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Neutrinos and Supernovae

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Neutrinos and Supernovae

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SUPA– University of Strathclyde.



Neutrinos are the most enigmatic particles in the Universe

Associated with some of the long standing problems in astrophysics

Solar neutrino deficit

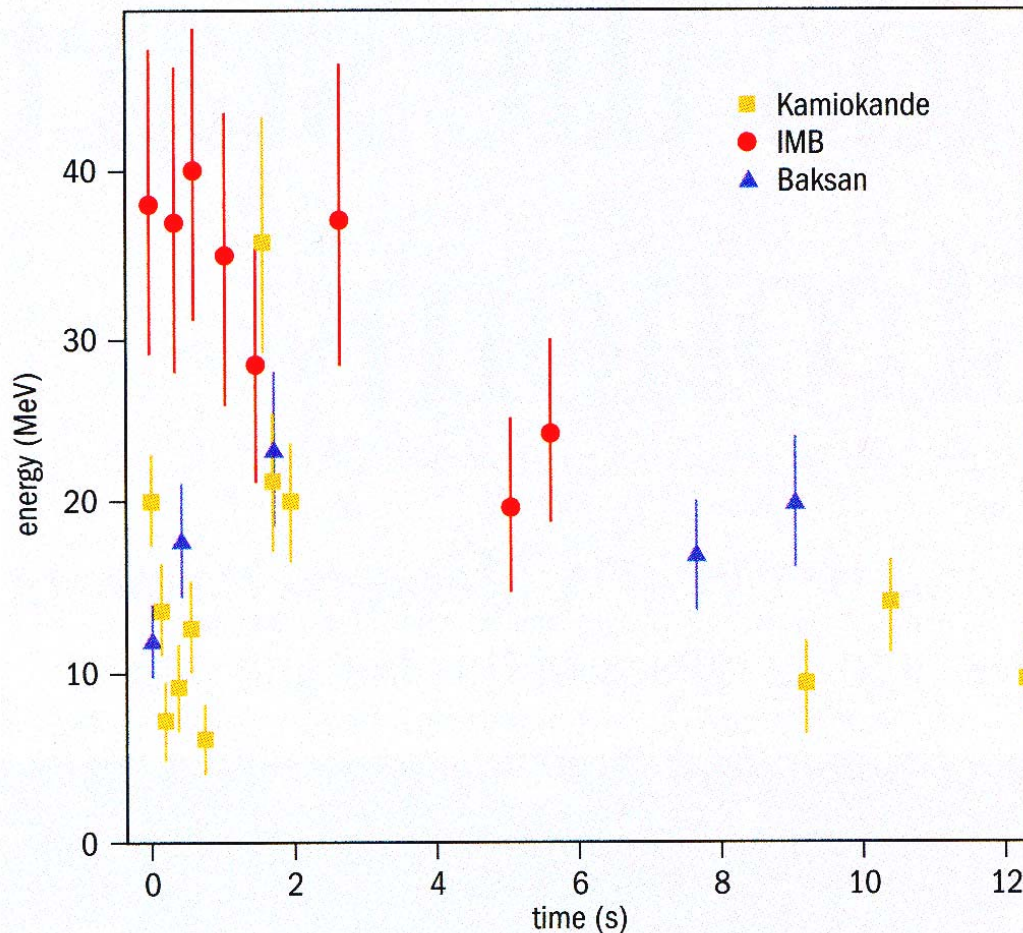
Formation of structure in the Universe

Supernovae II (SNe II)

Stellar/Neutron Star core cooling

Dark Matter/Dark Energy

Intensities in excess of 10^{30} W/cm² and luminosities up to 10^{53} erg/s

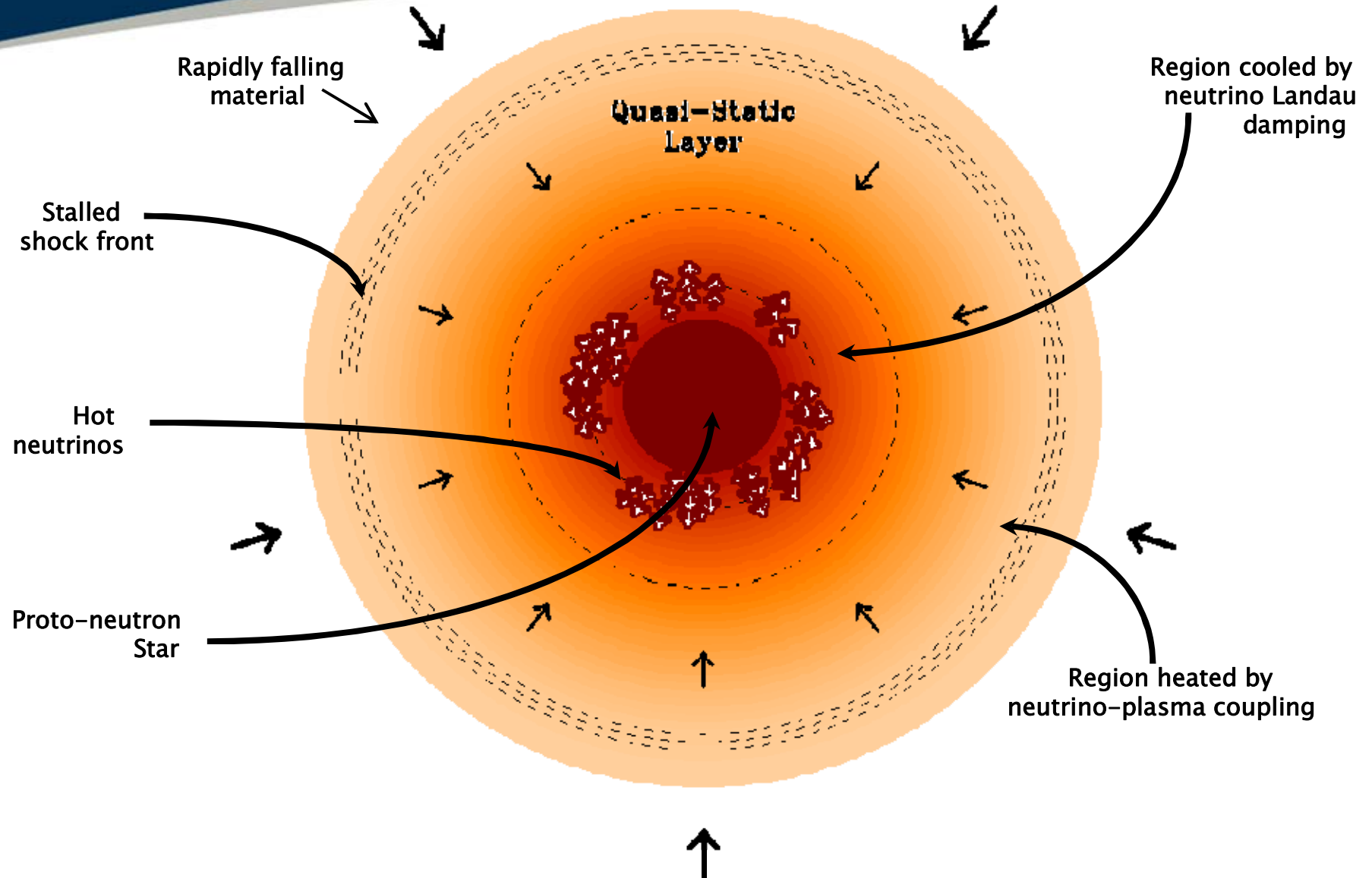


1st observation of neutrinos from outside solar system 1987

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Supernovæ Explosion





Supernova Explosion

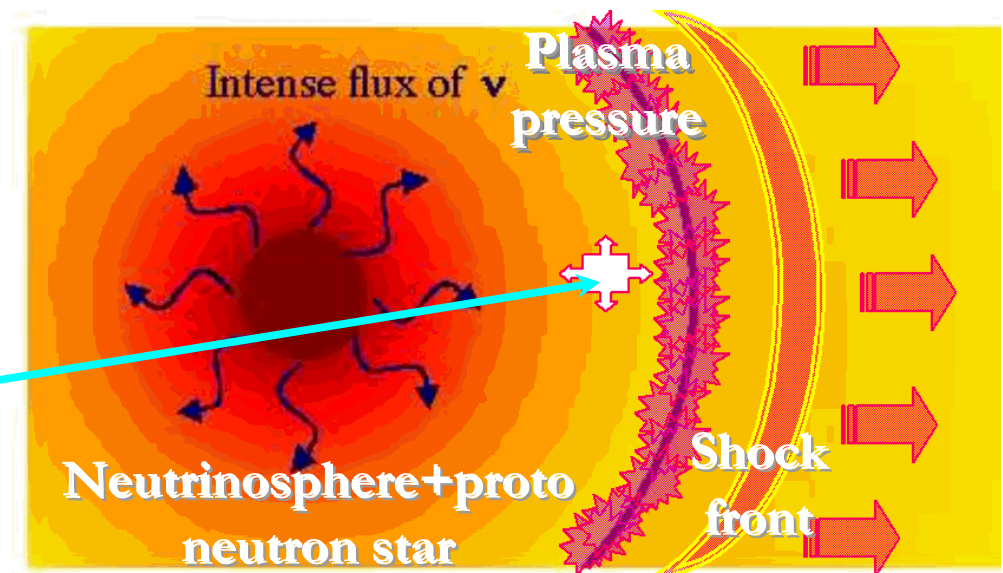
A supernova releases 5×10^{53} erg
(gravitational binding energy of the original star)

- neutrinos 99 % •
- kinetic energy+light $\sim 10^{51}$ erg •

How to turn an implosion
into an explosion?

⇒ Neutrino-plasma
scattering instabilities
in dense plasmas

Neutrino-plasma
heating





Neutrino Refractive Index

The interaction can be easily represented by neutrino refractive index.

The dispersion relation: $(E_\nu - V)^2 - p_\nu^2 c^2 - m_\nu^2 c^4 = 0$ (Bethe, 1986)

E is the neutrino energy, p the momentum, m_ν the neutrino mass.

The potential energy $V = \sqrt{2} G_F n_e$

G_F is the Fermi coupling constant, n_e the electron density

⇒ Refractive index

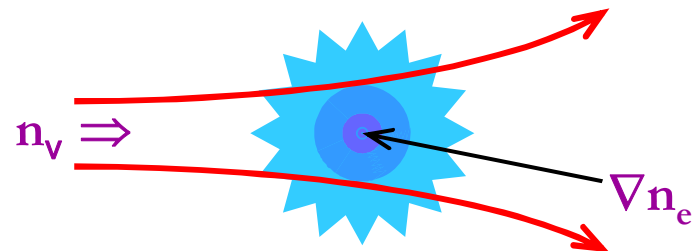
$$N_\nu = \left(\frac{ck_\nu}{\omega_\nu} \right)^2 = \left(\frac{cp_\nu}{E_\nu} \right)^2$$

$$N_\nu \cong 1 - \frac{2\sqrt{2}G_F}{\hbar k_\nu c} n_e$$

Note: cut-off density
 ε_ν neutrino energy

$$n_{ec} > \frac{\varepsilon_\nu}{2\sqrt{2}G_F}$$

Electron neutrinos are refracted away from regions of dense plasma - similar to photons.





For intense neutrino beams, we can introduce the concept of the Ponderomotive force to describe the coupling to the plasma. This can then be obtained from the 2nd order term in the refractive index.

