



*The Abdus Salam
International Centre for Theoretical Physics*



2030-24

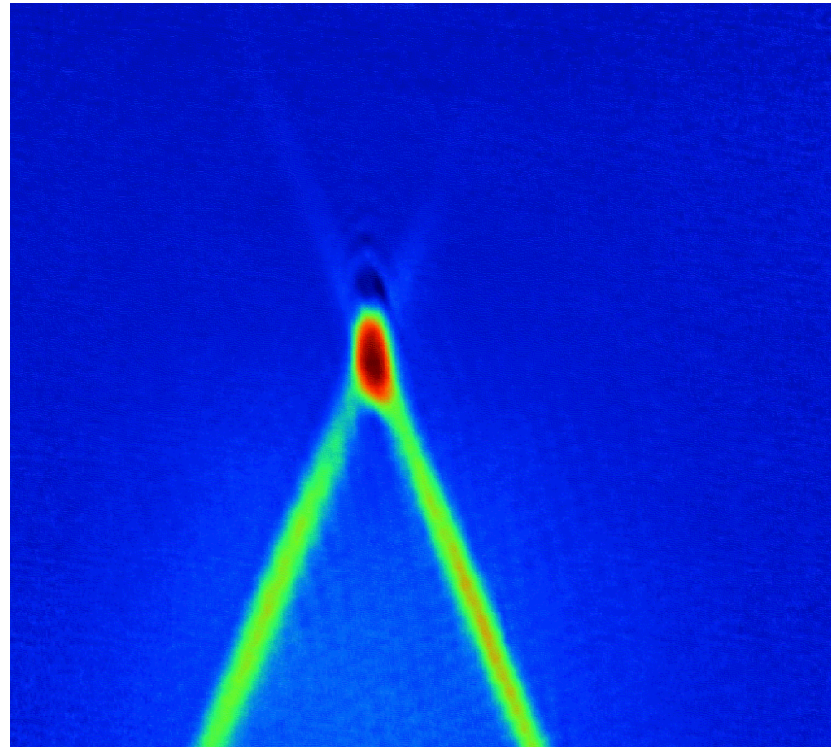
Conference on Research Frontiers in Ultra-Cold Atoms

4 - 8 May 2009

Recent advances on ultracold fermions

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FRANCE*

Recent Advances on Ultracold Fermi Gases at ENS



ICTP, Trieste, May 4-8, 2009

The ENS Fermi gas Team

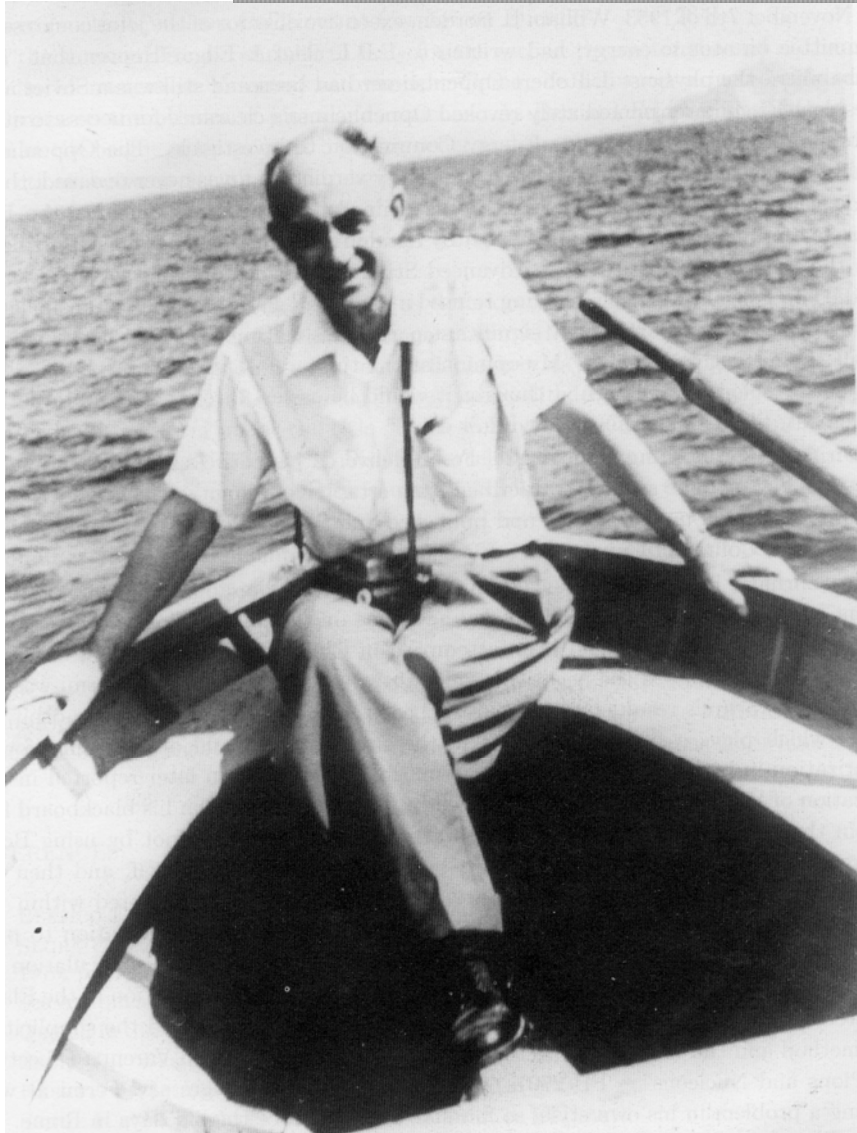
S. Nascimbène, N. Navon, K. Jiang,
L. Tarruell, M. Teichmann, G. Duffy,
J. McKeever, K. Magalhães, V. Bagnato

A. Ridinger, T. Salez, S. Chaudhuri,
U. Eismann, D. Wilkowski,
F. Chevy, Y. Castin, C. Salomon



Theory support: D. Petrov, G. Shlyapnikov, R. Combescot, I. Carusotto, C. Lobo, S. Stringari, L. Dao, A. Georges, O. Parcollet, C. Kollath, J.S. Bernier, L. De Leo, M. Köhl

A Cruise on the Fermi Sea



Enrico Fermi on lake Como

ITALIAN PHYSICAL SOCIETY
PROCEEDINGS
OF THE
INTERNATIONAL SCHOOL OF PHYSICS
"ENRICO FERMI"

COURSE CLXIV
edited by M. INGUSCIO, W. KETTERLE and C. SALOMON

Directors of the Course
VARENNA ON LAKE COMO

VILLA MONASTERO
20 - 30 June 2006

Ultra-cold Fermi Gases

2007

IOS
Press

AMSTERDAM, OXFORD, TOKIO, WASHINGTON DC

Analog simulators classical vs quantum



Classical analog simulator:
Strasbourg astronomical clock



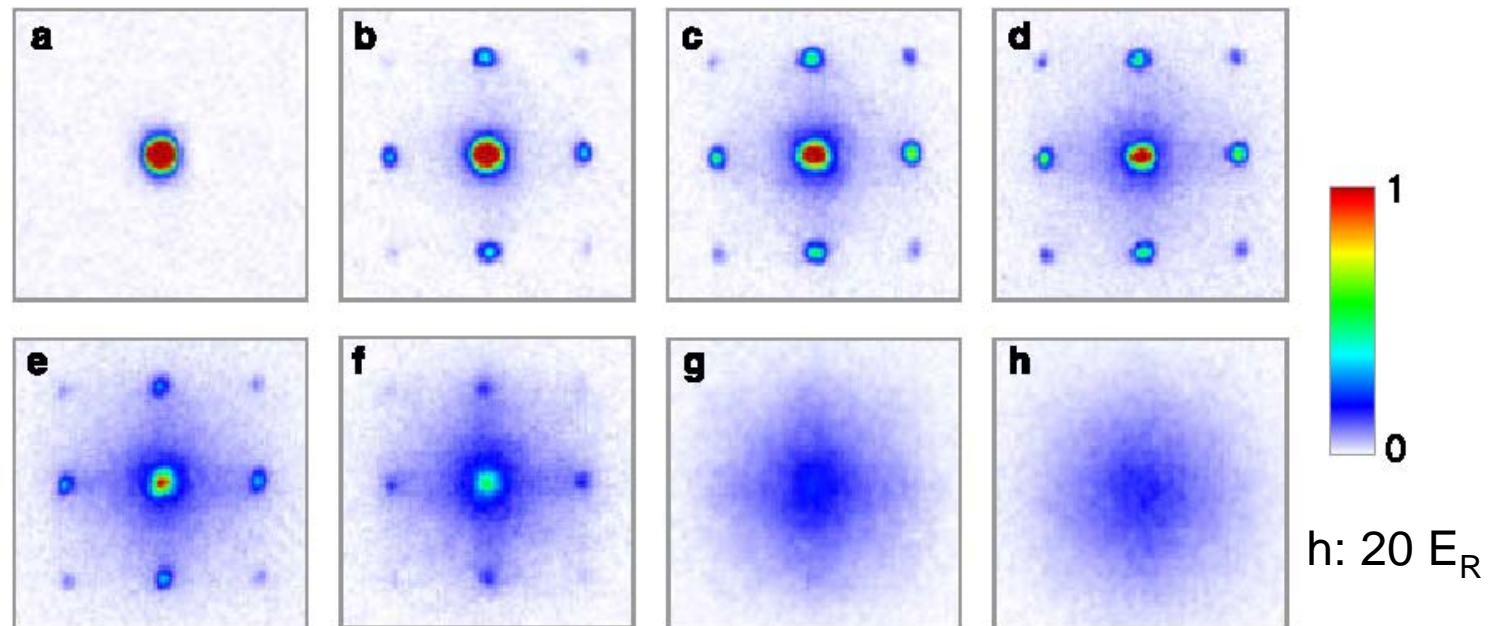
R.P. Feynman

Analog simulation of
many-body quantum effects

Examples of quantum simulators

1) Mott-insulator transition in 3D Optical lattice: bosons

Markus Greiner*, Olaf Mandel*, Tilman Esslinger†, Theodor W. Hänsch* & Immanuel Bloch* Nature, 415, 39,2002



Fermions: 3D Mott-insulator transition seen
in Zurich and Mainz (2008)

Second example of quantum simulator

Universal equation of state of unitary Fermi gas

$$\mu = (1 + \beta) \frac{\hbar^2}{2m} (6\pi^2 n)^{2/3} = \xi E_F$$

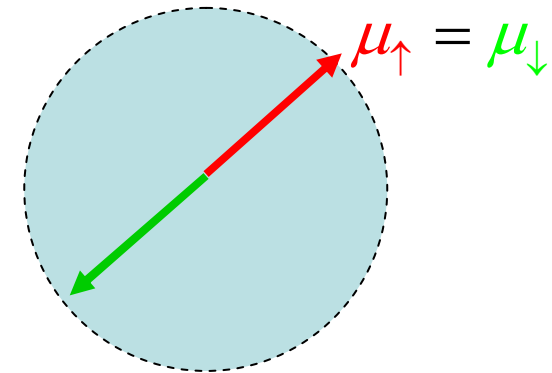
Determination of ξ

Experiment	<i>ENS (⁶Li)</i>	0.42(15)	Theory	<i>BCS</i>	0.59
	<i>Rice (⁶Li)</i>	0.46(5)		<i>Astrakharchik</i>	0.42(1)
	<i>JILA(⁴⁰K)</i>	0.46(10)		<i>Perali</i>	0.455
	<i>Innsbruck (⁶Li)</i>	0.27(10)		<i>Carlson</i>	0.42(1)
	<i>Duke (⁶Li)</i>	0.51(4)		<i>Hausmann</i>	0.36

Pairing with imbalanced Fermi surfaces motivation

Attractive Fermi gas with equal spin population
⇒ BCS theory, pairing at edge of Fermi surface

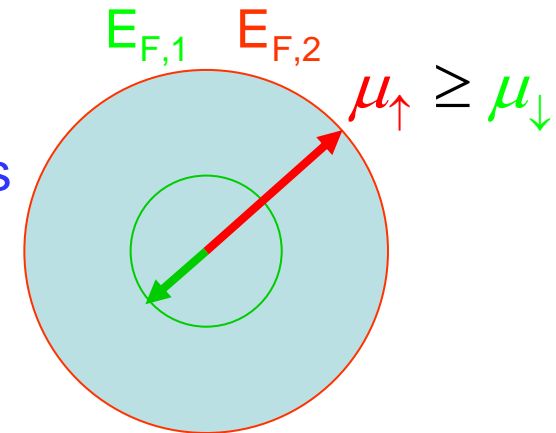
More than 20 theory papers in last 2 years !



