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International Centre for Theoretical Physics**



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**Joint ITER-IAEA-ICTP Advanced Workshop on Fusion and Plasma Physics**

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**Physics of Energetic Ions in Tokamaks**

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SWITZERLAND*

# Physics of Energetic Ions in Tokamaks

**Ambrogio Fasoli**

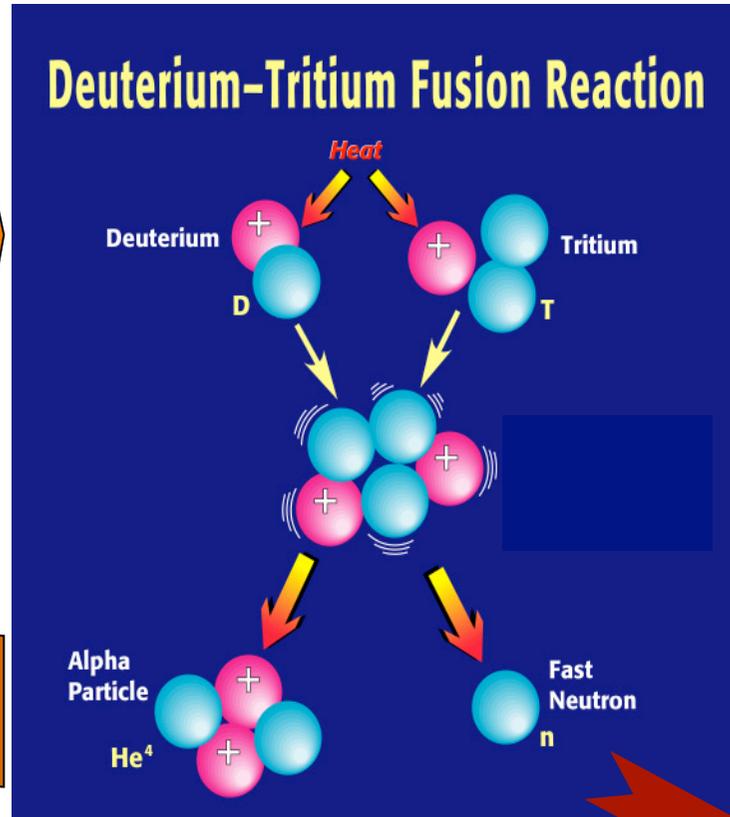
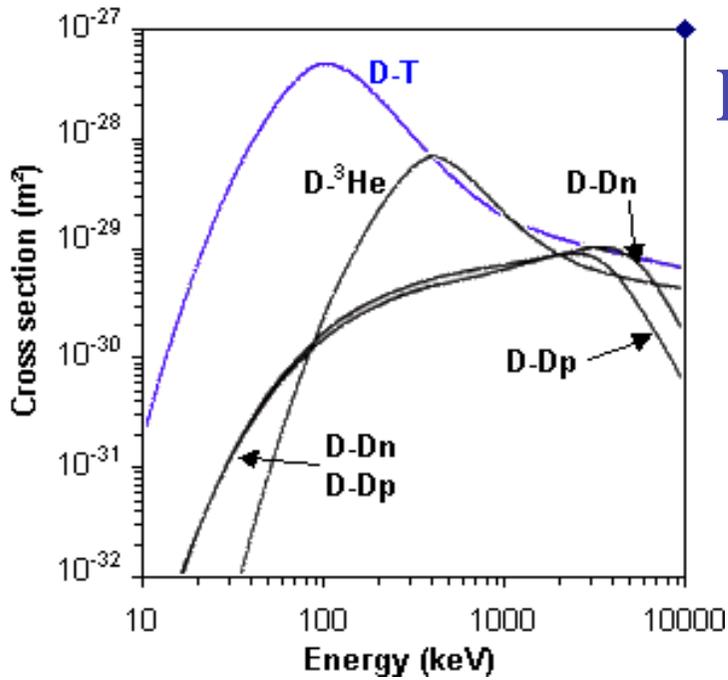
**Centre for Research in Plasma Physics (CRPP)  
Association EURATOM-Swiss Confederation  
Swiss Federal Institute of Technology, EPFL Lausanne\***



ITER-IAEA-ICTP Advanced Workshop, Trieste, October 2011

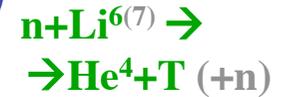


# Fusion reactions



Plasma self-heating

Tritium replenishment



Energy for electricity



# Definition of a burning plasma

- Fusion power density  $\equiv P_{\text{fusion}} = \frac{1}{4}n^2 \langle \sigma v \rangle E_{\text{fusion}}$  ( $n_D = n_T = n/2$ )
- $\alpha$  power density  $\equiv P_{\alpha} = 0.2 P_{\text{fusion}}$
- Thermal energy  $W \equiv 3nT$
- Energy balance

$$dW/dt = \underbrace{P_{\alpha}}_{\alpha\text{-heating}} + \underbrace{P_{\text{heat}}/V}_{\text{ext. heating}} - \underbrace{W/\tau_E}_{\text{losses}}$$

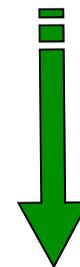
- Fusion energy gain:  $Q \equiv P_{\text{fusion}}/P_{\text{heat}} = 5 P_{\alpha}/P_{\text{heat}}$
- $\alpha$  heating fraction:  $f_{\alpha} \equiv P_{\alpha}/(P_{\alpha} + P_{\text{heat}}) = Q/(Q+5)$

$Q=1$   $f_{\alpha}=17\%$  *breakeven*

$Q=5$   $f_{\alpha}=50\%$

$Q=10$   $f_{\alpha}=67\%$

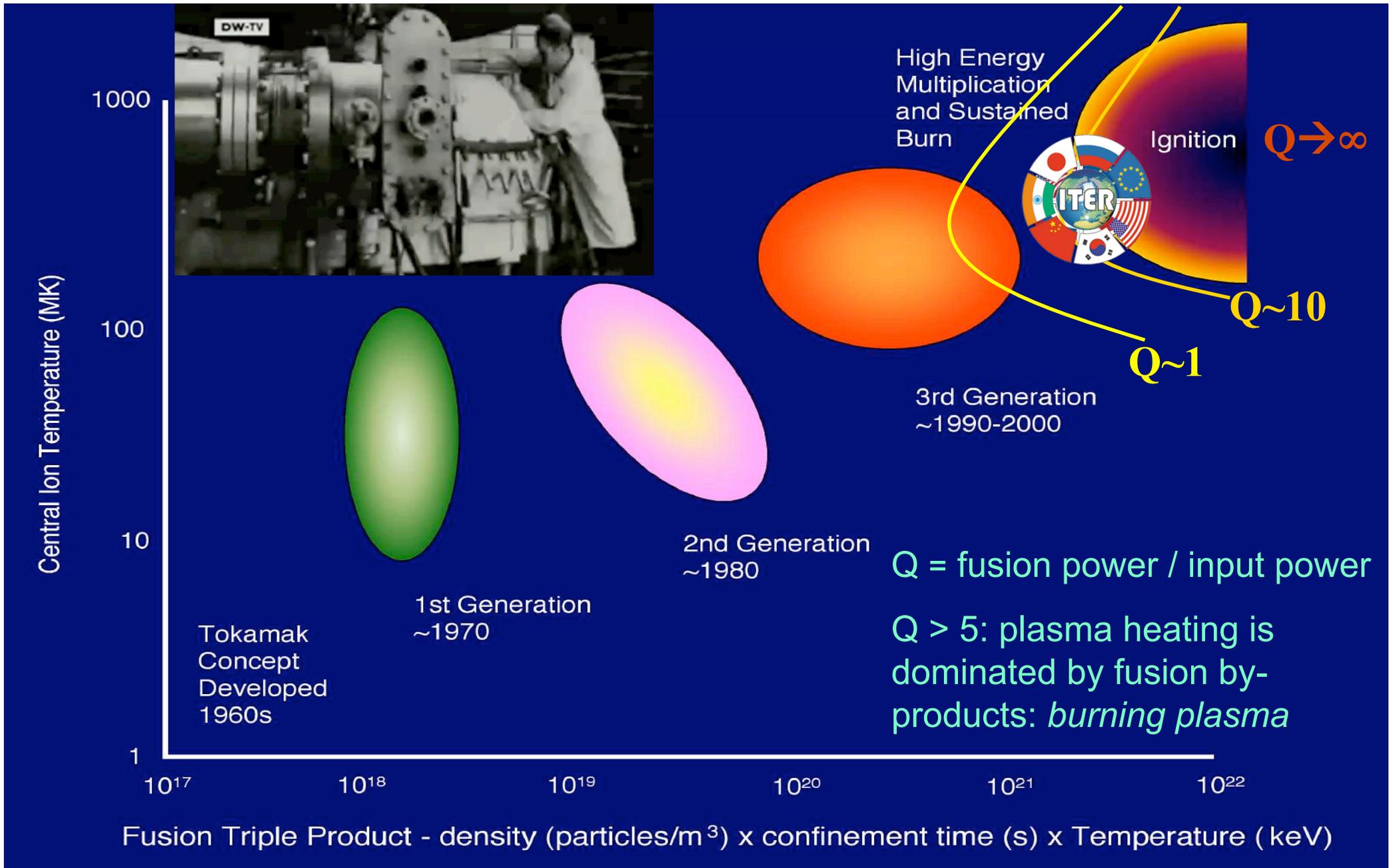
$Q=\infty$   $f_{\alpha}=100\%$  *ignition*



*burning  
plasma*



# Progress in magnetic fusion



# ITER

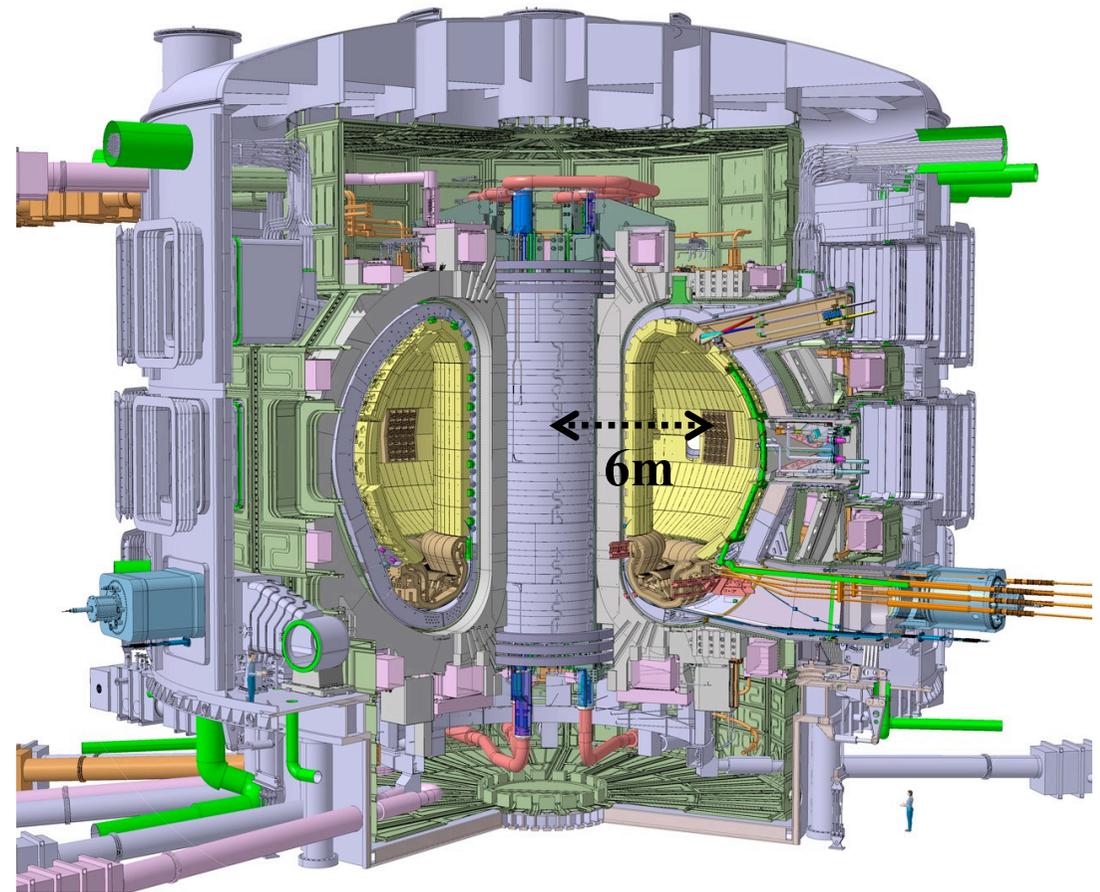
*Demonstration of the scientific and technological feasibility of fusion energy for peaceful purposes*

The first ever  
burning plasma

$$Q \geq 10$$

$$P_{\text{fusion}} \geq 500\text{MW}$$

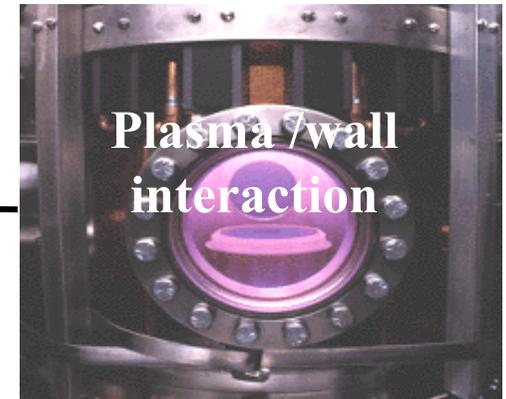
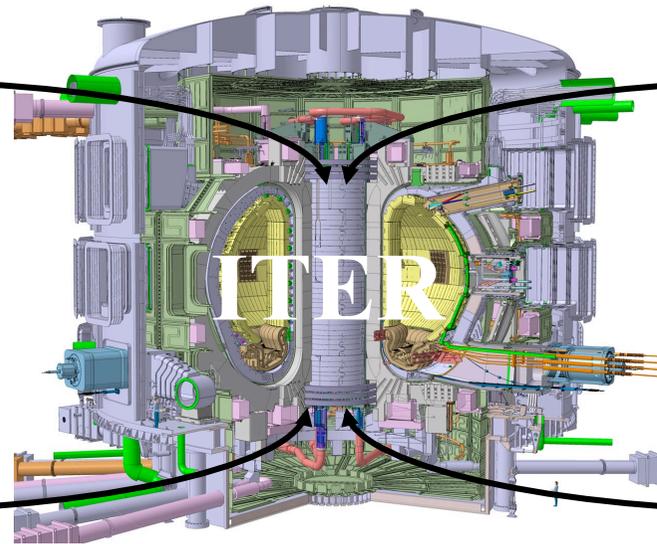
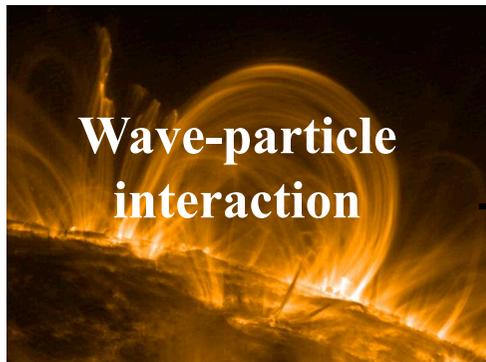
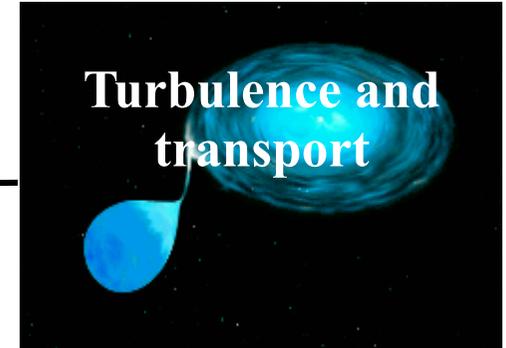
for ~500s



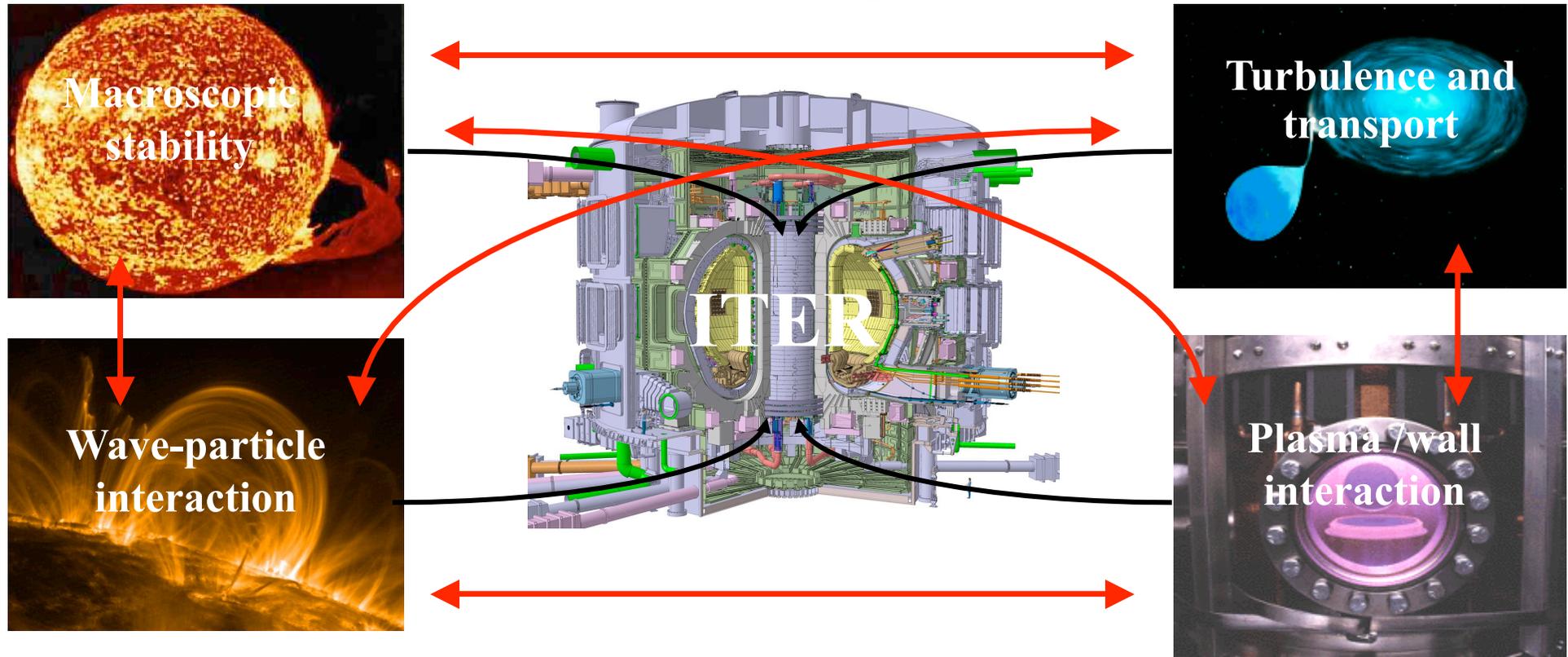
$$R \sim 6\text{m}; B \sim 5\text{T}; I_{\text{plasma}} \sim 15\text{MA}$$



# Progress in key physics areas is leading to next step burning plasma experiment



# Burning plasmas are complex systems in which all elements are coupled via the $\alpha$ 's

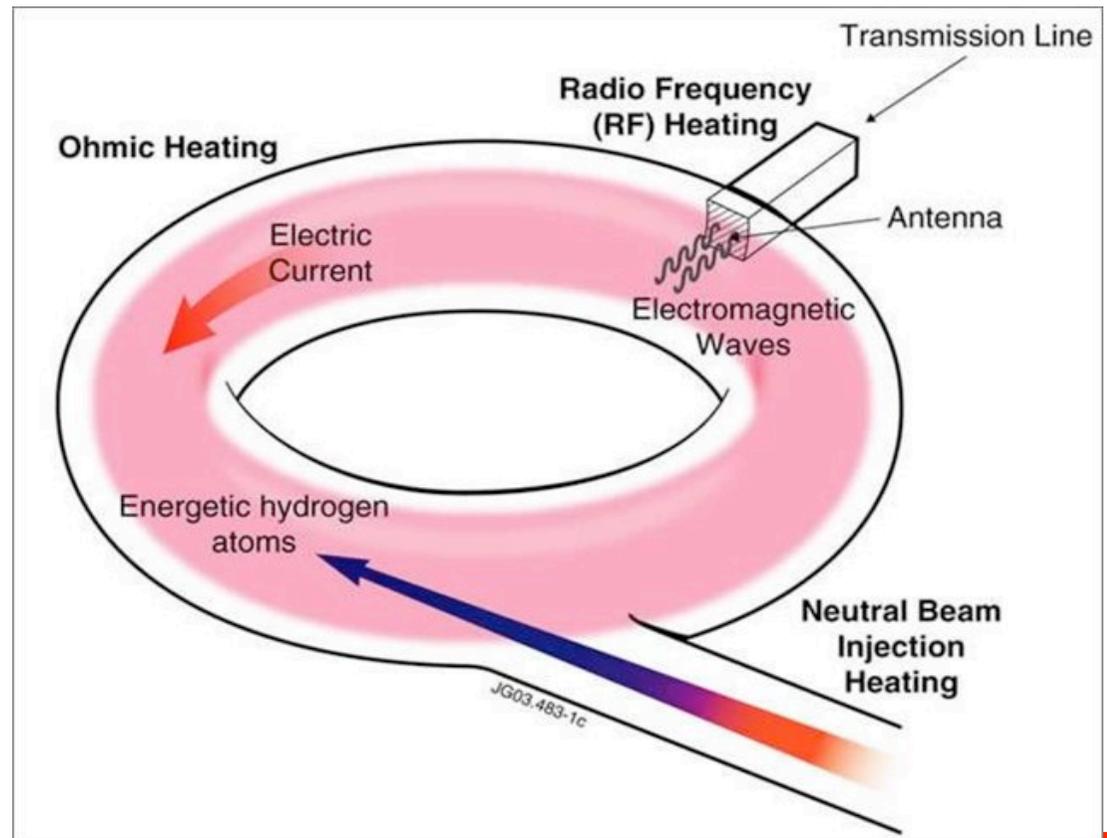


- The coupling of these elements makes extrapolations from weakly self-heated plasmas difficult and may lead to new phenomena
- A fundamental building block of burning plasma physics is the physics of energetic ions and the implications on self-heating

# Energetic ions from additional heating

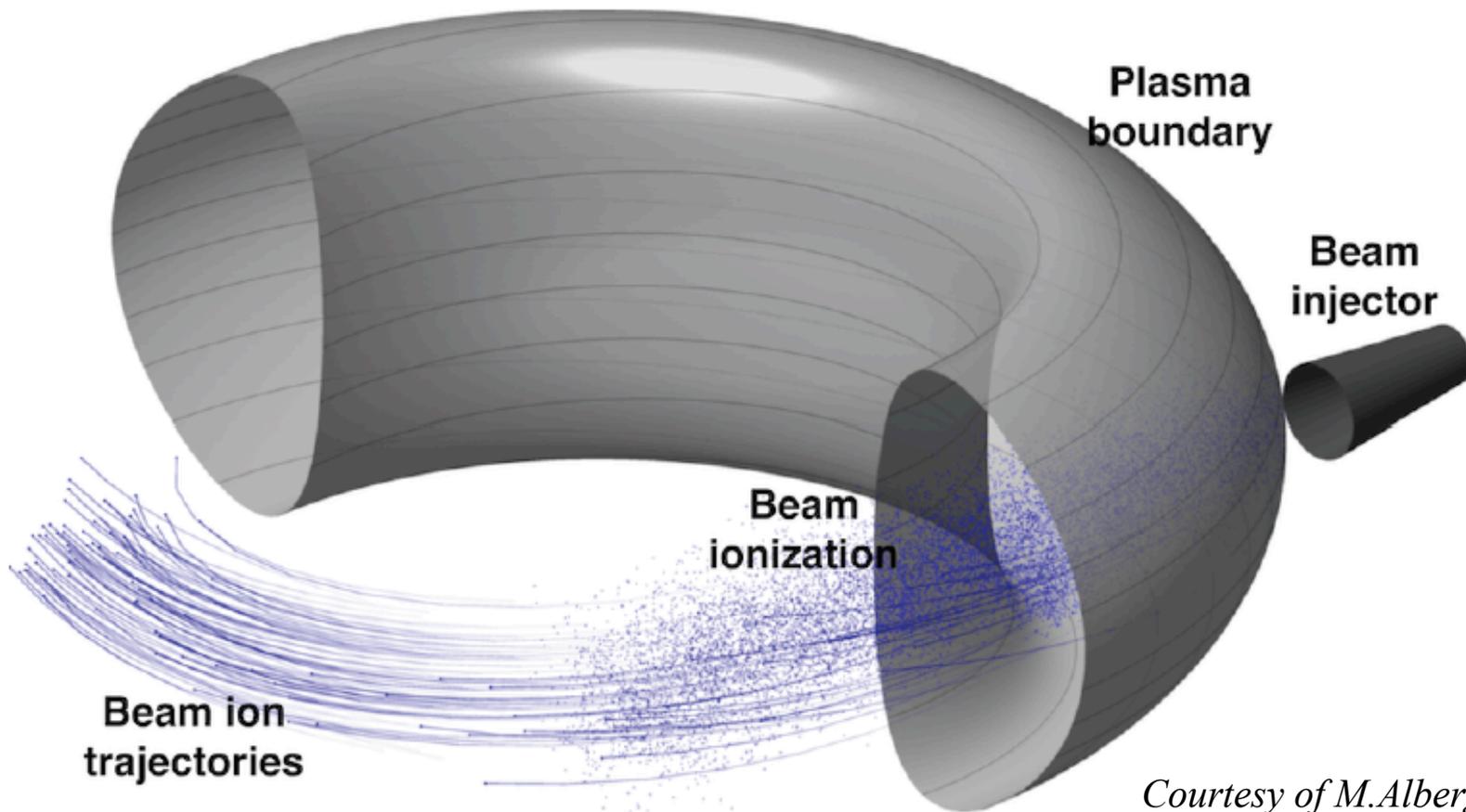
- Burning plasma regime is reached using external heating and current drive
  - *Electron cyclotron heating*
  - Ion cyclotron heating
  - Neutral beam heating

