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International Centre for Theoretical Physics**



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**Conference: From DNA-Inspired Physics to Physics-Inspired Biology**

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**Electrostatic Interactions between DNA Double Helices**

S. LEIKIN  
*NICHD/NIH*  
*Bethesda, MD 20892*  
*USA*

# Electrostatic interactions between DNA double helices

S. Leikin, *NICHD/NIH, Bethesda, MD, USA*

**In collaboration with:**

A.A. Kornyshev, D.J. Lee & A. Wynveen, *Imperial College, London, UK*

A.G. Chersvy & S.V. Malinin, *Forschungszentrum Jülich, Germany*

S.B. Zimmerman, *NIDDK/NIH, USA*

Kornyshev, Lee, Leikin, and Wynveen (2007). *Rev Mod Phys* **79**, 943-996

# Electrostatic interactions between DNA double helices

Predatory adaptation and evolution

Animals - speed

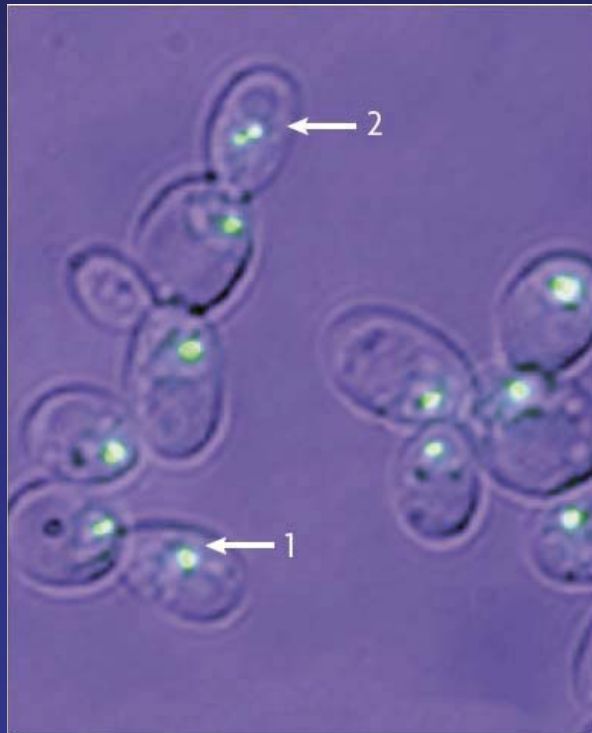


Humans - endurance



# Electrostatic interactions between DNA double helices

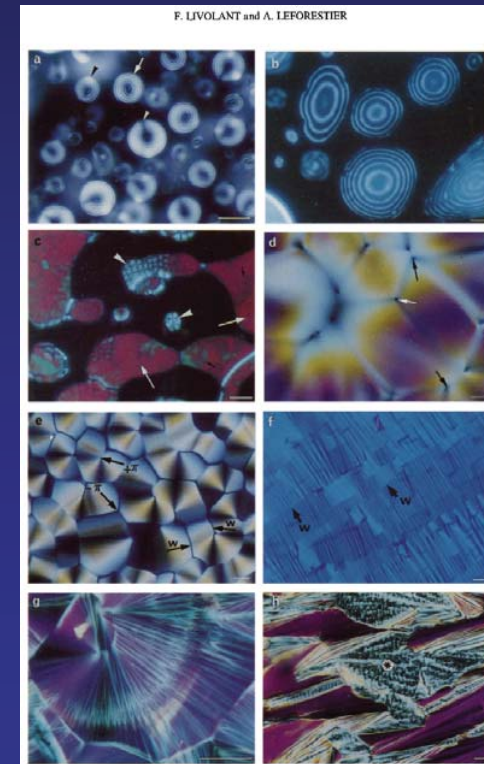
Homologous pairing



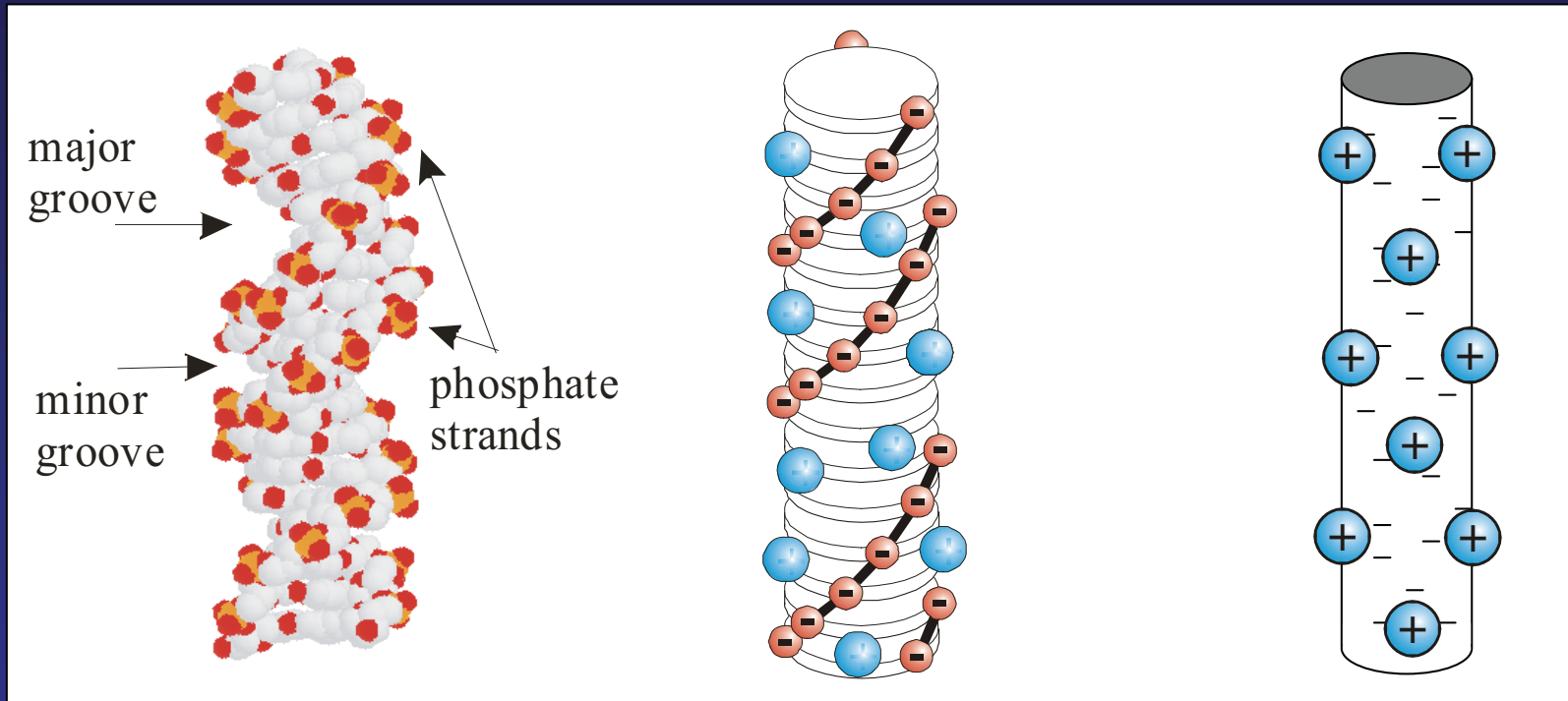
DNA packing



Poly- and meso-morphism



# Surface charge pattern



DNA

charged helix

charged cylinder  
with counterions



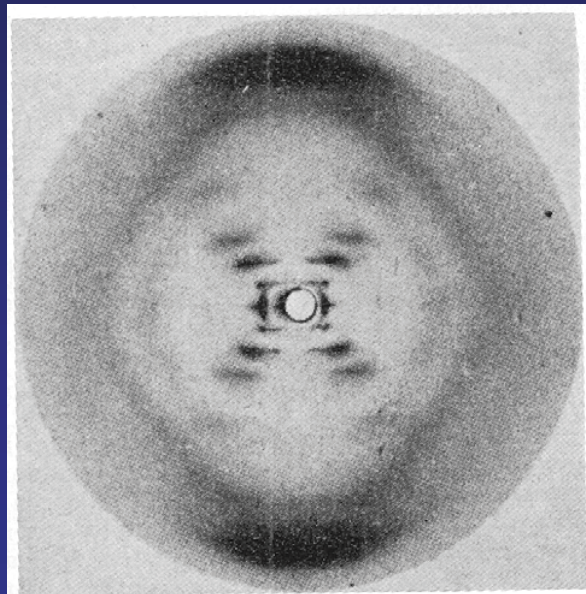
# DNA structure

# and interactions

$$I(\mathbf{k}) = \sum_{\nu, \mu} \sum_{i, j} f_i f_j \langle F_i^{\nu}(\mathbf{k}) F_j^{\mu}(-\mathbf{k}) \rangle$$

$$F_i^{\nu}(\mathbf{k}) = \frac{1}{(2\pi)^{3/2}} \int n_i^{\nu}(\mathbf{r}) \exp(i\mathbf{k}\mathbf{r}) d^3\mathbf{r}$$

$$\mathcal{E} \approx \frac{2\pi e^2}{\epsilon} \sum_{\nu, \mu=1}^2 \sum_{i, j} q_i q_j \int \frac{F_i^{T, \nu}(\mathbf{k}) F_j^{\mu}(-\mathbf{k})}{k^2 + \kappa_D^2} d^3\mathbf{k}$$



