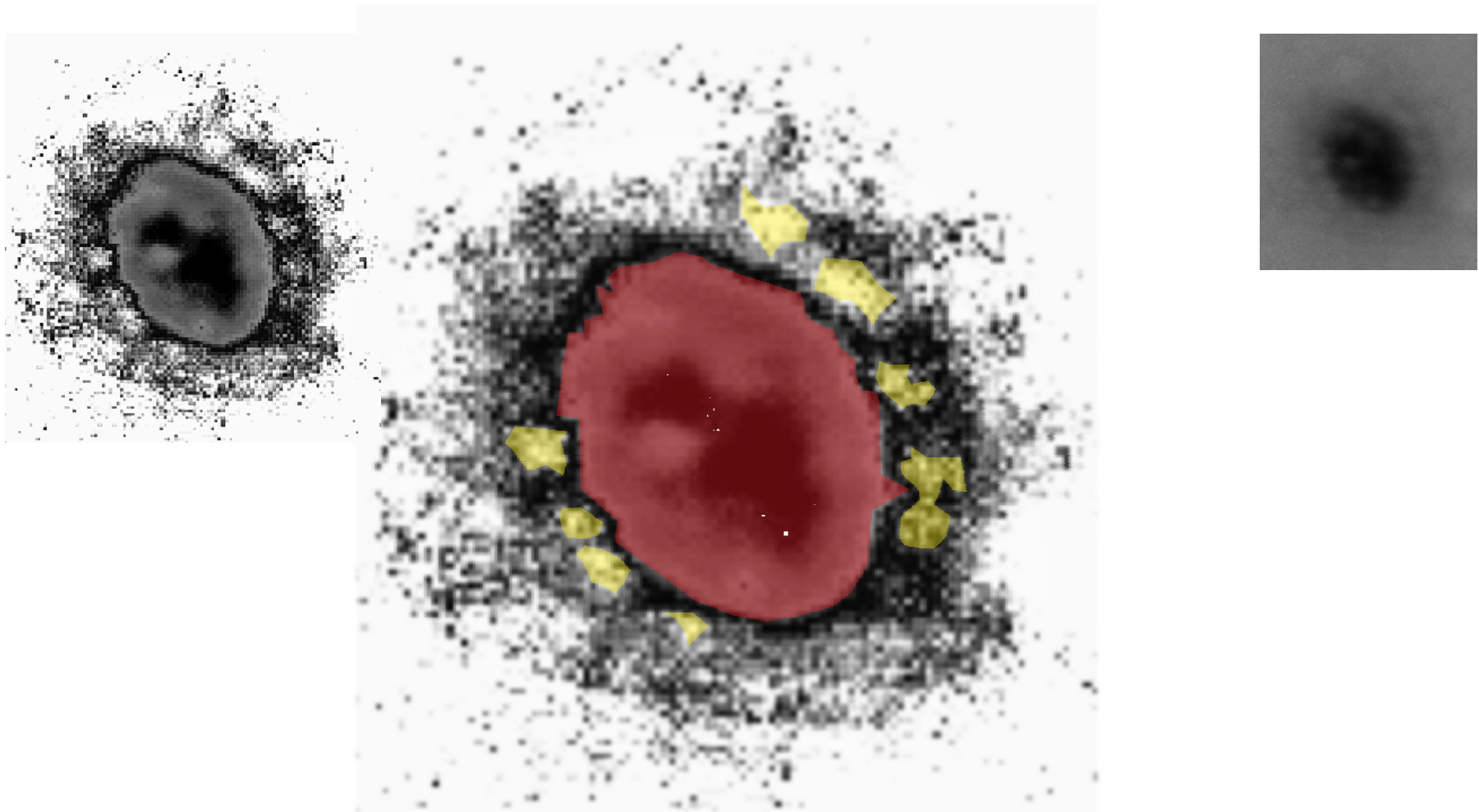
Quadrupole oscillations generate a thermal cloud

Surface oscillations in the BEC grow in magnitude, such oscillations are unstable in the presence of the thermal cloud

Vortices are nucleated and penetrate into the edges of the condensate

Form a lattice



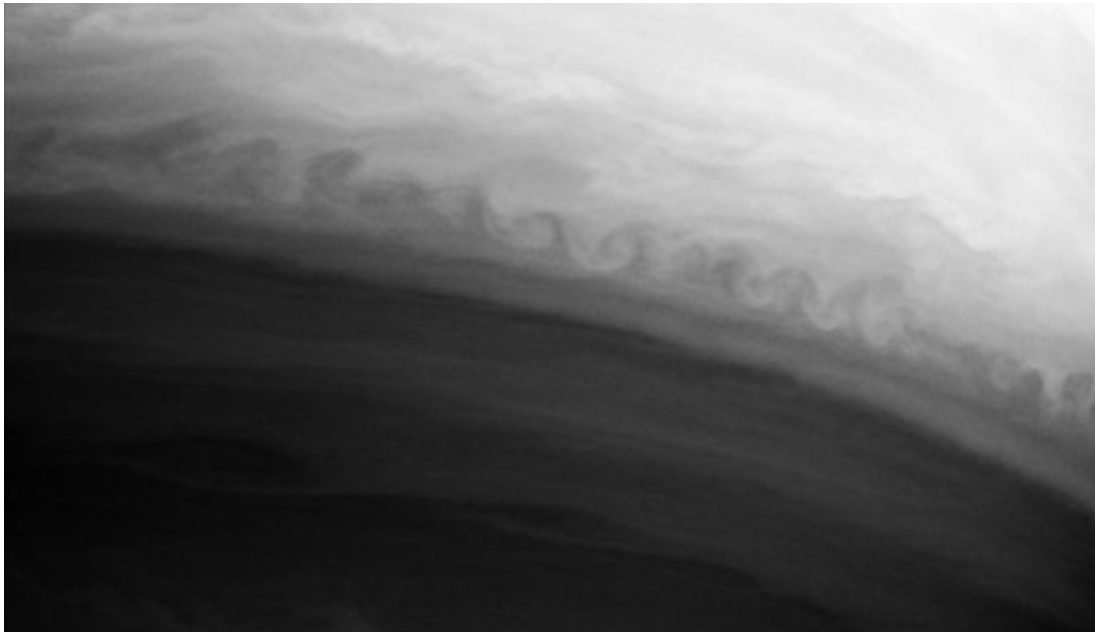


- Injection of vortices from the interface to the quantum fluid

First observation of an individual vortices forming at the edge and migrating to the interior , when rotating the BEC, was done by C. Foot's group in Oxford – PRL88,(2002).

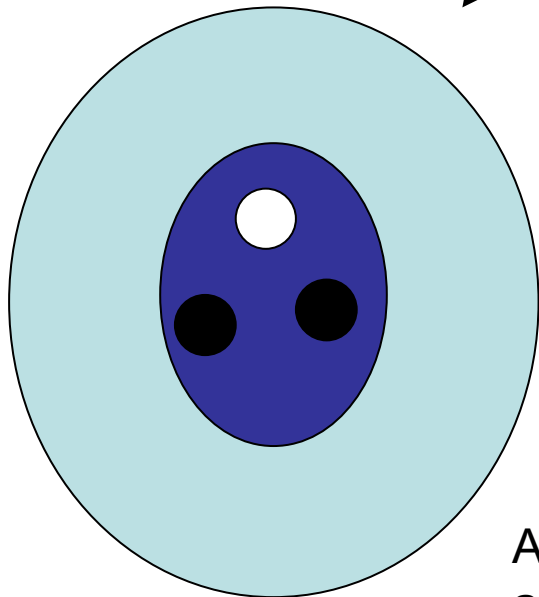
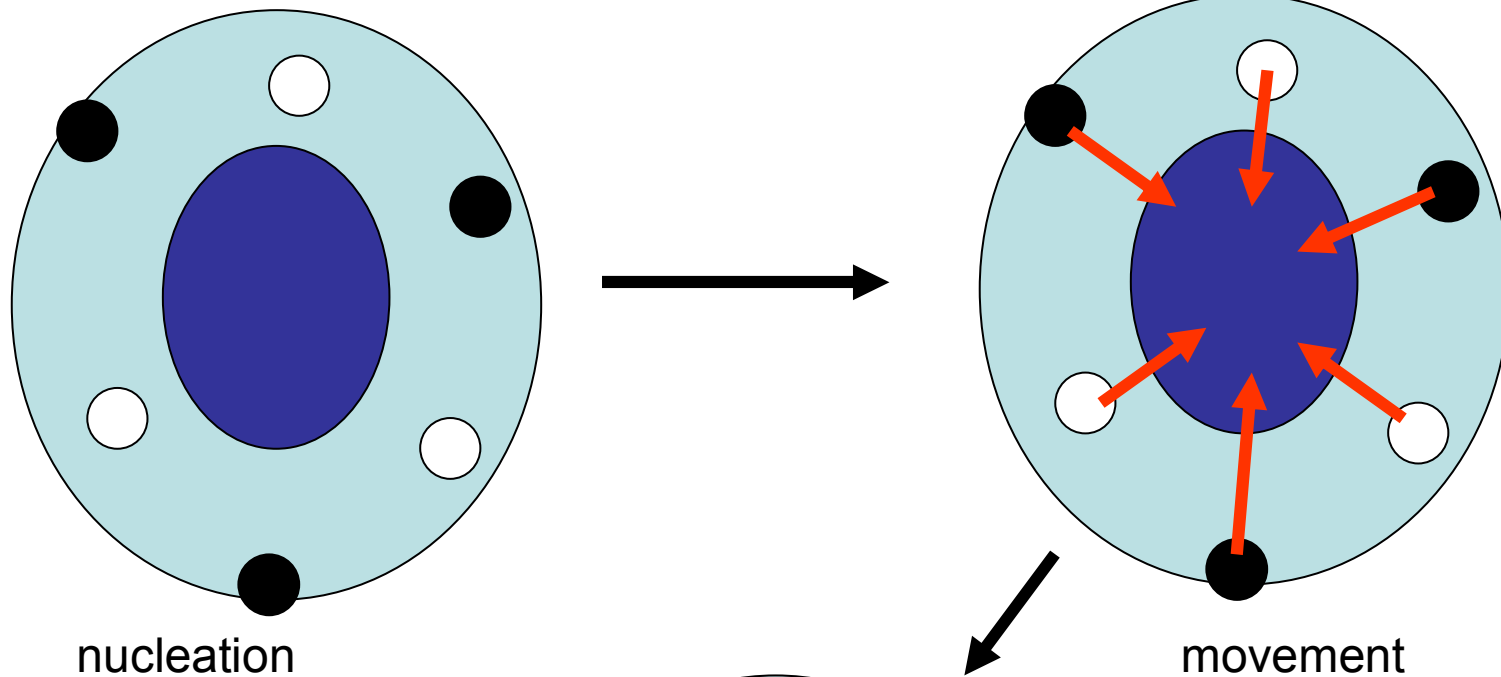
Kelvin type Instability

