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Mechanisms in Materials**

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**Electronic stopping of ionic projectiles in ice and metals**

J. Kohanoff  
*The Queen's University of Belfast  
United Kingdom*



# **Electronic stopping of ionic projectiles in ice and metals**

Jorge Kohanoff

Atomistic Simulation Centre  
Queen's University Belfast



**Trieste, 13 April 2010**



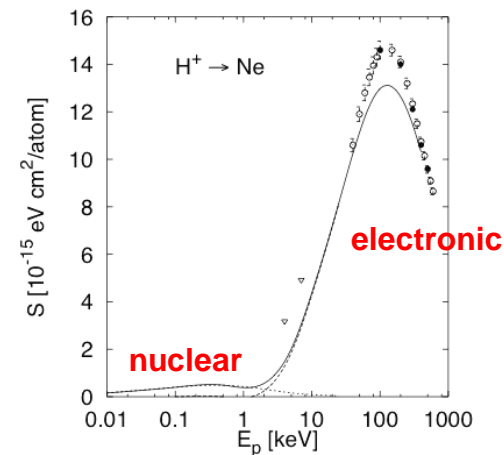
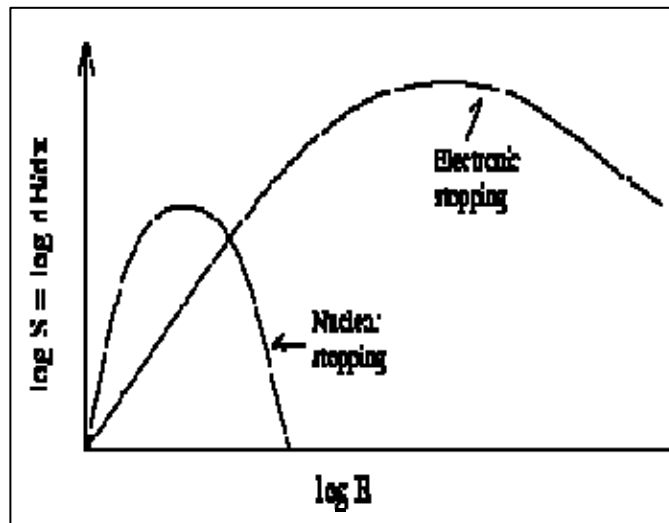
# **Ionic projectiles**

# Ionic projectiles

## electronic vs nuclear stopping

- Stopping power: energy deposited per unit length ( $S=dE/dx$ )
  - **Nuclear:** dominates at low energies
  - **Electronic:**
    - **Metals:** for  $v \rightarrow 0$ ,  $S \sim v$  (e-h pairs). Decrease at large  $v$  (Bethe)
    - **Insulators:** Threshold due to band gap  $v_{th} \approx 0.1-0.2$  a.u.

[First-principles on LiF: M. Pruneda et al., Phys. Rev. Lett. **99**, 235501 (2007)]



Schiefermuller et al., Phys. Rev. A **48**, 4467 (1993)

Cabrera-Trujillo et al., Phys. Rev. Lett. **84**, 5300 (2000)

# Ionic projectiles

## Regions of interest for biomolecular systems

- Water is an electronic insulator --  $E_g$  (water)  $\sim 10$  eV.
  - Threshold effects separate nuclear from electronic stopping. Low and high energy regimes can be treated separately
    - **Low energy ( $v < 0.1$  a.u., or 4 keV for C): adiabatic regime (GS electrons)**
    - **High energy ( $v > 0.1$  a.u.): sudden regime (purely electronic dynamics)**
- Depending on the energy levels of the projectile:
  - Electronic excitation, capture and ionization by low-energy ions is possible.
    - **Intermediate energy: impact fragmentation coexists with electronic excitation. Combined electron-nuclear dynamics required.**

# Computational methods

## Real-time electronic dynamics

- Sudden regime

- **Real-time electronic dynamics** via **TDDFT**
- Adiabatic GGA (**AGGA**) approximation to time-dependent XC
- **Fixed nuclei**
- Incident ion treated as a **moving external potential**
- **Channeling** to avoid direct impact

- **Time-dependent Kohn-Sham equations implemented in SIESTA**

- [A. Tsolakidis, D. Sanchez-Portal and R. M. Martin, Phys. Rev. B 66, 235416 (2002)]

$$i\hbar \frac{\partial \Psi_i^{KS}}{\partial t} = H \Psi_i^{KS}$$

with Kohn-Sham orbitals expanded in atomic orbital basis

$$\Psi_i^{KS}(r, t) = \sum_{\mu} c_i^{\mu}(t) \phi_{\mu}(r)$$

$$i\hbar \frac{\partial \mathbf{c}}{\partial t} = \mathbf{S}^{-1} \mathbf{H} \mathbf{c}$$

