



**The Abdus Salam
International Centre for Theoretical Physics**



2037-11

Introduction to Optofluidics

1 - 5 June 2009

Extended optical micromanipulation with test objects of special shape

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Introduction to optofluidics
Trieste, 2009

Extended optical micromanipulation with microstructures of special shape

Pál Ormos

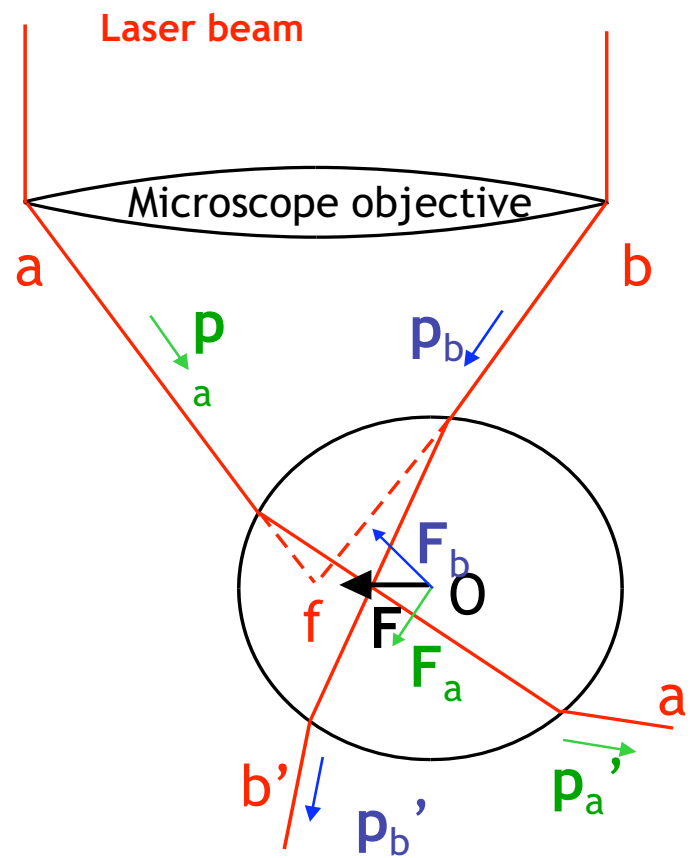
Institute of Biophysics
Biological Research Centre
Hungarian Academy of Sciences

Szeged
Hungary

Topics

- Structure building by photopolymerization
- Extended manipulation possibilities
- Rotation and torque measurement in optical tweezers
- Light generated and light driven optomechanical devices

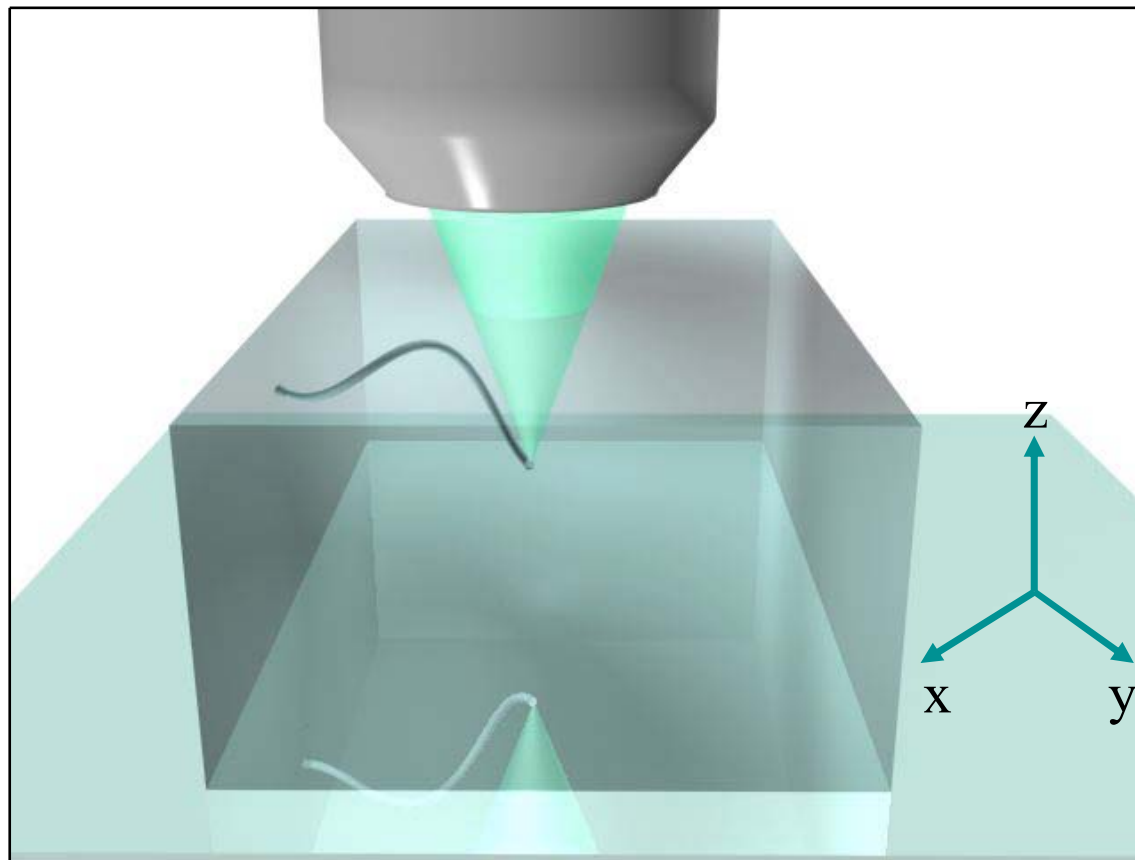
Optical tweezers



Trap non spherical objects

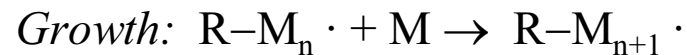
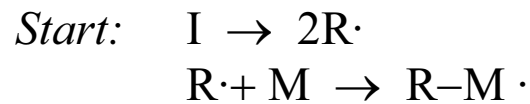
Gives additional control

Produce particles of arbitrary shape by two-photon photopolymerization



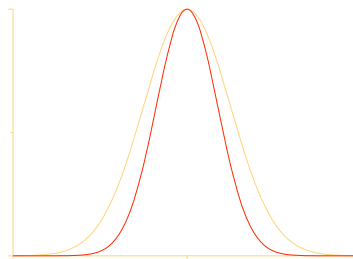
Produce particles of arbitrary shape by two-photon photopolymerization

The chemical process:

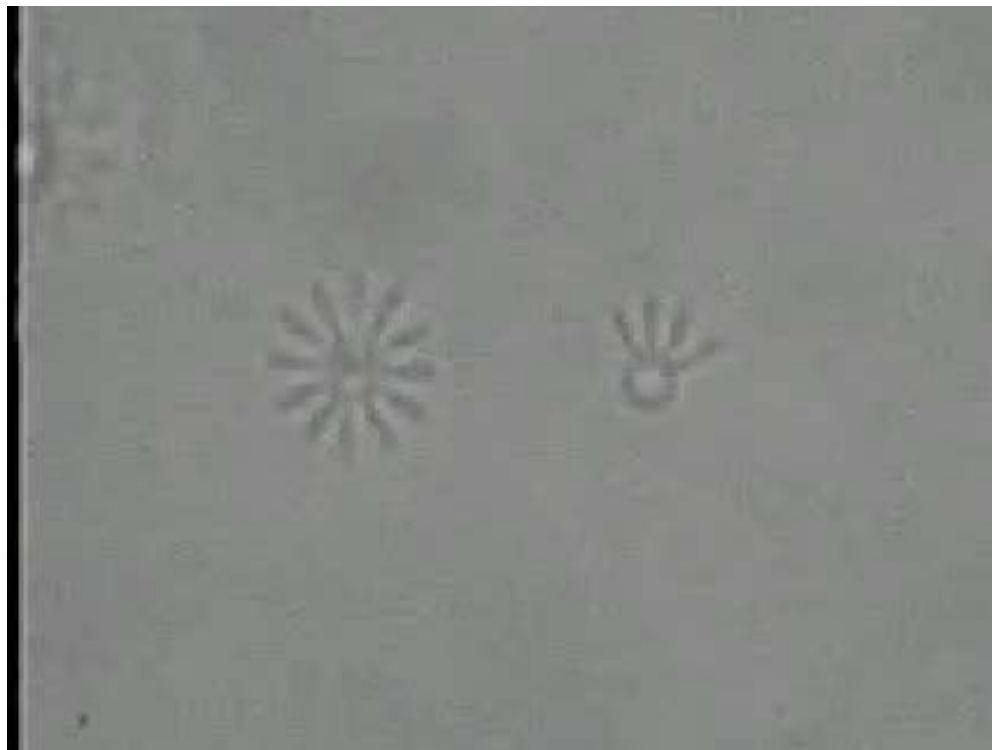


Two photon processes scale by the square of the intensity \Rightarrow better spatial resolution

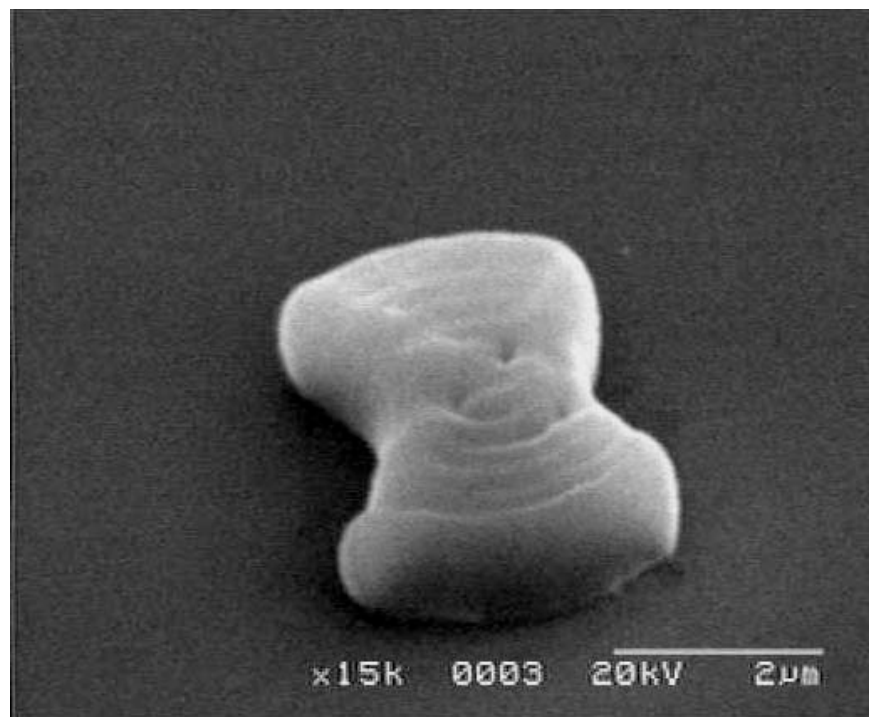
This brings smaller half width for a gaussian beam thus better spatial resolution



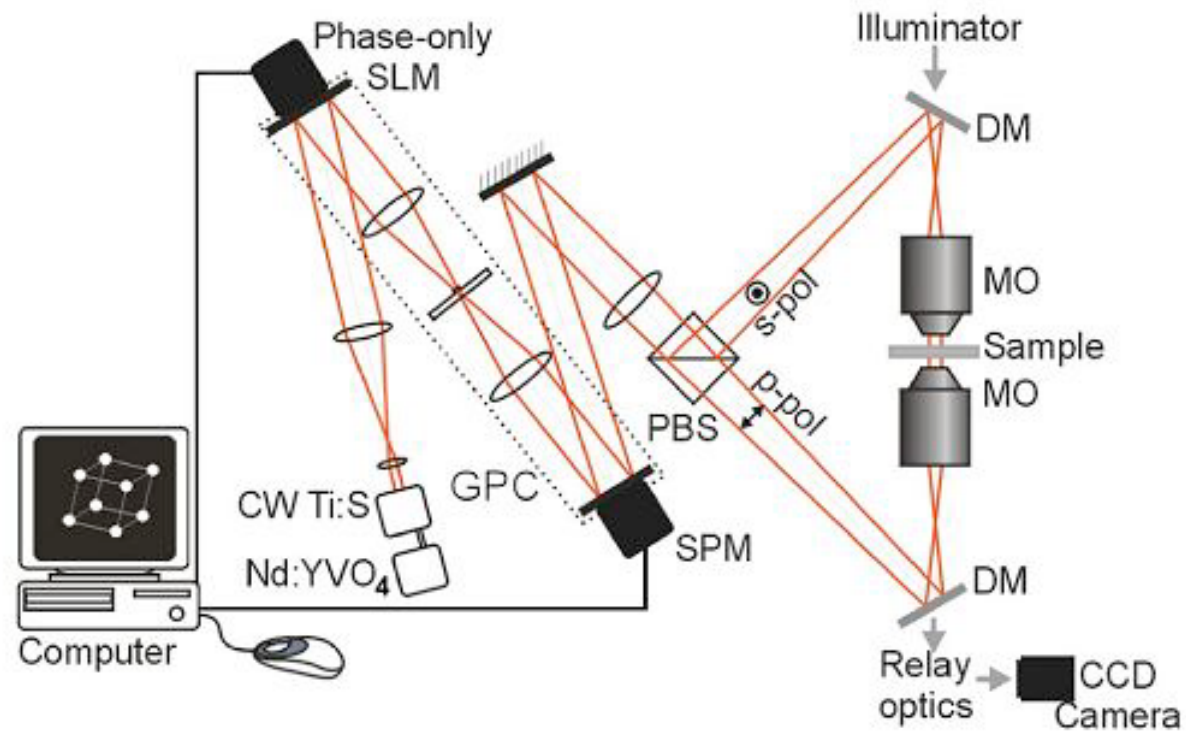
Produce particles of arbitrary shape by two-photon photopolymerization