Based on creation of  $\sim$ MeV ions, then thermalised by collisions



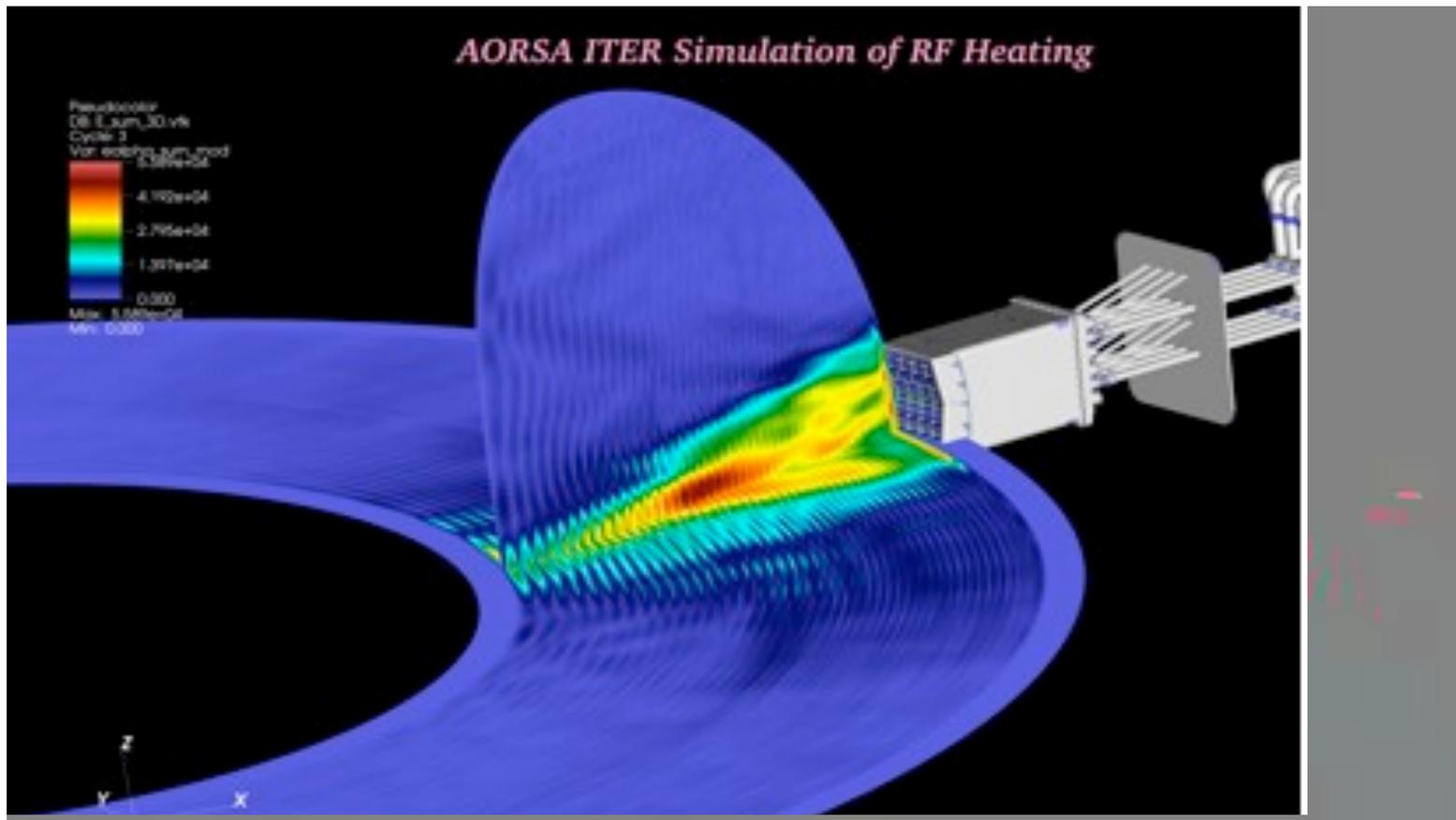
# Energetic ions from Neutral Beam Injection

- Ions at  $\sim 100\text{keV}$  in present devices,  $\sim 1\text{MeV}$  in ITER
- Injection geometry determines orbits. If tangential, mostly passing orbits

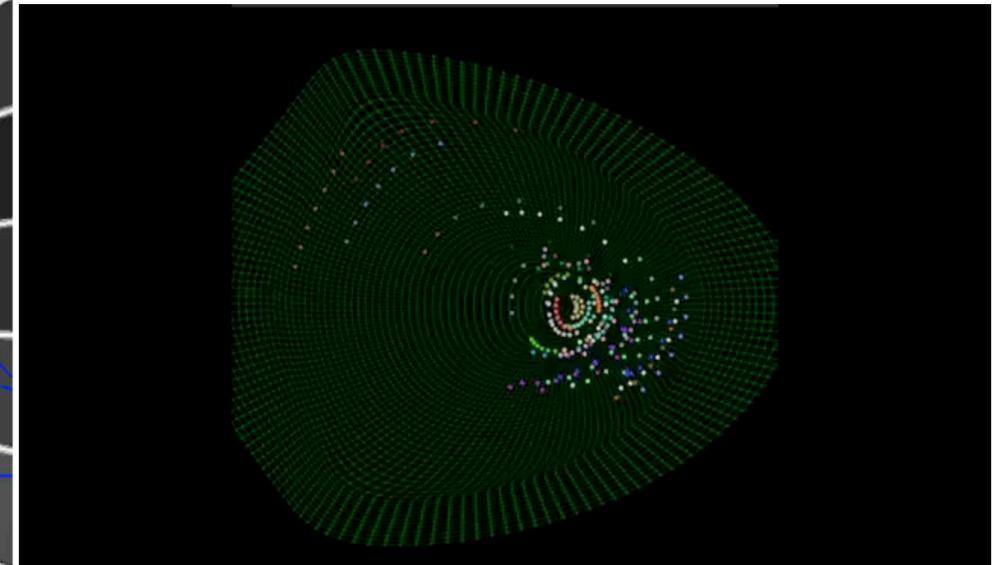
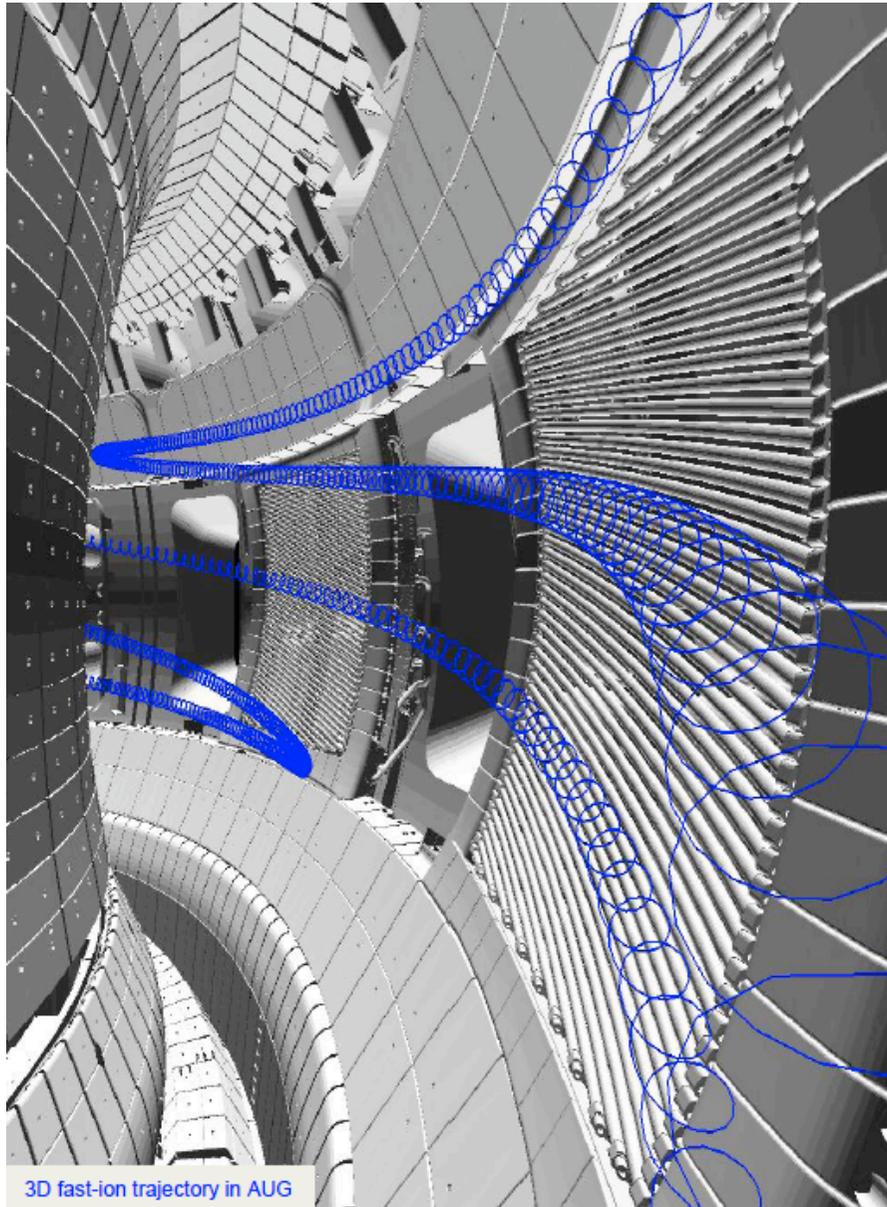


# Energetic ions from Ion Cyclotron Heating

- Wave fields at  $\omega \sim \omega_{ci}$  give energy to perpendicular motion of minority ions
  - Strongly anisotropic distribution function
  - Mostly trapped orbits



# Energetic ion orbits in tokamaks



GPU-NUBEAM DIII-D Simulation

# Sources of fast ions

Fast ion parameters in contemporary experiments compared with projected ITER values.

Tokamak	TFTR	JET	JT-60U	JET	ITER
Fast ion Source	Alpha Fusion	Alpha Fusion	Deuterium Co NBI	Alpha ICRF tail	Alpha Fusion
→ $\tau_S$ (s)	0.5	1.0	0.085	0.4	0.8
→ $\delta/a^a$	0.3	0.36	0.34	0.35	0.05
→ $P_f(0)$ (MW m <sup>-3</sup> )	0.28	0.12	0.12	0.5	0.55
→ $n_f(0)/n_e(0)$ (%)	0.3	0.44	2	1.5	0.85
→ $\beta_f(0)$ (%)	0.26	0.7	0.6	3	1.2
→ $\langle\beta_f\rangle$ (%)	0.03	0.12	0.15	0.3	0.3
→ $\max  R\nabla\beta_f $ (%)	2.0	3.5	6	5	3.8
→ $v_f(0)/v_A(0)$	1.6	1.6	1.9	1.3	1.9

*A.Fasoli et al.,  
NF (2007)*

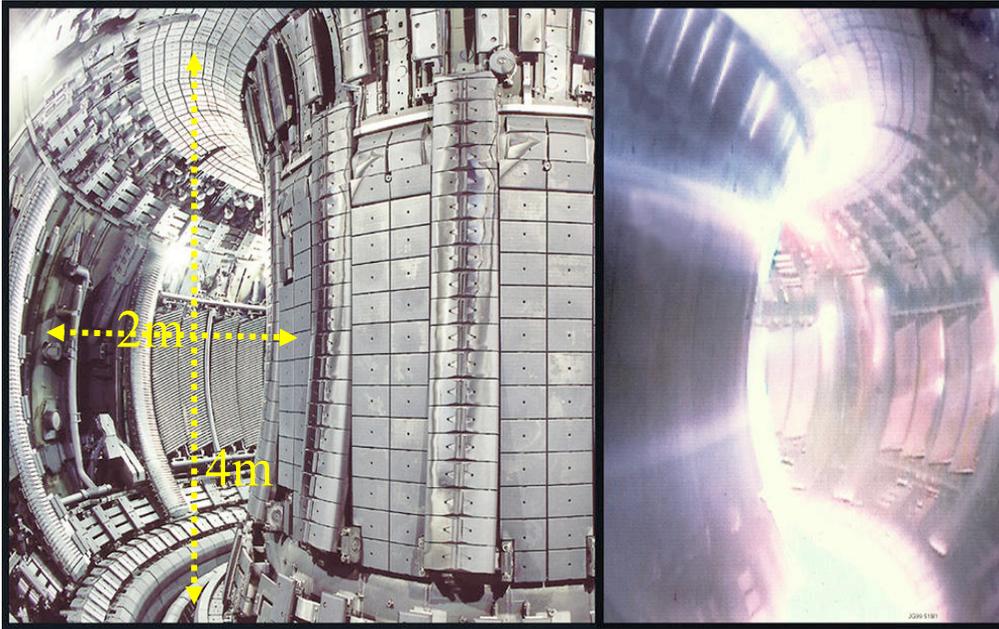
<sup>a</sup> Orbit shift from magnetic flux surface for banana particles:  $\delta = qp_f\sqrt{R/r}$ .

- Main differences between existing devices and ITER
  - Orbits: anisotropy, size relative to machine size:  $\rho^*_{fast} \gg \rho^*_{fast,ITER}$
  - Slowing down relative to confinement time  $\tau_S/\tau_E \gg \tau_S/\tau_{E,ITER}$



# Measurement of confined energetic ions Neutron / $\gamma$ ray emission profiles

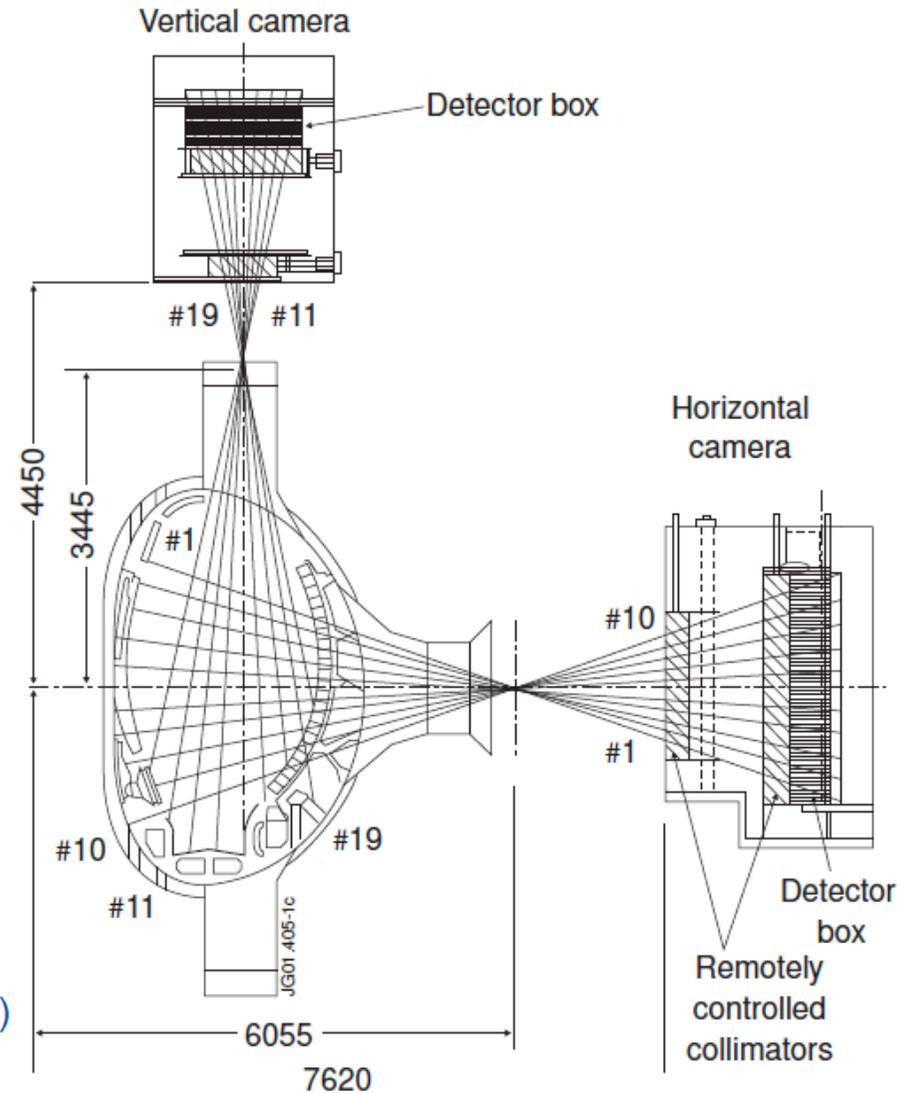
## The JET tokamak



$R \sim 3\text{m}$ ;  $B_T \leq 4\text{T}$ ;  $I_p \leq 4\text{MA}$ ; D, H, He, D-T

### Detectors:

- NE213 liquid scintillators (2.5 & 14 MeV)
- Bicron-418 plastic scintillators (14 MeV)
- CsI(Tl) photo-diodes (hard X-rays and  $\gamma$ -rays)



Courtesy of V.Kiptily



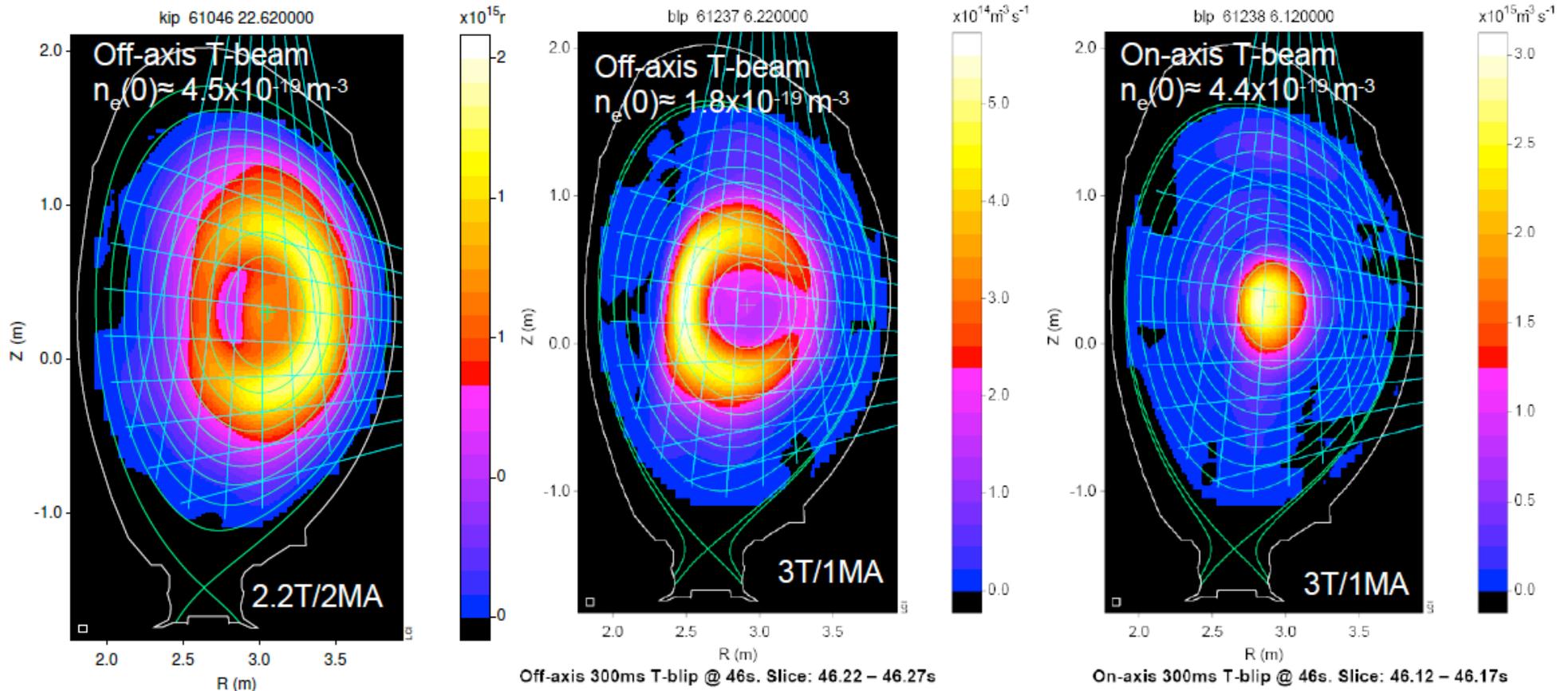
EUROPEAN FUSION DEVELOPMENT AGREEMENT



# Evidence for fast ions in JET - NBI

## Neutron emission profiles in trace-T experiments

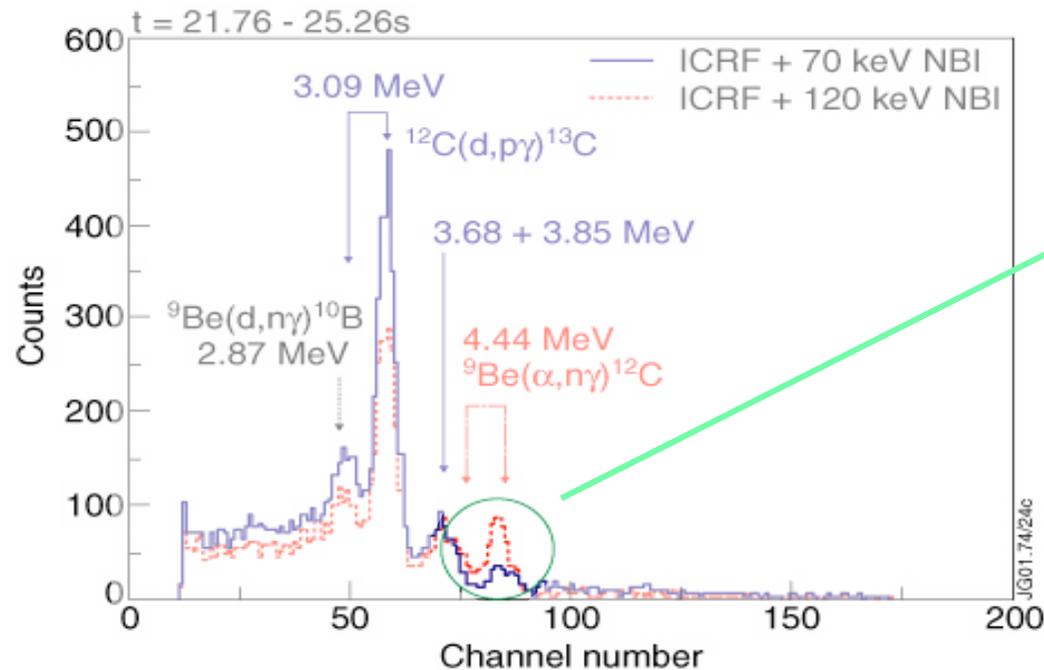
14-MeV neutron profile measurements in the **monotonic current** discharges with **T-NBI blips**