Definition
$$F_{POND} = \frac{N-1}{2} \nabla \xi \quad [\text{Landau \& Lifshitz, 1960}]$$

where ξ is the energy density of the neutrino beam.

$$N = 1 - \frac{2\sqrt{2}G_F n_e}{\epsilon_\nu} \Rightarrow F_{Pond} = -\frac{\sqrt{2}G_F n_e}{\epsilon_\nu} \nabla \xi$$

n_ν is the neutrino number density.

$$F_{Pond} \equiv -\sqrt{2}G_F n_e \nabla n_\nu$$



Neutrino Dynamics in Dense Plasma

Dynamics governed by Hamiltonian (Bethe, '86):

$$H_{eff} = \sqrt{\mathbf{p}_\nu^2 c^2 + m_\nu^2 c^4} + 2G_F n_e(\mathbf{r}, t)$$

| G_F - Fermi constant
| n_e - electron density

$$\mathbf{F}_{pond} = -\sqrt{2}G_F \nabla n_\nu(\mathbf{r}, t)$$

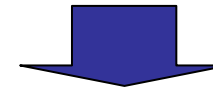
Force on a single electron
due to neutrino distribution

Ponderomotive force* due to neutrinos pushes electrons to regions of lower neutrino density

* ponderomotive force derived from semi-classical (L.O.Silva et al, '98) or quantum formalism (Semikoz, '87)



Effective potential due to **weak interaction** with background electrons
Repulsive potential



$$\mathbf{F} = -\sqrt{2}G_F \nabla n_e(\mathbf{r}, t)$$

Force on a single neutrino due to electron density modulations

Neutrinos bunch in regions of lower electron density



Neutrino Ponderomotive Force (2)

Force on one electron due to electron neutrino collisions f_{coll}

$$f_{\text{coll}} = \sigma_{\nu_e} \xi \quad \sigma_{\nu_e} = \left(\frac{G_F k_B T_e}{2\pi \hbar^2 c^2} \right)^2$$

σ_{ν_e} is the neutrino-electron cross-section

Total collisional force on all electrons is

$$F_{\text{coll}} = n_e f_{\text{coll}} = n_e \sigma_{\nu_e} \xi$$
$$\frac{F_{\text{Pond}}}{F_{\text{coll}}} = \frac{\sqrt{2\pi} \hbar^3 c^3 |k_{\text{Mod}}|}{G_F k_B^2 T^2 k_\nu}$$

$|k_{\text{mod}}|$ is the modulation wavenumber.

For a 0.5 MeV plasma $\frac{F_{\text{Pond}}}{F_{\text{coll}}} \approx 10^{10}$

$\sigma_{\nu_e} \Rightarrow$ collisional mean free path of 10^{16} cm.



Supernova II Physical Parameters

To form a neutron star 3×10^{53} erg must be released

(gravitational binding energy of the original star)

- **light+kinetic energy $\sim 10^{51}$ erg •**
- **gravitational radiation $< 1\%$ •**
- **neutrinos 99 % •**

¶ Electron density @ 100-300 km: $n_{e0} \sim 10^{29} - 10^{32} \text{ cm}^{-3}$

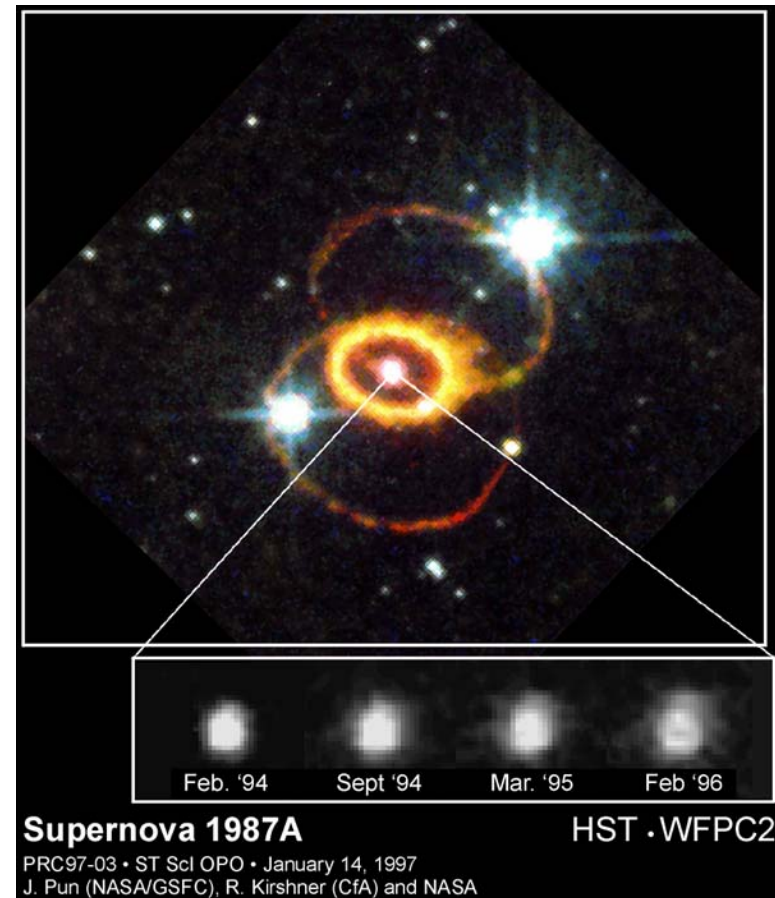
¶ Electron temperature @ 100-300 km: $T_e \sim 0.1 - 0.5 \text{ MeV}$

¶ ν_e luminosity @ neutrinosphere $\sim 10^{52} - 5 \times 10^{53} \text{ erg/s}$

¶ ν_e intensity @ 100-300 Km $\sim 10^{29} - 10^{30} \text{ W/cm}^2$

¶ Duration of intense ν_e burst $\sim 5 \text{ ms}$
(resulting from $p+e \rightarrow n+\nu_e$)

¶ Duration of ν emission of all flavors $\sim 1 - 10 \text{ s}$



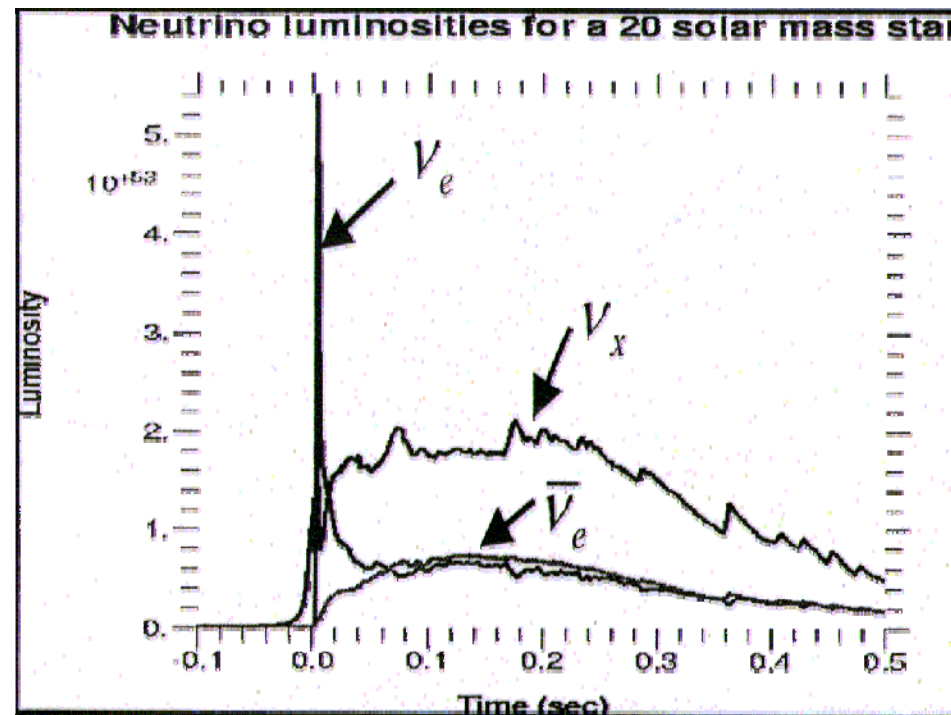


Neutrino heating is necessary for a strong explosion

The shock exits the surface of the proto-neutron star and begins to stall approximately 100 milliseconds after the bounce.

The initial electron neutrino pulse of 5×10^{53} ergs/second is followed by an “accretion” pulse of all flavours of neutrinos.

This accretion pulse of neutrinos deposits energy behind the stalled shock, increasing the matter pressure sufficiently to drive the shock completely through the mantle of the star.





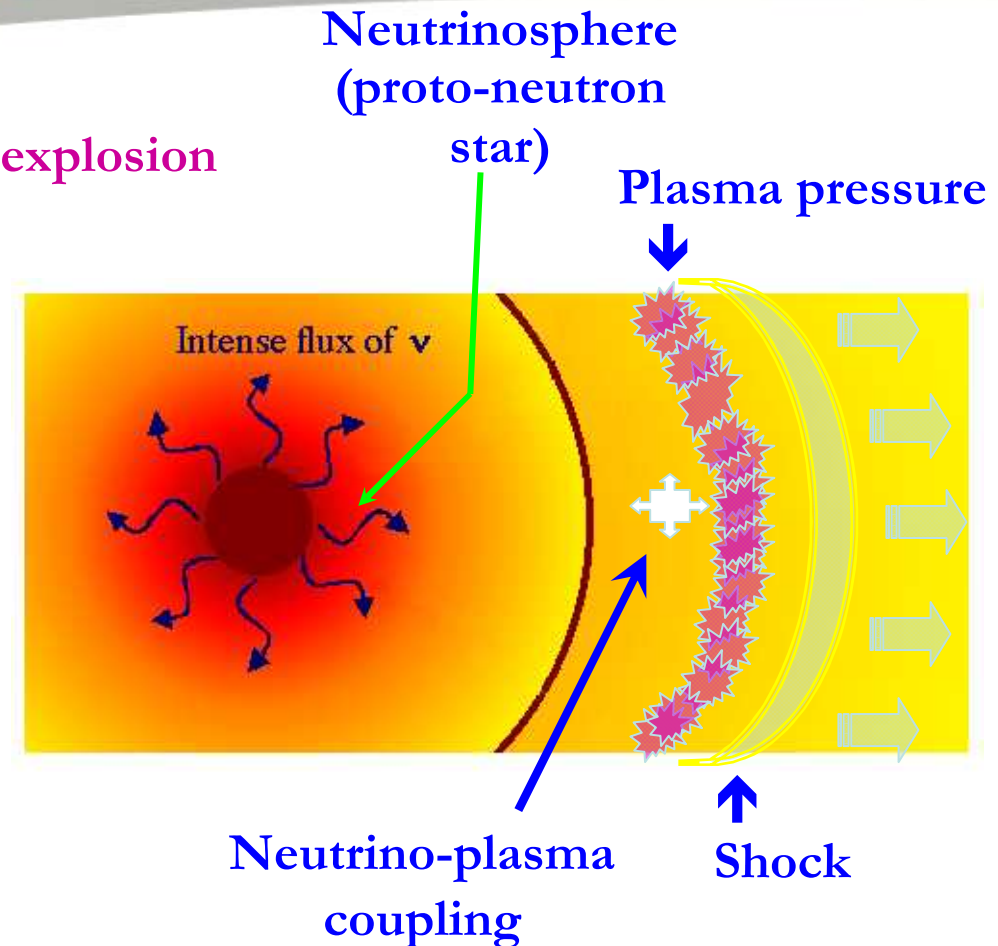
Supernova Explosion

- **How to turn an implosion into an explosion**

- New neutrino physics
- λ_{mfp} for $\nu\nu$ collisions $\sim 10^{16}$ cm in collapsed star
- λ_{mfp} for collective plasma-neutrino coupling $\sim 100\text{m}$