Special structures for structure building by optical manipulation

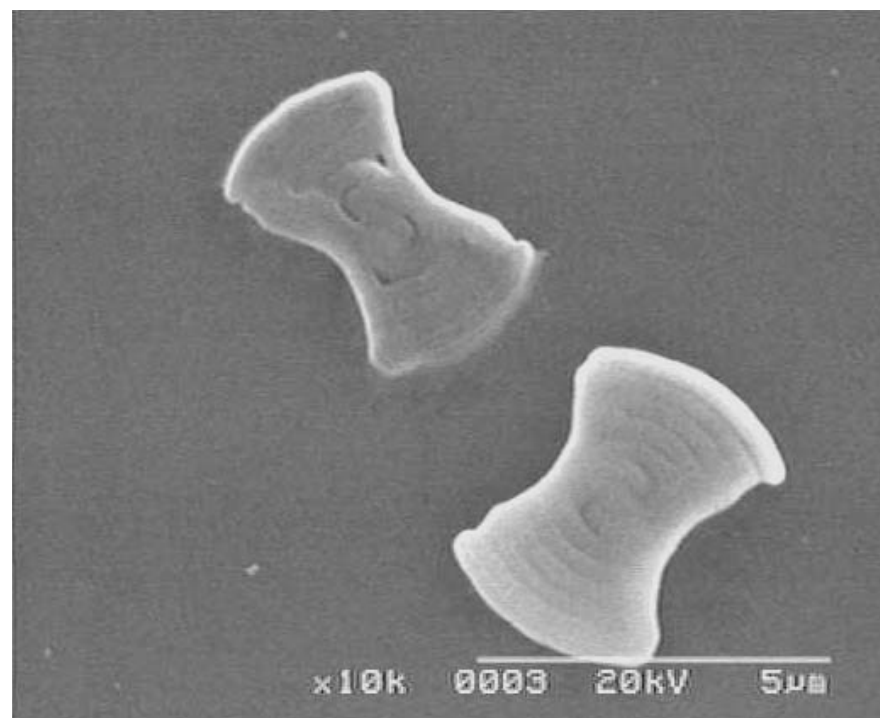


Multiple trap system of J. Glückstad

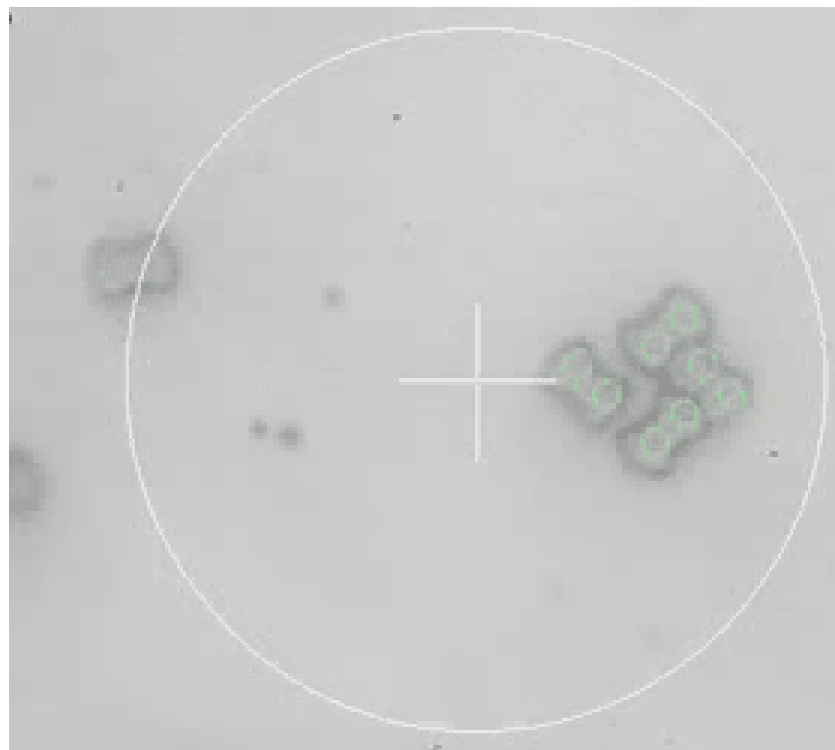


Jesper Glückstad, RISO

Special structures for structure building by optical manipulation

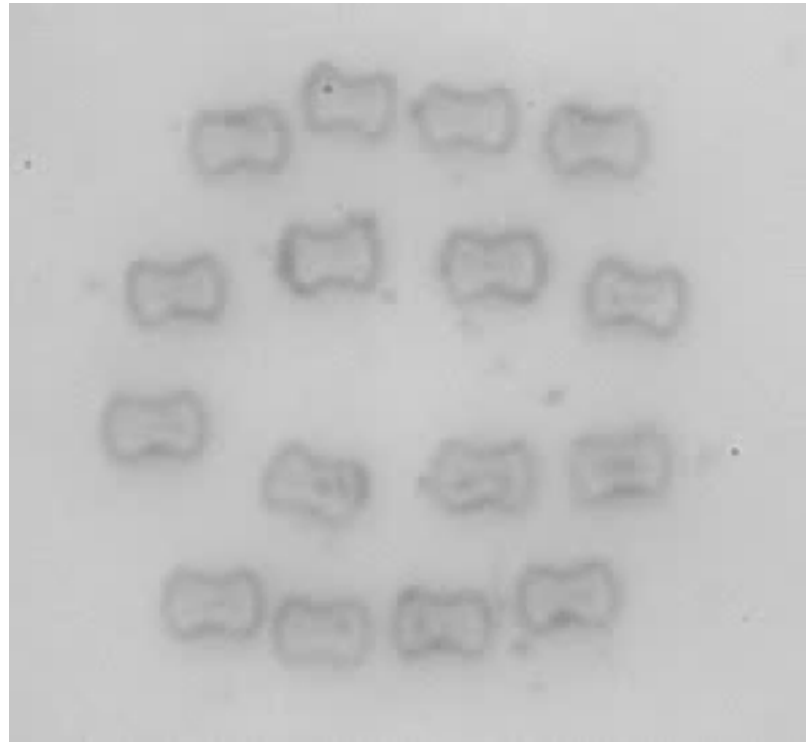


Special structures for structure building by optical manipulation



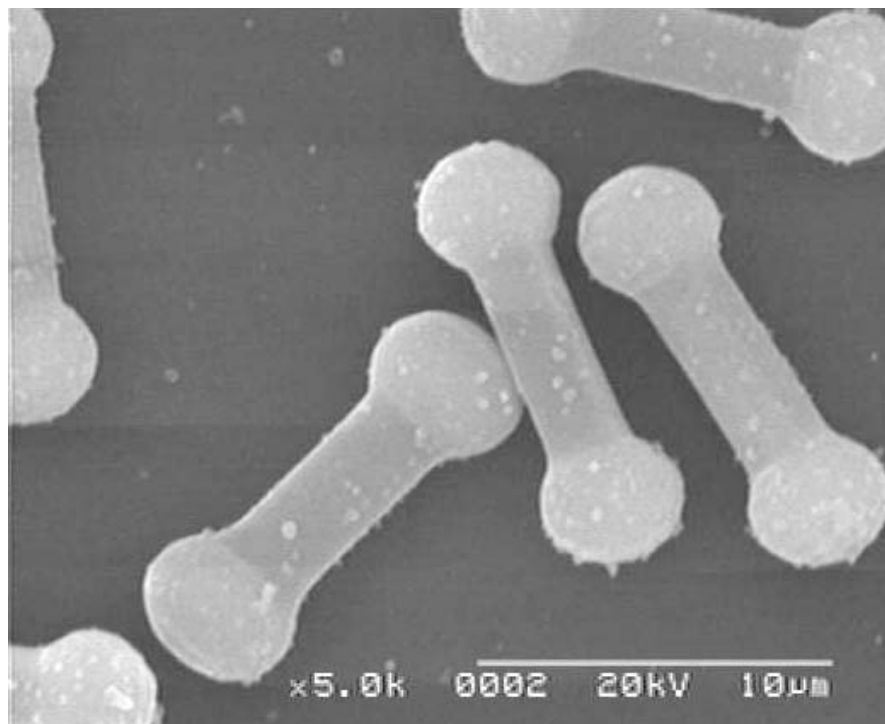
Collaboration with the Jesper Glückstad group at RISO

Special structures for structure building by optical manipulation

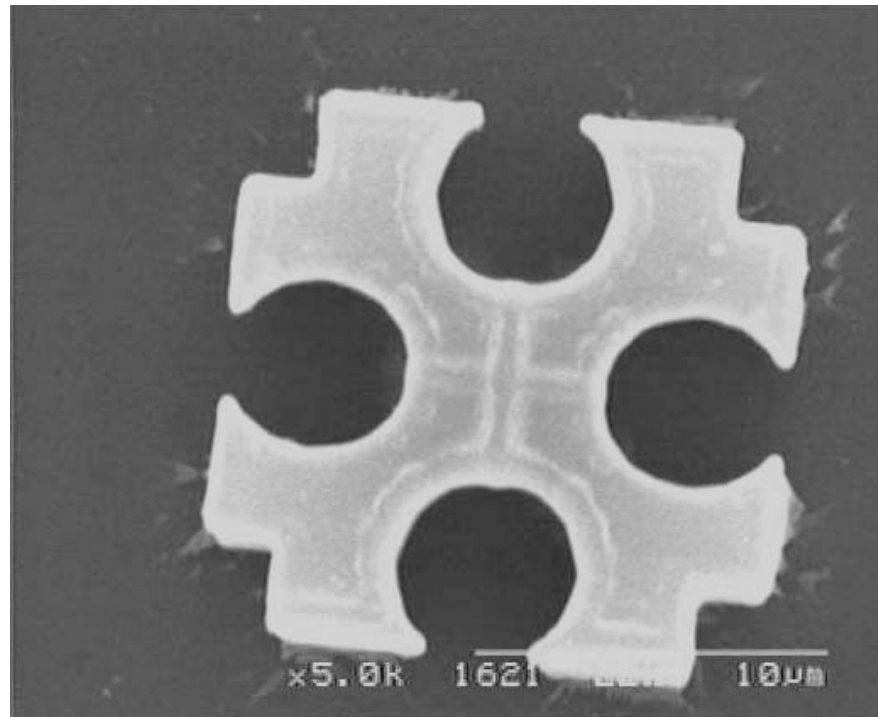


Collaboration with the Jesper Glückstad group at RISO

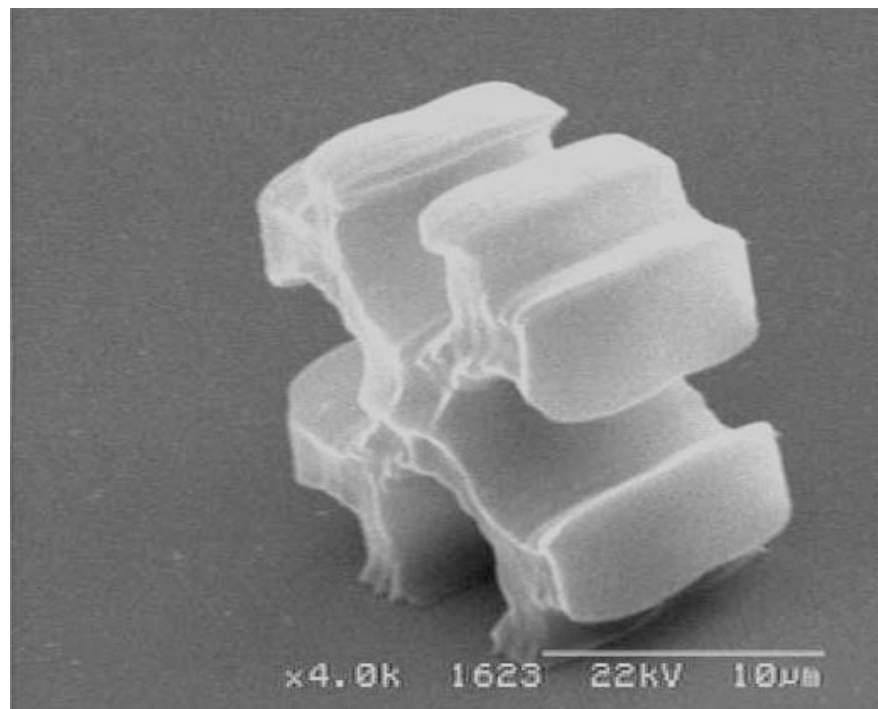
Special structures for structure building by optical manipulation



Special structures for structure building by optical manipulation



Special structures for structure building by optical manipulation



Special structures for structure building by optical manipulation



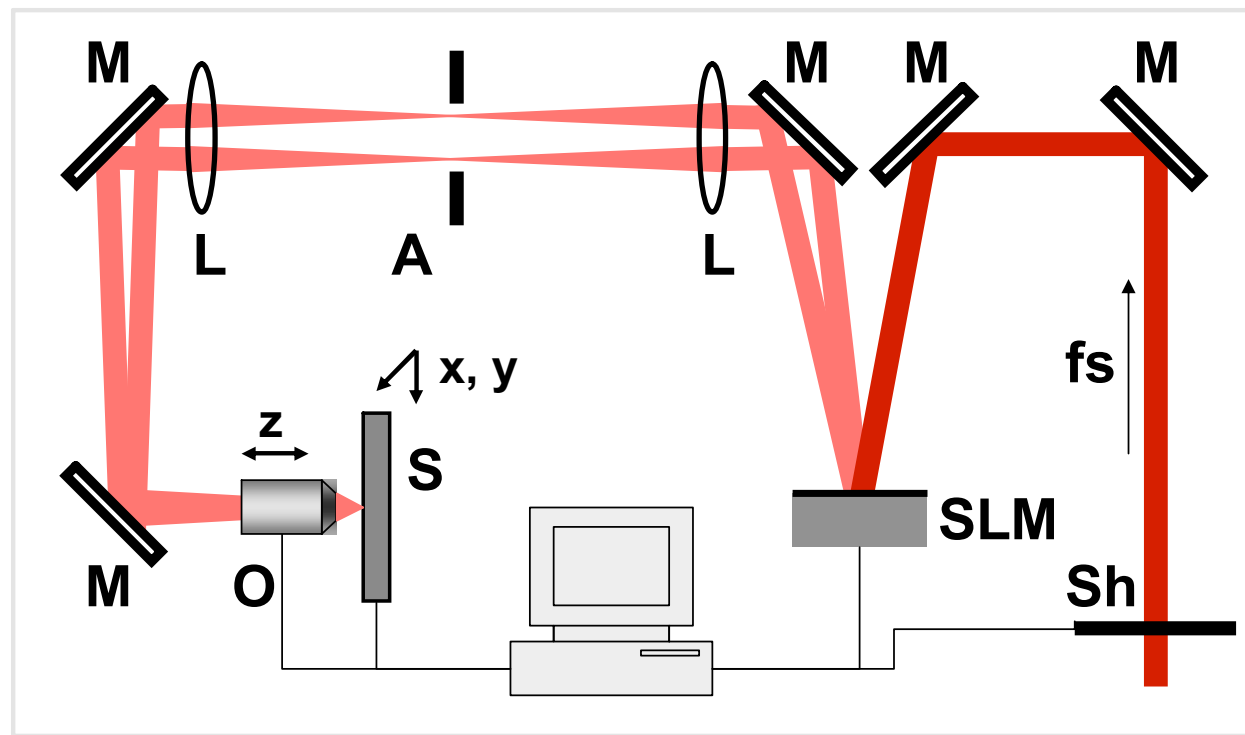
Collaboration with the Jesper Glückstad group at RISO