# Evidence for fast ions in JET – ICRH $\gamma$ -rays spectrum

Ex.:  ${}^4\text{He}$  acceleration by ICRH at  $f_{\text{ICRH}} = 3f_{\text{ci}}({}^4\text{He})$

$\gamma$ -ray emission spectrum

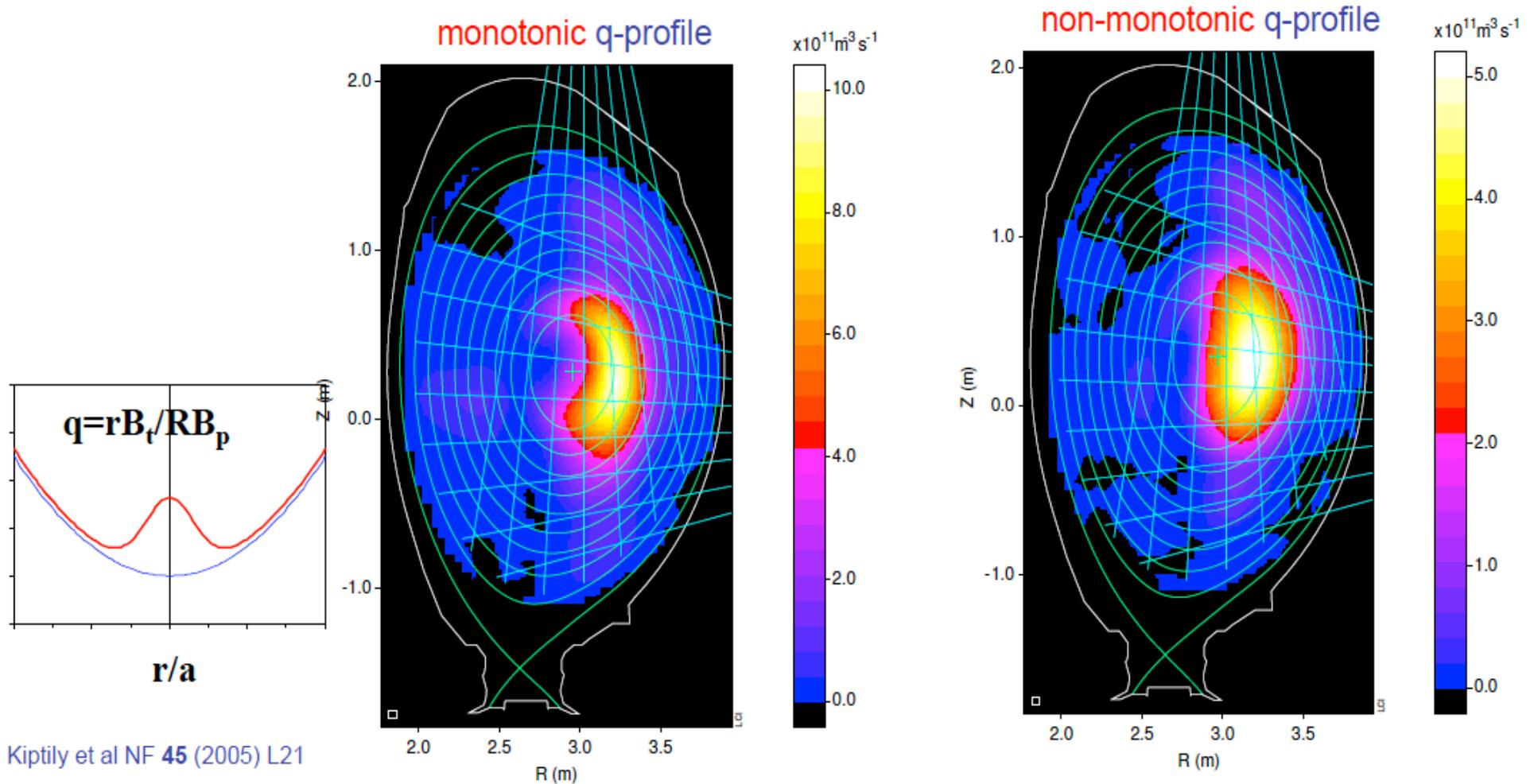


signal from reaction  
 ${}^9\text{Be}(\alpha, n\gamma){}^{12}\text{C}$   
 $\rightarrow$  signature of  ${}^4\text{He}$  ions with  
 $E_{\alpha} > \sim 2\text{MeV}$

# Evidence for fast ions in JET – ICRH

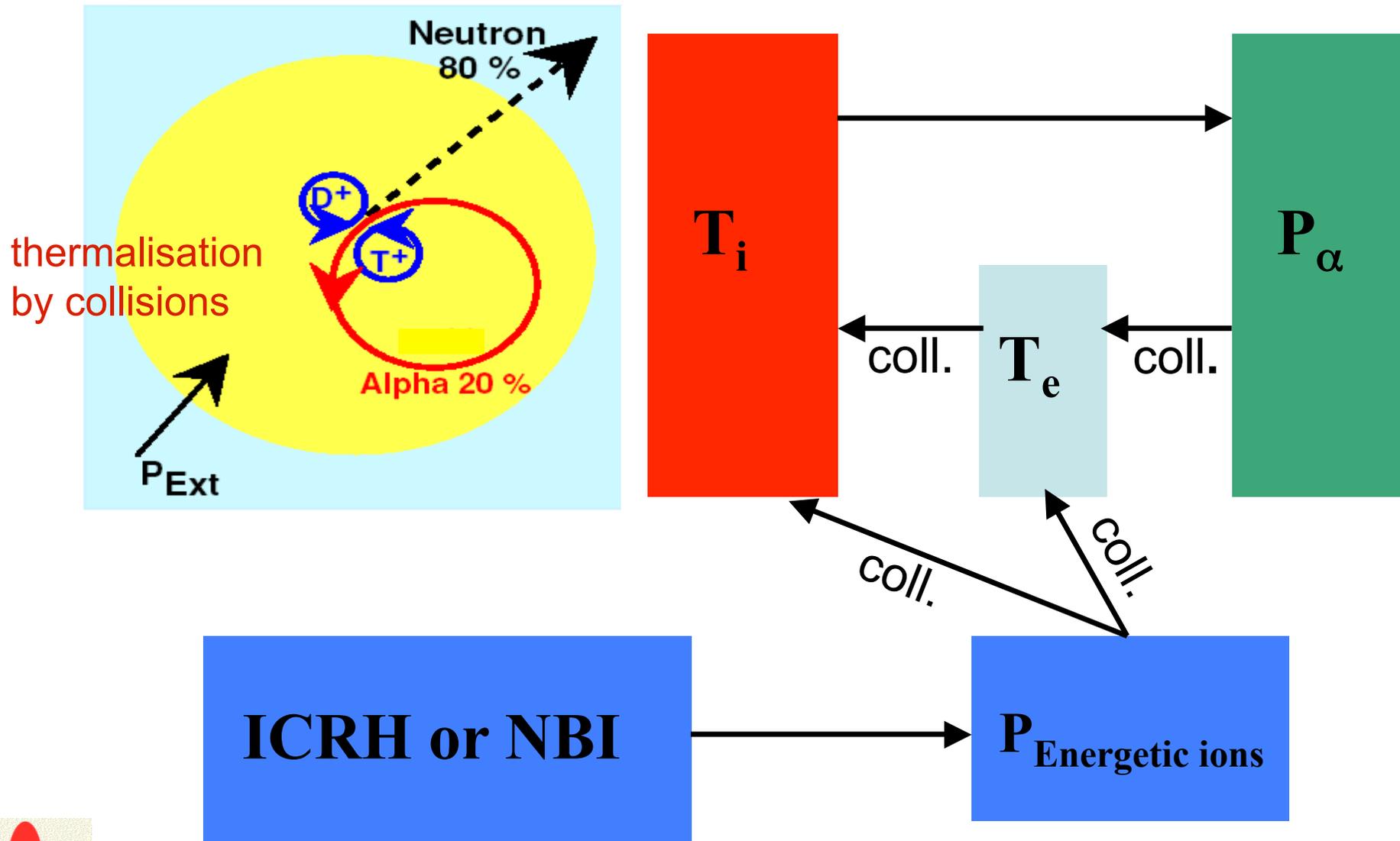
## $\gamma$ -rays profile

Ex.:  $^4\text{He}$  acceleration by ICRH at  $f_{\text{ICRH}} = 3f_{\text{ci}}(^4\text{He})$



Kiptily et al NF 45 (2005) L21

# External heating and self-heating



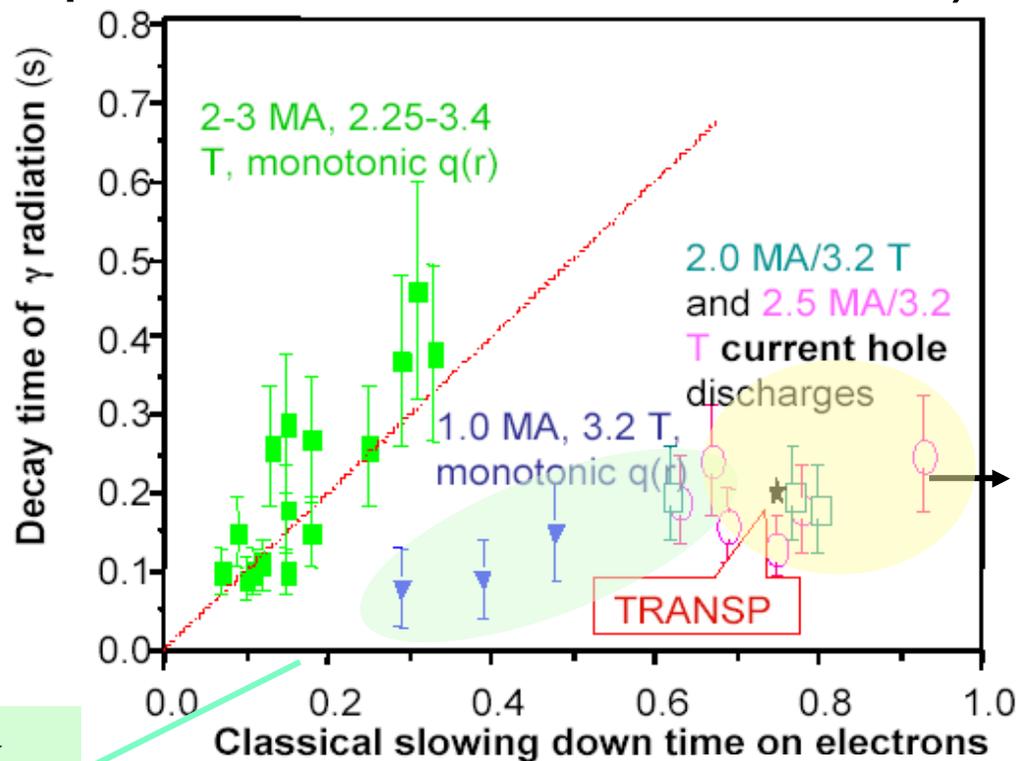
# External heating and self-heating

- To reach and sustain burning plasma regime, energetic ions must be well confined



# Self-heating: collisional slowing down

- JET trace T experiments:  $\gamma$ -ray spectroscopy  
→ direct observation of collisional slowing down  
(unless plasma current is too small)



Current profile not apt to confine  $\alpha$ 's

Too low current

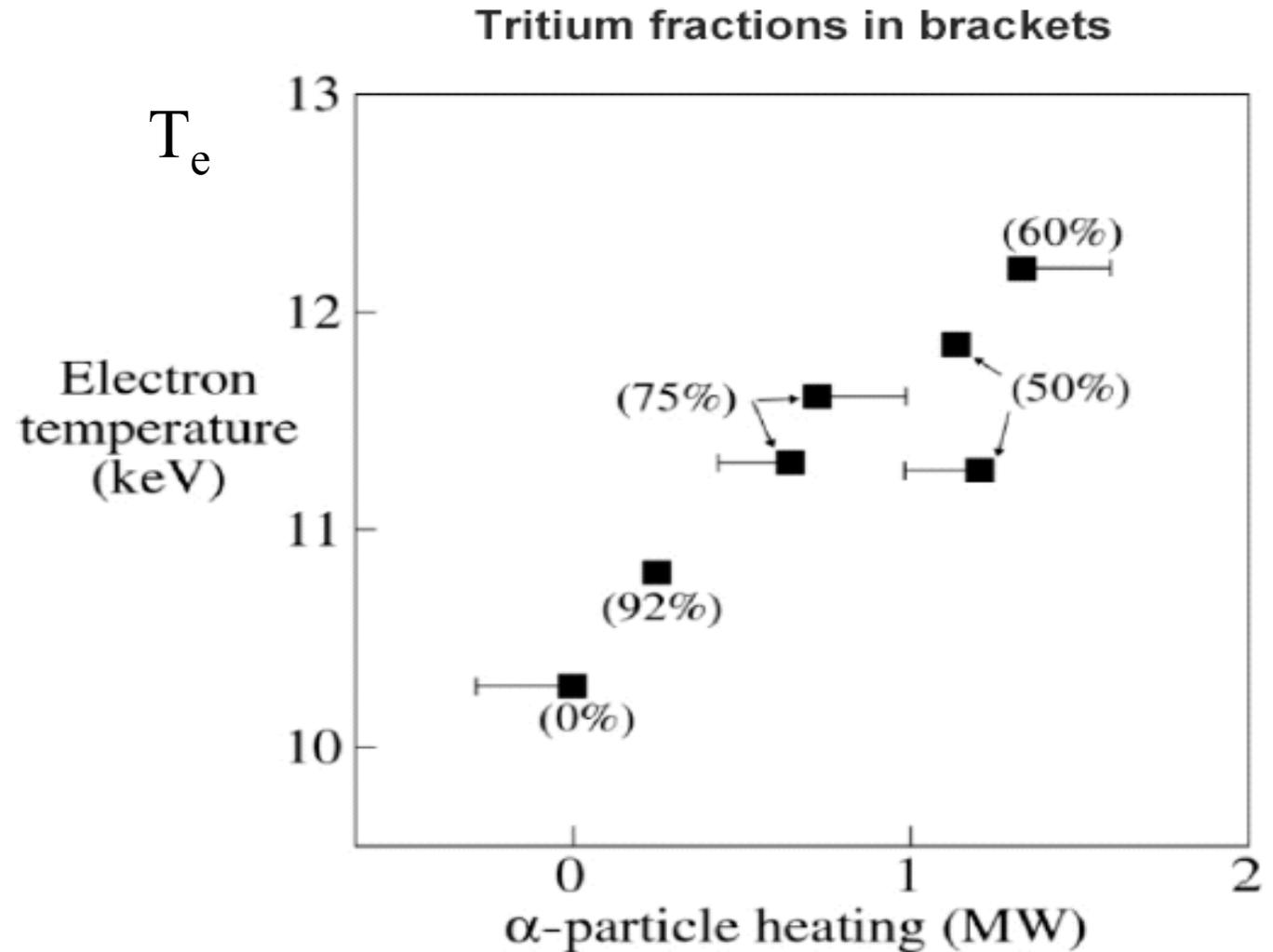


EUROPEAN FUSION DEVELOPMENT AGREEMENT



# Self-heating: $\alpha$ electron heating

- Electron heating in D-T ( $Q \approx 1$ ) on JET



# External heating and self-heating

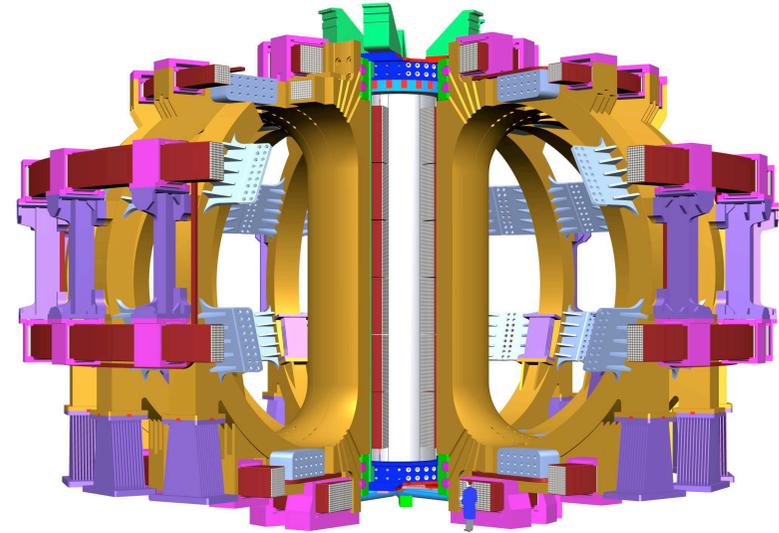
- To reach and sustain burning plasma regime, energetic ions must be well confined
- Need to understand and possibly minimize redistribution and loss mechanisms
  - Magnetic field imperfections (ripple and externally applied perturbations)
  - Low frequency MHD instabilities
  - Turbulence
  - Resonant interaction with Alfvén waves



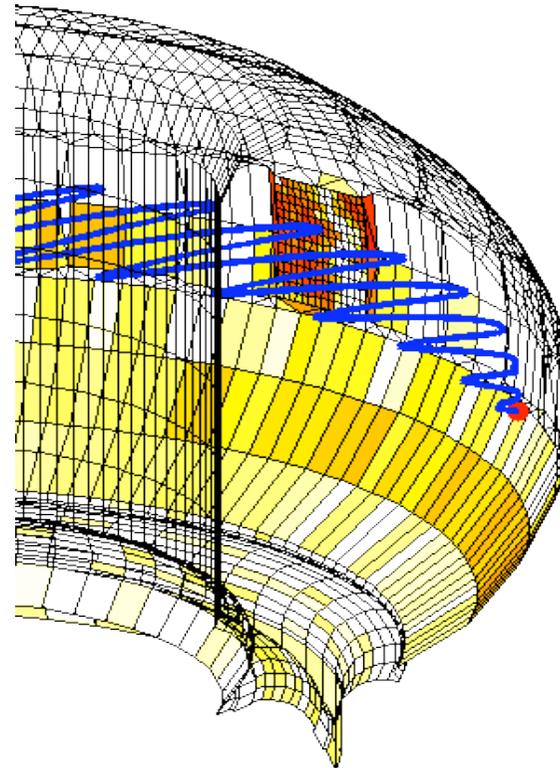
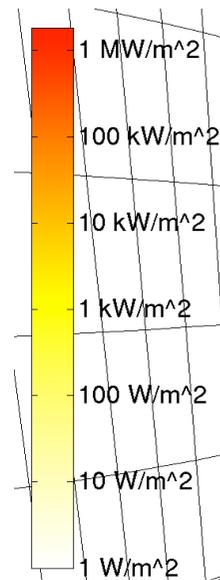
# Ripple losses

## ITER

- 18 toroidal field coils
  - Significant B-field ripple
  - Orbits can be calculated and power deposited on walls can be evaluated in Monte Carlo simulations



*ASCOT code*

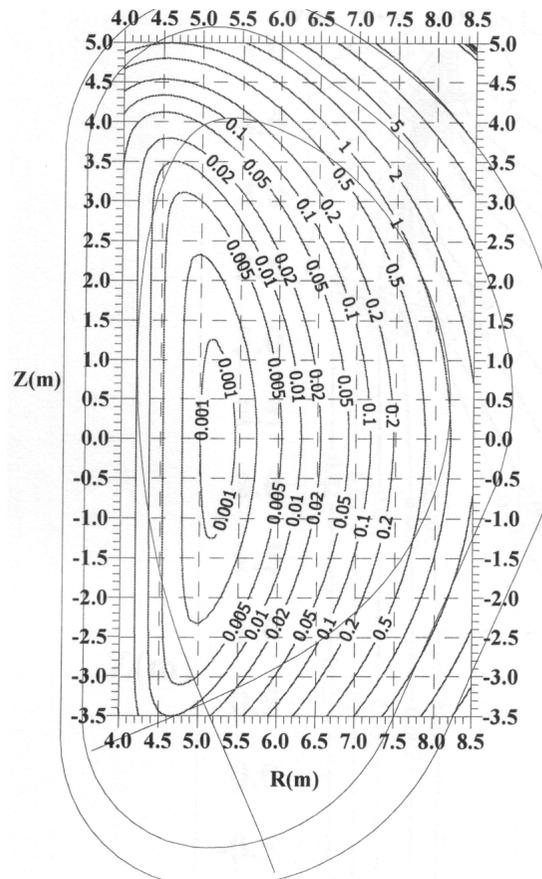


# Ripple losses - mitigation

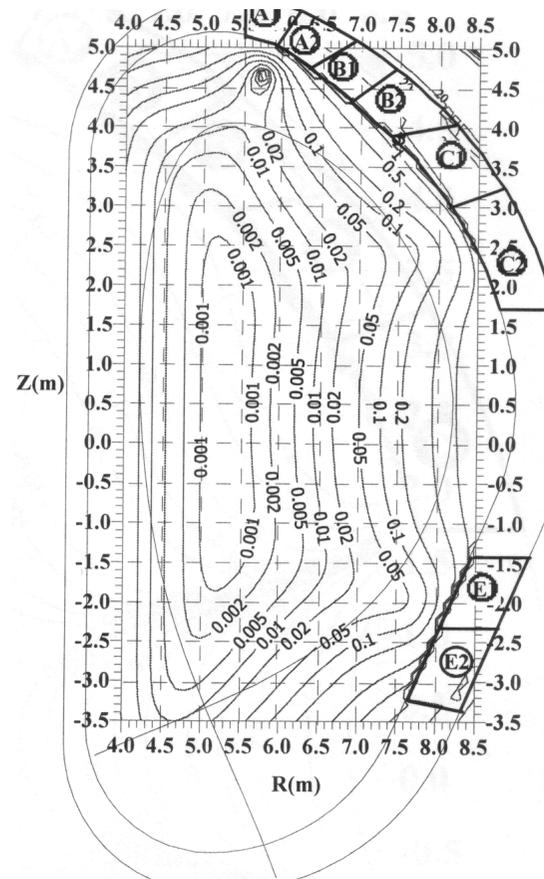
## ITER

- How can magnetic ripple be reduced?