- At the interface between two fluids with sufficient difference in velocity
- Generation of vortices



Planet Saturn, interface between two layers of atmosphere.

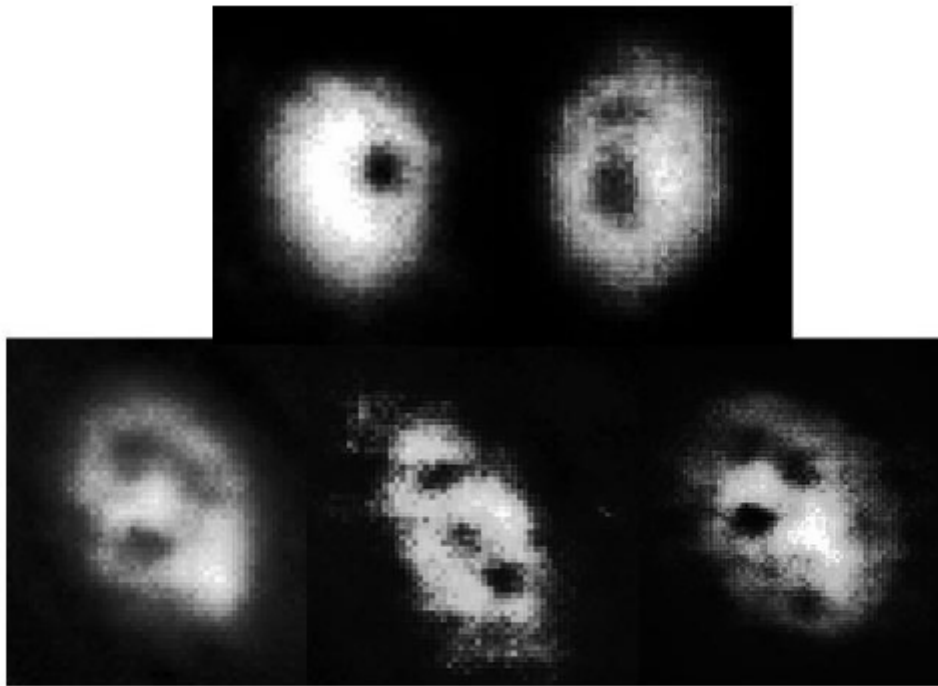
We generate vortices of both signs



Annihilation → final number at time of observation

EVOLUTION WITH AMPLITUDE AND TIME OF EXCITATION

large shot-to-shot fluctuation



Similar core →
equivalent circulation

Phys. Rev. A 79, 043618 (2009)

Fixing frequency \rightarrow varying amplitude and time of excitation

Amplitude or time

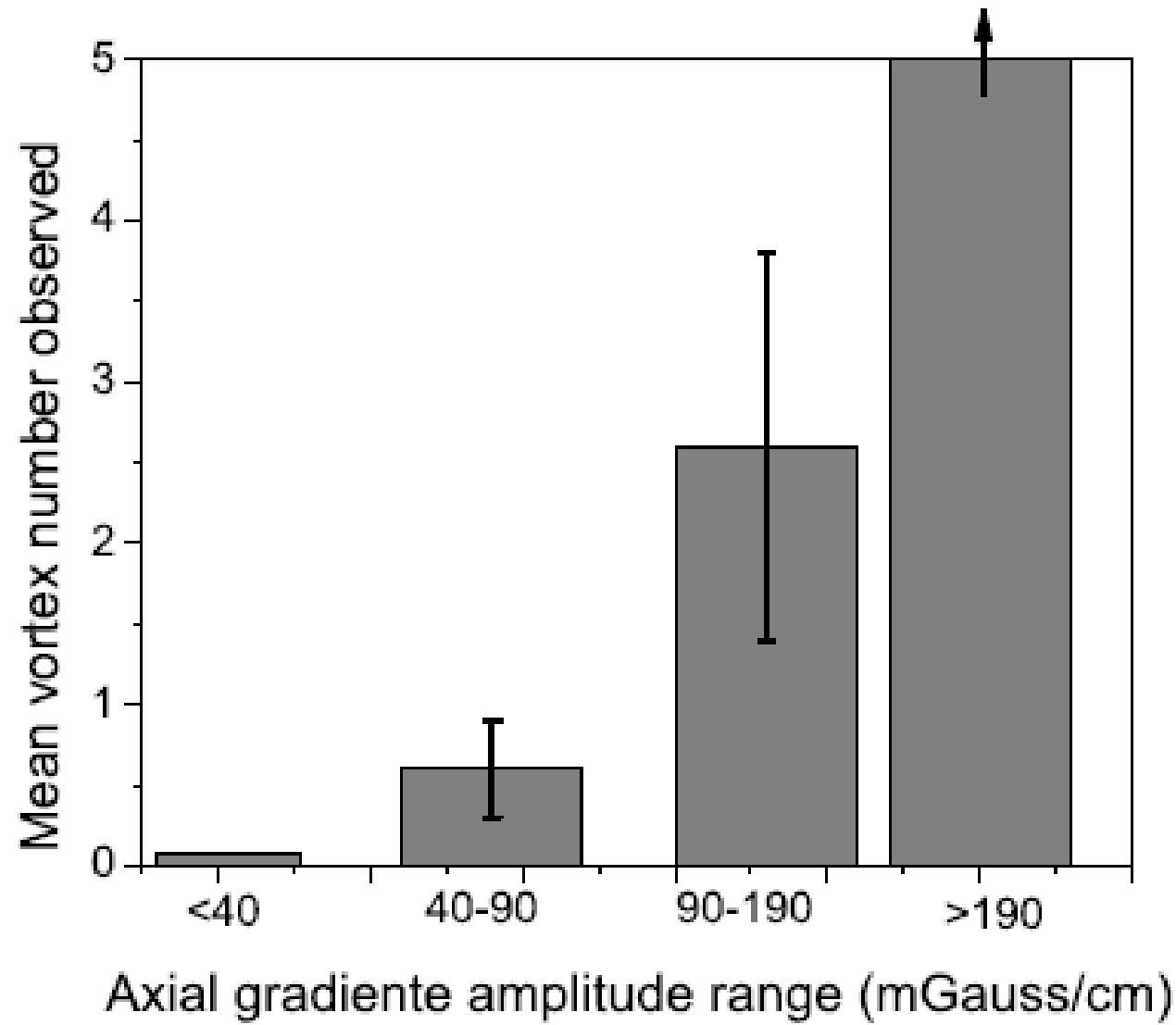


No vortices



Vortices

Fixed time of excitation – 20 ms, TOF 15 ms,
200Hz



VORTEX CLUSTERS

IN A MIXTURE OF VORTEX-ANTIVORTEX: IS POSSIBLE THE FORMATION OF CLUSTERS OF VORTICES

THEORY (Mottonen et al – PRA 71,033626(2005)) PREDICTS THAT:

-DIPOLE AND QUADRUPOLE ARE ENERGETICALLY AND DYNAMICALLY UNSTABLE

-TRIPOLE IS METASTABLE IN A STRONG INTERACTING TRAP

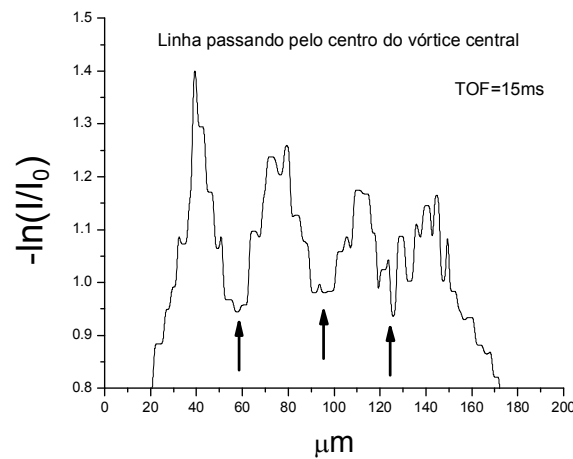
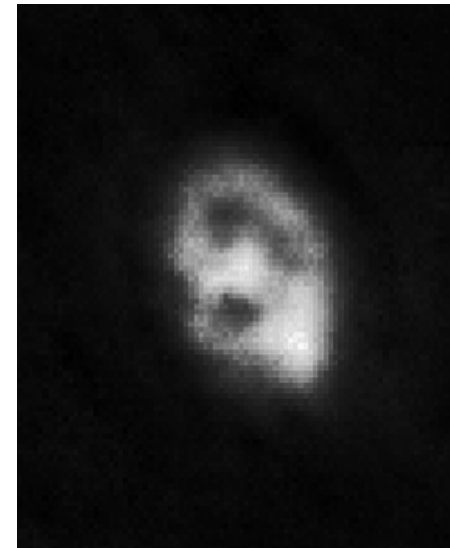
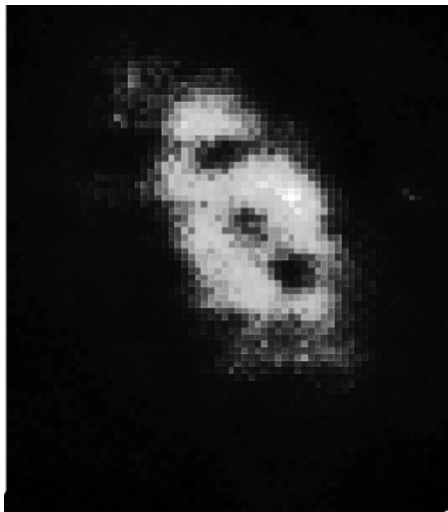
$g \sim N a/l > 108$ $l =$ oscillator length

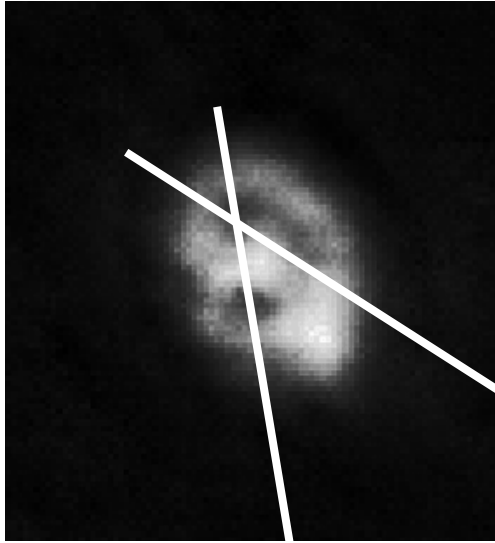
For us $g \sim 500 \rightarrow$ correct g for Metastable tripole

The only clear regularity we observe for a few vortices formed were when a three vortices configuration was observed

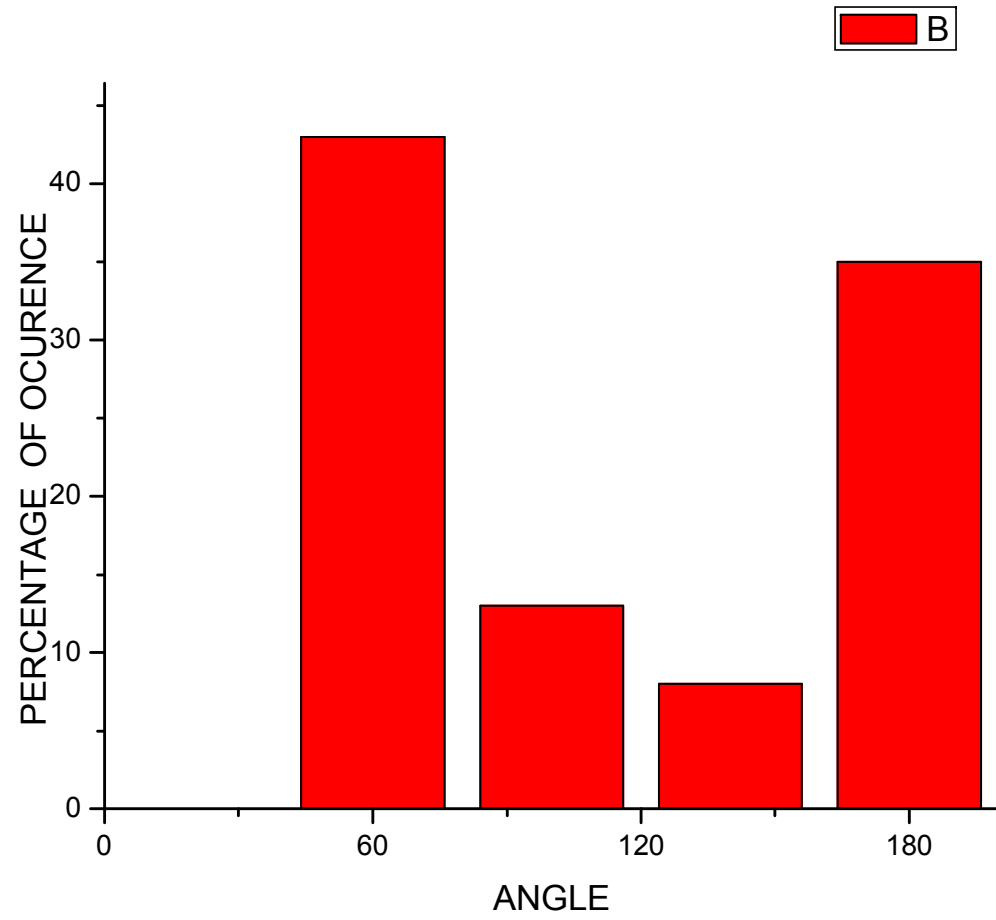
3 vortices stable configurations

From experimental observations, appears to be the only stable structure within the parameters of the experiment (time of excitation, time of resting, amplitude)





56 observations of
3 vortices



Stability and dynamics of vortex clusters in nonrotated Bose-Einstein condensates

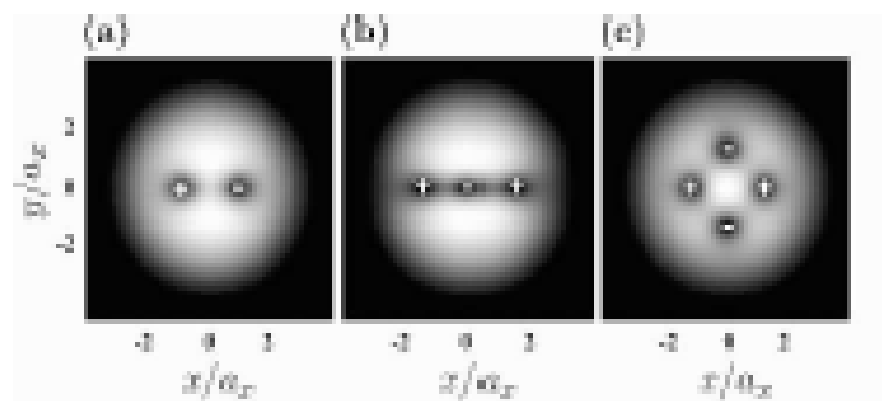
V. Pietilä,¹ M. Möttönen,^{1,2} T. Ioshima,³ J. A. M. Huhtamäki,¹ and S. M. M. Virtanen¹

¹Laboratory of Physics, Helsinki University of Technology, P.O. Box 4100, FI-00015 TKK, Finland

²Low Temperature Laboratory, Helsinki University of Technology, P.O. Box 5500, FI-00015 TKK, Finland

³Department of Physics, Graduate School of Science, Kyoto University, Kyoto 606-8502, Japan

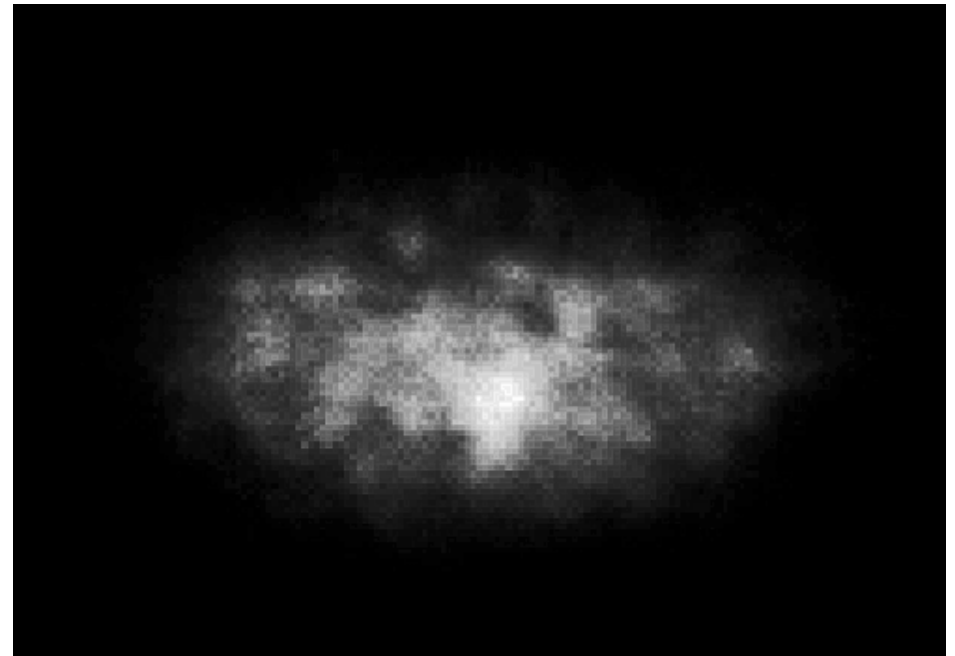
(Date: February 8, 2008)



