



**The Abdus Salam  
International Centre for Theoretical Physics**



**2272-6**

**Joint ICTP-IAEA School on Synchrotron Applications in Cultural Heritage and  
Environmental Sciences and Multidisciplinary Aspects of Imaging Techniques**

*21 - 25 November 2011*

**Ion Beam Analysis Techniques for Cultural Heritage and Environmental  
Applications**

Massimo Chiari  
*INFN, Florence  
Italy*

# Ion Beam Analysis Techniques for Cultural Heritage and Environmental Applications

Massimo Chiari / *I.N.F.N. Florence*

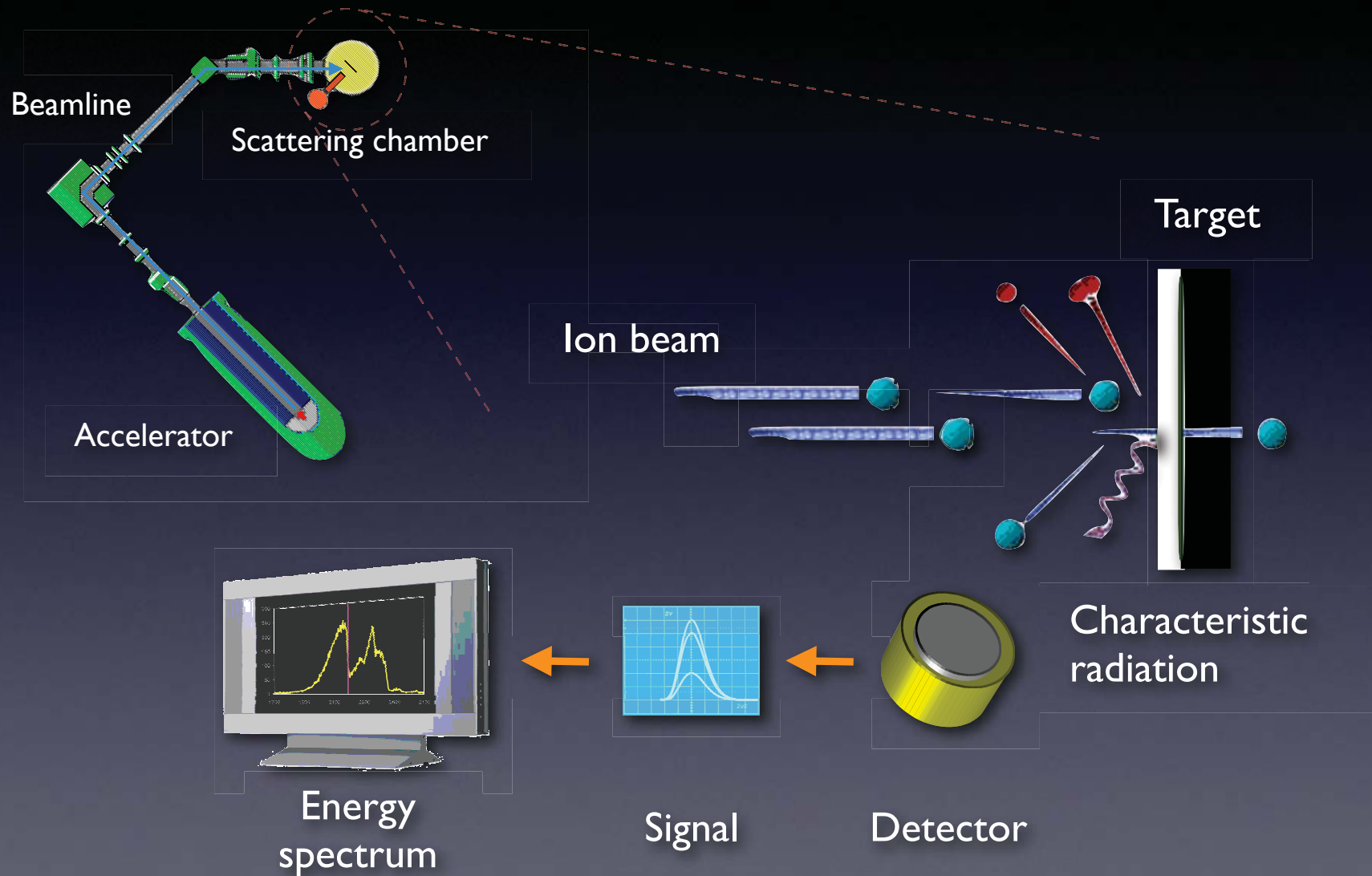


*chiari@fi.infn.it*



*max0068*

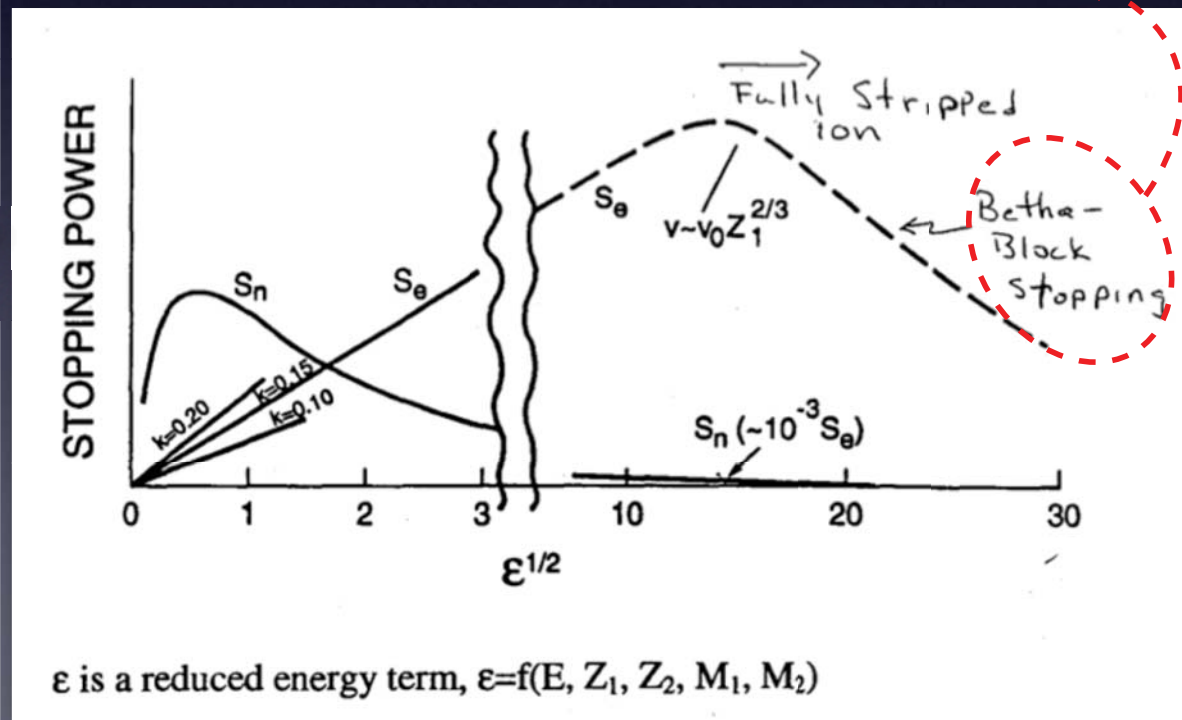
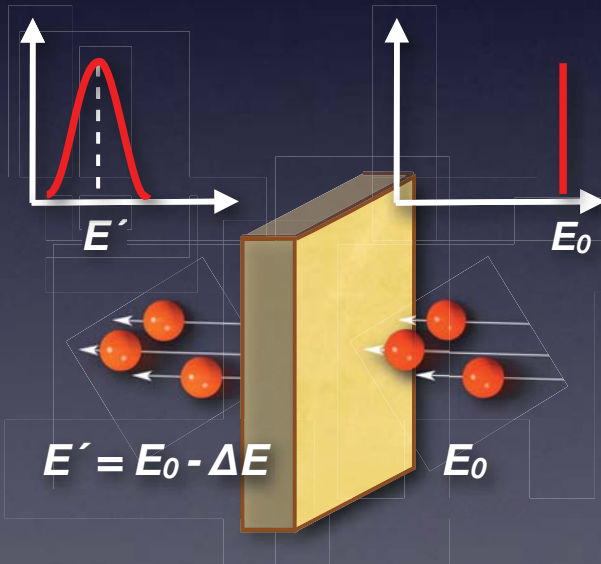
# IBA techniques basics



# Stopping power

The “stopping power” (the energy lost per unit length,  $dE/dx$ ) is a macroscopic and measurable quantity, describing the average interaction of the ion with the material:

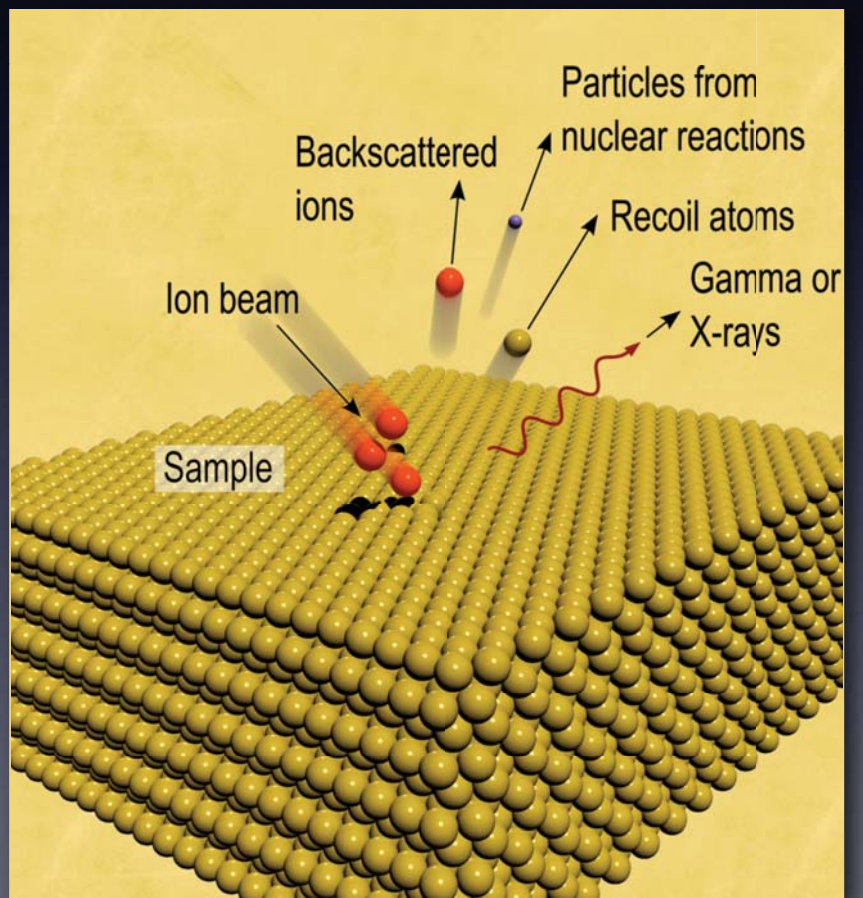
$$-\frac{dE}{dx} = \frac{4\pi}{m_e c^2} \cdot \frac{n z^2}{\beta^2} \cdot \left(\frac{e^2}{4\pi\epsilon_0}\right)^2 \cdot \left[ \ln \left( \frac{2m_e c^2 \beta^2}{I \cdot (1 - \beta^2)} \right) - \beta^2 \right]$$





# IBA

## *Ion Beam Analysis*



<b>Beam IN</b>	<b>Beam OUT</b>	<b>Analytical technique</b>
ion	ion	RBS, NRA
ion	target	ERDA, SIMS, SNMS
ion	X-ray	PIXE
ion	Gamma-ray	PIGE, Activation Analysis
ion	h $\nu$	Ionoluminescence (IL)

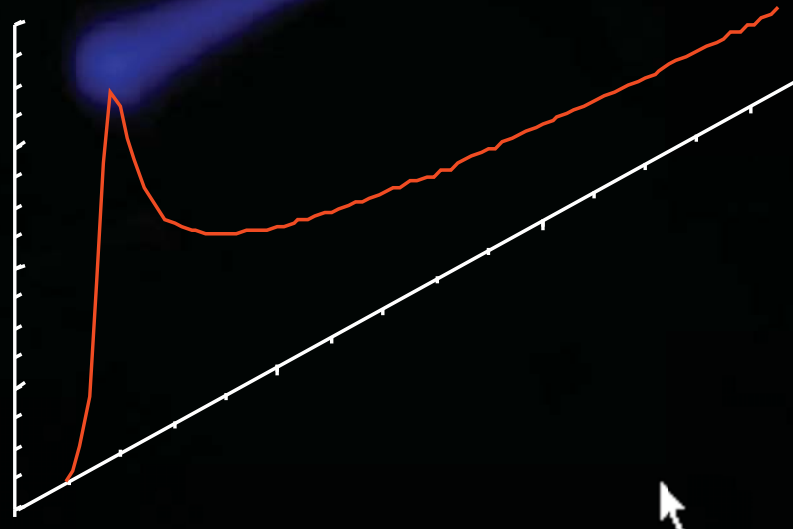
# General features of IBA

- Multielemental
- Quantitative analysis (“traceability”)
- High sensitivity (1-100 ppm in at/cm<sup>3</sup>; 10<sup>11</sup>-10<sup>12</sup> in at/cm<sup>2</sup>)
- Surface analysis (10 Å - 10 μm)
- Depth profiling
- Non-destructive
- No sample pre-treatment
- Microanalysis (lateral resolution <1 μm)
- 2D mapping

# External beam

## Advantages

direct analysis of artefacts having any shape and any size  
no sampling  
no charging, no preparation (conductive coating etc.)  
no heating, reduced damage risk  
easy sample positioning  
fast and efficient



## Disadvantages

energy loss  
energy straggling  
beam lateral spread

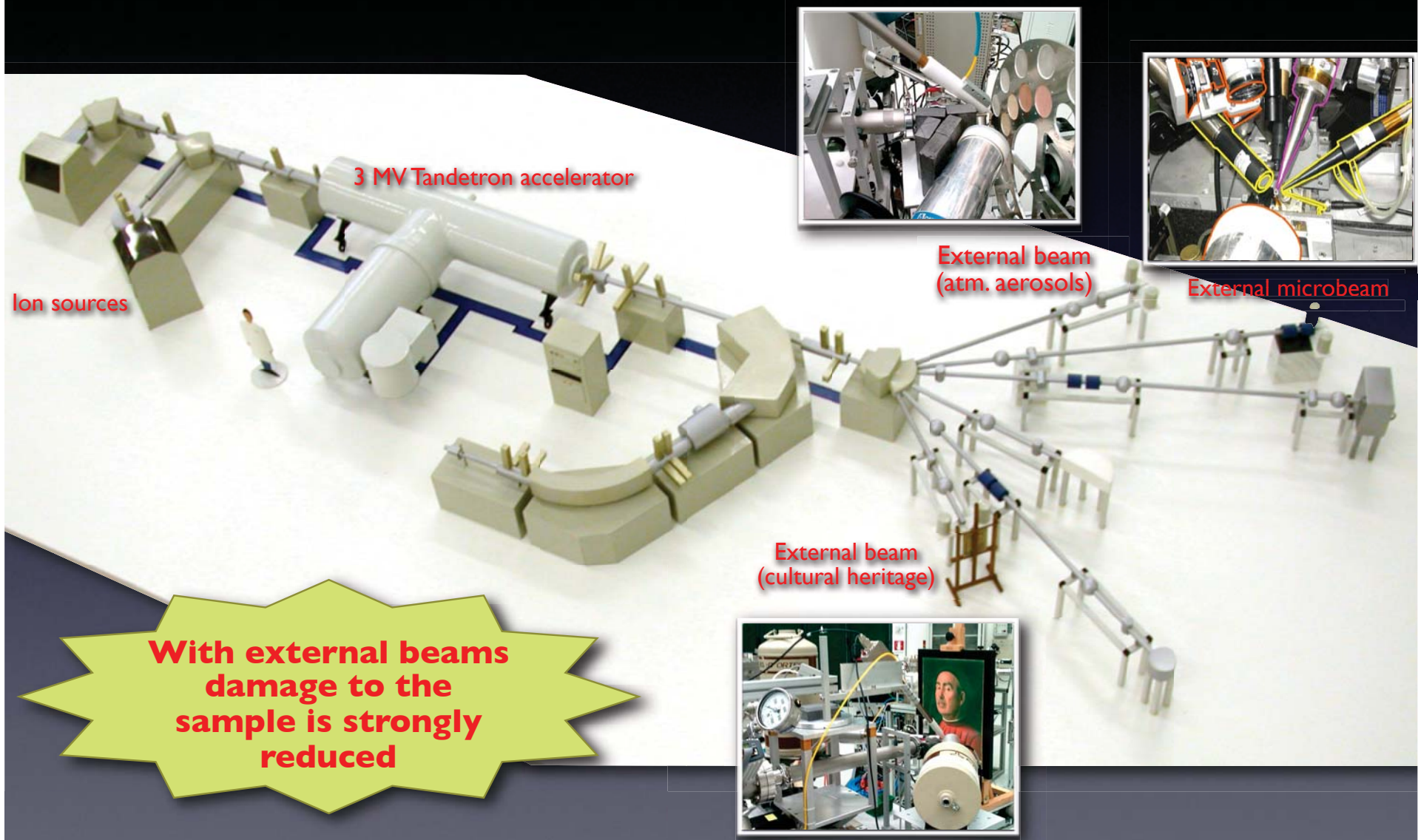
# The LABEC laboratory in Florence



- 3 MV Tandatron accelerator
- 3 independent ion sources
- 6 beam lines for IBA (3 external-beam lines)
- 1 beam line for AMS



# The external-beam lines at LABEC

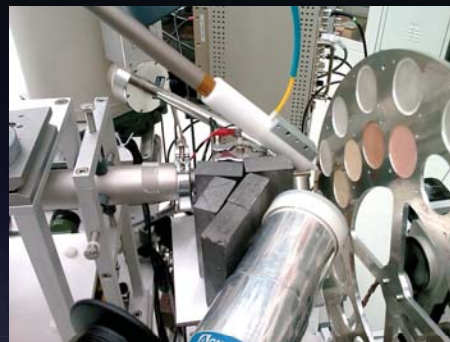


# External-beam set-ups



Cultural Heritage  
*-45° beamline*

- PIXE (x2)
- PIGE
- RBS



Atmospheric aerosol  
*+45° beamline*

- PIXE (x2)
- PIGE
- PESA

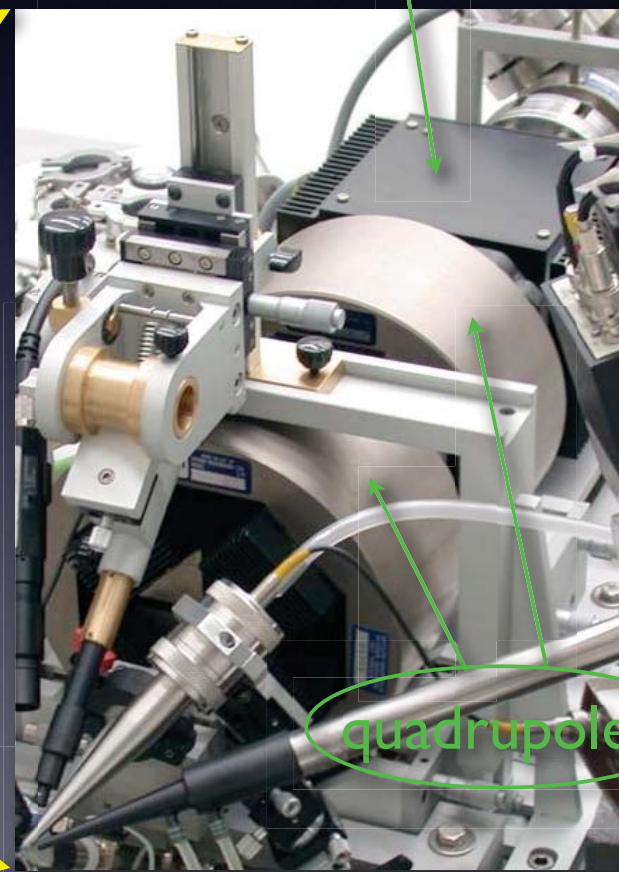
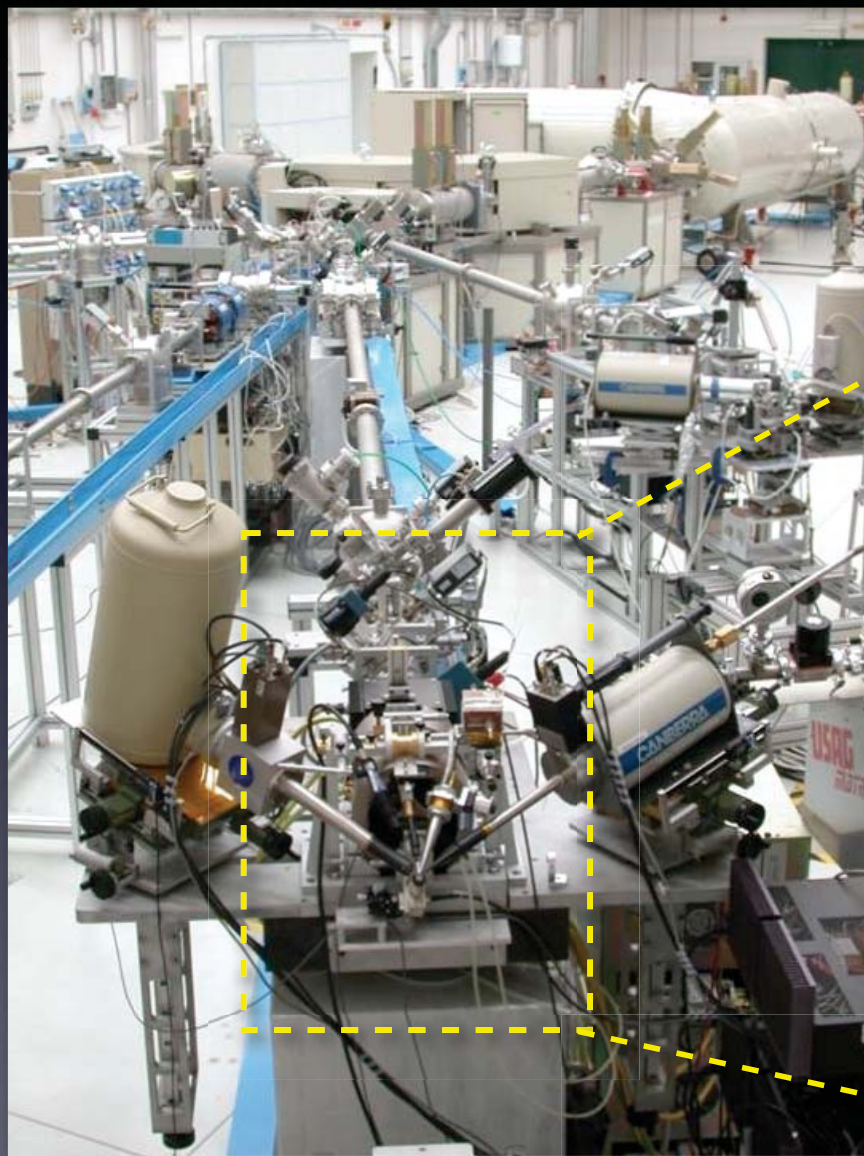


Microbeam  
*+30° beamline*

- 10  $\mu\text{m}$  @ 3MeV p
- PIXE (x2)
- PIGE
- RBS
- PESA/ERDA
- IBIL



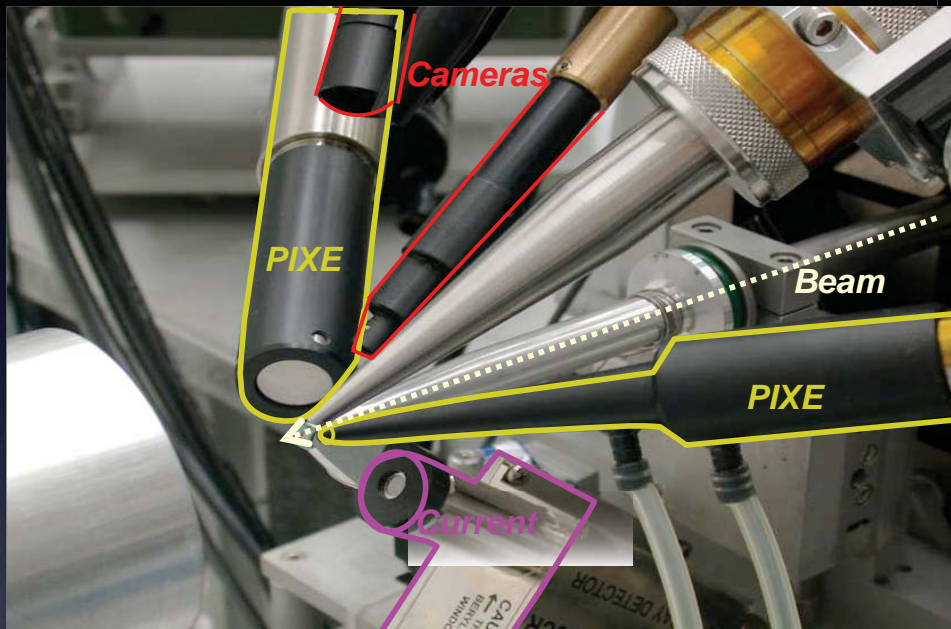
# The external microbeam line



scanning coils

quadrupoles

# Microbeam experimental set-up



- $\text{Si}_3\text{N}_4$  extraction window (100, 200 or 500 nm thick)
- Target at 2-3 mm from the exit window, path saturated with helium
- 3 MeV protons:  
**10  $\mu\text{m}$  spatial resolution**  
~10 keV energy straggling

Standard two detectors set-up, (“small” and “big”) optimized for low and medium-high energy X-rays detection

(+ PIGE, RBS, STIM, IBIL)



# External beam PIXE-PIGE facility

## **Ge Detector ( $\gamma$ )**

60 mm x 23 mm coaxial  
28% efficiency  
1 keV FWHM @ 1.33 MeV

He

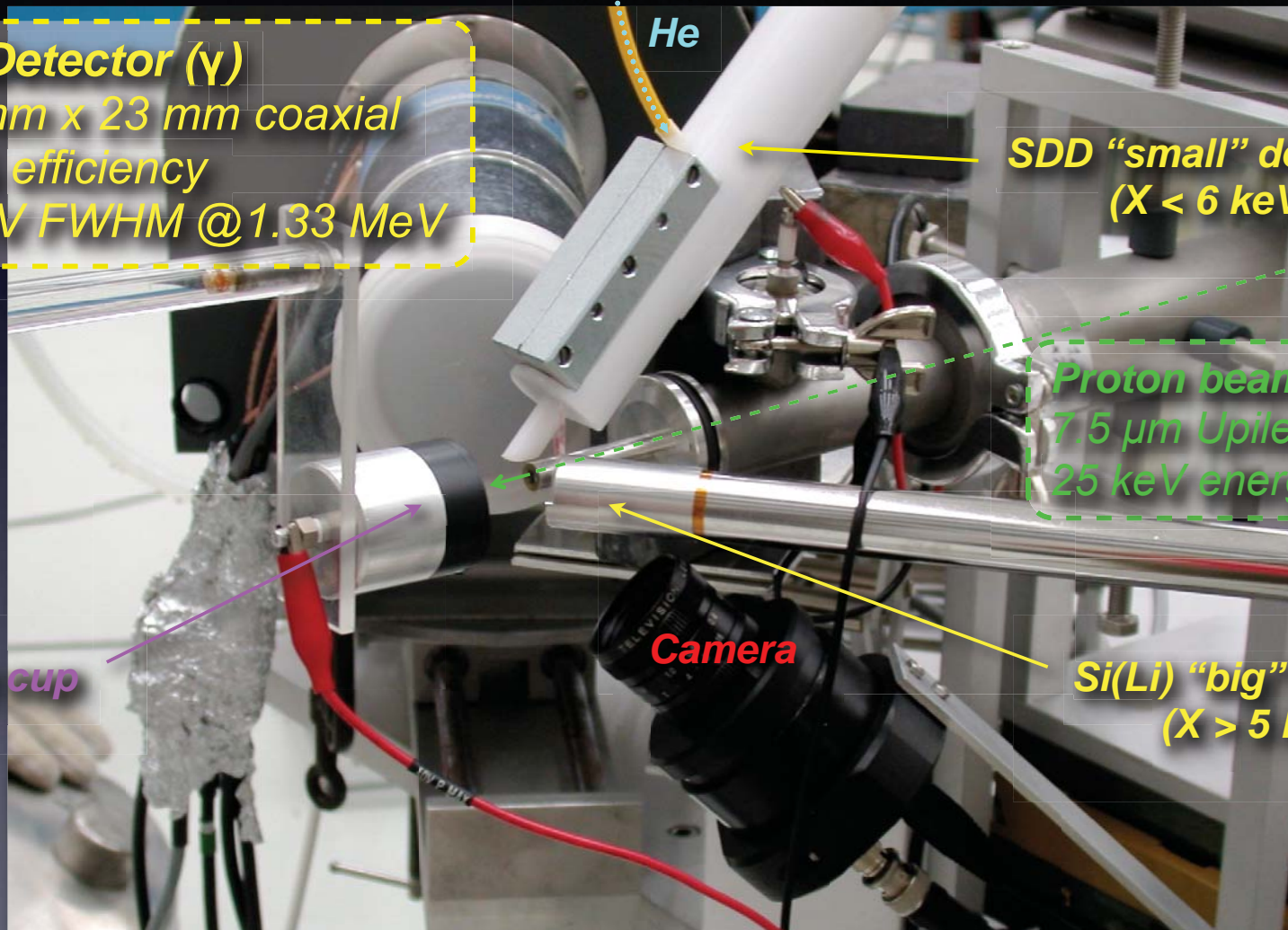
SDD "small" detector  
( $X < 6$  keV)

Proton beam  
7.5  $\mu\text{m}$  Upilex window  
25 keV energy spread

Faraday cup

Camera

Si(Li) "big" detector  
( $X > 5$  keV)



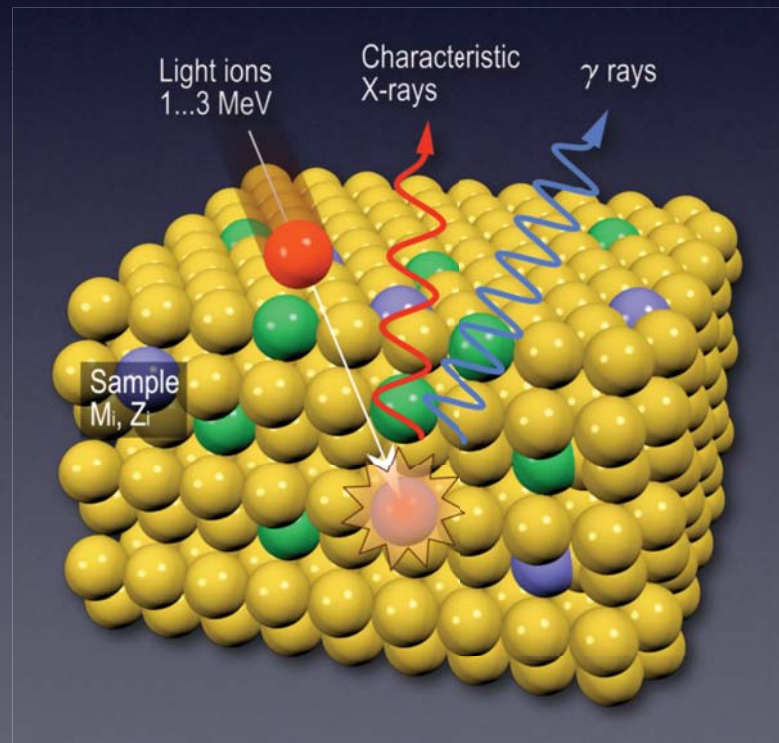
# PIXE

## *Particle Induced X-ray Emission*

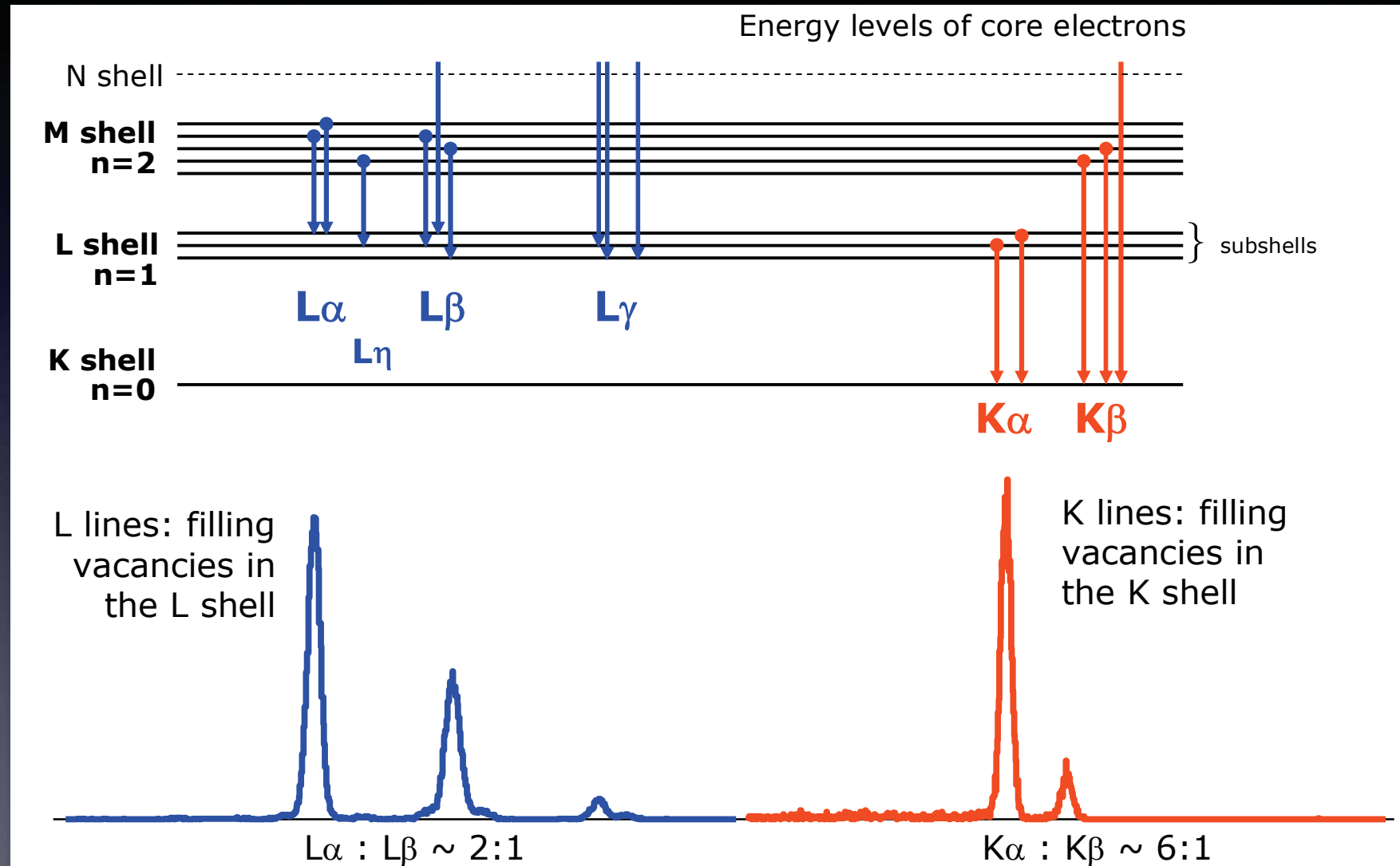
Emission of characteristic X-rays following ionization from incident ions