- **How?**

- New non-linear force — neutrino ponderomotive force
- For intense neutrino flux collective effects important
- Absorbs 1% of neutrino energy
 \Rightarrow sufficient to explode star



Bingham *et al.*, *Phys. Lett. A*, 220, 107 (1996)

Bingham *et al.*, *Phys. Rev. Lett.*, 88, 2703 (1999)



Two stream instability

Neutrinos driving electron plasma waves $v_{\phi} \sim c$
Anomalous heating in SNe II

Collisionless damping of electron plasma waves

Neutrino Landau damping
Anomalous cooling of neutron stars

Electroweak Weibel instability

Generation of quasi-static B field
Primordial B and structure in early Universe



Kinetic equation for neutrinos

(describing neutrino number density conservation / collisionless neutrinos)

$$\frac{\partial f_\nu}{\partial t} + \mathbf{v}_\nu \cdot \frac{\partial f_\nu}{\partial \mathbf{r}} - \sqrt{2} G_F \left(\nabla n_e(\mathbf{r}, t) + \frac{1}{c^2} \frac{\partial \mathbf{J}_e(\mathbf{r}, t)}{\partial t} - \frac{\mathbf{v}_\nu}{c} \times \nabla \times \frac{\mathbf{J}_e(\mathbf{r}, t)}{c} \right) \cdot \frac{\partial f_\nu}{\partial \mathbf{p}_\nu} = 0$$

Kinetic equation for electrons driven by neutrino pond. force

(collisionless plasma)

$$\frac{\partial f_e}{\partial t} + \mathbf{v}_e \cdot \frac{\partial f_e}{\partial \mathbf{r}} - \sqrt{2} G_F \left(\nabla n_\nu(\mathbf{r}, t) + \frac{1}{c^2} \frac{\partial \mathbf{J}_\nu(\mathbf{r}, t)}{\partial t} - \frac{\mathbf{v}_e}{c} \times \nabla \times \frac{\mathbf{J}_\nu(\mathbf{r}, t)}{c} \right) \cdot \frac{\partial f_e}{\partial \mathbf{p}_e} - e \left(\mathbf{E} + \frac{\mathbf{v}_e}{c} \times \mathbf{B} \right) \cdot \frac{\partial f_e}{\partial \mathbf{p}_e} = 0$$

+

Maxwell's Equations



Two stream instability driven by a neutrino beam

Usual perturbation theory over kinetic equations + Poisson's equation

$$\begin{aligned}n_e &= n_0 + n_{e1} & f_e &= f_{e0}(\mathbf{p}_e) + f_{e1} \\ \mathbf{v}_e &= \mathbf{v}_1 & f_\nu &= f_{\nu 0}(\mathbf{p}_\nu) + f_{\nu 1} \\ \mathbf{v}_\nu &= \mathbf{v}_{\nu 0} + \mathbf{v}_{\nu 1} & \mathbf{E} &= \mathbf{E}_1\end{aligned}$$

Dispersion relation for electrostatic plasma waves

$$1 + \chi_e(\omega_L, \mathbf{k}_L) + \chi_\nu(\omega_L, \mathbf{k}_L) = 0$$

Electron susceptibility

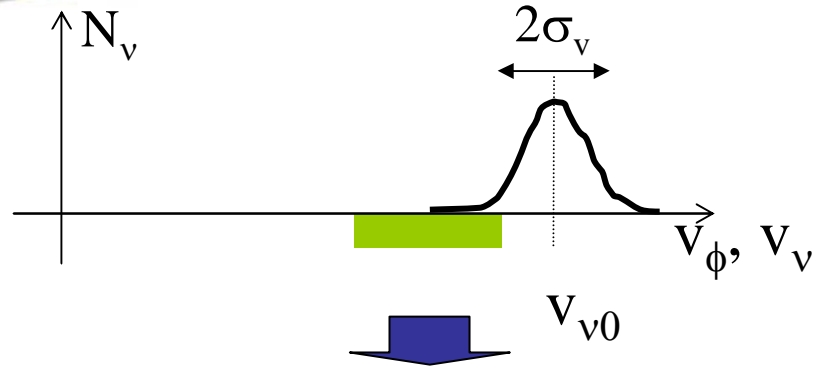
Neutrino susceptibility

$$\chi_\nu(\omega_L, \mathbf{k}_L) = -2 G_F^2 \frac{k_L^3 n_{e0} n_{\nu 0}}{m_e \omega_{pe0}^2} \left(1 - \frac{\omega_L^2}{c^2 k_L^2} \right)^2 \chi_e \int d\mathbf{p}_\nu \frac{\mathbf{k}_L \cdot \frac{\partial \hat{f}_{\nu 0}}{\partial \mathbf{p}_\nu}}{\omega_L - \mathbf{k}_L \cdot \mathbf{v}_\nu}$$

(Silva et al, PRL 1999)



Instability Regimes: hydrodynamic vs kinetic



Unstable PW modes (ω_L, k_L)

If region of unstable PW modes **overlaps** neutrino distribution function **kinetic regime becomes important**

$N_{e0} = 10^{29} \text{ cm}^{-3}$ $\langle E_\nu \rangle = 10 \text{ MeV}$
 $L_\nu = 10^{52} \text{ erg/s}$ $T_\nu = 3 \text{ MeV}$
 $R_m = 300 \text{ Km}$ $m_\nu = 0.1 \text{ eV}$

Kinetic instability

$\gamma \propto G_F^2$ if $\left| \frac{\omega_L}{k_L} - v_{v0} \right| \ll \sigma_{v_\nu}$

$\sigma_{v_\nu} / c \approx 10^{-16}$

Hydro instability

$\gamma \propto G_F^{2/3}$ if $\left| \frac{\omega_L}{k_L} - v_{v0} \right| \gg \sigma_{v_\nu}$

$\left| \frac{\omega_L}{ck_L} - \frac{v_{v0}}{c} \right| \approx \frac{\gamma_{\max}}{\omega_{pe0}} \beta_\phi \approx 10^{-14} - 10^{-11}$

where $v_\nu = p_\nu c^2 / E_\nu = p_\nu c^2 / (p_\nu^2 c^2 + m_\nu^2 c^4)^{1/2}$
 - for $m_\nu \rightarrow 0, \sigma \rightarrow 0$ **hydro regime** -



Estimates of the Instability Growth Rate

$n_{e0} = 10^{29} \text{ cm}^{-3}$
 $L_\nu = 10^{52} \text{ erg/s}$
 $R_m = 300 \text{ Km}$
 $\langle E_\nu \rangle = 10 \text{ MeV}$



Growth distance $\sim 1 \text{ m}$
(without collisions)

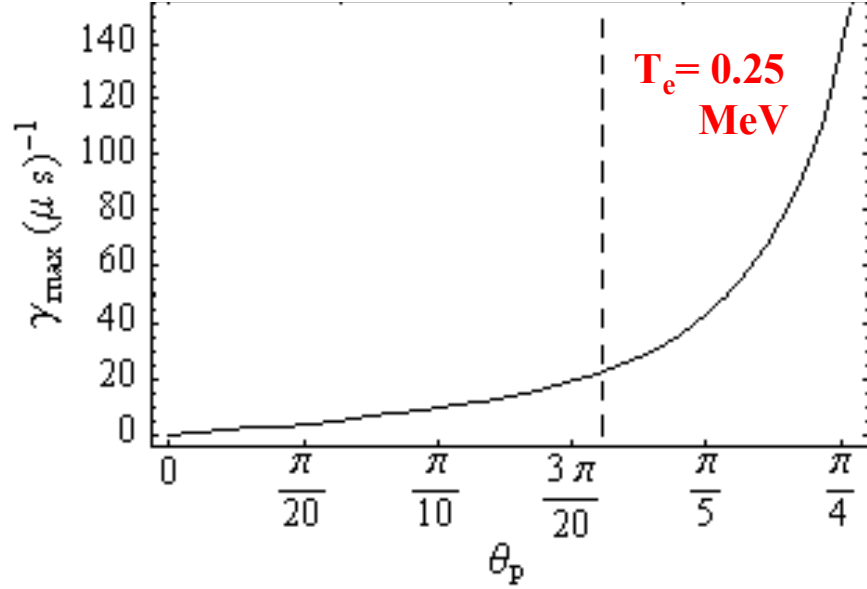
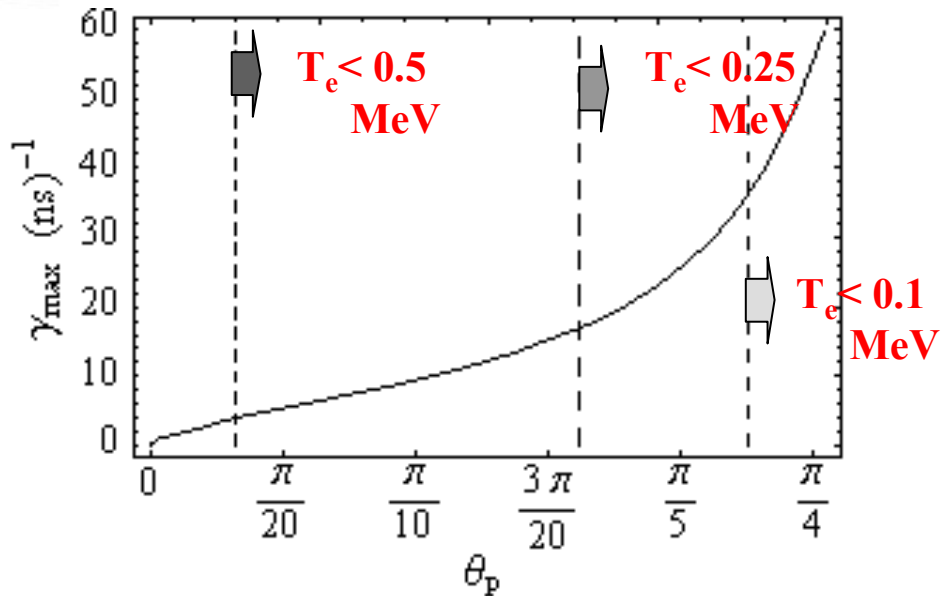
Growth distance $\sim 300 \text{ m}$
(with collisions)

- 6 km for 20 e-foldings -

Mean free path for
 neutrino electron single scattering
 $\sim 10^{11} \text{ km}$

Single ν -electron scattering $\propto G_F^2$

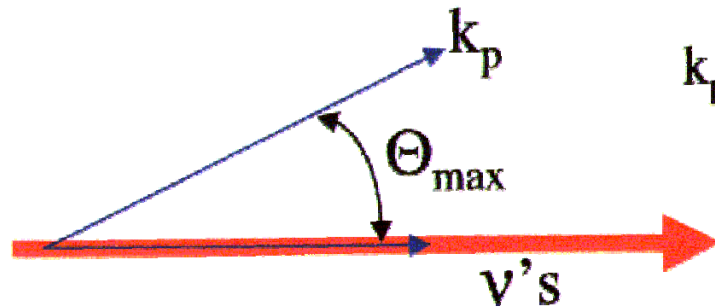
Collective mechanism much stronger than single particle processes





Saturation Mechanism

Neutrino streaming instability saturates by electron Landau damping



$$k_p \sim \omega_{pe0}/c \cos \Theta \quad \Theta_{\max} \sim \arccos(v_{th}/c)$$