M. Haque and collaborators : Phys. Rev. A 77, 053610(2008) - Dipoles

Increasing amplitude or time of excitation:

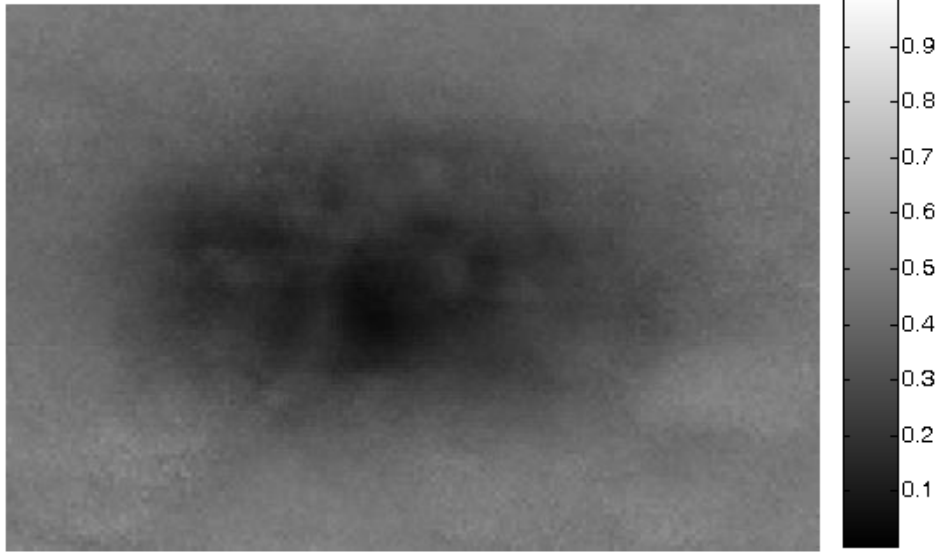
**Explosion → proliferation of many vortices
but no regular pattern**



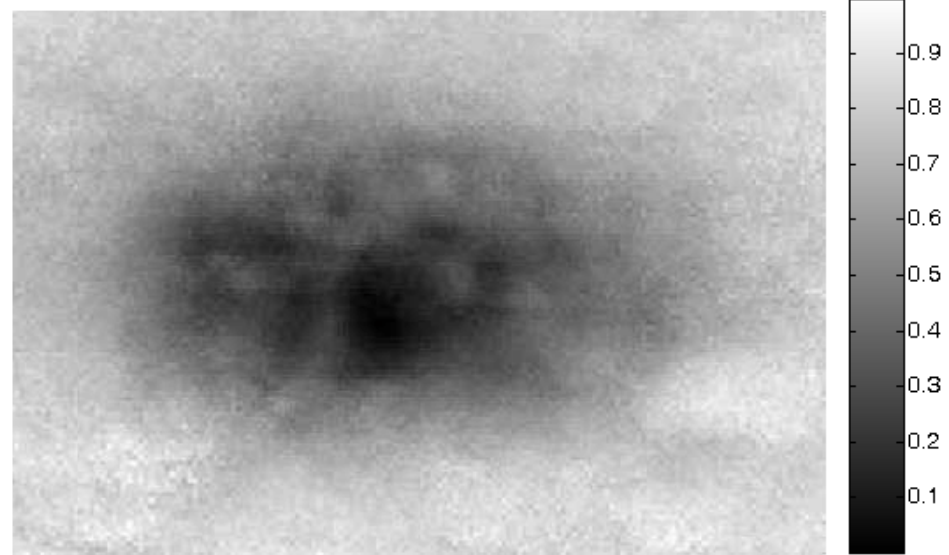
Changing in the behavior of free expansion

