



**The Abdus Salam  
International Centre for Theoretical Physics**



**2400-3**

**Workshop on Strongly Coupled Physics Beyond the Standard Model**

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**Gauge-Higgs unification and the LHC**

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# Gauge-Higgs Unification and the LHC

Yutaka Hosotani



Strongly coupled physics BSM  
ICTP, Trieste, 26 January 2012

*If the Higgs boson*

is 124 or 126 or ? GeV

with SM couplings, →

Explain “SM Higgs”.

with non-SM couplings,

is not seen at LHC,



{  
Higgs is stable.  
Higgs does not exist.

## *If the Higgs boson*

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with SM couplings,

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Higgs is stable.  
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**gauge-Higgs**



**Discovery**

of

**un-discovery**

of

**the Higgs boson**

**It's no surprise**

**in gauge-Higgs unification.**

# Gauge-Higgs Unification

$A_M$

4-dim. components  $A_\mu$

extra-dim. component  $A_y$

4D gauge fields  
 $\gamma, W, Z$

4D Higgs fields  
 $H$

Aharonov-Bohm phase

Symmetry breaking  
Hosotani mechanism



Higgs boson as an AB phase in extra dim

$$e^{i\hat{\theta}_H(x)} \sim P \exp \left\{ ig \int_C dy A_y \right\}$$

$$\hat{\theta}_H(x) = \theta_H + \frac{H(x)}{f_H}$$

$$\theta_H = \frac{\langle \text{Higgs} \rangle}{f_H} \rightarrow \left\{ \begin{array}{l} \blacksquare \text{ symmetry breaking} \\ \blacksquare \text{ masses for} \\ \text{quarks/leptons/W,Z} \end{array} \right.$$

$$\theta_H \sim \theta_H + 2\pi$$

differs from SM.



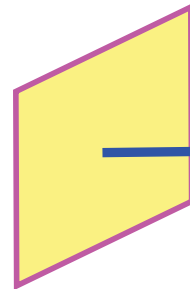
# $SO(5) \times U(1)$ in Randall-Sundrum warped space

$$ds^2 = e^{-2k|y|} dx_\mu dx^\mu + dy^2$$

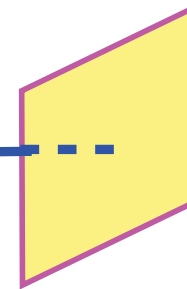
$$0 \leq |y| \leq L = \pi R$$

Agashe, Contino, Pomarol, 2005  
 YH, Oda, Ohnuma, Sakamura 2008  
 YH, Noda, Uekusa 2009

Planck brane



AdS  $\Lambda = -6k^2$



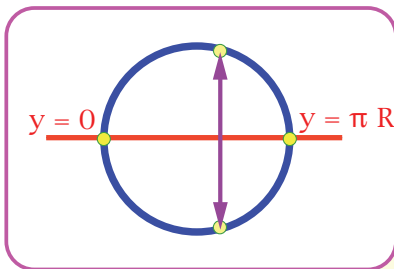
TeV brane

$SO(5) \times U(1)$

$g_A$   $g_B$

brane fermions  
 brane scalar

quarks, leptons



*Orbifold BC*

$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, -y) = P_0 \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, y) P_0^\dagger$$

$$\begin{pmatrix} A_\mu \\ A_y \end{pmatrix} (x, \pi R - y) = P_1 \begin{pmatrix} A_\mu \\ -A_y \end{pmatrix} (x, \pi R + y) P_1^\dagger$$

## 4D gauge bosons and Higgs

$$P_0 = P_1 = \begin{pmatrix} -1 & & & & \\ & -1 & & & \\ & & -1 & & \\ & & & -1 & \\ & & & & +1 \end{pmatrix}$$

$$SO(5) \rightarrow SO(4) \simeq SU(2)'_L \times SU(2)'_R$$

$W \ Z \ \gamma$

$$A_\mu \sim \left( \begin{array}{c} \square \end{array} \right)$$

**Higgs**

$$A_y \sim \left( \begin{array}{c} \phi_1 \\ \phi_2 \\ \phi_3 \\ \phi_4 \end{array} \right)$$