$T_e \uparrow \Rightarrow \Theta_{\max} \downarrow \Rightarrow$ Instability Shutdown

Modes with maximum growth rate

$$\mathbf{E}_k = E_k \delta(k_{\parallel} - \omega_{pe0}/c) \frac{\mathbf{k}}{|\mathbf{k}|}$$



Simplified Model

$$\frac{\partial |\mathbf{E}_k|^2}{\partial t} = 2\gamma_k |\mathbf{E}_k|^2$$

$$\gamma_k = 0 \text{ if } k > k_{\max}$$

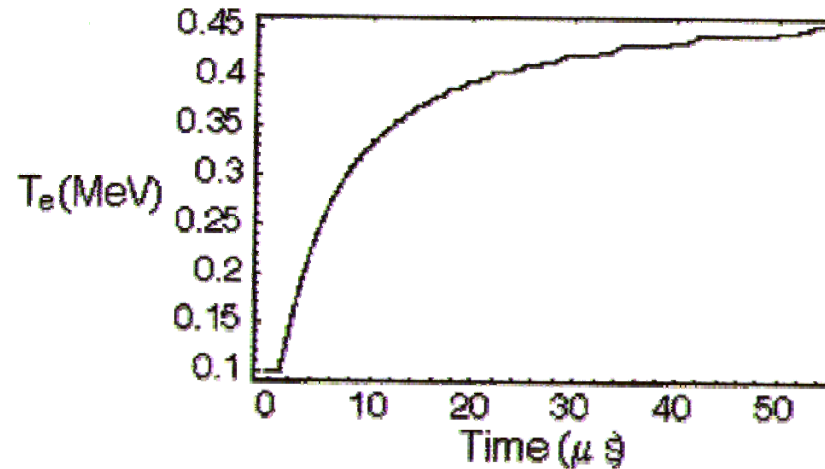
$$\frac{\partial W_{EPW}}{\partial t} = n_e \frac{\partial T_e}{\partial t} = \frac{1}{8\pi} \frac{\partial}{\partial t} \sum_{k \leq k_{\max}} |\mathbf{E}_k|^2$$

$$k_{\max} = \omega_{pe0}/v_{th}(T_e)$$



Electron Heating

$n_{e0} = 10^{29} \text{ cm}^{-3}$
 $L_v = 10^{52} \text{ erg/s}$
 $R_m = 300 \text{ Km}$
 $\langle E_v \rangle = 10 \text{ MeV}$
 $T_{e0} = 0.1 \text{ MeV}$



$$\Delta W_{EPW} \sim 10^{-4} W_p$$

including e-i collisions

- ¶ Preliminary results indicate strong heating up to 0.5 MeV;
- ¶ Further analysis is necessary to include relativistic corrections on electron Landau damping - present model overestimates eLD;
- ¶ Initial v_e burst (\sim ms) can heat the plasma efficiently;
- ¶ Detailed quasi-linear theory for v 's and e 's will give signatures of v -driven instabilities and more accurate results \rightarrow information to be included in supernovae code
- ¶ Stimulated "Compton" scattering must also be considered



Supernovæ explosion and neutrino driven instabilities

e-Neutrino burst
 $L_\nu \sim 4 \times 10^{53}$ erg/s , $\tau \sim 5$ ms

Neutrino emission of all flavors
 $L_\nu \sim 10^{52}$ erg/s , $\tau \sim 1$ s

**Due to electron Landau damping,
plasma waves only grow in the
lower temperature regions**

Supernova Explosion!



drives plasma waves through
neutrino streaming instability

plasma waves are damped
(collisional damping)

Plasma heating
@ 100-300 km from center

Stimulated
"Compton"
scattering

Less energy lost by
shock to dissociate iron

Pre-heating of outer layers
by short ν_e burst (~ms)

Revival of stalled shock in
supernova explosion
(similar to Wilson mechanism)

Anomalous pressure
increase behind shock



Neutrino play a critical role in Type II Supernovæ

- **Neutrino spectra and time history of the fluxes probe details of the core collapse dynamics and evolution.**
- **Neutrinos provide heating for “delayed” explosion mechanism.**
- **Sufficiently detailed and accurate simulations provide information on convection models and neutrino mass and oscillations.**



Plasma waves driven by electrons, photons, and neutrinos

Electron beam $(\partial_t^2 + \omega_{pe0}^2) \delta n_e = -\omega_{pe0}^2 n_{e-beam}$

Photons $(\partial_t^2 + \omega_{pe0}^2) \delta n_e = \frac{\omega_{pe0}^2}{2m_e} \nabla^2 \int \frac{d\mathbf{k}}{(2\pi)^3} \hbar \frac{N_\gamma}{\omega_{\mathbf{k}}}$

Neutrinos $(\partial_t^2 + \omega_{pe0}^2) \delta n_e = \frac{\sqrt{2} n_{e0} G_F}{m_e} \nabla^2 n_\nu$

δn_e Perturbed electron plasma density

Ponderomotive force

[physics/9807049](#), [physics/9807050](#)

Kinetic/fluid equations for electron beam, photons, neutrinos
coupled with electron density perturbations due to PW

Self-consistent picture of collective e, γ , ν -plasma interactions



In different astrophysical conditions involving intense neutrino fluxes, neutrino driven plasma instabilities are likely to occur

Anomalous heating in SNe II
Electroweak Weibel instability in the early universe
Enhanced Mixing by Turbulent structures

Challenge: reduced description of neutrino driven anomalous processes to make connection with supernovae numerical models



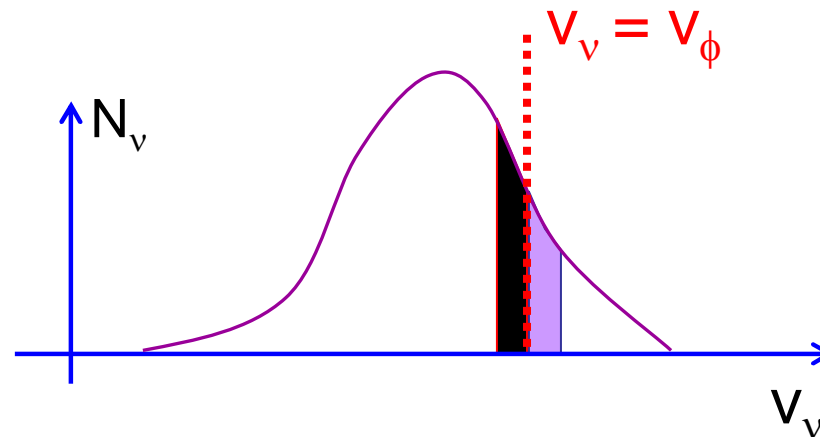
Neutrino Landau Damping I

What if the source of free energy is in the plasma?

Thermal spectrum of neutrinos interacting with turbulent plasma



Collisionless damping of EPWs by neutrinos moving resonantly with EPWs



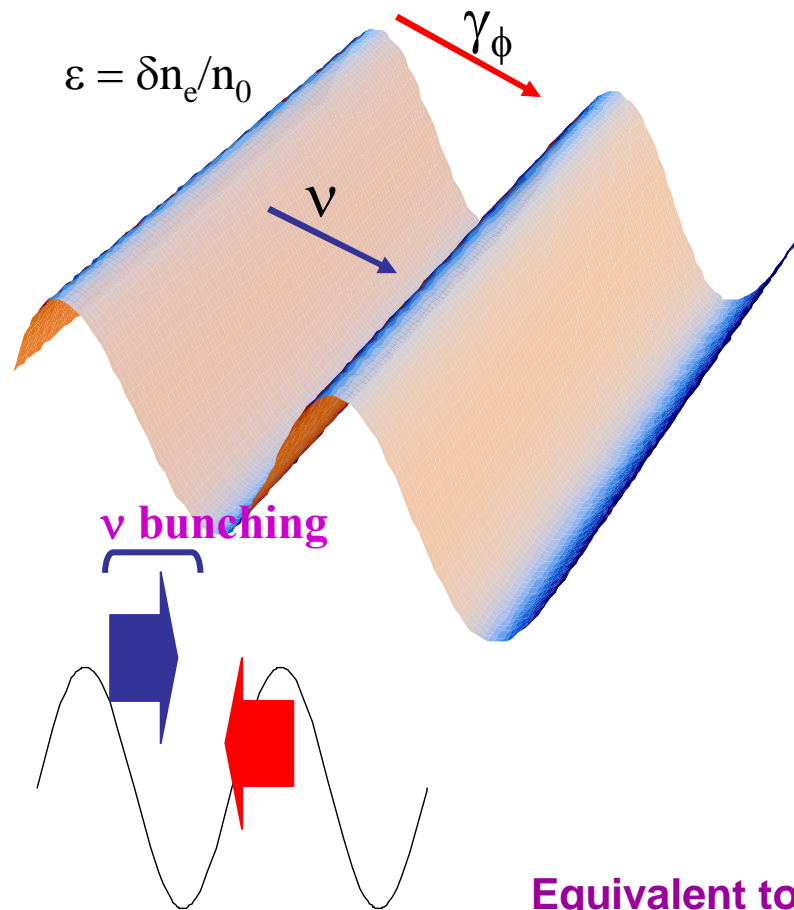
Physical picture for
electron Landau damping
(Dawson, '61)

General dispersion relation describes not only the neutrino fluid instability but also the neutrino kinetic instability

(Silva et al, PLA 2000)



Neutrino surfing electron plasma waves



$$|\Delta E_\nu|_{\max} \approx |\mathbf{F}| L_{dp} \approx 8\sqrt{2} G_F \varepsilon n_{e0}$$

$$\gamma_\phi = 10$$

$$\varepsilon = 10^{-2}$$

$$n_{e0} = 10^{32} \text{ cm}^{-3}$$

$$L_{dp} = \lambda_p \gamma_\phi^2 \approx 3 \times 10^{-2} \text{ cm}$$

$$dE_\nu / dL \approx 8\sqrt{2} G_F \varepsilon n_{e0} / (\lambda_p \gamma_\phi^2) \approx 200 \text{ eV} / \text{cm}$$

Equivalent to physical picture for RFS of photons (Mori, '98)



Neutrino Landau damping reflects contribution from the pole in neutrino susceptibility

$$\chi_\nu(\omega_L, \mathbf{k}_L) \propto \int d\mathbf{p}_\nu \frac{\mathbf{k}_L \cdot (\partial \hat{f}_{\nu 0} / \partial \mathbf{p}_\nu)}{\omega_L - \mathbf{k}_L \cdot \mathbf{v}_\nu} \longrightarrow \int d\mathbf{p}_\perp \int d\mathbf{p}_\parallel \left\{ P \int \frac{(\partial \hat{f}_{\nu 0} / \partial \mathbf{p}_\parallel)}{\mathbf{p}_\parallel - \mathbf{p}_{\parallel 0}} d\mathbf{p}_\parallel + i\pi \left(\frac{\partial \hat{f}_{\nu 0}}{\partial \mathbf{p}_\parallel} \right)_{\mathbf{p}_{\parallel 0}} \right\}$$

EPW wavevector $\mathbf{k}_L = \mathbf{k}_{L\parallel}$ defines parallel direction
 neutrino momentum $\mathbf{p}_n = \mathbf{p}_{v\parallel} + \mathbf{p}_{v\perp}$
 arbitrary neutrino distribution function $f_{\nu 0}$
 Landau's prescription in the evaluation of χ_ν

