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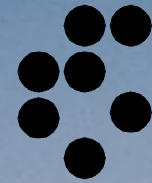
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**Joint ICTP-IAEA Workshop on Nuclear Data for Science and
Technology: Analytical Applications**

8 - 12 November 2010

The k₀-method of NAA: role of reference materials

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The k_0 -method of NAA: Optimization at the JSI, Slovenia

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Introduction



- k_0 -standardization method of NAA was launched in the 1970s
- **SINGCOMP** program: 1987 written for VAX
- **KAYZERO/SOLCOI** program: 1994, 1996, 2003 written for **DOS** and in 2004 written for **Windows**
- KAYZERO library - 144 nuclides (68 elements)
- k_0 -NAA became widespread as a practical analytical tool used to analyse different sample matrices

The k_0 -method of NAA



The k_0 -standardization method in its basic form assumes:

- known burn-up factor,
- constant irradiation conditions,
- well known neutron spectral parameters in particular irradiation channels,
- known neutron fluence gradients,
- absolutely calibrated an HPGe detector,
- calibrated counting geometry and
- negligible neutron self-shielding.

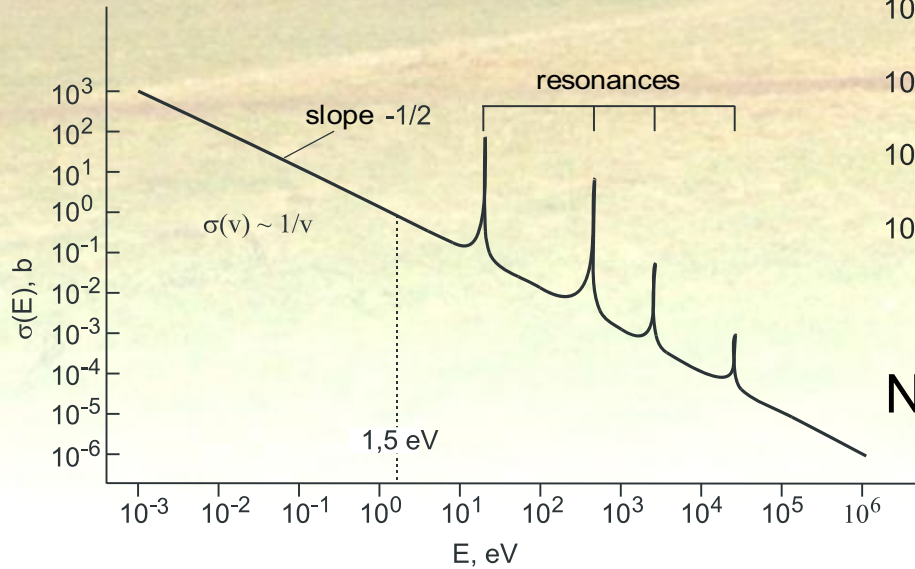
! which may not always be the case !

(n,γ) reaction rate

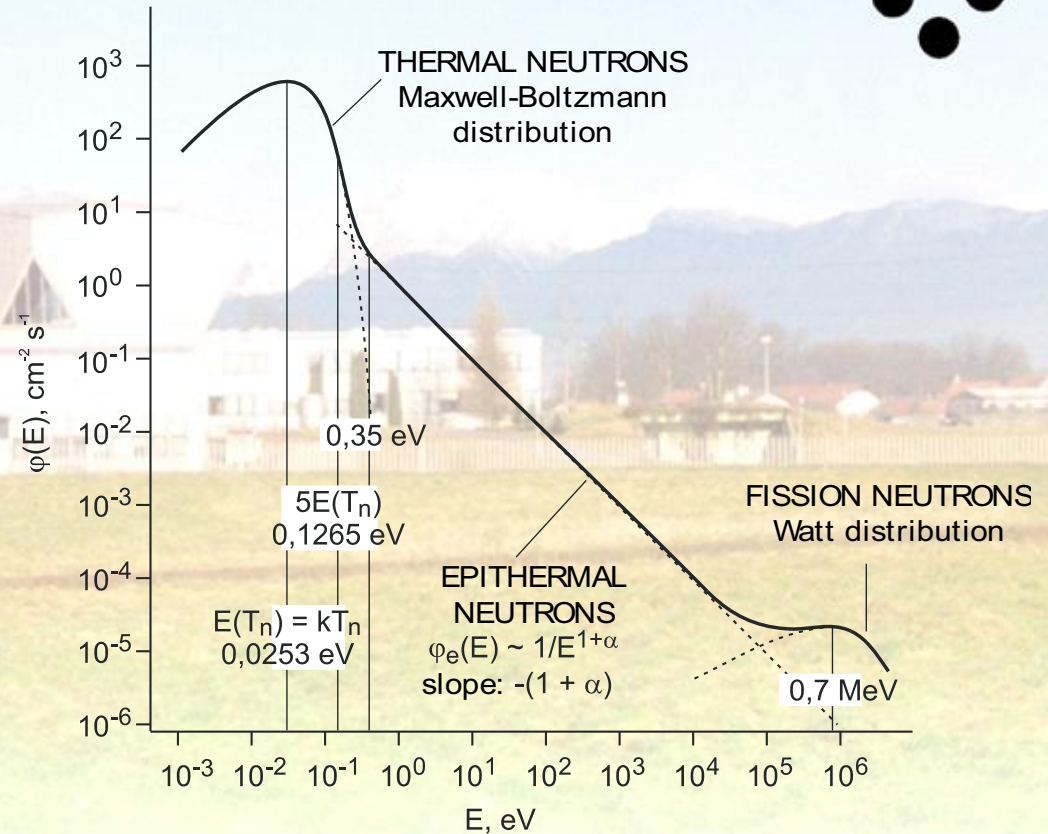


Specific reaction rate per target nuclide

$$R_X = \frac{R}{N_1} = \int_0^{\infty} \sigma(E) \varphi(E) dE$$



Cross-section vs. E ($\sigma(v) \sim 1/v$)



Neutron fluence rate distribution vs. E

k_0 -standardization: KAYZERO/SOLCOI



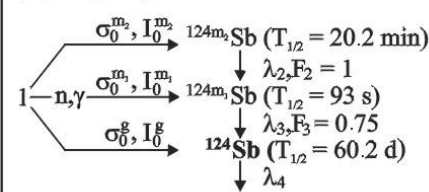
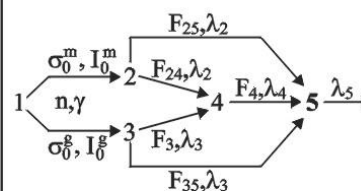
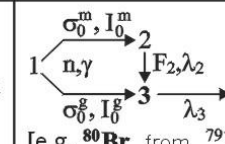
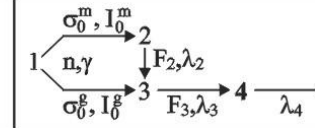
Thermal and epithermal activation

$$\rho_a = \frac{\left(\frac{N_p / t_m}{SDCW} \right)_a}{\left(\frac{N_p / t_m}{SDCW} \right)_{Au}} \frac{1}{k_{0,Au}(a)} \frac{G_{th,Au} f + G_{e,Au} Q_{0,Au}(\alpha)}{G_{th,a} f + G_{e,a} Q_{0,a}(\alpha)} \frac{\epsilon_{p,Au}}{\epsilon_{p,a}}$$

Only epithermal activation

$$\rho_a = \frac{\left[\left(\frac{N_p / t_m}{SDCW} \right)_{Cd} \right]_a}{\left[\left(\frac{N_p / t_m}{SDCW} \right)_{Cd} \right]_{Au}} \frac{1}{k_{0,Au}(a)} \frac{F_{Cd,Au} G_{e,Au} Q_{0,Au}(\alpha)}{F_{Cd,a} G_{e,a} Q_{0,a}(\alpha)} \frac{\epsilon_{p,Au}}{\epsilon_{p,a}}$$

Activation-decay scheme in the k_0 -method of NAA

Type	Activation-decay scheme	Type	Activation-decay scheme
I	$1 \xrightarrow[\sigma_0, I_0]{n, \gamma} 2 \xrightarrow{\lambda_2}$ [e.g. ^{75}As (n, γ) ^{76}As]	Vb	Special case: $\lambda_4 \ll \lambda_2$ and λ_3 [e.g. ^{199}Au from ^{198}Au (n, γ)]
IIa	$1 \xrightarrow[\sigma_0, I_0]{n, \gamma} 2 \xrightarrow{F_2, \lambda_2} 3 \xrightarrow{\lambda_3}$ [e.g. ^{101}Tc from ^{100}Mo (n, γ)]	Vc	Special case: $\lambda_3 \ll \lambda_2$ and λ_4 , $D_2 = D_4 = 0$ [e.g. $^{113\text{m}}\text{In}$ from ^{112}Sn (n, γ)]
IIb	Special case: $\lambda_2 \gg \lambda_3$ and $D_2 = 0$ [e.g. ^{233}Pa from ^{232}Th (n, γ)]	VI	Special case: ^{124}Sb [from ^{123}Sb (n, γ)] after long decay time ($D_2 = D_3 = 0$) 
IIc	Special case: $\lambda_2 < \lambda_3$ and $D_3 = 0$		VIIa
IIId	Special case: measurement of the 140.5 keV line of $^{99}\text{Mo}/^{99\text{m}}\text{Tc}$ [from ^{98}Mo (n, γ)]	VIIb	Special case: $F_2 = 0$ [e.g. ^{125}Sb from ^{124}Sn (n, γ)]
IIIa	$1 \xrightarrow[\sigma_0, I_0]{n, \gamma} 2 \xrightarrow{F_2, \lambda_2} 3 \xrightarrow{F_3, \lambda_3} 4 \xrightarrow{\lambda_4}$ [e.g. ^{97}Nb from ^{96}Zr (n, γ)]	VIII	
IIIb	Special case: $F_{24} = 0$		
IIIc	Special case: $\lambda_3 \gg \lambda_2$ and $\lambda_4, D_3 = 0$ $F_3 = 1, F_2 + F_{24} = 1$ [e.g. ^{105}Rh from ^{104}Ru (n, γ)]		
IVa			
IVb	Special case: $\lambda_2 \gg \lambda_3$ and $D_2 = 0$ [e.g. ^{60}Co from ^{59}Co (n, γ)]		
IVc	Special case: $\lambda_2 < \lambda_3$ and $D_3 = 0$		
Va			



Nuclear research reactor TRIGA Mark II (250 kW)

- Short and long irradiation in the CC:

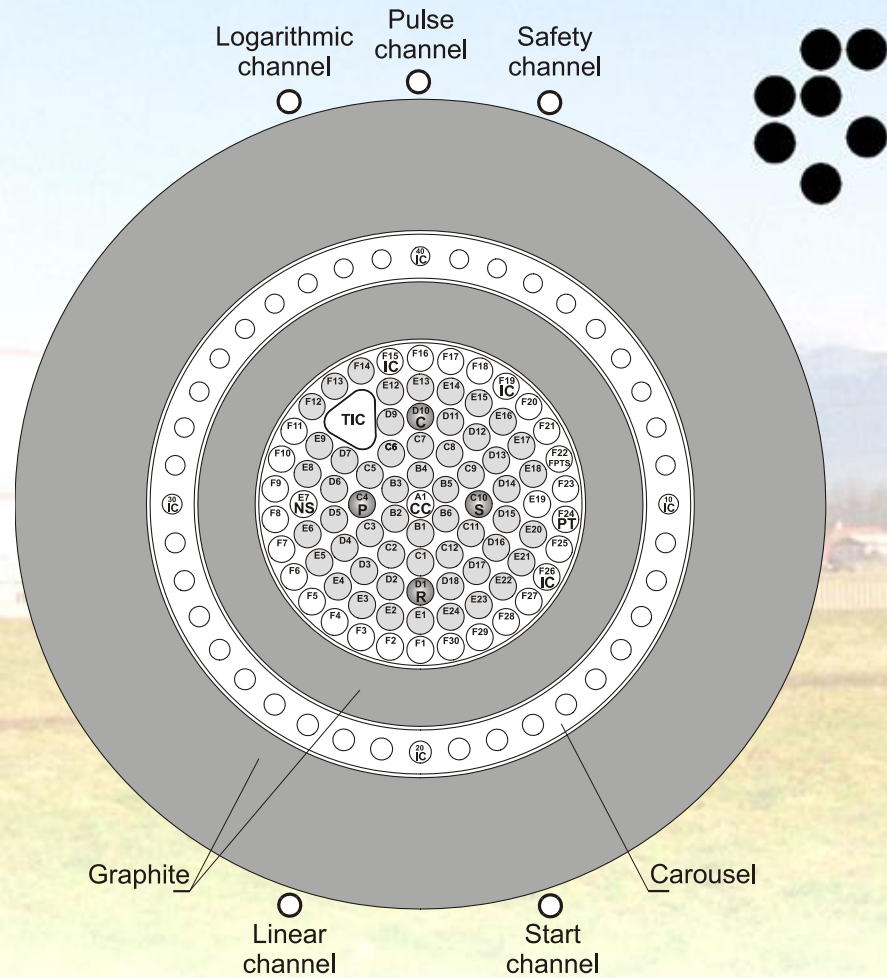
$$\varphi_{th} \sim 10 \cdot 10^{12} \text{ cm}^{-2} \text{ s}^{-1}$$

- Short irradiation in the PT and in the FPTs (up-to 30 min.)

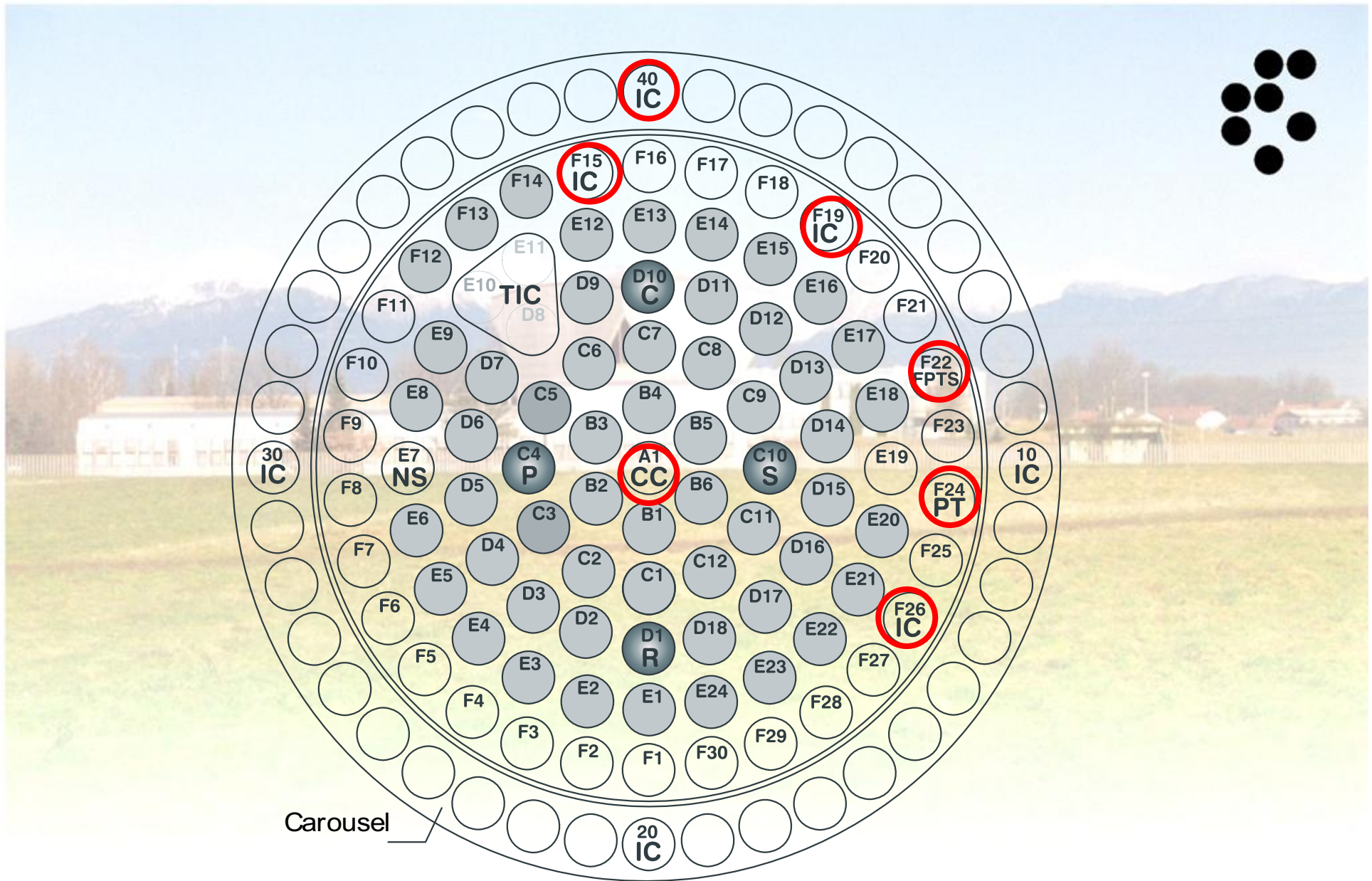
$$\varphi_{th} \sim 3.5 \cdot 10^{12} \text{ cm}^{-2} \text{ s}^{-1}$$

- Long irradiation in the IC-40 (typically 20 hours)

$$\varphi_{th} \sim 1.1 \cdot 10^{12} \text{ cm}^{-2} \text{ s}^{-1}$$



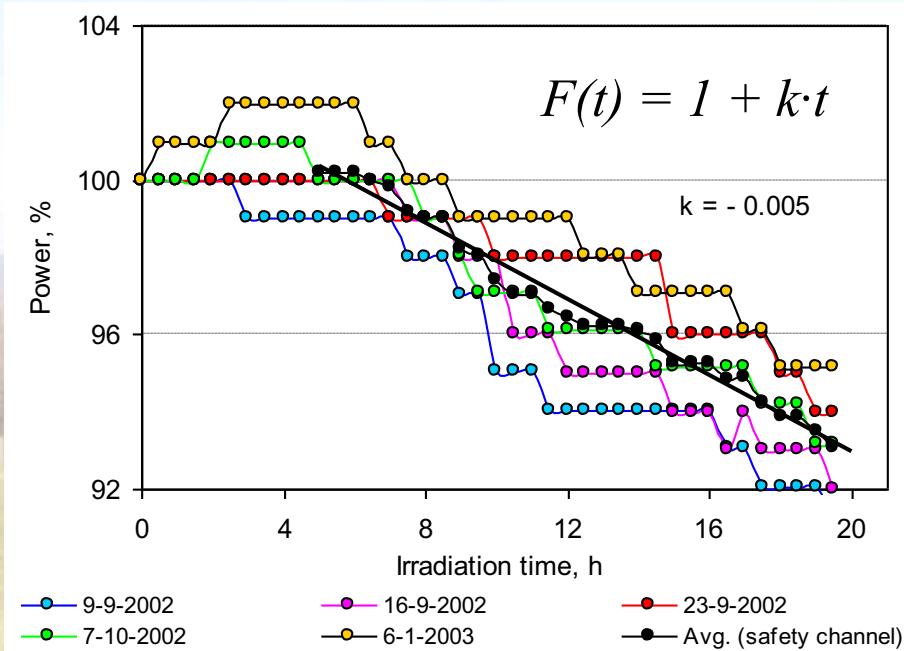
- Fuel elements 20 % U-235
- Control rods
- Neutron source
- Irradiation channels
- Fast pneumatic transfer system
- Pneumatic transport tube channel
- Central channel
- Triangular channel



Horizontal section of the TRIGA Mark II reactor (core No. 176)

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Temporal variation of the neutron fluence rate in the IC-40 channel

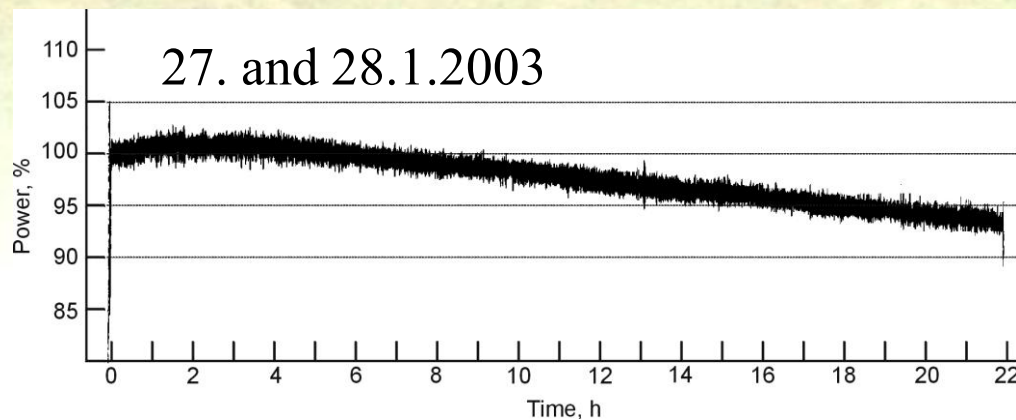


$$S' = \int_0^{t_{irr}} F(t) \lambda e^{\lambda(t-t_{irr})} dt$$

$$S' = S \left(1 + k \cdot t_{irr} \left(\frac{1}{S} - \frac{1}{\lambda \cdot t_{irr}} \right) \right)$$

$$F(t) \equiv 1 \Rightarrow S = 1 - e^{-\lambda t_{irr}}$$

Correction factor for saturation in the carousel, especially in the IC-40 position for continuous irradiation for 20 h (F_{sat})