4D Higgs doublet

brane scalar  $SO(4) \times U(1) \rightarrow SU(2)'_L \times U(1)'$   
 $\neq SU(2)_L \times U(1)_Y$   
 $\rightarrow U(1)_{EM}$

parameters

RS:  $k$  ,  $z_L = e^{kL}$

$g_A$  ,  $g_B$

fermions

inputs

$\alpha_w$  ,  $\sin^2 \theta_W$

$m_Z$

quark/lepton masses



One free parameter  $z_L$



## Warped space



Planck scale

input

$m_{\text{KK}}$   
TeV scale

output

Weak scale

$m_W$

input

$$m_{\text{KK}} = \pi k e^{-kL} \sim \pi \sqrt{kL} m_W$$

$$kL = 30 \sim 40 \text{ for } z_L = 10^{13} \sim 10^{17}$$



Symmetry breaking



## Effective interactions

*in SM*

$$f_H \sin \hat{\theta}_H \rightarrow v + H$$

$$\mathcal{L}_{\text{eff}} \sim -\left(\frac{1}{2} g f_H \sin \hat{\theta}_H\right)^2 \left\{ W_\mu^\dagger W^\mu + \frac{1}{2 \cos^2 \theta_W} Z_\mu Z^\mu \right\}$$
$$-y_f f_H \sin \hat{\theta}_H \bar{\psi}_f \psi_f$$

$$\hat{\theta}_H = \theta_H + \frac{H}{f_H} \quad f_H = \frac{2}{\sqrt{kL}} \frac{m_{KK}}{\pi g}$$

$$\begin{matrix} WWH \\ ZZH \\ \text{Yukawa} \end{matrix} = \text{SM} \times \cos \theta_H$$

# Matter content

YH, Oda, Ohnuma, Sakamura 2008

YH, Noda, Uekusa 2009

Planck brane

$SO(5) \times U(1)$

TeV brane

Quarks

$$\begin{pmatrix} \hat{T}_R \\ \hat{B}_R \end{pmatrix}$$

$$\begin{pmatrix} \hat{U}_R \\ \hat{D}_R \end{pmatrix}$$

$$\begin{pmatrix} \hat{X}_R \\ \hat{Y}_R \end{pmatrix}$$

$$\begin{pmatrix} T_L \\ B_L \\ t_L \\ b_L \\ t'_R \\ b'_R \end{pmatrix}_{\frac{2}{3}}$$

$$\begin{pmatrix} U_L \\ D_L \\ X_L \\ Y_L \\ b'_R \end{pmatrix}_{-\frac{1}{3}}$$

$$\Psi(x, -y) = P_0 \gamma^5 \Psi(x, y)$$

$$\Psi(x, \pi R - y) = P_1 \gamma^5 \Psi(x, \pi R + y)$$

Brane scalar

$$\hat{\Phi} \left(0, \frac{1}{2}\right)$$

$$\langle \hat{\Phi} \rangle \neq 0$$

$$\left(\frac{1}{2}, 0\right)$$

vector rep

$$\left(\frac{1}{2}, \frac{1}{2}\right) \oplus (0, 0)$$

$$\begin{pmatrix} \hat{L}_{2XR} \\ \hat{L}_{2YR} \end{pmatrix}$$

$$\begin{pmatrix} L_{2XL} \\ L_{2YL} \\ L_{3XL} \\ L_{3YL} \\ \nu'_{\tau R} \end{pmatrix}_0$$