For a Fermi-Dirac neutrino distribution

$$\gamma_{\text{Landau}} \approx -\frac{k_L c}{2} \pi \frac{\mathbf{G}_F^2 n_{e0} n_{\nu 0}}{m_e c^2 k_B T_\nu} \left(1 - \frac{\omega_L^2}{c^2 k_L^2} \right)^2 \frac{\text{Li}_2(-\exp E_F / T_\nu)}{\text{Li}_3(-\exp E_F / T_\nu)}$$



Intense fluxes of neutrinos in Supernovae

Neutrino dynamics in dense plasmas (making the bridge with HEP)

Plasma Instabilities driven by neutrinos

Supernovae plasma heating: shock revival

Neutrino mode conversion (Neutrino oscillations)

Neutrino Landau damping

Neutron star cooling

Solar neutrino deficit

Gamma-ray bursters: open questions

Conclusions



Free energy in particles (e , i , e^+) transferred to the fields (quasi-static \mathbf{B} field)

Fundamental plasma instability

laser-plasma interactions

shock formation

magnetic field generation in GRBs

Signatures: \mathbf{B} field + filamentation + collisionless drag

Free energy of neutrinos/anisotropy in neutrino distribution transferred to electromagnetic field



Usual perturbation theory over kinetic equations + Faraday's and Ampere's law

Cold plasma

$$(\omega^2 - k^2 c^2) \left(1 - \omega \Delta_\nu \phi(\hat{f}_{\nu 0}) \right) = \omega_{pe0}^2 \quad \mathbf{k} = k \mathbf{e}_z$$

$$\phi(\hat{f}_{\nu 0}) = \int d\mathbf{p}_\nu \frac{v_{\nu\perp}}{\omega - kv_{\nu z}} \cos^2 \theta \left\{ \frac{\hat{\mathcal{J}}_{\nu 0}}{\partial p_{\nu\perp}} + \frac{k}{\omega} v_{\nu\perp} \frac{\hat{\mathcal{J}}_{\nu 0}}{\partial p_{\nu z}} - \frac{k}{\omega} v_{\nu z} \frac{\hat{\mathcal{J}}_{\nu 0}}{\partial p_{\nu\perp}} \right\}$$

Monoenergetic ν beam ($m_\nu = 0$)

$$\hat{f}_{\nu 0} = \hat{f}_{\nu 0}(\mathbf{p}_{\nu\perp}, p_{\nu z})$$

$$(\omega^2 - k^2 c^2) \left(1 + \Delta_\nu \frac{k^2 c^2}{\omega^2} \beta_{\nu x0}^2 \right) = \omega_{pe0}^2 \quad \omega \approx i\gamma_{\text{Weibel}} \quad \& \quad |\gamma_{\text{Weibel}}| \ll |k|$$

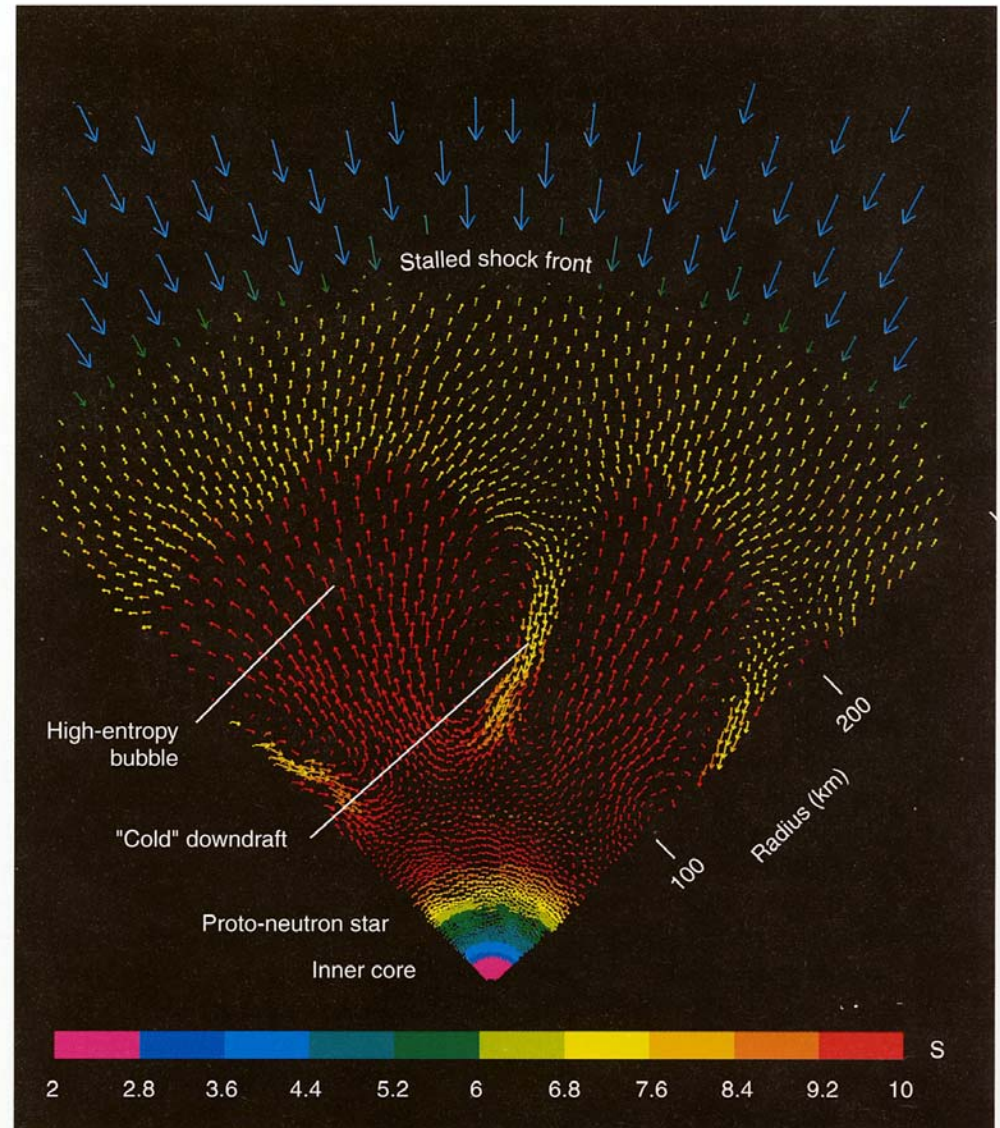
$$\gamma_{\text{Weibel}} = \beta_{\nu x0} \frac{k^2 c^2}{\sqrt{k^2 c^2 + \omega_{pe0}^2}} \Delta_\nu^{1/2} \propto \mathbf{G}_F$$

(Silva et al, PFCF 2000)



Detailed Simulations

The graphic shows a slice through the core region of a supernova 50 ms after the bounce. Each arrow represents a parcel of matter and the length and direction show velocity (colour represents entropy, S). Regions of higher entropy indicate heating. The shock front is apparent from the position where yellow arrows meet green ones (about 300 km from the core). Low entropy, high velocity material (blue arrows) is the rest of the star raining down onto the core. Neutrinos are present in the blue-green region about 40 km from the core where they are being absorbed in the quasi-static layer which then becomes heated (yellow).





MSW – Matter Effect

All neutrinos interact through neutral currents, Z boson.

Only electron neutrinos interact through charge current, W boson.

Refractive index for all flavours

$$N_{\mu,\tau} = 1 + \frac{\sqrt{2}G_F}{p_{\mu,\tau}} f(n_e, n_p, n_n)$$

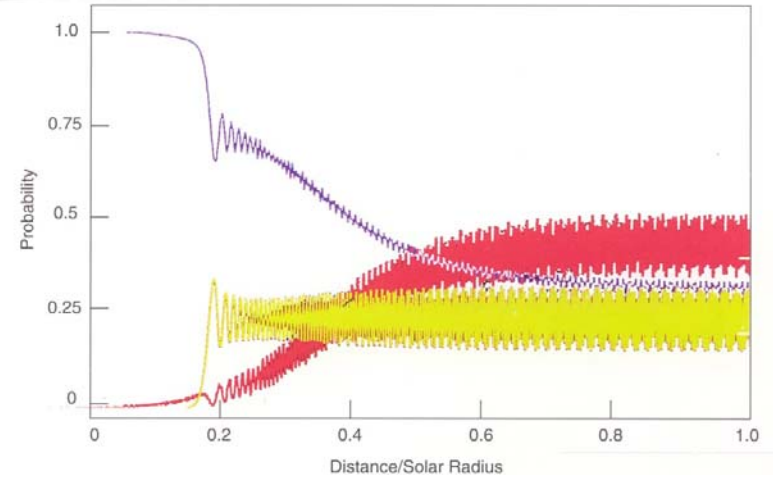
$$N_{\nu_e} = 1 + \frac{\sqrt{2}G_F}{p_{\nu_e}} f(n_e, n_p, n_n) - \frac{\sqrt{2}G_F}{p_{\nu_e}} n_e$$

Resonance coupling for $p_{\nu_e} = p_{\mu,\tau}$

$$\therefore \Delta m^2 = m_{\mu,\tau}^2 - m_{\nu_e}^2 = 2\sqrt{2}G_F n_e E_0$$

e.g. in a plasma density gradient

$$L_n = \left(\frac{1}{n} \frac{dn}{dx} \right)^{-1}$$



Probability of detecting a particular flavour of neutrino as they move out from the core through the body of the Sun:- electron neutrinos (purple), muon neutrinos (red), tau neutrinos (yellow).

Conversion probability:
Neutrino oscillate

$$C = 1 - \exp \left[-A \frac{\Delta m^2 E L_n}{G_F p^2} \right]$$

Solar data

$$\Delta m^2 \approx 8.9 \times 10^{-5} \text{ eV}^2$$

Atmospheric data

$$\Delta m^2 \approx 2.4 \times 10^{-4} \text{ eV}^2$$



The MSW effect – neutrino flavor conversion

Flavor conversion – electron neutrinos convert into another ν flavor
Equivalent to mode conversion of waves in inhomogeneous plasmas

$$\frac{d^2\psi_i}{dx^2} + k_i^2\psi_i = 0 \quad k_i^2 = \frac{E_i^2 - m_i^2c^4 - V_{eff\ i}}{c^2\hbar^2} \quad i = 1, 2, 3 \text{ (each } \nu \text{ flavor)}$$

Mode conversion when $k_1 = k_2$, $E_1 = E_2$

$$\frac{d^2\psi_1}{dx^2} + k_1^2\psi_1 = \lambda_1\psi_2 \quad \lambda_i = \frac{1}{2} \frac{\Delta m^2 c}{\hbar^2} \frac{E_i}{p_i} \sin 2\theta$$

$$\frac{d^2\psi_2}{dx^2} + k_2^2\psi_2 = \lambda_2\psi_1$$

Fully analytical MSW conversion probabilities derived in unmagnetized plasma and magnetized plasma