What is the nature and existence of superfluidity
when spin population or mass is imbalanced ?
Mismatched density and/or pairing with different masses

Ex:

Superconductors in magnetic field or quark matter



Cold gases: spin imbalance

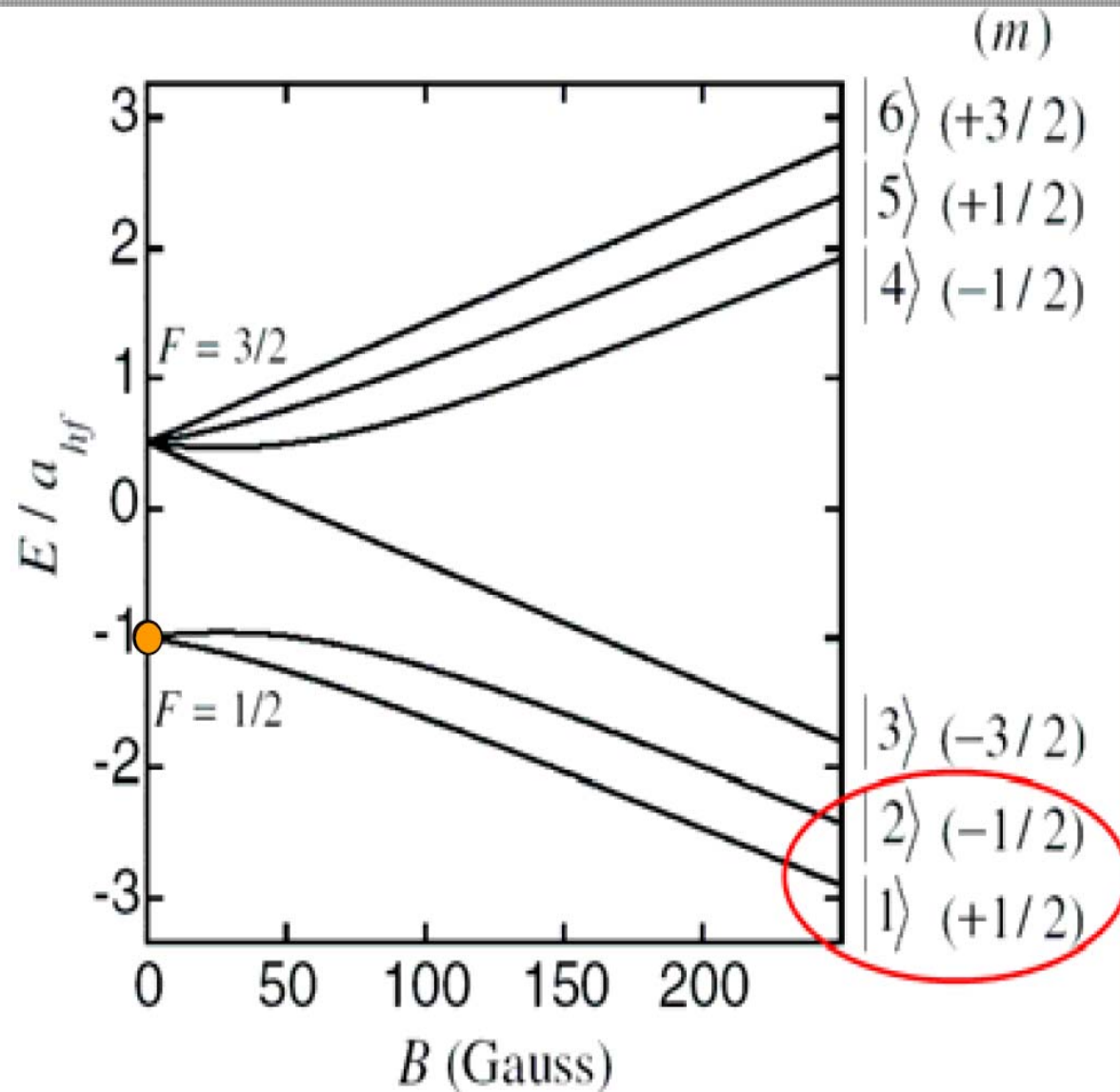
MIT and Rice expt: phase separation

Mixtures with different masses:

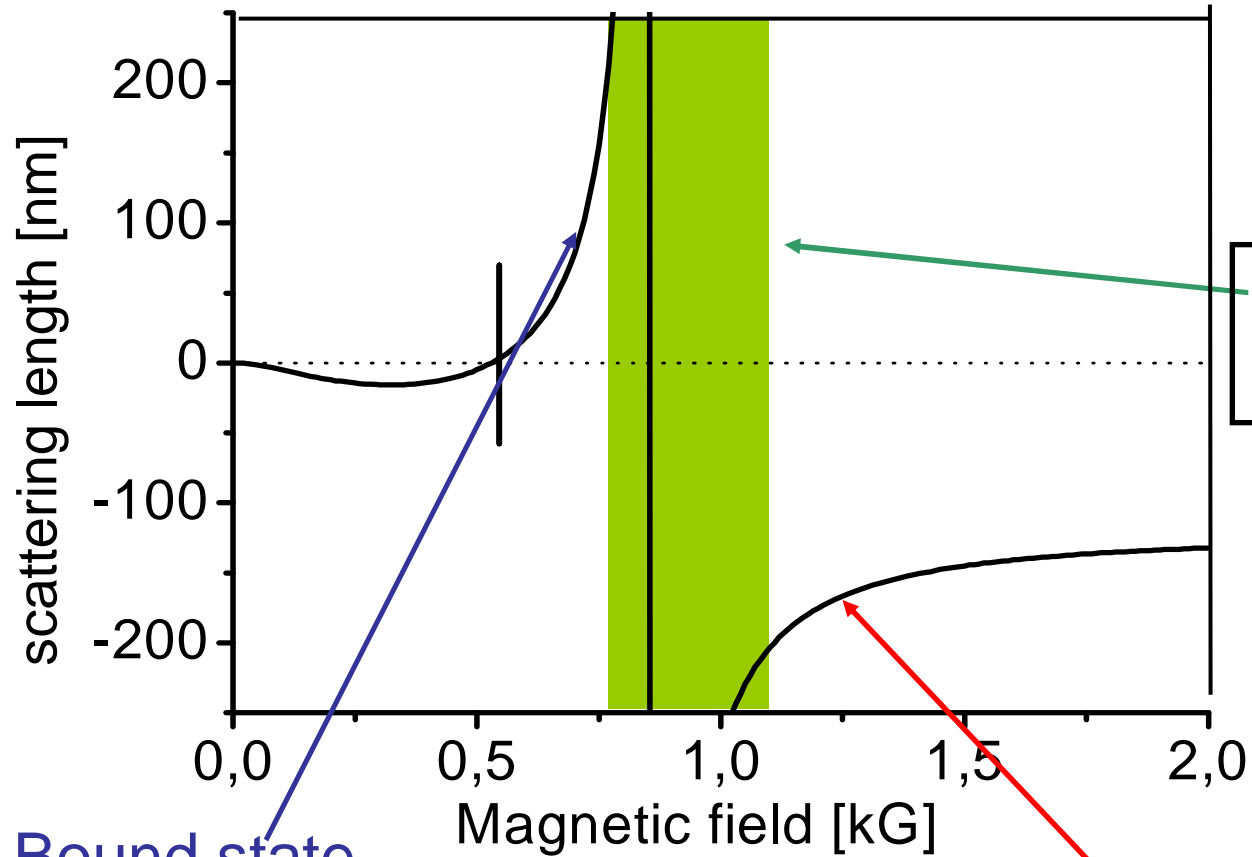
Innsbruck, Munich, Amsterdam, MIT, ENS

$$E_{F,i} = \frac{\hbar^2 k_{F,i}^2}{2m_i} = \frac{\hbar^2}{2m_i} (6\pi^2 n_i)^{2/3}$$