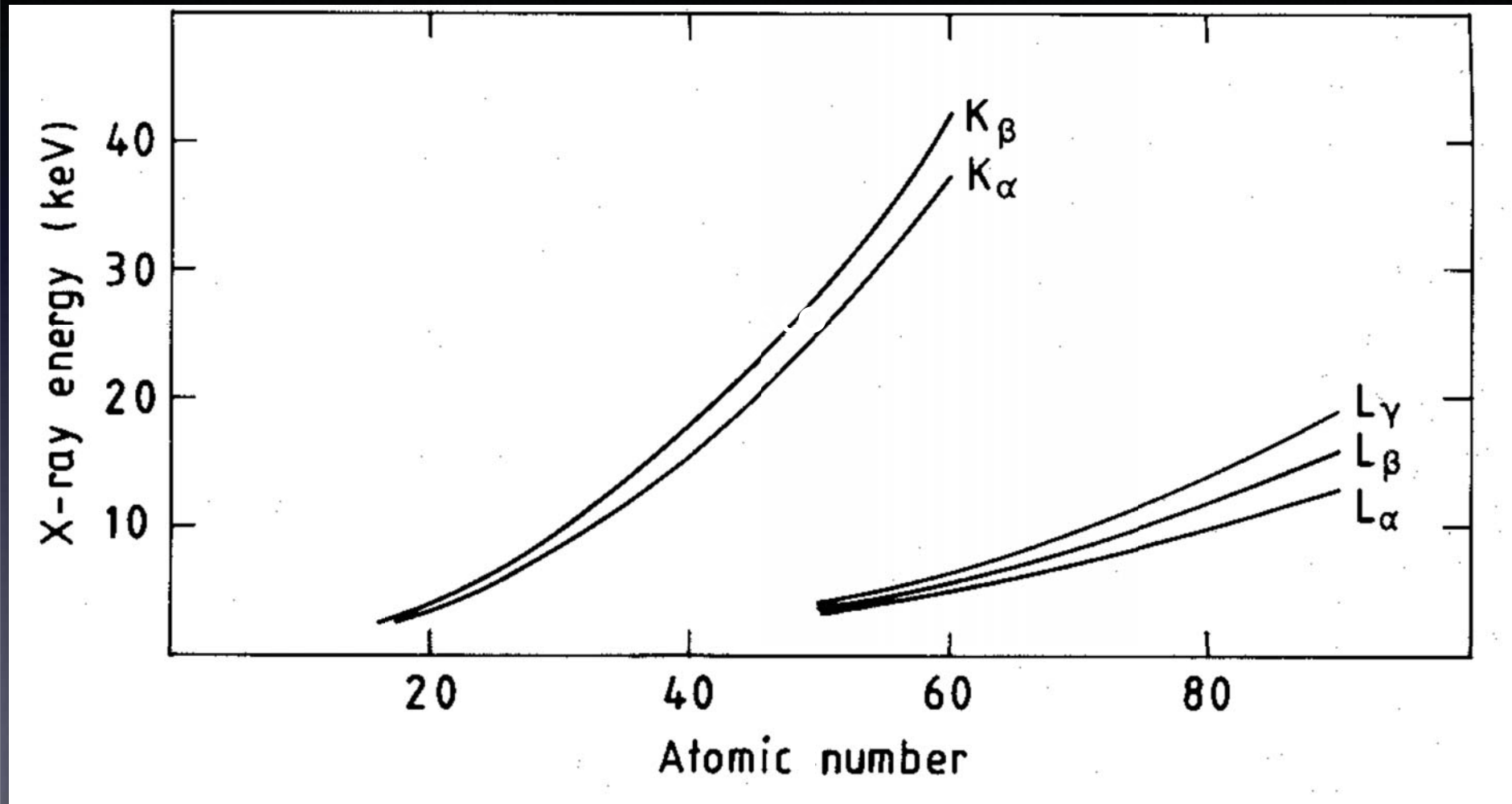
**Z > 10**



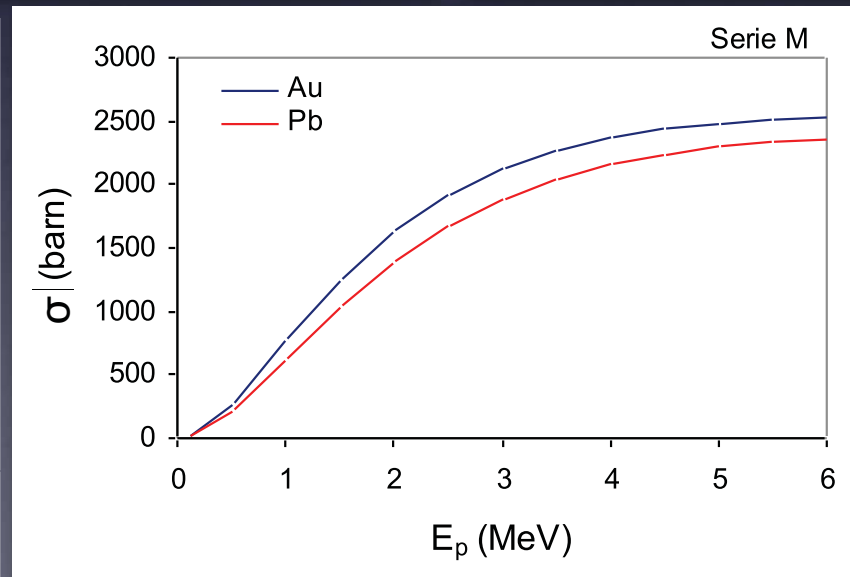
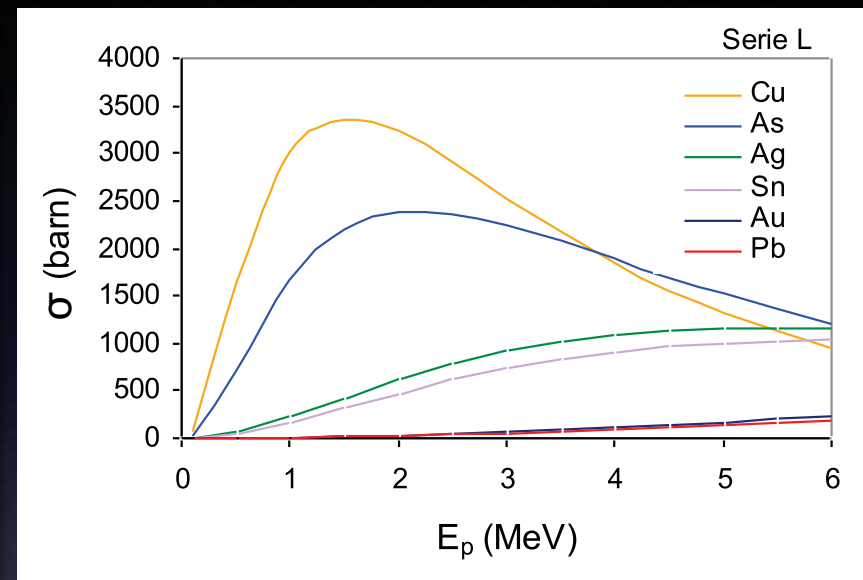
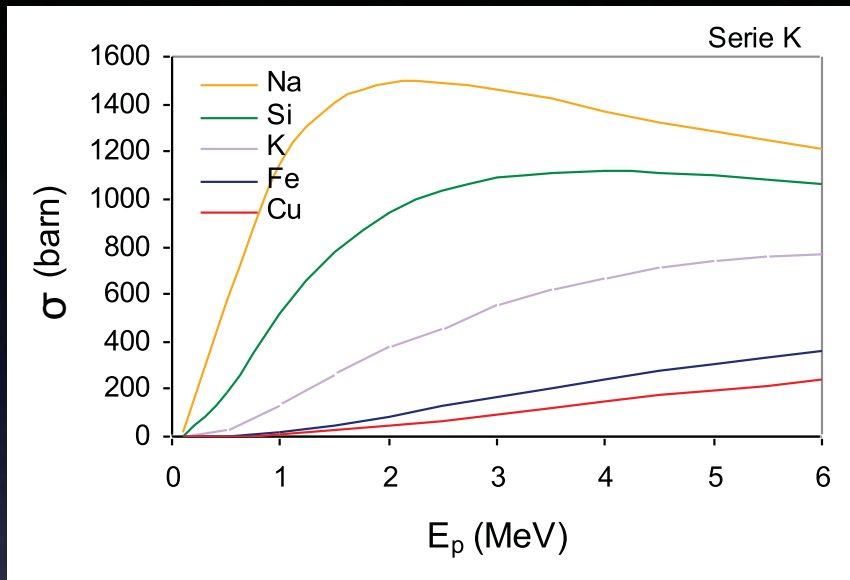
# Energy of characteristic X-rays



# Energy of characteristic X-rays



# X-ray production cross sections



# Advantages of PIXE

- very fast, high-sensitivity, **non-destructive** analysis
- **quantitative** analysis
- minimum energy of detected X-rays typically  $\sim 1$  keV
  - ➔ *all the elements with  $Z \geq 11$  are quantifiable simultaneously*

# Limitations of PIXE

- no information on the organic components
- no direct information on chemical bonds

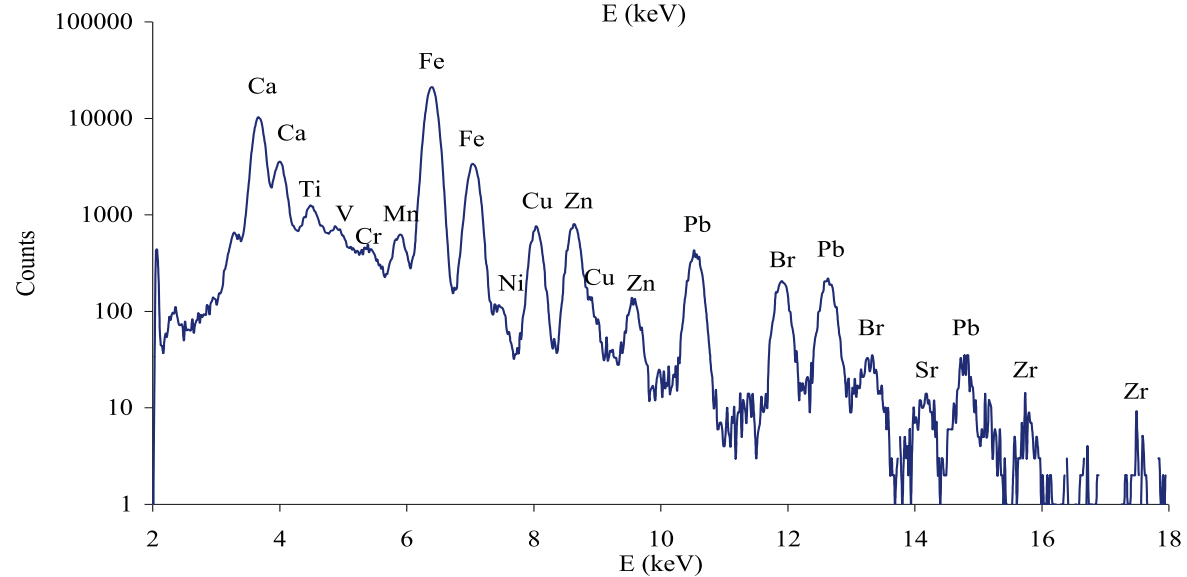
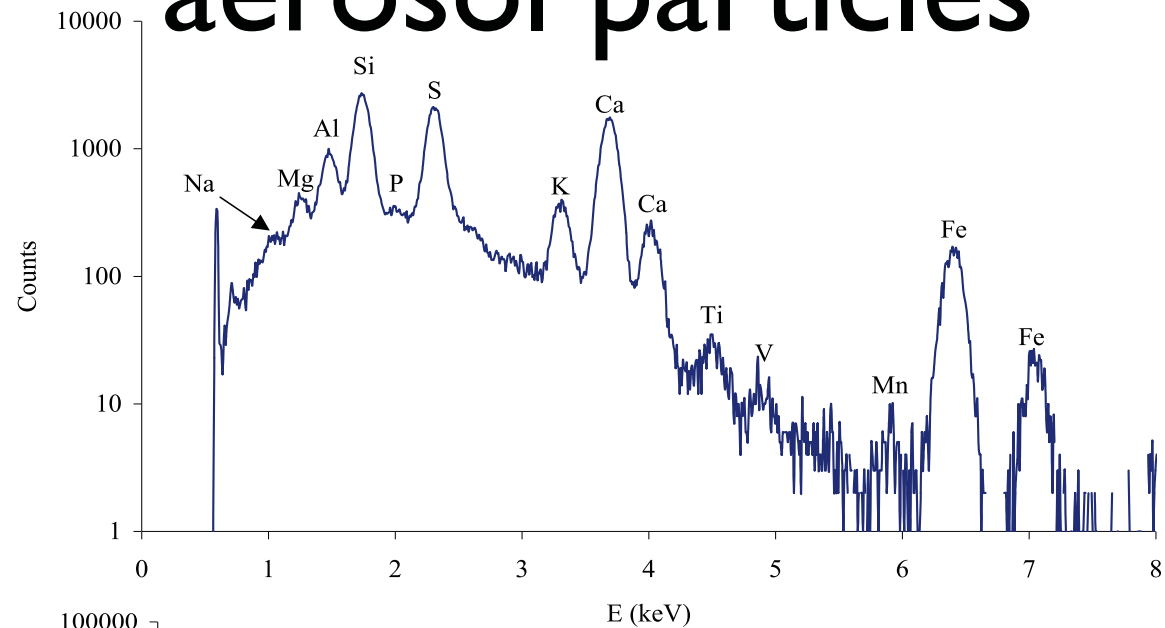
*but... hypothesis on stoichiometry through quantitative and multielemental analysis*

- no direct information on the stratigraphy and the depth distribution of the elements

*but... Differential PIXE*



# Example of PIXE spectra: aerosol particles





# Quantitative analysis (thin target)

$$Y_0(Z) = N_P \cdot N_Z \cdot t \cdot \sigma_{Z,E0} \cdot (\alpha_Z \cdot \epsilon_Z \cdot \Delta\Omega / 4\pi)$$

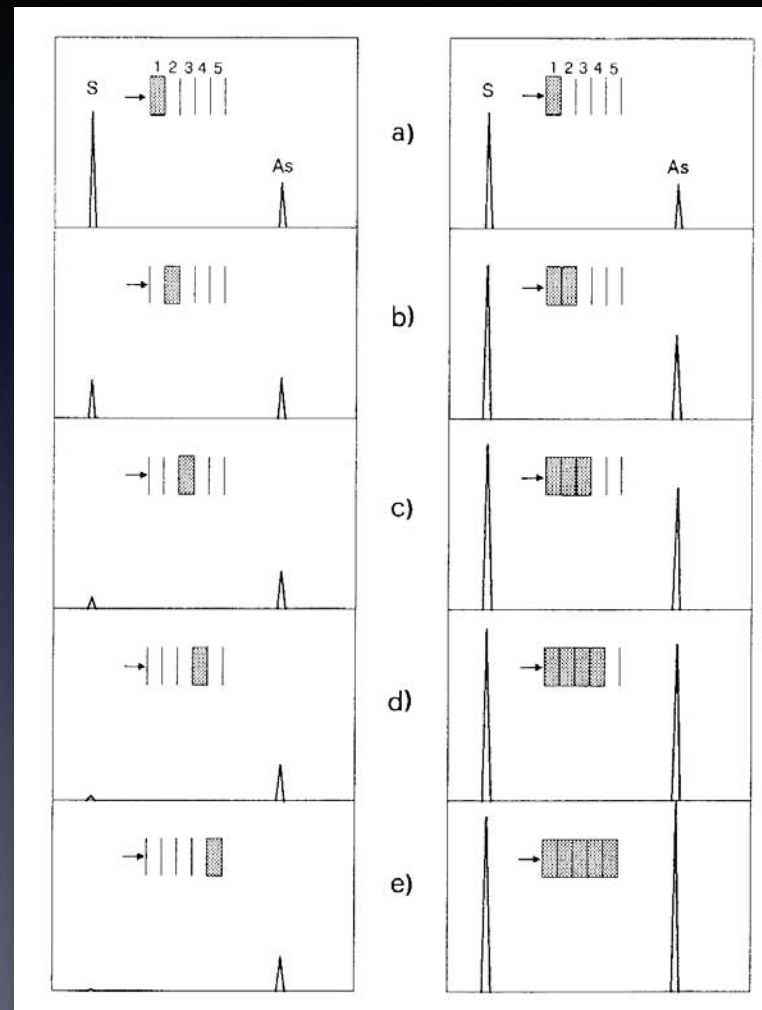
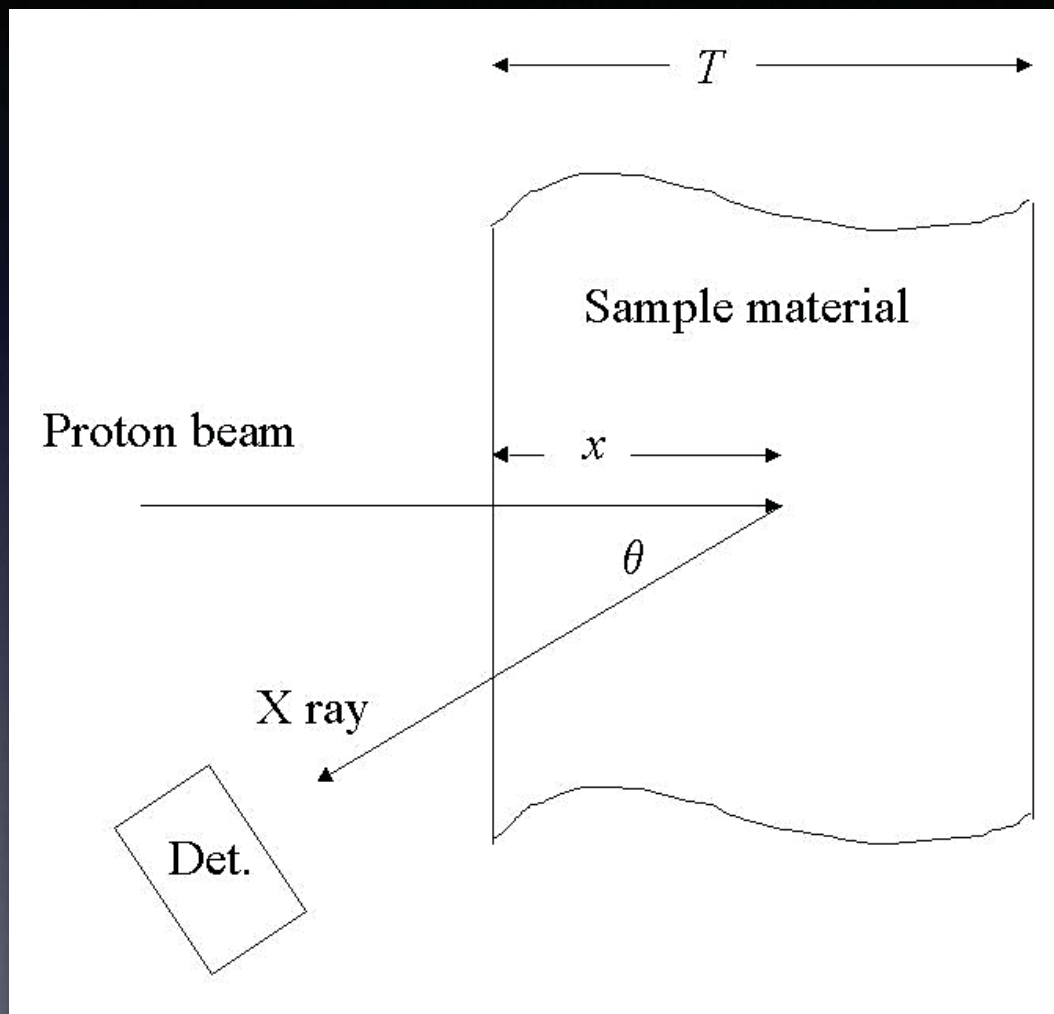
$$Y_0(Z) = (Q/e)(N_A/A)(\rho_Z t) \cdot \sigma_{Z,E0} \cdot (\alpha_Z \cdot \epsilon_Z \cdot \Delta\Omega / 4\pi)$$

with  $\eta_Z = (1/e)(N_A/A) \cdot \sigma_{Z,E0} \cdot (\alpha_Z \cdot \epsilon_Z \cdot \Delta\Omega / 4\pi)$

$$Y_0(Z) = \eta_Z \cdot Q \cdot (\rho_Z t)$$

$$(\rho_Z t) = Y_0(Z) / (\eta_Z \cdot Q)$$

# Thick targets



# Quantitative analysis (thick targets)

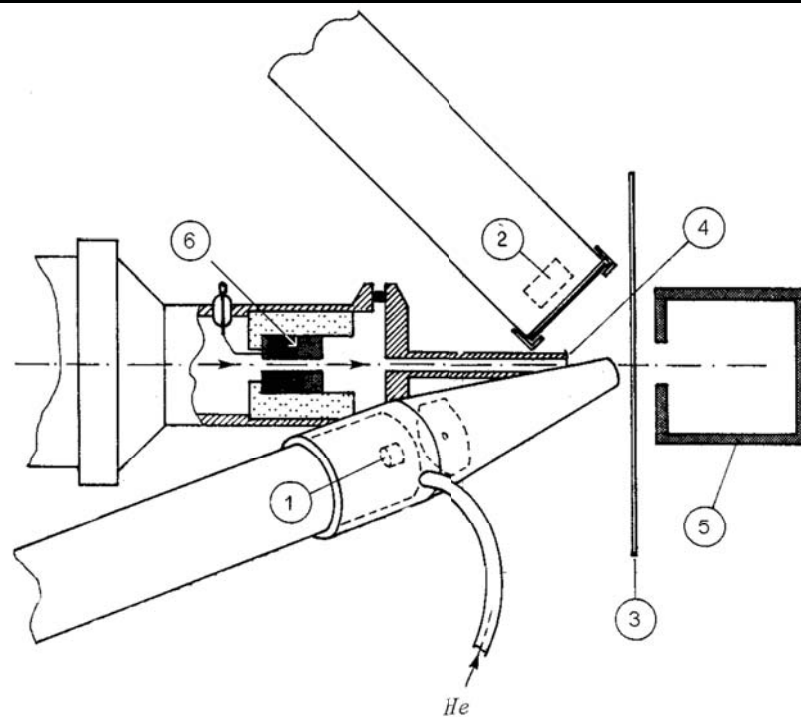
$$Y(Z) = (Q/e)(N_A/A)(\alpha_Z \cdot \varepsilon_Z \cdot \Delta\Omega/4\pi) \cdot \rho_Z \int_0^T \sigma_{Z,E} \cdot \exp(-\mu \cdot x / \cos\theta) \cdot dx$$

$$Y(Z) = (Q/e)(N_A/A)(\alpha_Z \cdot \varepsilon_Z \cdot \Delta\Omega/4\pi) (\rho_Z / \rho) \int_0^E \sigma_{Z,E} \cdot \exp(-\mu \cdot x / \cos\theta) \cdot dE / S(E)$$

$$F(Z) = Y_0(Z) / Y(Z) = \frac{\rho \cdot T \cdot \sigma_{Z,E0}}{\int_0^E \sigma_{Z,E} \cdot \exp(-\mu \cdot x / \cos\theta) \cdot dE / S(E)}$$

$$(\rho_Z t) = F(Z) \cdot Y(Z) / (\eta_Z \cdot Q)$$

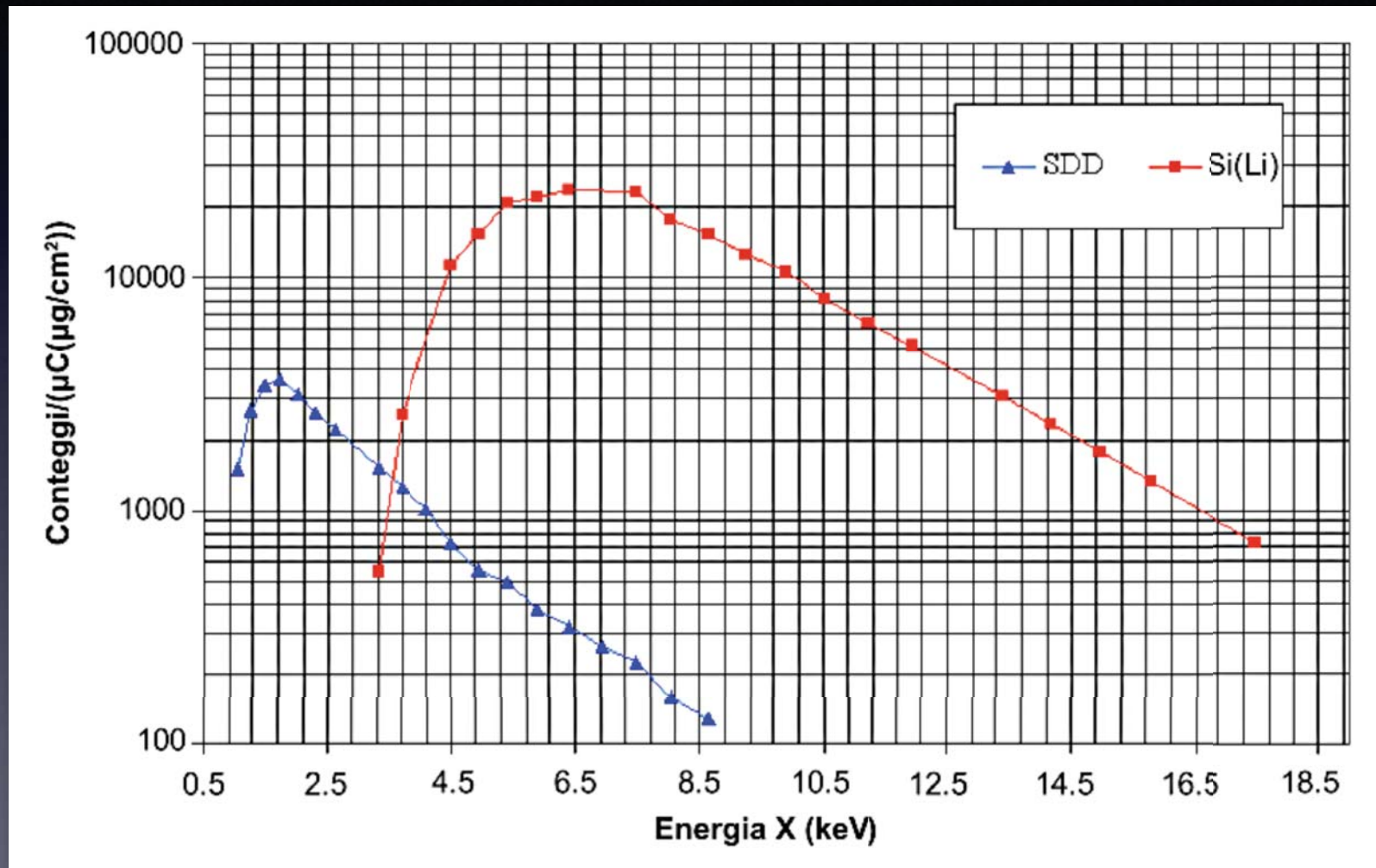
# 2-detectors PIXE set-up



- 1,2) X ray detectors    3) sample to analyse  
 4) beam exit window    5) Faraday cup  
 6) graphite collimator

Target	X-rays	What is needed	Detector features
Low-Z elements	Low energy High cross sections	Minimum dead layers Small solid angles	Thin entrance window Small active area
Medium-high-Z elements	High energy Low cross sections	Large solid angles Efficiency	Large active area Large active thickness

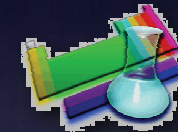
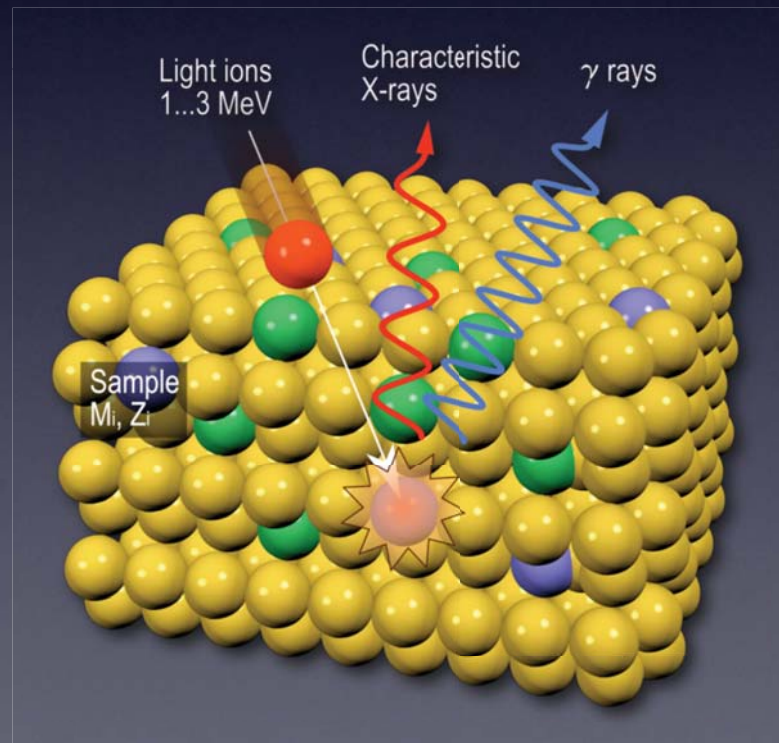
# Detection efficiency for a 2-detectors PIXE set-up



# PIGE

## *Particle Induced Gamma-ray Emission*

Prompt emission of gamma-rays during the ion beam irradiation



**Li, B, F,  
Na, Al...**

# Nuclear reactions with prompt emission of gamma -rays

Radiative capture (direct reaction)	$a + A \rightarrow B^* \rightarrow B + \gamma$	$^{27}\text{Al}(p,\gamma)^{28}\text{Si}$
Inelastic scattering	$a + A \rightarrow A^* + a'$ $\quad \searrow$ $\quad \quad A + \gamma$	$^{27}\text{Al}(p,p'\gamma)^{27}\text{Al}$
Rearrangement collisions	$a + A \rightarrow C^* + c$ $\quad \searrow$ $\quad \quad C + \gamma$	$^{27}\text{Al}(p,\alpha\gamma)^{24}\text{Mg}$



# List of proton-induced reaction

Element	$E_\gamma$ (keV)	Nuclear origin	Transition	Detection limit (%)	Possible interferences
Li	429	${}^7\text{Li}(p, n\gamma){}^7\text{Be}$	429 + 0	0.01	As(427), B(429)
	478	${}^7\text{Li}(p, p'\gamma){}^7\text{Li}$	478 + 0	$5 \times 10^{-4}$	Be(478), Mn(478)
Be	415	$\text{Be}^9(p, \gamma)\text{B}^{10}$	2154 + 1740	0.1	Ag(415)
	718	$\text{Be}^9(p, \gamma)\text{B}^{10}$	718 + 0		B(718)
	1023	$\text{Be}^9(p, \gamma)\text{B}^{10}$	1740 + 718		Ti(1022)
	1437	$\text{Be}^9(p, \gamma)\text{B}^{10}$	3590 + 2150		
	3562	$\text{Be}^9(p, \alpha\gamma)\text{Li}^6$	3562 + 0		
B	429	${}^{10}\text{B}(p, \alpha\gamma){}^7\text{Be}$	429 + 0	$5 \times 10^{-3}$	As(427), Li(429)
	478	${}^{10}\text{B}(p, \alpha\gamma){}^7\text{Be} + {}^7\text{Li}$	478 + 0		Li(478), Mn(478)
	718	${}^{10}\text{B}(p, p'\gamma){}^{10}\text{B}$	718 + 0		Be(718)
	2124	${}^{10}\text{B}(p, p'\gamma){}^{10}\text{B}$	2124 + 0		
	4433	${}^{11}\text{B}(p, \gamma){}^{12}\text{C}$	4433 + 0		N(4433)



# List of proton-induced reaction

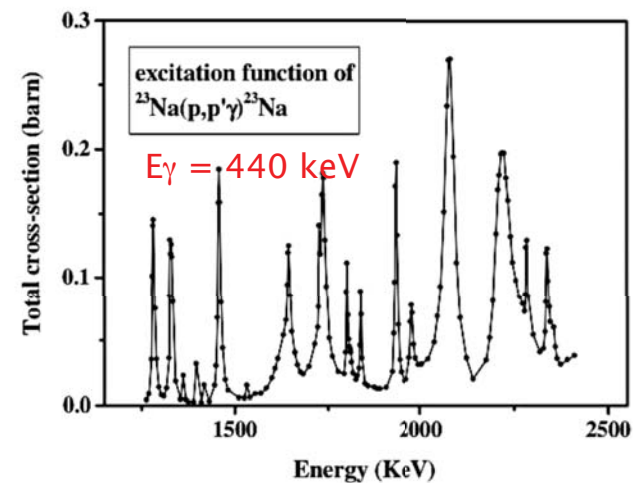
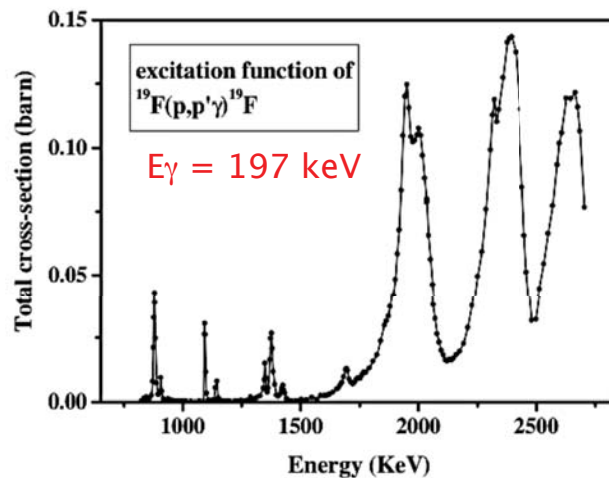
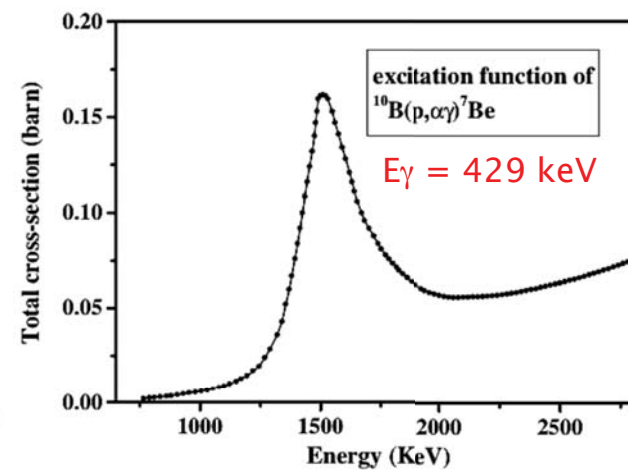
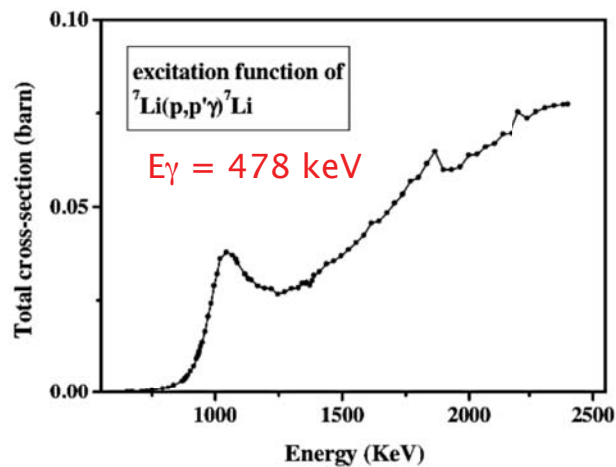
Element	$E_{\gamma}$ (keV)	Nuclear origin	Transition	Detection limit (%)	Possible interferences
C	2357	$^{12}\text{C}(p,\gamma)^{13}\text{N}$	2357 + 0	1	
N	1400	$^{14}\text{N}(p,\gamma)^{15}\text{O}$			Cr(1400)
	4433	$^{15}\text{N}(p,\alpha)^{12}\text{C}$	4433 + 0		B(4433)
O	110	$^{18}\text{O}(p,\gamma)^{19}\text{F}$	110 + 0		F(110), W(111)
	197	$^{16}\text{O}(p,\gamma)^{17}\text{F}$	197 + 0		F(197), Co(197), Ni(197), Ga(197), Ti(199), Ge(199)
	496	$^{16}\text{O}(p,\gamma)^{17}\text{F}$	496 + 0	5	Ga(493)
F	110	$^{19}\text{F}(p,p'\gamma)^{19}\text{F}$	110 + 0	$2 \times 10^{-4}$	O(110), W(111)
	197	$^{19}\text{F}(p,p'\gamma)^{19}\text{F}$	197 + 0	$5 \times 10^{-5}$	Co(197), Ni(197), Ga(197) Ti(199), Ge(199), O(197)
Na	439	$^{23}\text{Na}(p,p'\gamma)^{23}\text{Na}$	439 + 0	$10^{-3}$	Se(439)
	1368	$^{23}\text{Na}(p,\gamma)^{24}\text{Mg}$	1368 + 0		Mg(1368), Al(1368)
	1633	$^{23}\text{Na}(p,\alpha\gamma)^{20}\text{Ne}$	1633 + 0		

# List of proton-induced reaction

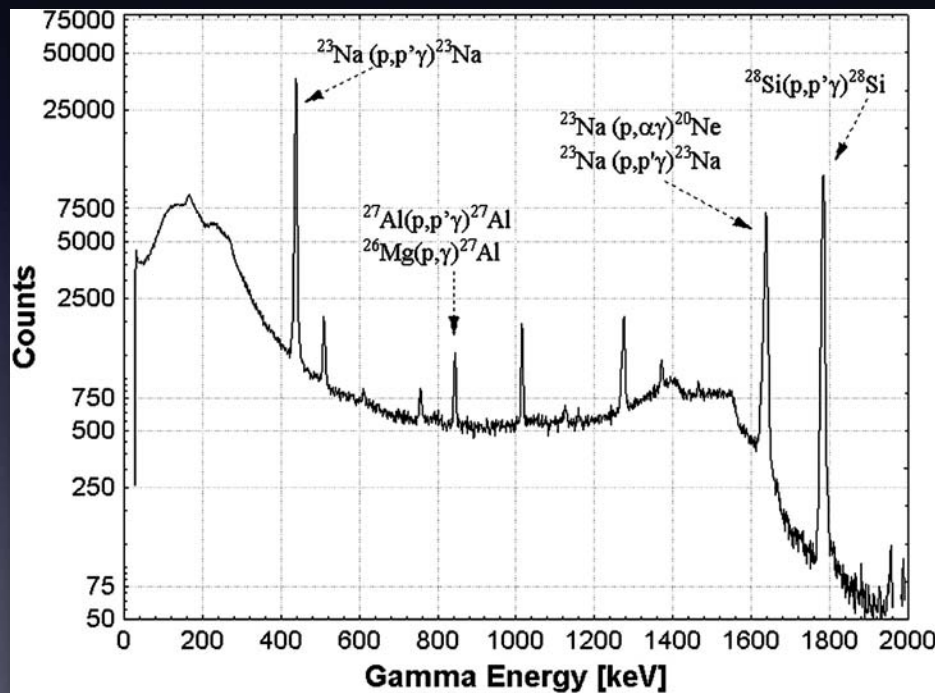
Element	$E_\gamma$ (keV)	Nuclear origin	Transition	Detection limit (%)	Possible interferences
Mg	170	$^{26}\text{Mg}(p,\gamma)^{27}\text{Al}$	1014 + 844	$5 \times 10^{-3}$	Al(170)
	390	$^{25}\text{Mg}(p,p'\gamma)^{25}\text{Mg}$	975 + 585		
	585	$^{25}\text{Mg}(p,p'\gamma)^{25}\text{Mg}$	585 + 0		
	844	$^{26}\text{Mg}(p,\gamma)^{27}\text{Al}$	844 + 0		Al(844)
	975	$^{25}\text{Mg}(p,p'\gamma)^{25}\text{Mg}$	975 + 0		
	1014	$^{26}\text{Mg}(p,\gamma)^{27}\text{Al}$	1014 + 0		Ti(1012), Al(1014)
	1368	$^{24}\text{Mg}(p,p'\gamma)^{24}\text{Mg}$	1368 + 0		Na(1368), Al(1368)
Al	170	$^{27}\text{Al}(p,p'\gamma)^{27}\text{Al}$	1014 + 844	$2 \times 10^{-3}$ $5 \times 10^{-3}$	Mg(170)
	844	$^{27}\text{Al}(p,p'\gamma)^{27}\text{Al}$	844 + 0		Mg(844)
	1014	$^{27}\text{Al}(p,p'\gamma)^{27}\text{Al}$	1014 + 0		Ti(1012), Mg(1014)
	1368	$^{27}\text{Al}(p,\alpha\gamma)^{24}\text{Mg}$	1368 + 0		Na(1368), Mg(1368)
	1779	$^{27}\text{Al}(p,\gamma)^{28}\text{Si}$	1779 + 0		Si(1779), P(1779)
Si	1273	$^{29}\text{Si}(p,p'\gamma)^{29}\text{Si}$	1273 + 0	3	
	1779	$^{28}\text{Si}(p,p'\gamma)^{28}\text{Si}$	1779 + 0		Al(1779), P(1779)