Photopolymerisation with SLM

Optical layout 2

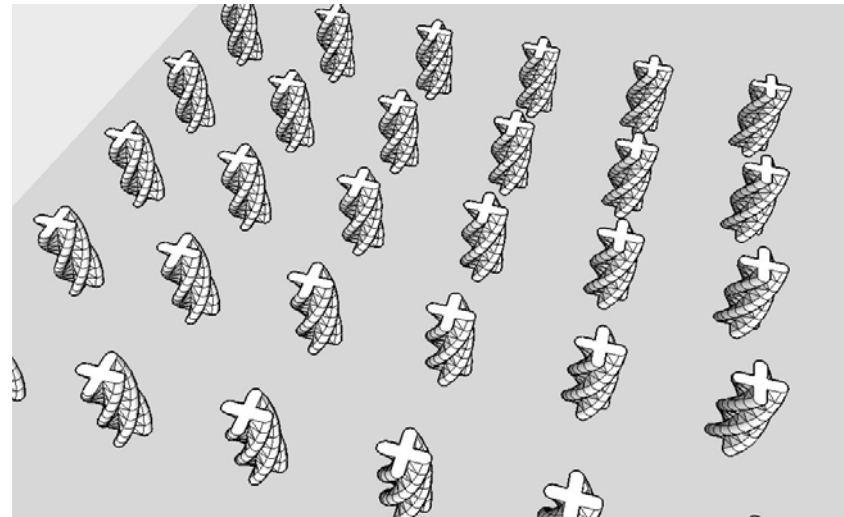
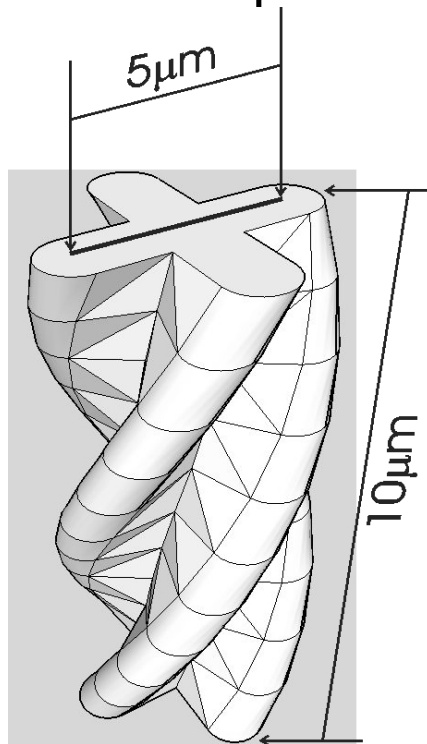
SLM

1 : 1 optics

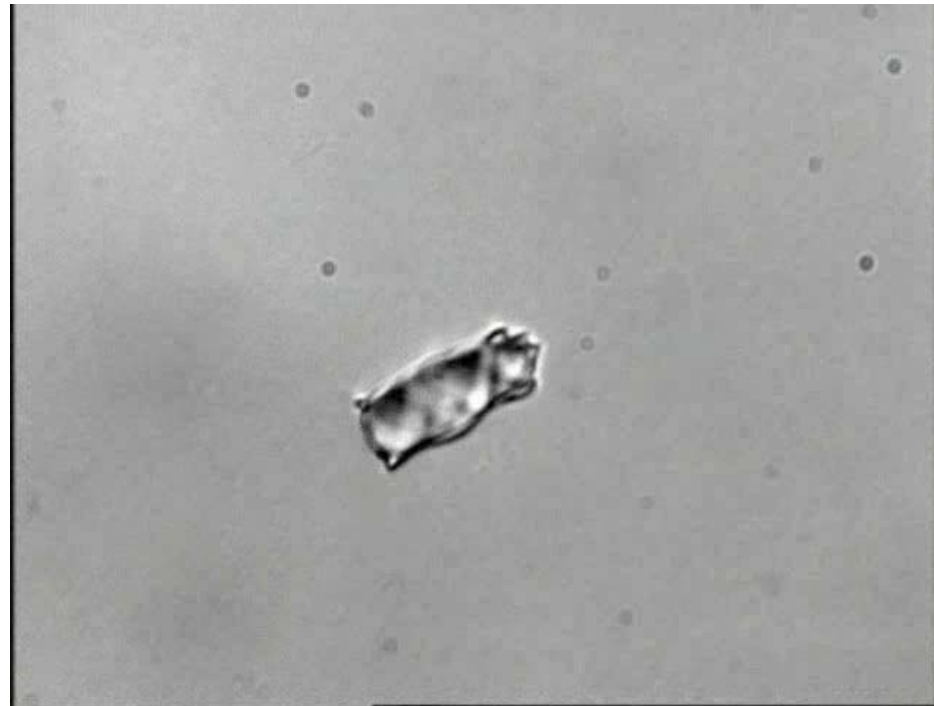


Test structures

To demonstrate the **applicability of SLMs** in photopolymerisation we produced **helical-shaped** objects to be manipulated later with **optical tweezer**



Rotating a holographically-made helical column by laser tweezers



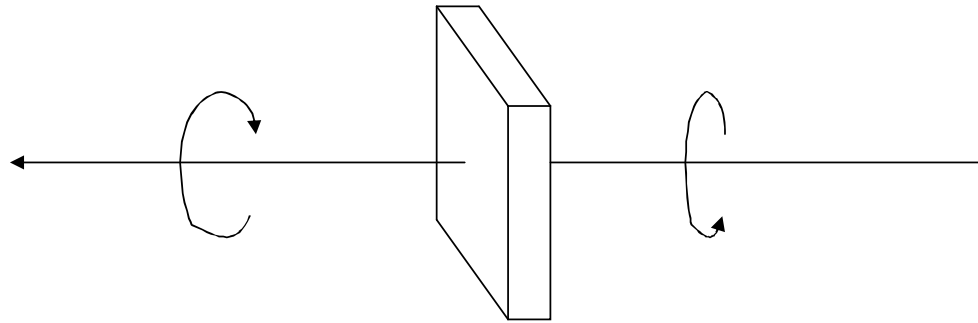
Rotation in optical tweezers

- Angular momentum carried by light
 - Rotate birefringent particles

- Helical scattering
 - Propeller

Polarised light acting on birefringent particle

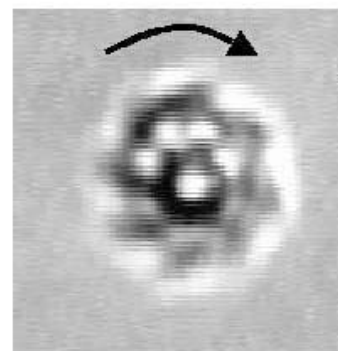
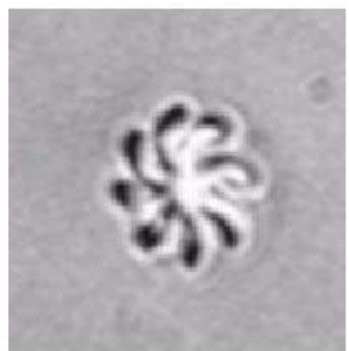
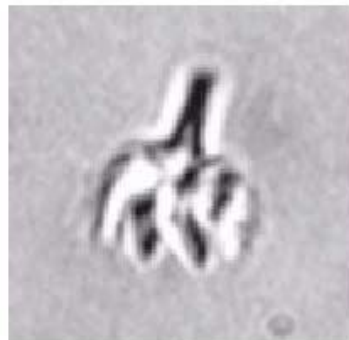
Electric field strength: $\vec{E} = E_0 e^{i\omega t} \cos \phi \bar{x} + iE_0 e^{i\omega t} \sin \phi \bar{y}$ (ϕ : ellipticity)



torque on unit surface of a birefringent material of thickness d :

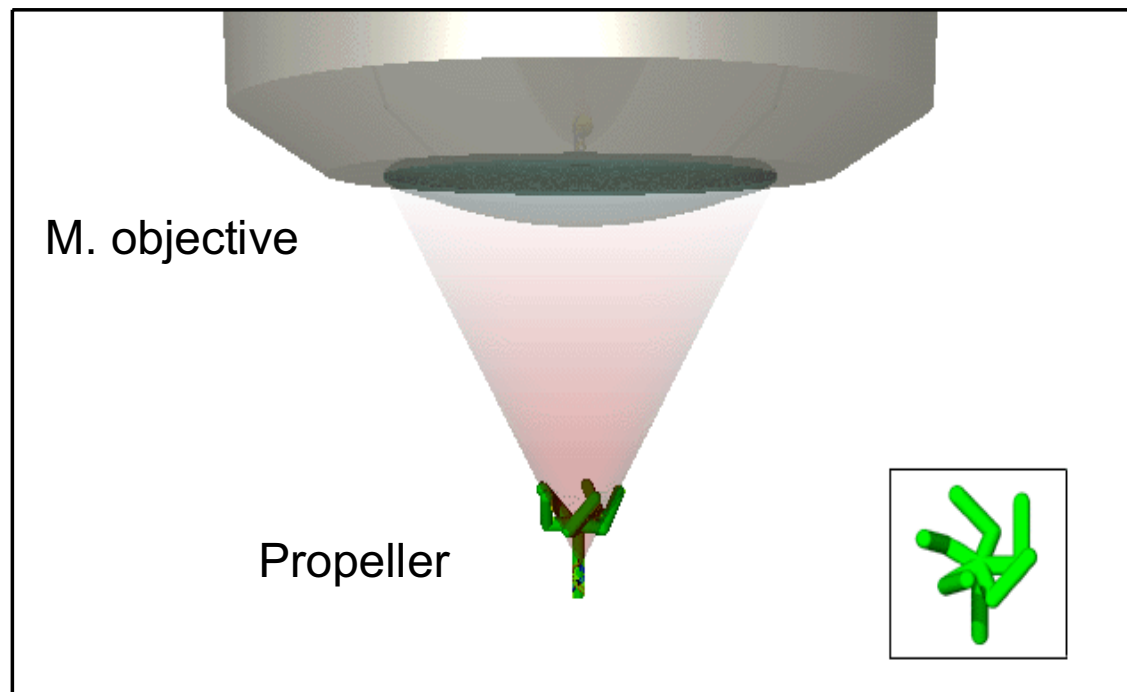
$$\begin{aligned} \bar{m} = & \frac{\varepsilon}{2\omega} E_0^2 \sin[kd(n_o - n_e)] \cos 2\phi \sin 2\theta + \\ & + \frac{\varepsilon}{2\omega} E_0^2 \{1 - \cos[kd(n_o - n_e)]\} \sin 2\phi \end{aligned}$$

Light driven propeller



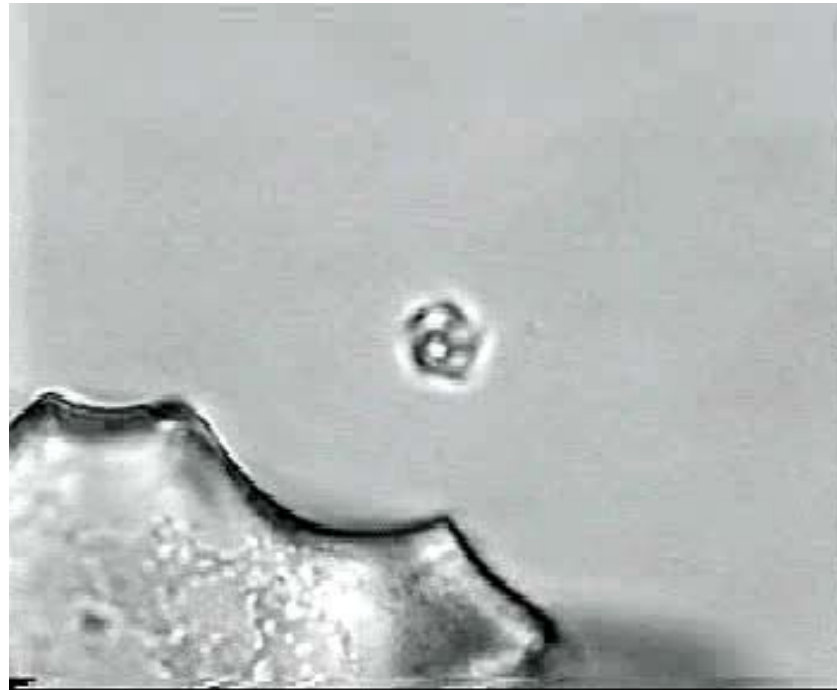
3 μm

Light driven propeller

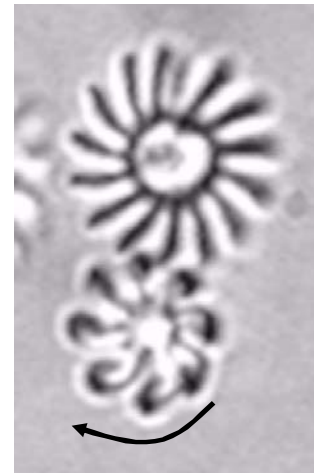
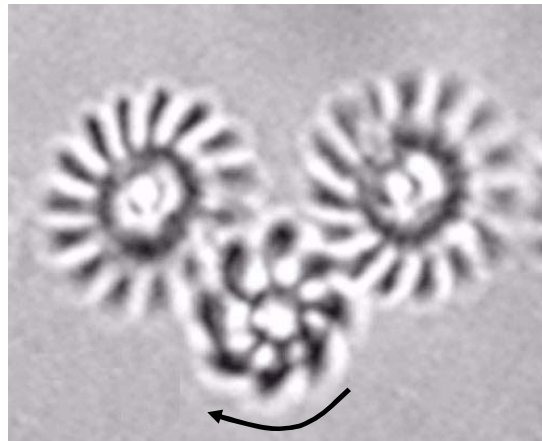
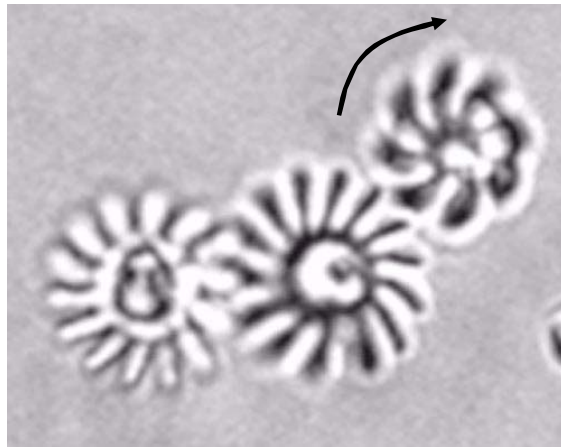