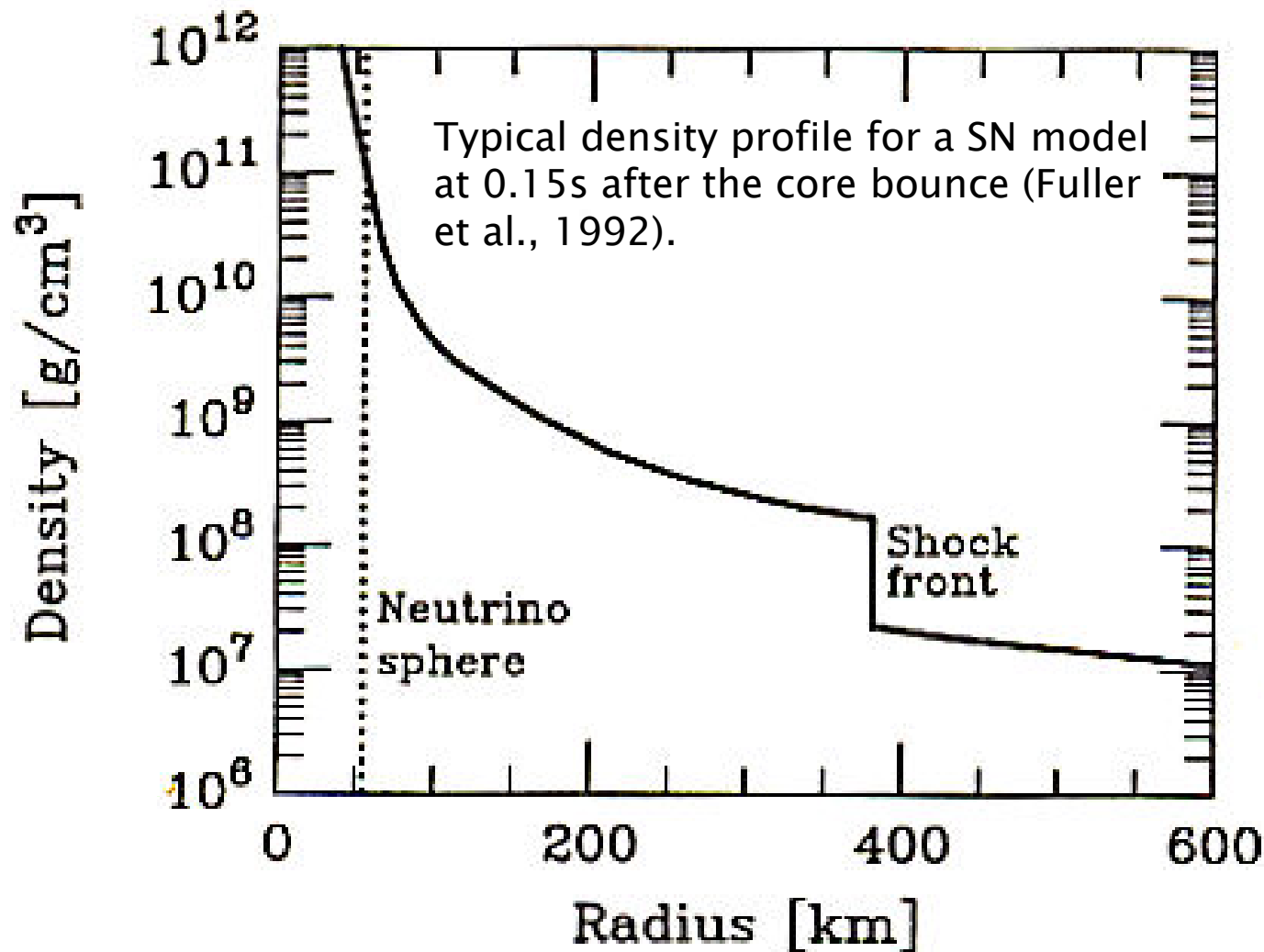
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Rutherford Appleton Laboratory

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A Serbeto, M Marklund, G Brodin**



Typical Density Profile





Length scales

← **Compton Scale**
HEP

Hydro Scale →
Shocks

Plasma scale

$$\lambda_D, \lambda_p, r_L$$

Can intense neutrino winds drive collective and kinetic mechanisms at the *plasma scale* ?

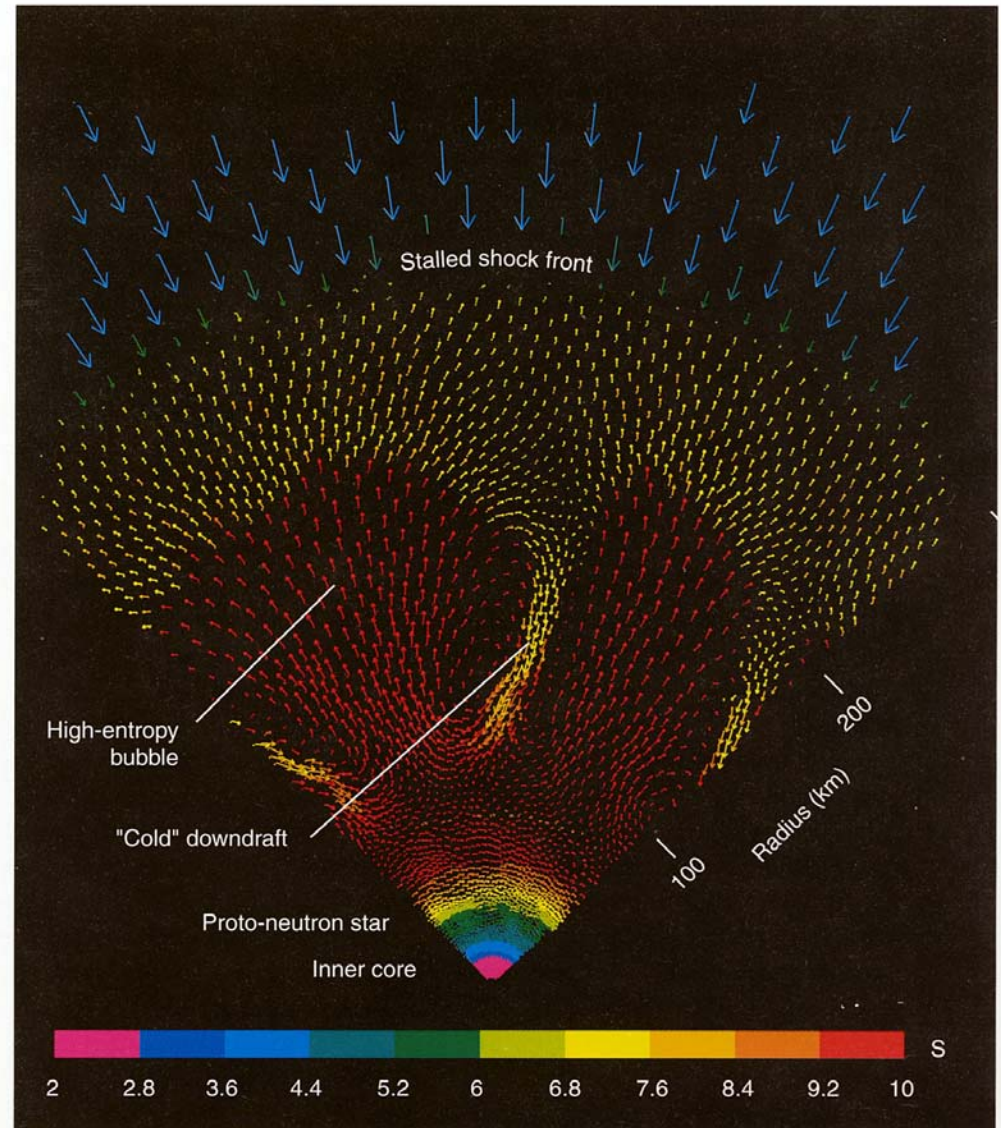
**Bingham, Bethe, Dawson,
Su (1994)**





Detailed Simulations

The graphic shows a slice through the core region of a supernova 50 ms after the bounce. Each arrow represents a parcel of matter and the length and direction show velocity (colour represents entropy, S). Regions of higher entropy indicate heating. The shock front is apparent from the position where yellow arrows meet green ones (about 300 km from the core). Low entropy, high velocity material (blue arrows) is the rest of the star raining down onto the core. Neutrinos are present in the blue-green region about 40 km from the core where they are being absorbed in the quasi-static layer which then becomes heated (yellow).





Anomalous heating by neutrino streaming instability

$$\left(\frac{\Delta E_\nu}{10^{50} \text{ erg}} \right) \approx 1.2 \times 10^{-1} \left(\frac{R}{500 \text{ Km}} \right)^3 \left(\frac{T}{2 \text{ MeV}} \right) \times \left\{ 0.145 \left(\frac{n}{10^{30} \text{ cm}^{-3}} \right) + \left(\frac{T}{2 \text{ MeV}} \right)^3 \right\}$$

Neutrino heating to re-energize stalled shock $\left(\frac{\Delta E_\nu}{10^{50} \text{ erg}} \right) \approx 1 - 0.1$

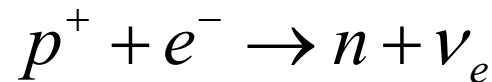
Sufficient neutrino energy deposited into electron energy to restart the stalled shock and explode the star.



Supernovæ II Neutrinos

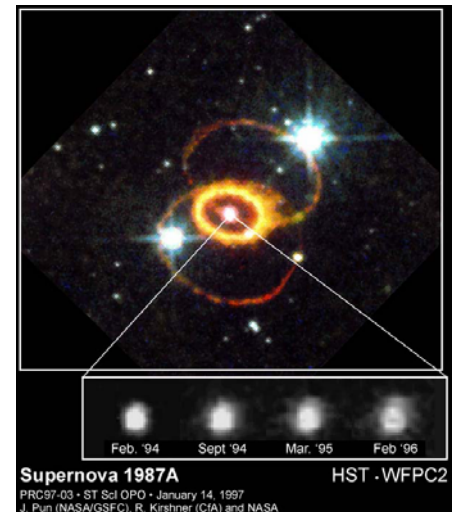
- A massive star exhausts its fusion fuel supply relatively quickly.
- The core implodes under the force of gravity.
- This implosion is so strong it forces electrons and protons to combine and form neutrons – in a matter of seconds a city sized superdense mass of neutrons is created.

- The process involves the weak interaction called “electron capture”



- A black hole will form unless the neutron degeneracy pressure can resist further implosion of the core. Core collapse stops at the “proto-neutron star” stage – when the core has a ~10 km radius.

- **Problem:** How to reverse the implosion and create an explosion?