# PIGE cross sections

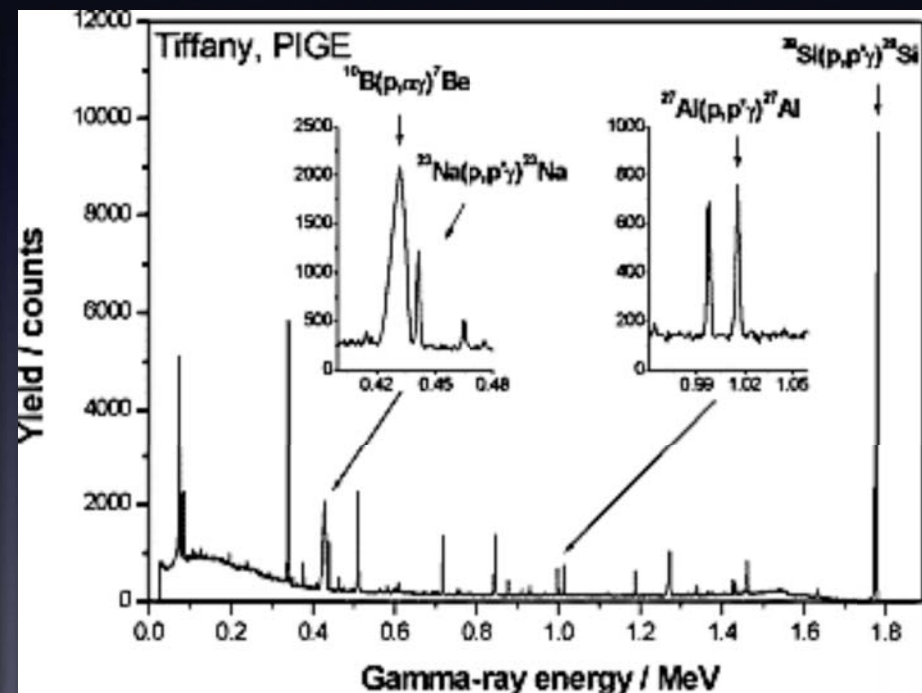
The cross sections are the superimposition of resonances (Breit-Wigner) on a continuum due to direct nuclear reactions



# Examples of PIGE spectra



Soda-lime glass



Borosilicate glass

# PIGE elemental analysis

The elemental concentrations ( $N_T$ ) are obtained from measured quantities (i.e. gamma-ray peak areas) using physical models implementing the sample structure and the physical microscopic data and processes:

$$Y_{\gamma}(E_0, \theta) = \varepsilon_{\text{abs}}(E_{\gamma}) \cdot N_p \cdot \int_0^{E_0} N_T \cdot \sigma(E_0, \theta) / S(E) dE$$

The principal needed microscopic data are **stopping powers** and **differential cross sections** of the interaction (as well as the detector absolute efficiency)

# Analytical applications of PIGE

## Cultural Heritage *i.e. thick targets*

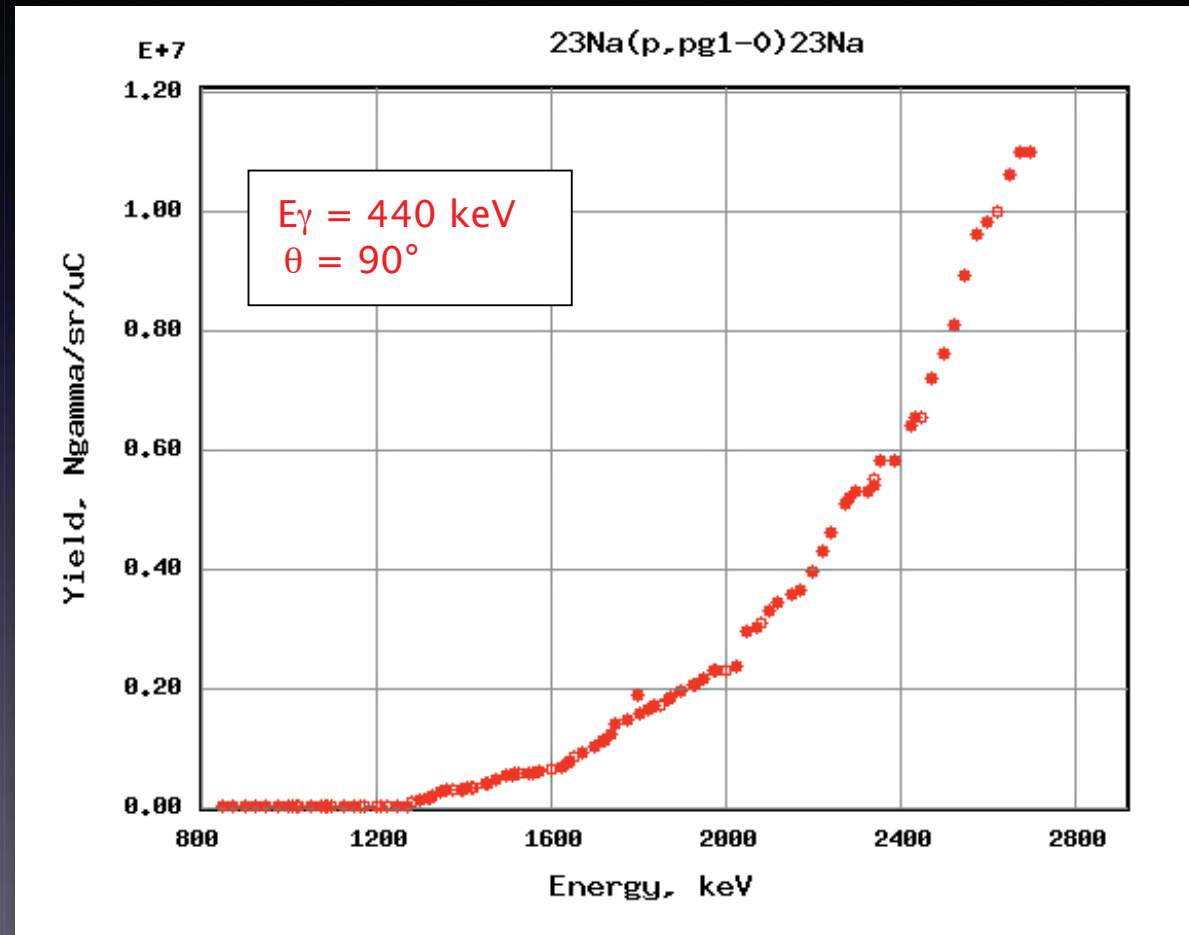
- (Semi-)quantitative determination of light elements like Na, Al or Si in infinitely thick targets
- Unknown concentrations typically deduced by comparing the  $\gamma$ -ray yields with those of **thick** standards of similar composition
- Differences in stopping powers are crucial

## Atmospheric Aerosols *i.e. thin targets*

- Quantitative determination of light elements (F, Na or Al) with no self-absorption of emitted radiation inside aerosol particles
- Unknown concentrations deduced by comparing the  $\gamma$ -ray yields with those of a **thin** elemental standard
- Choosing the beam energy is crucial (cross-sections have to be constant over the beam energy loss in the sample)



# Thick target gamma-ray yields



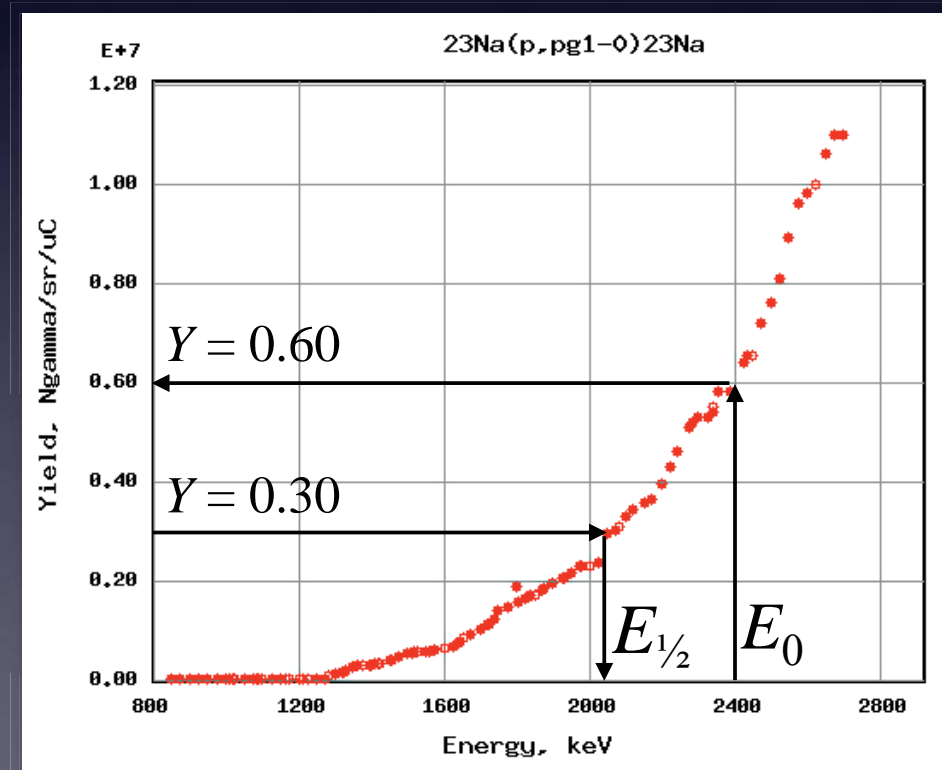
# PIGE quantitative analysis: comparison with thick standards

$$C_{camp} = C_{rif} \cdot Y_{camp}(E_0)/Y_{rif}(E_0) \cdot S_{camp}(E_{1/2})/S_{rif}(E_{1/2})$$

$E_{1/2}$  such as:

$$Y(E_0) = 2 \cdot Y(E_{1/2})$$

The “ $E_{1/2}$ ” method is valid as long as the excitation function varies slowly with the energy





# RBS

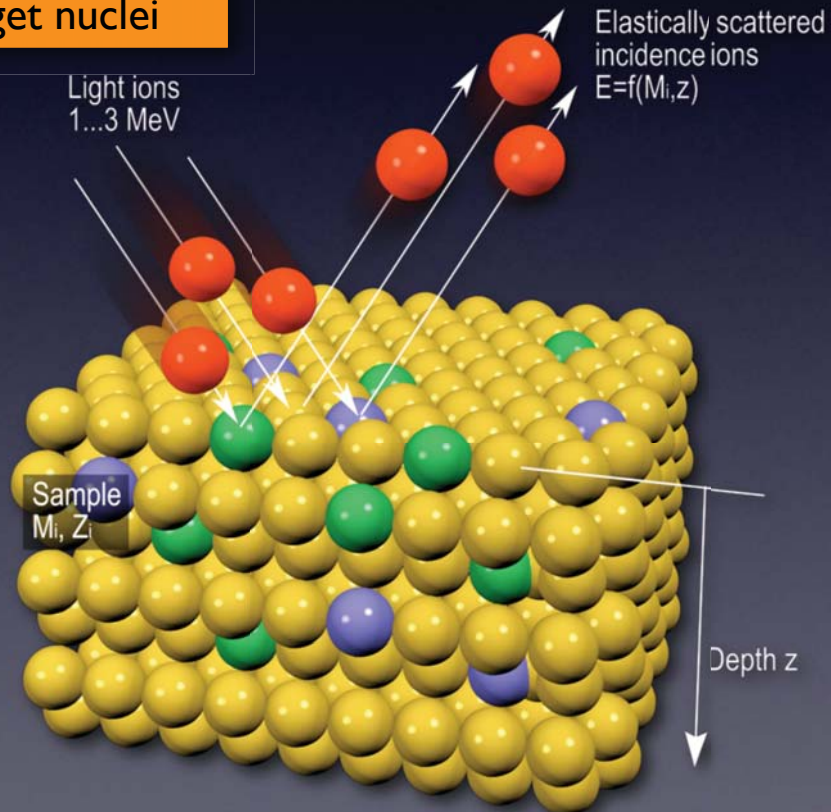
## Rutherford Backscattering Spectrometry

Elastic scattering at backward angles of the impinging ions by the target nuclei



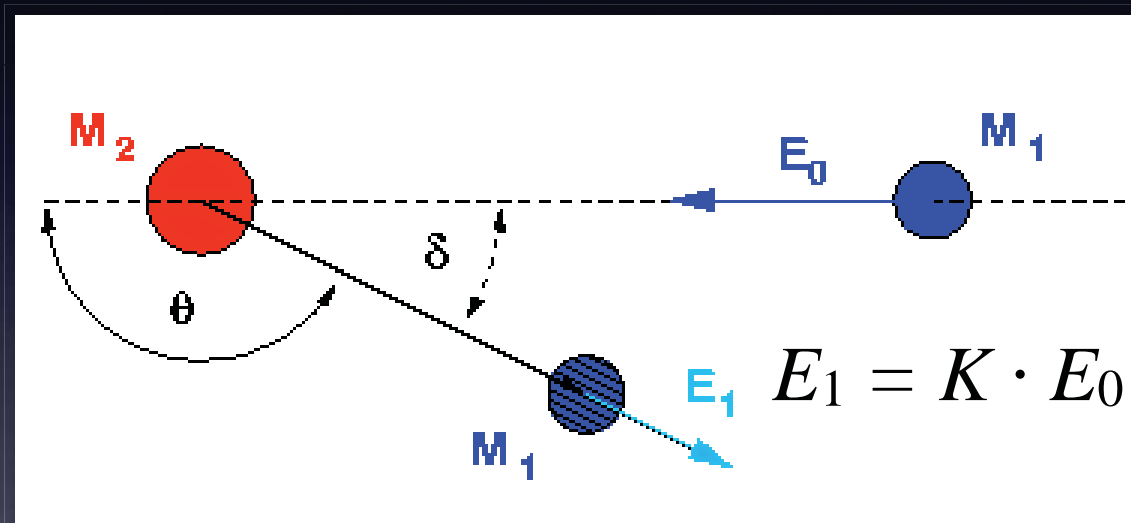
$A > A_p$

✓ depth profile



# Principles of RBS

For a given scattering angle  $\theta$ , the energy  $E_1$  of the incident ion (mass  $M_1$ ) after the collision is only a function of the mass  $M_2$  of the target nuclei

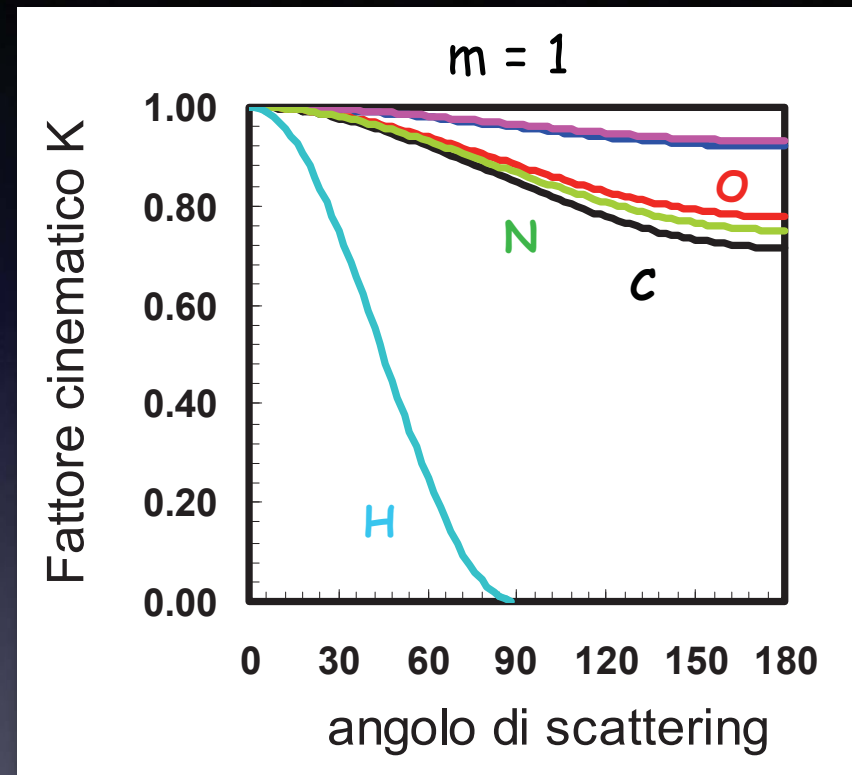
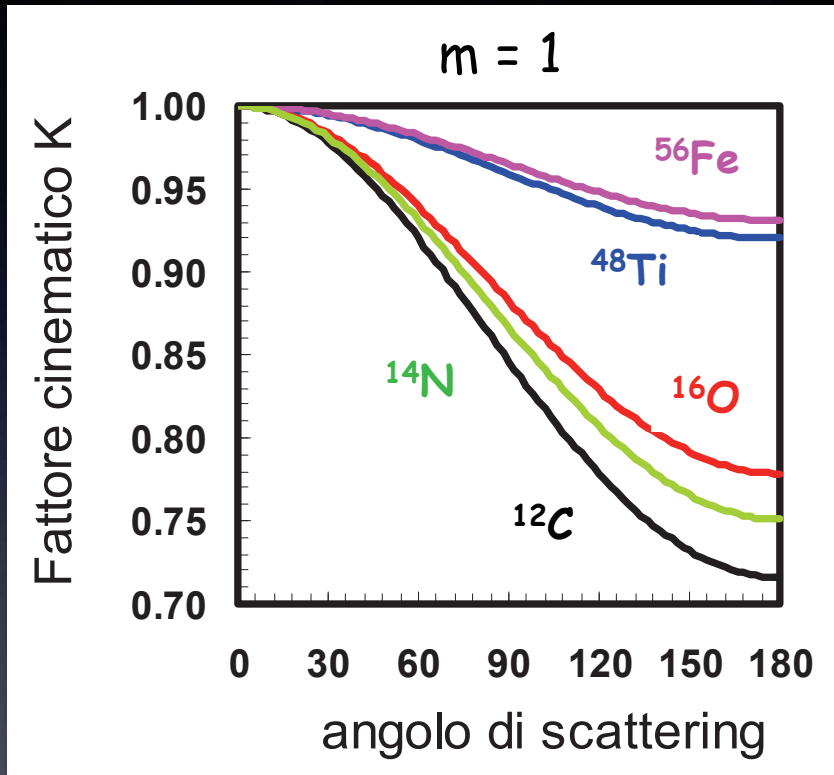


$$K = \frac{\left[ \sqrt{\left(\frac{M_2}{M_1}\right)^2 - \sin^2 \theta} + \cos \theta \right]^2}{\left(\frac{M_2}{M_1} + 1\right)^2}$$

larger  $\Delta E$  for smaller  $M$   
(light nuclei)

Larger  $\Delta E$  for larger  $\theta$   
(backscattering)

# The kinematic factor $K$



$M_2 \leq M_1 \Rightarrow$  only forward scattering (PESA)

# Elastic scattering cross section

The Rutherford formula:

$$\left(\frac{d\sigma}{d\Omega}\right)_{Ruth} = \left(\frac{Z_1 Z_2 e^2}{E}\right)^2 \frac{4}{\sin^4(\theta)} \frac{\left[\sqrt{1 - \left(\frac{M_1}{M_2} \sin \theta\right)^2} + \cos \theta\right]^2}{\sqrt{1 - \left(\frac{M_1}{M_2} \sin \theta\right)^2}}$$

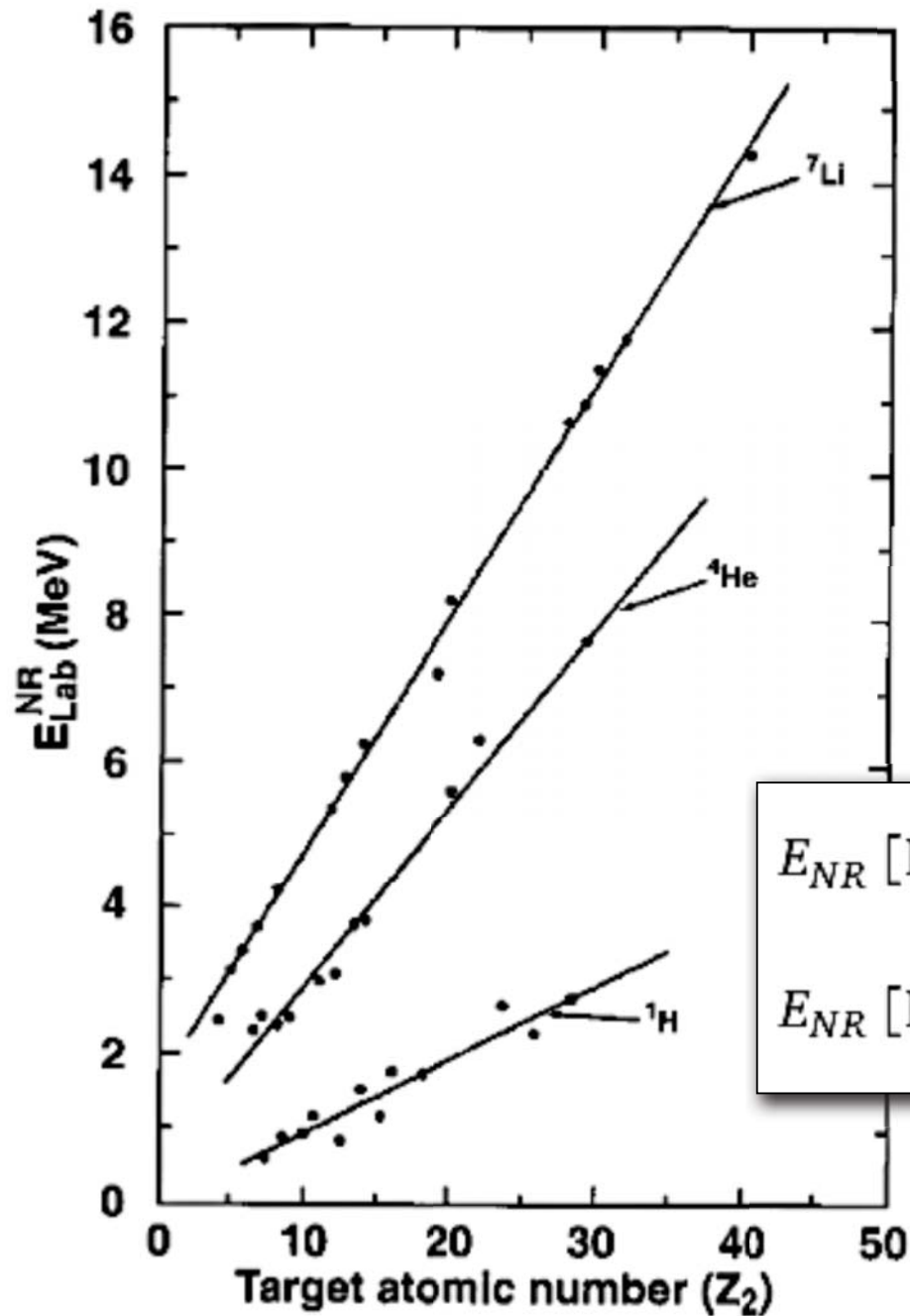
$Z_1$  Atomic number of the incident ion

$Z_2$  Atomic number of the target nucleus

$E$  Energy of the incident ion

$M_1$  Mass of the incident ion

$M_2$  Mass of the target nucleus

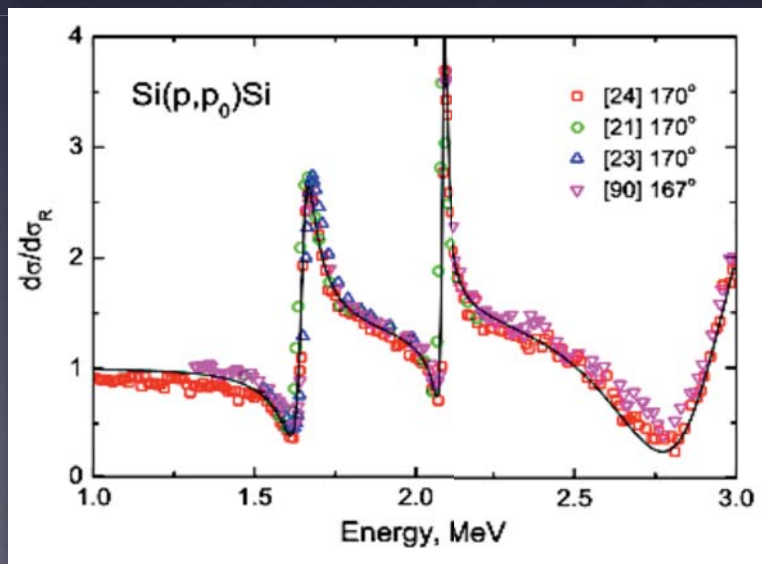
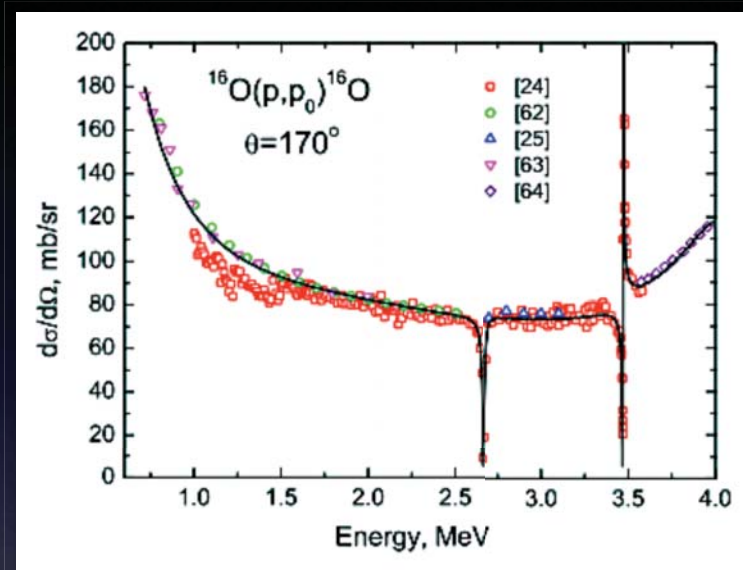
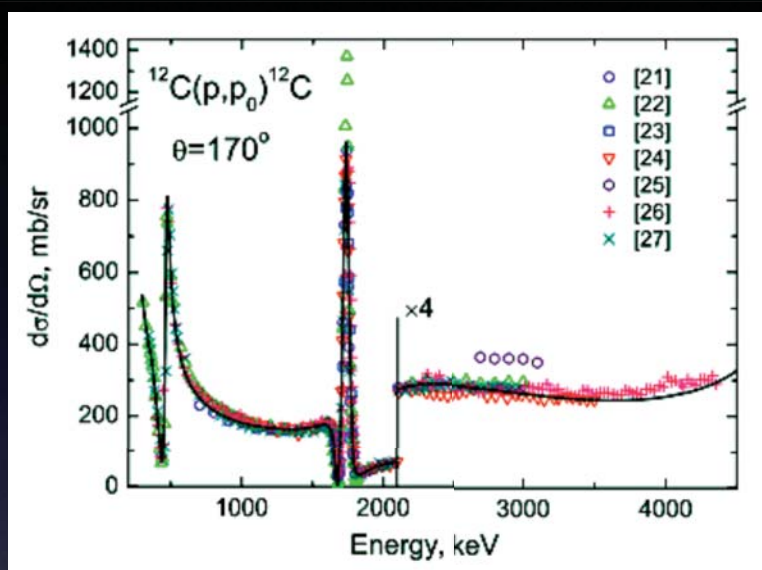


Energy (in the laboratory) at which the elastic scattering cross section deviates more than 4% from the Rutherford value (for scattering angles  $> 160^\circ$ )

$$E_{NR} [\text{MeV}] = \frac{M_1 + M_2}{M_2} \frac{Z_2}{10} \quad \text{for } Z_1 = 1$$

$$E_{NR} [\text{MeV}] = \frac{M_1 + M_2}{M_2} \frac{Z_1 Z_2}{8} \quad \text{for } Z_1 > 1$$

# Non-Rutherford cross sections



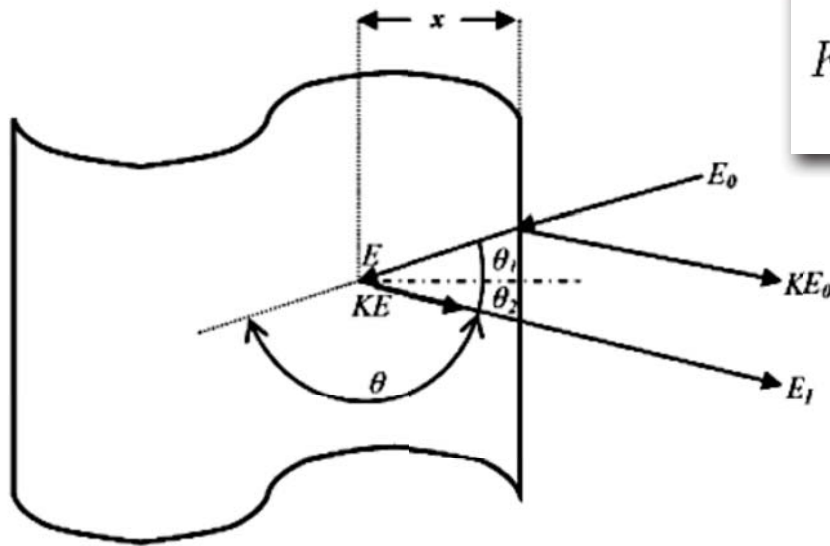
Evaluated and recommended experimental cross sections available from IBANDL web site ([www-nds.iaea.org/ibandl/](http://www-nds.iaea.org/ibandl/))



# Depth scale of RBS

The signal from an atom at the sample surface will appear in the energy spectrum at a position  $KE_0$ .

The signal from atoms of the same mass below the sample surface will be shifted by the amount of energy lost while the projectiles pass through the sample, both before ( $\Delta E_{in}$ ) and after a collision ( $\Delta E_{out}$ ).

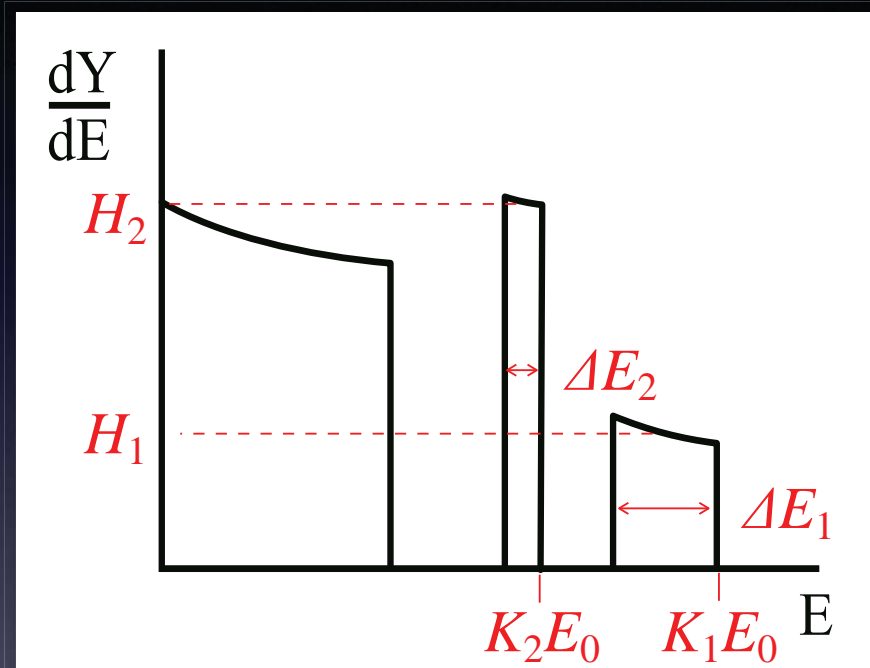


$$KE_0 - E_1 = \left[ \frac{Kx}{\cos \theta_1} \cdot \left( \frac{dE}{dx} \right)_{in} + \frac{x}{\cos \theta_2} \cdot \left( \frac{dE}{dx} \right)_{out} \right]$$

There exists a relation between the measured energy  $E_1$  and the depth  $x$  at which the scattering took place

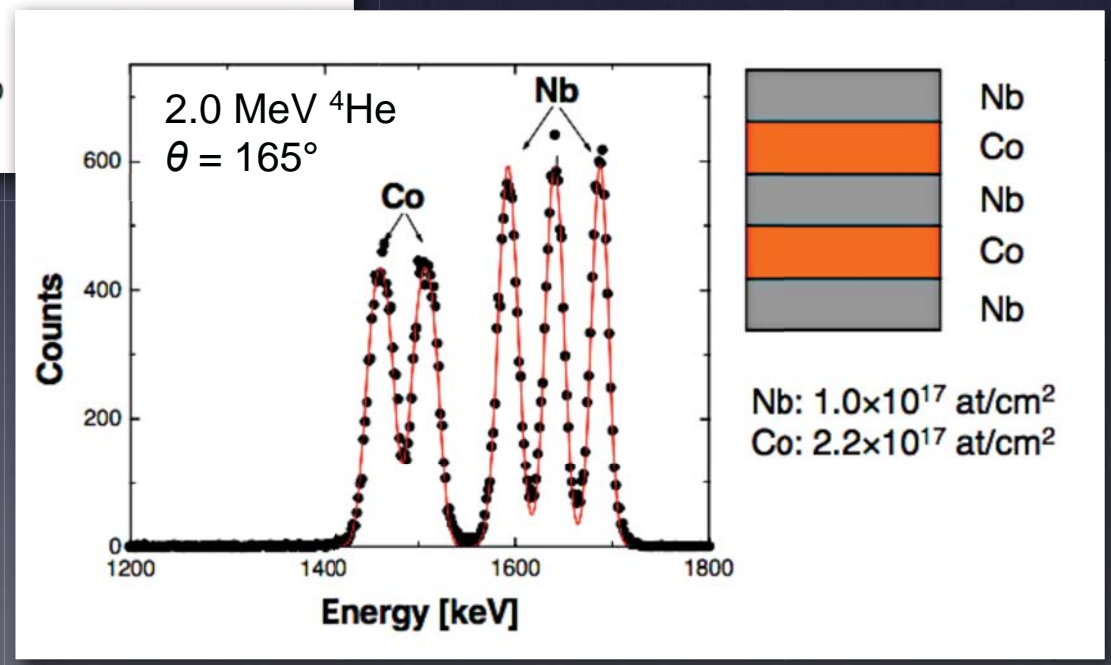
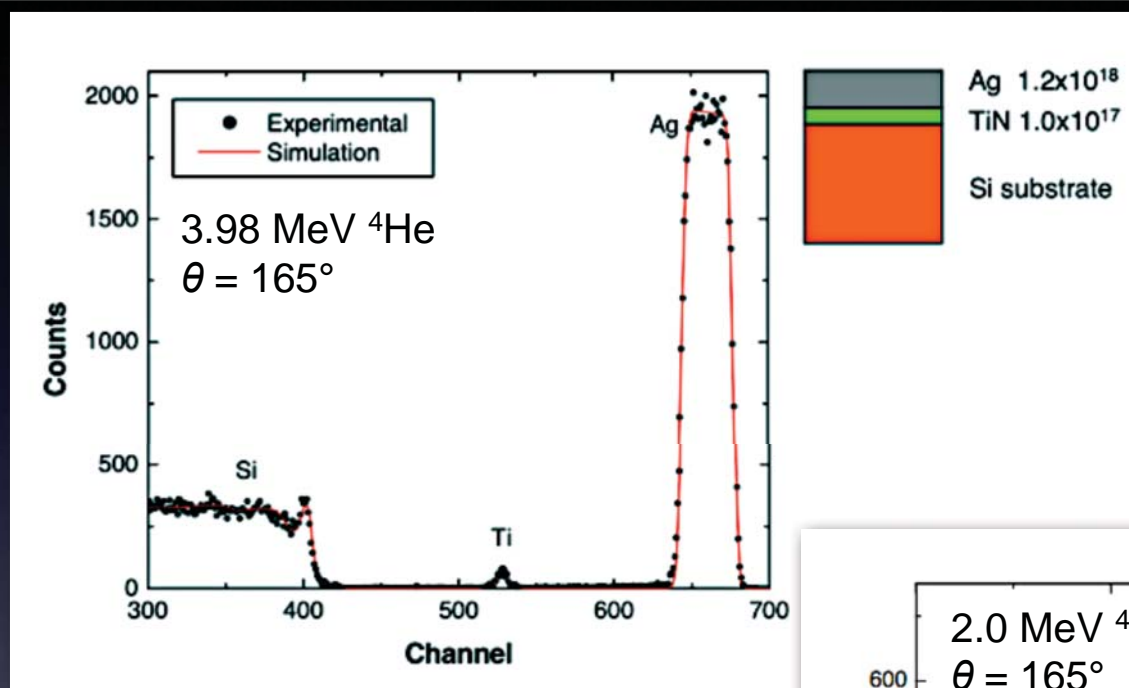


# The features of RBS spectra



- Position of the signal (mass perception *i.e.* kinematic factor)
- Width of the signal (depth/thickness perception *i.e.* stopping force)
- Height of the signal (quantitative analysis of elemental composition *i.e.* scattering cross section)

# Examples of RBS spectra

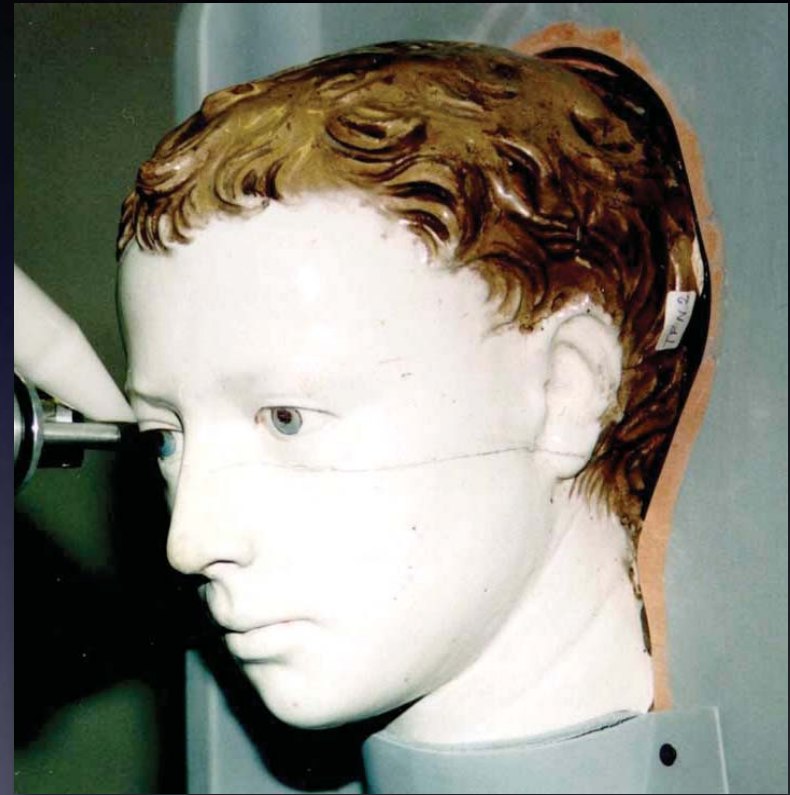


**Analysis of ancient  
manuscripts,**



PIXE analysis of the frontispiece of  
Pl.16,22, from Biblioteca  
Laurenziana in Florence

**...ceramics,**



Analysis of the Ritratto di fanciullo  
by Luca Della Robbia - before  
restoration at the Opificio delle  
Pietre Dure in Florence