→ Ferritic inserts



TF only



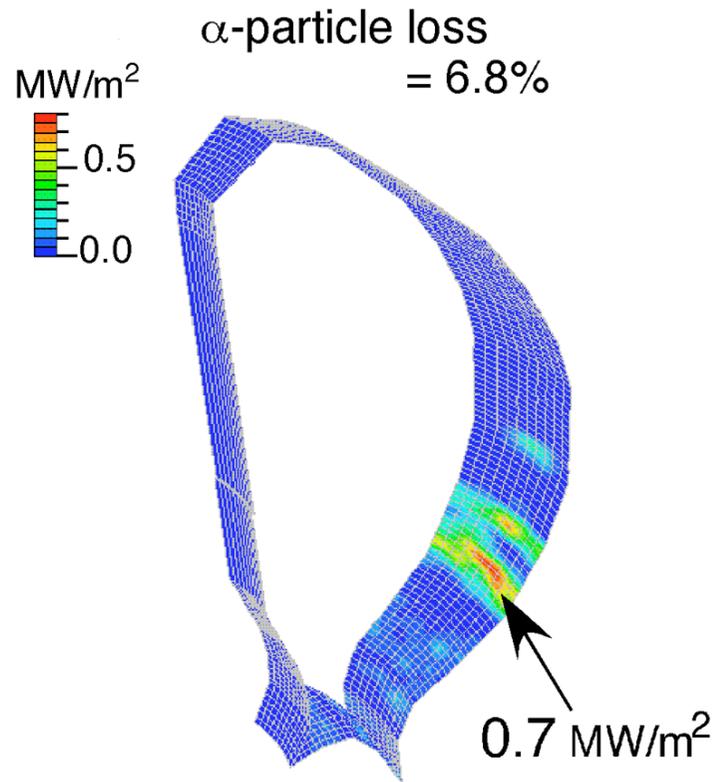
TF with ferritic inserts

*A.Fasoli et al., NF (2007)*

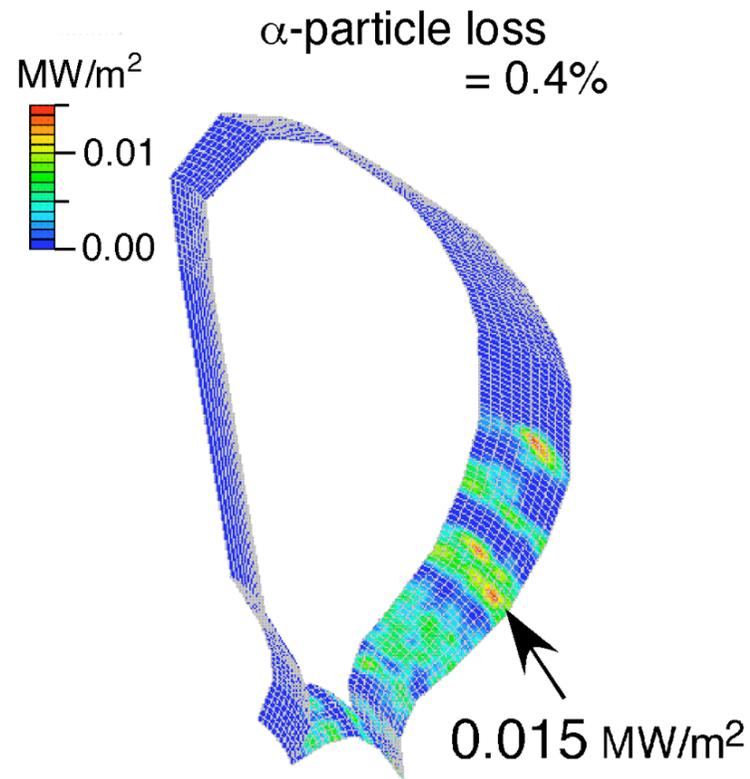
# Ripple losses - mitigation

## ITER

- How can magnetic ripple be reduced?  
→ Ferritic inserts



TF only



TF with ferritic inserts

*A.Fasoli et al., NF (2007)*

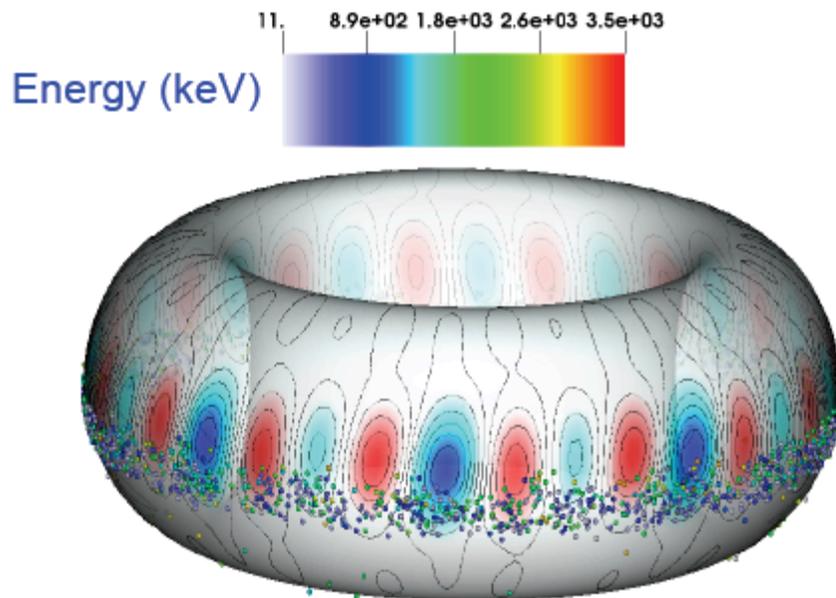


# Ripple losses – effect of test blanket modules

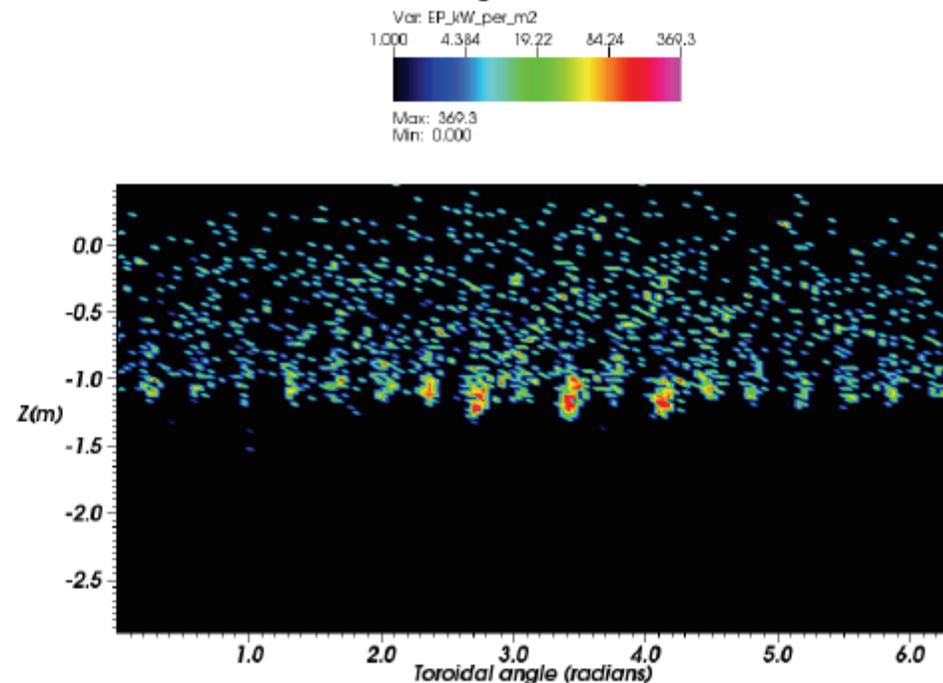
## ITER

- Additional problems: test blanket modules perturbing B locally

**ITER with 3 TBMs and TF ripple  
alpha loss patterns**



**Heat flux footprints on outer wall**



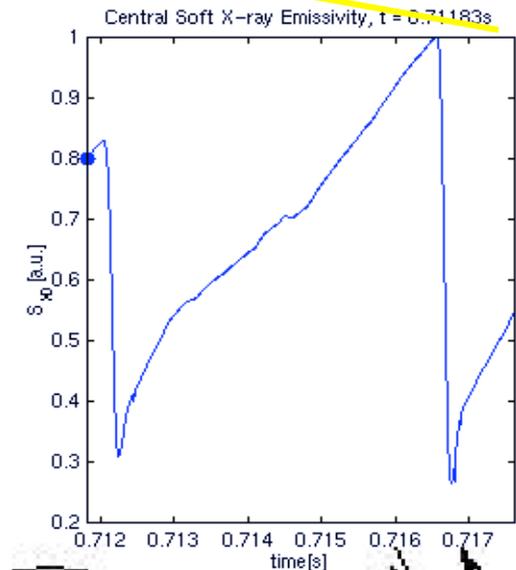
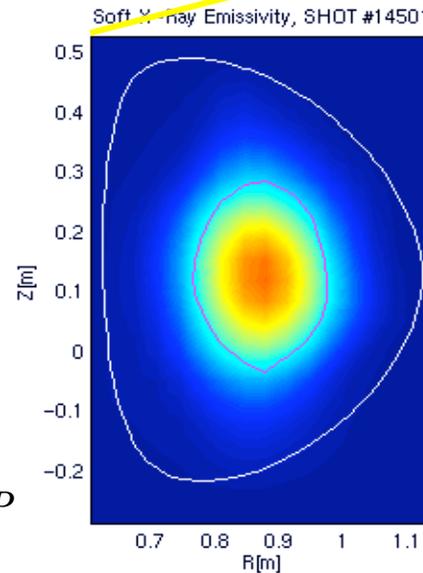
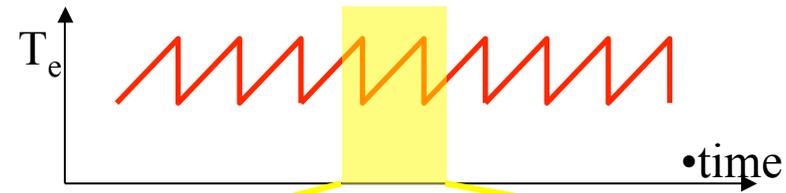
- Loss levels are acceptable
- Numerical tools are ready to address orbit losses in the presence of other possible perturbations (e.g. coils for ELM control)

*Courtesy of D.Spong*



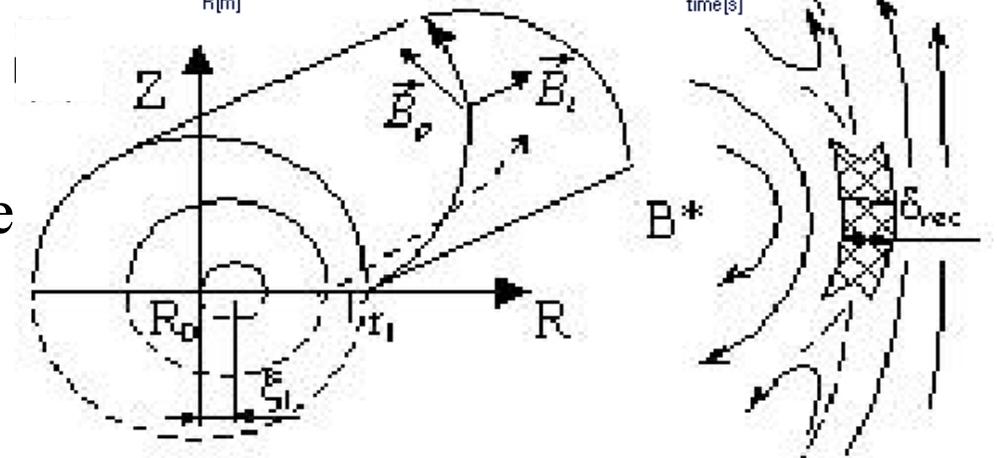
# Low frequency MHD - the sawtooth instability

- Sudden, very fast losses of energy and particles in core
- Ex.: X-ray emissivity ( $\sim T_e, n$ ) evolution in TCV



Courtesy of I.Furno, CRPP

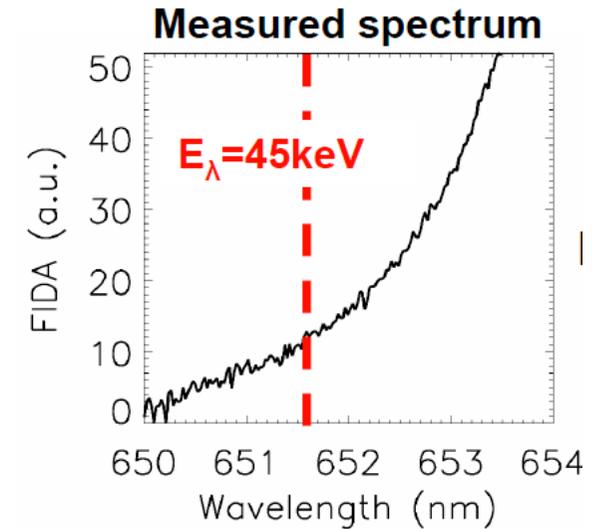
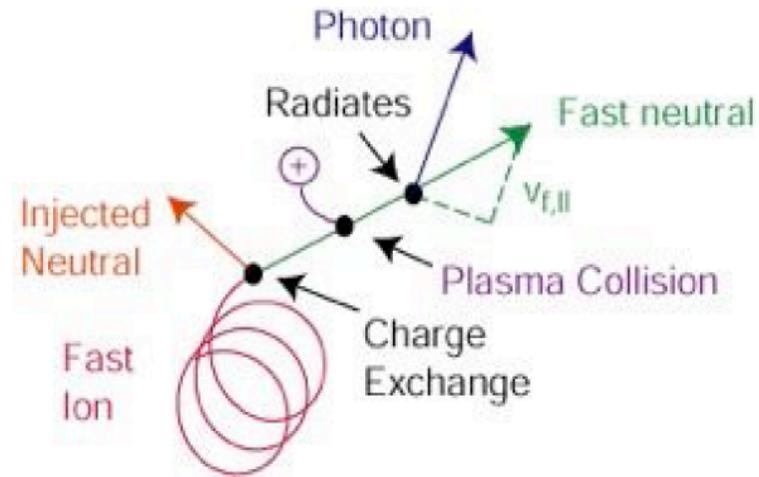
- local breaking of magnetic structure
- redistribution of energetic ions



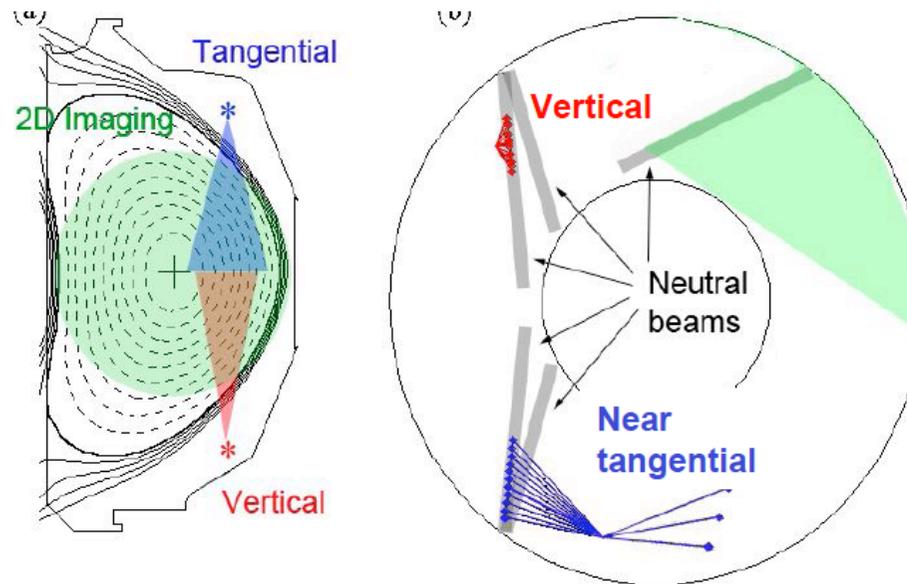
# Low frequency MHD - the sawtooth instability

*How to measure internal redistribution?*

→ Fast ion  $D\alpha$



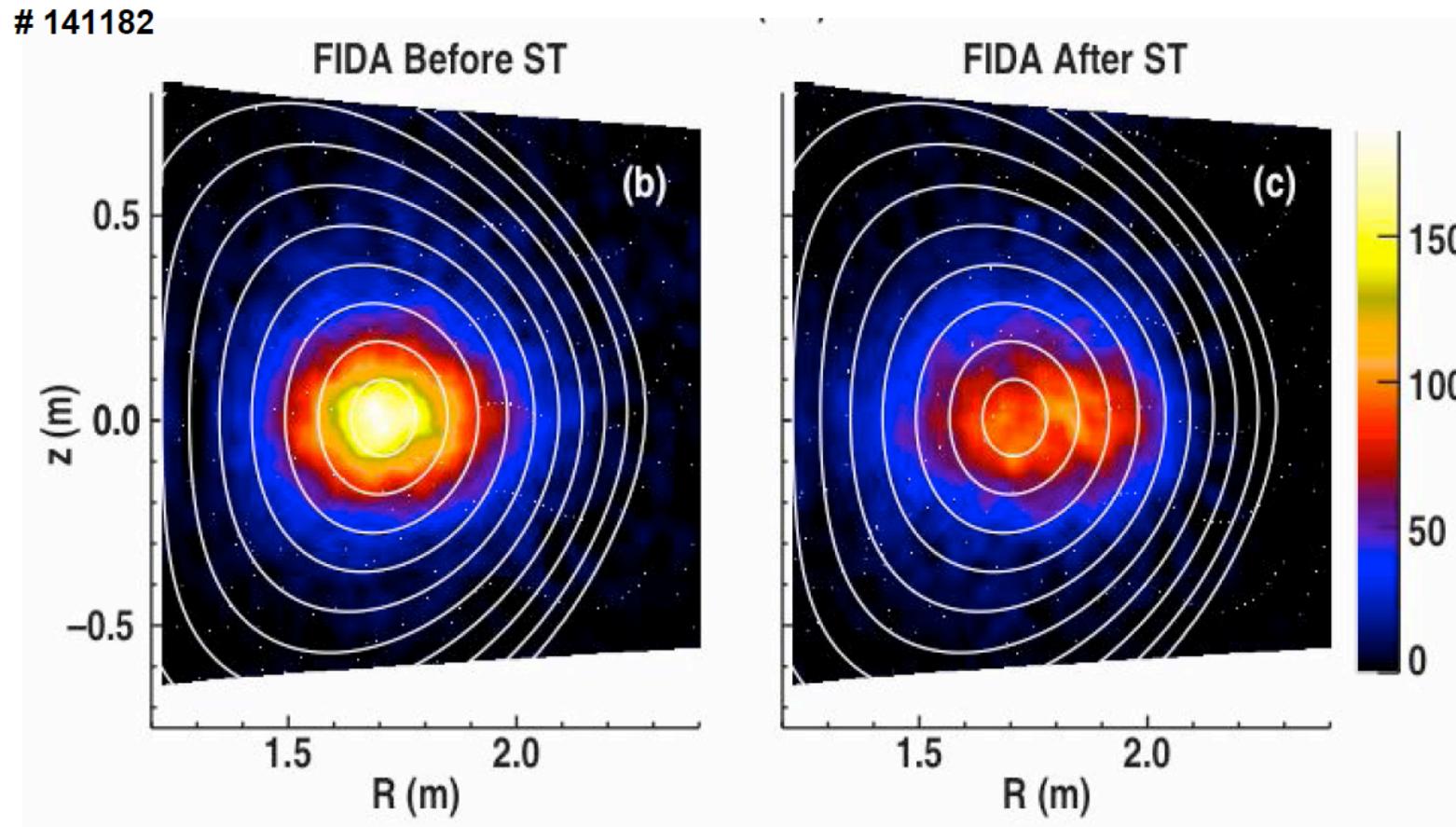
2D imaging



*Courtesy of W.Heidbrink  
and C.M.Muscatello*

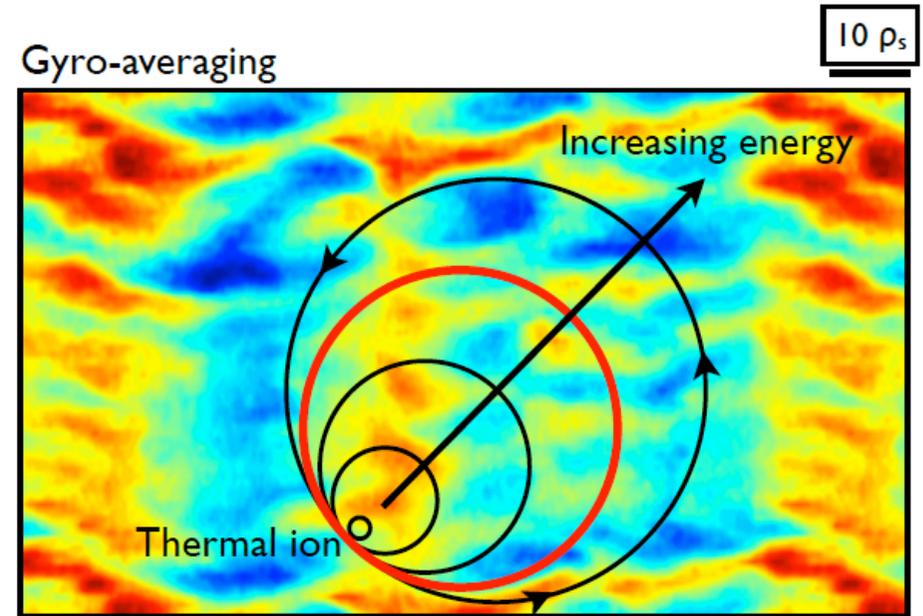
# Low frequency MHD - the sawtooth instability

Redistribution measured by Fast ion  $D\alpha$



# Energetic ion interaction with turbulence

- Large energetic ion orbits are expected to average out the effect of turbulence

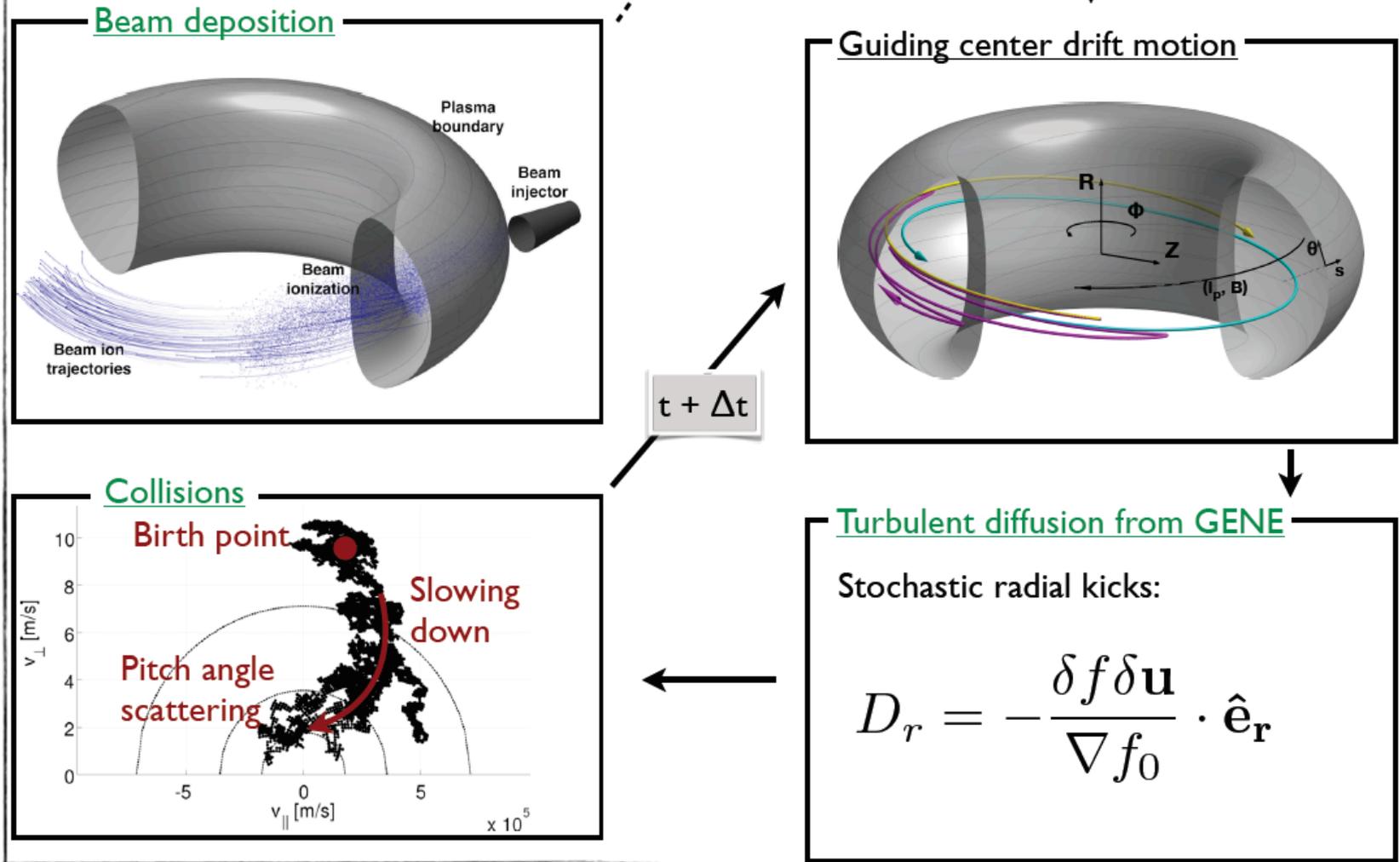


*Courtesy of M. Albergante*

- Are there conditions in which turbulent transport of energetic ions is significant?
- Experimental evidence of some anomalous cases exists
  - Deficit of energetic ions in DIII-D; Asdex-U anomalous NBI current drive profile
- Key parameters are  $E_{\text{energetic ions}}/T_{\text{plasma}}$ , and the slowing down time

# Fast ion interaction with turbulence Modelling

## The VENUS code

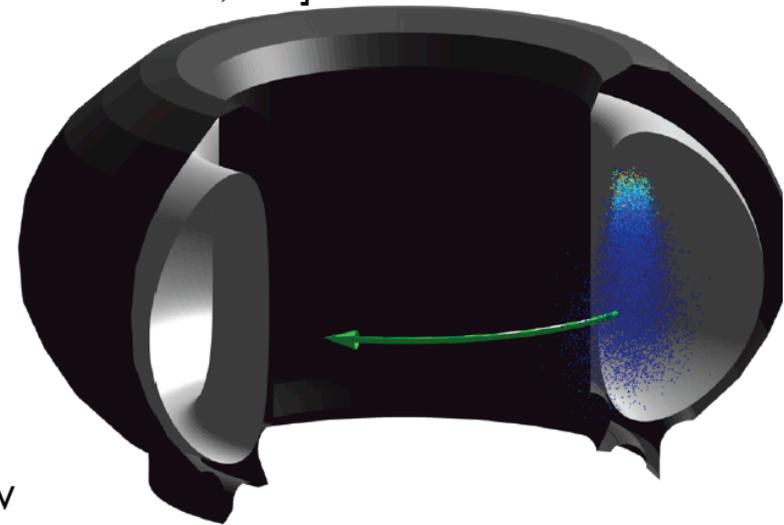


# Fast ion physics interaction with turbulence

## Conclusions of modelling

- Present devices (modest values of  $E_{\text{energetic ions}}/T_{\text{plasma}}$ )
  - Some anomalous transport of NBI ions, hence anomalous heating and current drive
- ITER
  - Negligible effect for NBI ions and for  $\alpha$ 's
- DEMO ?