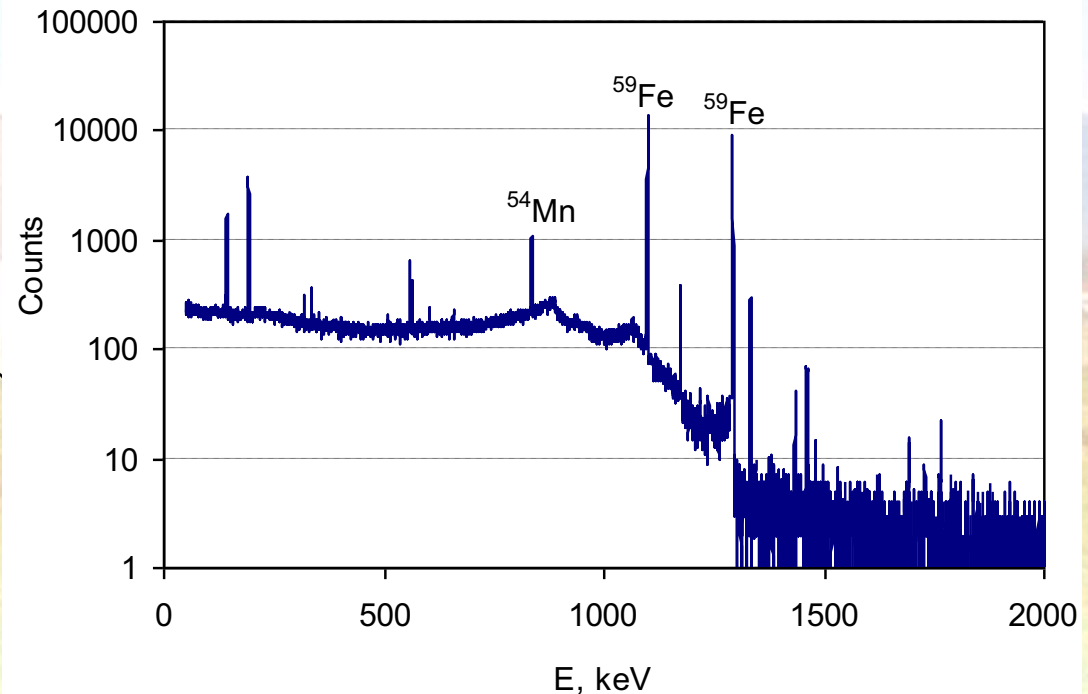
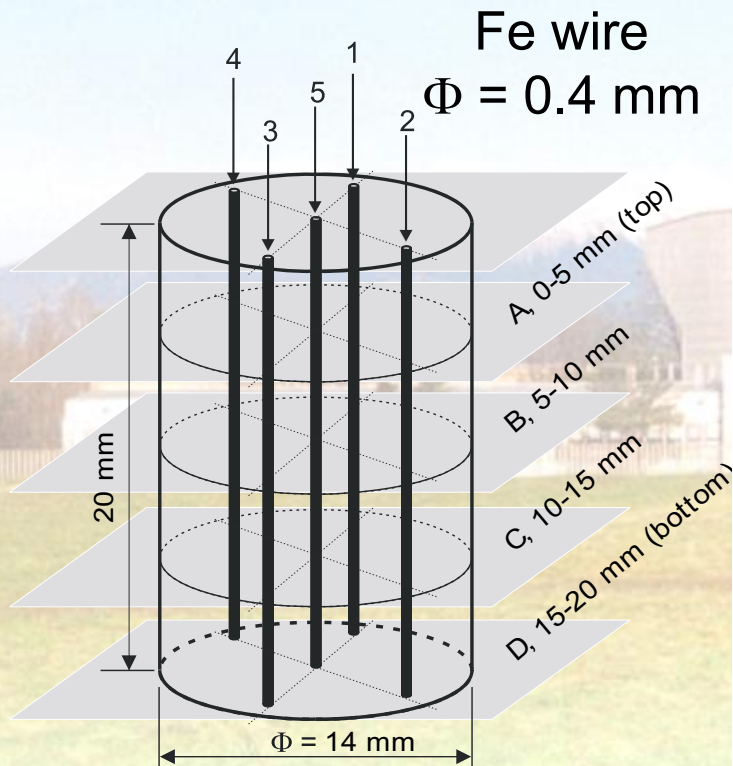
$$F_{sat} = \left(\frac{S'_c S_a}{S'_a S_c} - 1 \right) \cdot 100$$

Correction factor for saturation (F_{sat}) in the IC-40 channel



El.:	Nuclide	$T_{1/2}$ (min)	Activ. type	F_{sat} (%)			
				5 h	10 h	15 h	20 h
Au	¹⁹⁸ Au	3880.8	I	0.00	0.00	0.00	0.00
Na	²⁴ Na	0.000337; 897.6	IVb	0.04	0.14	0.32	0.56
K	⁴² K	741.6	I	0.05	0.18	0.40	0.70
Ca	⁴⁷ Ca	6531.84	I	0.00	-0.02	-0.04	-0.07
	⁴⁷ Sc	6531.84; 4822.56	IIa	-0.42	-0.84	-1.26	-1.68
	⁴⁹ Ca	8.718	I	1.12	2.29	3.42	4.50
Fe	⁵⁹ Fe	64080	I	-0.01	-0.04	-0.09	-0.16
Co	^{60m} Co	10.467	I	1.10	2.27	3.40	4.48
	⁶⁰ Co	10.467; 2772383	IVb	-0.01	-0.04	-0.10	-0.17
Zn	⁶⁵ Zn	351792	I	-0.01	-0.04	-0.10	-0.17
	^{69m} Zn	825.6	I	0.04	0.16	0.35	0.62
	⁷¹ Zn	2.45	I	1.19	2.37	3.49	4.57
Zr	⁹⁵ Zr	92188.8	I	-0.01	-0.04	-0.09	-0.16
	⁹⁵ Nb	92188.8; 5196; 50356.8	IIIa	-0.42	-0.86	-1.30	-1.75
	⁹⁷ Zr	1004.4	I	0.03	0.12	0.28	0.48
	⁹⁷ Nb	1004.4; 0.878; 72.1	IIIa	-0.25	-0.27	-0.17	-0.01
	^{97m} Nb	1004.4; 0.878	IIa	0.03	0.12	0.27	0.47
Eu	^{152m} Eu	558.72	I	0.07	0.26	0.56	0.97
	¹⁵² Eu	7121622.405	I	-0.01	-0.04	-0.10	-0.17
	¹⁵⁴ Eu	46; 4519653	IVb	-0.01	-0.04	-0.10	-0.17
U	²³⁹ U	23.45	I	0.95	2.12	3.25	4.33
	²³⁹ Np	23.45; 3394.08	IIb	0.00	0.01	0.01	0.02

