

# **Understanding and Predicting Atlantic Decadal SST Variability Using a Hierarchy of Models**

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# Collaborators

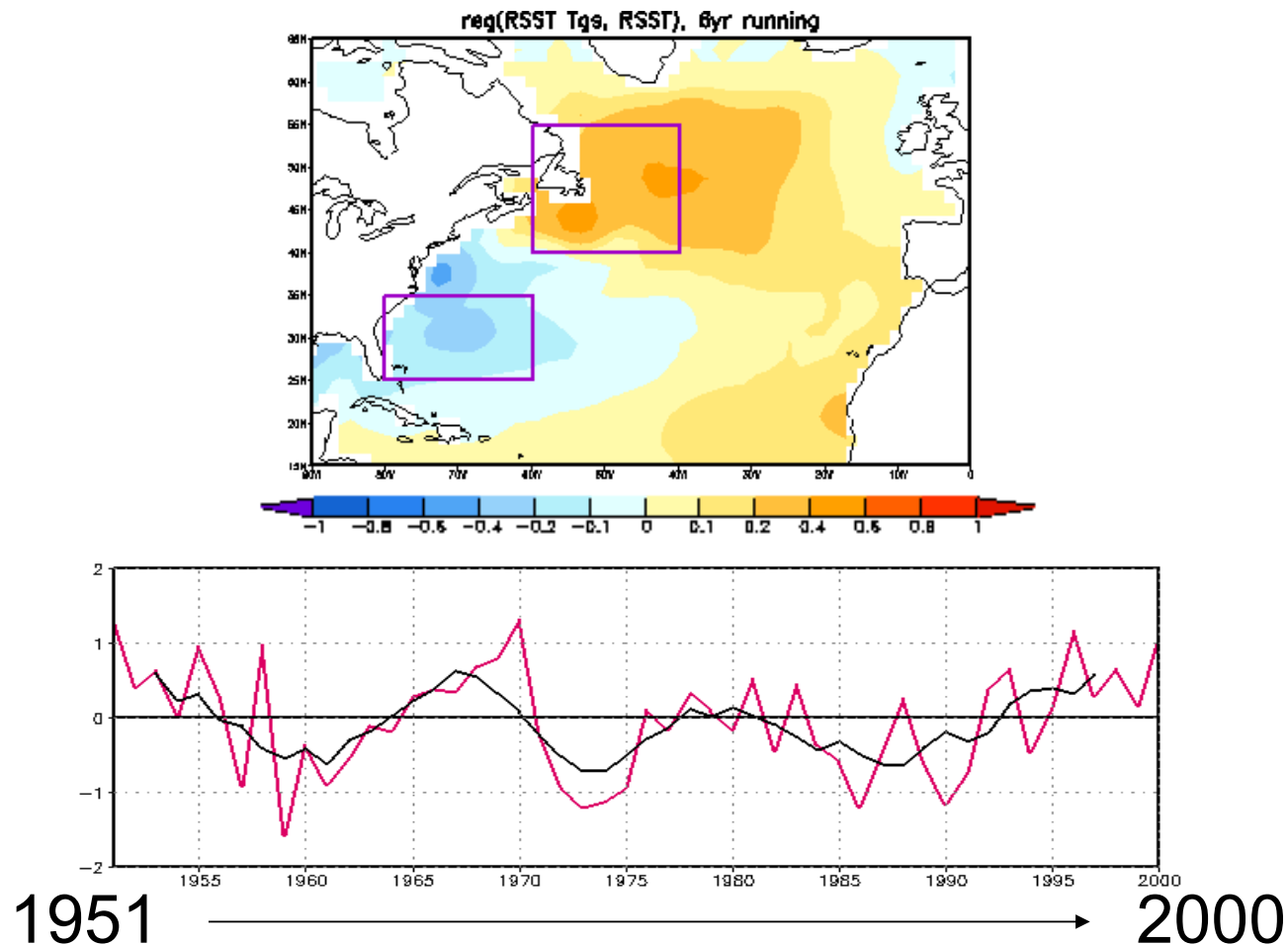
- Meizhu Fan - many of the results come from her PhD thesis.
- Ben Kirtman - developer of the “Interactive Ensemble”
- Hua Chen, Ioana Colfescu GMU graduate students

# Physical Problem

- Diagnose and understand the mechanisms of observed low frequency observed (1951-2000) North Atlantic SST variability.
- In particular, what were the roles of weather noise forcing, coupled feedbacks, and ocean dynamics?
- What are the implications for decadal predictability?

# Tripole

**Index:** area average SST difference. Northern box minus Southern. (Czaja and Marshall 2001, QJRMS)



# Tripole Mechanism Issues

- External forcing or internal variability?
- Remote or local origin?
- Why decadal time scale?
- Connections to other modes of variability (e.g. NAO, AO, AMO, TAV, PDO, AMOC)?
- Implications of understanding of mechanisms for predictability?

# A Menagerie of Models

- Hasselmann model (conceptual/motivational)
- Barsugli/Battisti model (conceptual/motivational)
- CGCM or reanalysis (data to interpret)
- AGCM ensemble (determine weather noise)
- Intermediate Coupled Model (parameterized atmospheric transients, controlled experiments)
- Czaja/Marshall model (conceptual/diagnostic)

## **The Four Mechanisms of Low Frequency Climate Variability (SST) (Sarachik et al., 1996)**

1. Forced by atmospheric weather noise  
(Hasselmann 1976)
2. Forced by oceanic “weather noise”
3. Intrinsic coupled variability (e.g. coupled  
ocean-atmosphere) that is not forced by  
weather noise
4. Externally forced

# Hasselmann's Model (Damped Brownian Motion)

- 0-dimensional (1 point) model.
- Slab mixed layer ocean forced by stochastic heat fluxes, feedbacks damp SST anomalies.
- Stochastic heat flux forcing (white spectrum) represents random atmospheric weather noise.
- What properties of the low frequency climate variability can this minimal model explain?



$$\rho c H \frac{dT}{dt} = N - \lambda T$$

*N is "weather noise"*

*let  $N = N_{\omega} e^{i\omega t}$*

*look for solutions  $T = T_{\omega} e^{i\omega t}$*

$$T_{\omega} = \frac{N_{\omega}}{\lambda + i\omega\rho cH}$$

*and for white noise  $|N_{\omega}| = \text{const.}$*

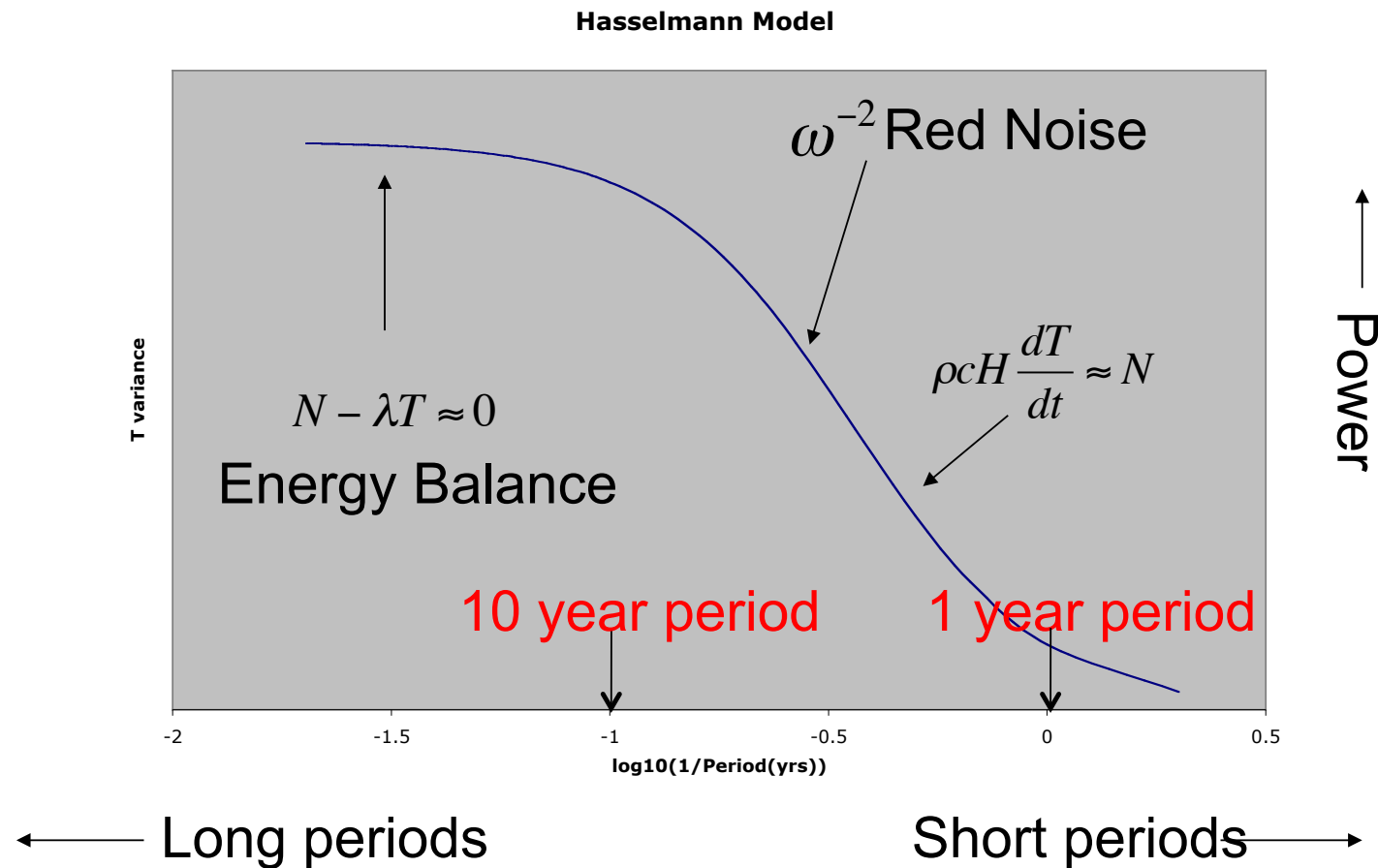
*So for high frequencies  $\omega\rho cH \gg \lambda$*

$$|T_{\omega}^2| \sim k_1 / \omega^2$$

*while for low frequencies*

$$|T_{\omega}^2| \sim k_2$$

## Response to white noise forcing for 50m slab mixed layer, damping $15 \text{ W m}^{-2} \text{ K}^{-1}$



# Properties of Hasselmann's Model

- No SST variability without weather noise forcing.
- Appears to explain redness of climate spectra (but not the peaks).
- Suggests a testable null hypothesis for climate variability: all low frequency variability is the response to forcing by random weather noise.

# The Plan

- Scale up Hasselmann's model to a CGCM class model.
- Force the ocean with *specified* weather noise surface fluxes.
- Main issues
  - What sense does it make to force a CGCM with weather noise? The CGCM produces its own chaotic weather variability that can't be predicted or controlled.
  - How to choose  $N$  ?

# Barsugli and Battisti (BB) Model

- 0-dimensional (1 point model)
- Slab atmosphere coupled to slab ocean
- Atmosphere forced by radiation, ocean (surface fluxes), and weather noise
- Ocean forced by atmosphere (surface fluxes)
- Makes contact with CGCM architecture
- Hasselmann model is a special case (energy balance limit).

# Barsugli and Battisti Model

- Atmosphere  $T_a$ , ocean  $T_o$ , weather noise  $N$
- Atmosphere ( $T_a$ ): 
$$\frac{dT_a}{dt} = -aT_a + bT_o + N$$
- Ocean ( $T_o$ ): 
$$\beta \frac{dT_o}{dt} = cT_a - hT_o$$
- Reduces to Hasselmann model for slave atmosphere ( $dT_a/dt \approx 0$ ).