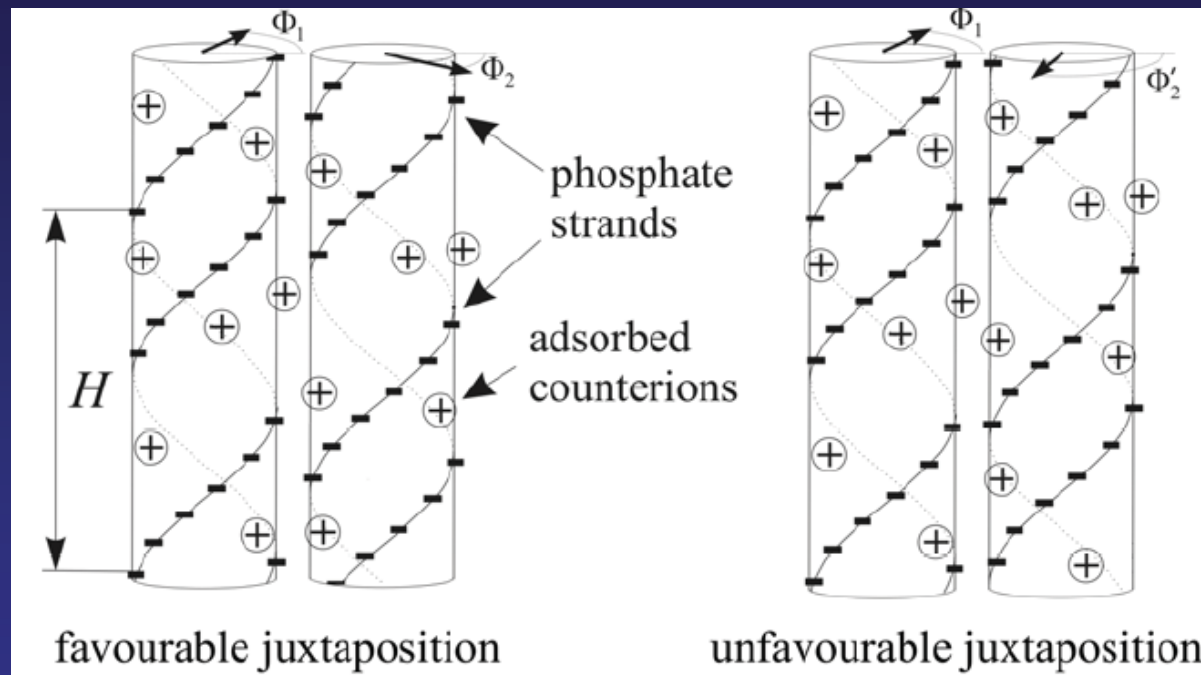
Sodium deoxyribonucleate from calf thymus. Structure B

Franklin & Gosling,  
*Nature* 171 (1953) 740

- **ideal, parallel helices** (1997)
- **ideal, crossed helices** (2000)
- **straight, non-ideal helices** (2004)
- **fluctuating helices** (ongoing)  
(static and dynamic torsional, stretching and bending fluctuations)
- **counterion correlations** (ongoing)  
(ideal helices, point counterions, no hydrogen bonding, simple limiting cases)