Galajda and Ormos, Appl. Phys. Lett. (2001)

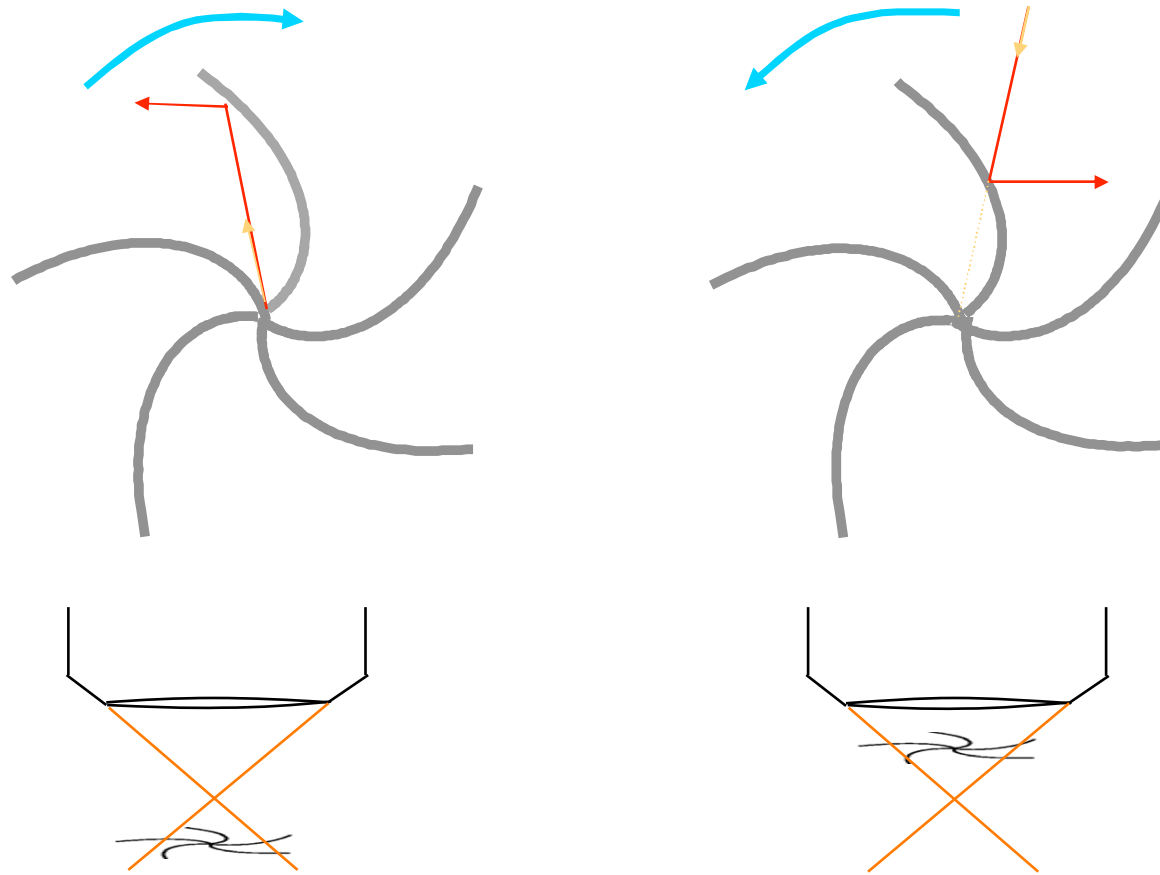
Light driven propeller



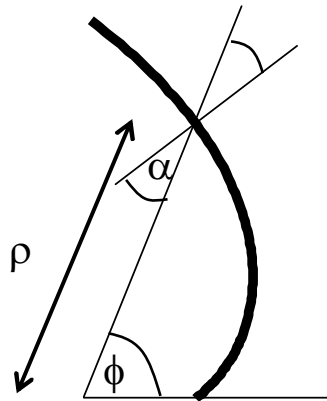
Complex optomechanical machines



Study of light induced rotation: controlling the direction

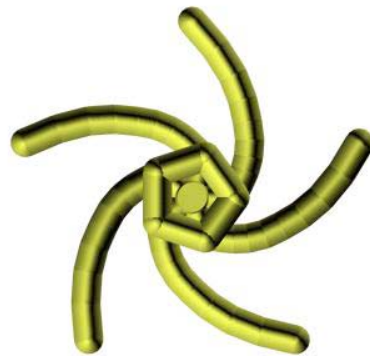


Study of light induced rotation: controlling the direction

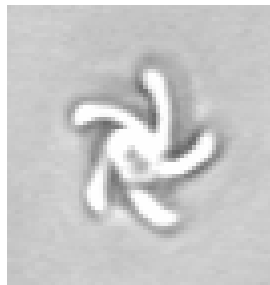
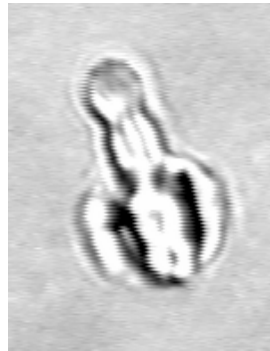


Equation of a logarithmic spiral in a polar coordinate system:

$$\rho = a \cdot e^{k\Phi} \quad k = \text{ctg}\alpha$$



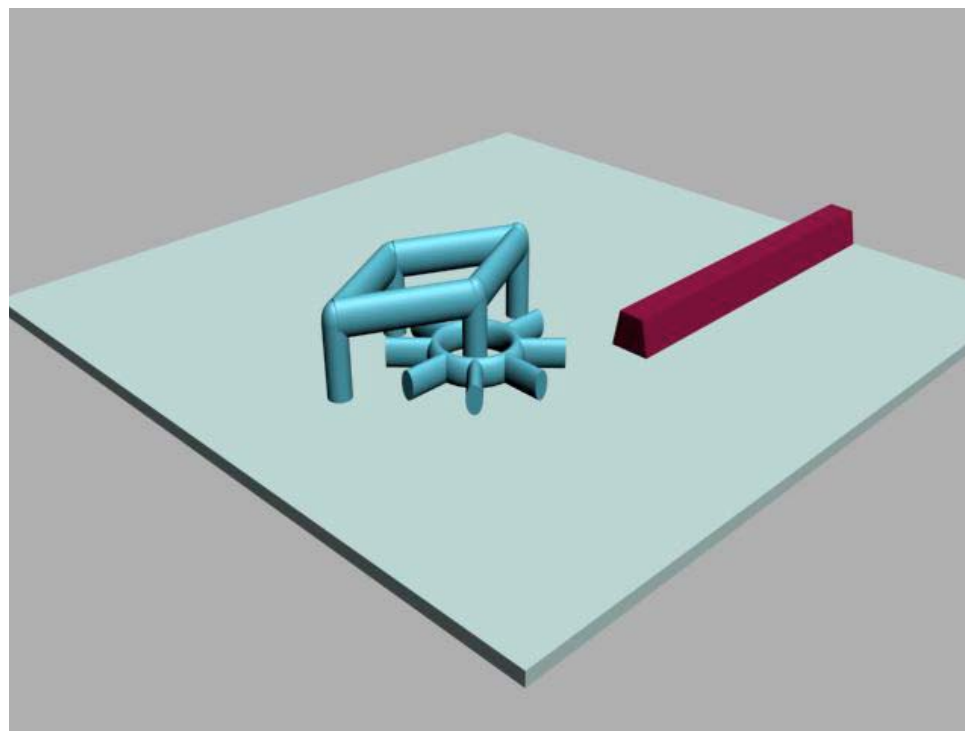
Study of light induced rotation: controlling the direction



Reverse rotational direction

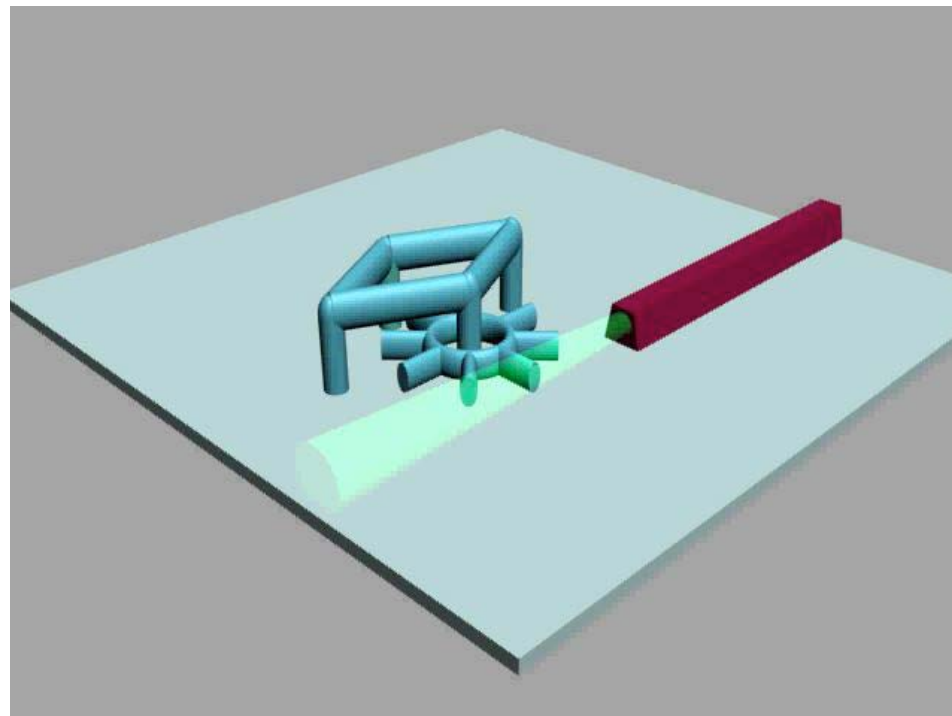


Integrated optical motor

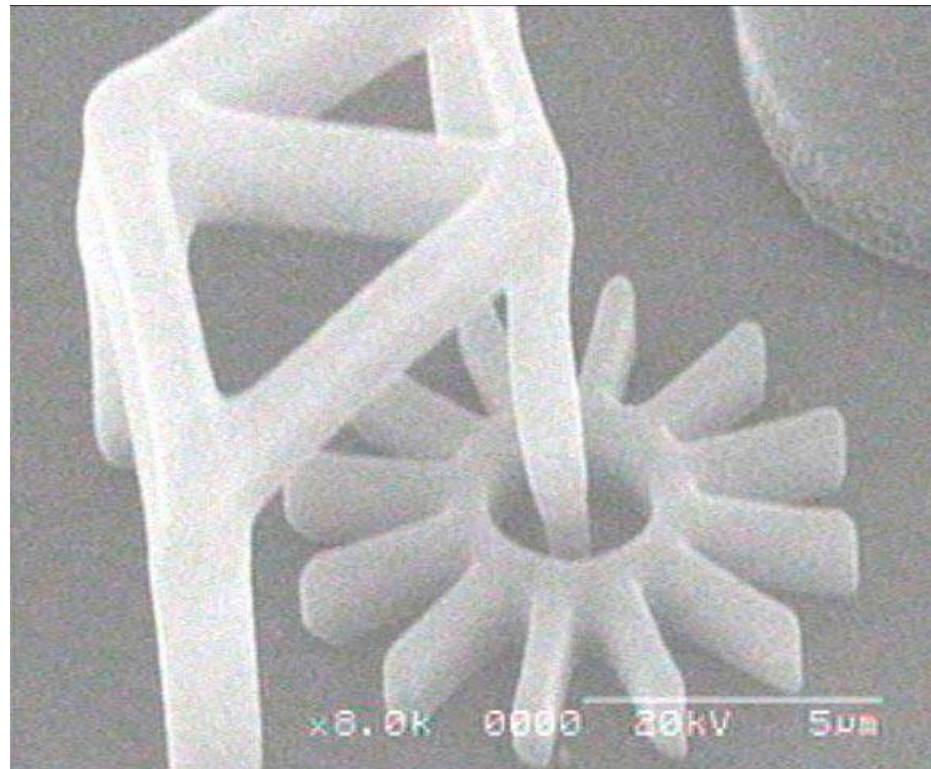


Kelemen et al. , Appl. Opt (2006)