${}^6\text{Li}$ Ground state in magnetic field



interacting fermions



BEC-BCS
Crossover

Bound state

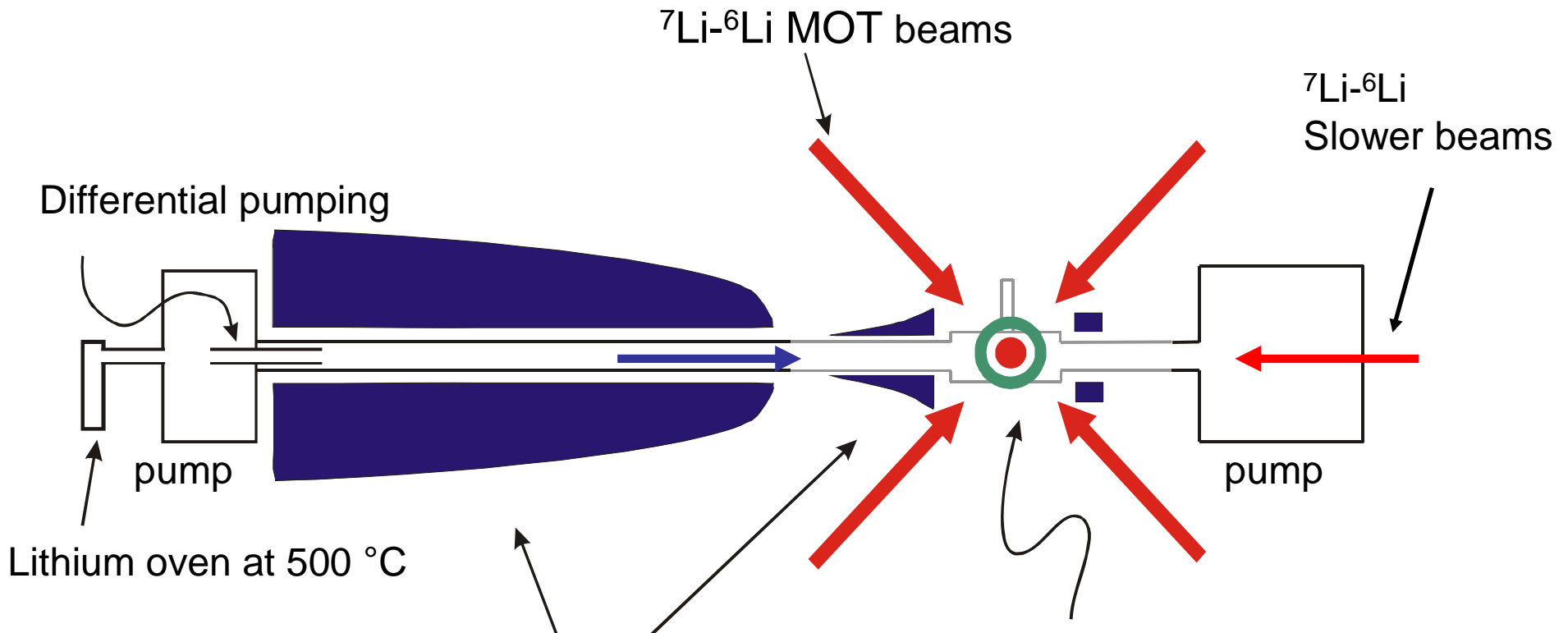
$$Eb = -\frac{\hbar^2}{ma^2}$$

condensate of molecules

No bound state

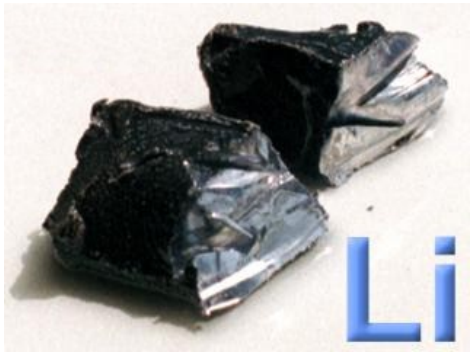
BCS phase

Second generation Set-up

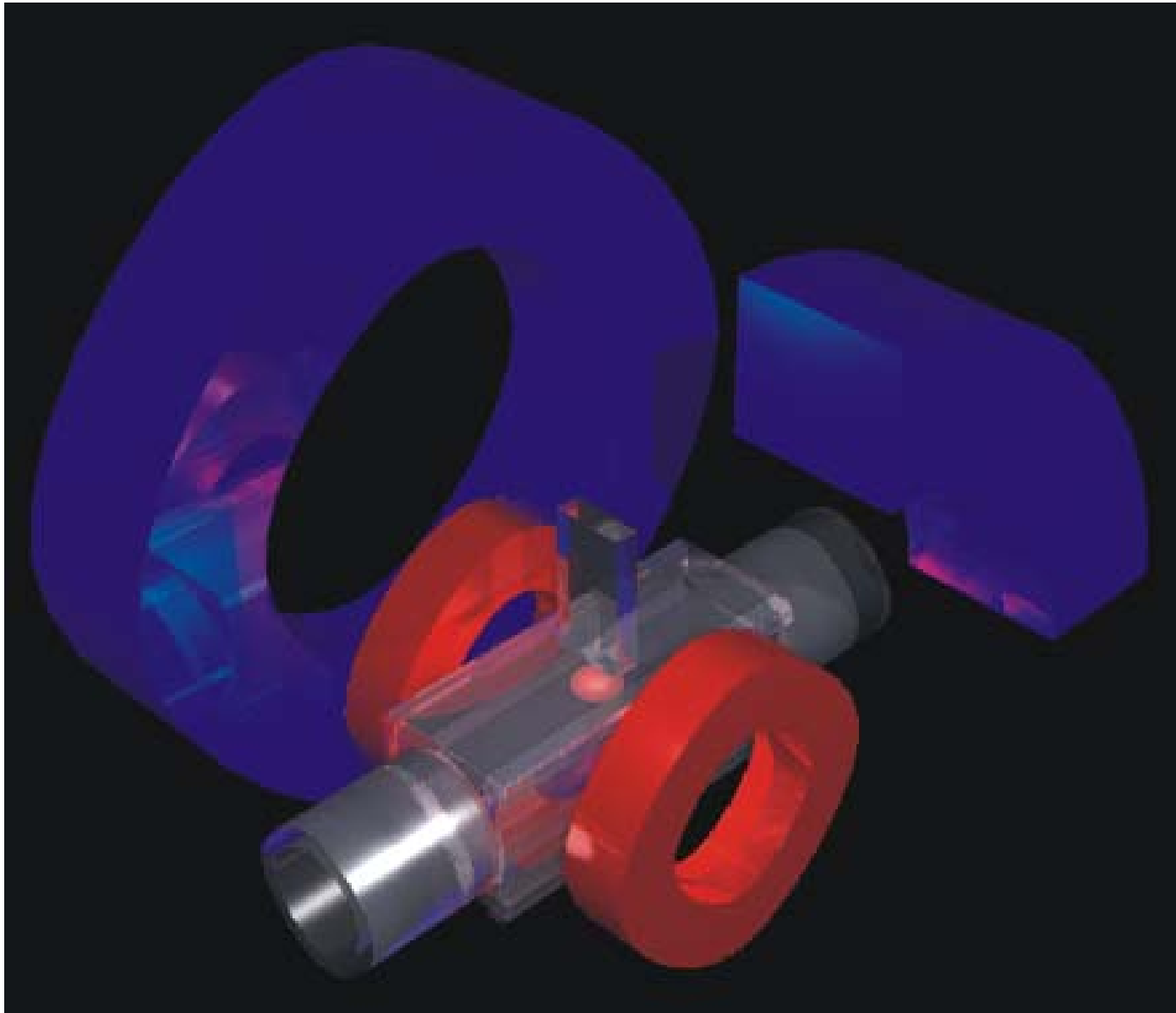


Zeeman slower
 $V_{\text{cap}} = 1000 \text{ m/s}$
Flux $\sim 2 \cdot 10^9 \text{ s}^{-1}$

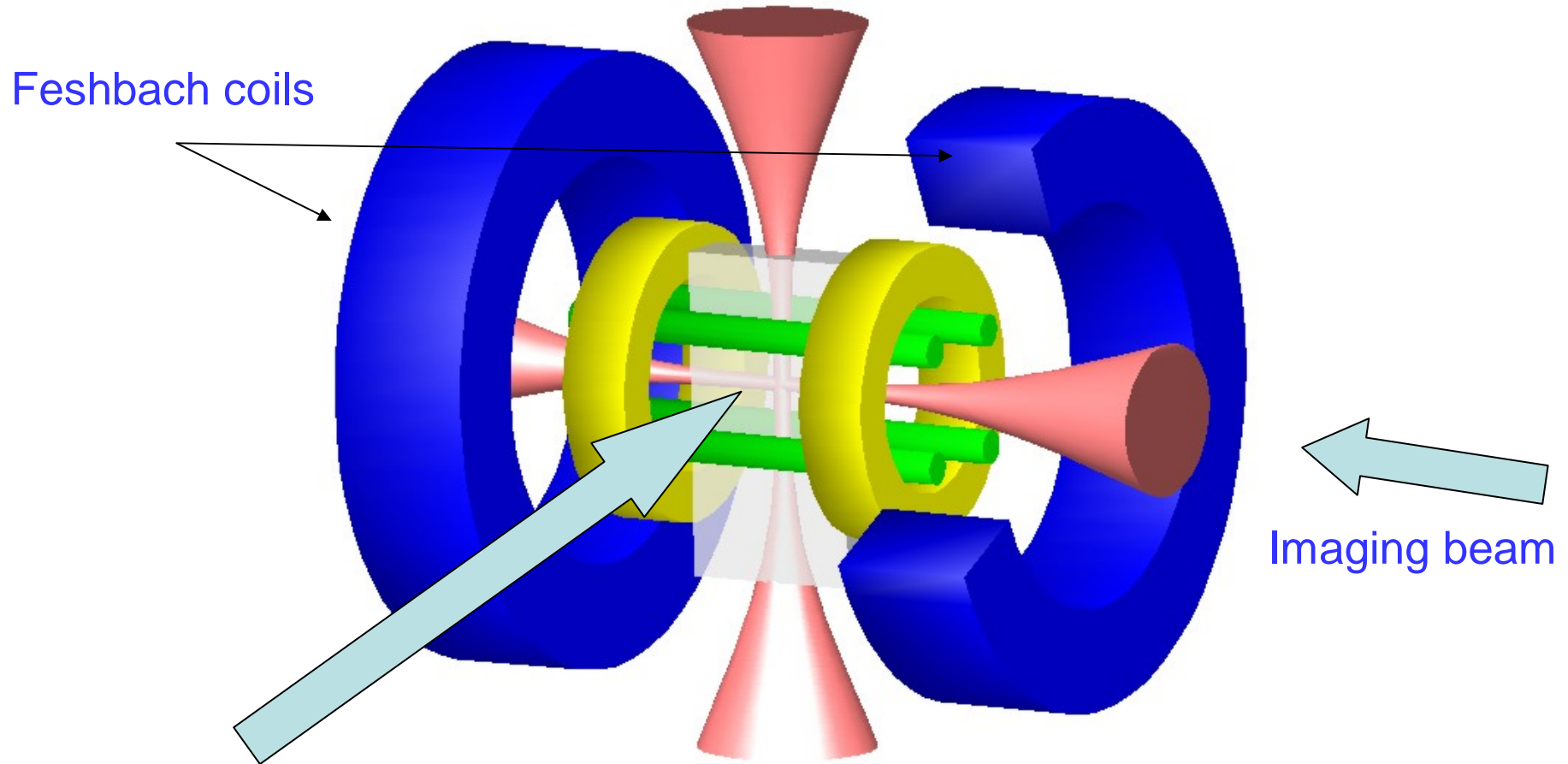
10^{10} atoms in ${}^7\text{Li}$ MOT
 $5 \cdot 10^8$ atoms in ${}^6\text{Li}$ MOT



Magnetic elevator



^6Li gas in an optical trap

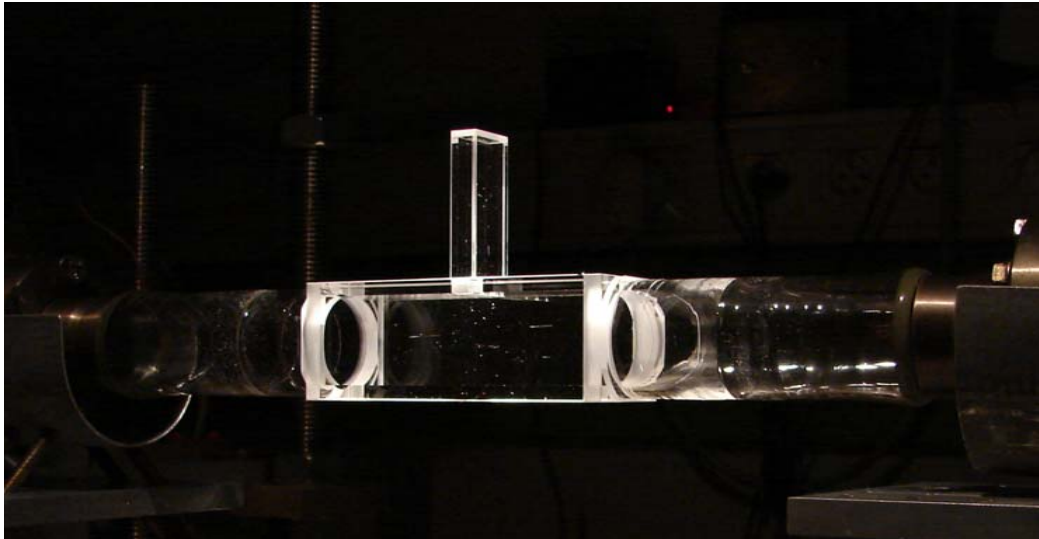


High B field
imaging beam

A single horizontal YAG beam
with 50 Watts and waist of $35\ \mu\text{m}$

Note: Vertical beam not used for the present data

Improvements on Lithium experimental setup



Enlarged glass cell
New laser sources: 120 mW diodes
New Zeeman slower
More stable Ioffe-Pritchard trap

120 Watt far detuned optical trap
(IPG Fiber laser)
Access for 3D optical lattice
3D high field imaging

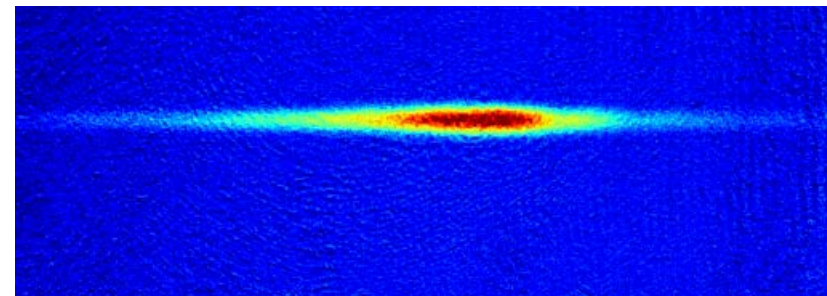
→ Sympathetic cooling of ^6Li by ^7Li in 20 seconds in magnetic trap followed by evaporation near Feshbach resonance in optical dipole trap (3 seconds).