Axial and radial gradients of the neutron fluence rate



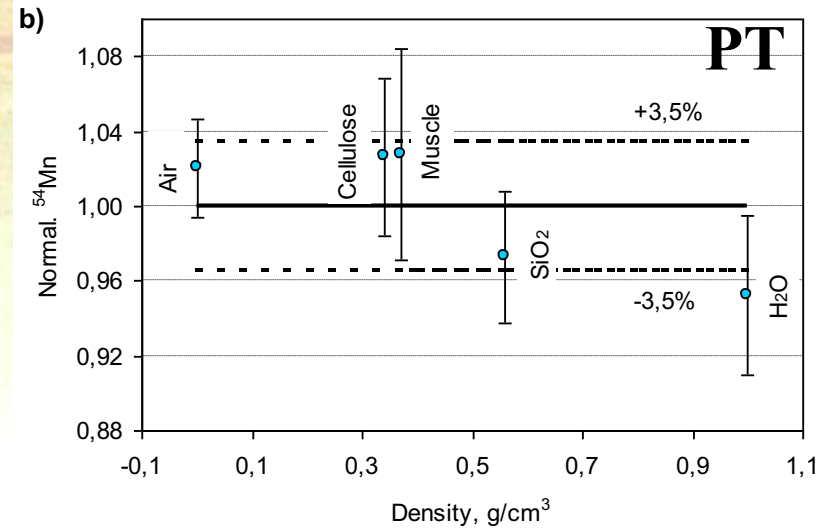
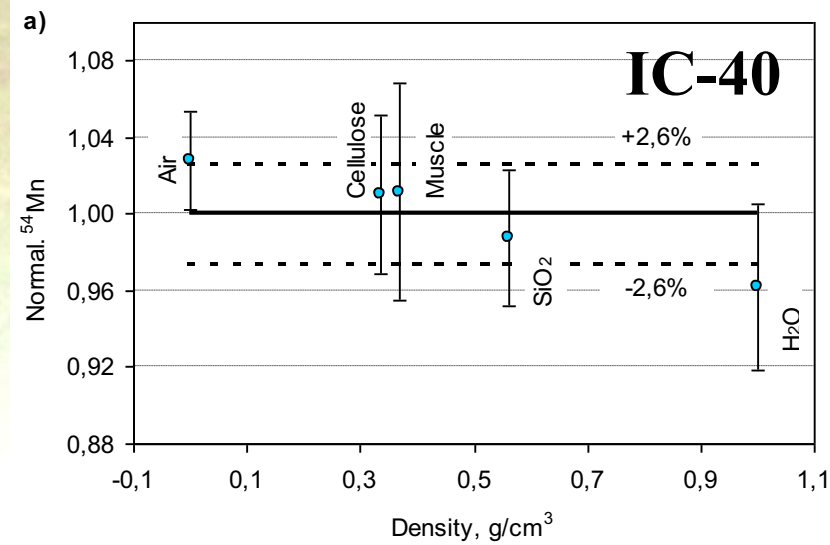
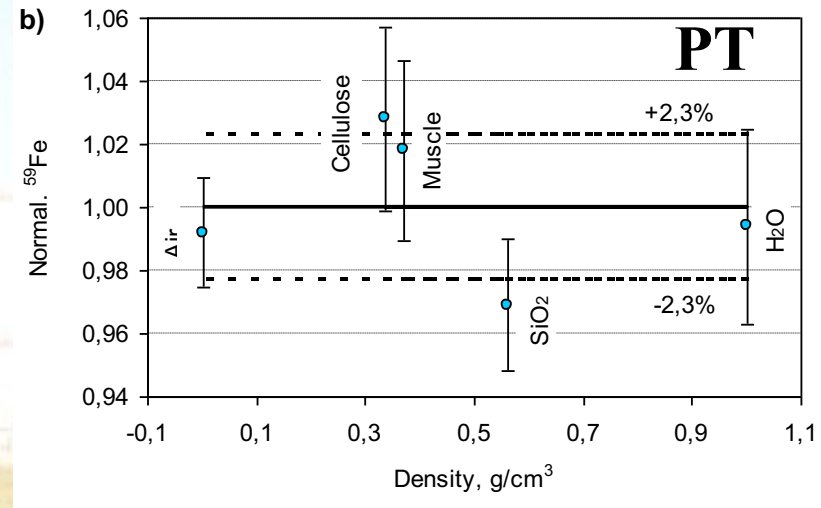
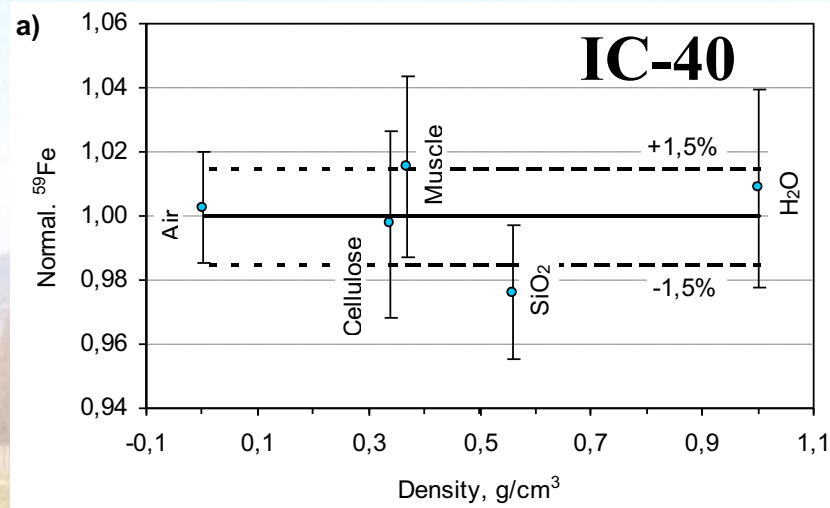
Thermal neutron fluence rate: $^{58}\text{Fe}(n,\gamma)^{59}\text{Fe}$

Fast neutron fluence rate: $^{54}\text{Fe}(n,p)^{54}\text{Mn}$

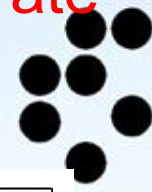
From the same γ spectrum !!!

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Normalized specific activities of ^{59}Fe vs. density for five matrices in the IC-40 and in the PT channels

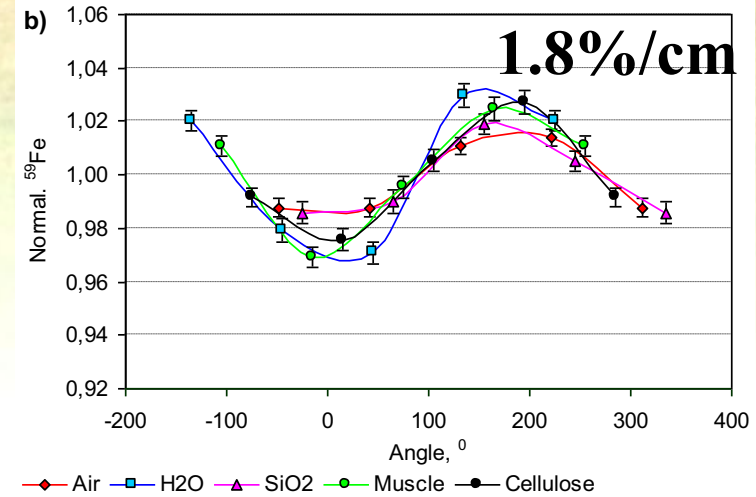
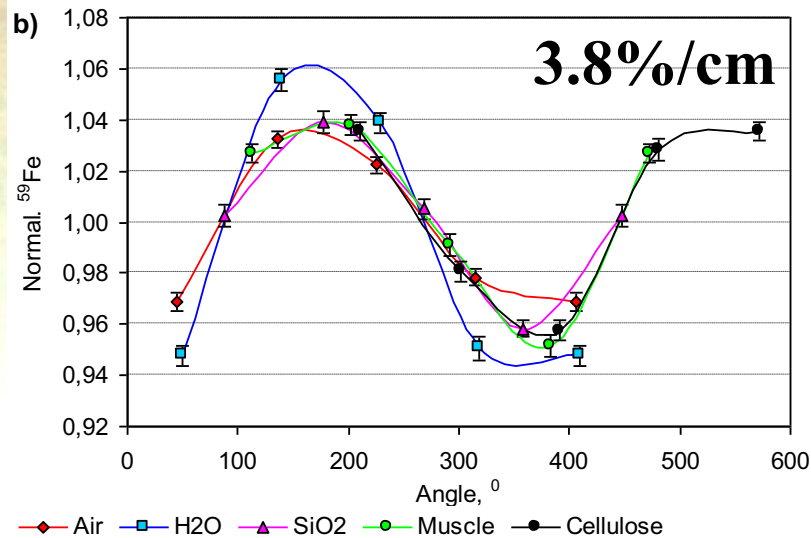
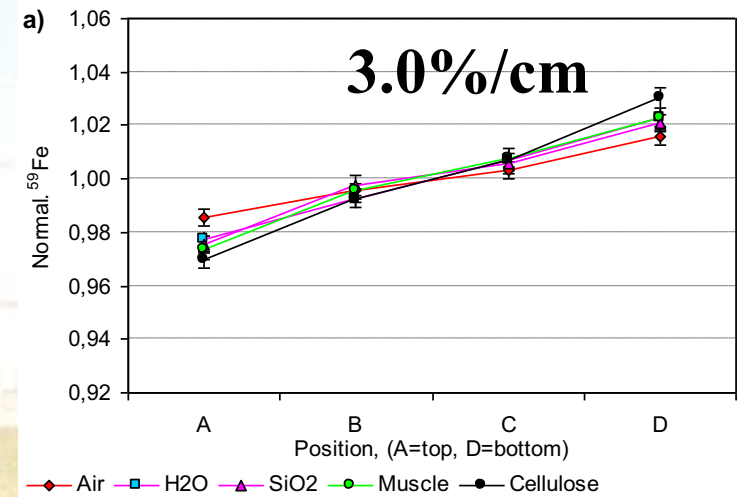
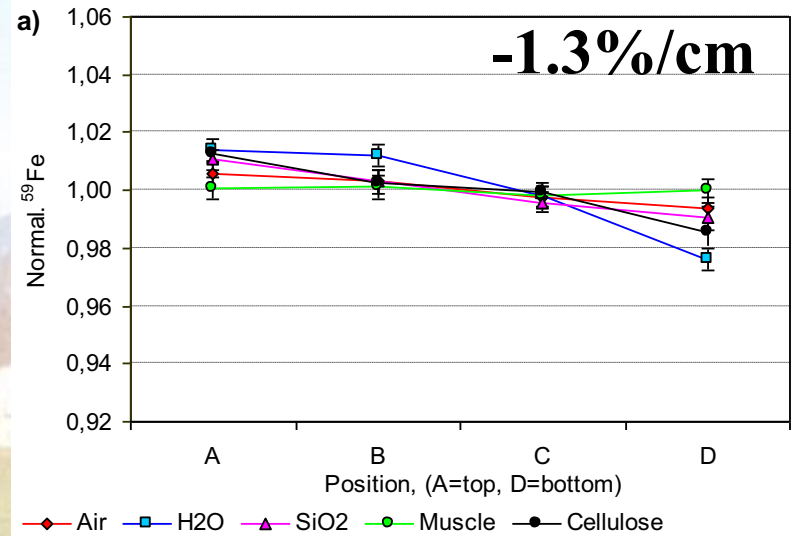


Axial and radial gradients of the thermal neutron fluence rate in different samples



PT

IC-40



Specific activities and G_{th} factors



Sample	PT			IC-40		
	Normal. ^{59}Fe	rsd, %	Total rsd, %	Normal. ^{59}Fe	rsd, %	Total rsd, %
Air	0.992	2.57	2.31	1.002	1.69	1.50
Cellulose	1.028	3.17		0.998	2.86	
Muscle	1.018	3.30		1.015	2.73	
SiO ₂	0.969	2.77		0.976	2.08	
H ₂ O	0.994	4.85		1.009	2.99	

G_{th} - not characteristic of nuclei, but dependent on **dimensions** and **composition** of the sample