Integrated optical motor



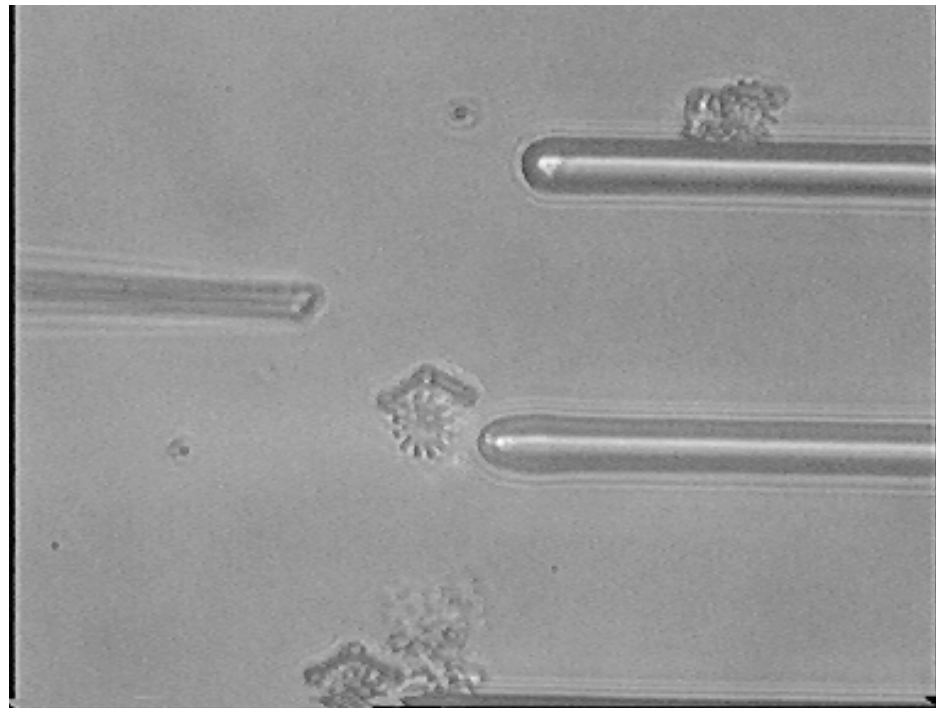
Integrated optical motor



Integrated optical motor



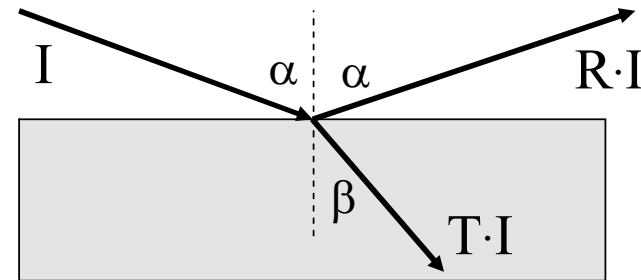
Integrated optical motor



Torque: 10^{-19} - 10^{-18} Nm @ 10 mW

Trap non spherical objects

Orientation of a flat particle in an optical trap



Fresnel-formulae:

1. The polarization and incidence planes are perpendicular:

$$R_{\perp} = \frac{\sin^2(\alpha - \beta)}{\sin^2(\alpha + \beta)}, \quad T_{\perp} = \frac{\sin 2\alpha \sin 2\beta}{\sin^2(\alpha + \beta)}$$

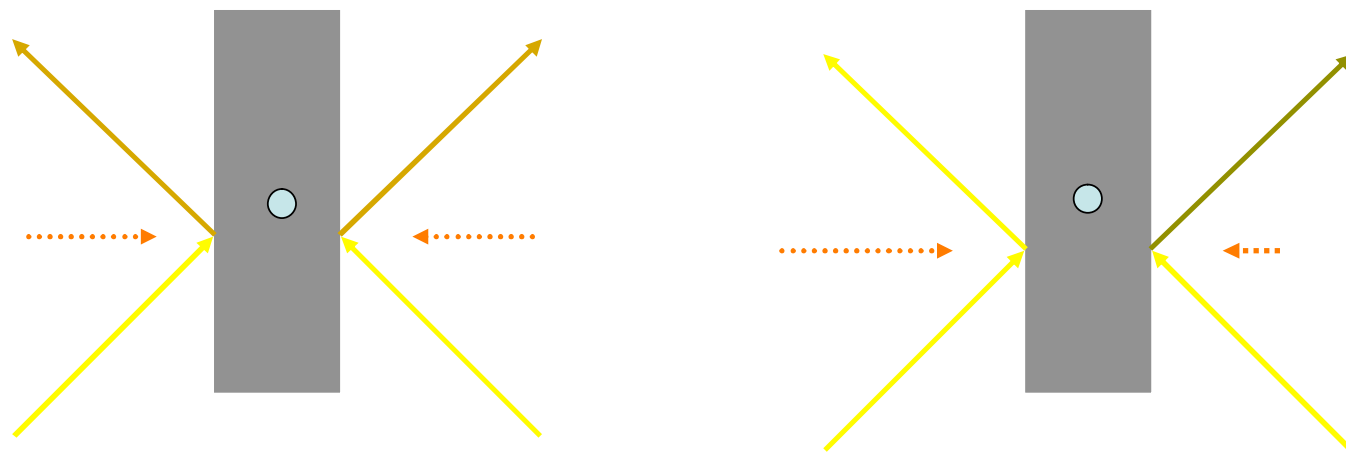
2. The polarization and incidence planes are parallel

$$R_{\parallel} = \frac{\operatorname{tg}^2(\alpha - \beta)}{\operatorname{tg}^2(\alpha + \beta)}, \quad T_{\parallel} = \frac{\sin 2\alpha \sin 2\beta}{\sin^2(\alpha + \beta) \cos^2(\alpha - \beta)}$$

3. General case (φ is the angle between polarization and incidence plane):

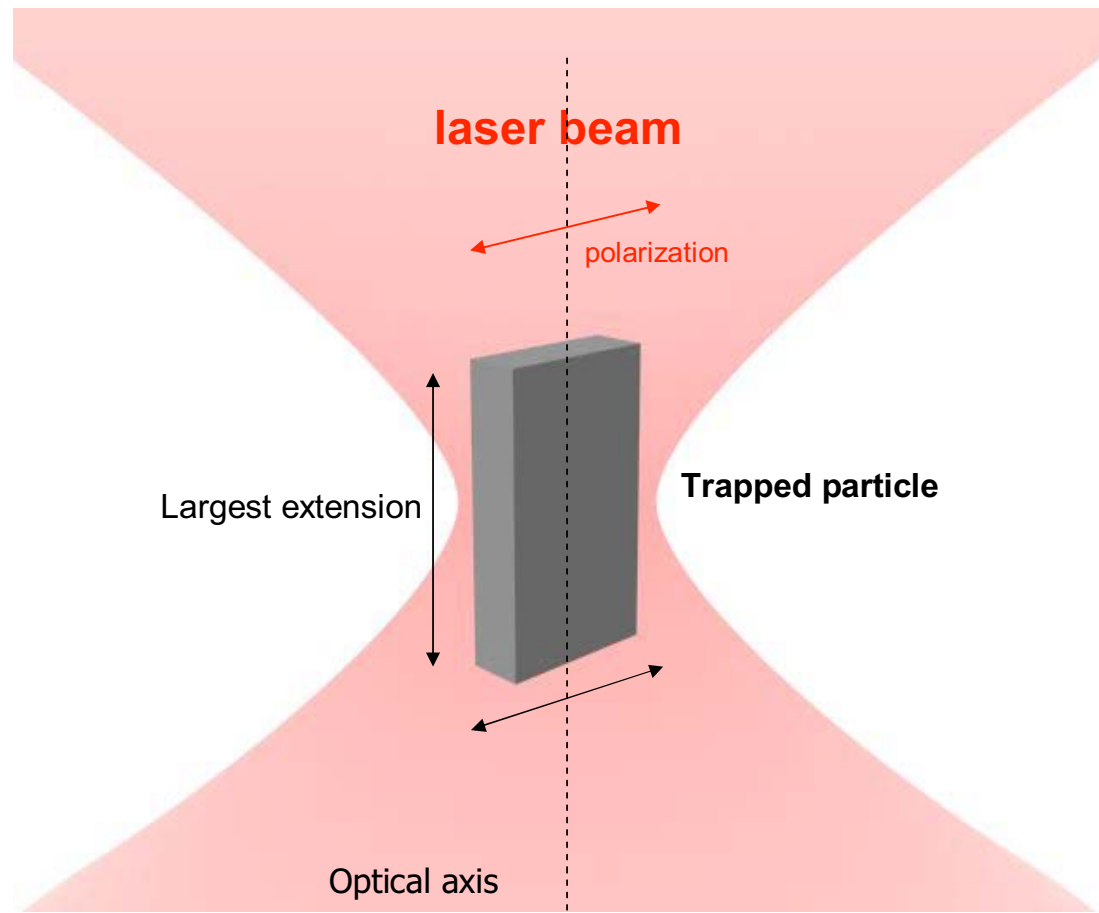
$$R = R_{\parallel} \cos^2 \varphi + R_{\perp} \sin^2 \varphi, \quad T = T_{\parallel} \cos^2 \varphi + T_{\perp} \sin^2 \varphi$$

Torque of linearly polarized light

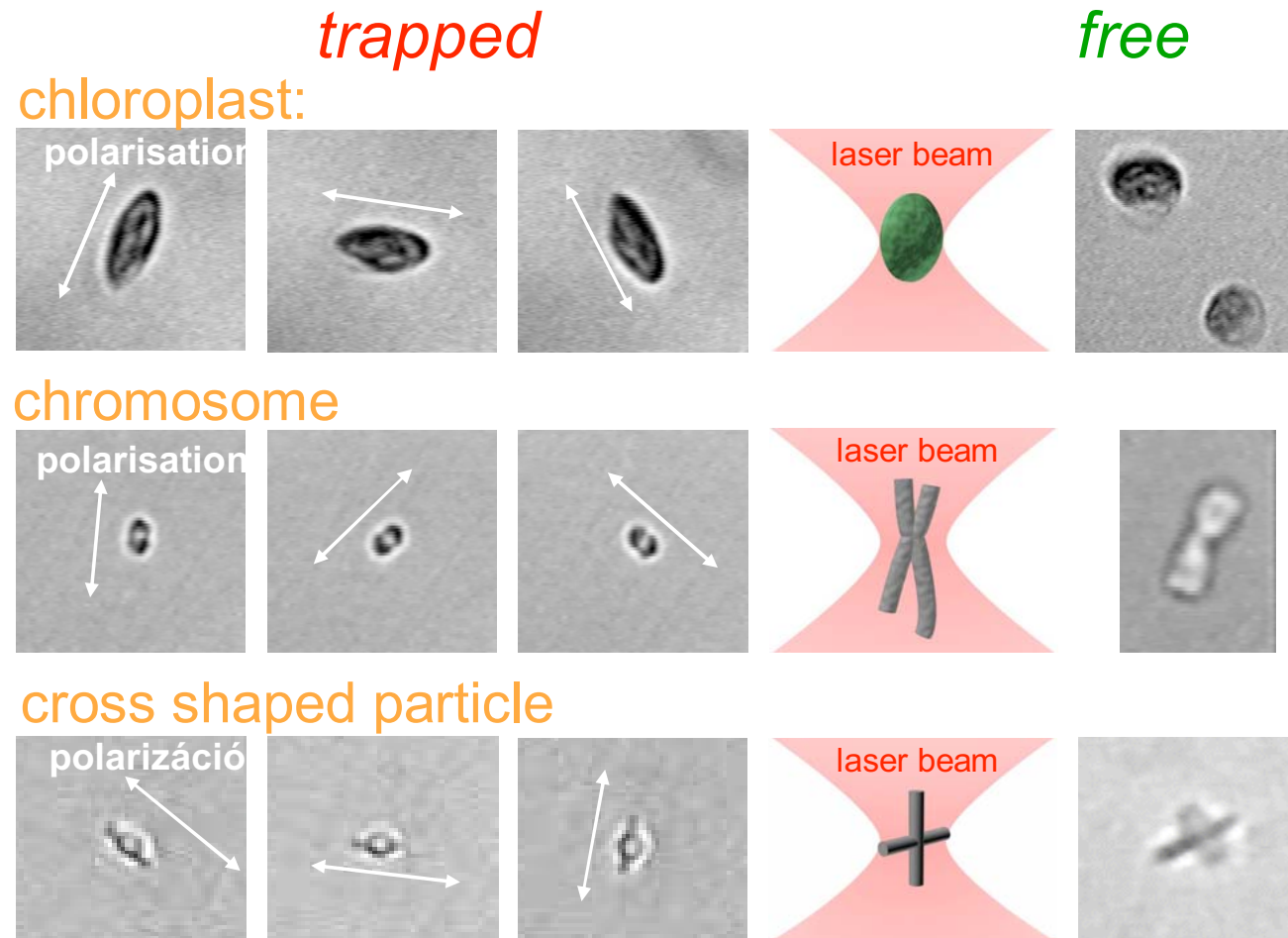


Polarization dependent light refraction (described by the Fresnel-formulae)

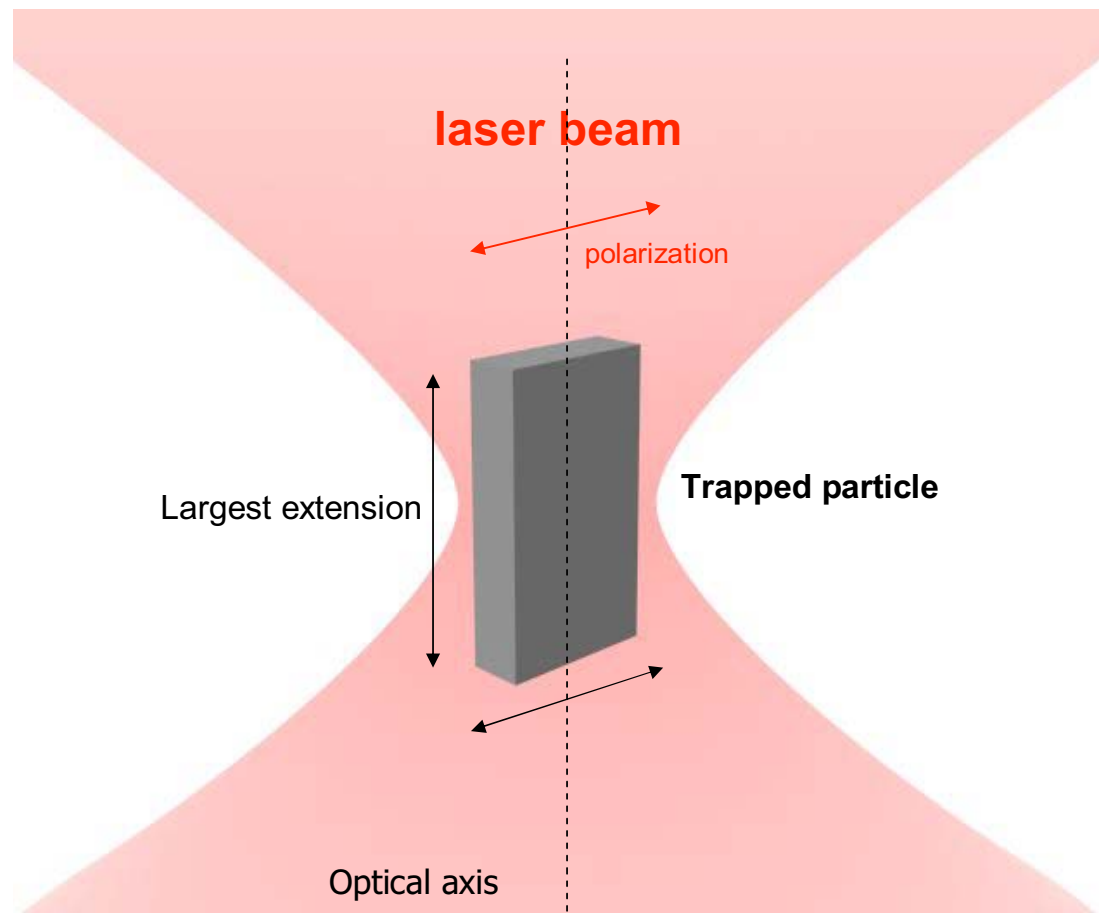
Orientation of a flat particle in trap formed by polarized light