# Helix-helix alignment

**Prediction:** Electrostatic interactions cause alignment of DNA backbones in hydrated aggregates

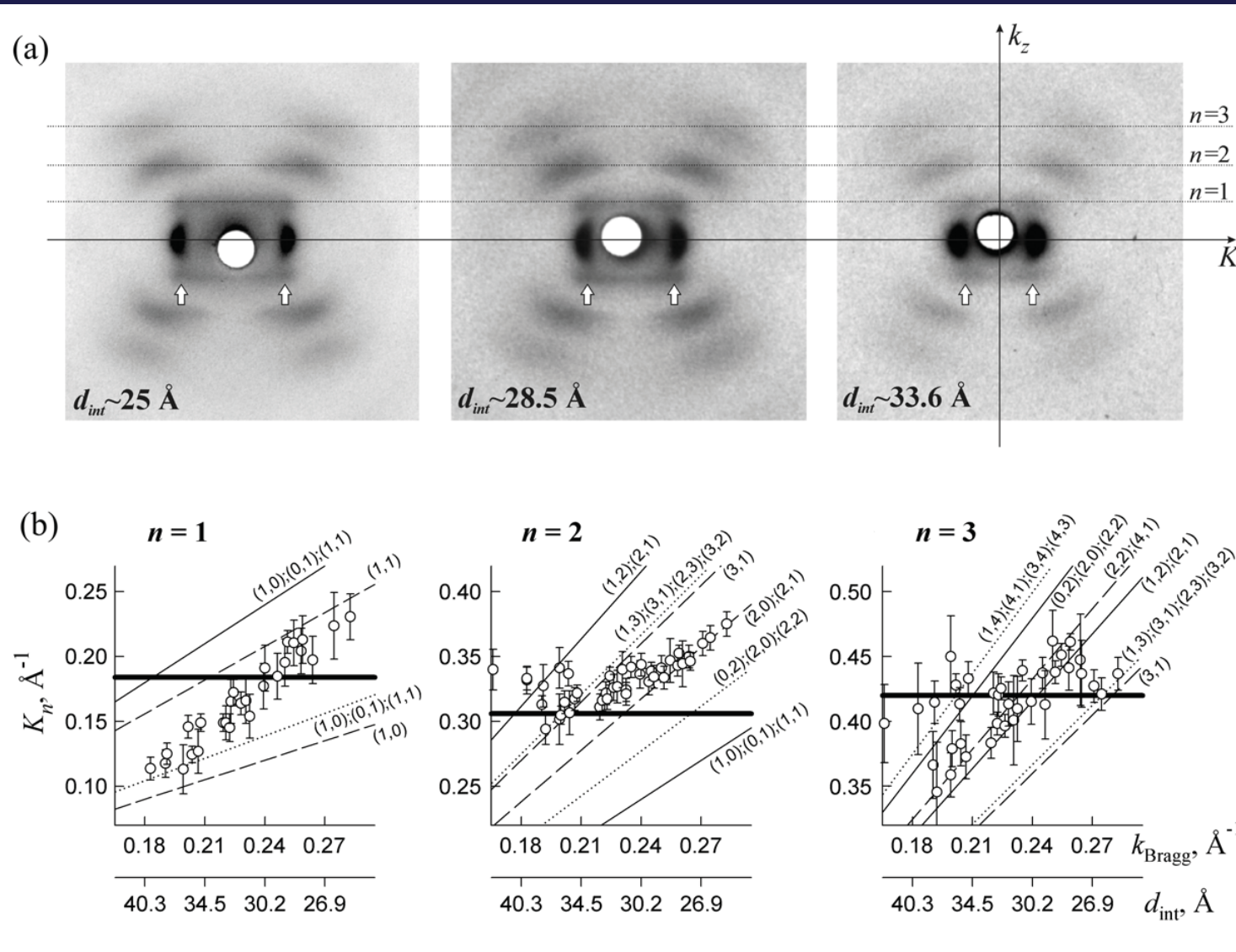


Kornyshev & Leikin, J. Chem. Phys. (1997)

“It therefore seems reasonable to suppose that in structure B the structural units [...] are relatively free from the influence of neighboring molecules, each unit being shielded by a sheath of water.”

Franklin & Gosling, Nature (1953)

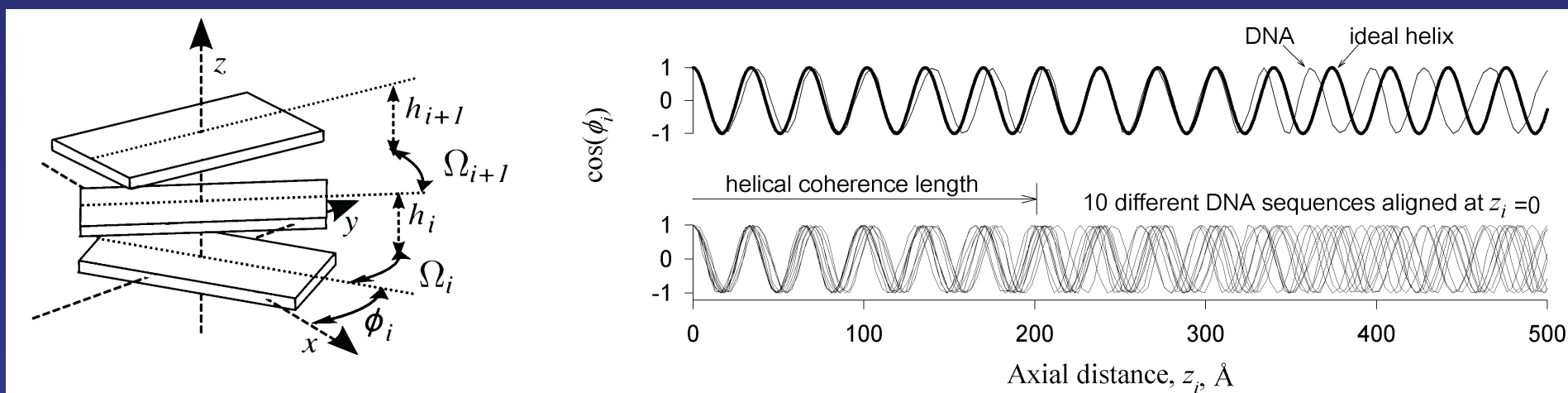
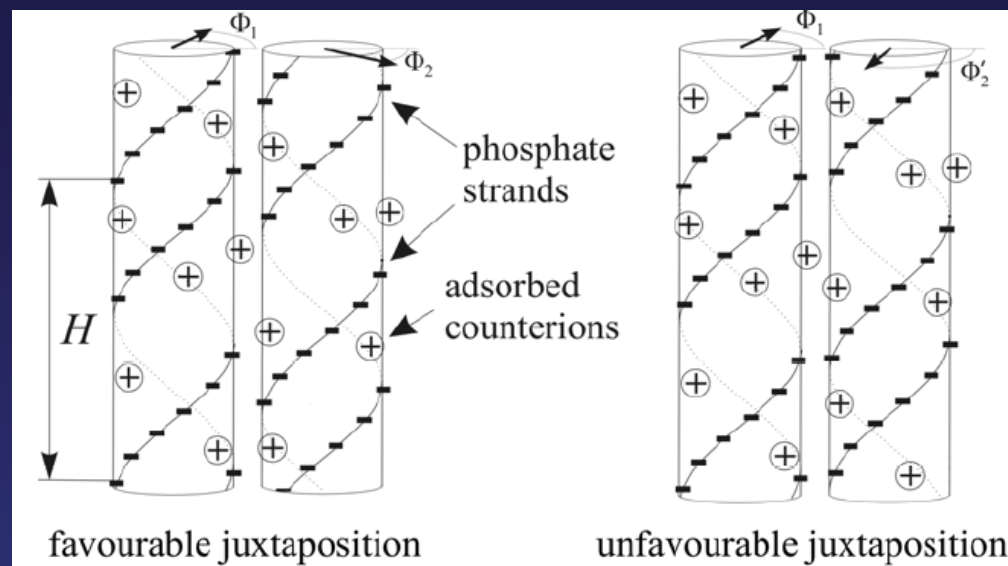
# Franklin & Gosling were wrong.