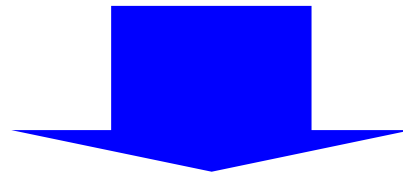




Neutrinos in the Standard Model

Leptons	Electron e	Muon μ	Tau τ
	Electron neutrino ν_e	Muon neutrino ν_μ	Tau neutrino ν_τ

An electron beam propagating through a plasma generates plasma waves, which perturb and eventually break up the electron beam



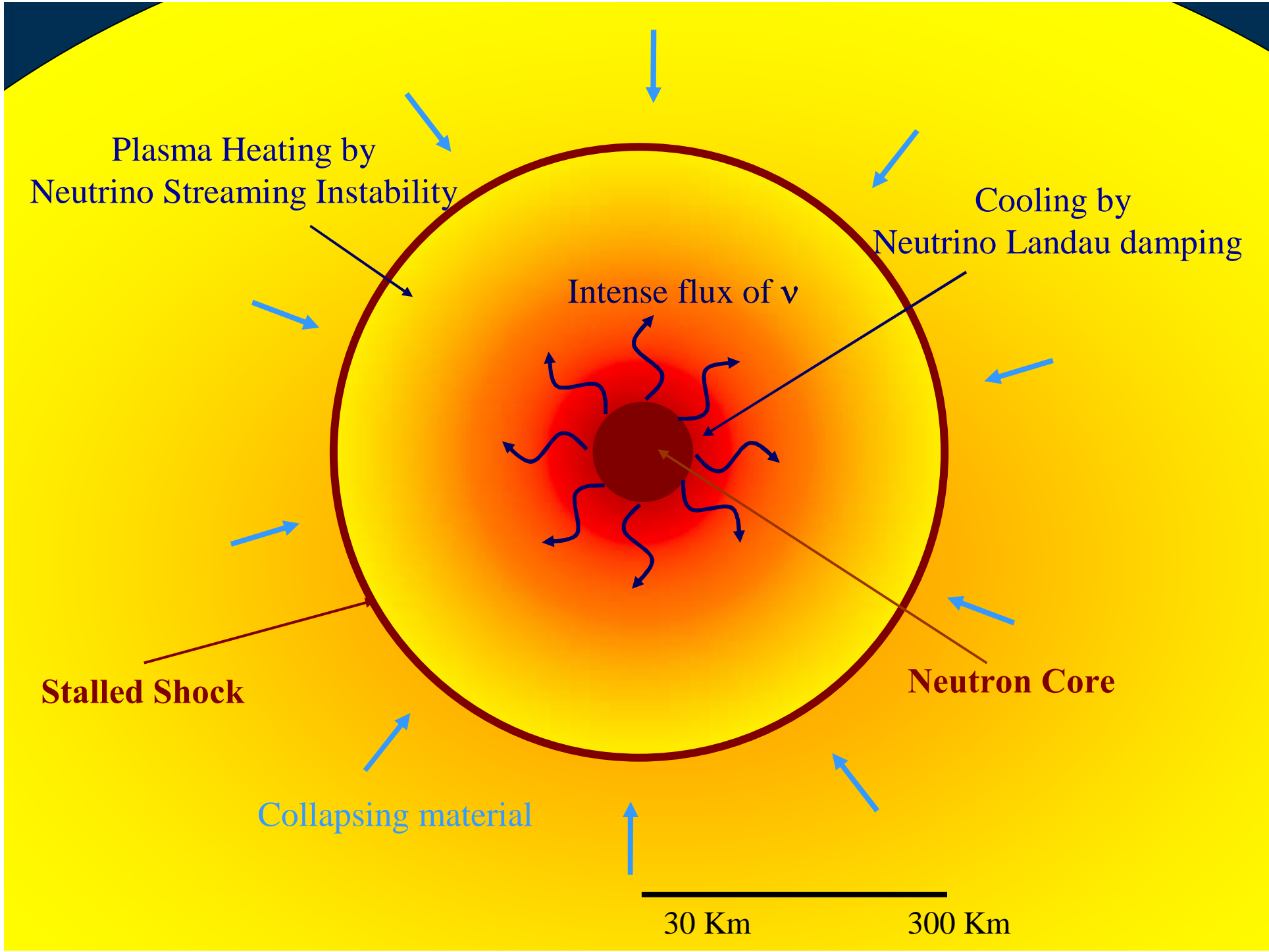
Electroweak theory unifies electromagnetic force and weak force

Electrons and neutrinos interact via the weak force

In a plasma neutrinos acquire an induced charge - dressed particle

$$e_\nu = -\frac{\sqrt{8\pi}}{k_B T_e} G_F n_{e_0} e_{electron}$$

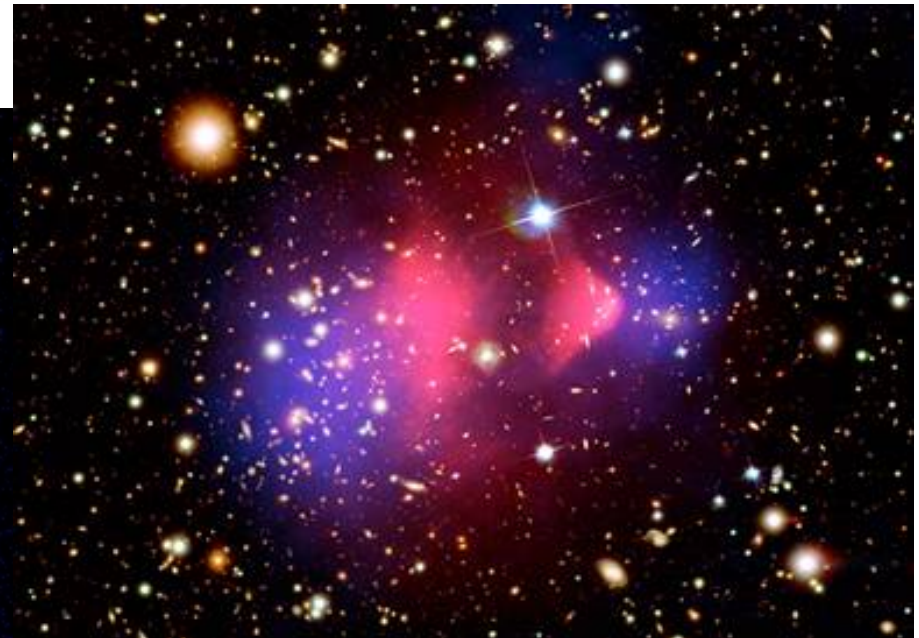
A similar scenario should also be observed for intense neutrino bursts





Bullet Cluster

1E 0657-56



Chandra 0.5 Msec image

0.5 Mpc

$z=0.3$



Neutrino Beam-Plasma Instability

Monoenergetic neutrino beam

$$f_{\nu 0} = n_{\nu 0} \delta(\mathbf{p}_\nu - \mathbf{p}_{\nu 0})$$

Dispersion Relation

$$\omega_L^2 = \omega_{pe0}^2 + \left(\frac{m_\nu^2 c^4 \cos^2 \theta}{E_{\nu 0}^2} + \sin^2 \theta \right) \frac{\aleph k_L^4 c^4}{\left(\omega_L - k_L c \cos \theta \frac{p_{\nu 0} c}{E_{\nu 0}} \right)^2}$$

$\theta \equiv \mathbf{k}_L \wedge \mathbf{p}_{\nu 0}$
 $\aleph = \frac{2 G_F^2 n_{\nu 0} n_{e 0}}{m_e c^2 E_{\nu 0}}$

¶ If $m_\nu \rightarrow 0$ direct forward scattering is absent

¶ Similar analysis of two-stream instability:

- maximum growth rate for $k_L v_{\nu 0 \parallel} = k c \cos \theta \approx \omega_{pe0}$
- $\omega = \omega_{pe0} + \delta = k_L v_{\nu 0 \parallel} + \delta$

<div style="border-left: 1px dashed black; padding-left: 5px;"> <p style="margin: 0;">↓</p> </div>	Weak Beam ($\delta / \omega_{pe0} \ll 1$)	Growth rate	$\gamma_{\max} = \frac{\sqrt{3}}{2} \omega_{pe0} \left(\frac{\tan^2 \theta}{\sin^2 \theta} \aleph \right)^{1/3}$	$\propto G_F^{2/3}$
	Strong Beam ($\delta / \omega_{pe0} \gg 1$)		$\gamma_{\max} \propto G_F^{1/2}$	

Single ν -electron scattering $\propto G_F^2$

Collective plasma process much stronger than single particle processes



- The “Big Bang” Model of cosmology predicts that neutrinos should exist in great numbers – these are called relic neutrinos.
- During the Lepton era of the universe neutrinos and electrons (plus anti particles) dominate:
 - $\sim 10^{86}$ neutrinos in the universe
 - Current density $n_\nu \sim 220 \text{ cm}^{-3}$ for each flavour!
- Neutrinos have a profound effect on the expansion of the universe:
 - Galaxy formation
 - Magnetic field generation
 - Dark matter
 - Dark energy

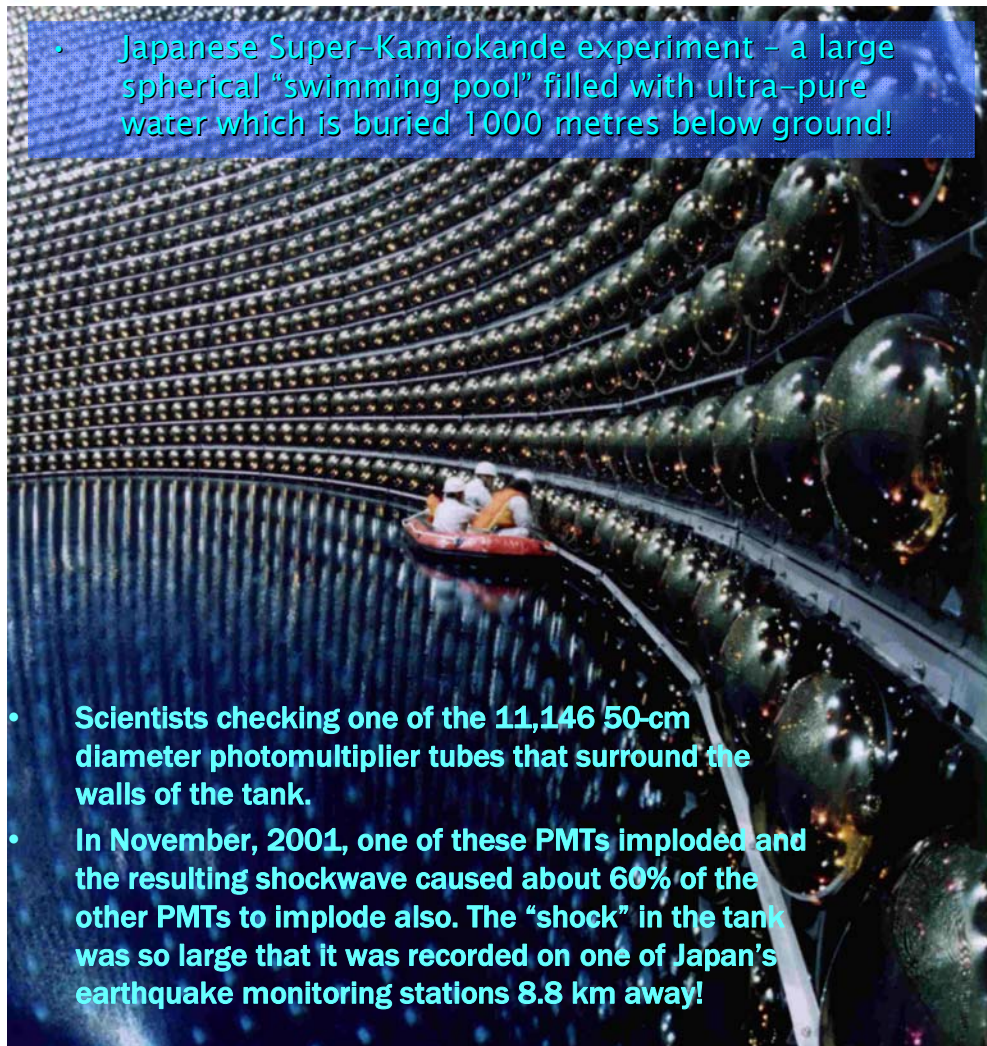
} **in the early universe**

Shukla *et al.*, 1998.
Semikoz *et al.*, 2004.