Cellulose
Muscle
H₂O

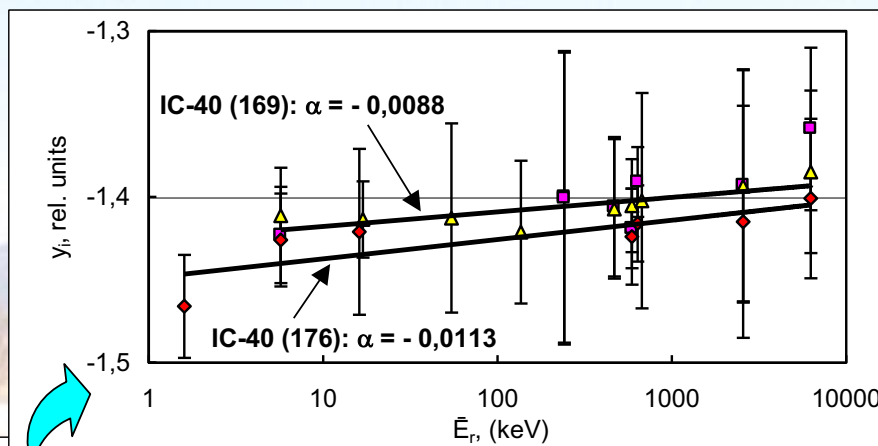
$G_{th,org} = 1.01$

$G_{th,inorg} = 0.97$

SiO₂

Spectral parameters of the neutron fluence rate:

f and α



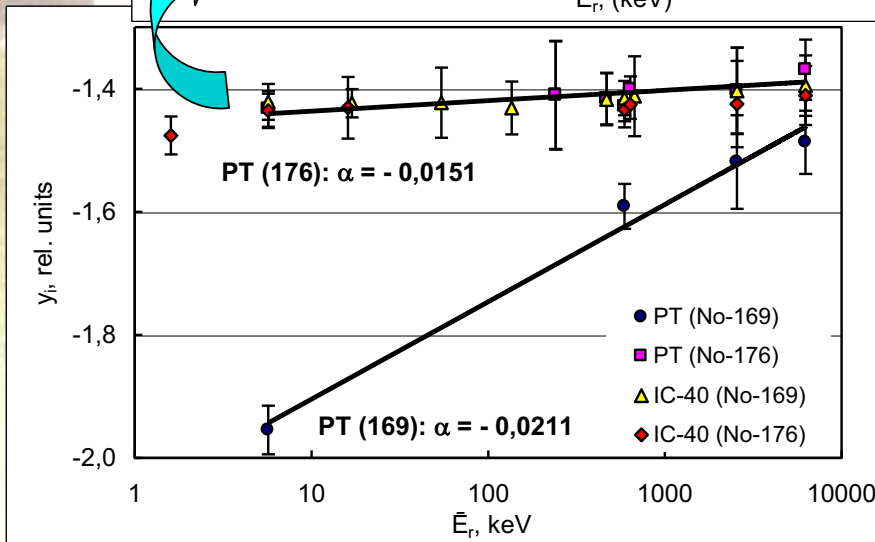
$$y_i = -\alpha \log \bar{E}_{r,i} - \log \left[(F_{Cd,i} R_{Cd,i} - 1) Q_{0,i}(\alpha) G_{e,i} / G_{th,i} \right]$$

$$y_i = -\alpha x_i - b_i$$

$$\alpha = - \frac{\sum_{i=1}^N x_i y_i - \frac{\sum_{i=1}^N x_i \sum_{i=1}^N y_i}{N}}{\sum_{i=1}^N (x_i)^2 - \frac{(\sum_{i=1}^N x_i)^2}{N}}$$

$$b = - \frac{1}{N} \left[\sum_{i=1}^N y_i + \alpha \sum_{i=1}^N x_i \right]$$

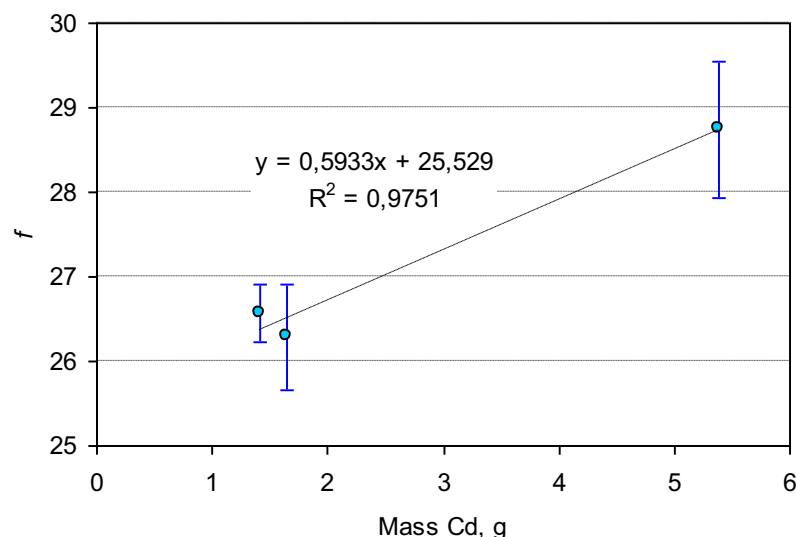
$$f = Q_{0,r}(\alpha) (F_{Cd,r} R_{Cd,r} - 1) \frac{G_{e,r}}{G_{th,r}}$$



Core No.	Irr. channel	Monitors Cd-ratio method	f	α
169	PT 13.6.2000	^{198}Au - ^{69m}Zn - ^{65}Zn - ^{95}Zr	31.78 ± 0.71	-0.0211 ± 0.0059
	IC-40 8.3.2001	^{198}Au - ^{60}Co - ^{56}Mn - ^{101}Tc - ^{233}Pa - ^{239}Np - ^{69m}Zn - ^{65}Zn - ^{95}Zr	27.34 ± 0.43	-0.0088 ± 0.0062
176	PT 3.4.2002	^{198}Au - ^{59}Fe - ^{56}Mn - ^{99}Mo - ^{99m}Tc - ^{69m}Zn - ^{65}Zn - ^{95}Zr	28.03 ± 0.81	-0.0151 ± 0.0068
	IC-40 16.4.2002	^{198}Au - ^{59}Fe - ^{116m}In - ^{176m}Lu - ^{69m}Zn - ^{65}Zn - ^{95}Zr	28.74 ± 0.81	-0.0113 ± 0.0046

Zr, Au, Zn, Co, U, Mn,
Mo, Th, In, Fe, Lu
(foils, wires, alloys)

Correction factor for inaccuracy in the determination of parameter f by “Cd-ratio for multi-monitor” method



IC-40 channel: $\alpha = - 0.0113$;

$f = 28.74$ (5.39 g Cd); $f_{corr} = 26.57$ (1.41 g Cd)

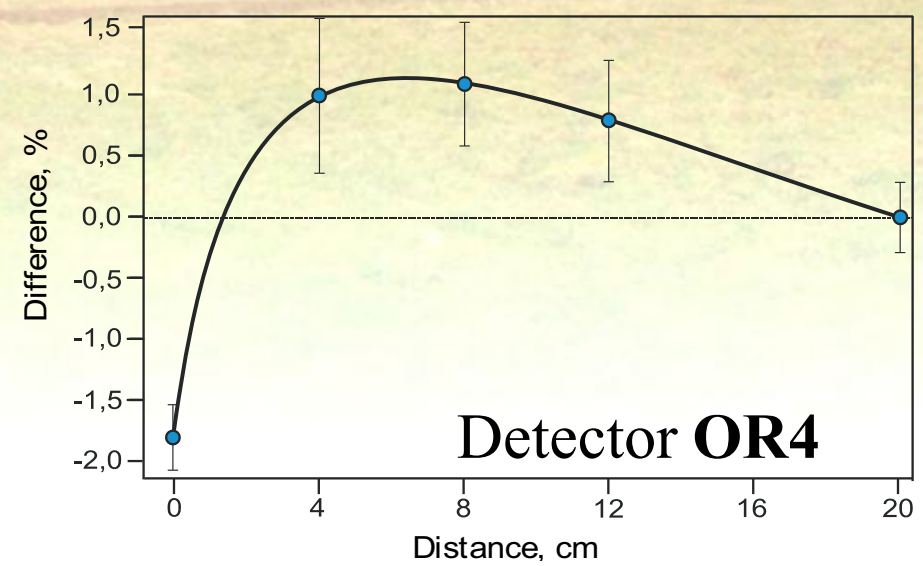
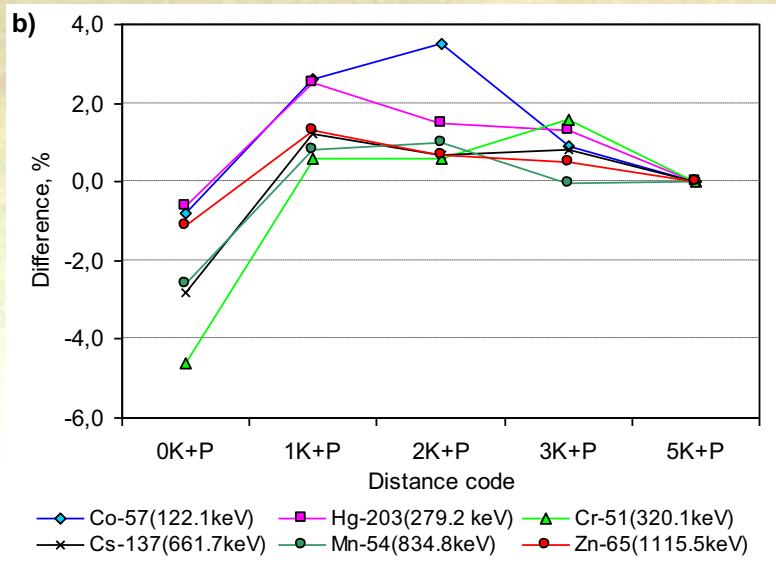
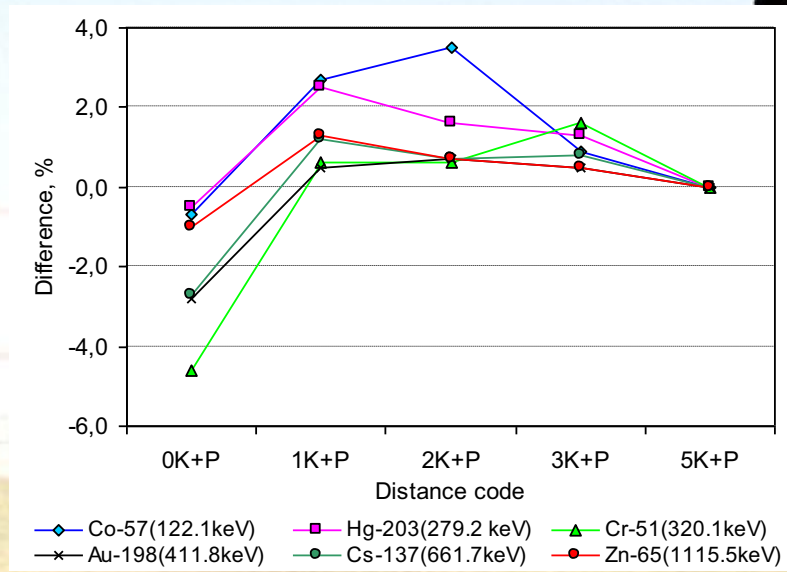
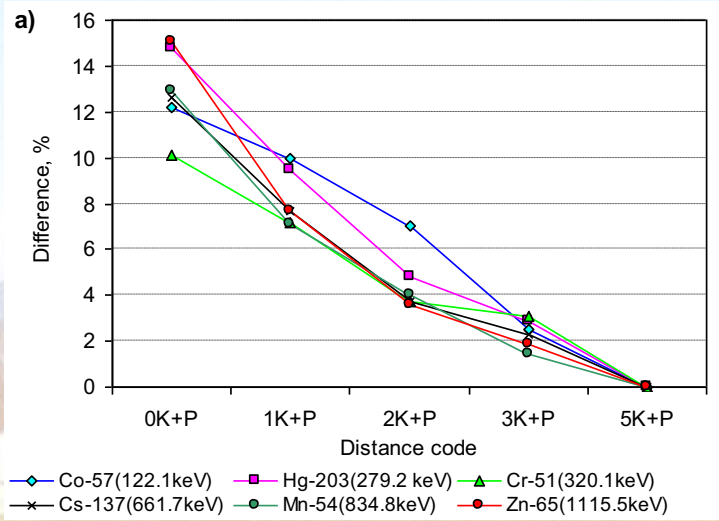
El.:	Nuclide	Q_0	\bar{E}_r , eV	$Q_0(\alpha)$	F_{masaCd} (%)
Au	^{198}Au	15.71	5.7	16.020	$\equiv 0.00$
Dy	^{165}Dy	0.19	224	0.182	2.87
Cr	^{51}Cr	0.53	7530	0.548	2.77
Zn	^{65}Zn	1.908	2560	2.052	2.37
Zn	^{69m}Zn	3.19	590	3.403	2.04
Zr	^{95}Zr	5.306	6260	5.819	1.53
Rb	^{86}Rb	14.8	839	15.943	0.01
Rb	^{88}Rb	23.3	364	24.883	-0.84
U	^{239}Np	103.4	16.9	106.75	-3.30
Zr	^{97m}Nb	251.6	338	268.69	-4.15