Kornyshev, Lee, Leikin, Wynveen & Zimmerman, Phys. Rev. Lett. (2005)



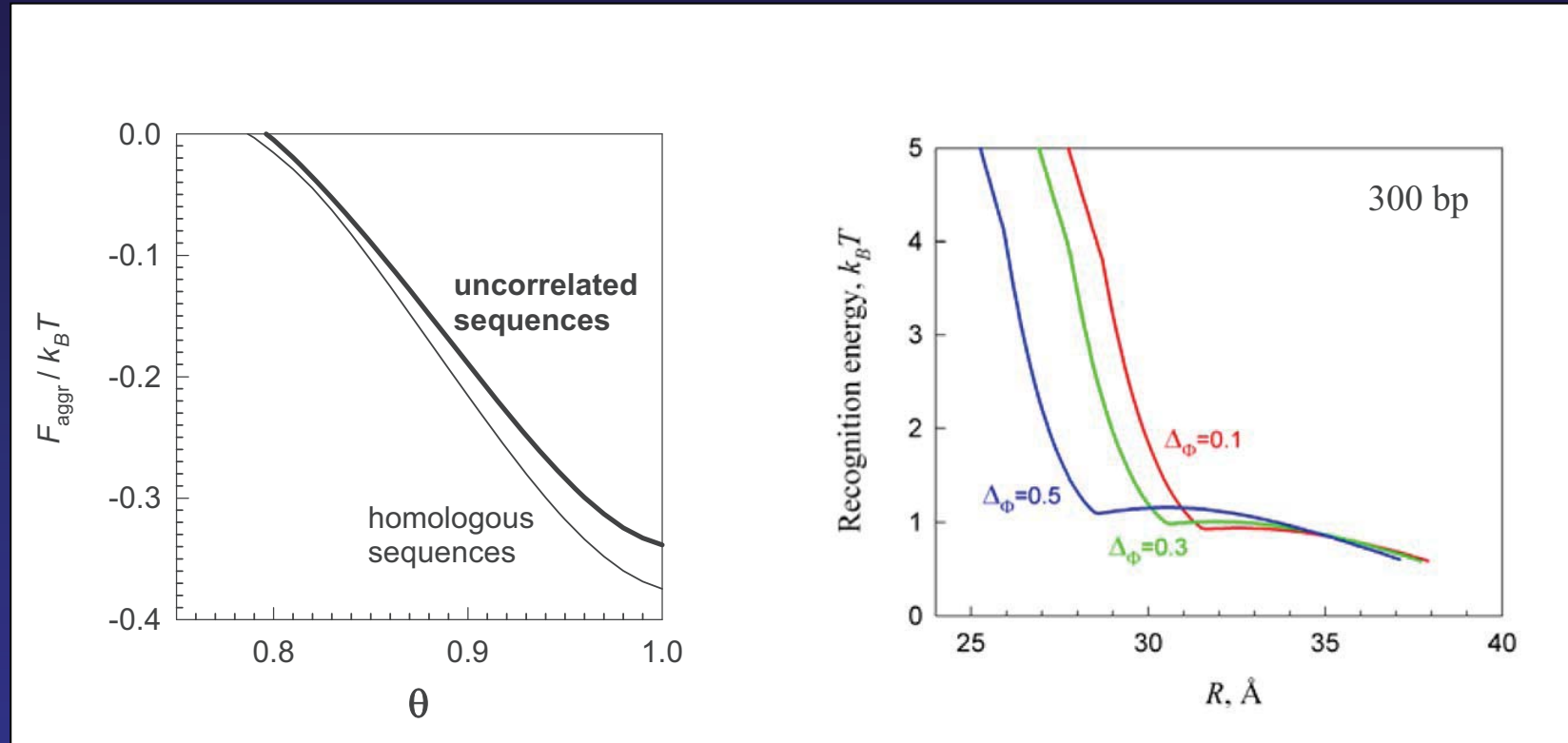
# But, how do non-ideal, fluctuating helices align?