# Computational methods

## Ehrenfest dynamics

- Sudden regime

- **Real-time electronic dynamics** via **TDDFT**
- Adiabatic GGA (**AGGA**) approximation to time-dependent XC
- **Classical MD for the nuclei**
- Incident ion treated as **another classical particle**
- **No channeling restrictions**

- **Ehrenfest equations implemented into SIESTA**

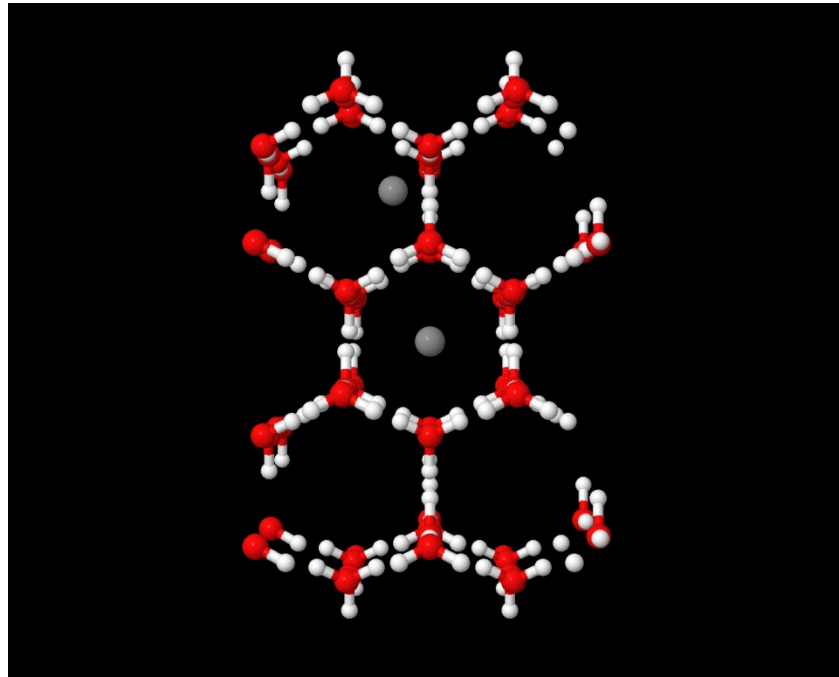
[D. Sanchez-Portal, J. Kohanoff and E. Artacho (unpublished)]



Leap-frog  
Crank-Nic.  
Projections

# Electronic stopping in ice

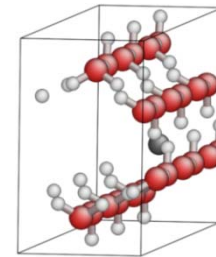
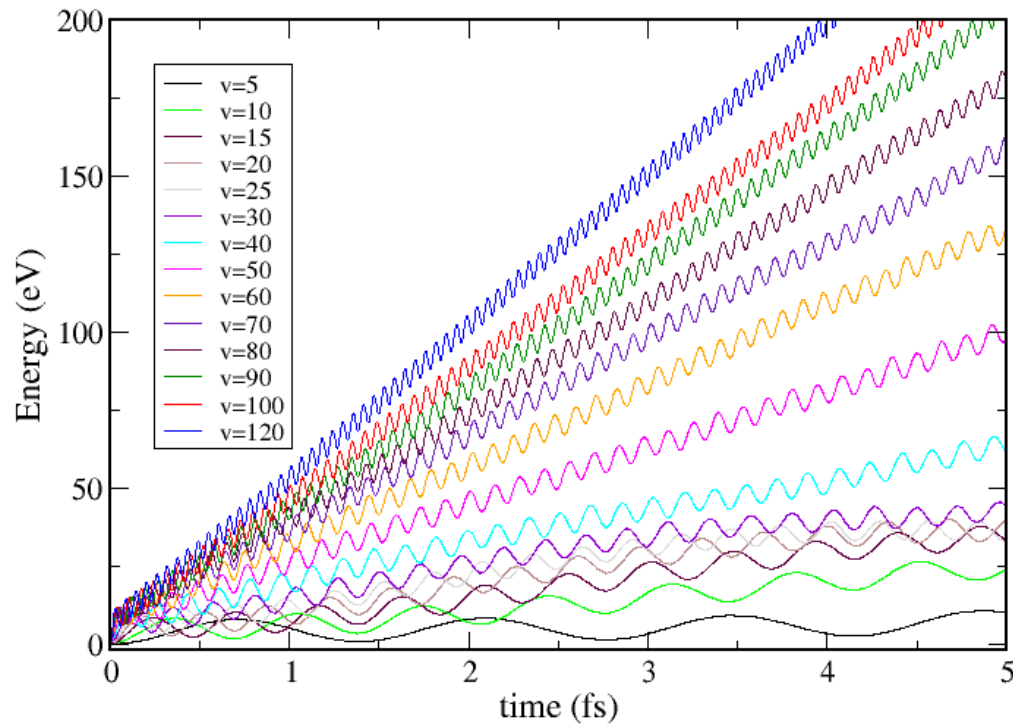
$H^+$  shooting through channels in hexagonal ice  
(24 and 40 water molecules – 3 and 5 units)