# Equivalent BB Model

- Atmosphere:

$$\frac{dT_a}{dt} = -aT_a + bT_o$$

- Ocean:

$$\beta \frac{dT_o}{dt} = cT_a - hT_o + N_f$$

- Forcing:

$$\text{if } \frac{1}{c} \frac{dN_f}{dt} + \frac{N_f}{a} = N$$

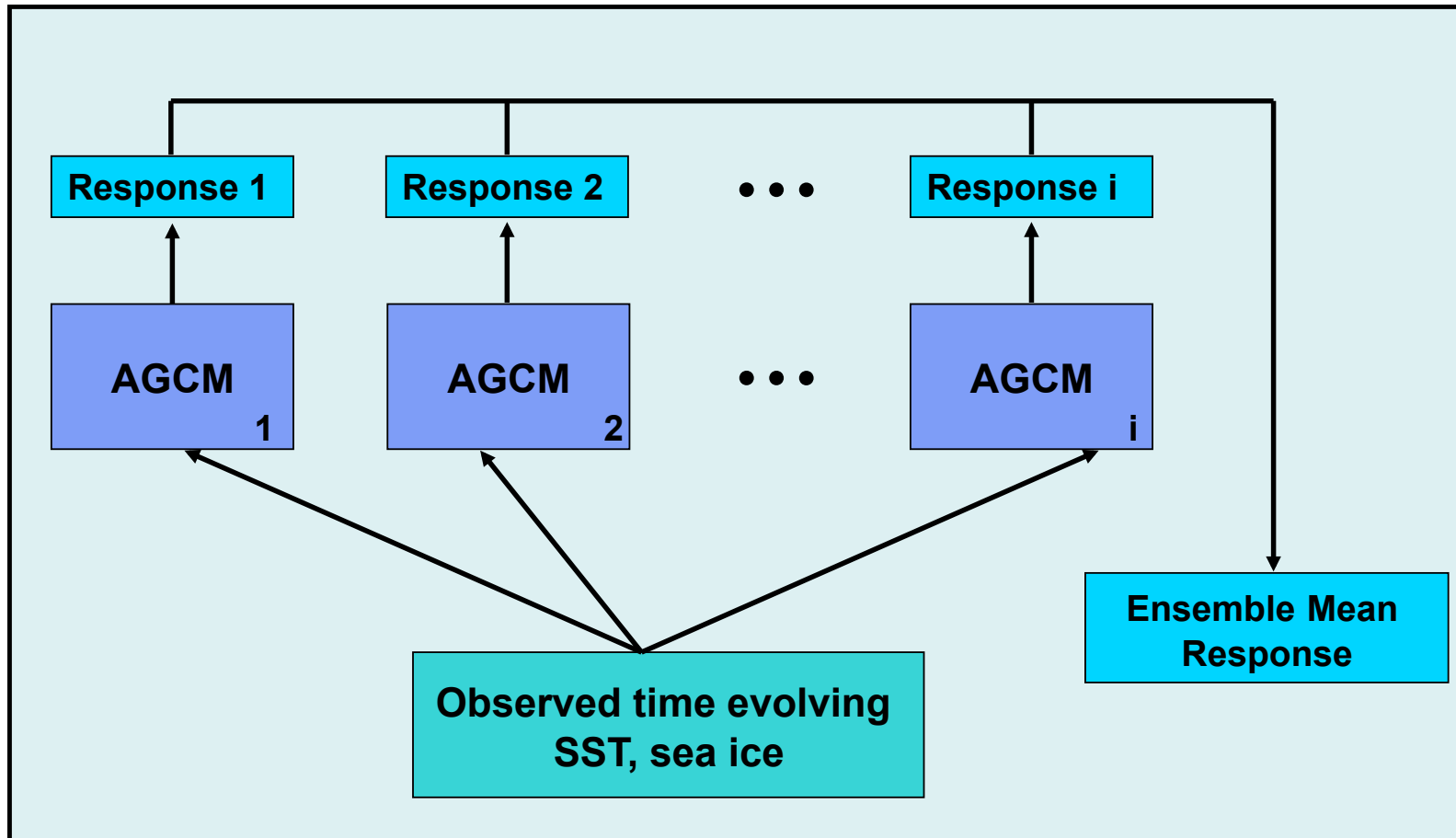
(but remember we don't know  $N$ )

- Noise free atmosphere, ocean forced by “weather noise” surface fluxes.
- Diagnostic only – the weather noise has to be determined from the output of the original model.



## **“AMIP Ensemble”**

- Force an ensemble of AGCMs with the same SST and external forcing evolution.
- Each ensemble member has a different initial condition.
- Gates et al. 1999.



Response of  $AGCM_i = SST \text{ forced signal} + Noise_i$

$Noise_i$  is distinct for each  $AGCM_i$

**AMIP/GOGA Ensemble**

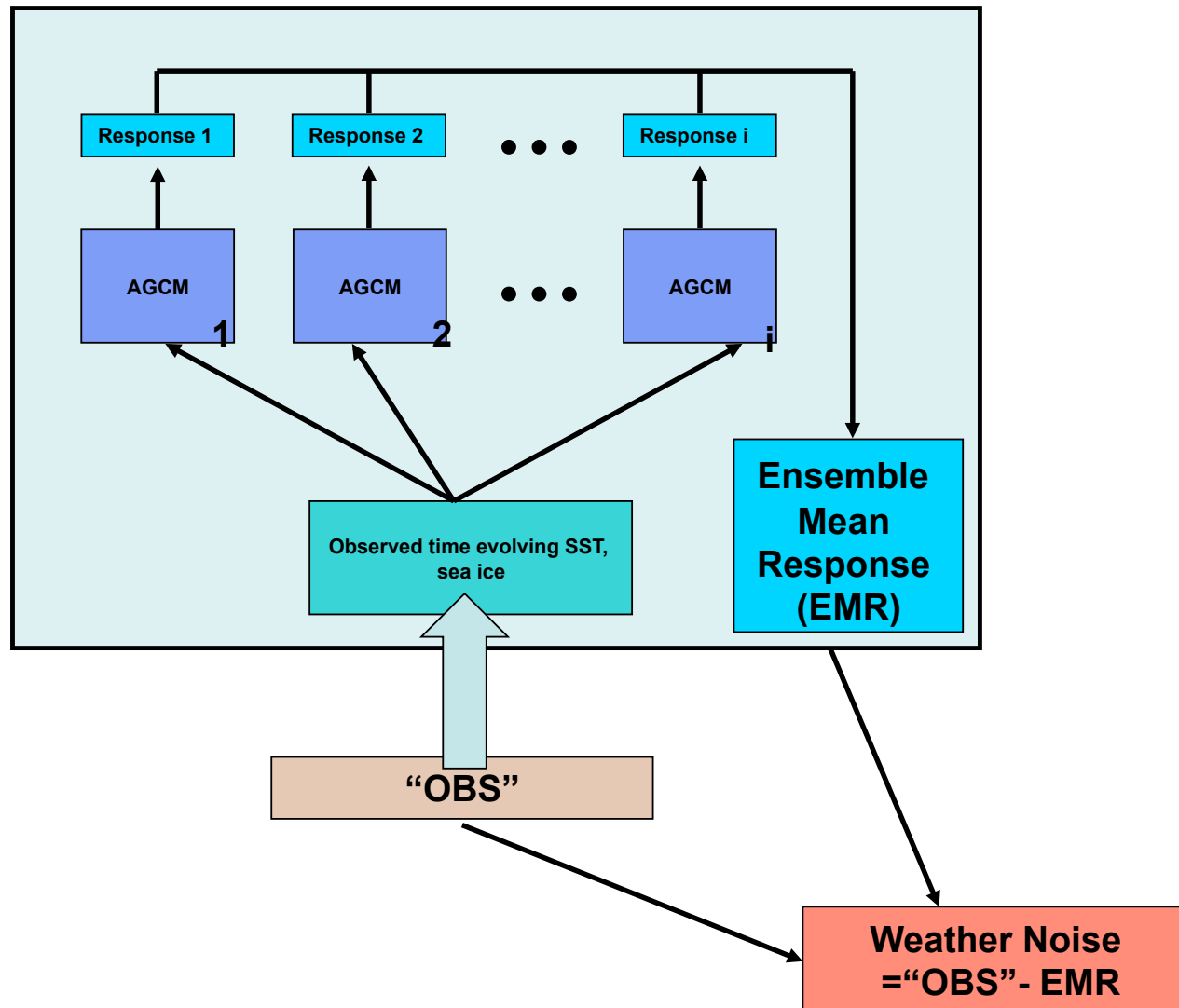
# AMIP Ensemble Properties

- The AMIP ensemble mean is the SST forced “signal.” It is independent of the choice of initial atmospheric states.
- Then the solution for each ensemble member is:  
(the SST/externally forced ensemble mean) + (the residual)
- The residuals are uncorrelated between ensemble members.
- The ensemble mean can be thought of as an atmospheric model with
  - parameterized transient eddy fluxes
  - No weather noise
- The residuals are the “weather noise” the non-parameterizeable and unpredictable part of the atmospheric evolution.

# Diagnosis of the Weather Noise

- To find the weather noise in data produced by an AGCM simulation (or in observations), remove the ensemble mean of the AMIP ensemble forced by the same SST and external forcing.

**Weather Noise = (observed) – (SST forced)**

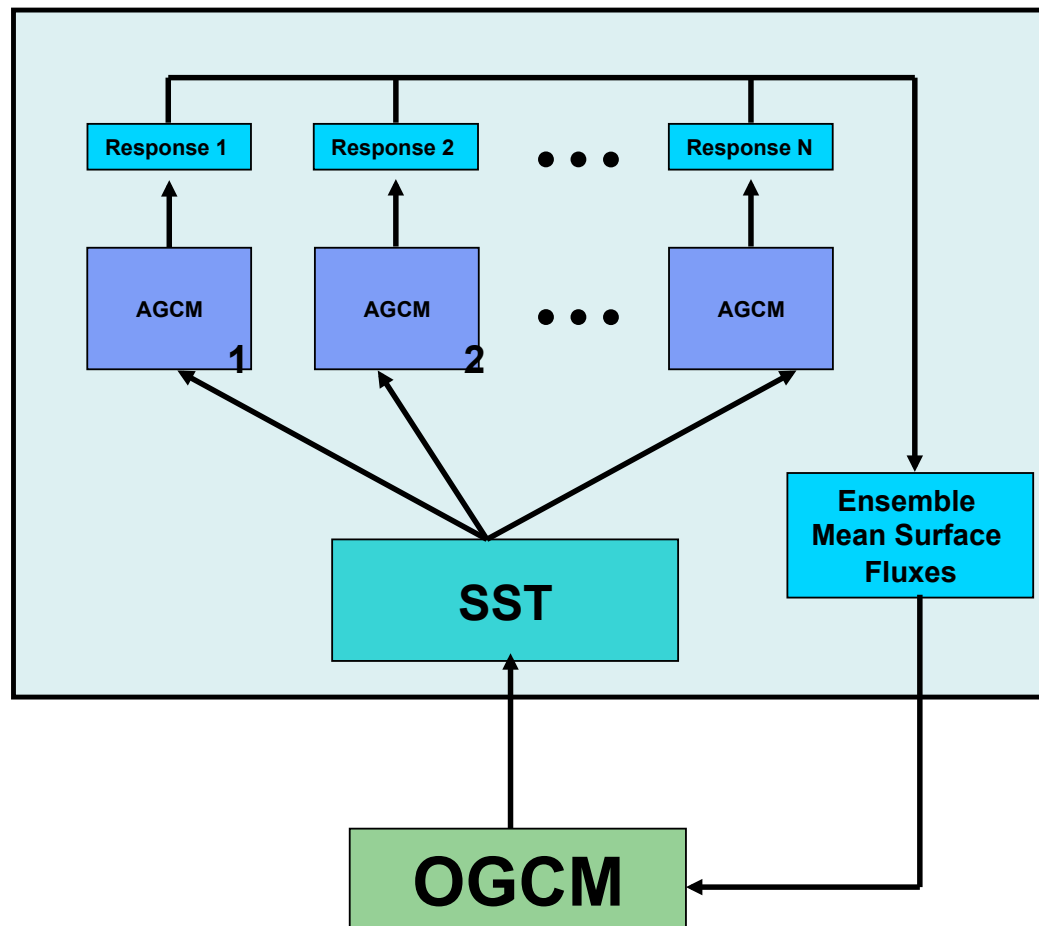


**Determination of the Weather Noise**

## **Other Ingredient: Coupled Model With a Noise Free Atmosphere (Intermediate Coupled Model)**

- Couple AGCM AMIP ensemble to OGCM.
  - Each AGCM ensemble member sees the same OGCM SST
  - OGCM sees ensemble mean surface fluxes from the atmospheres (no weather noise)
  - The AGCM ensemble and the OGCM interact just as the AGCM and OGCM do in a CGCM
- “Interactive Ensemble CGCM” or IE-CGCM
  - Kirtman and Shukla
  - CGCM class feedbacks, parameterizations

# Interactive Ensemble CGCM



# Properties of IE-CGCM

- Much reduced internal SST variability on *all time scales* compared to CGCM when no external forcing.
  - No intrinsic AMOC variability, as in other ICMs.
  - ***Proves*** that internally generated SST variability in the CGCM is forced primarily by atmospheric weather noise.
- Exceptions
  - ENSO-related SST variability in the equatorial Western Pacific
  - Internal ocean variability associated with strong currents (ocean “weather noise”).