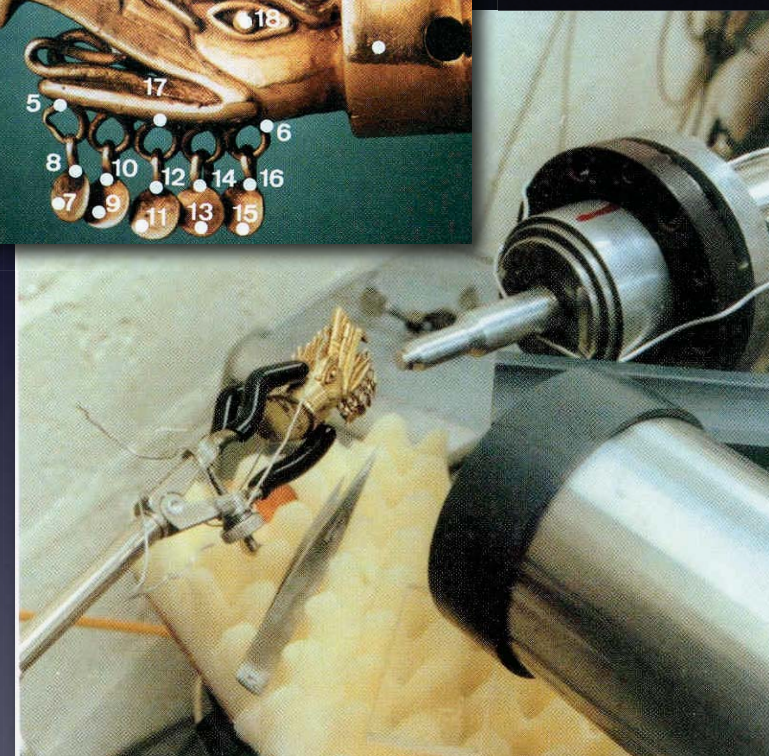
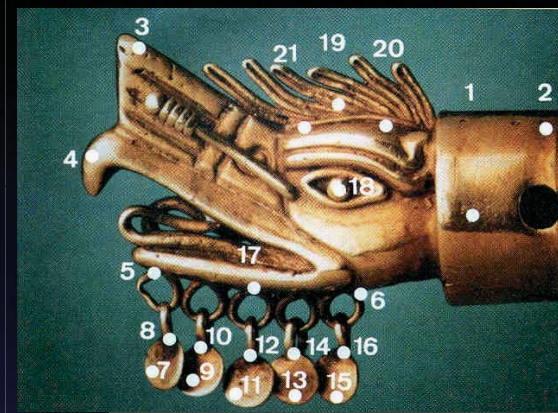


... drawings,



Micro-PIXE measurements of  
Portrait of Lucas de Leyde by  
Alfred Dürer  
A.Duval et al., (Louvre laboratory)

... jewels,



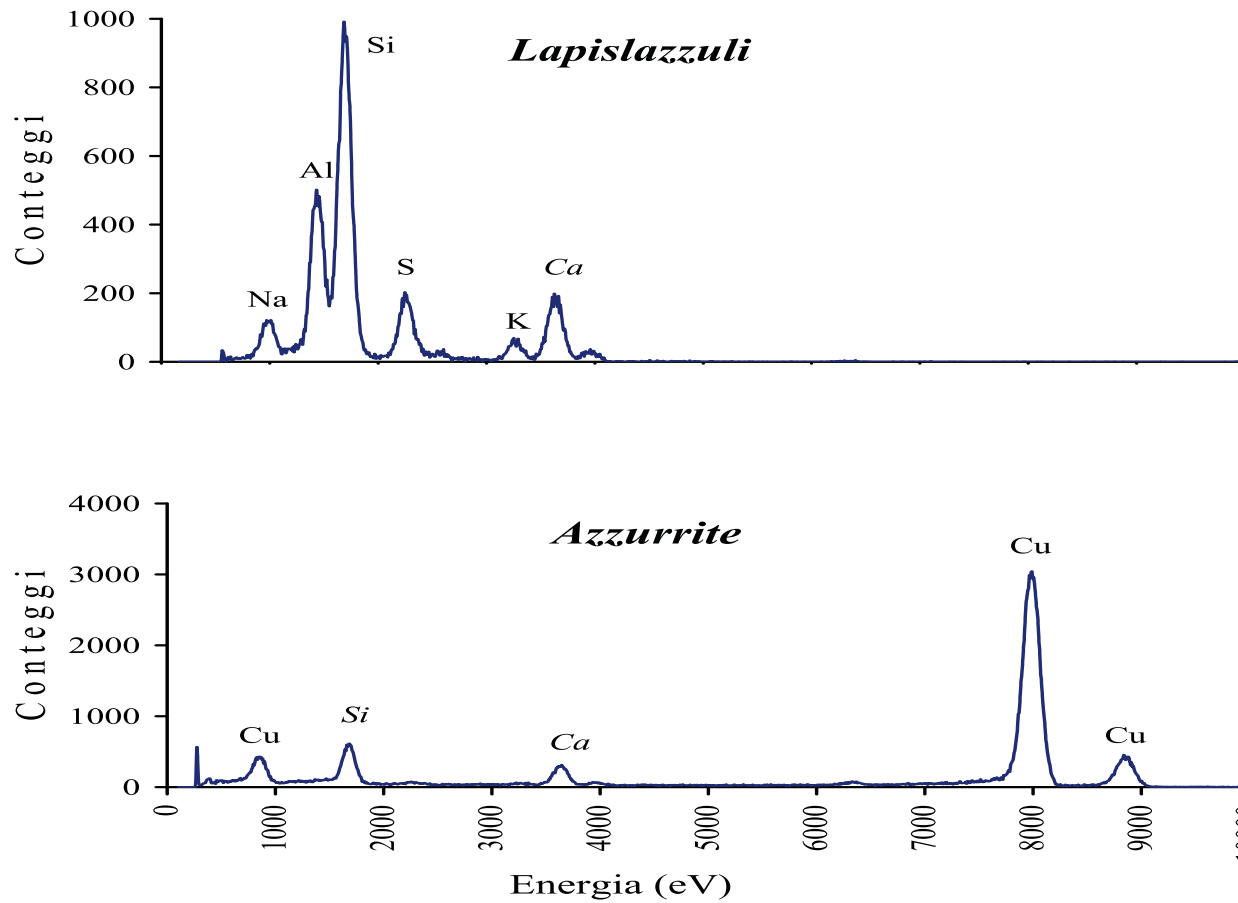
Micro-PIXE measurements of a  
Mexican gold alloy ornament  
G.Demortier and J.L.Ruvalcaba Sil  
(Namur)

## ...paintings



PIXE analysis of a painting by  
Lucas Cranach the Elder  
C. Neelmeijer et al.  
(Rossendorf Forschungszentrum, Dresda)

# Blue Temperas



Example of  
PIXE spectra  
of two blue  
pigments



# Blue Temperas

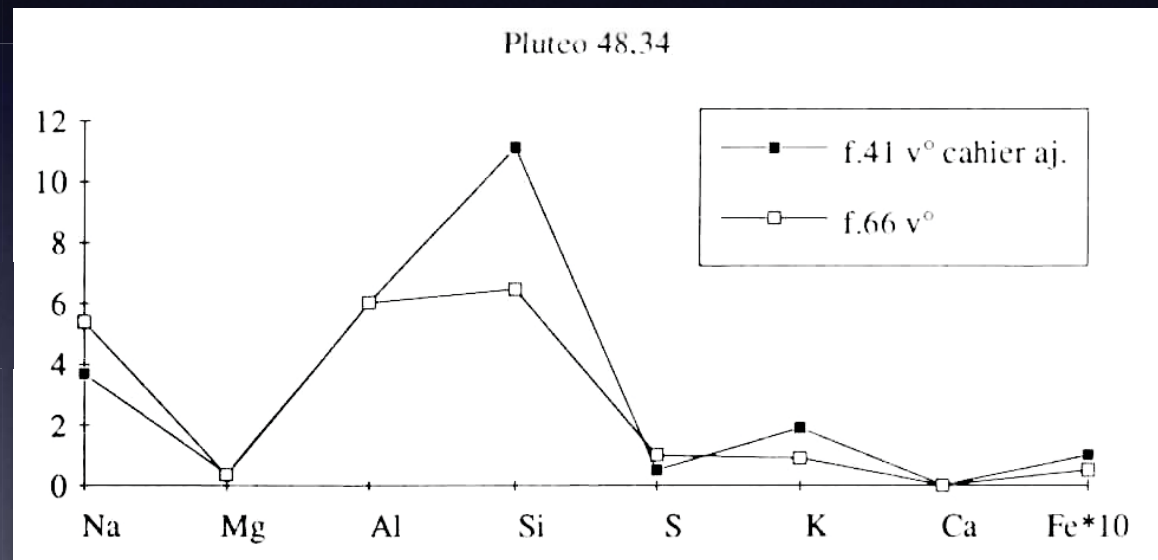


Pluteo 48, 34, f. 66 v°



Pluteo 48, 34, f. 41 v°

Extensive use of lapislazuli starting from XI century





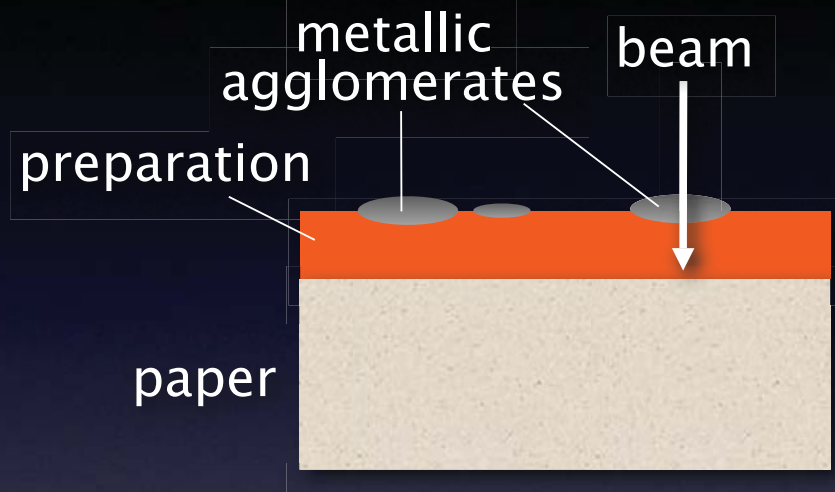
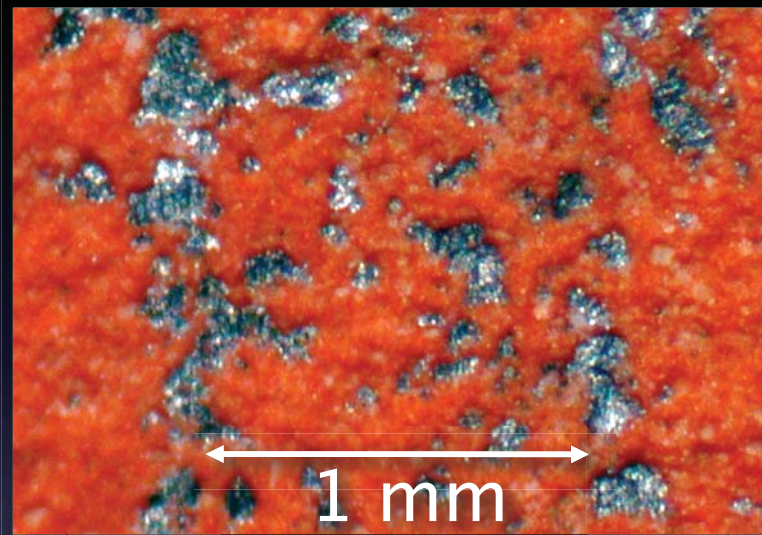
# Metal point drawings

**LEONARDO DA VINCI**  
**STUDY OF A DRAPERY**  
Roma, Istituto Nazionale  
per la Grafica

metal point, lead white  
red prepared paper



# Characteristics of metal point drawings



The extension of the metallic agglomerates on the surface is some tens of  $\mu\text{m}$



The beam size does not allow a detailed analysis

The beam can pass through the trace and hit the preparation



The contribution of the preparation must be taken into account

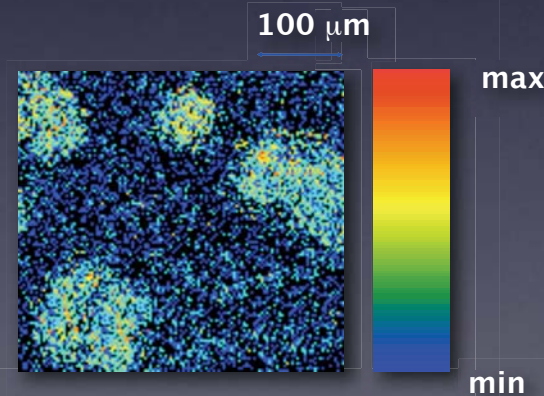
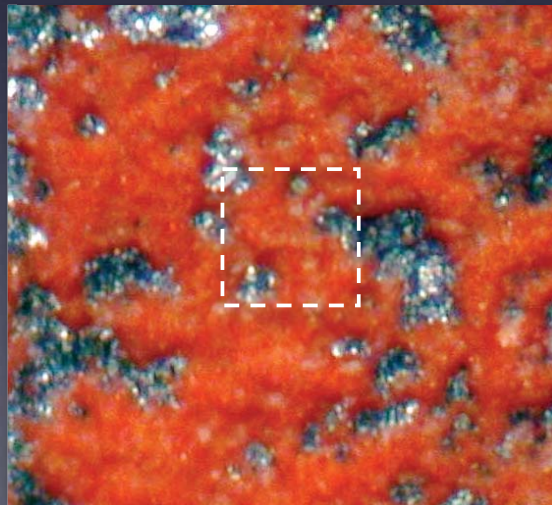


# MicroPIXE analysis of metal point drawings

**Four metallic points:**  
silver, lead, gold, copper

**Red preparation:**  
cinnabar, yellow ochre,  
lead white, bone white

Au Cu Pb

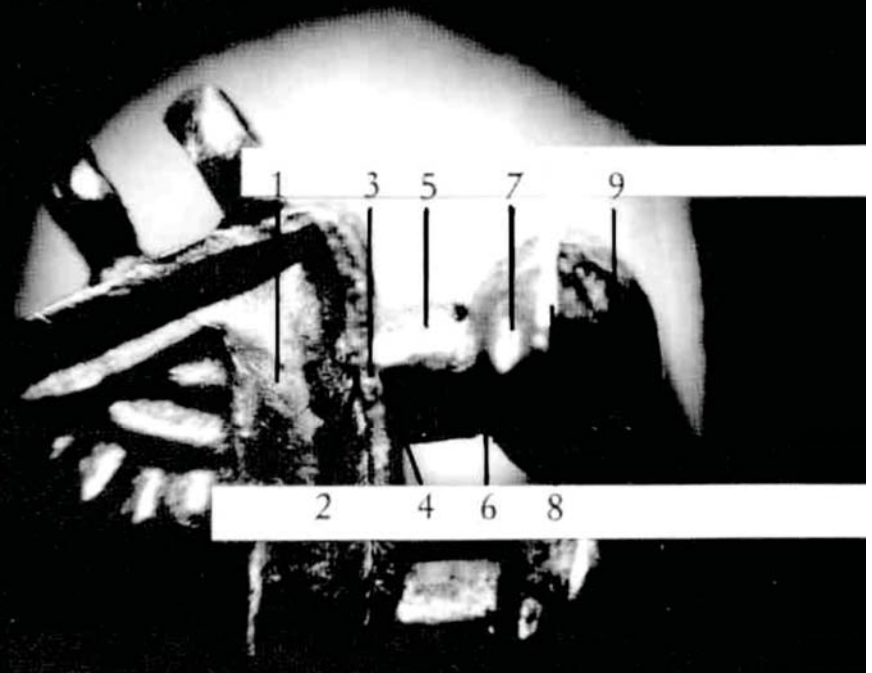


Elemental map on  
0.4x0.4 mm<sup>2</sup>

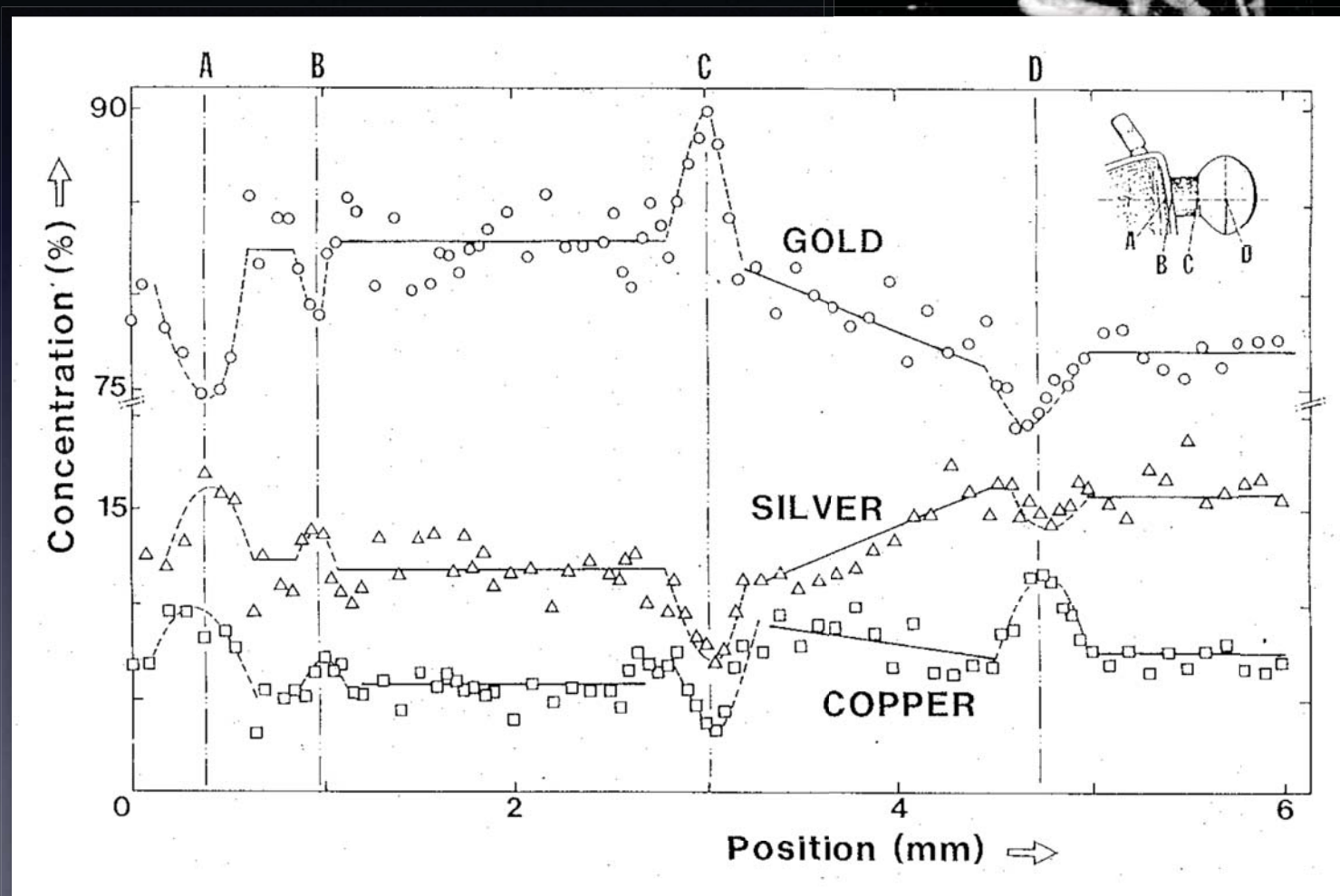
Lead stylus  
(Pb, trace of Sn)

Red preparation  
(S, Hg, Pb, Fe, P, Ca)

# Micro-PIXE measurements of an Achemenide pendant (IV century BC)



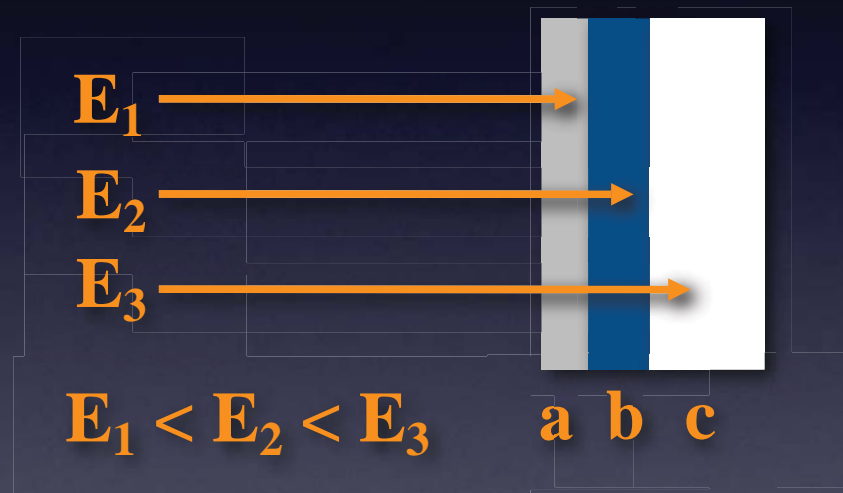
# Micro-PIXE measurements of an Achemenide pendant (IV century BC)



# Differential PIXE

Consists in performing measurements on the same area with beams of different energies

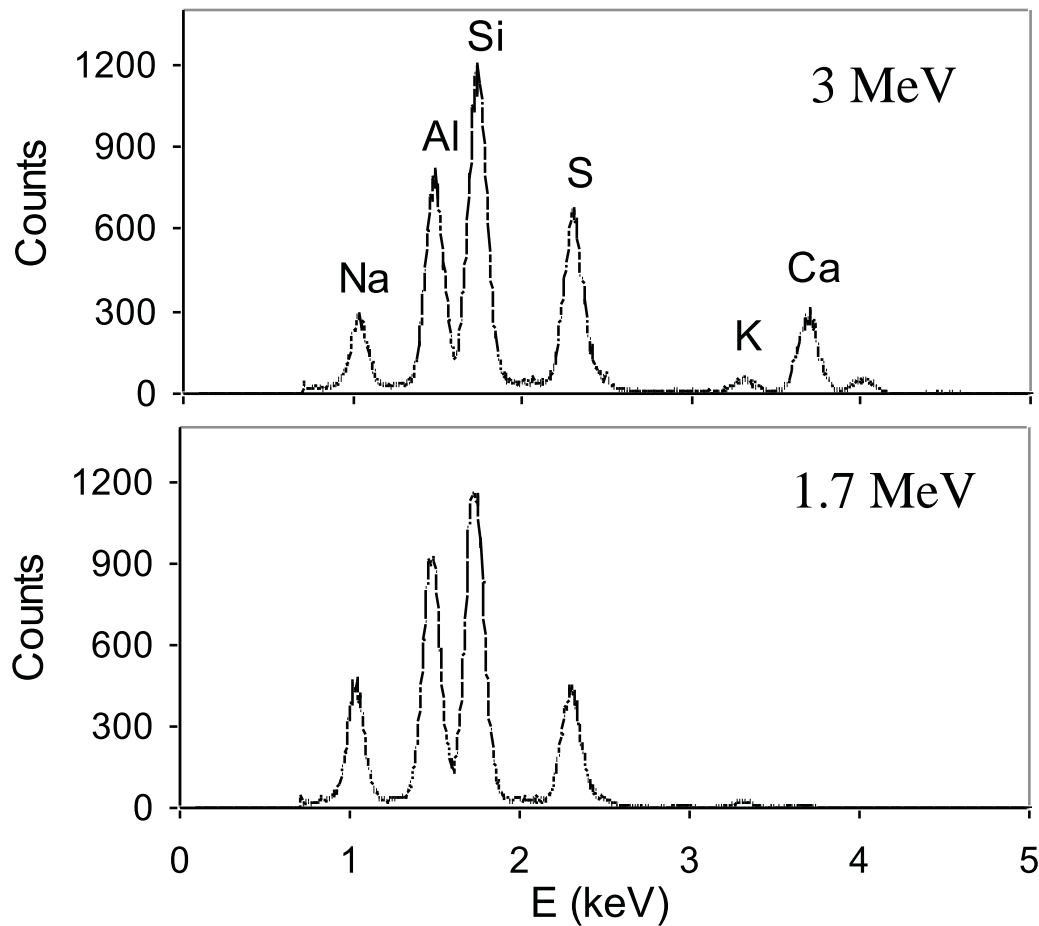
At different energies  
proton beam ranges  
are different



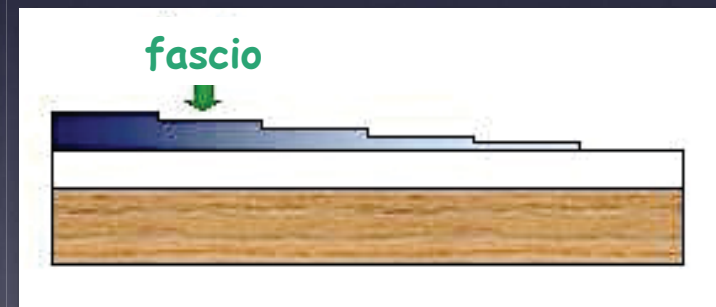
By comparing X-ray spectra taken at different energies,  
stratigraphic information can be obtained



# PIXE spectra at different energies



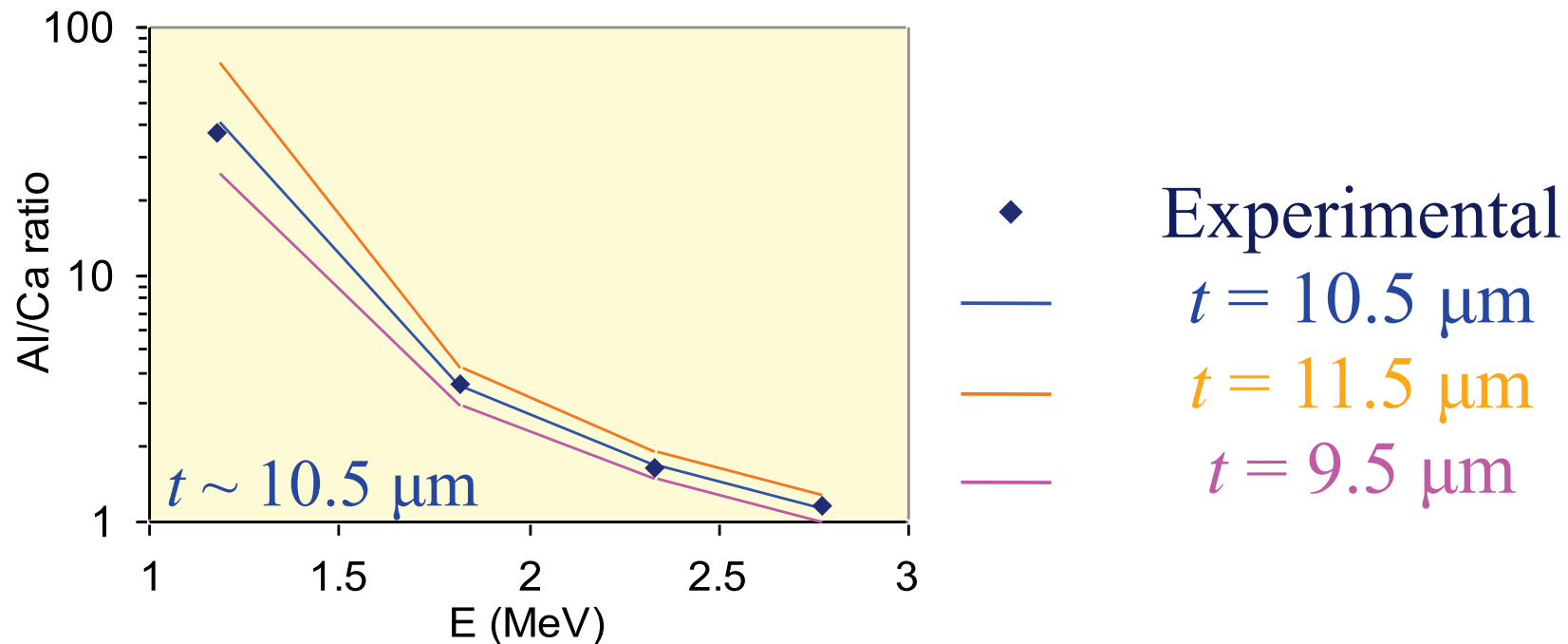
Blue paint layer  
(lapislazuli) on a substrate  
of calcium sulphate



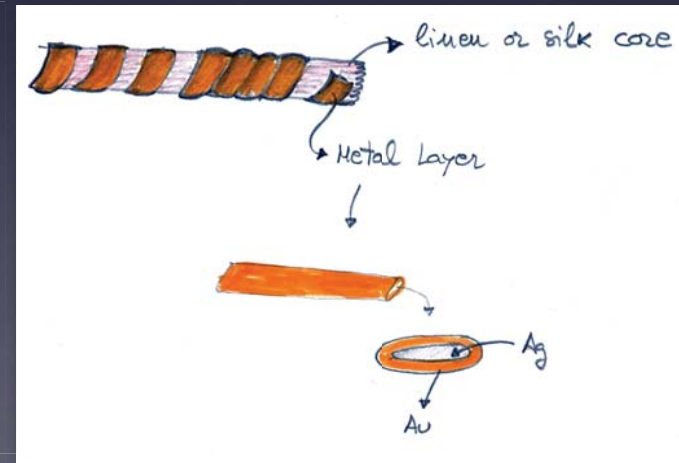
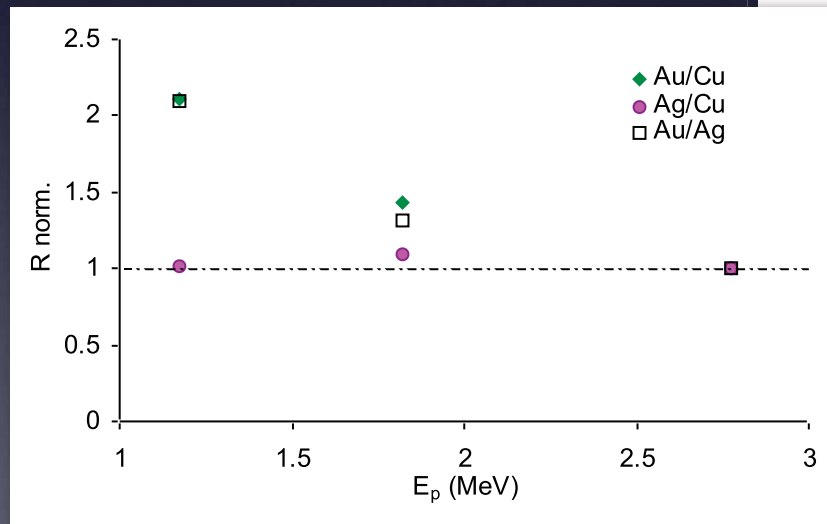
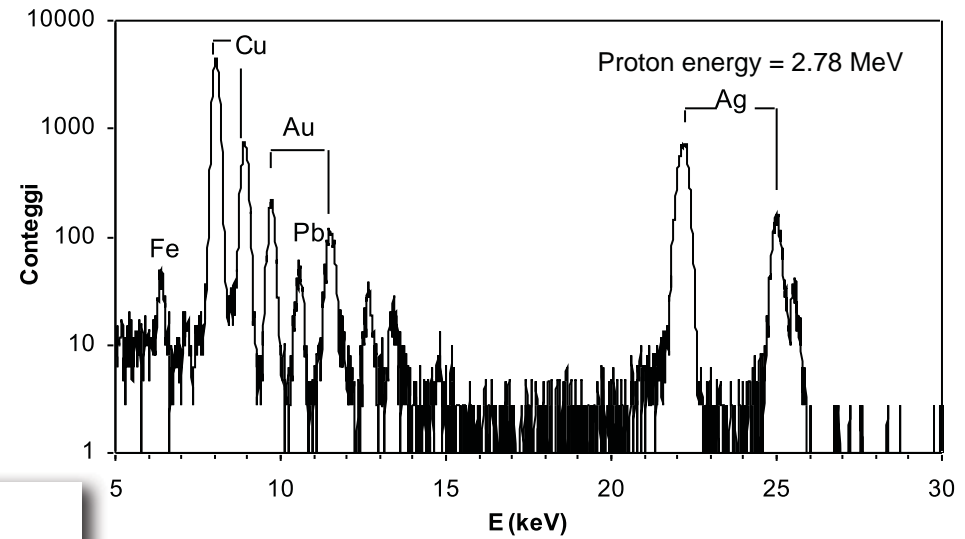
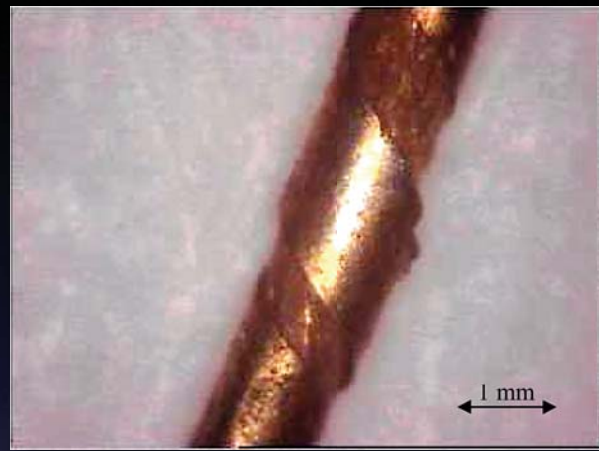


# Estimate of the paint layer thickness

$$\frac{Y_{\text{Al}}}{Y_{\text{Ca}}} = \frac{C_{\text{Al}}}{C_{\text{Ca}}} \frac{\int_{E_p}^{E_p - \Delta E_{\text{lap}}(t)} \sigma_X^{(\text{Al})}(E) e^{-\mu_{\text{lap}}^{(\text{Al})} \frac{x(E)}{\cos \theta}} \frac{dE}{S_{\text{lap}}(E)}}{e^{-\mu_{\text{lap}}^{(\text{Ca})} \frac{t}{\cos \theta}} \int_{E_p}^0 \sigma_X^{(\text{Ca})}(E) e^{-\mu_{\text{white}}^{(\text{Ca})} \frac{x'(E)}{\cos \theta}} \frac{dE}{S_{\text{white}}(E)}}$$

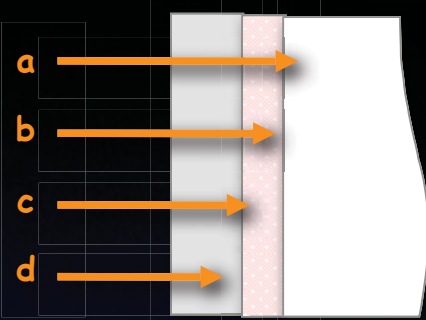
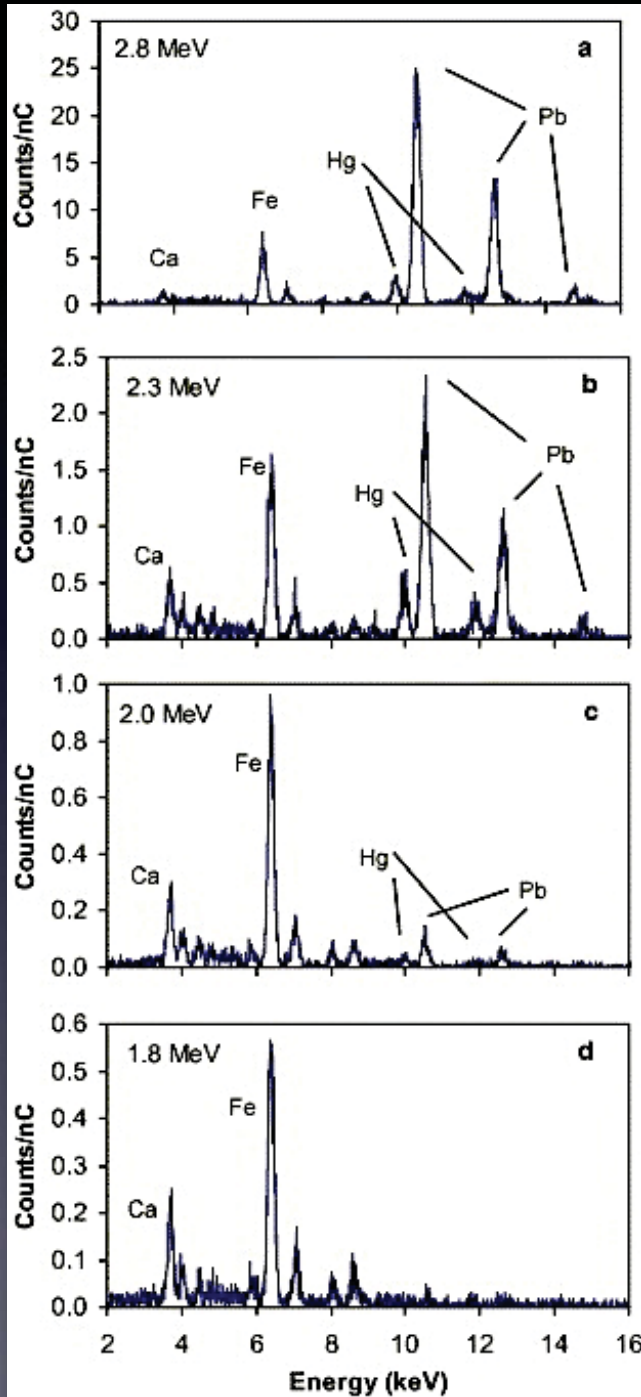


# Metal threads (Alhambra, Granada)



Enrichment of gold on the surface

# “Incarnato”



**paint layer:**

cinnabar (HgS, red pigment)+lead white

**preparation:**

lead white

Ca and Fe are in the varnish

# Lapis-lazuli pigment in paint layers



“Maddonna dei fusi”, Leonardo da Vinci (1501)

Lapis-lazuli is a blue pigment, mainly composed of lazurite ( $3\text{Na}_2\text{O} \cdot 3\text{Al}_2\text{O}_3 \cdot 6\text{SiO}_2 \cdot 2\text{Na}_2\text{S}$ )

Limited possibility of identifying lapis-lazuli by PIXE in canvas and wood paintings:

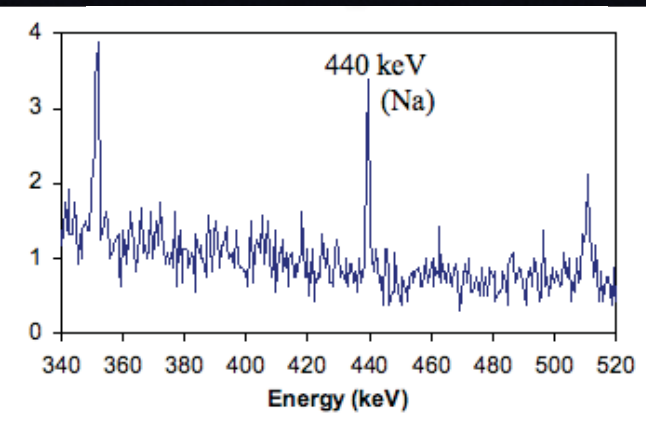
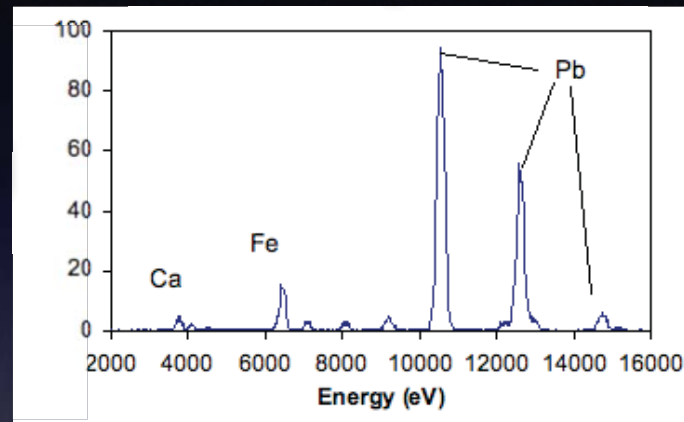
- *low-energy X-rays absorption in the varnish and in the paint layer itself*
- *signal interference from other pigments*

# Lapis-lazuli pigment in paint layers

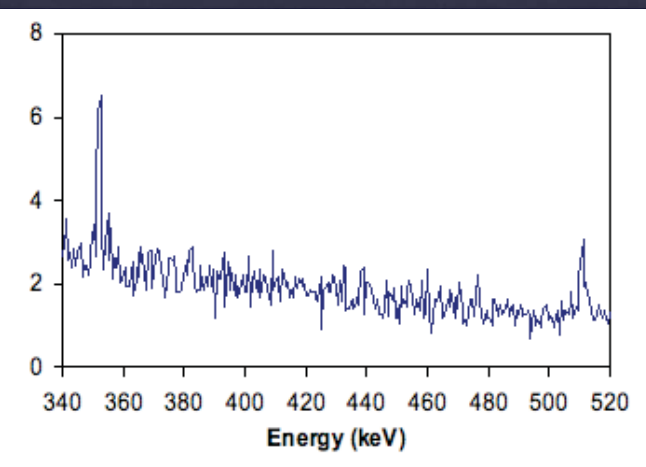
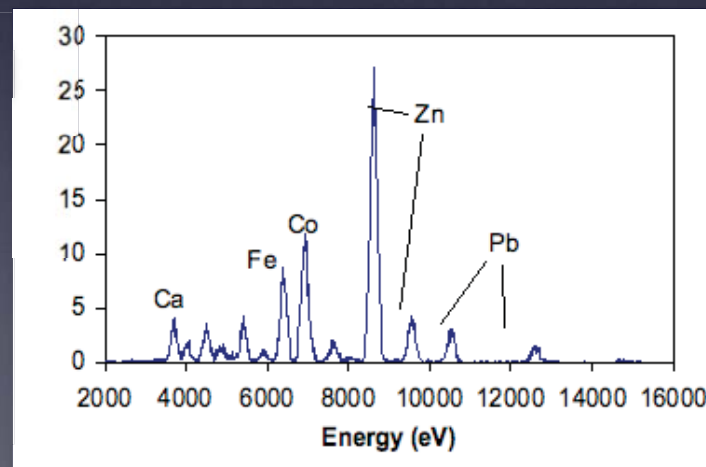
PIXE spectra

PIGE spectra

**Original**  
Blue pigment mixed  
with Lead white  
(Ca and Fe from  
the varnish)



**Restored**  
Cobalt blue and  
Zinc white (used  
only from XIX  
century!)





# Analysis of ancient Roman glasses



Roman glass mosaic tesserae from Villa Adriana, Tivoli (Italy)

Quantification of Na is of great importance for the characterization of ancient glasses

Two basic typologies of Western glass:

- **natron** (high  $\text{Na}_2\text{O}$ , low  $\text{K}_2\text{O}$  and  $\text{MgO}$ )  
*Roman and High Middle Ages*
- **plant ash** (low  $\text{Na}_2\text{O}$ , high  $\text{K}_2\text{O}$ )  
*since Middle Ages*



# Sodium in Roman glasses

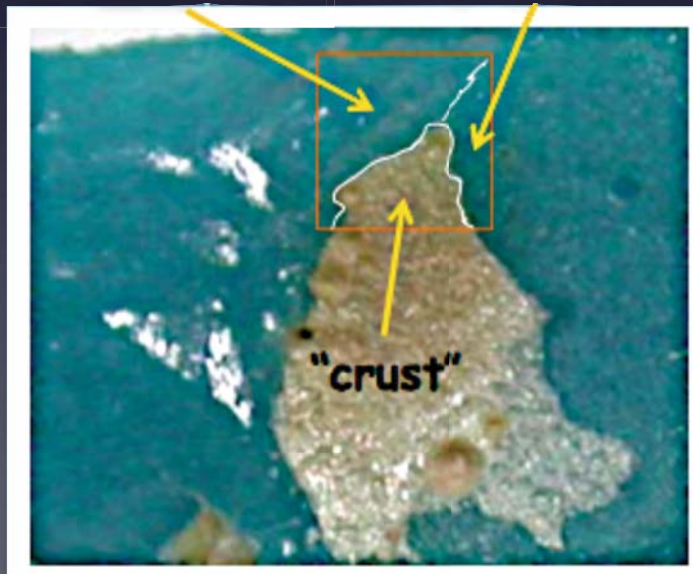
X-rays from the lightest elements strongly absorbed by crusts and *patinae*



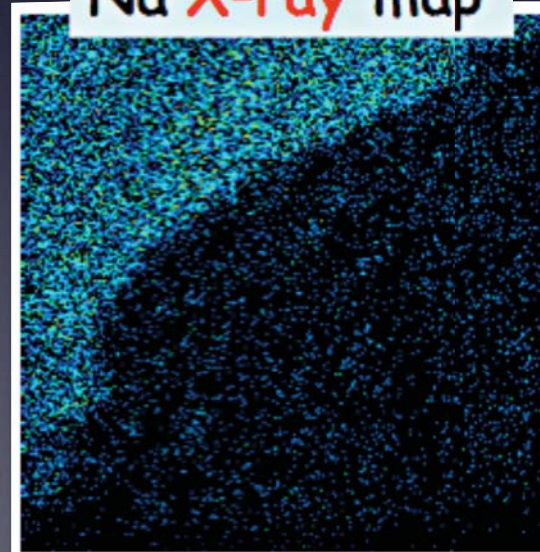
Roman glass mosaic tesserae

“freshly cut”  
zone

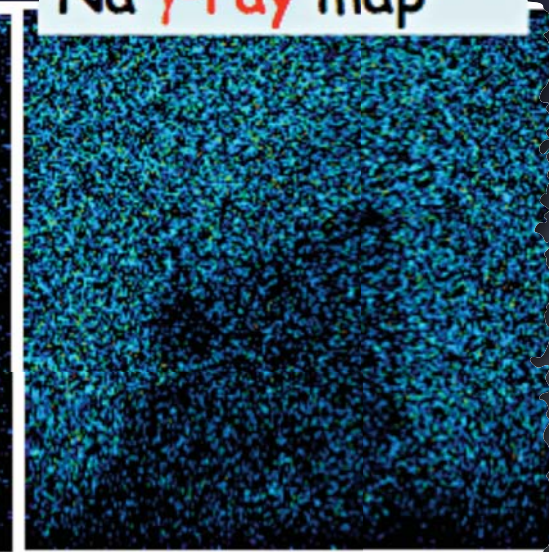
coloured but more  
opaque zone



Na X-ray map



Na  $\gamma$ -ray map

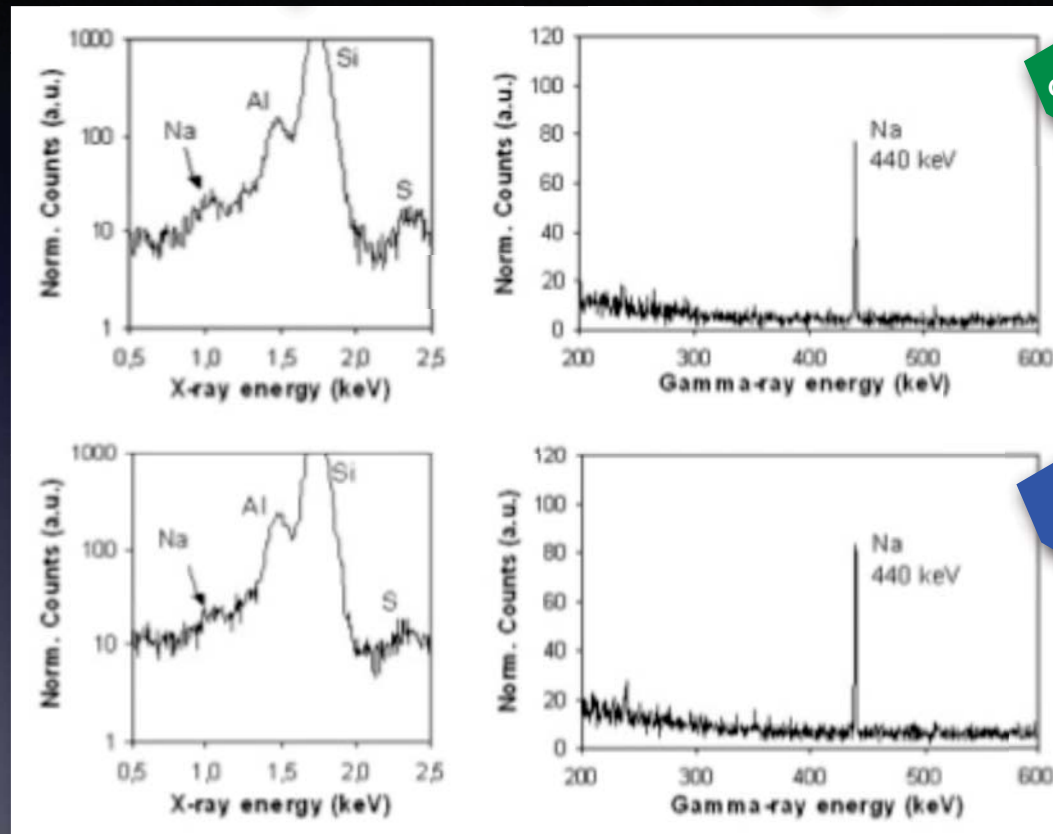


2 mm

# Sodium in Roman glasses

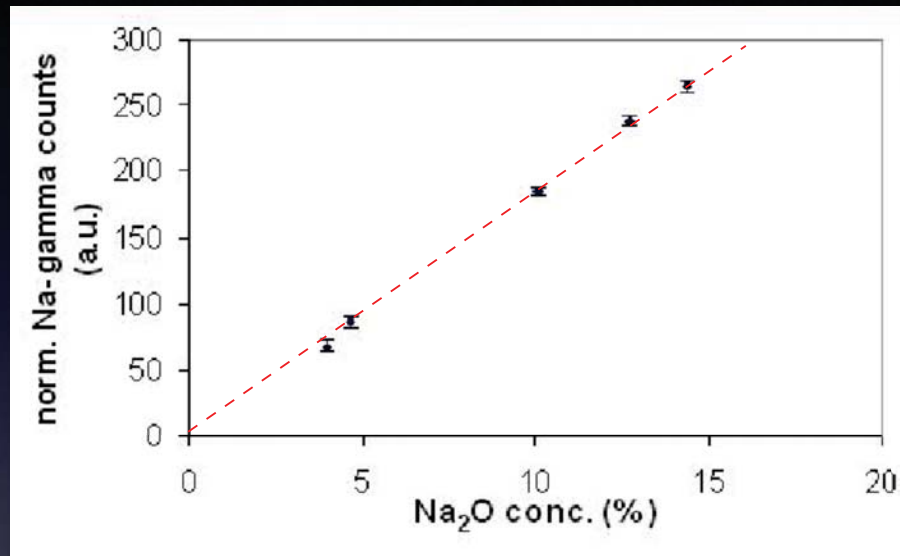
PIXE spectra

PIGE spectra



X-rays from the lightest elements strongly absorbed by crusts and *patinae*

# Sodium in Roman glasses

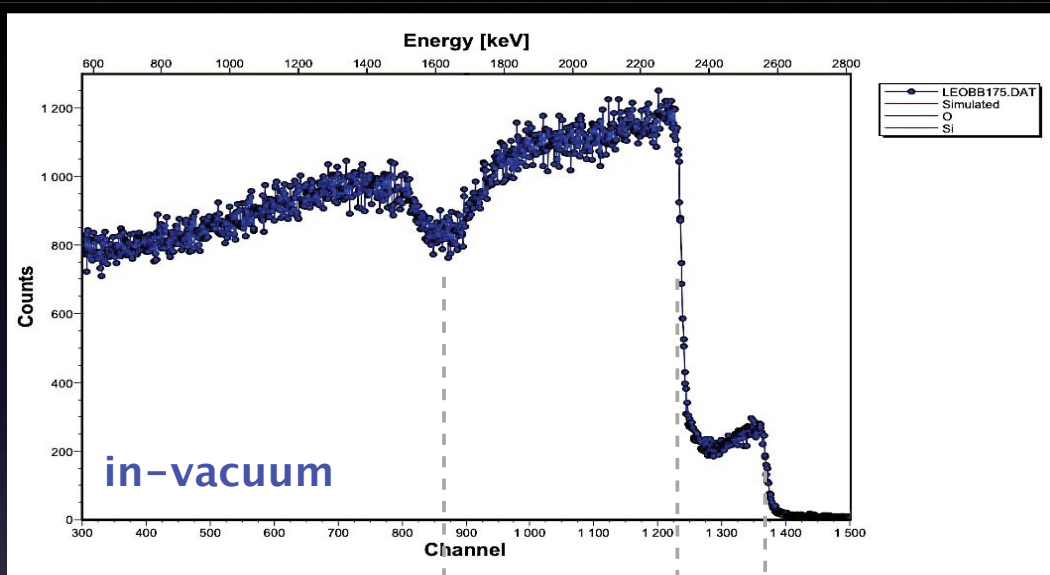


Estimate of Na content by comparing gamma-ray yields to those of thick glass standards (NIST SRM) with certified Na<sub>2</sub>O concentration

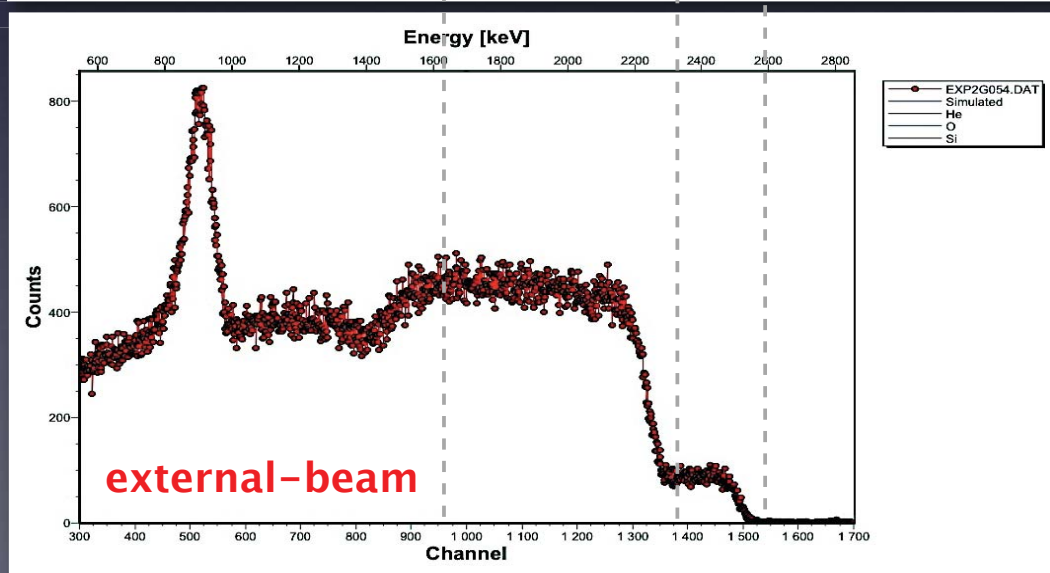
Concentration ranges perfectly compatible with the typical Roman soda-lime-silica glass

glass colour	main oxides (%)			
	Na <sub>2</sub> O	SiO <sub>2</sub>	CaO	PbO
green	~20	55-60	5-9	1-3
blue	~20	60-65	5-9	<0.1
turquoise	~20	55-60	5-9	<0.3
yellow	~15	55-60	5-9	5-8
red	~10	35-40	5-9	30-35

# RBS: External vs Vacuum



- 3 MeV protons on target
- $\theta = 150^\circ$
- $\text{SiO}_2$  target

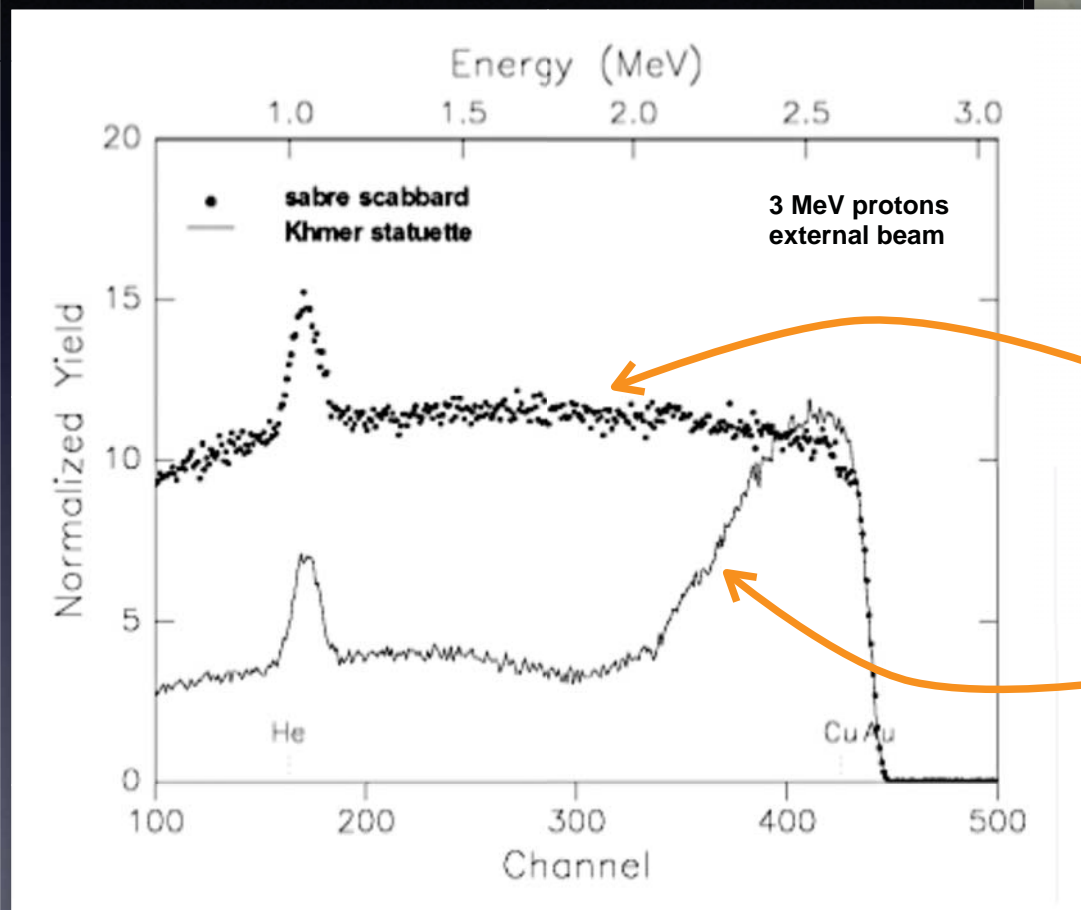


- Energy loss and energy straggling\* in exit window and external path in atmosphere

\* 25 keV FWHM for 7.5  $\mu\text{m}$  Upilex + 10 mm He



# Gold alloy or gilding

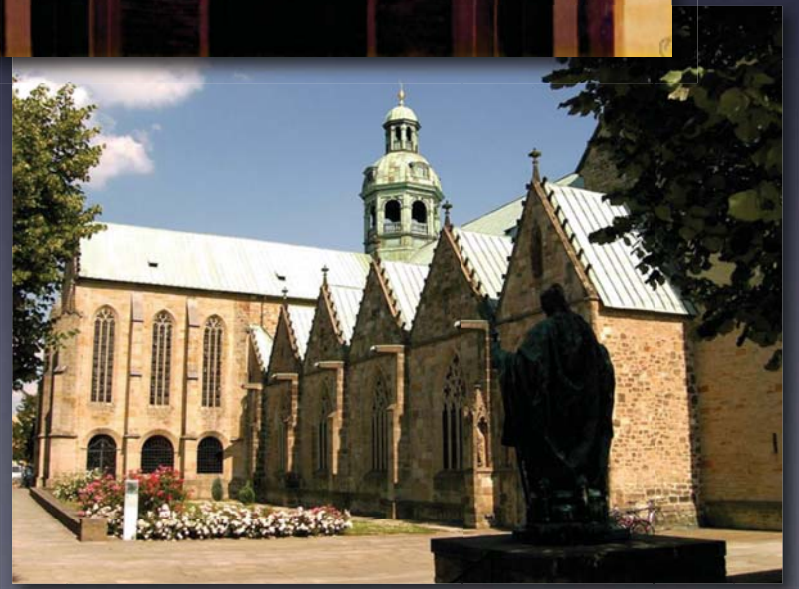
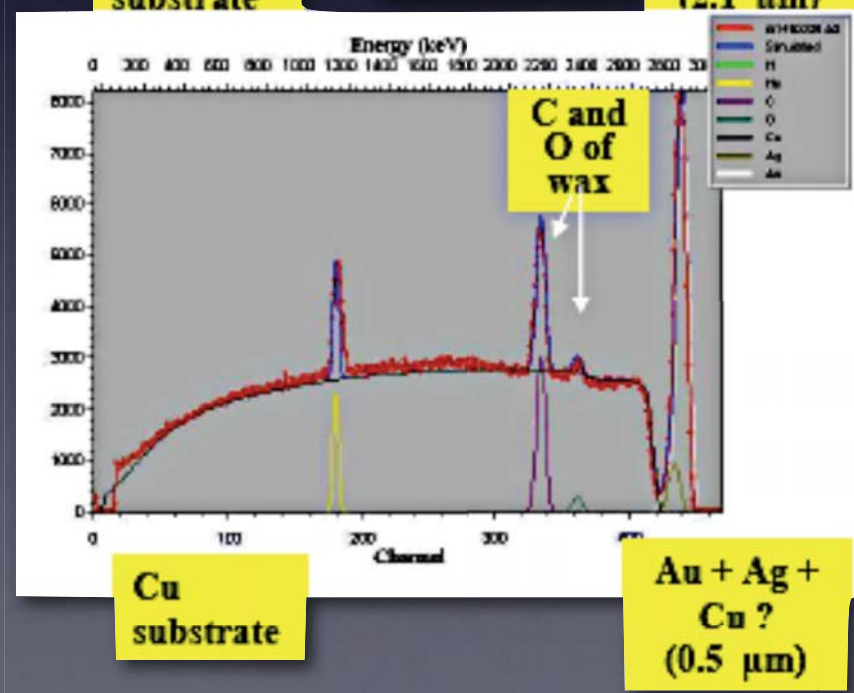
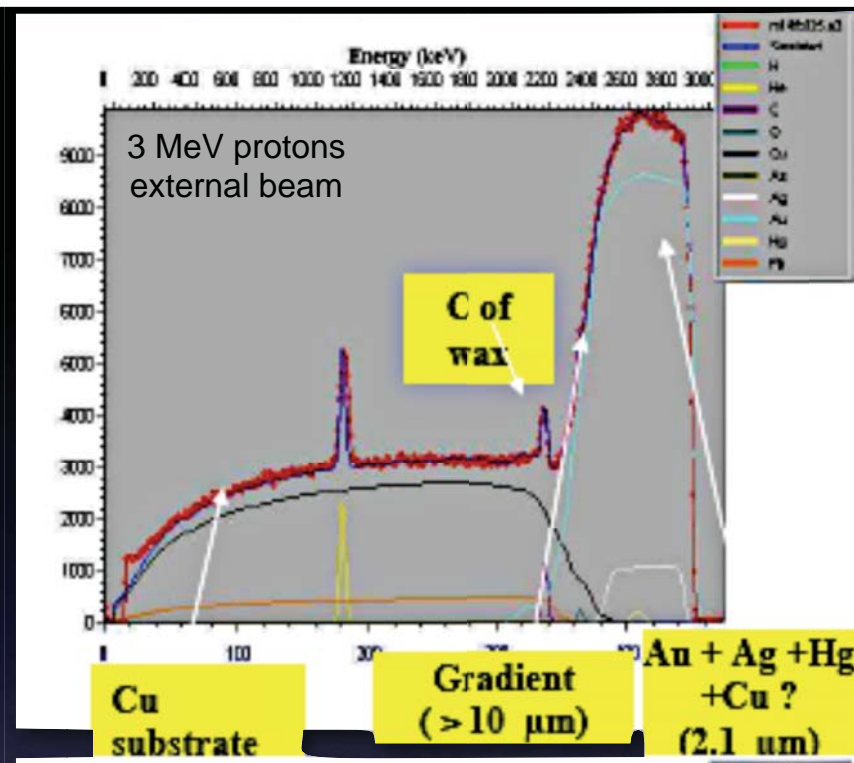


The scabbard is made of a thick Au-Cu alloy (thickness > 10  $\mu\text{m}$ ).

For comparison, the gilding of the statuette is about 2  $\mu\text{m}$  thick.

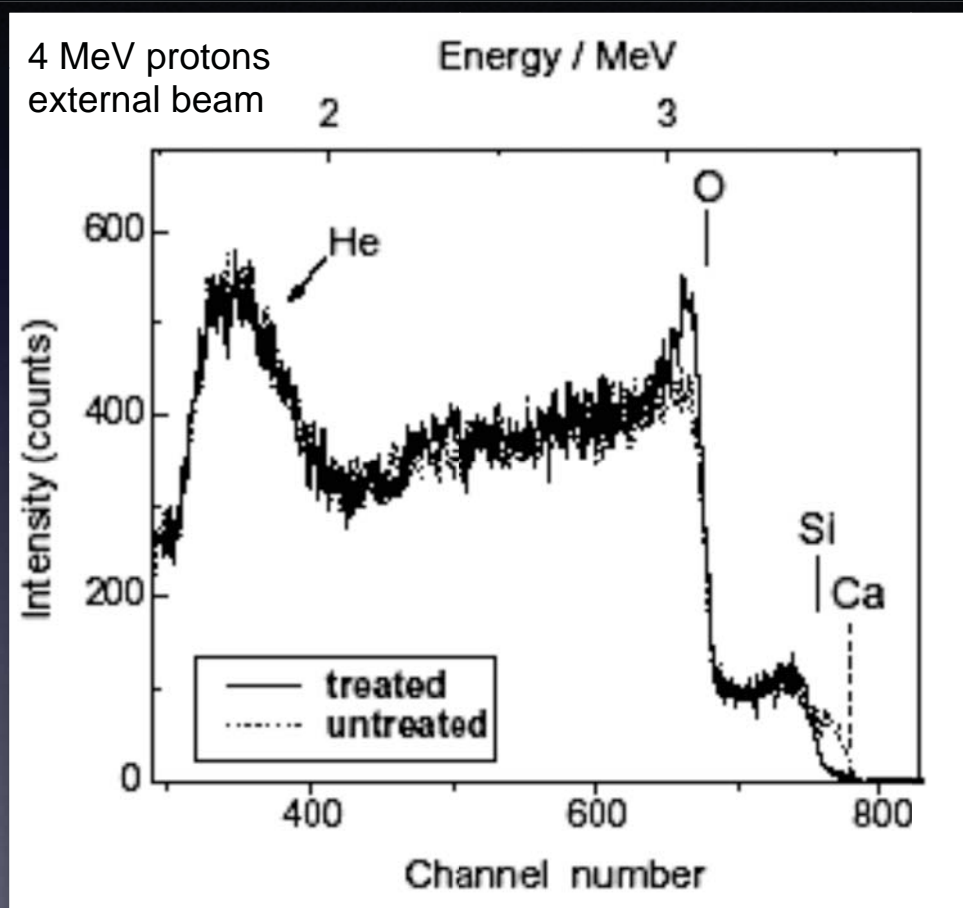
From the width of the Au signal it is possible to obtain the thickness of the gilding ( $dE/dx$  is known).

# RBS analysis of a gilded bronze chandelier (XI century) from the Cathedral of Hildesheim, Germany





# RBS study of glass corrosion



Leaching of Ca, K, Na from the interaction with moisture or water and formation of surface hydrate silicates (cfr. PIGE analysis)

# Complementary PIXE/RBS

In samples with a layered structure the elemental depth profile is needed to correctly calculate absorption effects in PIXE

## *PIXE strenghts*

- High sensitivity
- Excellent specificity

## *RBS strenghts*

- Traceable accuracy
- Excellent depth resolution

## *RBS weaknesses*

- Low sensitivity
- Poor mass resolution

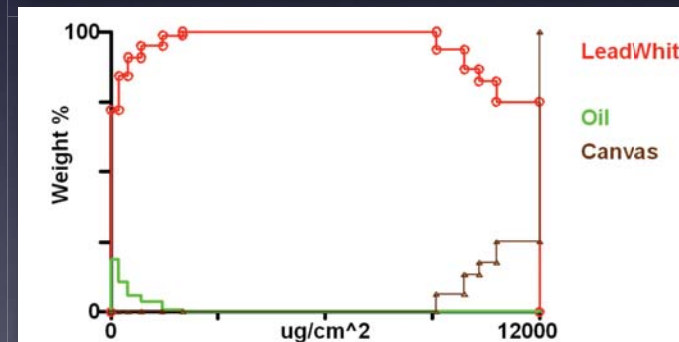
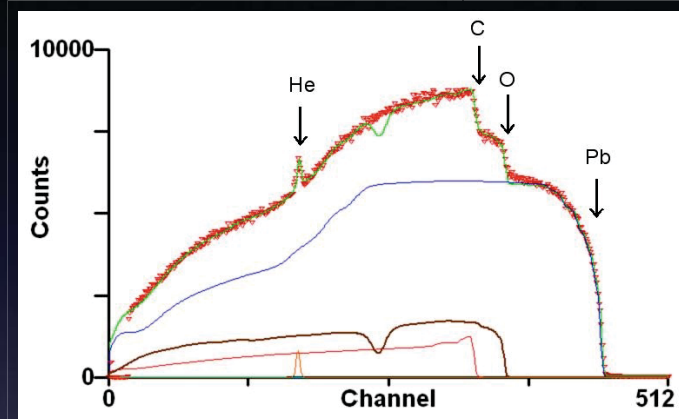
## *PIXE weaknesses*

- Poor traceability
- Poor depth resolution

# Characterization of paint layers by simultaneous PIXE/RBS analysis



"La Bohémienne", Frans Hals (1630)



The canvas is schematized as carbon plus chalk ( $\text{CaCO}_3$ )

Ochre pigment (ematite) detected and quantified thanks to simultaneous PIXE/RBS measurements:  $440 \cdot 10^{15}$  atoms/ $\text{cm}^2$   $\text{Fe}_2\text{O}_3$  in  $7000 \cdot 10^{15}$  atoms/ $\text{cm}^2$  of oil ( $\text{C}_{13}\text{O}_5$ )



# **The Dark Side of IBA**

**The problem of sample damage upon IBA analysis**

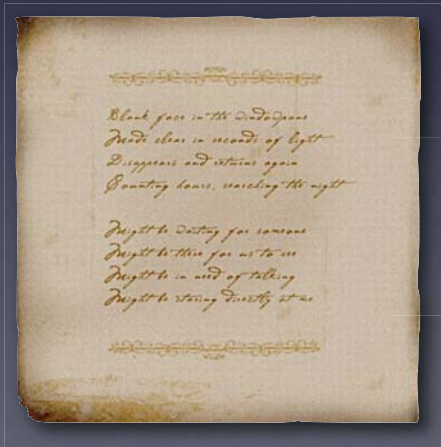
# Which materials suffer ion beam induced damage ?



Ceramics



Pigments



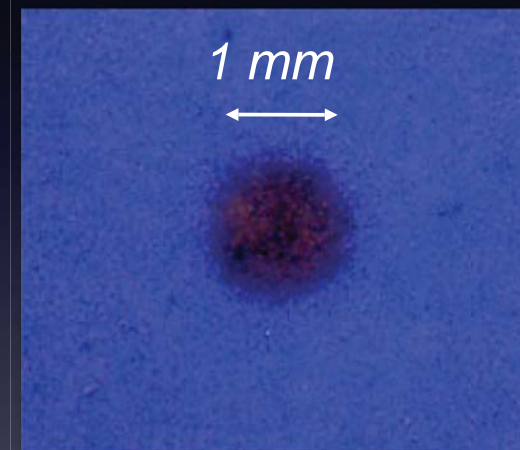
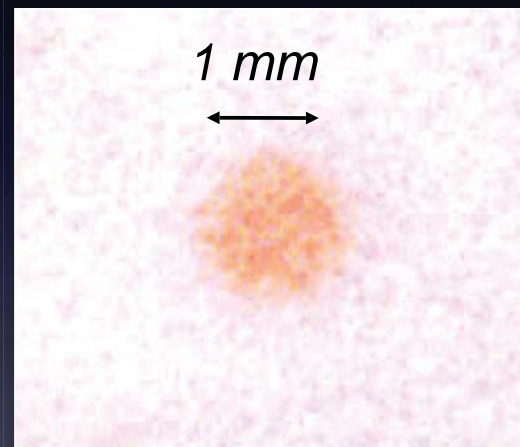
Paper



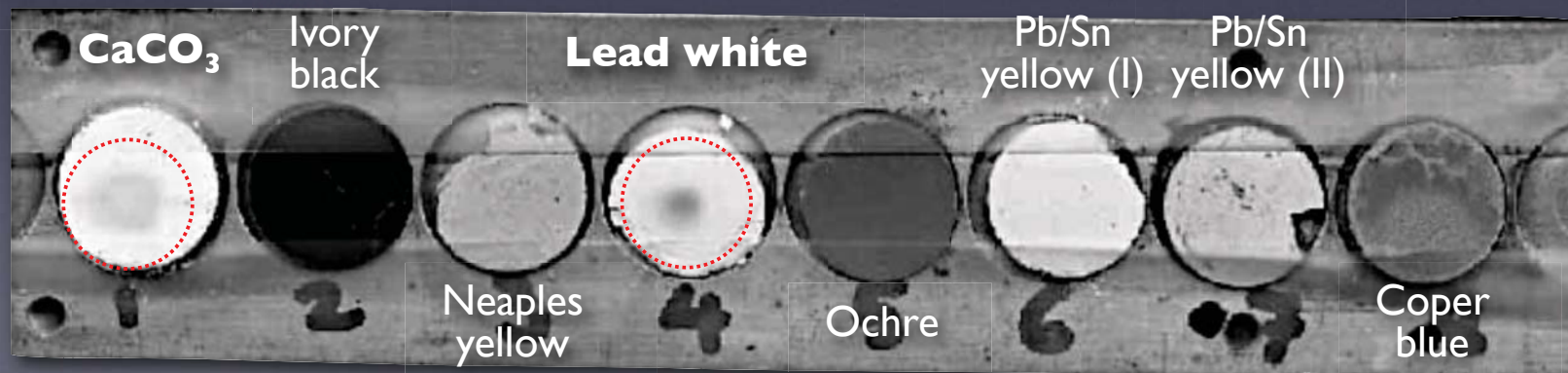
# The “dark spot” phenomenon

Appearance of dark spots during proton beam irradiation of ceramics and pigments (carbonate-based)

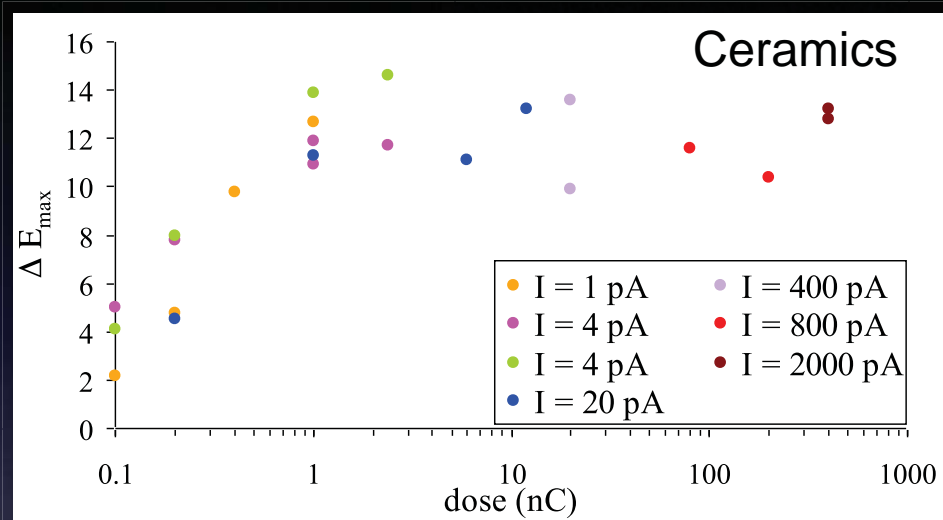
$E = 3 \text{ MeV}$   
 $i = 40 \text{ pA}$   
 $t = 60 \text{ s}$



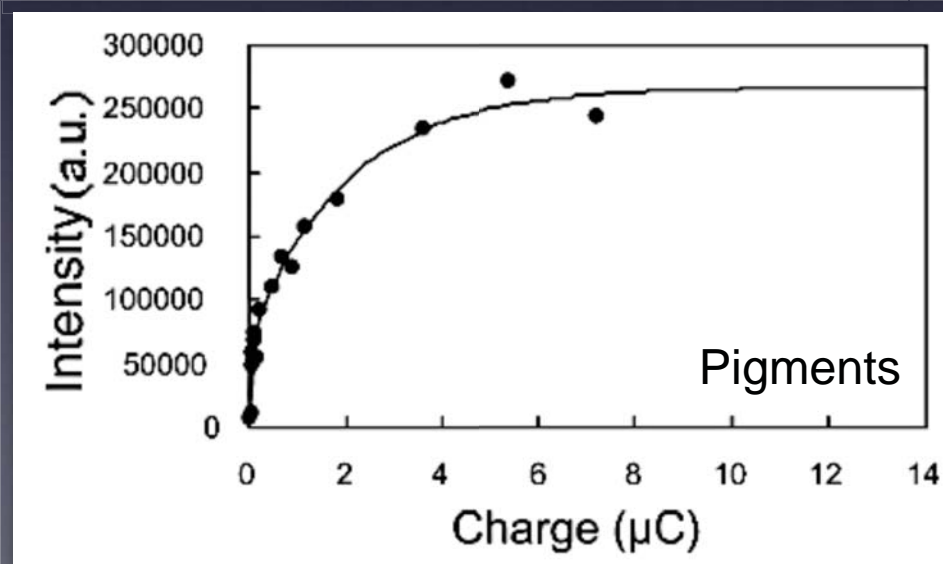
$E = 2.5 \text{ MeV}$   
 $i = 10 \text{ nA}$



# The damage and the beam dose

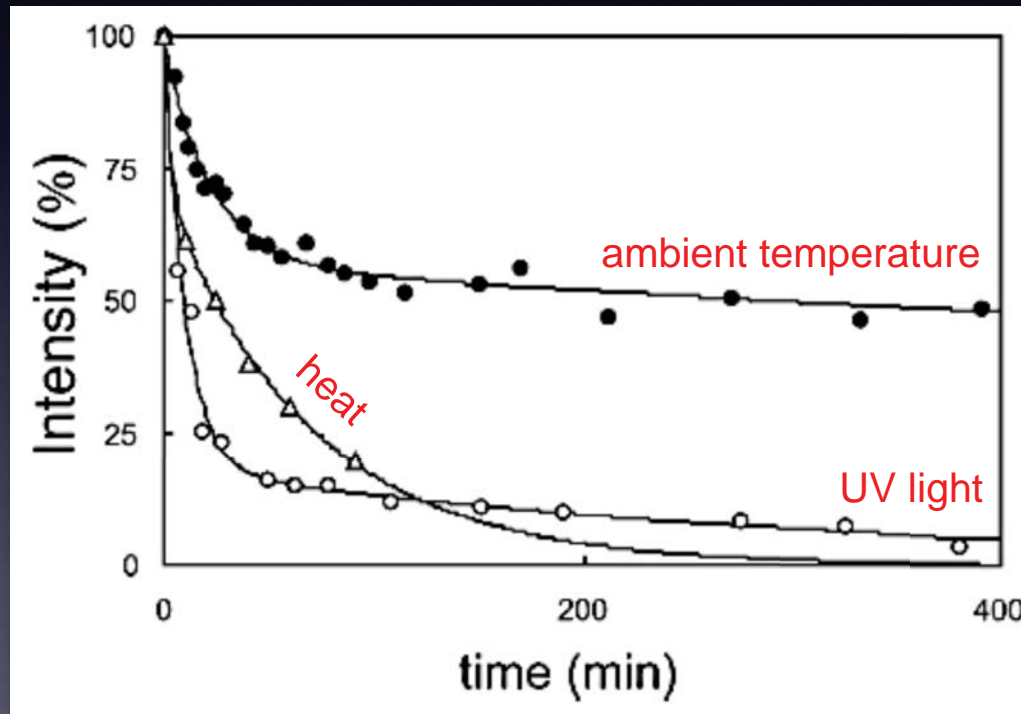


The chromatic variation or the intensity of the dark spot saturates with increasing beam charge



# Recovery of damage

Once the proton beam irradiation stops, the “dark spots” progressively fade out

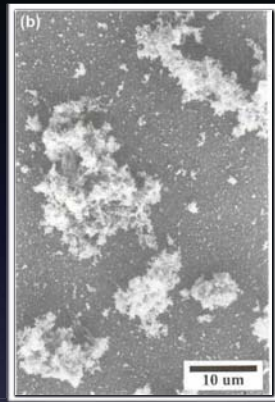


The apparent damage produced in valuable artistic objects can be anyway recovered even at ambient temperature.