Leptons

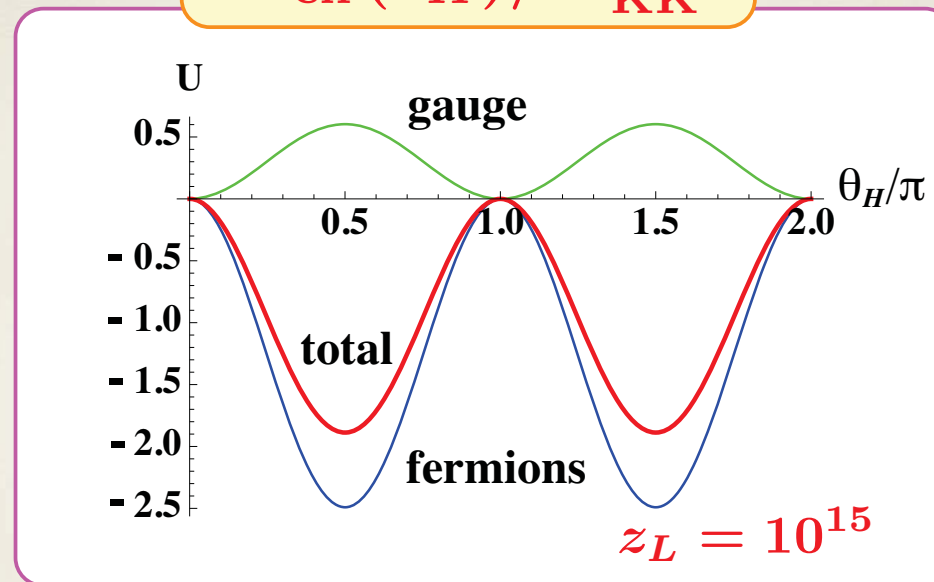
$$\begin{pmatrix} \hat{L}_{3XR} \\ \hat{L}_{3YR} \end{pmatrix}$$

$$\begin{pmatrix} \nu_{\tau L} \\ \tau_L \\ L_{1XL} \\ L_{1YL} \\ \tau'_R \end{pmatrix}_{-1}$$

Anomaly cancelation

# EW symmetry breaking by Hosotani mechanism

$$V_{\text{eff}}(\theta_H) / m_{\text{KK}}^4$$



$$\theta_H = \frac{\pi}{2}$$

$$SU(2)'_L \times U(1)' \rightarrow U(1)_{EM}$$

$$m_H = 135 \text{ GeV} (z_L = 10^{15})$$

$$\theta_H = \frac{\pi}{2}$$

**H parity**

YH, Ko, Tanaka, 2009

YH, Tanaka, Uekusa, 2010

$$\theta_H + \frac{H}{f_H} = \frac{\pi}{2} + \frac{H}{f_H} \longrightarrow \frac{\pi}{2} - \frac{H}{f_H}$$

$H : -$

all other SM particles : +

**Stable Higgs**



# H parity

$$SO(5) : \quad SO(4) \simeq SU(2)'_L \times SU(2)'_R \quad SO(5)/SO(4)$$
$$\{ T^\alpha \} = \quad \{ T^{a_L}, T^{a_R}, T^{\hat{a}}, T^{\hat{4}} \}$$

$$P_H : \quad \begin{aligned} SU(2)'_L &\leftrightarrow SU(2)'_R \\ T^{\hat{4}} &\rightarrow -T^{\hat{4}} \end{aligned}$$



Agashe, Contino, Da Rold, Pomarol 2006  
*T* parameter  $Zb\bar{b}$

Where is  $SU(2)_L \times U(1)_Y$   
in  $SO(5) \times U(1)$  ?

$SO(5) \times U(1)_X$

**B.C.**  $\rightarrow SO(4) \times U(1)_X \simeq SU(2)'_L \times SU(2)'_R \times U(1)_X$

Brane scalar  
 $\langle \hat{\Phi} \rangle \neq 0$

$\rightarrow SU(2)'_L \times U(1)' \neq SU(2)_L \times U(1)_Y$

$\theta_H \neq 0 \rightarrow U(1)_{EM}$

$$\text{SO}(5) \quad \{ T_L^a, T_R^a, \hat{T}^a, \hat{T}^4 \} \quad \{ I_L^a, I_R^a, \hat{I}^a, \hat{I}^4 \}$$

$$\text{SU}(2)'_L \times \text{SU}(2)'_R \quad \text{SU}(2)_L \times \text{SU}(2)_R$$

$$\begin{pmatrix} I_L^a \\ I_R^a \end{pmatrix} = \frac{1 \pm \cos \theta_H}{2} T_L^a + \frac{1 \mp \cos \theta_H}{2} T_R^a \mp \frac{\sin \theta_H}{\sqrt{2}} \hat{T}^a$$