“DEMO will be 8.5m major radius with a toroidal field of 6T, [...] whose density will be similar to the ITER density. DEMO is expected to be a high temperature device” [Ward, *Plasma Physics and Controlled Fusion*, 2011]



Same density as ITER's  
Peak temperature of 50 keV  
Neutral beam injection at 1.5 MeV  
On-axis, co-current, with  $E_{\text{nbi}}/T_e$  ratio  
▶ 35, same as ITER



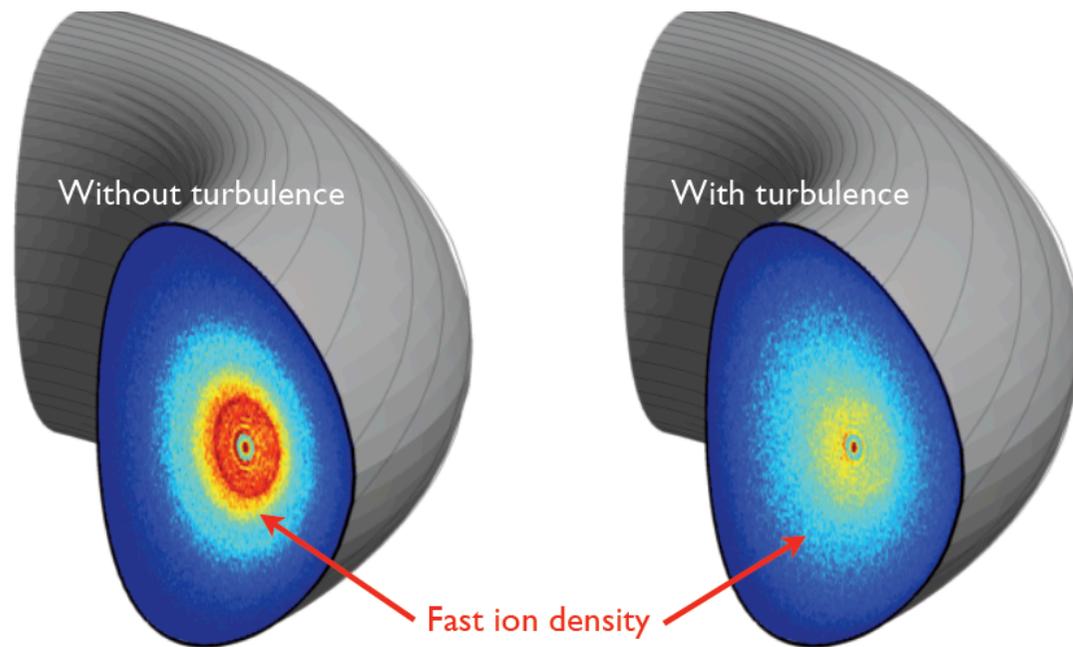
Courtesy of M.Albergante



# Fast ion physics interaction with turbulence

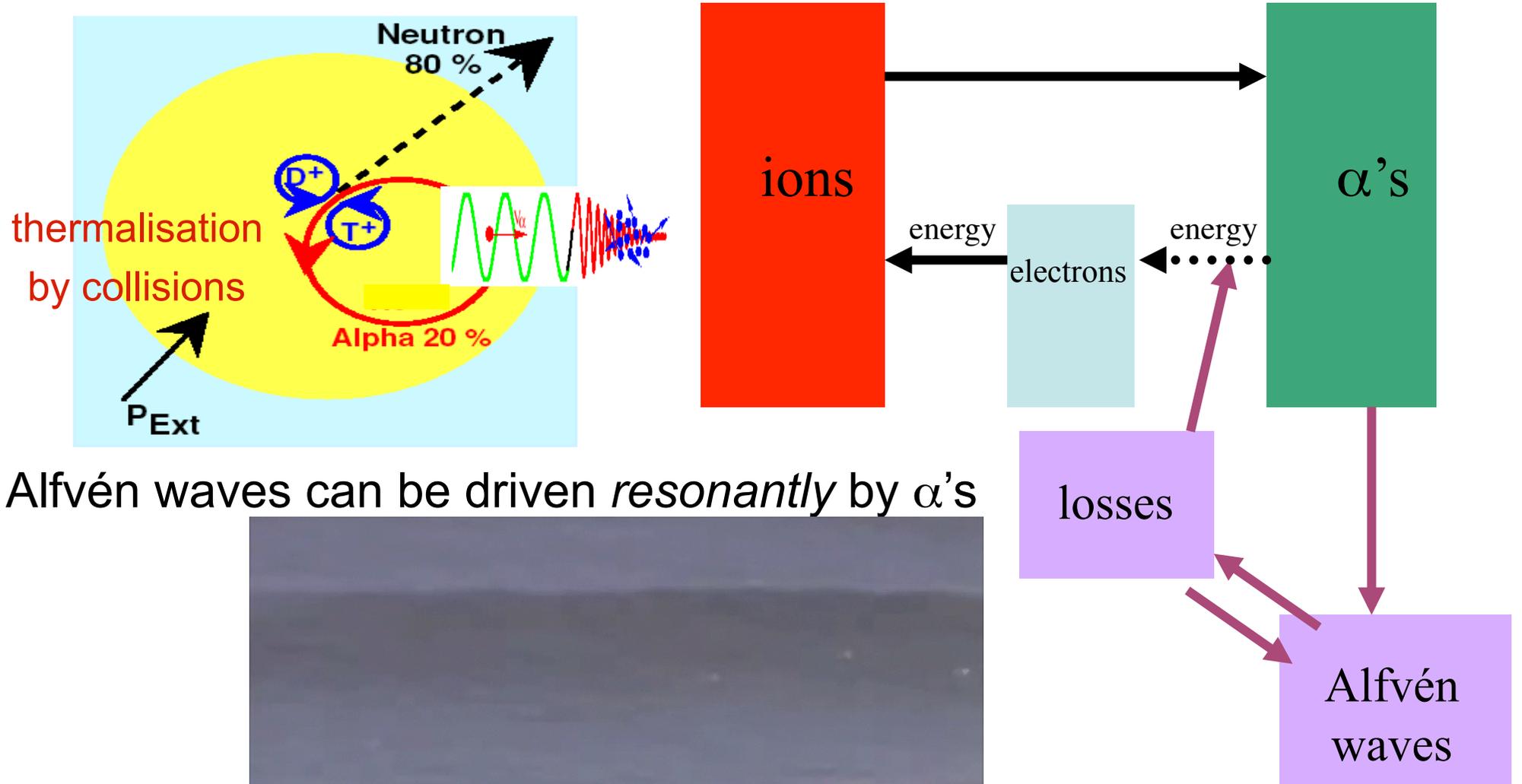
## Conclusions of modelling

- Present devices (large values of  $E_{\text{energetic ions}}/T_{\text{plasma}}$ )
  - Some anomalous transport of NBI ions, hence anomalous heating and current drive
- ITER
  - Negligible effect for NBI ions and for  $\alpha$ 's
- DEMO
  - NBI ions are redistributed

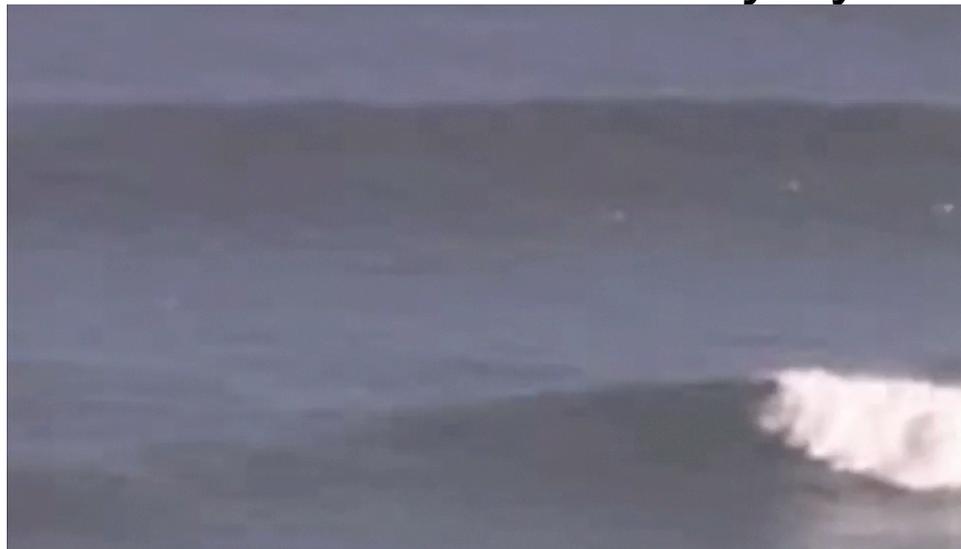


Particle losses do not change: they are negligible  
Particles are moved from core to mid-radius

# Resonant interaction with waves and self-heating



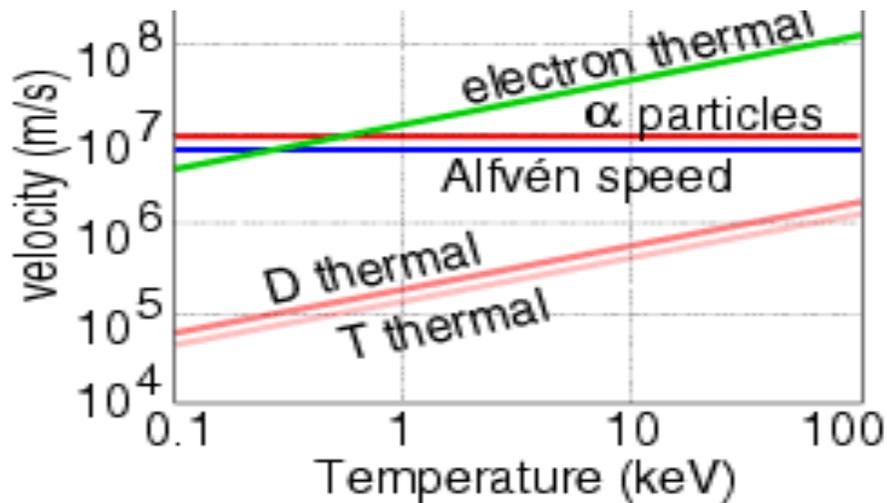
- Alfvén waves can be driven *resonantly* by α's



# Alfvén waves and Eigenmodes

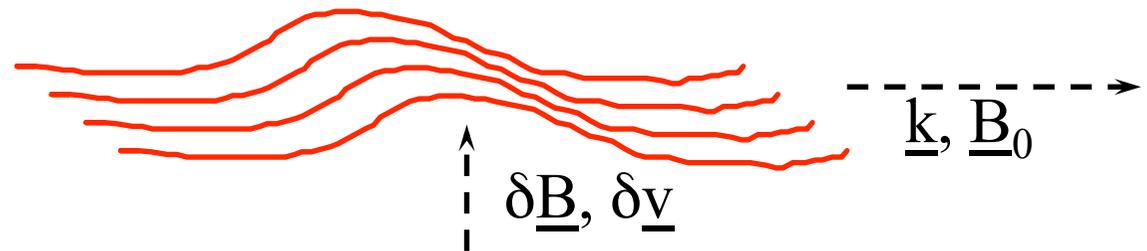
Typical velocities in a tokamak

$$B=4\text{T}; n=10^{20}\text{m}^{-3}$$



- $\alpha$ 's resonate with Alfvén Waves
- Alfvén Waves are driven unstable if
  - sufficient 'free' energy  $\nabla p_\alpha$
  - $\alpha$  drive > plasma damping

– B-field and plasma frozen together; field lines are strings with tension and inertia → Alfvén wave propagation



In tokamaks: weakly damped Alfvén Eigenmodes (AEs)



# Alfvén waves in nonuniform plasma

– Cylinder: Alfvén ‘continuum’

$$\omega^2(r) = k_{\parallel}^2(r) v_A^2(r)$$

- No globally propagating wave
  - small scales  $\rightarrow$  strong damping

– Torus: Fourier  $\phi \sim e^{i(m\theta - n\varphi - \omega t)}$

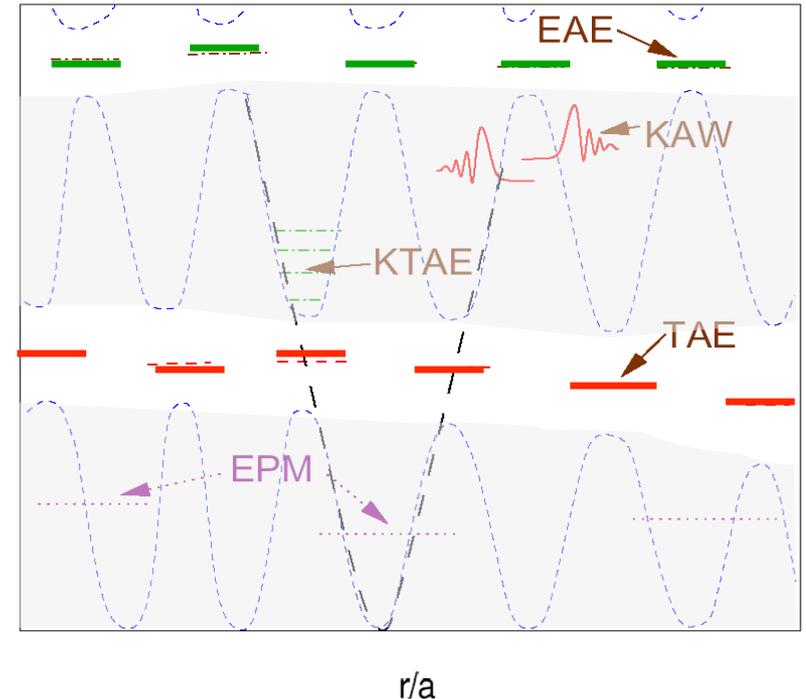
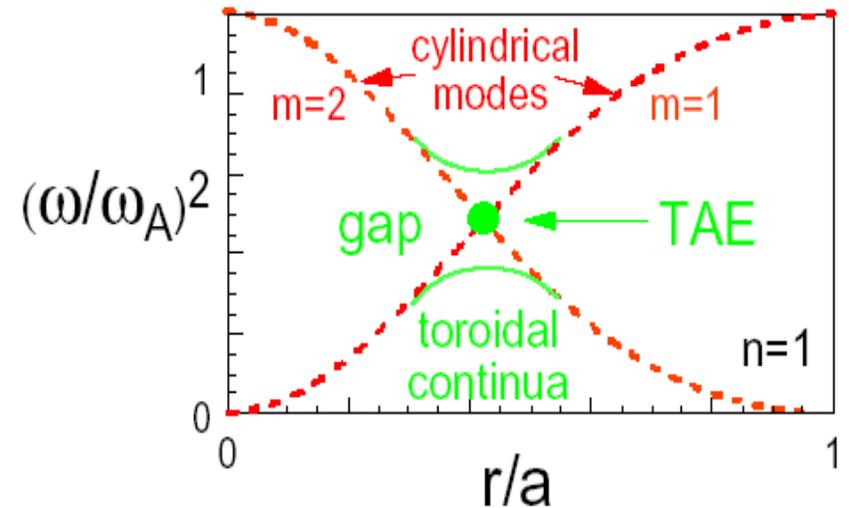
$$k_{\parallel} = 1/R (n - m/q(r)); \quad q(r) = rB_z / RB_{\theta}$$

Coupling of toroidal harmonics

$\rightarrow$  gaps in continuum spectrum  $\omega_A^2$

$\rightarrow$  weakly damped eigenmodes

Toroidal AEs, Elliptical AEs, ...



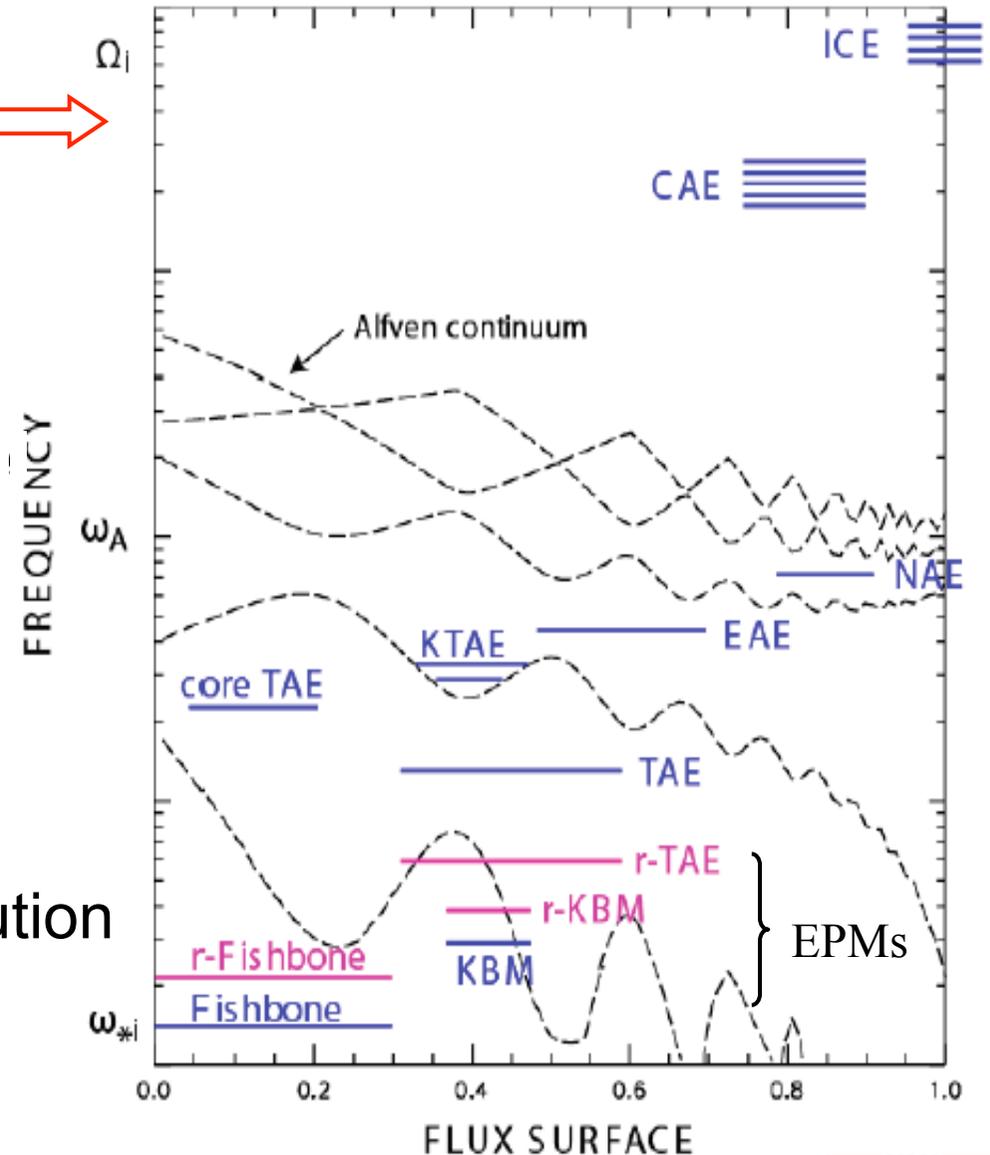
# Alfvén Waves and Eigenmodes

- Zoo of Alfvén Eigenmodes (AEs)



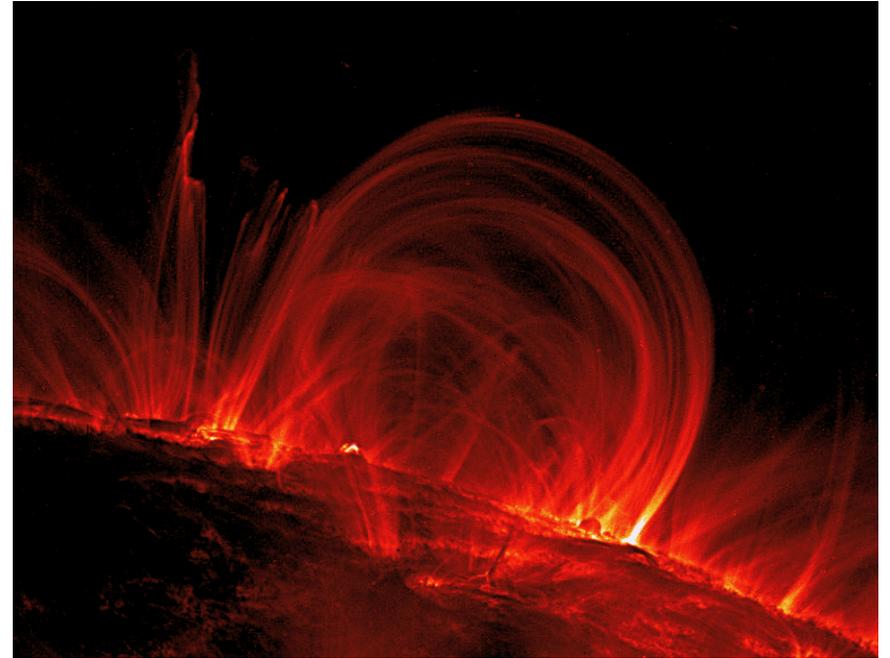
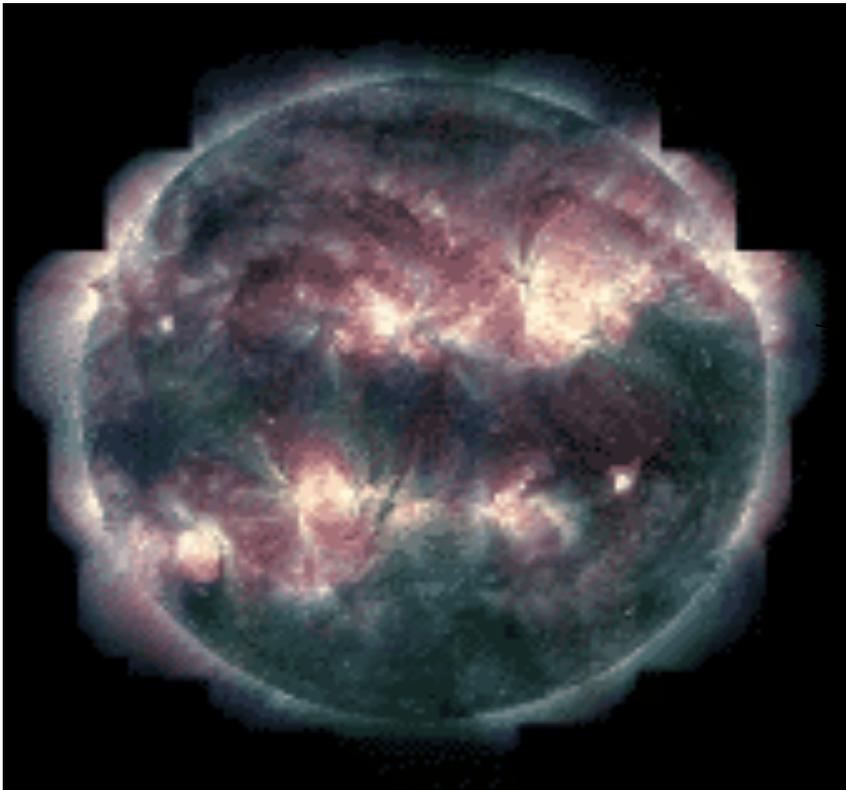
- Questions