$$q = \frac{G_{th,c}f + G_{e,c}Q_{0,c}(\alpha)}{G_{th,a}f + G_{e,a}Q_{0,a}(\alpha)}$$

$$\frac{\partial q}{\partial f} = \frac{Q_{0,a}(\alpha) - Q_{0,c}(\alpha)}{(f + Q_{0,a}(\alpha))^2}$$

$$F_{masaCd} = \left(\frac{q_{corr} - 1}{q} \right) \cdot 100$$

Geometrical correction factor for absolute calibration of OR4



Correction factor for measuring geometry (F_{geom})



Distance	Detector			
	OR1	OR2	CA1	OR4
0K+P	-7.7 ± 0.9	-4.1 ± 0.2	-6.5 ± 0.8	-1.8 ± 0.3
0.5K+P	-0.8 ± 0.9	$+1.7 \pm 0.9$	$+1.3 \pm 0.7$	$+1.3 \pm 0.7$
1K+P	0.0 ± 0.6	$+1.6 \pm 0.6$	$+1.0 \pm 0.6$	$+1.0 \pm 0.6$
2K+P	$+1.1 \pm 0.8$	$+0.8 \pm 0.9$	$+1.1 \pm 0.5$	$+1.1 \pm 0.5$
3K+P	-	-	-	$+0.8 \pm 0.8$
4K+P	$\equiv 0.0 \pm 0.4$	$\equiv 0.0 \pm 0.4$	-	-
5K+P	-	-	$\equiv 0.0 \pm 0.4$	$\equiv 0.0 \pm 0.3$

Code: 1K = 4 cm; Data for F_{geom} are given in %

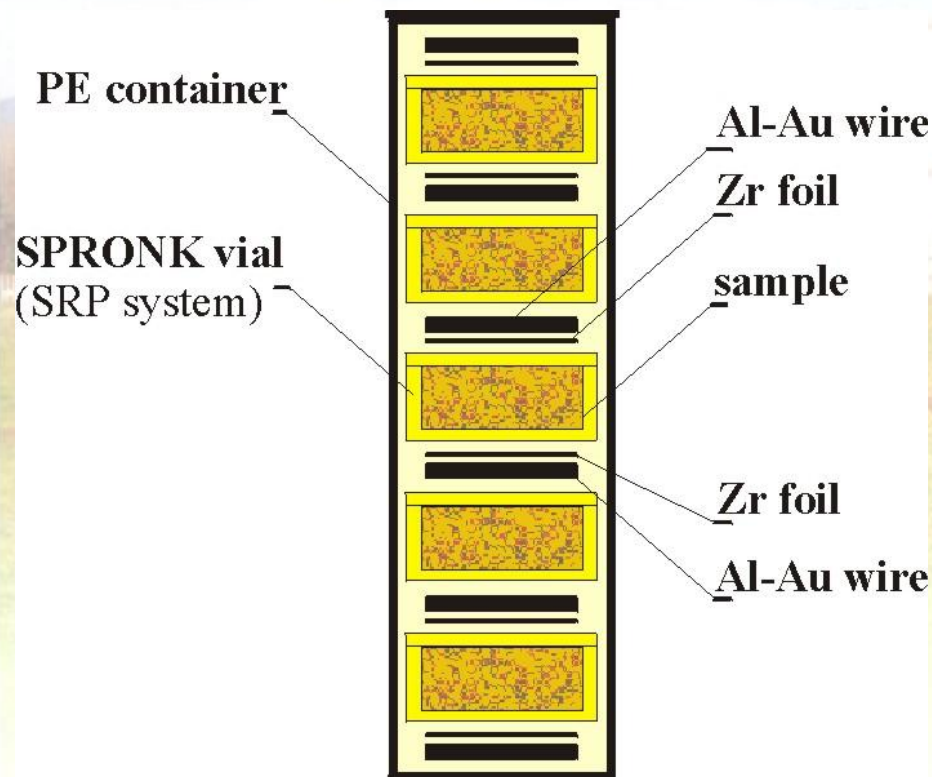
Total correction factor (F_c) for inorganic matrix



$$F_c = \left(1 + \frac{F_{sat}}{100}\right) \cdot \left(1 + \frac{F_{inorg}}{100}\right) \cdot \left(1 + \frac{F_{masaCd}}{100}\right) \cdot \left(1 + \frac{F_{geom}}{100}\right)$$

El.	Nuclide	Distance	Total correction factor F_c			
			OR1	OR2	CA1	OR4
As	⁷⁶ As	Reference	1.024	1.024	1.024	1.024
Co	⁶⁰ Co	0K+P	0.970	1.008	0.983	1.032
Cr	⁵¹ Cr	0K+P	0.976	1.014	0.988	1.038
Cs	¹³⁴ Cs	0K+P	0.944	0.981	0.956	1.004
Rb	⁸⁶ Rb	1K+P	1.018	1.034	0.994	1.028
Sb	¹²⁴ Sb	0K+P	0.924	0.960	0.936	0.983
Sc	⁴⁶ Sc	0K+P	0.976	1.014	0.989	1.038
Sr	⁸⁵ Sr	0K+P	0.942	0.979	0.954	1.002
Ta	¹⁸² Ta	0K+P	0.920	0.956	0.932	0.979
Yb	¹⁷⁵ Yb	1K+P	1.058	1.075	1.034	1.069
Zn	⁶⁵ Zn	0K+P	0.970	1.008	0.983	1.032

k_0 -INAA analytical procedure



- Sample and standard are prepared in **sandwich form** and irradiated in the carousel facility of the TRIGA Mark II reactor (250 kW)
- Measurement on an HPGe absolutely calibrated detector
- Evaluation of the spectrum by **HyperLab** program
- Calculation of the effective solid angle between sample and HPGe detector
- Calculation of element concentration by **KAYZERO** program

Verification of the corrected k_0 -NAA procedure

- inorganic matrices:
 - BCR-320 River Sediment ($n = 14$)
 - IAEA SL-3 Lake Sediment ($n = 3$)
 - IAEA Soil-7 ($n = 15$)
 - IAEA-405 Estuarine Sediment ($n = 3$)
- organic matrices:
 - IAEA Sea plant ($n = 4-11$)
 - IAEA 336 Lichen ($n = 5-7$)
 - NIST 2871 Domestic Sludge ($n = 3$)
 - IJS PT-SL1 Sewage Sludge ($n = 5-6$)

IAEA Soil-7
Detector OR4



El.	Nuclide	Experimental data					Literature data		
		δ_{nocorr} , %	δ_{corr} , %	$S_{d,}$ %	$S_{a,tot}$, %	(n)	Recomm. mg/kg (dry weight)	S_{RM} , %	(n)
As	⁷⁶ As	6.5	9.9	1.72	4.35	15	13.4	6.34	25
Ce	¹⁴¹ Ce	-13.6	-8.3	4.48	5.45	15	61	10.7	15
Co	⁶⁰ Co	-7.4	-2.2	3.26	4.39	15	8.9	9.55	32
Cr	⁵¹ Cr	8.3	15.2	3.21	4.39	15	60	20.8	41
Cs	¹³⁴ Cs	-0.3	2.5	1.81	4.58	15	5.4	13.9	16
Eu	¹⁵⁴ Eu	2.9	7.5	3.39	4.72	15	1.0	20.0	10
Hf	¹⁸¹ Hf	-10.9	-6.0	3.61	4.73	15	5.1	6.86	11
La	¹⁴⁰ La	-7.0	-0.9	4.29	5.32	15	28	3.57	12
Nd	¹⁴⁷ Nd	-19.3	-14.2	6.22	6.96	15	30	20.0	7
Rb	⁸⁶ Rb	0.6	3.6	3.31	4.60	15	51	8.82	24
Sb	¹²⁴ Sb	4.4	5.1	3.56	4.97	15	1.7	11.8	18
Sc	⁴⁶ Sc	-4.2	1.9	3.35	4.49	15	8.3	12.6	22
Sm	¹⁵³ Sm	-8.7	-5.9	1.84	3.44	15	5.1	6.86	12
Sr	⁸⁵ Sr	1.3	4.7	5.49	11.2	15	108	5.09	19
Ta	¹⁸² Ta	-4.5	-4.2	3.67	5.23	15	0.8	25.0	12
Tb	¹⁶⁰ Tb	8.7	10.9	2.26	4.00	15	0.6	33.3	12
Th	²³³ Pa	-3.5	-0.5	1.26	3.30	15	8.2	13.4	18
U	²³⁹ Np	-2.6	-4.1	5.99	6.85	15	2.6	21.1	14
Yb	¹⁷⁵ Yb	-14.3	-8.1	4.04	5.05	15	2.4	14.6	12
Zn	⁶⁵ Zn	-8.9	-3.7	3.30	4.44	15	104	5.77	44
Zr	⁹⁵ Zr	-0.4	4.0	7.16	7.76	15	185	5.68	15