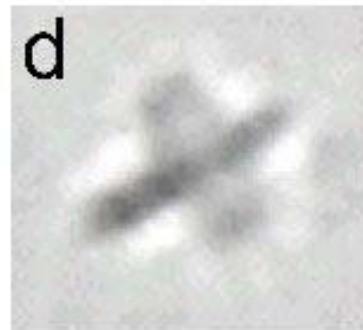
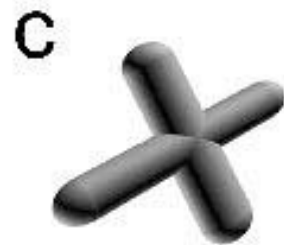
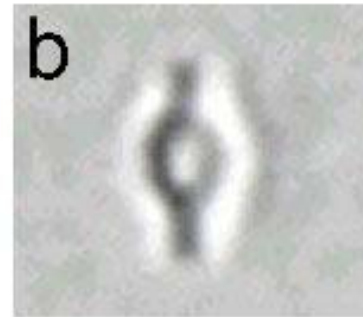
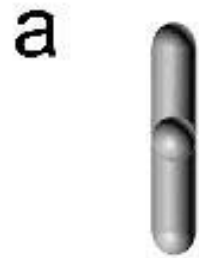
Orientation of different particles in laser tweezers



Orientation of a flat particle in trap formed by polarized light

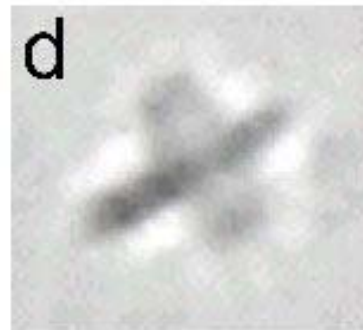
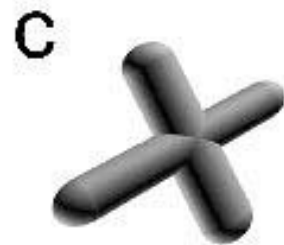
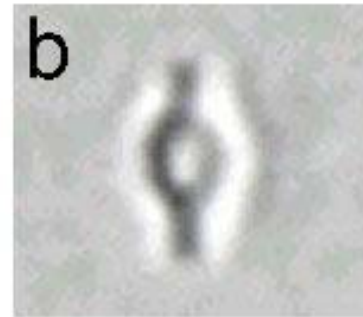
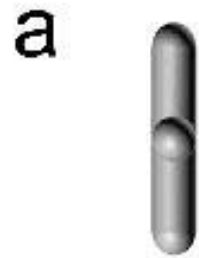


Rotor to characterize the system



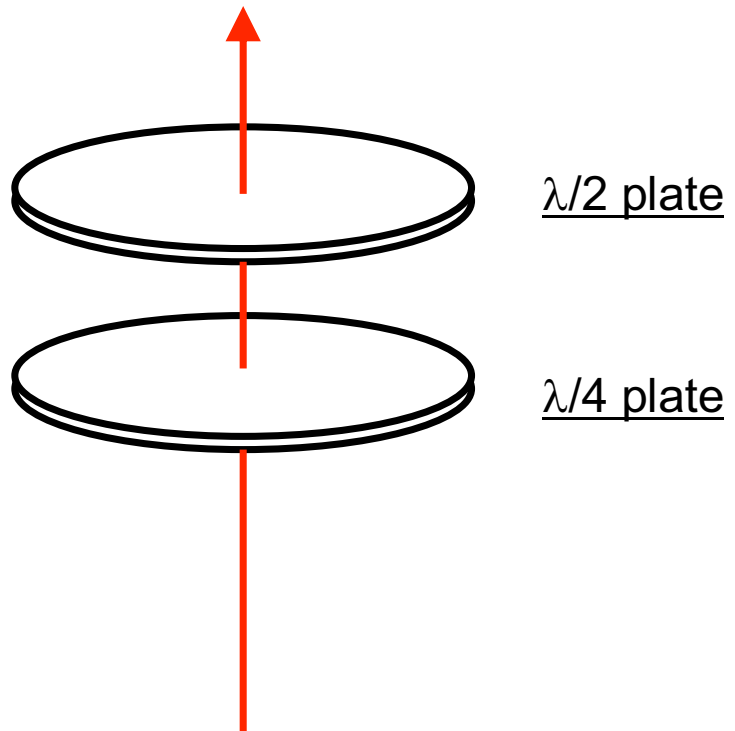
3 μm

Rotor to characterize the system

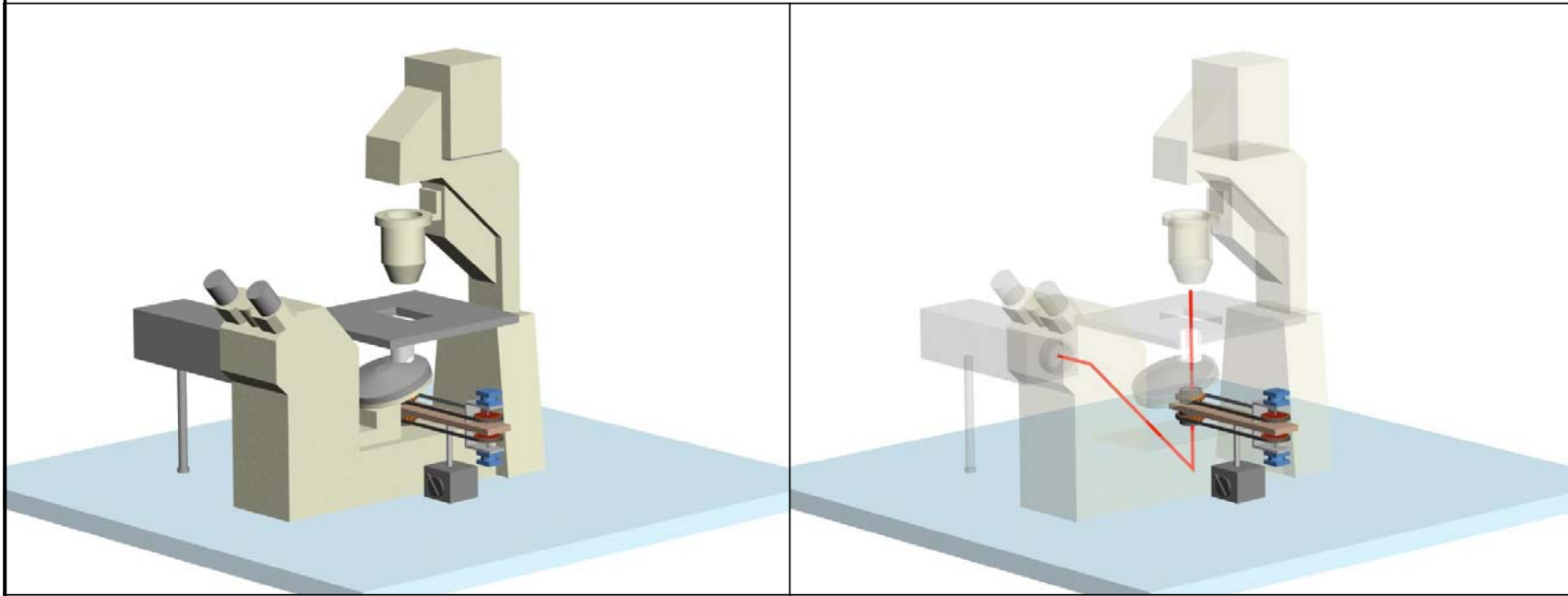


3 μm

Laser beam adjustment



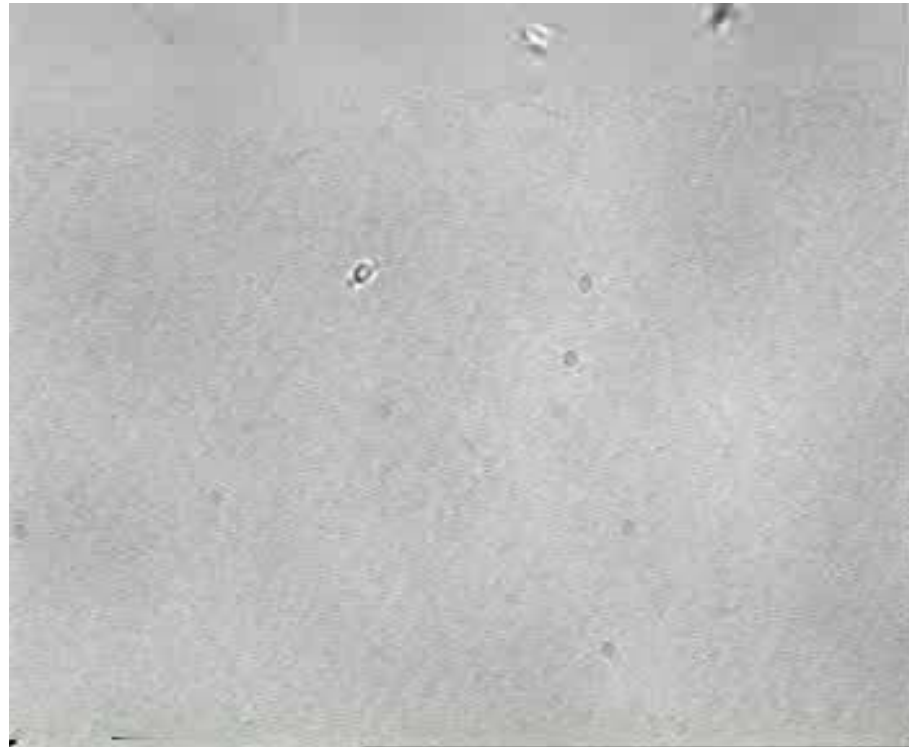
Experimental layout



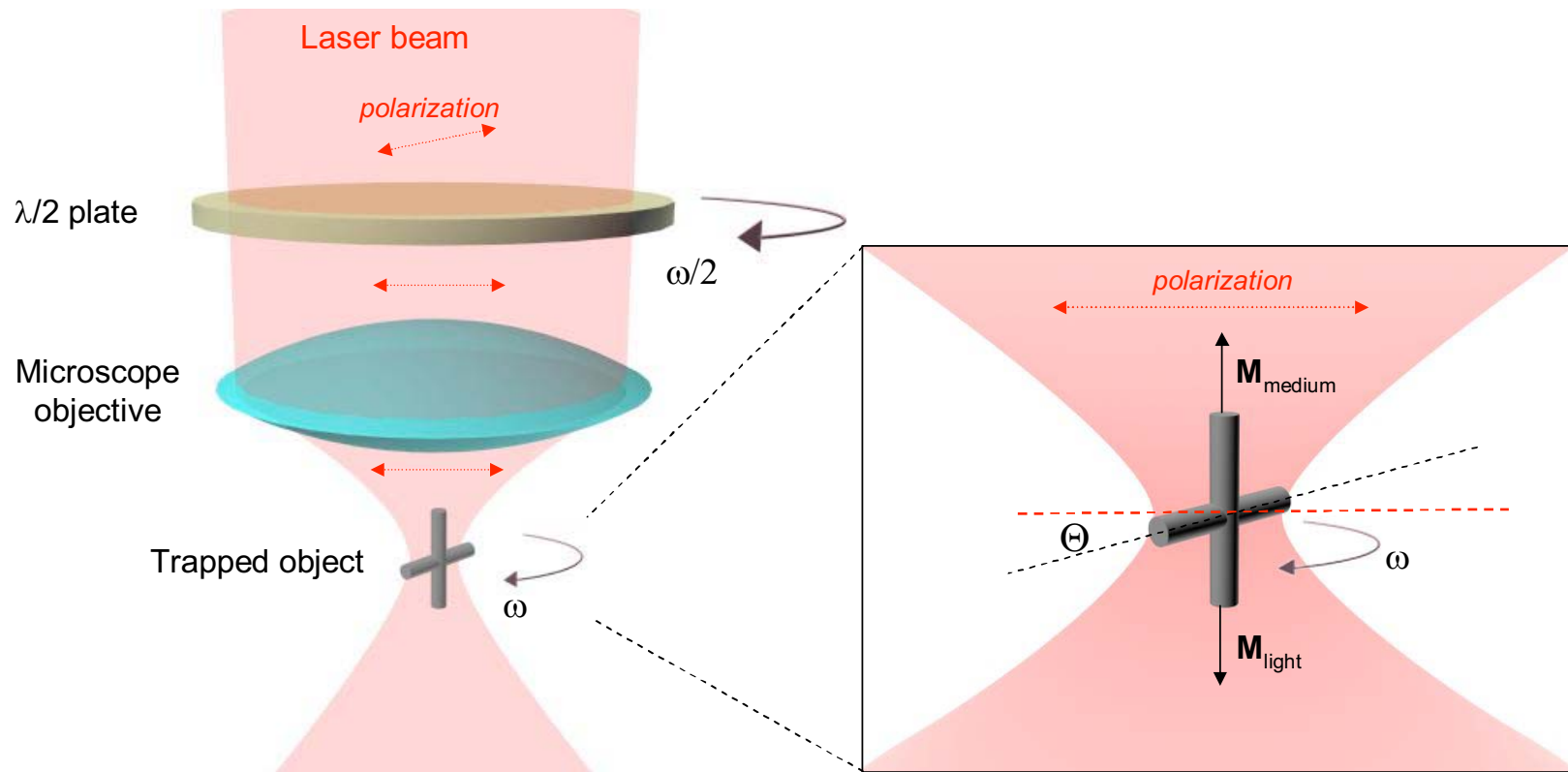
Main components:

- Zeiss Axiovert 135 (Zeiss Plan Apochromat oil immersion 100x/1.4 objective)
- Cell Robotics 980-1000, 995 nm laser
- $\lambda/2$ és $\lambda/4$ plates rotated with stepping motors
- camera, digitizer, computer

Rotation of trapped particle

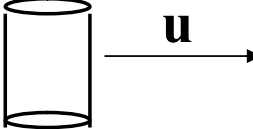


Measure the connection between torque and orientation



Viscous drag

In balance: $M_{drag} = M_{light}$

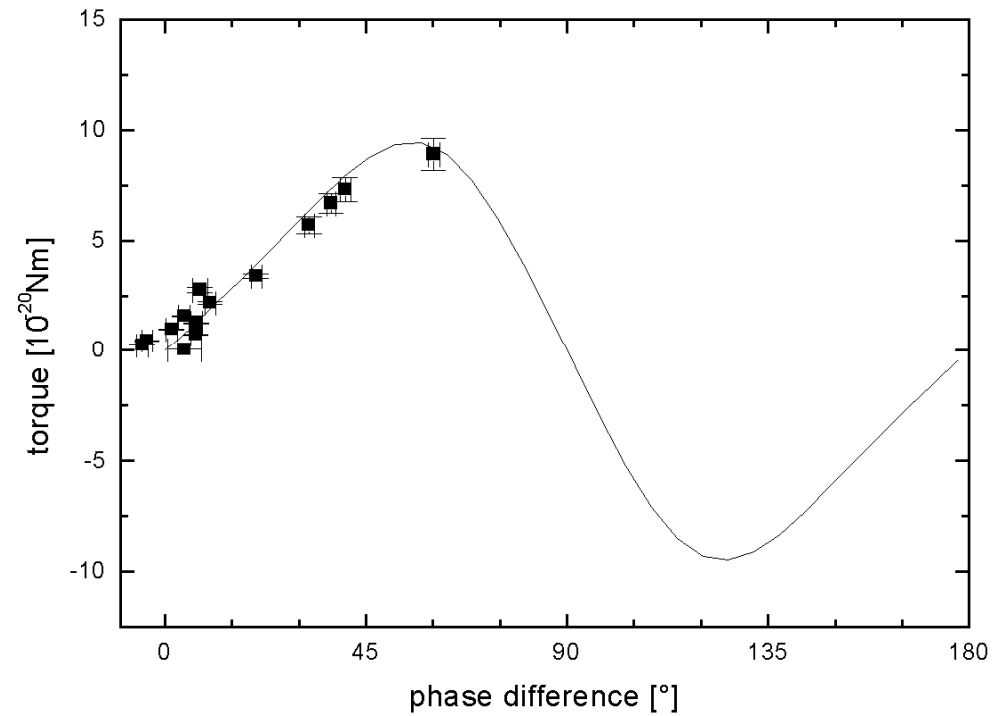
For a cylinder: 

$$F_{drag} = \frac{4\pi\eta l}{\frac{1}{2} - C - \ln \frac{Ru\rho}{4\eta}}$$

η : viscosity, \mathbf{u} : speed, \mathbf{R} : radius, \mathbf{l} : length, ρ : density, \mathbf{C} : Euler constant

Torque as a function of phase difference

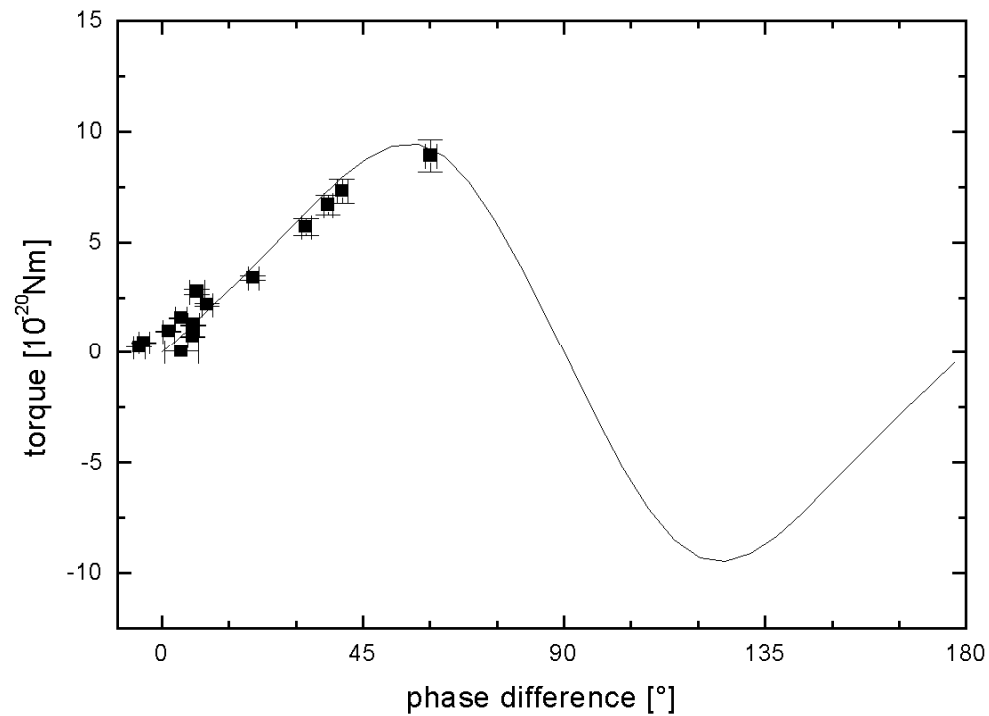
experiment vs. ray tracing simulation



Galajda and Ormos, Opt. Exp. (2003)

Torque as a function of phase difference

experiment vs. ray tracing simulation

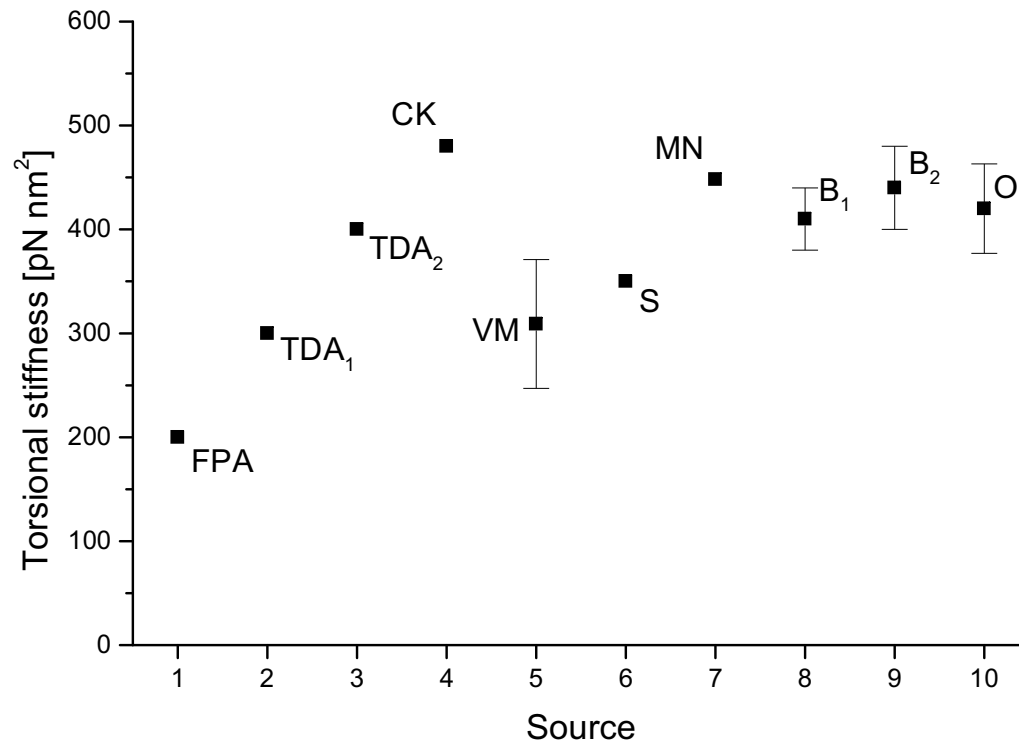


Galajda and Ormos, Opt. Exp. (2003)

Good properties of the method

- Torque can be applied and measured continuously
(statically or dynamically)
- Torque can be adjusted independently from grabbing force
- to a large extent

Torsional stiffness of DNA according to different sources



Marks:

FPA: typical values obtained from fluorescence anisotropy

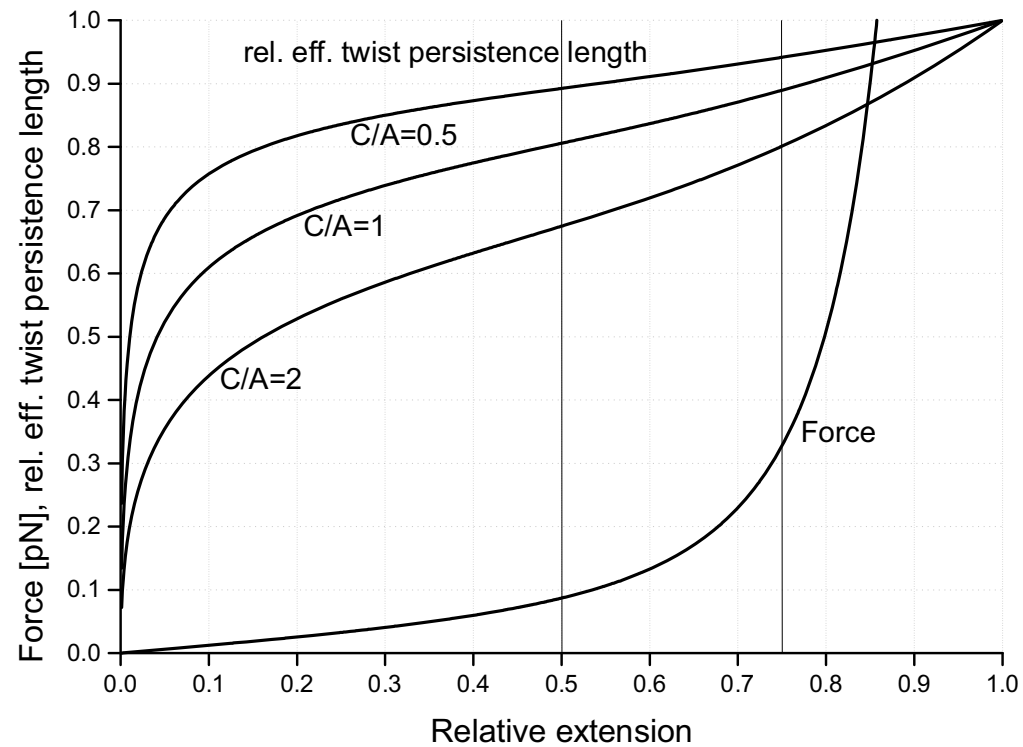
TDA₁, TDA₂: values calculated based on the distribution of topoisomers

CK: ciklizációs kinetikai vizsgálatokból nyert érték values obtained from cyclisation kinetic experiments

VM, S, MN: values based on single molecule elongation experiments used different models

B₁, B₂: values obtained by two independent types of experiments (Bustamante group)

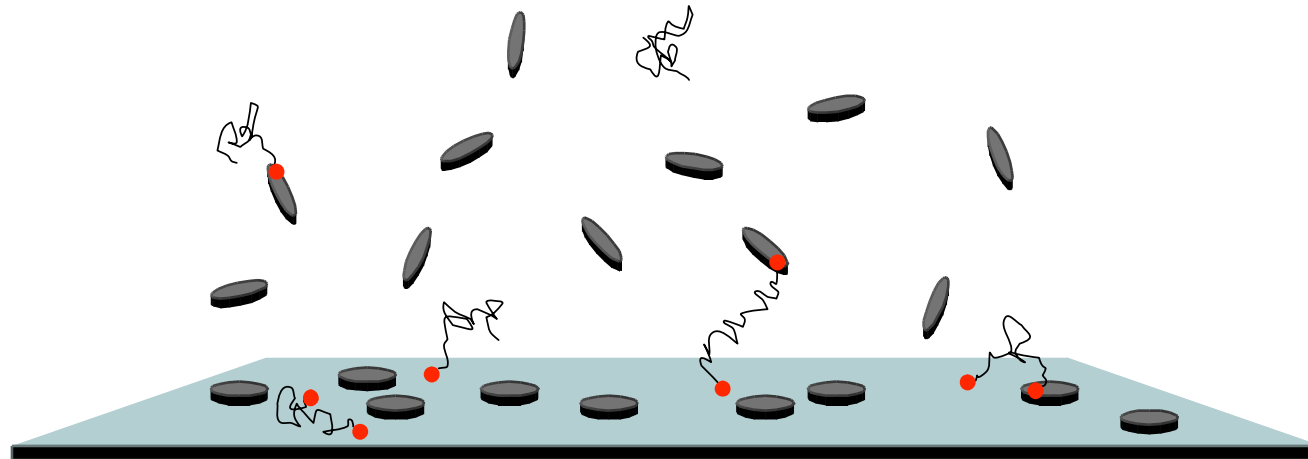
Elastic properties of polymers



Relative torsional persistence length as a function of relative elongation:

Moroz;Nelson model: the effective torsional stiffness (and the effective torsional persistence length C_{eff}) depend on the elongation. At maximal elongation C_{eff} equals C .