**NON REGULAR – MANY
POSITIONS, ORIENTATIONS AND
LENGTH**

Original



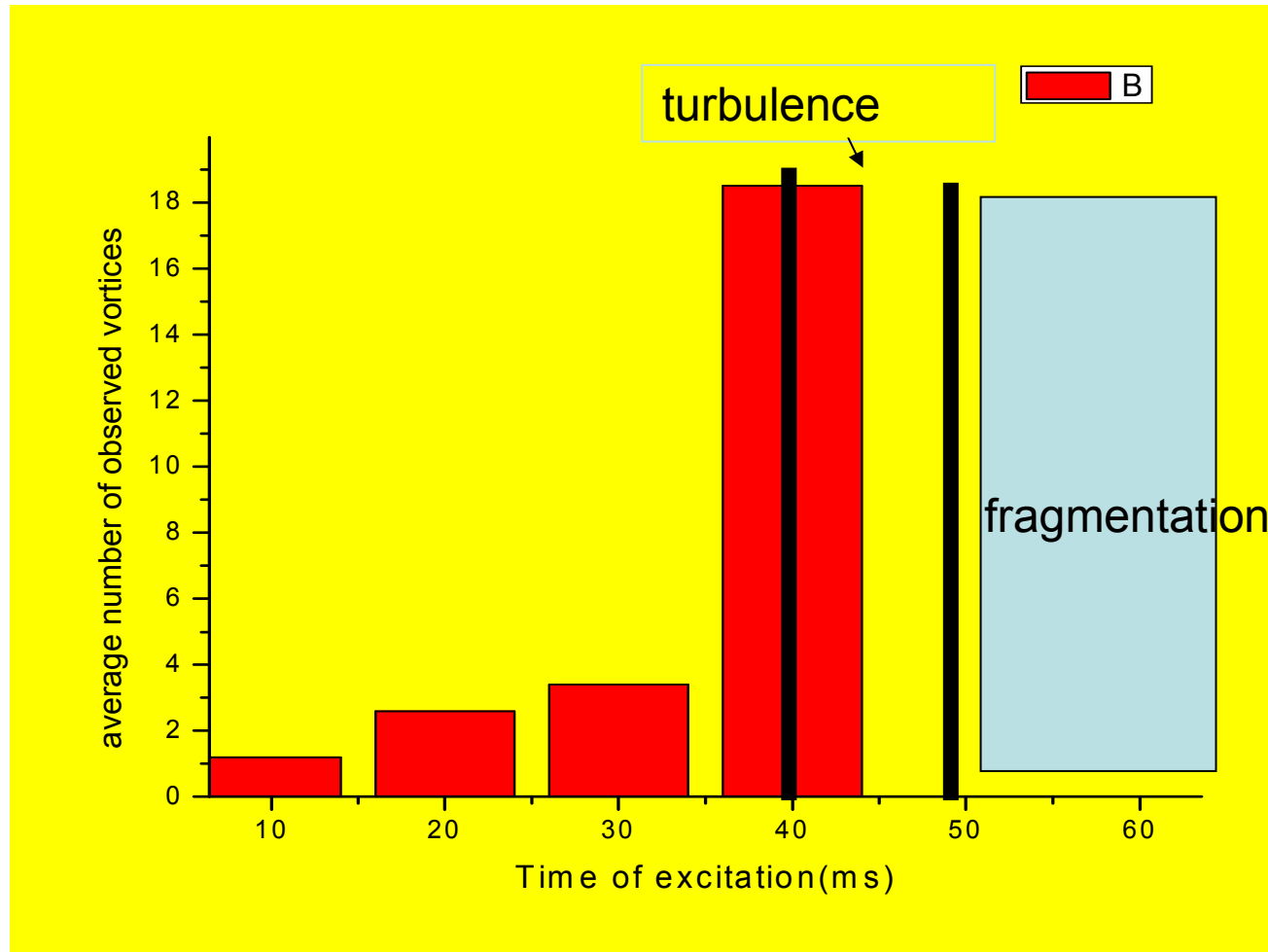
Aumento do Contraste



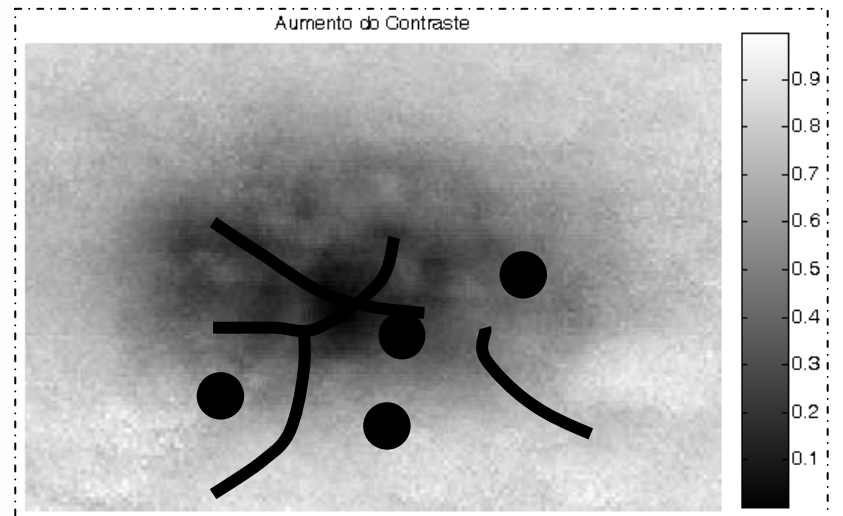
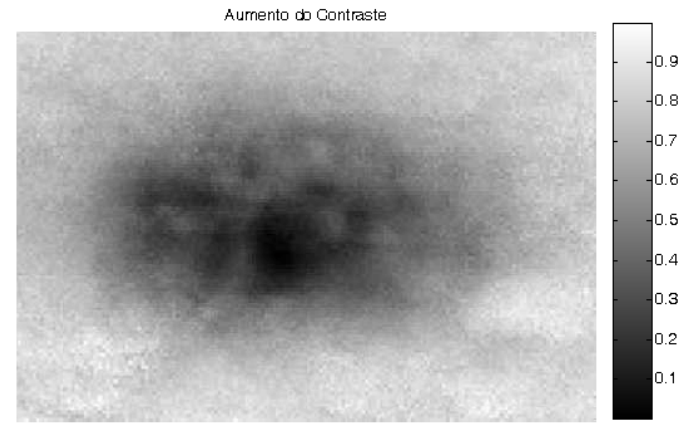
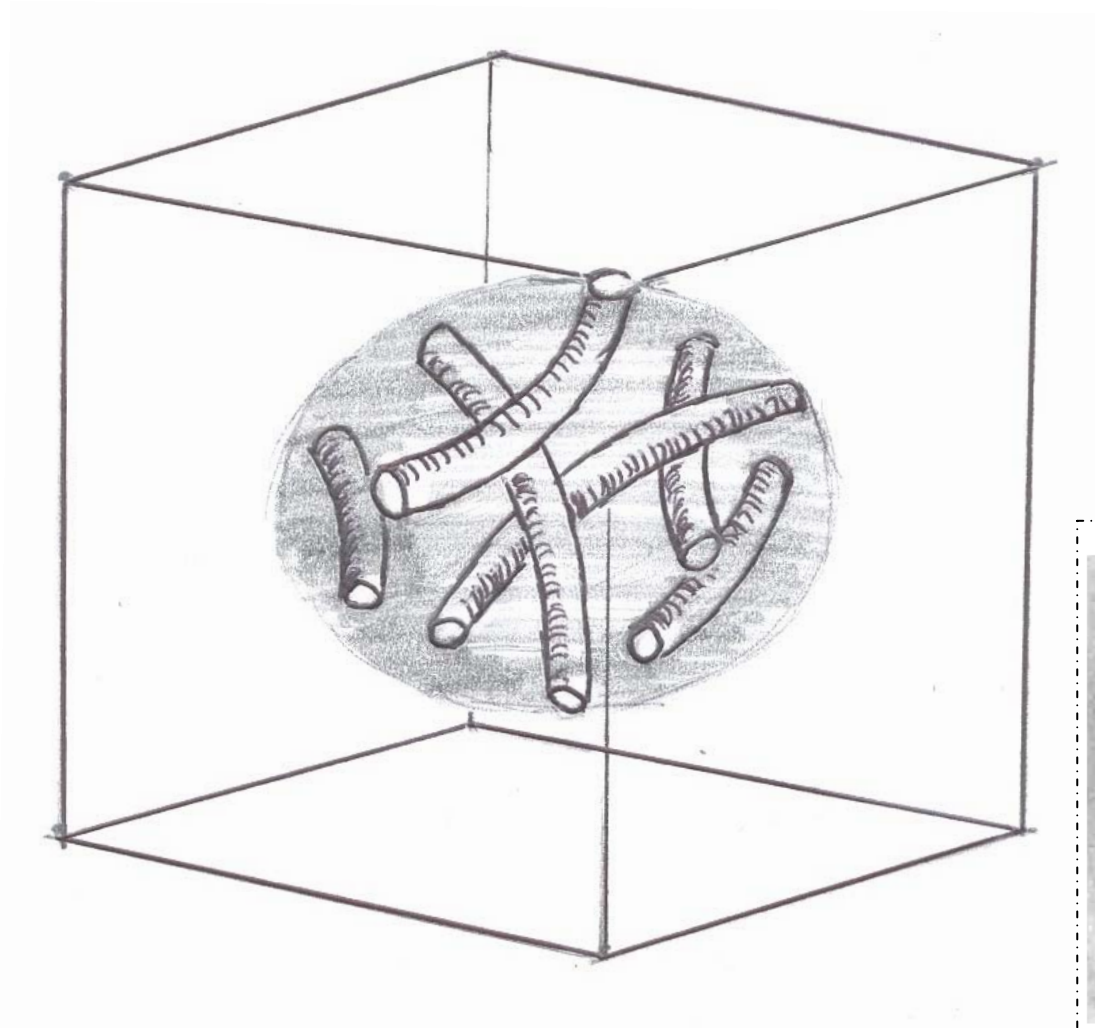
Characteristics of turbulence

Average Numbers of vortices as a function of excitation time

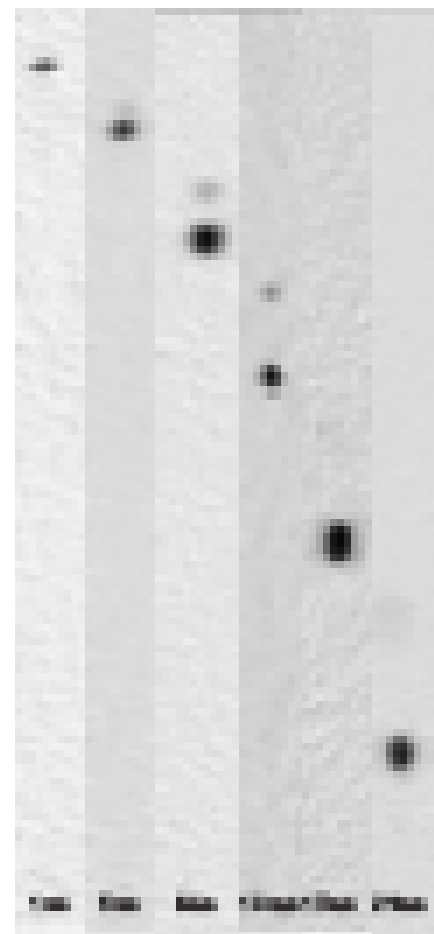
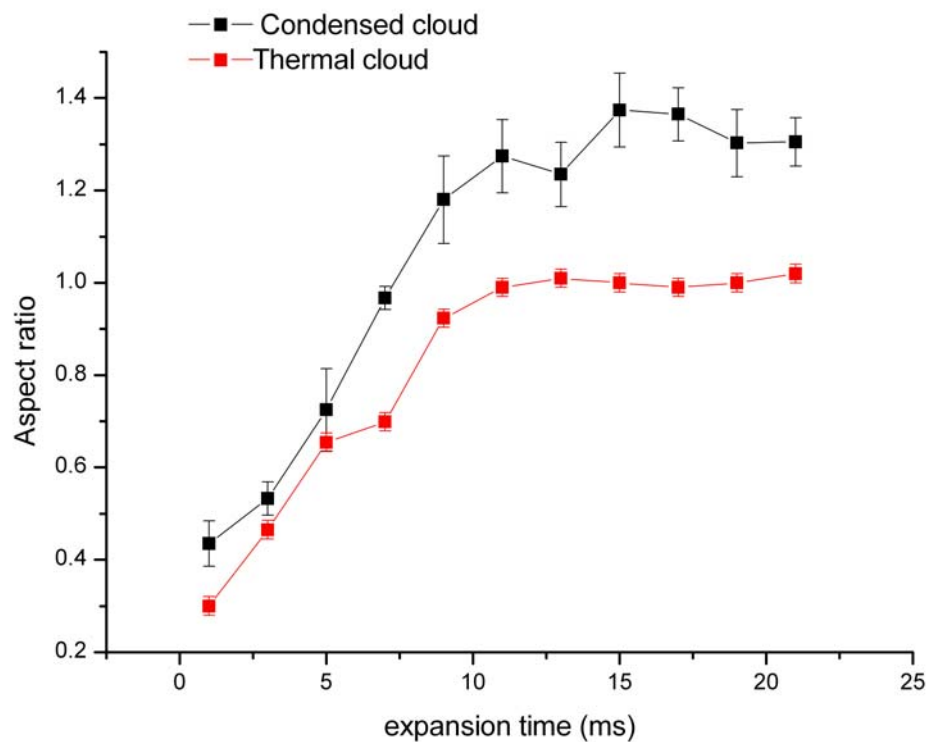
Excitation frequency : 200Hz, Amplitude 250 mV