**Note:**  $T_L^a + T_R^a = I_L^a + I_R^a$  : custodial  $SU(2)_V$

$$W^\pm \text{ couples to } I_L^1 \pm iI_L^2$$

$$Z \quad c_W I_L^3 - s_W Q_Y = c_\phi Q_X + s_\phi I_R^3, \quad s_\phi = t_W$$

$$\gamma \quad Q_{EM} = I_L^3 + I_R^3 + Q_X = T_L^3 + T_R^3 + Q_X$$

$$\text{Higgs} \quad \hat{I}^4 = \hat{T}^4$$

YH, Sakamura 2007

Contino, Marzocca, Pappadopulo, Rattazzi 2011

Hatanaka, YH, Shimotani

$$\left. \begin{array}{l} W_{\mu}^{\pm} \\ \left( \begin{array}{c} Z_{\mu} \\ \gamma_{\mu} \\ \tilde{Z}_{\mu} \end{array} \right) \end{array} \right\} \begin{array}{l} W_{\mu}^1, W_{\mu}^2 \\ \left( \begin{array}{c} W_{\mu}^3 \\ B_{\mu}^X \\ W_{\mu}^{\prime 3} \end{array} \right) \end{array} \left. \begin{array}{l} \\ \\ \end{array} \right\} \begin{array}{l} SU(2)_L \\ U(1)_X \\ SU(2)_R \end{array}$$

Furthermore

$$\sum W_{\mu}^{(n)}(x) \left\{ C(z; \lambda_W^{(n)}) I_L^+(\theta_H) - \frac{\sin \theta_H}{\sqrt{2}} [\hat{S}(z; \lambda_W^{(n)}) - C(z; \lambda_W^{(n)})] \hat{T}^+ \right\}$$

All KK modes participate.



# Collider signatures

◇  $\theta_H = \frac{1}{2}\pi \Rightarrow$  Absence of single-Higgs production  
Higgs pair production

Higgs = missing energy, momentum

hard to confirm at LHC/ILC

←  $\nu, \bar{\nu}$  background

*Cheung, Song, 1004.2783, Alves, 1008.0016*  
*YH, Tanaka, Uekusa, 1103.6076*

## Gauge couplings precision measurements

- ◇ Forward-backward asymmetry in  $e^+e^- \rightarrow Z \rightarrow \ell\bar{\ell}, q\bar{q}$
- ◇ Z-decay branching fractions

	No. data	SM	$z_L : 10^{15}$	$z_L : 10^{10}$	$z_L : 10^5$
$\sin^2 \theta_W$		0.2312	0.2309	0.2303	0.2284
$\chi^2(AFB)$	6	10.8	6.3	6.4	7.1
$\chi^2(Z \text{ decay})$	8	13.6	16.5	37.7	184.5