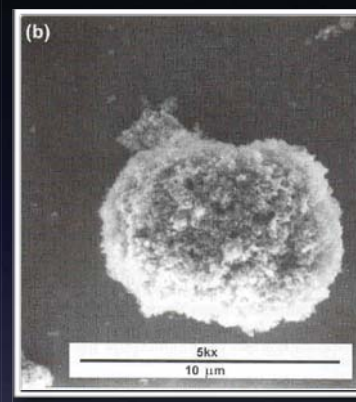
# Airborne particulate matter (aerosol)

Solid or liquid particles with a diameter from  $10^{-3}$  to  $10^2$   $\mu\text{m}$

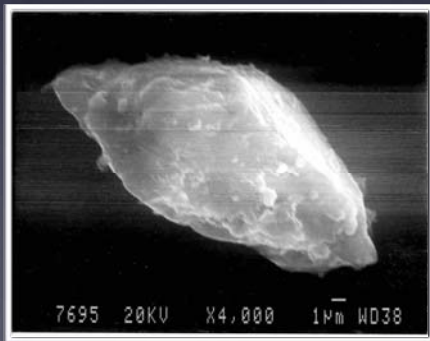
Origin: primary or secondary



Diesel engine emission



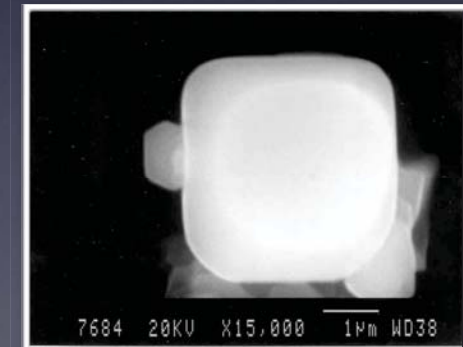
Black carbon



Mineral dust



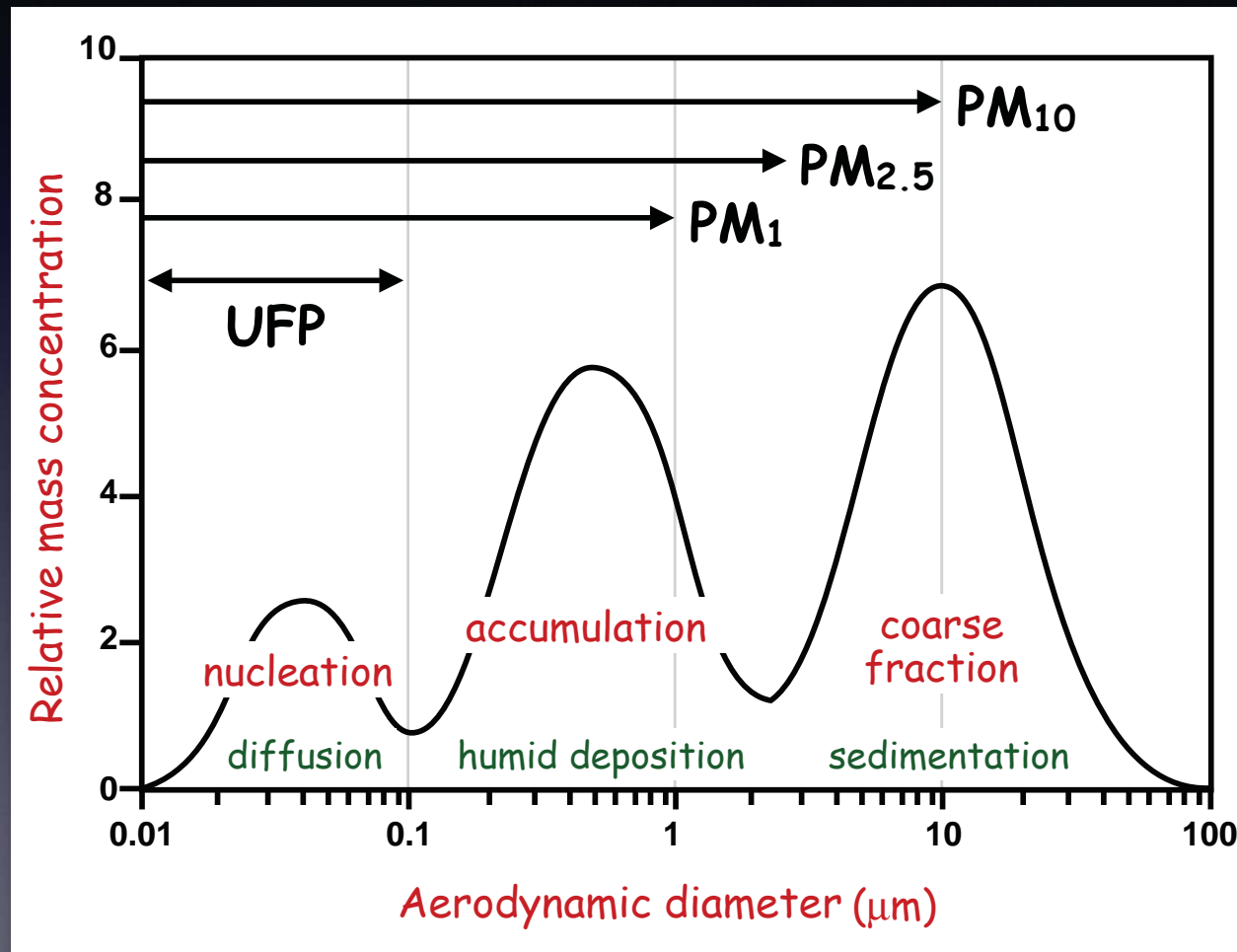
Vegetal fibre



NaCl crystal

# Aerosol average distribution

**Aerodynamic diameter:** diameter of a sphere of unit density ( $1 \text{ g/cm}^3$ ) that has the same gravitational settling velocity as the particle in question.





# Natural sources of aerosols



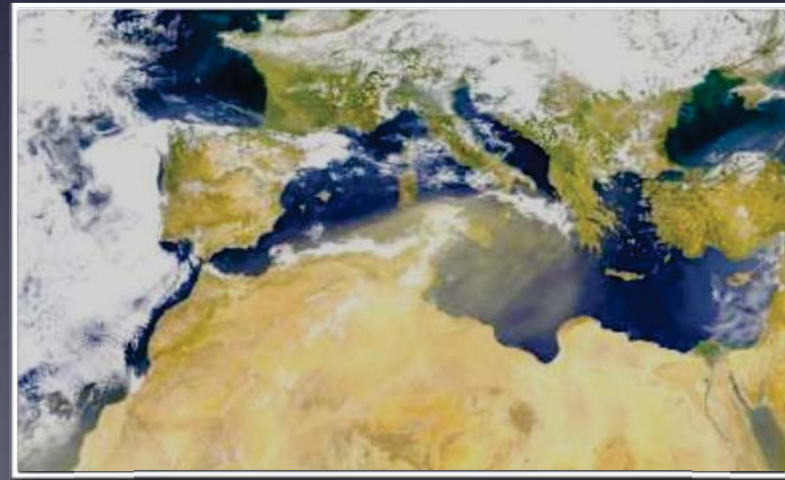
Sea Spray



Volcanic eruptions



Forest fires



Desert dust transport

# Anthropogenic sources of aerosols



Traffic



Thermoelectric  
power plants



Waste incinerator



Domestic heating



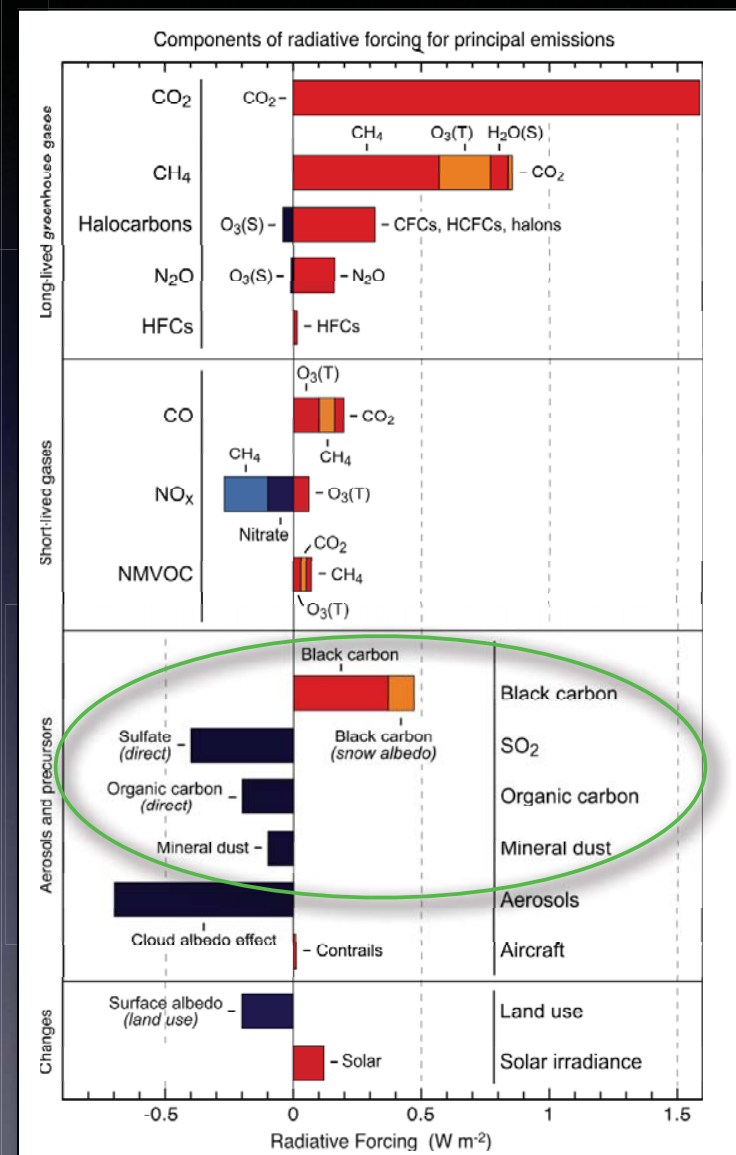
Industrial activities

# Aerosol impact on environment

- Cloud formation
- Absorption and scattering of solar radiation



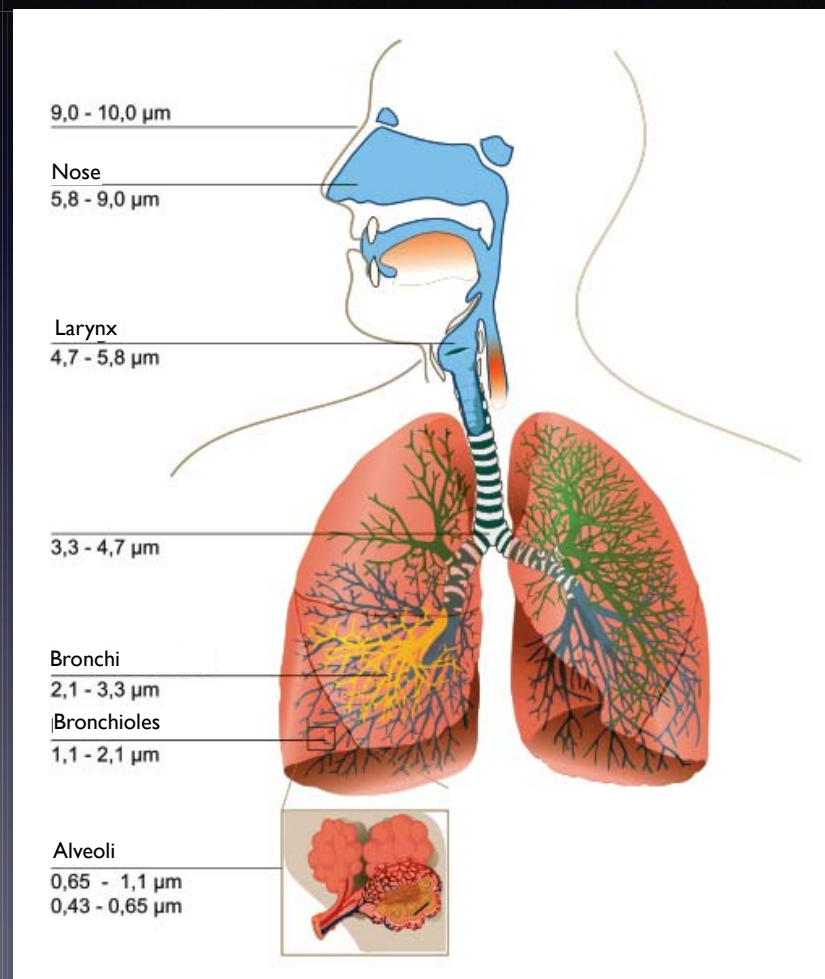
## Climate forcing





# Aerosol impact on human health

- Chronic or severe respiratory diseases
- Toxic or carcinogen effects



## EU LIMIT VALUES FOR PARTICULATE MATTER CONCENTRATION

*New European regulation (2008/50/CE)*

### **PM<sub>10</sub>**

- Annual avg.  $<40 \mu\text{g}/\text{m}^3$
- Daily avg.  $<50 \mu\text{g}/\text{m}^3$  (not more than 35 days/year)

### **PM<sub>2.5</sub>**

- Annual avg.  $<25 \mu\text{g}/\text{m}^3$  within 2015 (PM<sub>2.5</sub>  $<10 \mu\text{g}/\text{m}^3$  according to WHO)

# Aerosol impact on cultural heritage



*Funerary monument from 1837, English Cemetery, Florence (before and after restoration)*

- Soiling
- Black crust formation
- Soluble salt crystallization



- Aesthetic damages
- Chemical reactions and physical interaction with the materials



# What do we need...

Many good quality data concerning:

- PM concentration and composition
- size distribution
- optical properties
- time and space evolution
- ...

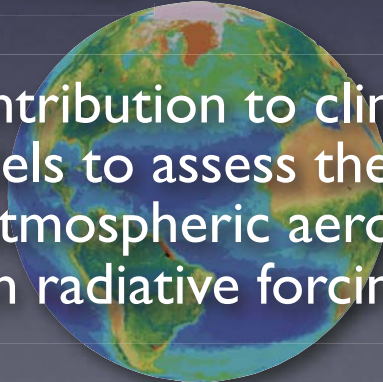


Identification e  
quantification of  
PM emission  
sources through  
receptor models

**OUTPUT**



Contribution to  
pollution abatement  
policies to improve  
air quality



Contribution to climate  
models to assess the role  
of atmospheric aerosols  
in radiative forcing

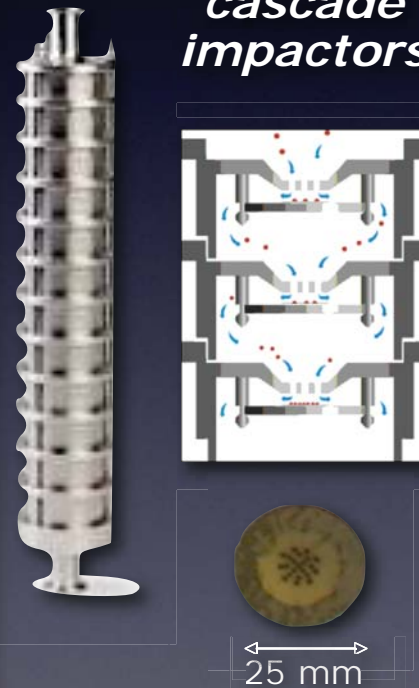
# Why IBA techniques?

- Aerosol sampling campaign produce huge amounts of small samples data ( $10\text{-}300\ \mu\text{g}/\text{cm}^2$ )

*PM<sub>x</sub> sequential samplers*



*Multistage cascade impactors*



*Continuous samplers*

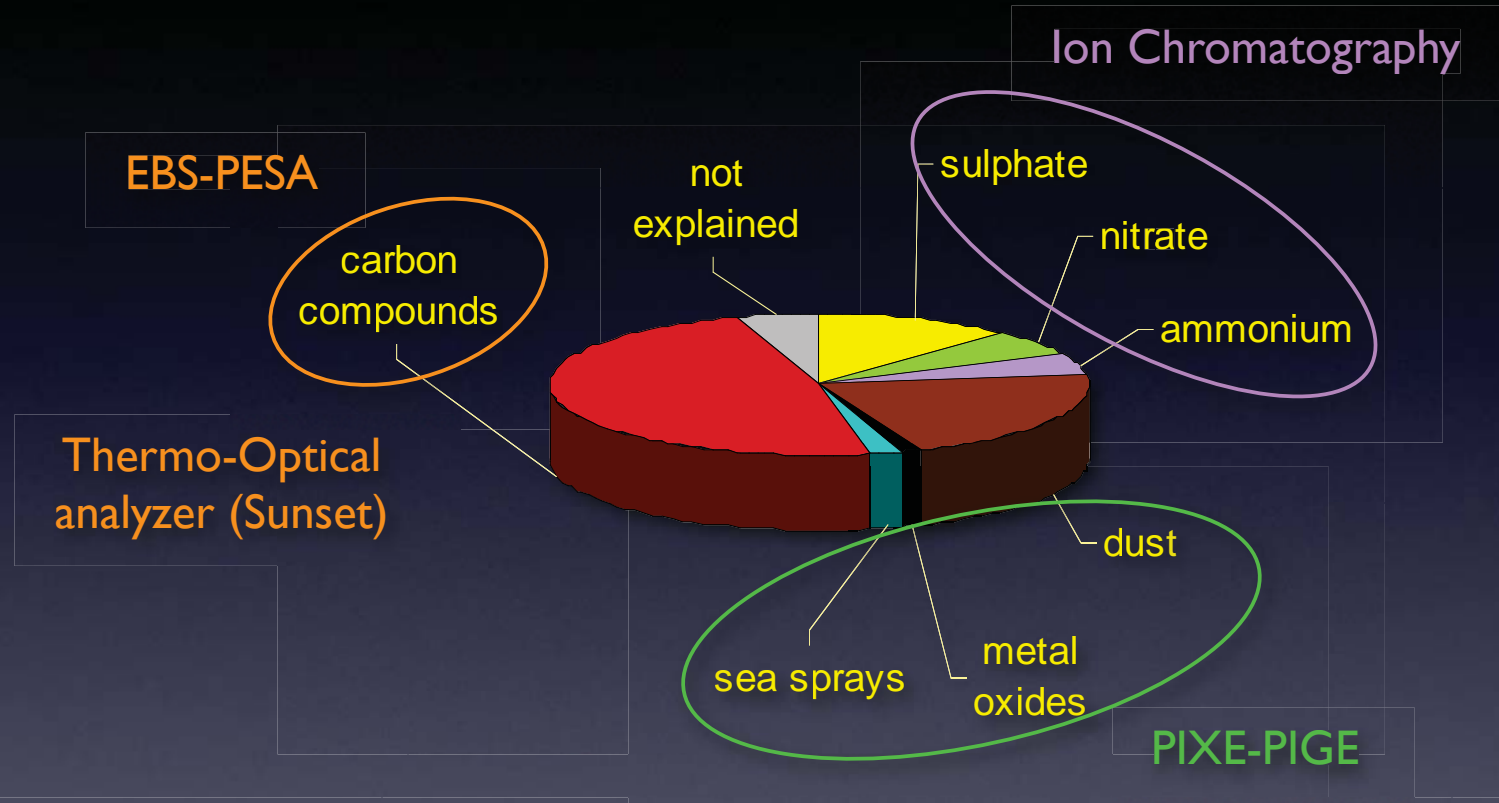


*"hourly samples"*

100 mm

- Multielemental, fast, high sensitive, quantitative, non-destructive techniques are necessary

# IBA in the context



- Aerosol campaigns need an integrated approach involving different analytical techniques
- PIXE is the most widely used IBA technique (it detects all elements from Na to Pb)

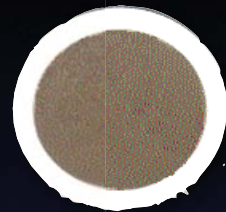
# PM<sub>x</sub> daily samples



PM<sub>1</sub>

PM<sub>2.5</sub>

PM<sub>10</sub>



47 mm

*Typical filters:*

Nuclepore ( $C_{15}H_{14}CO_3$ )

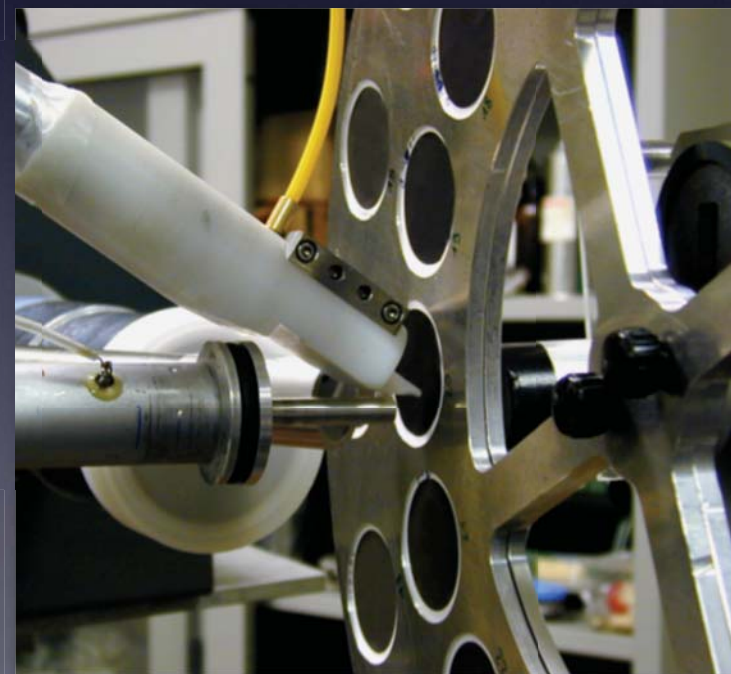
Cellulose ( $C_{12}H_{30}O_{15}$ )

Teflon ( $CF_2$ )

Quartz fiber (boro-silicate)

- Beam current 5 ÷ 50 nA
- Beam size: 1 mm x 2 mm (scanning the sample)
- Measuring time: 5 ÷ 10 minutes

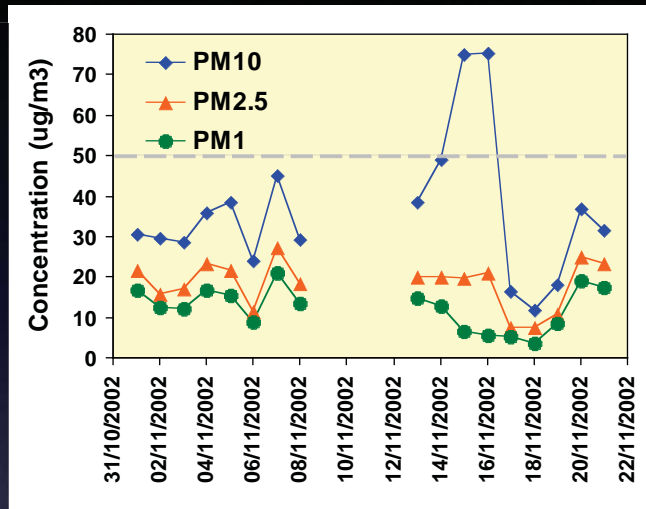
**1 year of daily samples:  
2-3 days**



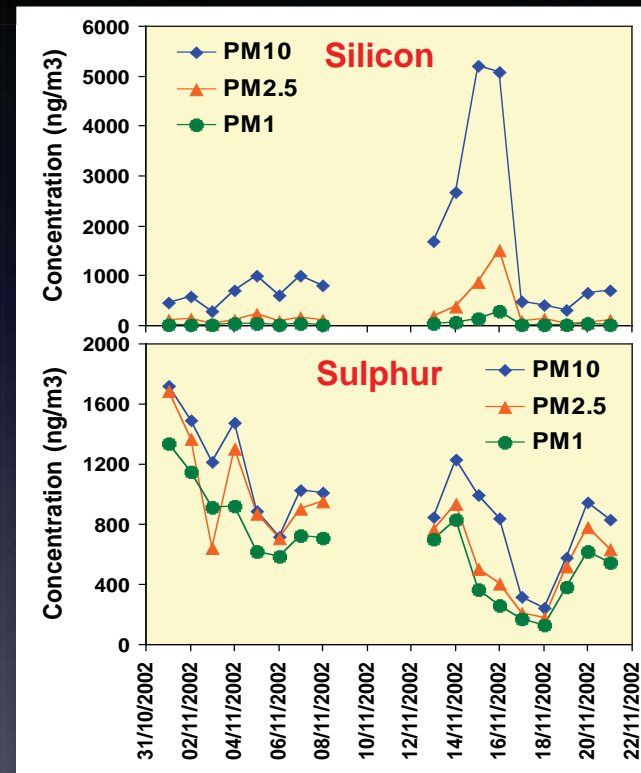


# Saharan dust transport events

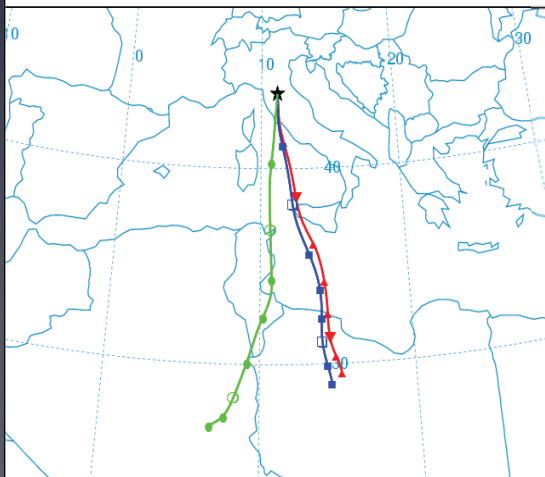
Increase in PM10 concentration



Increase of soil related elemental concentrations



NATIONAL OCEANIC ATMOSPHERIC ADMINISTRATION  
Backward trajectories ending at 12 UTC 16 Nov 02  
FNL Meteorological Data



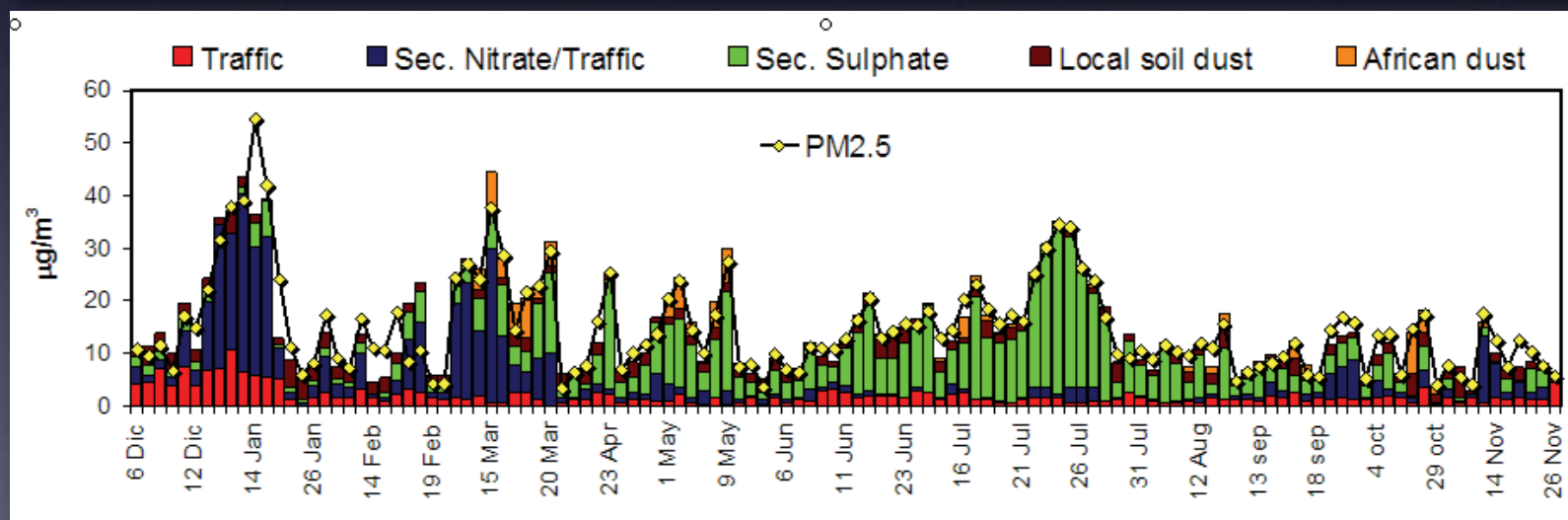
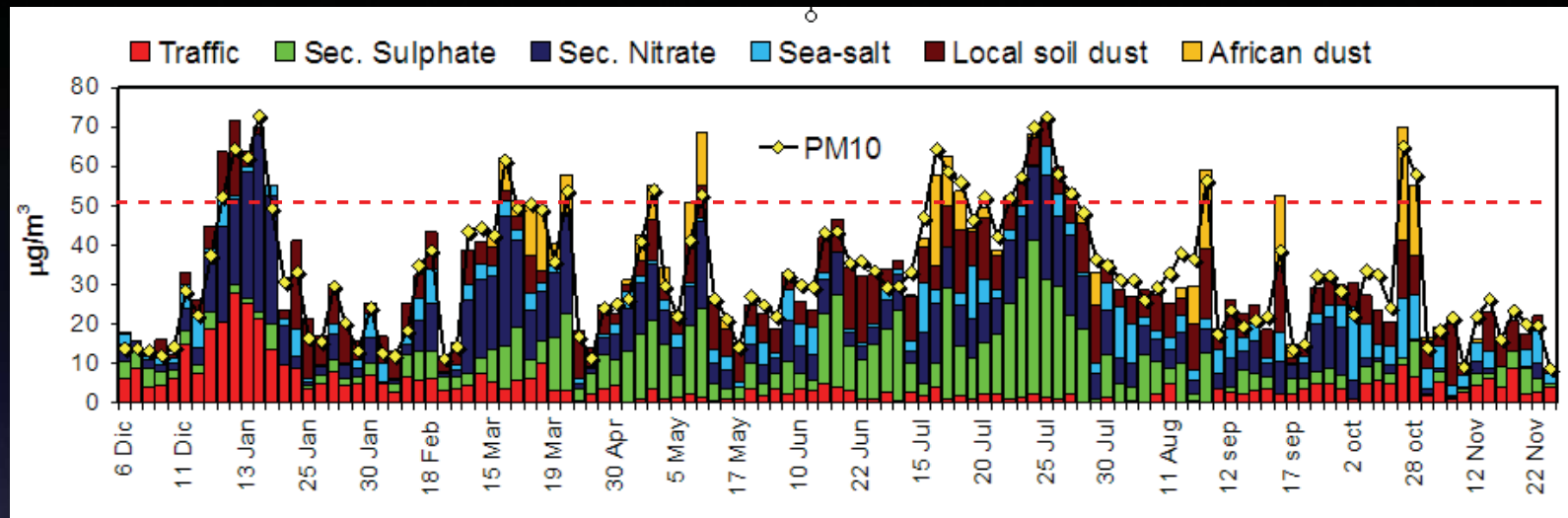
Air masses coming from Sahara

Change in elemental ratios

	Ti/Fe	Si/Fe	Al/Fe
15-Nov-02	0.09	2.79	1.07
16-Nov-02	0.10	2.52	1.01
other days	0.05 ± 0.02	1.81 ± 0.43	0.56 ± 0.22



# Identification of aerosol sources



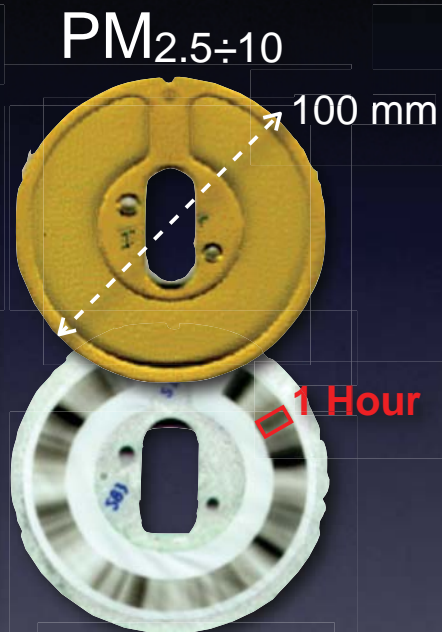
PM10 and PM2.5 daily samples collected simultaneously for one year (Dec. 2004 – Dec. 2005) in Elche, Spain

# Fine and coarse hourly samples

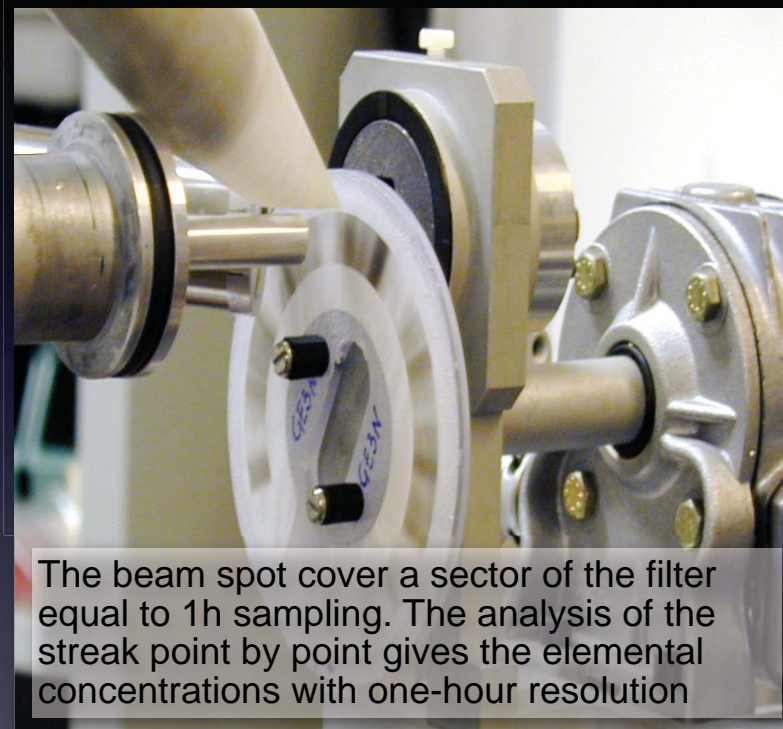
## Continuous “streaker” sampler



Kapton foils  
Nuclepore



$PM_{2.5}$



The beam spot cover a sector of the filter equal to 1h sampling. The analysis of the streak point by point gives the elemental concentrations with one-hour resolution

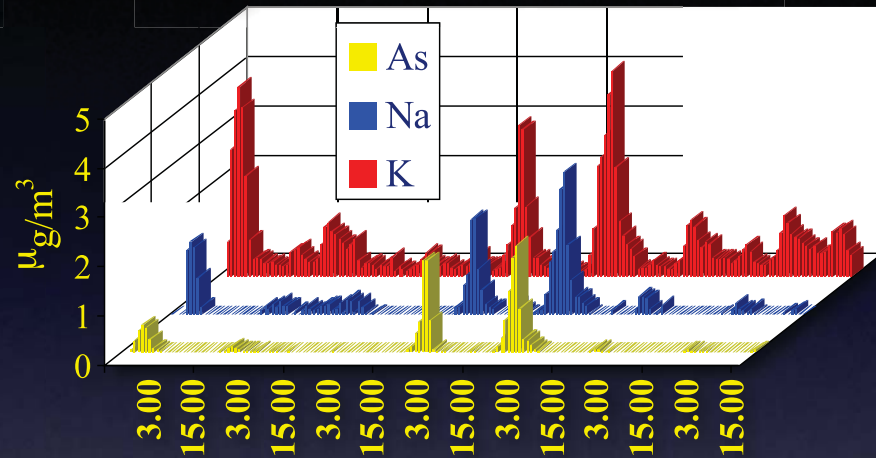
**1 week at 1h resolution:  
9 hours (168 spots)**