S_{RM} – 95% confidence interval of the reference material (RM)

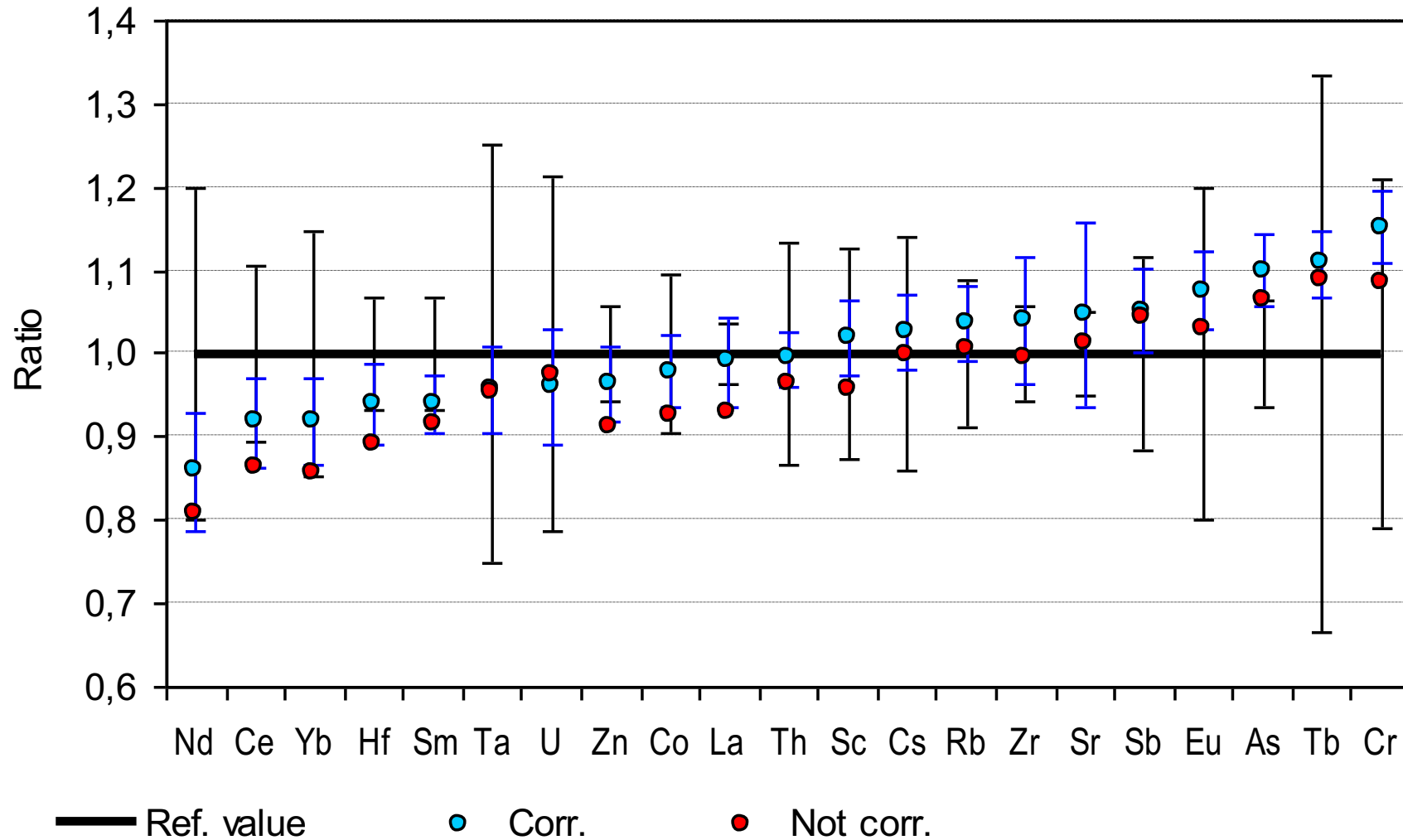
δ_{nocorr} – difference between arithmetic mean value of standard k_0 -procedure and recommended value

δ_{corr} – difference between arithmetic mean value of corrected k_0 -procedure and recommended value

$\delta_{a,tot}$ – total uncertainty

8.-12. November 2010, Trieste, Italy

Inorganic matrix: IAEA Soil-7 (n = 15) - OR4



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IAEA 336 Lichen Detector OR4



El.	Nuclide	Experimental data					Literature data		
		δ_{nocorr} , %	δ_{corr} , %	s_d , %	$s_{a,\text{tot}}$, %	(n)	Recomm. mg/kg (dry weight)	s_{RM} , %	(n)
As	⁷⁶ As	10.6	11.4	4.16	5.77	5	0.63	12.7	17
Ba	¹³¹ Ba	-1.5	-4.7	8.31	11.6	5	6.4	17.2	11
Br	⁸² Br	-3.8	-3.8	2.33	3.99	6	12.9	13.2	18
Ce	¹⁴¹ Ce	-4.1	-4.3	3.39	4.59	5	1.28	13.3	13
Co	⁶⁰ Co	-0.6	-1.2	1.57	3.33	5	0.29	17.2	19
Cs	¹³⁴ Cs	5.6	3.2	3.14	5.25	5	0.110	11.8	13
Fe	⁵⁹ Fe	1.1	0.8	0.70	3.05	5	430	11.6	35
Hg	²⁰³ Hg	-43.6*	-44.8*	11.8	12.3	5	0.2	20.0	15
K	⁴² K	-0.4	2.9	5.12	5.94	7	1840	10.9	24
La	¹⁴⁰ La	-8.5	-6.1	4.35	5.37	5	0.66	15.1	12
Mn	⁵⁶ Mn	2.5	5.3	#	3.02	2	63	11.1	29
Na	²⁴ Na	0.9	4.2	2.82	4.12	7	320	12.5	20
Sb	¹²⁴ Sb	1.5	-2.2	6.06	6.98	5	0.073	13.7	12
Se	⁷⁵ Se	-3.9	-5.8	4.47 \$	6.91	5	0.22	18.2	12
Sm	¹⁵³ Sm	-2.0	-1.5	5.62	6.33	5	0.106	13.2	15
Sr	⁸⁵ Sr	17.2	14.5	6.39	11.6	5	9.3	11.8	19
Th	²³³ Pa	11.8	9.5	11.1	11.5	5	0.14	14.3	16
Zn	⁶⁵ Zn	4.2	3.6	0.69	3.04	5	30.4	11.2	38

* - "outlier";

\$ - standard deviation (s_d) of independent measurements < standard deviation of N_p (net peak area in the spectrum 6.0%);

- for s_d was taken into account standard deviation of the N_p (0.3%)

s_{RM} - 95% confidence interval of the reference material (RM)

δ_{nocorr} - difference between arithmetic mean value of standard k_0 -procedure and recommended value

δ_{corr} - difference between arithmetic mean value of corrected k_0 -procedure and recommended value

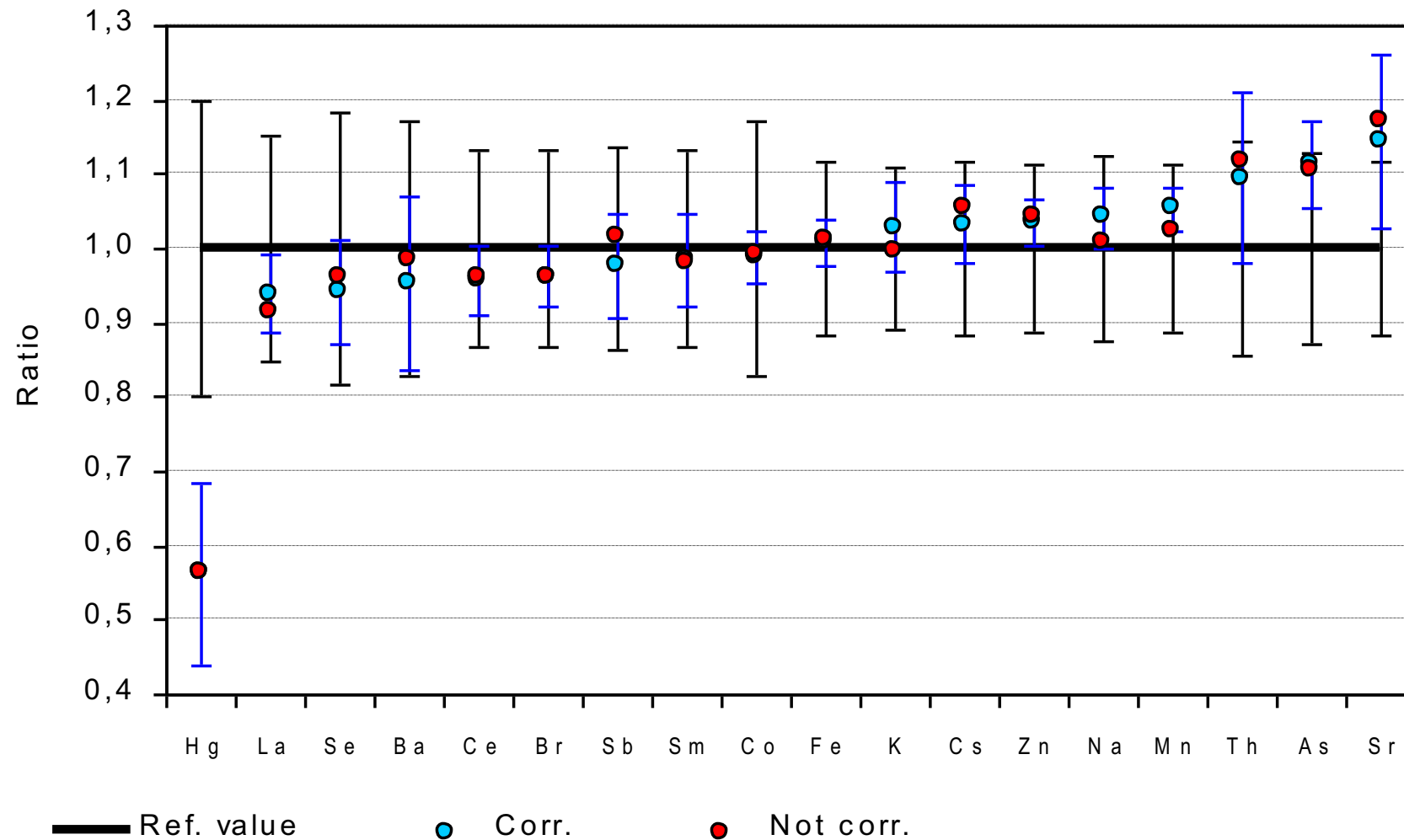
$\delta_{a,\text{tot}}$ - total uncertainty