 $z_L \geq 10^{15}$

YH, Tanaka, Uekusa, 2011

# KK $Z^{(1)}$ & $\gamma^{(1)}$

$Z^{(1)}$

$z_L$	$10^5$	$10^{15}$
$m$	653	1130
$\Gamma$	104	422

in GeV

$\gamma^{(1)}$

$z_L$	$10^5$	$10^{15}$
$m$	678	1144
$\Gamma$	446	1959

in GeV

Large widths

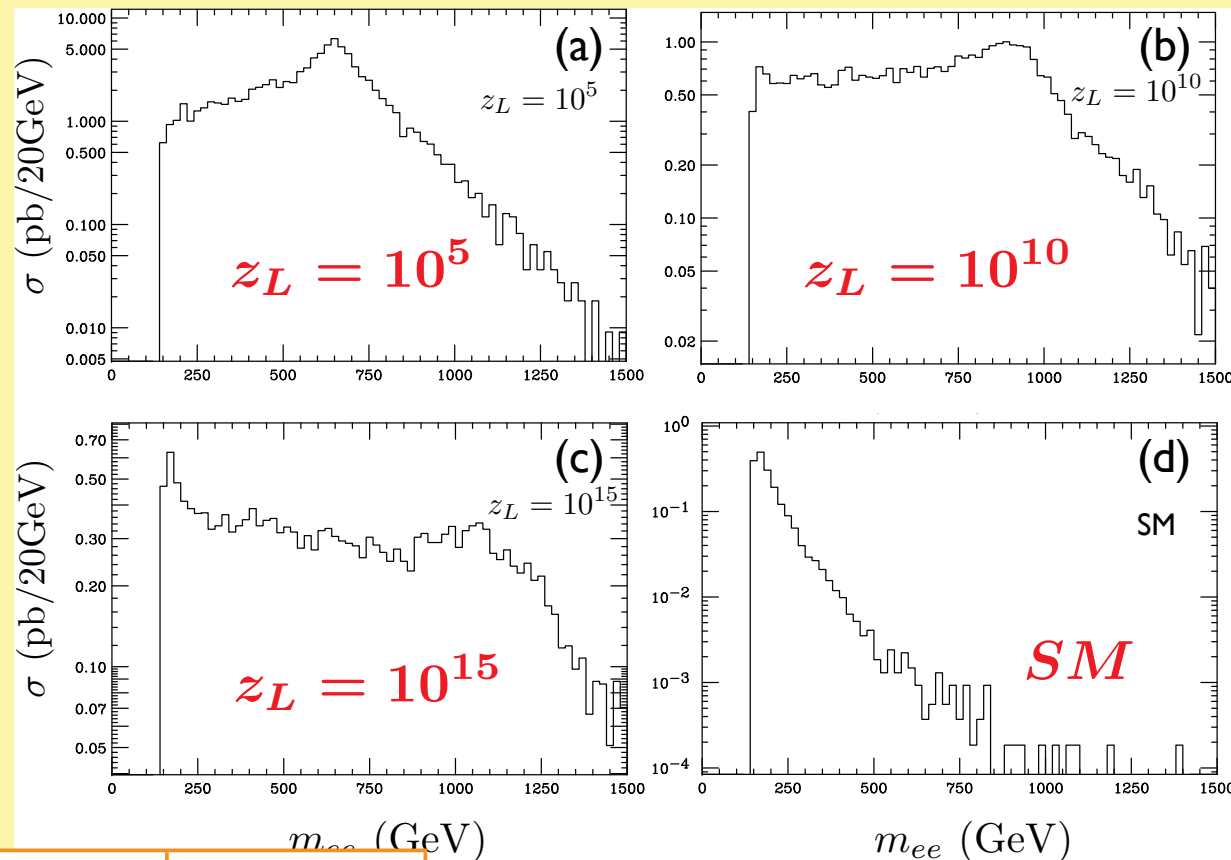
Larger couplings for right-handed quarks and lepton

$\sim \times 10$

“strong couplings at TeV”

LHC (3.5 + 3.5 TeV)

$$q\bar{q} \rightarrow Z^{(1)}, \gamma^{(1)} \rightarrow e^+e^-$$



$Z^{(1)}$

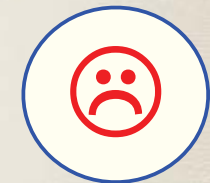
$z_L$	$10^5$	$10^{15}$
$m$	653	1130
$\Gamma$	104	422