- Beam current 20 ÷ 50 nA
- Beam size: 1 mm x 2 mm
- Measuring time: 3 minutes

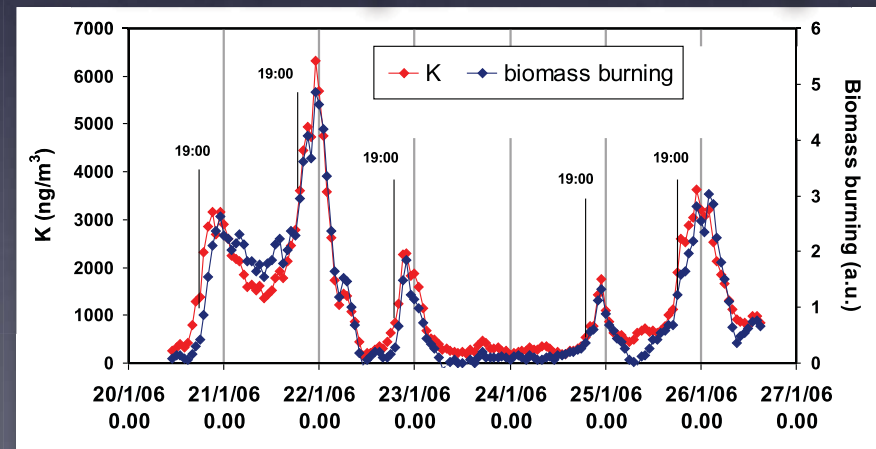
# Elemental time series

Size fractionation  
+  
High time resolution  
+  
Low elemental detection limit  
+  
Broad range of elements  
=  
New insight into short-term  
dynamics of atmospheric  
pollution by trace elements

*Fugitive industrial emissions*

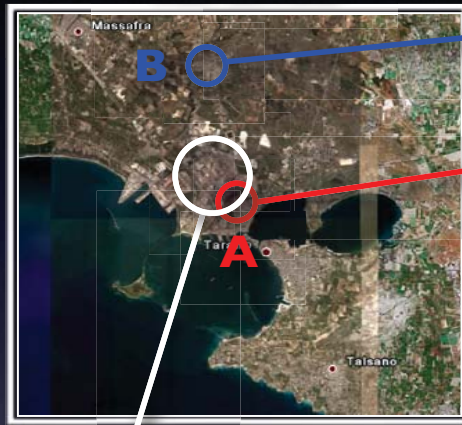


*Wood burning for domestic heating*



# Identification of industrial emissions: steel plants in Taranto (Italy)

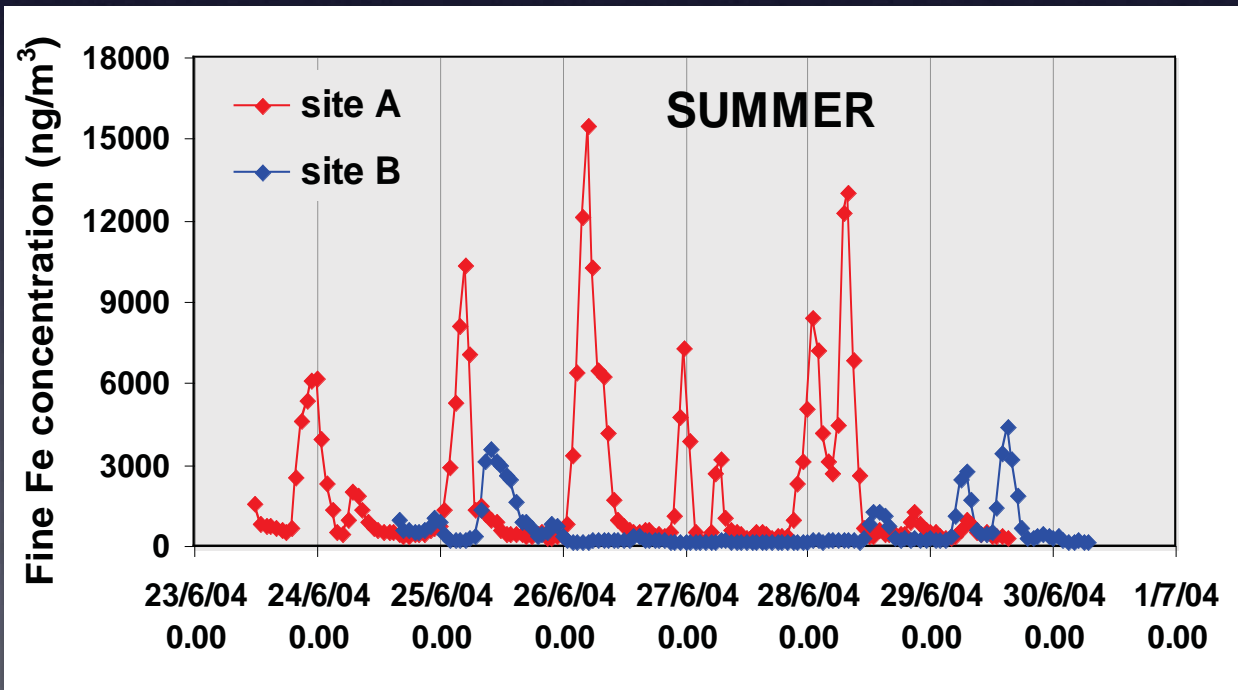
Taranto



Site B: small town 7 km N of Taranto

Site A: urban district adjacent to the industrial area

Industrial area

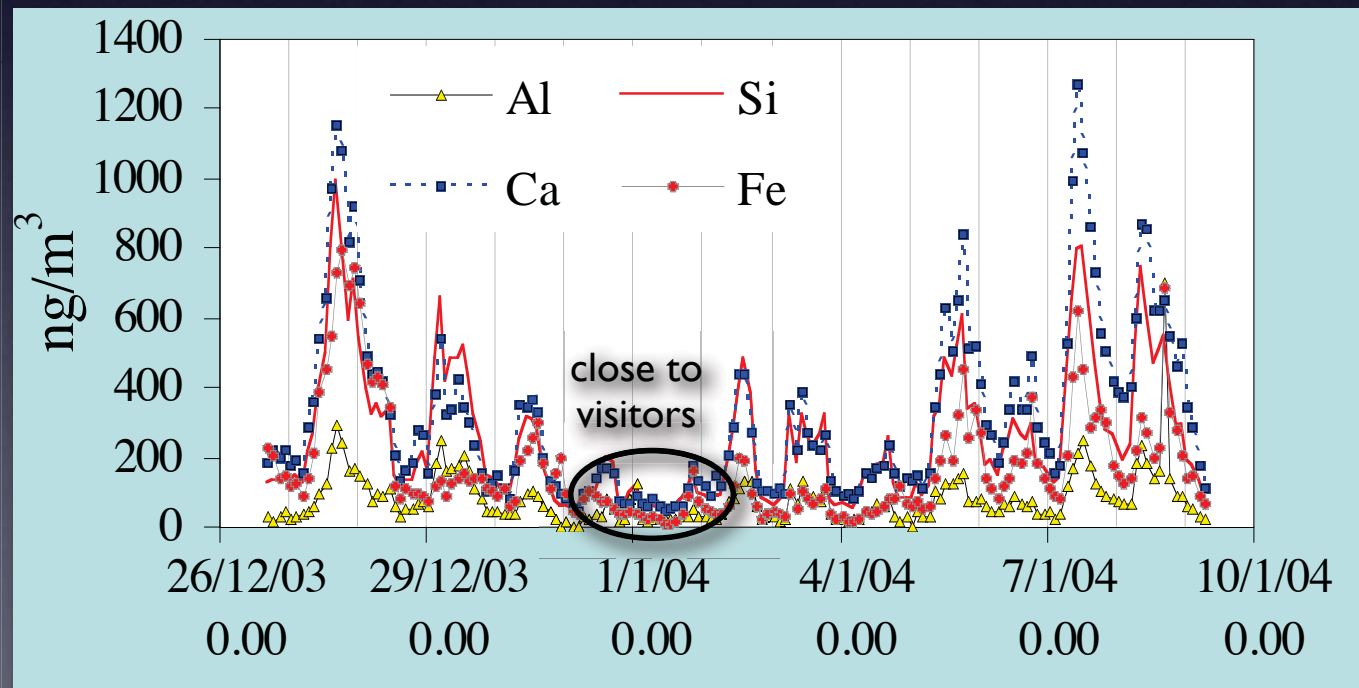




# Impact of tourism on cultural heritage

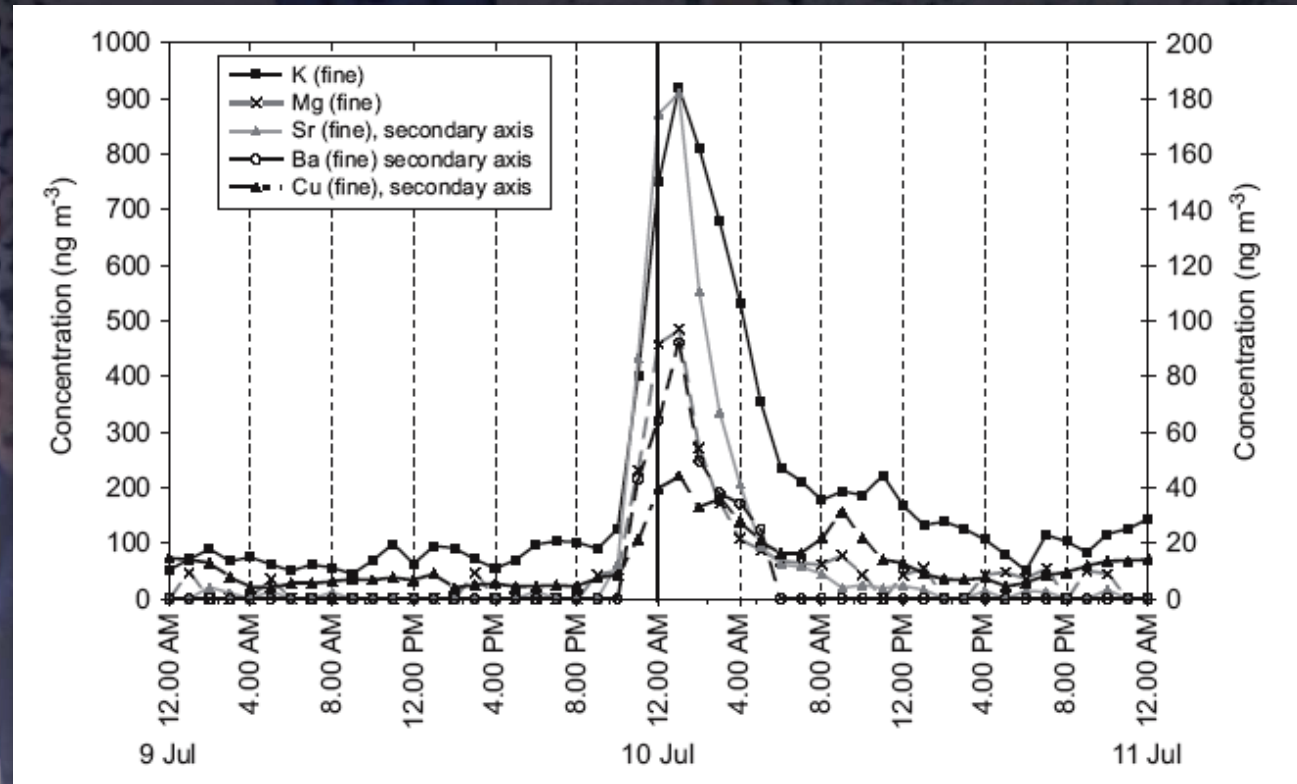


Michelozzo's Courtyard  
(Palazzo Vecchio, Florence)



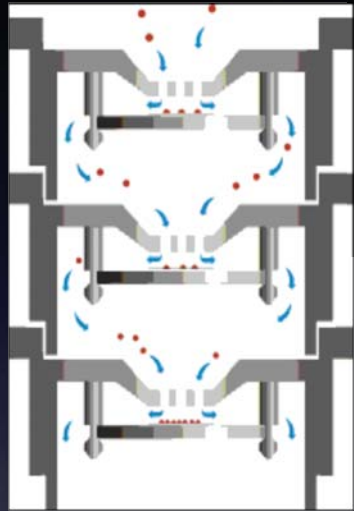


# Identification of anthropic emissions: fireworks



During the night between 9 and 10 July 2006 fireworks were burnt to celebrate the Italian football team, winner of the FIFA World Cup

# Multi-stage cascade impactors



- SDI (Small Deposit area Impactor)
  - 12 stages from 45 nm to 8.5  $\mu\text{m}$  (11 l/min.)
  - Small particle collection area (< 8 mm)

- Developed to collect aerosol (in remote areas) for PIXE in-vacuum analysis with large beams
- In an external set-up it is not possible to work with large beams

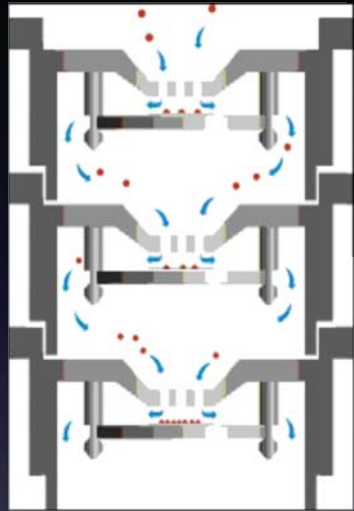
Kapton, Mylar or polycarbonate foils



25 mm



# Multi-stage cascade impactors



- SDI (Small Deposit area Impactor)
  - 12 stages from 45 nm to 8.5  $\mu\text{m}$  (11 l/min.)
  - Small particle collection area (< 8 mm)

- Developed to collect aerosol (in remote areas) for PIXE in-vacuum analysis with large beams
- In an external set-up it is not possible to work with large beams

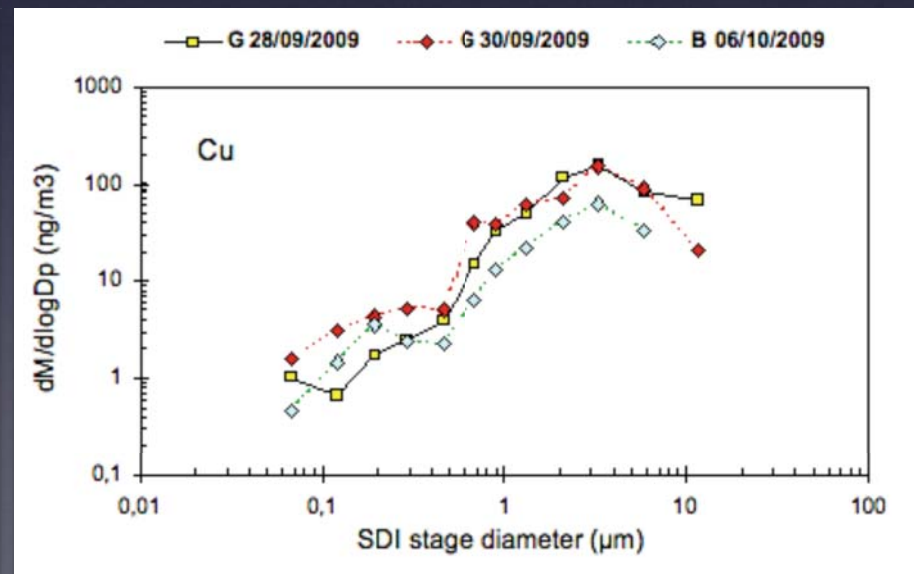
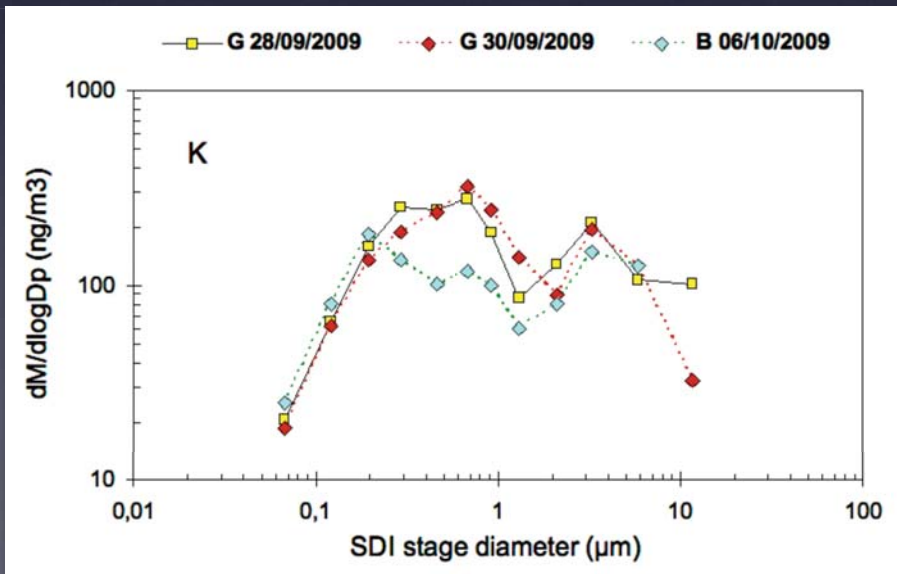
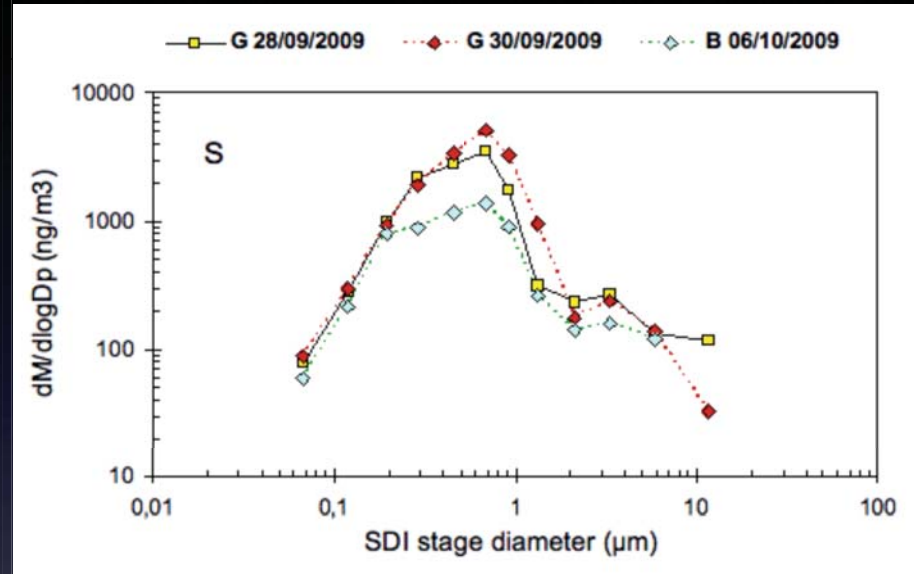
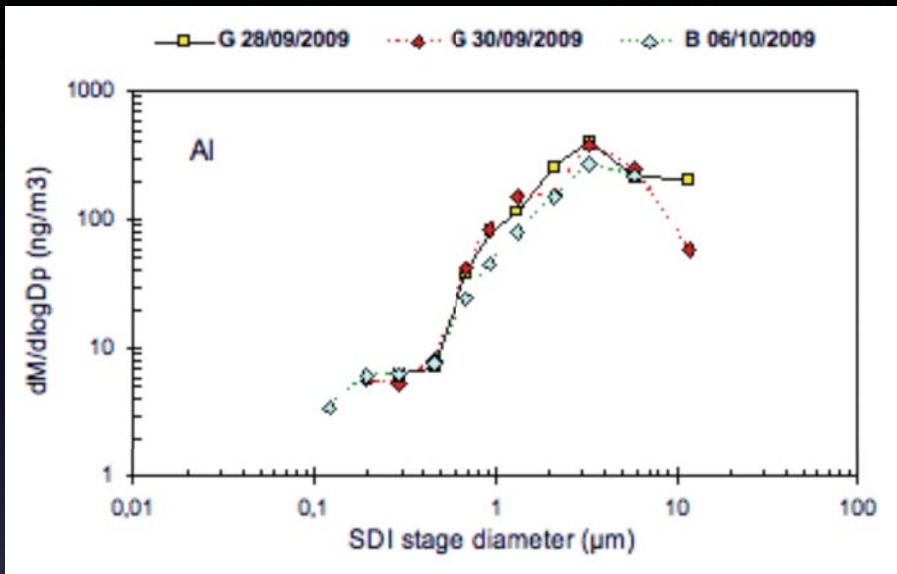
Kapton, Mylar or polycarbonate foils



25 mm

**Homogeneous scanning of the deposit area**

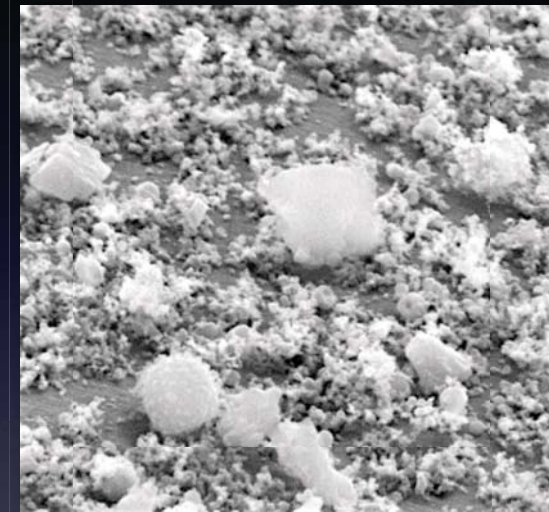
# Dimensional distributions





# Matrix effects in PIXE

- Aerosol deposit can be considered a thin target ( $\Delta E \leq 120$  keV for protons of few MeV energy in  $PM_{10}$ )
- Small cross section variations within energy loss inside the sample
- Self-absorption of emitted radiation inside aerosol particles:
  - *it is a problem for a PIXE quantitative analysis for low-Z elements: Na, Mg, Al, Si*
  - *it can not be calculated considering an average matrix composition*



mandatory  
for studying  
mineral  
dust



# PIGE for atmospheric aerosols

PIGE measurements can be used to correct the underestimation of PIXE due to low-energy X-rays absorption in the aerosol particles

Aerosol particles are a thin target (for 3 MeV protons  $\Delta E$  is about 120 keV for “coarse mode” particles, i.e. PM10)

$$n_{\gamma} = n_p N \Delta\Omega \epsilon \int_{E_0 - \Delta E}^{E_0} \frac{d\sigma}{d\Omega}(E, \theta) \frac{dE}{S(E)}$$

If the PIGE cross sections are constant over the energy range  $\Delta E$  then:

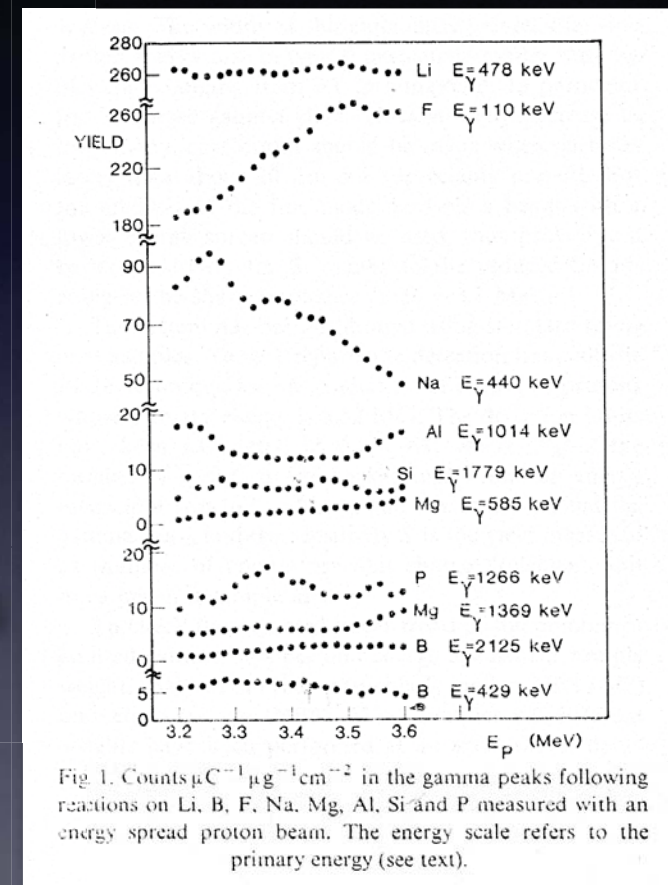
$$n_{\gamma} = n_p \sigma \Delta\Omega N t$$

The unknown concentrations can be deduce by comparing the  $\gamma$ -ray yield to those of **thin** elemental standards

# Spreading the beam for PIGE

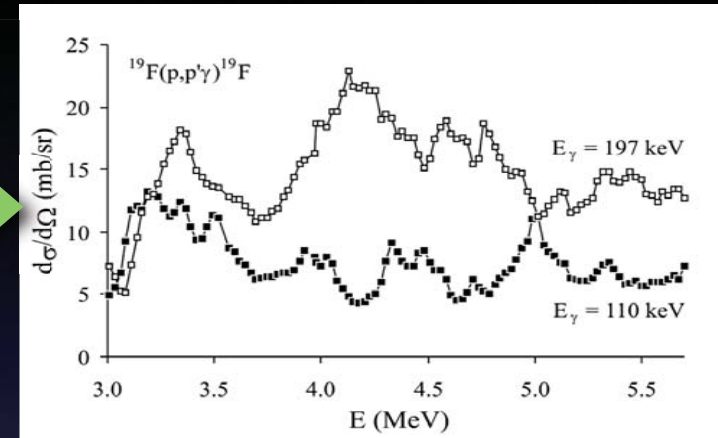
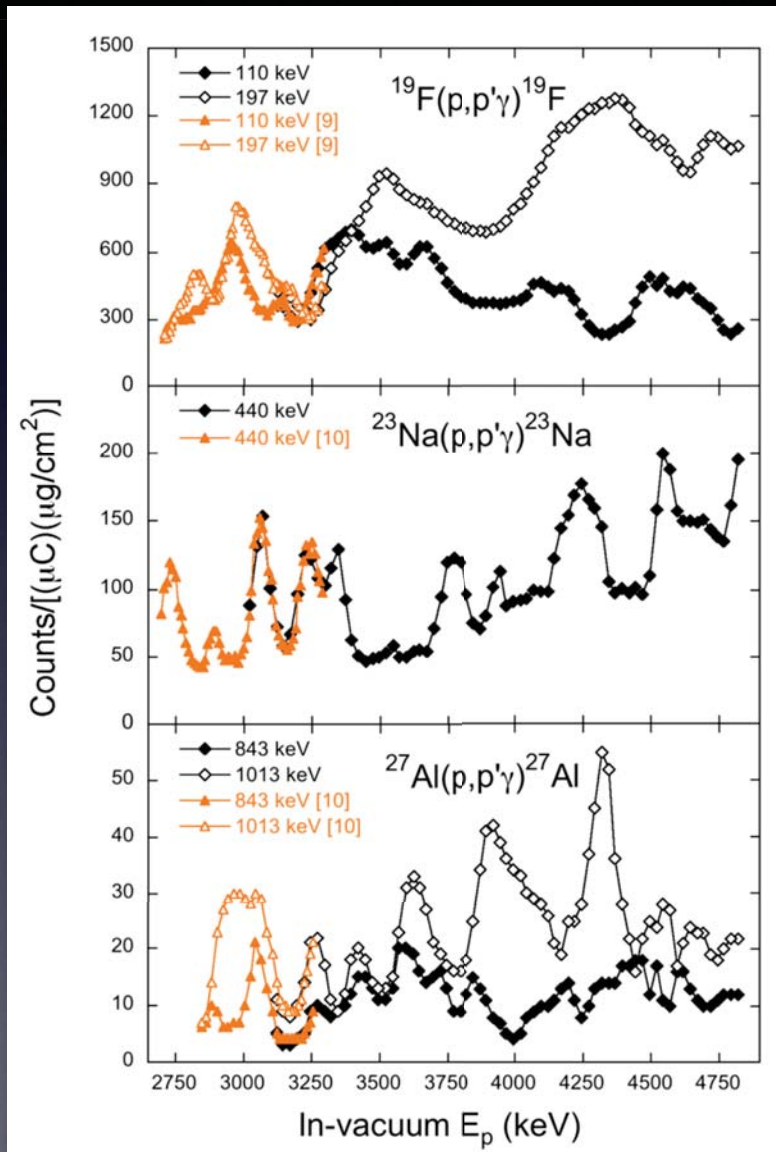
- Finding energy intervals where prompt gamma-ray emission cross sections are **constant** and **high** enough.
- Prerequisite to provide an analytical method with good sensitivity and not affected by sample weight and matrix effects, suitable to large-scale analysis.
- Smooth the fluctuations in the PIGE cross sections (i.e. use a diffuser).

**Use an external beam !**

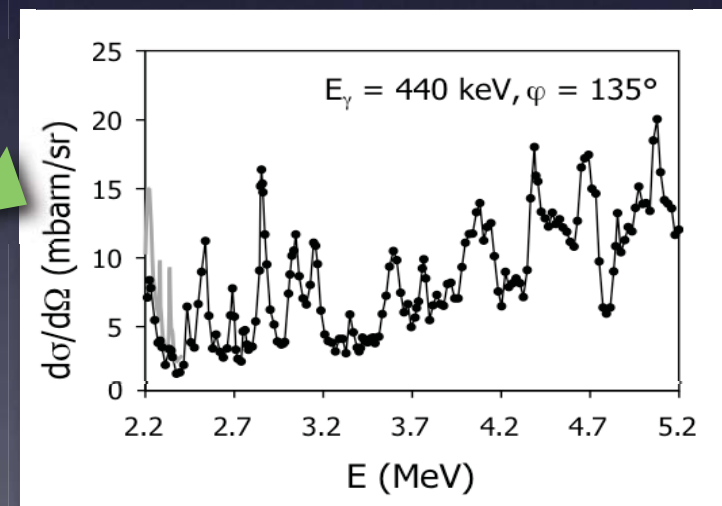


C. Boni et al., NIM B 40/41, 1989

# PIGE yields with external proton beam



A. Cacioli et al., NIM B 249, 2006



A. Cacioli et al., NIM B 266, 2008

G. Calzolari et al., NIM B 268, 2010

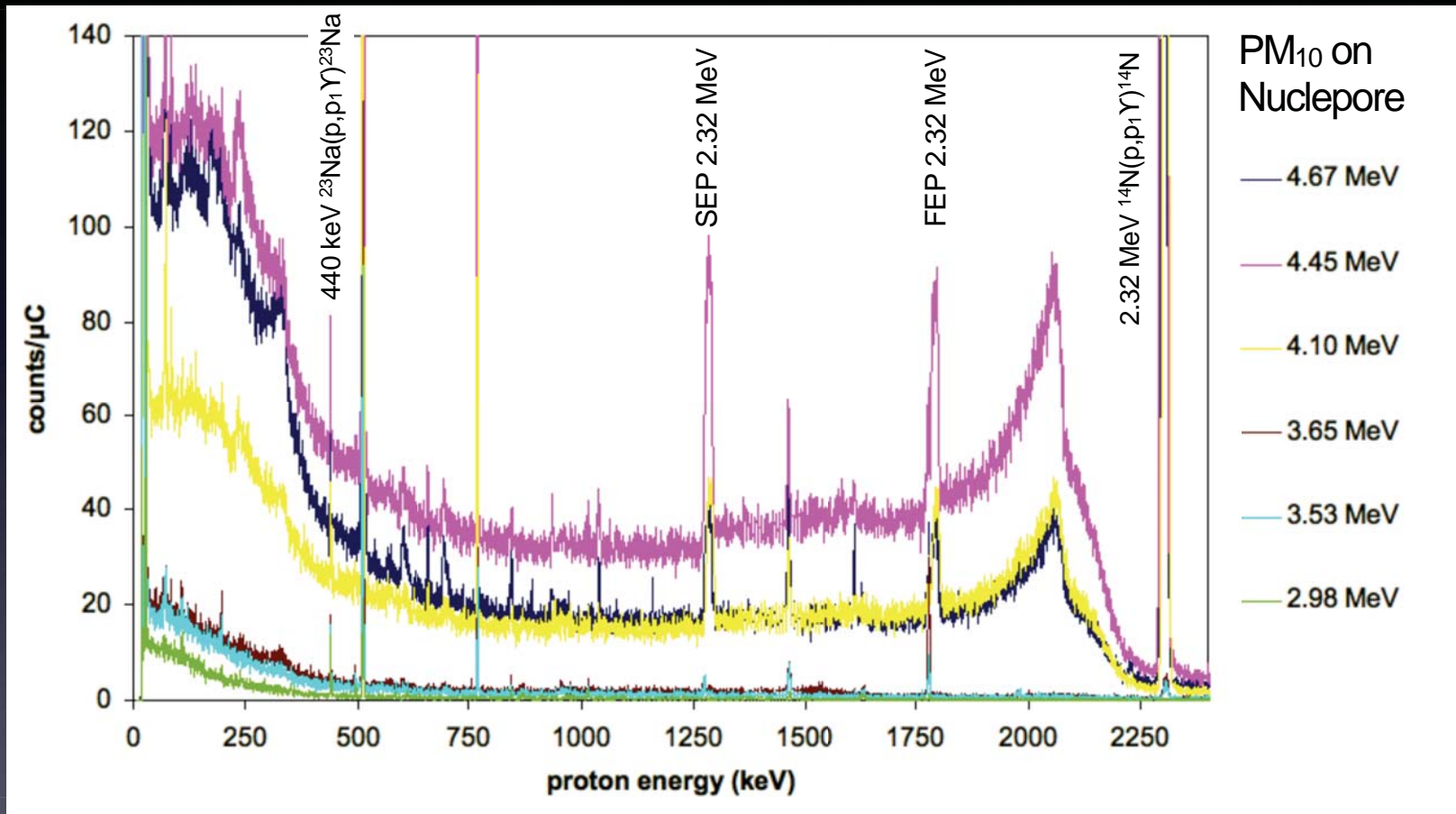
# Energy plateau region for PIGE

Reaction	$E_\gamma$ (keV)	$E_p$ (keV)	$E_p$ on target <sup>a</sup> (keV)	Width (keV)	Average yield [counts/( $\mu\text{C}\cdot\mu\text{g}/\text{cm}^2$ )]
$^{19}\text{F}(p,p'\gamma)^{19}\text{F}$	110	4020	3863	175	380
		4395	4248	100	250
	197	3945	3785	125	700
		4420	4274	150	1250
$^{23}\text{Na}(p,p'\gamma)^{23}\text{Na}$	440	2990	2791	70	50
		3520	3346	100	50
		3670	3501	100	55
		4045	3889	75	90
		4470	4326	100	100
		4695	4556	100	150
$^{27}\text{Al}(p,p'\gamma)^{27}\text{Al}$	843	4370	4223	75	14
		4745	4607	75	10
	1013	3065	2870	120	29
		3820	3657	75	18
		4695	4556	75	23

<sup>a</sup> The proton beam energy  $E_p$  on target is calculated taking into account the energy loss in the 7.5  $\mu\text{m}$  Upilex exit window and in the external path of 5 mm of air and 5 mm of He.