X10 increase in ^6Li number in optical dipole trap:

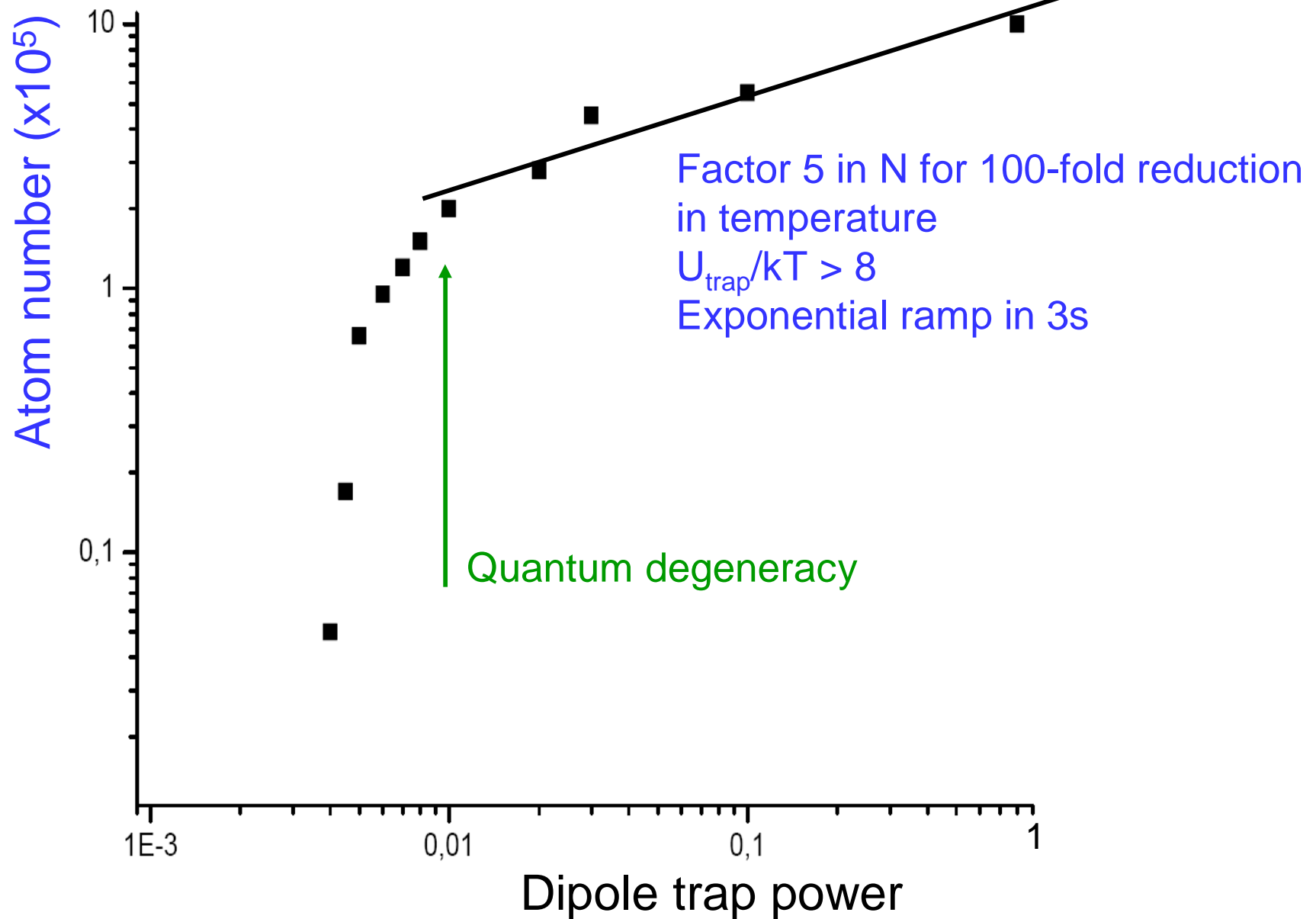
$5 \cdot 10^6$ atoms at $80\mu\text{K}$

$3 \cdot 10^5$ atoms per spin state
at $T/T_F \sim 0.1$

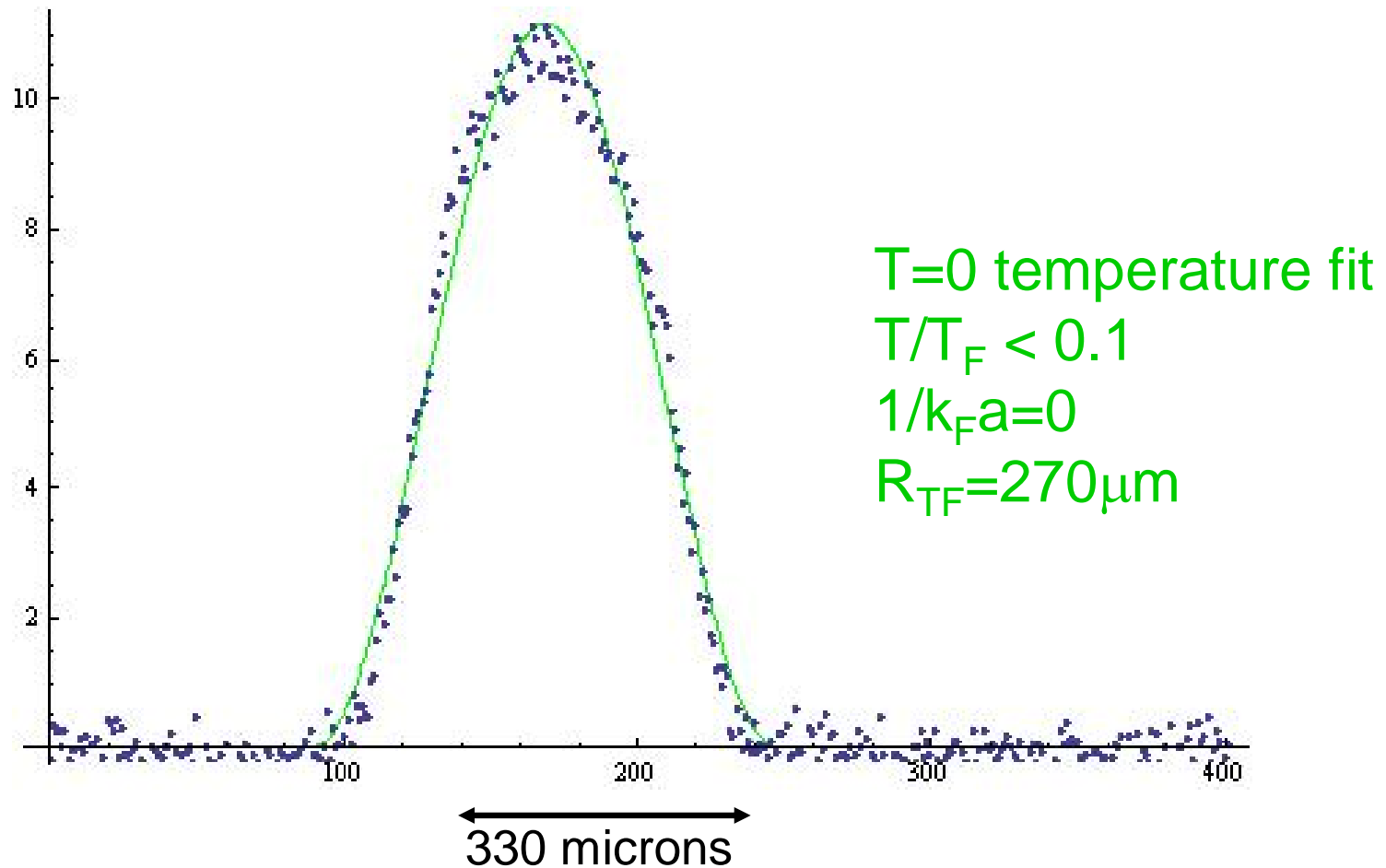
Cycle duration: 40 seconds



Efficient ${}^6\text{Li}$ evaporation

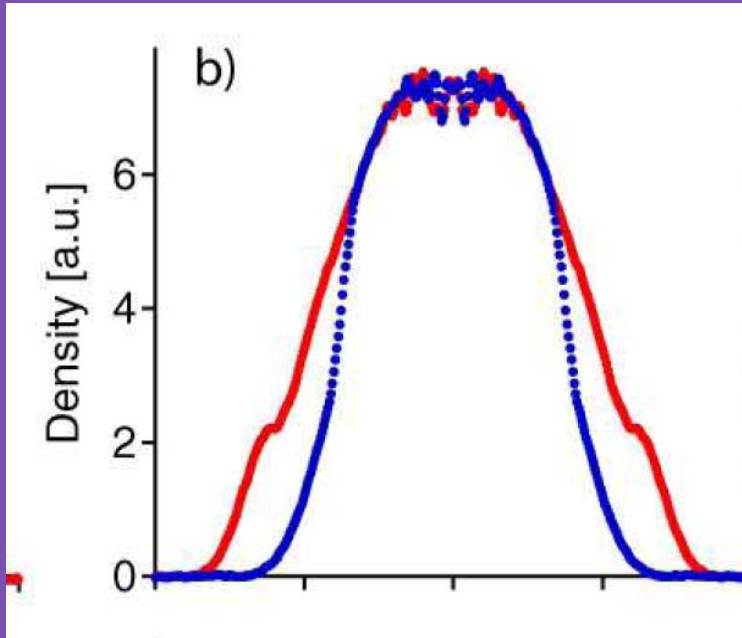


Axial Thomas-Fermi profiles in the balanced case



10^5 atoms per spin state in dipole trap
with 40 Hz axial, and 2 kHz radial frequencies

Imbalanced case: previous work

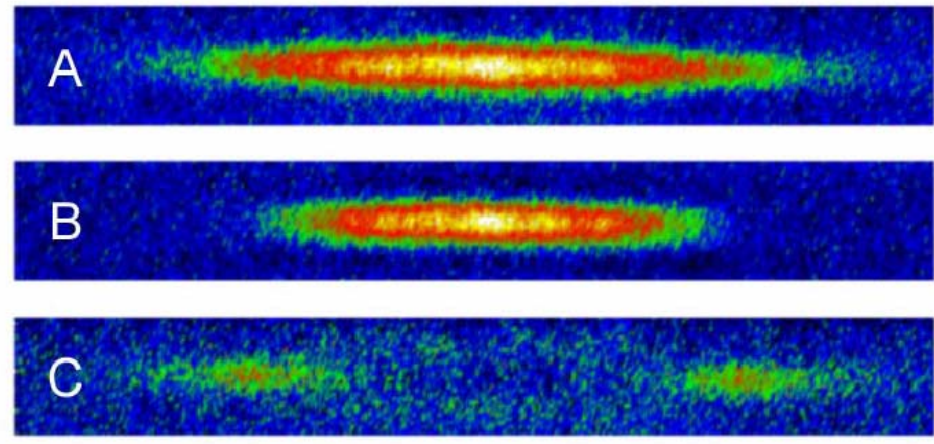


MIT: 3 phases

- Fully paired superfluid core
- Intermediate mixture
- Fully polarized rim

M.W. Zwierlein, *et al.*, *Science*, **311**
(2006) 492.