Twist single DNA molecules: the sample



DNS:

λ -DNS in linear form (15.6 μm contour length, Fermentas)

Discs:

1 μm diameter polystyrol beads (Polysciences Polybead Polyesterene Microspheres) compressed mechanically:

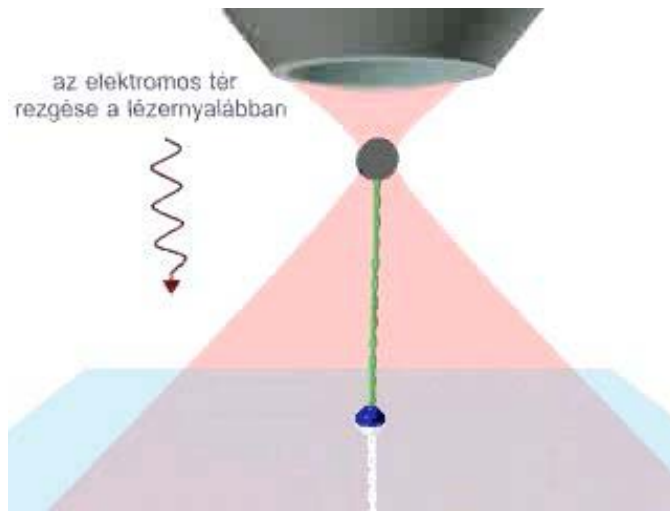
Suspension

MES 50 mM, pH 5.0: 2 μL λ -DNS suspension, 5 μL "disc suspension" and 100 μL MES.

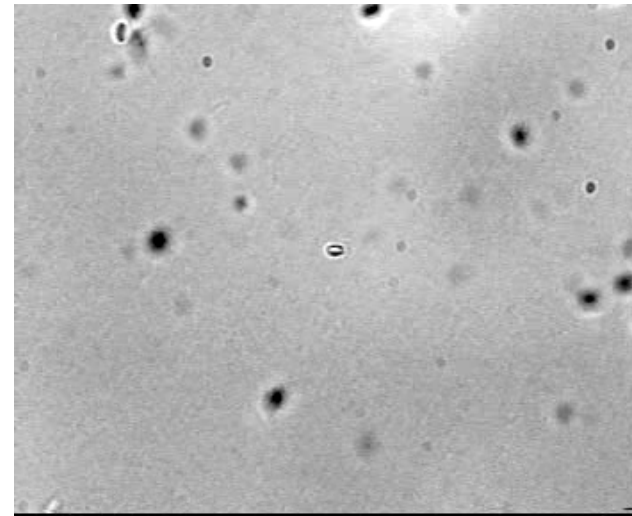
Surface:

Thin polystyrol layer on glass (spin coat: polisztiröl-toluol drop (50 mg/ml) on glass, 3000 rpm, 30 sec)

Twisting DNA with optical tweezers

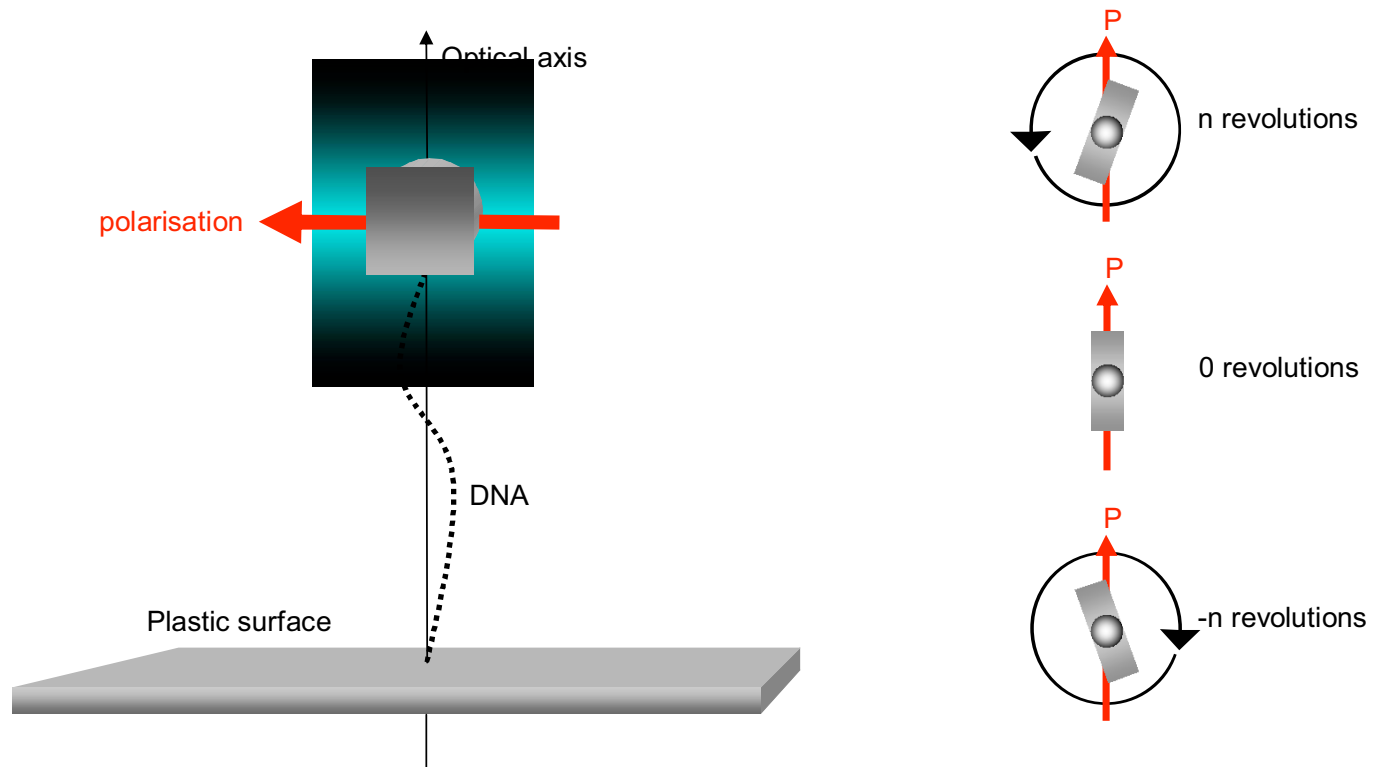


animation



experiment

Measuring the torque



Measuring torque

$$\tau = -k\alpha$$

$$E = \frac{1}{2}k\alpha^2$$

$$\rho(\alpha) \propto e^{-\frac{E}{k_B T}} = e^{-\frac{k\alpha^2}{2k_B T}}$$

calibration

$$k_M \alpha_M = k_L \alpha_L$$

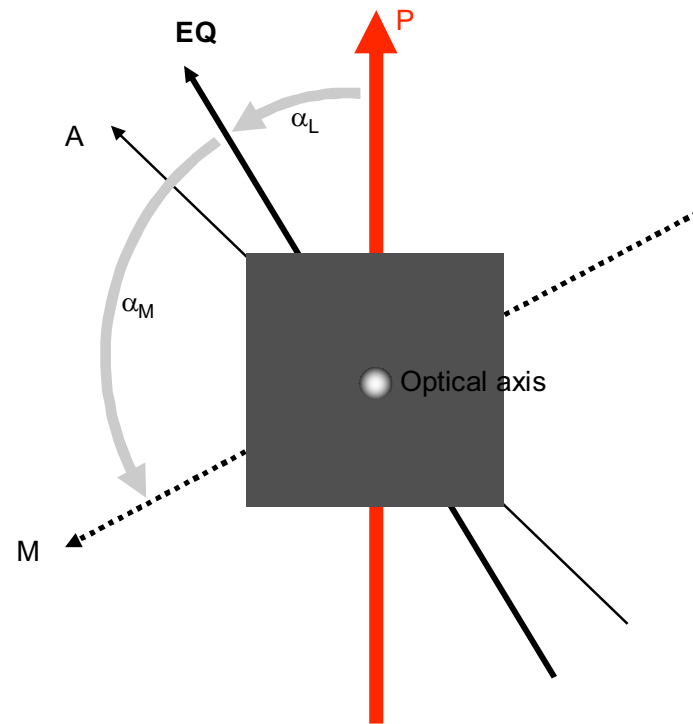
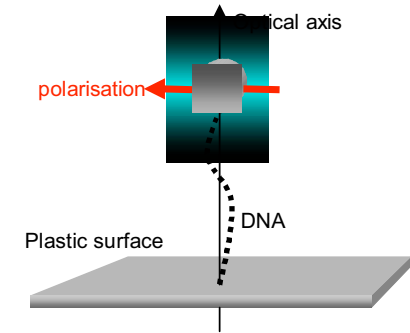
$$k_{eff} = k_M + k_L$$

$$k_M = k_{eff} \left(1 - \frac{\Delta_{EQ}}{\Delta_P}\right)$$

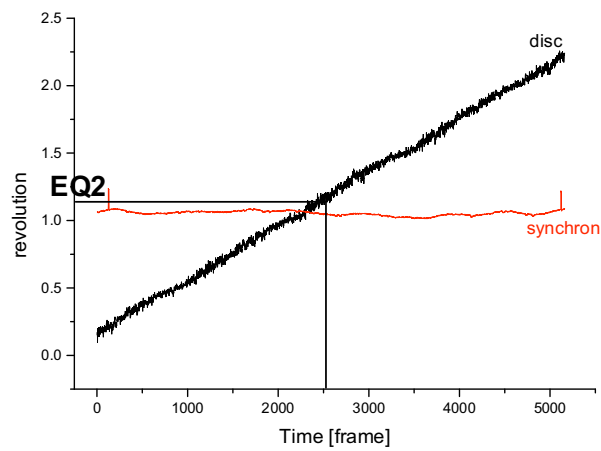
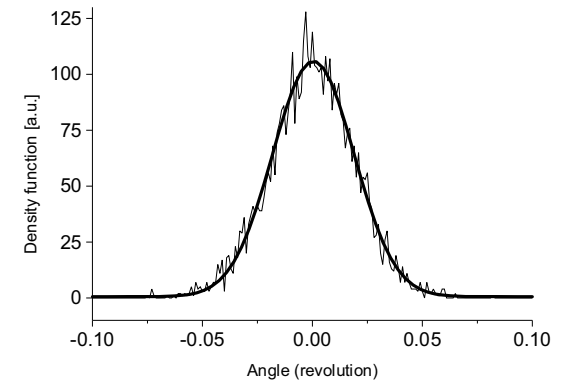
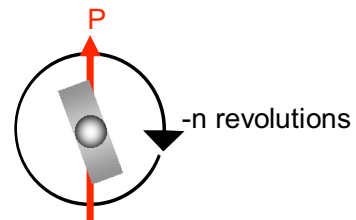
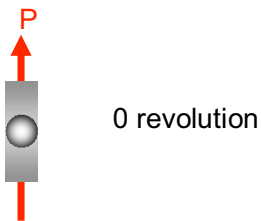
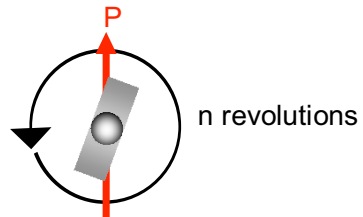
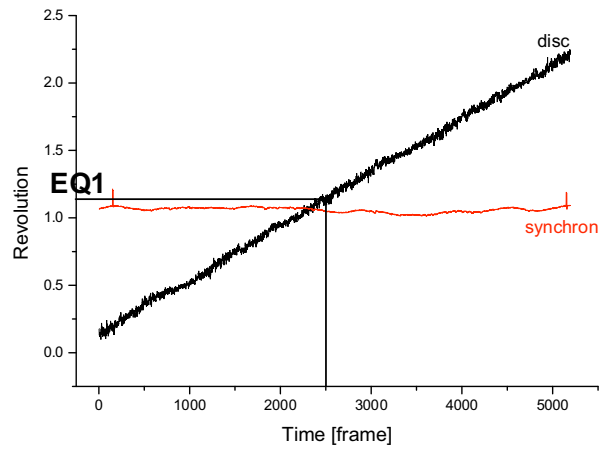
torque

$$G = k_M l$$

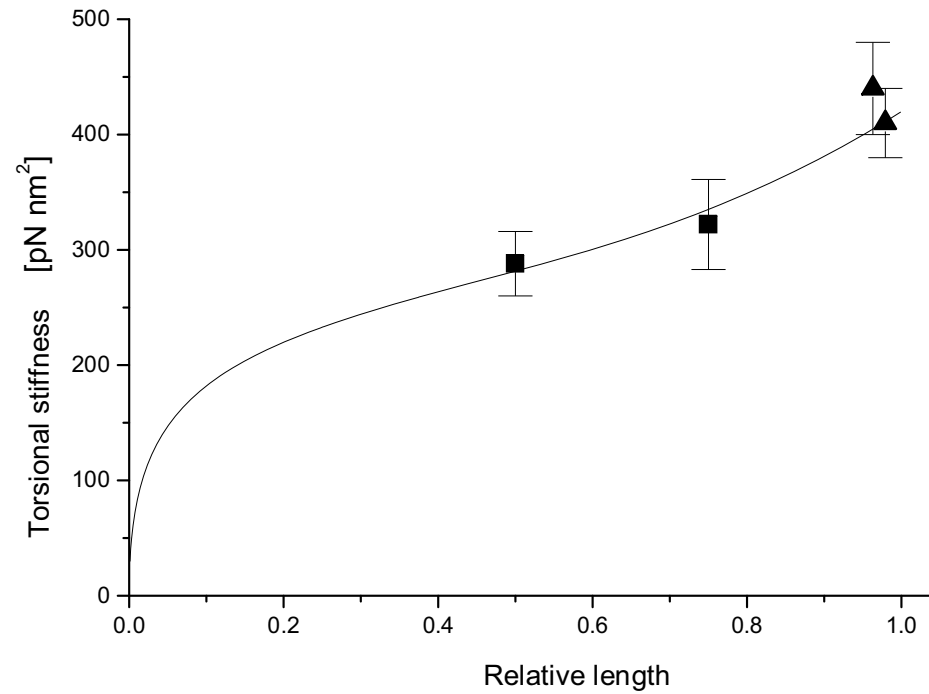
torsional modulud



The measurement – typical experimental data



Results



Effective torsional stiffness of dsDNA measured at 0.5 and 0.75 relative elongations and the local torsional stiffness of 420 ± 43 pN nm² calculated with the Moroz-Nelson model.

Oroszi, et al. Phys.Rev.Lett(2006).

Participants

András Dér

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