# Energy plateau for Na measurement



$E_p$ (MeV)	4.67	4.45	4.10	3.65	3.53	2.98
MDL ( $\text{ng}/\text{cm}^2$ )	73	133	93	70	60	37

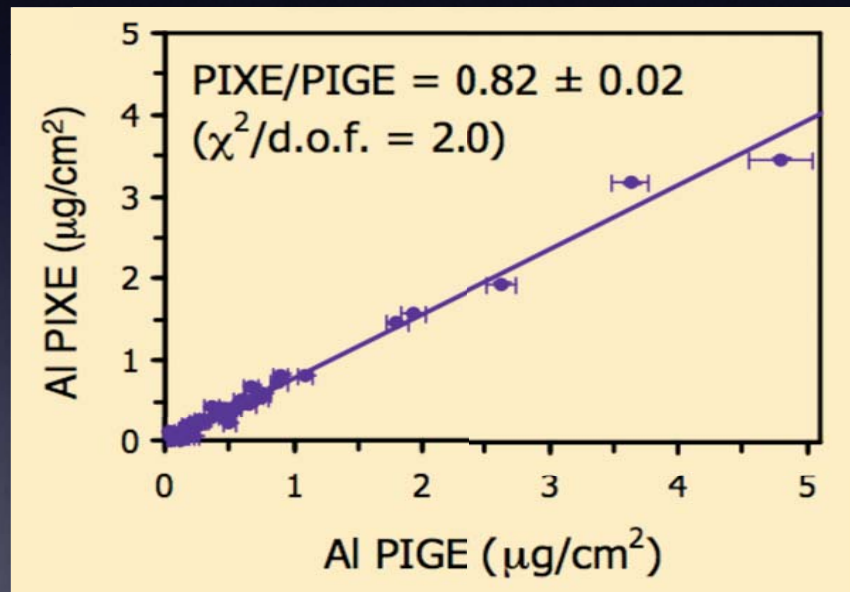
# Measurement of Na in PM<sub>10</sub> samples

Sampling site	E <sub>p</sub> (keV)	PIGE (μg/cm <sup>2</sup> )	PIXE (μg/cm <sup>2</sup> )	PIXE/PIGE
Lampedusa (Re)	3520	19.6 ± 0.9	13.3 ± 0.2	0.68 ± 0.04
Lampedusa (Re)	3670	20.0 ± 0.8	13.3 ± 0.2	0.67 ± 0.03
Lampedusa (Re)	4045	20.7 ± 0.7	13.2 ± 0.1	0.64 ± 0.02
Lampedusa (Re)	4470	20.9 ± 0.8	13.3 ± 0.1	0.64 ± 0.03
Lampedusa (Re)	4695	20.8 ± 0.5	13.5 ± 0.2	0.65 ± 0.02
Sesto F.no (U)	4045	8.4 ± 0.6	5.5 ± 0.1	0.65 ± 0.05
Livorno (Ru)	4045	16.0 ± 0.6	11.2 ± 0.1	0.70 ± 0.03
Prato (T)	4045	7.3 ± 0.5	5.1 ± 0.1	0.69 ± 0.05

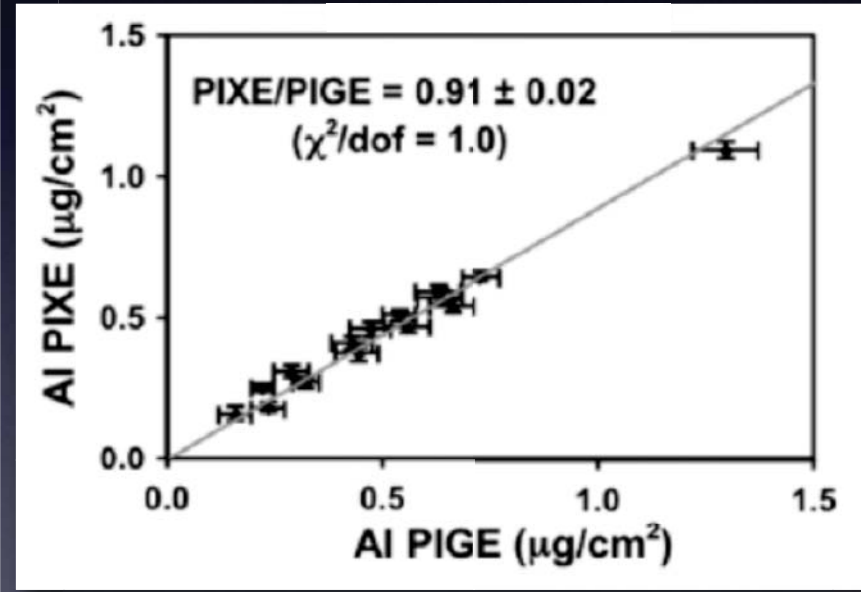
- PIGE reproducibility independent from the used plateau
- The self-absorption effects are almost the same for all the samples: Na concentration is underestimated by 30-35%

# Measurements of Al in dust particles

Airborne mineral dust  
collected in-flight over  
Sahel desert

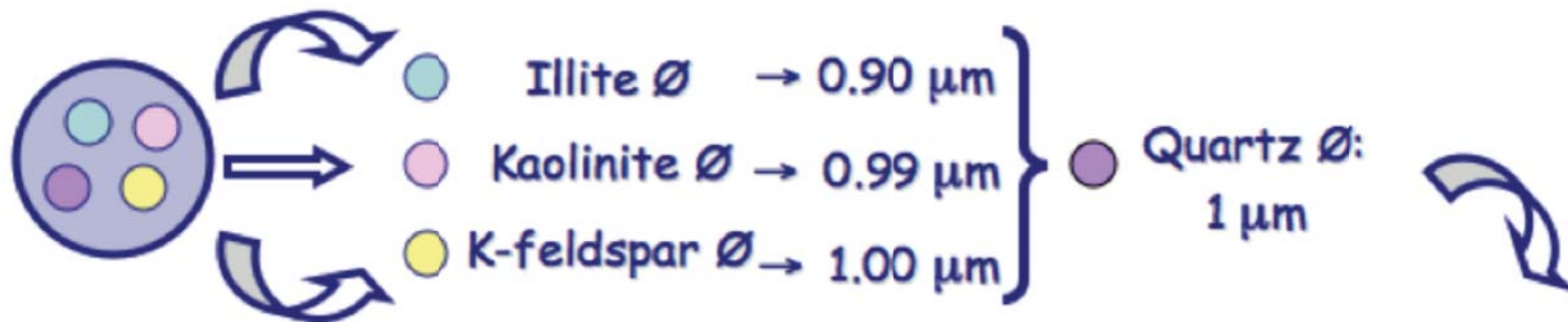


Mineral dust archived in  
Antarctic ice cores



Correct the concentration of low-Z elements obtained by PIXE  
Accurate study of geochemical composition of mineral dust

# Study of geochemical composition of mineral dust



$$\left( \frac{\text{PIXE}}{\text{PIGE}} \right)_{\text{ice dust}}^{\text{Al}} = 0.91$$

$$\text{AF} = \frac{1 - \exp(-a \cdot D)}{a \cdot D}, \quad a = \frac{2}{3} \cdot \mu \cdot \rho$$

B. Holynska and A. Markowicz, XRS 10, 1981

	Na	Mg	Al	Si	K
<u>Kaolinite</u>			0.91	0.90	
K-feldspar	0.79		0.91	0.92	0.97
<u>Illite</u>		0.87	0.91	0.91	0.97
Quartz				0.94	

Scheme of the evaluation of the attenuation for the light elements in a dust sample, in the hypothesis that it is mainly composed by a mix of pure minerals, namely Kaolinite, Illite, K-feldspar and Quartz.



# Study of desert aerosol composition



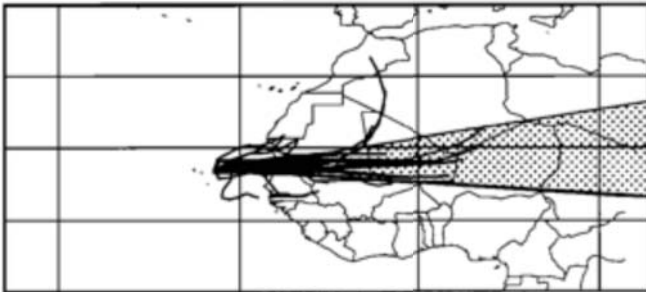
Mineral dust is one of the major components of atmospheric aerosols (~40% on a global scale): it has important effects on the radiative budget of the atmosphere and thus on climate change.

Estimates of the global mean direct radiative forcing by mineral dust vary in a wide range (+0.09 to  $-0.46 \text{ W/m}^2$ ), owing to uncertainties in the mineralogical composition and size distribution.

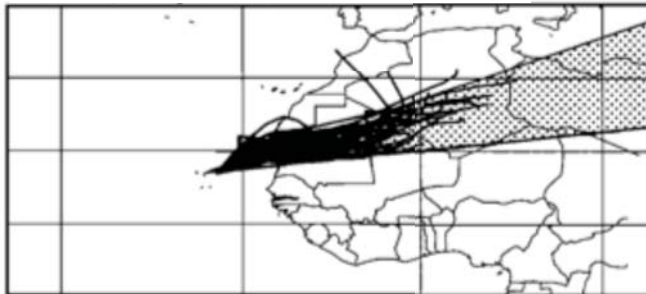
**An accurate quantitative analysis of airborne dust is needed.**

# Fingerprinting the desert dust

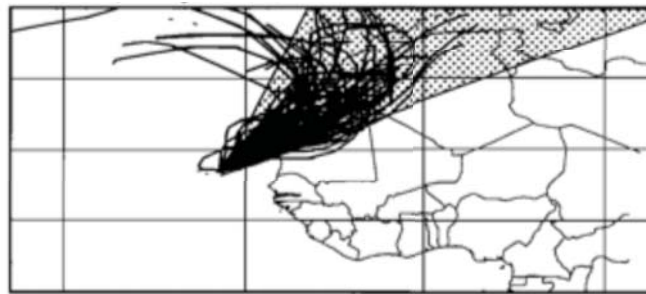
Sahel sector



south and central Sahara sector



north and west Sahara sector



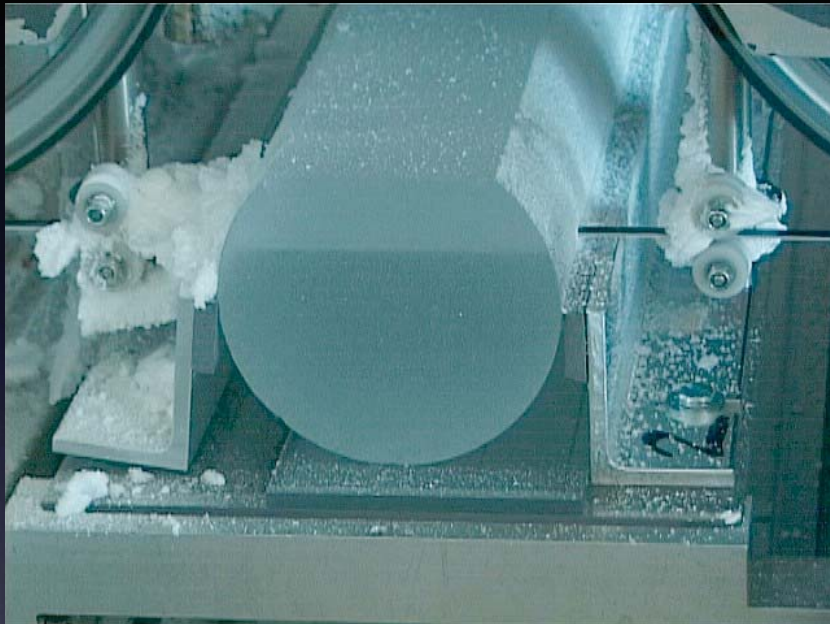
- Interelemental ratios in mineral dust measured at a receptor site can be used to differentiate source regions.

**Table 1.** Elemental Ratios of Dust Collected at Sal According to the Sectors of Origin Presented in Figure 2\*

	Sector 1	Sector 2	Sector 3
Si/Al			
Mean	2.03	2.21	2.32
s.d.	0.09	0.07	0.10
Ca/Al			
Mean	0.20	0.36	0.60
s.d.	0.05	0.07	0.19
Fe/Ca			
Mean	2.71	1.43	0.90
s.d.	0.59	0.32	0.30
K/Ca			
Mean	0.96	0.62	0.43
s.d.	0.21	0.10	0.11

- If not corrected, elemental ratios prevent the possibility of distinguishing the origin of the dust.

# Study of ice core dust composition



EPICA ice core (length 3190 m).  
Ice sampled to an age of 800 kyr BP.

Polar ice cores are extensive archives of records of past atmospheric compositions, allowing paleoclimate research.

Snow, accumulated and compressed into solid ice, contains traces of the gases and the aerosols being in the atmosphere at the deposition time.

No post-depositional processes affect dust.

# Study of ice core dust composition



Italian-French "Station Concordia"  
at Dome C.

No local dust sources in Antarctica.

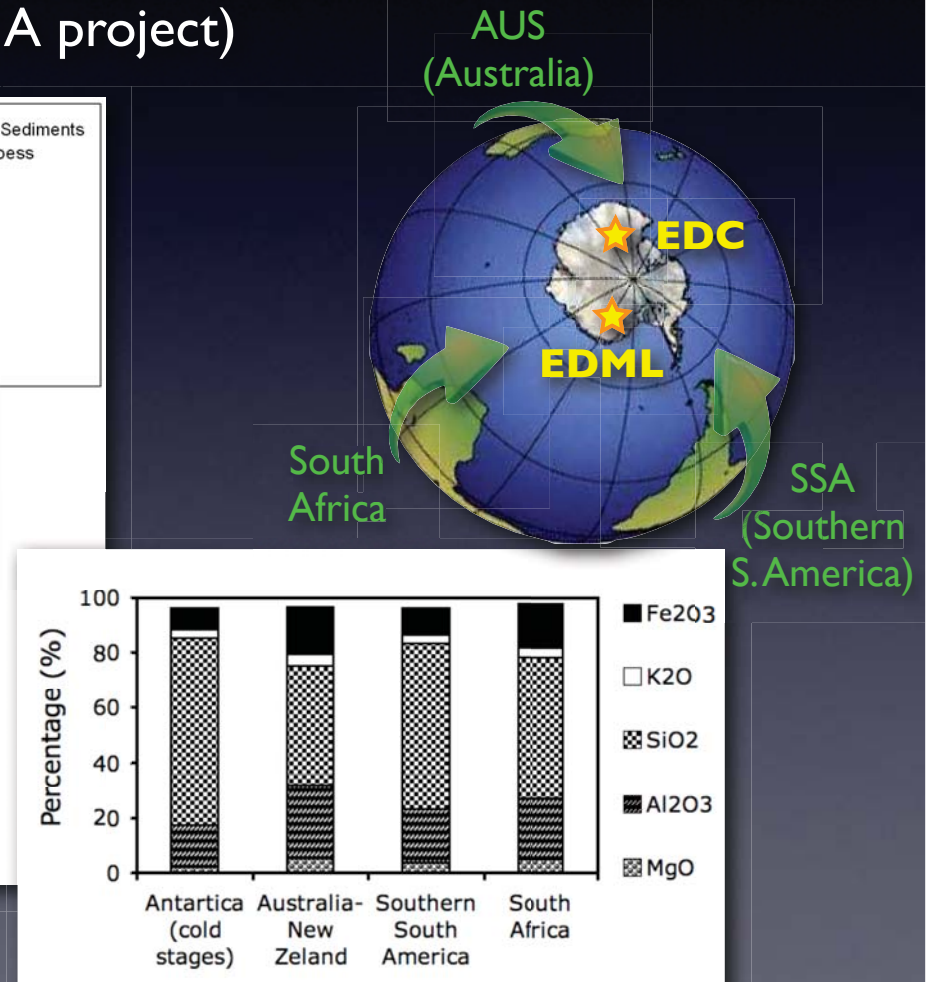
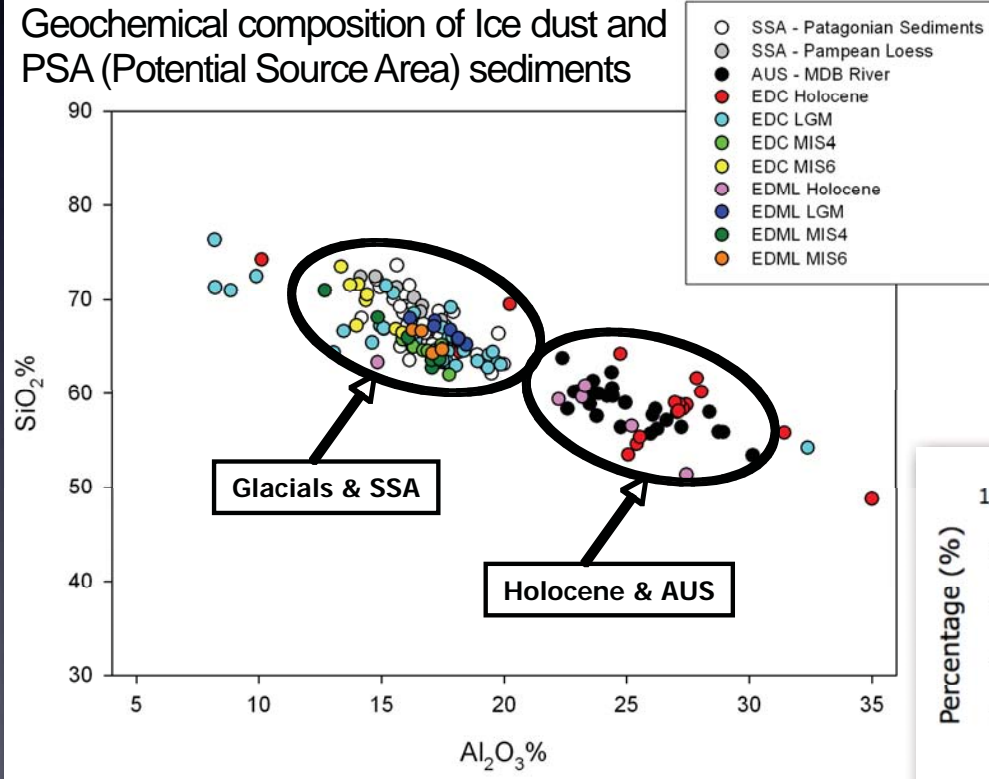
Dust particles reach the inner Antarctic areas after long-range transport from continental areas in Southern Hemisphere.

**From the analysis of the geochemical composition of ice core dust it is possible to infer the dust source location.**



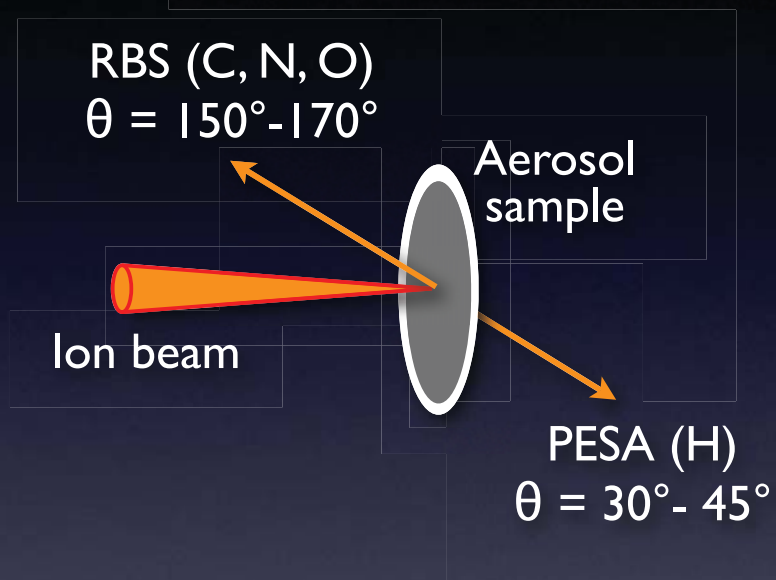
# Ice core and PSA dust composition

The study of the composition of dust particles deposited over the Antarctic ice sheet and archived in ice core samples (spanning the last 220 kyr) helps to investigate global climate changes (EPICA project)



*F. Marino et al., Geophys. Res. Lett. 36, 2009*

# Elastic scattering techniques & the aerosols



- RBS and PESA are “killing apps” to determine the light elements in aerosol samples
- Use of proton beams is mandatory to perform simultaneous PIXE measurements

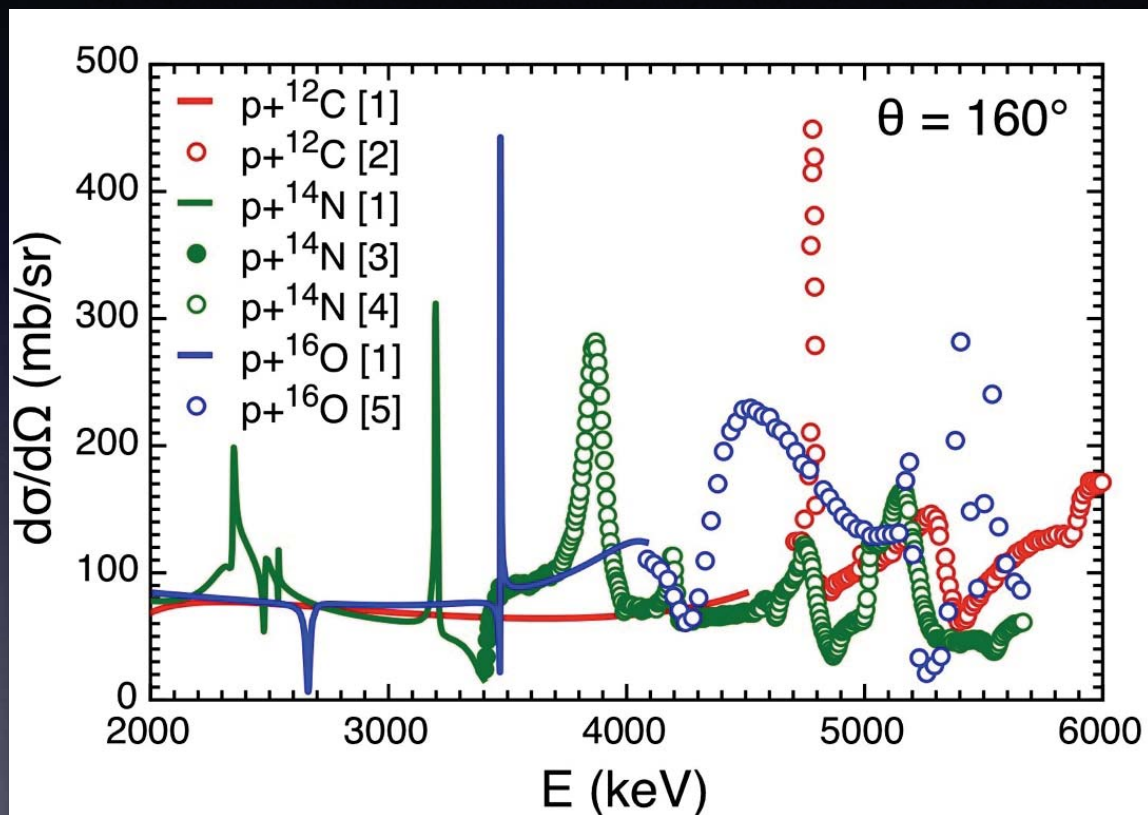
- *C and O by 1.15 MeV protons backscattering,  $\theta = 150^\circ$  (Rubin et al., Anal. Chemistry 29, 1947)*
- *C by 16 MeV protons backscattering,  $\theta = 120^\circ$  (Andrae and Barnard, NIM 181, 1981)*
- *H, C, N and O by 30 MeV alpha particles forward scattering/recoil,  $\theta = 64^\circ$  (Cahill et al., NIM B 3, 1984)*
- *C and O by 3-4 MeV protons backscattering (Boni et al., NIM B 15, 1986)*

# Typical filtering / collecting substrata

Name	Composition	Thickness (mg/cm <sup>2</sup> )
Quartz and Glass fibre	Silicate and Borosilicate	5 - 7
Cellulose Acetate	C <sub>12</sub> H <sub>30</sub> O <sub>15</sub>	~ 5
Cellulose Nitrate	C <sub>2</sub> H <sub>15</sub> N <sub>5</sub> O <sub>20</sub>	~ 5
Cellulose Mixed Ester	85% cell.nitrate 15% cell.acetate	~ 5
Teflon (ring supported)	PTFE: (CF <sub>2</sub> ) <sub>n</sub>	0.5 - 0.7
Nuclepore	C <sub>15</sub> H <sub>14</sub> CO <sub>3</sub>	~ 0.9

Teflon filter is an ideal substratum for H, C, N, O measurements

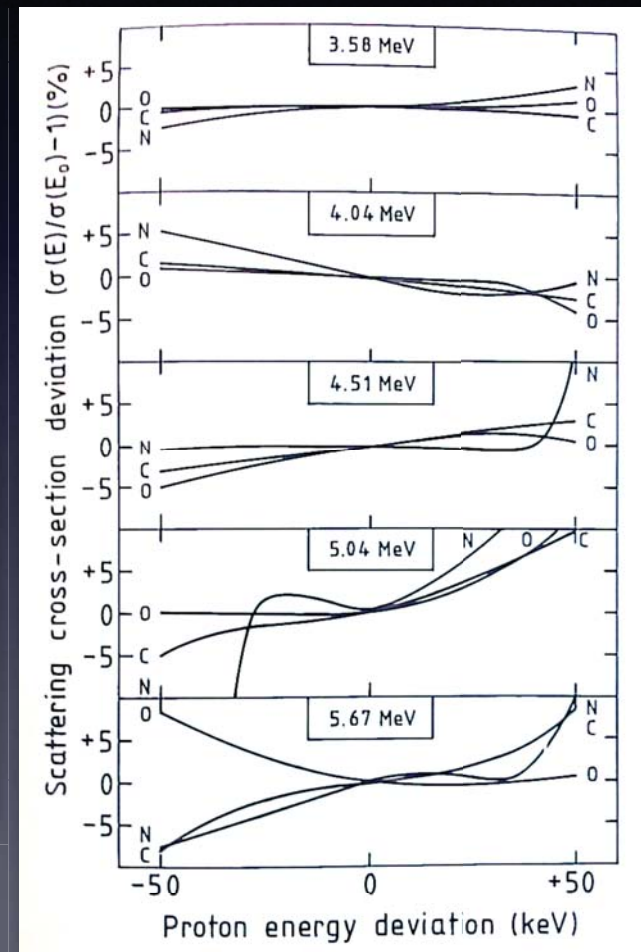
# Choosing proton energy for RBS / PESA



[1] SigmaCalc ([www-nds.iaea.org/sigmacalc/](http://www-nds.iaea.org/sigmacalc/))

[2] Swint et al., Nucl. Phys. 86, 1966 [4] West et al., Phys. Rev. 179, 1969

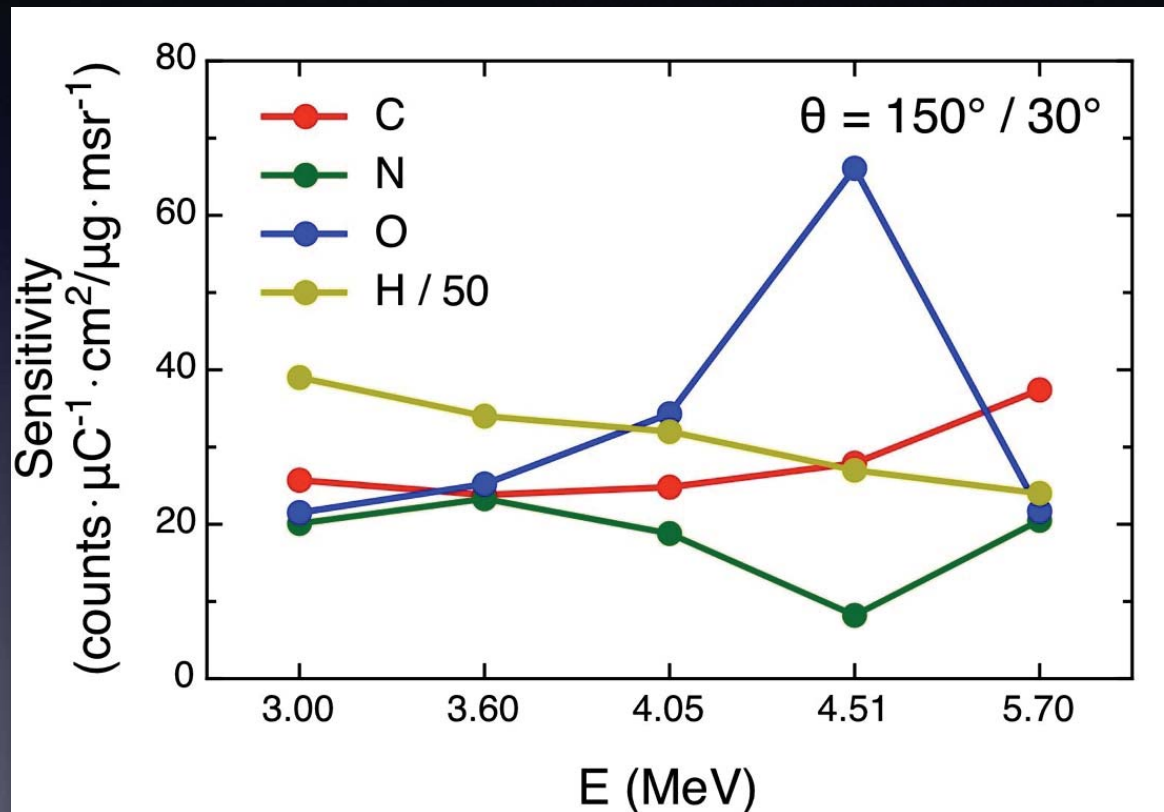
[3] Bashkin et al., Phys. Rev. 114, 1959 [5] Harris et al., Nucl. Phys. 38, 1962



Martinsson, NIM B 15, 1986



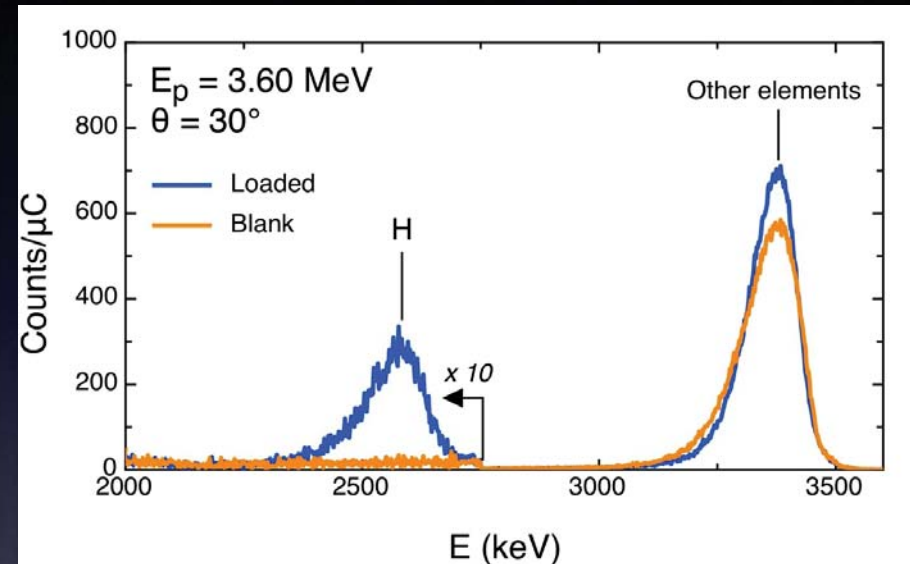
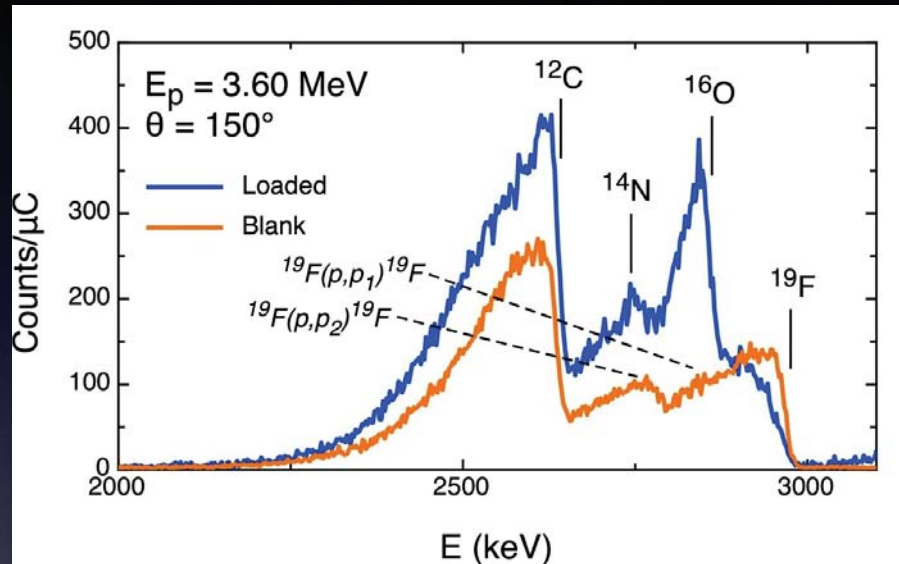
# Sensitivity values for C, N, O, H by RBS / PESA



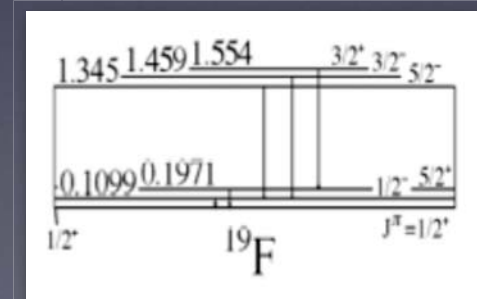
Measured with a thin Upilex-S standard ( $\text{H}_{10}\text{C}_{22}\text{N}_2\text{O}_4$ , 7.5  $\mu\text{m}$ )



# RBS/PESA on Teflon (CF<sub>2</sub>) filters

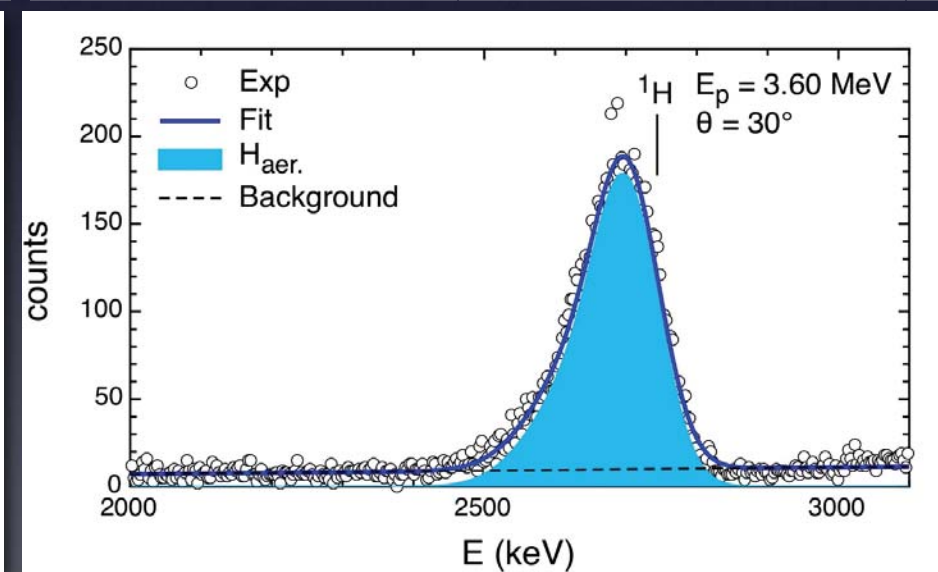
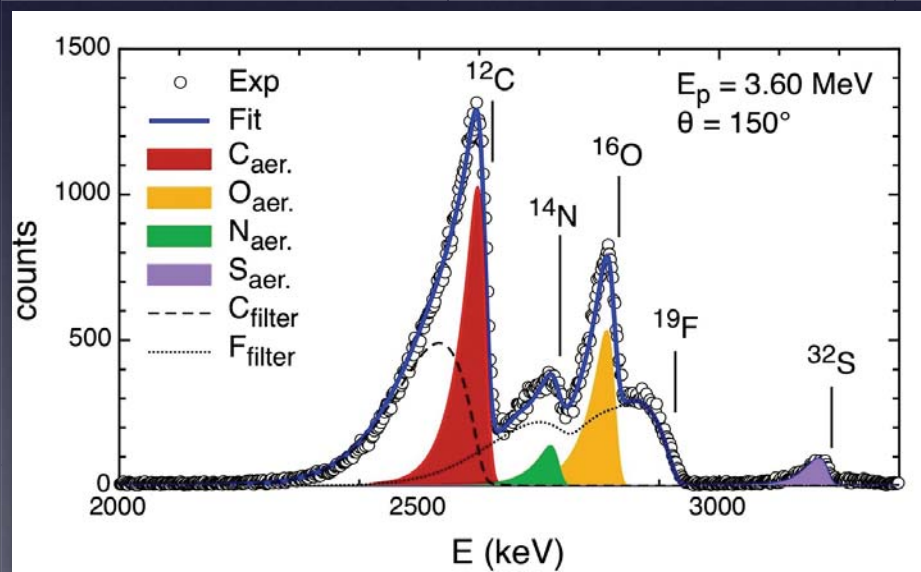


- Teflon (CF<sub>2</sub>) filter is the ideal collecting substratum for RBS and PESA measurements
- Background in the RBS spectra due to:
  - $p$  elastically scattered by C and F of the filter
  - $p$  inelastically scattered,  $(p,p')$  reactions, by F of the filter



# Quantitative analysis of C and other light elements

Fitting and simulations codes of RBS and PESA spectra (i.e. SIMNRA v6.05 by M. Meyer) implementing validated microscopic data and advanced physical models and effects



# Typical detection limits and uncertainties

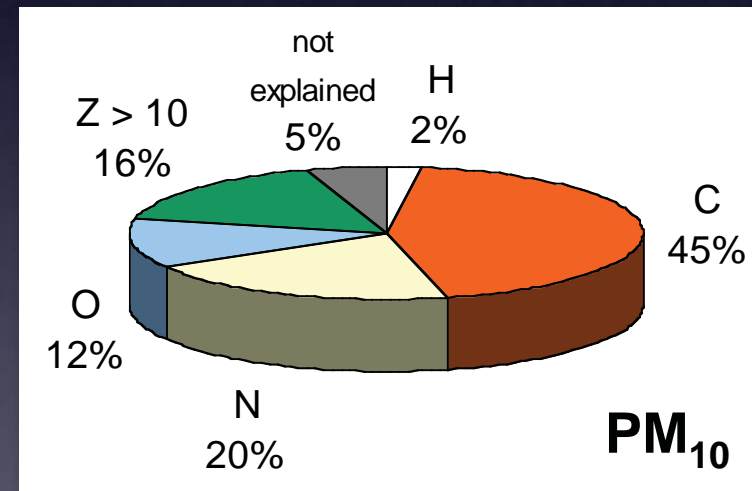
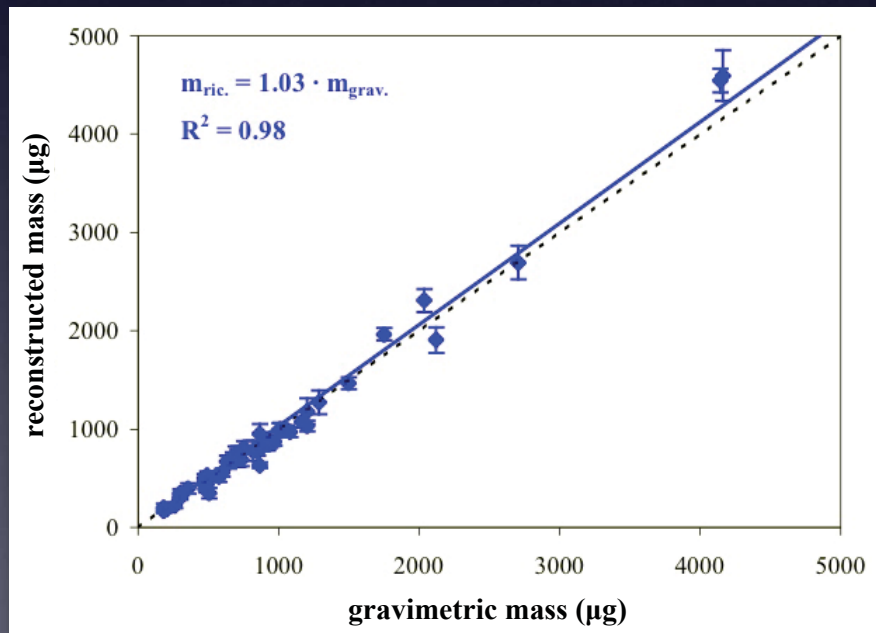
$i = 5-10 \text{ nA}$   
 $t = 5-6 \text{ min.}$

	Detection limit ( $\mu\text{g}/\text{cm}^2$ )	Detection limit ( $\mu\text{g}/\text{m}^3$ ) *	Uncertainty
<b>H</b>	0.10	0.02	5-10%
<b>C</b>	4.0	1.0	5-10%
<b>N</b>	2.0	0.5	10-30%
<b>O</b>	2.0	0.5	10-20%
<b>Z &gt; 10</b>	0.005 - 0.05	0.001 - 0.01	5-20%

\* Considering a 47 mm diameter Teflon filter and sampling for 24 h at 2.3  $\text{m}^3/\text{h}$  (European standard, EN12341)

# Gravimetric mass reconstruction

The coupling of IBA techniques (PIXE, PIGE, RBS and PESA) allows the “mass closure”: the sum of the mass of all the measured elements is equal to the gravimetric mass within 20% for all the samples (and within 10% for 85% of the samples)



Airborne particulate matter characterization in the industrial district of Montelupo Fiorentino, Florence, Italy (September 2002 - June 2003)



Thanks for  
your attention!

# Bibliography

- R. Tesmer, M. Nastasi ed.s *“Handbook of Modern Ion Beam Materials Analysis”* MRS
- S.A.E. Johansson, J.L. Campbell, K.G. Malmqvist ed.s *“Particle-induced X-ray emission spectrometry (PIXE)”* John Wiley & sons
- W.-K. Chu, J.W. Mayer, M.-A. Nicolet *“Backscattering Spectrometry”* Academic Press
- G. Deconninck et al. *“Prompt gamma-ray spectroscopy and its use in elemental analysis”* At. Energy Rev. suppl. no. 2 (1981) 151