- Linear stability
- Nonlinear interactions: redistribution and losses



# Alfvén waves exist also in space plasmas

## E.g. coronal loops



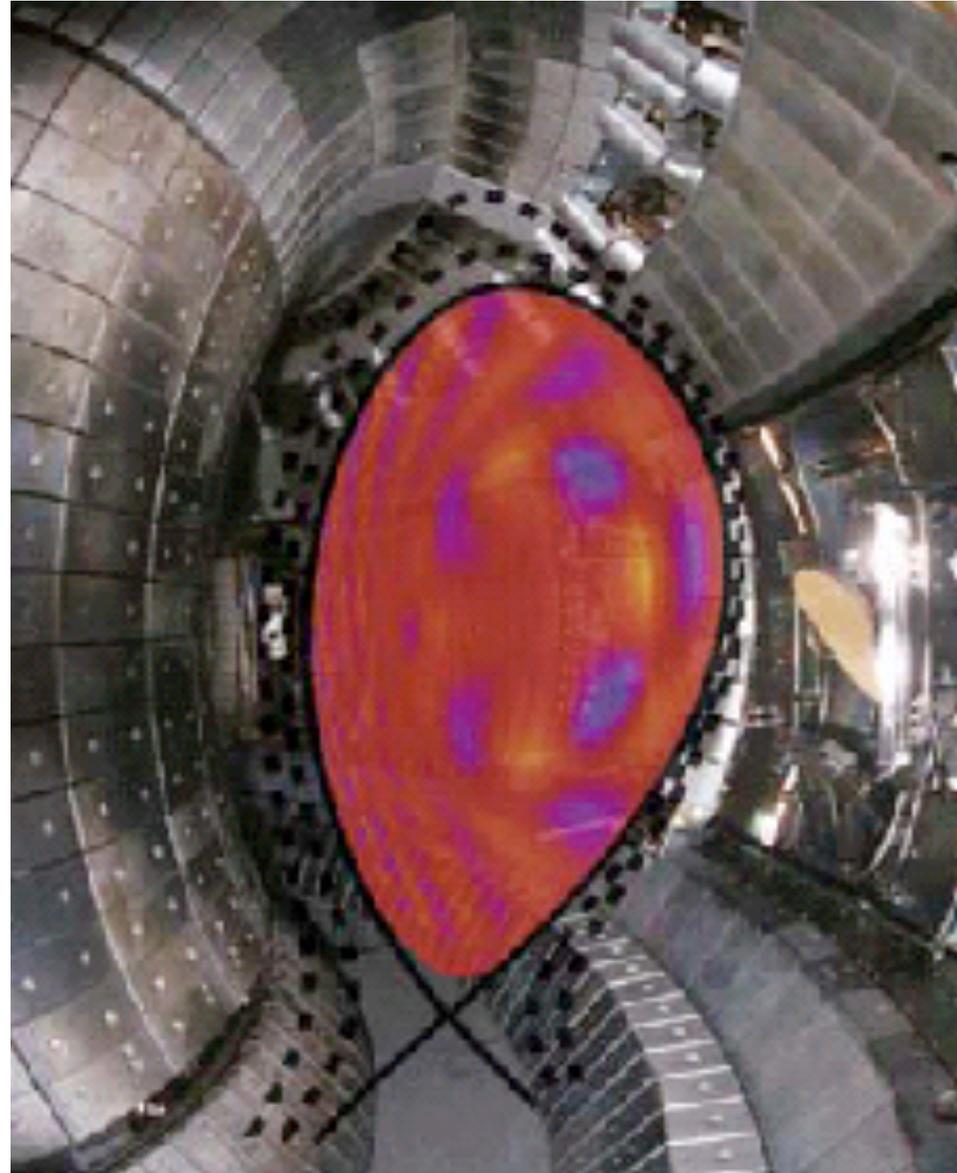
*Courtesy of NASA*

A.J.C.Belien et al., PRL ('96)

- From remote observations of frequencies  
→ information on B-field and density inside loop

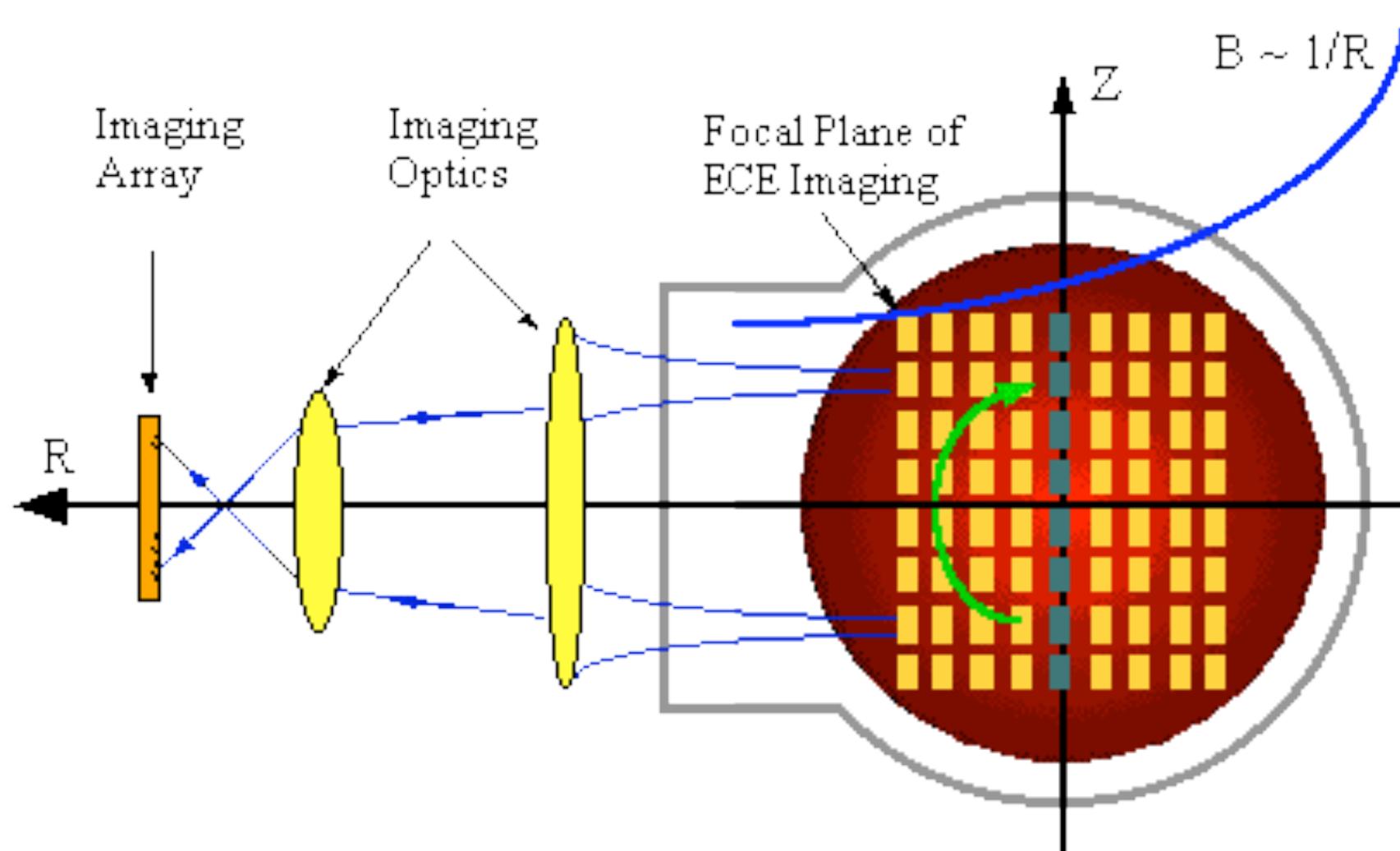
# Ex. of TAE calculated structure

LIGKA code  
Asdex-Upgrade



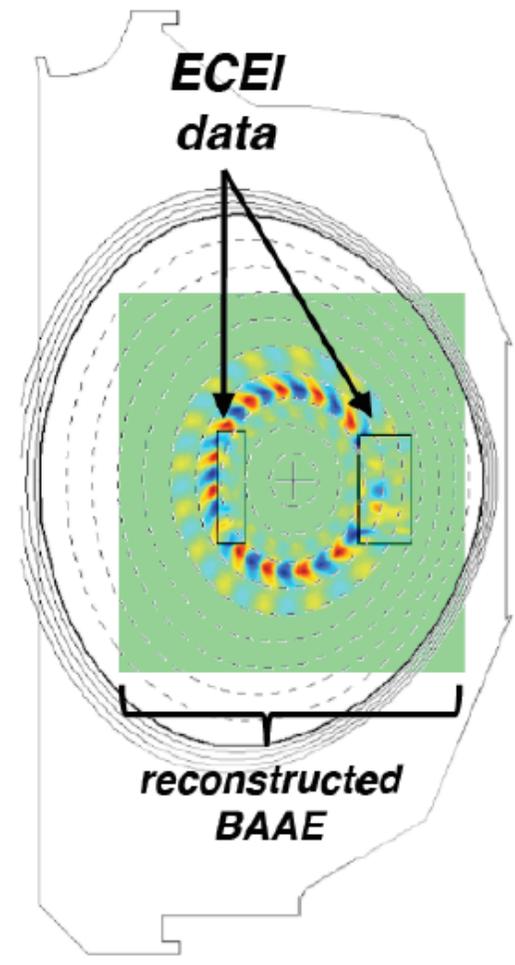
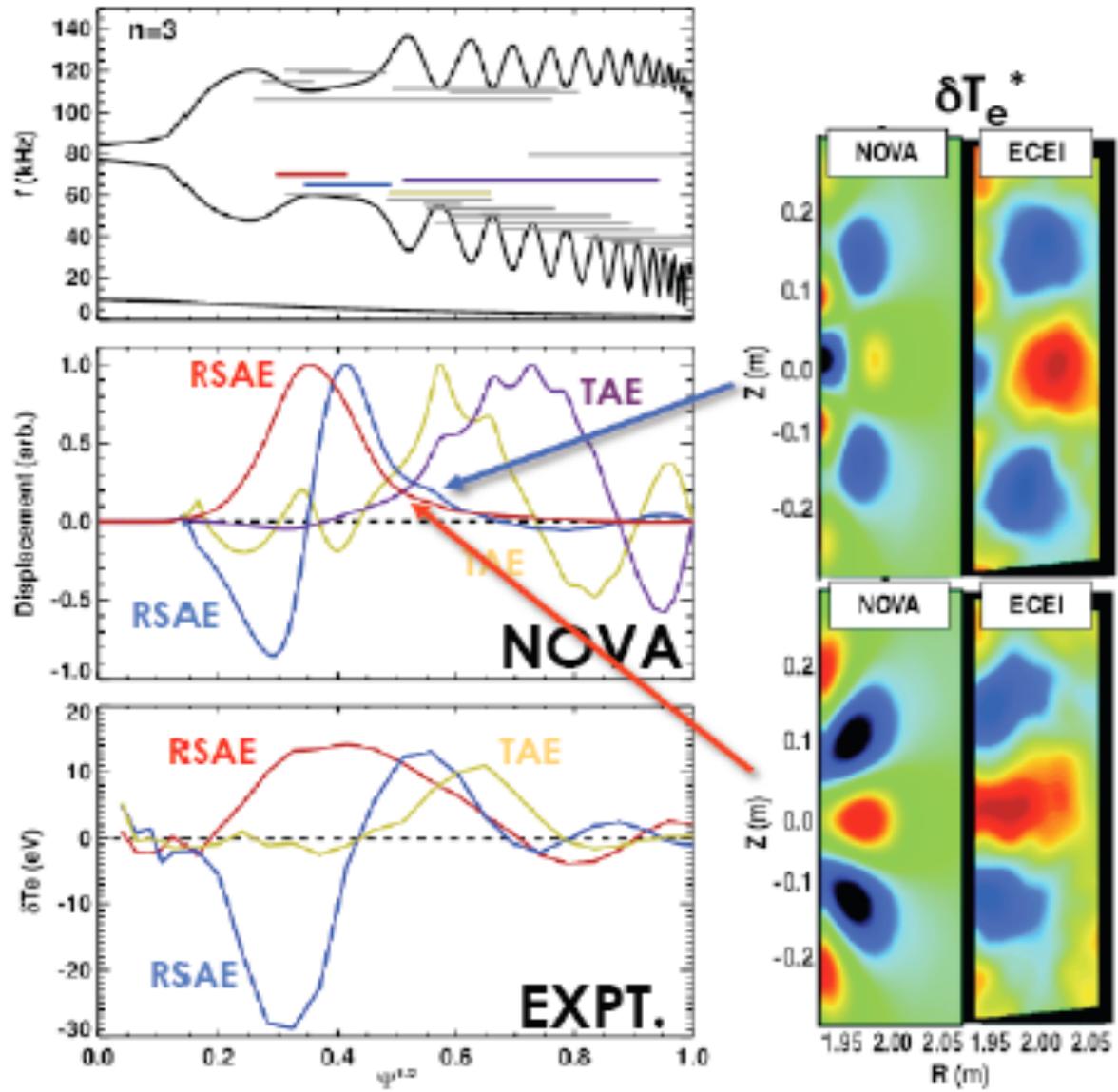
# 2D measurements of AEs

E.g. via Electron Cyclotron Emission imaging



# 2D measurements of AEs by ECEI in DIII-D

## UNSTABLE MODES IN COLOR



# AE instability drive

- Fast particle drive

$$\gamma = \int \left[ \omega \frac{dF}{dE} - \text{const} \times n \frac{dp_{fast}}{dr} \right] F_{resonance}(v, v_A) dv$$

- Unstable AEs  $\leftrightarrow$  sufficient  $dp_{fast}/dr$  & proximity to resonance

- Resonance: passing  $v_{||} = v_A (v_A/3, v_A/5, \dots)$

trapped

-bounce frequency  $|v| = v_A/2(R/r)^{1/2}$

-precession frequency  $|v| = v_A/2qk_{\theta}\rho_L$



# AE damping mechanisms

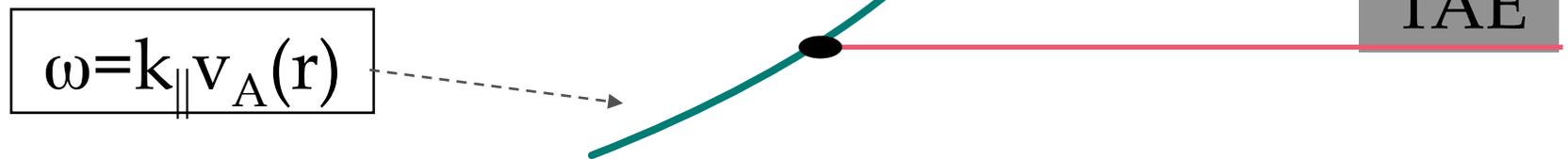
- Direct ion, electron Landau

$$- v_{th||i,e} \sim v_{\text{Alfvén}} \quad (\text{or } v_{\text{Alfvén}}/3)$$

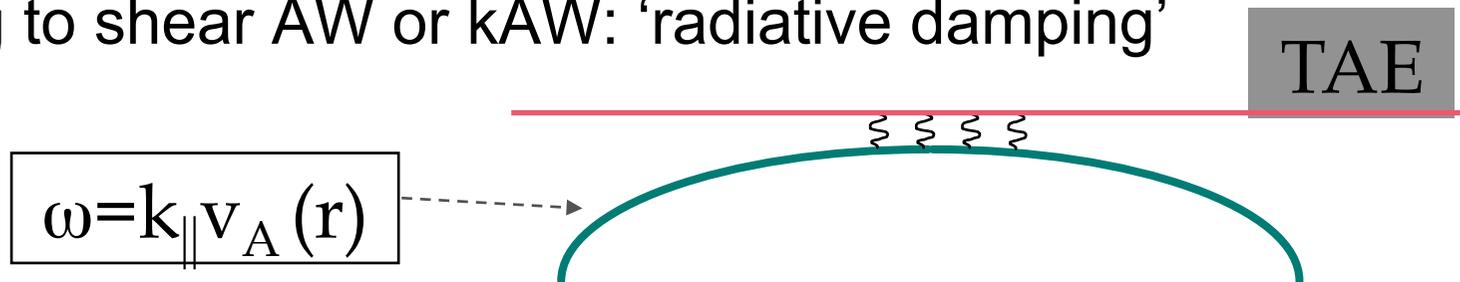
- Mode conversion

- Directly to shear AW (fluid theory) or to kinetic AW (kinetic theory): ‘continuum damping’

– large  $\gamma/\omega$  up to  $\sim 5-10\%$



- Tunneling to shear AW or kAW: ‘radiative damping’



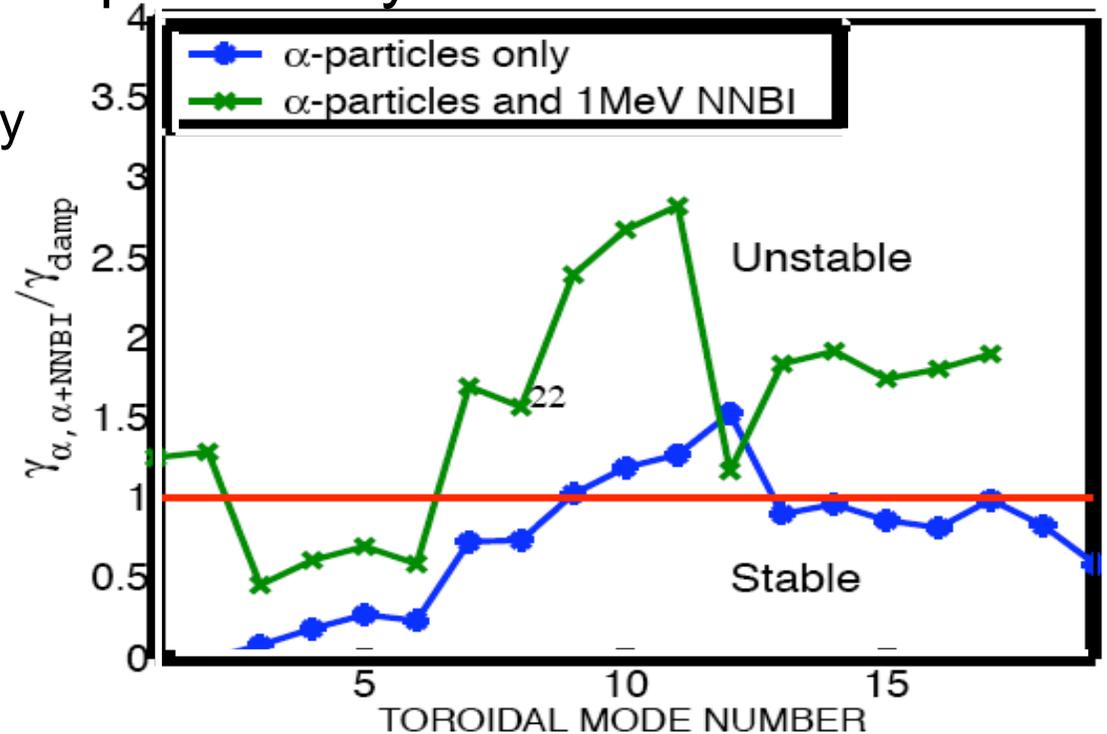
- Collisional damping

# AE linear stability: questions and status

- Most unstable modes in ITER scenarios?
- Parameters that control stability?
- Drive and damping mechanisms qualitatively understood

– Ex. of predictions on TAE stability in ITER baseline scenario with  $\beta_\alpha(0) \sim 1\%$  (NOVA-K code)

*Courtesy of N. Gorelenkov*



- But we need a quantitative assessment of stability limits, i.e. of drive and damping, in ITER relevant scenarios

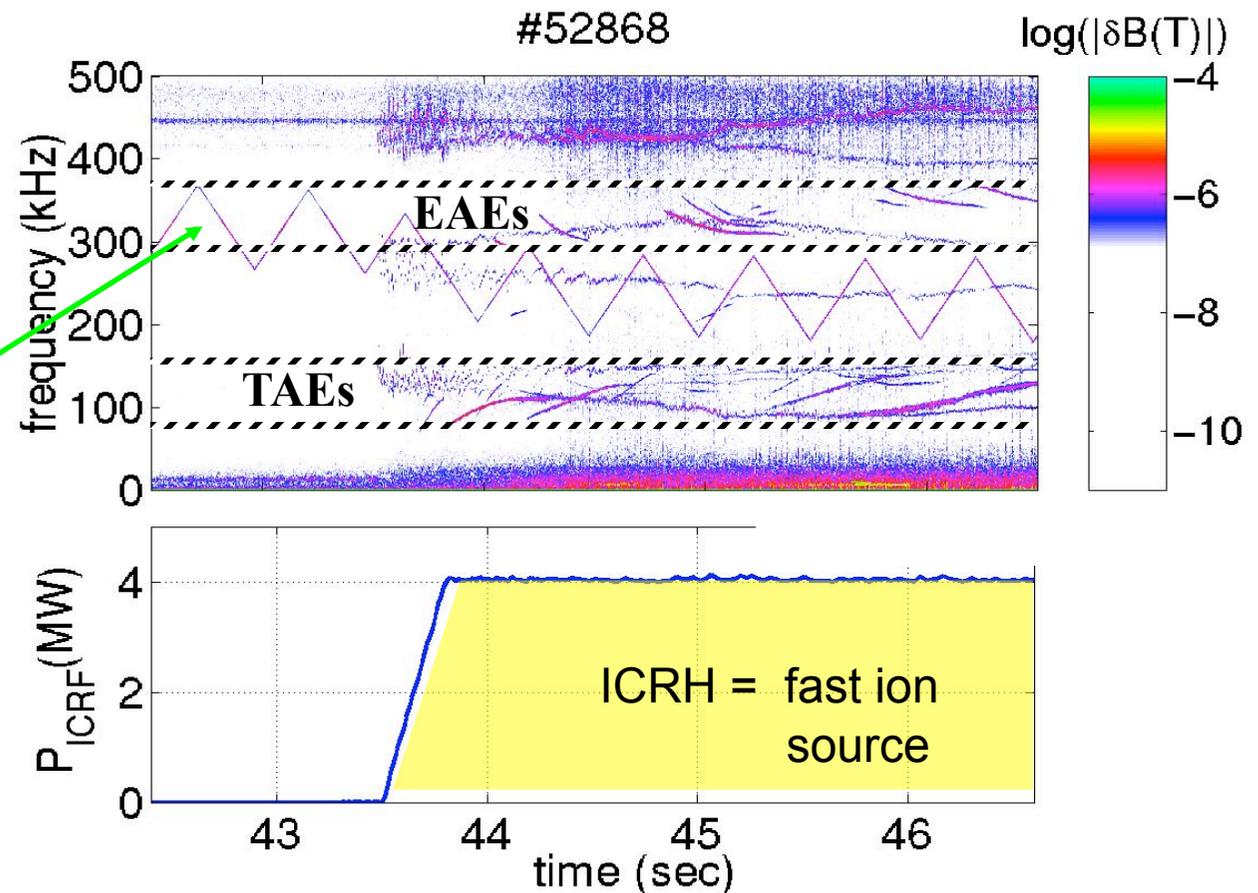
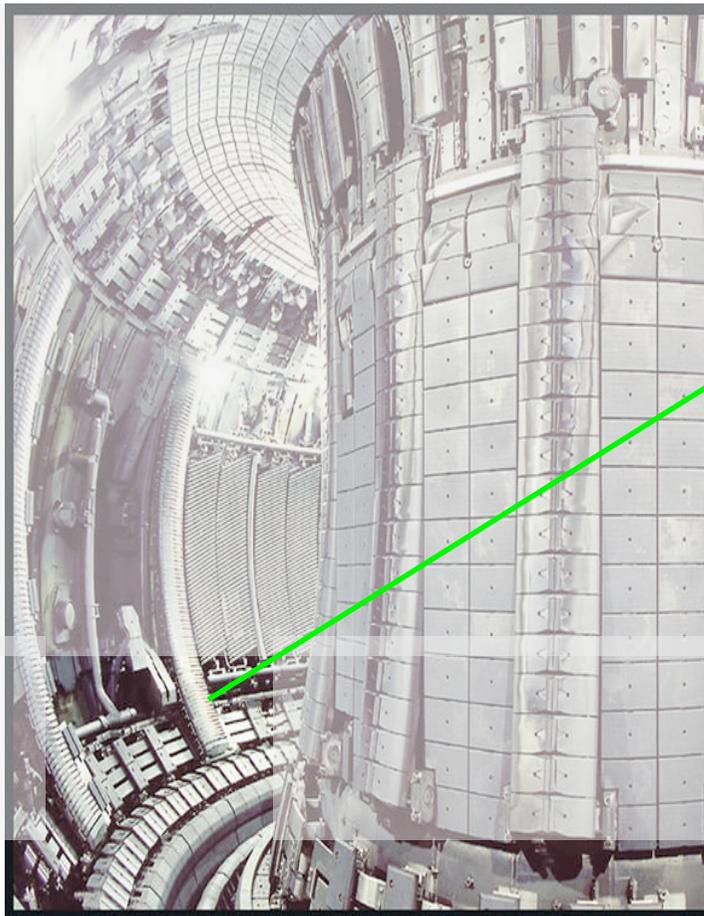
# Active and passive spectroscopy of AEs