Rice: 2 phases
Fully paired superfluid core
Fully polarized rim

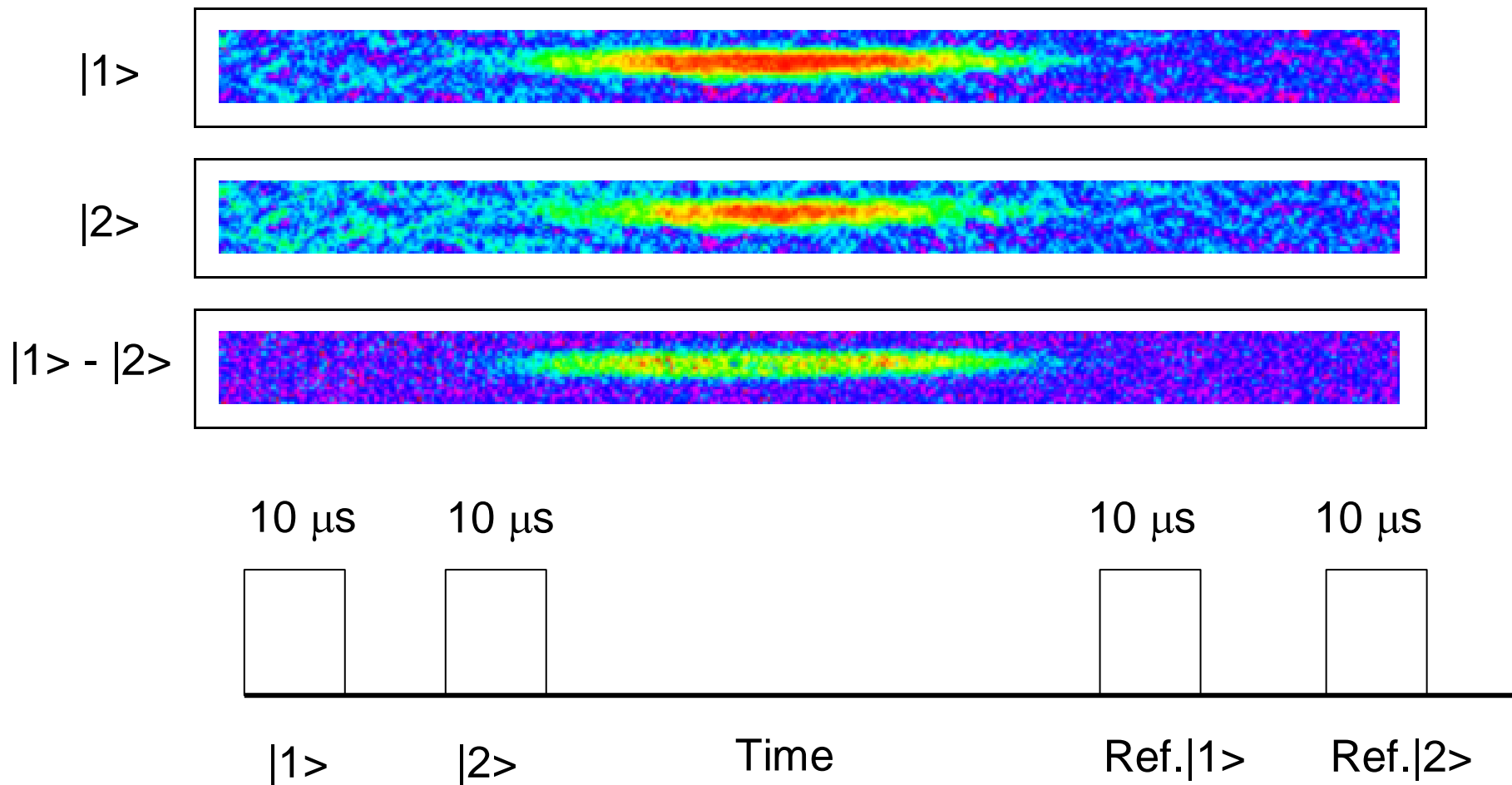


G.B. Partridge, W. Li, R.I. Kamar, Y.-A. Liao, R.G. Hulet, *Science*, **311** (2006)
503.

See Frédéric Chevy talk

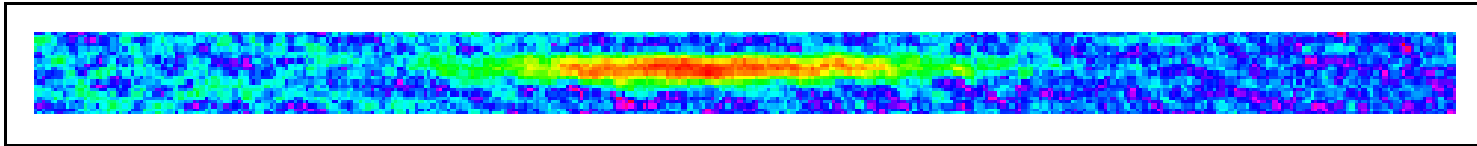
Imbalanced case: ENS

$$P = \frac{N_1 - N_2}{N_1 + N_2} = 0.39$$

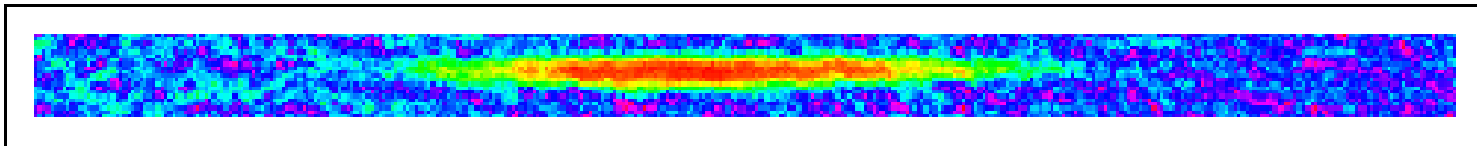


Check: invert absorption image order

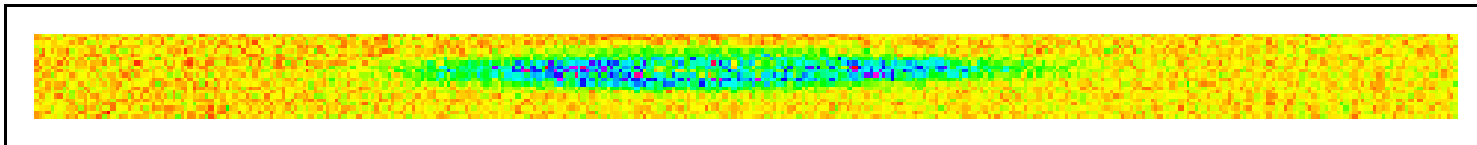
$|2\rangle$



$|1\rangle$



$|1\rangle - |2\rangle$

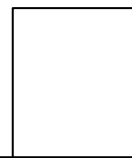
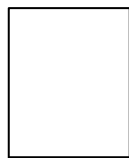


10 μ s

10 μ s

10 μ s

10 μ s



$|2\rangle$

$|1\rangle$

Time

Ref. $|2\rangle$

Ref. $|1\rangle$

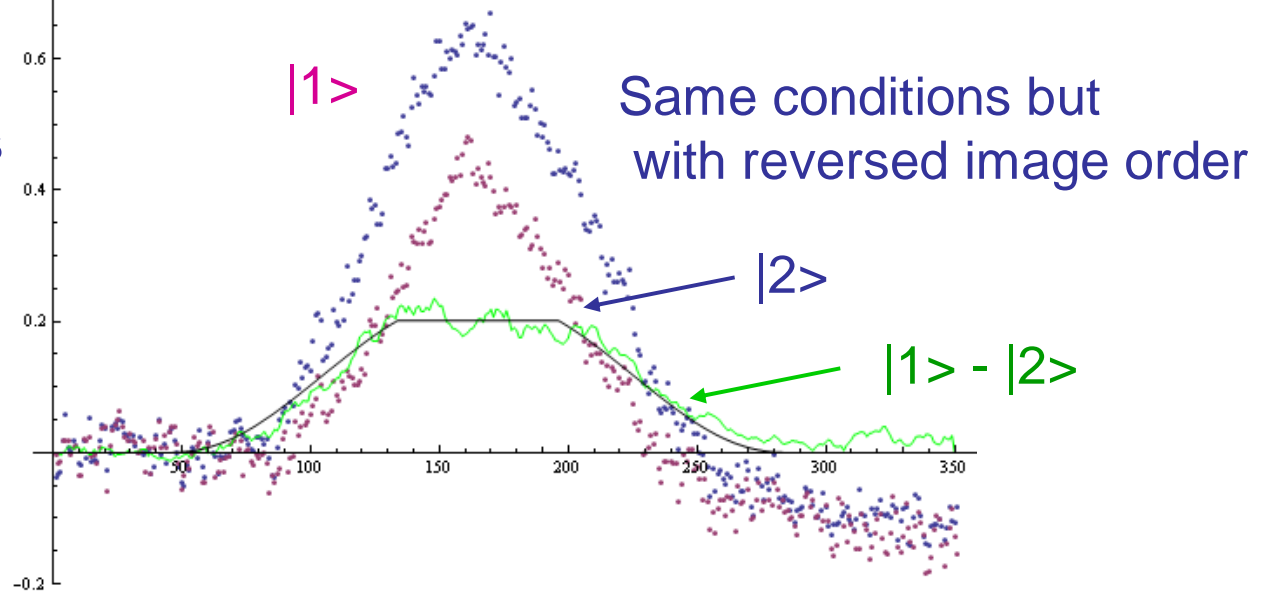
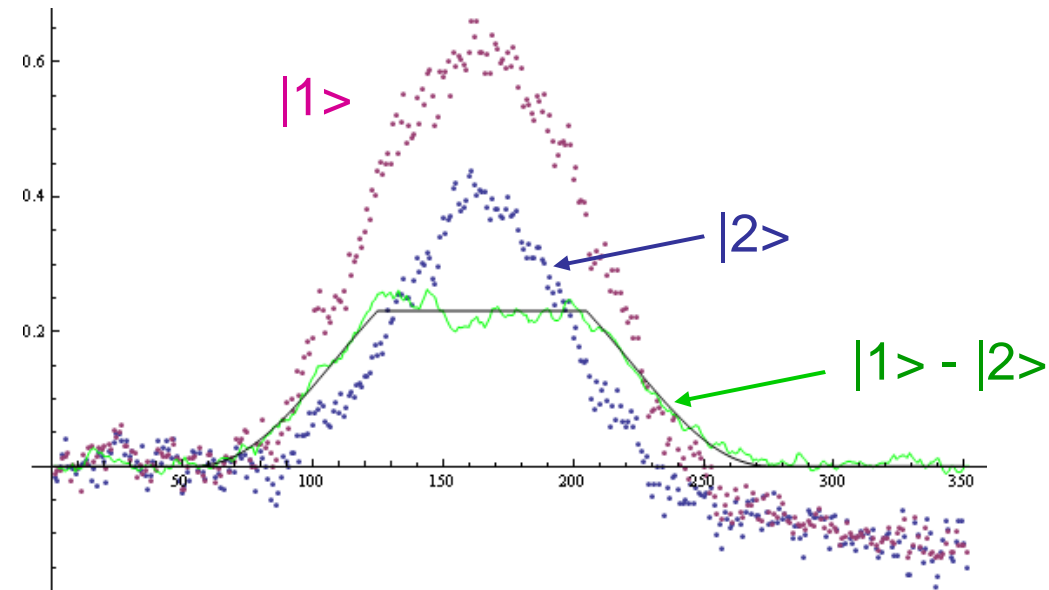
Profiles integrated along vertical direction

$P=0.39$
 $N1= 1.1 E5$
 $N2= 5.0 E4$

Flat top: characteristic
of equal densities
in SF core.

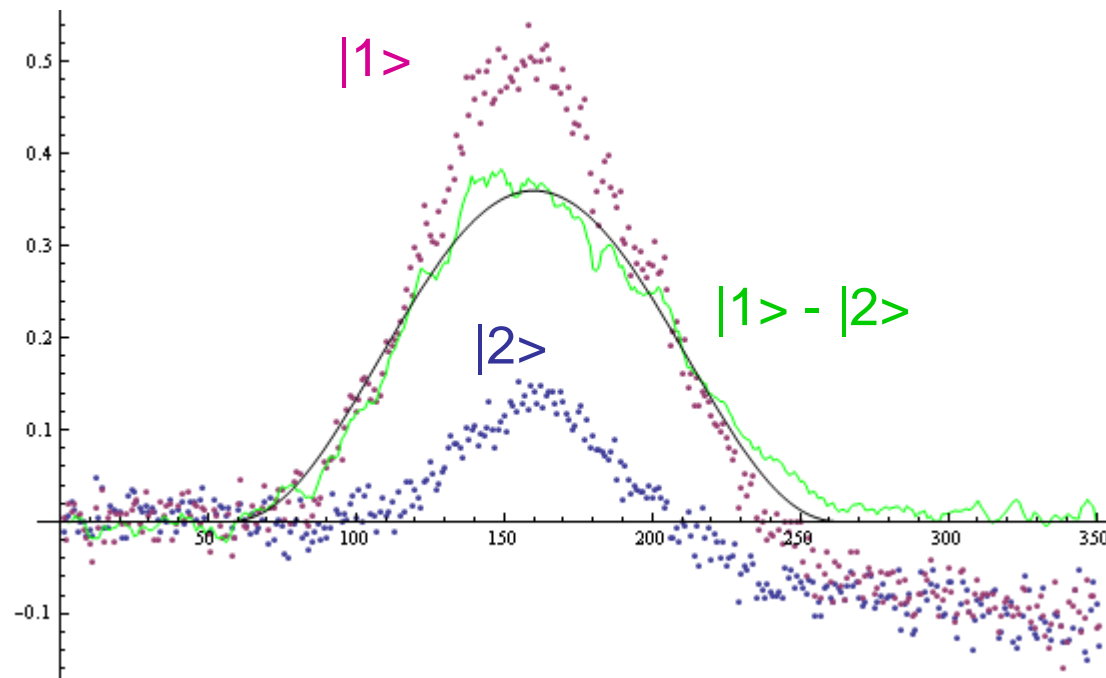
No violation of LDA
Consistent with 3 phases
scenario.