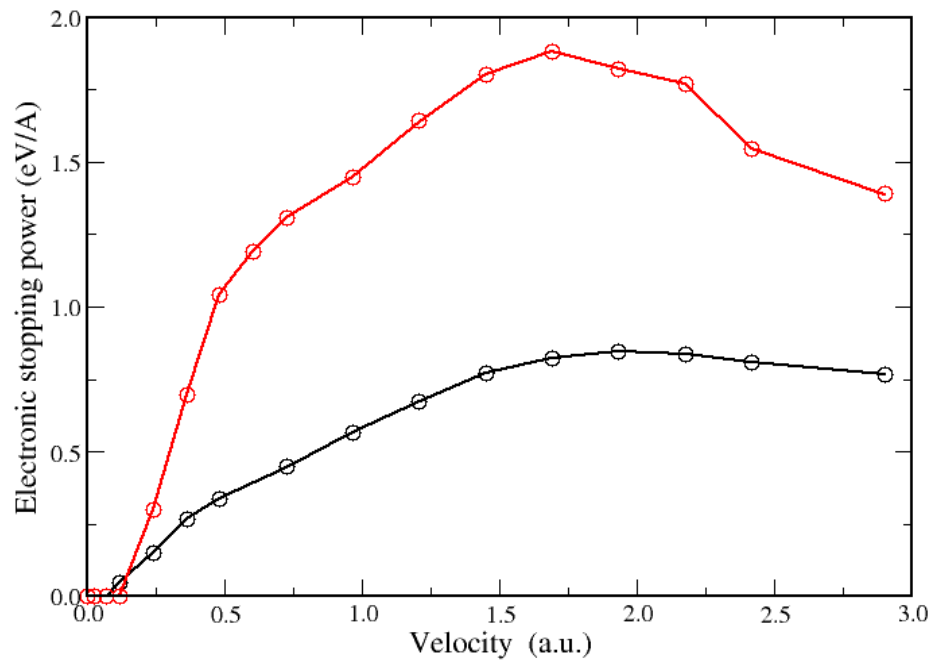
# Non-adiabatic stopping channeling of H<sup>+</sup> through hexagonal ice