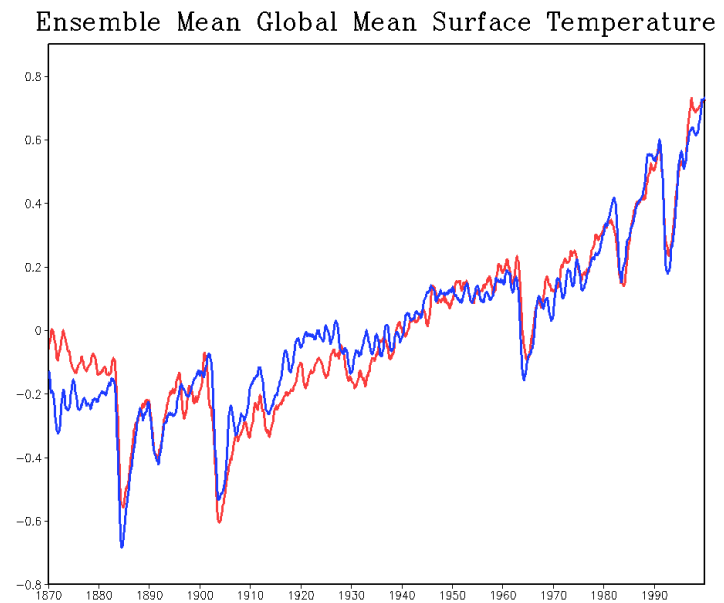
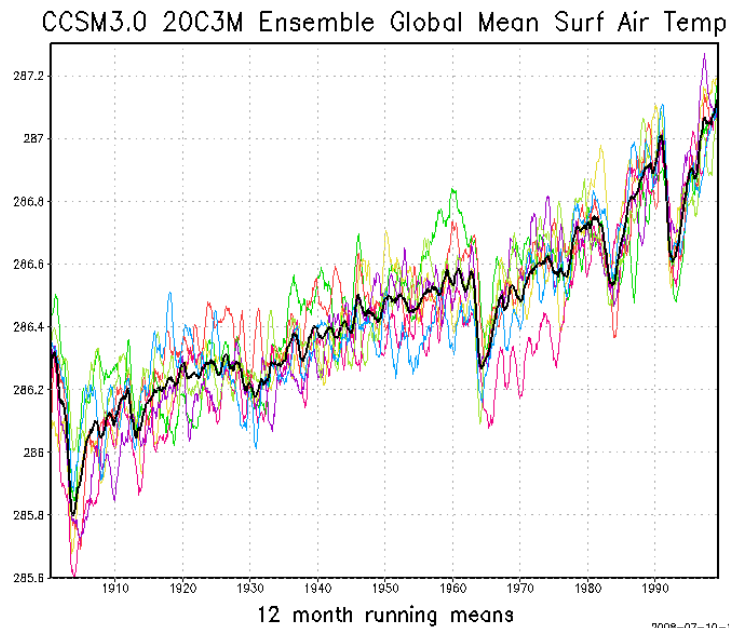


# Response to Observed External Forcing 1870-2000 (20C3M)

## CCSM3 CMIP4

Colors = ensemble members  
Black = ensemble mean

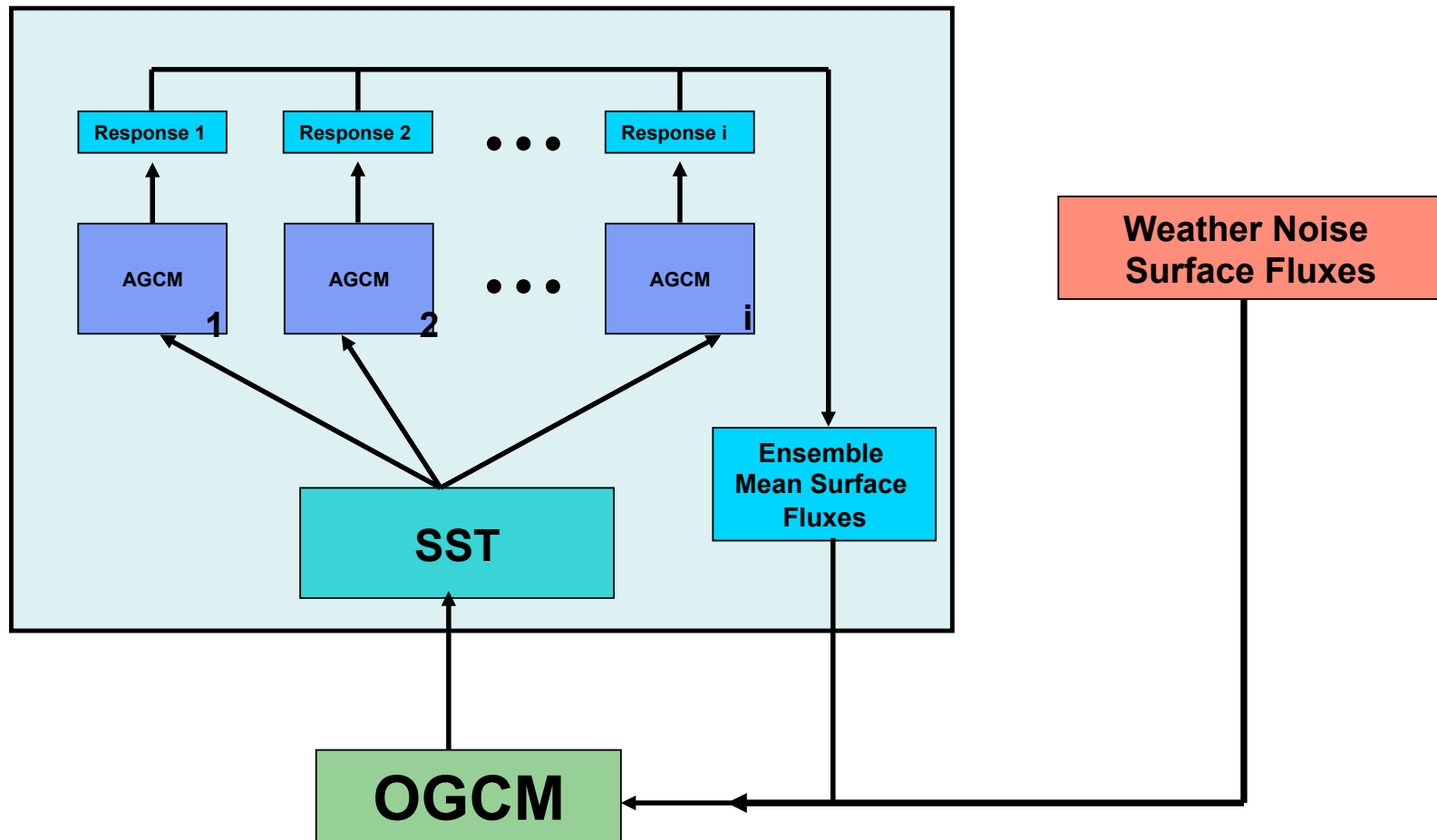
Red = CCSM3 ensemble mean  
Blue = CCSM3 IE



# Noise Forced IE-CGCM

- Specified weather noise surface flux forcing is added to the surface fluxes seen by ocean
  - Heat, momentum, fresh water
- Weather noise is calculated from observations (or CGCM output) and the SST forced AMIP ensemble
- The model is an ICM with deterministic solutions to the weather noise forcing.
- **It is many times more “complex” and more expensive than the underlying CGCM ( $\rightarrow \infty$ ).**
- Applied to the BB model, this procedure yields the “equivalent BB model,” a diagnostic coupled model.

# Noise Forced Interactive Ensemble



# Other Ways to Think About Weather Noise Forced IE CGCM:

- It is like an **OGCM simulation** forced by observed fluxes but with feedbacks correctly taken into account.
  - “OGCM” simulations typically include atmospheric feedbacks (e.g. damping) as well as specified observed fluxes. This is inconsistent.
- It is a type of **Coupled Data Assimilation**
  - CGCM-like model constrained by data

# Tripole Problem

- Simulate the observed 1951-2000 tripole index using a CGCM-class model forced by observed weather noise.
- Try to understand the results in the framework of the simple model of Frankignoul and Hasselmann (1976) as extended by Marshall et al. (2001), Czaja and Marshall (2001):
  - Weather noise
  - Atmospheric feedback to SSTA
  - Gyre circulation
  - AMOC

# Earlier Work

- Kushnir 1994; Deser and Blackmon 1993
  - Observational
- Seager et al 2000
  - Force ocean with reanalysis surface fluxes. Heat flux forcing dominates, ocean dynamics secondary for SST
- Marshall et al. 2001; Czaja and Marshall 2001
  - Observational diagnosis. Simple model of tripole variability
- Eden and Willibrand 2001
  - Force OGCM in NA with NCEP reanalysis surface fluxes
- Eden and Greatbatch 2003
  - Force OGCM in NA with simple stochastic atmosphere
- Visbeck et al. 2003
  - Role for ocean dynamics at longer time scales
- Bellucchi et al. 2008
  - Analysis of tripole simulated in SINTEX-G CGCM

# Data and Models

- NCEP reanalysis 1951-2000, monthly means
- COLA CGCM and IE-CGCM
  - COLA V2 AGCM (T42, L18)
  - MOM3 OGCM (1.5°, finer meridional near equator) non-polar domain
  - Anomaly coupled