$P= 0.34$
 $N1= 1.1 E5$
 $N2= 6.0 E4$



Clogston-Chandrasekhar limit

$P=0.75$ with $N_1=8.7e4$ et $N_2=1.2e4$



Plateau non longer present on difference of integrated densities. Breakdown of SF phase

Outlook (1)

Preliminary results !

Data analysis and exp. checks ongoing !

Preliminary conclusion: 3 phases scenario as MIT despite of high aspect ratio (50).

Role of trap anisotropy to explore in more detail.

Dynamics:

Collective modes

second sound (recent paper by Trento group)

Temperature effects

Another way to imbalance Fermi spheres

Fermi mixtures

Ex: ${}^6\text{Li}$ - ${}^{40}\text{K}$, ${}^6\text{Li}$ - ${}^{173}\text{Yb}$, ${}^6\text{Li}$ - ${}^{87}\text{Sr}$

Different masses

Different tunnel rates in optical lattices

Stability of Fermi-Fermi mixture (F. Schreck talk)

Heteronuclear bosonic molecules (K. Dieckmann talk)

Polar molecules

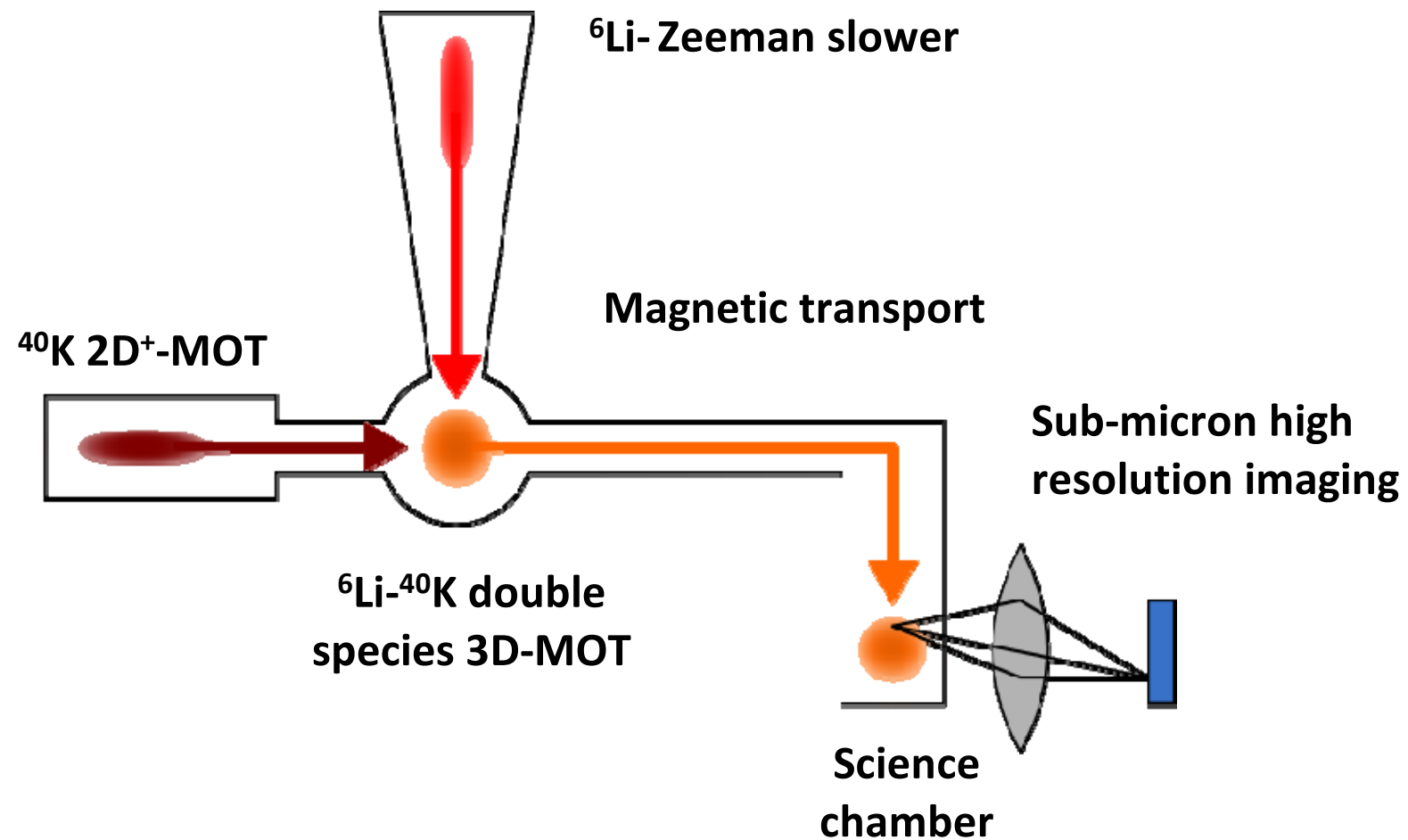
Few-body physics (D. Petrov talk)

Ground state in harmonic trap in the limit of large mass imbalance: Wigner crystal

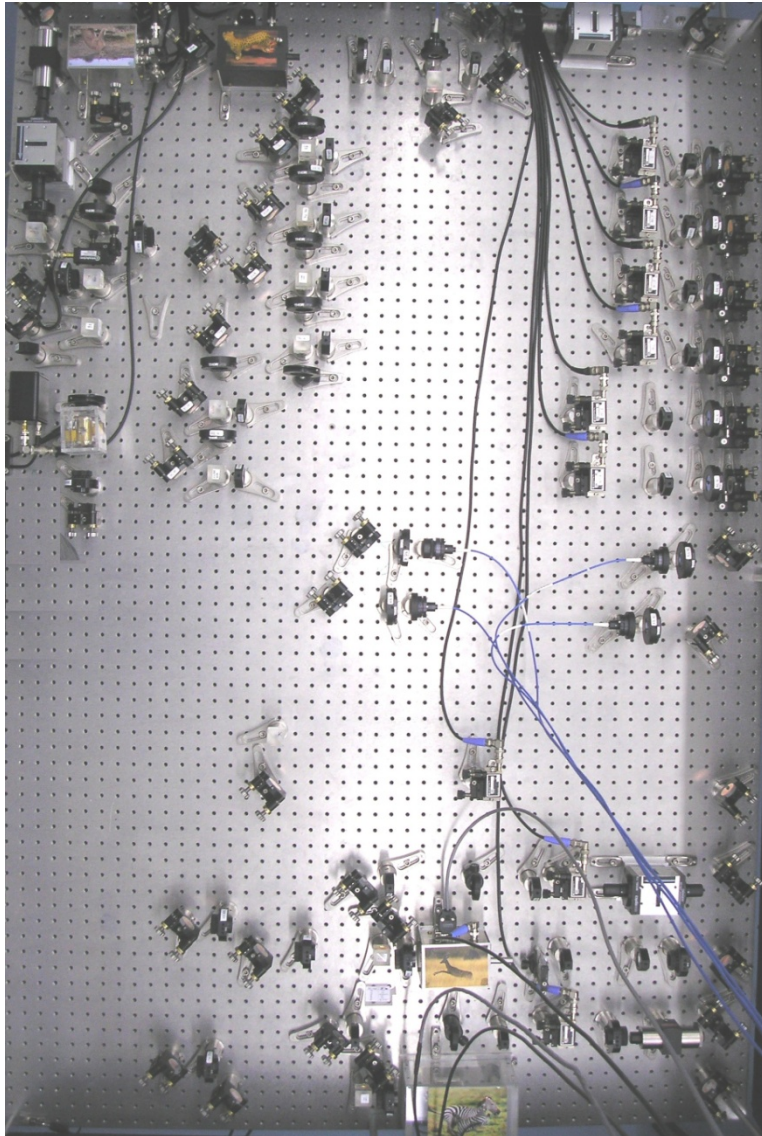
Quantum simulation of mixtures in optical lattices

Disorder induced by local interactions with impurities (Castin)