Energy transferred to electrons



# Electronic stopping power

## channeling of H<sup>+</sup> through hexagonal ice



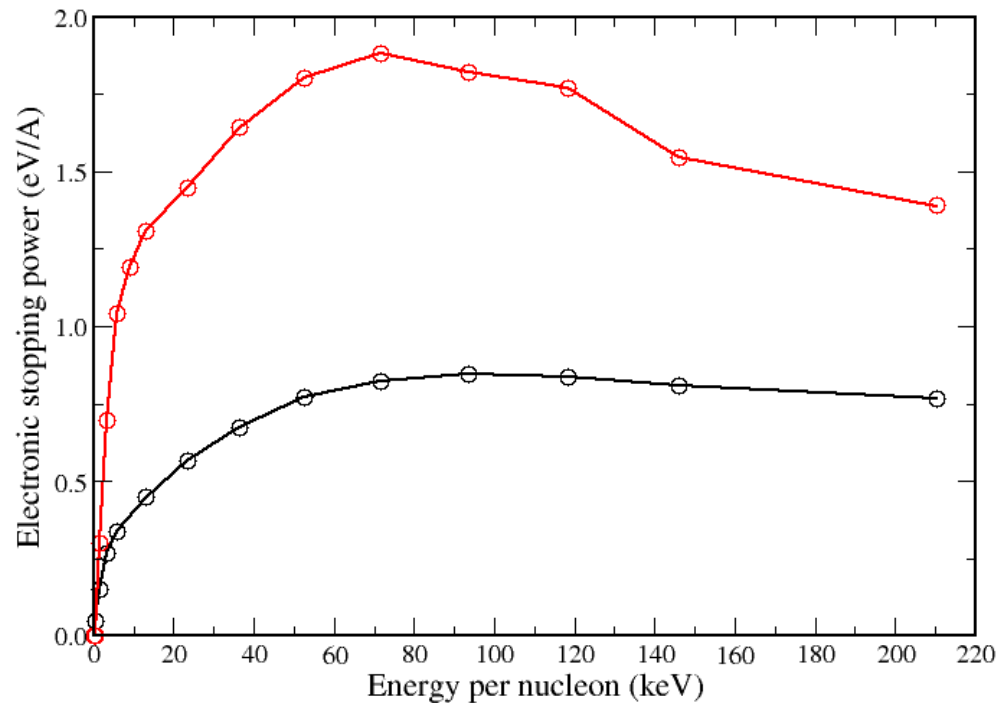
- $S_e$  through center of channel is about half that of LiF
- Channels in ice are more open
- $S_e$  increases by a factor of 3 when proton travels closer to water molecules

# Electronic stopping power

## channeling of H<sup>+</sup> through hexagonal ice

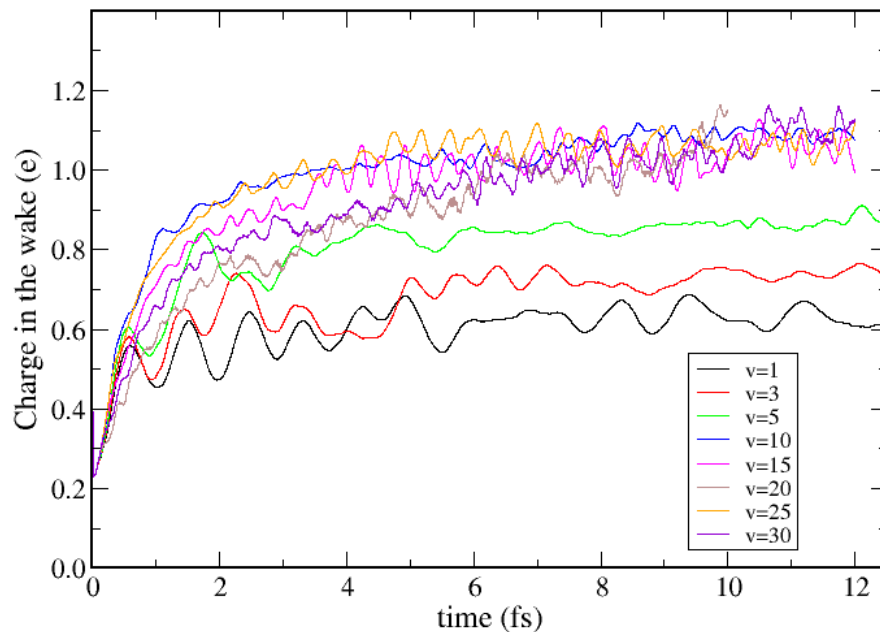
Experiment: P. Bauer et al., NIMB 93, 132 (1994)