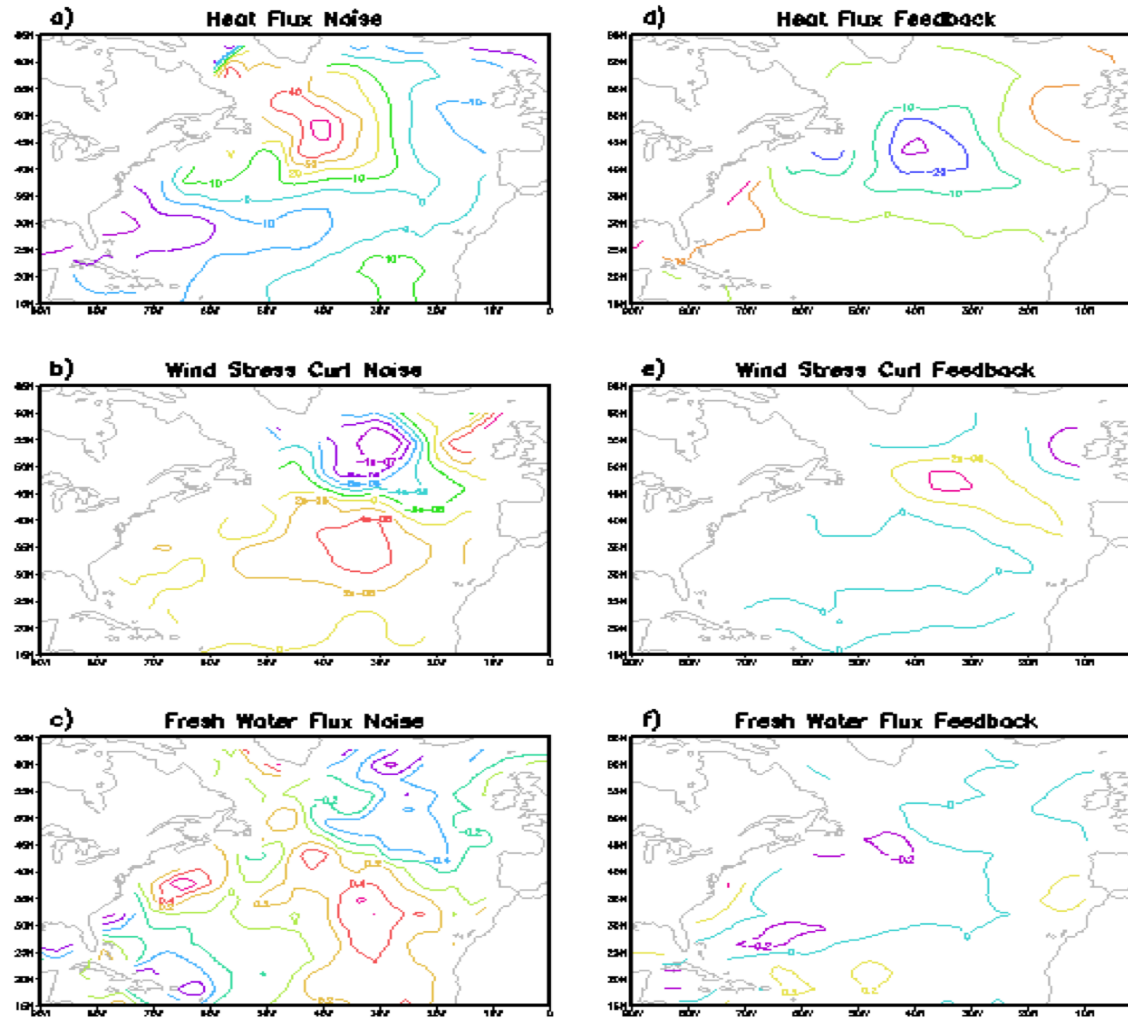
## Elements of Tripole SST Variability

- Weather noise (NAO variability)
- Feedback of SST → NAO
  - In terms of heat flux is this positive? negative?
- Ocean dynamics heat flux
  - Gyre circulations
    - Modulations of mean gyre
    - Intergyre gyre
  - AMOC



# Weather Noise and Feedbacks

regression 7 year running mean onto tripole



# Experiments

- Force Interactive Ensemble (IE) CGCM with weather noise surface fluxes for 1951-2000.
- If the SST variability was the response to the weather noise, it will be reproduced.
  - Further experiments will then isolate the role of various processes in the SST variability (e.g. ocean dynamics, location and type of weather noise forcing, ...)
- Diagnostic only (“additive noise”).

# Need to Understand Model's Own Internal Variability

- The model matters. Different models may produce different results due to different biases
- Perfect model, perfect data application
  - The COLA CGCM NAO and tripole patterns are shifted eastward  $\sim 25^\circ$  from the observed locations
  - The tripole is forced by weather noise heat fluxes

# Experiments to Diagnose Observed Variability

- Forcing Data: 1951-2000 NCEP reanalysis monthly surface fluxes and SST

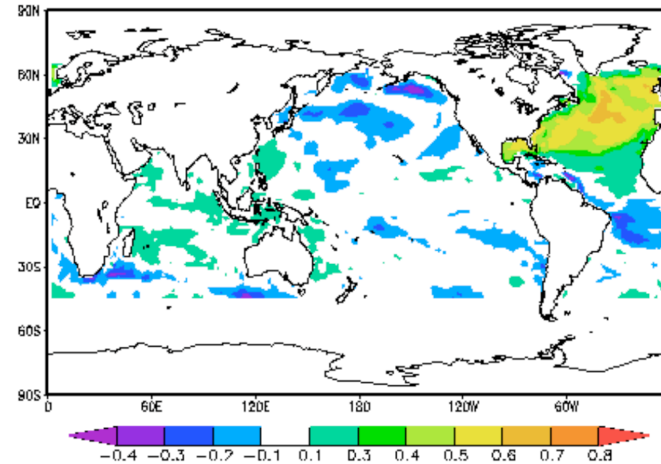
Experiment	Forcing Noise	Forcing Region
Gctl	all	Global ocean
NActl	all	North Atlantic 15°N~65° N
NAh	heat	...
NAm	momentum	...

Note: “all” ~ freshwater, heat, and momentum

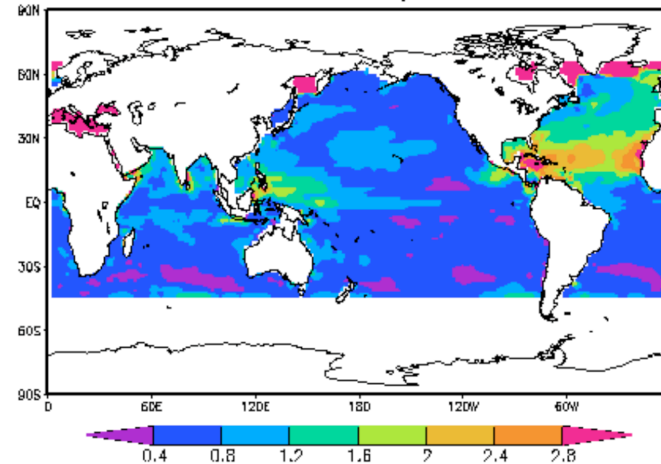
- N.B.: biased model, inaccurate data, no external forcing in model or analysis*

# NActl Reconstruction of Monthly SSTA

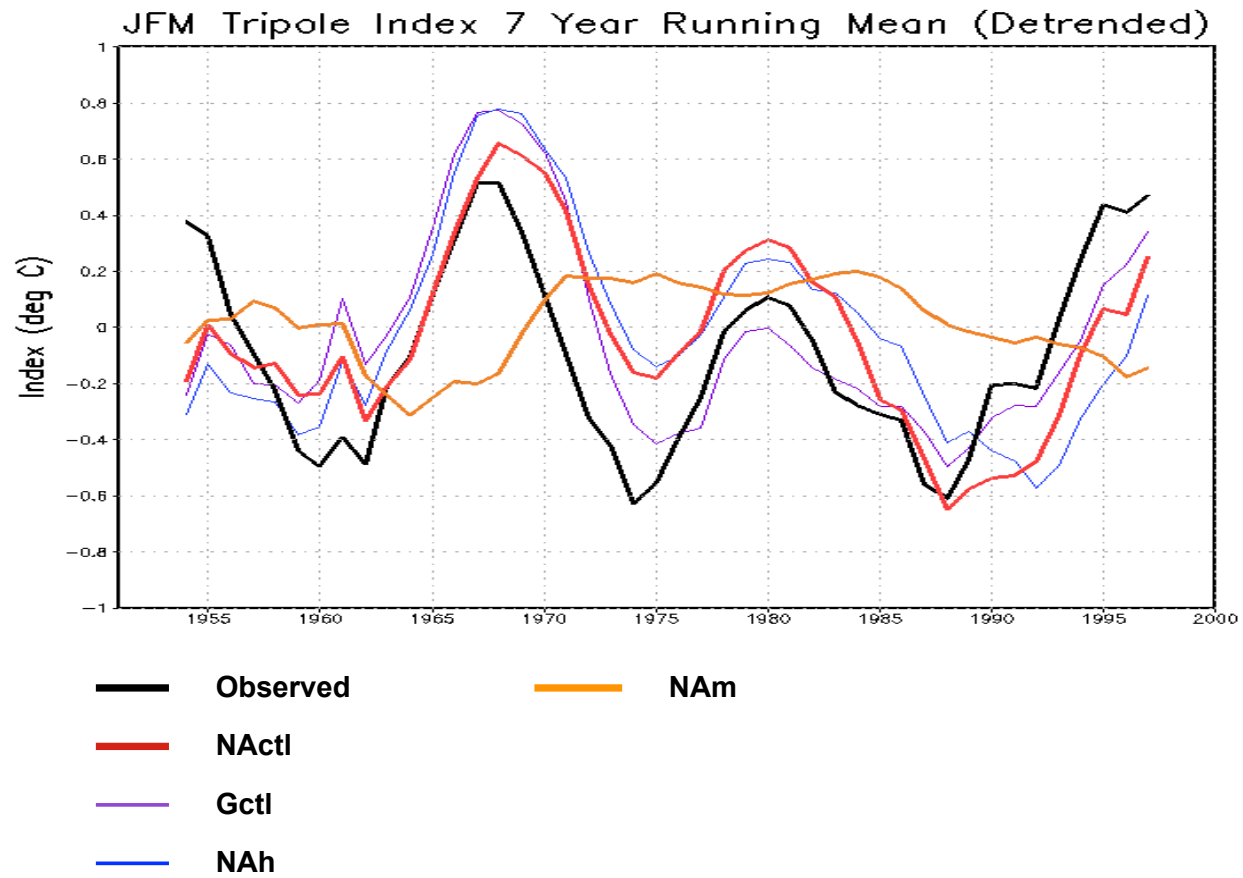
(a) SST Corr NActl & OBS, 1951–2000



(b) SST Variance Ratio NActl/OBS, 1951–2000



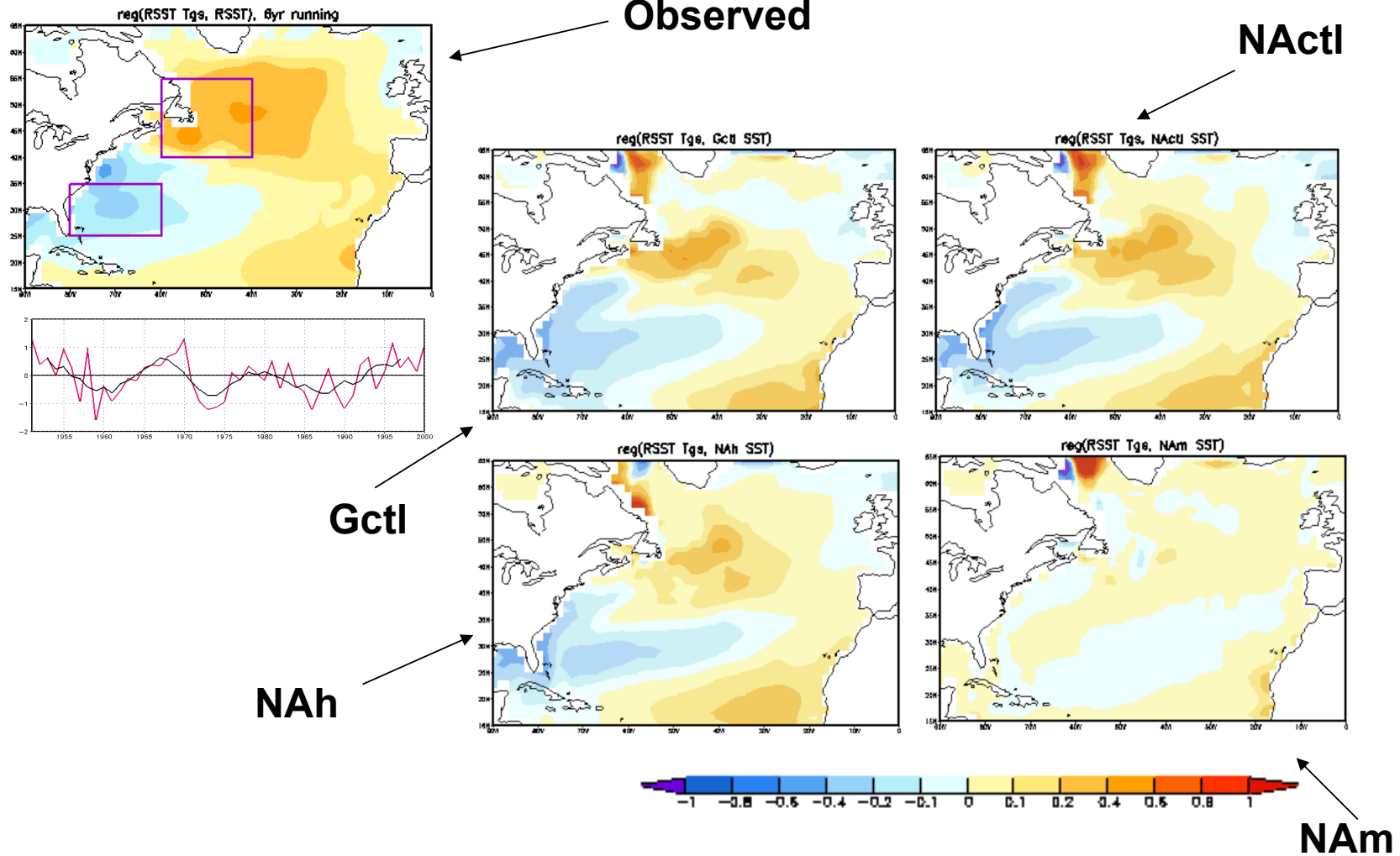
# Tripole Index (Detrended)