in GeV

Large BG from  $\gamma^{(1)}$



$z_L > 10^{15}$



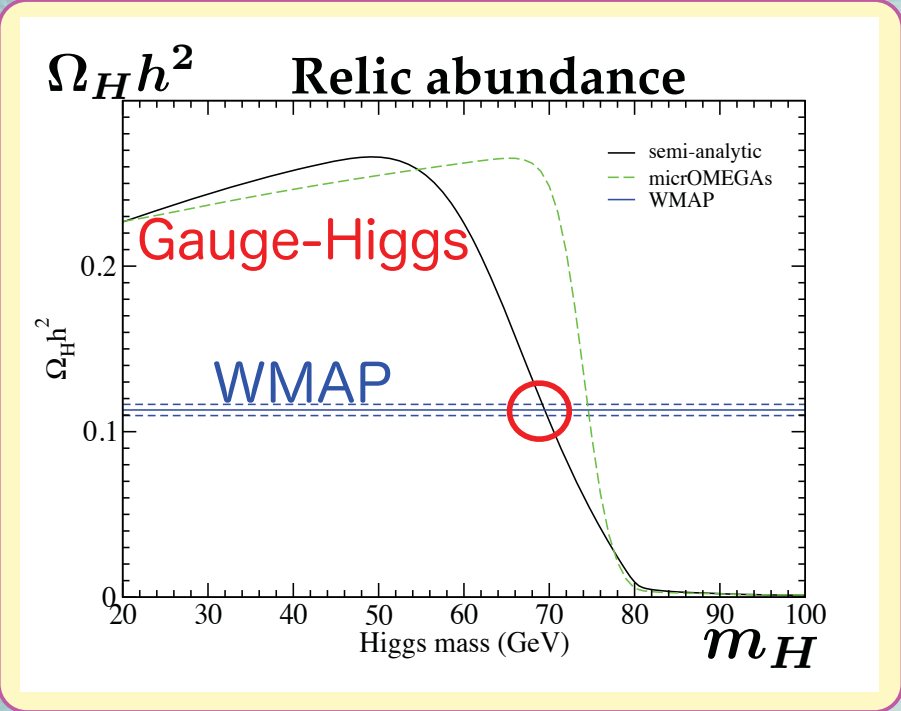


Stable Higgs



Dark Matter

YH, Ko, Tanaka, 2009



WMAP data



$m_H = 70 \sim 75 \text{ GeV}$

$z_L$	$10^5$	$10^{10}$	$10^{15}$
$m_H$	72 GeV	108	135

Collider signatures  $\Rightarrow z_L > 10^{15} \Rightarrow m_H = 135 \text{ GeV}$

Dark matter  $\Rightarrow m_H = 70 \sim 75 \text{ GeV} \Rightarrow z_L \sim 10^5$

$m_H = 70 \sim 75 \text{ GeV}$  compatible with  $z_l > 10^{15}$  ?

Yes

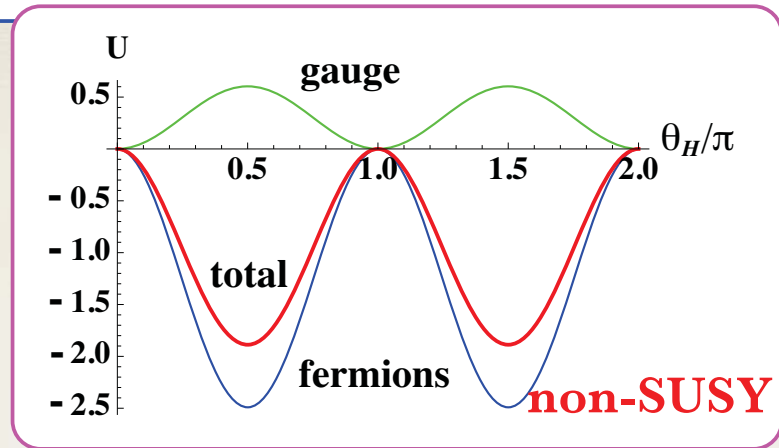
Hatanaka, YH, 2011

SUSY

exact  $\Rightarrow m_H = 0$

broken  $\Rightarrow 70 \sim 75 \text{ GeV}$

$$V_{\text{eff}} = \pm \frac{1}{2} \int \frac{d^4 p}{(2\pi)^4} \sum_n \ln \left\{ p^2 + m_n(\theta_H)^2 \right\}$$