Cherstvy, Kornyshev, and Leikin, J. Phys. Chem., 2004  
 Wynveen, Lee, Kornyshev, and Leikin, Nucl. Acids Res., 2008

# Homologous pairing of dsDNA

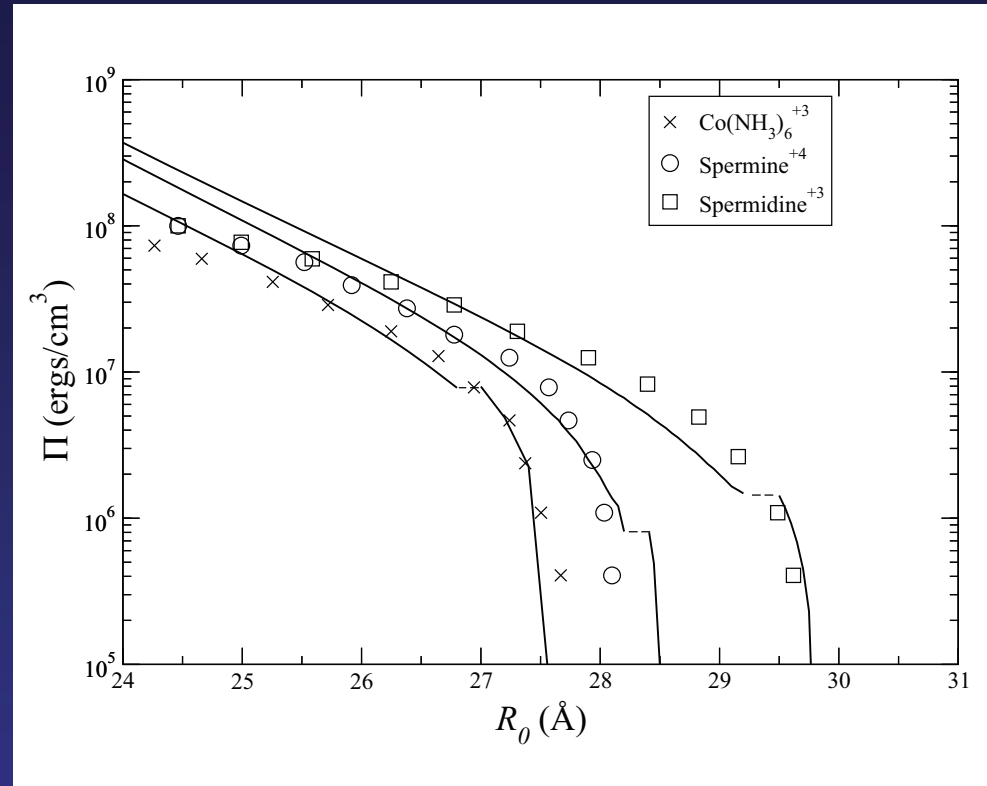
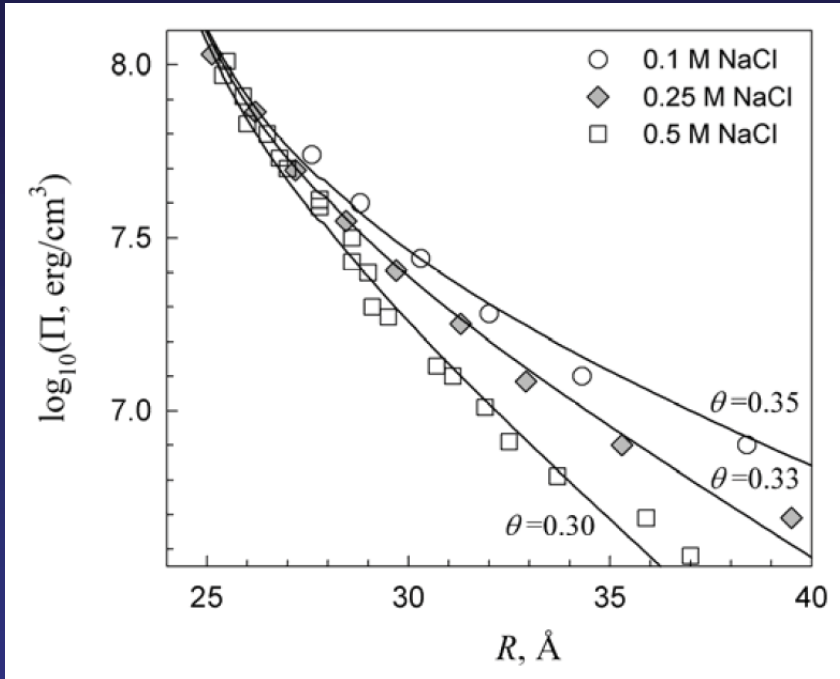
Double stranded DNA (dsDNA) have an innate homology recognition ability