# Summary of Results

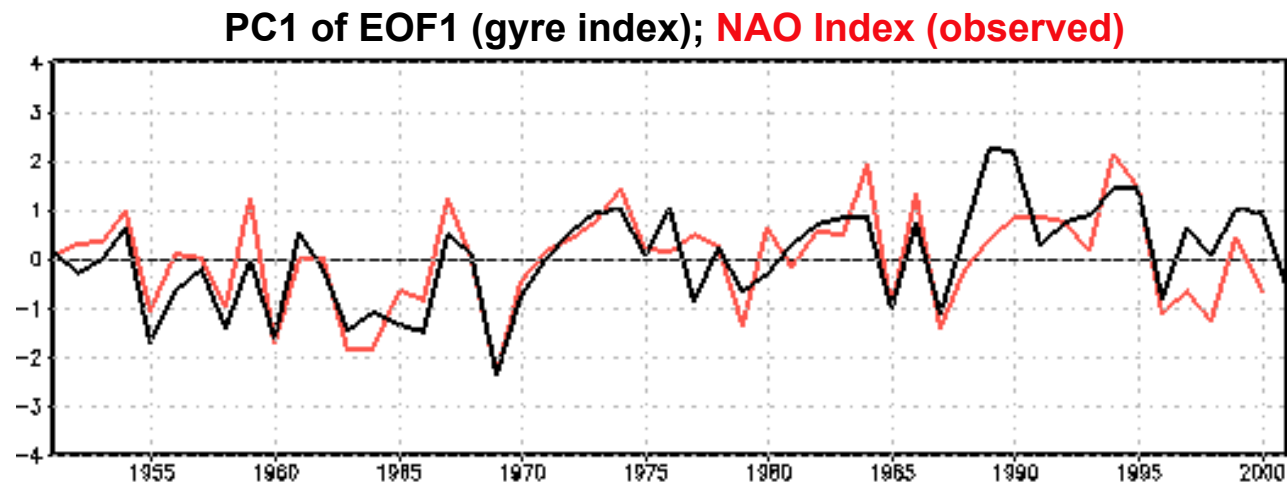
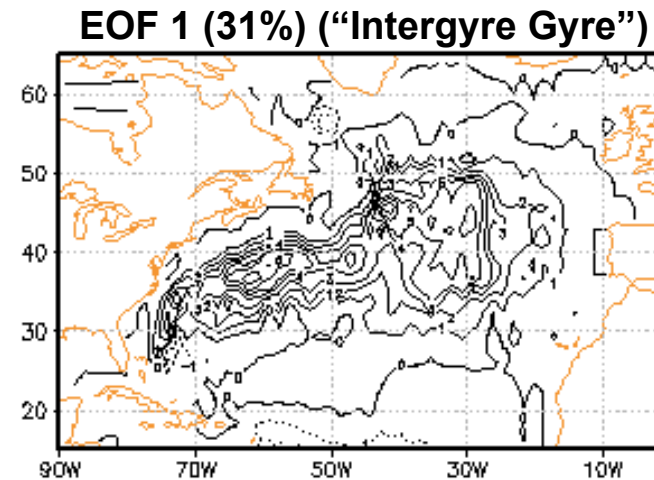
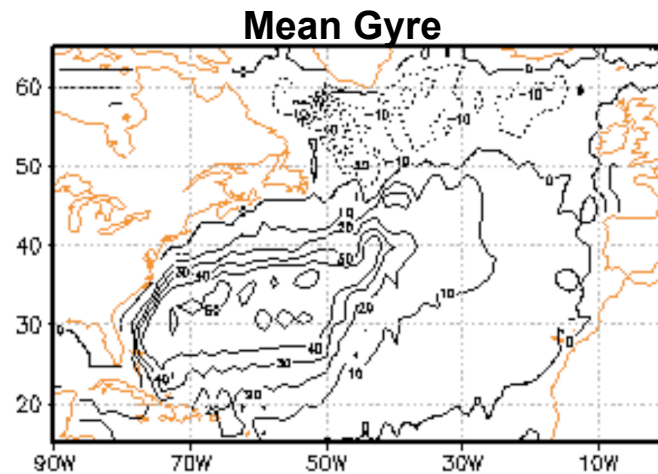
- The tripole index is locally forced by the weather noise heat flux ( $G_{ctl}$ ,  $NA_{ctl}$ ,  $NA_h$ ).
- Wind stress weather noise forces a tripole response that damps the full response.