## – Passive

- Modes observed if destabilized by fast particles (NBI, ICRH, *fusion  $\alpha$ 's*)

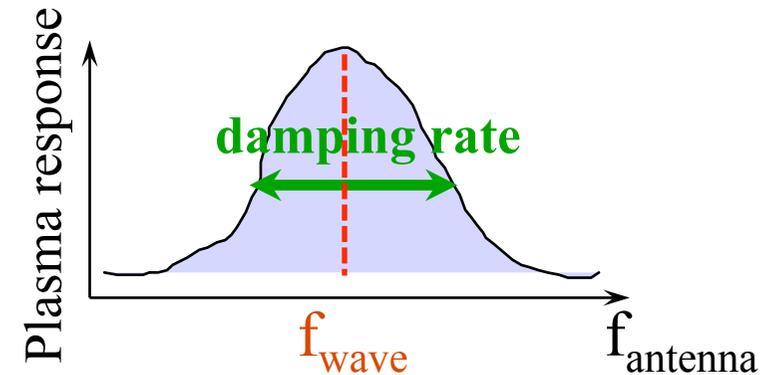
## – Active

- In-vessel antennas drive low amplitude perturbations
- Plasma response measured on B-probes: global modes  $\leftarrow$  Resonances

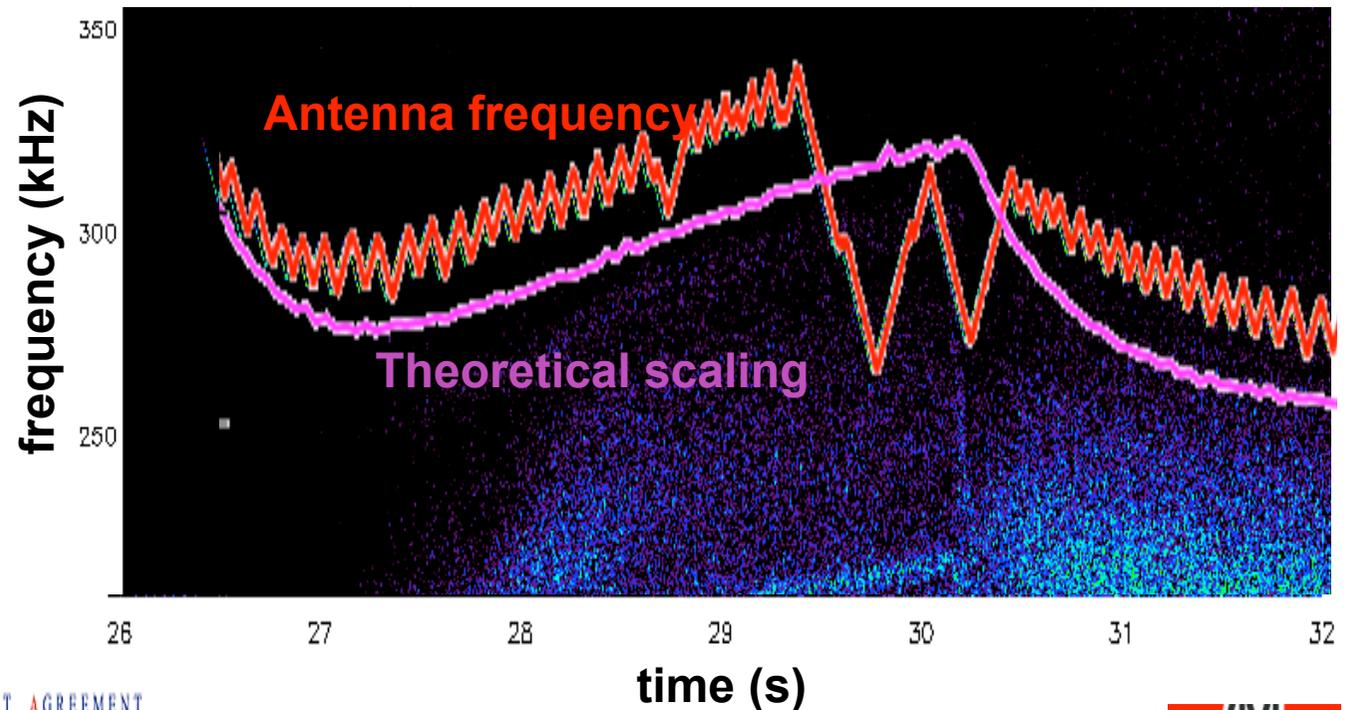


# Measurement of Alfvén wave damping rate

- Alfvén Wave = resonance in plasma response to antenna signal
- Width of resonance  $\rightarrow$  damping rate



- Waves are tracked throughout plasma discharge



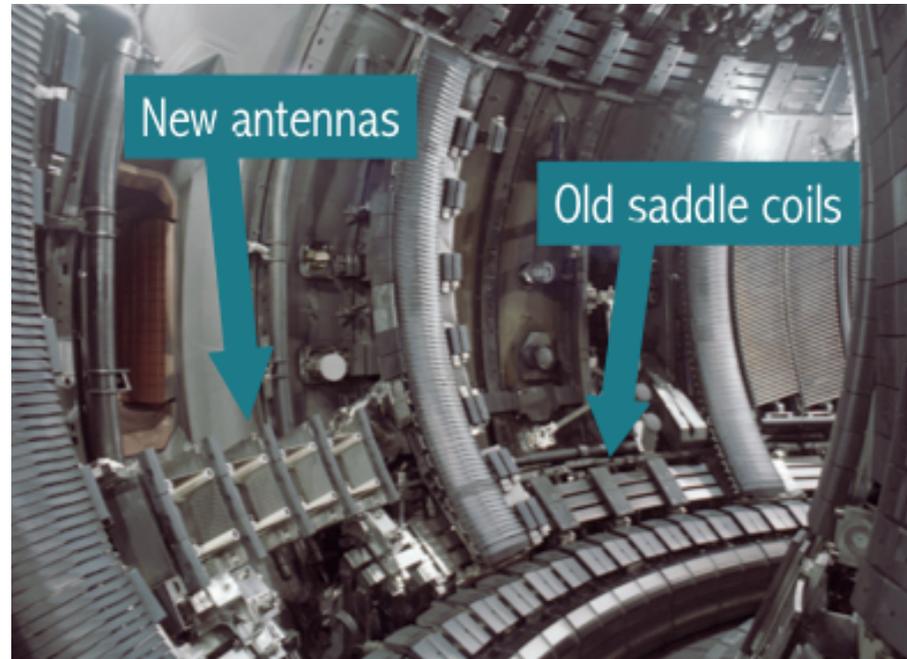
# Alfvén Eigenmode Active Diagnostics

Aim: address physics of mode damping, identify modes most prone to instability in burning plasma scenarios, and parameters to control stability



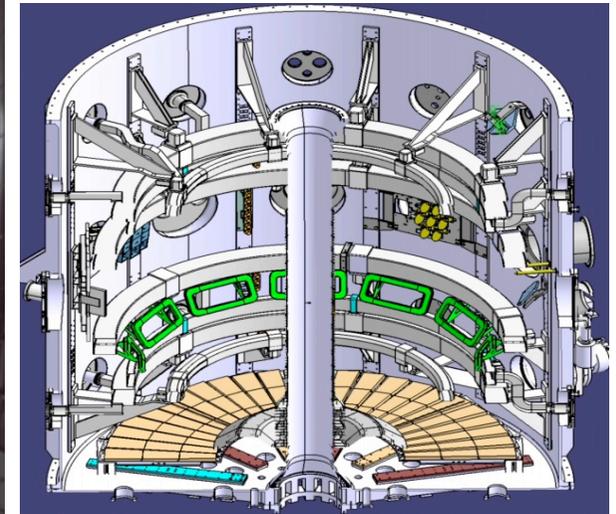
Alcator  
C-Mod

high field & density,  $T_e \sim T_i$



ITER-relevance for size and shape scaling, scenarios

MAST



tight aspect ratio,  
broad range of  $\beta$

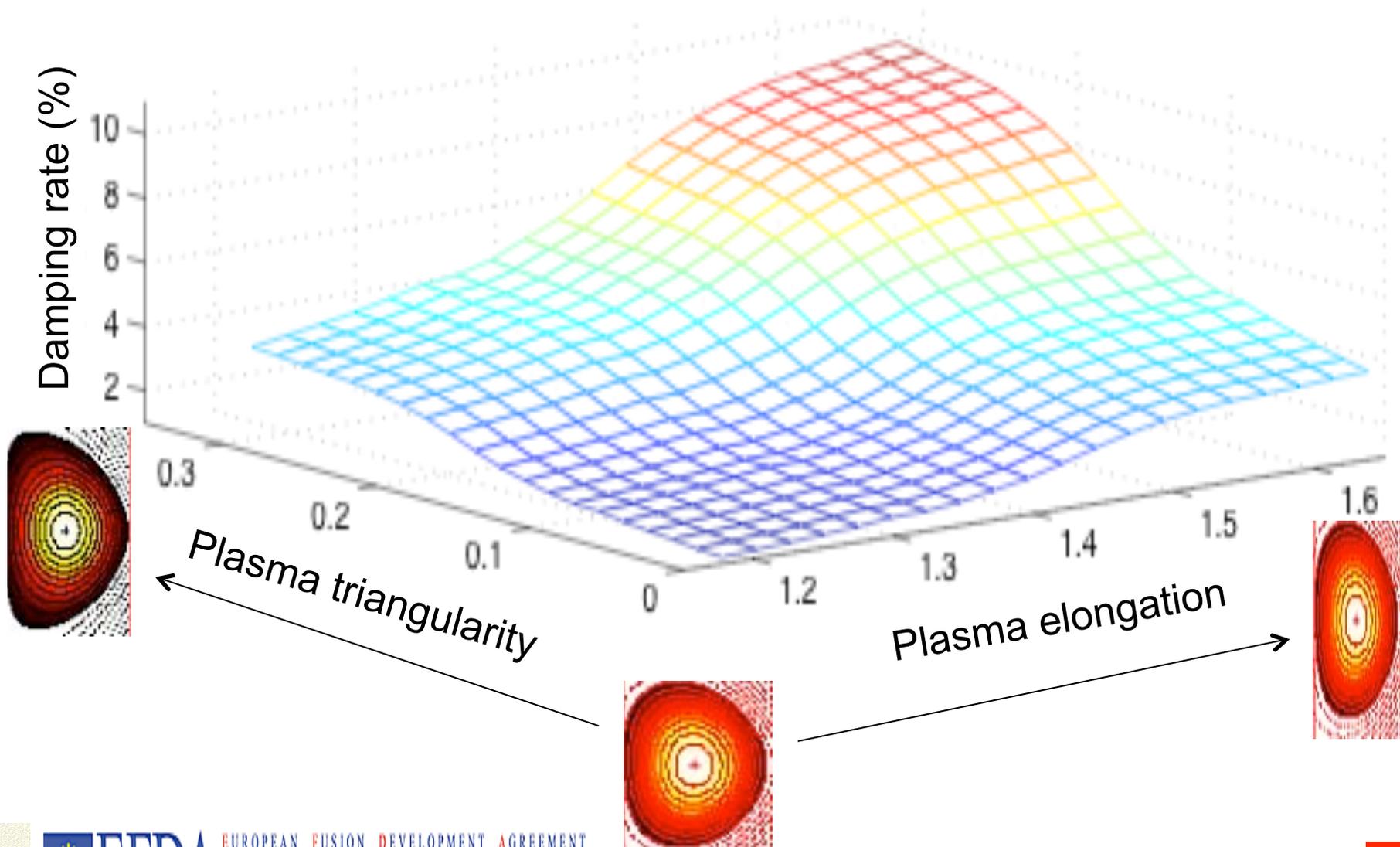
# Fusion technology interlude

## Remote handling of Alfvén wave antennas in JET



# Ex. of result on Alfvén wave damping

## Damping rates increase if plasma is shaped



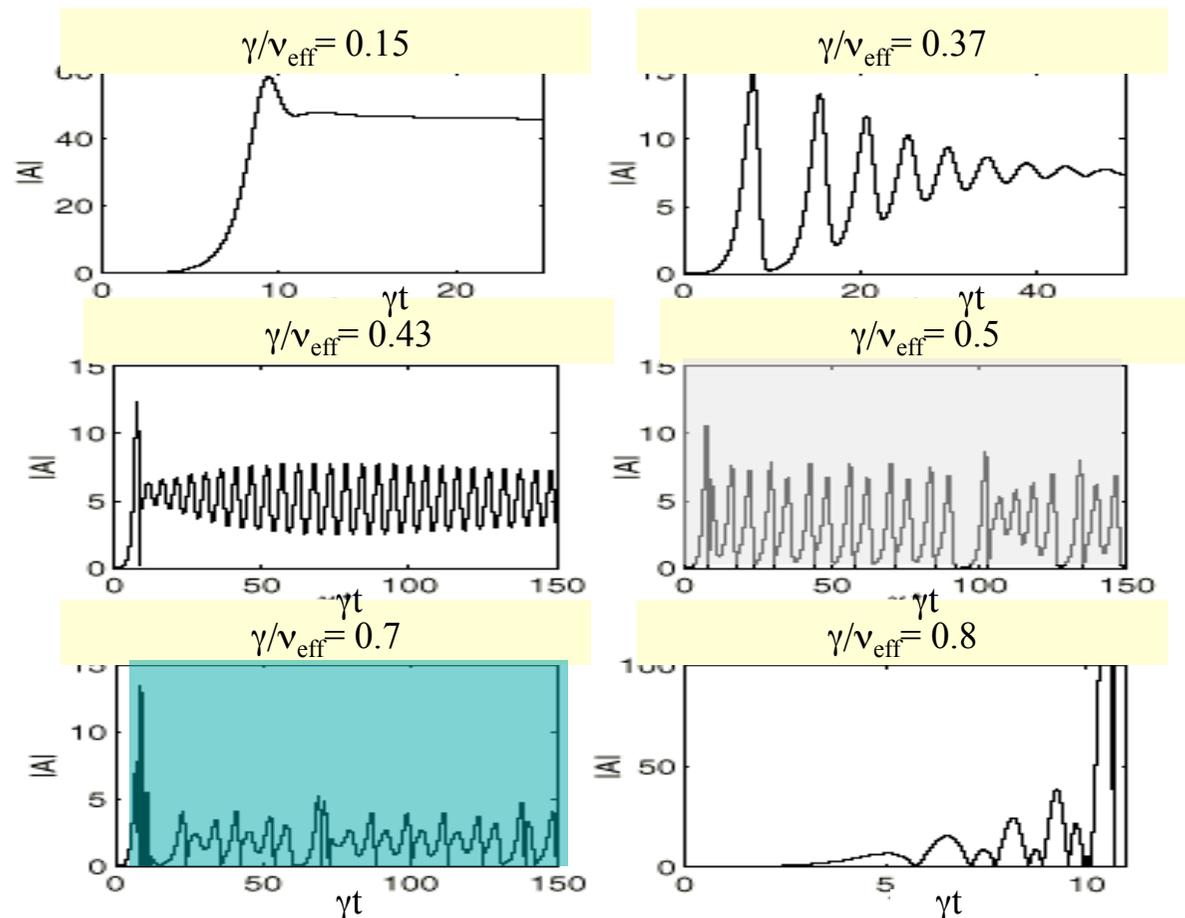
# Nonlinear AE wave-particle interaction

- Wave flattens particle distribution: less drive, but relaxation processes 'refresh' distribution

$$\exp(-i\phi) \frac{dA}{dt} = \frac{\gamma}{\cos\phi} A - \frac{\gamma_L}{2} \int_0^{t/2} \tau^2 d\tau \int_0^{t-2\tau} d\tau_1 \exp\left[-\nu_{\text{eff}}^3 \tau^2 (2\tau/3 + \tau_1)\right] A(t-\tau) A(t-\tau-\tau_1) A^*(t-2\tau-\tau_1)$$

Amplitude evolution determined by

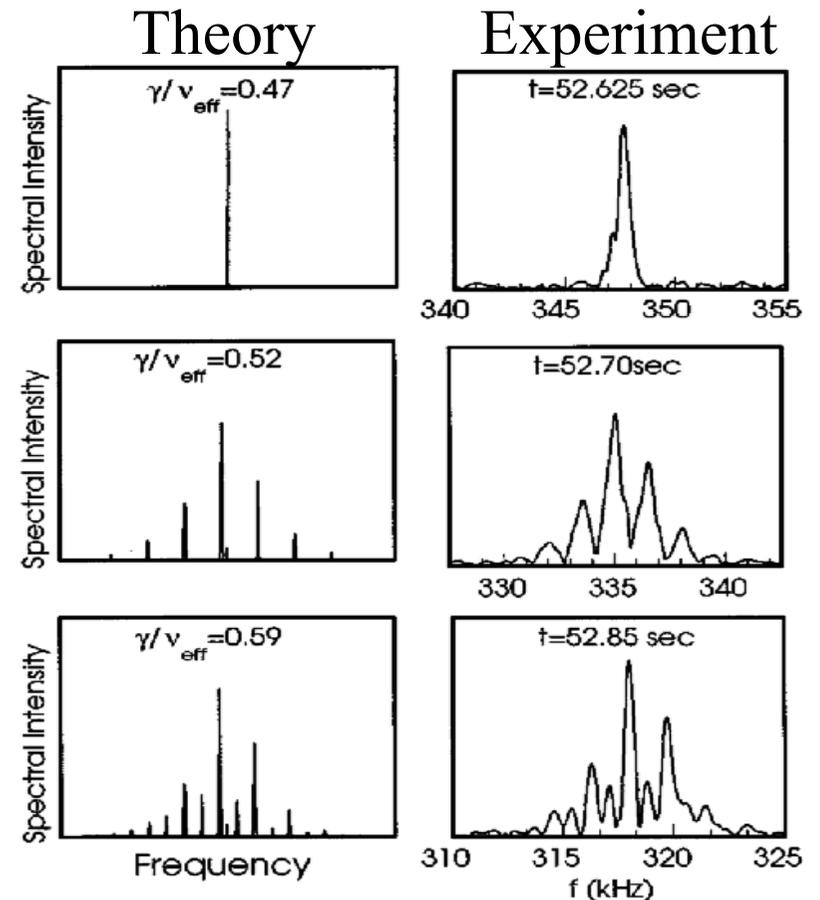
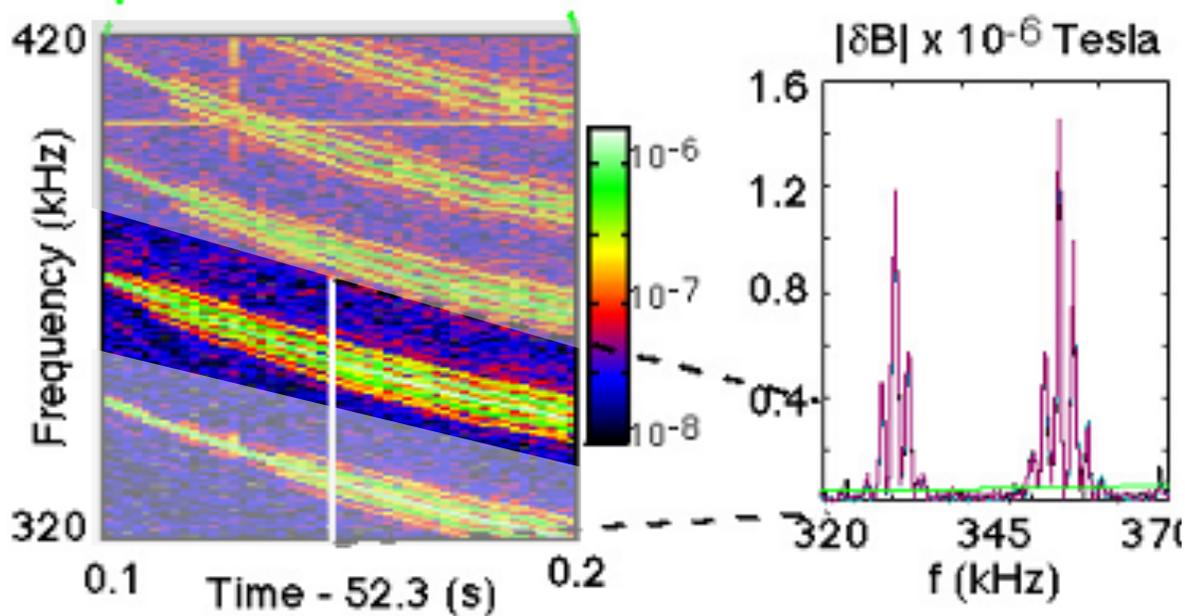
- $\gamma = \gamma_{\text{drive}} - \gamma_{\text{damp}}$
- vs. coll. freq.  $\nu_{\text{eff}}$



# Nonlinear AE wave-particle interaction

## → Fast ion phase space dynamics

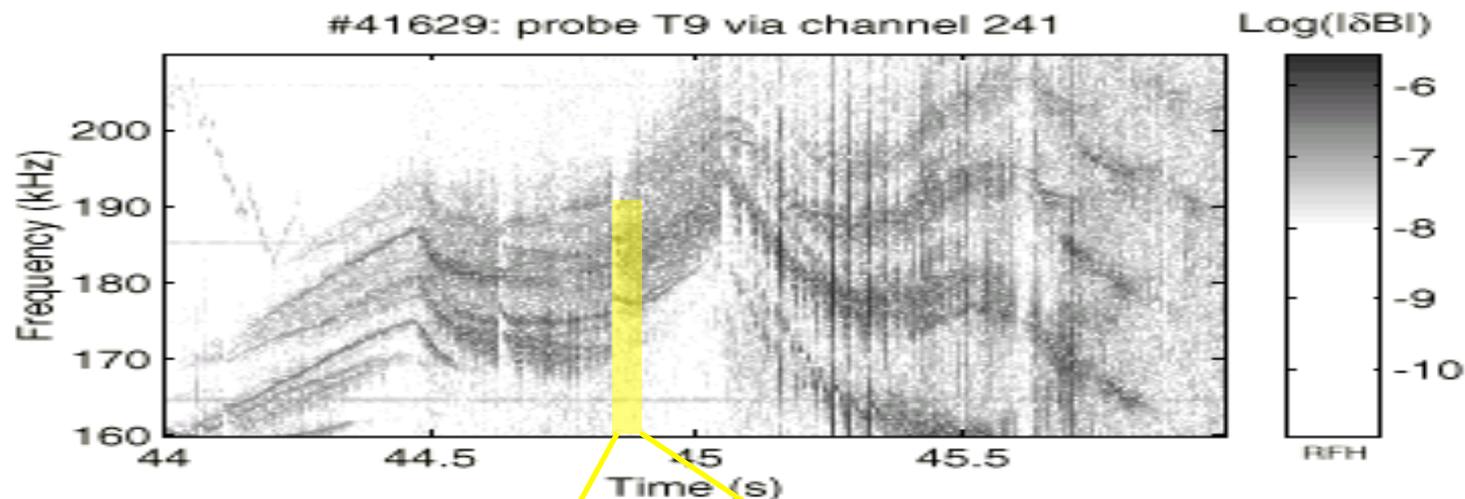
- ‘Pitchfork’ splitting and period doubling
- Spectral features →  $\gamma$  and  $v_{\text{eff}}$ ; Ex.: ICRH driven n=7 TAE