Theory: Kornyshev & Leikin, Phys. Rev. Lett., 2001  
Cherstvy, Kornyshev & Leikin, J. Phys. Chem., 2004

Experiment: Inoue, Sugiyama, Travers, Ohyama, Biochemistry, 2007  
Baldwin et. al, J. Phys. Chem., 2008  
Prentiss et al. (this meeting)

# Rationalization of measured forces



Undulations of DNA dramatically enhance and extend the range of structure-dependent forces.

$$E_{\text{undulations}}/E_0 \sim \exp(d^2/\lambda^2)$$

Force measurements: Parsegian, Rau, et al., 1984-2008

Theory: Kornyshev, Lee, Leikin & Wynveen, 2007-2009

# Chiral interactions, cholesteric phase, poly- and meso-morphism

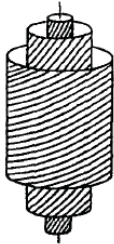
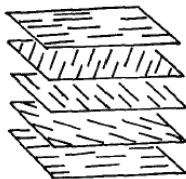
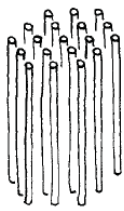
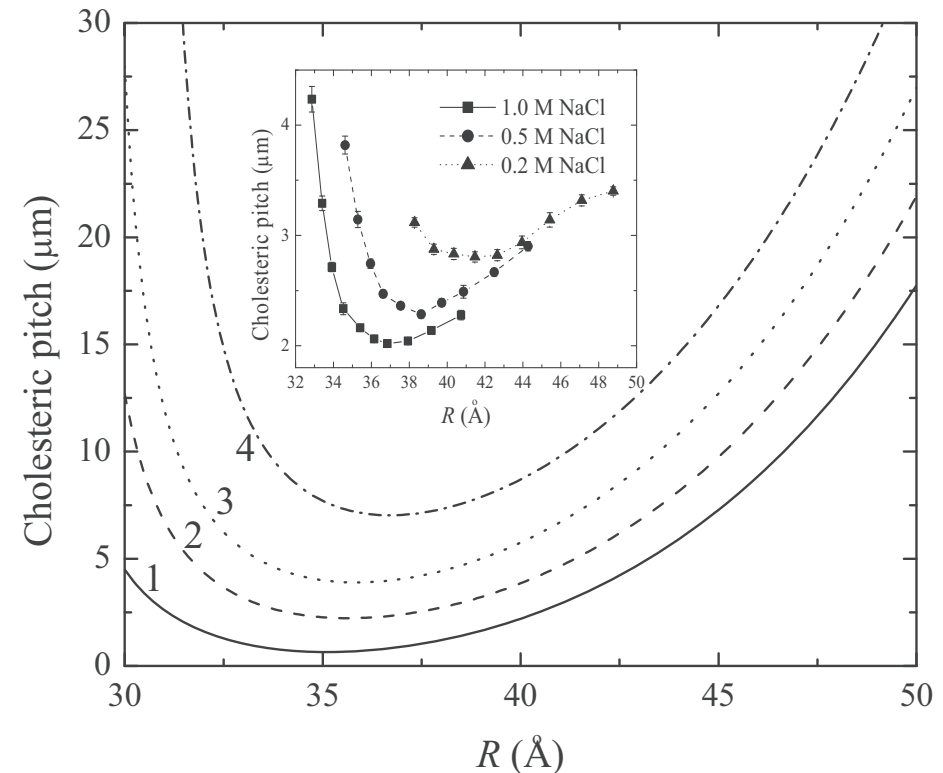
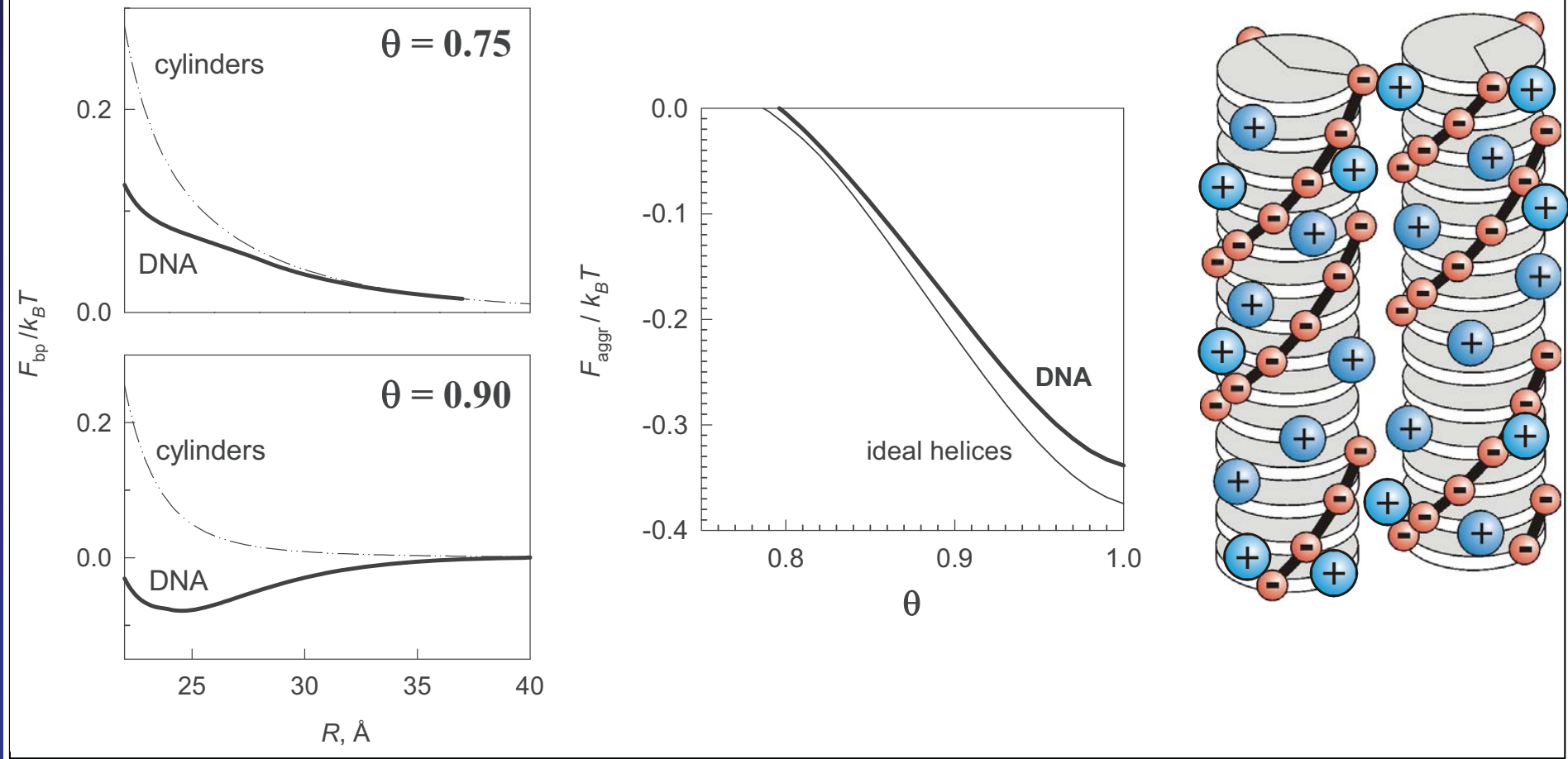
----- DNA concentration ----->		
blue phases (precholesteric stages)	cholesteric phase	2D columnar hexagonal phase
$d > 49 \text{ \AA}$	$49 \text{ \AA} > d > 32 \text{ \AA}$	$31.5 \text{ \AA} > d > 29 \text{ \AA}$
$C < 160 \text{ mg/ml}$	$160 \text{ mg/ml} < C < 380 \text{ mg/ml}$	$380 \text{ mg/ml} < C < 447 \text{ mg/ml}$
$\alpha \approx 2^\circ$	$0.7^\circ > \alpha > 0.46^\circ$	$\alpha = 0$
		