# Extract Model Patterns by Regression of Simulation Results Against Observed Tripole Index

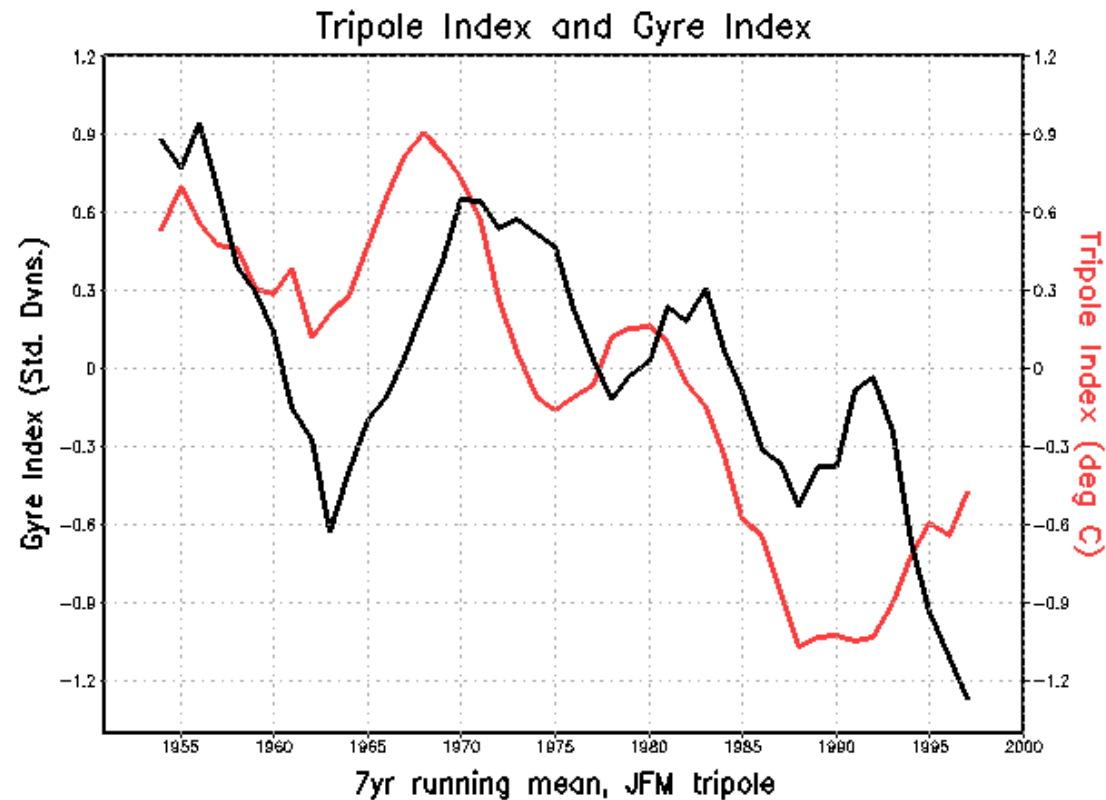




# Gyre Circulation and Variability in NAtl

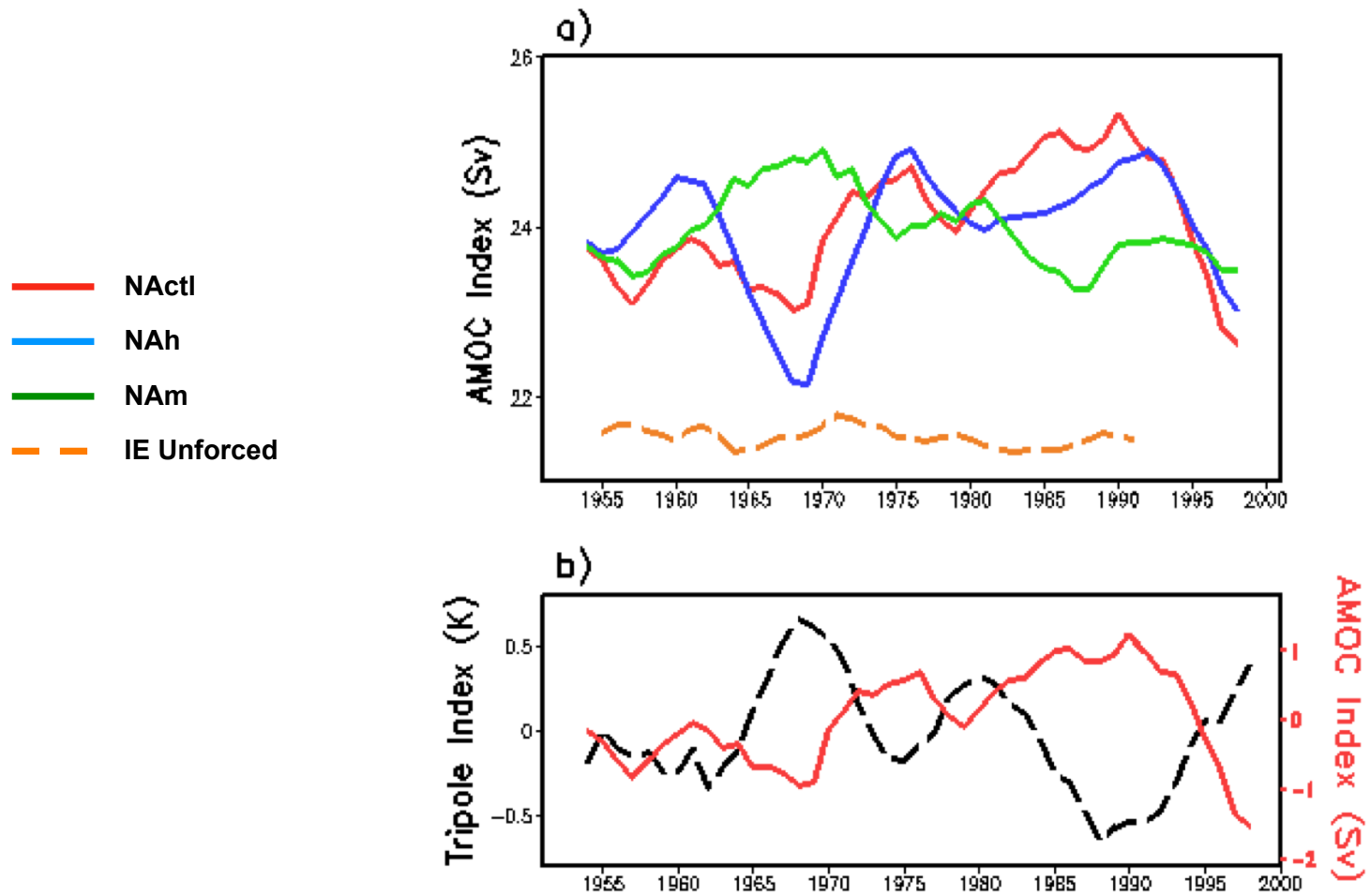


# Tripole and Intergyre Intergyre Gyre Indices NActl



Gyre index: area avg. streamfn., 60°W-40°W, 35°-45°N

# AMOC



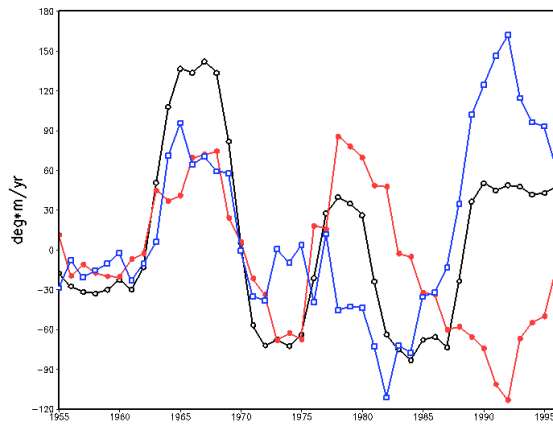
# Heat Budget Analysis

- Vertical integral over full depth of the ocean
  - Heat storage tendency = dynamics tendency + surface heat flux
    - Surface heat flux is total (noise + feedback)
    - Heat storage tendency calculated from monthly mean output
    - Dynamics tendency obtained as residual

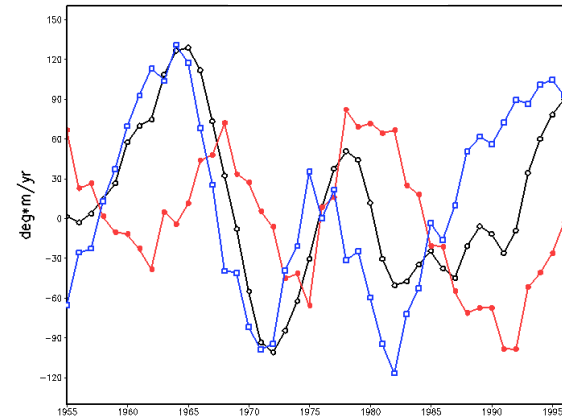
# Heat Budget Tendencies

## 7 year running annual means

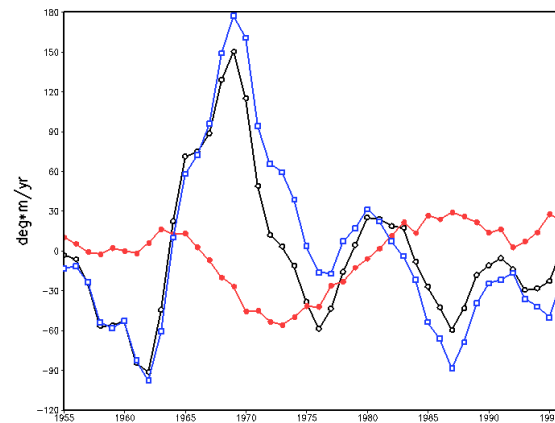
NActl



NAh

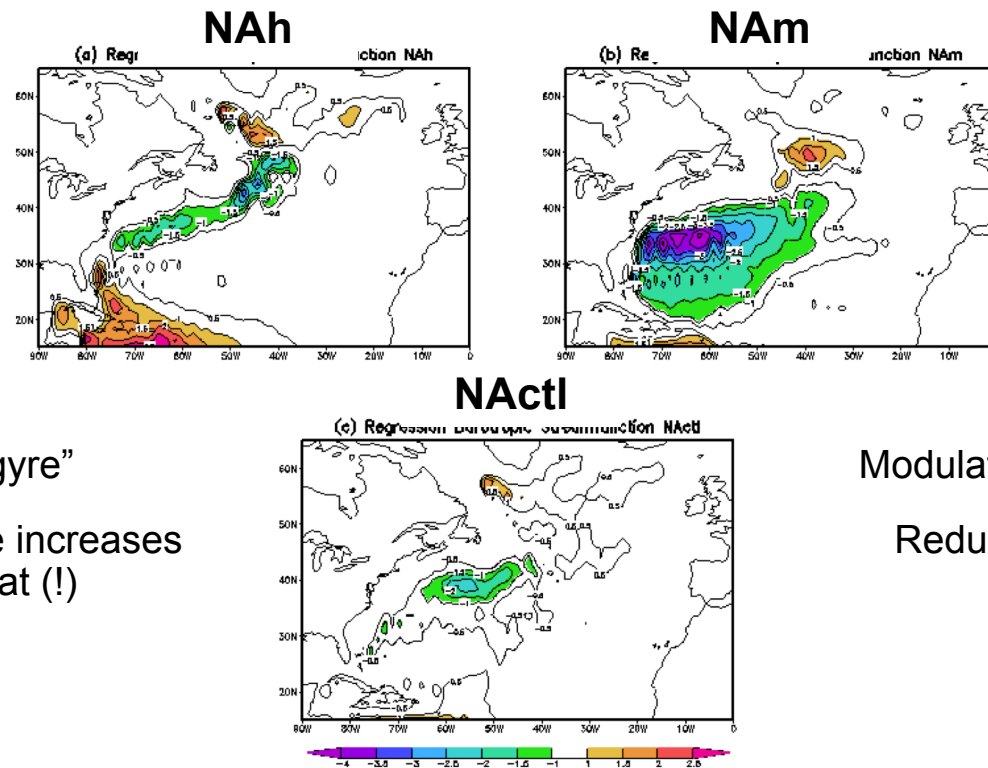


NAm



- Heat storage tendency
- Net surface heat flux
- Ocean Dynamics tendency

# Regression of Barotropic Streamfunction Against Ocean Dynamics Tendencies



“Intergyre gyre”  
Counterclockwise increases  
tripole  $\Delta$  heat (!)

Modulation of mean gyres:  
Reduction increases  $\Delta$   
heat

# Simple Model

## Czaja and Marshall 2001

Interpretation: Parameterized ocean heat budget. Heat storage parameterized as proportional to  $\Delta T$

$$\frac{d\Delta T}{dt} = -\lambda\Delta T + \alpha N + g\psi_g \quad (1)$$

$\Delta T$  Tripole temperature difference, north minus south

$\psi_g$  Intergyre gyre strength (IGG, positive clockwise)

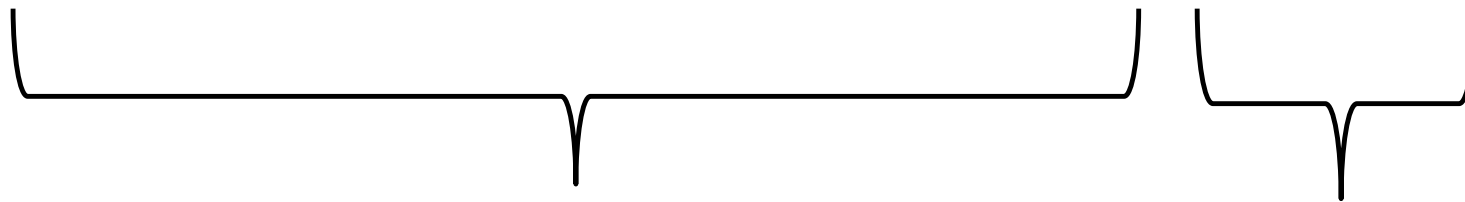
$N$  Tripole surface heat flux noise difference, north minus south

$\lambda$  Damping parameter

$g$  IGG heat storage tendency parameter (CM01 assume  $>0$ )

$\alpha = 1/(\rho c H)$  with heat budget interpretation, effective depth  $H$

$$\frac{d\Delta T}{dt} = -\lambda\Delta T + \alpha N + g\psi_g$$



Hasselmann model + Ocean dynamics



# Simple Model II

$$\tau = \gamma N - f' \Delta T$$

$\tau$  Tripole wind stress difference, north minus south

$\gamma$  Relates tripole wind stress to surface heat flux (<0)

$f'$  Feedback factor for tripole on wind stress, >0 when the feedback heat flux is >0.

$$\psi_g = a \int_{t-t_d}^t \tau dt \approx -f \Delta T \left( t - \frac{t_d}{2} \right)$$

$t_d$  Delay time for wind stress to set up the IGG, related to Rossby wave propagation

# Simple Model III

$$\frac{d\Delta T}{dt} = -\lambda\Delta T - fg\Delta T\left(t - \frac{t_d}{2}\right) + \alpha N \quad (2)$$

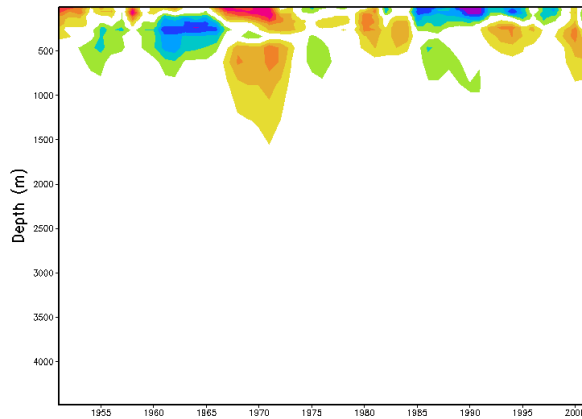
- Stochastically forced delayed oscillator equation.
- If  $N=0$ , properties governed by the parameter  **$R = fg/\lambda$** 
  - $R < 0$  solutions are damped, non-oscillatory
  - $R > 0$  solutions are oscillatory
    - $R < R_0$  decaying ( $1 < R_0 < \pi$ )
    - $R > R_0$  growing

# Simple Model Parameter Estimation and Results

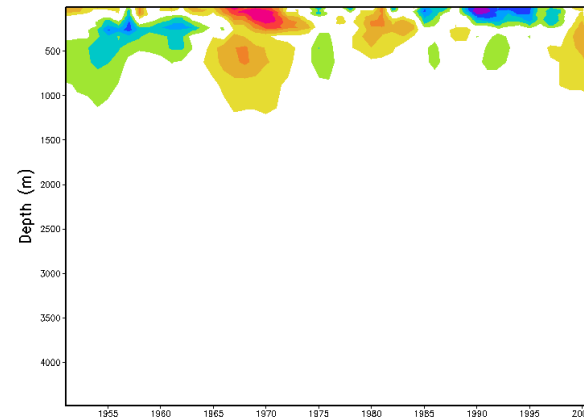
- With the heat budget interpretation, we can now determine the parameters  $\lambda$ ,  $f$ ,  $g$ ,  $H$ ,  $t_d$  from the properties of the numerical simulations.
- Use the simple model to estimate the predictability of the tripole.
  - ❖ Annual mean data averaged over the calendar year.