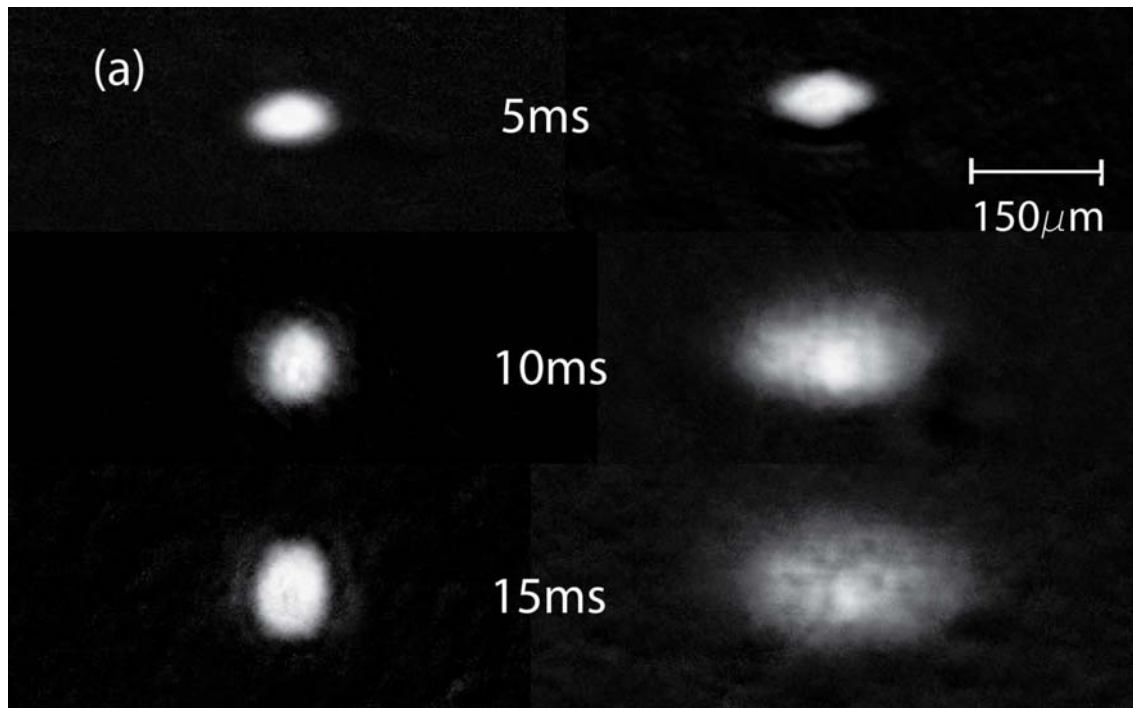
Tangle vortices region



Observation of aspect ratio inversion of the quantum cloud- energy conversion

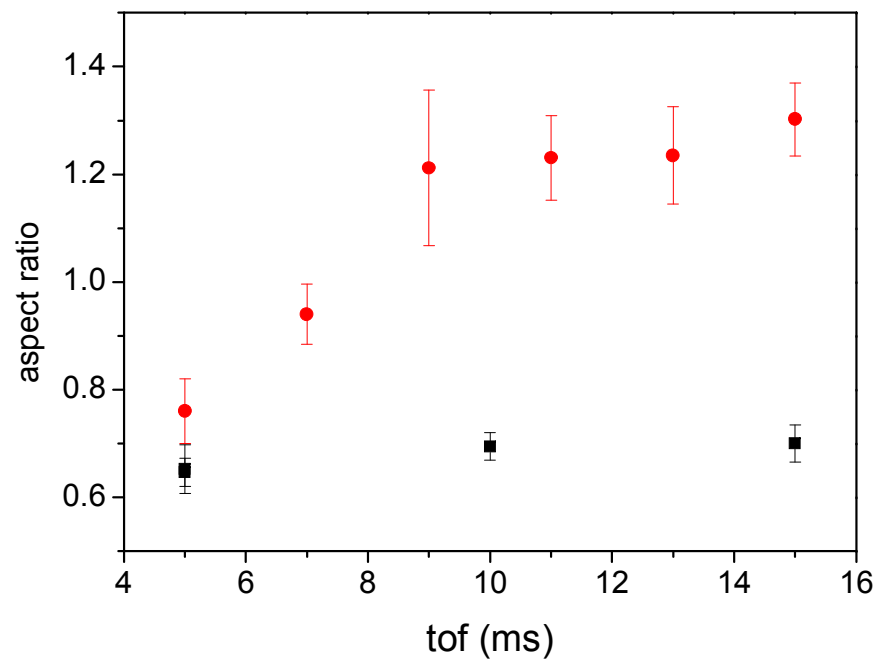


For a large number of vortices, the inversion is not observed



Non usual hydrodynamic behavior during expansion

■ turbulent cloud
● normal BEC



Arxiv: 0904.2564

ANALYSIS OF ROTATING CLOUDS → CHANGE IN BEHAVIOR DURING EXPANSION

Phys. Rev. Lett. 88,070405(2002)

(Edwards, Clark, Pedri, Pitaevskii and Stringari)

Phys. Rev. Lett. 88,070406 (Hechenblaikner, Hodby, Hopkins, Marago and Foot)

- “since the instantaneous moment of inertia is them proportional to the asymmetry of the cross section...”
- “ Preventing the released condensate from attaining a circular cross section..”

Clear the presence of angular momentum affects the expansion

The absence of inversion in the ratio may be an indicative of Turbulence . That would be a new effect in the atomic quantum fluid.

How we explain the formation of tangle vortices?

- EXCITATION IN AT LEAST TWO PLANS
- ENOUGH AMPLITUDE TO TRANSFER MANY UNITS OF ANGULAR MOMENT
- Two axis of oscillations (not equivalent)
- Tangle vortices (Feynman)
- When the vortices become tangle, the flow has a strong random element, varying rapidly from point to point (lost of inversion)

Quantum turbulence in a trapped Bose-Einstein condensate

Michikazu Kobayashi and Makoto Tsubota

Department of Physics, Osaka City University, Sumiyoshi-Ku, Osaka 558-8585, Japan

(Received 16 March 2007; published 31 October 2007)

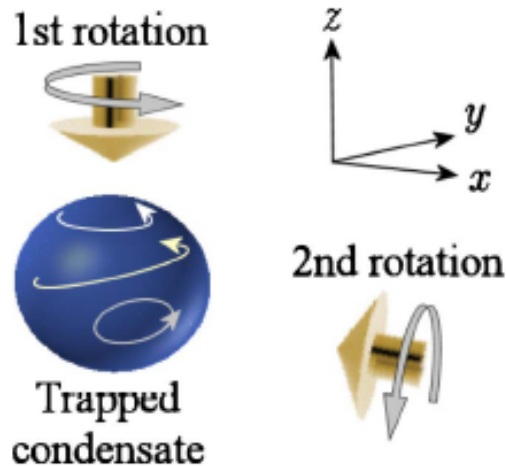


FIG. 1. (Color online). Schematic sketch of the rotation. The first rotation is applied along the z axis and the second rotation is applied along the x axis.