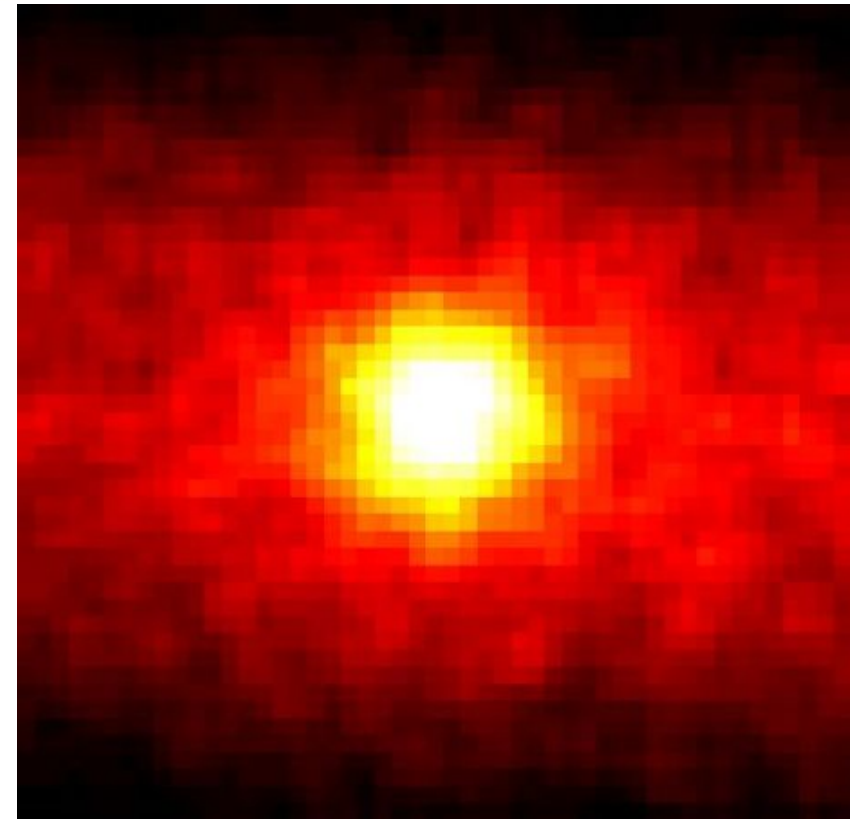


Neutrinos from the Sun – Super-Kamiokande

- Japanese Super-Kamiokande experiment – a large spherical “swimming pool” filled with ultra-pure water which is buried 1000 metres below ground!



- Scientists checking one of the 11,146 50-cm diameter photomultiplier tubes that surround the walls of the tank.
- In November, 2001, one of these PMTs imploded and the resulting shockwave caused about 60% of the other PMTs to implode also. The “shock” in the tank was so large that it was recorded on one of Japan’s earthquake monitoring stations 8.8 km away!

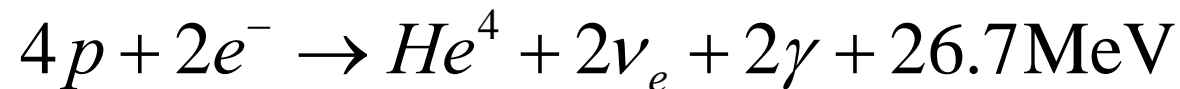


- **Super-Kamiokande obtained this neutrino image of the Sun!**



Solar Neutrinos

The p-p chain



3% of the energy is carried away by neutrinos

One neutrino is created for each ≈ 13 MeV of thermal energy

The “Solar Constant”, S (Flux of solar radiation at Earth) is

$$S = 1.37 \times 10^6 \text{ erg/cm}^2\text{s}$$

Neutrino flux at Earth, ϕ_ν ,

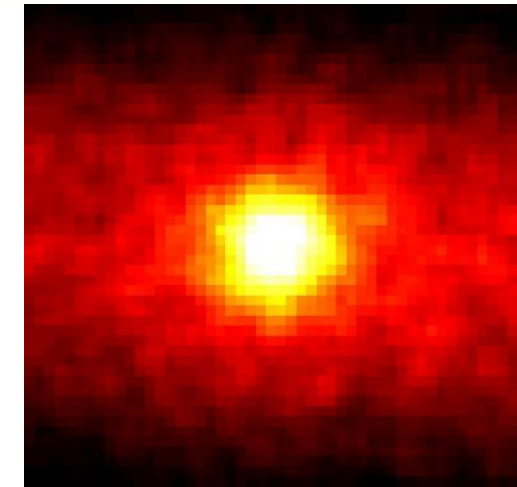
$$\phi_\nu = S / 13 \text{ MeV} \approx 6.7 \times 10^{10} \text{ neutrinos/cm}^2\text{s}$$

These are all electron neutrinos (because the p-p chain involves electrons).

PROBLEM: Only about one-thirds of this flux of neutrinos is actually observed.

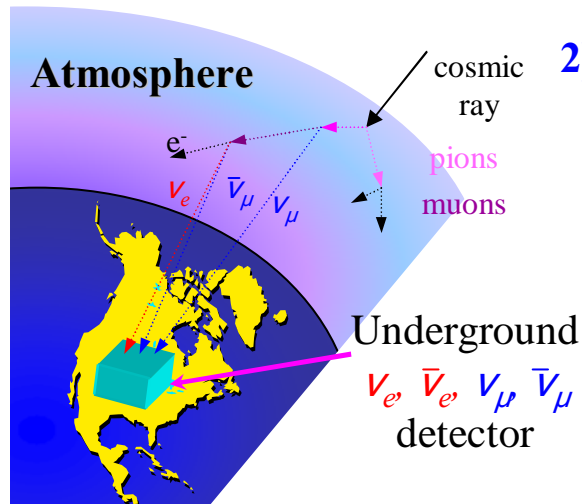
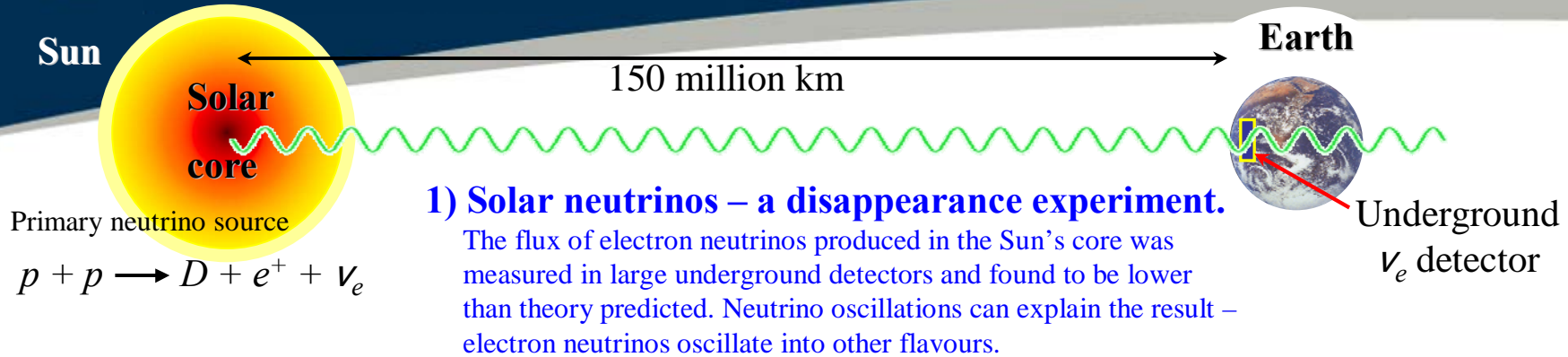
SOLUTION: The MSW Effect

Neutrinos interact with the matter in the Sun and “oscillate” into one of the other neutrino “flavours” – Neutrino matter oscillations – electron neutrinos get converted to muon or tau neutrinos and these could not be detected by the early neutrino detectors!

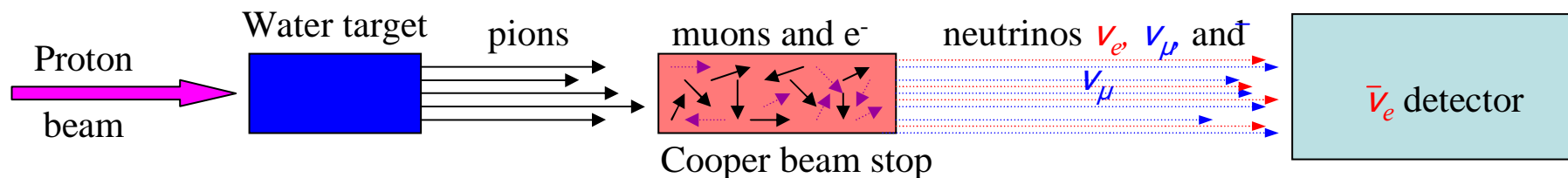




Three Types of Evidence for Neutrino Oscillations



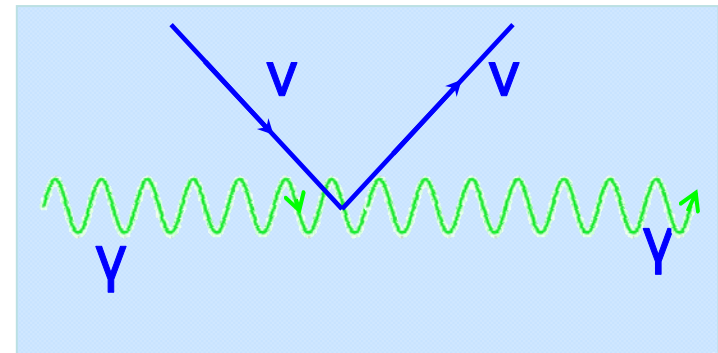
3) LSND – an appearance experiment. Positive pions decay at rest into positive muons, which then decay into muon neutrinos, positrons and electron neutrinos. Negative pions decay and produce electron antineutrinos, but the rate is almost negligible. A giant liquid-scintillator neutrino detector located 30 metres downstream looks for the appearance of electron antineutrinos as the signal that the muon antineutrinos have oscillated.





- Neutrino Landau Damping – resonance between neutrinos & plasma turbulence
- Neutrino Cooling: Stellar Evolution, Neutron Star Cooling
 - In dense stellar interiors escaping neutrinos carry off excess energy.
- Kinetic Theory of Neutrino Plasma Coupling

↳ Neutrino Landau Damping
➤ Turbulent Plasma; Relativistic Electron Plasma Waves are resonant with neutrinos ➡ neutrinos damp waves.



- Neutrino Luminosity: $L_\nu = 10^{42}$ ergs/sec
- Interacting with Plasma: $T_e = 10$ keV, $n_e = 10^{28}$ cm⁻³
- Neutrino Landau Damping Cooling Time: $\tau_c = 10^5$ Yrs
- Compton production of neutrino pairs + photon–neutrino scattering:
 $\tau_c = 10^7$ Yrs



Neutrino Astrophysics

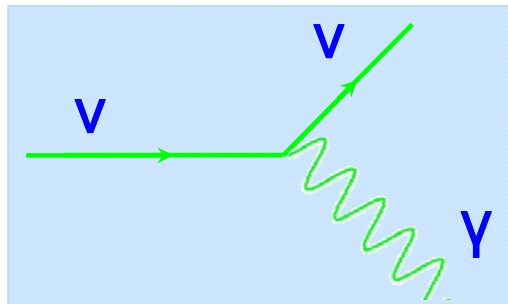
- Magnetic Field Effects:

- Filamentation Instability

Breaking up of uniform beam of neutrinos

- Transverse photon emission

- γ -rays



Pulsar driven bow shock in the interstellar medium

- New asymmetric ponderomotive force $\propto \underline{P}_\nu \cdot \underline{B}$
 - Radially uniform emission of neutrinos
 - Exerts a macroscopic force
 - The force is in the opposite direction to the magnetic field
 - Can contribute to birth velocity of pulsars

Natural Plasma Laboratories