8.-12. November 2010, Trieste, Italy

Organic matrix: IAEA 336 Lichen (n = 5-7)



OR4



8.-12. November 2010, Trieste, Italy

Statistical uncertainties



$$\bar{\delta} = \frac{\sum_{i=1}^N \bar{\delta}_i \cdot w_i}{\sum_{i=1}^N w_i}$$

Weighted average deviation
of RM means from certified value

$\bar{\delta}_i$ Average deviation of independent measurements for a particular RM

$$w_i = \frac{1}{s_{x_i, \text{tot}}^2 + s_{RM}^2}$$

Weight with
our and reference
standard deviation

- Statistical consistency : $s_{\text{int}} \approx s_{\text{ext}}$
- $s_{\text{int}} \gg s_{\text{ext}}$: estimation of $s_{x_i, \text{tot}}$ values contains common systematic uncertainty or average results are biased
- $s_{\text{int}} \ll s_{\text{ext}}$: suggested that one or more uncommon uncertainties were not taken into account when estimating the $s_{x_i, \text{tot}}$ values
- $\bar{\delta} \ll s_{\text{int}}$: reliability of the measurement is good

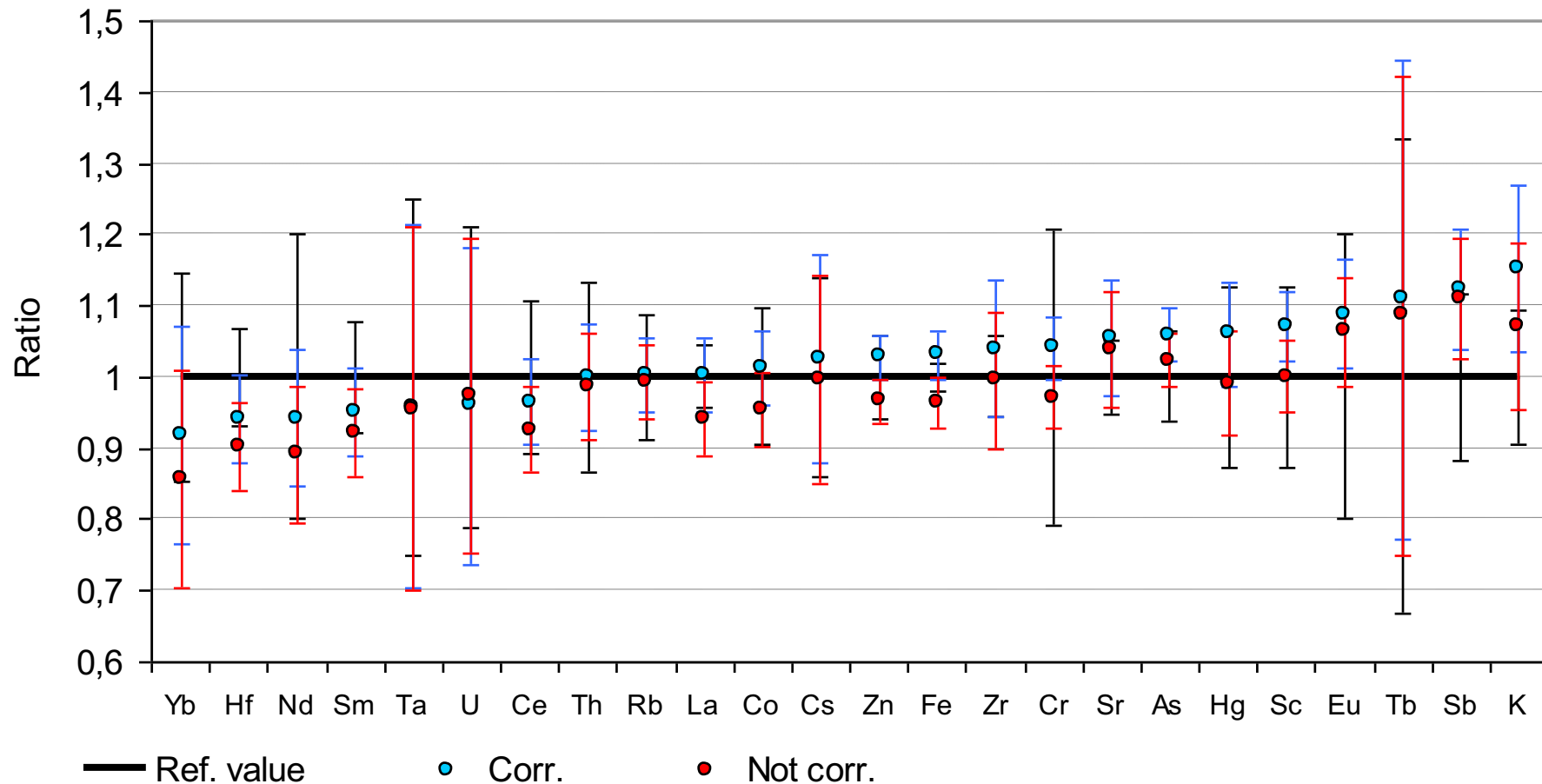
$$s_{\text{int}} = \frac{1}{\sqrt{\sum_{i=1}^N w_i}}$$

Internal
Statistical
uncertainty

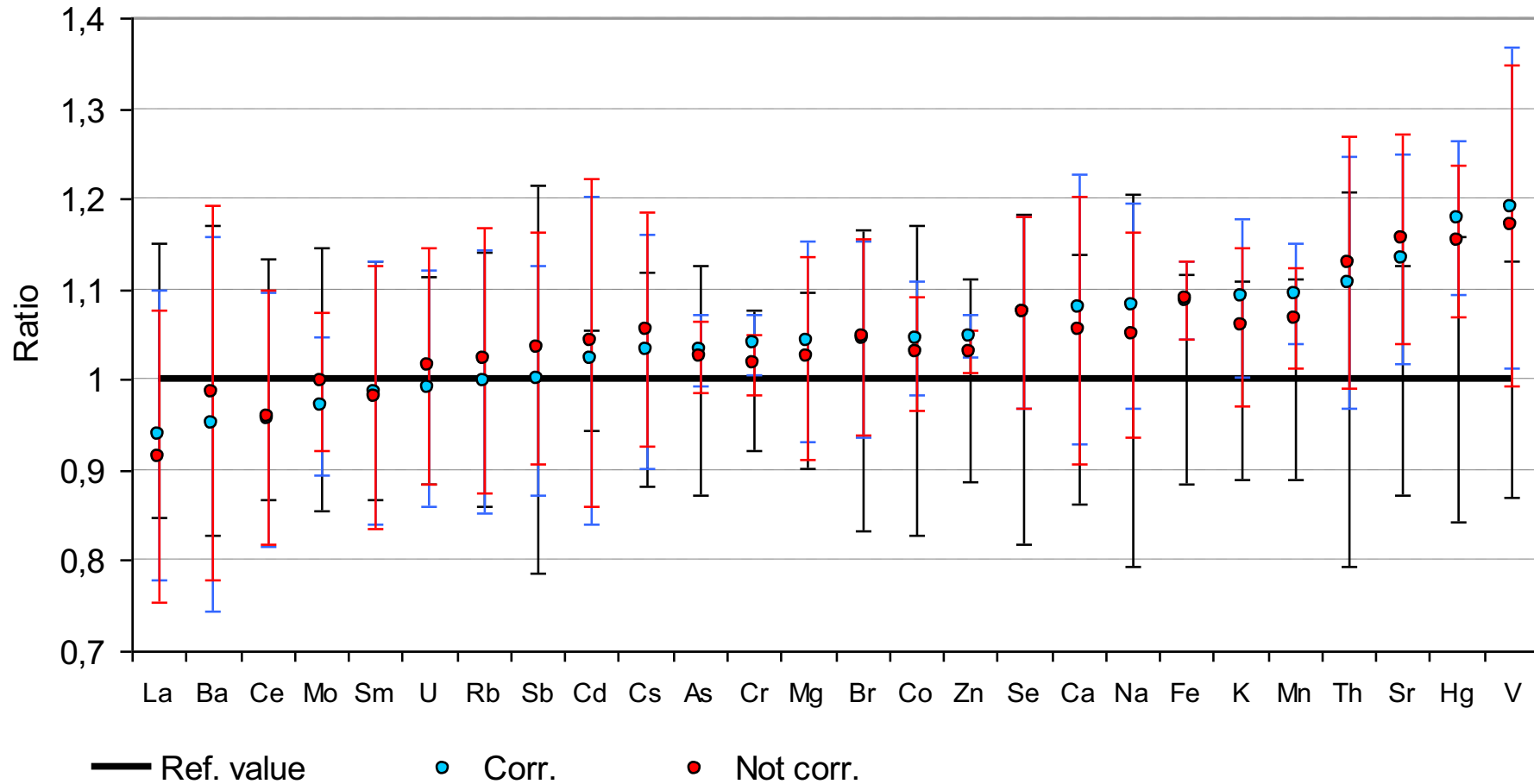
$$s_{\text{ext}} = \sqrt{\frac{\sum_{i=1}^N w_i \left(\bar{\delta}_i - \bar{\delta} \right)^2}{(N-1) \sum_{i=1}^N w_i}}$$

External
Statistical
uncertainty

Weighted average for 4 inorganic matrices



Weighted average for 4 organic matrices



Conclusions



- Standard procedure of k_0 -NAA (KAYZERO/SOLCOI ver. 5a - February 2003) was applied for determination of major and trace elements in a suite of RMs or CRMs
- Four correction factors were introduced in the standard procedure of k_0 - NAA:
 - F_{sat}
 - F_{org} or F_{inorg}
 - F_{masaCd}
 - F_{geom}
- The results obtained by corrected procedure of k_0 -NAA show relatively better agreement with CRMs value than results without correction for mostly recommended or certified elements in organic and inorganic matrices

Conclusions (cont)



- Hg - “outlier” from 95% CI in IAEA 336 Lichen (organic matrix) obtained with both procedures due to **losses during irradiation** in the semi-open plastic vials
- The biggest difference between standard and corrected procedure of k_0 -NAA in **organic** matrices is for **Sb (3.6%)**
- The biggest difference between standard and corrected procedure of k_0 -NAA in **inorganic** matrices is for **K (8.0%)**