The ENS Fermi mixture experiment ${}^6\text{Li}$ - ${}^{40}\text{K}$

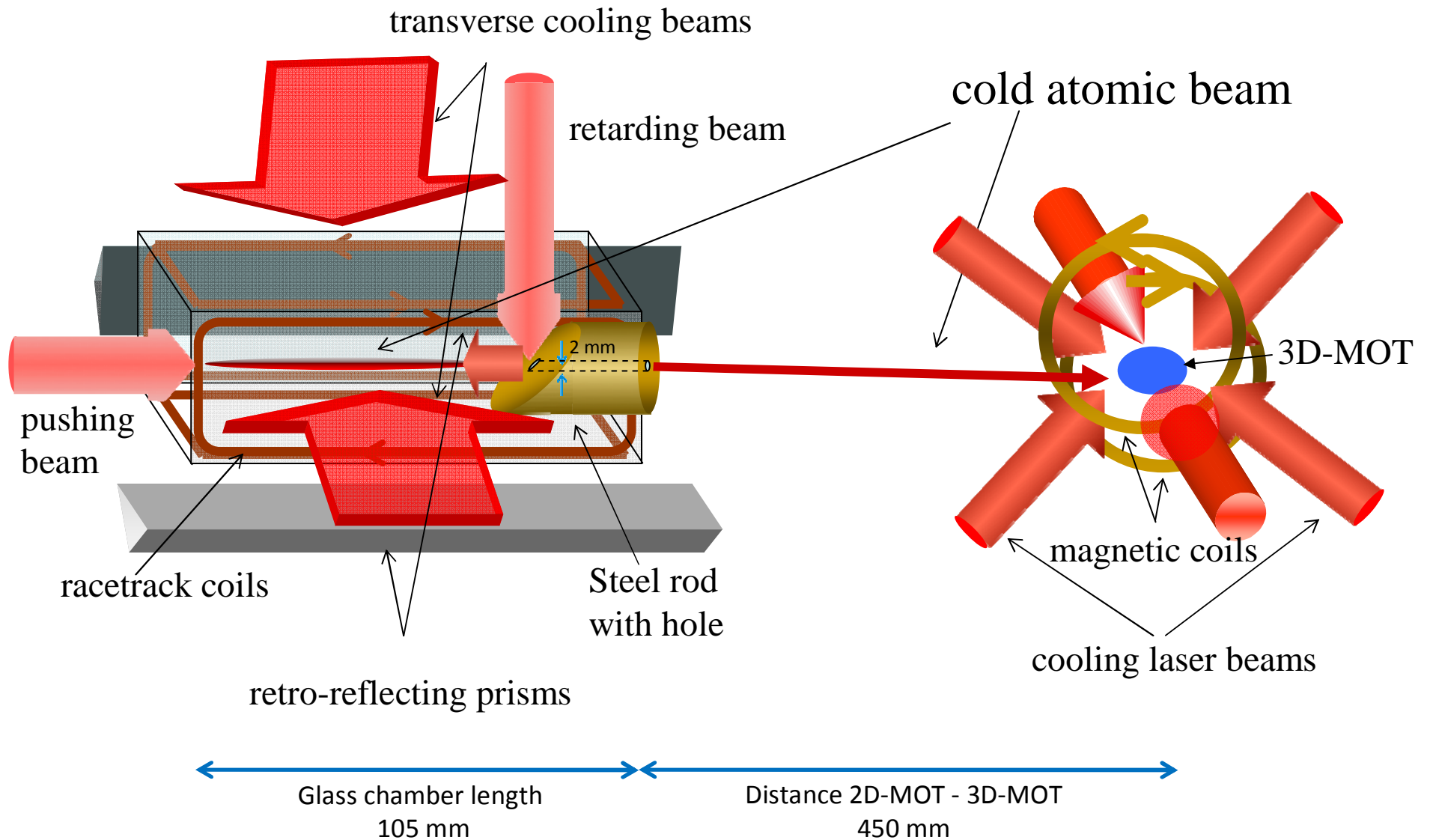


Potassium 767 nm Laser Setup



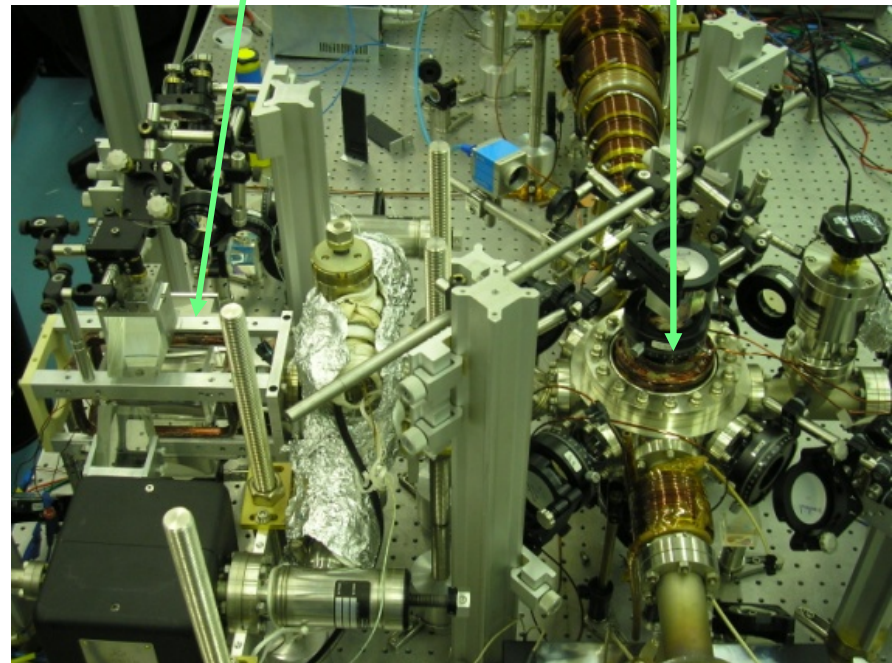
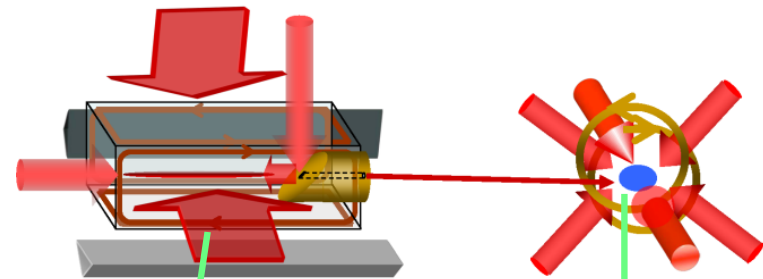
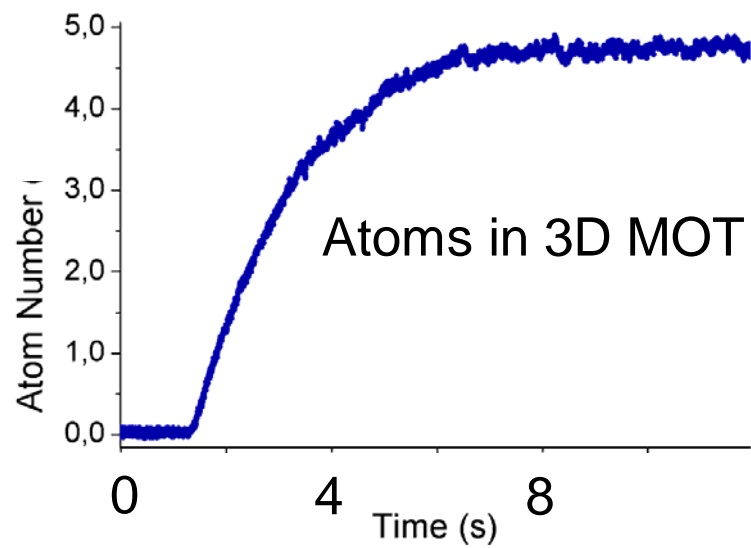
- Master laser diode
 - $P = 53 \text{ mW}$ @ $I = 105 \text{ mA}$
(200 mA max.)
- Toptica Pound-Drever-Hall locking system 20 MHz
- 3x Tapered amplifier (Eagleyard):
 - $P_{\text{TA, max}} = 1.5 \text{ W}$ @ 3 A
& 20 mW injection
 - $P_{\text{TA, typ}} = 700 \text{ mW}$ @ 1.8 A
& 15 mW injection
(almost saturated)
 - $P_{2\text{D}/3\text{D}} = 190 \text{ mW}$
after AOMs + fibers

Potassium 2D⁺ MOT



^{40}K 3D MOT loading

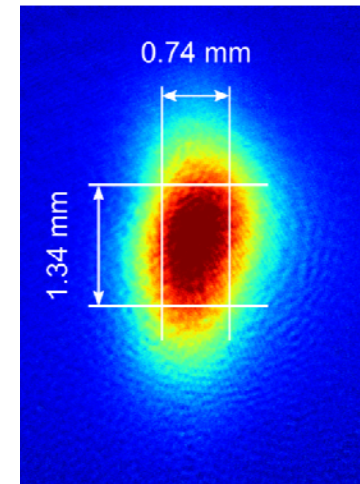
- 2D+ MOT
 - Flux : $2 \cdot 10^9$ at./s
 - Mean velocity 20 m/s



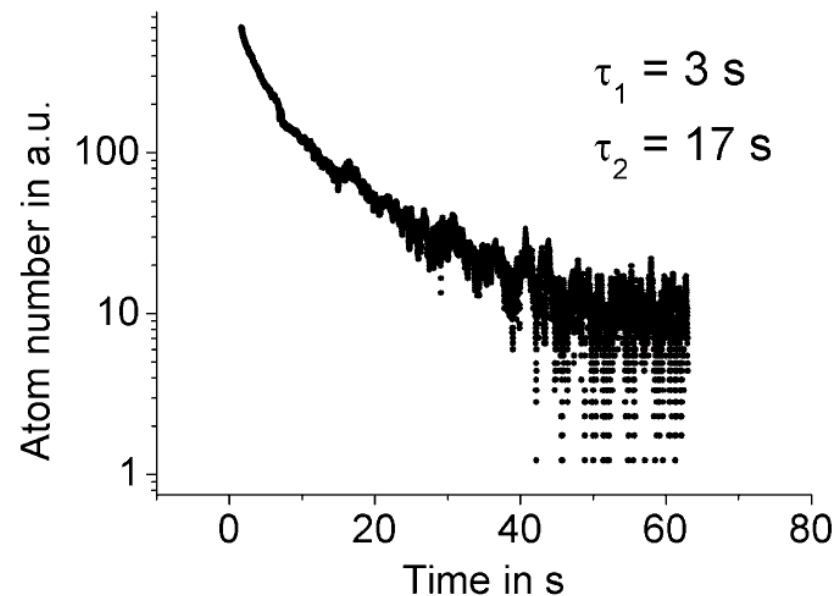
^{40}K 3D MOT parameters

- 3D-MOT

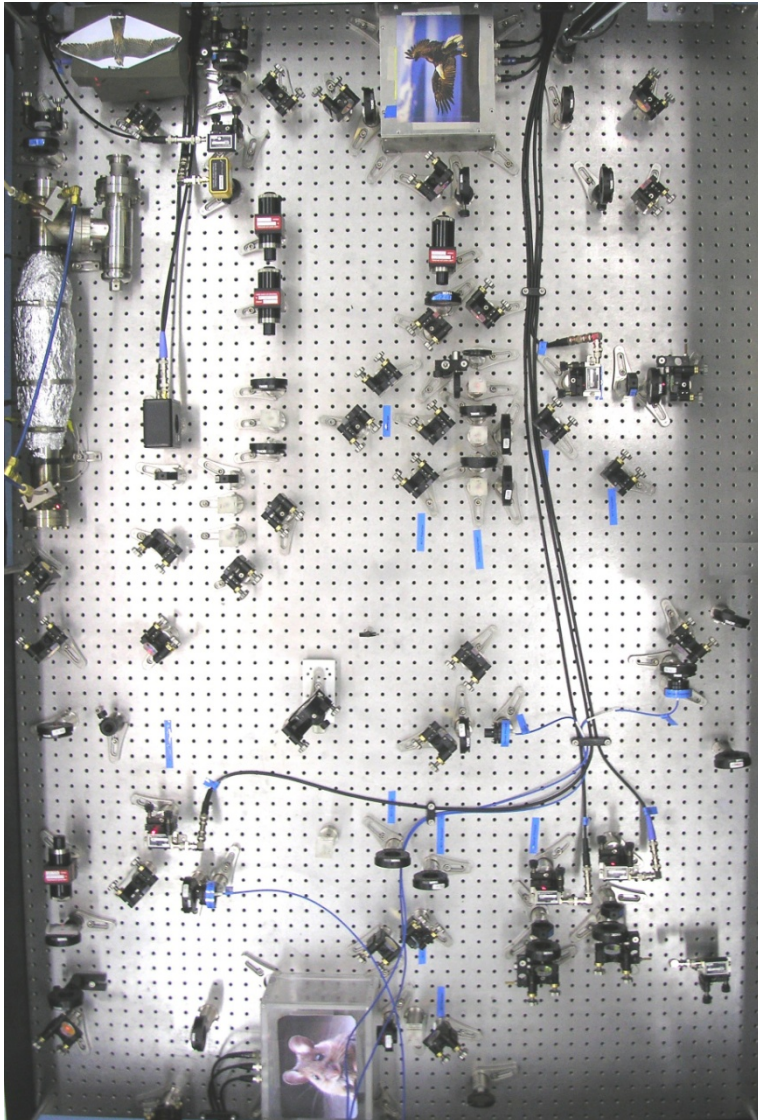
- Number of atoms $5 \cdot 10^9$ at.
- Lifetime 3 s / 17 s
- 3D-MOT temperature 230 μK
- Compressed MOT temperature $> 500 \mu\text{K}$