# Vertical Structure of Annual Mean Tripole T: $H \approx 500\text{ m}$

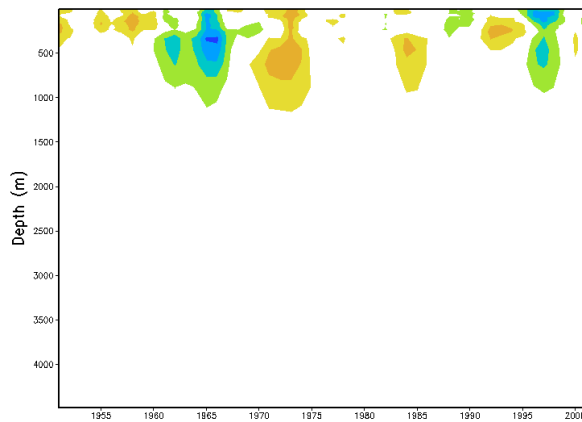
NActl



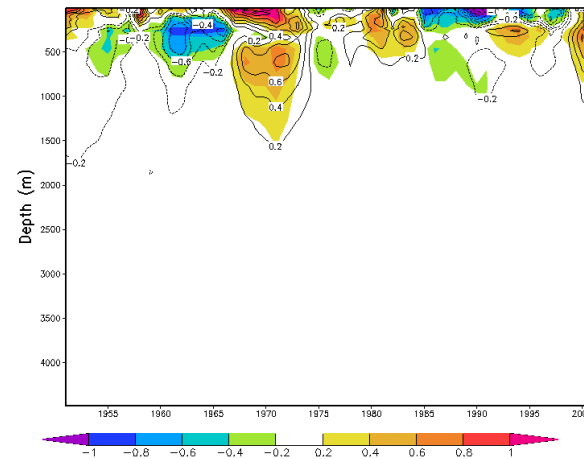
NAh



NAm



NActl and NAh+NAm



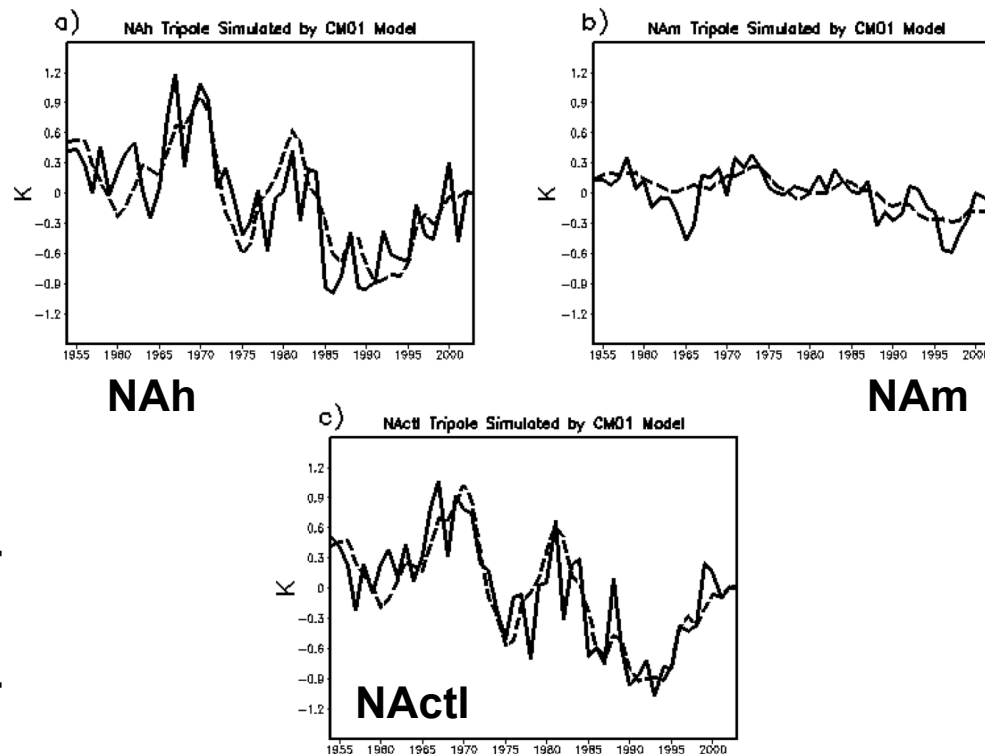
# Fit Parameters

- Define gyre index for IGG
  - Use the barotropic stream function from NAh (noise heat flux forcing only), averaged over a box between the two tripole boxes.
- Do lag regression of  $\Delta T$  against gyre index.
  - $t_d/2 = 3\text{-}4$  years
  - $f = -3 \text{ K Sv}^{-1}$ 
    - Implies negative heat flux feedback on tripole SSTA

- **$R = 0.48$** 
  - $0 < R < 1$  implies the unforced solutions are damped oscillatory
- **$g = -0.054 \text{ K Sv}^{-1} \text{ yr}^{-1}$** 
  - So  $g < 0$ , while CM01 assert  $g > 0$  is a given
  - Therefore counter-clockwise IGG increases tripole  $\Delta T$

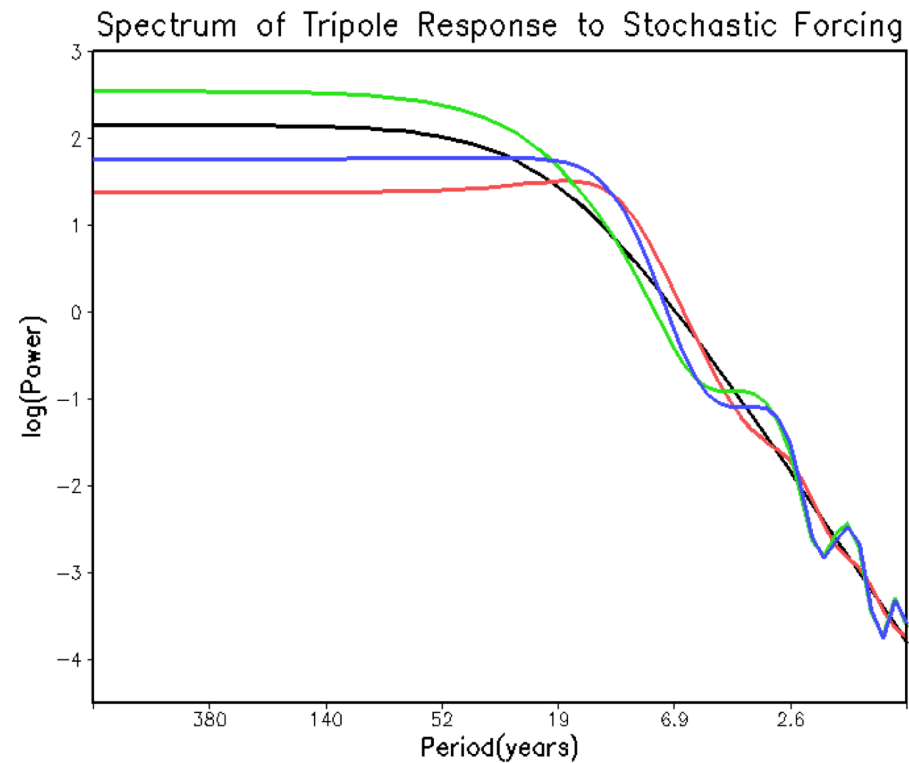
## Simple Model (eq. 3) Verification

- Force with observed heat flux noise
- Use initial conditions 1950-1953, observed noise



# Power Spectrum of Response to Stochastic Forcing

- **Black:** Hasselmann
- **Blue:** full model
- **Red:** feedback wind stress only
- **Green:** noise wind stress only





# Implications for Predictability

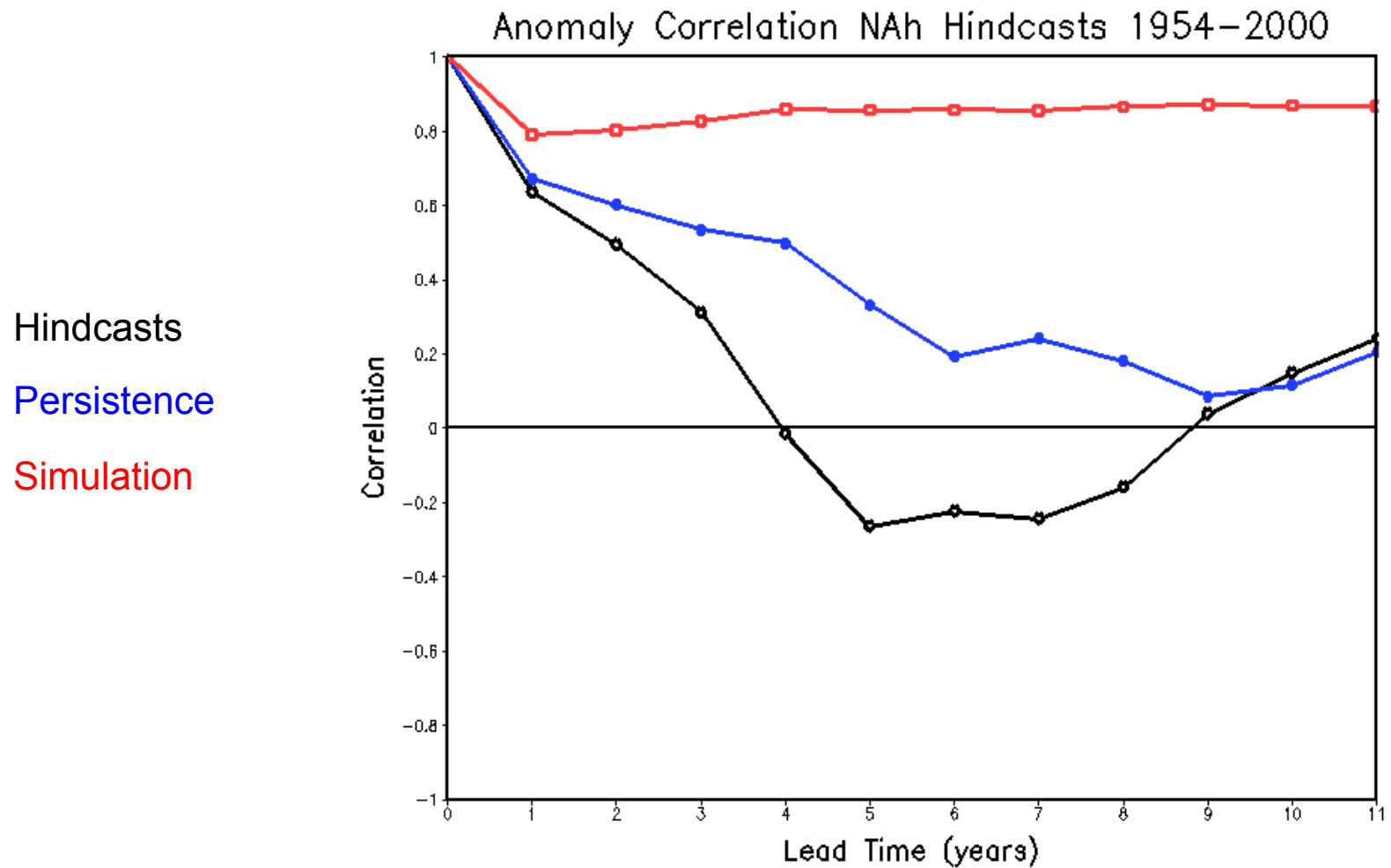
- Tripole is weather noise forced, but the weather noise can't be predicted.
  - Therefore weather noise destroys predictability.
  - Predictability arises from accuracy of the initial state, realism of the model feedbacks.
  - Hypothesis: the best model to make predictions is the interactive ensemble with weather noise forcing = 0, best ocean initial state.