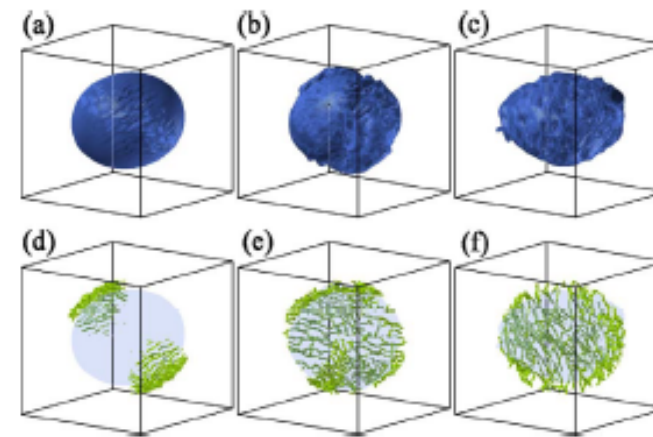
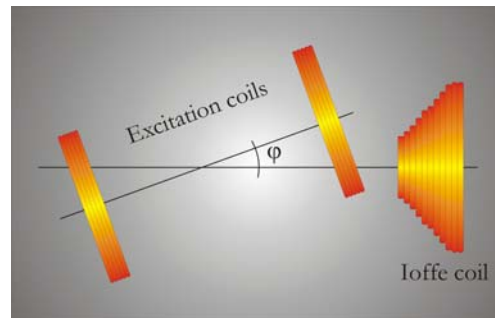
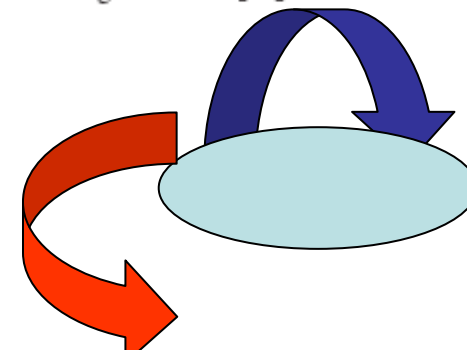
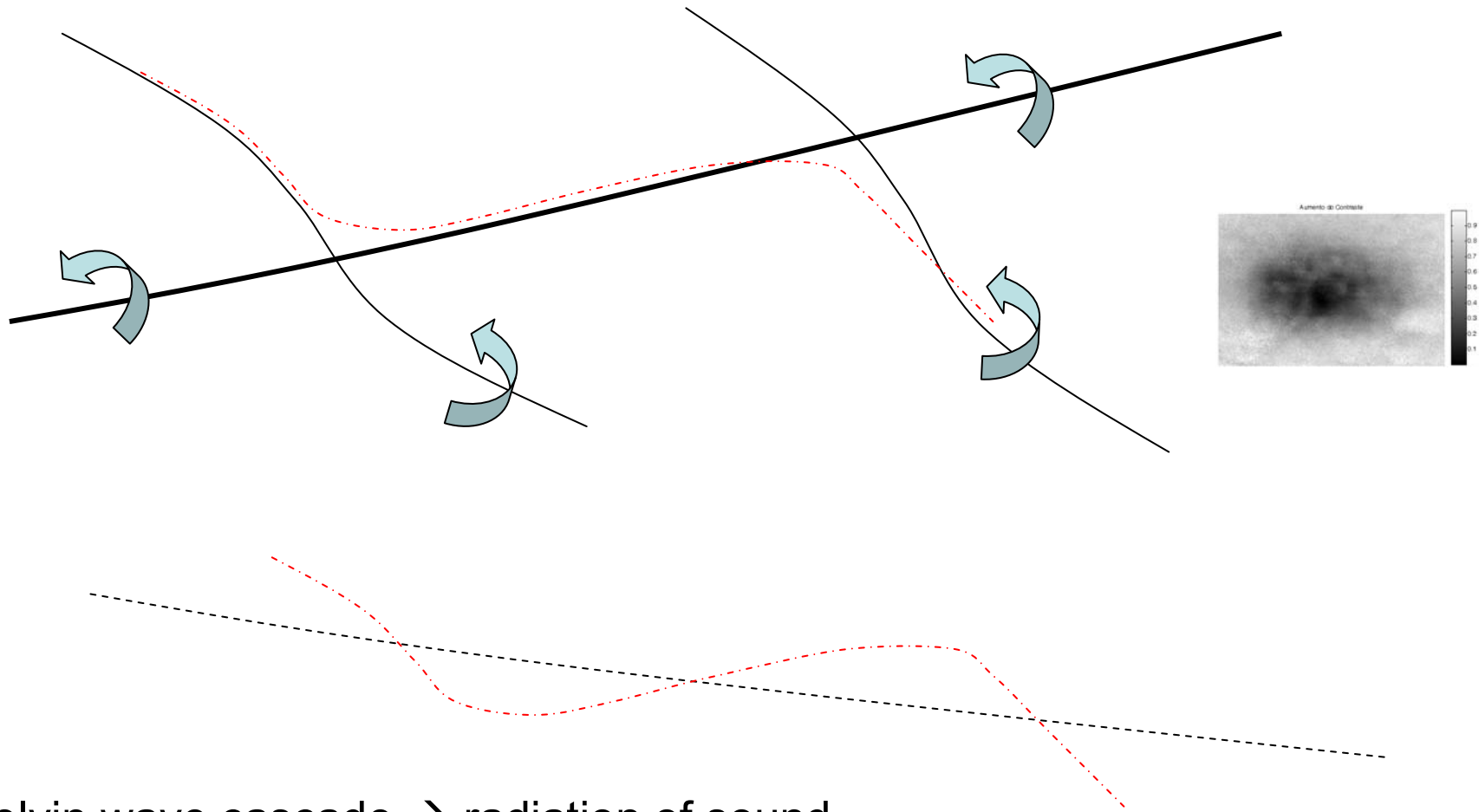


FIG. 4. (Color online). Isosurface plots of 5% of the maximum condensate density (a)–(c) and configuration of quantized vortices inside the Thomas-Fermi radius R_{TF} (d)–(f). (a), (d) $t\omega = 10$; (b), (e) $t\omega = 50$; (c), (f) $t\omega = 300$. The method for identifying vortices in (d)–(f) is the same as that in Fig. 7 in Ref. [15].



Dissipation in QT KELVIN WAVES

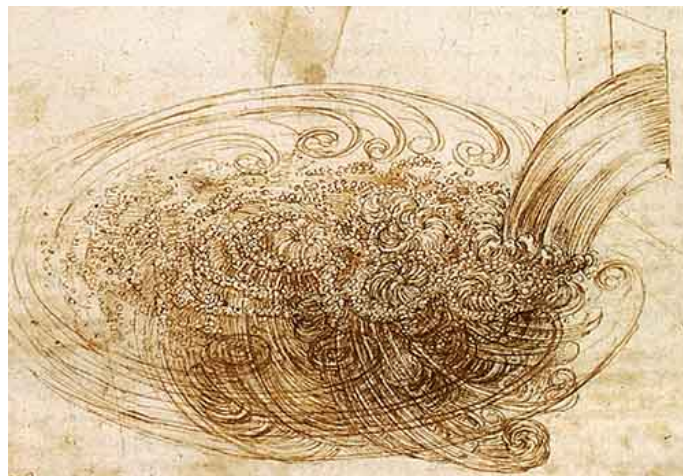
Vortex breaking and reconnecting

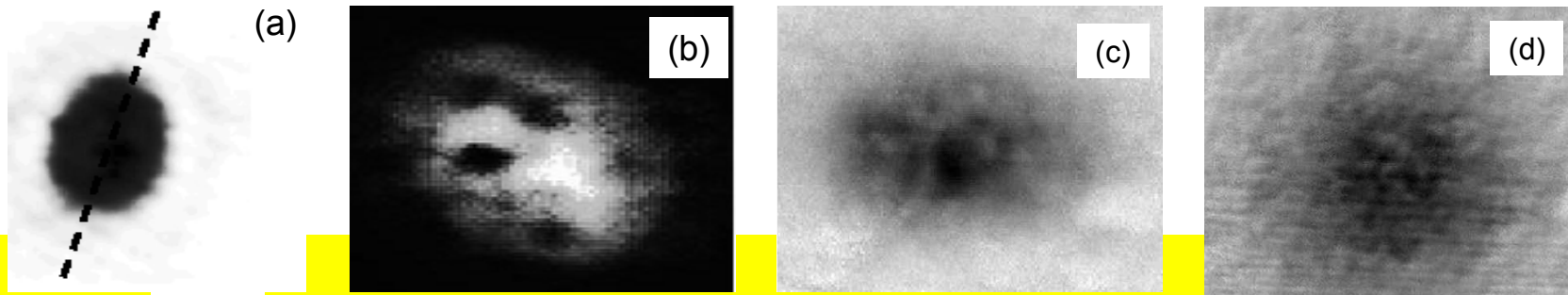


Kelvin wave cascade → radiation of sound

PRESENTLY

- Controlling turbulence in BEC is possible (changing fraction of condensate, changing interaction, etc)**
- Kolmogorov spectrum(how to measure in a BEC after expansion?)**
- Quantum turbulence - dissipation mechanisms**





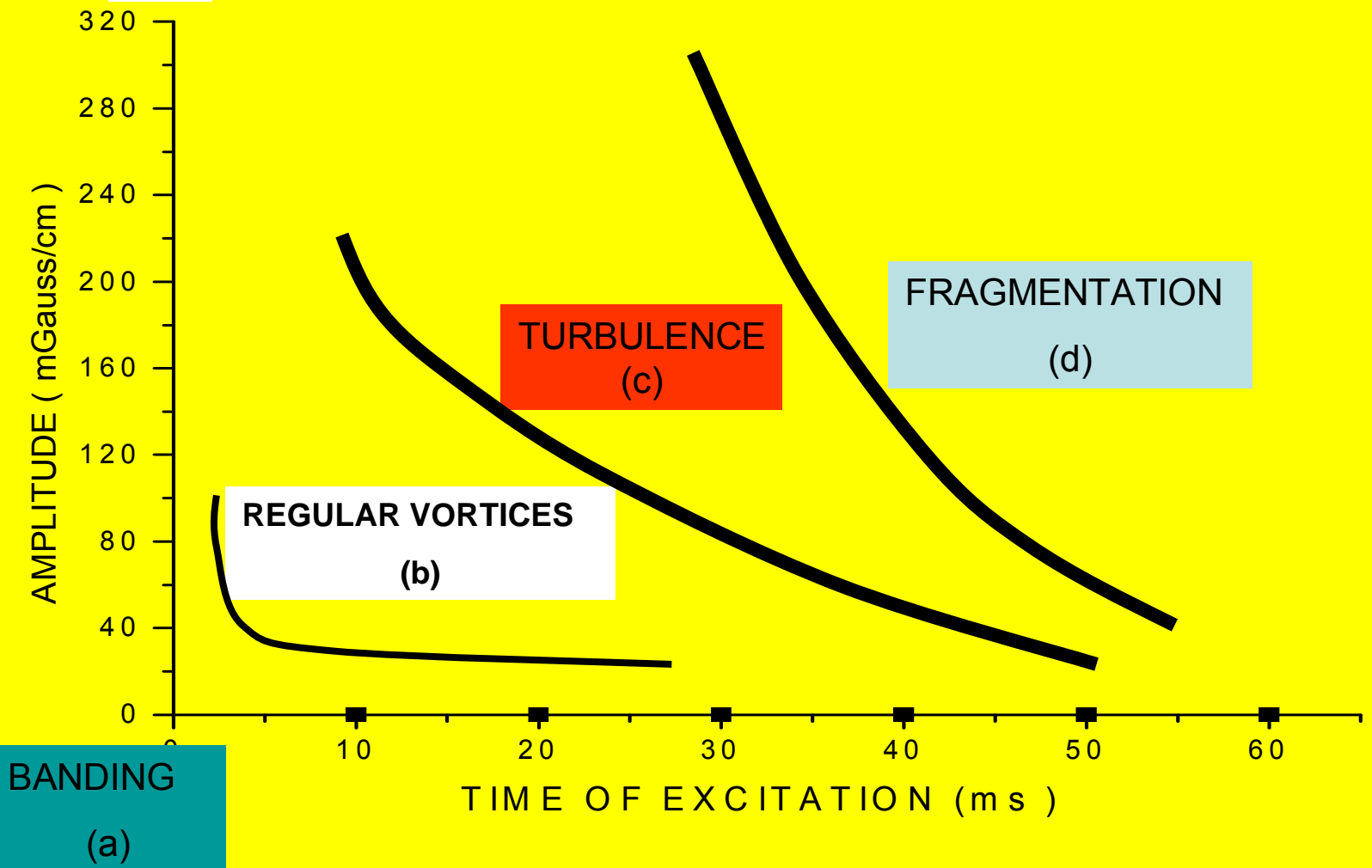
(a)