double twist	simple twist	no twist (except along screw dislocations)

Fig. 25. Geometrical configurations as a function of DNA concentration in the different liquid crystalline phases. The concentration  $C$  was calculated from the interhelix distances  $d$  measured by X-ray diffraction experiments (Durand *et al.* 1992<sup>32</sup>). The twist angle  $\alpha$  was deduced from the cholesteric pitch  $P$  ( $0.8 \mu\text{m}$  in blue phases and  $2.5 \mu\text{m}$  in the cholesteric) and the interhelix distance  $d$ .



Theory: Kornyshev, Leikin & Malinin, Eur. Phys. J. E, 2002  
 Experiment: Stanley, Hong & Strey, Biophys. J., 2005

# Counter-Ion Specific Aggregation



Kornyshev & Leikin, Phys. Rev. Lett., 1999

Cherstvy, Kornyshev & Leikin, J. Phys. Chem., 2004



## **Main conclusions**

**Helical structure of sugar-phosphate backbone strongly affects interactions between DNA. Conversely, interactions affect the structure of DNA in assemblies.**

**Static and dynamic undulations strongly enhance and extend the range of the structure-dependent forces  
Torsional and stretching fluctuations affect these forces relatively weakly.**

**dsDNA have an innate ability to recognize sequence homology through electrostatic interactions due to sequence dependence of the DNA backbone structure**

**Does direct sequence homology recognition between *dsDNA* occur *in vivo* and what is its role in homologous recombination?**