– ^{39}K MOT : $N_{\text{at}} > 8 \cdot 10^9$



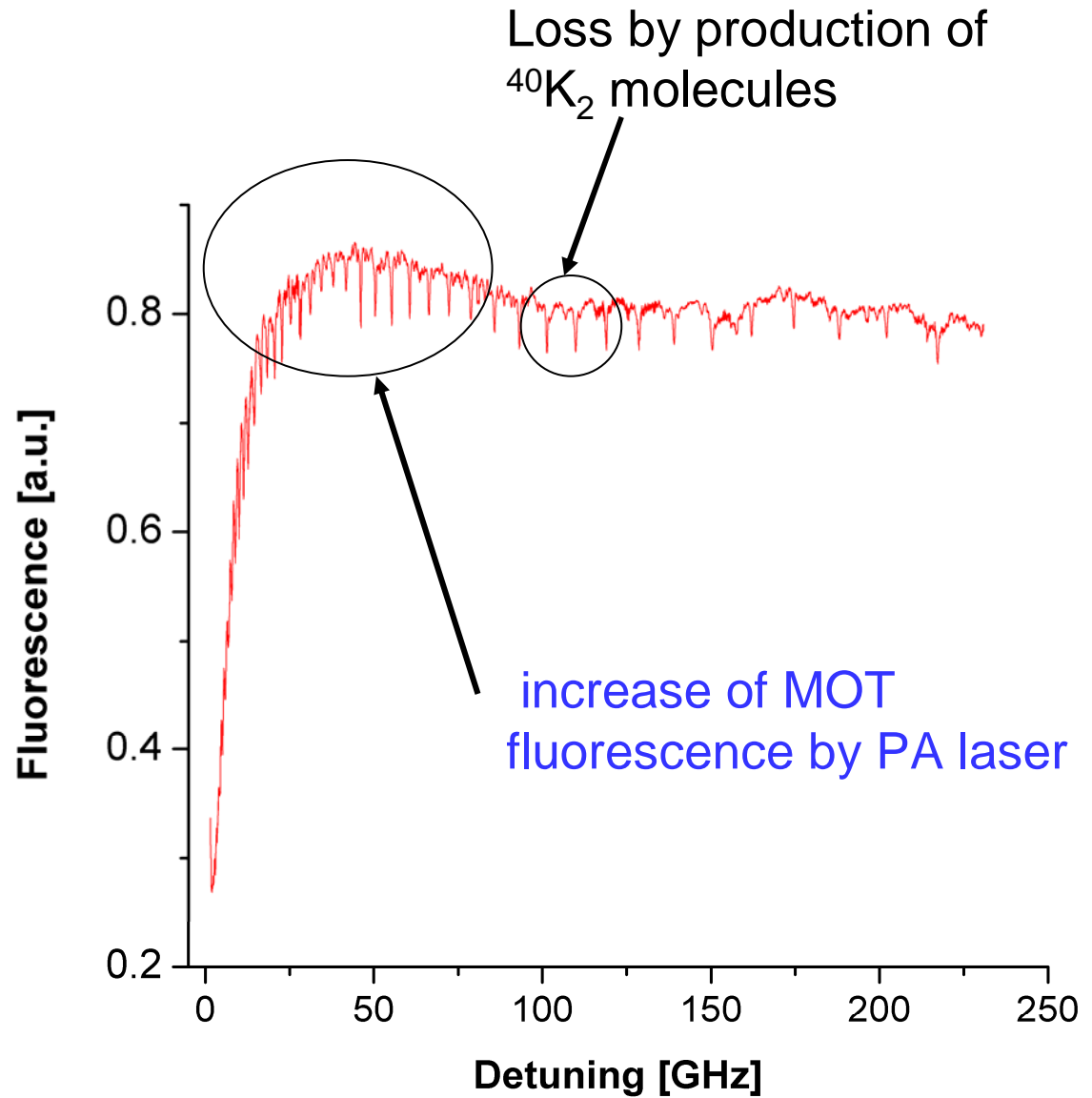
Lithium 6 laser system at 671 nm



- Master laser diode
 - $P = 40 \text{ mW} @ I = 120 \text{ mA}$
 - Topica Pound-Drever-Hall locking system 20 MHz
 - 2x Tapered amplifier (Topica):
 - $P_{\text{TA, max}} = 500 \text{ mW} @ 960 \text{ mA}$
& 15 mW injection
 - $P_{\text{Zeeman}} = 120 \text{ mW}$ after AOM
+ fibers
 - $P_{\text{MOT}} = 140 \text{ mW}$ after
AOMs + fibers
- Double MOT
6Li: $5 \cdot 10^8$ atoms loaded in 5 s.
40K: $5 \cdot 10^9$ atoms loaded in 5 s.

Photoassociation of Potassium 40

Scan an intense laser
below S-P resonance
Look at MOT steady state
fluorescence.
1.4 W/ 4.4 mm²
retroreflected PA beam



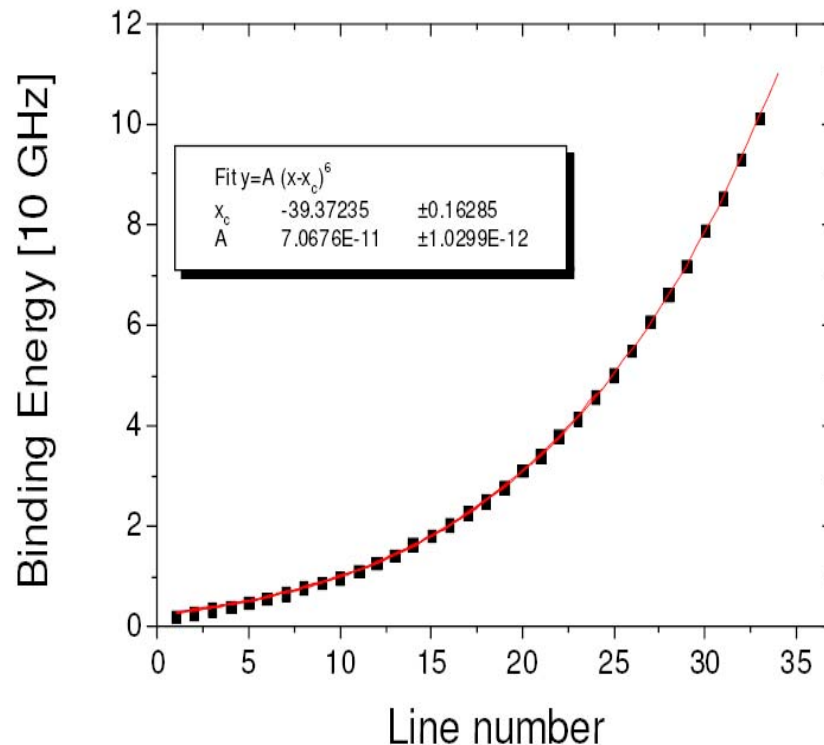
Energy of photoassociation lines

For $V(R) = -C_3/R^3$ long range potential (dipole-dipole),
the energy of high lying bound states scales as:

$$E_n = -A(n - n_0)^6$$

This is simply deduced from a WKB approx. with hard core at short range.

R. Le Roy and R. Bernstein, J. Chem. Phys. 52, 1970



A is related to C_3
and to the exponent
of long range potential

We find $A/h = 0.7067$

Giving $C_3 = 14.13 (20)$ a.u.

Very good agreement with
Wang et al. value: $14.14 (5)$

Summary

- Next step: photoassociation of 40K-6Li mixture
Towards polar molecules in GS with dipole moment of 3.6 D
- Magnetic transport and evaporation to quantum degeneracy
- Simulation in 2D and 1D of various Hamiltonians
Lattices with frustration
Challenge: cool in the lattice to get $k_B T < J_{ex} = t^2 / U$

See proposals to cool in lattice by removal of high entropy atoms

- [T. L. Ho, Q. Zhou, arXiv:0808.2652](#)
- [J. S. Bernier, C. Kollath, A. Georges, L. De Leo, F. Gerbier, C. Salomon, M. Köhl , Arxiv 0902.0005](#)

Effect of photoassociation laser light shift

Overall shape of Fluorescence signal determined by :

MOT beam fluo.

PA laser fluo.

PA light shift,

which depends on detuning

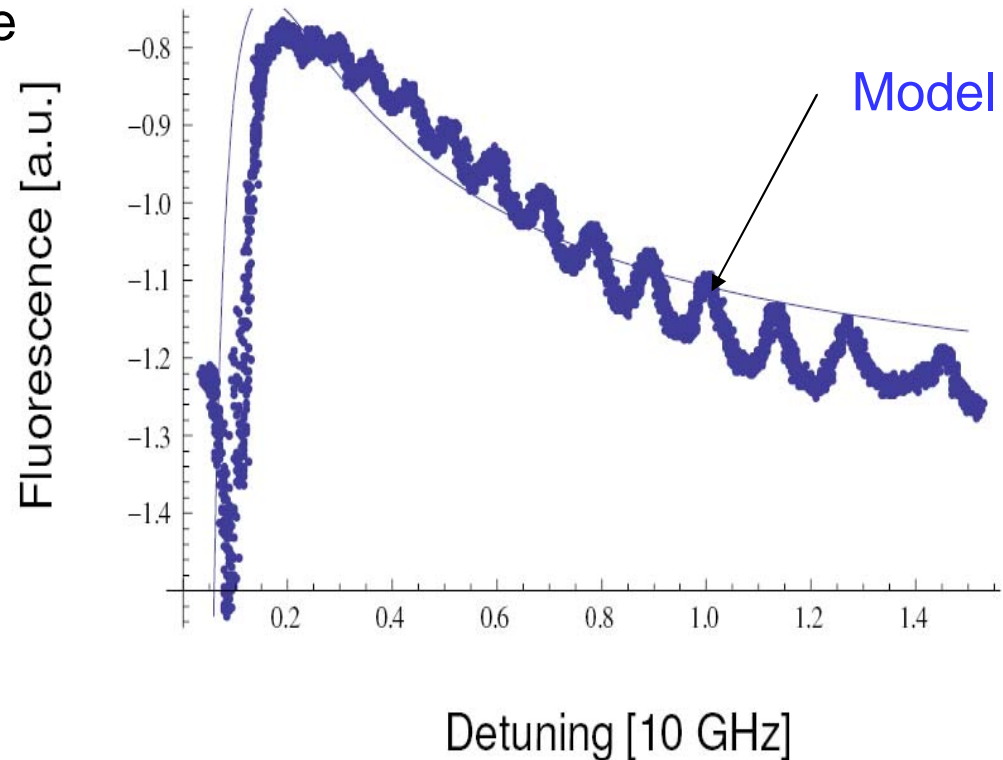
Simple model:

$$\Phi_{\text{MOT}} = \frac{\Gamma}{2} \left(\frac{s}{1+s} \right),$$

$$s = \frac{I_{\text{MOT}}/I_{\text{sat}}}{1 + 4\Delta_0^2/\Gamma^2}.$$

$$\Delta' = \frac{\Delta_{\text{PA}}}{2} \ln(1 + s_{\text{PA}}),$$

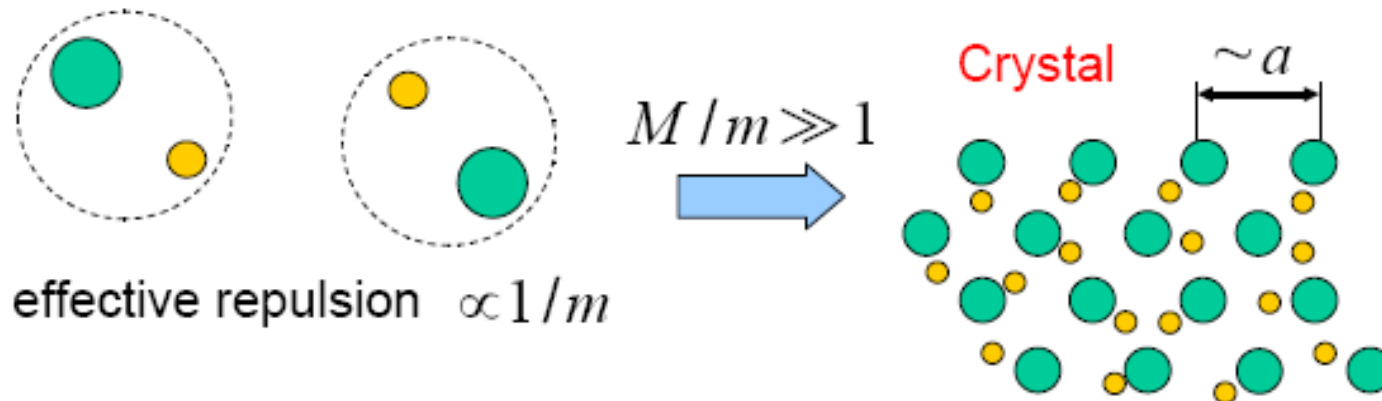
Thus: $\Phi_{\text{tot}} = A \left(\frac{s}{1+s} + \frac{s_{\text{PA}}}{1+s_{\text{PA}}} \right)$ with $s = \frac{I_{\text{MOT}}/I_{\text{sat}}}{1 + 4(\Delta_0 - \Delta')^2/\Gamma^2}.$



What is the ground state of a mixture of strongly interacting Fermi gases with large mass difference ?

A Wigner Crystal !

D. Petrov, G Astrakharchik, D. Papoular, C. Salomon, G. Shlyapnikov, PRL 99 (2007)



$$[-\nabla^2/M + U_{eff}(R)]\psi(R) = E\psi(R)$$

$$R \gg a \rightarrow U_{eff}(R) \approx \frac{2\hbar^2}{m a R} \exp[-2R/a]$$