*W, Z, Higgs*

*$\tilde{W}, \tilde{Z}, \tilde{Higgs}$*

$$\{ m_n \}$$

$$\tilde{m}_n = \sqrt{m_n^2 + \Lambda_{\text{gh}}^2}$$

*t*

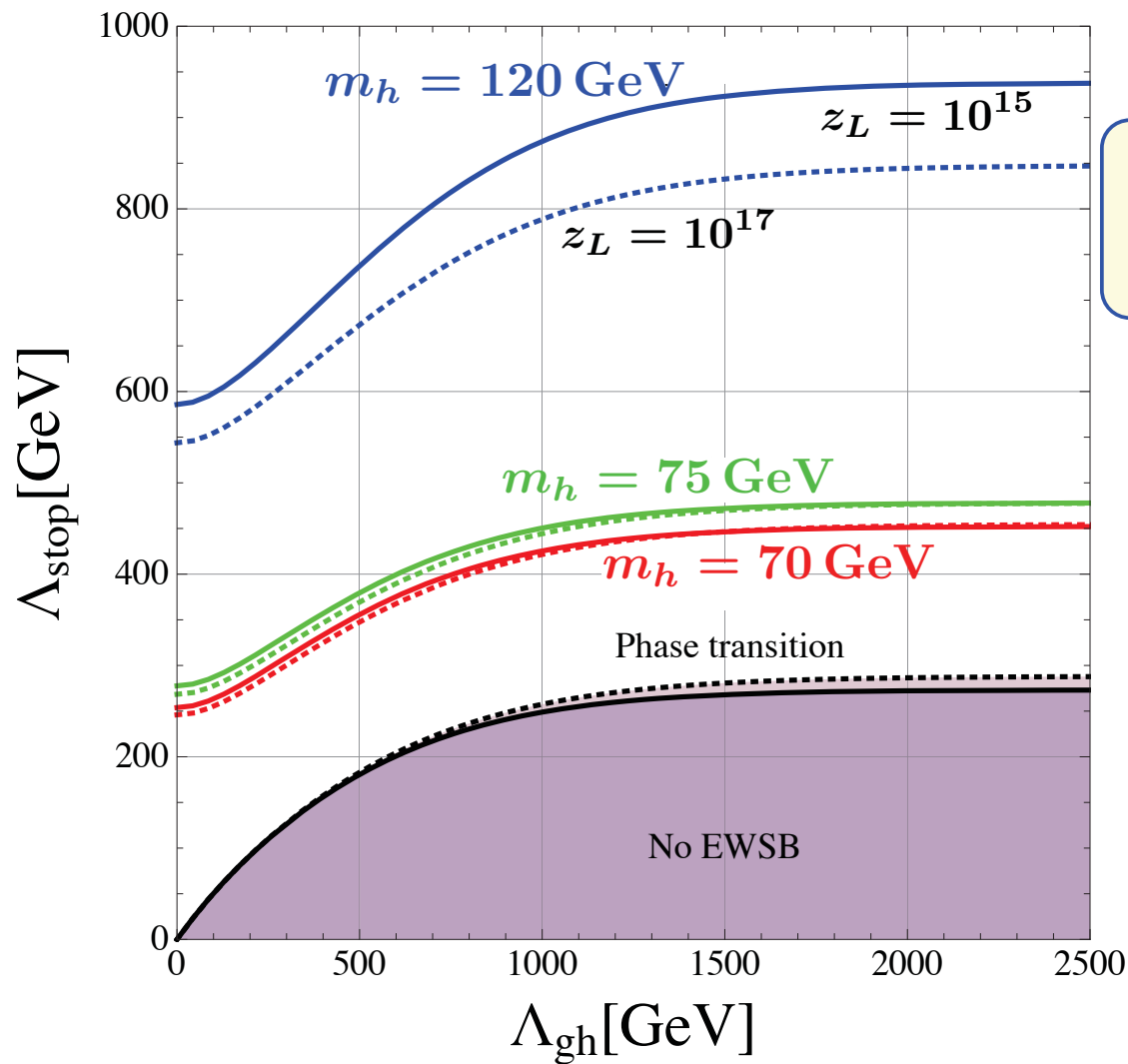
*$\tilde{t}$*

$$\{ m_n \}$$

$$\{ \tilde{m}_n = \sqrt{m_n^2 + \Lambda_{\text{stop}}^2} \}$$

SUSY





$\Lambda_{\text{stop}} = 450 - 475 \text{ GeV}$   
 $\Lambda_{\text{gh}} > 1 \text{ TeV}$

**stop mass**  
**480 - 505 GeV**  
 for  $m_h = 70 \sim 75 \text{ GeV}$

**800 - 900 GeV**  
 for  $m_h \sim 120 \text{ GeV}$



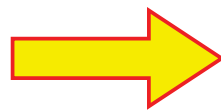
# Summary

*If the Higgs boson*

is 124 or 126 or ? GeV with non-SM couplings,

or

is not seen at LHC (as Higgs is stable),



**gauge-Higgs** (extra dimensions).