## Example: Retrospective Predictions with Simple Model (Hindcasts)

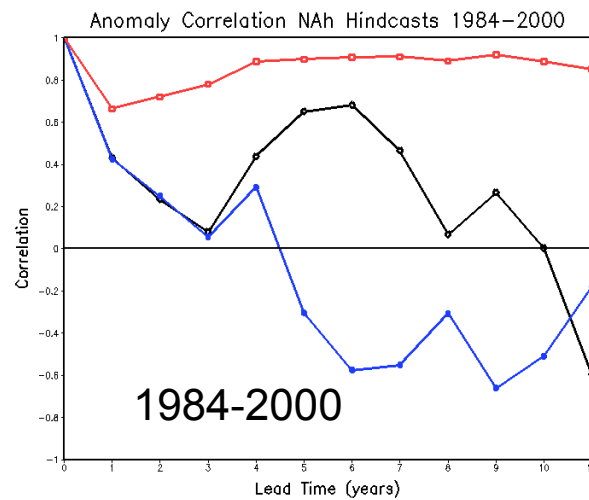
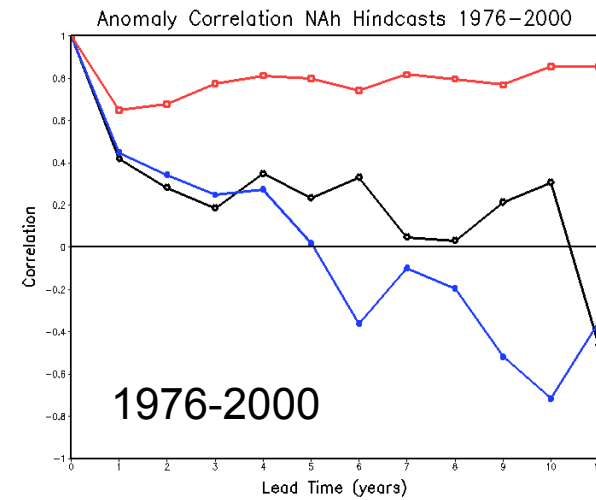
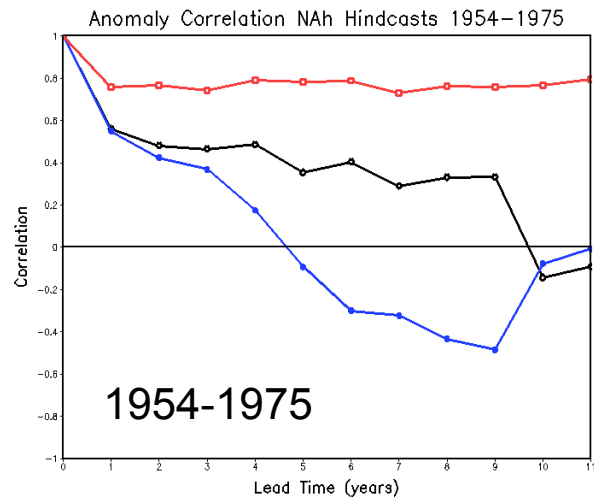
$$\frac{d\Delta T}{dt} = -\lambda\Delta T - fg\Delta T\left(t - \frac{t_d}{2}\right) + \alpha N$$

- Set heat flux noise to zero
- NAh initial conditions
  - Need  $\Delta T$  for 3, 2, and 1 years before initial time
  - Initial growth possible, but turns out not to play an important role
- 12 year predictions starting each year 1954-1999
- Verified against NAh  $\Delta T$

# Hindcast Verification Simple Model



# Subperiods

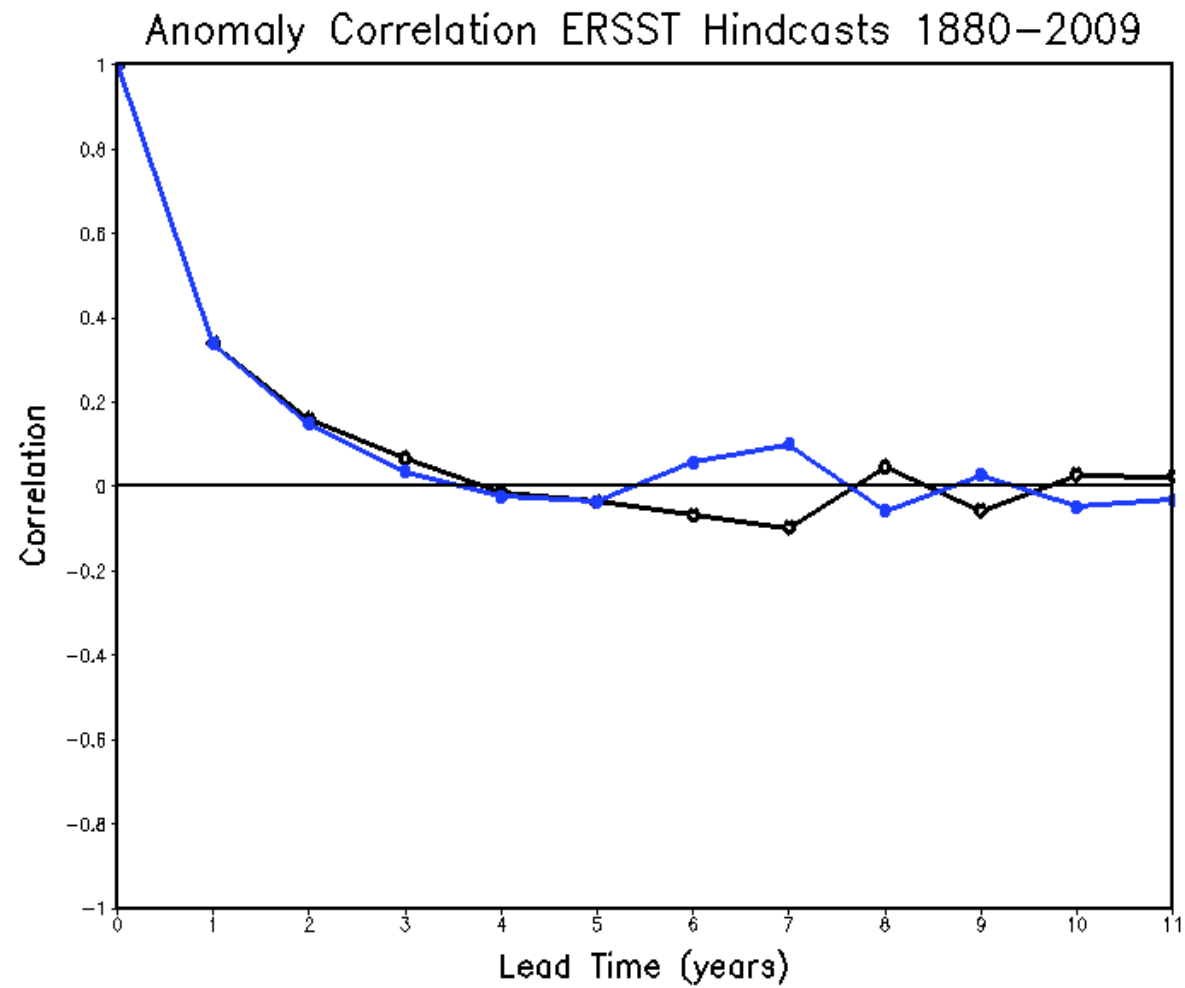


Hindcasts

Persistence

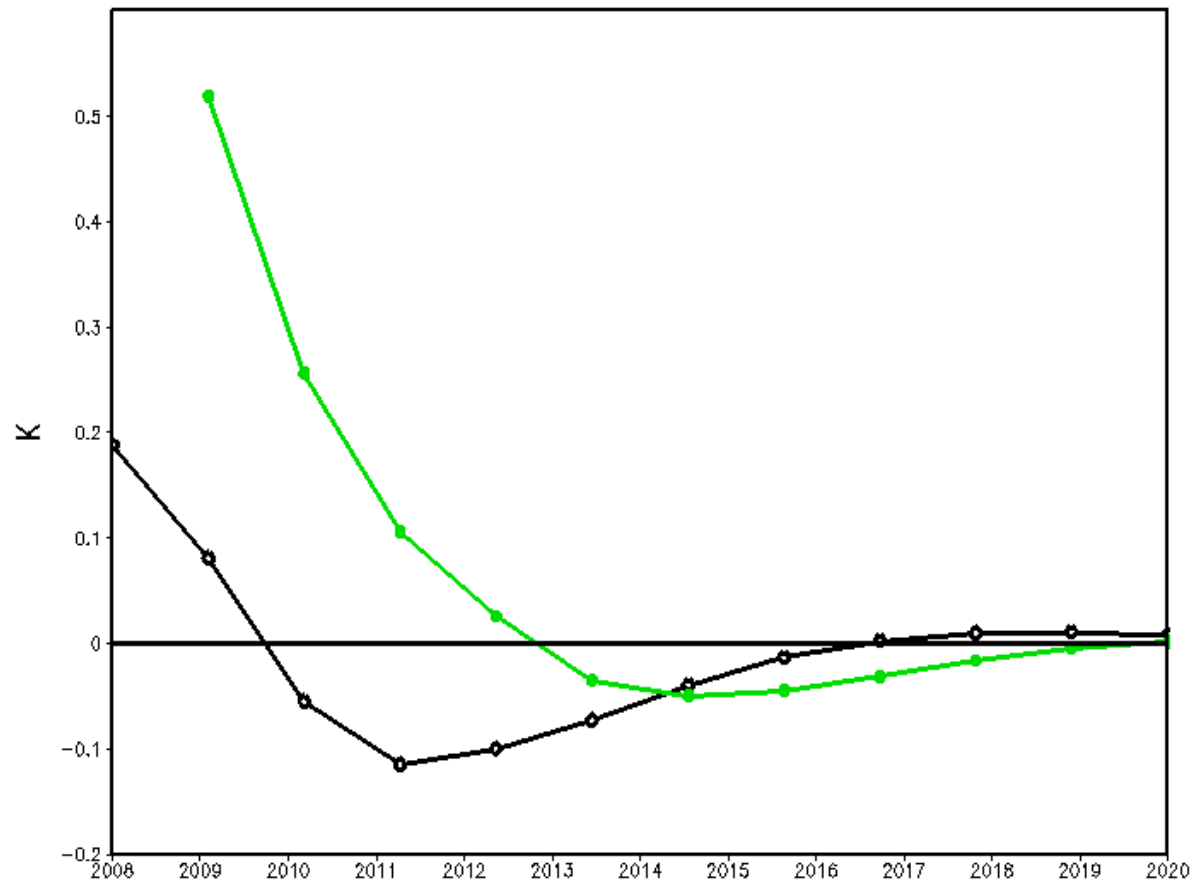
Simulation

# Hindcasts from 1880-2009 ERSST Initial Conditions



# Tripole $\Delta T$ Predictions from 2008 and 2009 ICs

Predicted Tripole Index, 2008 and 2009 Ann Mn ICs

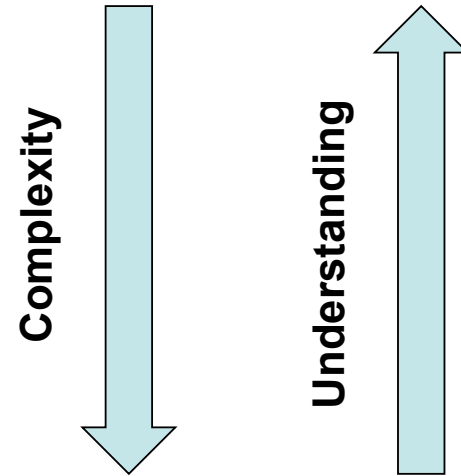


## COLA Model Diagnosis of the Observed North Atlantic SST Variability

- The reconstructed later 20th century North Atlantic tripole SST variability is predominantly forced by the local weather noise.
- In the context of the simple model of Czaja and Marshall (2001), the tripole is in a damped oscillatory regime, even though the atmospheric heat flux feedback to the tripole is negative, because the intergyre gyre carries heat in the opposite direction from that found/assumed in other studies.
- A decadal peak in the spectrum should result from the simple model with  $R > 0$  forced by white noise (Czaja and Marshall 2001).
- The simple model indicates no decadal predictability of the tripole variability.

# Hierarchy of Models

- CGCM or reanalysis
- Intermediate Coupled model
- AGCM ensemble
- Czaja/Marshall model
- Barsugli Battisti model
- Hasselmann model





# For Additional Details

- Wu, Z., E. K. Schneider, and B. P. Kirtman, 2004: Causes of low frequency North Atlantic SST variability in a coupled GCM. *Geophys. Res. Lett.*, **31**, L09210, doi:10.1029/2004GL019548.
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