# Nonlinear AE wave-particle interaction

## Chaotic regime

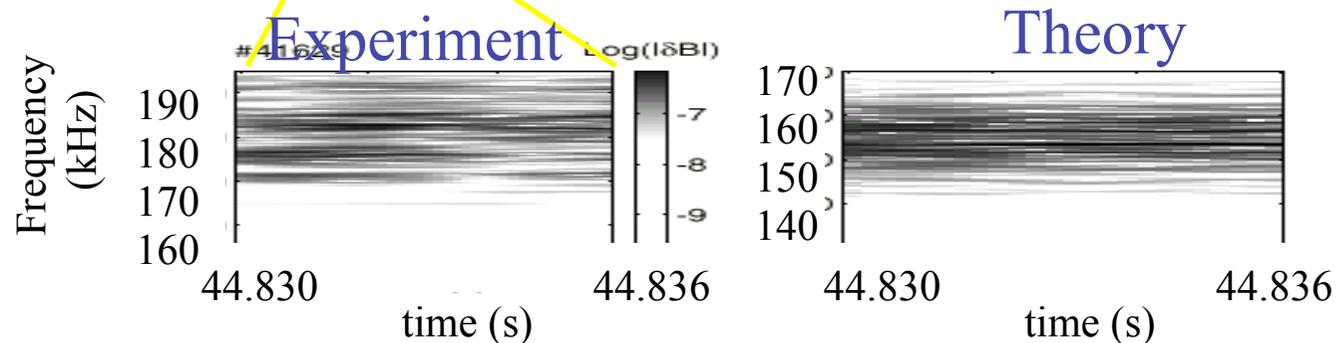
Larger  $\gamma/v_{\text{eff}}$ : chaotic AE oscillations



broadening reproduced  
by theory for

$$\gamma/v_{\text{eff}} = 0.7$$

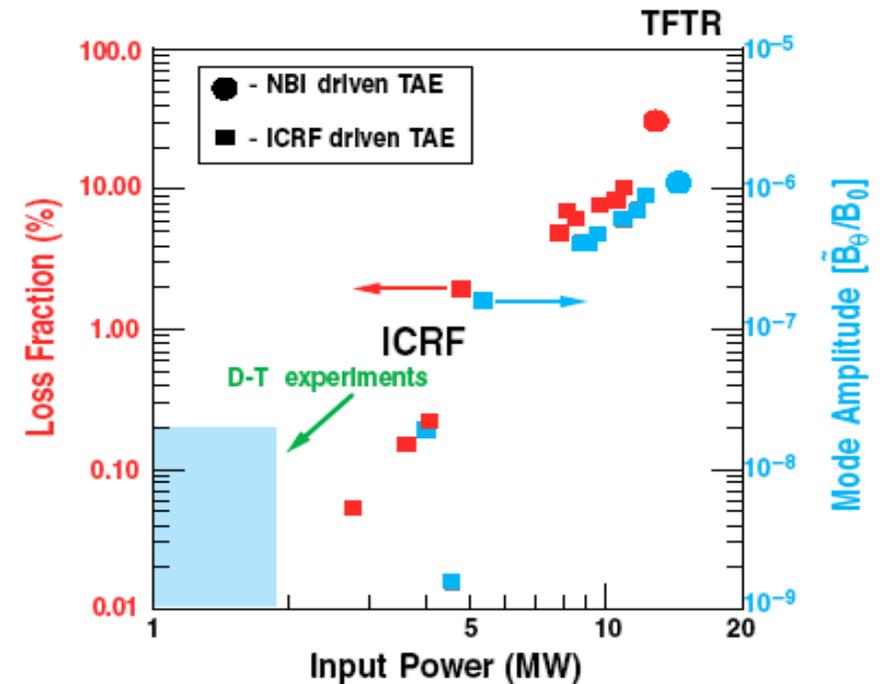
$$\gamma/\omega = 3\%$$



# AE redistribution and losses

## Questions and opportunities

- Limits to ITER operational scenarios?
  - ITER can withstand only  $\sim 5\%$  of  $\alpha$  losses
- Why were losses not observed in DT?
  - Q too low both in TFTR and JET
  - Losses clearly seen for other fast ions

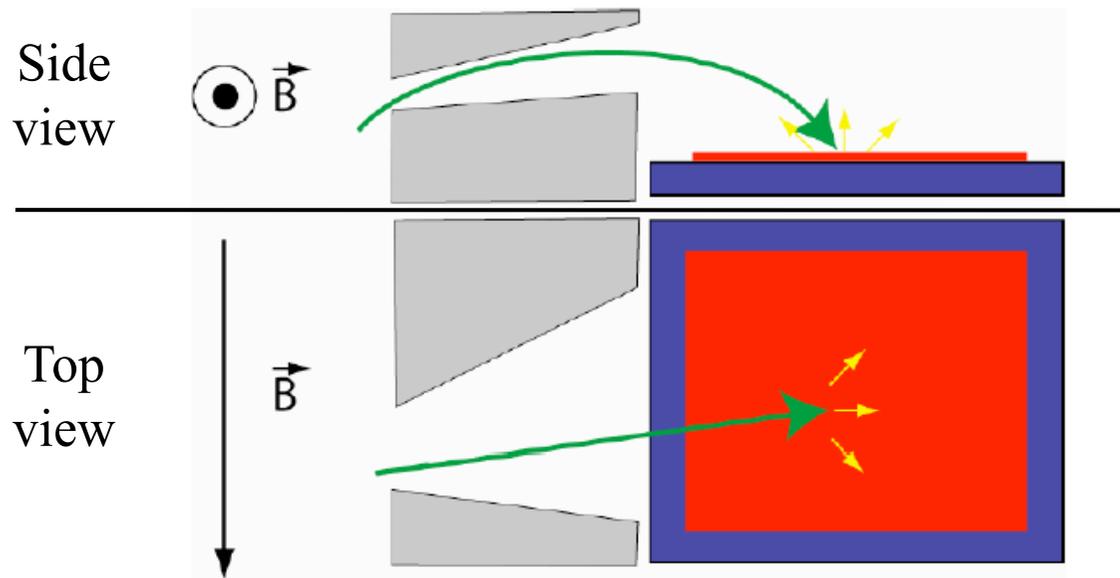


- Good qualitative understanding of weakly nonlinear regimes
- First self-consistent models for ITER
  - Need validation from data on energetic ion redistribution



# AE redistribution and losses

## Measurement techniques - scintillator probe



- Gyromotion of fast ions
- Particle selection by slits
- Light emission by scintillator

Gyro-radius

$$\rho \propto \frac{mV_{\perp}}{ZB}$$

Pitch-angle

$$\theta = \cos^{-1} \frac{V_{\parallel}}{V}$$

Species

$\rho$  @B=3T

$\alpha$ (3.5 MeV)

9.0 cm

P(3.0 MeV)

8.3 cm

T(1.0 MeV)

8.3 cm

# AE redistribution and losses

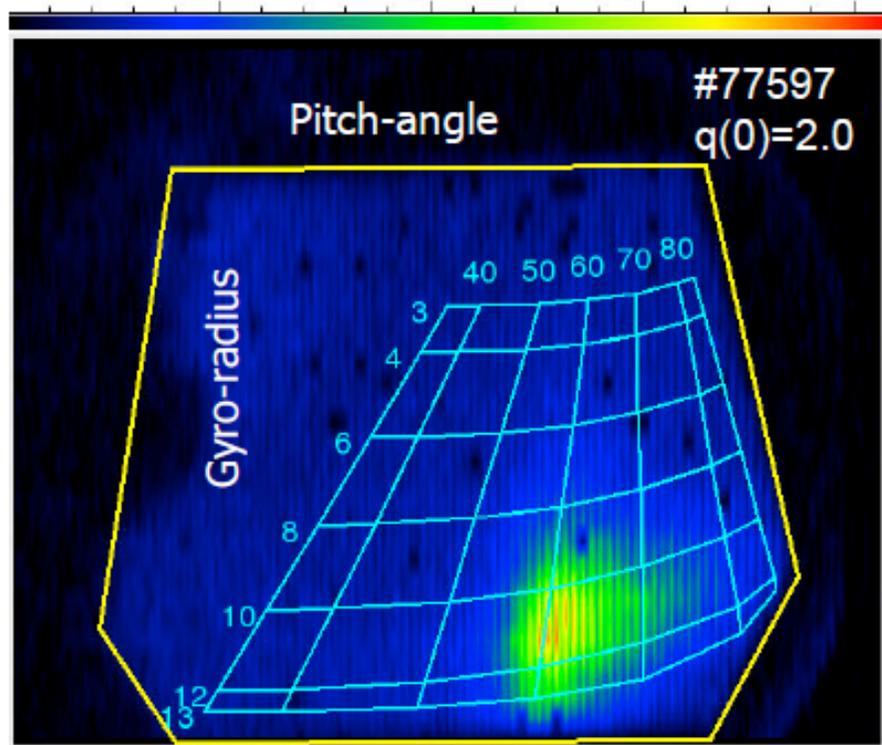
## Measurement techniques - JET scintillator probe



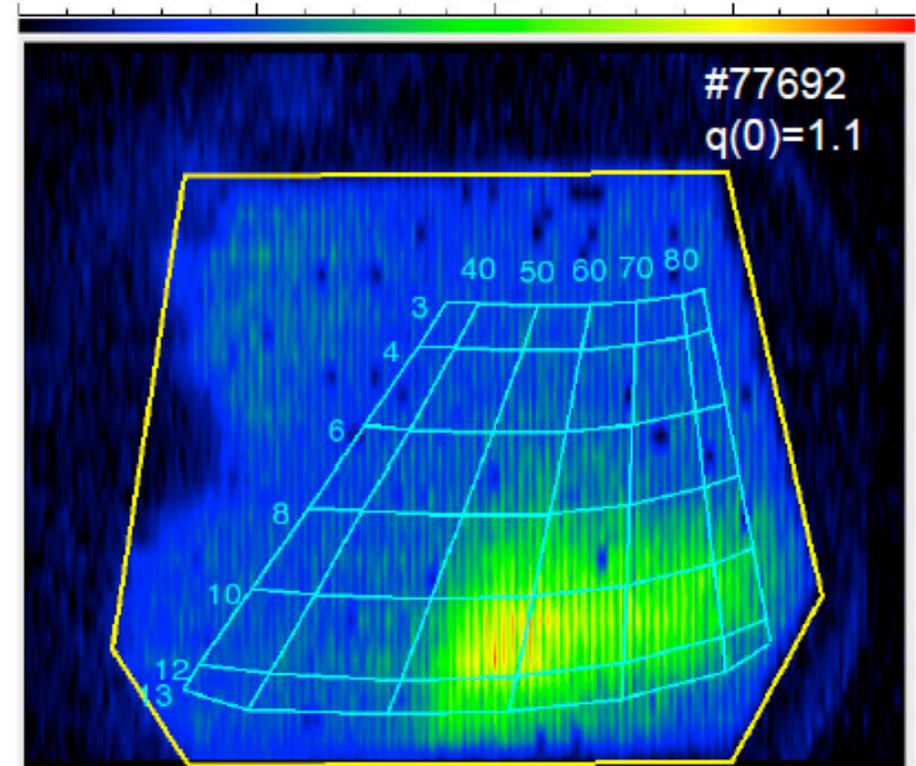
# AE redistribution and losses

## JET scintillator probe – ex. data on first orbit losses

1-MeV tritons and 3-MeV protons



Discharge 2.7T / 1.8 MA

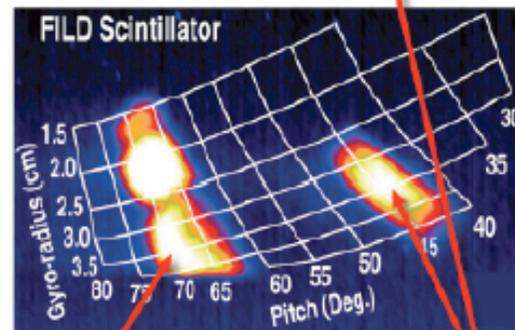
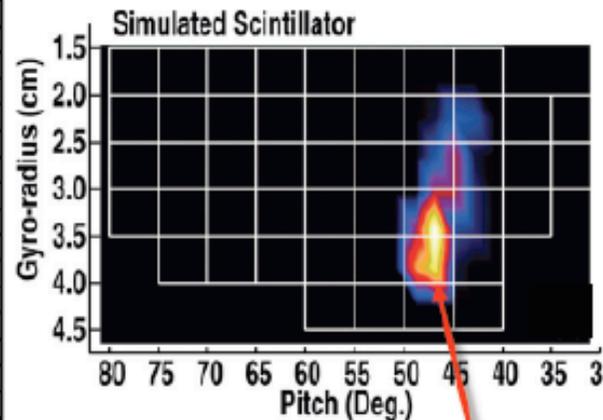
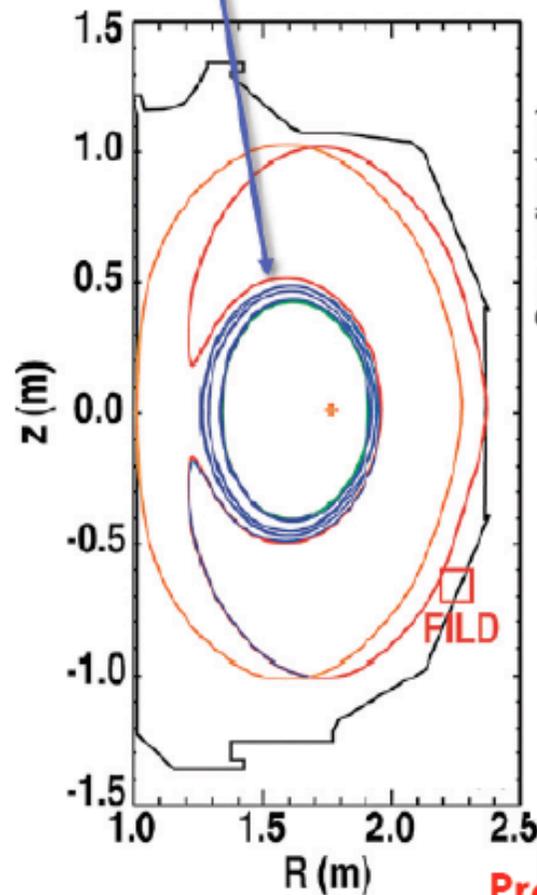


Discharge 2.7T / 2.5 MA

# AE redistribution and losses

## DIII-D scintillator probe – ex. data on AE losses

### Typical Loss Trajectory



Prompt losses  
(not modeled)

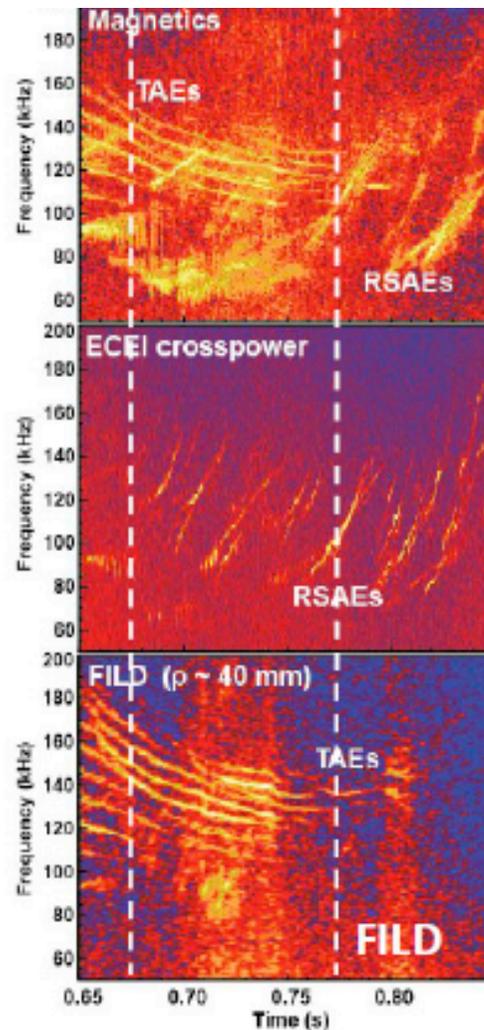
AE induced  
losses

- Loss simulations follow particles from TRANSP distribution function in presence of NOVA eigenmodes
  - Amplitudes obtained from experiment
- Losses at FILD peak near injection energy (80 keV)
- Most common loss mechanism observed is transition of counter passing particles to trapped lost orbit

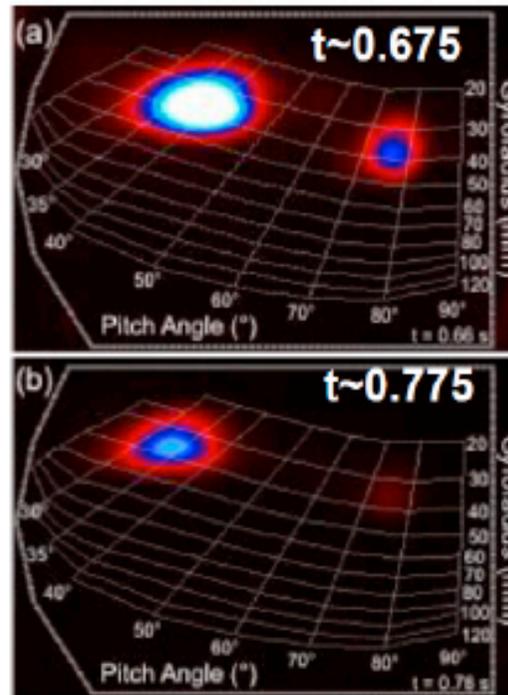
M.A. Van Zeeland, et al., Phys. Plasmas, 18, 056114(2011)

# AE redistribution and losses

## Asdex-U scintillator probe – ex. data on AE losses



### FILD SCINTILLATOR



- FILD spectrogram shows clear coherent losses from beam driven TAEs
- FILD Scintillator indicates TAE induced losses appear near gyro-radius corresponding to injection energy

*M. Garcia-Munoz et al., IAEA FEC, Daejeon, Korea (2010)*

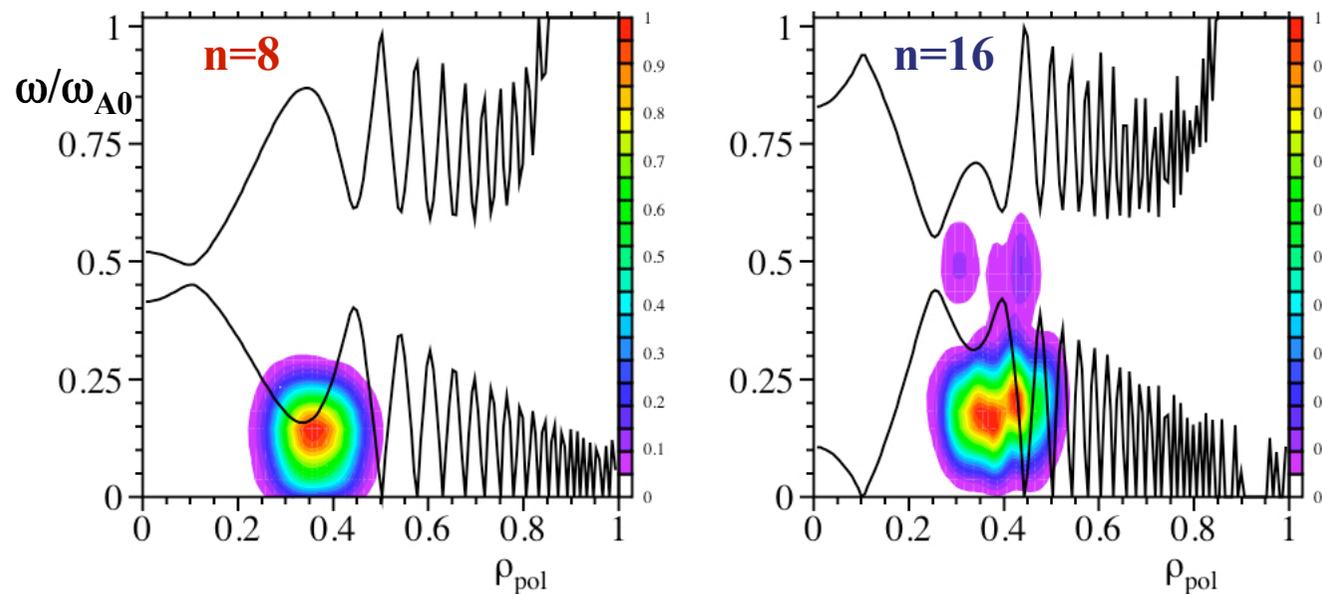
*M. Garcia-Munoz et al., Nucl Fusion 51 103013 (2011)*

# Energetic ions and burning plasma physics

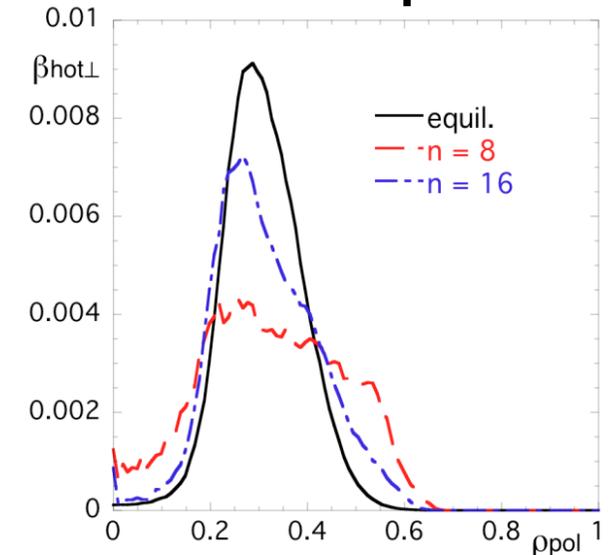
## Example of self-consistent simulation

- H-mode scenario in FAST device
  - Spectrum of Alfvénic fluctuations similar to that expected in ITER
  - Hybrid MHD-gyrokinetic code *XHMGC*
  - Radial redistribution, with limited global losses, of ICRH created fast ions

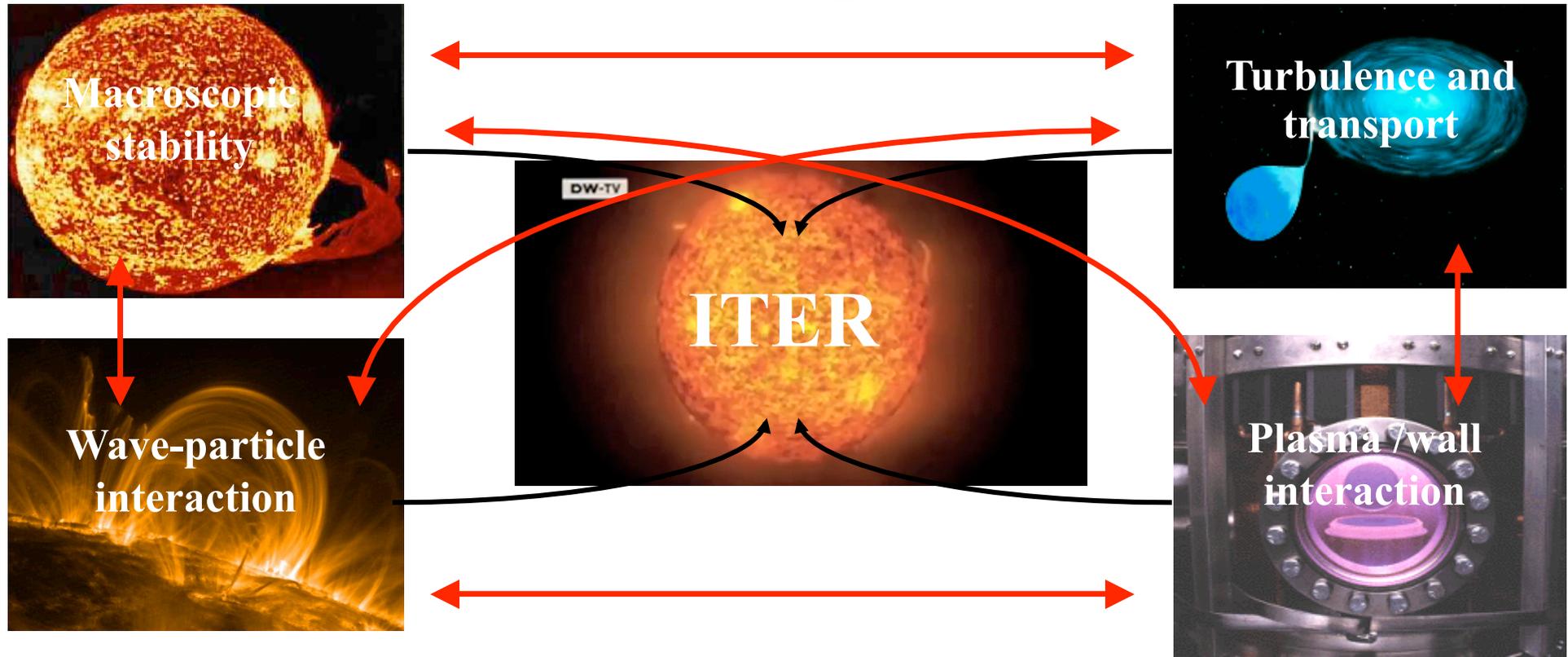
### Mode spectrum and radial structure



### Fast ion radial profile



# Burning plasmas are self-organized systems in which all elements are coupled via energetic ions



- Progress is possible in today's weakly self-heated plasmas
- But to demonstrate the feasibility of fusion we need to produce and control actual burning plasmas, such as ITER