**Peak at 90 keV/nucleon**



# Non-adiabatic stopping

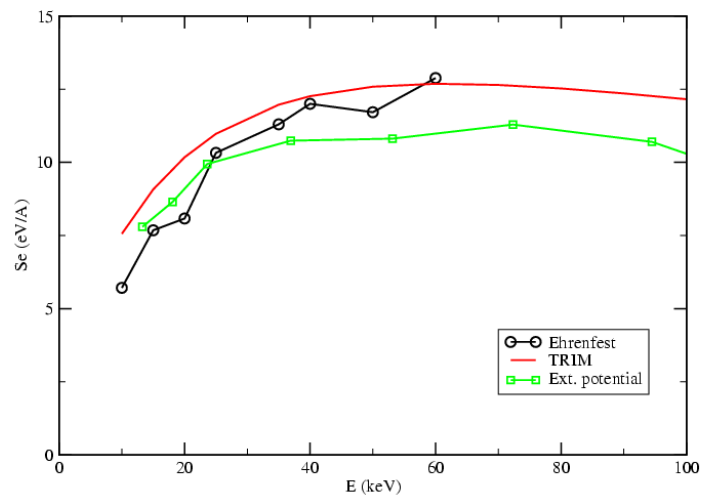
## Charge state of the proton



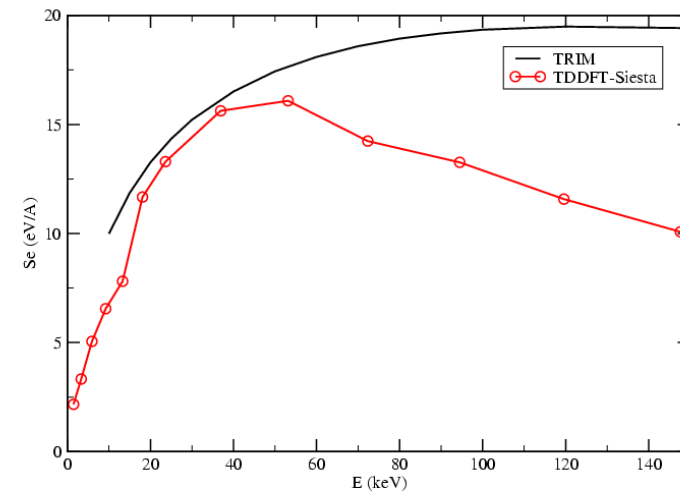
- At low speed the proton drags the electronic charge with it, forming H.
- At higher speed, electrons respond to the proton, but too late, creating a wake.
- Eventually, the electronic wake detaches and the proton travels as  $H^+$ .

# Electronic stopping in metals

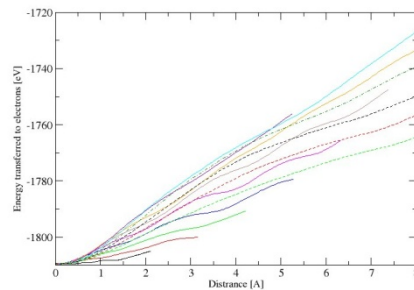
Electronic stopping of protons in Al



Electronic stopping in Cu



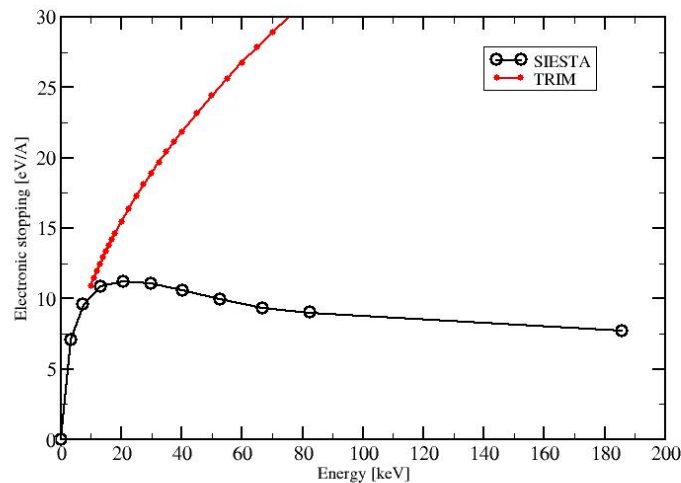
Stopping of protons in Al



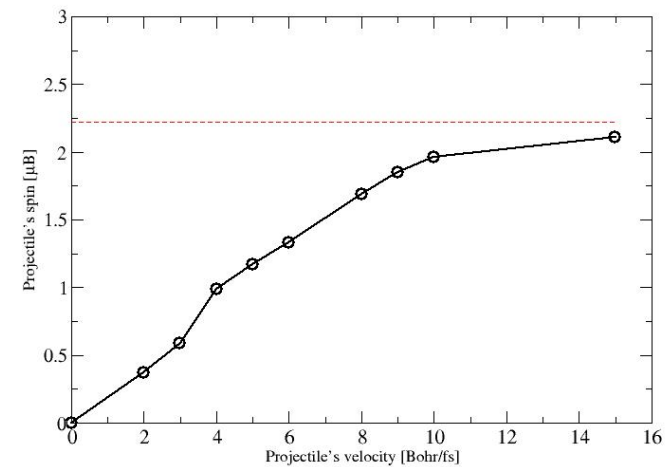
SRIM stopping tables reproduced !

# Nuclear materials: stopping of Fe in Fe

Electronic stopping of an interstitial Fe in bulk Fe



Magnetization of the projectile



It is possible to compute  $S_e$  for heavier projectiles  
FM vs PM: influence of EDOS apart from  $\rho$