(b)

(c)

(d)

■ B



V.I. Yukalov

Bose systems in spatially random or time-varying potentials

Abstract

Bose systems, subject to the action of external random potentials, are considered. For describing the system properties, under the action of spatially random potentials of arbitrary strength, the stochastic mean-field approximation is employed. When the strength of disorder increases, the extended Bose-Einstein condensate fragments into spatially disconnected regions, forming a granular condensate. Increasing the strength of disorder even more transforms the granular condensate into the normal glass. The influence of time-dependent external potentials is also discussed. Fastly varying temporal potentials, to some extent, imitate the action of spatially random potentials. In particular, strong time-alternating potential can induce the appearance of a nonequilibrium granular condensate.

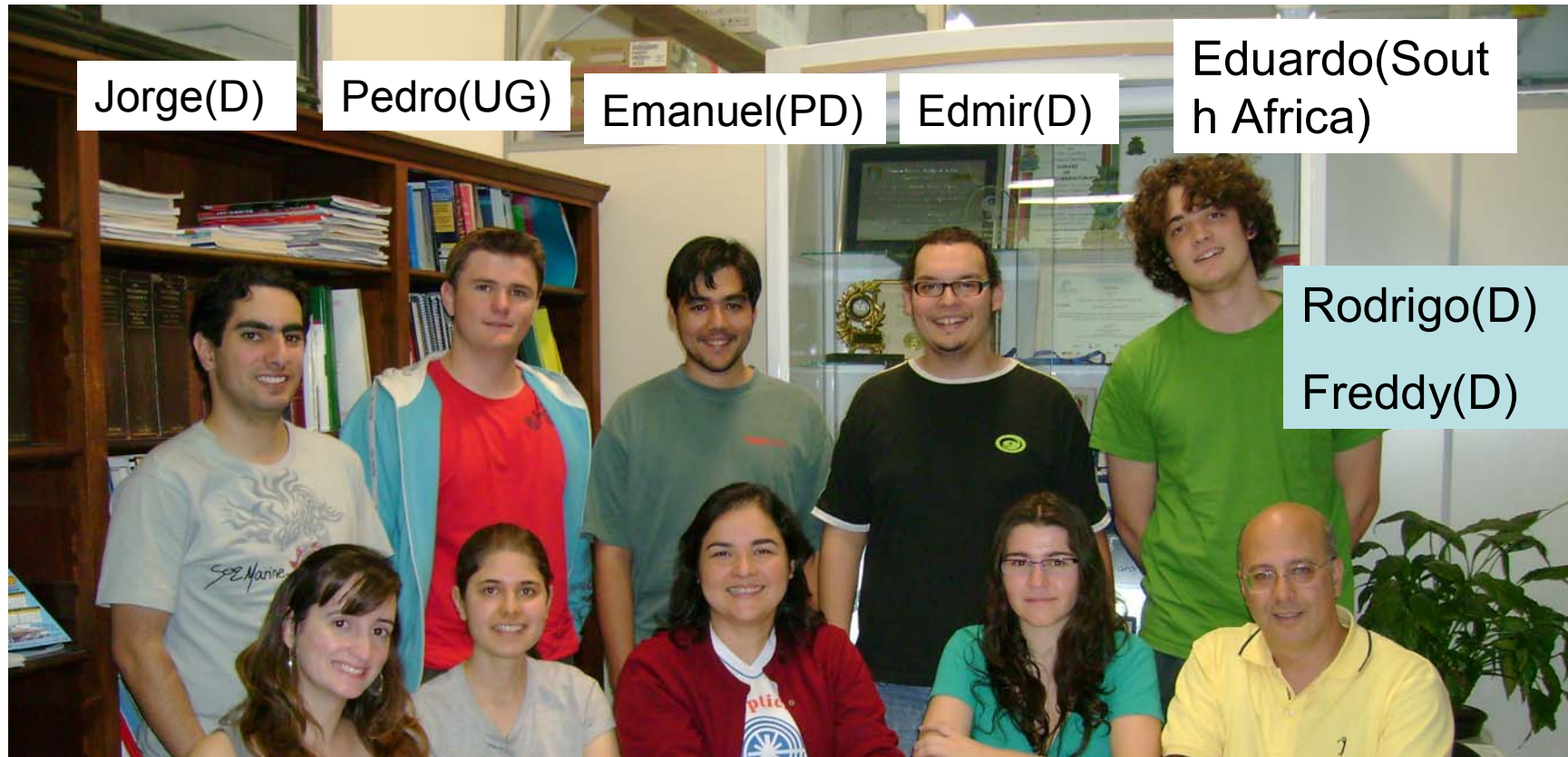
SPECIAL ISSUE OF J. LAS. PHYS.

[arXiv:0904.0749](https://arxiv.org/abs/0904.0749)

CONCLUSIONS:

- Many observations: tangle vortices(QT), Clusters, new hydrodynamic expansion, fragmentation, evidences of ripplons, ...
 - BUT
 - Much more to do ...

BEC - LABORATORY



Jorge(D)

Pedro(UG)

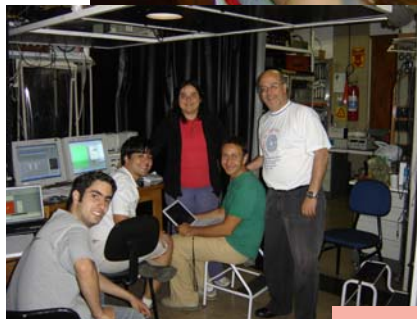
Emanuel(PD)

Edmir(D)

Eduardo(South Africa)

Rodrigo(D)

Freddy(D)



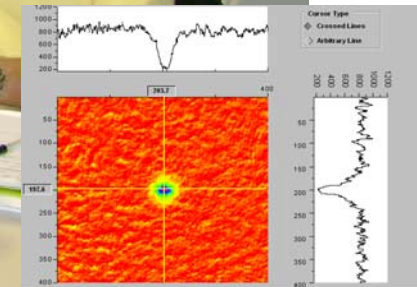
Patricia
(UG)

Mônica
(MS)

Kilvia
(Res.)

Cora
(UG)

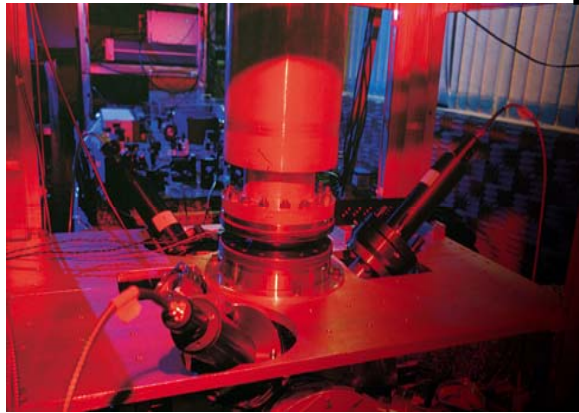
V. Yukalov (Russia)
G. Roati (Italy)



2 POSTDOC POSITIONS IN ATOMIC PHYS.

One faculty position – second semester 2009

www.cepof.ifsc.usp.br



<http://www.lasphys.com/workshops/lasphys10>

**19th INTERNATIONAL LASER PHYSICS WORKSHOP
(Foz do Iguaçu, July 5-9, 2010)**

The nineteenth annual International Laser Physics Workshop (LPHYS'10) will be held from July 5 to July 9, 2010, in the [Carimã Hotel](#), [Foz do Iguaçu](#), Brazil. The city of Foz do Iguaçu is situated near the world-famous falls, the Iguazu Falls. That is why the excursion on the [Iguazu Falls](#) for participants of LPHYS'10 will be organized by the Local Organizing Committee.



LPHYS'10

THANKS